## Top electroweak couplings study with the Matrix Element Method

## using di-muonic state at $\sqrt{s}=500 \mathrm{GeV}$, ILC

## 51th General Meeting

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## Outline

- Introduction
- Status
- Seed issues
- Analysis with Matrix element method
- Summery and Plan


## Top EW couplings at the ILC

$\square$ Top quark is the heaviest particle in the SM. Its large mass implies that this is strongly coupled to the mechanism of electroweak symmetry breaking (EWSB)
$\rightarrow$ Top EW couplings are good proves for New physics behind EWSB
$\square$ The ILC is advanced in the $t \bar{t} Z^{0}$ and $t \bar{t} \gamma$ couplings study

- Top pair production process, $e^{+} e^{-} \rightarrow t \bar{t}$, goes directly through the $t \bar{t} Z^{0}$ and $t \bar{t} \gamma$


## The general Lagrangian

$\left.\mathcal{L}_{\text {int }}=\sum_{v=\gamma, Z} g^{v}\left[V_{l}^{v} \bar{t} \tau^{l}\left(F_{1 V}^{v}\right)+\left(F_{14}^{v}\right) /(5) t+\frac{i}{2 m_{t}} \partial_{\nu} V_{l} \bar{t} \sigma^{l \nu}\left(\widetilde{F_{2 V}^{v}}\right)+\left(F_{2 A}^{v}\right)_{(5)}\right) t\right]$
$F_{2 A}^{v}$ can be a complex number $\rightarrow \mathbf{1 0}$ real form factors eg)


- Composite models yields typically $10 \%$ deviation of $g_{L, R}^{Z}\left(=F_{1 V}^{Z} \pm F_{1 A}^{Z}\right)$
- In the $2 \mathrm{HDM}, F_{2 A}^{\gamma}$ which is a CP-violating parameter can be non-zero


## Alternative : Di-leptonic state

Idea : Top quark decays before hadronization because of its large width
$\rightarrow$ Angles of the final state have the information of $t \bar{t} Z^{0} / \gamma$ vertex
$\rightarrow$ Use the di-leptonic state to obtain more angles


At most, there are 9 angles related to $\mathrm{tt} Z / \gamma$ vertex $\left(\cos \theta_{t}, \cos \theta_{W^{+}}, \phi_{W^{+}}, \cos \theta_{l^{+}}, \phi_{l^{+}}, \cos \theta_{W^{-}}, \phi_{W^{-}}, \cos \theta_{l^{-}}, \phi_{l^{-}}\right)$

## Situation

च The hadronization of $b, \bar{b}$
च ISR, beamsstrahlung, beam energy spread
$\nabla \mathrm{YY} \rightarrow$ hadrons

## Kinematical reconstruction

1. Define the $\chi_{\mu}^{2}$;

$$
\chi_{\mu}^{2}=\chi_{\mu^{+}}^{2}+\chi_{\mu^{-}}^{2}, \quad \chi_{\mu^{ \pm}}^{2}=\left(\frac{E_{\mu^{ \pm}}^{*}\left(\theta_{t}, \phi_{t}\right)-m_{W^{ \pm}} / 2}{\sigma\left[E_{\mu^{ \pm}}^{* *}\right]}\right)^{2}
$$

The energy of $\mu^{ \pm}$in the $W^{ \pm}$rest frame, $E_{\mu^{ \pm}}^{* *}$, must be equal to $m_{W^{ \pm}} / 2$ and it can be written by two parameters $\left(\theta_{t}, \phi_{t}\right)$.
2. Define the $\chi_{b}^{2}$;

$$
\chi_{b}^{2}=\left(\frac{E_{b}^{\text {meas. }}-E_{b}^{\text {rec. }}\left(\theta_{t}, \phi_{t}\right)}{\sigma\left[E_{b}^{\text {meas. }}\right]}\right)^{2}+\left(\frac{E_{\bar{b}}^{\text {meas. }}-E_{\bar{b}}^{\text {rec. }}\left(\theta_{t}, \phi_{t}\right)}{\sigma\left[E_{b}^{\text {meas. }}\right]}\right)^{2}
$$

Although the energy of $b$ quarks can be only poorly measured, we can eliminate bcharge ambiguity by comparing the measured energy to the reconstructed energy.
3. Compound $\chi_{t o t}^{2}$; $\chi_{t o t}^{2}=\chi_{\mu}^{2}+\chi_{b}^{2}$

One minimizes the $\chi_{t o t}^{2}$ to obtain optimal solution of $\left(\theta_{t}, \phi_{t}\right)$.

## Seed issues

Until last GM : Truth values were used for initial seeds of the parameters.
$\rightarrow$ Repeat to put complete random values on seeds $\sim 20$ times.

## Sample A.

- Distributions can be reconstructed but miss pairing of bW slightly increase.
- When masses are varied with BW constraints, results are almost same


Ratio of the miss pairing of bW


## Seed issues

## Sample B.

It doesn't work for now ...
We have used $k_{e^{-}}, k_{e^{+}}$to reconstruct the ISR/BS effects. (as next slide)

- Unknown parameters: $\vec{P}_{v}, \vec{P}_{\bar{v}},\left(E_{b}, E_{\bar{b}}\right), k_{e^{-}}, k_{e^{+}}=>8$ (10)
-Constraints : $E_{C M}, \vec{P}_{\text {init }}, m_{t}, m_{\bar{t}}, m_{W^{+}}, m_{W^{-}},\left(E_{b}, E_{\bar{b}}\right)=>8$ (10)
$\rightarrow$ Although solutions are obtained, the optimal one cannot be selected.
$\rightarrow$ Have not well discussed about this problem yet.
(It seems that an Ukrainian student is working on it with Francois.)


## Considering ISR/BS effects

Collinear approximation:
Photons are emitted on the beam directions by ISR/BS

$$
\begin{align*}
\vec{e}^{-} & =\hat{\eta}_{e^{-}} E_{e^{-}}  \tag{1}\\
\vec{e}^{+} & =\hat{\eta}_{e^{+}} E_{e^{+}} \tag{2}
\end{align*}
$$

with,

$$
\begin{align*}
\hat{\eta}_{e^{-}} & =\left(\sin \theta_{c}, 0, \quad \cos \theta_{c}\right)  \tag{3}\\
\hat{\eta}_{e^{+}} & =\left(\sin \theta_{c}, 0,-\cos \theta_{c}\right)  \tag{4}\\
E_{e^{ \pm}} & =E=250 \mathrm{GeV} \tag{5}
\end{align*}
$$

where $\theta_{c}$ is the beam crossing angle, $\theta_{c}=7 \mathrm{mrad}$.
In this approximation, the directions are not changed but only the energies are changed. Then the electron and positron thre-momenta become:

$$
\begin{array}{rll}
\left(\vec{e}^{-}\right)^{*} & =\hat{\eta}_{e^{-}} E_{e^{-}}^{*}=\hat{\eta}_{e^{-}} E\left(1-k_{e^{-}}\right) & \text {with } \\
k_{e^{-}}=\frac{E-E_{e^{-}}^{*}}{E}  \tag{7}\\
\left(\vec{e}^{+}\right)^{*}=\hat{\eta}_{e^{+}} E_{e^{+}}^{*}=\hat{\eta}_{e^{+}} E\left(1-k_{e^{+}}\right) & \text {with } & k_{e^{+}}=\frac{E-E_{e^{+}}^{*}}{E}
\end{array}
$$

where $E_{e^{ \pm}}^{*}$ is the energy of electron or positron just before collision.

## Investigate the effects of reducing angles

At most we can reconstruct 9 angles with di-leptonic channel;

$$
\left(\cos \theta_{t}, \cos \theta_{W^{+}}, \phi_{W^{+}}, \cos \theta_{l^{+}}, \phi_{l^{+}}, \cos \theta_{W^{-}}, \phi_{W^{-}}, \cos \theta_{l^{-}}, \phi_{l^{-}}\right)
$$

We investigate the effects of reducing number of angles
(1) 9 (full)
(2) $7\left(\cos \theta_{t}, \cos \theta_{W^{+}}, \phi_{W^{+}}, \cos \theta_{l^{+}}, \phi_{l^{+}}, \cos \theta_{W^{-}}, \phi_{W^{-}}\right)$or $\left(\cos \theta_{t}, \cos \theta_{W^{+}}, \phi_{W^{+}}, \cos \theta_{W^{-}}, \phi_{W^{-}}, \cos \theta_{l^{-}}, \phi_{l^{-}}\right)$
(3) $5\left(\cos \theta_{t}, \cos \theta_{W^{+}}, \phi_{W^{+}}, \cos \theta_{W^{-}}, \phi_{W^{-}}\right)$
(4) $1\left(\cos \theta_{t}\right)$
$\rightarrow$ (2) (4) can be reconstructed with the semi-leptonic state in principle.

## Status

Estimate the precision at Truth level for each case.
$\rightarrow$ At first, we fit 4 form factors simultaneously. ( $\left.\mathcal{R} e \delta \tilde{F}_{1 V}^{\gamma}, \mathcal{R e} \delta \tilde{F}_{1 V}^{Z}, \mathcal{R e} \delta \tilde{F}_{1 A}^{\gamma}, \mathcal{R} e \delta \tilde{F}_{1 A}^{Z}\right)$
Sample (made by my brief generator)
Di-muonic state of top pair production
$500 \mathrm{GeV}, 500 \mathrm{fb}^{-1},\left(P_{e^{-}}, P_{e^{+}}\right)=( \pm 0.8, \mp 0.3)$
$\left(\mathcal{R e} \delta \tilde{F}_{1 V}^{\gamma}, \mathcal{R e} \delta \tilde{F}_{1 V}^{Z}, \mathcal{R e} \delta \tilde{F}_{1 A}^{\gamma}, \mathcal{R e} \delta \tilde{F}_{1 A}^{Z}\right)=(0,-0.1,0,+0.1)$

- (1) provides the best precision.
- (4) cannot reconstruct precisely
$\rightarrow$ Need to check if there are bugs
$\rightarrow$ Investigate sensitivity for other parameters
(1) $\left[\begin{array}{lll}\mathcal{R} e & \delta \tilde{F}_{1 V}^{\gamma} & -0.0025 \pm 0.0059 \\ \mathcal{R} e & \delta \tilde{F}_{1 V}^{Z} & -0.0984 \pm 0.0103 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{\gamma} & -0.0064 \pm 0.0108 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{Z} & +0.0805 \pm 0.0170\end{array}\right]$
(2) Ongoing
(3) $\left[\begin{array}{lll}\mathcal{R} e & \delta \tilde{F}_{1 V}^{\gamma} & -0.0011 \pm 0.0060 \\ \mathcal{R} e & \delta \tilde{F}_{Z}^{Z} & -0.0985 \pm 0.0110 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{\gamma} & +0.0077 \pm 0.0134 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{Z} & +0.0905 \pm 0.0196\end{array}\right]$
(4) $\left[\begin{array}{lll}\mathcal{R} e & \delta \tilde{F}_{1 V}^{\gamma} & +0.0026 \pm 0.0060 \\ \mathcal{R} e & \delta \tilde{F}_{1 V}^{Z} & -0.2143 \pm 0.0157 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{\gamma} & -0.1120 \pm 0.0113 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{Z} & +0.0842 \pm 0.0198\end{array}\right]$
or $\left[\begin{array}{ccc}\mathcal{R} e & \delta \tilde{F}_{1 V}^{\gamma} & +0.0047 \pm 0.0061 \\ \mathcal{R} e & \delta \tilde{F}_{Z}^{Z} & -0.1845 \pm 0.0152 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{\gamma} & 0 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{Z} & +0.0717 \pm 0.0196\end{array}\right]$


## Summery

## Seed issues

- Random values are used for seeds instead of MC truth values.
- Sample A.

Similar distribution can be reconstructed.

- Sample B.

When $k_{e^{-}}, k_{e^{+}}$are included, reconstruction doesn't work well

## Analysis

$\square$ Investigate the effects of reducing number of angles.

- More angles are used, higher precision can be obtained.
- Sensitivity for other parameters should be checked.


## Back up

## Investigate the effects of reducing angles

Modify the $|M|^{2}$ for each cases as following



(4) $\left|M_{\lambda_{e}-, \lambda_{e}+}\right|^{2}=\sum_{\lambda_{t}, \lambda_{\bar{E}}}\left|M_{e-e^{+} \rightarrow t \bar{t}}^{\lambda_{-} \lambda^{2}}\right|^{2}$

## Alternative : The Matrix Element Method

## The Matrix Element Method (MEM)

The most efficient method when all the kinematics can be reconstructed

## MEM with the 9 angles and the cross-section

- All 10 form factors can be fitted simultaneously
$\rightarrow \sim 0.01$ precision is obtained at parton level study with di-leptonic state
Statistical uncertainties and correlation with the SM LO as normalization

$\rightarrow$ Estimate the ultimate precision considering all effects


## Kinematical Reconstruction : Strategy

Di-muonic state : $e^{+} e^{-} \rightarrow t \bar{t} \rightarrow \boldsymbol{b} \bar{b} \mu^{+} v \mu^{-} \bar{v}$ Measurable $\left[\begin{array}{l}\underline{\text { muon's }}: E_{\mu^{+}}, \theta_{\mu^{+}}, \phi_{\mu^{+}}, E_{\mu^{-}}, \theta_{\mu^{-}}, \phi_{\mu^{-}} \\ \underline{\text { b-jet's }}:\left(E_{b}\right), \theta_{b}, \phi_{b},\left(E_{\bar{b}}\right), \theta_{\bar{b}}, \phi_{\bar{b}}\end{array}\right.$
Missing

$$
\begin{aligned}
& {\left[\begin{array}{l}
\underline{\text { b-jet's }}:\left(E_{b}\right),\left(E_{\bar{b}}\right) \\
\underline{\text { neutrino's }}: E_{v}, \theta_{v}, \phi_{v}, E_{\bar{v}}, \theta_{\bar{v}}, \phi_{\bar{v}} \\
=>6 \text { (8) unknowns }
\end{array}\right.}
\end{aligned}
$$

## Strategy

(1) Recover them from 8 kinematical constraints $\left[\begin{array}{l}\text { initial state }:\left(\sqrt{s}, \vec{P}_{\text {init. }}\right)=(500, \overrightarrow{0}) \\ \text { mass : } m_{t}, m_{\bar{t}}, m_{W^{+}}, m_{W^{-}}\end{array}\right.$
$\rightarrow$ But the equation is non-linear and the b-charge ambiguity remains.
$\rightarrow$ Typically 4 solutions per an event
(2) Select the optimal one by comparing $E_{b}, E_{\bar{b}}$ between recovered and measured

## Results : Polar angle distribution of top, $\cos \theta_{t}$

(Before cut)

(After cut)


- In the case of Left, migrations of events passing from forward to backward are observed.
$\leftarrow$ The miss pairing of $W$ and $b$
- After selection of reliable events by the quality of the kinematical reconstruction, migrations become smaller.


## Ratio of the miss pairing <br> Left <br> Right

Before cut (efficiency $=\sim 92 \%$ )
8.9 \%
6.0 \%

After cut
(efficiency $=\sim 50 \%$ )
5.5 \%
3.0 \%

## Results : All 10 form factors fit with MEM

Fit of all $\mathbf{1 0}$ form factors at same time
$\square$ Precision is typically $\sim 0.03$


|  | Precision of $\widetilde{F}_{1 V}^{\gamma}$ | $N / N_{\text {di-muonic }}$ |
| :---: | :---: | :---: |
| This result | $\mathbf{0 . 0 1 1}$ | $\mathbf{1}$ |
| Parton level | $\mathbf{0 . 0 0 4}$ | $\mathbf{\sim 4}$ |
| Semi-leptonic study | $\mathbf{0 . 0 0 2}$ | $\sim \mathbf{2 5}$ |

$\rightarrow$ Comparable with the previous study
$\square$ Biases are thought to results from the detector effects and the miss pairing of Wb
$\rightarrow$ One can reduce them by convoluting $|M|^{2}$ with

## Preliminary

(efficiency = ~50 \%)

$$
\swarrow\left[\begin{array}{cc}
\mathcal{R} e \delta \tilde{F}_{1 V}^{\gamma} & -0.0015 \pm 0.0108 \\
\mathcal{R} e \delta \tilde{F}_{1 V}^{Z} & -0.0271 \pm 0.0187 \\
\mathcal{R} e \delta \tilde{F}_{1 A}^{\gamma} & -0.0314 \pm 0.0156 \\
\mathcal{R} e \delta \tilde{F}_{1 A}^{Z} & +0.0277 \pm 0.0246 \\
\mathcal{R} e \delta \tilde{F}_{2 V}^{\gamma} & -0.0266 \pm 0.0317 \\
\mathcal{R} e \delta \tilde{F}_{2 V}^{Z} & -0.0702 \pm 0.0504 \\
\mathcal{R} e \delta \tilde{F}_{2 A}^{\gamma} & -0.0082 \pm 0.0211 \\
\mathcal{R} e \delta \tilde{F}_{2 A}^{Z} & -0.0164 \pm 0.0360 \\
\mathcal{I} m \delta \delta \tilde{F}_{2 A}^{\gamma} & -0.0427 \pm 0.0206 \\
\mathcal{I} m & \delta \tilde{F}_{2 A}^{Z}
\end{array}+0.0220 \pm 0.0297\right]
$$

$$
\tilde{F_{1 V}^{\tilde{v}}}=-\left(F_{1 V}^{v}+F_{2 V}^{v}\right), \quad \tilde{F_{2 V}^{\tilde{v}}}=F_{2 V}^{v}
$$

$$
\tilde{F_{1 A}^{v}}=-F_{1 A}^{v}, \quad \tilde{F_{2 A}^{v}}=-i F_{2 A}^{v}
$$ the detector effects and applying relevant cuts.

## Thrust axis method

We use the thrust axis method for the measurement of 2 b -jets.
(1) Collect all hadronized particles and photons from isolated leptons in the ILC frame
(2) Boost them to their rest frame and calculate thrust axis in this frame (defined as the $B B$ frame in this slide)
(3) Boost the vectors along thrust axis to the ILC' frame
(ILC' frame : the frame in which head-on-collision occurs)


## Results : Distributions of the 9 -angles

$$
\cos \theta_{t}, \cos \theta_{W^{+}}, \phi_{W^{+}}, \cos \theta_{\mu^{+}}, \phi_{\mu^{+}}, \cos \theta_{W^{-}}, \phi_{W^{-}}, \cos \theta_{\mu^{-}}, \phi_{\mu^{-}}
$$


$\square$ Different between Left and Right polarization
$\rightarrow$ These have the information of the polarization of top

## Results : Variance matrix of 10 form factors fit

## Preliminary (efficiency $=\sim 50 \%$ )

$$
\left[\begin{array}{cccccccccc}
\mathcal{R} e \delta \tilde{F}_{1 V}^{\gamma} & \mathcal{R} e \delta \tilde{F}_{1 V}^{Z} & \mathcal{R} e \delta \tilde{F}_{1 A}^{\gamma} & \mathcal{R} e \delta \tilde{F}_{1 A}^{Z} & \mathcal{R} e \delta \tilde{F}_{2 V}^{\gamma} & \mathcal{R} e \delta \tilde{F}_{2 V}^{Z} & \mathcal{R} e \delta \tilde{F}_{2 A}^{\gamma} & \mathcal{R} e \delta \tilde{F}_{2 A}^{Z} & \mathcal{I} m \delta \tilde{F}_{2 A}^{\gamma} & \mathcal{I} m \delta \tilde{F}_{2 A}^{Z} \\
0.0108 & -0.14 & -0.03 & +0.09 & +0.62 & -0.10 & +0.02 & -0.06 & +0.04 & -0.02 \\
& 0.0187 & +0.09 & -0.02 & -0.10 & +0.61 & -0.06 & +0.02 & -0.01 & +0.03 \\
& & 0.0156 & -0.11 & -0.01 & +0.03 & +0.02 & 0 & +0.05 & +0.01 \\
& & & 0.0246 & -0.01 & 0 & +0.01 & +0.03 & +0.01 & +0.05 \\
& & & & 0.0317 & -0.17 & +0.03 & -0.12 & 0 & -0.03 \\
& & & & & 0.0504 & -0.11 & -0.06 & -0.02 & 0 \\
& & & & & & 0.0211 & -0.17 & -0.04 & +0.01 \\
& & & & & & 0.0360 & -0.01 & -0.45 \\
& & & & & & & 0.0206 & -0.13 \\
& & & & & & 0.0297
\end{array}\right]
$$

## Results : No cut \& Loose cut \& Tight cut

No cut (efficiency = ~92 \%)
Left 8.9\% Right 6.0\%


Loose cut (efficiency $=\sim 80 \%$ ) Tight cut (efficiency $=\sim 50 \%$ )
Left 8.1\% Right 5.5\%
$\left[\begin{array}{lll}\mathcal{R} e & \delta \tilde{F}_{1 V}^{\gamma} & -0.0047 \pm 0.0088 \\ \mathcal{R} e & \delta \tilde{F}_{1 V}^{Z} & -0.0236 \pm 0.0154 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{\gamma} & -0.0460 \pm 0.0126 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{Z} & +0.0631 \pm 0.0198 \\ \mathcal{R} e & \delta \tilde{F}_{2 V}^{\gamma} & -0.0669 \pm 0.0253 \\ \mathcal{R} e & \delta \tilde{F}_{2 V}^{Z} & -0.0206 \pm 0.0417 \\ \mathcal{R} e & \delta \tilde{F}_{2 A}^{\gamma} & +0.0011 \pm 0.0160 \\ \mathcal{R} e & \delta \tilde{F}_{2 A}^{Z} & -0.0370 \pm 0.0283 \\ \mathcal{I} m & \delta \tilde{F}_{2 A}^{\gamma} & -0.0143 \pm 0.0163 \\ \mathcal{I} m & \delta \tilde{F}_{2 A}^{Z} & -0.0110 \pm 0.0237\end{array}\right]$
$\left[\begin{array}{lll}\mathcal{R} e & \delta \tilde{F}_{1 V}^{\gamma} & -0.0015 \pm 0.0108 \\ \mathcal{R} e & \delta \tilde{F}_{1 V}^{Z} & -0.0271 \pm 0.0187 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{\gamma} & -0.0314 \pm 0.0156 \\ \mathcal{R} e & \delta \tilde{F}_{1 A}^{Z} & +0.0277 \pm 0.0246 \\ \mathcal{R} e & \delta \tilde{F}_{2 V}^{\gamma} & -0.0266 \pm 0.0317 \\ \mathcal{R} e & \delta \tilde{F}_{2 V}^{Z} & -0.0702 \pm 0.0504 \\ \mathcal{R} e & \delta \tilde{F}_{2 A}^{\gamma} & -0.0082 \pm 0.0211 \\ \mathcal{R} e & \delta \tilde{F}_{2 A}^{Z} & -0.0164 \pm 0.0360 \\ \mathcal{I} m & \delta \tilde{F}_{2 A}^{\gamma} & -0.0427 \pm 0.0206 \\ \mathcal{I} m & \delta \tilde{F}_{2 A}^{Z} & +0.0220 \pm 0.0297\end{array}\right]$

## True and Miss pairing of Wb



Right-handed electron case (eRpL), Blue line Little difference between true and miss associated distributions

Left-handed electron case (eLpR), Red line
Miss association changes angular
distribution significantly

## $\rightarrow$ The migration effect happens in only the case of eLpR

## The $t \bar{t} Z^{0} / \gamma$ couplings: CP-conserving

$$
\begin{array}{r}
\left.\mathcal{L}_{\mathrm{int}}=\sum_{v=\gamma, Z} g^{v}\left[V_{l}^{v} \bar{t} \gamma^{l}\left(F_{1 V}^{v}+F_{1 A}^{v}\right) \gamma_{5}\right) t+\frac{i}{2 m_{t}} \partial_{\nu} V_{l} \bar{t} \sigma^{l \nu}\left(F_{2 V}^{v}+F_{2 A}^{v} \gamma_{5}\right) t\right] \\
g_{L}^{Z}=F_{1 V}^{Z}-F_{1 A}^{Z}, \quad g_{R}^{Z}=F_{1 V}^{Z}+F_{1 A}^{Z}
\end{array}
$$

$\square$ Deviation from the SM of $g_{L}^{Z}, g_{R}^{Z}$ will be typically $10 \%$ in composite models

arXiv:1505.06020 [hep-ph]

## The $t \bar{t} Z^{0} / \gamma$ couplings : CP-violating

$$
\left.\mathcal{L}_{\mathrm{int}}=\sum_{v=\gamma, Z} g^{v}\left[V_{l}^{v} \bar{t} \gamma^{l}\left(F_{1 V}^{v}+F_{1 A}^{v} \gamma_{5}\right) t+\frac{i}{2 m_{t}} \partial_{\nu} V_{l} \bar{t} \sigma^{l \nu}\left(F_{2 V}^{v}+F_{2 A}^{v}\right)^{\prime}\right) t\right]
$$

$\square F_{2 A}^{\gamma}$ is the electric dipole moment which is forbidden in the SM
$\rightarrow$ Probes for CP-violating beyond the Kobayashi-Maskawa mechanism eg) 2 HDM can yield $\sim 0.01$



## Kinematical Reconstruction : True pairing

- Intersections of green and red lines are solutions in terms of $\left(\theta_{t}, \phi_{t}\right)$
- Blue line shows the comparison of the $E_{b}, E_{\bar{b}}$ between rec. and meas.
$\rightarrow$ The optimal solution is selected obtained
$E_{\mu^{+}}^{* *}\left(\theta_{t}, \phi_{t}\right)=\frac{m_{W^{+}}}{2}$

$$
\chi_{b}^{2}=\left(\frac{E_{b}^{\text {meas. }}-E_{b}^{\text {rec. }}\left(\theta_{t}, \phi_{t}\right)}{\sigma\left[E_{b}^{\text {meas. }}\right]}\right)^{2}+\left(\frac{E_{\bar{b}}^{\text {meas. }}-E_{\bar{b}}^{\text {rec. }}\left(\theta_{t}, \phi_{t}\right)}{\sigma\left[E_{\bar{b}}^{\text {meas. }}\right]}\right)^{2}=20
$$

$E_{\mu^{*}}^{* *}\left(\theta_{t}, \phi_{t}\right)=\frac{m_{W^{-}}}{2}$

The energy of $\mu^{ \pm}$in $W^{ \pm}$ frame is equal to $m_{W^{ \pm}} / 2$



## Kinematical Reconstruction : Miss pairing

- Blue line is far from intersections of green and red line
$\rightarrow$ Miss pairing is excluded by the $E_{b}, E_{\bar{b}}$ comparision.

$$
E_{\mu^{+}}^{* *}\left(\theta_{t}, \phi_{t}\right)=\frac{m_{W^{+}}}{2}
$$

$$
\chi_{b}^{2}=\left(\frac{E_{b}^{\text {meas. }}-E_{b}^{\text {rec. }}\left(\theta_{t}, \phi_{t}\right)}{\sigma\left[E_{b}^{\text {meas. }}\right]}\right)^{2}+\left(\frac{E_{\bar{b}}^{\text {meas. }}-E_{\bar{b}}^{\text {rec. }}\left(\theta_{t}, \phi_{t}\right)}{\sigma\left[E_{\bar{b}}^{\text {meas. }}\right]}\right)^{2}=20
$$

$$
E_{\mu^{-}}^{* *}\left(\theta_{t}, \phi_{t}\right)=\frac{m_{W^{-}}}{2}
$$

The energy of $\mu^{ \pm}$in $W^{ \pm}$ frame is equal to $m_{W^{ \pm}} / 2$



