



Higgs Recoil Study for ILC

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ILD Analysis/Software Meeting
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Outline

Updates to the Higgs Recoil Study $m_H = 125$ GeV

Recoil Mass Study

- Estimate Higgs mass and cross section **model independently**.
→ Check cut efficiency uniformity for each Higgs decay modes.
- Improve fitting method.
- Try to estimate mass precision by **mass template method**.
- Semi-model independent analysis is also tried.
- We compare different polarization scenarios.

CP-mixture Study

- CP-mixture η (coefficient of CP odd Higgs amplitude) can be measured from **Z boson production angle**.
- Check $\cos\theta$ distribution by extrapolating number of events from recoil mass fitting, and look at the **asymmetry**.
- η should be calculated also by samples with anomalous coupling for ZZH.

Short Summary for

RECOIL MASS STUDY

Lepton Selections and BG Rejections

Production Mode	Higgs mass (GeV)	E_{CM} (GeV)	Integrated Luminosity	Spin Polarization	Detector Simulation
$e^+e^- \rightarrow Zh \rightarrow \mu\mu h, eeh$	125	250	250 fb^{-1}	$P(e^-, e^+) = (\mp 0.8, \pm 0.3)$	ILD_01_v05 (DBD ver.)

- Lepton selection

- di-lepton (μ, e) selection : based on deposited energy in CAL
- Good track selection : based on error in forward/barrel
- Impact parameter (for di-muon) : to suppress μ from τ decays
- Bremsstrahlung recovery (for di-electron)

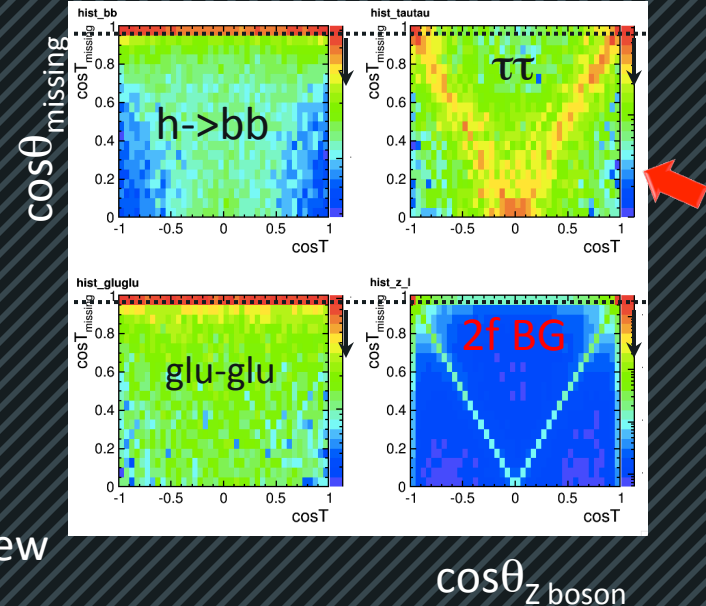
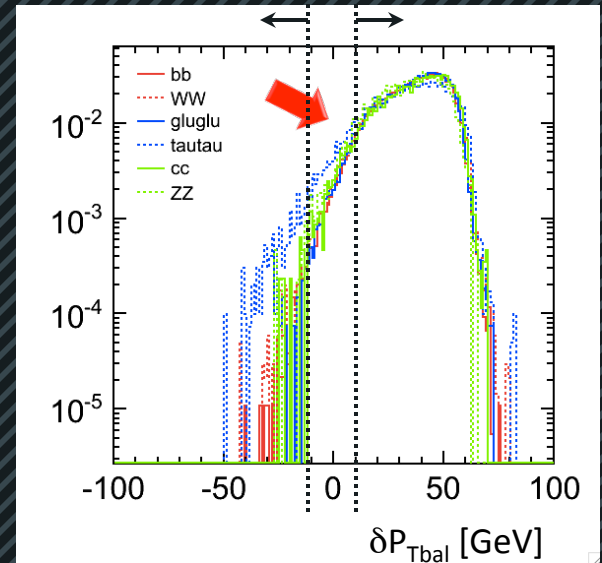
- BG rejection

p_{Tdl}	Transverse momentum of di-lepton
M_{dl}	Invariant mass of di-lepton
acoplanarity	Balance of di-lepton azimuth
δP_{Tbal}	Balance b/w PT of di-lepton & photon
$ \cos\theta_{miss} $	Angle of undetected particles
M_{recoil}	Recoil mass
Likelihood	$M_{dl}, \cos\theta_{dl}, P_{Tdl},$ acoplanarity

$\mu\mu h$	signal	ll	ll $\nu\nu$	lfff
No Cut	2603	3.2M	507166	390041
After Cut	1386	322	1479	1054
eeh	signal	ll	ll $\nu\nu$	lfff
No Cut	2729	7.8M	520624	404279
After Cut	1190	1496	2203	937

Unbiased Selection

- δP_{Tbal} and $\cos\theta_{missing}$ cut has bias for Higgs decay modes especially $h \rightarrow \tau\tau$.
- To avoid this bias problem, some additional conditions are needed
- $\delta P_{Tbal} = P_{Tdl} - P_{Tphoton}$
 - photon should satisfy ...
 - $m_{2\gamma} > 0.2$ [GeV]
 - or $E_{\gamma} > 60$ [GeV]
- $\cos\theta_{missing}$: $\cos\theta$ of all PFOs
 - $|\cos\theta_{missing}| < 0.99$
 - or $|\cos\theta_{Zboson}| < 0.8$
- These additional condition **avoid bias**, but efficiency of **BG rejection** is sacrificed.



	bb	glu-glu	$\tau\tau$	BG (II)
$\cos\theta_{miss} < 0.99$	95.1%	92.8%	99.2%	41.1%
$\cos\theta_{miss} < 0.99$ or $ \cos\theta < 0.8$	99.3%	99.1%	99.8%	74.6%

← New

Signal Efficiency

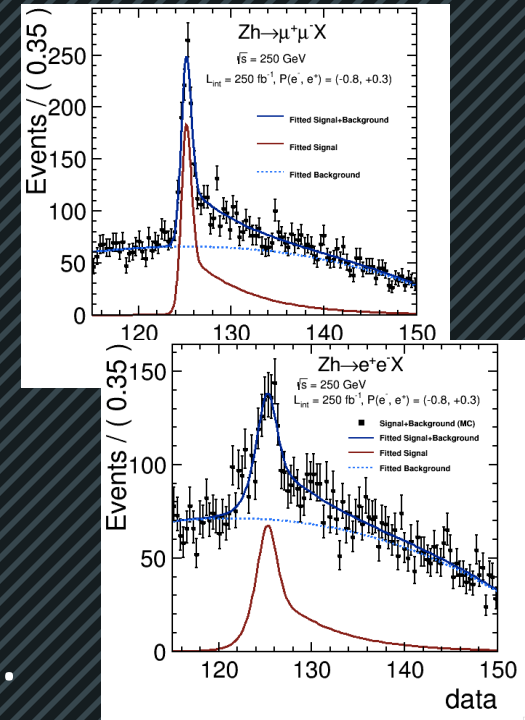
- After that, bias of signal efficiency for Higgs decay is eliminated.

H decay mode	$\mu\mu h$ efficiency [%]	eeh efficiency [%]
bb	55.61	45.62
WW	55.39	44.95
gluglu	55.16	45.02
$\tau\tau$	55.42	44.49
cc	55.60	45.14
ZZ	54.04	45.51

- Systematic error due to efficiency in decay modes is 3%.
- (If we could use the information on measured cross section for higgs decay modes, the error should be much smaller)

Fitting and Results

- Fitting functions
 - GPET x Novosibirsk for signal
 - 3rd order polynomial for BG
- Toy-MC study is performed: fixing parameters except mean of Gaussian, signal and BG yields, in order to estimate statistical error of mass and cross section.



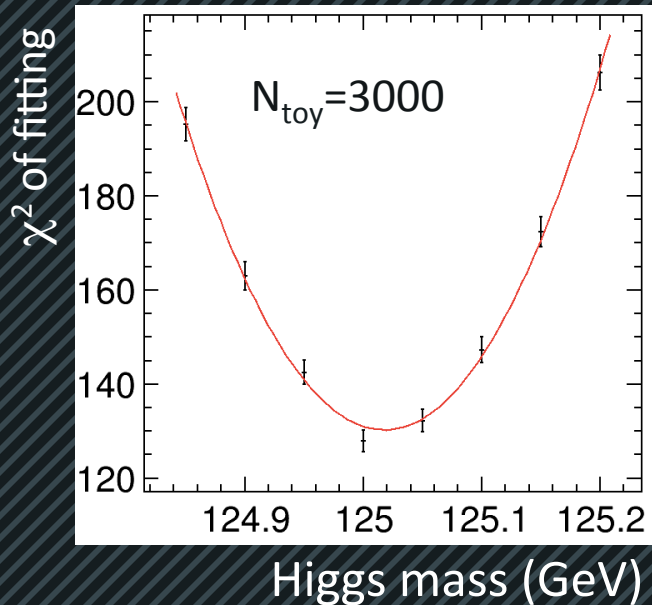
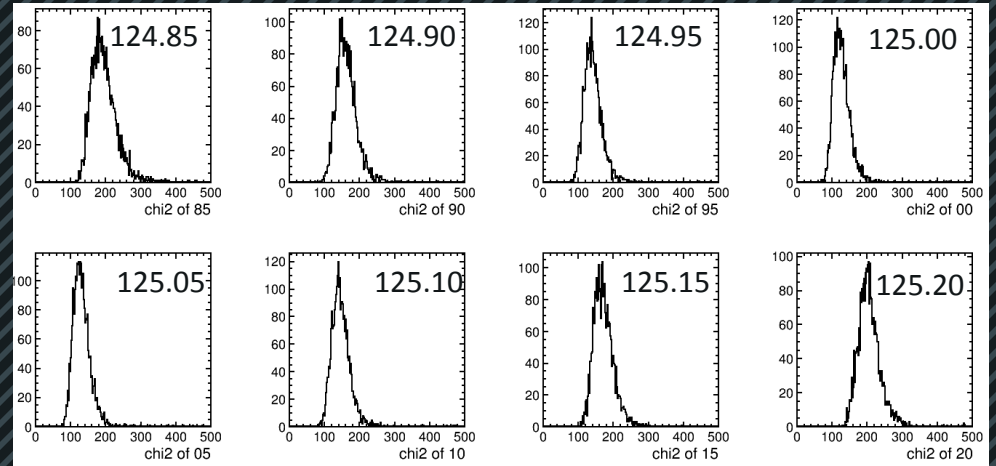
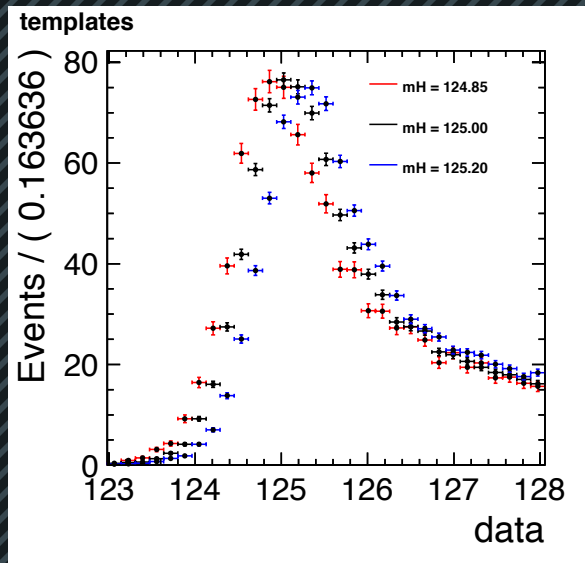
$\mu\mu h, eeh$ @250GeV		$\mu\mu h$		eeh		combined	
		Left	Right	Left	Right	Left	Right
MI	cross section	4.2%	3.8%	6.0%	6.0%	3.4%	3.2%
	mass [MeV]	34	31	231	214	34	31
semi-MI	cross section	3.8%		5.6%		3.1%	
	mass [MeV]	33		89		31	

✘ semi-MI means that visible energy cut is performed.

Mass Template Method

- To avoid systematic bias of mass parameter, mass template method was tried.
- Fit dataset by PDFs from template samples with different Higgs mass.
- Template samples with $M_{\text{Higgs}} = 124.85, 124.90, 124.95, 125.00, 125.05, 125.10, 125.15, \text{ and } 125.20$ are used (8points).
- Signal PDF is used as histograms reconstructed from template samples.
- BG PDF is used as 3rd order polynomial from DBD sample fitting.
- Toy-MC is made for data points, and mean of χ^2 values is plotted and fitted by parabola.
- Mass value at minimum χ^2 point is estimated Higgs mass so that we can evaluate mass error from that.

Result



histograms of χ^2

- Minimum position :
 $x = 125.018 \pm 0.021$ (GeV)

Next plan for

CP MIXTURE STUDY

Introduction

- In SM CP property of Higgs(h) is purely even.
- In 2HDM, there can be CP purely odd Higgs(A), and it is possible that h and A are mixed.
 - One of the parameters of this mixture is η , which is coefficient of CP odd Higgs amplitude.

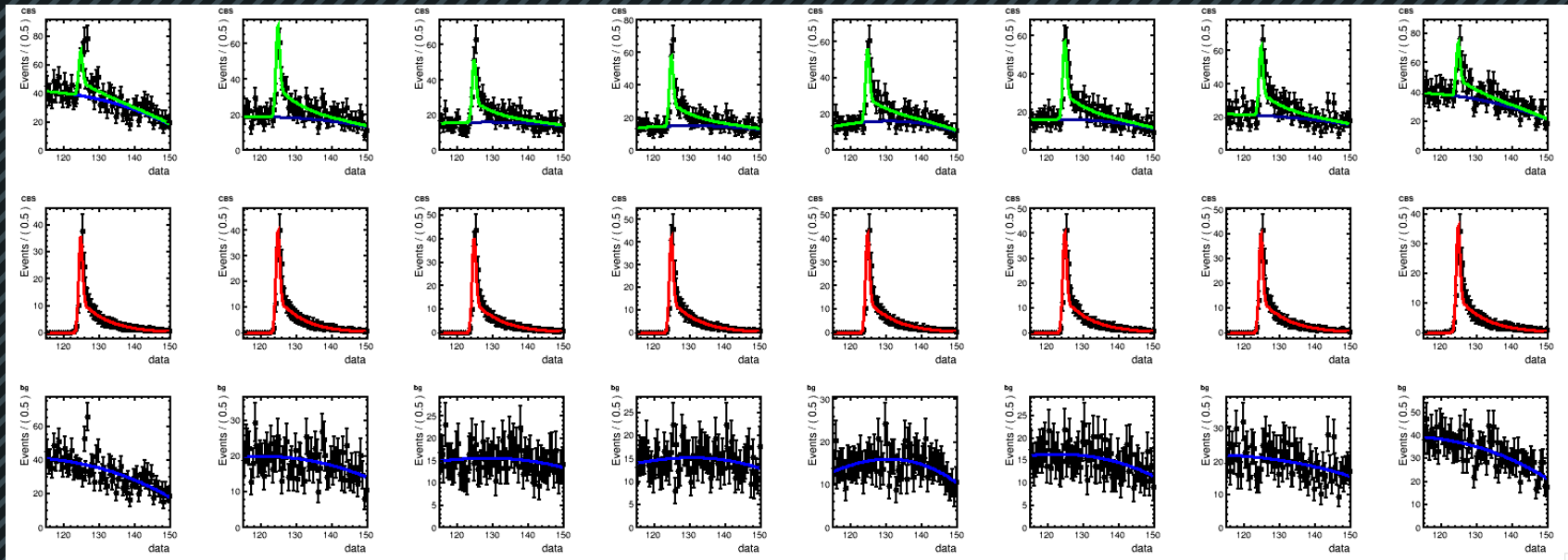
$$\mathbf{M}_{\phi Z} = \mathbf{M}_{hZ} + \eta \cdot \mathbf{M}_{AZ}$$

- When η has non-zero value, it affects Z production angle in $ee \rightarrow Zh$ event.

= We can observe asymmetry

$$\frac{d\sigma}{d\cos\theta} = \frac{G_F^2 M_Z^6 \beta}{16\pi} \frac{1}{D_Z(s)} (v_e^2 + a_e^2) \left[1 + \frac{s\beta^2}{8M_Z^2} (1 - \cos^2\theta) + \eta \frac{v_e a_e}{v_e^2 + a_e^2} \frac{2s\beta}{M_Z^2} \cos\theta + \eta^2 \frac{s^2 \beta^2}{4M_Z^4} \left(1 - \sin^2 \frac{\theta}{2} \right) \right]$$

Procedure of CP-mixture Study



$\cos\theta_{Z \text{ boson}}$

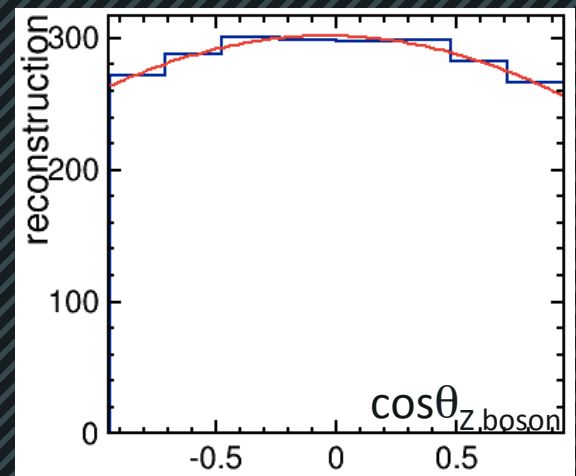
-0.95

Extrapolation

0.95



- Look Z production angle of $\mu\mu h$.
- Estimate N_{sig} by **recoil mass fitting** for each region of $\cos\theta_{Z \text{ boson}}$.
- Fit the obtained distribution by parabola, and check asymmetry.



Re-calculation η

$$\frac{d\sigma}{d\cos\theta} = \frac{G_F^2 M_Z^6 \beta}{16\pi} \frac{1}{D_Z(s)} (v_e^2 + a_e^2) \left[1 + \frac{s\beta^2}{8M_Z^2} (1 - \cos^2\theta) + \eta \frac{v_e a_e}{v_e^2 + a_e^2} \frac{2s\beta}{M_Z^2} \cos\theta + \eta^2 \frac{s^2 \beta^2}{4M_Z^4} \left(1 - \sin^2 \frac{\theta}{2} \right) \right]$$

$$\times \begin{cases} v_e - a_e = \frac{e}{\cos\theta_w \sin\theta_w} \left(-\frac{1}{2} + \sin^2\theta_w \right) \\ v_e + a_e = \frac{e}{\cos\theta_w \sin\theta_w} \left(-\sin^2\theta_w \right) \end{cases}$$

When define coefficients of pol2 of $\cos\theta$ distribution as p_1 and p_2 , η can be expressed by looking ratio p_1/p_2 .

$$\eta = \frac{M_Z^2}{2s} \left[-\frac{16}{\beta} \frac{v_e a_e}{v_e^2 + a_e^2} \pm \sqrt{\frac{16^2}{\beta^2} \left(\frac{v_e a_e}{v_e^2 + a_e^2} \right)^2 - \frac{4s p_1}{M_Z^2 p_2}} \right] = 0.06654 \times \left[-2.411 \pm \sqrt{5.811 - 30.06 \times \frac{p_1}{p_2}} \right]$$

$$\Rightarrow \eta = -0.044 \pm 0.105 \text{ (SM sample)}$$

or, if $O(\eta^2)$ is ignored...

$$\eta = -\frac{\beta}{16} \frac{v_e^2 + a_e^2}{v_e a_e} \frac{p_1}{p_2} = -0.4148 \dots \times \frac{p_1}{p_2}$$

$$\Rightarrow \eta = -0.075 \pm 0.157 \text{ (SM sample)}$$

Next Plan

- We have a generator with anomalous ZZH coupling, which is expressed by a , b , b^{\sim} parameters.
 - parameter of a will change only total cross section.
 - b and b^{\sim} change $\cos\theta$ distribution but it is complicated (right figure)
 - I should check the relation between “ η ” and “ a , b , b^{\sim} ”.
- I will try to estimate η value in other calculation.

