

# Slepton mass measurement in a $\tilde{\tau}$ co-annihilation scenario

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# Outline

This is a status report !!!

## 1 Outline

## 2 Studying SUSY in rich models

## 3 A bench-mark point: STC4

- STC4 @ 500 GeV
- STC4 @ 500 GeV: Globaly
- STC4 @ 500 GeV:  $\tilde{e}, \tilde{\mu}$
- STC4 @ 500 GeV:  $\tilde{\tau}_1$ 
  - Massive SGV  $\gamma\gamma$  production
  - Fitting the  $\tilde{\tau}_1$  end-point

## 4 Outlook & Conclusions

# Aim of the study

Suppose SUSY is there and has a rich spectrum of sparticles accessible at the ILC. Then:

- **Easy** - wrt. things like  $\tilde{H}$  only, WIMP only: Lots to see.
- **Hard** - wrt. things like  $\tilde{H}$  only, WIMP only: Lots to Disentangle.

Specifically:

- When data starts coming in, what is is first light ?
- How do we quickly determine a set of model parameters ?
- What is then the optimal use of beam-time in such a scenario ?
- And in a staged approach ?
- Spectrum in continuum vs. threshold-scans?
- Special points, eg. between  $\tilde{\tau}_1\tilde{\tau}_2$  and  $\tilde{\tau}_2\tilde{\tau}_2$  thresholds.
- Clean vs. high cross-section.
- And so on ...

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## Background from SM:

- **Real missing energy** + pair of SM-particles = di-boson production, with neutrinos:
  - $WW \rightarrow \ell\nu\ell\nu$
  - $ZZ \rightarrow f\bar{f}\nu\nu$
- **Fake missing energy** + pair of SM-particles =  $\gamma\gamma$  processes, ISR, single IVB.
  - $e^+e^- \rightarrow e^+e^-\gamma\gamma \rightarrow e^+e^-\bar{f}\bar{f}$ , with both  $e^+e^-$  un-detected.
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# Observables:

Observable	Gives	If
Edges (or average and width)	Masses	... not too far from threshold
Shape of spectrum	Spin	
Angular distributions	Mass, Spin	
Invariant mass distributions from full reconstruction	Mass	... cascade decays
Angular distributions from full reconstruction	Spin, CP,	... masses known
Un-polarised Cross-section in continuum	Mass, coupling	
Polarised Cross-section in continuum	Mass, coupling, mixing	
Decay product polarisation	Mixing	... $\tilde{\tau}$ decays
Threshold-scan	Mass(es), Spin	

# Observables: Pair-production, two-body decay

Consider  $e^+e^- \rightarrow XX$ , followed by  $X \rightarrow UY$ , where Y is a detectable (SM) particle. Then

- $E_Y \text{ max(min)} = \frac{E_{\text{Beam}}}{2} \left( 1 - \left( \frac{M_U}{M_X} \right)^2 \right) \left( 1_{(-)}^{(+)} \sqrt{1 - \left( \frac{M_X}{E_{\text{Beam}}} \right)^2} \right)$ , so that

- $M_X = E_{\text{Beam}} \sqrt{1 - (\Delta/\Sigma)^2}$

- $M_U = E_{\text{Beam}} \sqrt{1 - (\Delta/\Sigma)^2} \sqrt{1 - \Sigma/E_{\text{Beam}}}$   
 $(\Delta = E_Y \text{ max} - E_Y \text{ min}; \Sigma = E_Y \text{ max} + E_Y \text{ min})$

If the spectrum is flat (eg if X is a sfermion) between the end-points:

- $\langle E_Y \rangle = (E_Y \text{ max} + E_Y \text{ min})/2$  and  $\sigma_{E_Y} = \sqrt{(E_Y \text{ max} - E_Y \text{ min})/12}$ , which gives

- $M_U = E_{\text{Beam}} \sqrt{1 - \frac{2\langle E_Y \rangle}{E_{\text{Beam}}}} \sqrt{1 - \left( \frac{6\sigma_{E_Y}^2}{\langle E_Y \rangle} \right)^2}$

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# Example: STC4

## STC4-8

- 11 parameters.
- Separate gluino
- Higgs, un-coloured, and coloured scalar parameters separate

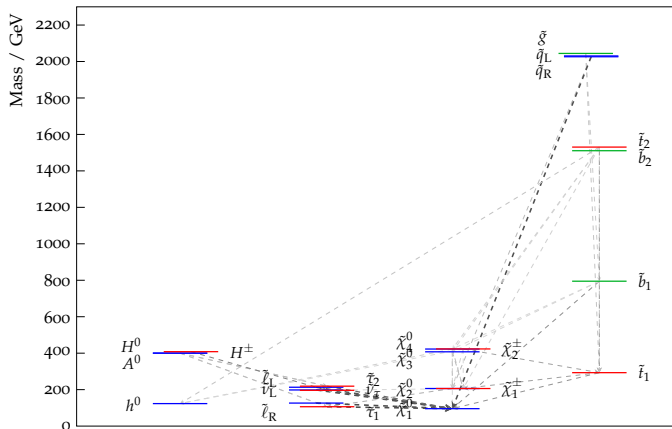
Parameters chosen to deliver all constraints (LHC, LEP, cosmology, low energy).

At  $E_{CMS} = 500$  GeV:

- All sleptons available.
- No squarks.
- Lighter bosinos, up to  $\tilde{\chi}_3^0$  (in  $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_3^0$ )

(See H. Baer, J. List, arXiv:1307:0782.)

## Full STC4 mass-spectrum





## Channels and observables at 250, 350 and 500 GeV

Channel	Threshold	Available at	Can give
$\tilde{\tau}_1 \tilde{\tau}_1$	212	250	$M_{\tilde{\tau}_1}$ , $\tilde{\tau}_1$ nature, $\tau$ polarisation
$\tilde{\mu}_R \tilde{\mu}_R$	252	250+	+ $M_{\tilde{\mu}_R}$ , $M_{\tilde{\chi}_1^0}$ , $\tilde{\mu}_R$ nature
$\tilde{e}_R \tilde{e}_R$	252	250+	+ $M_{\tilde{e}_R}$ , $M_{\tilde{\chi}_1^0}$ , $\tilde{e}_R$ nature
$\tilde{\chi}_1^0 \tilde{\chi}_2^0$ *)	302	350	+ $M_{\tilde{\chi}_2^0}$ , $M_{\tilde{\chi}_1^0}$ , nature of $\tilde{\chi}_1^0$ , $\tilde{\chi}_2^0$
$\tilde{\tau}_1 \tilde{\tau}_2$ *)	325	350	+ $M_{\tilde{\tau}_2}$ , $\theta_{mix}$ $\tilde{\tau}$
$\tilde{e}_R \tilde{e}_L$ *)	339	350	+ $M_{\tilde{e}_L}$ , $\tilde{\chi}_1^0$ mixing, $\tilde{e}_L$ nature
$\tilde{\nu}_\tau \tilde{\nu}_\tau$	392	500	7 % visible BR ( $\rightarrow \tilde{\tau}_1 W$ )
$\tilde{\chi}_1^\pm \tilde{\chi}_1^\pm$ *)	412	500	+ $M_{\tilde{\chi}_1^\pm}$ , nature of $\tilde{\chi}_1^\pm$
$\tilde{e}_L \tilde{e}_L$ *)	416	500	+ $M_{\tilde{e}_L}$ , $M_{\tilde{\chi}_1^0}$ , $\tilde{e}_L$ nature
$\tilde{\mu}_L \tilde{\mu}_L$ *)	416	500	+ $M_{\tilde{\mu}_R}$ , $M_{\tilde{\chi}_1^0}$ , $\tilde{\mu}_R$ nature
$\tilde{\tau}_2 \tilde{\tau}_2$ *)	438	500	+ $M_{\tilde{\tau}_2}$ , $M_{\tilde{\chi}_1^0}$ , $\tilde{\tau}_2$ nature, $\theta_{mix}$ $\tilde{\tau}$
$\tilde{\chi}_1^0 \tilde{\chi}_3^0$ *)	503	500+	+ $M_{\tilde{\chi}_3^0}$ , $M_{\tilde{\chi}_1^0}$ , nature of $\tilde{\chi}_1^0$ , $\tilde{\chi}_3^0$

\*) : Cascade decays.

+ invisible  $\tilde{\chi}_1^0 \tilde{\chi}_1^0$ ,  $\tilde{\nu}_e \tilde{\mu} \tilde{\nu}_e \tilde{\mu}$ .

# Features of STC4 @ 500 GeV

- The  $\tilde{\tau}_1$  is the NLSP.
- For  $\tilde{\tau}_1$ :  $E_{\tau,min} = 2.3$  GeV,  $E_{\tau,max} = 45.5$  GeV:  
 $\gamma\gamma - \text{background} \Leftrightarrow \text{pairs} - \text{background}$ .
- For  $\tilde{\tau}_2$ :  $E_{\tau,min} = 52.4$  GeV,  $E_{\tau,max} = 150.0$  GeV:  
 $WW \rightarrow l\nu l\nu - \text{background} \Leftrightarrow \text{Polarisation}$ .
- For  $\tilde{e}_R$  or  $\tilde{\mu}_R$ :  $E_{l,min} = 7.3$  GeV,  $E_{l,max} = 99.2$  GeV: Neither  $\gamma\gamma$  nor  $WW \rightarrow l\nu l\nu$  background severe.
- For  $\text{pol}=(1,-1)$ :  $\sigma(\tilde{e}_R\tilde{e}_R) = 1.3$  pb !
- $\tilde{\tau}$  NLSP  $\rightarrow \tau$ :s in most SUSY decays  $\rightarrow$  SUSY is background to SUSY.
- For  $\text{pol}=(1,-1)$ :  $\sigma(\tilde{\chi}_2^0\tilde{\chi}_2^0)$  and  $\sigma(\tilde{\chi}_1^+\tilde{\chi}_1^-) = \text{several hundred fb}$  and  $\text{BR}(X \rightarrow \tilde{\tau}) > 70\%$ . For  $\text{pol}=(1,-1)$ :  $\sigma(\tilde{\chi}_2^0\tilde{\chi}_2^0)$  and  $\sigma(\tilde{\chi}_1^+\tilde{\chi}_1^-) \approx 0$ .

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- For  $\text{pol}=(-1,1)$ :  $\sigma(\tilde{\chi}_2^0\tilde{\chi}_2^0)$  and  $\sigma(\tilde{\chi}_1^+\tilde{\chi}_1^-) =$  several hundred fb and  $\text{BR}(X \rightarrow \tilde{\tau}) > 70\%$ . For  $\text{pol}=(1,-1)$ :  $\sigma(\tilde{\chi}_2^0\tilde{\chi}_2^0)$  and  $\sigma(\tilde{\chi}_1^+\tilde{\chi}_1^-) \approx 0$ .

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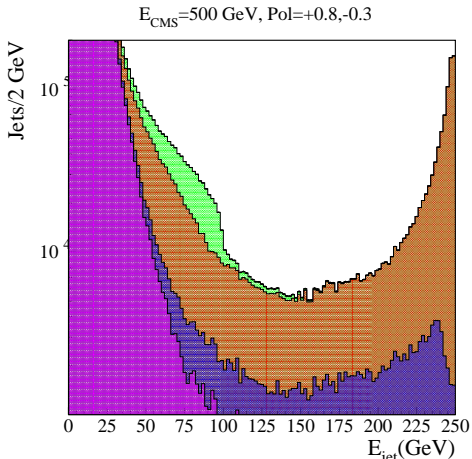
## Strategy:

- Global preselection to reduce SM, while efficiency for **all** signals stays above  $\sim 90\%$ .
- The further select for **all sleptons** ( $\tilde{e}_R, \tilde{e}_L, \tilde{\mu}_R, \tilde{\mu}_L, \tilde{\tau}_1$ ).
- Next step: **specific** selections for  $\tilde{e}_R$  and  $\tilde{\mu}_R$ , for  $\tilde{e}_L$  and  $\tilde{\mu}_L$ , and for  $\tilde{\tau}_1$ .
- Last step: add **particle id** to separate  $\tilde{e}$  and  $\tilde{\mu}$ , special cuts for  $\tilde{\tau}_1$ .
- Check results both for **RL and LR** beam-polarisation.

# STC4 global

After a few very general cuts:

- Missing energy  $> 100$
- Less than 10 charged tracks
- $|\cos \theta_{P_{tot}}| < 0.95$
- Exactly two  $\tau$ -jets
- Visible mass  $< 300$  GeV
- $\theta_{acop}$  between 0.15 and 3.1



Magenta:  $\gamma\gamma$ , Blue: 3f,  
Red: Rest of SM, Green: SUSY.

# STC4 sleptons @ 500 GeV: $\tilde{e}, \tilde{\mu}$

- **Selections** for  $\tilde{\mu}$  and  $\tilde{e}$ :
  - Correct charge.
  - $P_T$  wrt. beam and one  $\ell$  wrt the other.
  - Tag and probe, ie. accept one jet if the other is “in the box”.
- **Further selections** for R:
  - Cuts on polar angle and angle between leptons
- $E_{jet}$ , beam-pol 80%, -30%...
- **Further selections** for L (LR):
  - $q_{jet} \cos \theta_{jet}$
  - $M_{vis} \neq M_Z$

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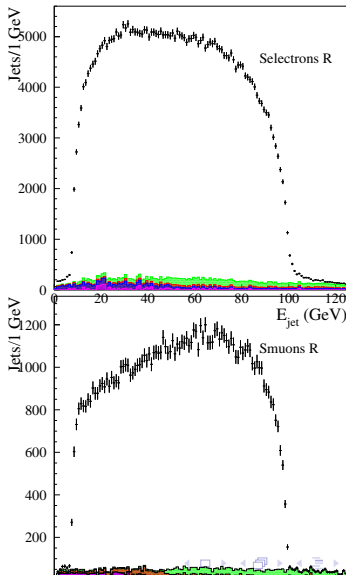
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  - Cuts on polar angle and angle between leptons.
- $E_{jet}$ , beam-pol 80%, -30%...
- **Further selections** for L (LR):
  - $q_{jet} \cos \theta_{jet}$
  - $M_{vis} \neq M_Z$

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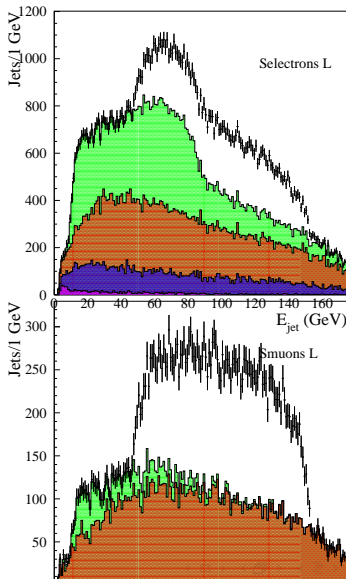
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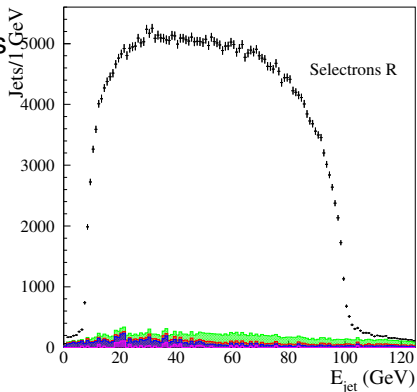


# Masses from $\tilde{e}$ , $\tilde{\mu}$ in the continuum

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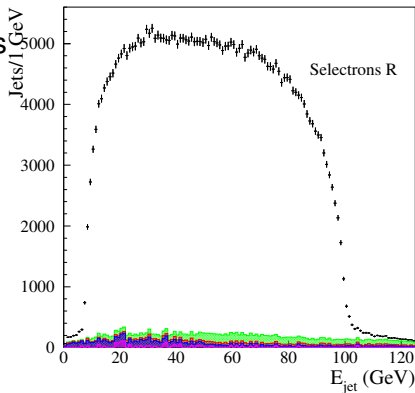
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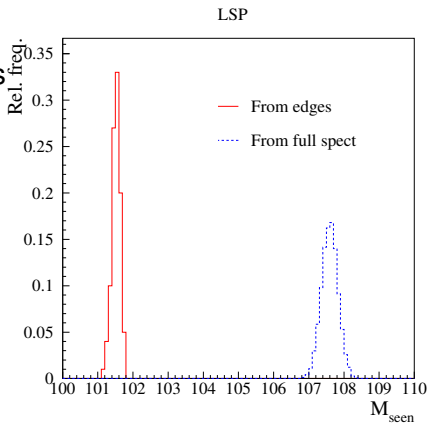
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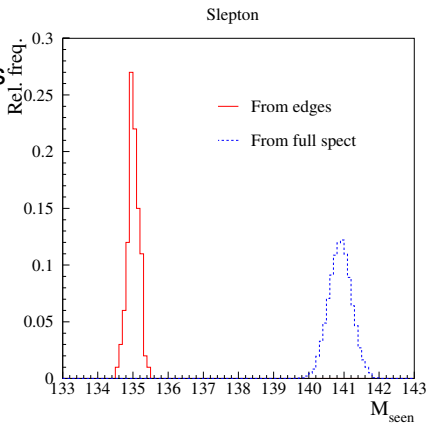
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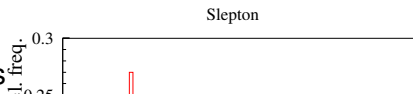
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Results from edges ( $E_{CMS}=500, 500 \text{ fb}^{-1}$  @ [+0.8,-0.3])

$$M_{\tilde{e}_R} = 135.01 \pm 0.19 \text{ GeV}/c^2$$

$$M_{\tilde{\chi}_1^0} = 101.51 \pm 0.14 \text{ GeV}/c^2$$

Results for full spectrum ( $E_{CMS}=500, 500 \text{ fb}^{-1}$  @ [+0.8,-0.3])

$$M_{\tilde{e}_R} = 140.90 \pm 0.33 \text{ GeV}/c^2$$

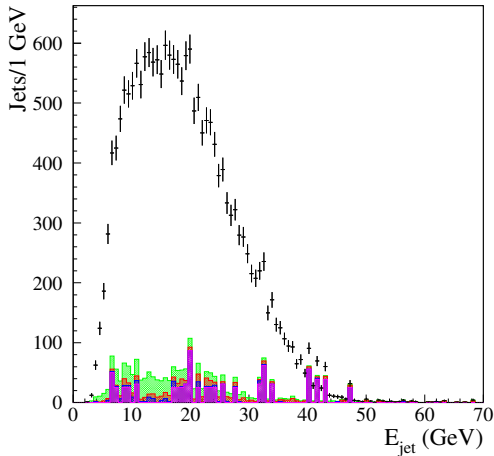
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- Make calibration curve with ToyMC.

# STC4 sleptons @ 500 GeV: $\tilde{\tau}_1$

Selections for  $\tilde{\tau}_1$ :

- Correct **charge**.
- $P_T$  wrt. beam and one  $\tau$  wrt the other.
- $M_{jet} < M_{\tau}$
- $E_{vis} < 120$  GeV,  $M_{vis} \in [20, 87]$  GeV.
- Cuts on **polar angle** and **angle between leptons**.
- Little energy below 30 deg, or not in  $\tau$ -jet.
- At least one  $\tau$ -jet should be **hadronic**.
- **Anti- $\gamma\gamma$  likelihood**.





# Massive SGV $\gamma\gamma$ production

- **Note the few  $\gamma\gamma$  events just at the end-point !**
- Don't want to do "dirty tricks" to fit the end-point  $\Rightarrow$  need more stat.
- But I've already used all existing generated events, and that only represents  $20 \text{ fb}^{-1}$ , but is nevertheless 580 GB in 1134 stdheps  $\Rightarrow$
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- Callable Whizard is already an option in SGV, but:
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- Using the **existing meta-data** files for aa\_2f, easy to script a massive production.
- Specify wanted integrated lumi, maximum number of events/job , and the set of meta-data files to parse.
- On the German NAF:
  - 1615 jobs of 0.5 MEvents
  - Total generated: **0.8 GEvents**.
  - Wall-clock time first started to last completed: **3 hours** (with typically 200-300 jobs running at the same time).
  - Written to analysis ntuple: 83 MEvents, size **330 GB** (compare: would have needed TB:s of stdheps!)
- Some notes:
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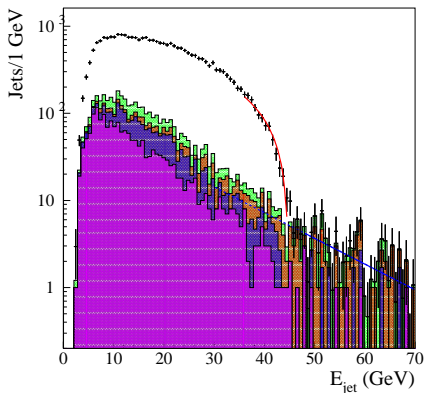
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# Fitting the $\tilde{\tau}_1$ end-point

- Only the upper end-point is relevant.
- Background subtraction:
  - $\tilde{\tau}_1$ : Important SUSY background, but region above 45 GeV is signal free. Fit exponential and extrapolate.
- Fit line to (data-background fit).

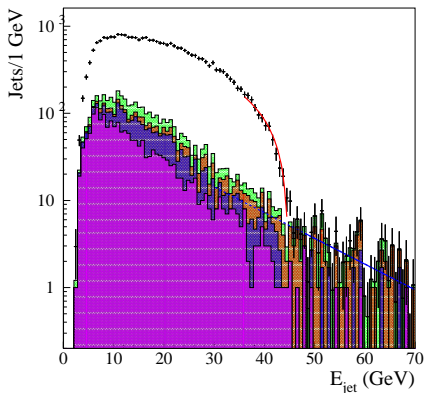
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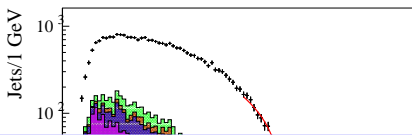
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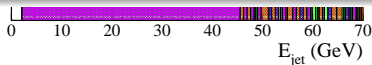
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## Results for $\tilde{\tau}_1$

$$E_{max, \tilde{\tau}_1} = 44.51^{+0.12}_{-0.10} \text{ GeV}$$

Translates to an error of  $\sim 0.06 \text{ GeV}/c^2 \oplus 1.3 \Delta(M_{\tilde{\chi}_1^0})$  on the mass, where the error from  $M_{\tilde{\chi}_1^0}$  **largely dominates**



# Reminder: SPS1a' results (Phys.Rev.D82:055016,2010)

The previous  $\tilde{\tau}$  study in the very similar model SPS1a' gave:

## Results for $\tilde{\tau}_1$

$$M_{\tilde{\tau}_1} = 107.73_{-0.05}^{+0.03} \text{ GeV}/c^2 \oplus 1.3\Delta(M_{\tilde{\chi}_1^0})$$

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## Results for $\tilde{\tau}_2$

$$M_{\tilde{\tau}_2} = 183_{-5}^{+11} \text{ GeV}/c^2 \oplus 18\Delta(M_{\tilde{\chi}_1^0})$$

The error from the endpoint largely dominates

## Results from cross-section for $\tilde{\tau}_1$

$$\Delta(N_{\text{signal}})/N_{\text{signal}} = 3.1\% \rightarrow \Delta(M_{\tilde{\tau}_1}) = 3.2 \text{ GeV}/c^2$$

## Results from cross-section for $\tilde{\tau}_2$

$$\Delta(N_{\text{signal}})/N_{\text{signal}} = 4.2\% \rightarrow \Delta(M_{\tilde{\tau}_2}) = 3.6 \text{ GeV}/c^2$$

End-point + Cross-section  
 $\rightarrow \Delta(M_{\tilde{\chi}_1^0}) = 1.7 \text{ GeV}/c^2$

## Also: $\tau$ polarisation in $\tilde{\tau}_1$ decays

$$\Delta(\mathcal{P}_\tau)/\mathcal{P}_\tau = 9\%.$$

# Outlook & Conclusions

- Study best method to analyse spectra, eg
  - Optimal statistic for clean signals.
- Specific reconstruction methods for  $e$ ,  $\mu$ , and  $\tau$ .
- Make a coherent SGV study of **all channels**, at **all  $E_{CMS}$  stages**.
  - Also channels not studied in SPS1a'
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- Status:
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# Thank You !

## BACKUP

## BACKUP SLIDES

## Observables: Pair-production, two-body decay (less text)

- So, there are two SUSY parameters, and two independent observables in the spectrum.
- Any pair of observables can be chosen, edges, average, standard deviation, width, ...
- Which choice is the best depends on the situation.
- Just a bit of algebra to extract the two SUSY masses.
- Note that if  $E_{beam} \gg M_X$ , there is just one observable (low edge becomes 0, width becomes average/2), so one should not operate too far above threshold !
- Note that there are two decays in each event: two measurements per event.
- Also note that there are not enough measurements to make a constrained fit, even assuming that the two SUSY particles in the two decays are the same:  $(2 \times 4 \text{ unknown components of 4-momentum } (=8)) - (\text{total E and p conservation } (=4)) + 2$

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However:

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- ... and the **angular distributions** both in production and decay can be measured.
- From this the **spins** can be determined, which is **essential** to determine that what we are seeing is **SUSY**.

Furthermore:

- Looking at more complicated decays, such as cascade decays, there are enough constraints if some (but not all) masses are known.
- Allows to reconstruct eg. the slepton mass in  $\tilde{\chi}_2^0 \rightarrow \tilde{\ell} \ell \rightarrow \ell \ell \tilde{\chi}_1^0$  if chargino and LSP masses are known.
- Order-of-magnitude better mass resolution.

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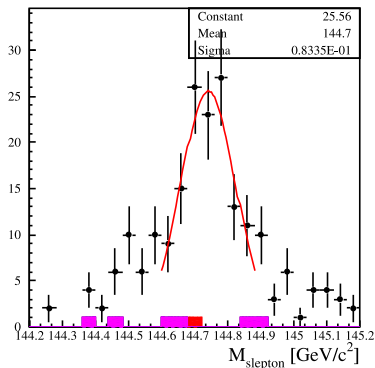
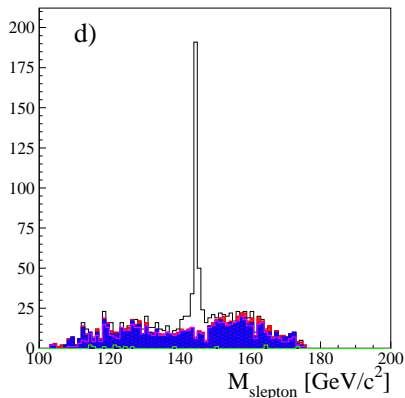
Furthermore:

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- Allows to reconstruct eg. **the slepton mass** in  $\tilde{\chi}_2^0 \rightarrow \tilde{\ell}\ell \rightarrow \ell\ell\tilde{\chi}_1^0$  if chargino and LSP masses are known.
- Order-of-magnitude better mass resolution.

# Observables: Pair-production, two-body decay

However:

- If the masses are known from other measurements, there are



- Order-of-magnitude better mass resolution.

# Observables

But this is not all !

- The **cross-section** in  $e^+e^- \rightarrow XX$  close to threshold depends both on coupling, spin and kinematics ( $= \beta$ ).
- The distribution of the **angle between the two SM-particles** depends on  $\beta$ , in a complicated, but calculable way.
- The cross-section is different for L and R SUSY particles.
- So checking how much the cross-section changes when **switching beam-polarisations** measures mixing.
- Measure the **helicity of the SM particle**  $\rightarrow$  properties of the particles in the decay, ie. in addition to the produced X, also the invisible U. In one case this is possible: In  $\tilde{\tau} \rightarrow \tau \tilde{\chi}_1^0 \rightarrow X \nu_\tau \tilde{\chi}_1^0$ .

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# Extracting the $\tilde{\tau}$ properties

See Phys.Rev.D82:055016,2010

Use polarisation (0.8,-0.22) to reduce bosino background.

From decay kinematics:

- $M_{\tilde{\tau}}$  from  $M_{\tilde{\chi}_1^0}$  and end-point of spectrum =  $E_{\tau,max}$ .
- Other end-point hidden in  $\gamma\gamma$  background: Must get  $M_{\tilde{\chi}_1^0}$  from other sources. ( $\tilde{\mu}$ ,  $\tilde{e}$ , ...)

From cross-section:

- $\sigma_{\tilde{\tau}} = A(\theta_{\tilde{\tau}}, \mathcal{P}_{beam}) \times \beta^3 / s$ , so
- $M_{\tilde{\tau}} = E_{beam} \sqrt{1 - (\sigma s / A)^{2/3}}$ : no  $M_{\tilde{\chi}_1^0}$  !

From decay spectra:

- $\mathcal{P}_{\tau}$  from exclusive decay-mode(s): handle on mixing angles  $\theta_{\tilde{\tau}}$  and  $\theta_{\tilde{\chi}_1^0}$



# Topology selection

Take over SPS1a'  $\tilde{\tau}$  analysis principle

$\tilde{\ell}$  properties:

- Only two particles (possibly  $\tau$ :s:s) in the final state.
- Large missing energy and momentum.
- High Acolinearity, with little correlation to the energy of the  $\tau$  decay-products.
- Central production.
- No forward-backward asymmetry.

+ anti  $\gamma\gamma$  cuts.

Select this by:

- Exactly two jets.
- $N_{ch} < 10$
- Vanishing total charge.
- Charge of each jet =  $\pm 1$ ,
- $M_{jet} < 2.5 \text{ GeV}/c^2$ ,
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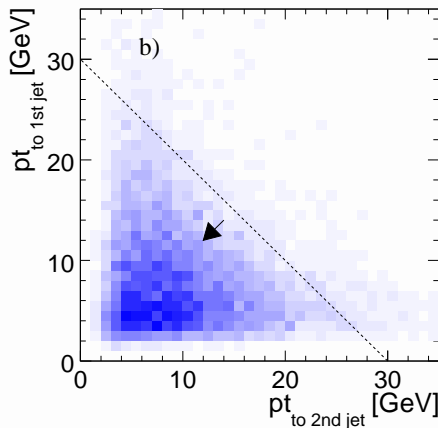
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- $\tilde{\tau}_1$ :
  - $(E_{jet1} + E_{jet2}) \sin \theta_{acop} < 30$  GeV.
- $\tilde{\tau}_2$ :
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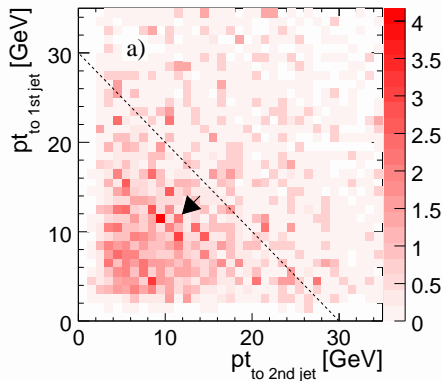
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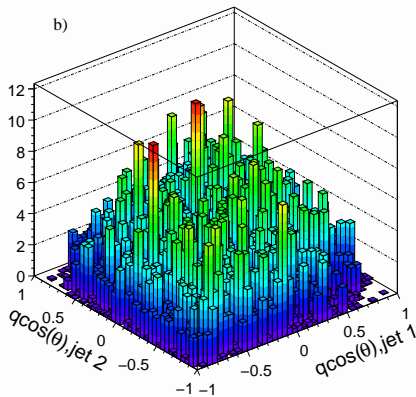
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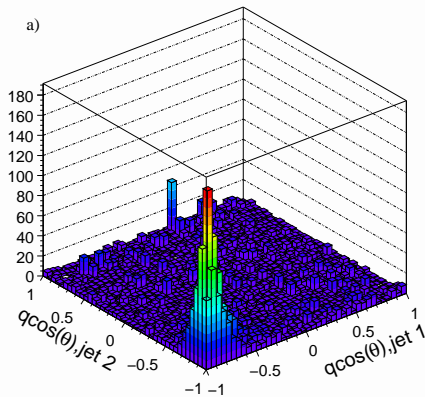
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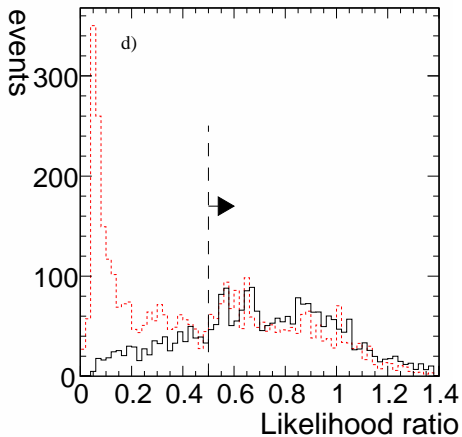
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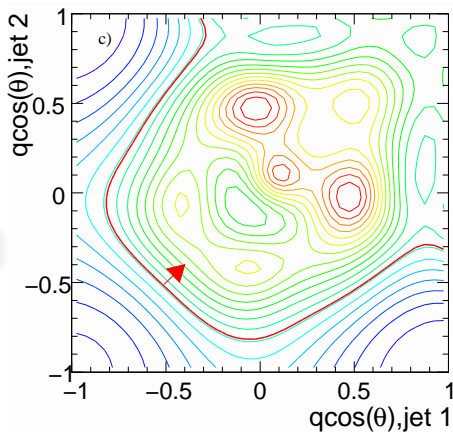




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# $\tilde{\mu}$ channels

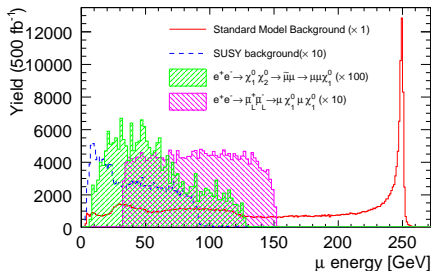
Use “normal” polarisation (-0.8,0.22).

- $\tilde{\mu}_L \tilde{\mu}_L \rightarrow \mu \mu \tilde{\chi}_1^0 \tilde{\chi}_1^0$
- $\tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \mu \tilde{\mu}_R \tilde{\chi}_1^0 \rightarrow \mu \mu \tilde{\chi}_1^0 \tilde{\chi}_1^0$

- Momentum of  $\mu$ 's

- $E_{miss}$

- $M_{\mu\mu}$

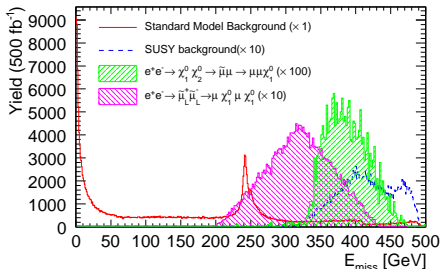


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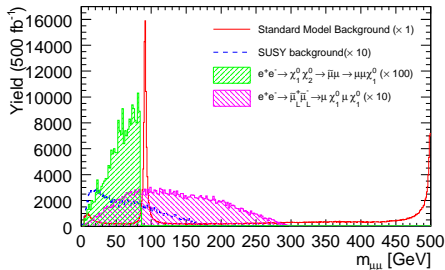


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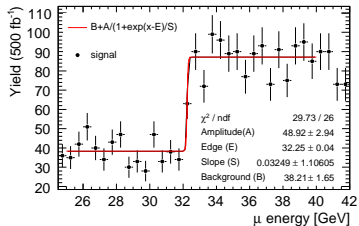
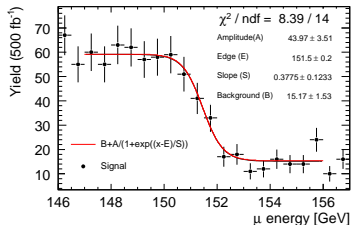
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- $\theta_{missingp} \in [0.1\pi; 0.9\pi]$
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- $M_{\mu\mu} \notin [80, 100]\text{GeV}$  and  $> 30 \text{ GeV}/c^2$

Masses from edges. Beam-energy spread dominates error.

$$\Delta(M_{\tilde{\chi}_1^0}) = 920 \text{ MeV}/c^2$$

$$\Delta(M_{\tilde{\mu}_L}) = 100 \text{ MeV}/c^2$$



$\tilde{\mu}_L \tilde{\mu}_L$ 

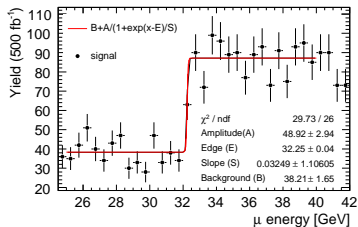
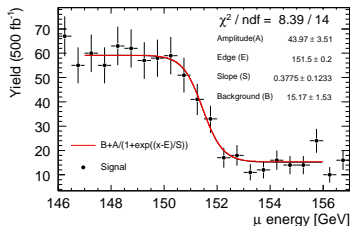
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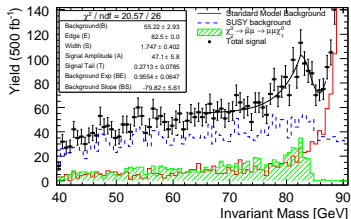
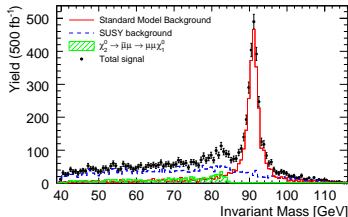
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- $\theta_{\text{missing } p} \in [0.2\pi; 0.8\pi]$
- $p_{T\text{miss}} > 40\text{GeV}/c$
- $\beta$  of  $\mu$  system  $> 0.6$ .
- $E_{\text{miss}} \in [355, 395]\text{GeV}$

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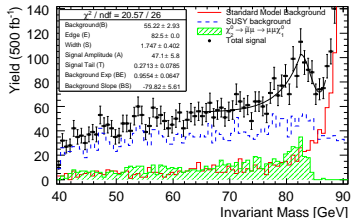
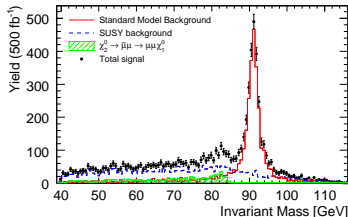
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## $\tilde{\mu}_R$ threshold scan

From these spectra, we can estimate  $M_{\tilde{e}_R}$ ,  $M_{\tilde{\mu}_R}$  and  $M_{\tilde{\chi}_1^0}$  to  $< 1$  GeV.

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- 10 points, 10 fb<sup>-1</sup>/point.
- Luminosity  $\propto E_{CMS}$ , so this is  $\Leftrightarrow 170 \text{ fb}^{-1}$  @  $E_{CMS}=500 \text{ GeV}$ .

Error on  $M_{\tilde{\mu}_R} = 197 \text{ MeV}$

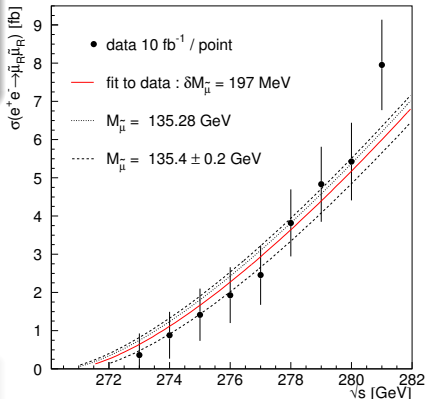
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