

Measuring the CP state of tau pairs from Higgs decay at ILC in ILD

June 2016: first update

15 July 2016: Further update

updates after ECFA-LC workshop @Santander

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CP-violating coupling of Higgs to fermions possible at tree level

$$\mathcal{L} \sim g \bar{f} (\cos \psi_{CP} + i \gamma^5 \sin \psi_{CP}) f H$$

CP conserving coupling: $\psi_{CP} = 0$

maximally violating $\psi_{CP} = \pi/2$

consider projection of spin on some axis: \uparrow, \downarrow

spin state of pair of spin $1/2$ particles

produced by spin-0 parent: $\sim (|\uparrow\downarrow\rangle + e^{2i\psi} |\downarrow\uparrow\rangle)$

$\psi_{CP} = 0$: CP even eigenstate

$\psi_{CP} = \pi/2$: CP odd eigenstate

otherwise a mixture

decays of Higgs to tau pairs allows this to be probed

H decay to taus has significant BR

tau spin **s** can be partially reconstructed from decay product distribution

$$\Gamma(\tau \rightarrow X) \sim (1 + a \mathbf{h}(X) \cdot \mathbf{s})$$

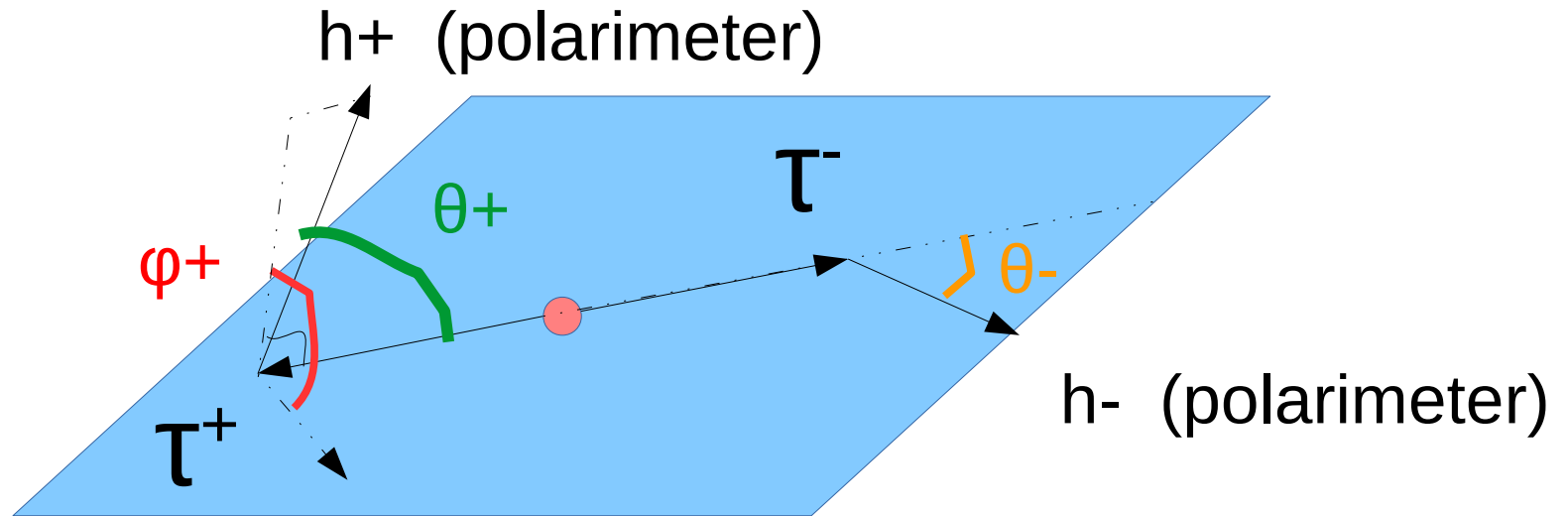
h(X) is the polarimeter vector
most likely tau spin direction for a
given configuration X of its decay products

easy to calculate for $\tau^\pm \rightarrow \pi^\pm \nu$ (~11%)
 $\pi^\pm \pi^0 \nu$ (~26%)

CP effects best seen in correlation of
spin components transverse to tau momentum:

$$\Gamma(\text{CP even/odd} \rightarrow f^+ f^-) \sim 1 - s_z^+ s_z^- \text{ +/- } s_\perp^+ s_\perp^-$$

July update



$$dN/(d \cos \theta^+ d \cos \theta^- d \phi^+ d \phi^-) \propto 1 + \cos \theta^+ \cos \theta^- - \sin \theta^+ \sin \theta^- \cos(\Delta \phi - 2\psi_{\text{CP}}).$$

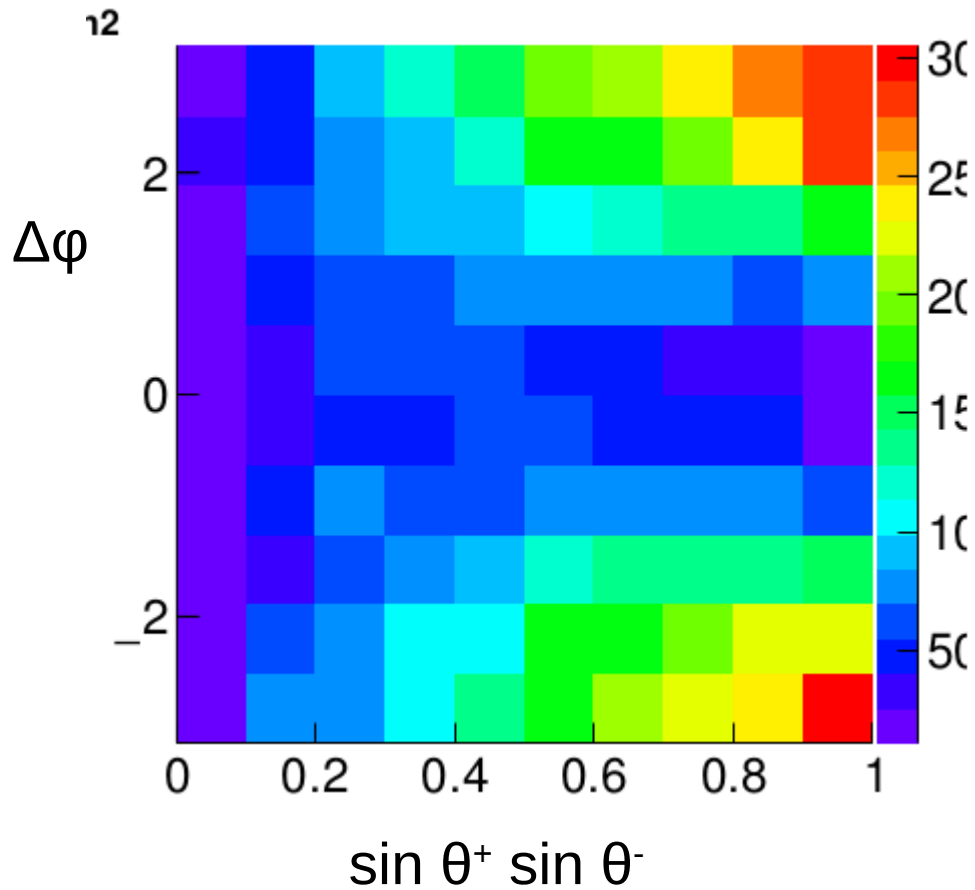
θ, φ are direction of polarimeter wrt tau- momentum in tau rest frames
 $\Delta \varphi = \varphi^+ - \varphi^-$; ψ_{CP} is the CP mixing angle we want to measure

$\Delta \varphi$ distribution sensitive to ψ_{CP}

events with large $(\sin \theta^+ \sin \theta^-)$ are more strongly affected by ψ_{CP}
until now I have integrated over $\sin \theta^+ \sin \theta^-$
today I will show effect of not doing this integration

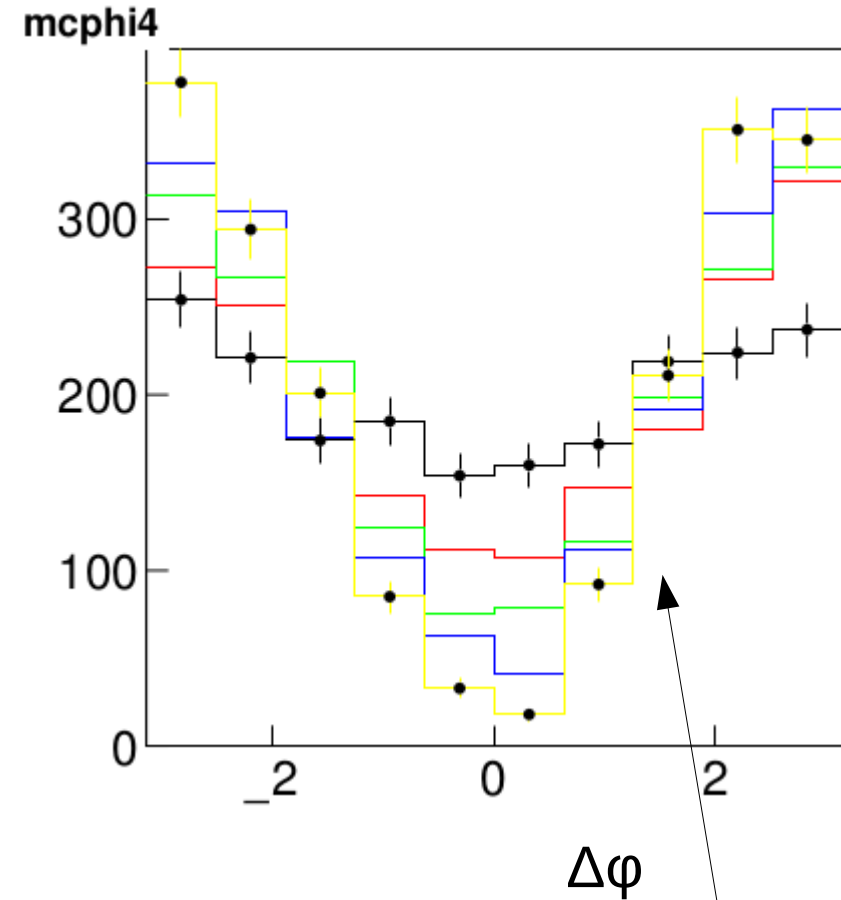
July update

colours = different ranges of $\sin \theta^+ \sin \theta^-$



one polarimeter
along tau direction

both polarimeters
perpendicular to
tau direction



we want to measure phase
of this modulation

signal only, MC truth

July update

split simulated & reconstructed MC data
into 5 bins of $\sin \theta^+ \sin \theta^-$

in each bin:

estimate size of modulation and
number of signal & background events

use this to make templates for toy MC experiments.

for each toy experiment,

perform **simultaneous** likelihood fit to data in
5 bins and 3 channels (Z \rightarrow ee, mm, qq)
to extract single value of ψ_{CP}

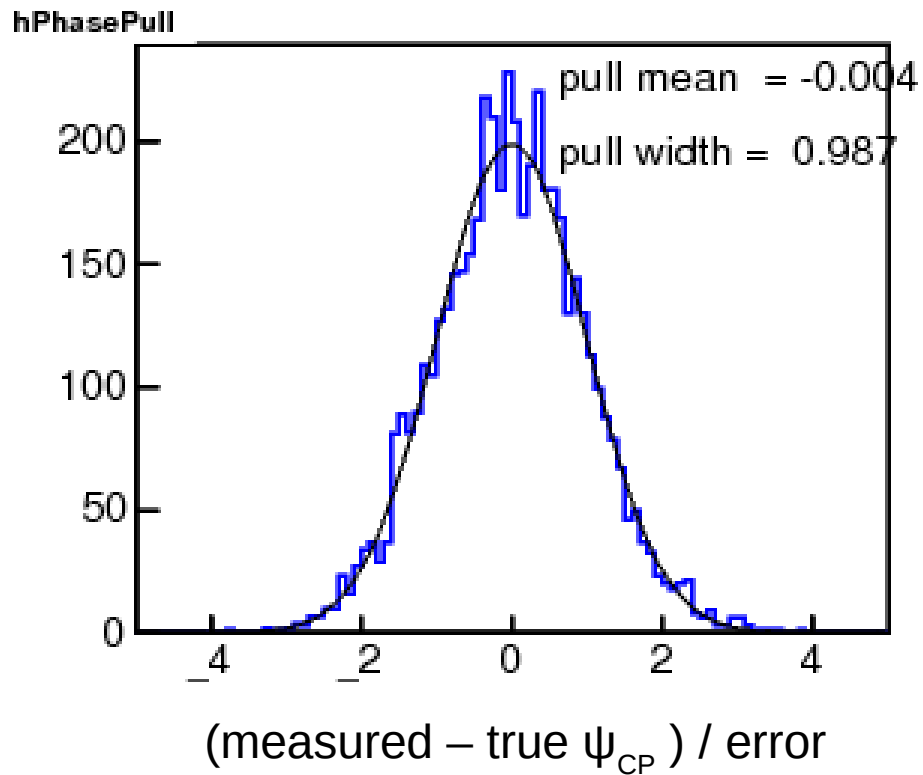
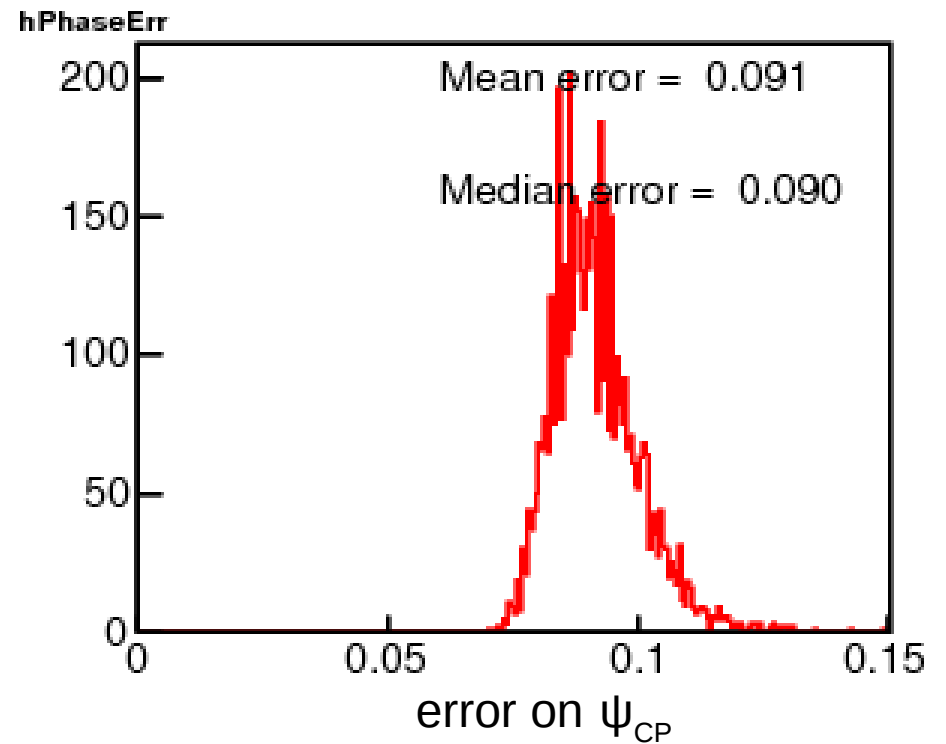
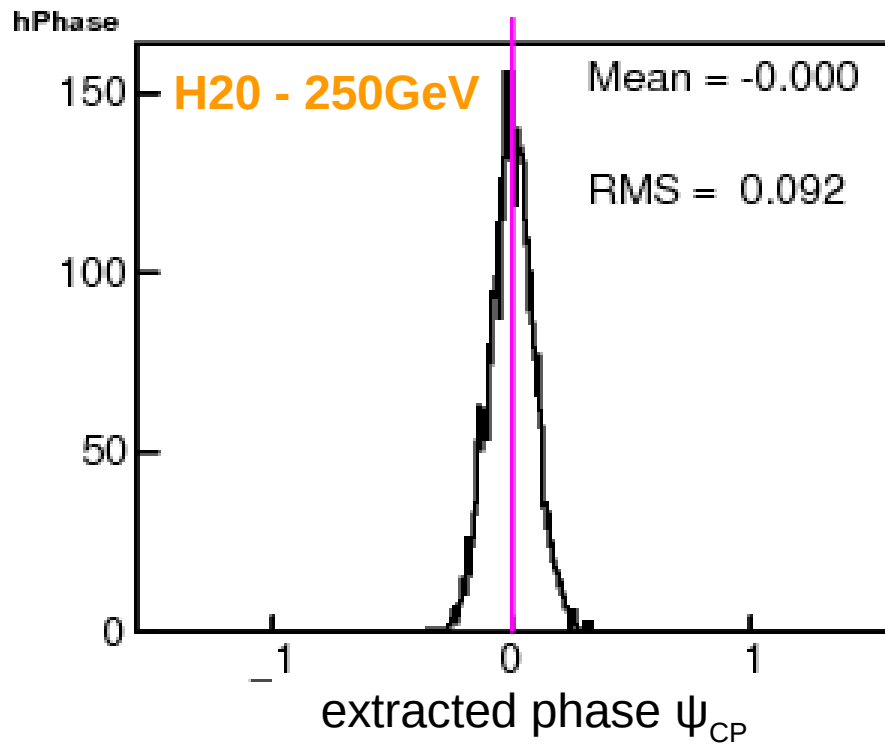
(simultaneous fit is better behaved:

otherwise rather small number of events per experiment,
and somewhat non-gaussian errors)

also:

a few small tweaks to selection cuts

now include also rather small contribution to H20 luminosity from
(-0.8, -0.3) and (+0.8, +0.3) polarisations @ 250 GeV



July update

integrating over $\sin \theta^+ \sin \theta^-$

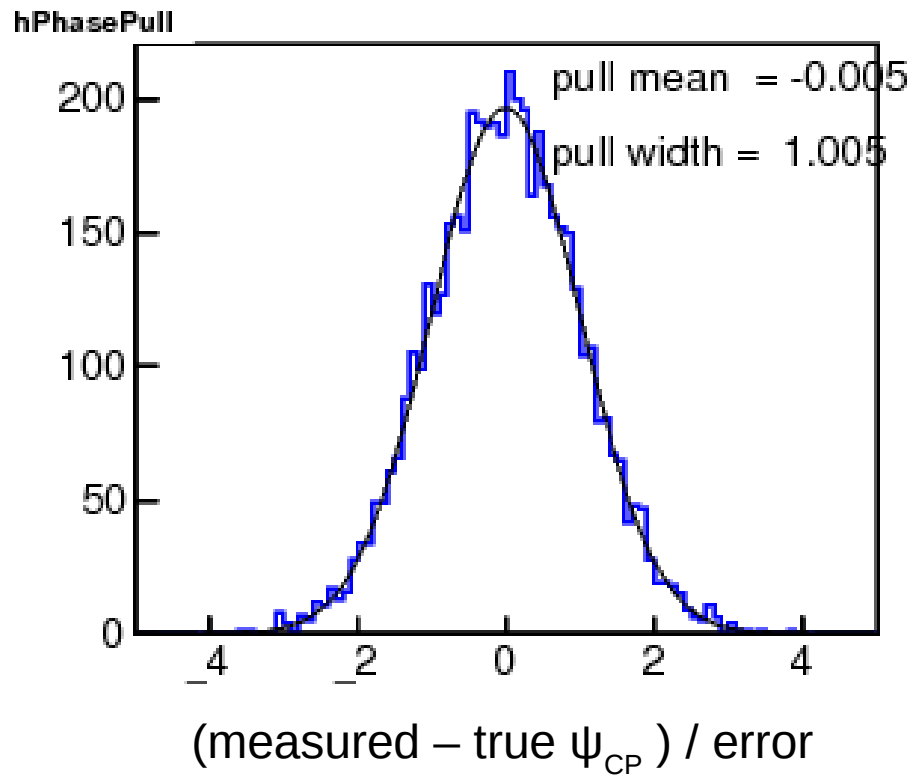
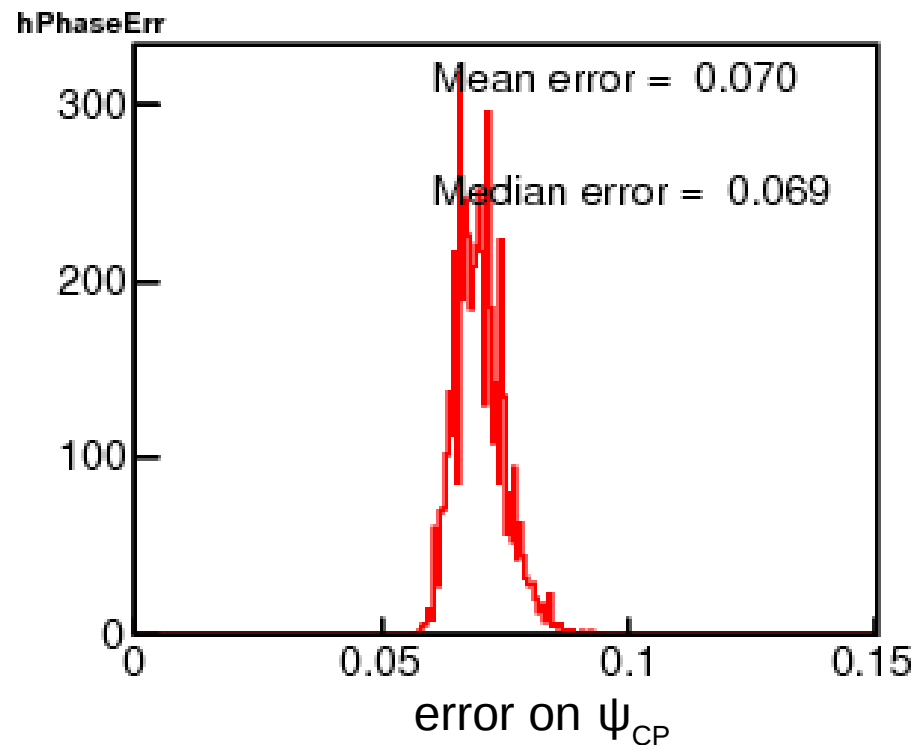
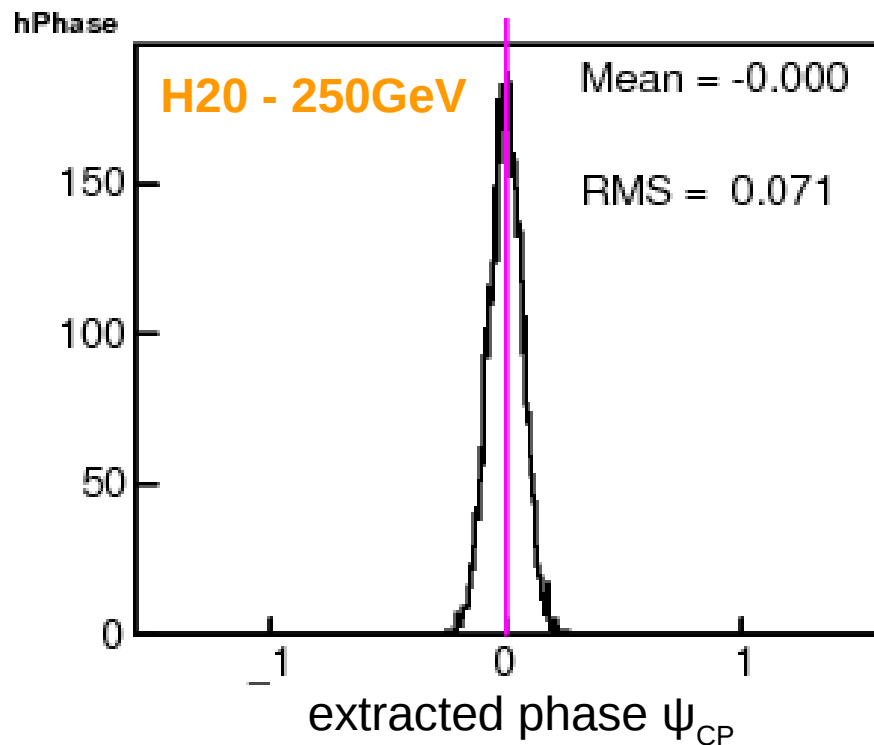
all channels

results of 5000 toy mc experiments

no bias in phase extraction

pull distribution looks good

expected uncertainty: 90 mrad \sim 5.2 deg



July update

5 bins in $\sin \theta^+ \sin \theta^-$

all channels

results of 5000 toy mc experiments

no bias in phase extraction

pull distribution looks good

expected uncertainty: 70 mrad \sim 4.0 deg

Summary (July update)

split data according to how perpendicular
the polarimeters are to the tau momentum

H20 precision on ψ_{CP} improves: 90 \rightarrow 70 mrad

rather than binning data,
a true 2d approach should improve result further
 \rightarrow now studying

paper writing is progressing reasonably well

old slides

Full simulation & reconstruction

Whizard 2.2.8, CIRCE2 beam-strahlung, ISR

$e^+ e^- \rightarrow f^+ f^- \tau^+ \tau^-$ ($\tau^+ \tau^-$ from 125 GeV Higgs)

$e^+ e^- \rightarrow f^+ f^- \tau^+ \tau^-$ ($\tau^+ \tau^-$ not from Higgs)

$f = e, \mu, (uds)$ (some generator level cuts, particularly for $e^+ e^- \tau^+ \tau^-$)

Pythia v8.212 for hadronisation & FSR

~~.. Tauola c++ v1.1.4~~ **UPDATE: tau decays now in Pythia**

1. signal decays: $\tau^\pm \rightarrow \pi^\pm \nu$ and/or $\tau^\pm \rightarrow \pi^\pm \pi^0 \nu$ “rho / ρ ”

2. all τ^\pm decays

include spin correlations (H_{SM} , $H_{CP}(\psi_{CP}=\pi/4)$, non-H)

Mokka simulation: ILD model ILD_o1_v05

standard Marlin/ILDConfig reconstruction [ilcsoft v01-17-09]

background overlay

standard Pandora steering (with recent photon reco)

UPDATE

found various FSR-related problems:

I had added FSR to electron and quark channels,
but not to muon channel

I had not applied FSR correctly:
when tau radiates FSR,
tauola did not realise it comes from Higgs →
does not apply spin correlations in tau decay

now perform tau decays within pythia v8.212 instead of Tauola,
“at same time” as doing FSR.
(tau spin correlations can be included from Pythia v8.150)
seems to give consistent results.

UPDATE

now include $e^+ e^- \rightarrow c \bar{c} \tau^+ \tau^-$, $b \bar{b} \tau^+ \tau^-$ processes

[previously only light uds quarks considered]

General strategy

consider 250 GeV running in H20 scenario

$$\text{Pol}(e^-,e^+) = (-0.8, +0.3), 1350 \text{ fb}^{-1}$$

$$\text{Pol}(e^-,e^+) = (+0.8, -0.3), 450 \text{ fb}^{-1}$$

select $e^+e^- \rightarrow (H \rightarrow \tau \tau) (Z \rightarrow ee, \mu\mu, qq)$ events

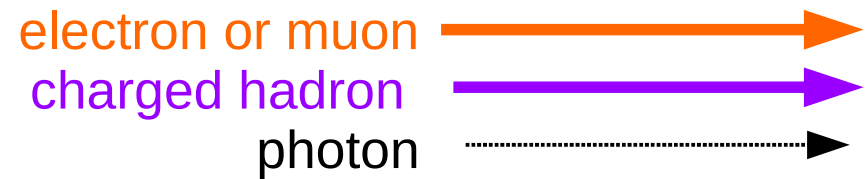
fully reconstruct tau momenta

reconstruct tau polarimeter vectors

look at angle between transverse components of polarimeters

use toy MC experiments to extract sensitivity to CP mixing angle

selection: leptonic Z decay



one leptonic Z decay candidate

→ **particle ID**

≥ 2 additional charged hadrons

→ tau seeds

associate photons → π^0

with tau seeds

veto events with significant additional activity

select $\tau^\pm \rightarrow \pi^\pm \nu$ and $\tau^\pm \rightarrow \pi^\pm \pi^0 \nu$ decays

→ **photon reconstruction**

fully reconstruct tau momenta

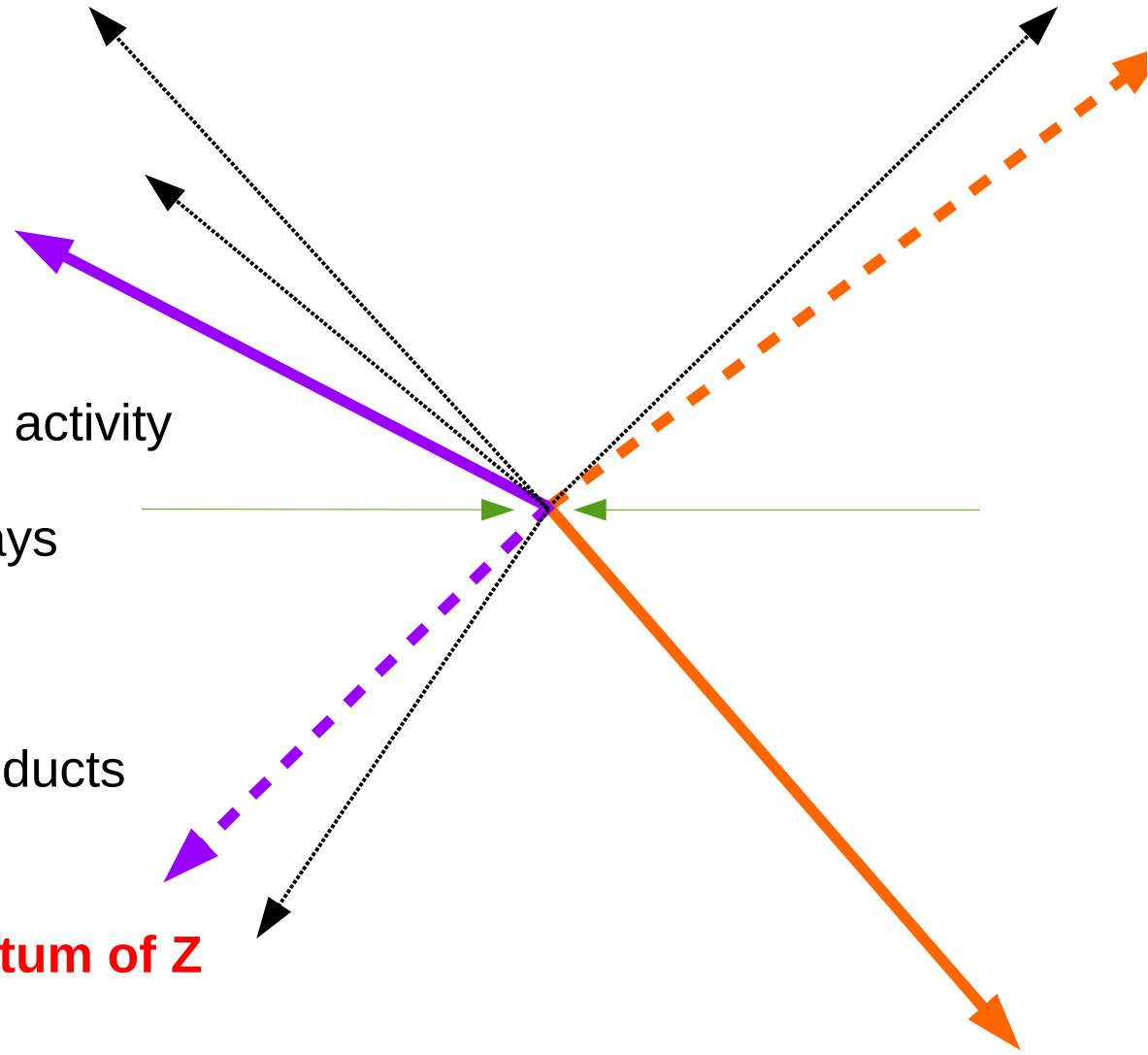
use impact parameters of tau products

balance event p_T

impose tau mass

→ **impact parameters ; momentum of Z**

require tau-tau mass $\sim m_H$



selection: hadronic Z decay

two tau-like jets (TauFinder)

→ **tau identification**

select $\tau^\pm \rightarrow \pi^\pm \nu$ and $\tau^\pm \rightarrow \pi^\pm \pi^0 \nu$ decays

→ **photon reconstruction**

rest of event → “Z”

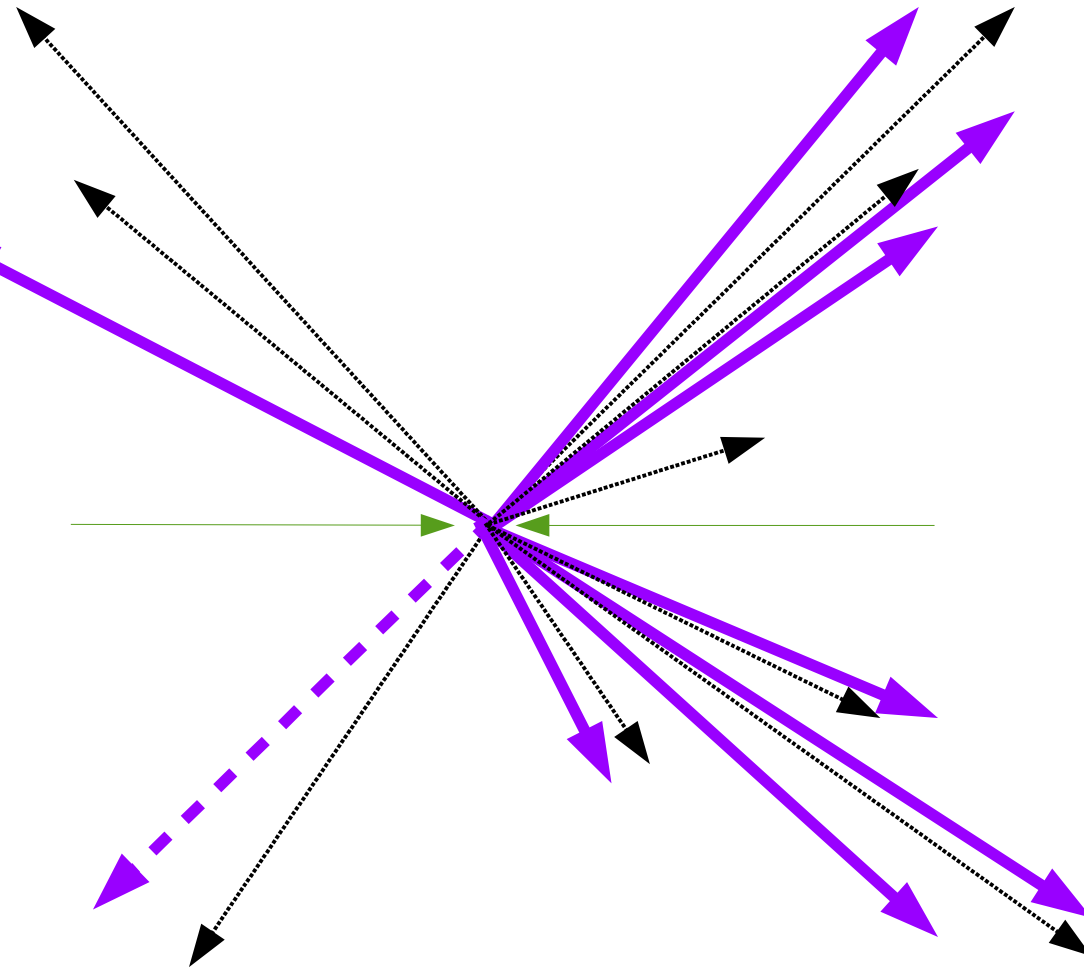
require mass consistent with m_Z

fully reconstruct tau momenta

→ **impact parameters ;**

→ **momentum of Z → JER**

require tau-tau mass $\sim m_H$



UPDATE

various tweaks to reconstruction

e.g.

lepton ID

identification of FSR & bremsstrahlung photons

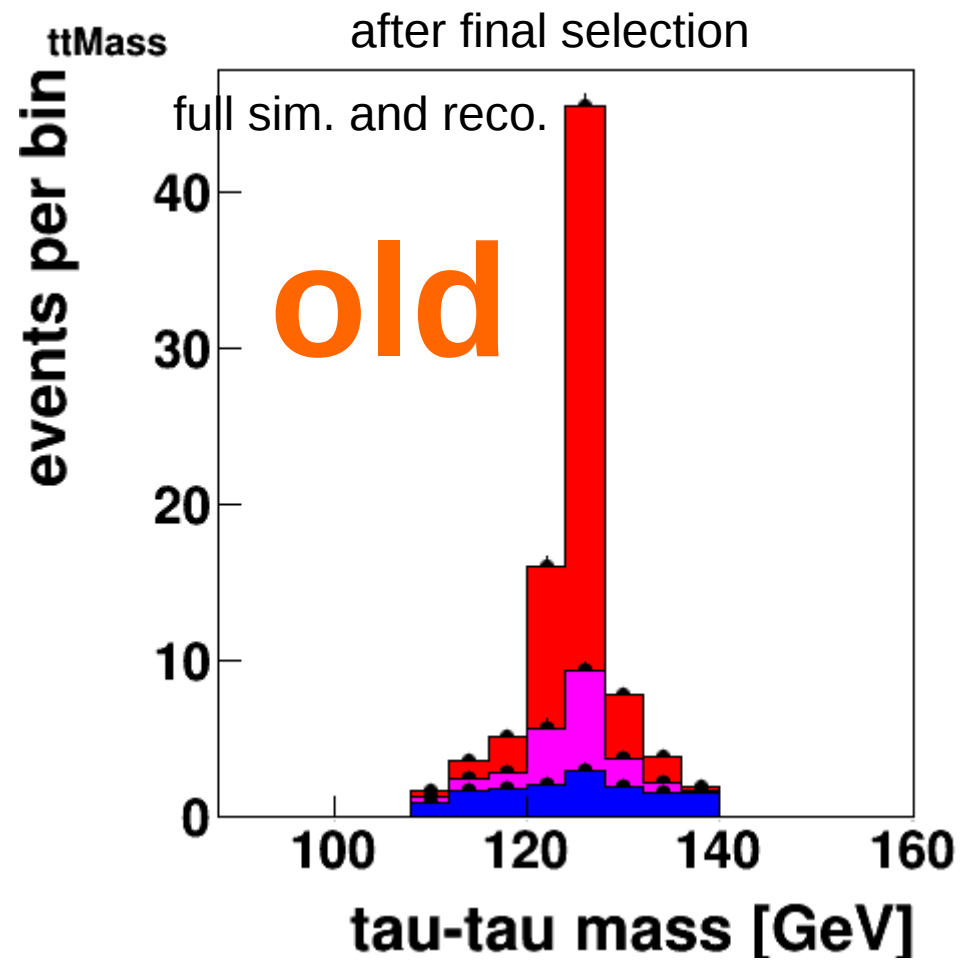
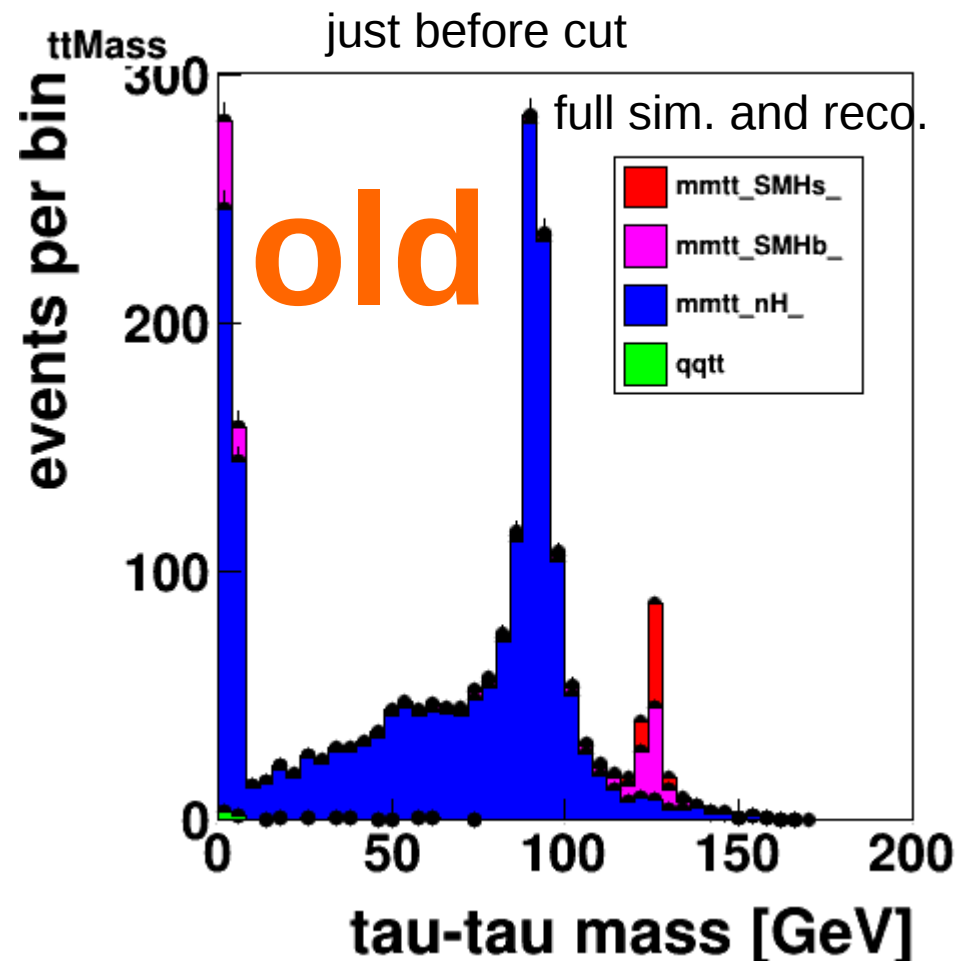
various tweaks to selection cuts

most to improve signal selection efficiency

some to improve background rejection

Invariant mass of reconstructed tau-tau system

muon channel, 1350 fb⁻¹ @ P(e⁻,e⁺) = (-0.8, +0.3)

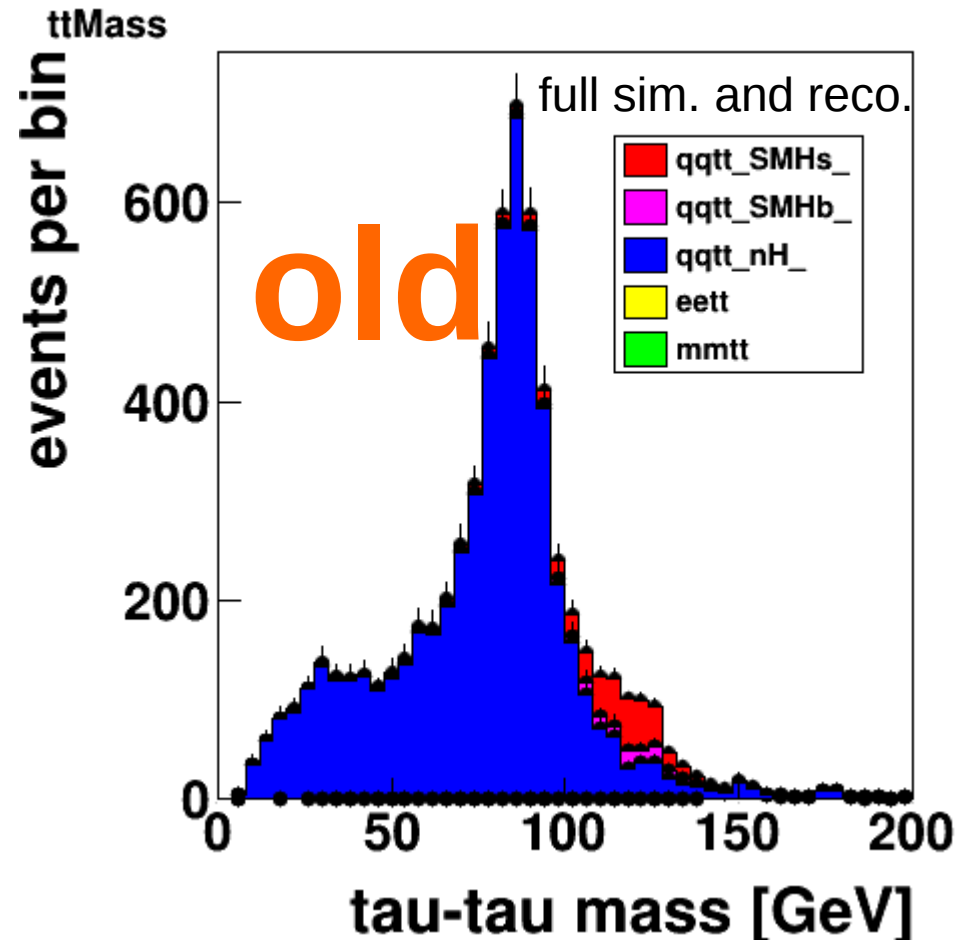


$\mu\mu$ tau tau (SM Higgs, tau \rightarrow pi or rho) signal
 $\mu\mu$ tau tau (SM Higgs, other tau decay channels)
 $\mu\mu$ tau tau (non-Higgs) background

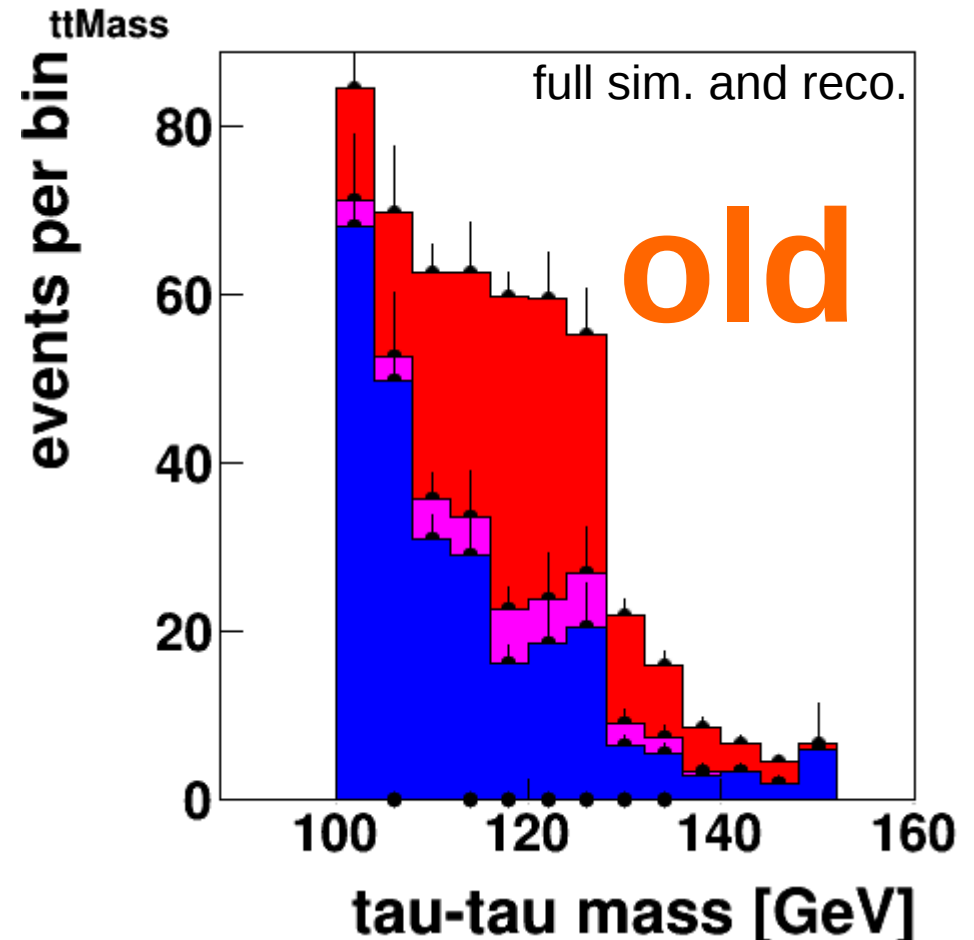
pretty good tau
momentum
reconstruction

Invariant mass of reconstructed tau-tau system

hadronic channel, 1350 fb⁻¹ @ $P(e^-, e^+) = (-0.8, +0.3)$

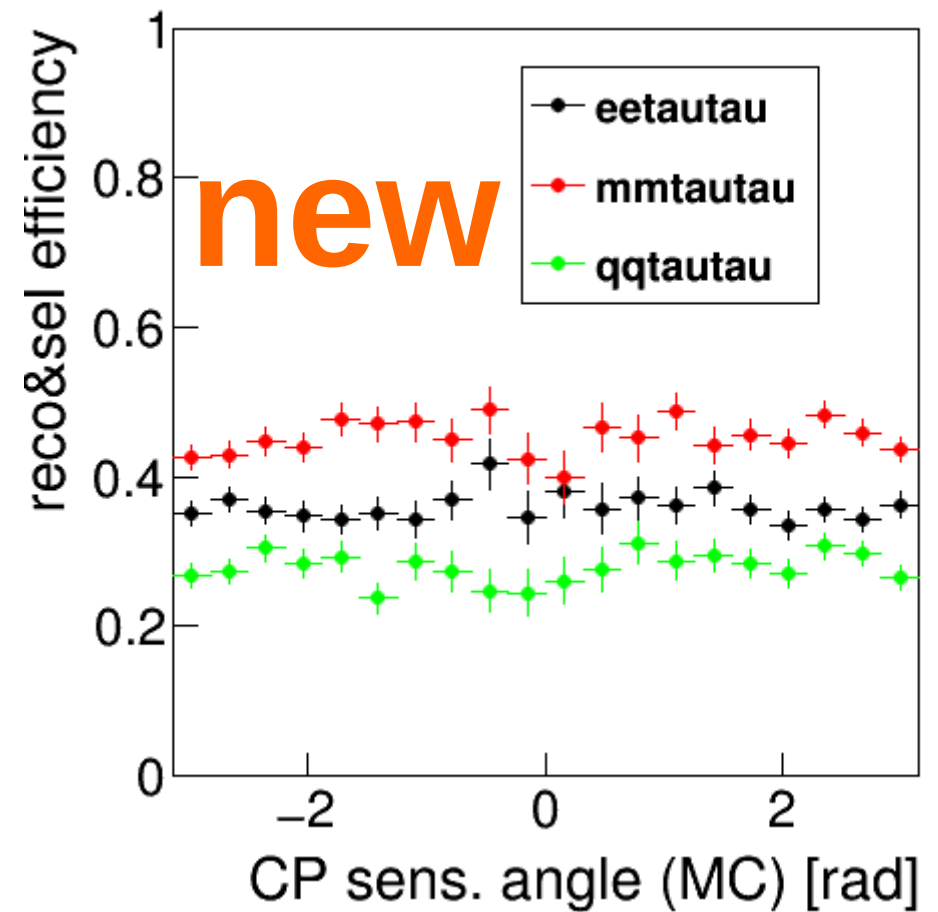
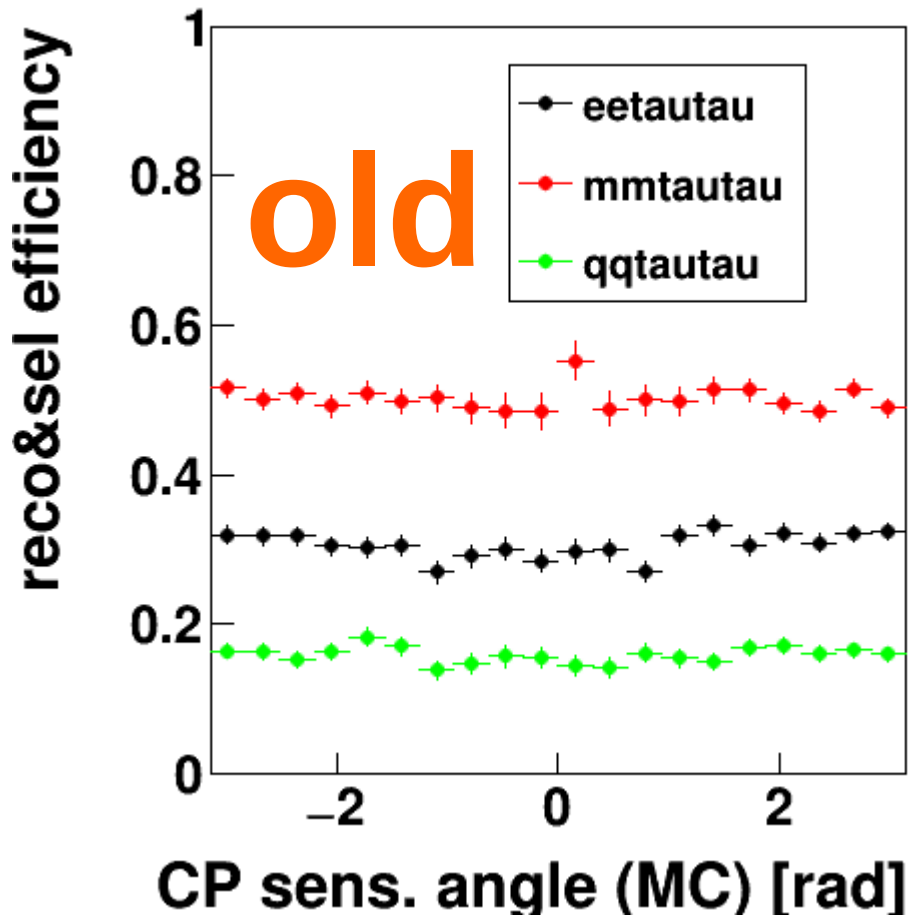


$\mu\mu$ tau tau (SM Higgs, tau \rightarrow pi or rho) signal
 $\mu\mu$ tau tau (SM Higgs, other tau decay channels)
 $\mu\mu$ tau tau (non-Higgs) background



tau momentum
reconstruction much worse
 \rightarrow jet energy resolution

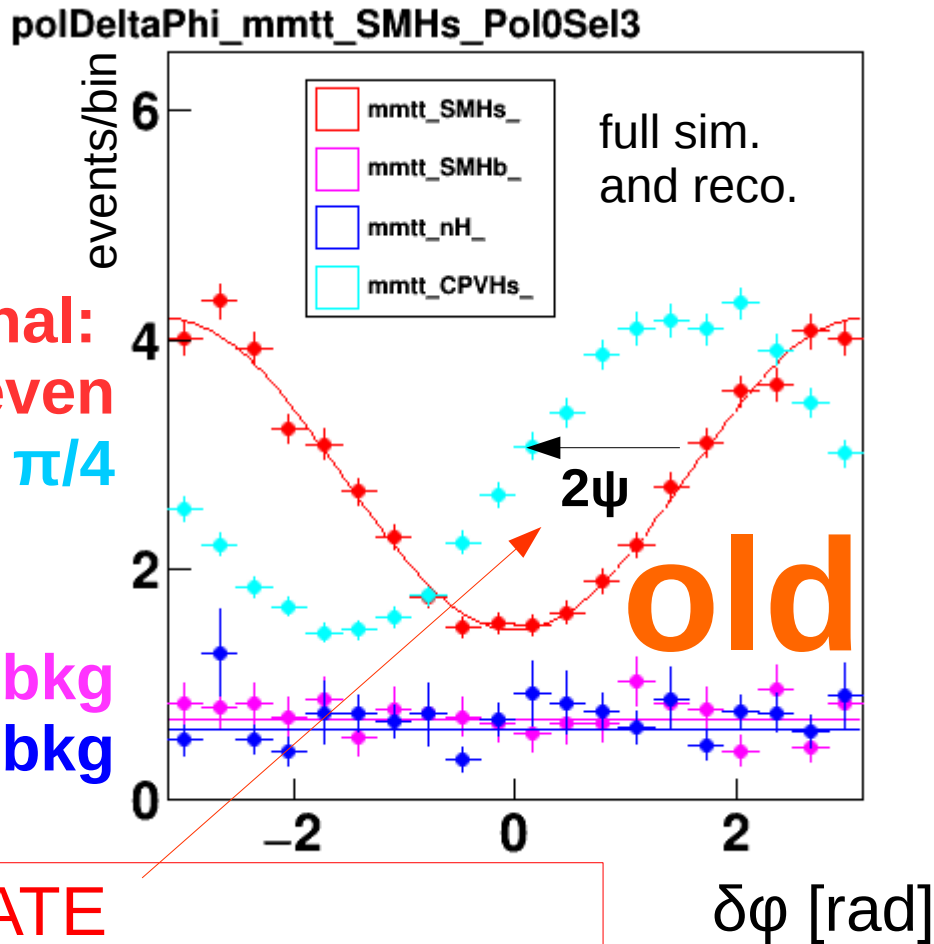
Reconstruction and selection efficiency



muon channel efficiency reduced somewhat
(due to now-included FSR?)
others slightly increased
(improved selection cuts?)
remain ~flat wrt CP angle

transverse spin correlations: after selection and reconstruction

muon channel
1350 fb-1 @ P(e-,e+) = (-0.8, +0.3)



signal:
CP even
 $\psi = \pi/4$

Higgs bkg
non-H bkg

UPDATE
definition of angular shift
shift in distr $\sim 2\psi_{CP}$

$$\mathcal{L} \sim g \bar{f} (\cos \psi_{CP} + i \gamma^5 \sin \psi_{CP}) f H$$

$$\sim 1 + a (\delta\phi + \psi_{CP})$$

clear phase shift for $\psi_{CP} = \pi/4$

statistics and the contrast “a”
determines how well we can
measure ψ_{CP}

$$a_{MC} = \pi^2/16 \sim 0.6$$

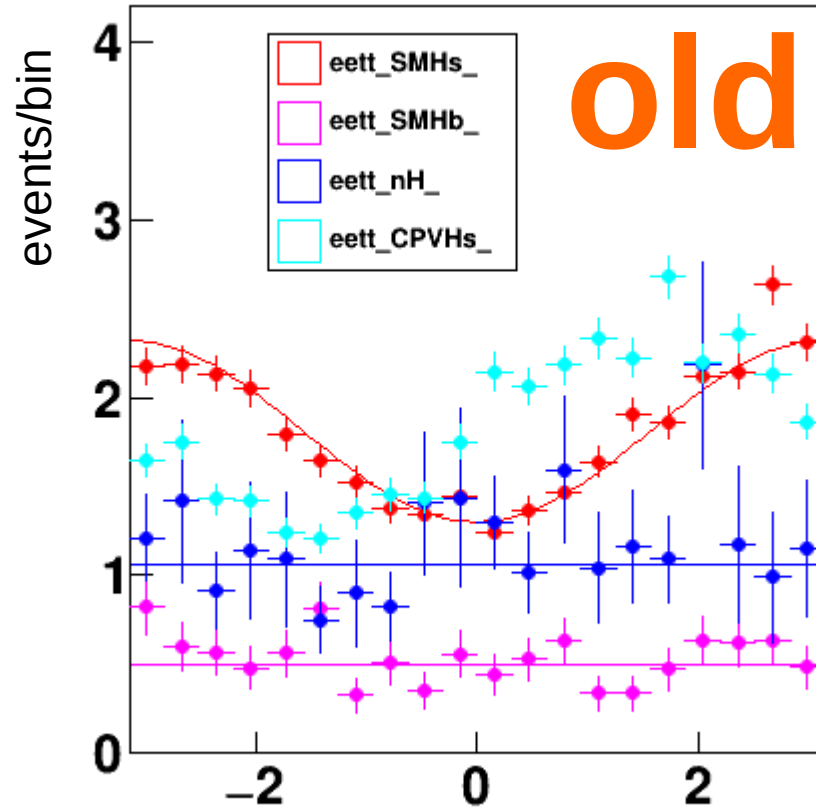
$$a_{reco} \sim 0.5$$

backgrounds small and flat

transverse spin correlations: electron channel

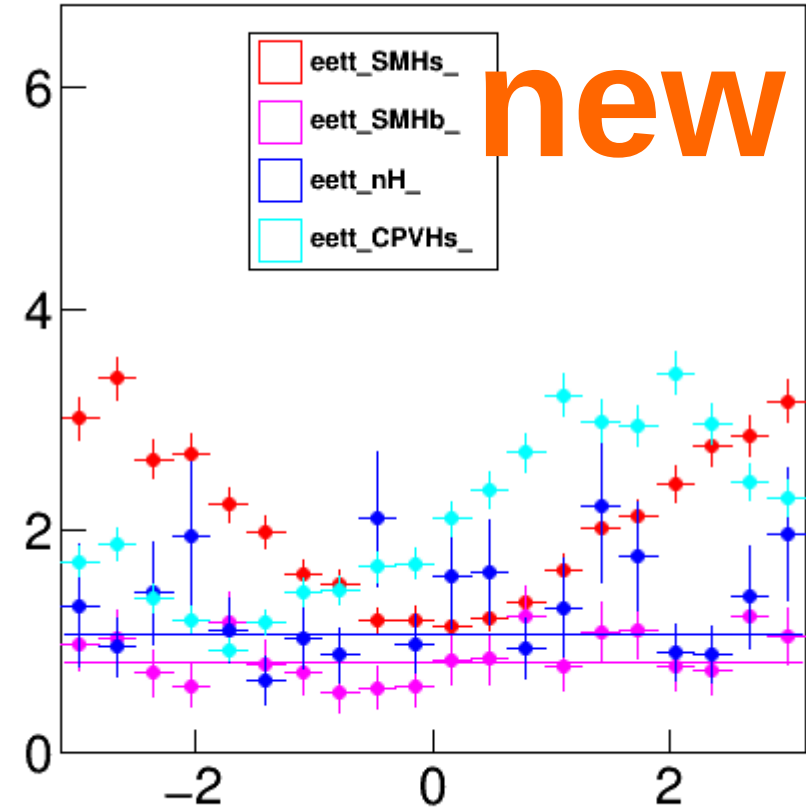
1350 fb⁻¹ @ $P(e^-, e^+) = (-0.8, +0.3)$

polDeltaPhi_eett_SMHs_Pol0Sel3



signal:
CP even $\psi = 0$
 $\psi = \pi/4$
Higgs bkg
non-H bkg

polDeltaPhi_eett_SMHs_Pol0Sel3



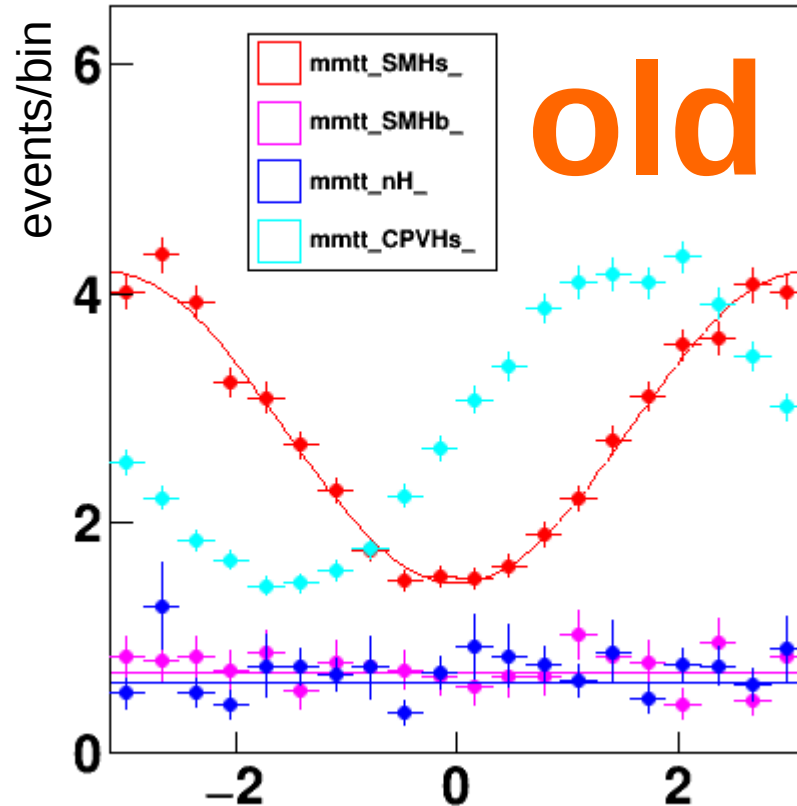
slightly more signal (better selection)

more modulated signal (FSR problem fixed)

transverse spin correlations: muon channel

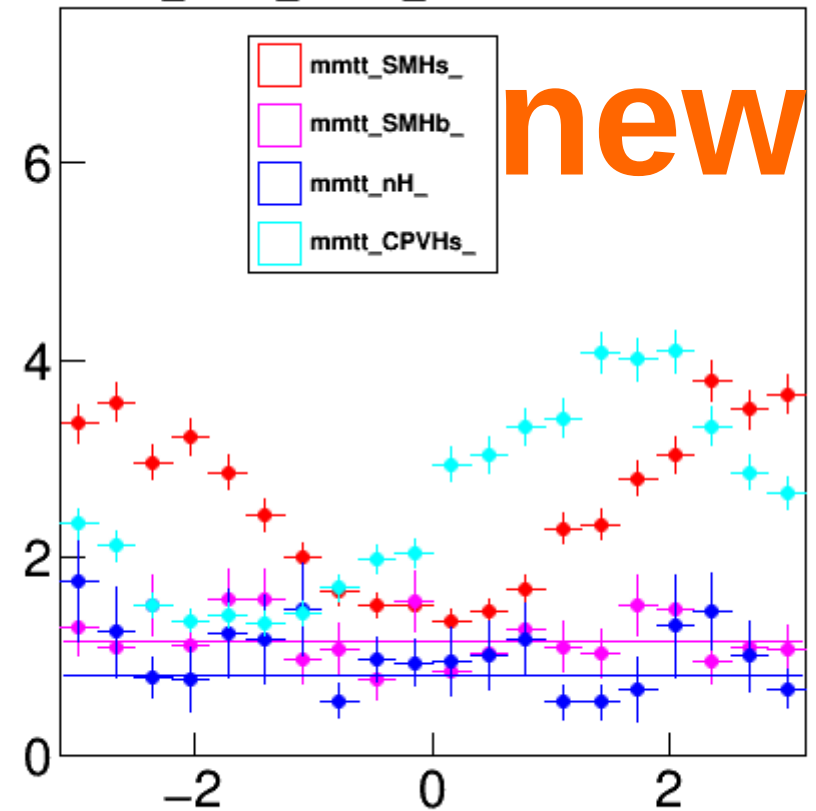
1350 fb⁻¹ @ $P(e^-, e^+) = (-0.8, +0.3)$

poiDeltaPhi_mmtt_SMHs_Pol0Sel3



signal:
CP even $\psi = 0$
 $\psi = \pi/4$
Higgs bkg
non-H bkg

poiDeltaPhi_mmtt_SMHs_Pol0Sel3

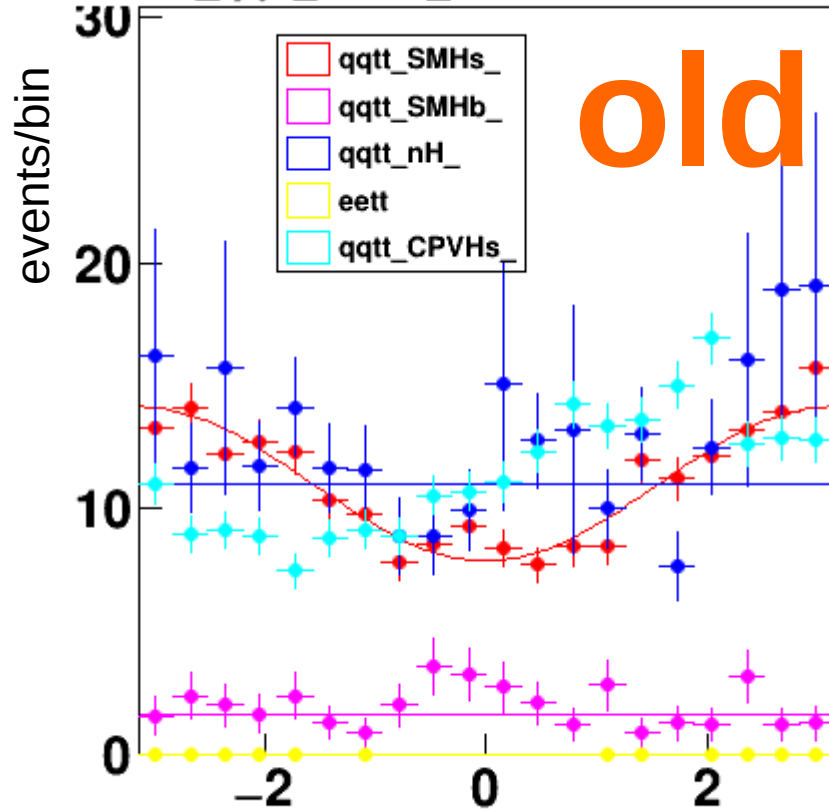


slightly less signal, and less modulated
(FSR now included)

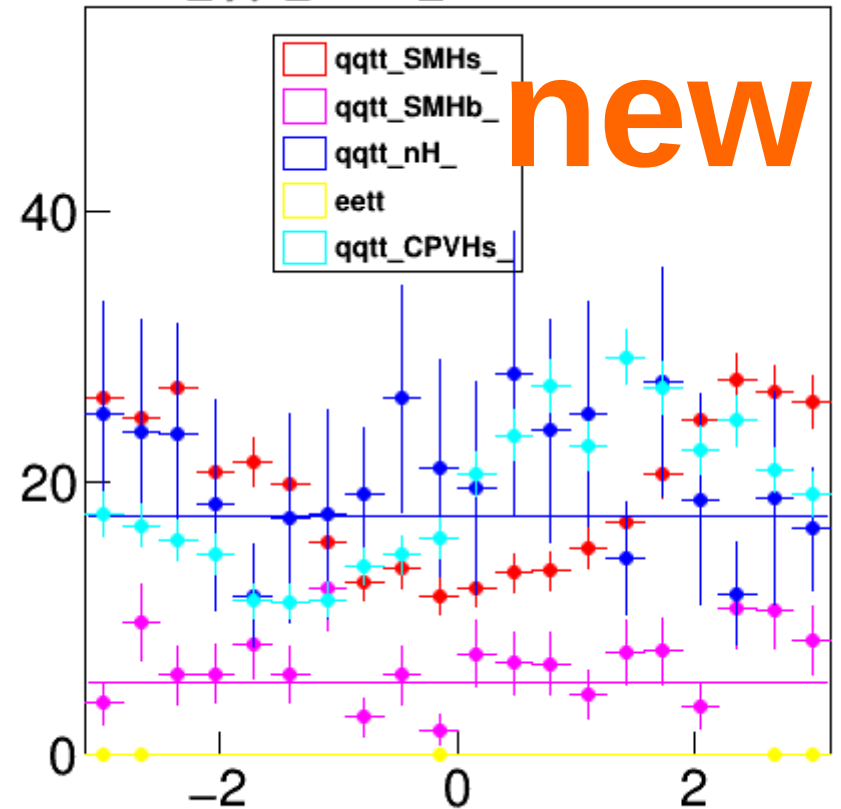
transverse spin correlations: quark channel

1350 fb⁻¹ @ $P(e^-, e^+) = (-0.8, +0.3)$

polDeltaPhi_qqtt_SMHs_Pol0Sel3



polDeltaPhi_qqtt_SMHs_Pol0Sel3



signal:
CP even $\psi = 0$
 $\psi = \pi/4$
Higgs bkg
non-H bkg

more events (added cctautau, bbtautau)

slightly more modulated (FSR fixed)

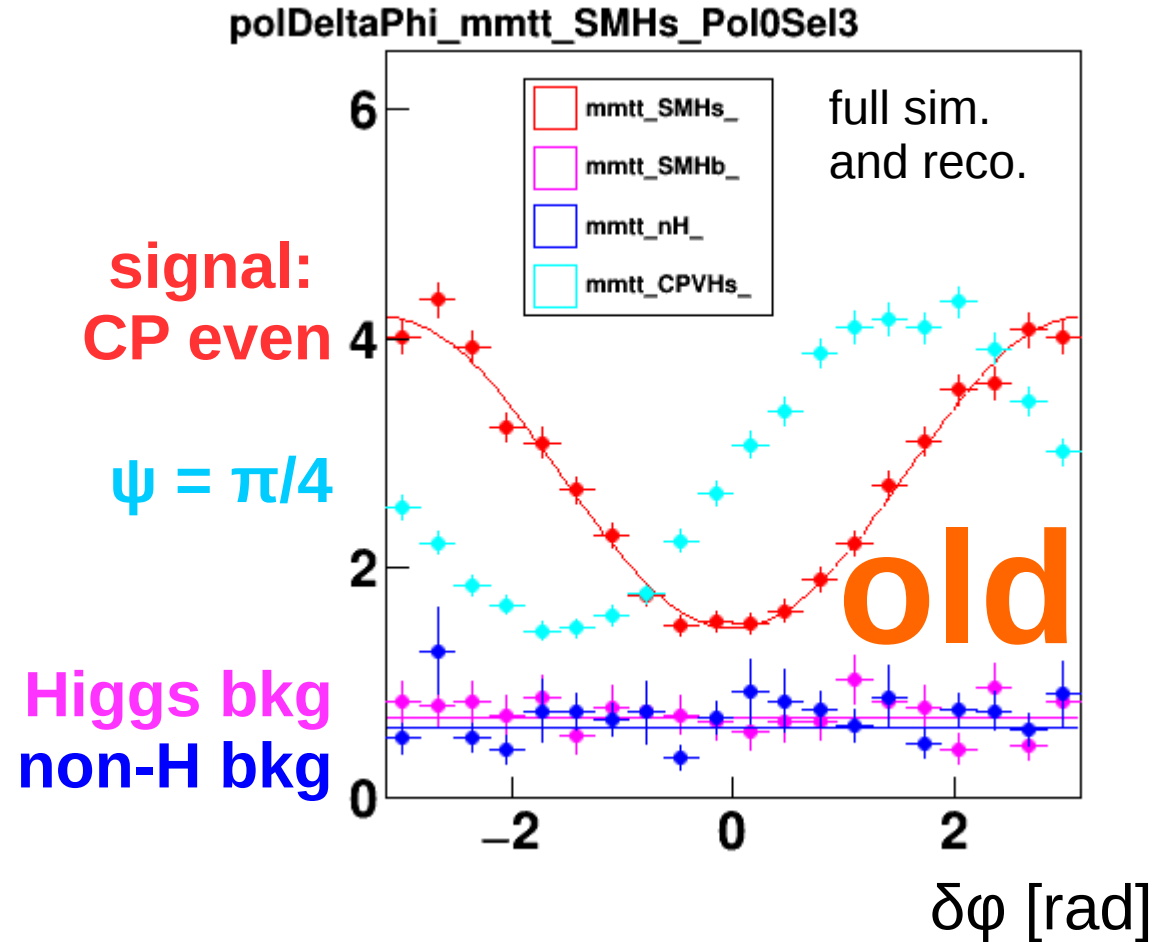
Estimation of sensitivity

Assume: sinusoidal signal
flat background
→ fit parameters

Use fit functions to run
toy MC experiments

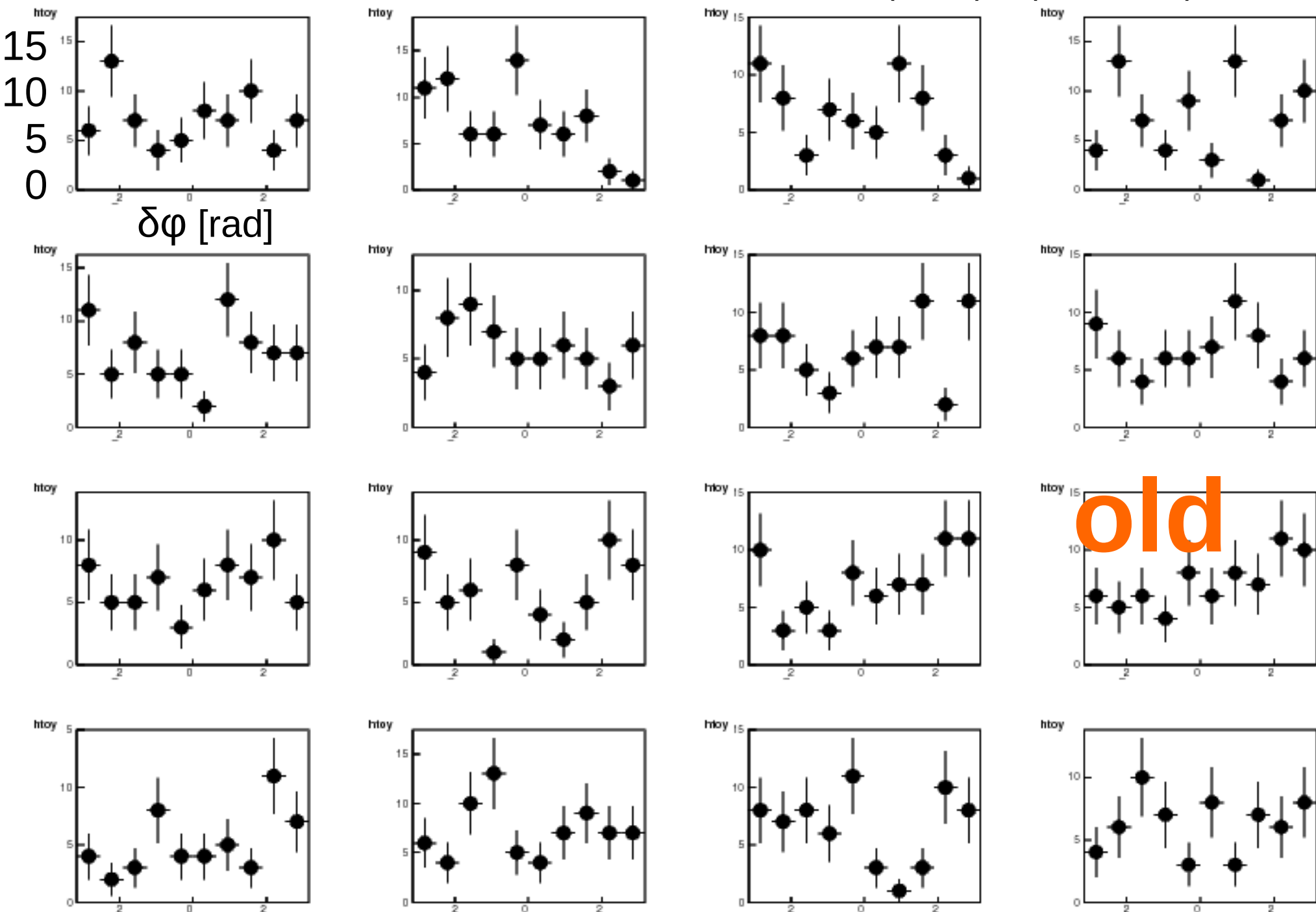
assume total xsec
independent of CP
→ maybe not a valid assumption:
extra information in xsec variation

extract phase of $\delta\phi$ variation
using unbinned maximum
likelihood fit



$\mu\tau$ channel some toy MC experiments

$P(e^-, e^+) = (-0.8, +0.3)$, 1350 fb $^{-1}$



UPDATE

Toy MC exps:

improved **estimation of uncertainty** on extracted phase:

manual scan to find points where $-2*\log(\text{like})$ increases by 1.0

[previously directly used MINUIT errors]

pull distributions now all have width 1.0 +/- 0.1

[previously up to ~1.4 in some cases]

expected error distribution rather non-symmetrical

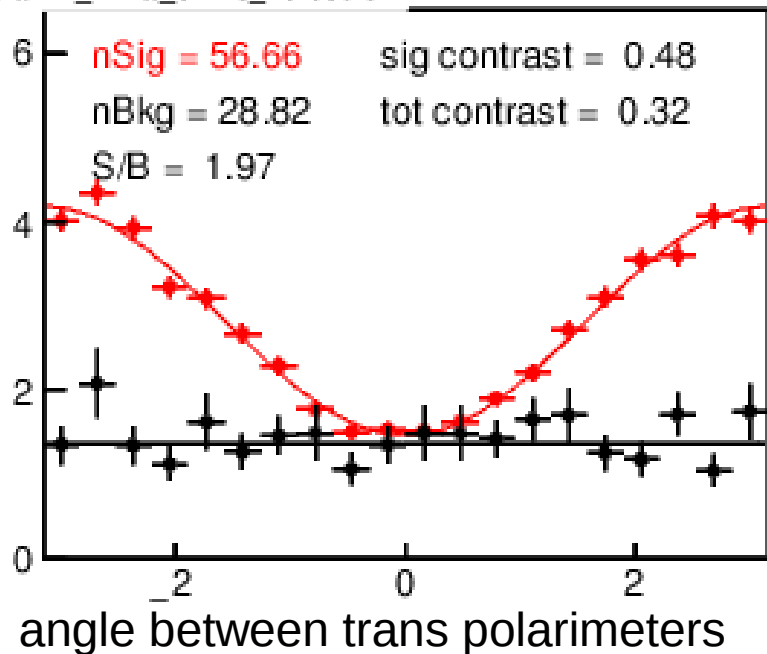
→ now quote **median** rather than **mean** error [do you agree?]

(gives an artificial “improvement”)

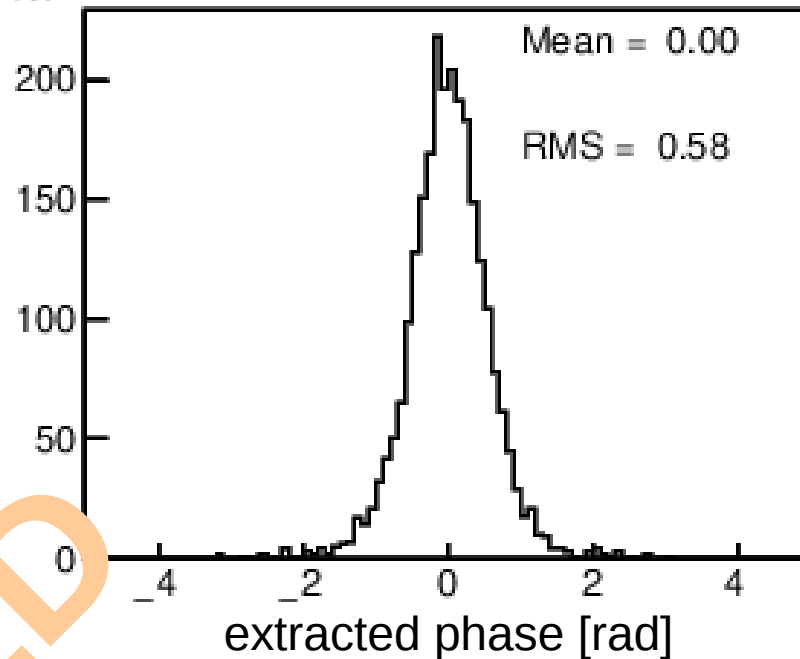
results of toy MC experiments: $\mu\mu\tau$ channel

$P(e^-, e^+) = (-0.8, +0.3)$, 1350 fb⁻¹

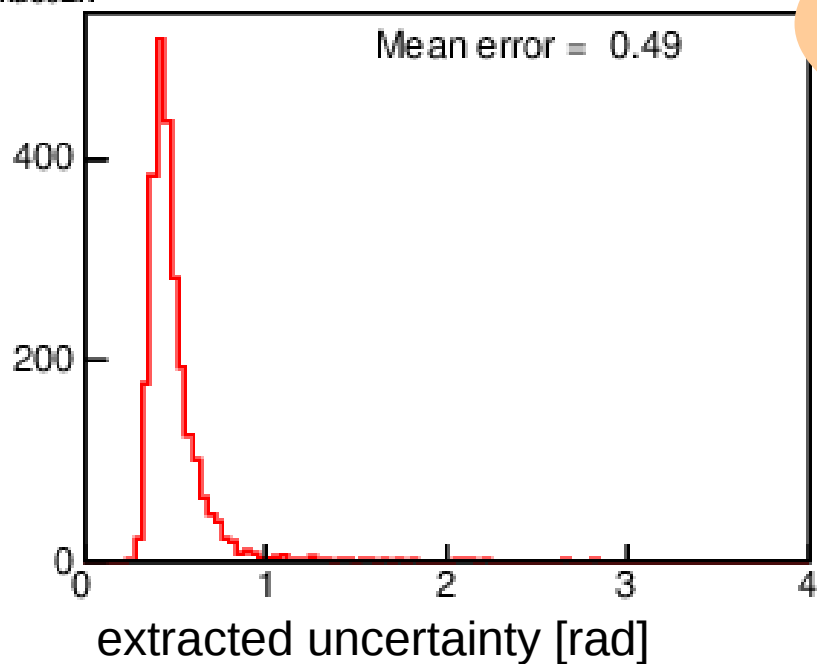
polDeltaPhi_mmtt_SMHs_Pol0Sel3



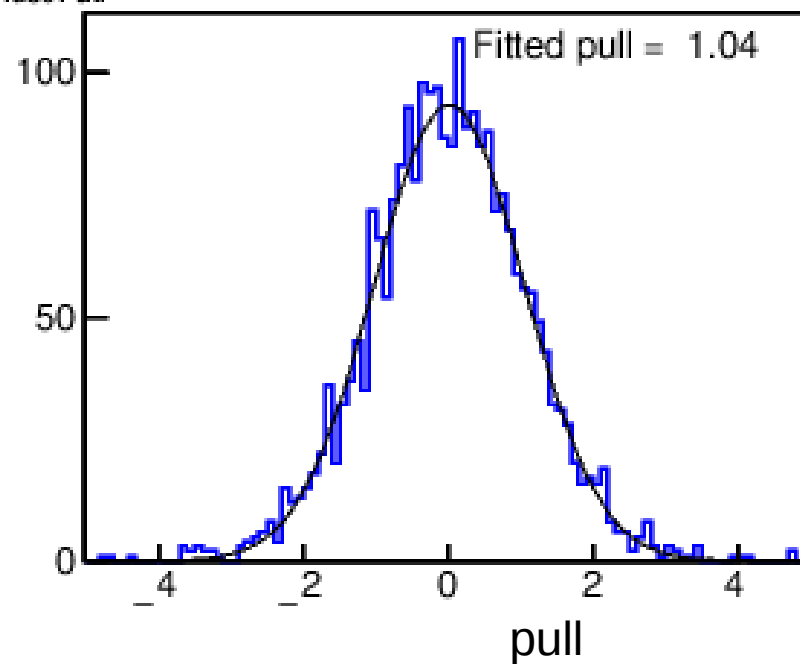
hPhase



hPhaseErr

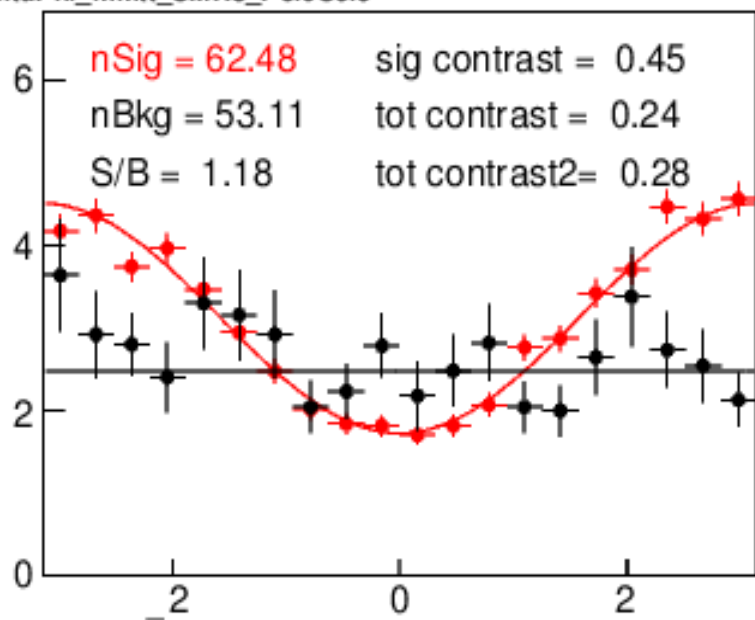


hPhasePull



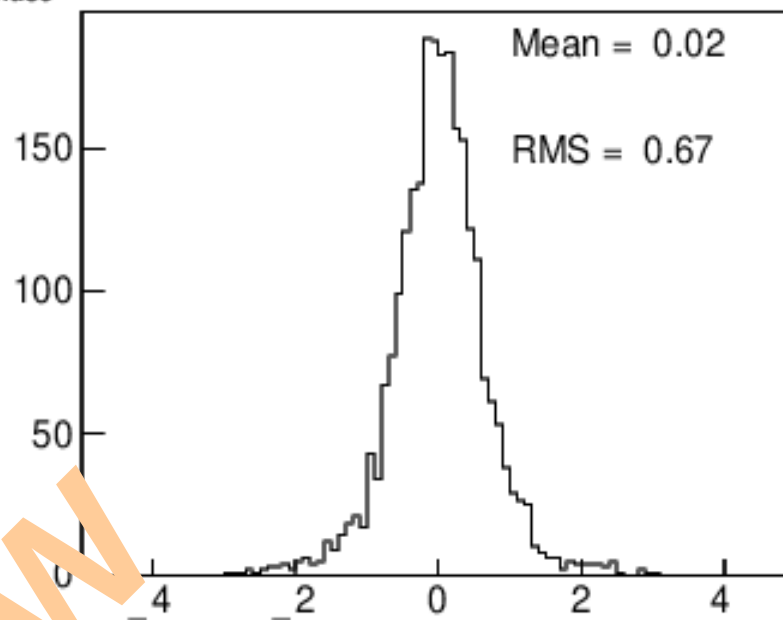
UPDATED: muon channel, full H20 (sum of both polarisations)

poiDeltaPhi_mmtt_SMHs_Pol0Sel3



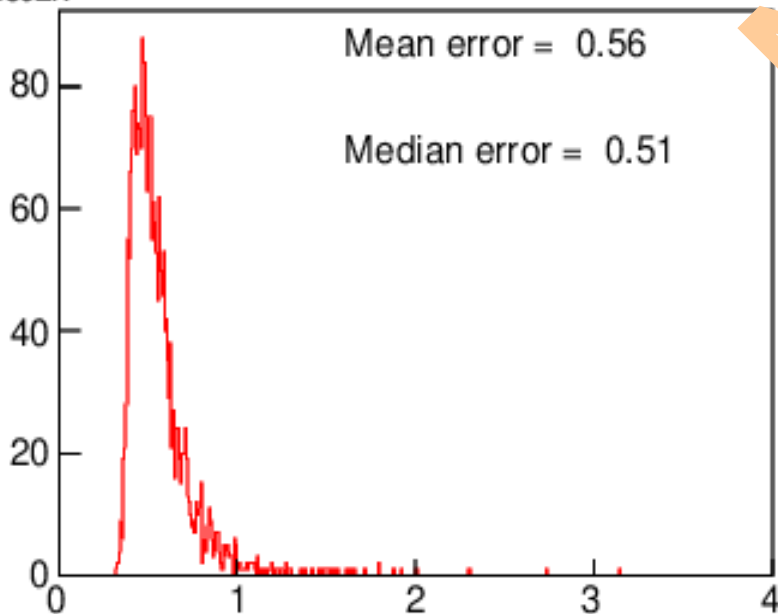
angle between trans polarimeters

hPhase



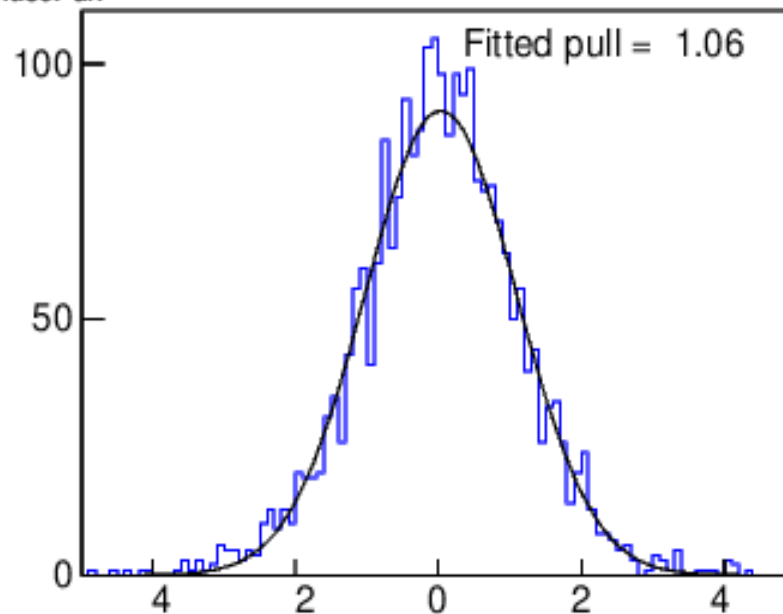
extracted phase [rad]

hPhaseErr



extracted uncertainty [rad]

hPhasePull

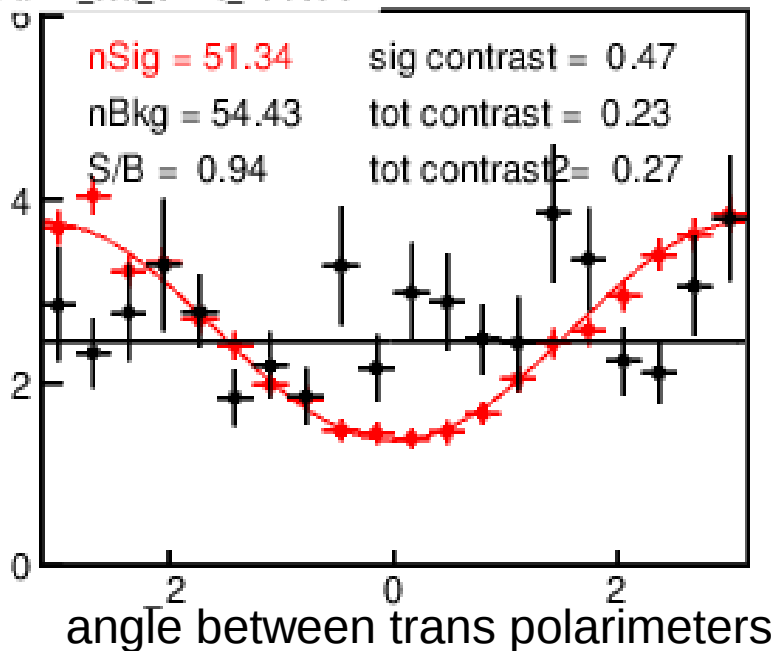


pull

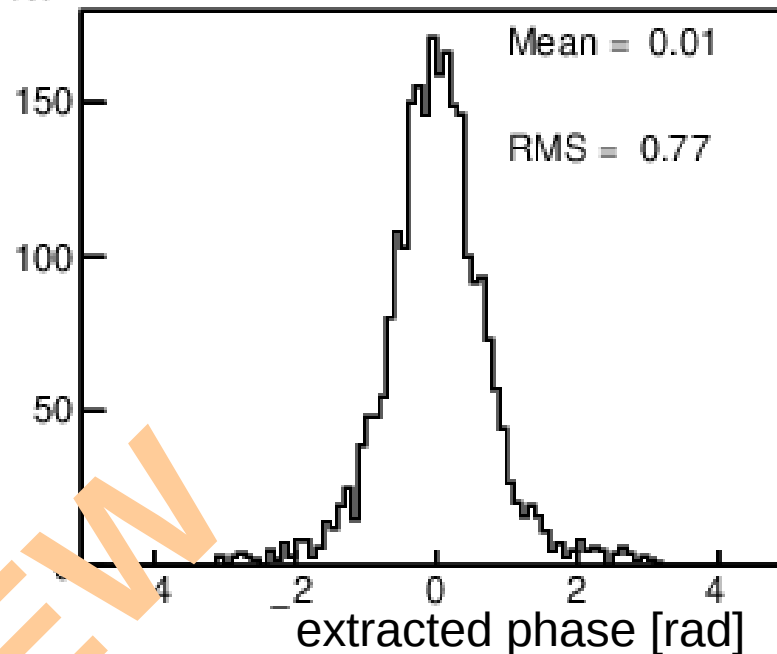
NEW

UPDATED: electron channel, full H2O (sum of both polarisations)

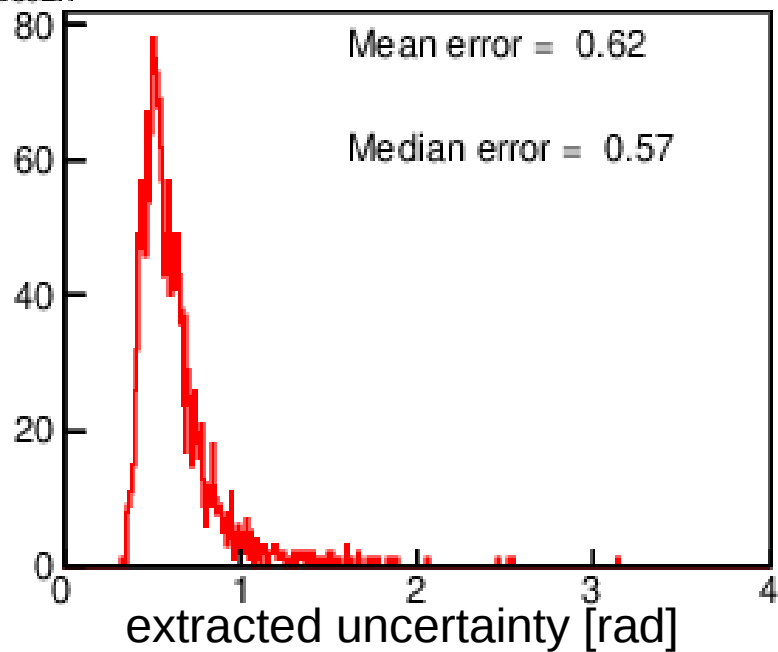
polDeltaPhi_eett_SMHs_Pol0Sel3



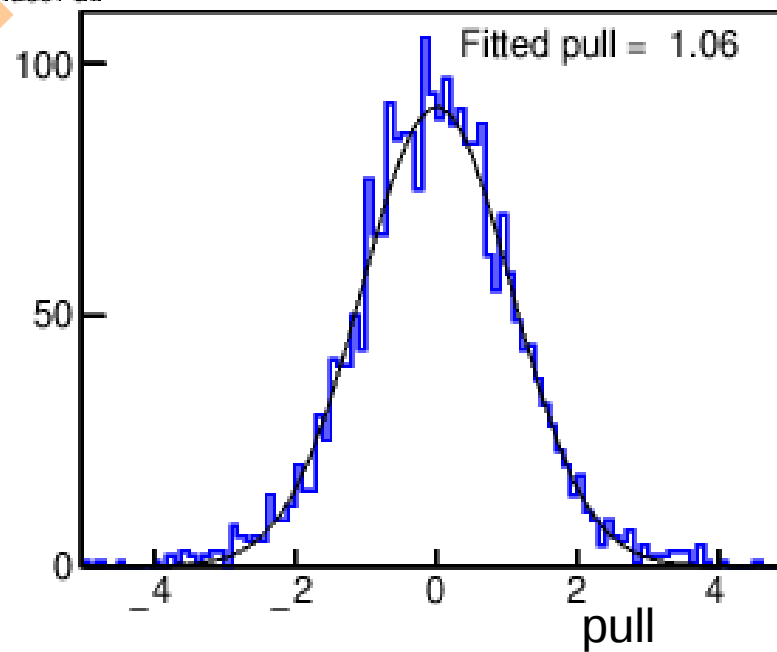
hPhase



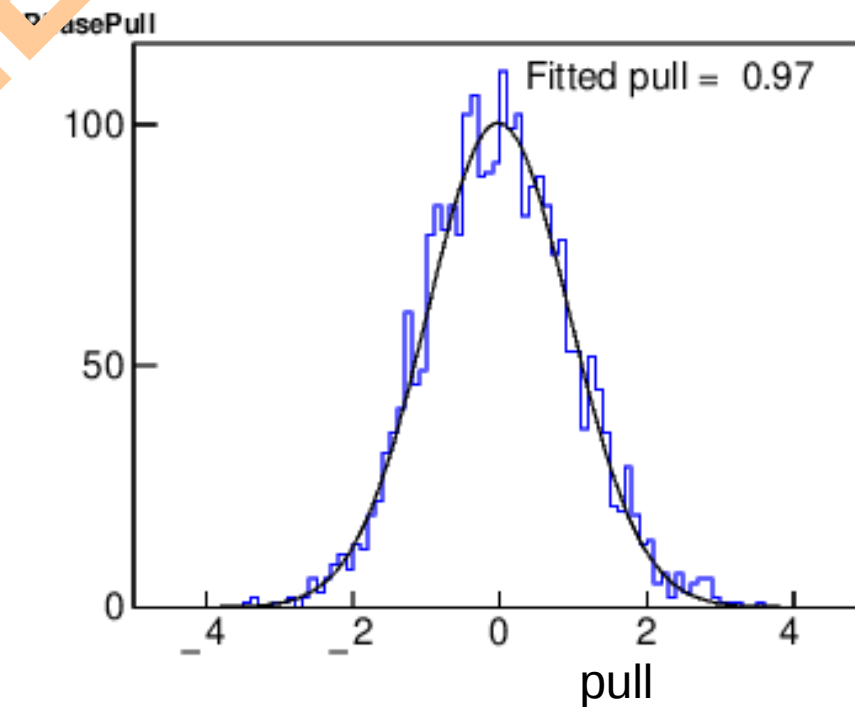
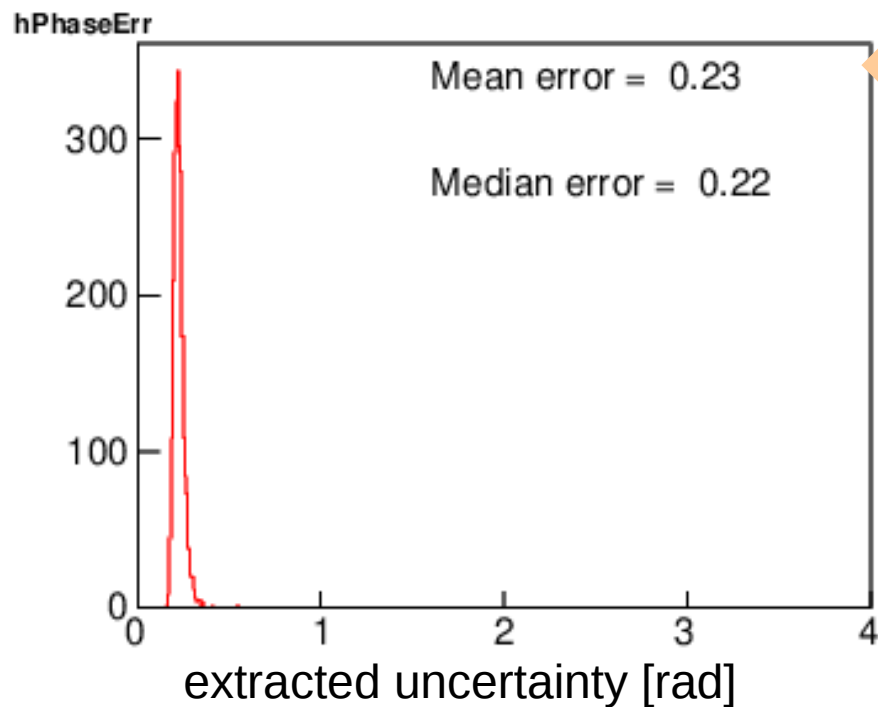
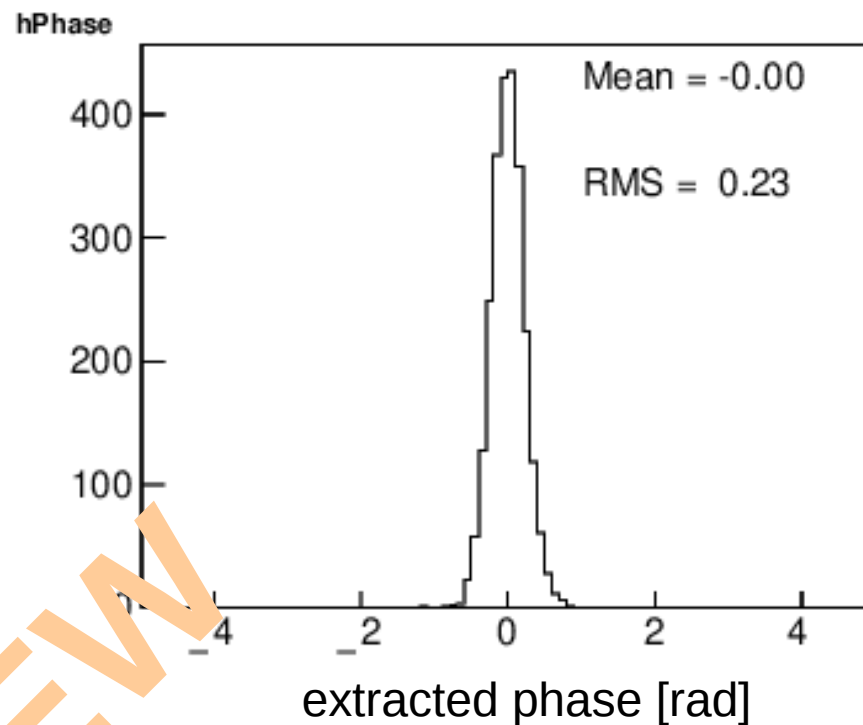
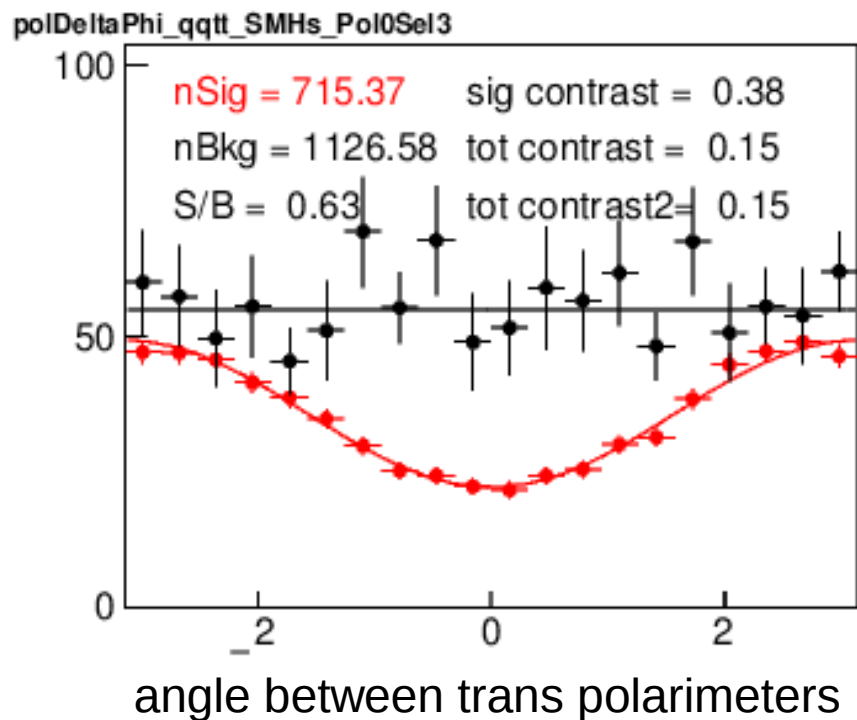
hPhaseErr



hPhasePull



UPDATED: quark channel, full H20 (sum of both polarisations)



NEW

(prelim results@Santander)

expected statistical uncertainties on

CP mixing angle 2ψ [$\psi = 0$: CP even, $2\psi = \pi$: CP odd]

channel	e e $\tau\tau$		$\mu\mu\tau\tau$		q q $\tau\tau$	
polarisation	(-0.8, +0.3) 1350 fb-1	(+0.8, -0.3) 450 fb-1	(-0.8, +0.3) 1350 fb-1	(+0.8, -0.3) 450 fb-1	(-0.8, +0.3) 1350 fb-1	(+0.8, -0.3) 450 fb-1
signal efficiency	31%	30%	50%	51%	16%	15%
# selected signal events	36.3	7.9	56.7	12.9	221	48
signal contrast	0.28	0.28	0.48	0.50	0.28	0.25
Signal / Background	1.0	1.2	2.0	2.2	0.74	0.92
mean err on 2ψ [rad]	0.9	1.4	0.5	0.9	0.4	0.8
mean error on 2ψ [rad]	0.8		0.5		0.4	
mean error on 2ψ	0.3 rad $\sim \pi/10$ rad ~ 17 degrees					

[n.b. people usually quote error on ψ]

expected statistical uncertainties on

updated results

CP mixing angle 2ψ [$\psi = 0$: CP even, $2\psi = \pi$: CP odd]

channel	e e $\tau\tau$		$\mu\mu\tau\tau$		q q $\tau\tau$ (uds/cc/bb)	
polarisation	(-0.8, +0.3) 1350 fb-1	(+0.8, -0.3) 450 fb-1	(-0.8, +0.3) 1350 fb-1	(+0.8, -0.3) 450 fb-1	(-0.8, +0.3) 1350 fb-1	(+0.8, -0.3) 450 fb-1
signal efficiency	36%	35%	45%	45%	28/25/19%	28/25/19%
# selected signal events	42.1	9.2	51.0	11.4	584	131
signal contrast	0.47	0.47	0.44	0.46	0.38	0.38
Signal / Background	0.95	0.92	1.2	1.3	0.62	0.73
median error on 2ψ [rad]	0.61	1.1	0.57	0.97	0.25	0.47
median error on 2ψ [rad]	0.57		0.51		0.22	
median error on 2ψ	0.190 rad $\sim \pi/16.5$ rad ~ 10.9 degrees					
median error on ψ	5.45 degrees					

summary

various updates to analysis:

fixed treatment of FSR

improvements to lepton and event selection

error estimation in toy MC experiments

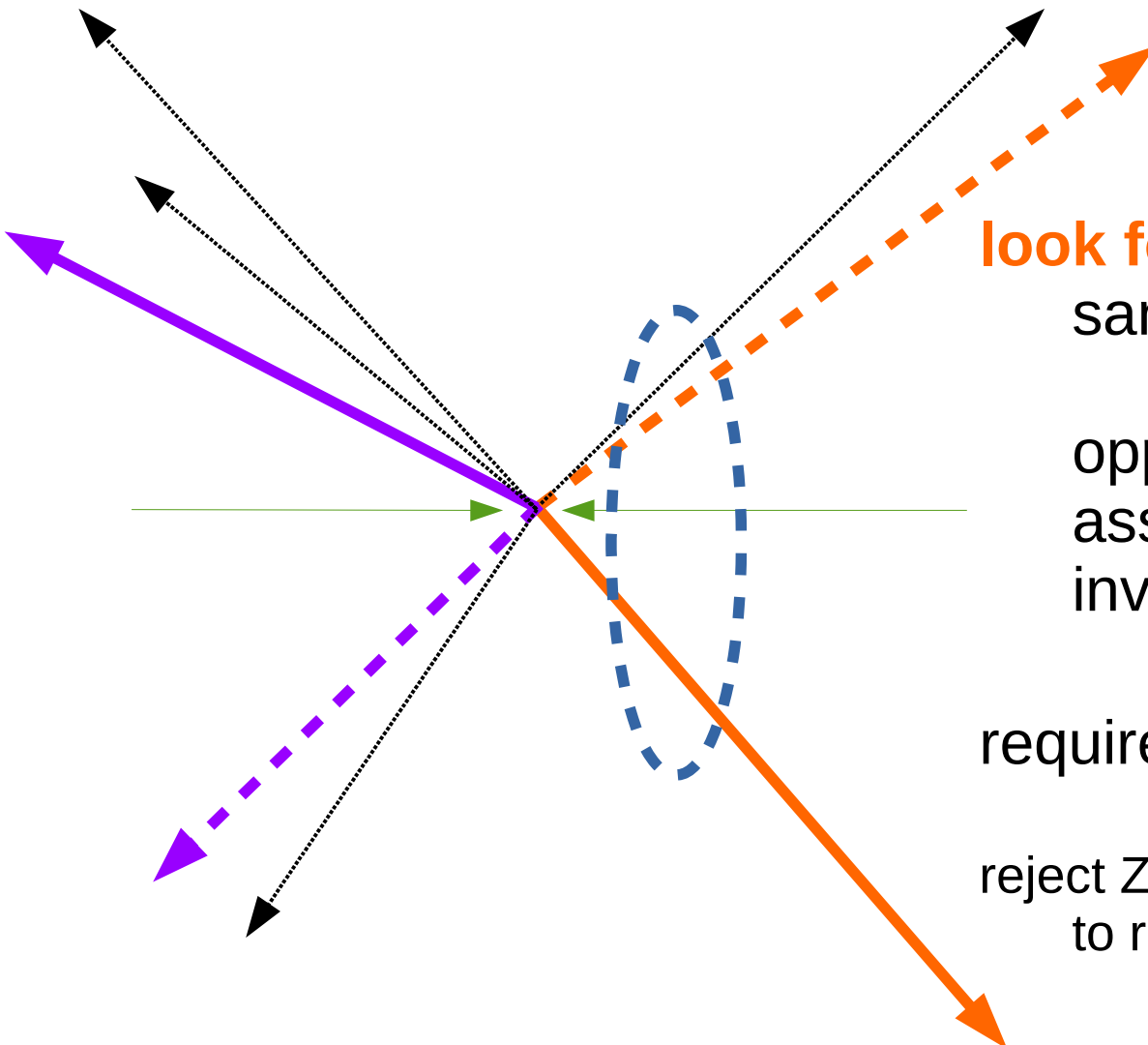
definition of final CP mixing angle

updated estimate of sensitivity ~ 5.5 degrees on Ψ_{CP}


$$\mathcal{L} \sim g \bar{f} (\cos \Psi_{CP} + i \gamma^5 \sin \Psi_{CP}) f H$$

writing a paper on 250 GeV
then move to 500 GeV.

backup slides



look for $Z \rightarrow e^+e^-, \mu^+\mu^-$
same flavour leptons
(PandoraPFA PID)
opposite charge
associate FSR
invariant mass not too far from m_Z

require exactly 1 Z candidate

reject $Z \rightarrow ee$ with very forward electrons
to reduce non-H backgrounds

electron or muon

charged hadron

photon

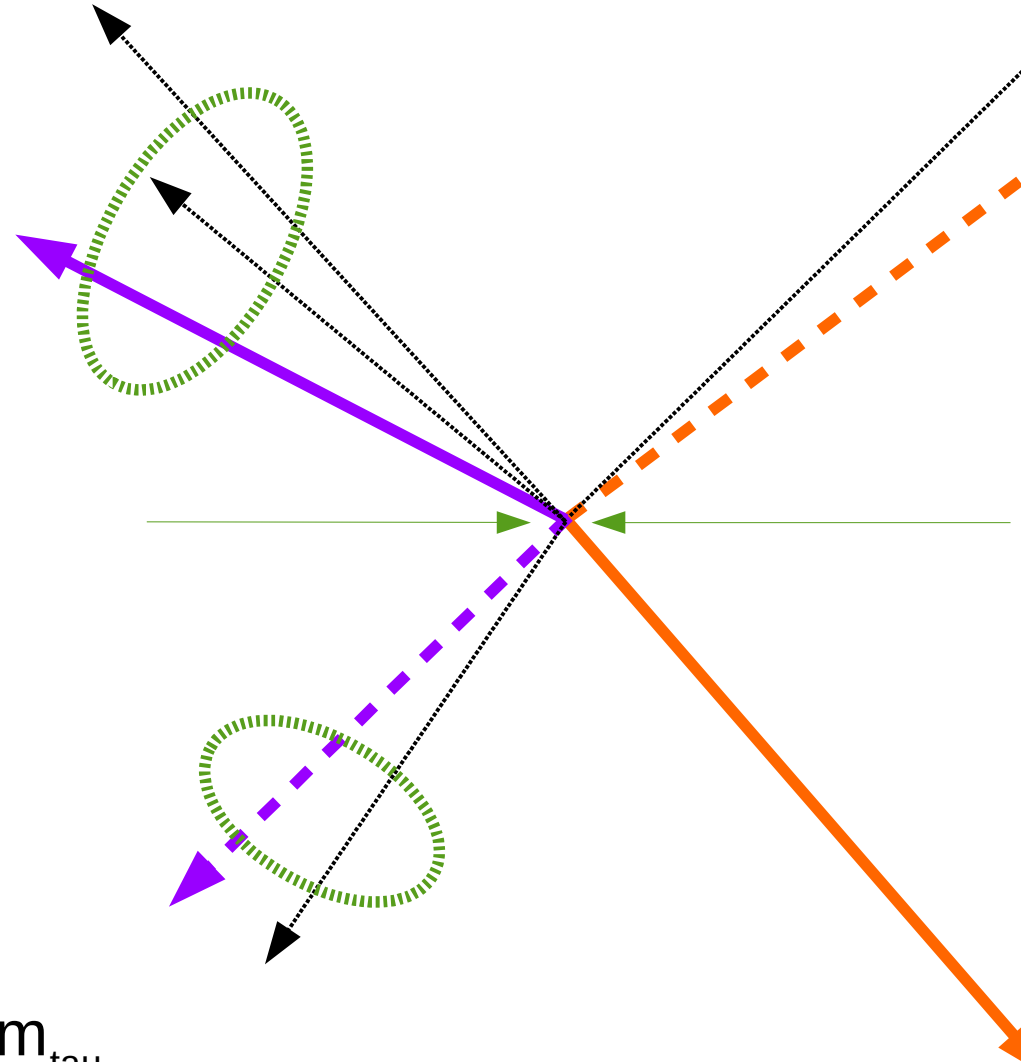
Identify hadronic tau candidates

≥ 2 additional charged PFOs
2 most energetic \rightarrow tau seeds

require oppositely charged seeds
not identified as e/mu

group remaining photons into π^0 s
if $m < m_{\text{tau}}$ with a tau seed
use mass constrained kinematic π^0 fit

add unpaired photons to nearest
tau candidate if resulting mass $< m_{\text{tau}}$



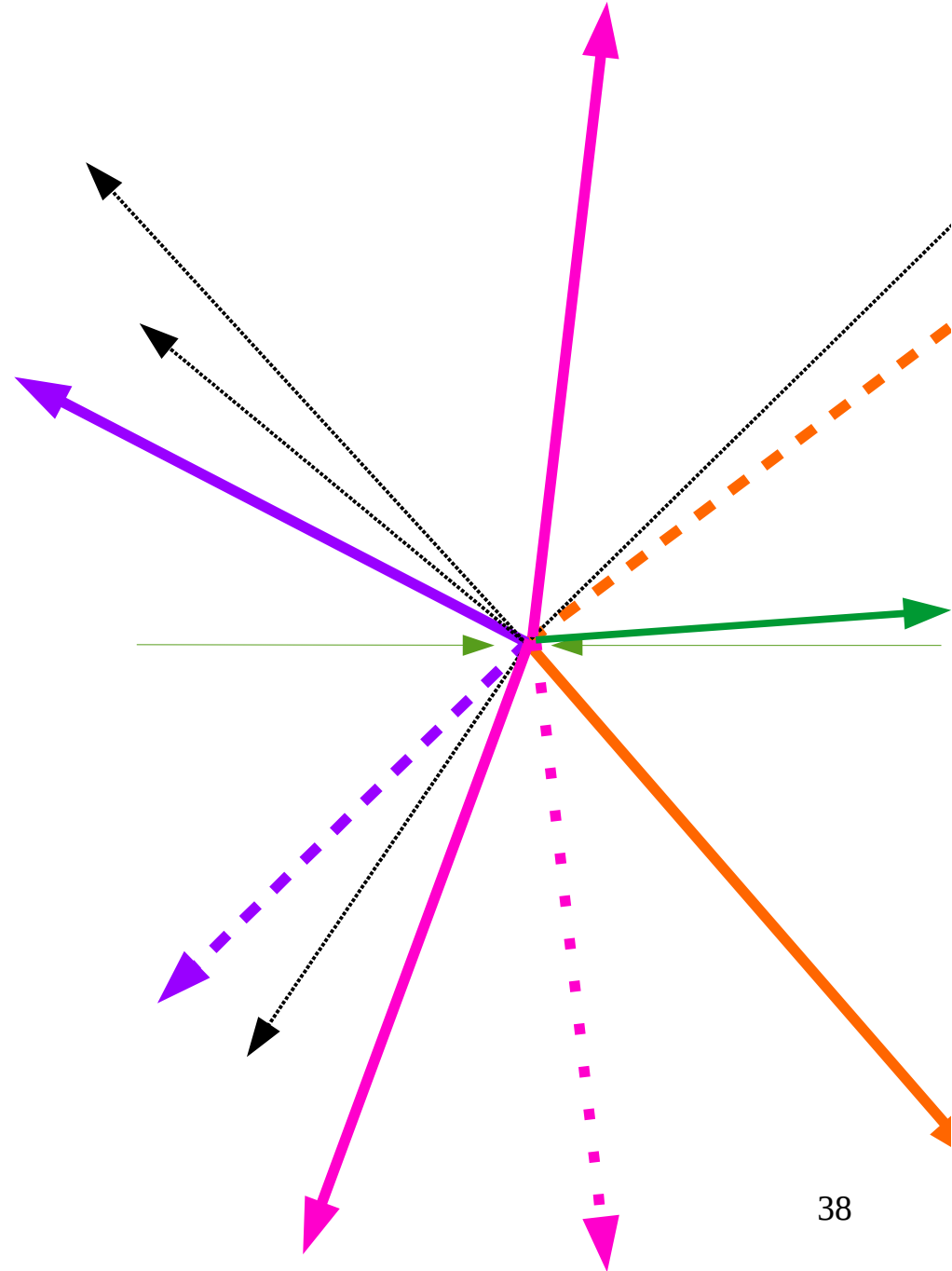
electron or muon

charged hadron

photon

veto events with > 10 GeV
charged or neutral hadron
energy or p_T
in addition to
Z and tau candidates

(some from underlying event allowed)





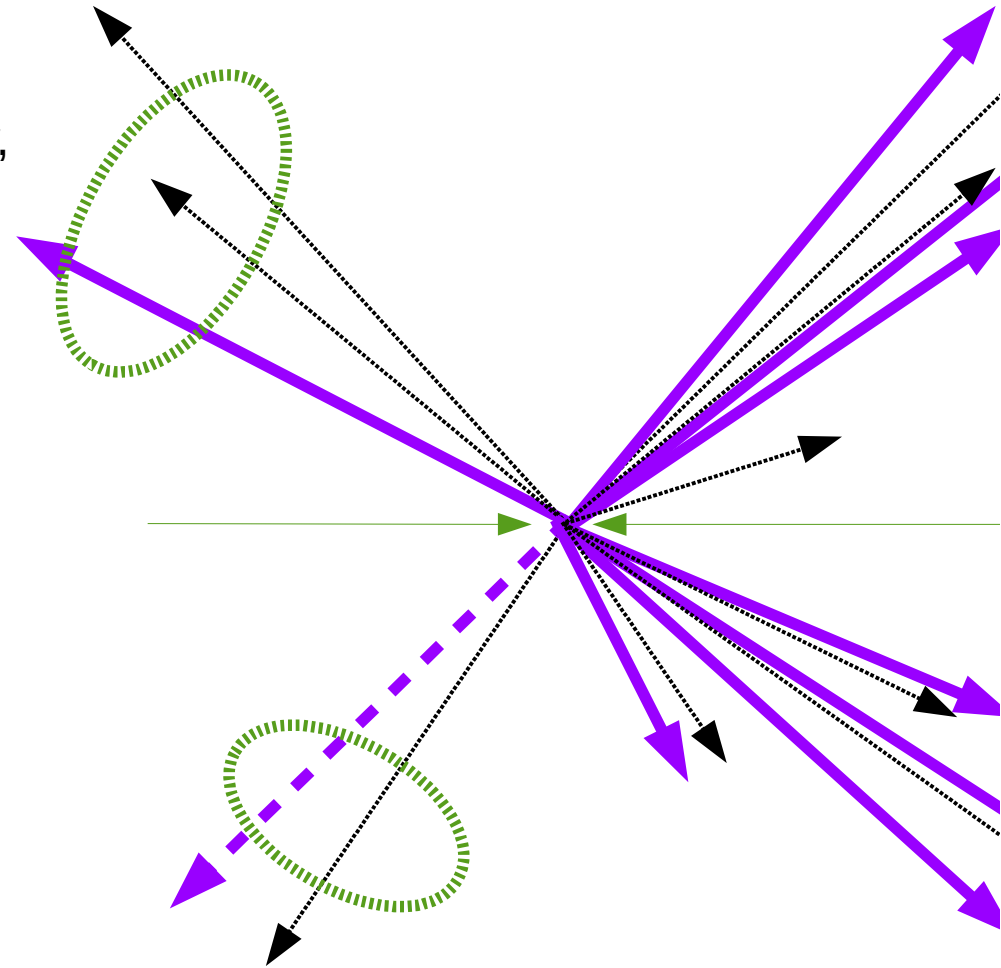
Hadronic Z decay channels

use TauJetFinder (T. Suehara) to look for narrow, isolated, low mass tau jet candidates

require exactly 2 tau jet candidates, each with a single charged particle oppositely charged

Assign remainder of event to the Z:
require a certain range of invariant mass and recoil mass for this system

The proceed as for leptonic channels



event reconstruction depends largely on:

tau decay mode identification

→ pattern recognition in ECAL

impact parameter resolution

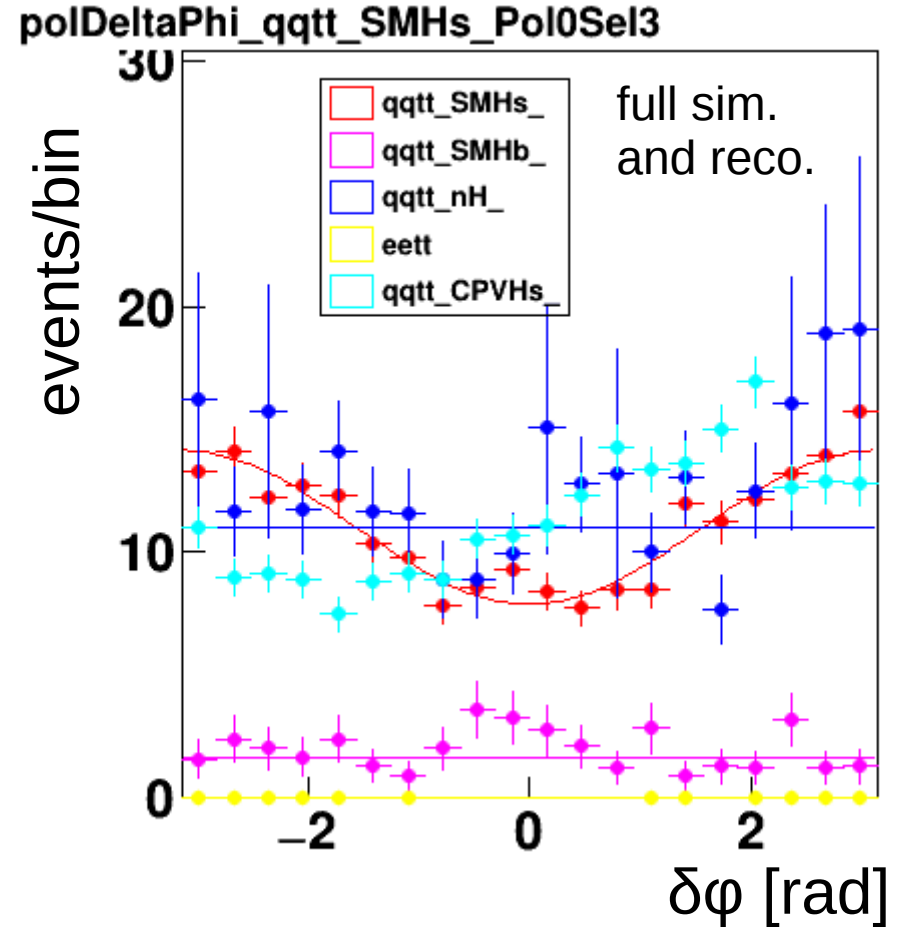
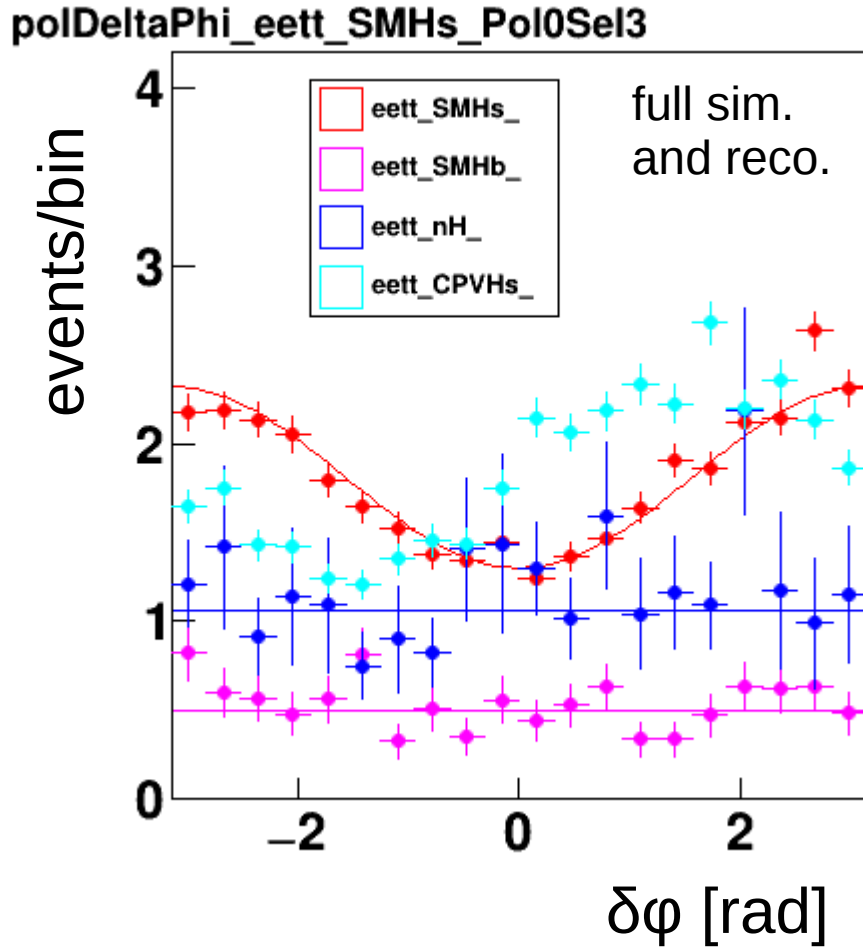
→ vertex detector

jet energy resolution

electron channel

hadronic channel

1350 fb⁻¹ @ P(e⁻,e⁺) = (-0.8, +0.3)



significantly less signal contrast
significantly larger backgrounds
higher statistics in hadronic channel

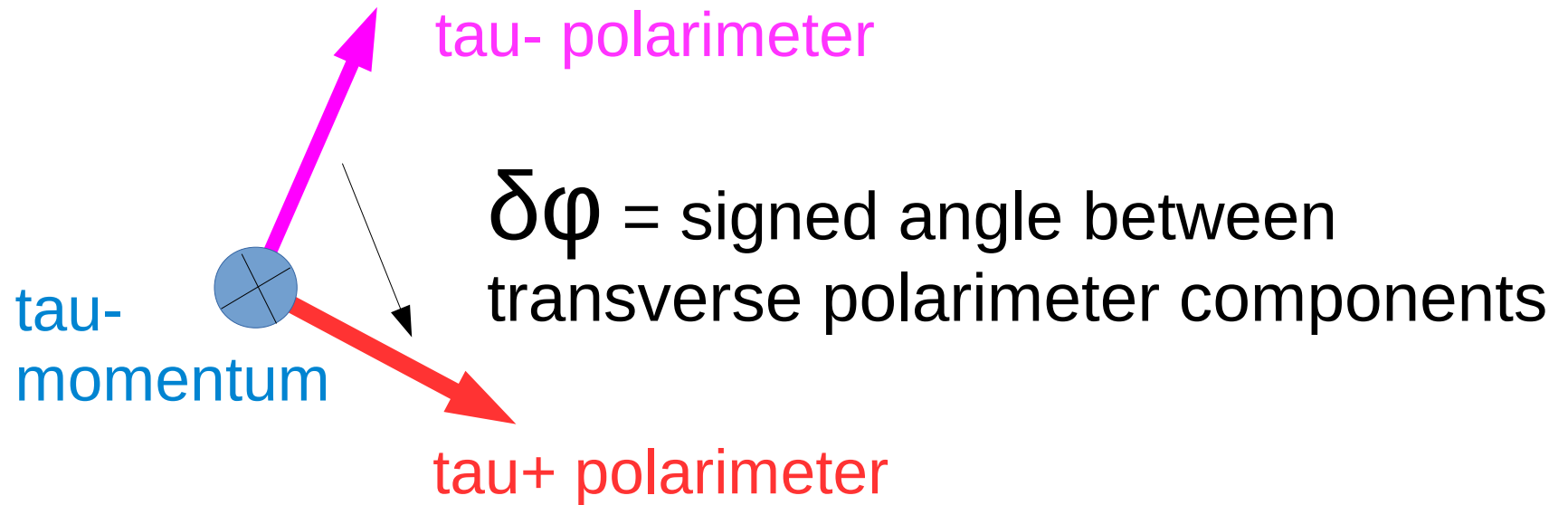
old plots

typical selection efficiencies

selection chan. → (tau decays) ↓	$e e \tau \tau$	$\mu \mu \tau \tau$	$q q \tau \tau$
signal (pi, pi)	~39 %	~68 %	~20 %
signal (pi, rho)	~33 %	~53 %	~17 %
signal (rho rho)	~27 %	~44 %	~14 %

PRELIMINARY

transverse spin correlations

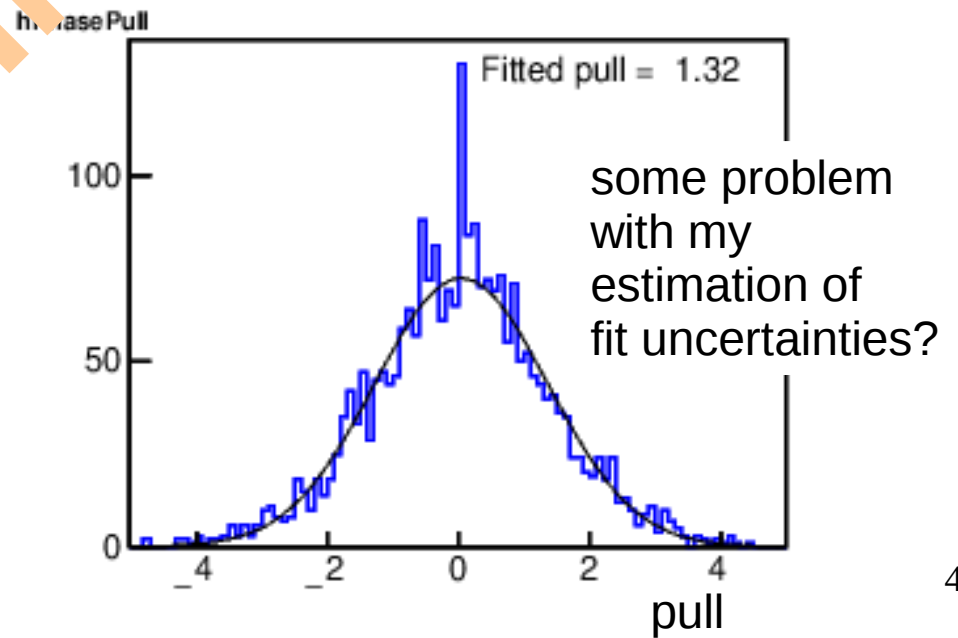
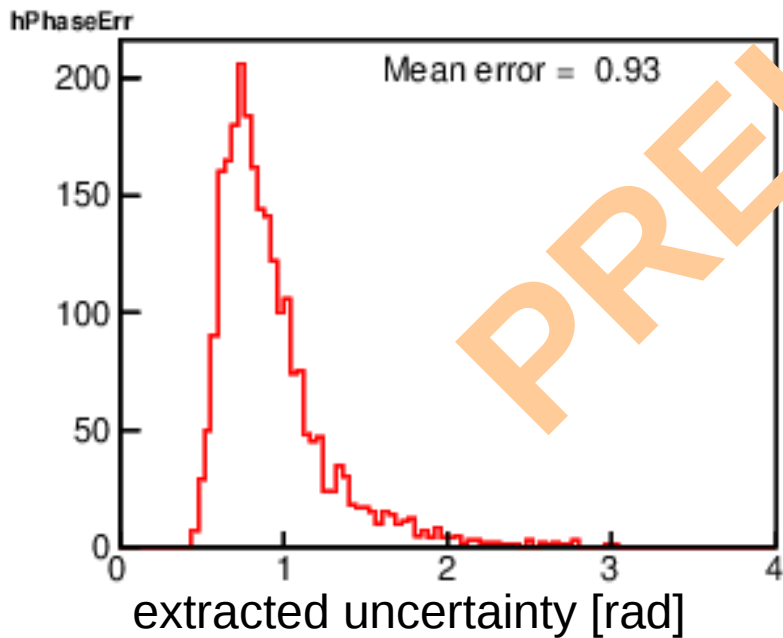
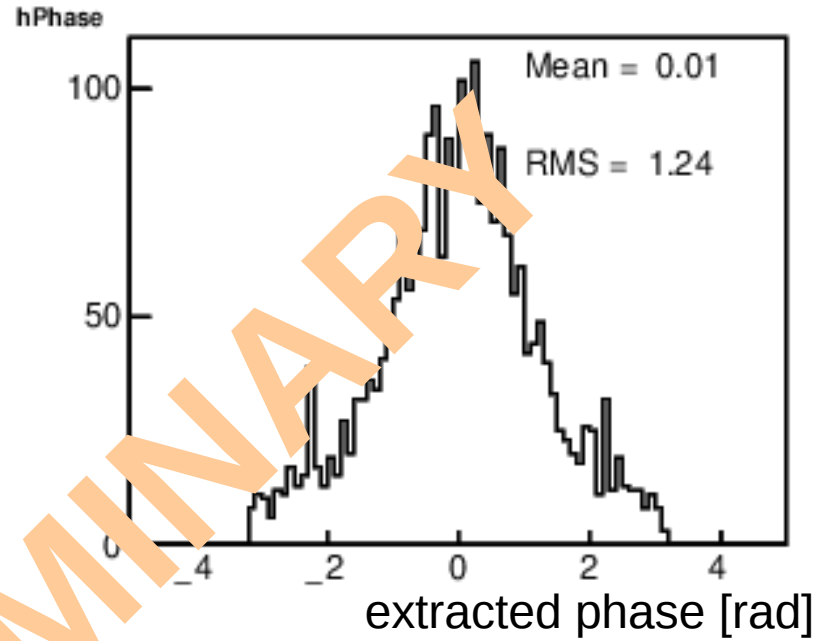
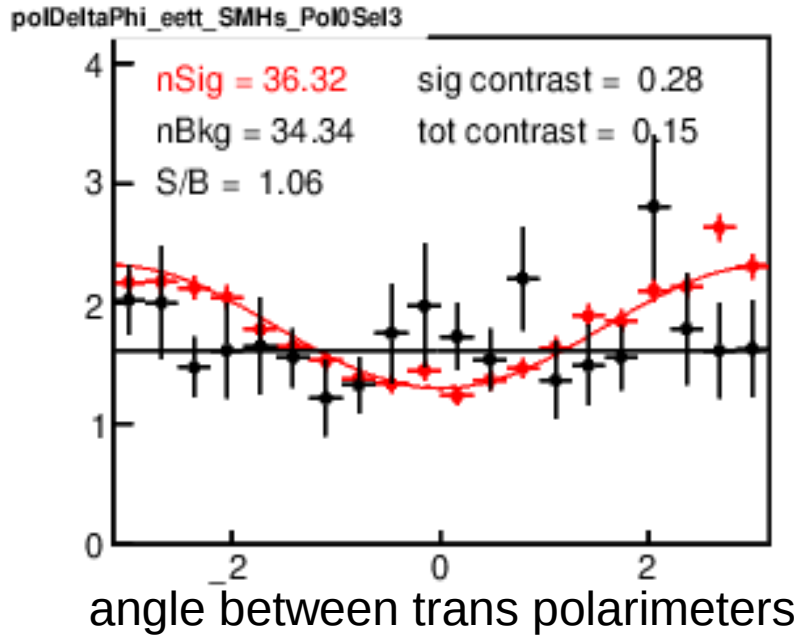


If everything is known perfectly, this is distributed as

$$f(\delta\varphi) \sim 1 + (\pi^2/16) \cos(\delta\varphi + \psi)$$

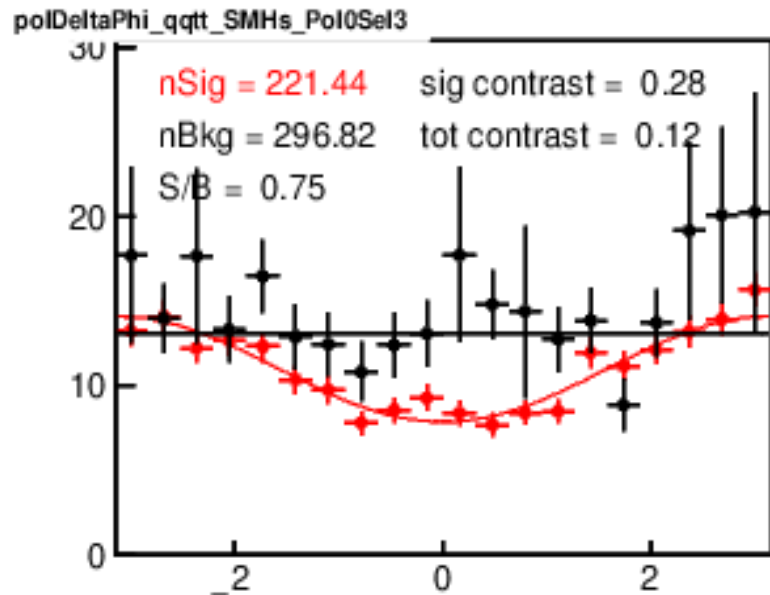
results of toy MC experiments: $e\bar{e}\tau$ channel

$P(e^-, e^+) = (-0.8, +0.3)$, 1350 fb⁻¹

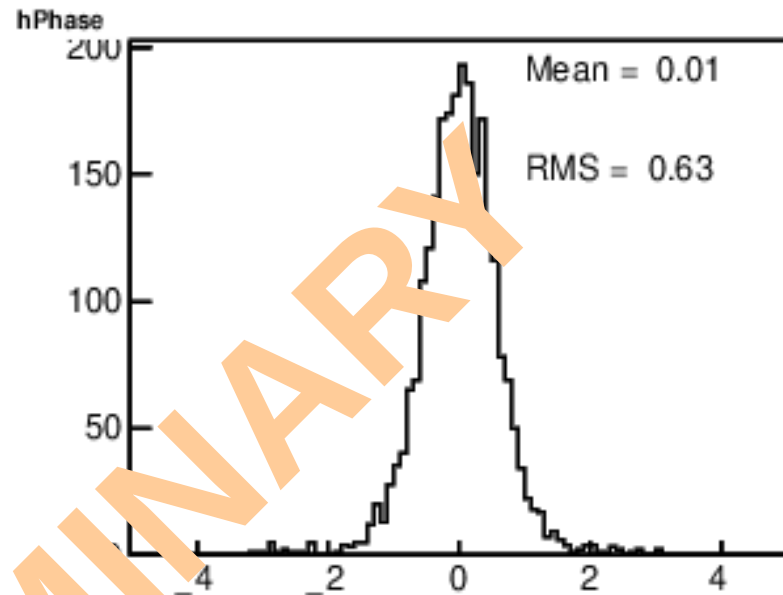


results of toy MC experiments: qq τ channel

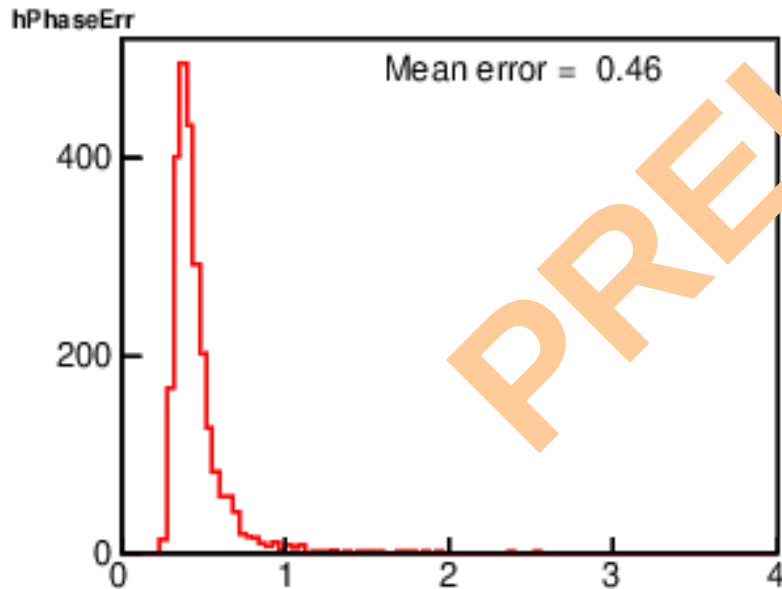
$P(e^-, e^+) = (-0.8, +0.3)$, 1350 fb $^{-1}$



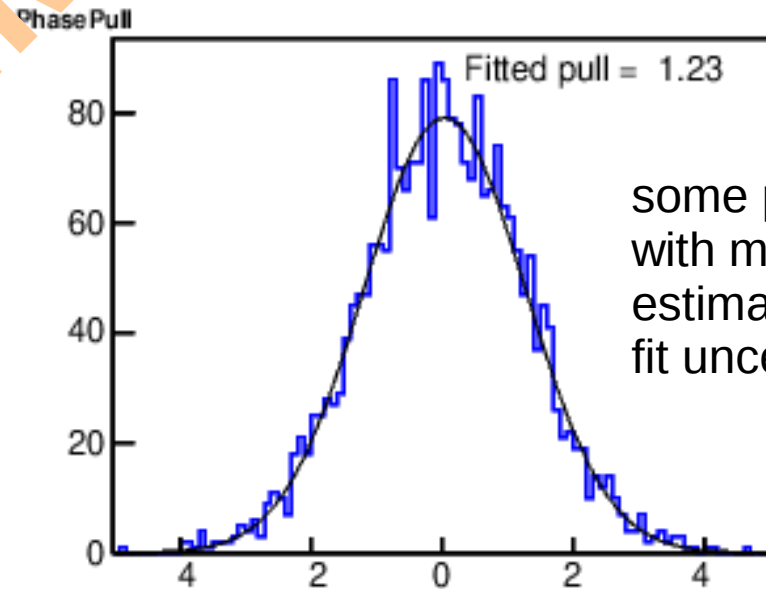
angle between trans polarimeters



extracted phase [rad]



extracted uncertainty [rad]



some problem with my estimation of fit uncertainties?

pull

Results *all preliminary*

several caveats:

- selections not carefully optimised
- included major, but not all, backgrounds
- increased MC statistics required in places
- pull distributions not perfect:
probable underestimation of uncertainties

CP Violation needed to explain baryon asymmetry of universe

currently known sources of CPV not sufficient

Higgs of the minimal SM is CP even eigenstate,
with CP conserving couplings

more complex models often also have CP odd states
(H_{125} being pure CP odd is \sim ruled out by LHC)

in the case of CP violation in the Higgs sector,
H and/or its decay products may not be an eigenstate of CP

could the Higgs sector be an additional source of CPV?

leptonic preselection:

exactly 1 Z candidate:

pair of opposite sign, same MarlinPandora PID leptons

$E_{lep} > 20 \text{ GeV}$

add photons within $\cos\Theta > 0.99$ of lepton

$(m - m_Z) < 10 \text{ (15) GeV}$ for $mumu$ (ee)

reject if $Z \rightarrow ee$ & $|\cos\theta(\text{electron})| > 0.95$

require ≥ 2 additional charged PFOs

highest energy pair considered as tau seeds

require than tau seeds not identified as electron or muon

and that seeds have opposite charge

starting with highest energy photons,

look for π^0 candidates which match a tau seed

[reasonable probability in constrained mass π^0 fit,

total mass with seed $< m_{\tau}$]

unpaired photons: attach to nearest tau if mass $< m_{\tau}$

leptonic selection

tighter lepton-lepton mass cut, within 10 GeV of m_Z for electrons

total pT and energy of remaining charged PFOs < 10 GeV

total pT and energy of neutral hadron PFOs < 10 GeV

visible mass of each tau jet < 1 GeV

no more than 1 pi0 candidate attached to each tau jet

<4 photon PFOs attached to each tau jet

successful reconstruction of tau momenta

110 GeV < tau-tau mass < 140 GeV

recoil mass > 110 (120) GeV for ee (mm)

hadronic preselection

exactly 2 tau jets from TauFinder

each tau jet contains 1 charged particle, not identified as electron or muon

each tau jet contains 0 neutral hadrons

each tau jet contains ≤ 3 photons

oppositely charged tau jets

hadronic selection

invariant mass of remainder of event $70 \rightarrow 110$ GeV

successful reconstruction of tau momenta

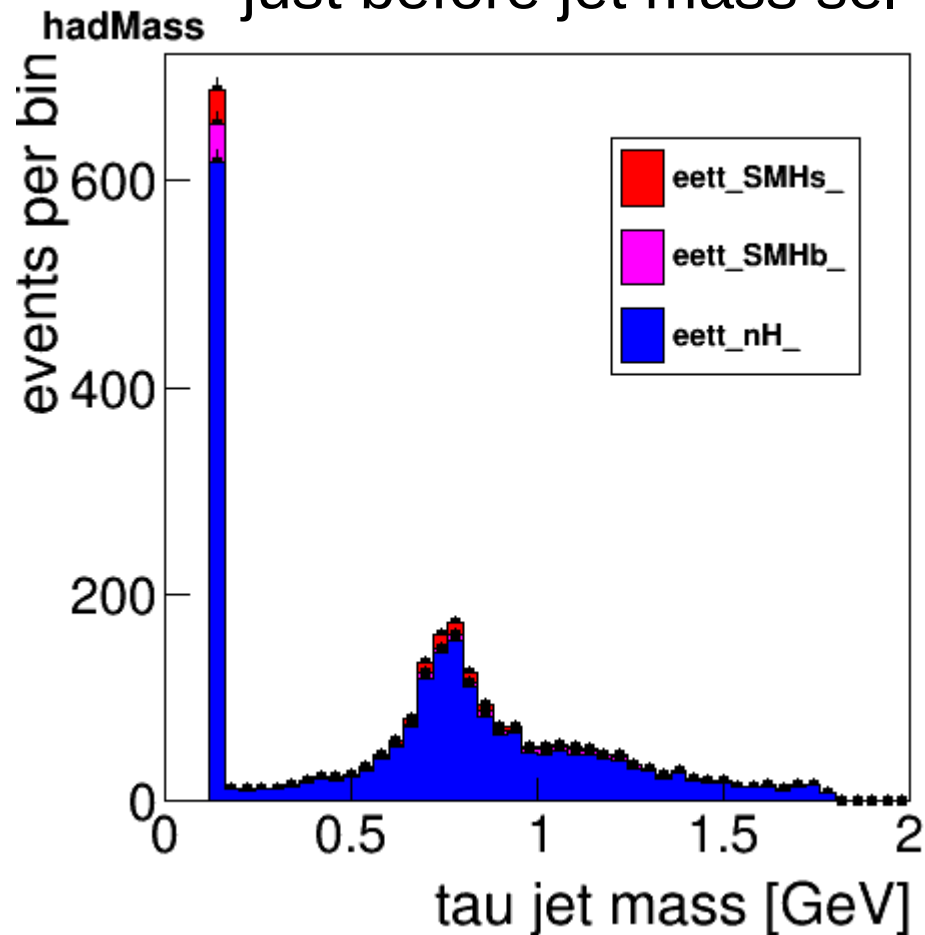
$100 \text{ GeV} < \text{tau-tau mass} < 150 \text{ GeV}$

recoil mass > 110 GeV

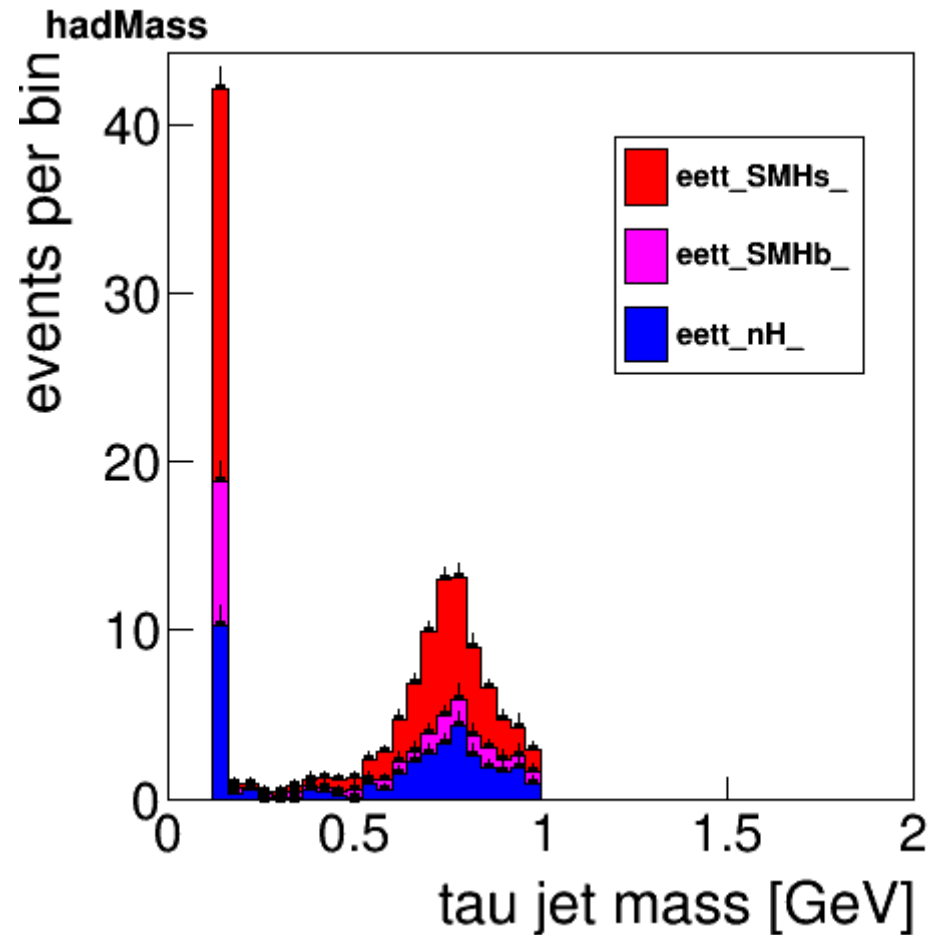
Tau jet mass (e e $\tau \tau$ selection)

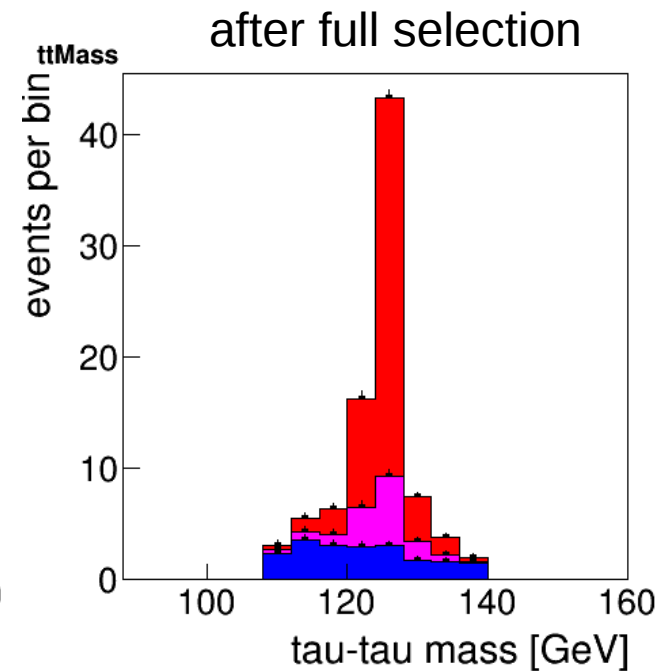
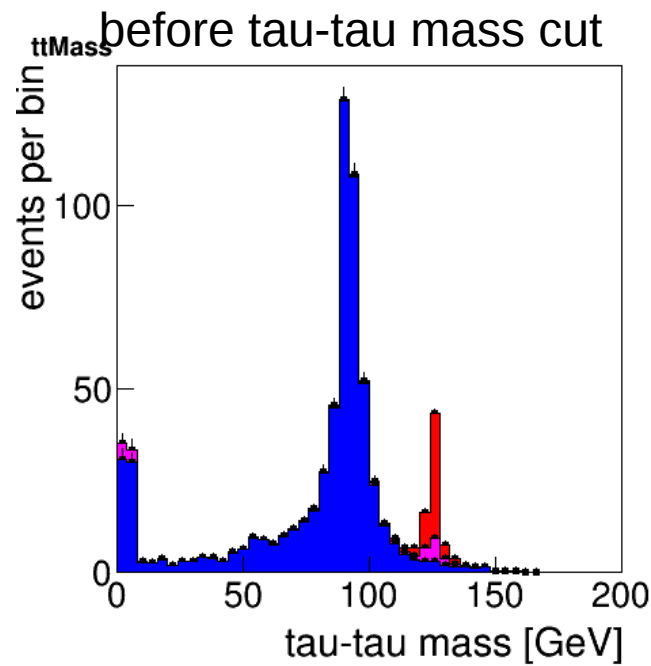
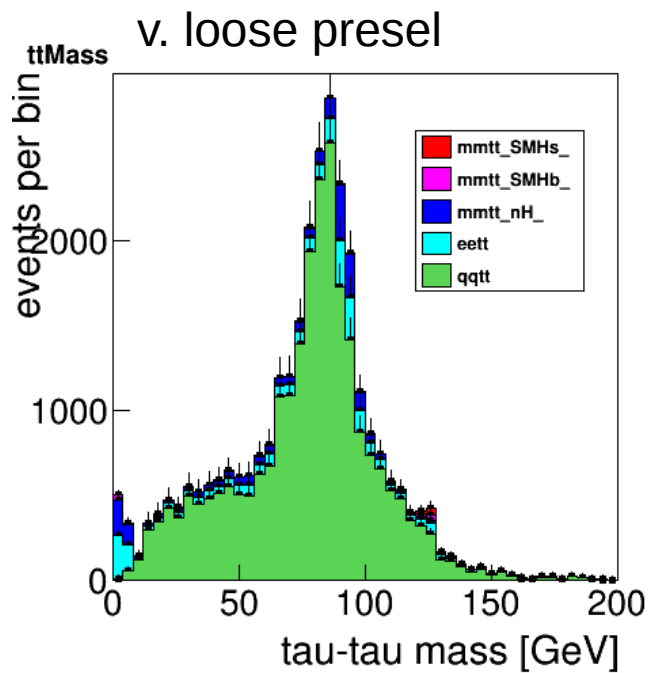
$P(e^-, e^+) = (-0.8, +0.3)$, 1350 fb⁻¹

just before jet mass sel



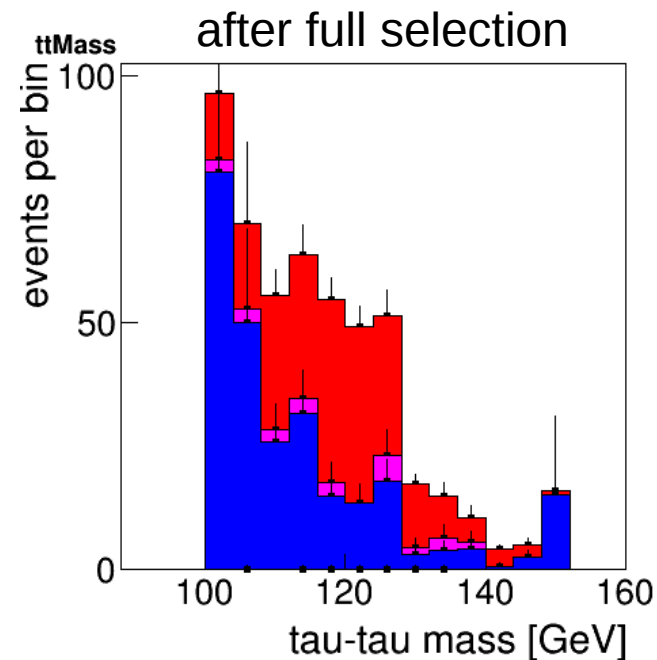
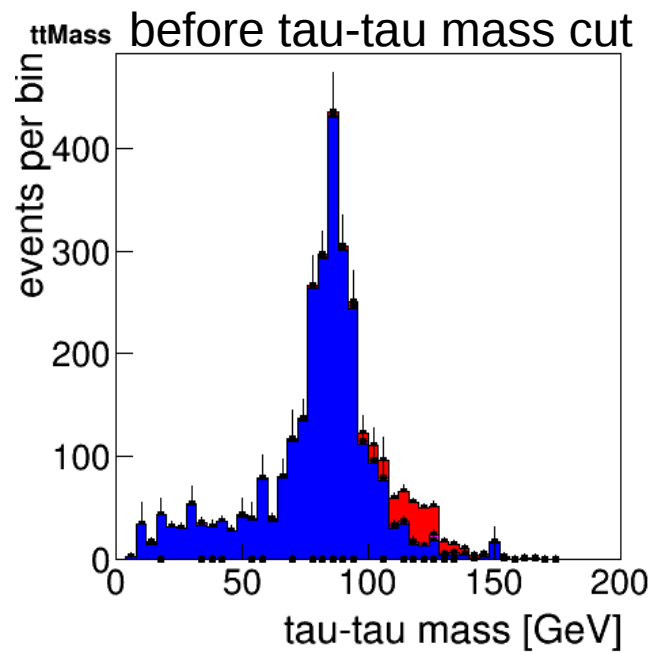
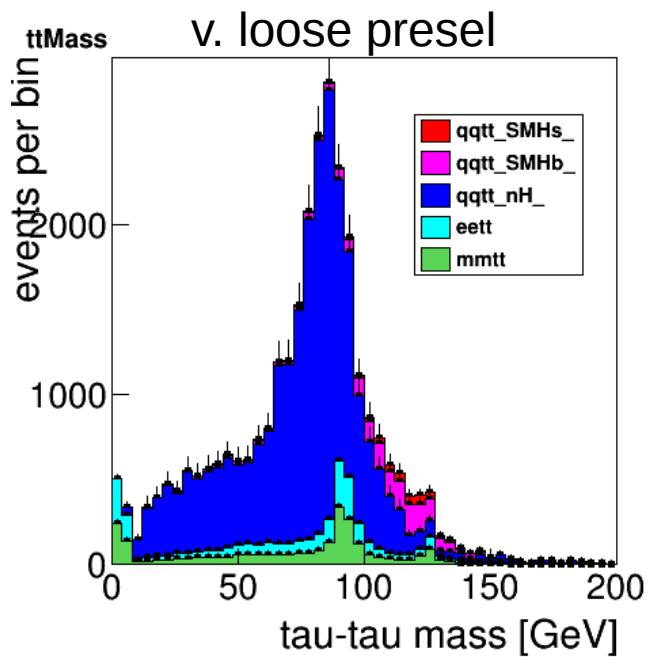
final selection





reconstructed tau-tau invariant mass
 $P(e^-, e^+) = (-0.8, +0.3), 1350 \text{ fb}^{-1}$

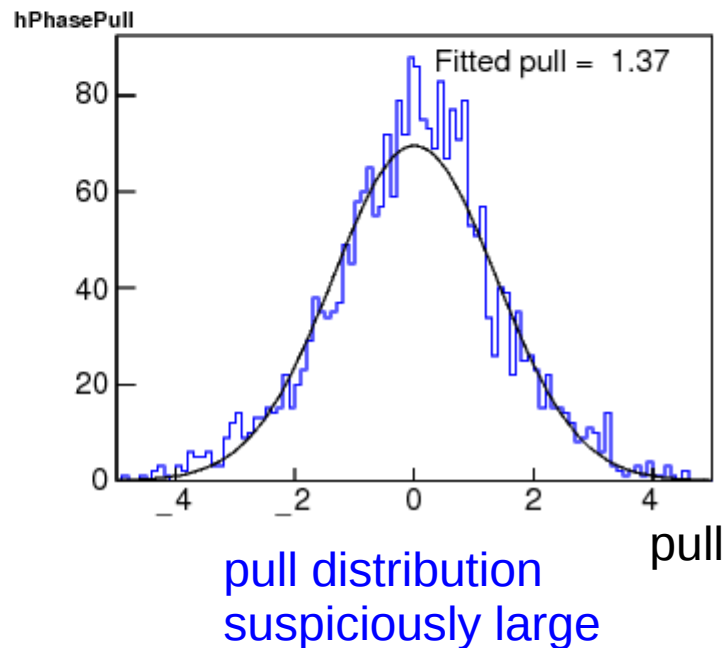
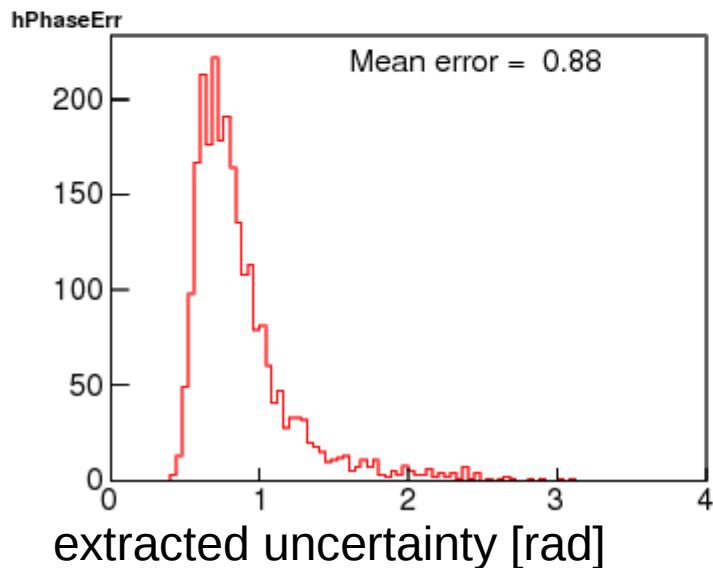
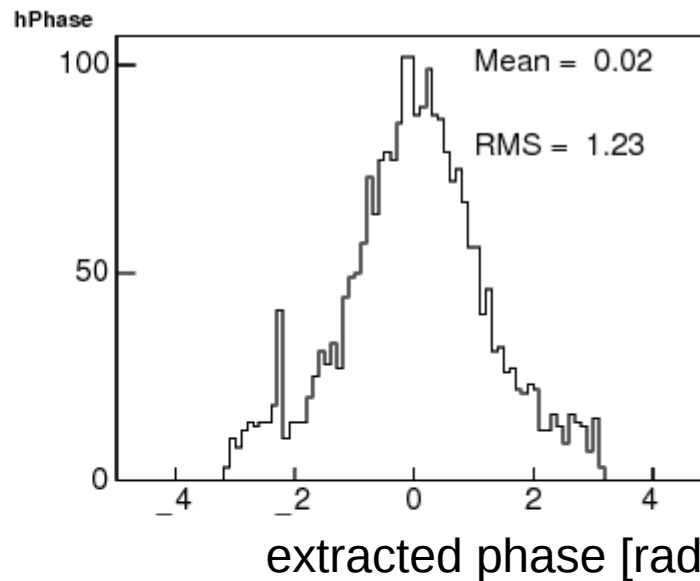
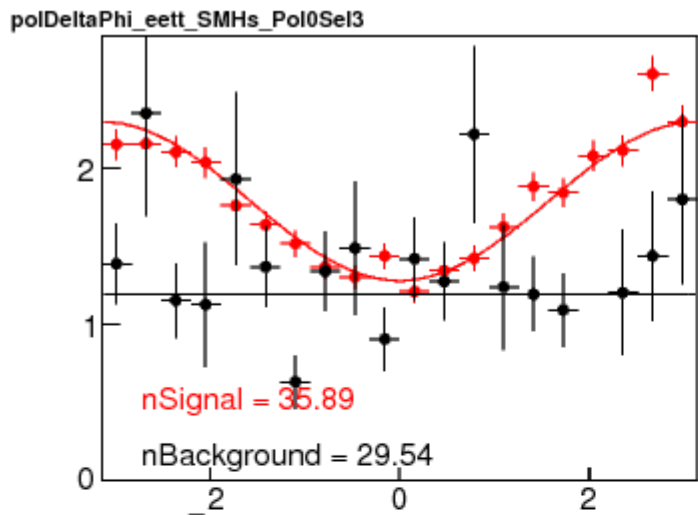
$\mu \mu \tau \tau \uparrow$
 $q q \tau \tau \downarrow$



e $\pi\pi$ channel

results of toy MC experiments

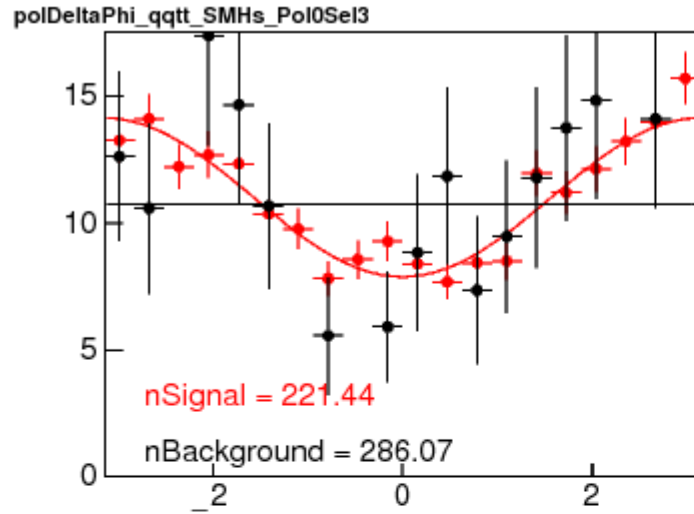
$P(e^-, e^+) = (-0.8, +0.3)$, 1350 fb $^{-1}$



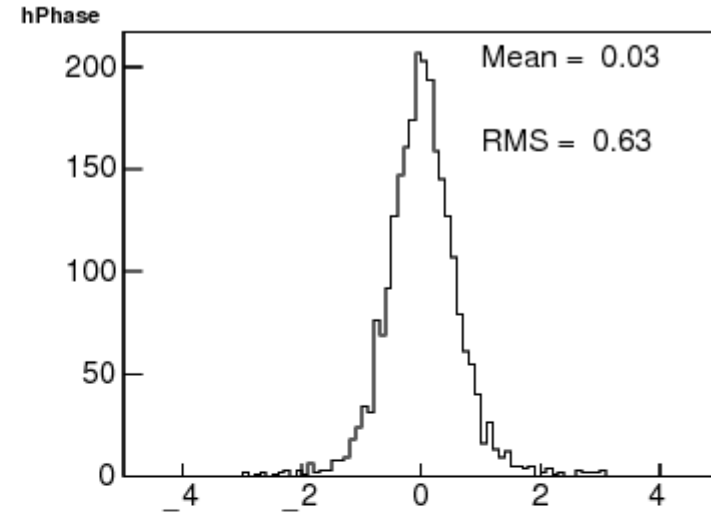
qq $\pi\pi$ channel

results of toy MC experiments

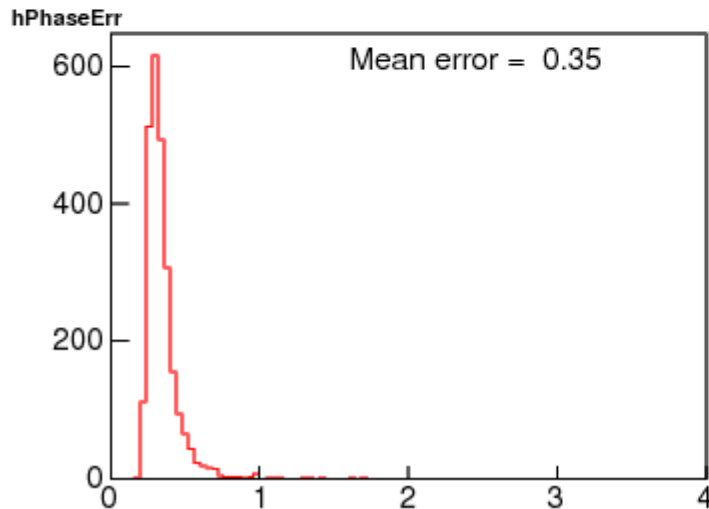
$P(e^-, e^+) = (-0.8, +0.3)$, 1350 fb $^{-1}$



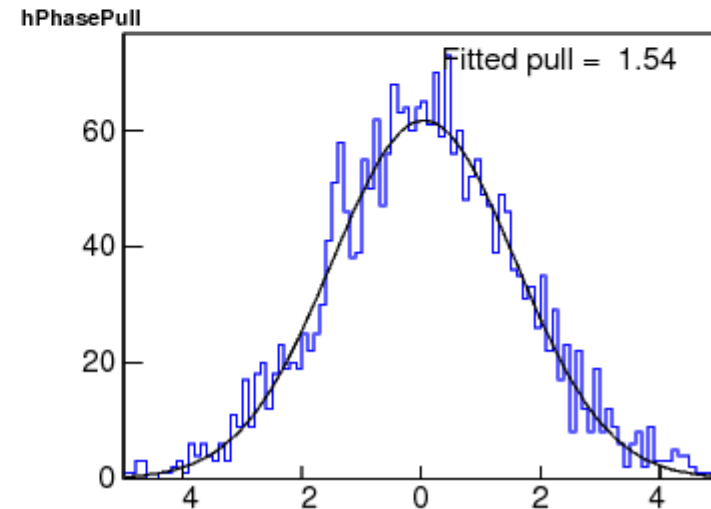
angle between trans polarimeters



extracted phase [rad]



extracted uncertainty [rad]

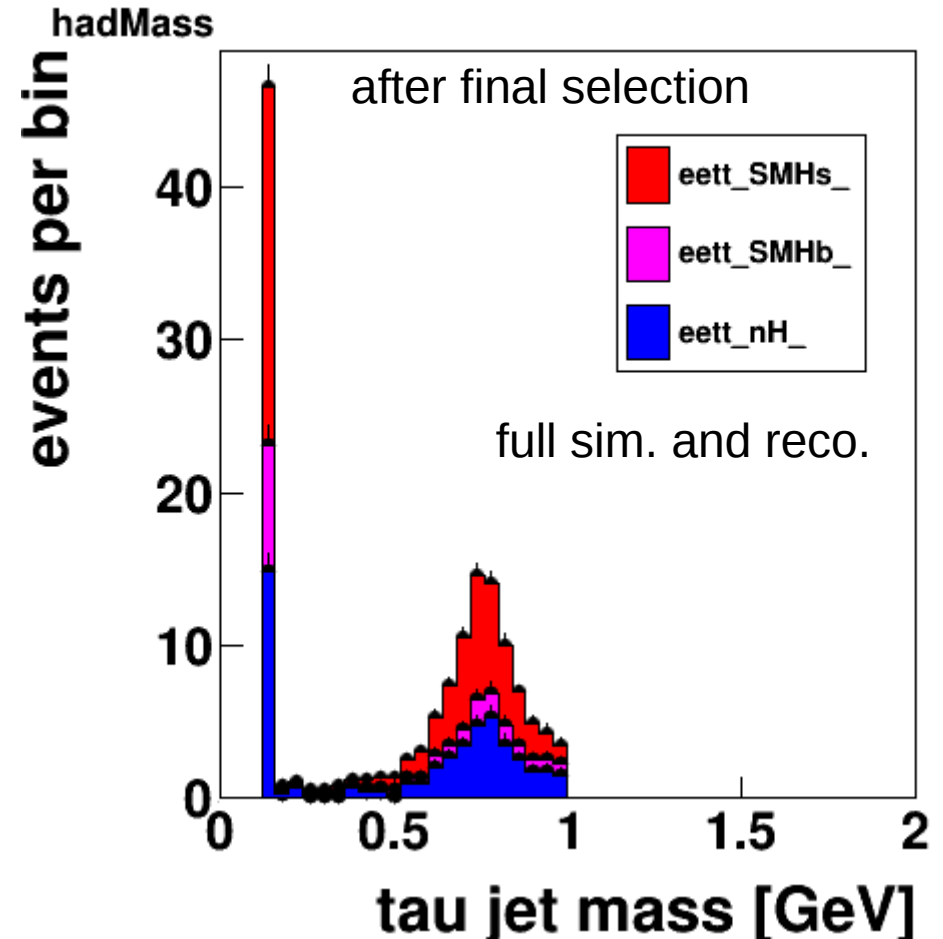
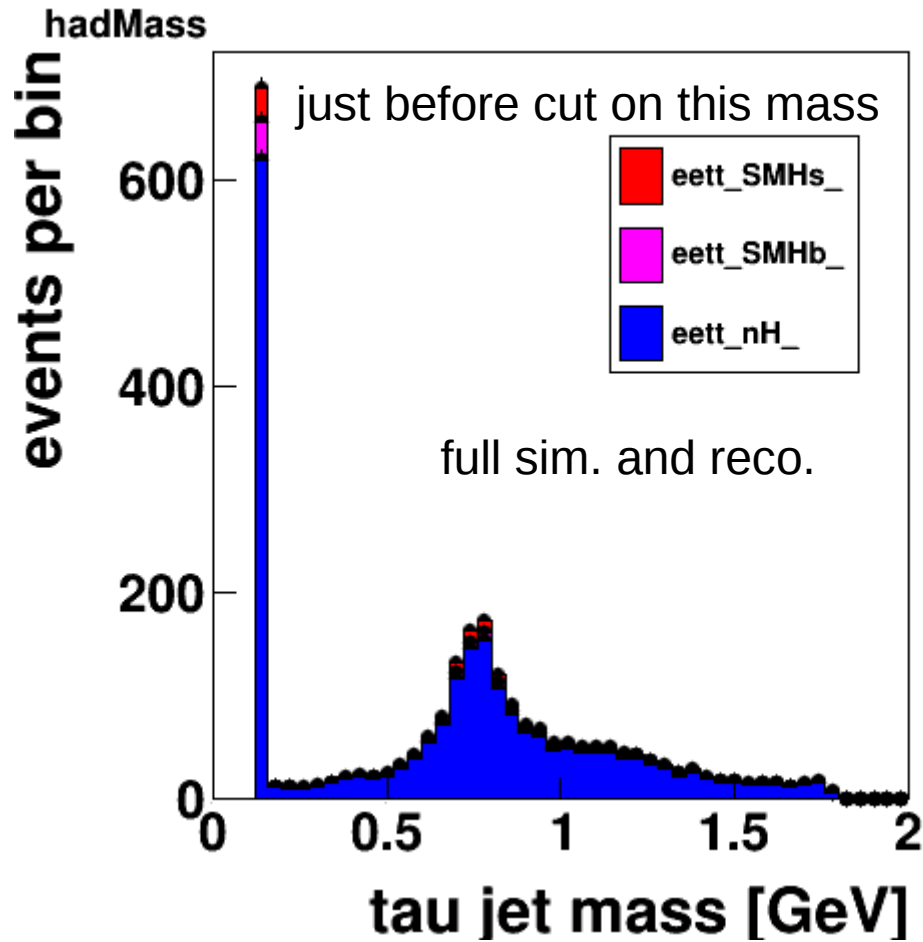


pull distribution
suspiciously large

pull

Visible mass of tau candidate jets

electron channel, 1350 fb⁻¹ @ $P(e^-,e^+) = (-0.8, +0.3)$



e e tau tau (SM Higgs, tau \rightarrow pi or rho) signal

e e tau tau (SM Higgs, other tau decay channels)

e e tau tau (non-Higgs) background