

# Higgs boson pair production in new physics models at hadron, lepton, and photon colliders

Daisuke Harada  
(KEK)

in collaboration with

E. Asakawa (Ochanomizu), S. Kanemura (U. of Toyama),  
Y. Okada (KEK), K. Tsumura (ICTP)

arXiv:1009.4670 [hep-ph]  
to be published in Phys. Rev. D

# Introduction

The standard model for elementary particles is very successful in describing high energy phenomena up to  $O(100)$  GeV.

The Higgs sector is the last unknown part of the Standard Model.

Once the Higgs boson is found at the Tevatron or the LHC, its property such as the mass, the decay width, production cross section and the decay branching ratios will be measured in order to confirm the SM.

The Higgs mechanism will be tested by determining the coupling constants of the Higgs boson to the weak gauge boson.

The measurement of the Yukawa coupling constants will clarify the mass generation mechanism of quarks and charged leptons.

It is also important to measure the Higgs self-coupling.

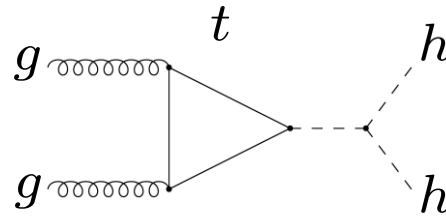
- Test for the Higgs potential
- Search for New Physics effect

We study the impacts of new physics effects on the hhh measurement at LHC, ILC / CLIC and PLC in several new physics model beyond the SM.

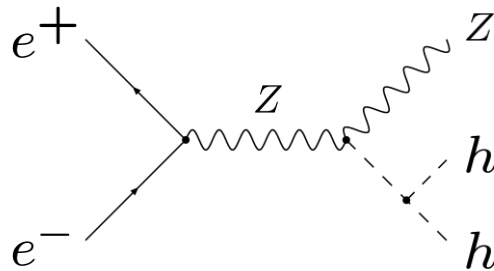
# Measurement of hhh coupling

## Measurement of hhh coupling at collider experiment

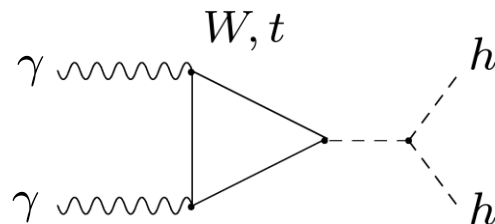
- LHC (SLHC)  $gg \rightarrow hh$



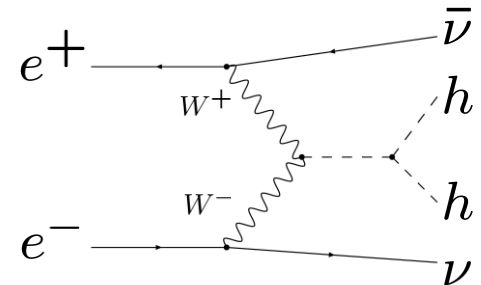
- ILC  $e^+e^- \rightarrow Zh h$   
 $\sqrt{s} = 500\text{GeV}$



- Photon Collider (PLC)  $\gamma\gamma \rightarrow hh$



- ILC/CLIC  $e^+e^- \rightarrow hh\bar{\nu}\nu$   
 $\sqrt{s} \geq 1\text{TeV}$



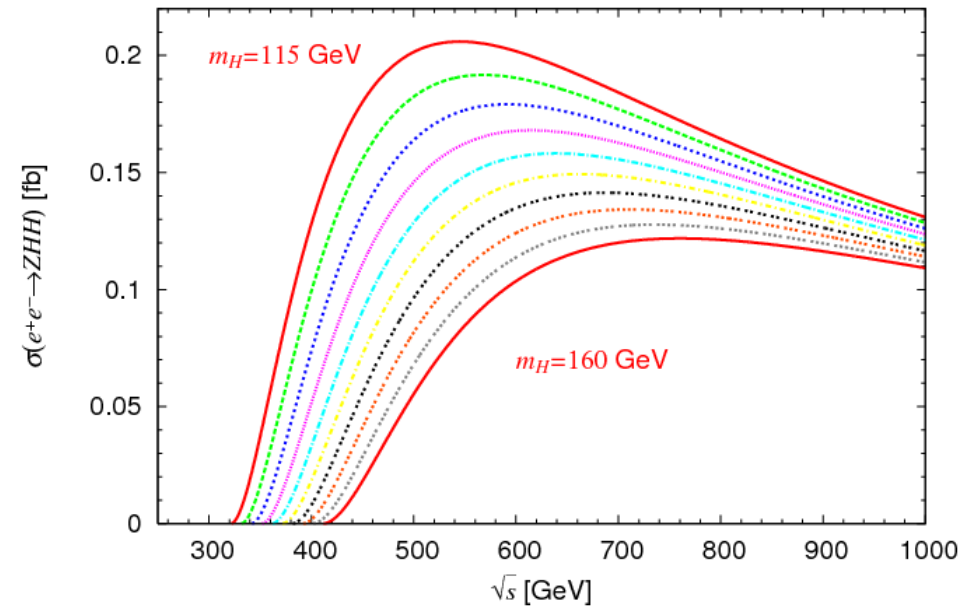
# Cross section of Zhh and W-fusion

At the ILC / CLIC, we can use two processes to measure the hhh coupling.

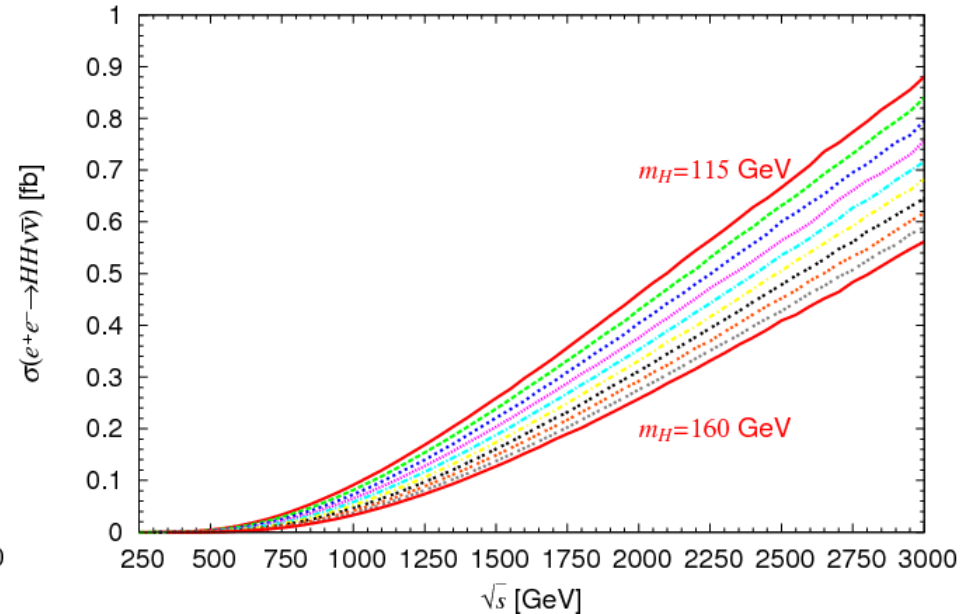
$$e^+e^- \rightarrow Zhh$$

$$e^+e^- \rightarrow hh\bar{\nu}\nu$$

Cross Section



Cross Section



The cross sections of Zhh and WW fusion processes at the ILC  
for  $m_h = 115 - 160$  GeV

At the 2<sup>nd</sup> stage of ILC (  $\sqrt{s} = 1$  TeV ) and CLIC, WW fusion process becomes dominant due to the t-channel enhancement.

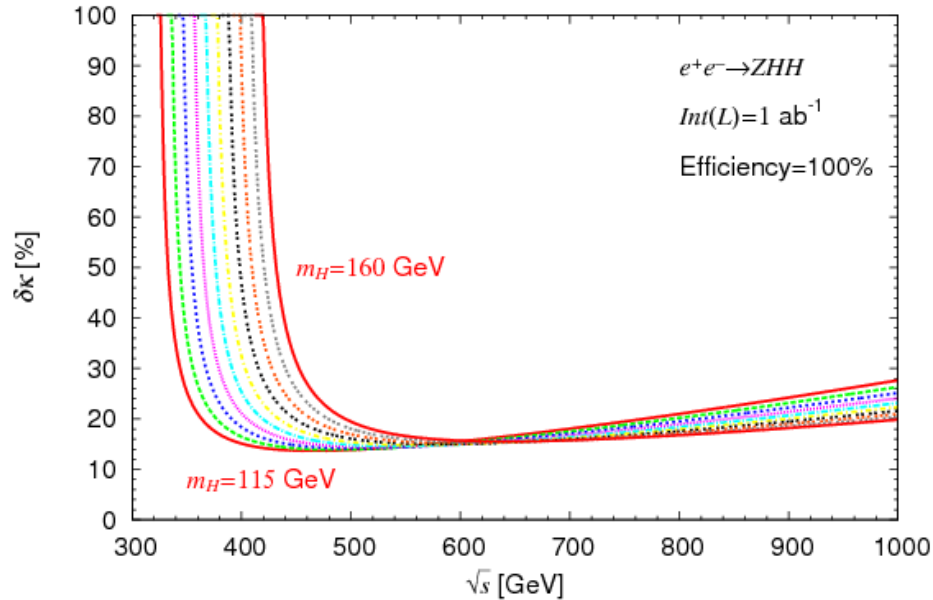
# hhh measurement at ILC / CLIC

The statistical sensitivity for the hhh coupling constant at the ILC and CLIC.

$$\lambda_{hhh} = \lambda_{hhh}^{\text{SM}} (1 + \delta\kappa)$$

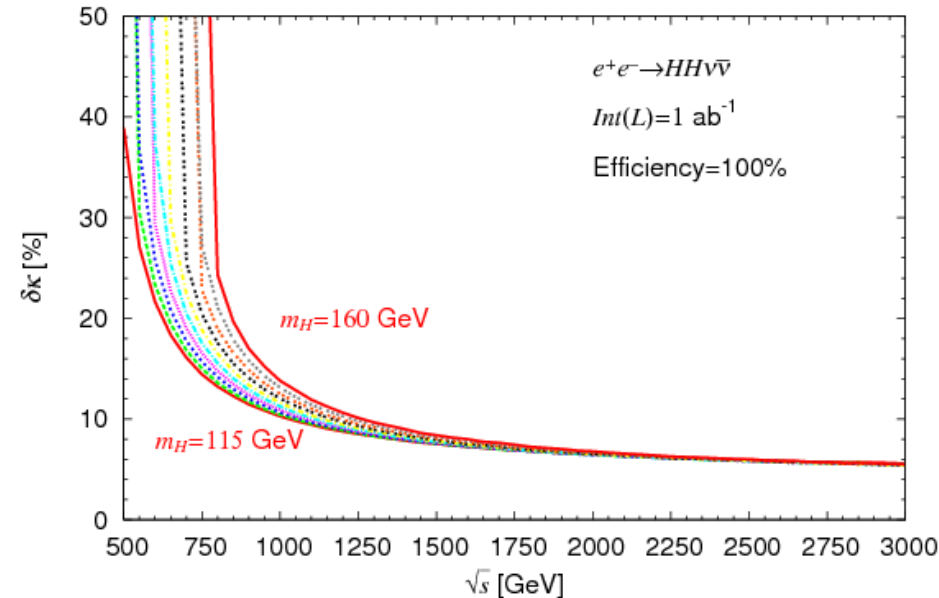
$$e^+e^- \rightarrow Zhh$$

Higgs Self-coupling Sensitivity



$$e^+e^- \rightarrow hh\bar{\nu}\nu$$

Higgs Self-coupling Sensitivity



At the 1<sup>st</sup> stage of the ILC (  $\sqrt{s} < 500$  GeV ), ZHH process is useful to measure the hhh coupling.

For  $m_h = 120$  GeV

Optimal energy for Higgs self-coupling measurement is  $\sqrt{s} = 400 - 500$  [GeV]

At multi-TeV collider, we can determine with an accuracy of 10% by using WW fusion process.

# New Physics effect on hhh coupling

Higgs mass is the only free parameter in the Higgs potential.

## Effective Higgs potential

$$V = \frac{1}{2}m_h^2 h^2 + \frac{1}{3!}\lambda_{hhh} h^3 + \frac{1}{4!}\lambda_{hhhh} h^4 + \dots$$

In the SM, tree level hhh (hhhh) couplings are uniquely defined by Higgs boson mass.

$$\lambda_{hhh}^{\text{SM}} = \frac{3m_h^2}{v}$$

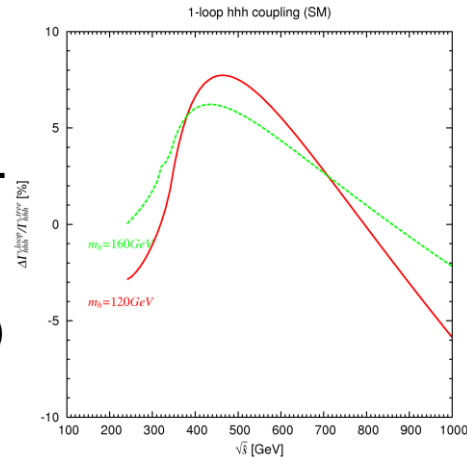
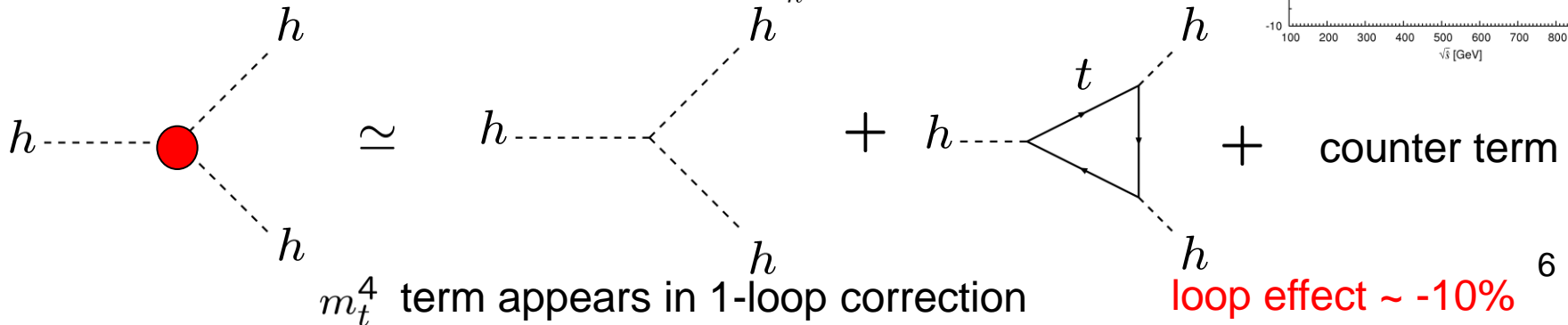
$$\lambda_{hhhh}^{\text{SM}} = \frac{3m_h^2}{v^2}$$

- Non-decoupling effect

In the SM, top loop correction is known as non-decoupling effect.

## Effective hhh coupling

$$\Gamma_{hhh}^{\text{SM}} \simeq \frac{3m_h^2}{v} - \frac{N_c m_t^4}{\pi^2 v^3} = \frac{3m_h^2}{v} \left[ 1 - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} + \dots \right] \equiv \lambda_{hhh}^{\text{SM}} (1 + \delta\kappa)$$

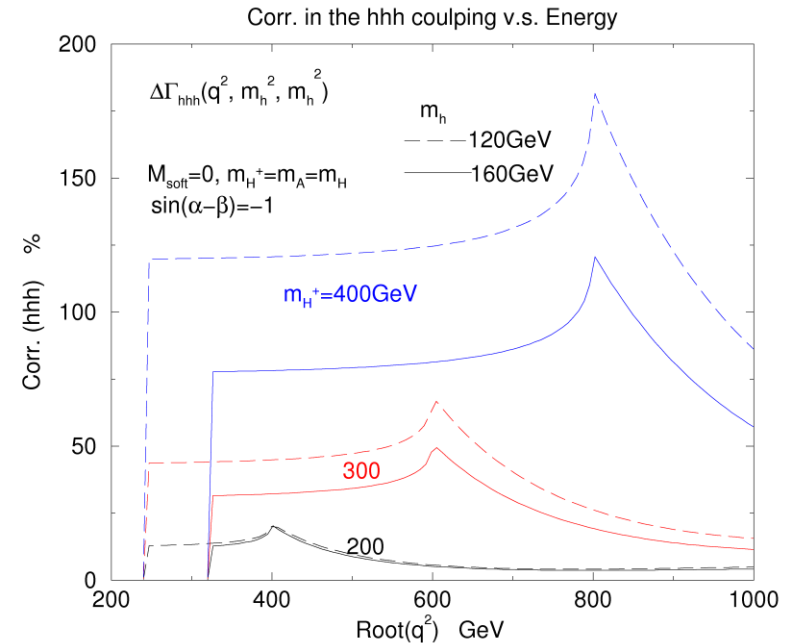
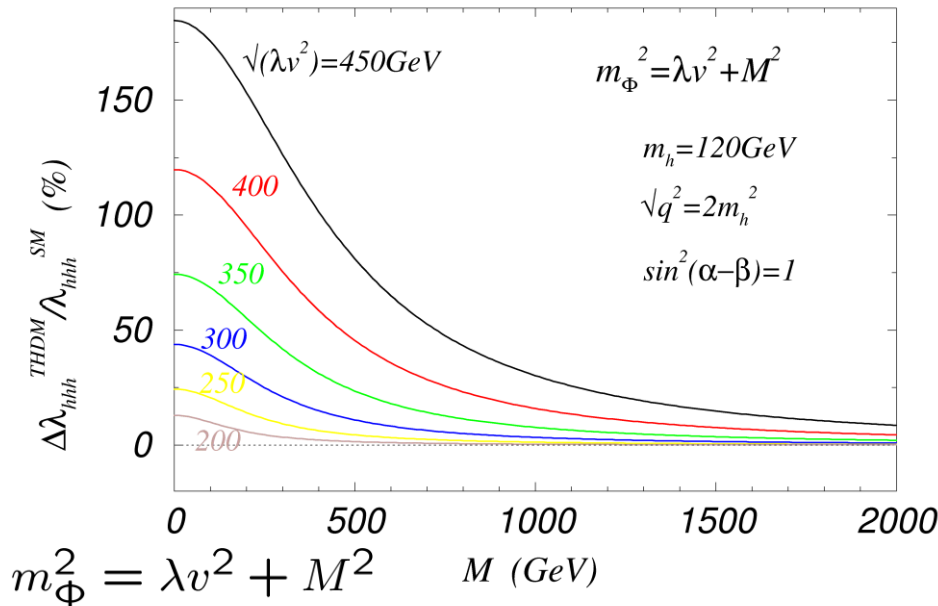


# Effective hhh coupling in THDM

S. Kanemura, Y. Okada, E. Senaha, C. P. Yuan

$M \sim 0$   
non-decoupling

$M \gg v$   
decoupling



Effective hhh coupling ( $\Phi = H, A, H^\pm$ )

$$\Gamma_{hhh}^{\text{THDM}} \simeq \frac{3m_h^2}{v} \left[ 1 + \sum_\Phi \frac{m_\Phi^4}{12\pi^2 v^2 m_h^2} \left( 1 - \frac{M^2}{m_\Phi^2} \right)^3 - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} \right]$$

$m_\Phi^4$  term appear in 1-loop correction

$$\frac{\Delta \Gamma_{hhh}^{\text{THDM}}}{\Gamma_{hhh}^{\text{SM}}} \equiv \frac{\Gamma_{hhh}^{\text{THDM}} - \Gamma_{hhh}^{\text{SM}}}{\Gamma_{hhh}^{\text{SM}}}$$

We set  $M=0$ .  $H, A, H^\pm$  receive their masses from the VEV.

heavier Higgs boson loop effect  $\sim 100\%$  non-decoupling

# THDM and Scalar LQ

In order to study the impact of the new physics effect on the double Higgs production processes at the LHC, ILC / CLIC and PLC, we focus on the following models.

1. Two Higgs doublet model (THDM) with SM-like limit ← Charged scalar particle

Higgs potential

$$V_{\text{THDM}} = \mu_1^2 |\Phi_1|^2 + \mu_2^2 |\Phi_2|^2 - (\mu_3^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ + \lambda_1 |\Phi_1|^4 + \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{\lambda_5}{2} \{(\Phi_1^\dagger \Phi_2)^2 + \text{h.c.}\}$$

SM-like limit  $\sin(\alpha - \beta) = -1$

Lightest Higgs has the same tree-level coupling as the SM Higgs boson and the other Higgs bosons do not couple to gauge bosons.

2. Scalar leptoquark (LQ) model ← Colored scalar particle

Higgs potential

$$V_{\text{LQ}} = V_{\text{SM}} + M_{\text{LQ}}^2 |\phi_{\text{LQ}}|^2 + \lambda_{\text{LQ}} |\phi_{\text{LQ}}|^4 + \lambda' |\phi_{\text{LQ}}|^2 |\Phi|^2$$

LQ-lepton-quark interaction

$$\mathcal{L} = (g_{1L} \bar{Q}^c i \tau_2 L + g_{1R} \bar{u}_R^c e_R) S_1 + \tilde{g}_{1R} \bar{d}_R^c e_R \tilde{S}_1 + \text{h.c.}$$

These couplings do not contribute to the double Higgs production processes.



# Chiral and Vector-like 4<sup>th</sup> generation

In addition to the SM Lagrangian, we introduce following Yukawa couplings.

These models have the colored fermion.

3. Chiral 4<sup>th</sup> generation model

Yukawa coupling

$$Q'_L = \begin{pmatrix} t'_L \\ b'_L \end{pmatrix} \quad t'_R \quad b'_R$$

$$\mathcal{L}_{\text{Yuk}} = -y_{t'} \bar{Q}'_L t'_R \tilde{\Phi} - y_{b'} \bar{Q}_L b'_R \Phi + \text{h.c.}$$

$$\text{S parameter} \quad \Delta S = \frac{N_c}{6\pi} \left( 1 - 2Y \ln \frac{m_u^2}{m_d^2} \right)$$

In order to avoid constraint from S and T parameters, we set  $m_{t'} - m_{b'} = 55 \text{ GeV}$

4. Vector-like 4<sup>th</sup> generation model

3<sup>rd</sup> generation quark

Vector-like singlet quark

Yukawa coupling

$$Q_{0L} = \begin{pmatrix} t_{0L} \\ b_{0L} \end{pmatrix} \quad + \quad t'_L \quad t'_R$$

$$\mathcal{L}_{\text{Yuk}} = -y_{t'} \bar{Q}_{0L} t'_{0R} \tilde{\Phi} - M t'_{0L} t'_{0R} + \text{h.c.}$$

We assume that vector-like quark only mix with 3<sup>rd</sup> generation quark.

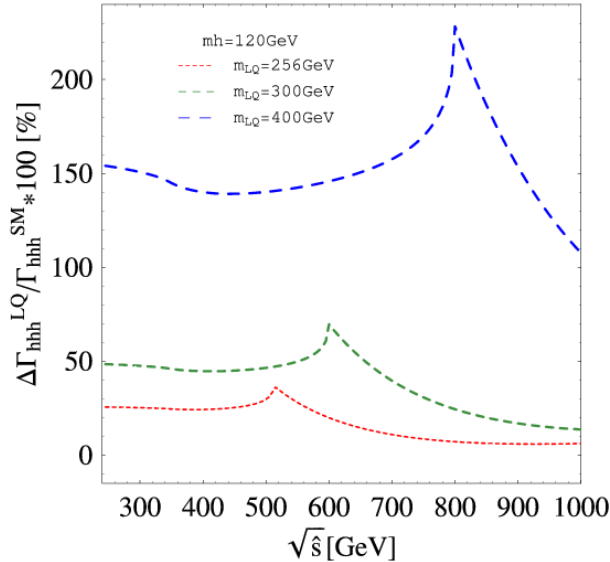
$$\begin{pmatrix} t_X \\ t'_X \end{pmatrix} = \begin{pmatrix} c_X & -s_X \\ s_X & c_X \end{pmatrix} \begin{pmatrix} t_{0X} \\ t'_{0X} \end{pmatrix} \quad (X = L, R)$$

S and T parameter  Allowed parameter space.  $y_{t'} = 1, M \geq 1 \text{ TeV}$

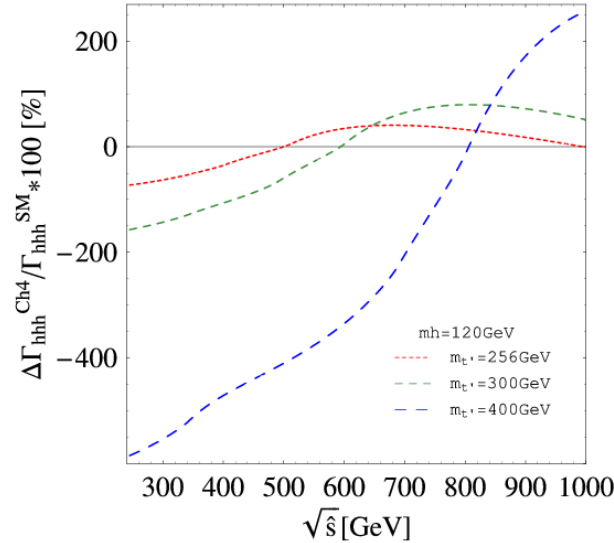
# Effective hhh coupling in LQ and 4<sup>th</sup> generation model

For  $m_h = 120$  GeV

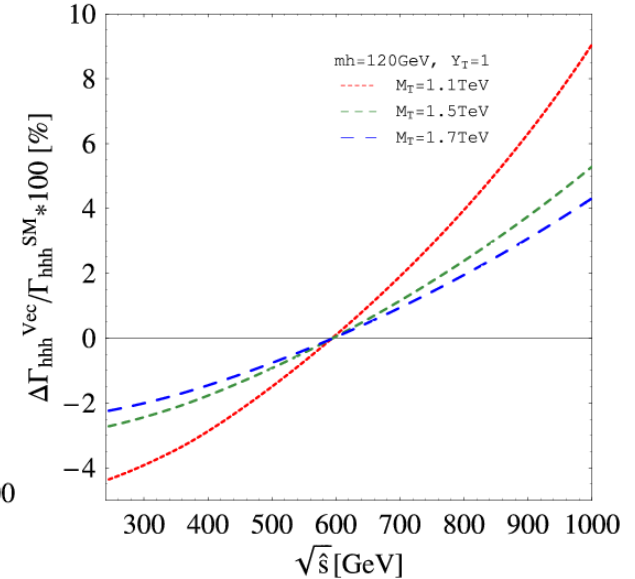
Scalar LQ



Chiral 4<sup>th</sup> generation



Vector-like 4<sup>th</sup> generation



## Effective hhh coupling

Scalar LQ

We set  $M_{LQ} = 0$

$$\Gamma_{hhh}^{LQ} \simeq \frac{3m_h^2}{v} \left[ 1 + \frac{N_c m_{\phi_{LQ}}^4}{12\pi^2 v^2 m_h^2} \left( 1 - \frac{M_{LQ}^2}{m_{\phi_{LQ}}^2} \right)^3 - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} \right]$$

Chiral 4<sup>th</sup> generation

$$\Gamma_{hhh}^{Ch4} \simeq \frac{3m_h^2}{v} \left[ 1 - \frac{N_c (m_{t'}^4 + m_{b'}^4)}{3\pi^2 v^2 m_h^2} - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} \right]$$

Vector-like 4<sup>th</sup> generation

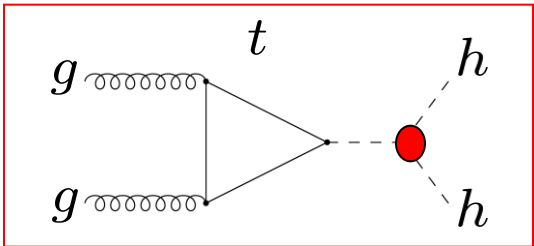
$$\Gamma_{hhh}^{Vec} \simeq \frac{3m_h^2}{v} \left[ 1 - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} \frac{m_t^2}{M^2} - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} \right] \quad (M \geq 1 \text{ TeV})$$

LHC

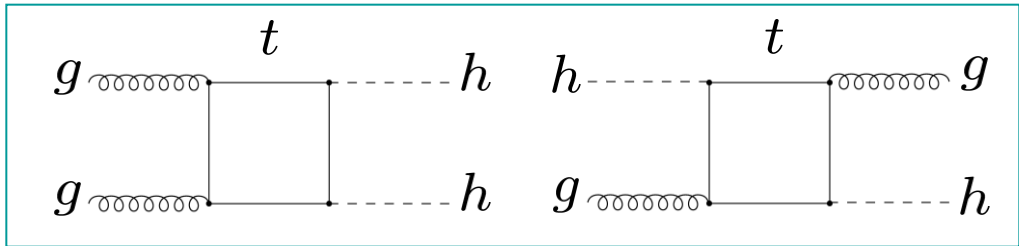
$$gg \rightarrow hh$$

$\mathcal{M}(l_1, l_2)$  top loop diagrams

triangle

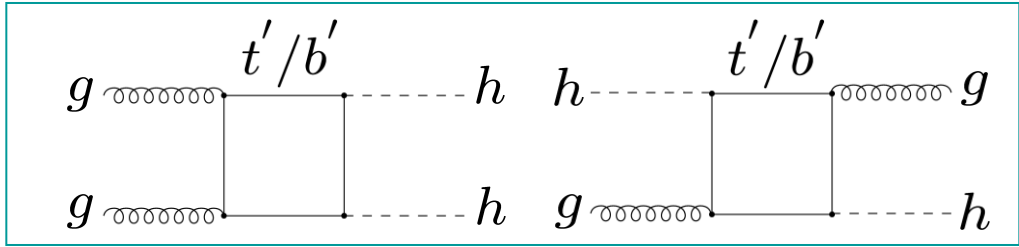
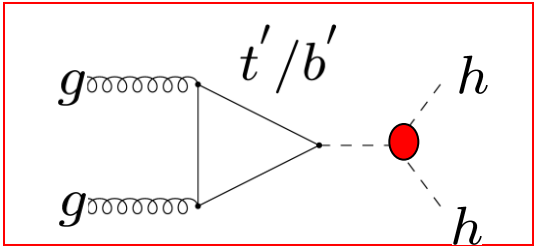


box

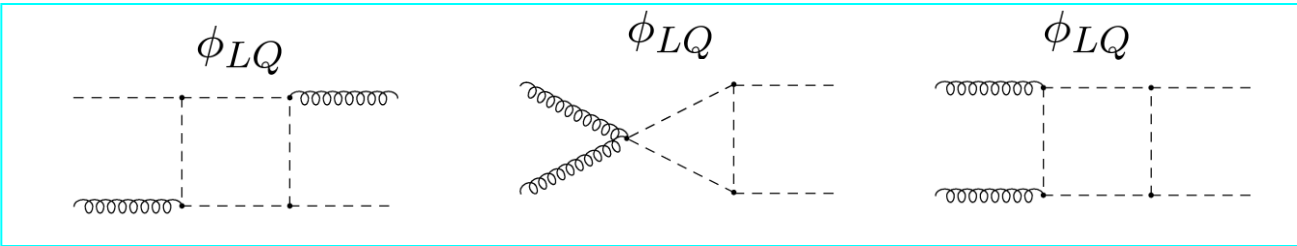
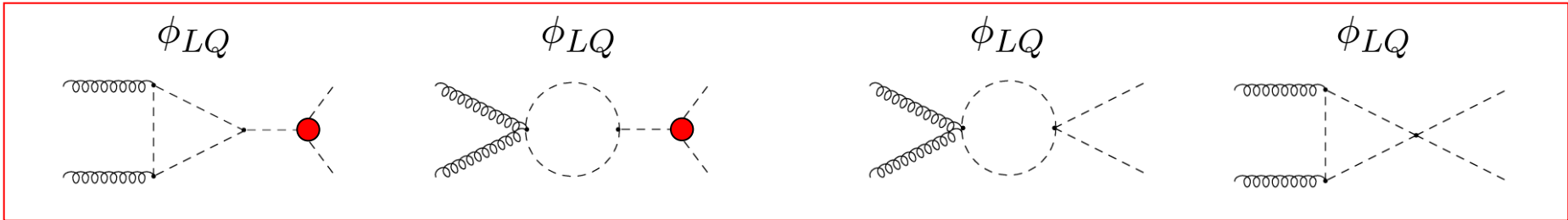


$\Delta\mathcal{M}(l_1, l_2)$  Additional one-loop diagrams

4<sup>th</sup> generation



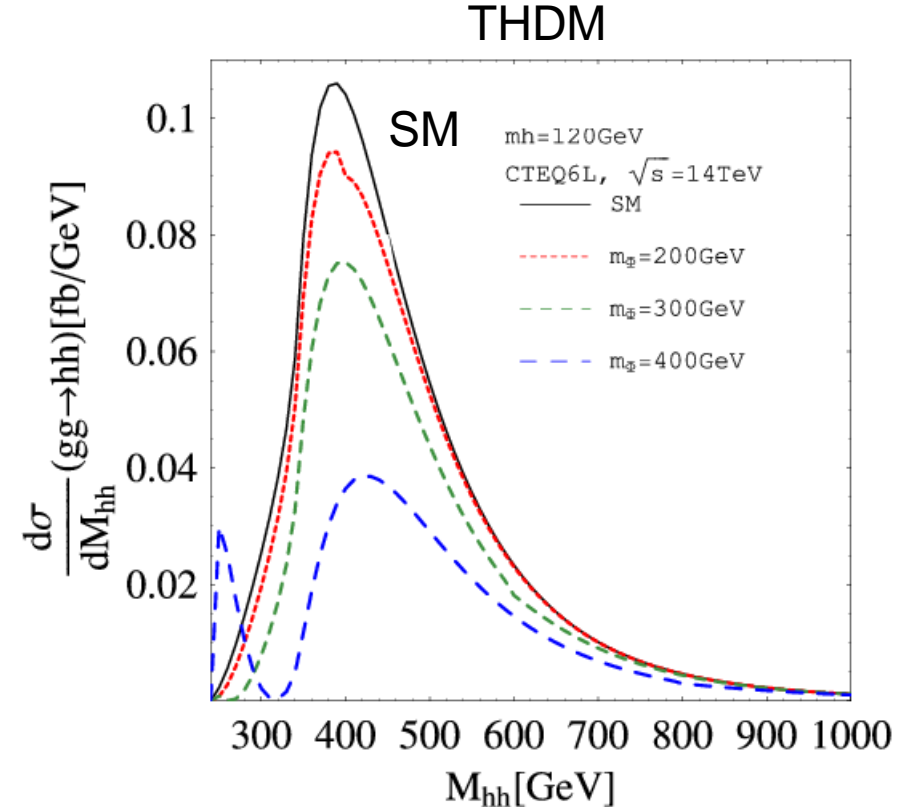
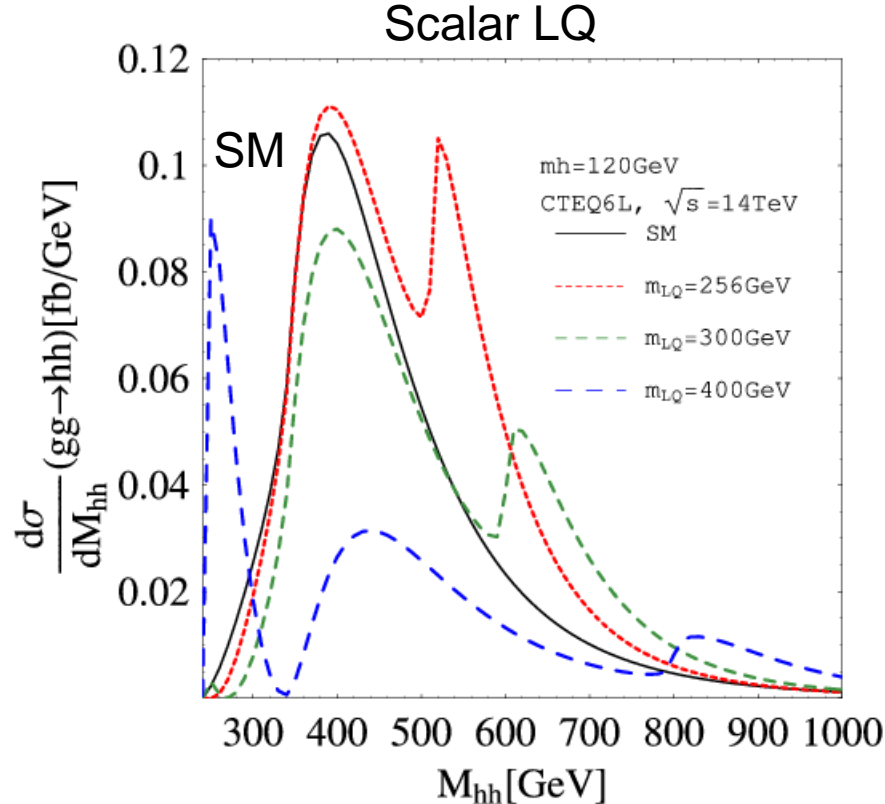
Scalar LQ



# Gluon fusion process in Scalar LQ and THDM

Invariant mass distribution of gluon fusion process

For  $m_h = 120$  GeV



$M_{hh} \sim 250$  GeV

This peak comes from the large  $hhh$  coupling constant through the triangle diagram

$M_{hh} \sim 400$  GeV

Interference effect of triangle and box diagrams.

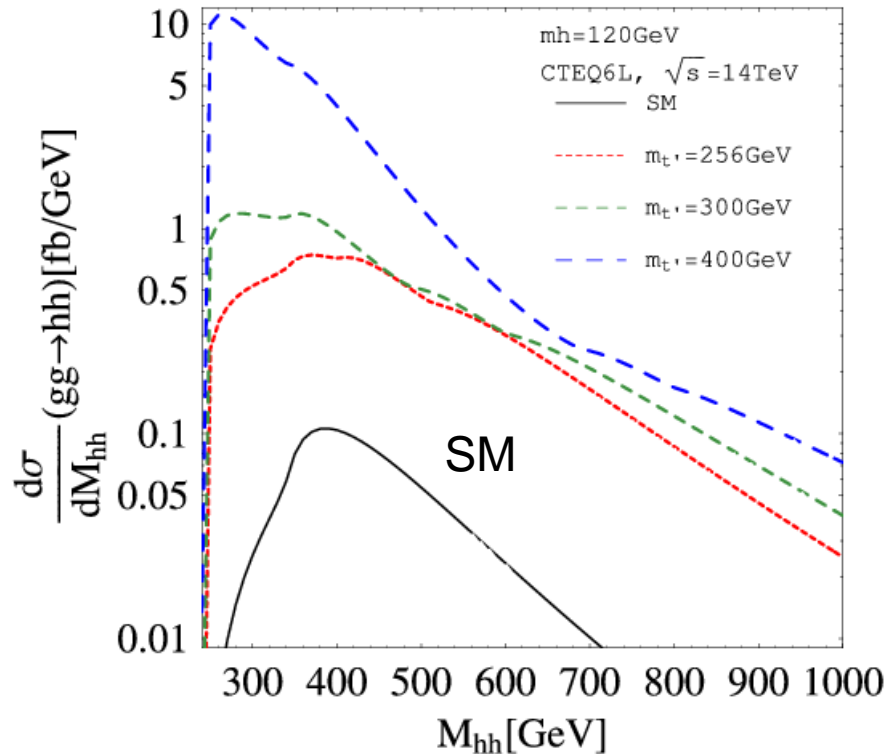
These two contributions are destructive to each other

# Gluon fusion process in 4<sup>th</sup> generation model

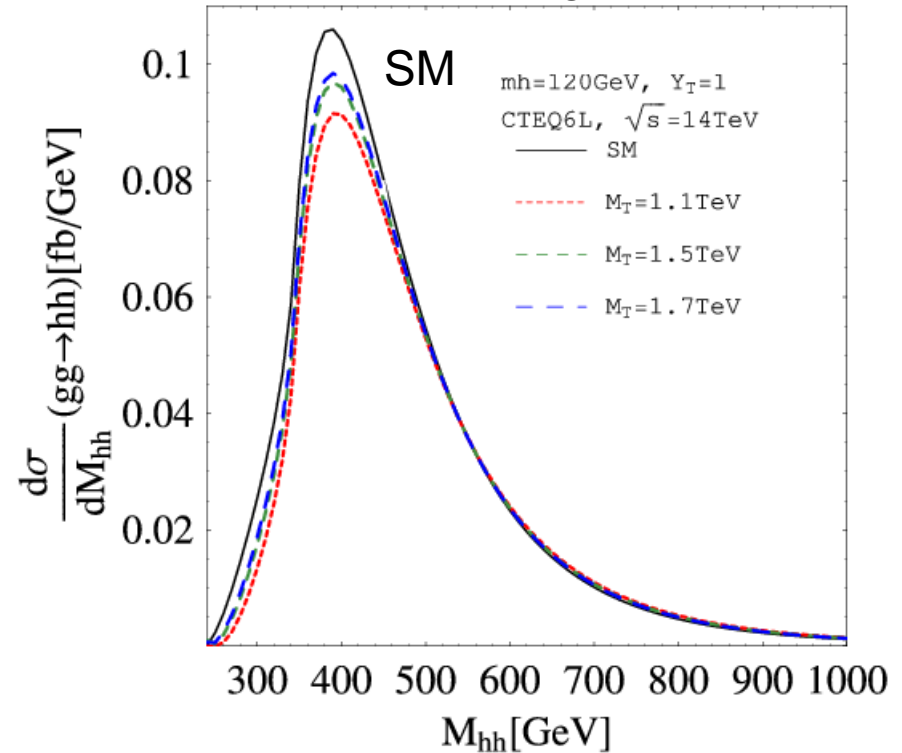
Invariant mass distribution of gluon fusion process

For  $m_h = 120$  GeV

Chiral 4<sup>th</sup> generation



Vector-like 4<sup>th</sup> generation



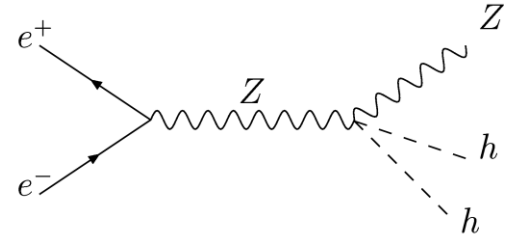
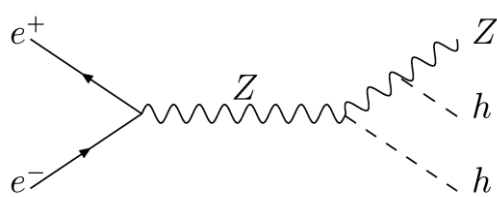
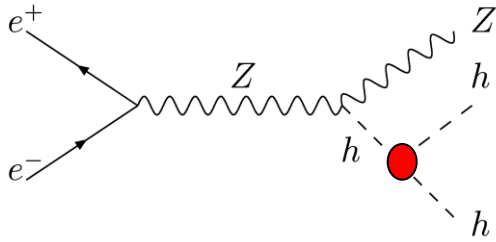
The cross section of the chiral 4<sup>th</sup> generation model can be 10-100 times larger than that of the SM.

In the vector-like 4<sup>th</sup> generation model, the deviations of the cross section from the SM value are at most 5%, which can not be large because of their decoupling nature.

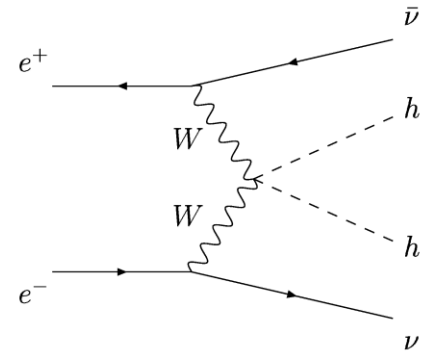
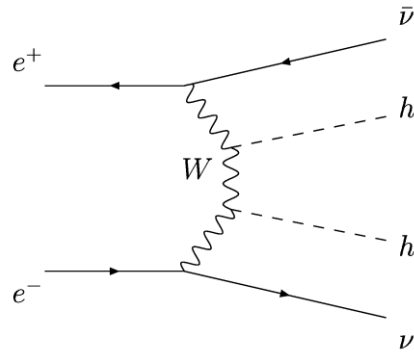
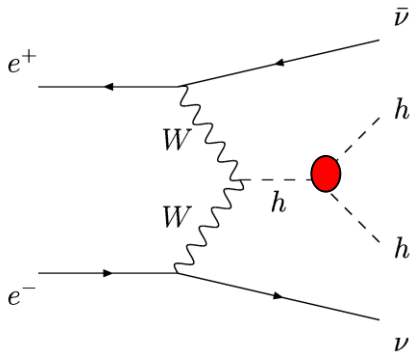
**ILC / CLIC**

# New Physics effect on Zhh and WW fusion

$$e^+e^- \rightarrow Zhh$$



$$e^+e^- \rightarrow hh\bar{\nu}\nu$$





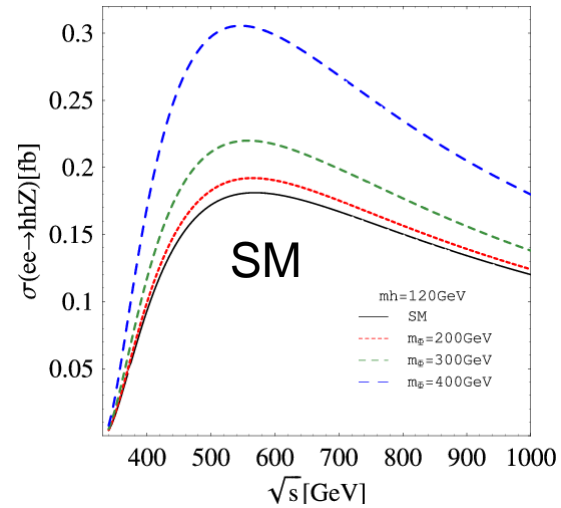
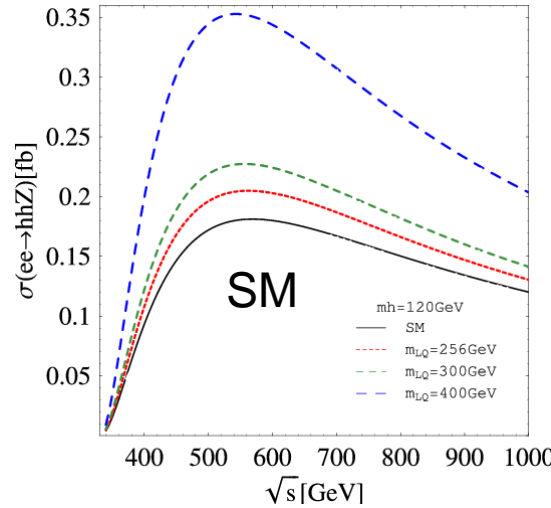
# Zhh and WW fusion in Scalar LQ and THDM

For  $m_h = 120$  GeV

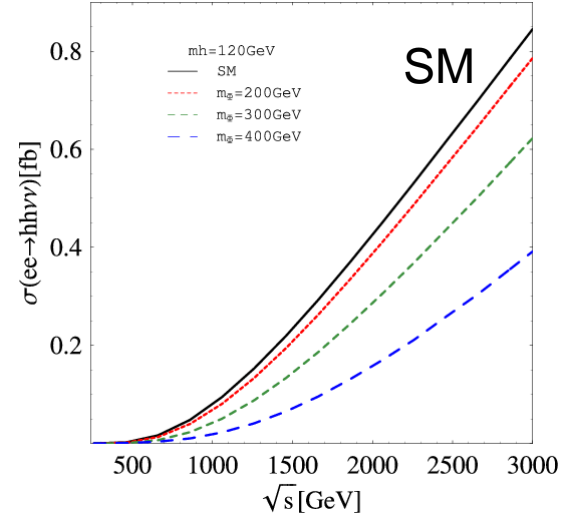
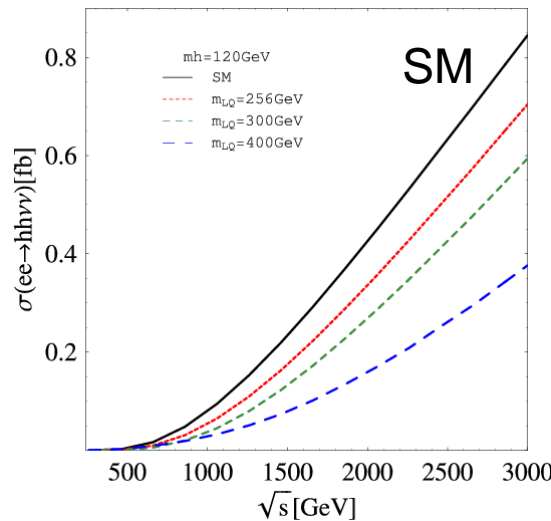
Scalar LQ

THDM

$$e^+e^- \rightarrow Zhh$$



$$e^+e^- \rightarrow hh\nu\nu$$



The cross section of WW fusion becomes small because of the negative interference.

The anomalous hhh coupling dependence in the cross section of WW fusion is opposite to that in Zhh process.

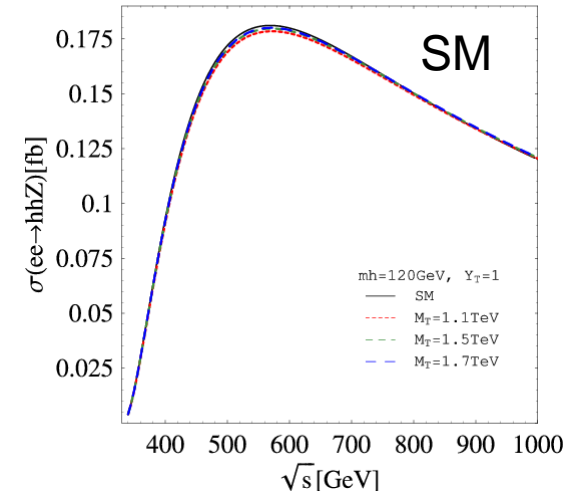
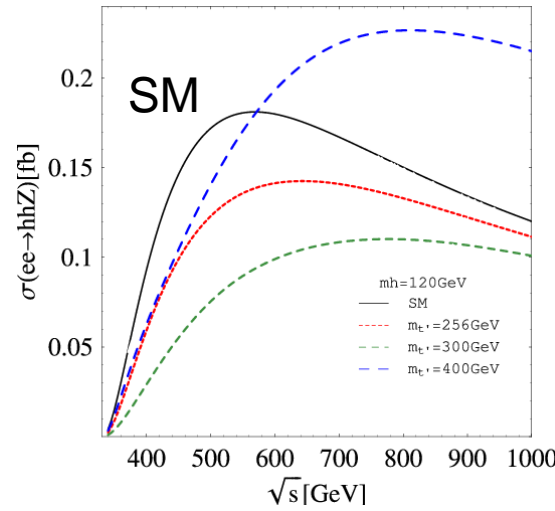
# Zhh and WW fusion in 4<sup>th</sup> generation model

For  $m_h = 120$  GeV

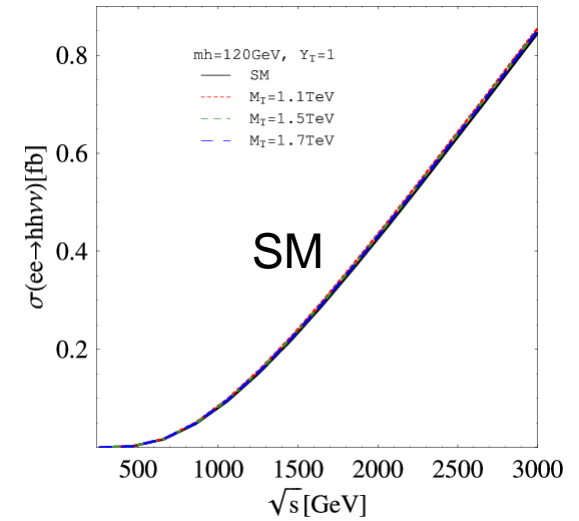
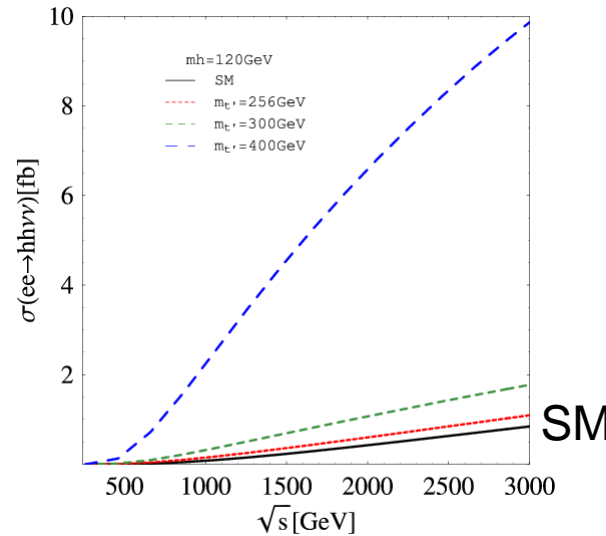
$$e^+e^- \rightarrow Zhh$$

Chiral 4<sup>th</sup> generation

Vector-like 4<sup>th</sup> generation



$$e^+e^- \rightarrow hh\nu\bar{\nu}$$



In the chiral 4<sup>th</sup> generation model, the production rate becomes significantly large.

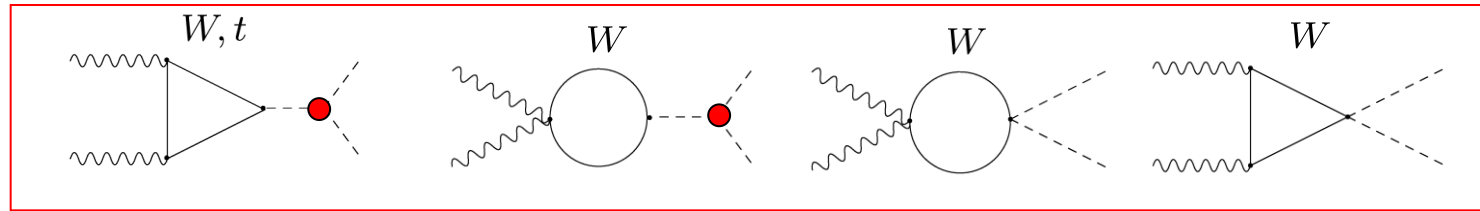
The impact of the vector-like quark is quite small in these processes.

# PLC

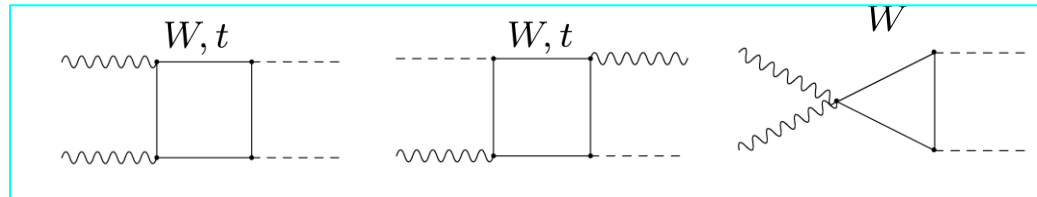
$$\gamma\gamma \rightarrow hh$$

$\mathcal{M}(l_1, l_2)$  W boson and top loop diagrams

triangle diagrams

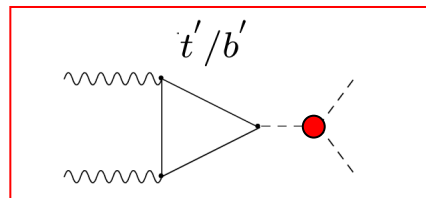


box diagrams

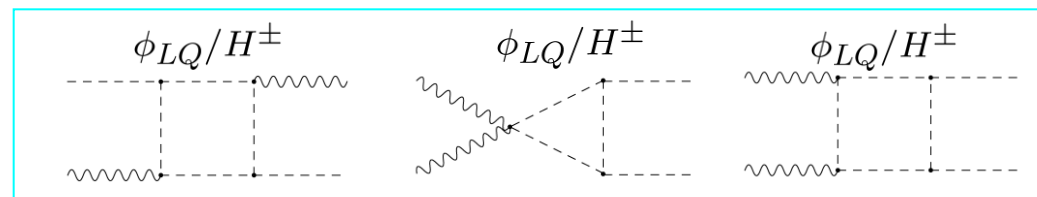
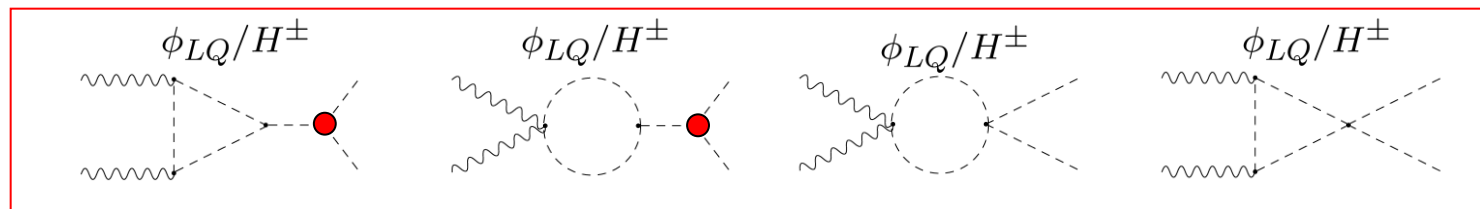


$\Delta\mathcal{M}(l_1, l_2)$  Additional one-loop diagrams

4<sup>th</sup> generation



Scalar LQ / THDM with SM-like limit

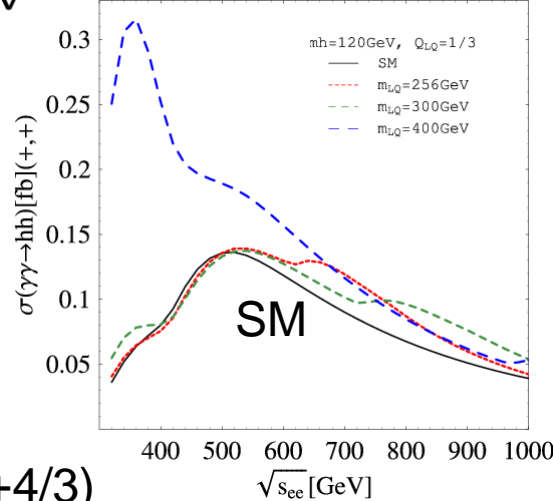


# Full cross section in Scalar LQ and THDM

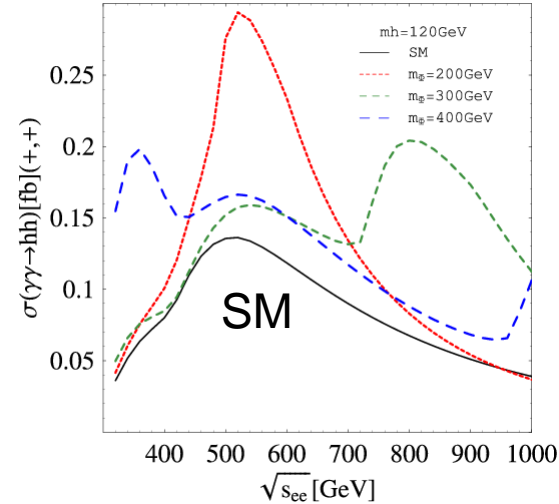
Cross section of  $e^-e^- \rightarrow \gamma\gamma \rightarrow hh$  process at PLC

For  $m_h = 120$  GeV

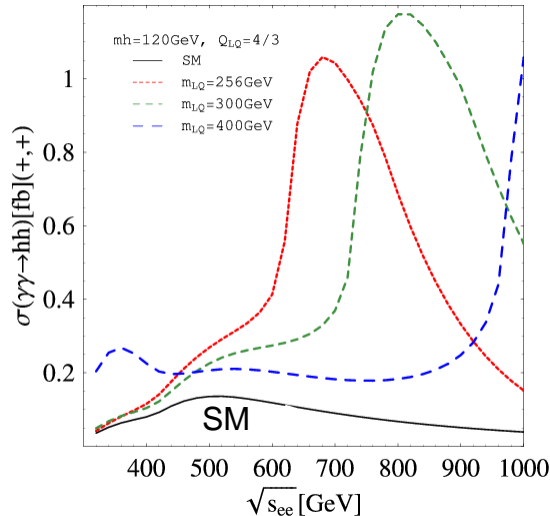
Scalar LQ (Q=+1/3)



THDM



Scalar LQ (Q=+4/3)



$\sqrt{s_{ee}} \sim 350$  GeV

Cross section is enhanced by the effective hhh coupling

$\sqrt{s_{ee}} \sim 500$  GeV

Threshold enhancement of top pair production

$\sqrt{s_{ee}} > 600$  GeV

Threshold enhancement of charged Higgs (Scalar LQ)  
pair production in THDM (LQ)

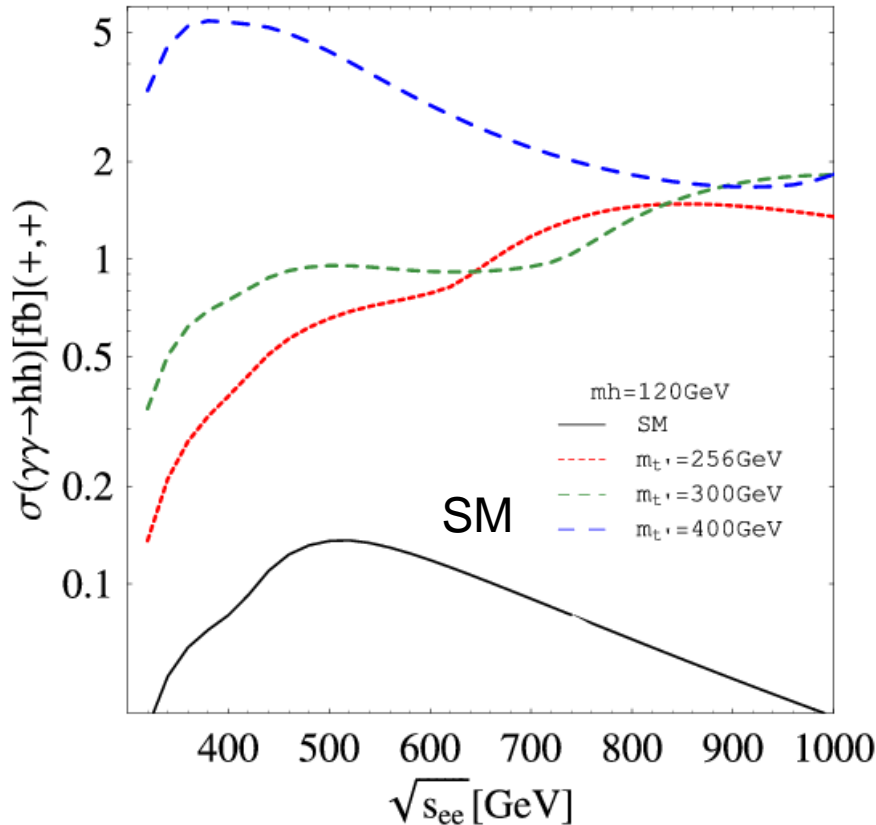
The effects of scalar LQs depend on not only their masses but also their electric charges.  $\mathcal{M}_{LQ} \propto N_c Q_s^2$  21

# Full cross section in 4<sup>th</sup> generation model

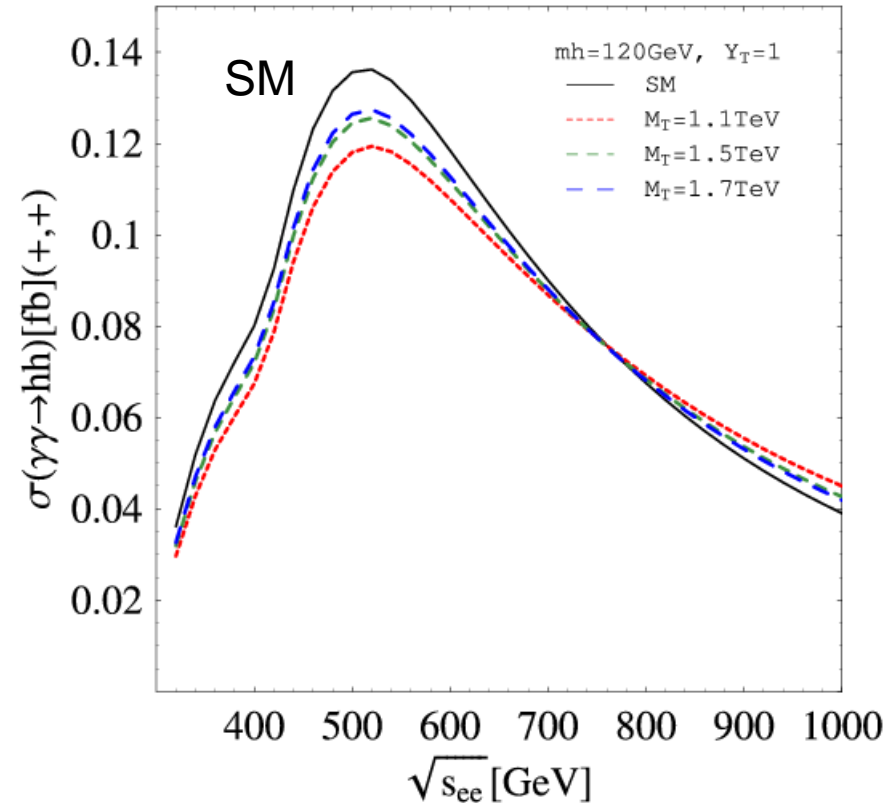
Cross section of  $e^-e^- \rightarrow \gamma\gamma \rightarrow hh$  process at PLC

For  $m_h = 120$  GeV

Chiral 4<sup>th</sup> generation



Vector-like 4<sup>th</sup> generation



In the chiral 4<sup>th</sup> generation model, fourth generation fermions contribute to both triangle and box diagrams can enhance the cross section by a factor of 10 for wide range of  $\sqrt{s_{ee}}$

In the vector-like 4<sup>th</sup> generation model, new physics effects are small.

# Summary

We studied double Higgs production processes at LHC, ILC / CLIC and PLC in THDM with SM-like limit, scalar LQ, chiral and vector-like 4th generation model.

- The cross section is largely changed by two effects.
  - additional contribution of new particle loop  
PLC, LHC
  - Effective 1-loop hhh vertex enhanced by the non-decoupling effect  
ILC / CLIC, PLC, LHC
- These four Higgs boson pair production processes at different colliders can play complementary roles in exploring new physics through the Higgs sector.

Additional particles in new physics model can also significantly affect the  $gg \rightarrow hh$  and  $\gamma\gamma \rightarrow hh$  processes according to their color and electric charges.

- Double Higgs production process is useful to distinguish 4<sup>th</sup> generation quark is whether chiral or vector-like model.

In the vector-like 4<sup>th</sup> generation model, a non-decoupling limit cannot be taken due to the severe experimental constraints

- The deviation of the cross section from the SM strongly depend on each new physics model.

$$\sqrt{s} = 400 - 500 \text{ GeV} \quad \sqrt{s} = 500 \text{ GeV} \quad \sqrt{s} = 1 - 3 \text{ TeV}$$

Model	$m_h[\text{GeV}]$	$\frac{\Gamma_{hhh}^{\text{NP}} - \Gamma_{hhh}^{\text{SM}}}{\Gamma_{hhh}^{\text{SM}}}$	$\Delta r_{\text{NP}}^{gg \rightarrow hh}$	$\Delta r_{\text{NP}}^{e^+e^- \rightarrow hhZ}$	$\Delta r_{\text{NP}}^{\gamma\gamma \rightarrow hh}$	$\Delta r_{\text{NP}}^{e^+e^- \rightarrow hh\nu\bar{\nu}}$
THDM	120	+120%	-50%	+(80-70)%	+50%	-(80-50)%
THDM	160	+70%	-50%	+(60-50)%	+110%	-(80-50)%
LQ( $Q = 1/3, 4/3$ )	120	+150%	-40%	+(110-100)%	+130%, +100%	-(70-60)%
LQ( $Q = 1/3, 4/3$ )	185	+60%	-30%	+50%	+150%, +150%	-(80-50)%
Ch4	120	-590%	+7800%	-(30-20)%	+3100%	+(260-110)%
Ch4	210	-140%	+2200%	—	—	+(970-210)%
Vec	120	-4%	-10%	-2%	-10%	+(5-1)%
Vec	160	-2%	-5%	-1%	-10%	+(3-0)%



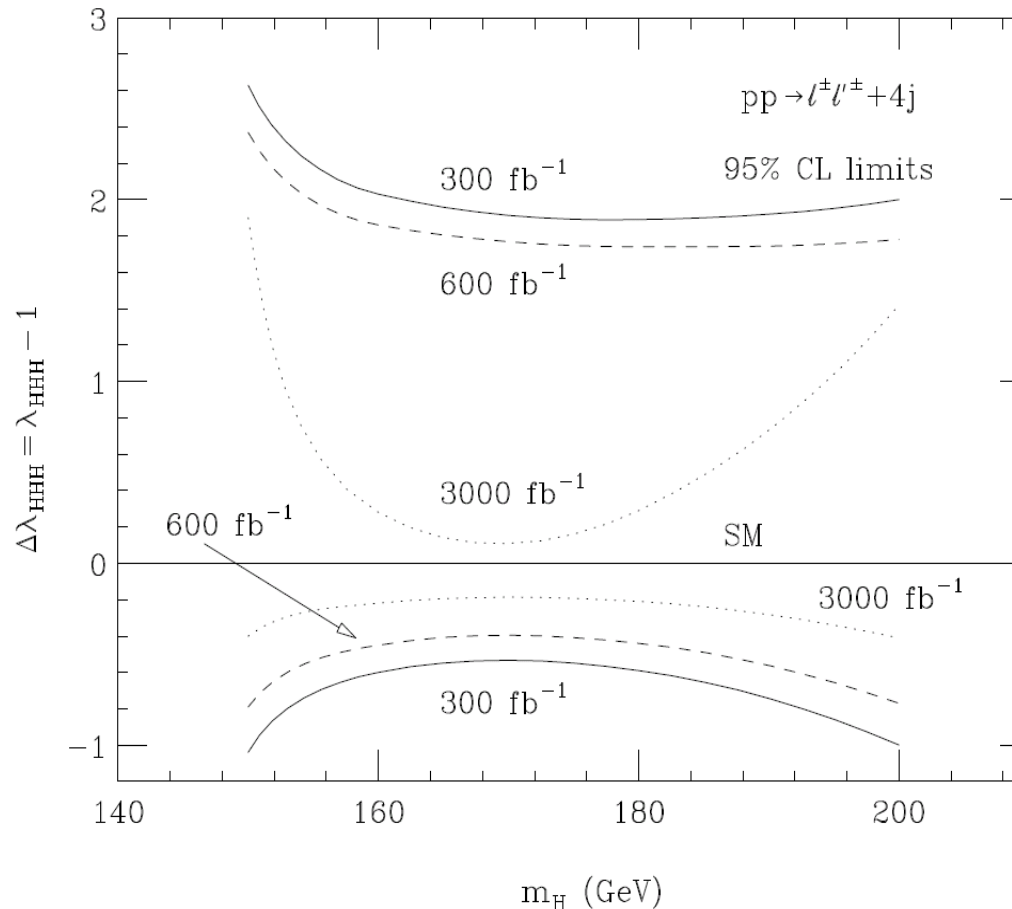
# Backup Slide

# hhh measurement at the LHC

U. Baur, T. Plehn, D. Rainwater

$$\lambda_{hhh} = \lambda_{hhh}^{\text{SM}}(1 + \delta\kappa)$$

$$pp \rightarrow hh \rightarrow (W^+W^-)(W^+W^-) \rightarrow l^\pm l'^\pm + 4j$$



$$\lambda_{hhh} = \lambda_{hhh}^{\text{SM}} = \frac{3m_h^2}{v} \quad (\delta\kappa = 0)$$

At the LHC, vanishing Higgs self-coupling is excluded.  $\lambda_{hhh} = 0$  ( $\delta\kappa = -1$ )

At the SLHC, Higgs self-coupling can be determined with an accuracy of 20-30%.  
 $160\text{GeV} \leq m_h \leq 180\text{GeV}$

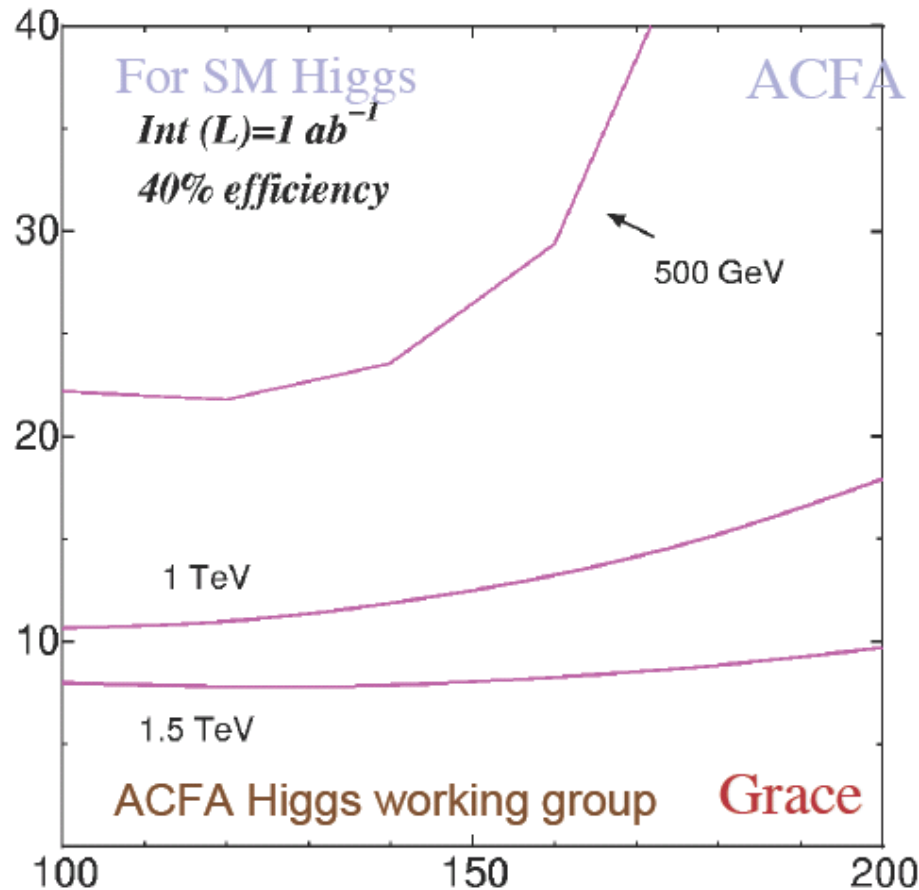
# hhh measurement at the ILC

ACFA Higgs Working Group 2002

$$\lambda_{hhh} = \lambda_{hhh}^{\text{SM}}(1 + \delta\kappa)$$

$\delta\Lambda/\Lambda$  [%]

Higgs self coupling sensitivity



$$\int \mathcal{L} dt = 1 \text{ ab}^{-1}$$

1<sup>st</sup> ILC

$$\sqrt{s} = 500 \text{ GeV}$$

At the 1<sup>st</sup> ILC, Higgs self-coupling can be determined with an accuracy of 20-30 %.

$$m_h < 170 \text{ GeV}^{27}$$

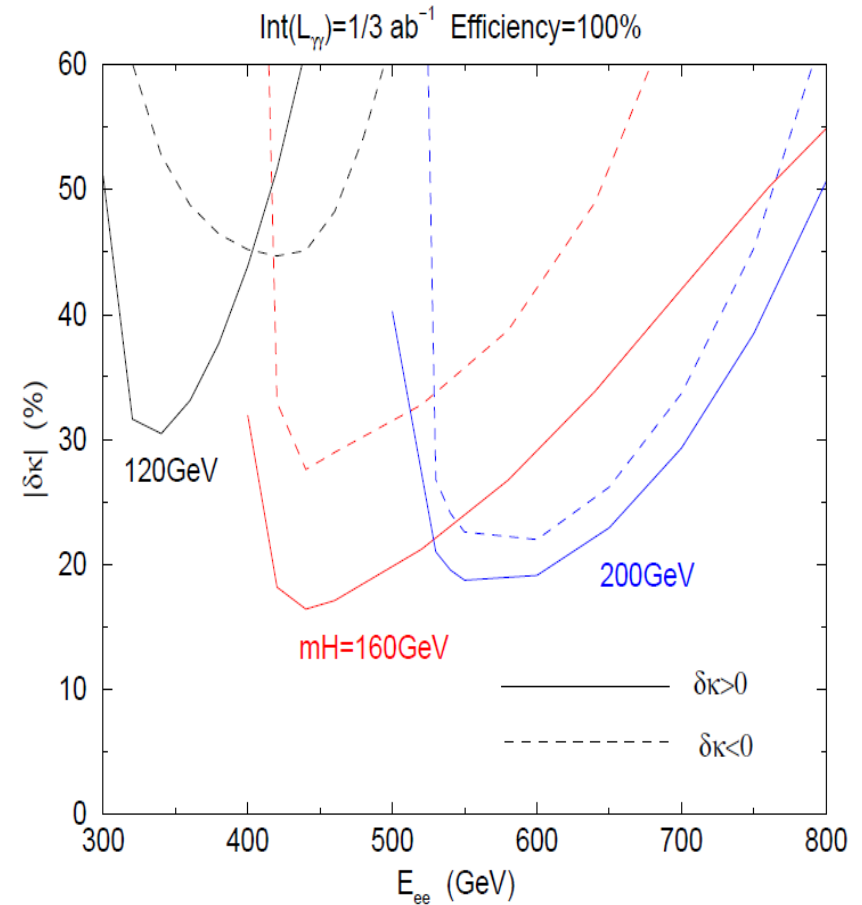
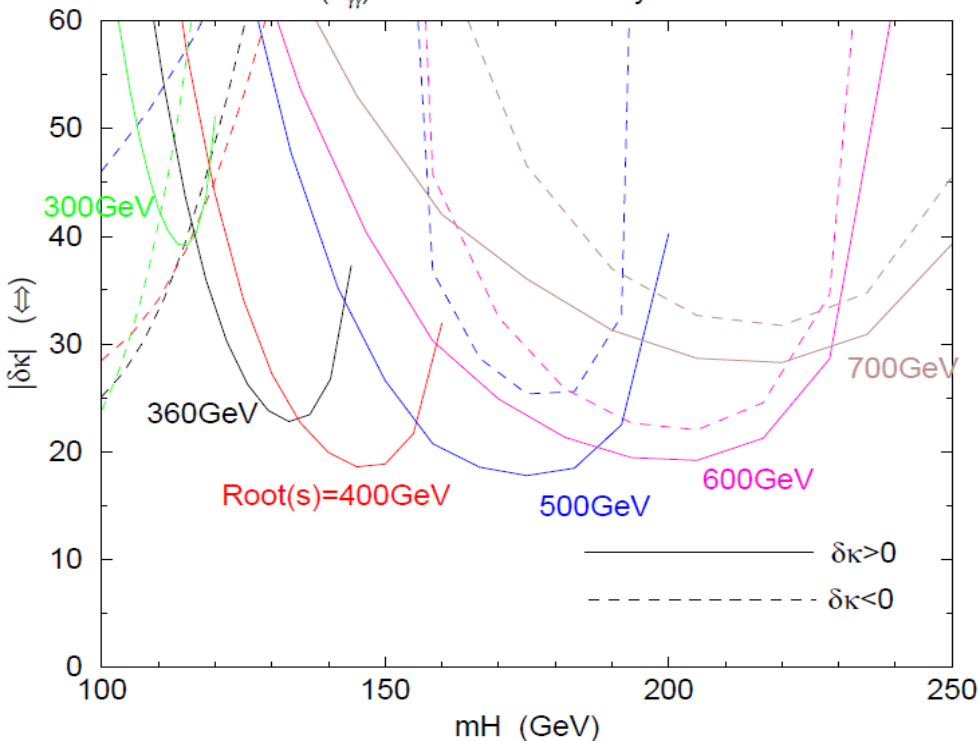
# hhh measurement at the PLC

E.Asakawa, D. Harada, S. Kanemura, Y. Okada, K. Tsumura at TILC 08

## Higgs Self Coupling Sensitivity

### Higgs self coupling sensitivity

$\text{Int}(\mathcal{L}_{\gamma\gamma})=1/3\text{ab}^{-1}$  Efficiency 100%



Photon linear collider ( $E_{ee} < 500\text{GeV}$ ) is useful to measure the HHH coupling for  $m_H = 150\text{-}200$ .

# Sensitivity

- Sensitivity

$$N = L_{\gamma\gamma}\sigma(0)$$

$$N \pm \sqrt{N} = L_{\gamma\gamma}\sigma(\Delta\kappa)$$

$$L_{\gamma\gamma}\sigma(\delta\kappa)$$

