

# Status of two-track separation simulation with resistive Micromegas



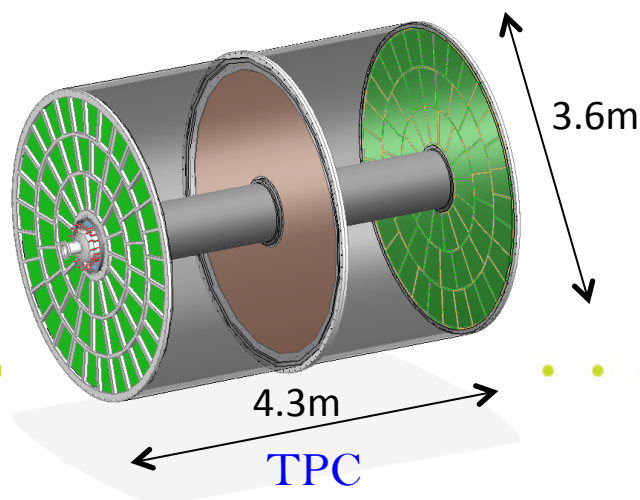
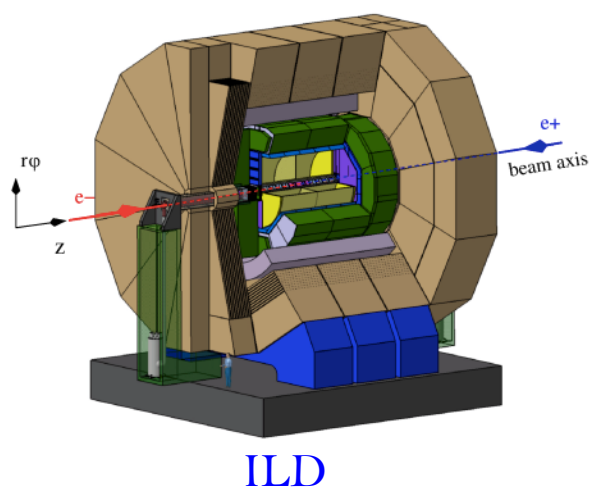
A. Bellerive



Carleton  
UNIVERSITY

# Outline

- Introduction and requirement for **LCTPC** at **ILD**
- Will **ask** these **3** questions:
  - 1) What is the optimal pad size and pad layout?
  - 2) How is electronics signal sampled, shaped and optimized?
  - 3) How to study the LCTPC ability to reconstruct multiple tracks in both the  $r$ - $\Phi$  and  $r$ - $Z$  planes?
- Description of simulation for future study of **two-track** separation with **LCTPC**





# Time Projection Chamber (TPC) for ILD

TPC is the central tracker for International Linear Detector

- Large number of 3D points → continuous tracking
- Good track separation and pattern recognition
- Low material budget inside the calorimeters (*c.f.* PFA)
  - Barrel:  $\sim 5\% X_0$
  - Endplates:  $\sim 25\% X_0$

## TPC Requirements :

- **Momentum resolution:**

$$\delta(1/p_T) < 9 \times 10^{-5} \text{ GeV}^{-1}$$

- **Single hit resolution 3.5T:**

$$\sigma(r\phi) < 100 \mu\text{m (overall)}$$

$$\sigma(z=0) \approx 400 \mu\text{m}$$

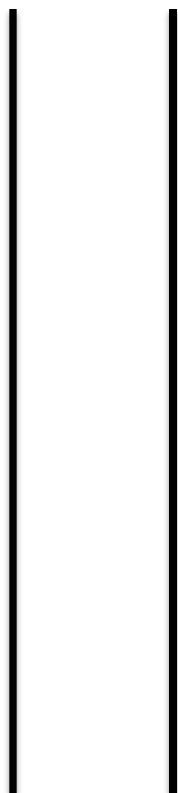
- **Tracking eff. for  $p_T > 1 \text{ GeV}$ : 97%**

- **dE/dx resolution  $\sim 5\%$**

# Goal: Resolution Measurement

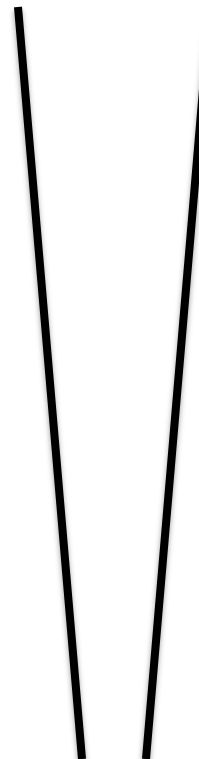
- ❑ **Resolution** is the precision to which the **position** of a passing particle can be measured
- ❑ Requirements of the TPC (at 3.5T) are:
  - **Transverse** (xy) resolution of 100 microns over 2m of drift, **60 microns** at  $Z=0$
  - **Longitudinal** (z) resolution of 1400 microns over 2m of drift, **400 microns** at  $Z=0$





parallel

$\neq$

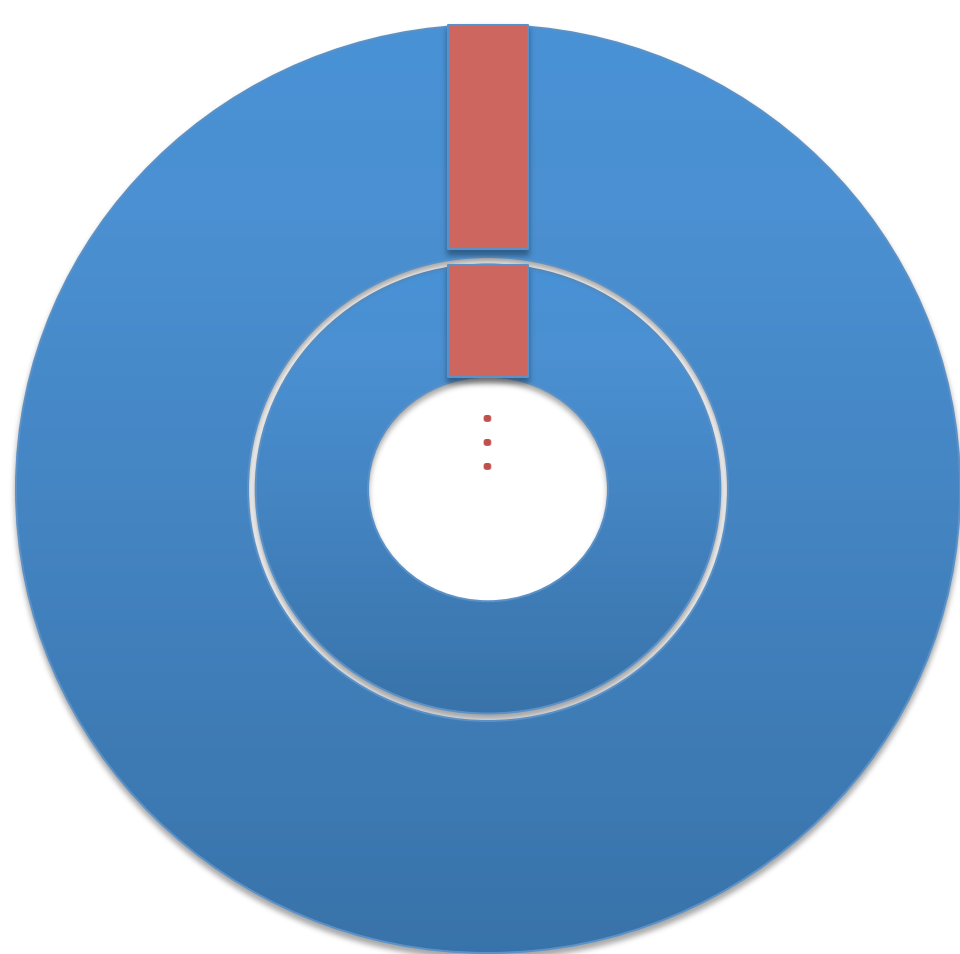


pointing

**Pattern recognition** (Kalman fitter): go from outer to inner to resolved two track if track are forced to point at the IP

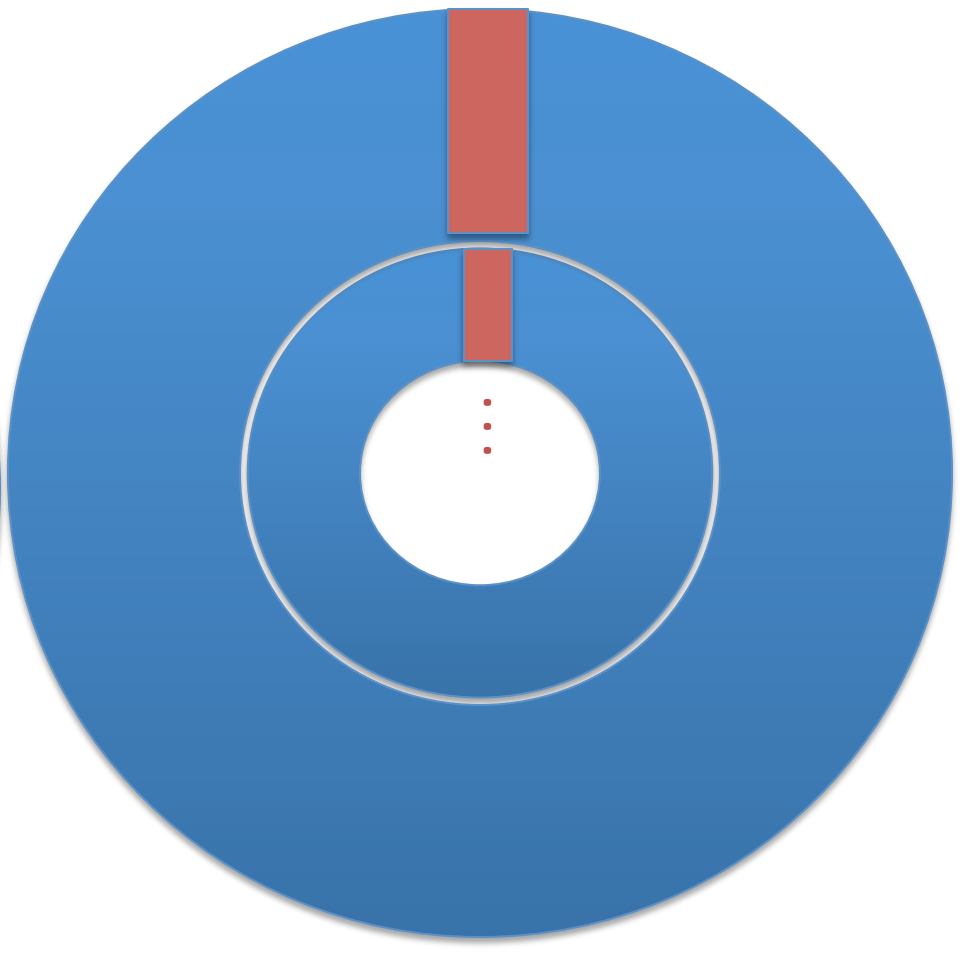
- In the r- $\Phi$  **two-track** separation is limited by the pad pitch and therefore by the pad geometrical & arrangement
- For best single hit resolution requires at least 3 pads per hits: charge sharing allows for much better **single-hit** resolution than  $d/\sqrt{12}$
- Over all for pad of pitch  $d$ , significant information can be extracted from a pad row when **two tracks** are as near as about  $1.5 d$  in that row
- **Should look at pad pitch versus radius**
- Larger occupancy and more curlers at smaller radius
- Connect track segments with high resolution Silicon Inner Tracker (SIT) and the Silicon External Tracker (SET)

# r- $\Phi$ plane (track matching)



Same pad pitch versus radius

Simplify module design and construction



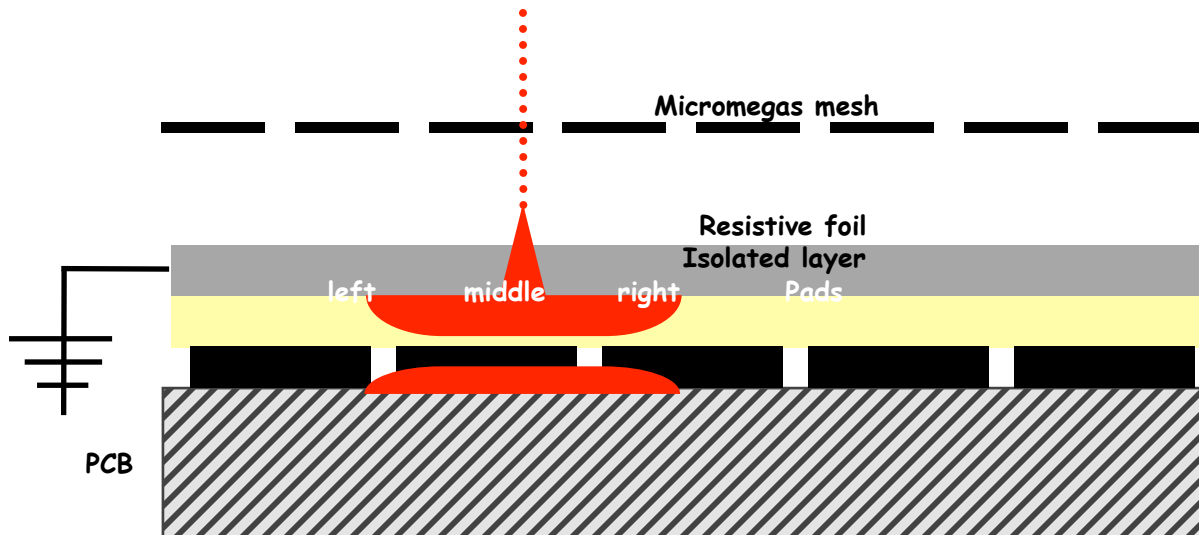
Pad pitch varies versus radius

Allow better match with inner tracker

- In the r-z the resolution is driven by our ability to precisely measure the **drift time**
- For each pad we have charge (ADC) as a function of fixed time intervals (25 – 40 ns)
- Fit rise of pulse to get Z with better single hit resolution than the sampling time
- Sampling time the same for each module (cannot be better at smaller radius... can it?)
- Prone to use fast shaping time electronics (100 ns)
- GEM: all pads in a hit have identical signal shape
- MM with resistive layer: neighboring pads have **delayed** signals



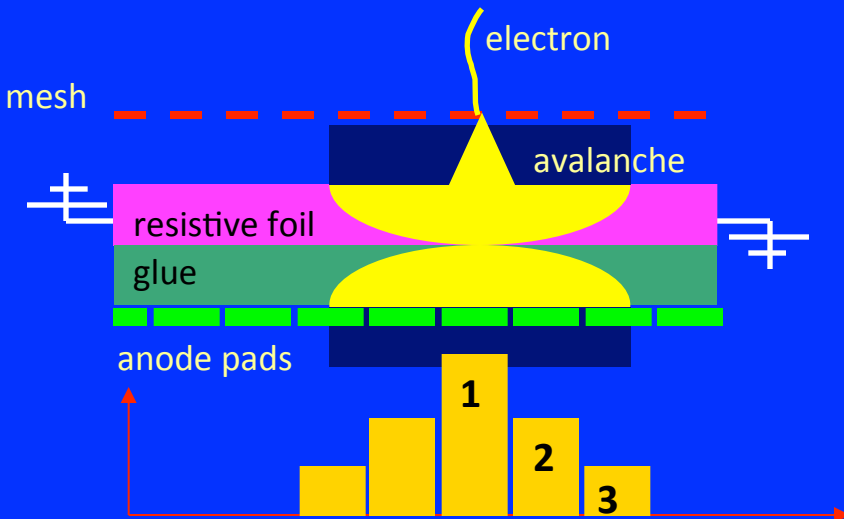
# Charge Dispersion Resistive Anode $r$ - $\Phi$ plane



# Charge dispersion

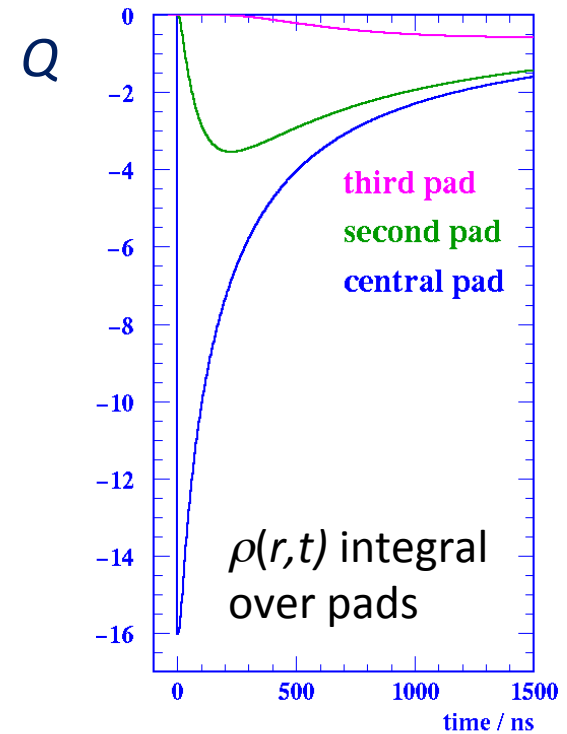
- A high resistivity film bonded to a readout plane with an insulating spacer
- 2D continuous RC network defined by material properties and geometry.
- point charge at  $r = 0$  &  $t = 0$  disperses with time.

## Micromegas + resistive anode



$$\frac{\partial \rho}{\partial t} = \frac{1}{RC} \left[ \frac{\partial^2 \rho}{\partial r^2} + \frac{1}{r} \frac{\partial \rho}{\partial r} \right]$$

$$\Rightarrow \rho(r, t) = \frac{RC}{2t} e^{-\frac{r^2 RC}{4t}}$$



ns



# Pulse shape origin

Transverse diffusion

Transverse diffusion

$$T(x) = \frac{1}{\sigma_x \sqrt{2\pi}} \exp\left(\frac{-x^2}{2\sigma_x^2}\right)$$

Longitudinal diffusion

Longitudinal diffusion

$$L(t) = \frac{1}{\sigma_t \sqrt{2\pi}} \exp\left(\frac{-t^2}{2\sigma_t^2}\right)$$

Intrinsic rise time

Induction gap

$$R(t) = \begin{cases} \frac{t}{T_{rise}} & \text{for } 0 < t < T_{rise} \\ 1 & \text{for } t > T_{rise} \\ 0 & \text{for } t < 0 \end{cases}$$

Preamplifier effect

Preamplifier Response

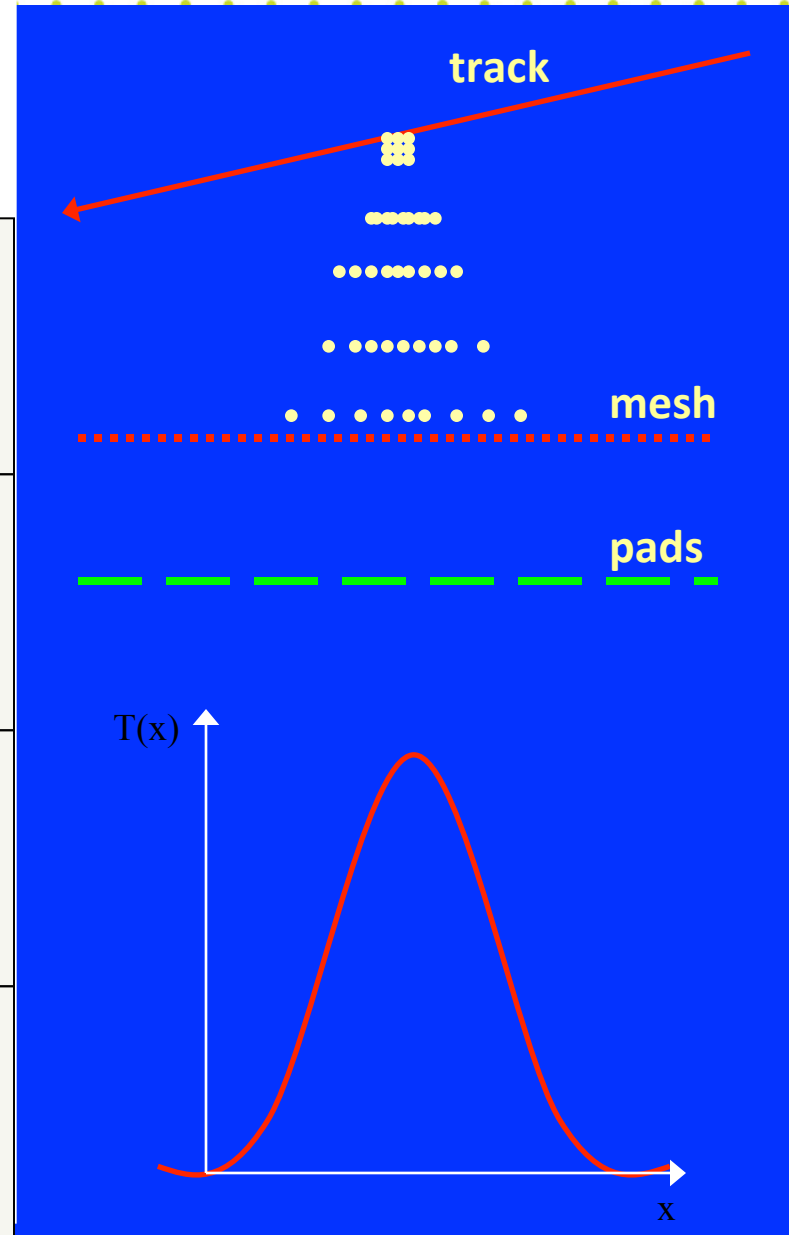
$$H(t) = \begin{cases} \exp\left(-\frac{t}{t_f}\right) \left(1 - \exp\left(\frac{t}{t_r}\right)\right) & \text{for } t > 0 \\ 0 & \text{for } t < 0 \end{cases}$$

Resistive foil + glue

Resistive foil + glue

$$\rho(x, y, t) = \left(\frac{1}{\sigma_t \sqrt{\pi th}}\right)^2 \exp\left(\frac{-(x^2 + y^2)}{4th}\right)$$

$$h = 1/RC$$





# Pulse shape origin

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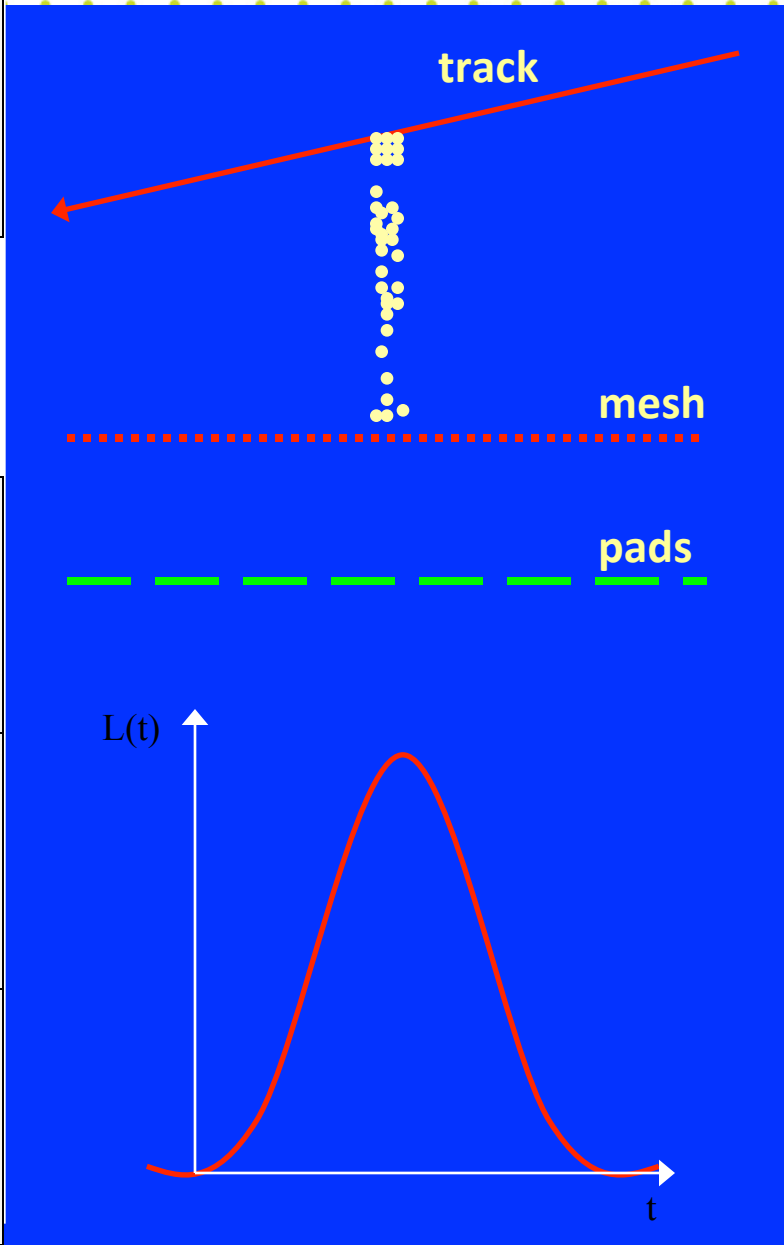
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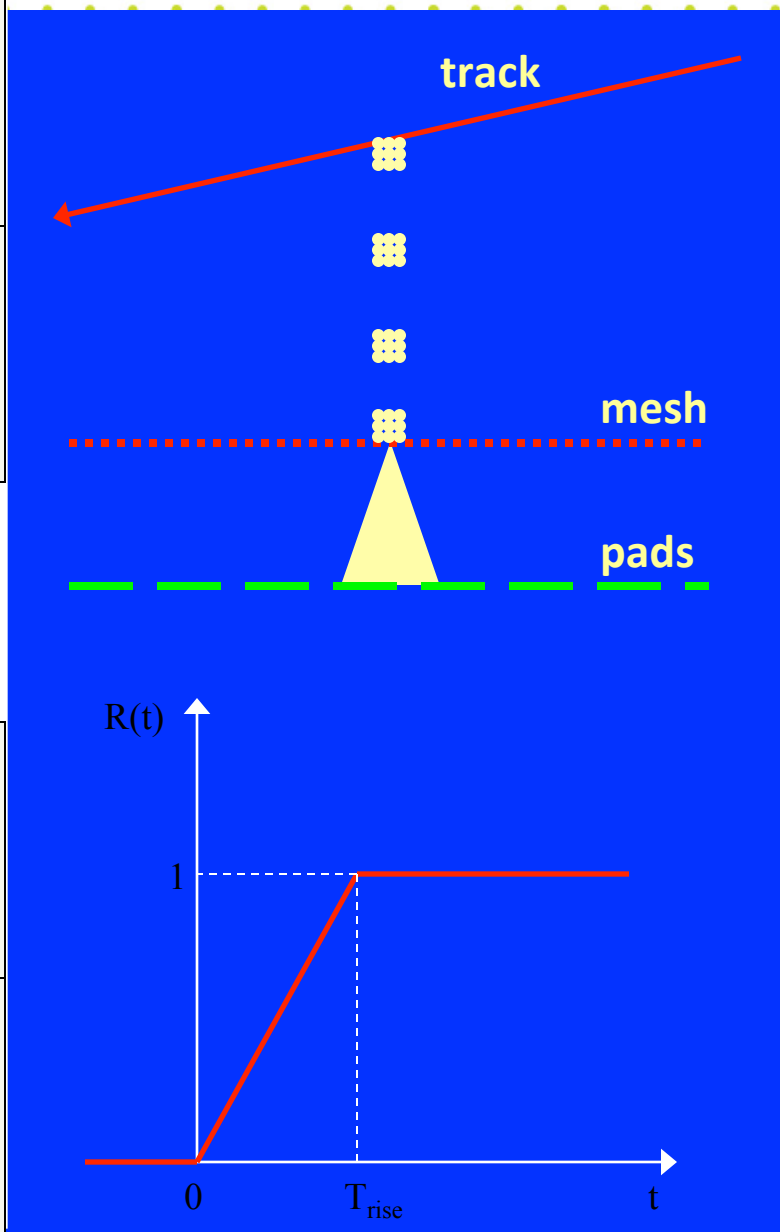
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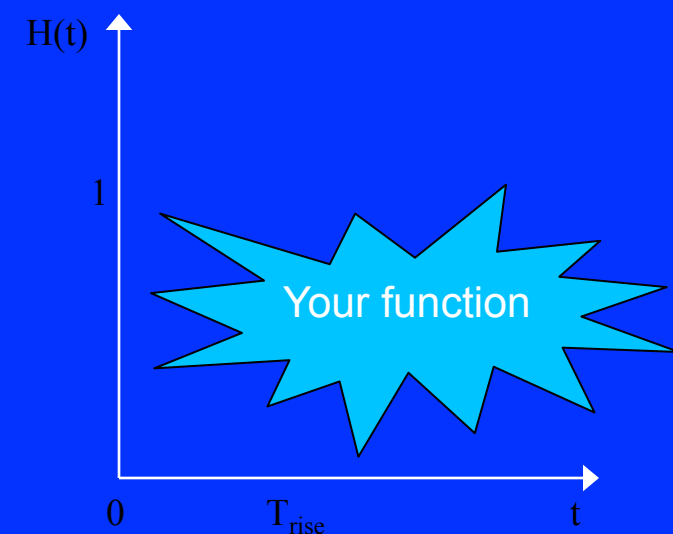
<p>Transverse diffusion</p> <p>Transverse diffusion</p>	$T(x) = \frac{1}{\sigma_x \sqrt{2\pi}} \exp\left(\frac{-x^2}{2\sigma_x^2}\right)$
<p>Longitudinal diffusion</p> <p>Longitudinal diffusion</p>	$L(t) = \frac{1}{\sigma_t \sqrt{2\pi}} \exp\left(\frac{-t^2}{2\sigma_t^2}\right)$
<p>Intrinsic rise time</p> <p>Induction gap</p>	$R(t) = \frac{t}{T_{rise}} \quad \text{for } 0 < t < T_{rise}$ $= 1 \quad \text{for } t > T_{rise}$ $= 0 \quad \text{for } t < 0$
<p>Preamplifier effect</p> <p>Preamplifier Response</p>	$A(t) = \exp\left(-\frac{t}{t_f}\right) \left(1 - \exp\left(-\frac{t}{t_r}\right)\right) \quad \text{for } t > 0$ $= 0 \quad \text{for } t < 0$
<p>Resistive foil + glue</p> <p>Resistive foil + glue</p>	$\rho(x, y, t) = \left(\frac{1}{\sigma_t \sqrt{\pi th}}\right)^2 \exp\left(\frac{-(x^2 + y^2)}{4th}\right)$ $h = 1/RC$





# Pulse shape origin

<p>Transverse diffusion Transverse diffusion</p>	$T(x) = \frac{1}{\sigma_x \sqrt{2\pi}} \exp\left(\frac{-x^2}{2\sigma_x^2}\right)$
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<p>Preamplifier effect Preamplifier Response</p>	$H(t) = \exp\left(-\frac{t}{t_f}\right) \left(1 - \exp\left(-\frac{t}{t_r}\right)\right) \quad \text{for } t > 0$ $= 0 \quad \text{for } t < 0$
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Resistive foil + glue

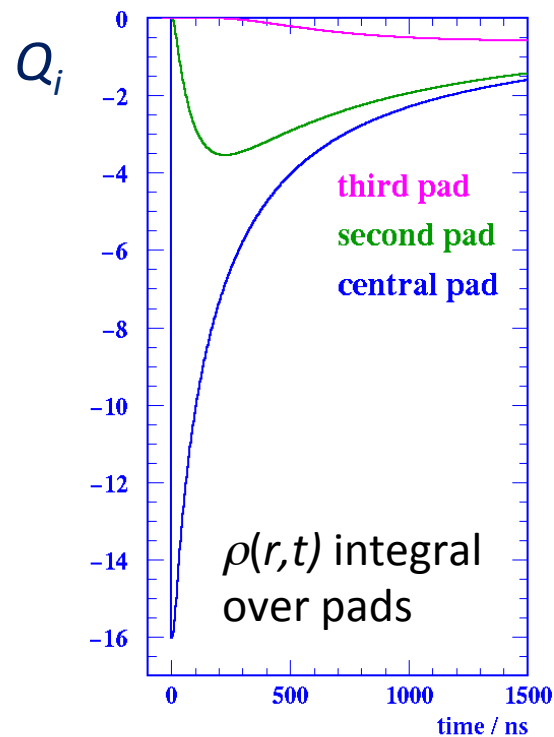
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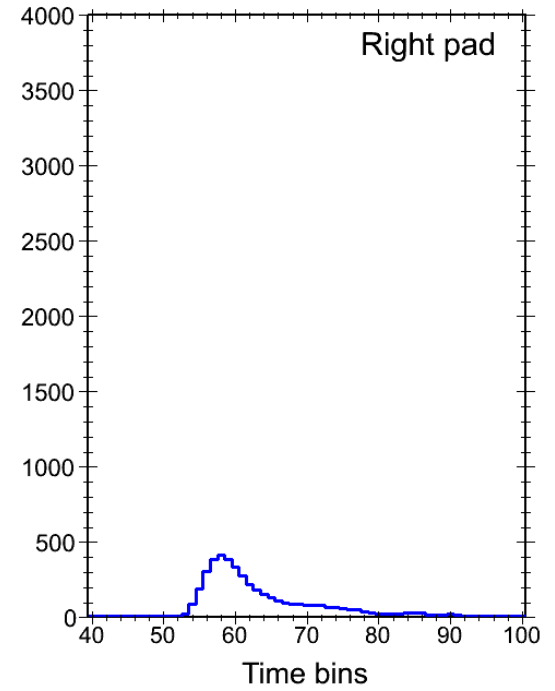
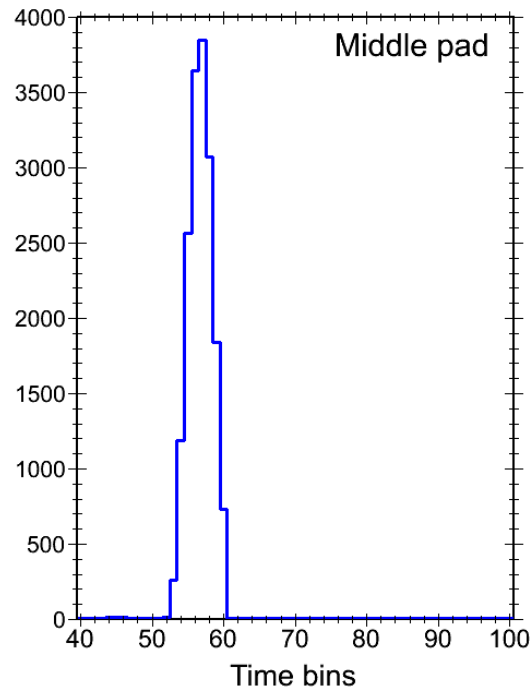
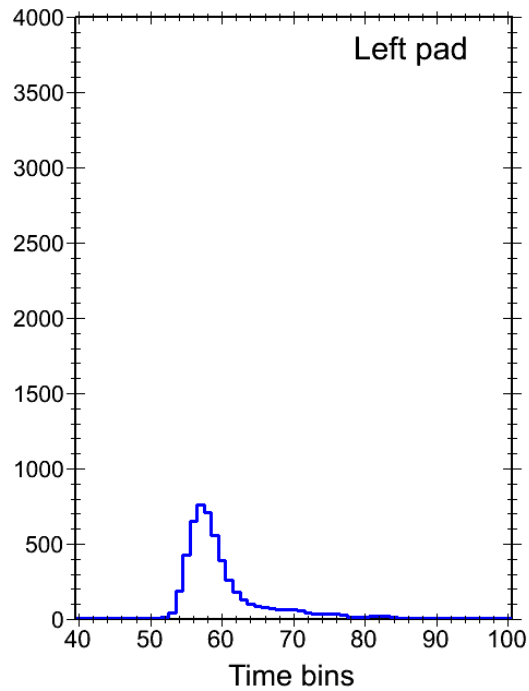
$$Q_i = \int \rho_i(r) dr$$

Stand alone simulation





# Pad Amplitude



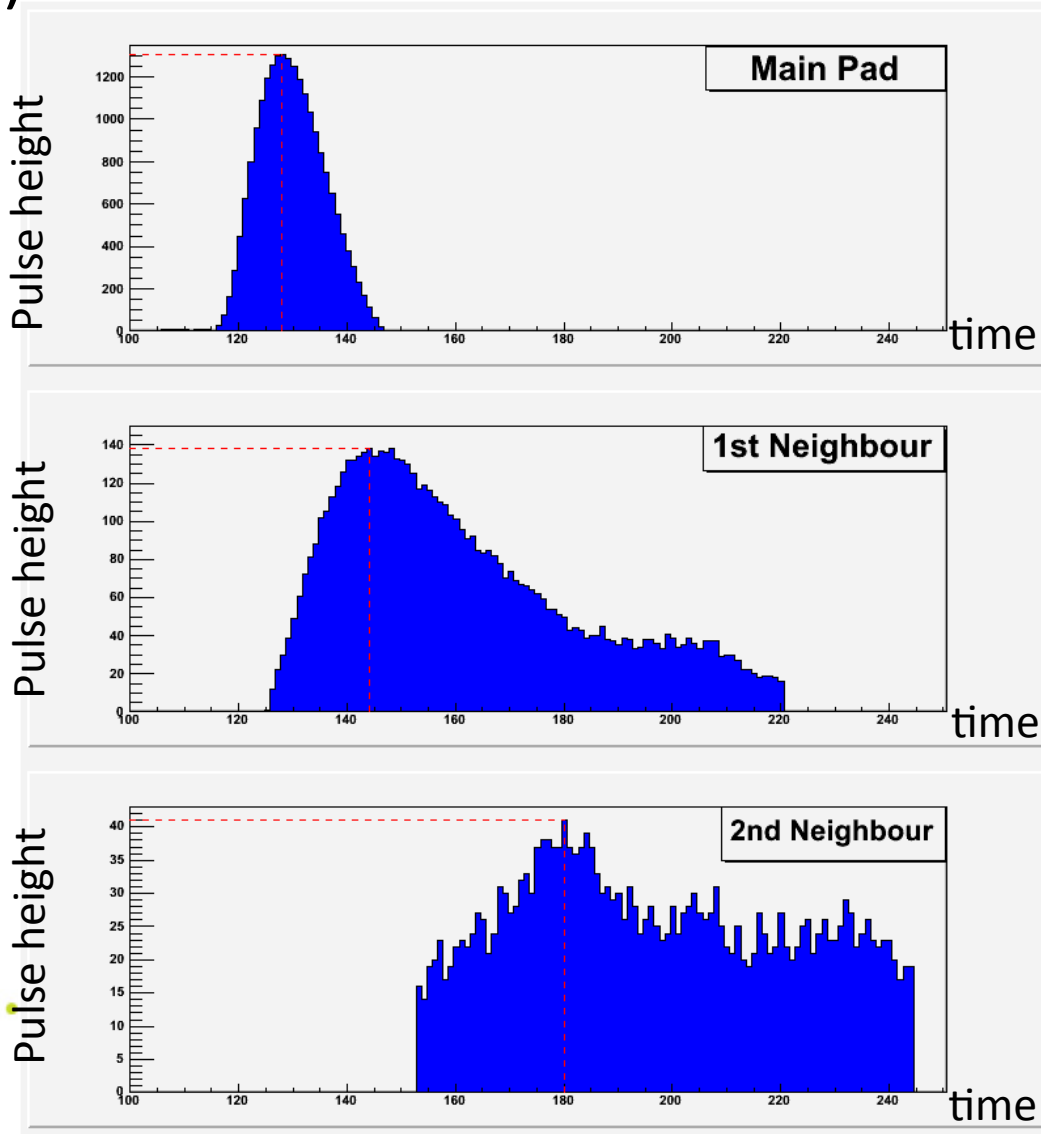


# Pad Amplitude

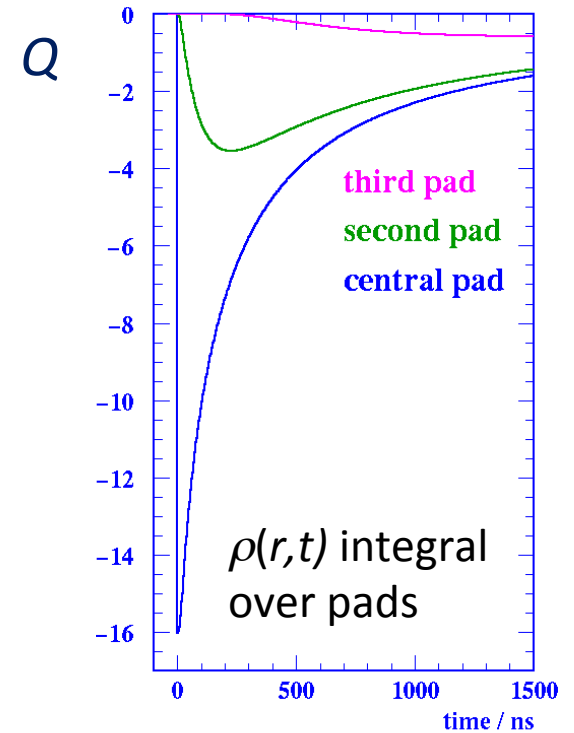
- 1) Use the maximum as the amplitude  
Single Point Maximum (SPM)

$$A_i = \text{max pulse height}$$

P(i)



Default method used  
in MarlinTPC

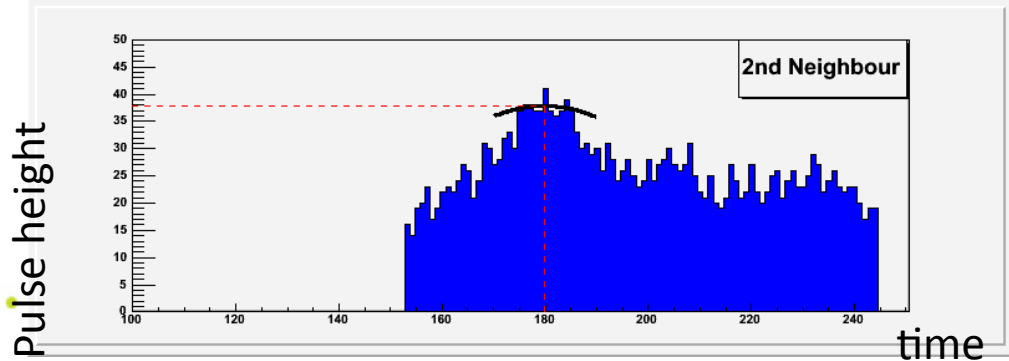
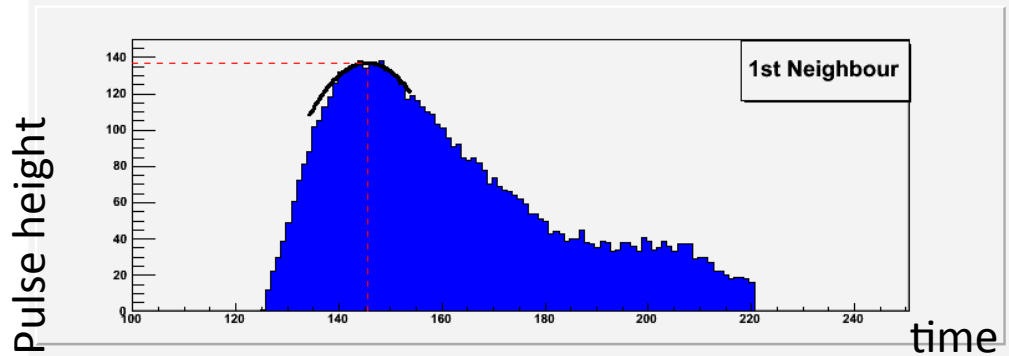
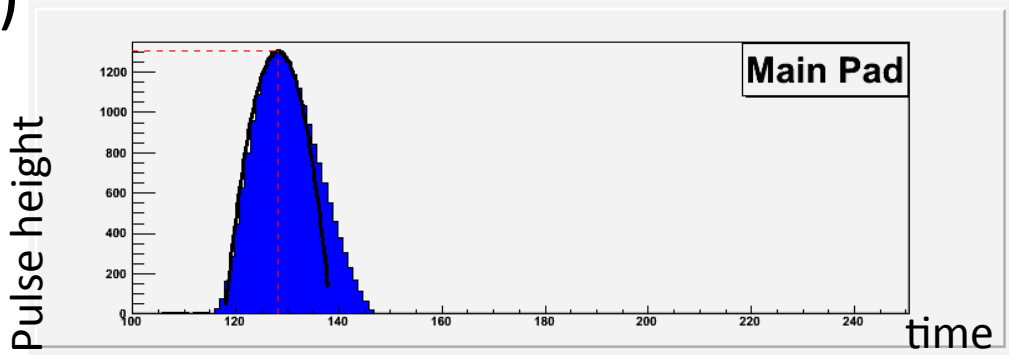


$nS$

## 2) Maximum of Parabola Quadratic Fit Method (QFM)

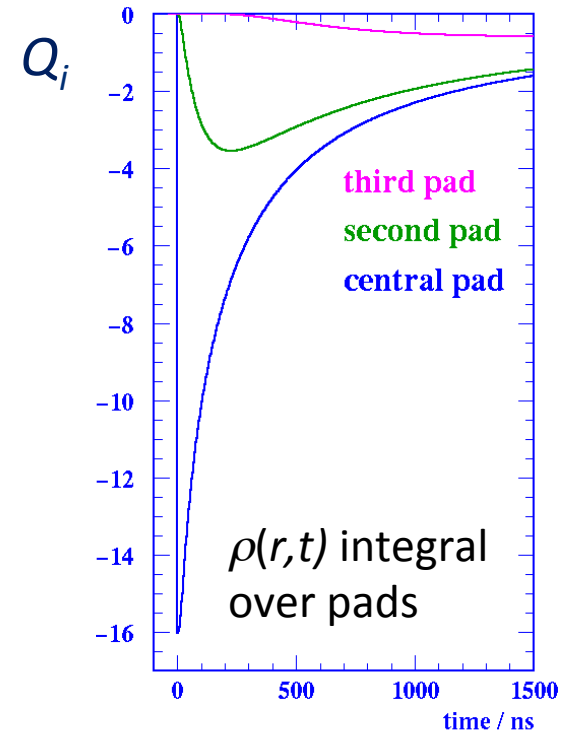
$$A_i = \text{max of parabola}$$

$P(i)$



# Pad Amplitude

Method use pre-2011



$ns$

3) Integrate above threshold

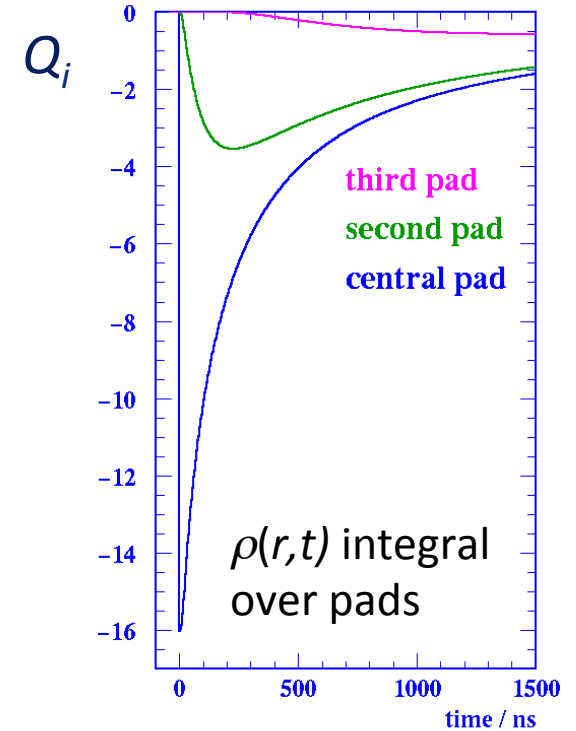
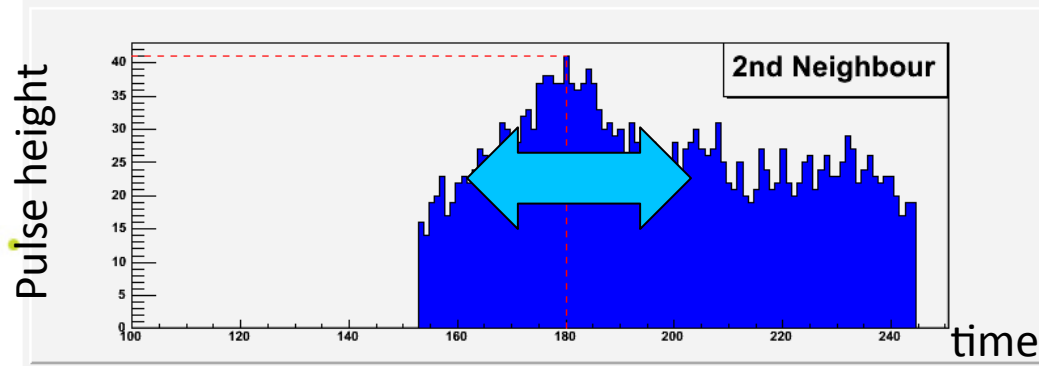
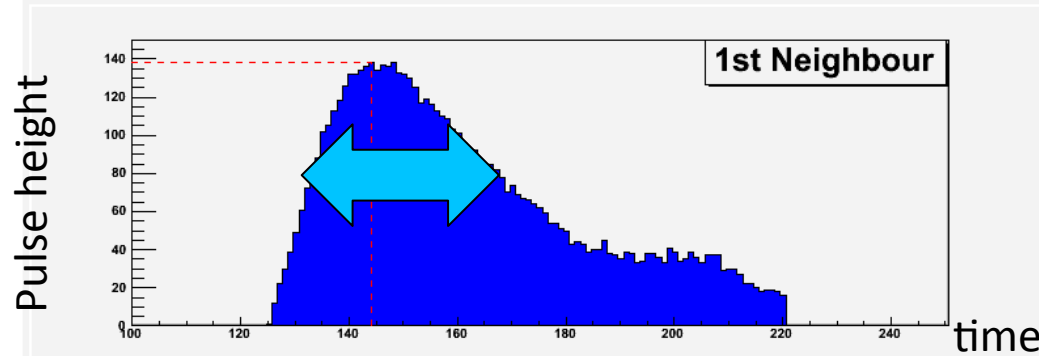
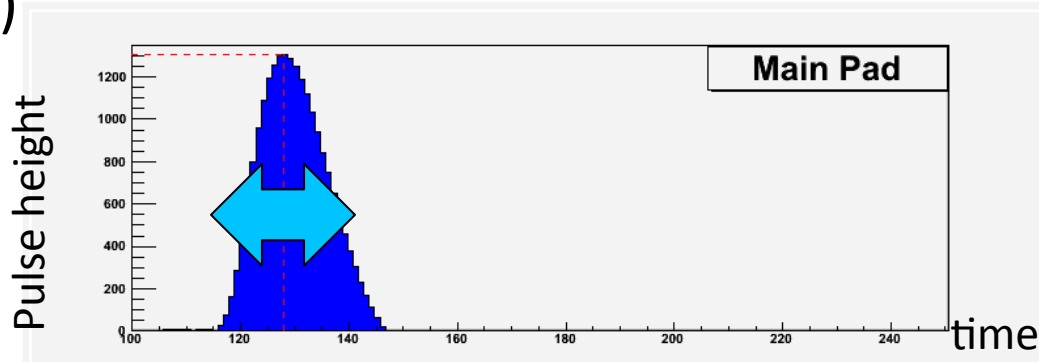
Re-integration method (RM)

$$A_i = \text{Sum } P(i)$$

# Pad Amplitude

Method use in 2011 (still to be implemented for the 2015 data)

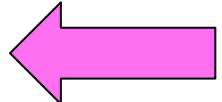
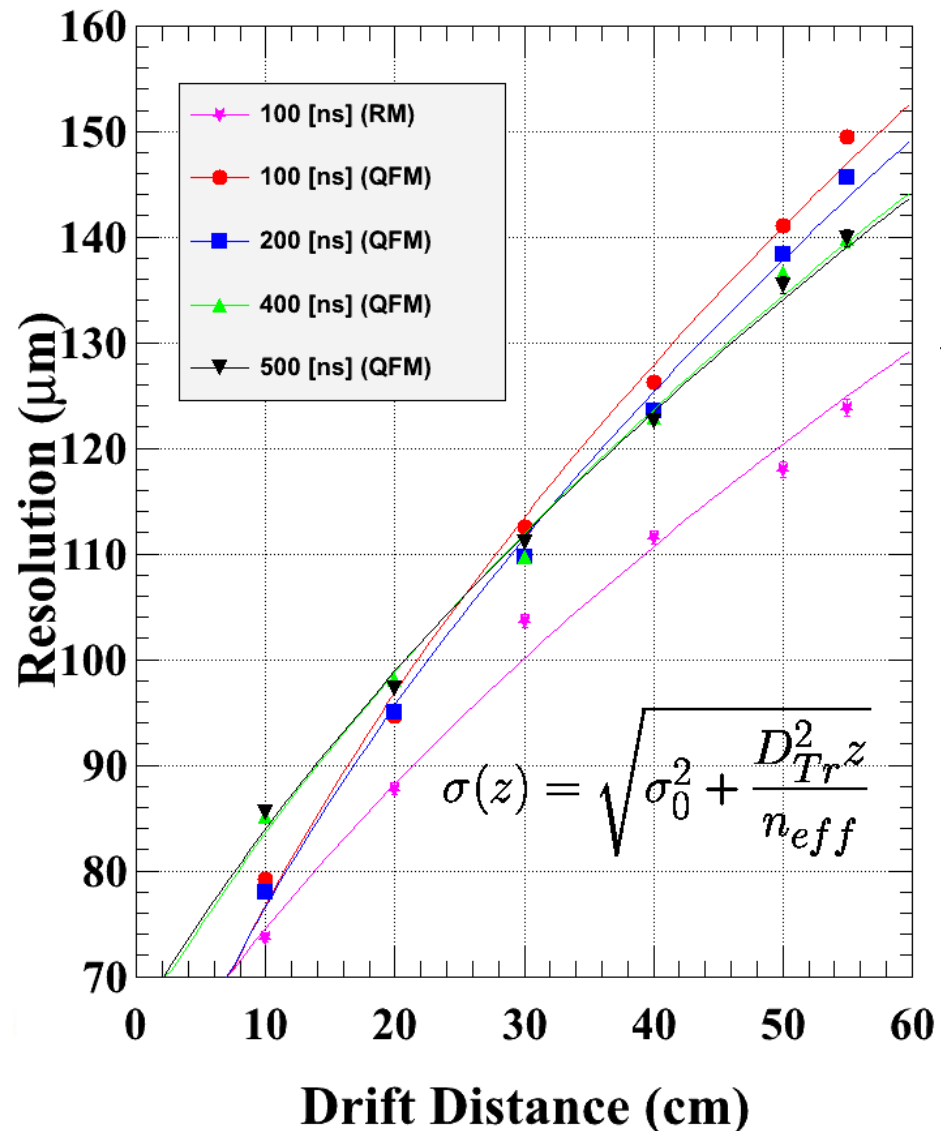
$P(i)$



$nS$

# Transverse Resolution MM

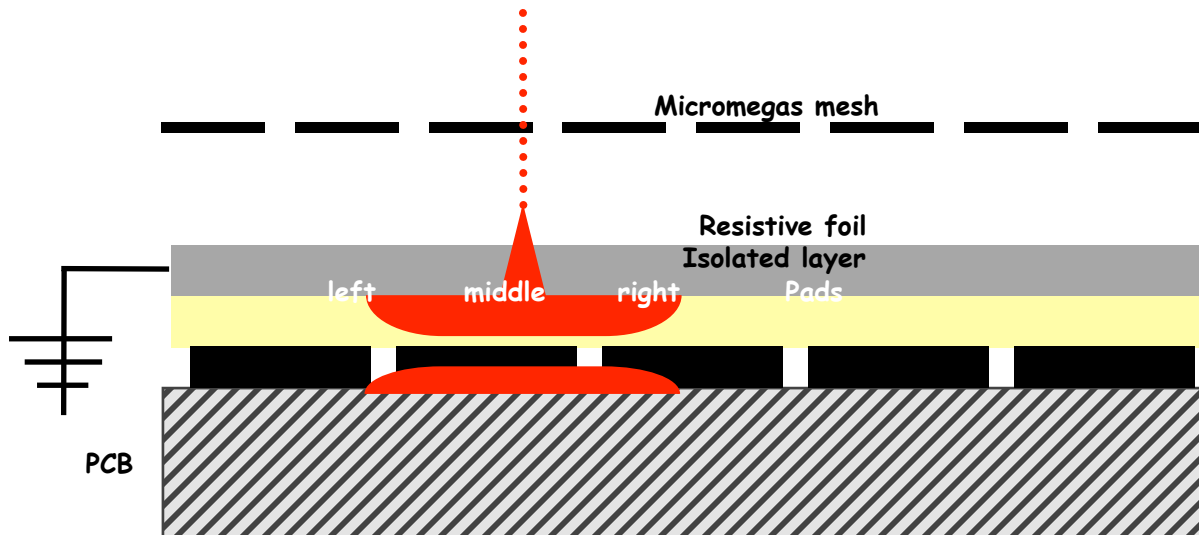
Resolution v. Drift Distance (All Scans)



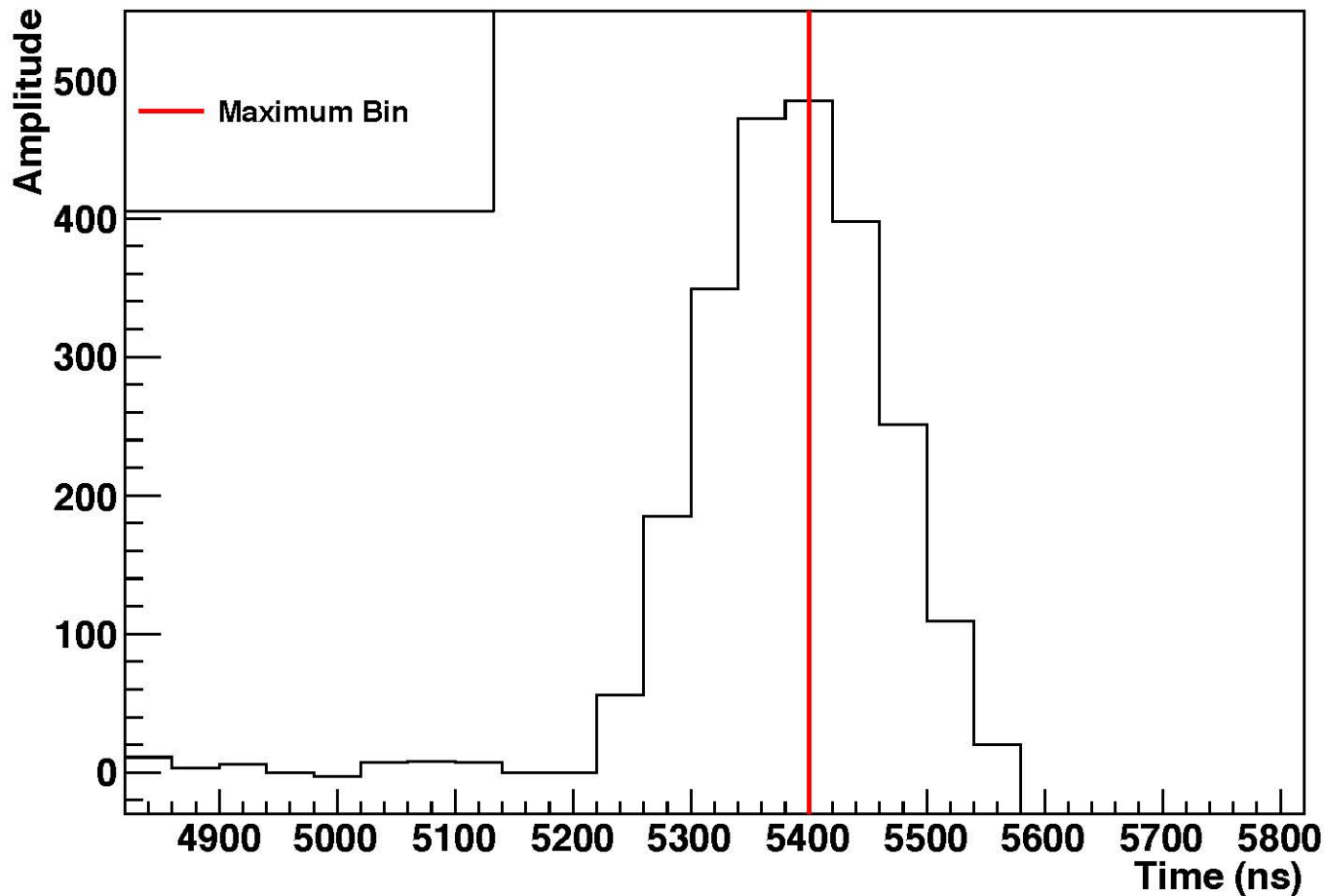
2011 data  
Single module

Source:  
Nicholi Shiell  
M.Sc. Thesis  
Carleton University

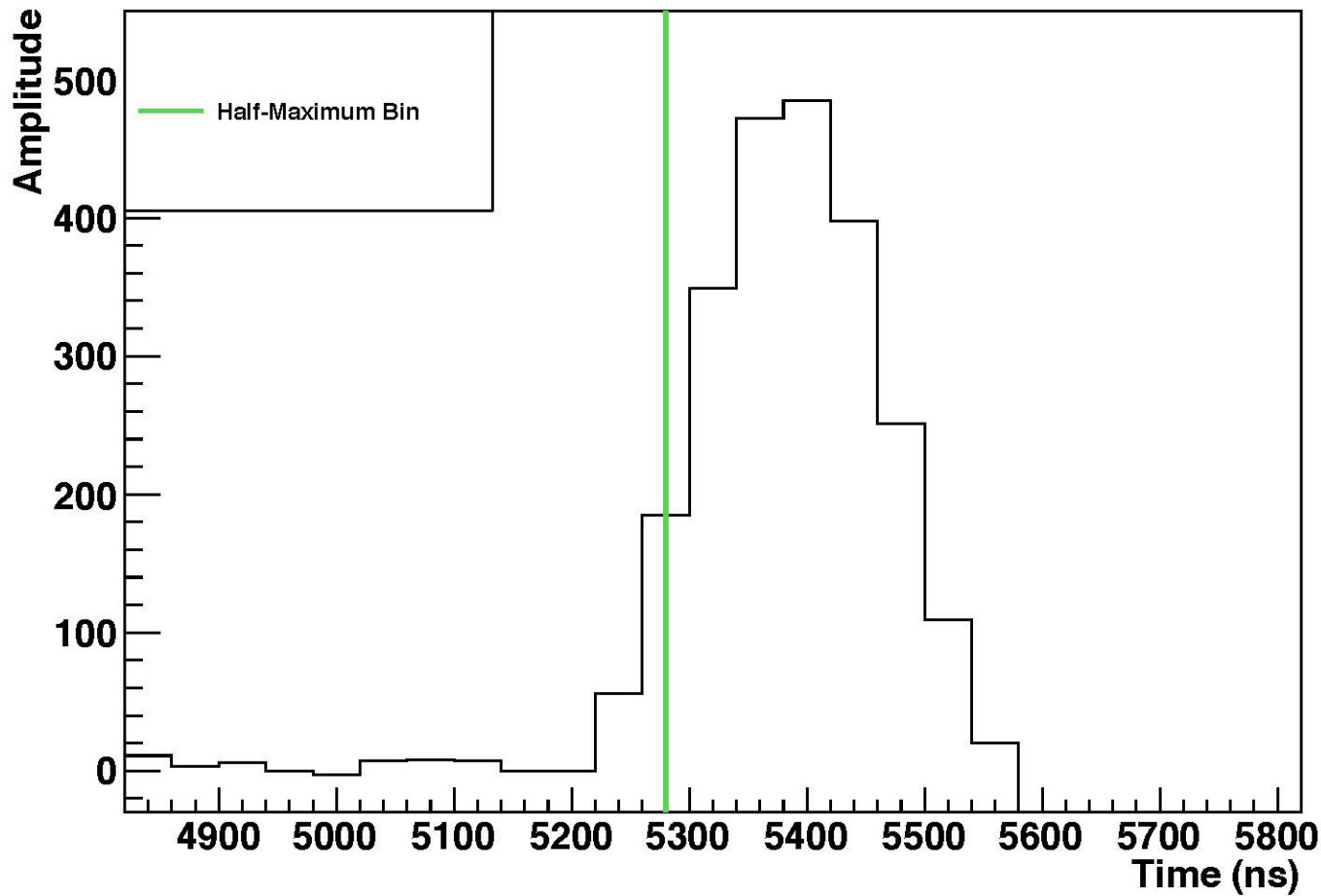
# Charge Dispersion Resistive Anode **r-z plane**



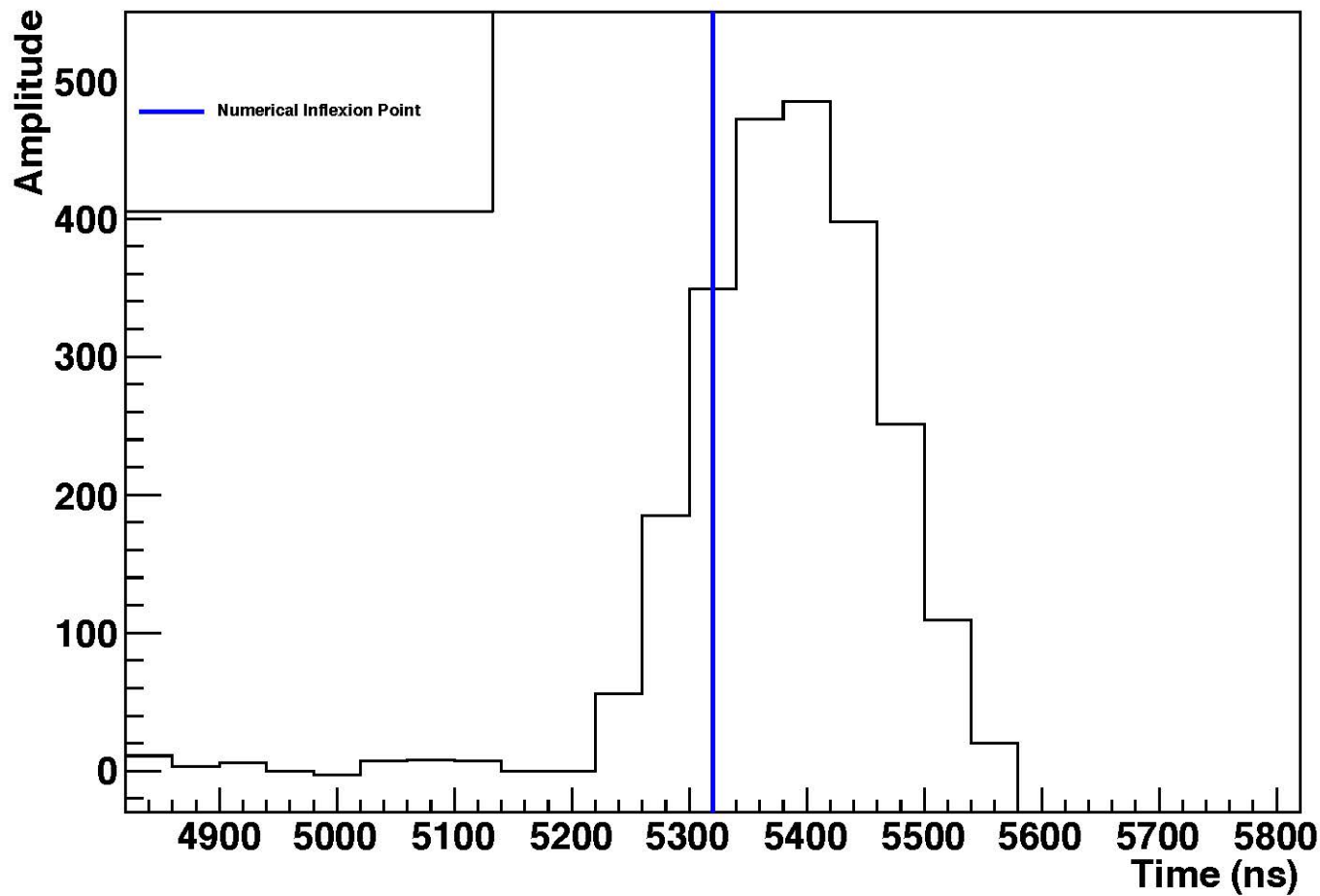
Run 03047, Module 3, Row2



Run 03047, Module 3, Row2

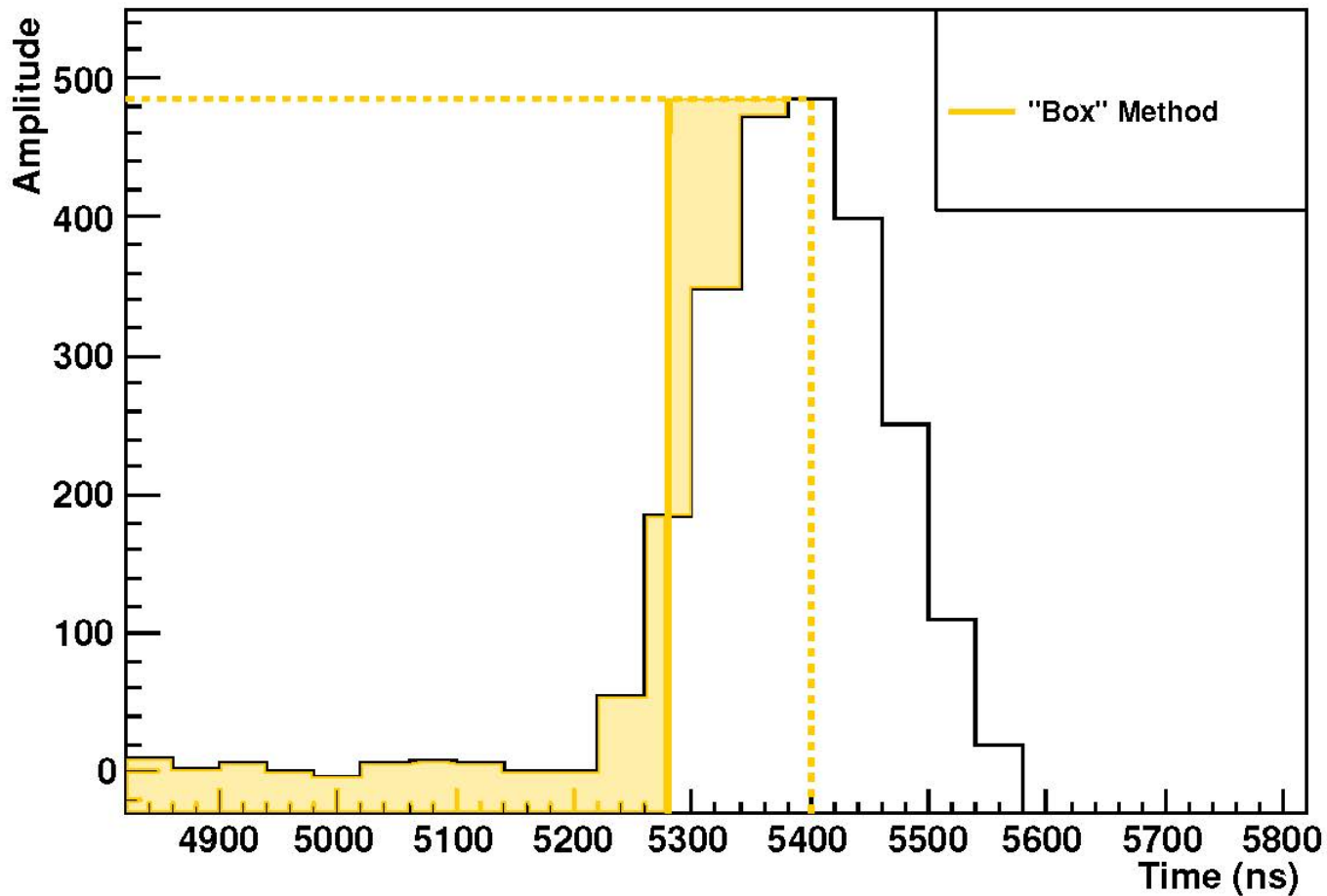


Run 03047, Module 3, Row2

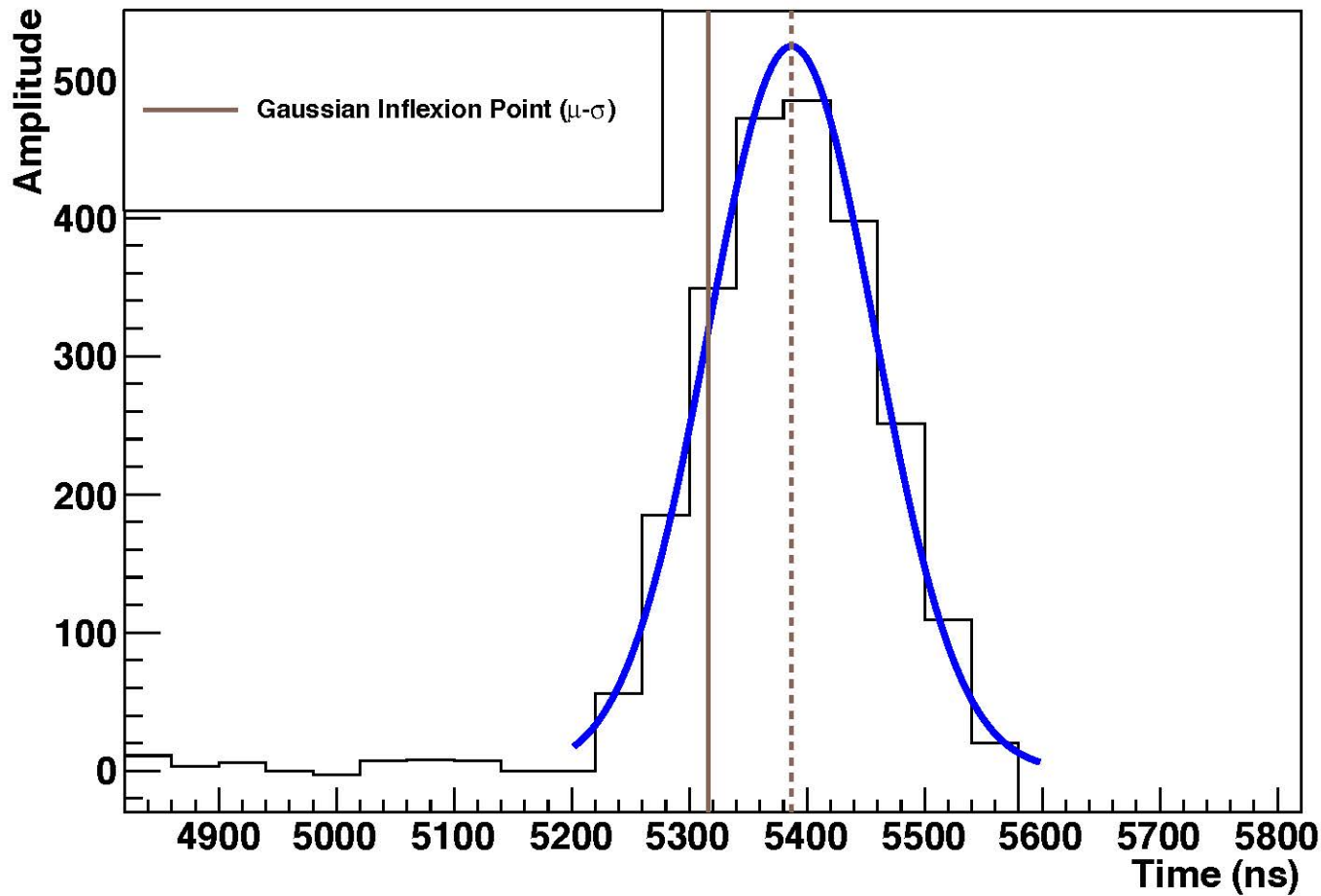




Run 03047, Module 3, Row2

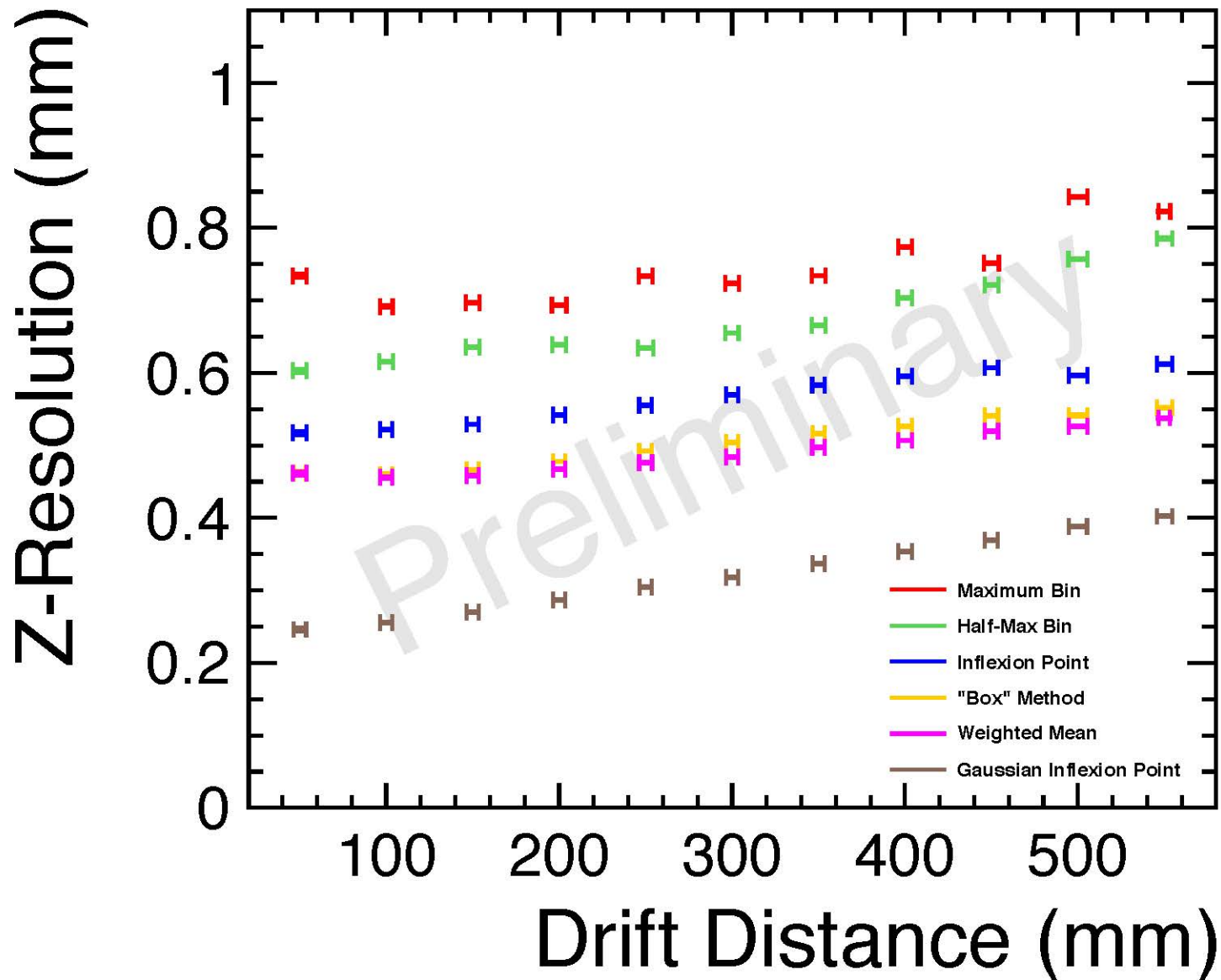


Run 03047, Module 3, Row2

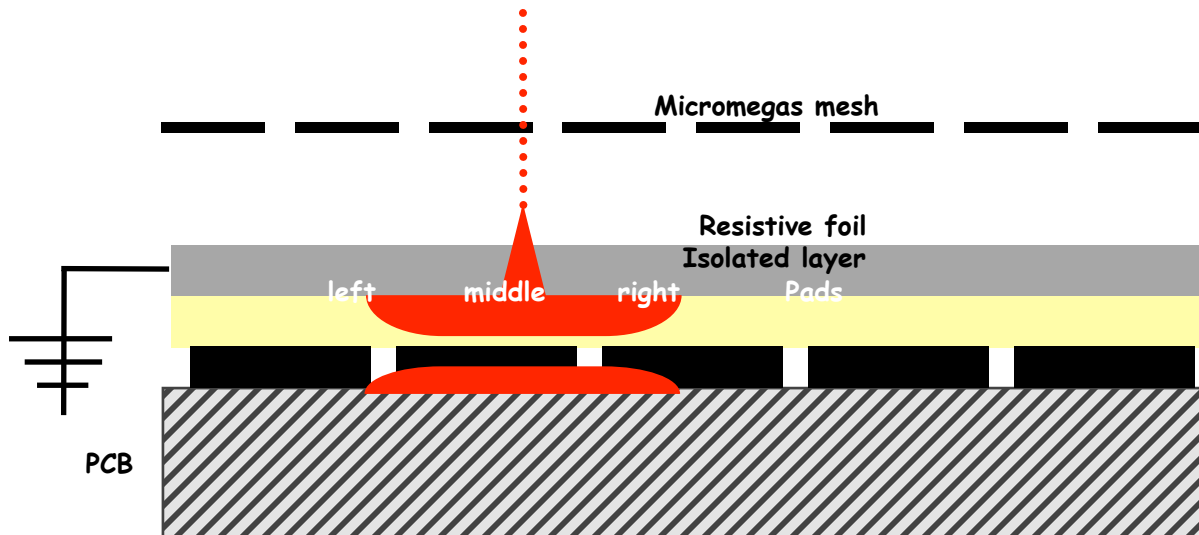


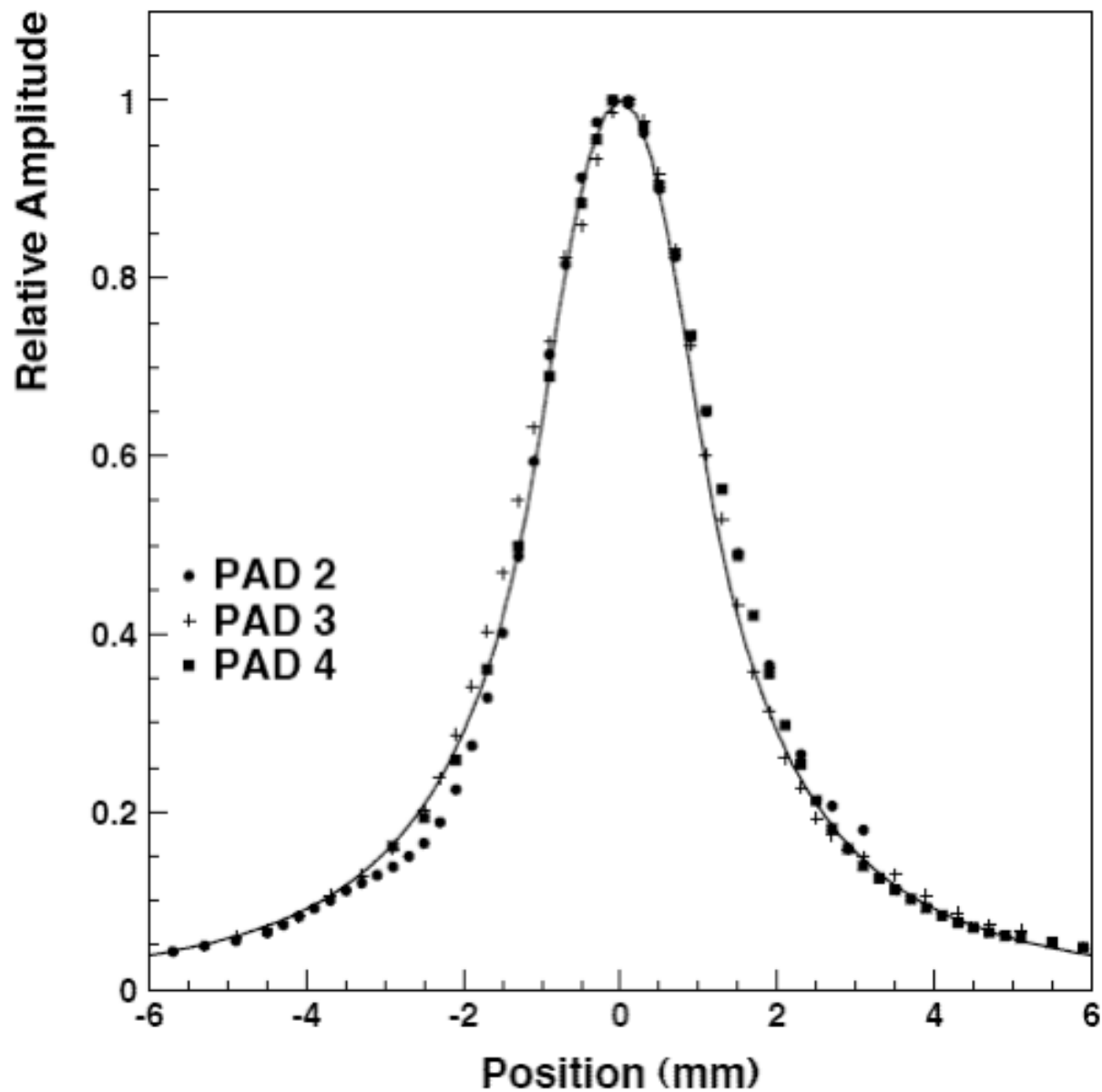
# Z resolution

2014 Z-Resolution Comparison, B=1T

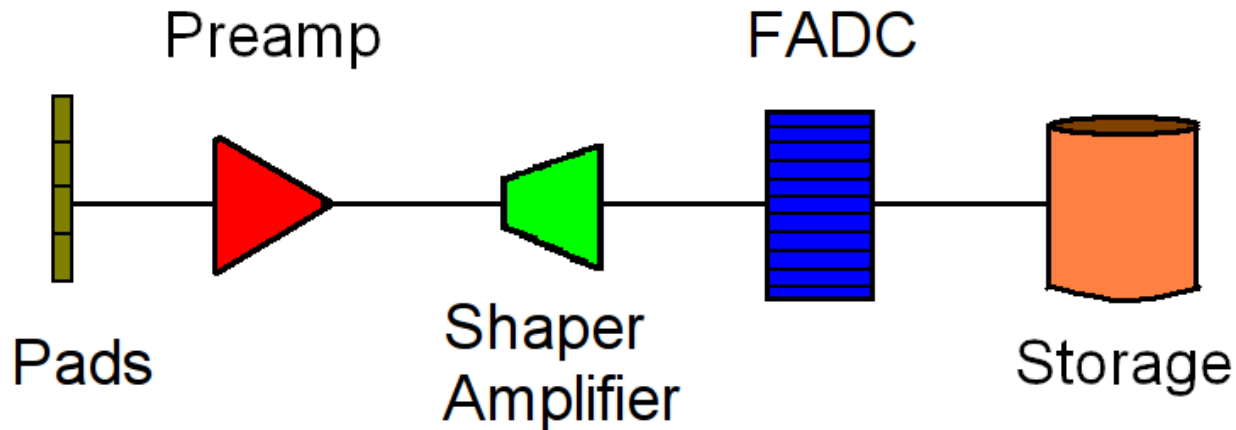
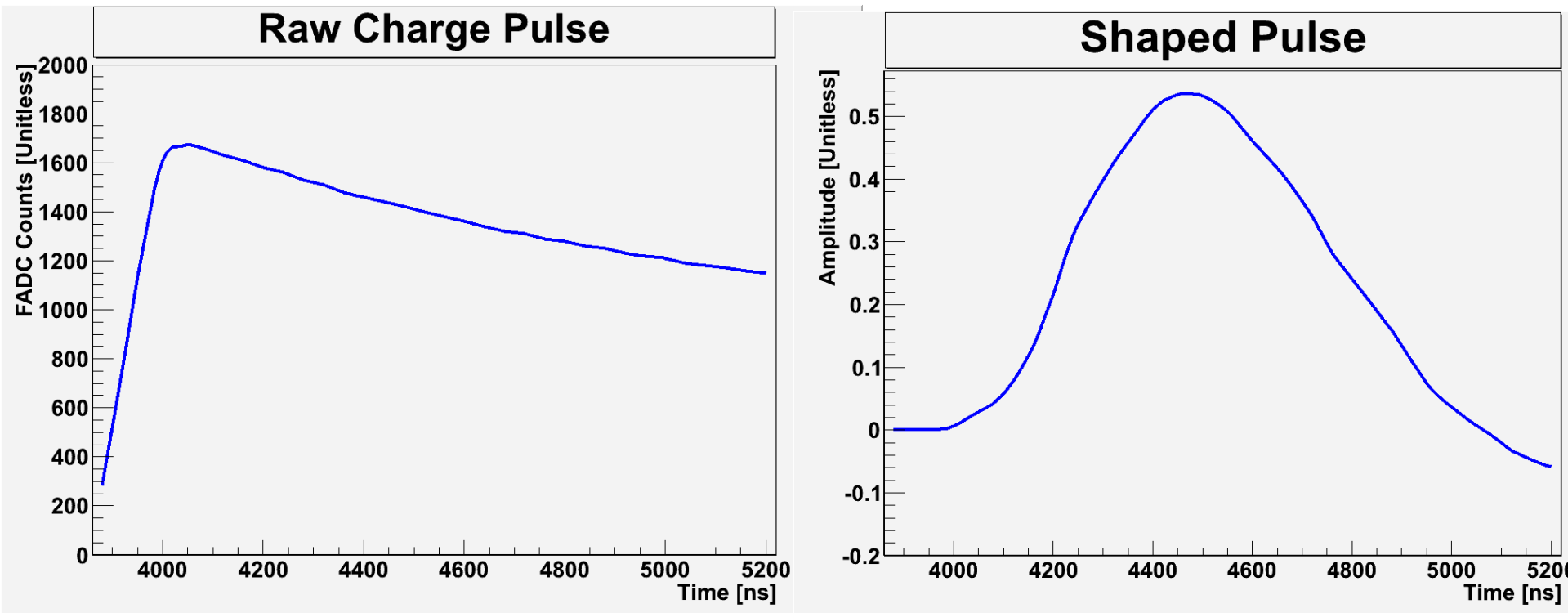


# Charge Dispersion Resistive Anode Simulation

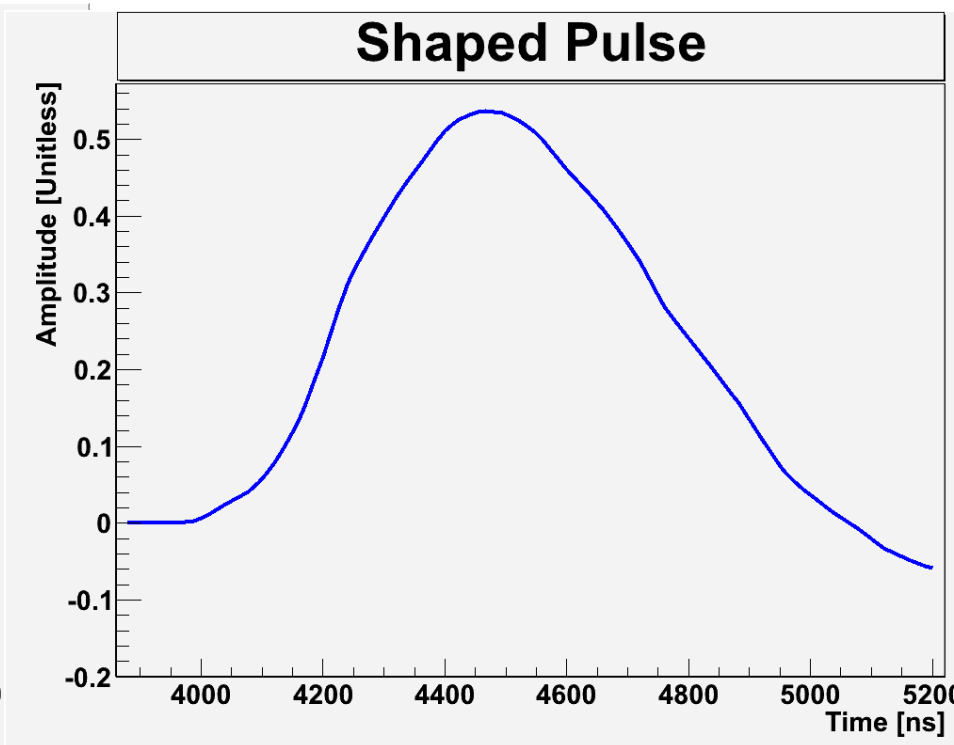
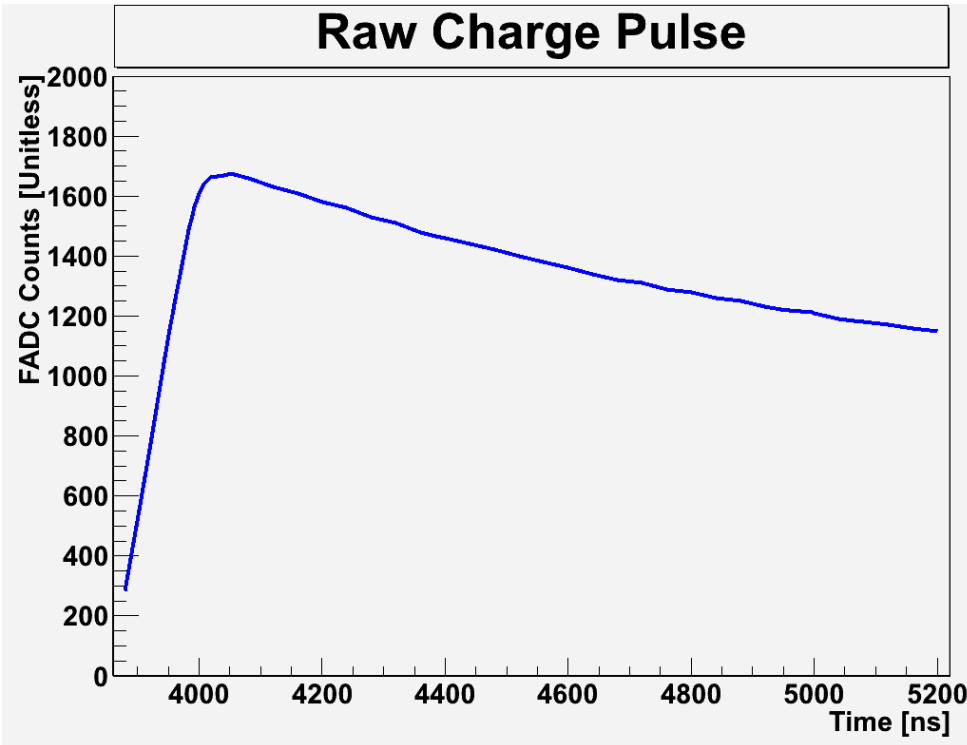




# Raw Charge Shape versus Shaped Pulse



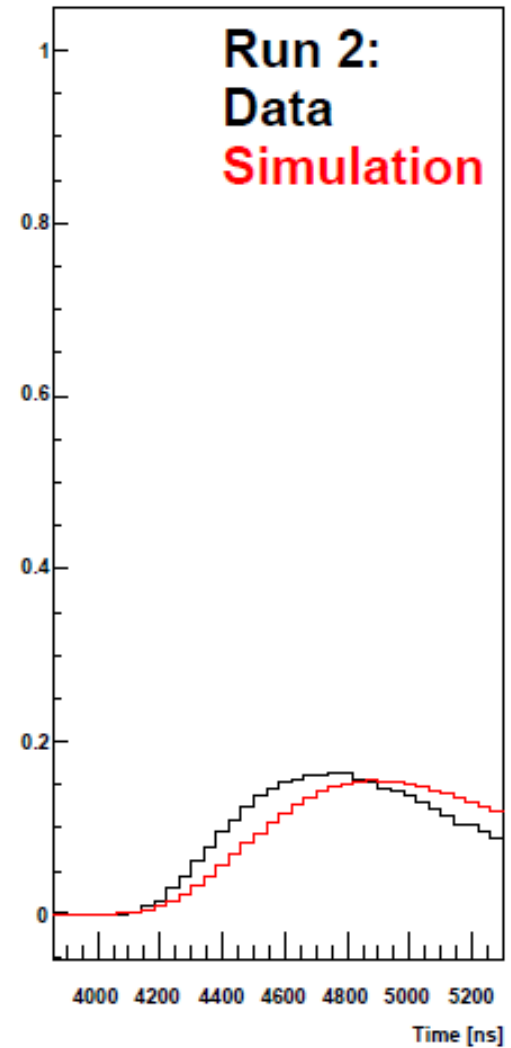
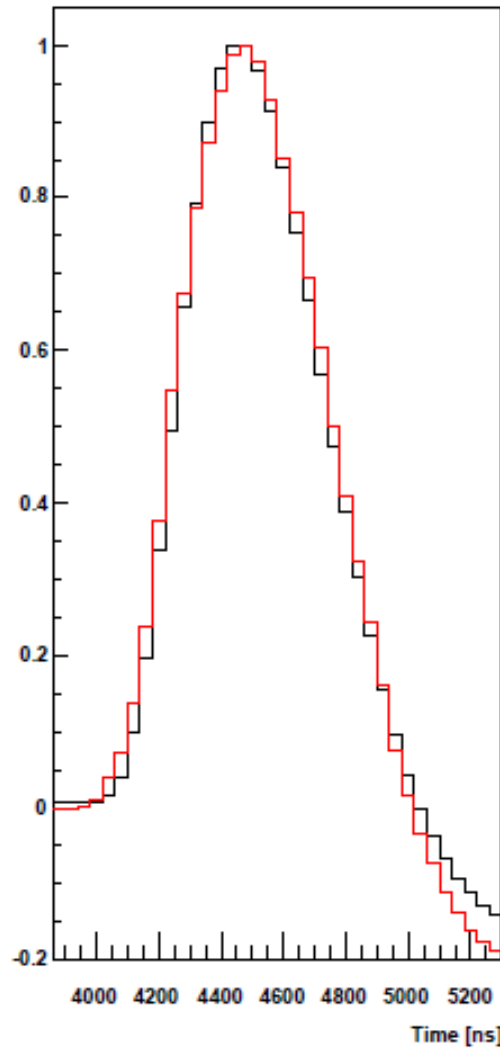
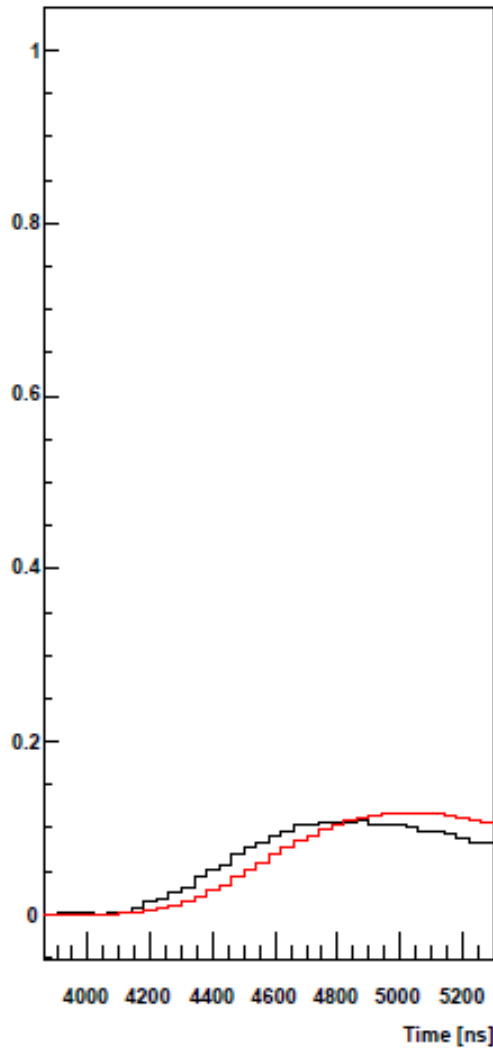
# Raw Charge Shape versus Shaped Pulse



$$H(t) = A_0 \left( \frac{t}{\tau} \right)^3 \sin\left( \frac{t}{b\tau} \right) \exp\left( -\frac{t}{\tau} \right)$$

from Eric Delagnes et al at Saclay

# Simulation pulses (ok)





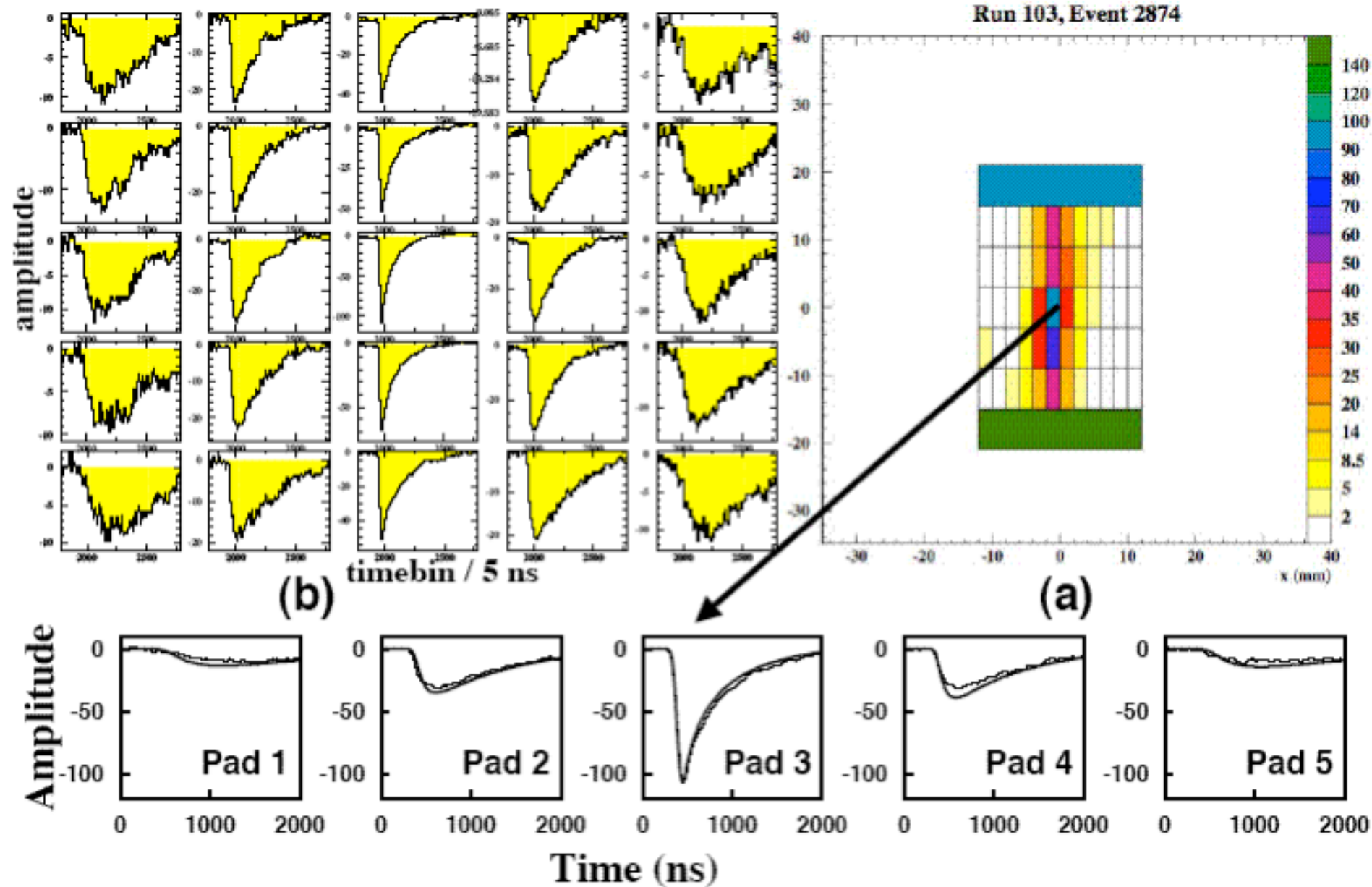


# Simulation pulses

Parameter	Initial value	Final value
Drift speed	76.98 $\mu\text{m}/\text{ns}$	fixed
Transverse diffusion	95.4 $\mu\text{m}/\text{root}(\text{cm})$	fixed
Longitudinal diffusion	231.289 $\mu\text{m}/\text{root}(\text{cm})$	fixed
Resistivity	2.9 $\text{M}\Omega/\text{sq}$	fixed
Glue thickness	75 $\mu\text{m}$	fixed
Dielectric constant	4.5	2.66
Induction time	120 ns	166 ns
b (shaper)	3.7	3.42
$\tau$ (shaper)	151 ns	151 ns
Pad angular width	0.001984 rad	fixed
Pad height	6.84 cm	fixed
Lower radius of bottom row	1.522457785 m	fixed
$X_0$ track	event dependent	
$\phi$ track	event dependent	
Drift distance	30 cm	30 cm



# Simulation – hits along tracks (ok)





# Overview of Simulation

- For each pad we have **charge** (ADC) as a function of **time** (40 ns intervals)
- Define pad geometry (to do)

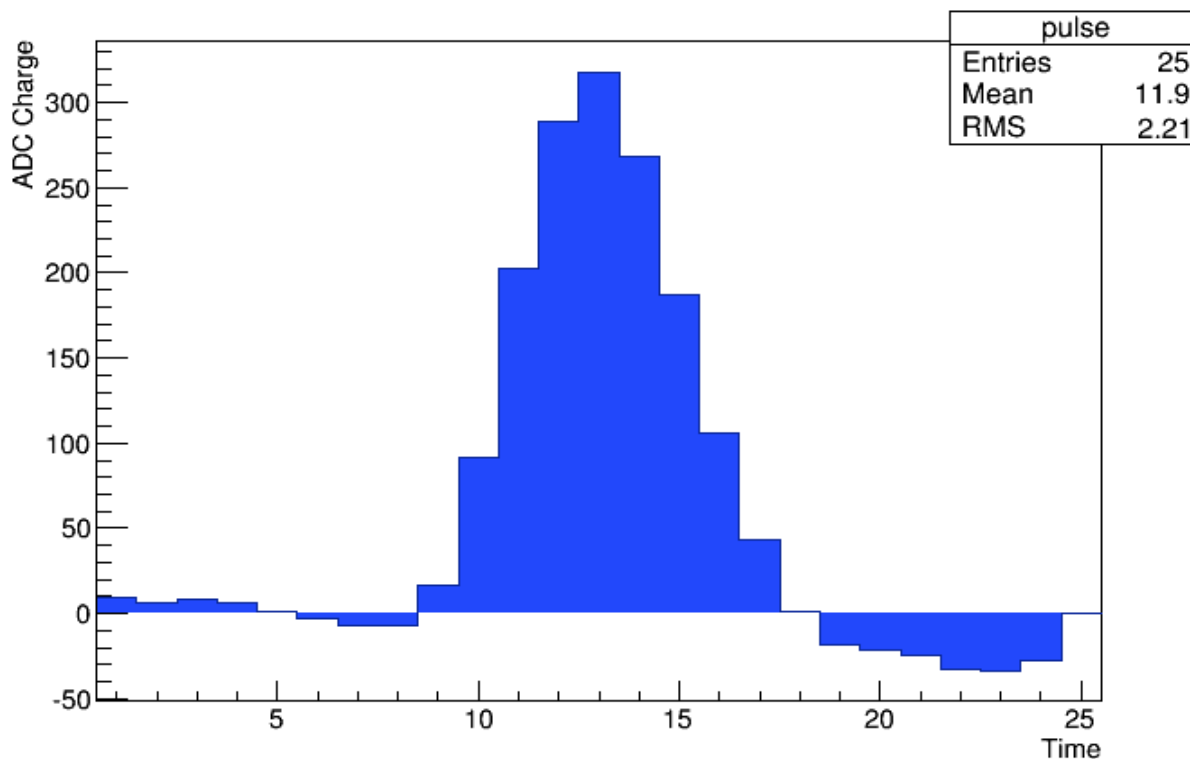
## Steps from ionization to tracks:

- 1) Generate ionization along tracks (ok)
- 2) Drift ions: longitudinal & transverse diffusion (ok)
- 3) Signal pulse: induction gap, resistive layer and electronics shaping (ok)
- 4) Determine **amplitude** and **arrival time** of each pad pulse (in dev: algorithm to deal with overlapping pulses)
- 5) Group **pulses** on each row into **hits**
- 6) Use hit positions to fit **tracks**
- 7) Get two-track resolution / single-hit resolution



# Pulse Amplitude/Time Determination

- Each readout pad produces an **electronic pulse** which encodes the charge
- Need to determine the **amplitude/time** of this pulse
- **New method:** *Reintegration* over fixed time interval and *Gaussian Inflection* (assume negligible error on time zero)





# Conclusions

- Simulation of resistive layer validated with data
- The basic framework for producing hits is in place
- Still need to fine-tune pulse finding in multi-track environment
- Define geometry: using GEAR file LCTPC
- Project for new M.Sc. Student at Carleton
- Benchmarked two-track separation power of the MM with resistive layer