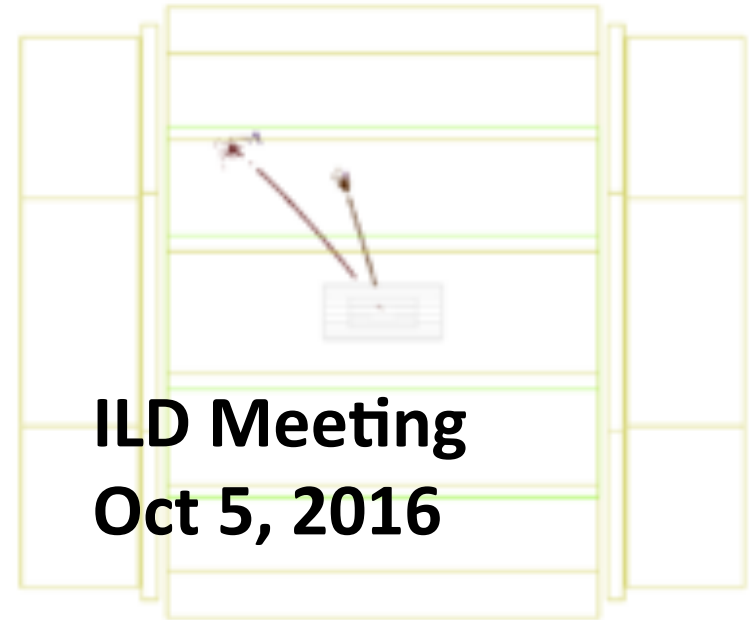
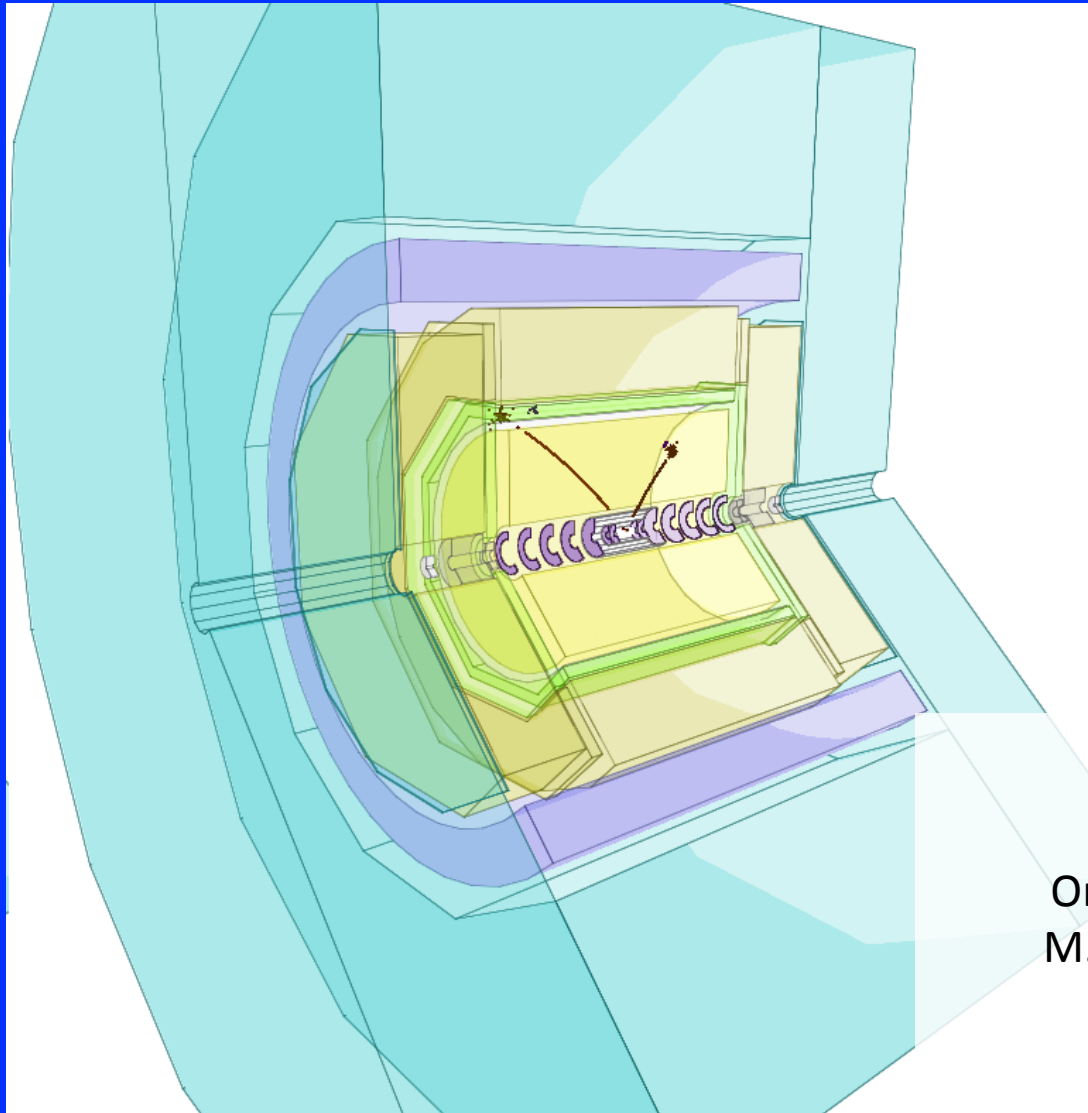


Characterizing Light Higgsinos from Natural SUSY at ILC $\sqrt{s} = 500$ GeV



**ILD Meeting
Oct 5, 2016**

Jacqueline Yan (KEK)

On behalf of H. Baer (Univ of Oklahoma),
M. Berggren, S.-L. Lehtinen, J. List (DESY),
K. Fujii (KEK), T. Tanabe (Univ of Tokyo)

Goal of Light Higgsino Study

J. Yan, T. Tanabe, K. Fujii et al

Demonstrate measurement precision of Higgsino masses and production cross sections

Serve as a basis for future discussions of ILC run scenario in the case of new particles being discovered

Results of masses and cross sections (= "observables") as input

S.-L. Lehtinen (DESY) et al

determine SUSY parameters

e.g. M_1 , M_2 , μ , $\tan\beta$

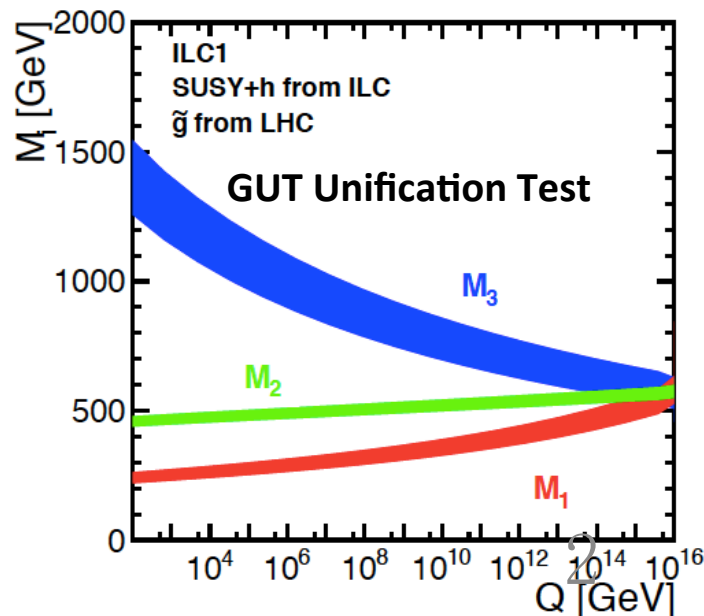
Why?

- To get info about unobserved sparticles
- To test GUT-scale models

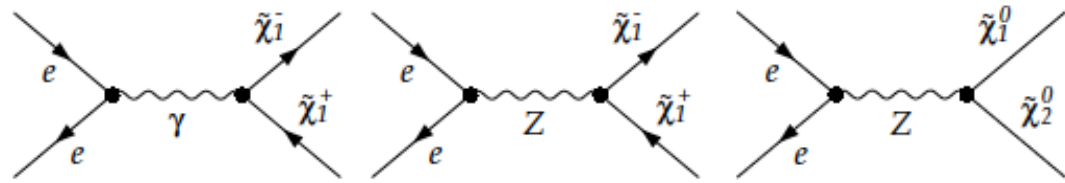
How?

- Global χ^2 fit of to observables

Study required input parameters and precisions; interplay with Higgs precision measurements



Benchmarks in this Study



RNS model (Radiatively-driven natural SUSY)

- 4 light Higgsinos: $\tilde{\chi}_1^0$ $\tilde{\chi}_2^0$ $\tilde{\chi}_1^+$ $\tilde{\chi}_1^-$ (LSP)

- ΔM about 10-20 GeV complies with naturalness (ISR tag not needed)

This study: $\sqrt{s} = 500$ GeV
Full detector simulation

NUHM2 model parameters [arXiv:1404.7510]

Benchmark	ILC1	ILC2
M_0 [GeV]	7025	5000
$M_{1/2}$ [GeV]	568.3	1200
A_0 [GeV]	-10427	-8000
$\tan\beta$	10	15
μ [GeV]	115	150
M_A [GeV]	1000	1000
$M(\chi_1^0)$ [GeV]	102.7	148.1
$M(\chi_{1^\pm})$ [GeV]	117.3	158.3
$M(\chi_2^0)$ [GeV]	124.0	157.8
$M(\chi_3^0)$ [GeV]	267.0	538.8

Currently studying ILC1 benchmark

(Pe-, Pe+)	(-1.0,+1.0)	(+1.0,-1.0)
$\sigma(\chi_1^+ \chi_1^-)$ [fb]	1800	335
$\sigma(\chi_1^0 \chi_2^0)$ [fb]	491	379

$BR(\chi_1^+ \rightarrow \chi_1^0 qq')$	67%
$BR(\chi_1^+ \rightarrow \chi_1^0 lv)$ (l=e, μ)	22%
$BR(\chi_2^0 \rightarrow \chi_1^0 qq')$	58%
$BR(\chi_2^0 \rightarrow \chi_1^0 ll)$ (l=e, μ)	7.4%

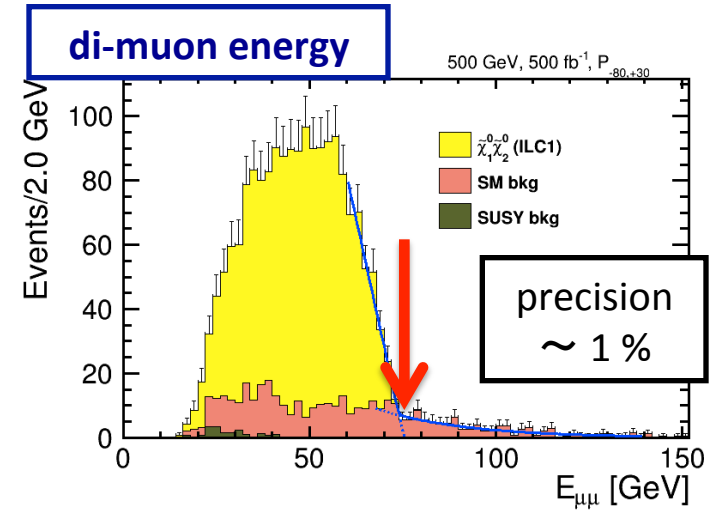
Higgs precision measurements useful for parameter determination

Defined at GUT scale
Defined at weak scale
Observables

Extraction of Higgsino Mass and Cross Section

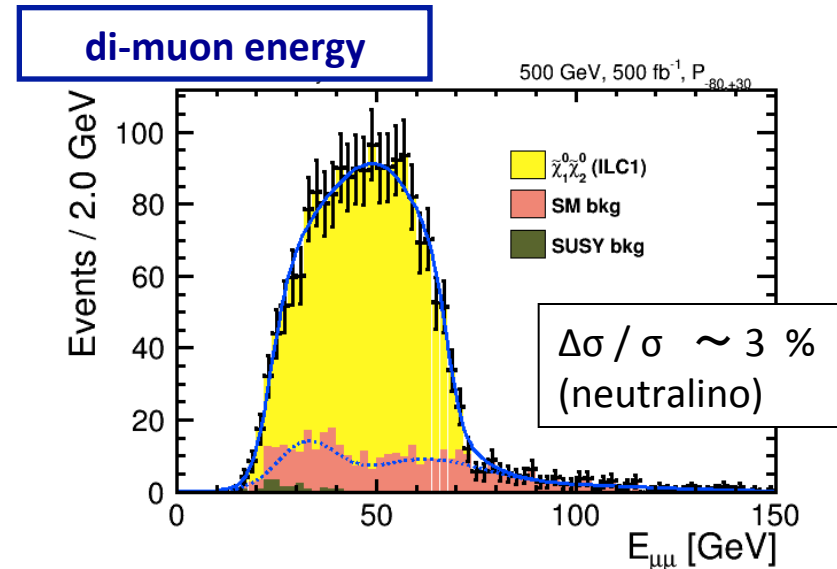
Mass :

- Kinematic edges of dilepton/dijet energy and invariant mass are functions of \sqrt{s} and Higgsino masses
- **Extract kinematic edges by a fit to distributions \rightarrow calculate masses**
(requires correction for detector resolution)



Cross section:

Count number of events under dilepton / dijet energy



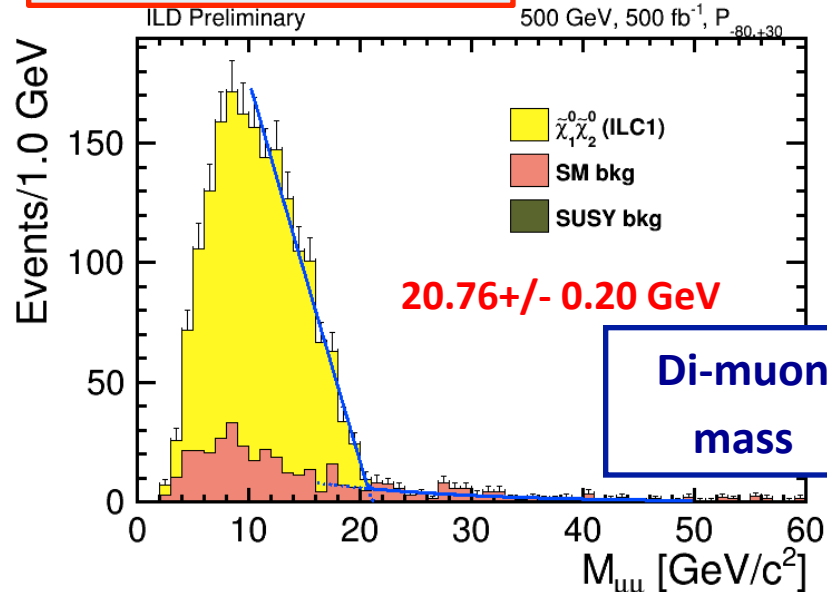
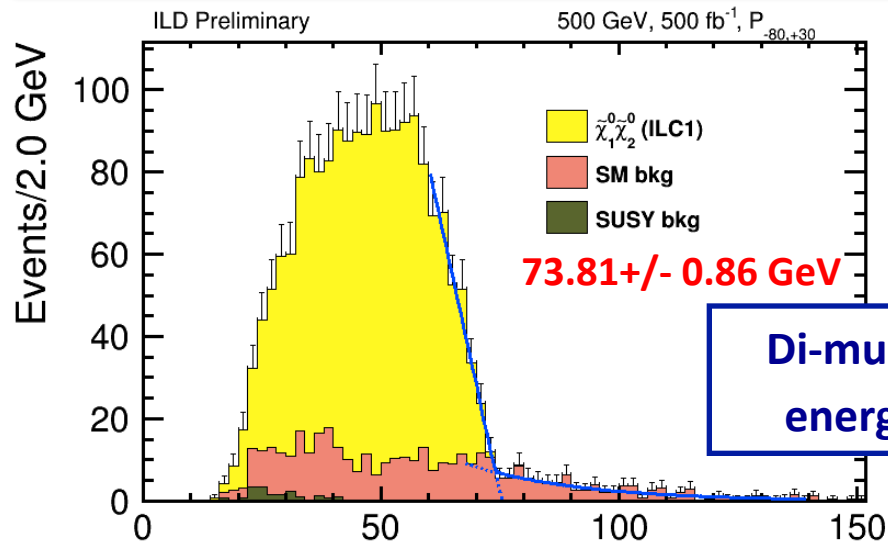
- Use Toy Monte Carlo to obtain mass and cross section precisions

Neutralino mixed production with leptonic decay

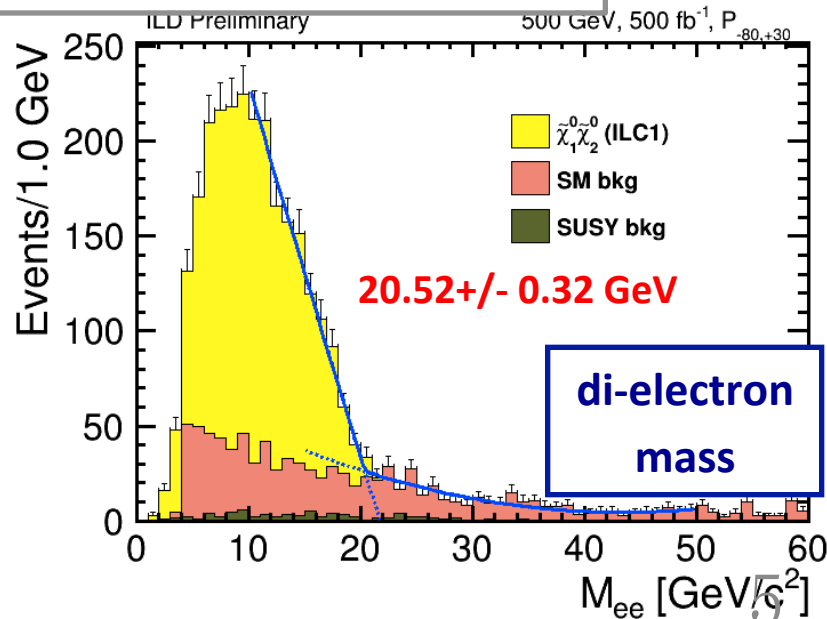
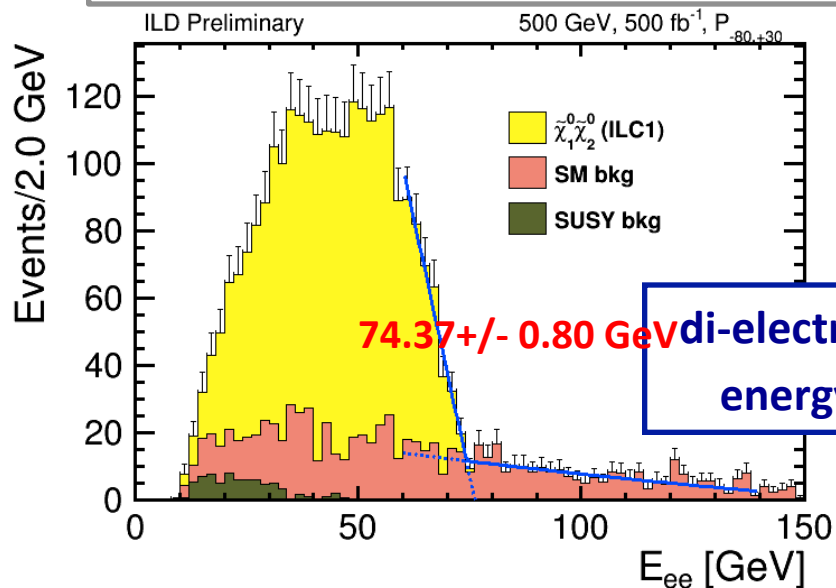
$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 l^+ l^-$$

Left Polarization (P_{e-}, P_{e+}) = (-0.8, +0.3)

Edge precision $\sim 1\%$



Theoretical values: $E_{\mu\mu}^{\text{max}} = 74.93 \text{ GeV}$ $\Delta M = 21.28 \text{ GeV}$

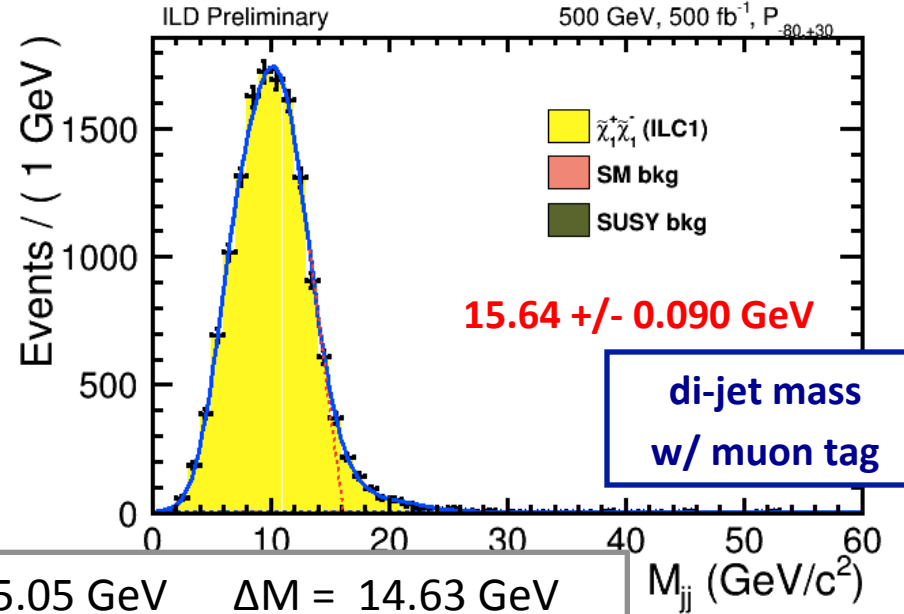
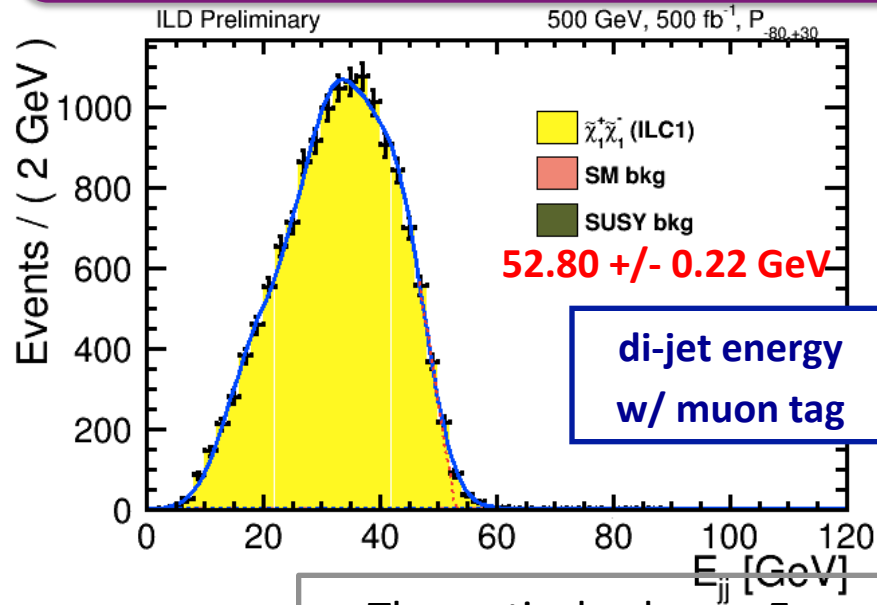


Chargino pair production with semileptonic decay

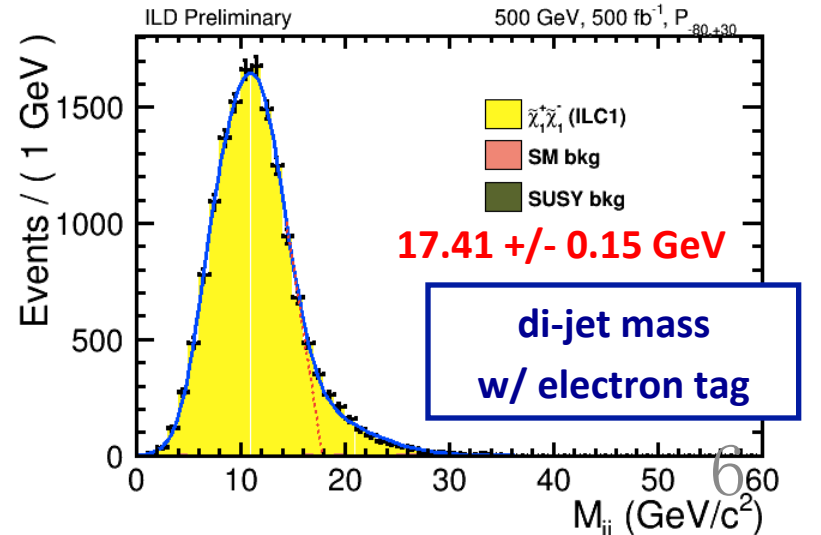
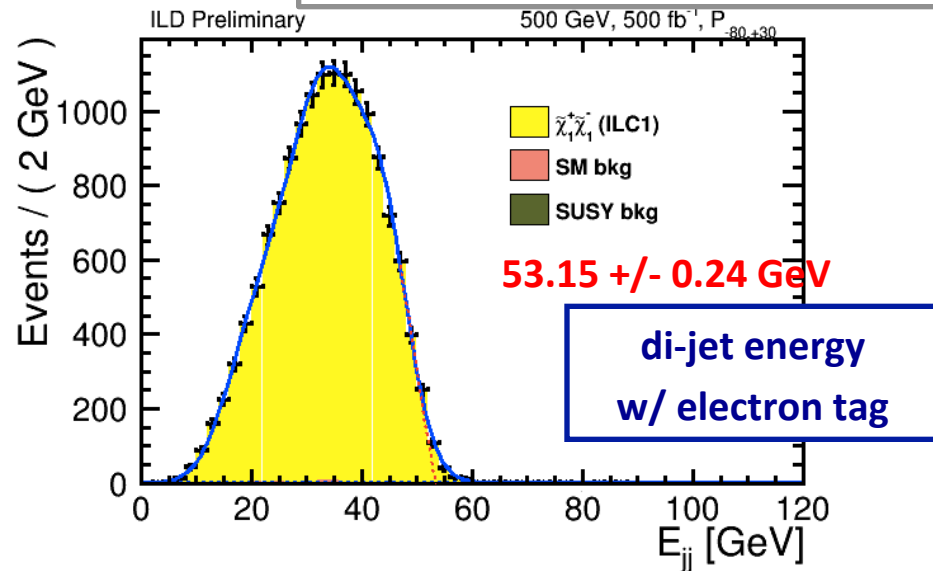
$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q q' \ell \nu$$

Left Polarization (Pe-,Pe+) = (-0.8, +0.3)

Almost all bkg rejected

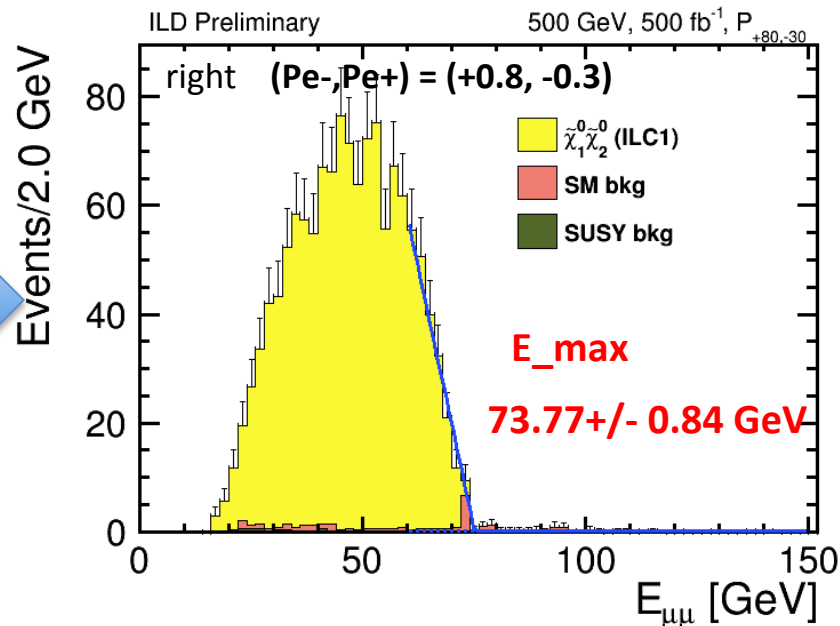
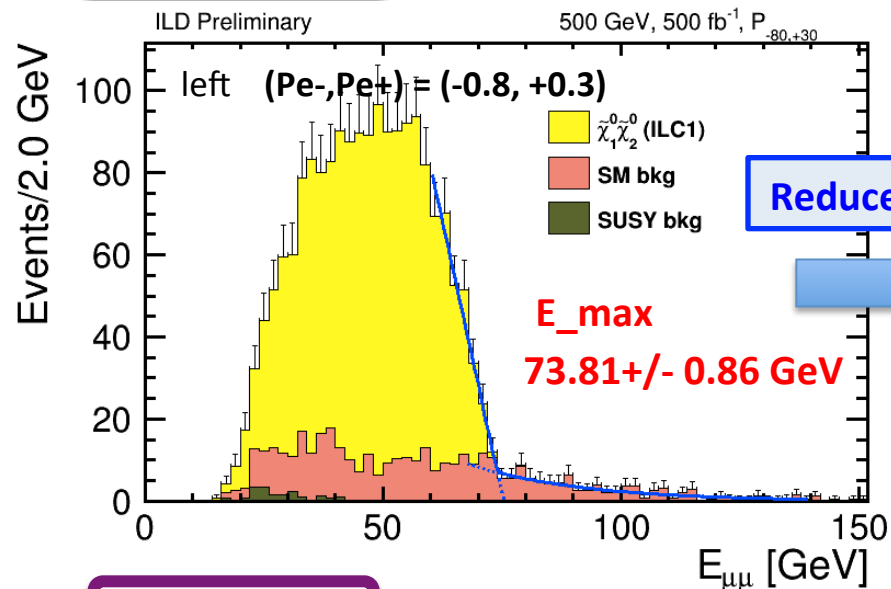


Theoretical values: $E_{max} = 55.05$ GeV $\Delta M = 14.63$ GeV

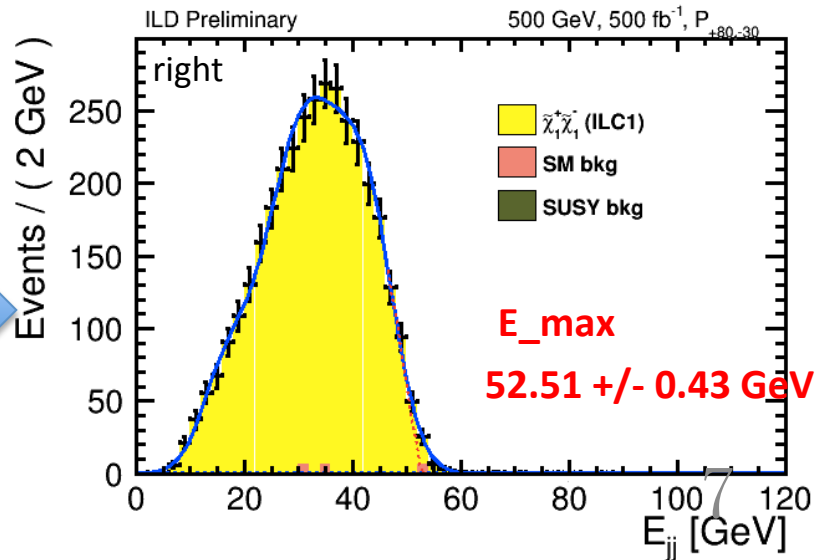
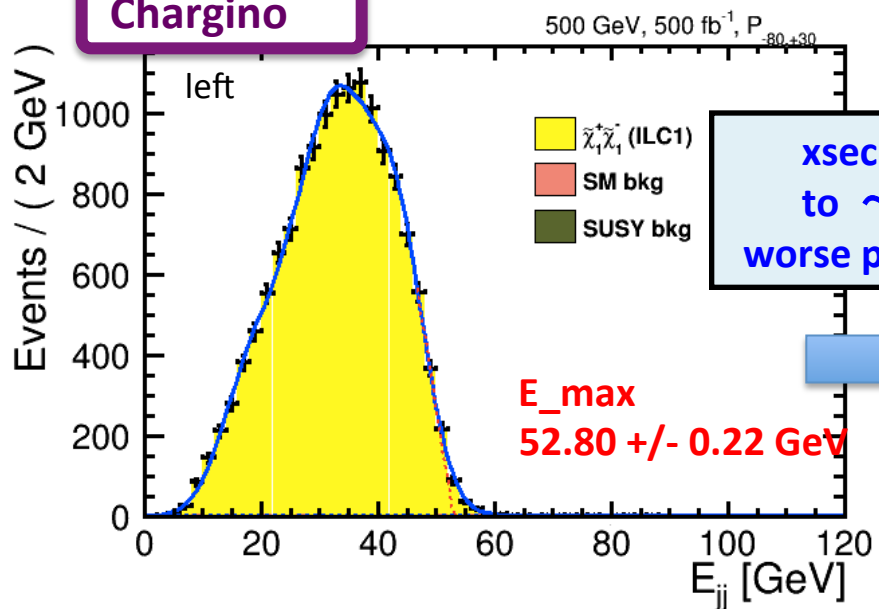


Left polarization vs right polarization

Neutralino



Chargino



Higgsino Mass Precisions (combined)

apply χ^2 fit to “observables” (kinematic edges)

(E_{ll_max} , E_{jj_max} , M_{ll_max} , M_{jj_max} are functions of Higgsino masses)

Neutralino

4 channels (mm, ee, left, right)

N1N2	MN1	$\Delta MN1/MN1$	MN2	$\Delta MN2/MN2$
	102.54	0.758%	123.36	0.688%
H20		0.424%		0.385%

Scale results to H20

For each polarization:

- Default : 500 fb⁻¹
- H20: 1600 fb⁻¹

Chargino

4 channels (m tag, e tag, left, right)

C1C1	MN1	$\Delta MN1/MN1$	MC1	$\Delta MC1/MC1$
	116.60	0.447%	132.79	0.435%
H20		0.250%		0.243%

8 channels (m, e, left, right, N1N2, C1C1)

ALL	MN1	$\Delta MN1/MN1$	MN2	$\Delta MN2/MN2$	MC1	$\Delta MC1/MC1$
	110.56	0.405%	130.90	0.372%	126.09	0.396%
H20		0.226%		0.208%		0.221%

Theoretic values: MN1 = 102.70 GeV MN2 = 123.98 GeV, MC1 = 117.33 GeV

MN1: χ^0_1 mass MN2: χ^0_2 mass MC1: χ^\pm_1 mass

- combined statistical mass precision $\sim 0.2\%$ (H20)
- Dominated by precision of chargino channel (higher cross section)
- Neutralino results consistent with theoretic values
- Chargino results deviated due to jet energy resolution

H20		0.424%	4 channels (m tag, e tag, left, right)		0.385%	H20: 1600 fb ⁻¹	
Chargino							
C1C1	MN1	$\Delta MN1/MN1$	MC1	$\Delta MC1/MC1$			
	116.60	0.447%	132.79	0.435%			
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ALL							
		$\Delta MN1/MN1$	MN2	$\Delta MN2/MN2$	MC1	$\Delta MC1/MC1$	
		0.405%	130.90	0.372%	126.09	0.396%	
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Theoretic values: MN1 = 102.70 GeV MN2 = 123.98 GeV, MC1 = 117.33 GeV

MN1: χ^0_1 mass MN2: χ^0_2 mass MC1: χ^\pm_1 mass

Cross section precisions

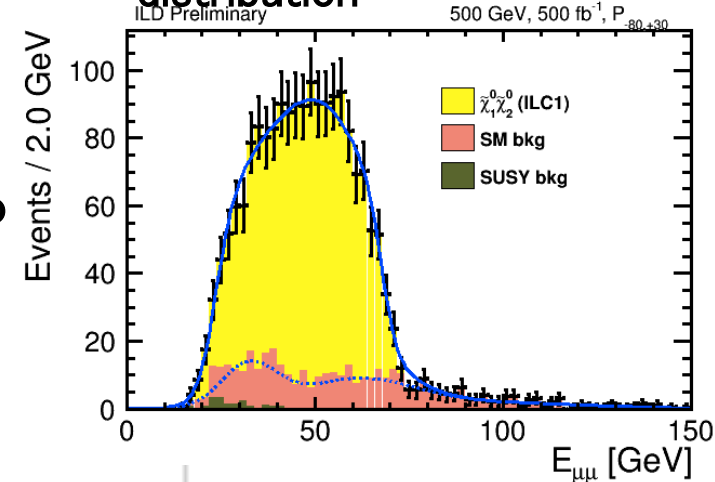
- Neutralino (N1N2): 1 –1.5% (H20)

right polarization has better precision due to suppressed BKG

- Chargino (C1C1) : 0.3–0.7% (H20)

scales with size of cross section

Count # of events under distribution



N1N2	$\Delta \sigma / \sigma$	C1C1	$\Delta \sigma / \sigma$
left, mumu	3.49%	left, mu-tag	0.85%
left, ee	3.17%	left, e-tag	0.83%
combined	2.35%	combined	0.59%
H20	1.31%	H20	0.33%
N1N2	$\Delta \sigma / \sigma$	C1C1	$\Delta \sigma / \sigma$
right mumu	2.80%	right mu-tag	1.75%
right ee	2.41%	right e-tag	1.71%
combined	1.83%	combined	1.22%
H20	1.02%	H20	0.68%

Summary for Light Higgsino Study

Precision measurement of light Higgsinos with small ΔM (10-20 GeV)

- Motivated by both experiment (complementary to LHC) and theory (naturalness)

This study: Full ILD detector simulation

L=500 fb⁻¹ at $\sqrt{s} = 500$ GeV, (Pe-, Pe+) = (-0.8,+0.3),(+0.8, -0.3)

- Analysis of **neutralino mixed production** ($\chi_1^0 \chi_2^0$) and **chargino pair production** ($\chi_1^+ \chi_1^-$)
- Data selection yields good S/B ratio ; almost no background for chargino
- **Fit kinematic edges to extract Higgsino masses**
- **Fit to overall distribution to extract production cross sections**

Obtained results for ALL channels

- **Mass precision $\sim 0.2\%$**
- **Cross section precision:**
neutralino: 1 – 1.5%
chargino: 0.3 – 0.7%

(from full H20 run, three \sqrt{s})

**results obtained in this study become
input to SUSY parameter determination**

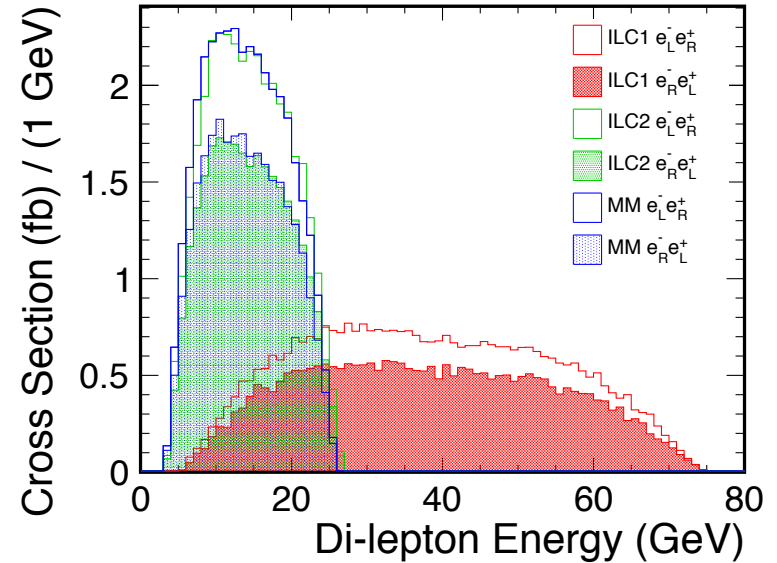
To extract other SUSY parameters, test GUT-scale physics and SUSY-breaking mechanism

$$\begin{aligned}\Delta M_1 &= 1.5\% \\ \Delta M_2 &= 1.0\% \\ \Delta M_3 &= 11.6\% \\ \Delta \mu &= 0.1\% \\ \Delta \tan \beta &= 2.5\%\end{aligned}$$

Plans for Higgsino Studies

- Analyze more challenging benchmarks with smaller ΔM
 → compare precision of SUSY parameter extraction
- Summarize the results of this analysis in document
- First draft for section on Higgsino is done
- Move towards publication

$$e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0, \quad \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0\ell^+\ell^-$$



Event Generator: WHIZARD v1.95 (DBD setup)
 Cross sections for $\sqrt{s}=500$ GeV with TDR beam parameters

	ILC1	ILC2	mirage12_15
ch1ch1.eL.pR	1799.9 fb	1530.5 fb	1536.6 fb
ch1ch1.eR.pL	334.5 fb	307.2 fb	308.0 fb
neu1neu2.eL.pR	490.9 fb	458.9 fb	460.6 fb
neu1neu2.eR.pL	378.5 fb	353.8 fb	355.1 fb

Additional Material

Motivation for Searching Light Higgsinos with Small ΔM

❖ From experimental point of view:

- LHC already excluded large regions with large $\Delta M = M(\text{NLSP}) - M(\text{LSP})$
- Remaining region with compressed spectrum very small visible energy release, near impossible to probe at LHC
→ ILC is essential

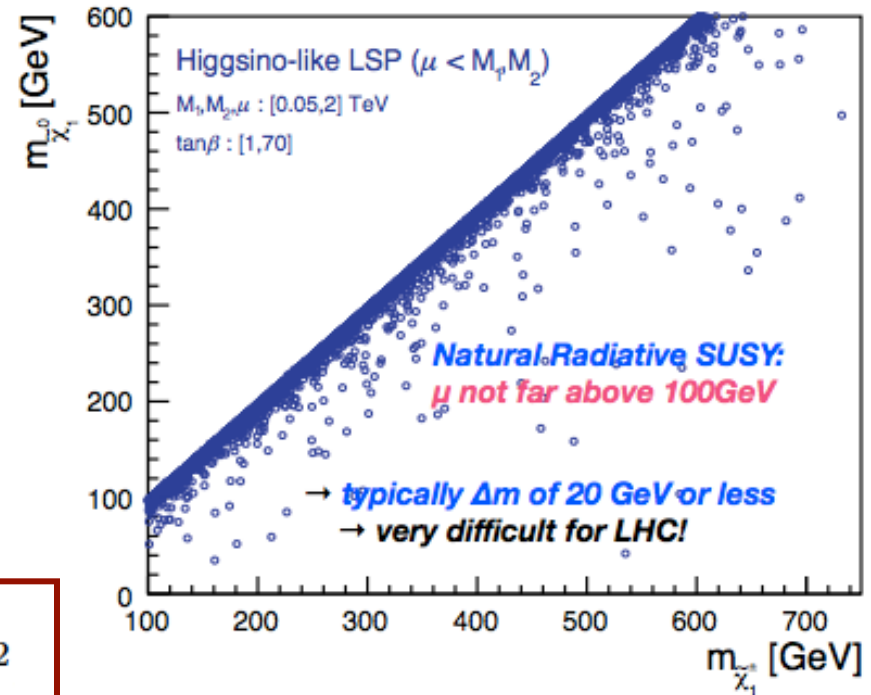
❖ From theoretical point of view:

Compressed Higgsino spectra related to naturalness [e.g. arXiv:1212.2655, arXiv:1404.7510]

$$\frac{M_Z^2}{2} = \frac{m_{H_d}^2 + \sum_d^d - (m_{H_u}^2 + \sum_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2$$

- To maintain **small electroweak fine tuning ΔEW ($< \sim 3\%$)**, all contributions on right-hand-side should be comparable to $M(Z)$ **→ requires $\mu \sim 100\text{--}300$ GeV**
 top and bottom squarks in the few TeV regime, gluino mass 2–4 TeV,
 1st, 2nd generation squarks and sleptons in the 5–30 TeV regime

- μ feeds mass to both SM (W, Z, h) and SUSY particles (Higgsinos)
- Higgsino masses not too far from masses of W, Z, h (~ 100 GeV)



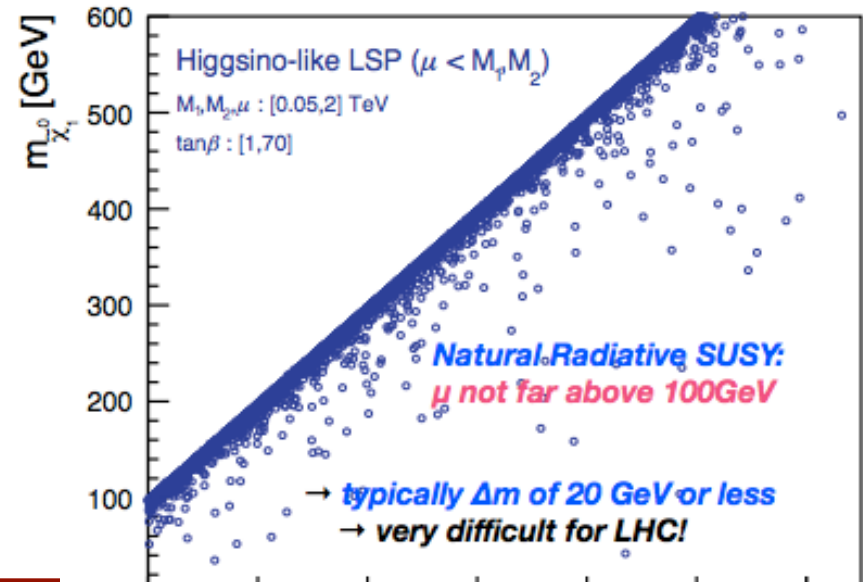
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→ **ILC is essential**

❖ From theoretical point of view:

Compressed Higgsino spectra related to naturalness [e.g. arXiv:1212.2655, arXiv:1404.7510]



If SUSY particles exist at all,
they may be in a region
only accessible by the ILC (?)

How do these signals look in the detector? (1)

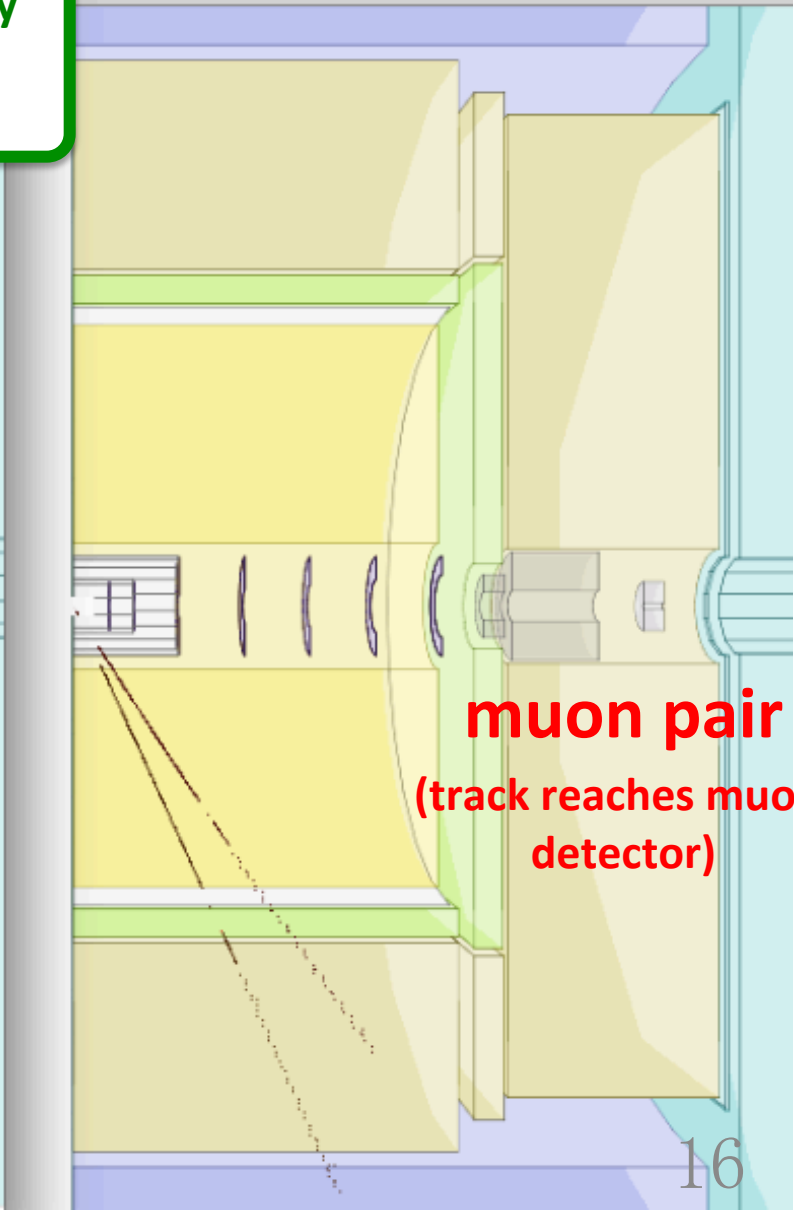
$\sqrt{s} = 500 \text{ GeV}$

Neutralino mixed production with leptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$



electron pair
(compact EM showers)



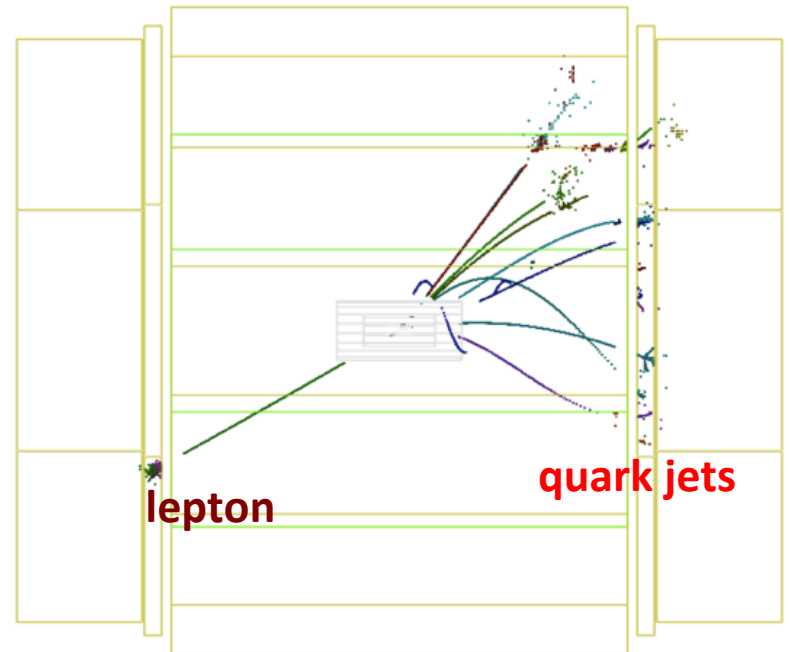
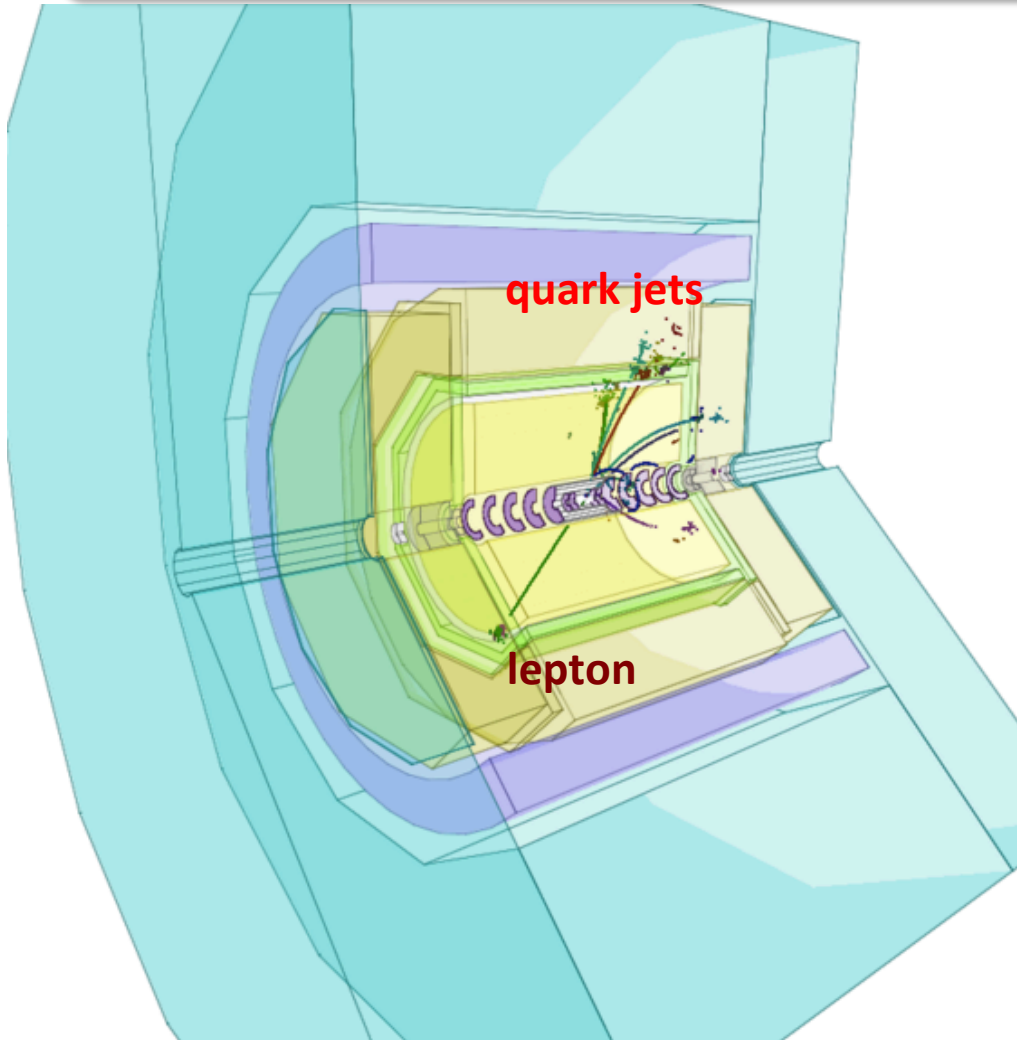
muon pair
(track reaches muon detector)

How do these signals look in the detector? (2)

$\sqrt{s} = 500 \text{ GeV}$

Chargino pair production with semileptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q q' \ell \nu$$



Event Selection

Neutralino mixed production with leptonic decay

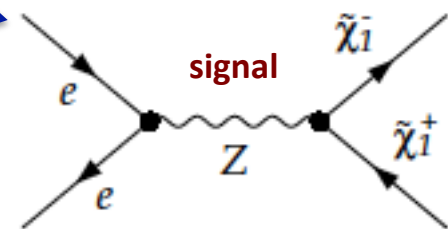
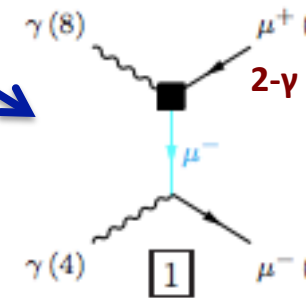
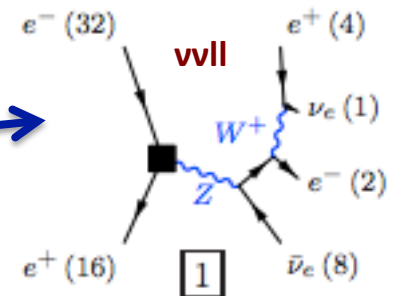
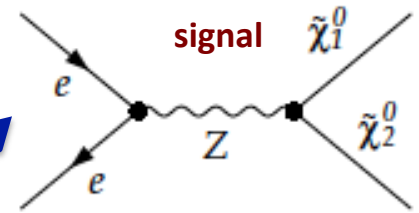
$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

- Reconstruct **two leptons (ee or $\mu\mu$)** which originate from **Z^* emission in decay of $\tilde{\chi}_2^0$ to $\tilde{\chi}_1^0$**
- Major residual bkg. are 4f processes accompanied by large missing energy (vll)
- 2- γ processes are removed by BeamCal veto, cuts on lepton track p_T , and coplanarity

Chargino pair production with semileptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qq' \ell \nu$$

- Reconstruct **two jets which originate from W^* emission in decay of $\tilde{\chi}_1^\pm$ to $\tilde{\chi}_1^0$**
- Use lepton (e or μ) from the other chargino as tag
- BeamCal veto, cuts on missing p_T , # of tracks, # of leptons, and coplanarity remove almost all bkg.



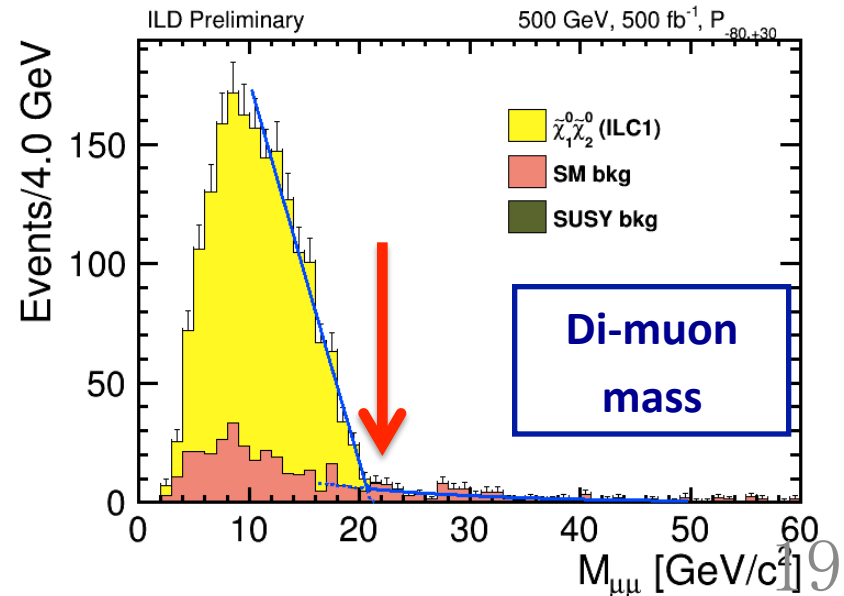
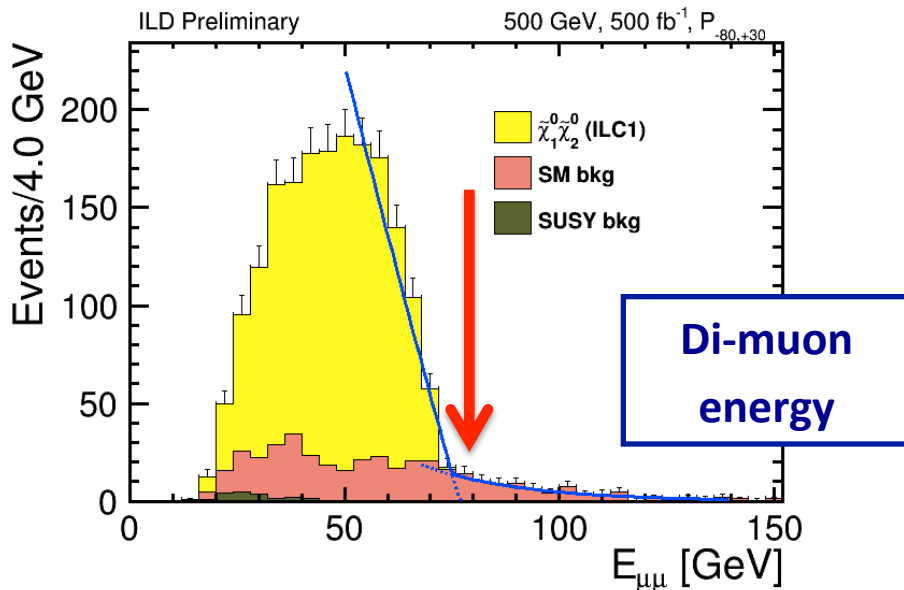
Extraction of Higgsino Mass

Neutralino mixed production with leptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$

- The position of the kinematic edges of the dilepton energy (E_{ll}) and invariant mass (M_{ll}) are functions of CM energy and the two neutralino masses.
- $E_{ll,max}$ and $M_{ll,max}$ are extracted by a fit to obtain the neutralino masses
 need correction for detector/reconstruction effects

Similar for case of chargino pair production ($ll \rightarrow jj$)



Cuts have been designed so as not to destroy upper edge

- Use toy MC (generated from MC data fit) to evaluate statistical uncertainty

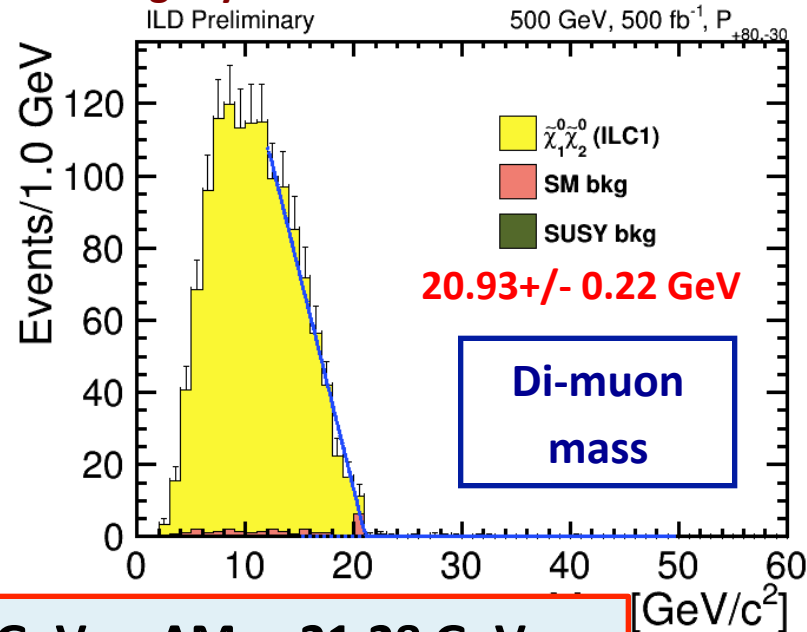
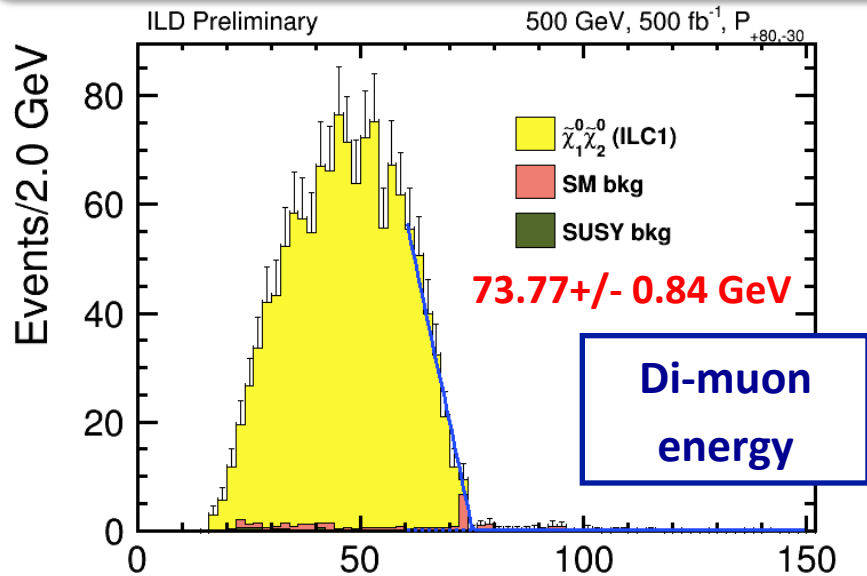
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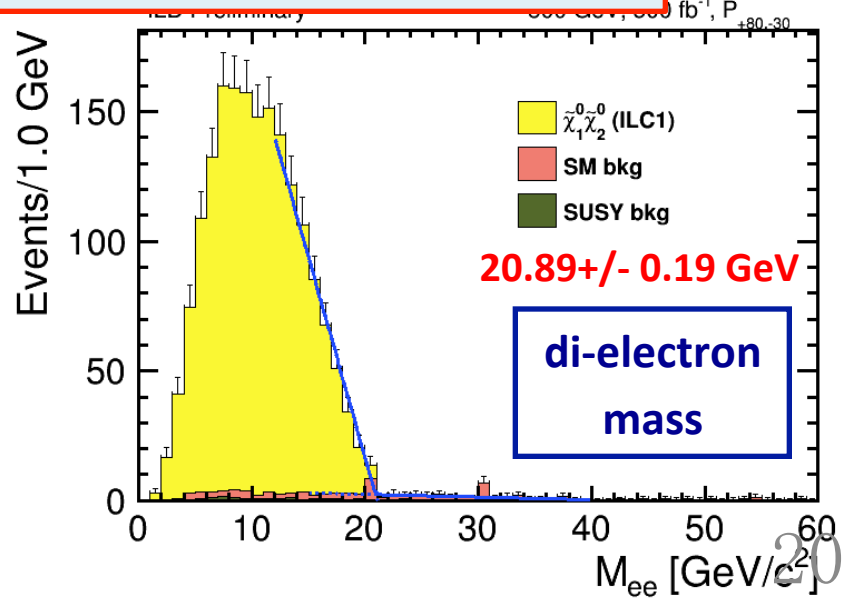
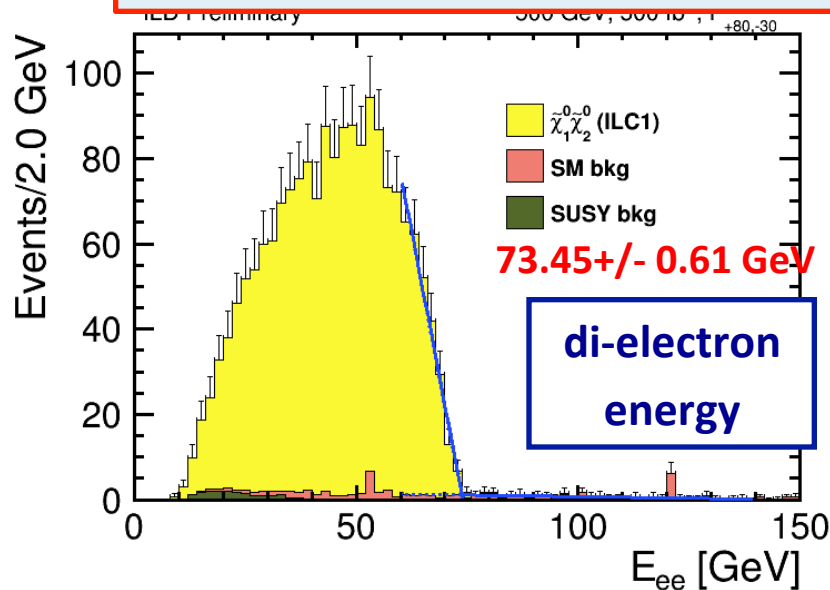
Right Polarization (Pe-,Pe+) = (+0.8, -0.3)

Much less bkg
Precision slightly better

Edge precision < ~ 1%



Theoretical values: E_{max} = 74.93 GeV ΔM = 21.28 GeV

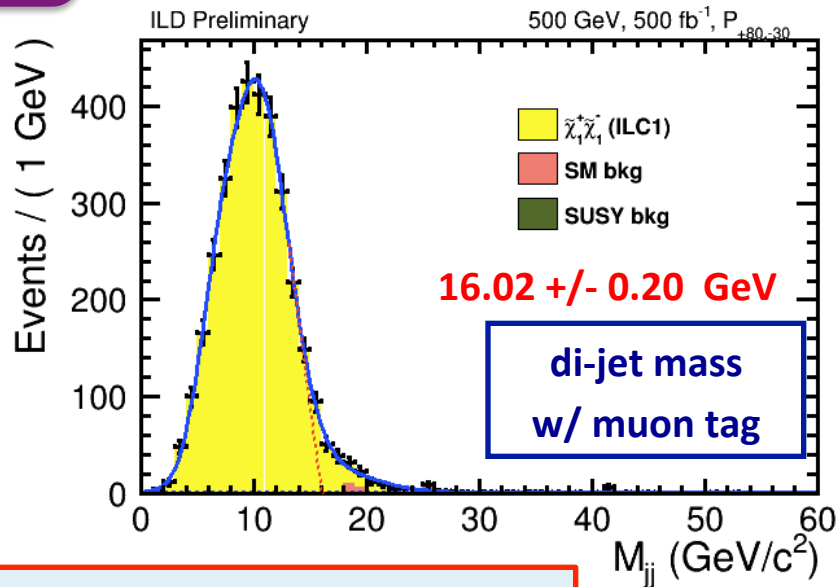
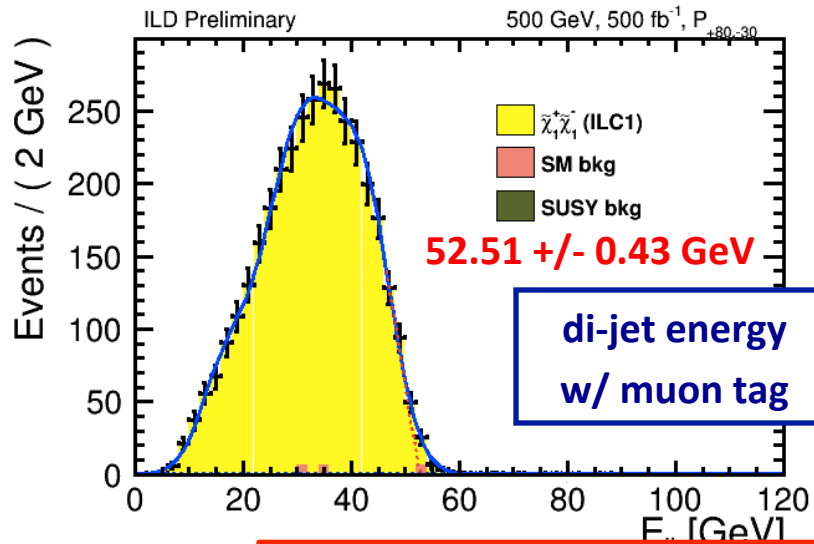


Chargino pair production with semileptonic decay

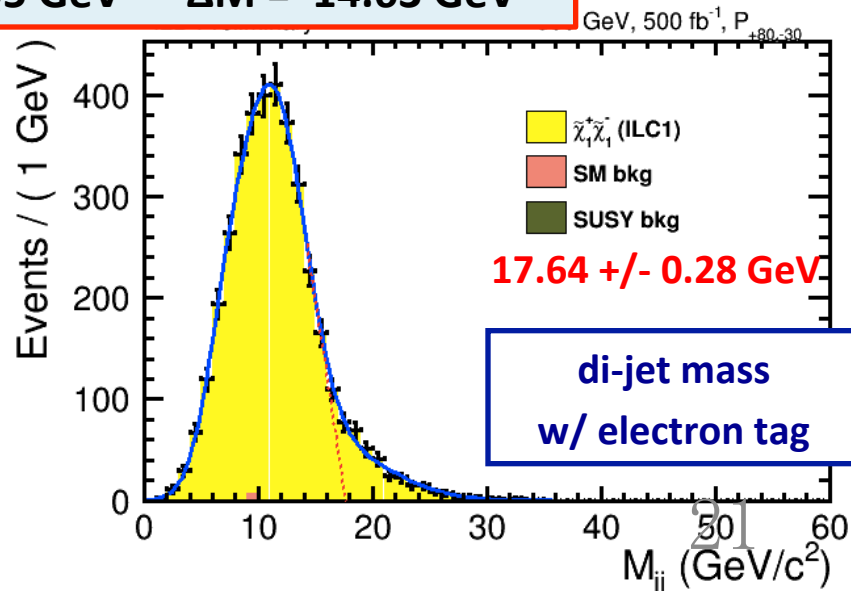
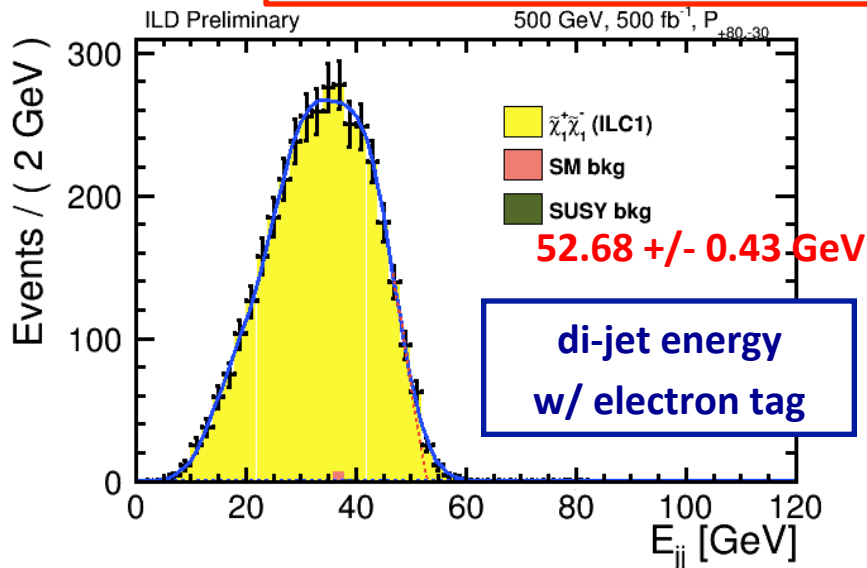
$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qq' \ell \nu$$

right Polarization (P_{e^-}, P_{e^+}) = (+0.8, -0.3)

Cross section $\sim 1/5$ of left polarization



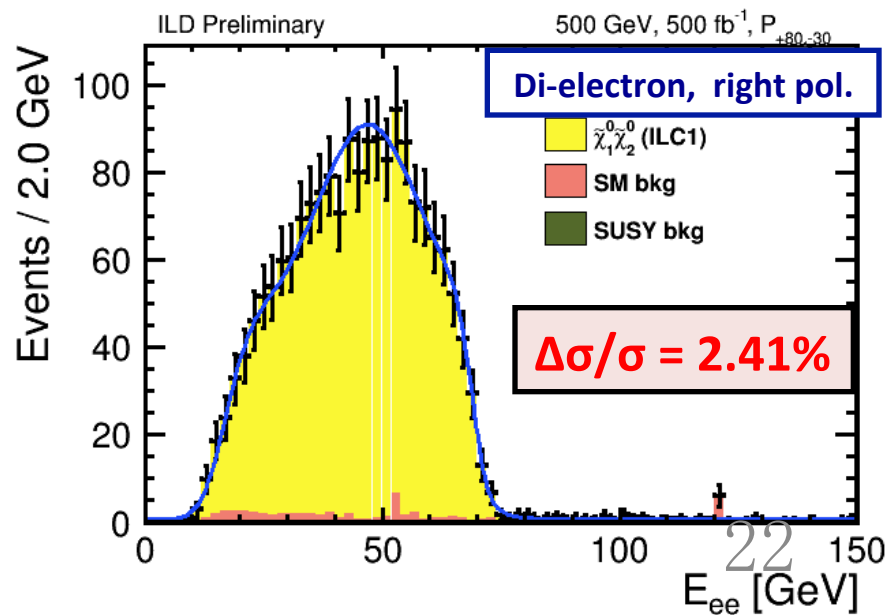
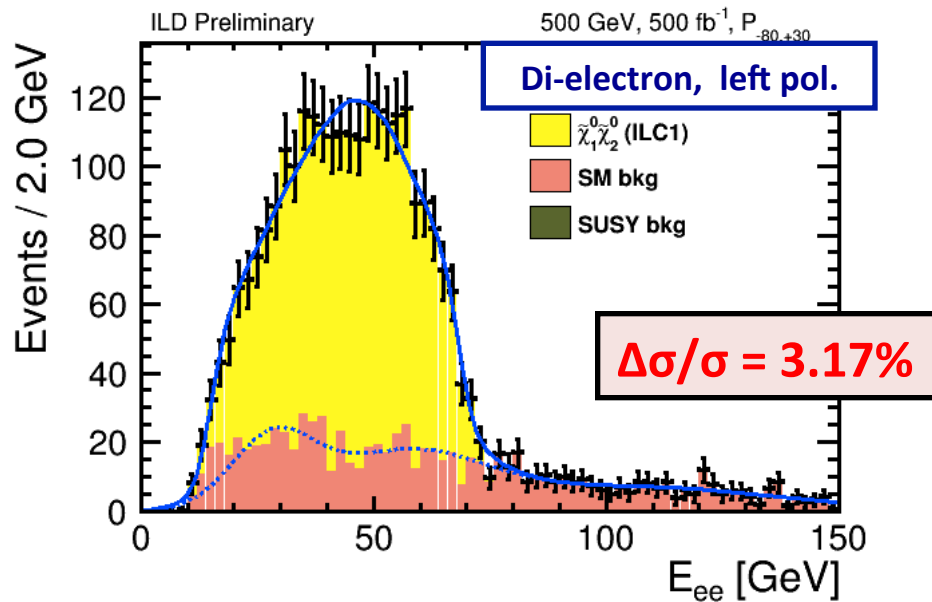
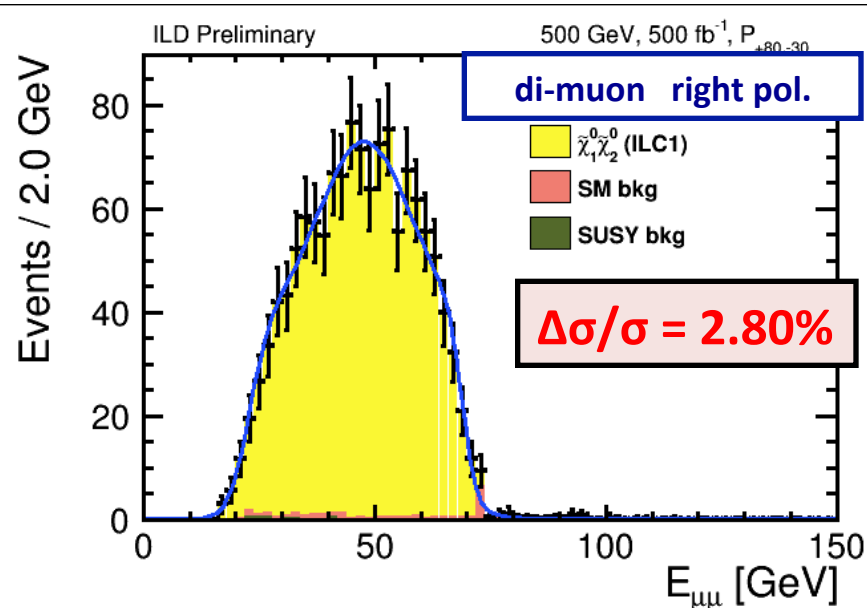
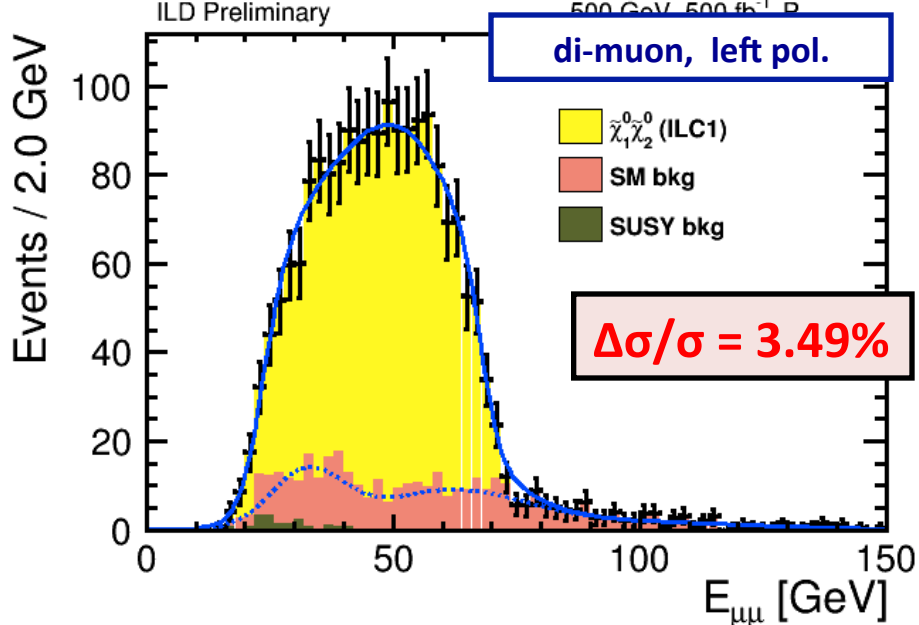
Theoretical values: $E_{max} = 55.05$ GeV $\Delta M = 14.63$ GeV



Extraction of Cross Section

Uncertainty of right pol is about 3 / 4 of left pol
dependent on statistics (evaluated using Toy MC)

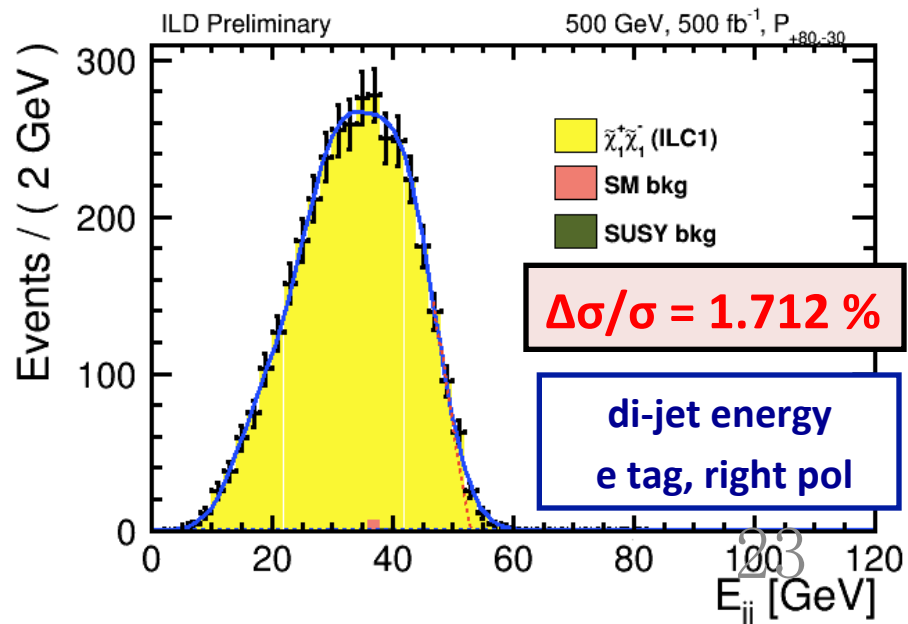
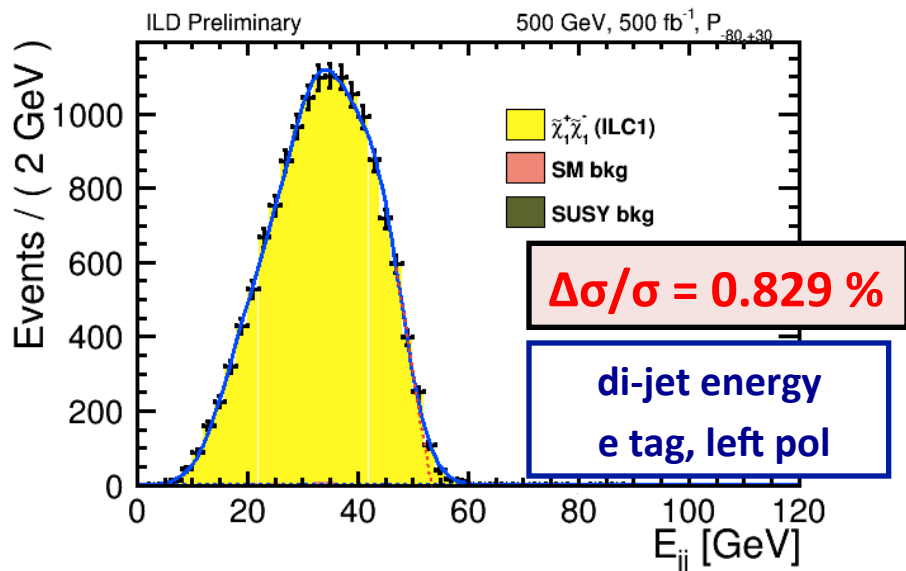
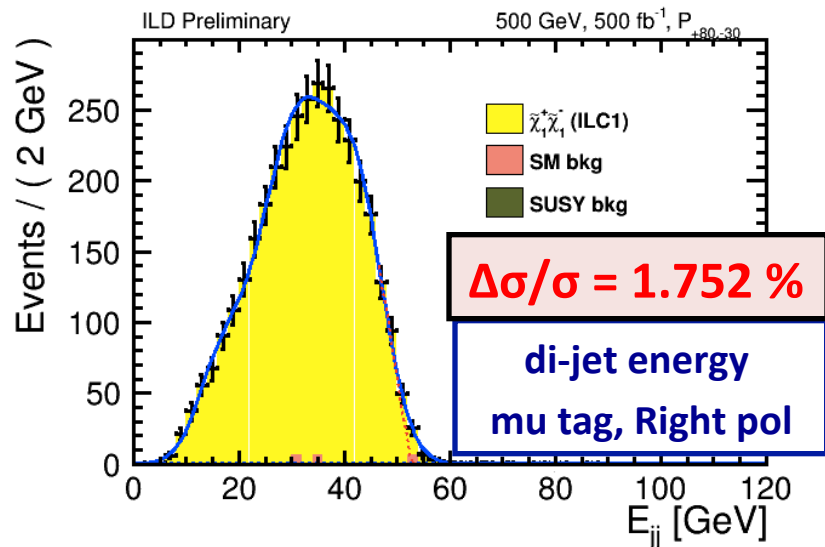
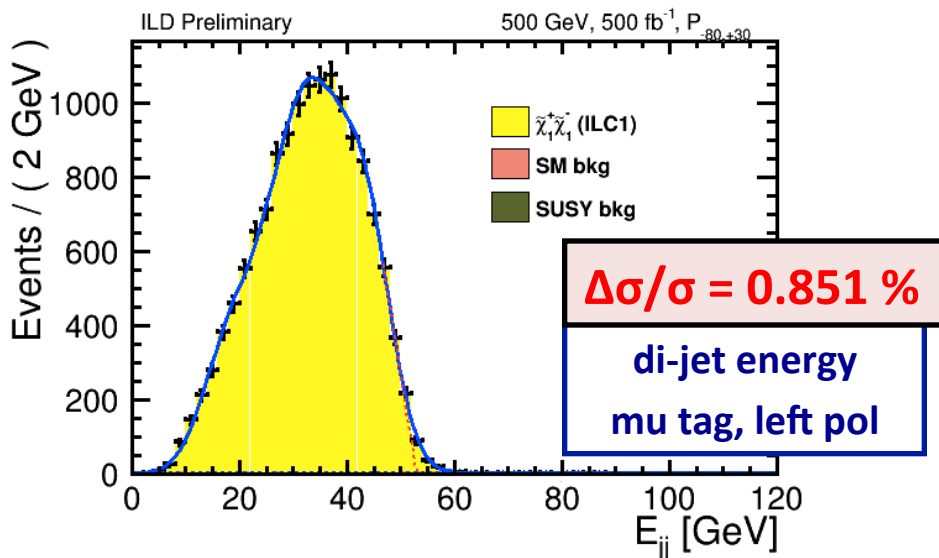
N1N2



Extraction of Cross Section

C1C1

- Left pol has x2 better precision
- dependent on statistics



Mass Precisions (individual channels)

$\sqrt{s} = 500 \text{ GeV}$

Convert precisions of kinematic edges to those of Higgsino masses

$L = 500 \text{ fb}^{-1}$

MN1: χ^0_1 mass

MN2: χ^0_2 mass

MC1: χ^\pm_1 mass

Neutralino: 1 – 2%

polarization		MN1	MN2	ΔMN1	$\Delta \text{MN1}/\text{MN1}$	ΔMN2	$\Delta \text{MN2}/\text{MN2}$
left	mm	102.26	123.02	1.77	1.7%	1.76	1.4%
left	ee	100.30	120.81	2.17	2.2%	2.15	1.8%
right	mm	103.06	123.99	1.82	1.8%	1.81	1.5%
right	ee	103.41	124.30	1.44	1.4%	1.43	1.1%

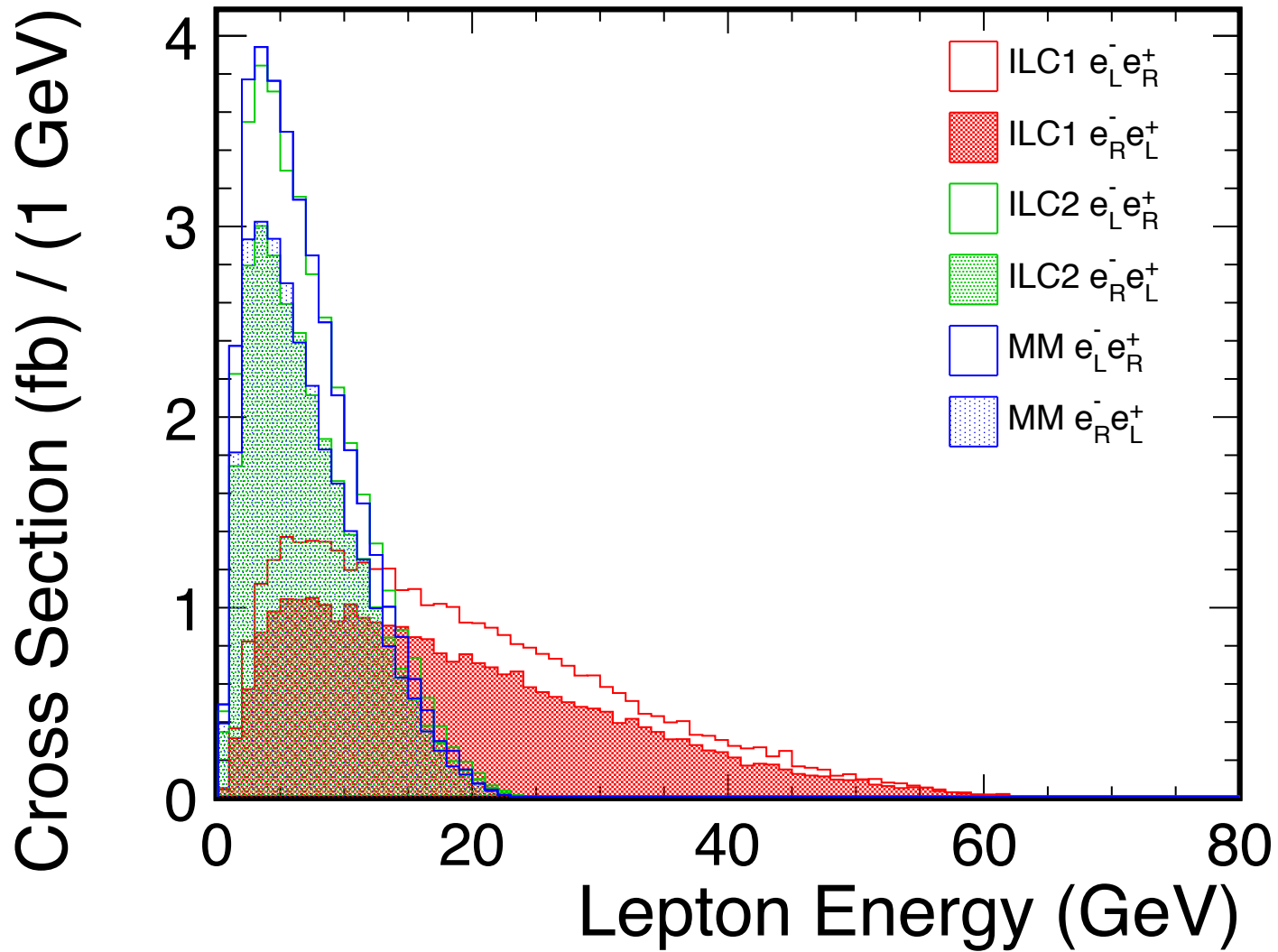
Chargino: left pol is better than 1%

~ 2 times better than right pol

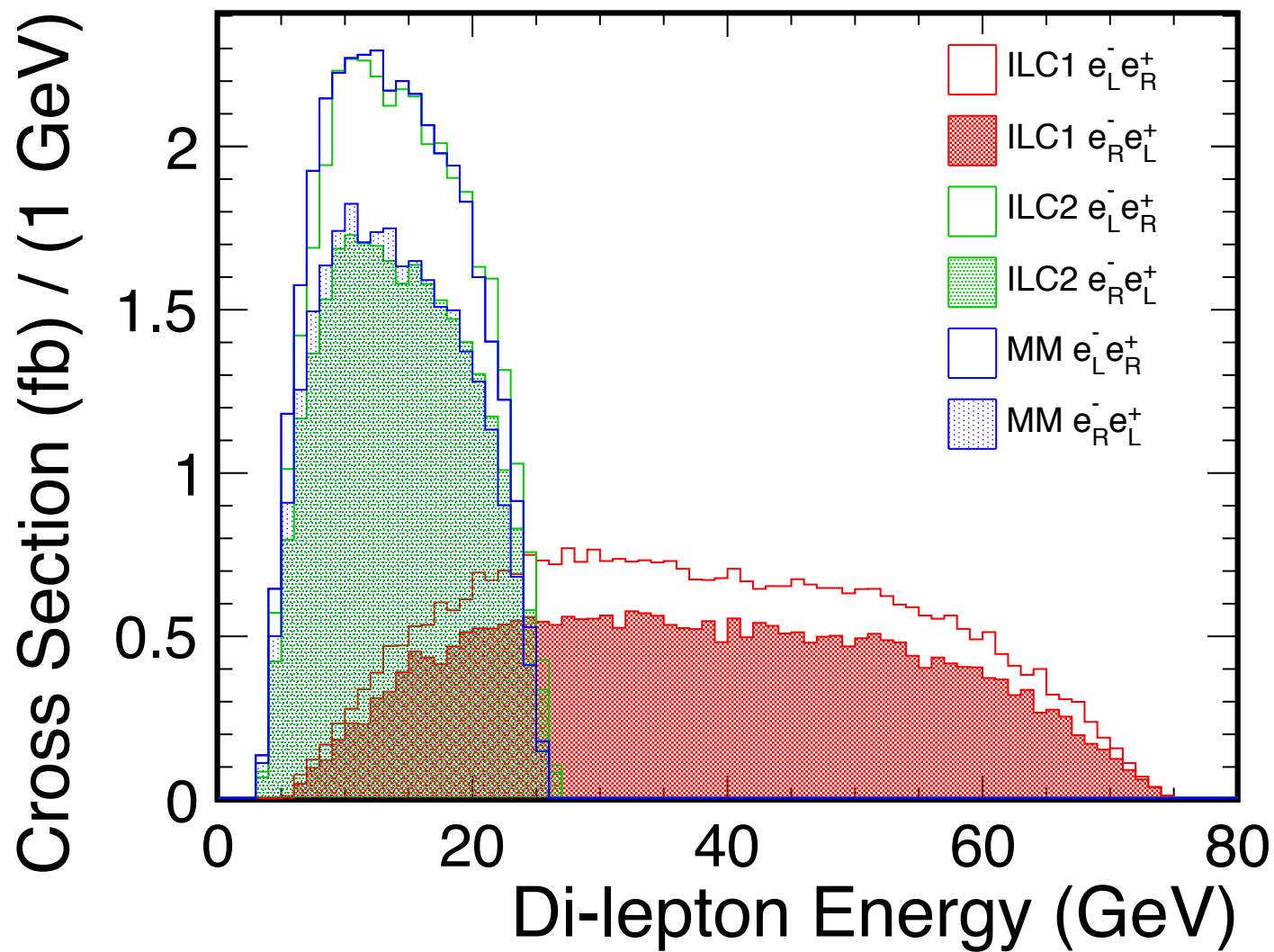
polarization		MN1	MC1	ΔMN1	$\Delta \text{MN1}/\text{MN1}$	ΔMC1	$\Delta \text{MC1}/\text{MC1}$
left	mu tag	113.50	129.14	0.82	0.7%	0.82	0.6%
left	e tag	122.96	140.37	1.19	1.0%	1.18	0.8%
right	mu tag	116.42	132.44	1.76	1.5%	1.75	1.3%
right	e tag	125.34	142.98	2.20	1.8%	2.18	1.5%

Theoretic values MN1 = 102.70 GeV MN2 = 123.98 GeV, MC1 = 117.33 GeV

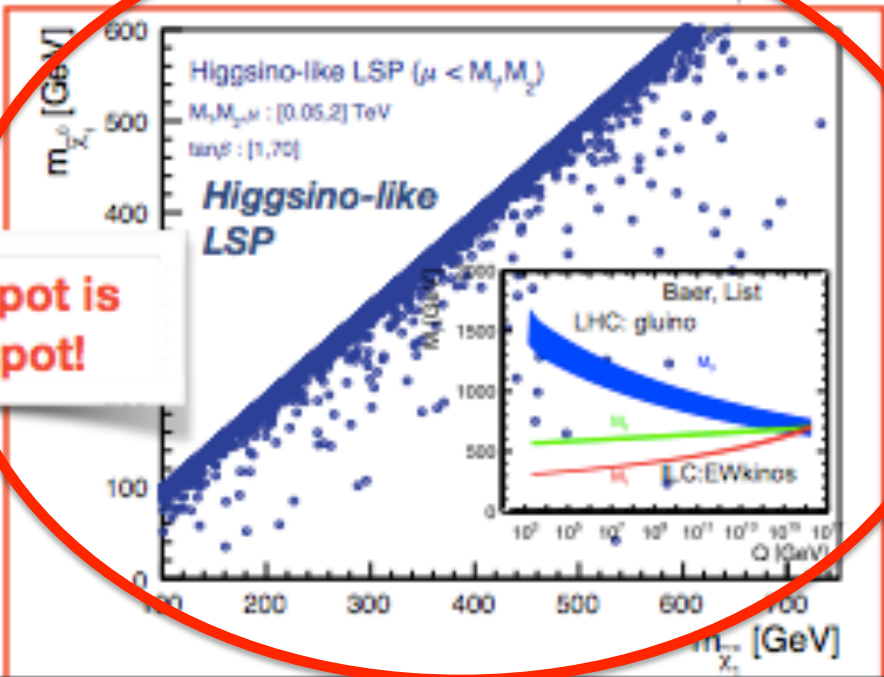
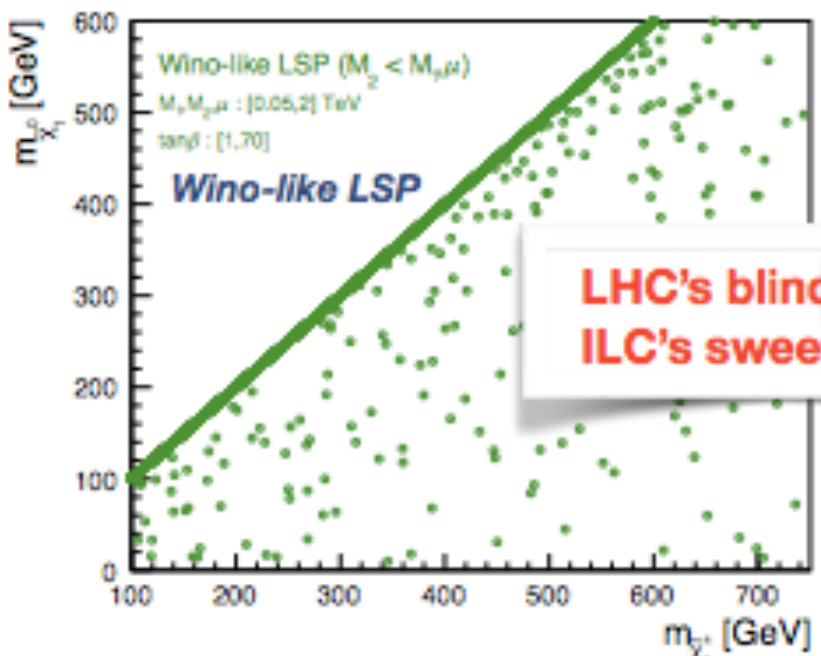
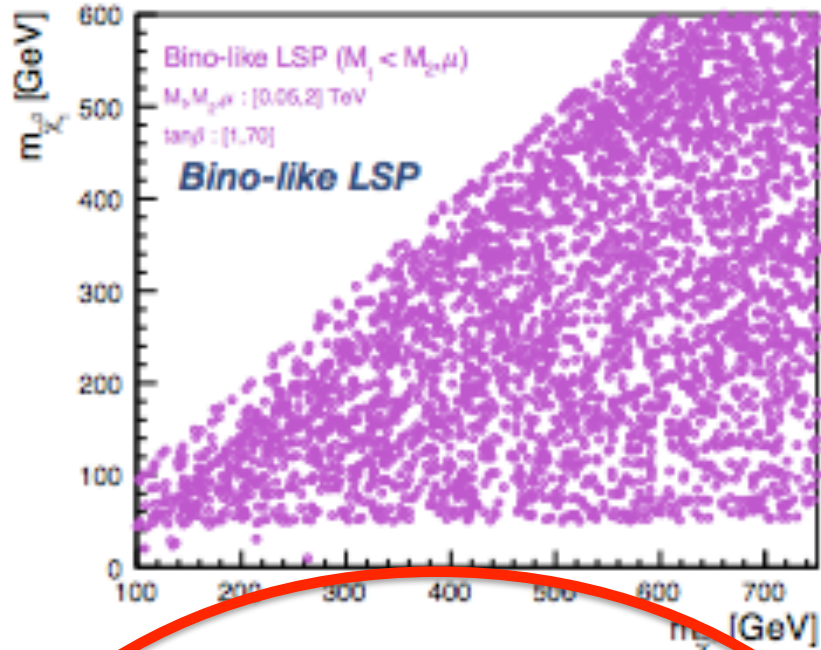
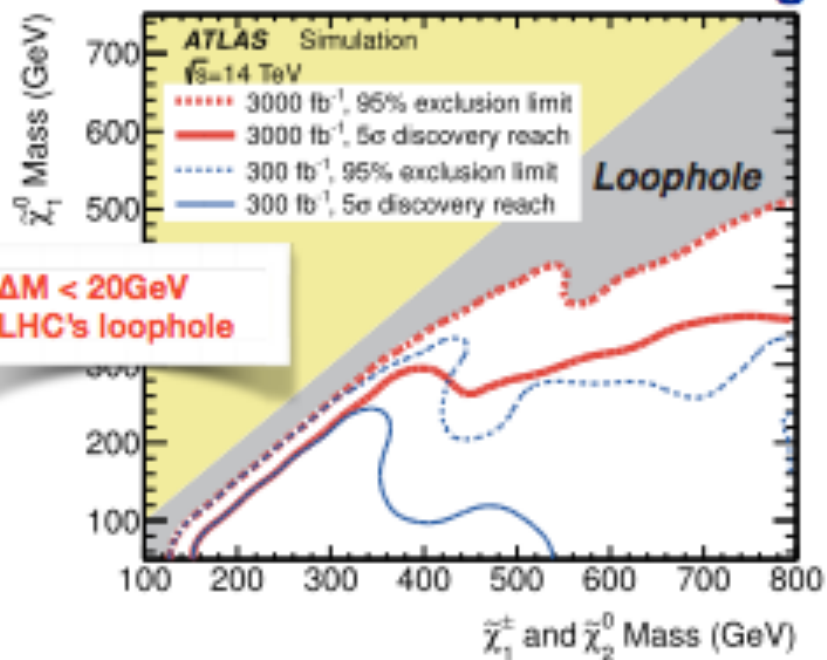
$$e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0, \quad \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0\ell^+\ell^-$$



$$e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0, \quad \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0\ell^+\ell^-$$

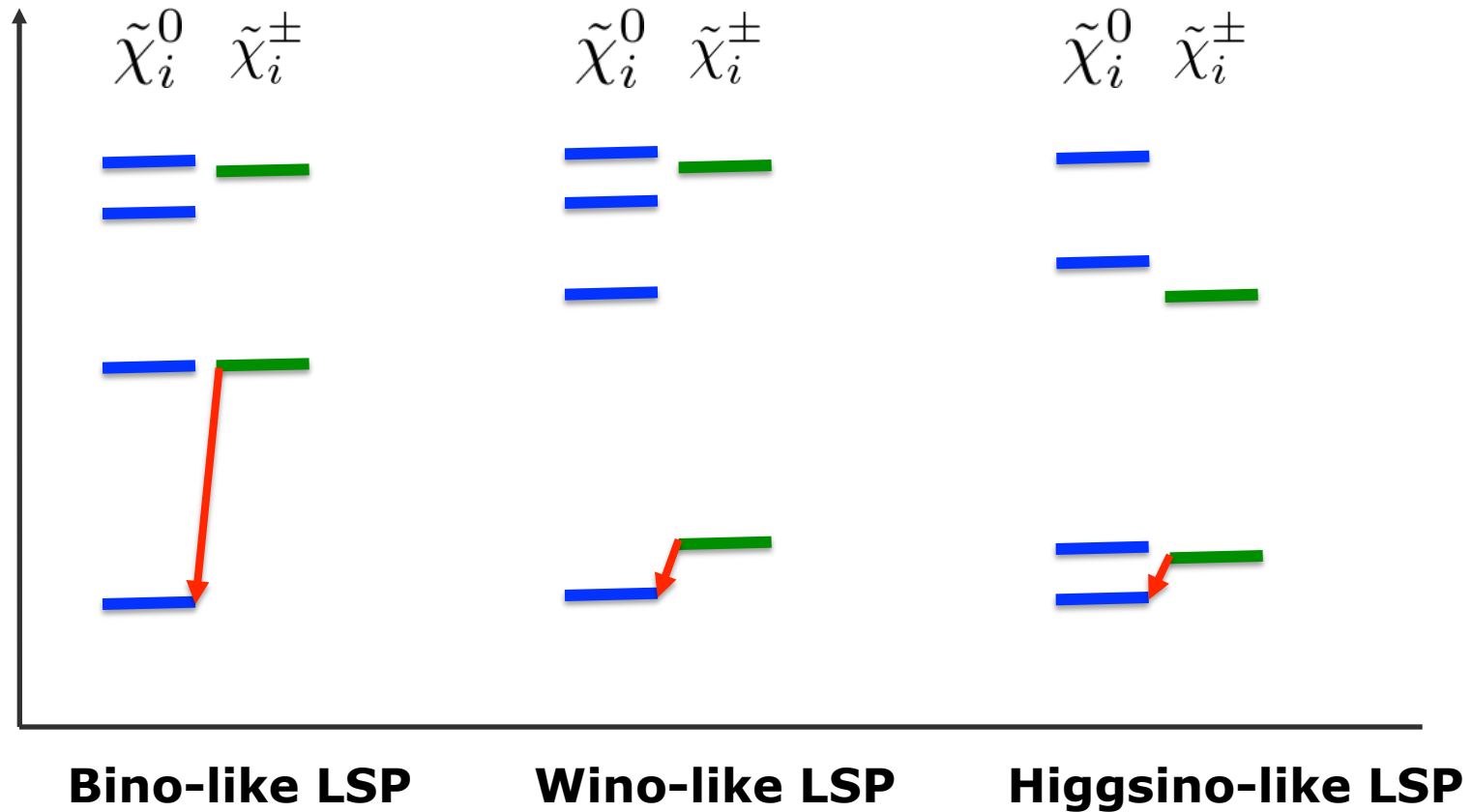


Chargino Search



LHC's blind spot is ILC's sweet spot!

SUSY Electroweak Sector



LSP/NLSP typically degenerate
(depends on mixing)

SUSY Parameter Determination

Why?

- To get information about unobserved sparticles
- To test GUT-scale models

How?

- Global χ^2 fit of SUSY parameters to observables using **Fittino** [hep-ph/0412012]
- Fit GUT scale (NUHM2) parameters

Reminder:

Benchmark	ILC2
M_0 [GeV]	5000
$M_{1/2}$ [GeV]	1200
A_0 [GeV]	-8000
$\tan\beta$	15
μ [GeV]	150
M_A [GeV]	1000

Defined at GUT scale
Defined at weak scale

Observables and assumed precision for ILC2 benchmark

observable	value	uncertainty
mass $\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm$	~ 160 GeV	0.2 GeV
$BR(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 l^+ l^-)$	0.106	0.1
$BR(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 q \bar{q})$	0.590	0.1
$BR(\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 q \bar{q}')$	0.671	0.1
$BR(\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 l \nu_l)$	0.329	0.1
$\sigma(\tilde{\chi}_1^0 \tilde{\chi}_2^0)$, 4 polarisations	140 – 300 fb $^{-1}$	1%
$\sigma(\tilde{\chi}_1^\pm \tilde{\chi}_1^\mp)$, 4 polarisations	200 – 970 fb $^{-1}$	1%

- Uncertainty to be updated with results from simulation study
- Study required precision that allows for full parameter determination

Fits of NUHM2 Parameters

ILC2

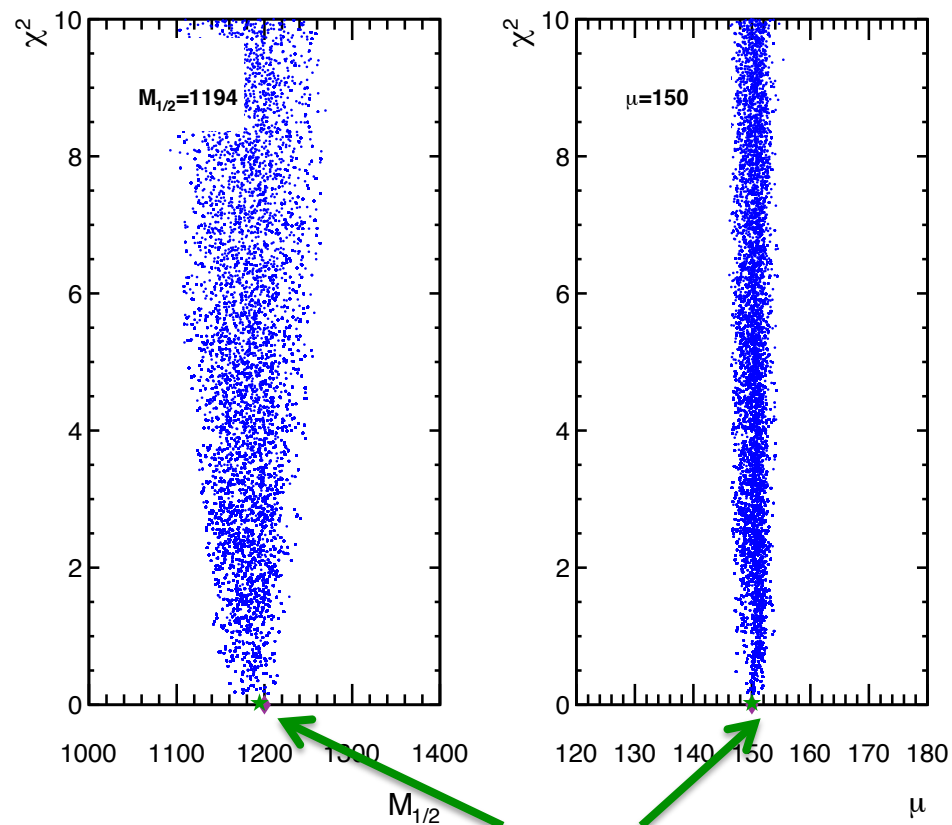
All 6 parameters are simultaneously varied. Initial values are set to be near the model values.

Each blue point corresponds to a set of parameter values. The χ^2 value is computed for each point.

Using the χ_1^0 , χ_2^0 , χ_1^\pm masses and production cross sections, $M_{1/2}$ can be determined.

Adding Higgs mass and BR as measured at the ILC fixes μ and possibly constrains other parameters

In addition, if χ_3^0 can be observed in $\chi_2^0 \chi_3^0$, $\tan\beta$ can be constrained as well. (ILC1)



Outlook

- Test gaugino mass unification by fitting weak scale parameters M_1 and M_2

ILC1

Cross sections (pure beam polarizations)
 $\sqrt{s}=500$ GeV with TDR beam parameters

(Pe-, Pe+)	(-1.0,+1.0)	(+1.0,-1.0)
$\sigma(\chi_1^+ \chi_1^-)$ [fb]	1800	335
$\sigma(\chi_1^0 \chi_2^0)$ [fb]	491	379
$\sigma(\chi_2^0 \chi_3^0)$ [fb]	11.0	8.42
$\sigma(\chi_1^0 \chi_1^0)$ [fb]	2.03	1.56
$\sigma(\chi_2^0 \chi_2^0)$ [fb]	0.53	0.41
$\sigma(\chi_1^0 \chi_3^0)$ [fb]	0.28	0.20

Branching ratios

$\text{BR}(\chi_1^+ \rightarrow \chi_1^0 qq')$	67%
$\text{BR}(\chi_1^+ \rightarrow \chi_1^0 lv)$ (l=e, μ)	22%
$\text{BR}(\chi_2^0 \rightarrow \chi_1^0 qq')$	58%
$\text{BR}(\chi_2^0 \rightarrow \chi_1^0 ll)$ (l=e, μ)	7.4%