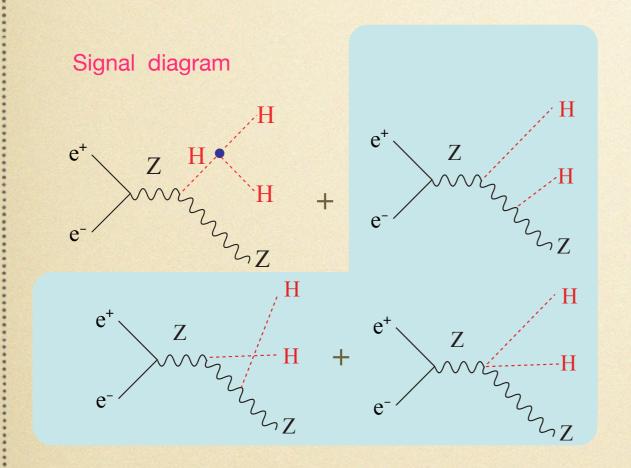
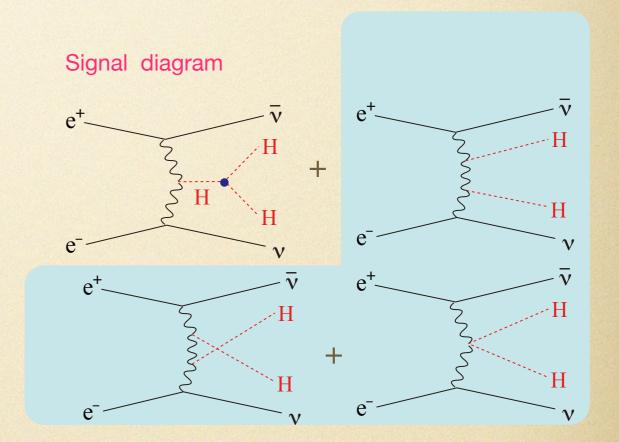
# correlations between $\lambda_{HHHH}$ and $g_{HHVV}$ , $g_{HVV}$

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Asian Physics & Software Group Meeting, Dec. 18, 2015

### double Higgs production





• how the uncertainties of  $g_{HHVV}$  and  $g_{HVV}$  become systematic errors of  $\lambda_{HHH}$  measurement?

#### parametrisation

$$\sigma = S\kappa_{\lambda}^{2} + Q\kappa_{q}^{2} + B\kappa_{b}^{2} + I_{SQ}\kappa_{\lambda}\kappa_{q} + I_{SB}\kappa_{\lambda}\kappa_{b} + I_{QB}\kappa_{q}\kappa_{b}$$

 $κ_{\lambda}$ : coupling  $λ_{HHH}$  scaled to SM value

κ<sub>q</sub>: coupling HHVV scaled to SM value

кь: coupling HVV scaled to SM value

S: contribution from  $\lambda_{HHH}$  diagram

Q: contribution from quartic HHVV diagram

B: contribution from HVV diagram

I<sub>SQ</sub>: interference between diagrams with  $\lambda_{HHH}$  and HHVV

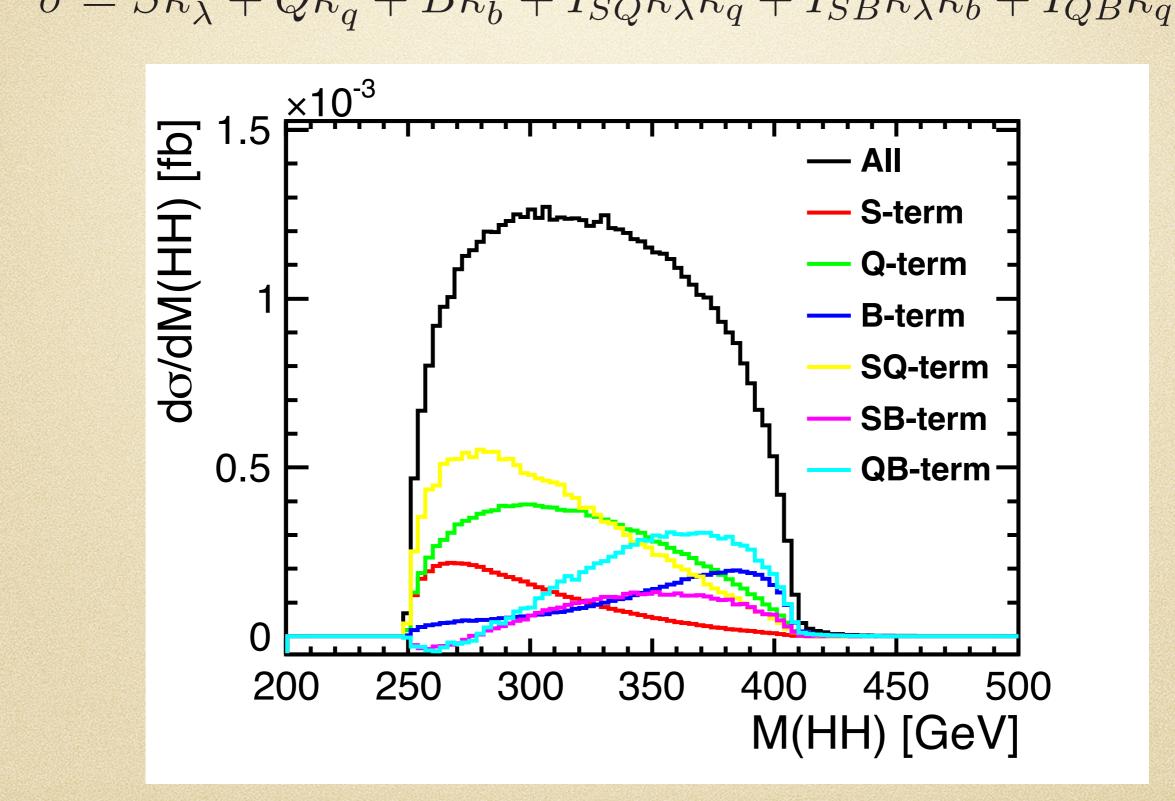
I<sub>SB</sub>: interference between diagrams with  $\lambda_{HHH}$  and HVV

IQB: interference between diagrams with HHVV and HVV

(values calculated by physsim)

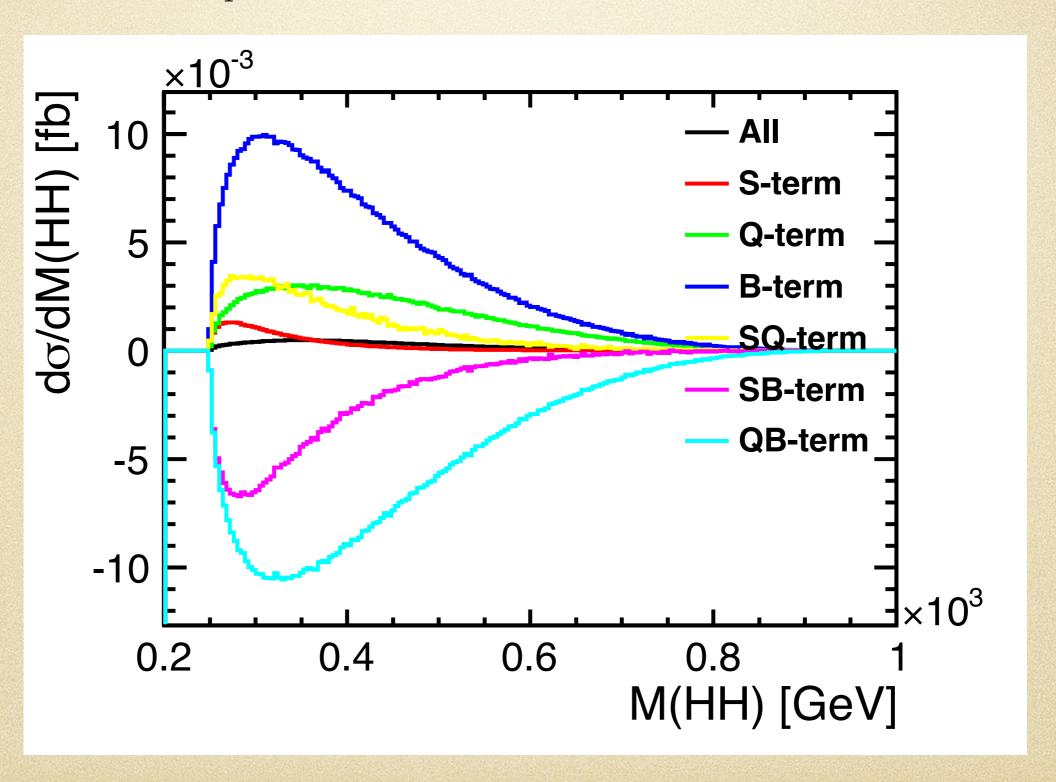
### dσ/dM(HH) for each term: ZHH @ 500 GeV

$$\sigma = S\kappa_{\lambda}^{2} + Q\kappa_{q}^{2} + B\kappa_{b}^{2} + I_{SQ}\kappa_{\lambda}\kappa_{q} + I_{SB}\kappa_{\lambda}\kappa_{b} + I_{QB}\kappa_{q}\kappa_{b}$$



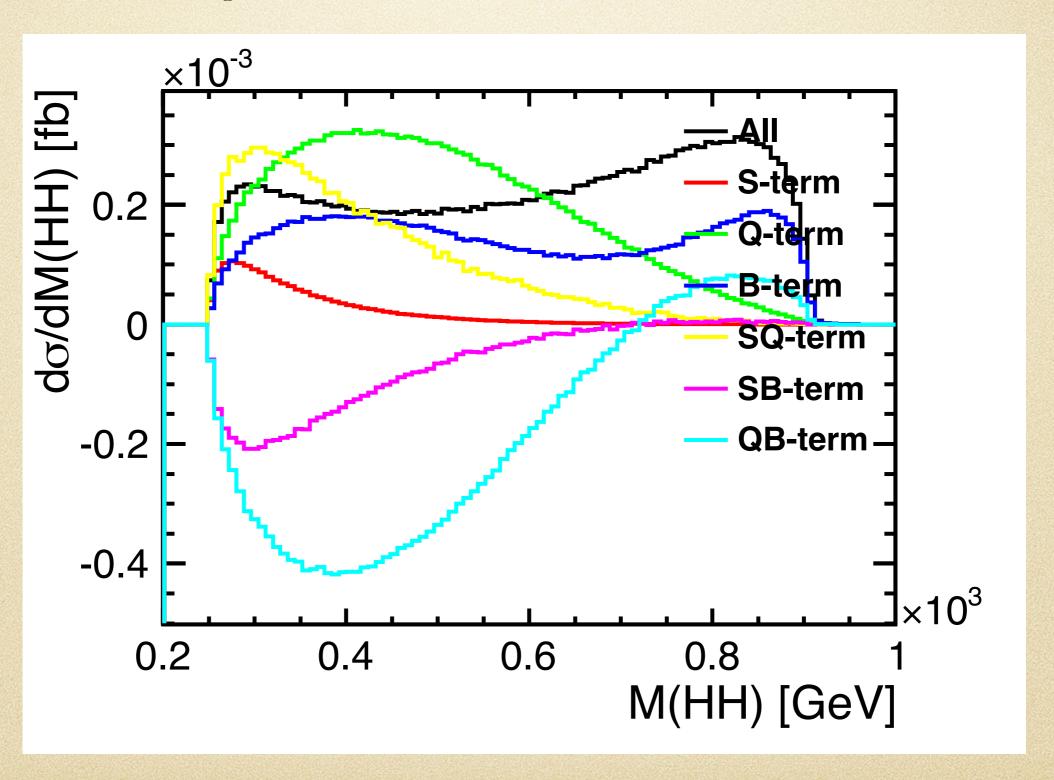
### dσ/dM(HH) for each term: vvHH@1 TeV

$$\sigma = S\kappa_{\lambda}^{2} + Q\kappa_{q}^{2} + B\kappa_{b}^{2} + I_{SQ}\kappa_{\lambda}\kappa_{q} + I_{SB}\kappa_{\lambda}\kappa_{b} + I_{QB}\kappa_{q}\kappa_{b}$$



#### dσ/dM(HH) for each term: ZHH@1 TeV

$$\sigma = S\kappa_{\lambda}^{2} + Q\kappa_{q}^{2} + B\kappa_{b}^{2} + I_{SQ}\kappa_{\lambda}\kappa_{q} + I_{SB}\kappa_{\lambda}\kappa_{b} + I_{QB}\kappa_{q}\kappa_{b}$$



### fitting $\kappa_{\lambda}$ , $\kappa_{q}$ , $\kappa_{b}$

$$\sigma = S\kappa_{\lambda}^{2} + Q\kappa_{q}^{2} + B\kappa_{b}^{2} + I_{SQ}\kappa_{\lambda}\kappa_{q} + I_{SB}\kappa_{\lambda}\kappa_{b} + I_{QB}\kappa_{q}\kappa_{b}$$

no contraint 
$$\chi^2 = \sum_i^n (\frac{\sigma_i - \sigma_i'}{\Delta \sigma_i})^2 \quad \frac{\sigma: \text{ measured value}}{\Delta \sigma: \text{ measurement error}} \\ \sigma': \text{ predicted value}$$

3 observables are considered σ<sub>ZHH</sub> @ 500 GeV

σzhh @ 1 TeV

 $\sigma_{vvHH}$  @ 1 TeV

20.2%

 $\Delta \sigma / \sigma$ 

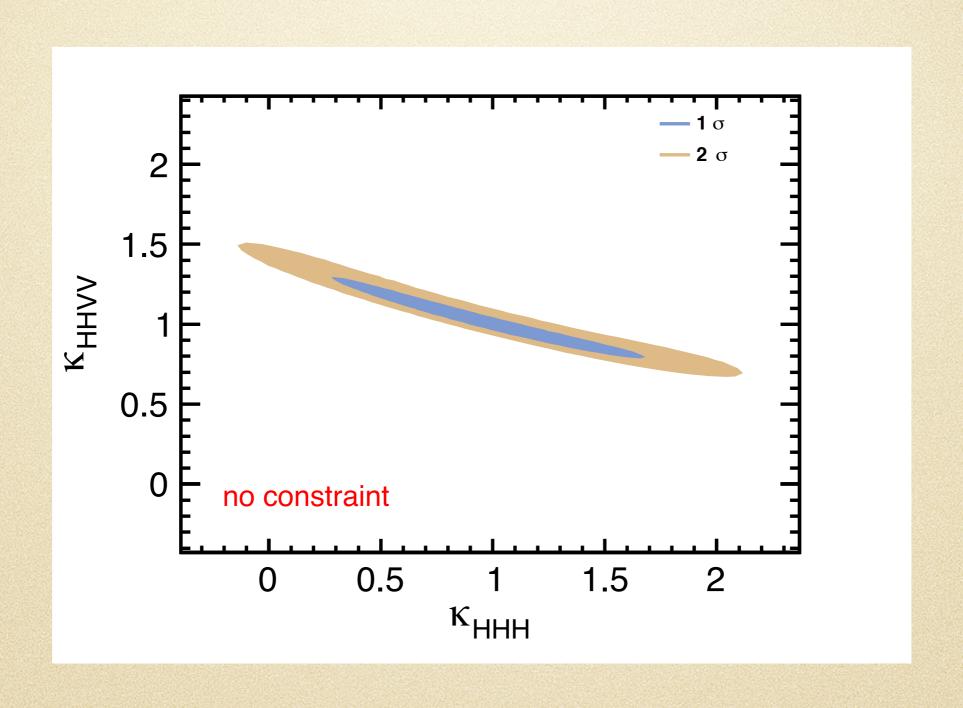
19.2%

15.2%

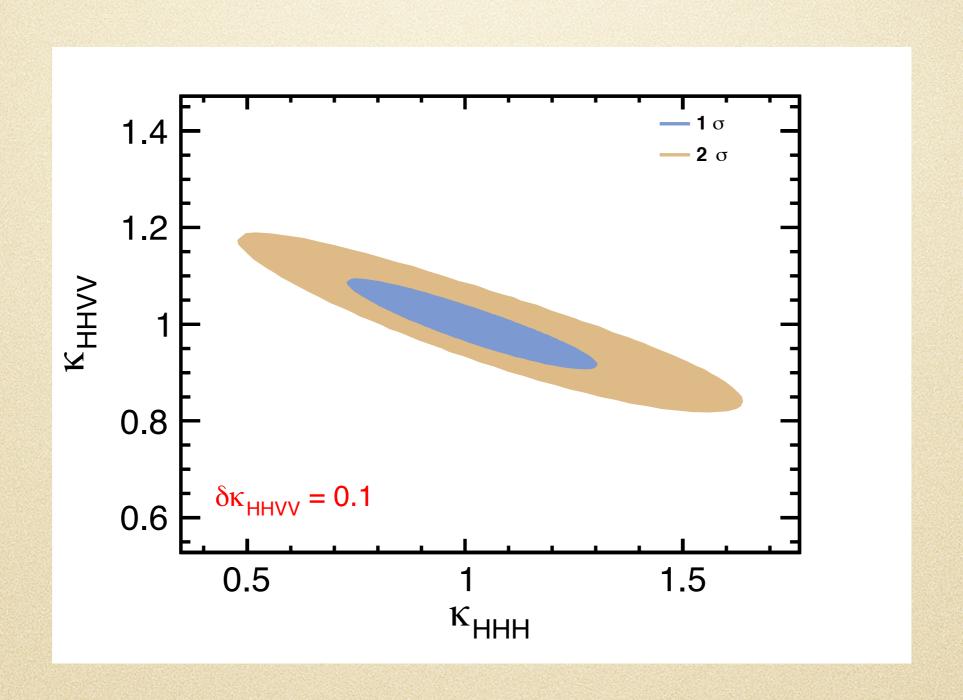
#### with constraints on $\kappa_q$ , $\kappa_b$ from other measurements

$$\chi^2 = \sum_{i}^{n} \left(\frac{\sigma_i - \sigma_i'}{\Delta \sigma_i}\right)^2 + \left(\frac{\kappa_q - \kappa_q'}{\delta \kappa_q}\right)^2 + \left(\frac{\kappa_b - \kappa_b'}{\delta \kappa_b}\right)^2$$

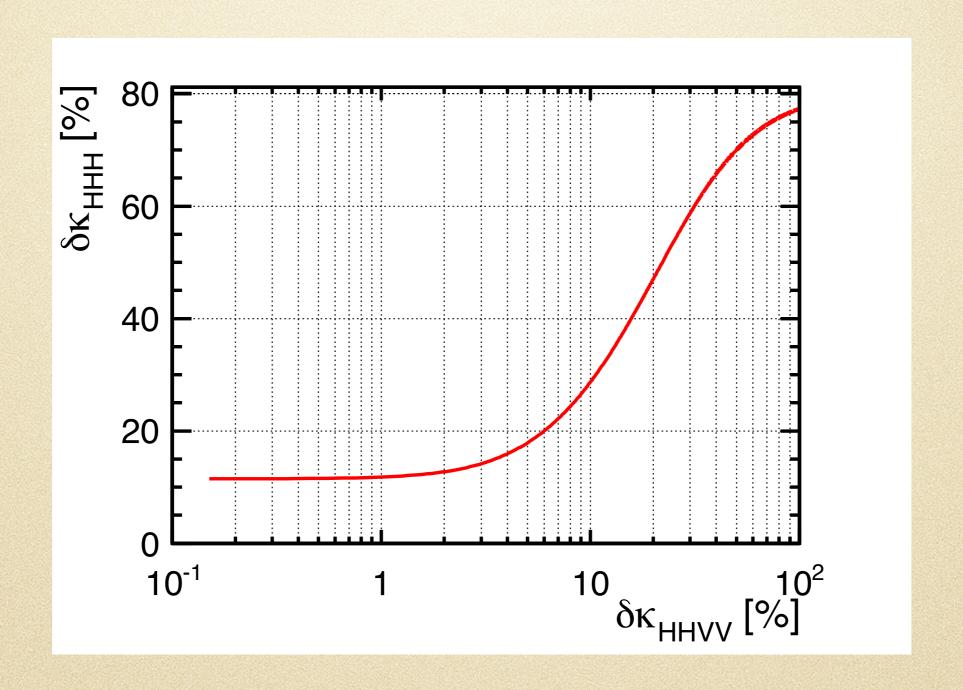
### results: w/o constraint on $\kappa_q$ (but $\kappa_b$ fixed) (3 observables)



### results: $\delta \kappa_q = 10\%$ (but $\kappa_b$ fixed) (3 observables)

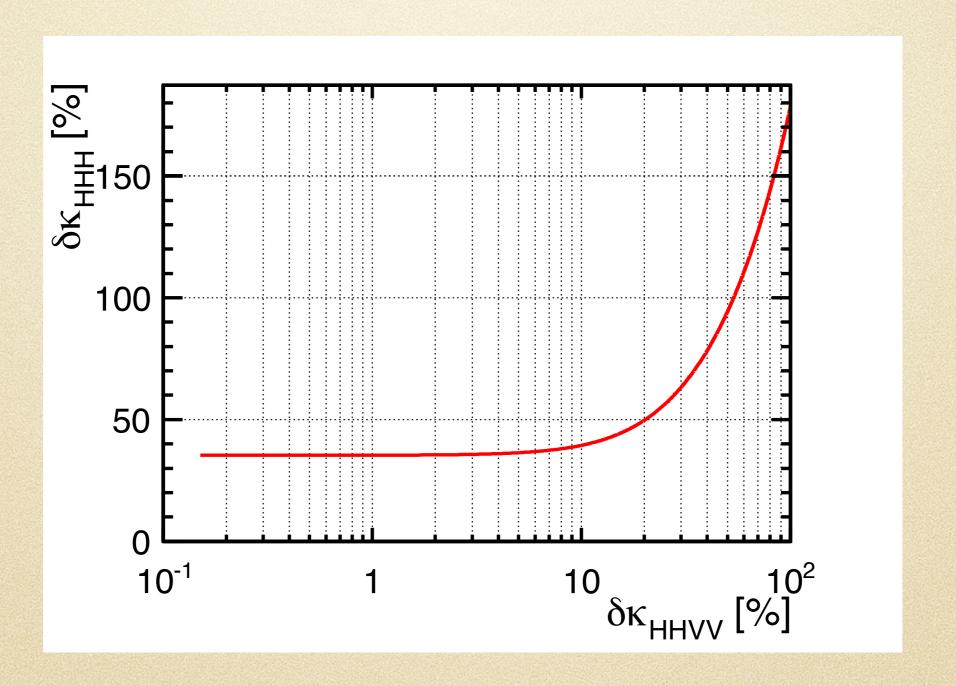


### results: $\delta \kappa_{\lambda}$ versus $\delta \kappa_{q}$ (but $\kappa_{b}$ fixed) (3 observables)

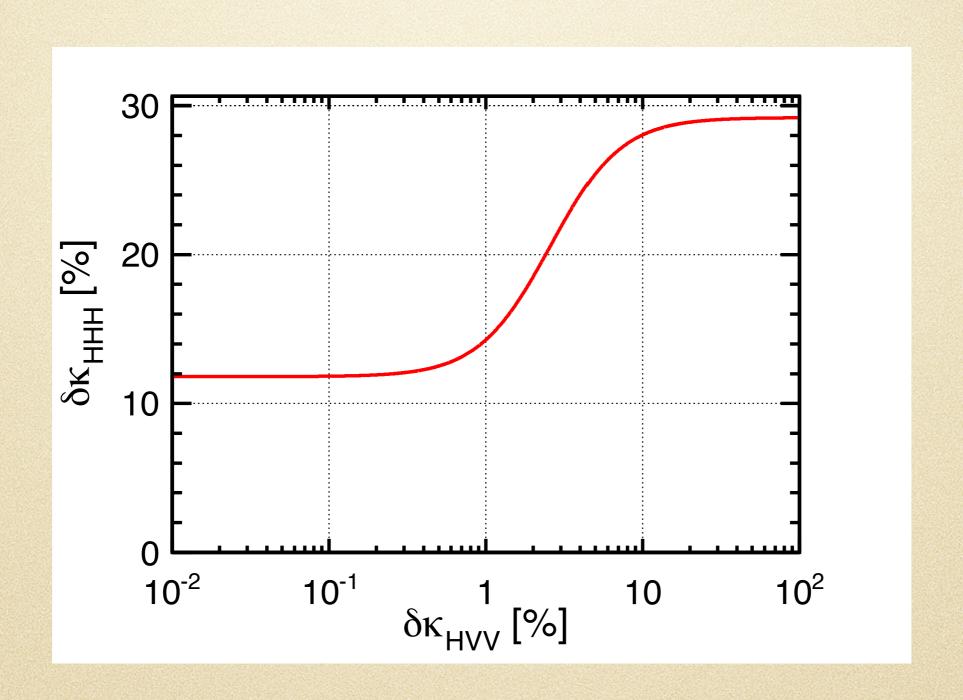


results:  $\delta \kappa_{\lambda}$  versus  $\delta \kappa_{q}$  (but  $\kappa_{b}$  fixed)

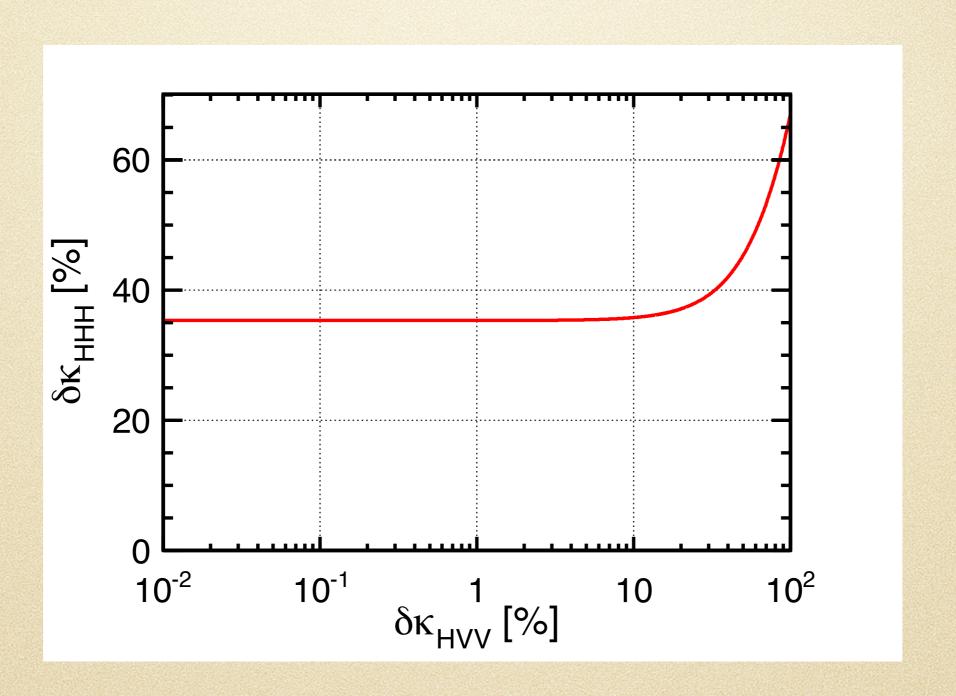
(1 observable: ZHH @ 500 GeV only)



### add in $\delta \kappa_b$ : $\delta \kappa_\lambda$ versus $\delta \kappa_b$ (w/ $\delta \kappa_q = 1\%$ ) (3 observables)



add in  $\delta \kappa_b$ :  $\delta \kappa_\lambda$  versus  $\delta \kappa_b$  (w/  $\delta \kappa_q$  = 1%) (1 observable: ZHH @ 500 GeV only)



#### my observation

### in order to get similar precision for HHH as obtained assuming fixed both HVV and HHVV

#### when HVV is fixed

- 500 GeV only: HHVV < 10% (~5%) would be needed
- 500 GeV + 1 TeV: HHVV < 1% (~0.5%) would be needed

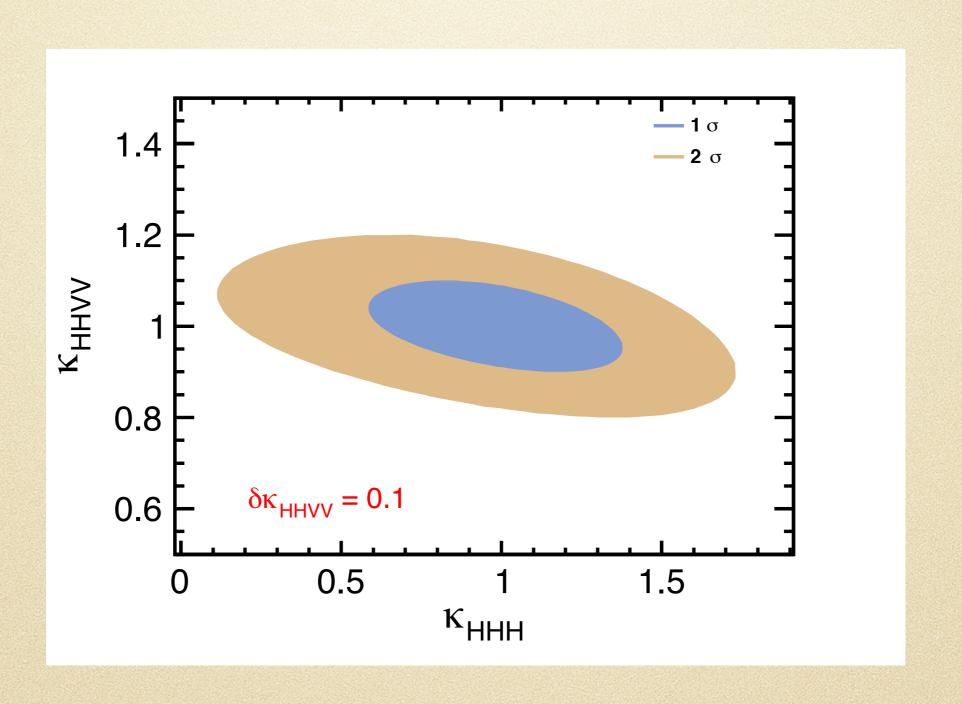
#### when HVV is fluctuated

- 500 GeV only: HVV ~ 10% would be needed
- 500 GeV + 1 TeV: HVV < 1% (~0.5%) would be needed

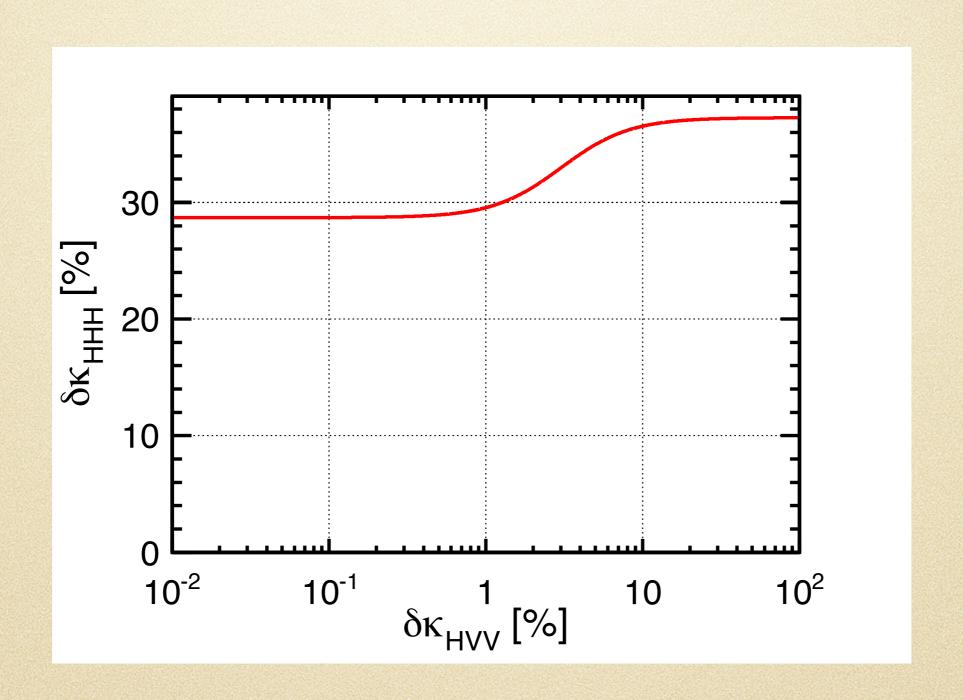
### backup

results:  $\delta \kappa_q = 10\%$  (but  $\kappa_b$  fixed)

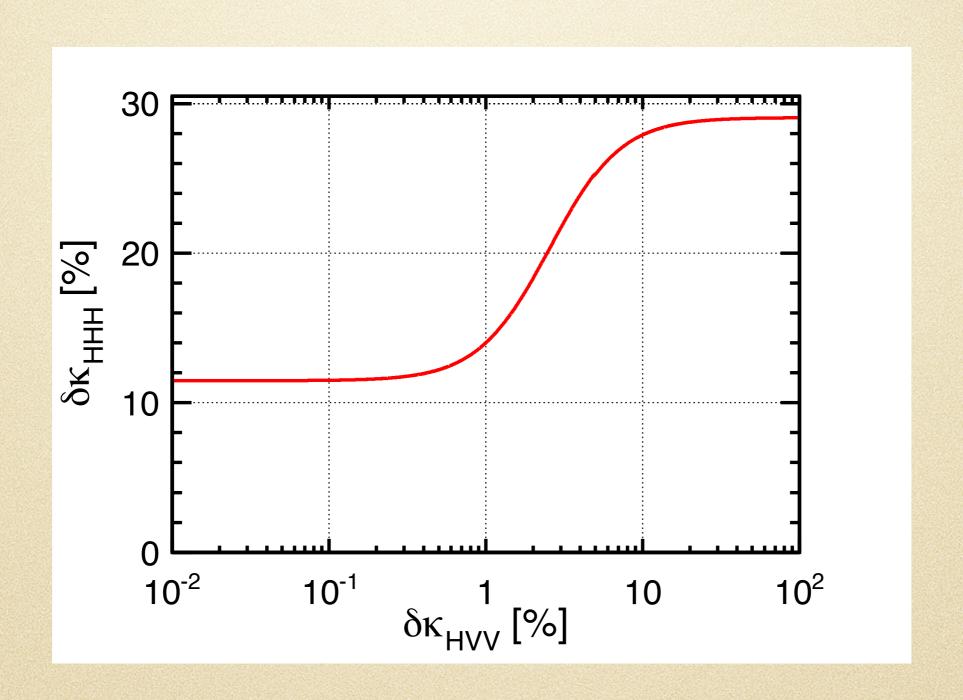
(1 observables: ZHH @ 500 GeV only)



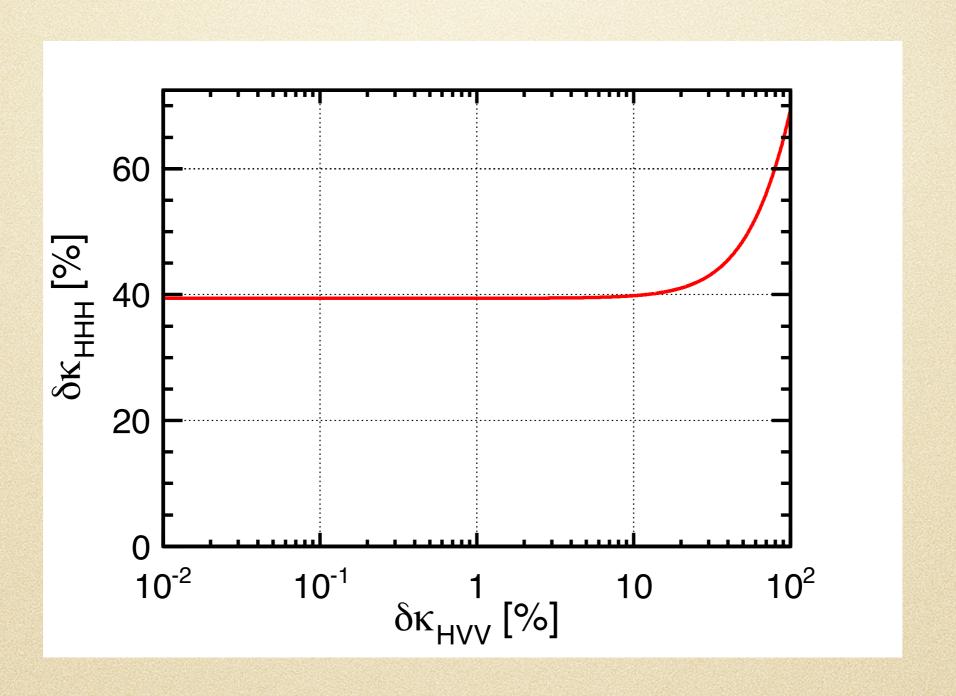
# add in $\delta \kappa_b$ : $\delta \kappa_\lambda$ versus $\delta \kappa_b$ (w/ $\delta \kappa_q$ = 10%) (3 observables)



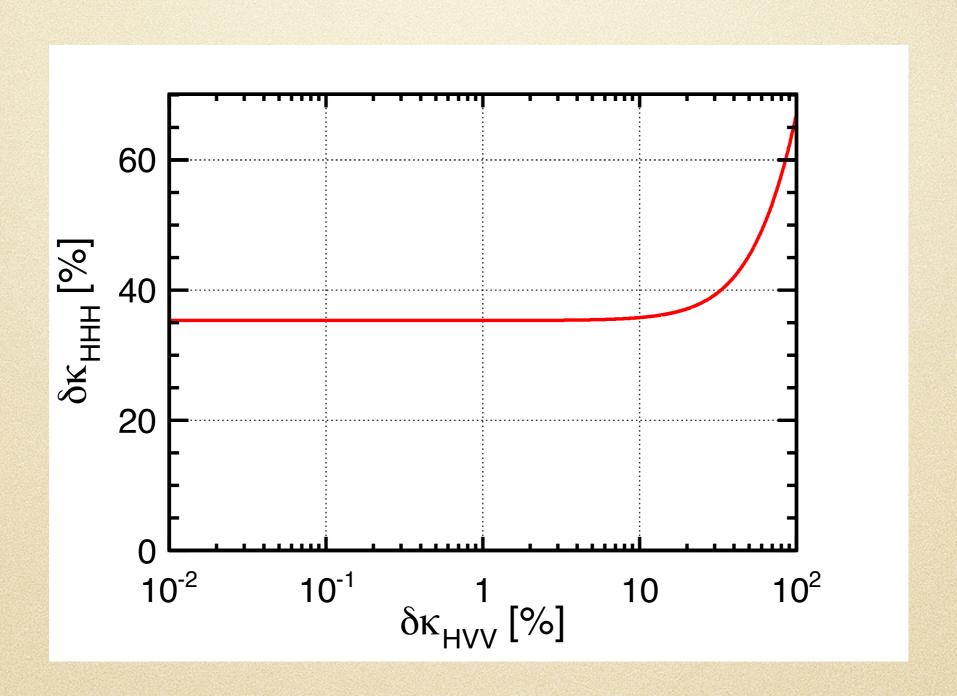
# add in $\delta \kappa_b$ : $\delta \kappa_\lambda$ versus $\delta \kappa_b$ (w/ $\delta \kappa_q$ = 0.1%) (3 observables)



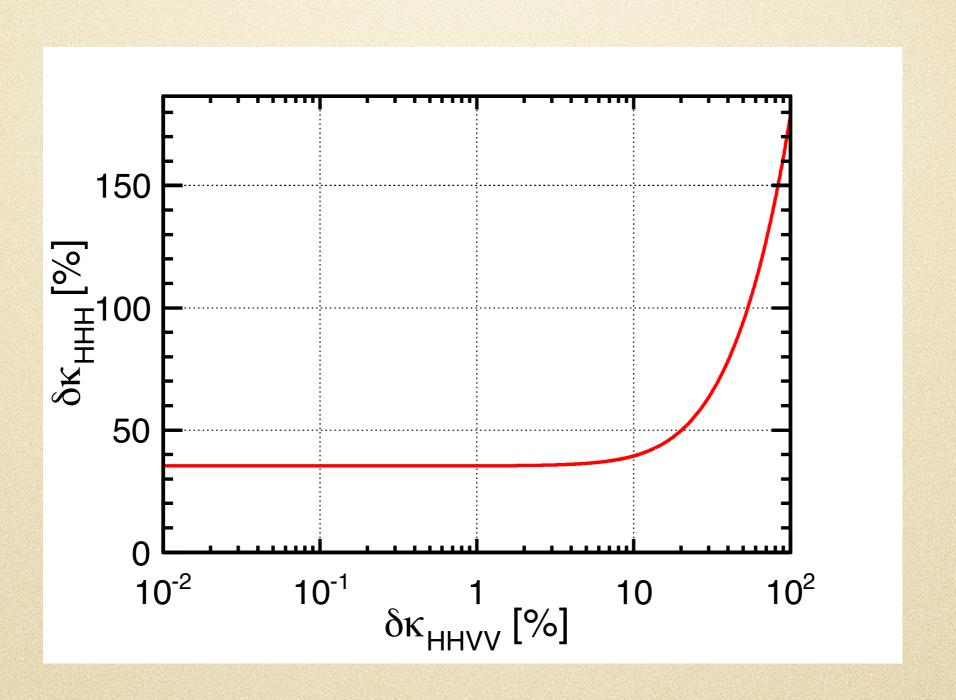
add in  $\delta \kappa_b$ :  $\delta \kappa_\lambda$  versus  $\delta \kappa_b$  (w/  $\delta \kappa_q$  = 10%) (1 observables: ZHH @ 500 GeV only)



add in  $\delta \kappa_b$ :  $\delta \kappa_\lambda$  versus  $\delta \kappa_b$  (w/  $\delta \kappa_q$  = 0.1%) (1 observables: ZHH @ 500 GeV only)



add in  $\delta \kappa_b$ :  $\delta \kappa_\lambda$  versus  $\delta \kappa_q$  (w/  $\delta \kappa_b$  = 1%) (1 observables: ZHH @ 500 GeV only)



add in  $\delta \kappa_b$ :  $\delta \kappa_\lambda$  versus  $\delta \kappa_q$  (w/  $\delta \kappa_b$  = 10%) (1 observables: ZHH @ 500 GeV only)

