

# ILC Damping Ring Lattice Error Tolerances

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October 25, 2012



# DTC04 Summary – KILC

## Status

- All collider operating configurations can be accommodated (5Hz, 10Hz, electrons, positrons)
- Tunable
  - Range of phase trombone  $> 1 \lambda$
  - Range of chicane  $\pm 4\text{mm}$
- Established BPM resolution and alignment tolerances required to achieve  $< 2 \text{ pm-rad}$  with emittance tuning
- Demonstrated existence of a particular deployment of corrector magnets sufficient to achieve  $< 2 \text{ pm-rad}$
- Demonstrated adequate dynamic aperture with wiggler nonlinearities and magnet multipole errors (but not simultaneously)

## Ongoing effort

- Explore range of tolerable multipole errors
- Identify the multipole responsible for reducing dynamic aperture
- Explore tune plane to identify operating point with more DA
- Compute DA with wiggler nonlinearities and multipole errors and misalignments simultaneously
- Investigate emittance tuning with fewer BPMs and/or fewer correctors
- Investigate alternate sextupole distributions for more DA
- Explore implications of reduced energy spread of injected bunch (0.75%)



# DTC04 Summary – KILC

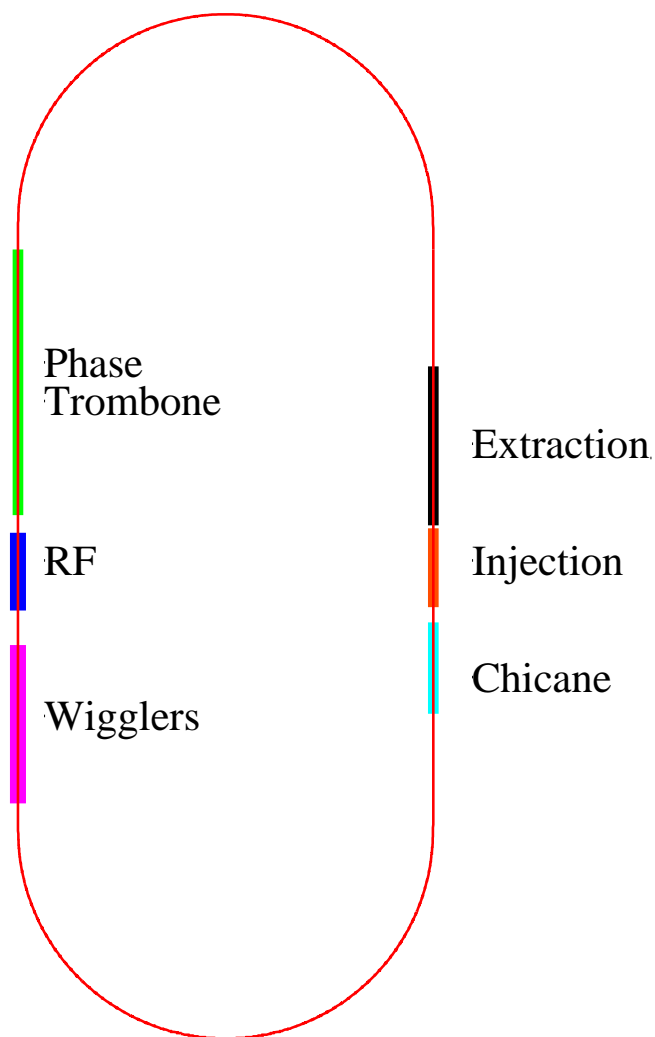
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# Layout - Reminder



Circumference - 3238 m

$5.6 \mu\text{m-rad} < \gamma\epsilon_x < 6.4 \mu\text{m-rad}$

54 Wignlers

length 2.1 m

$B_{\text{peak}}$  2.2 T

Poles 14

Period 30cm

$24\text{ms} > \tau_x > 12\text{ms}$

Phase trombone  $\rightarrow \pm 0.5 \lambda_\beta$

Chicane  $\rightarrow \pm 3\text{mm}$  pathlength

Up to 12 - 650MHz RF cavities

$\Rightarrow \sigma_l = 6\text{mm}$

Each cell contains :

1 - 3m dipole,  $\theta = \pi/75$

3 – quadrupoles

4 - sextupoles

3 - corrector magnets

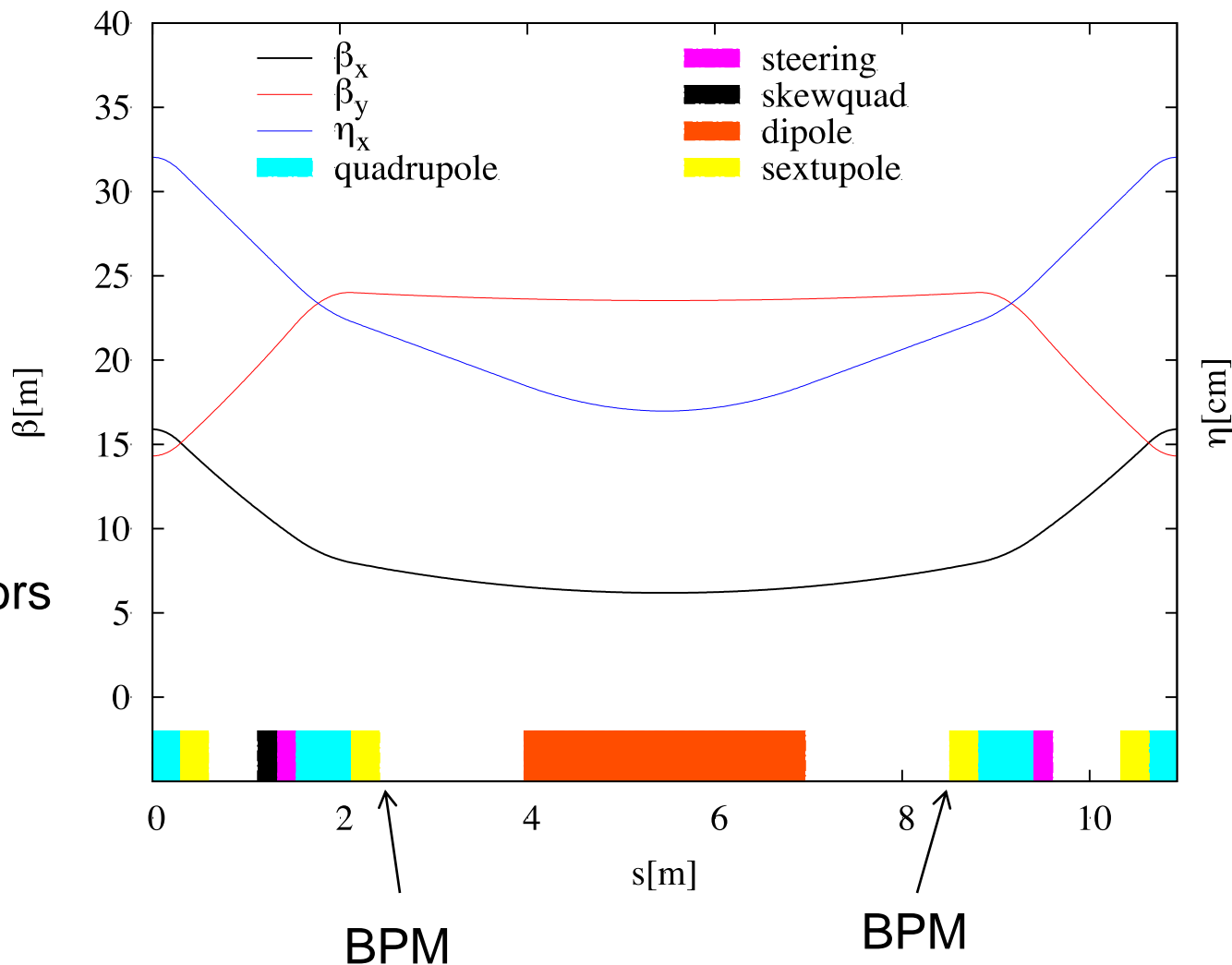
1-horizontal steering  $\beta_x$

1-vertical steering  $\eta_x$

1- skew quad

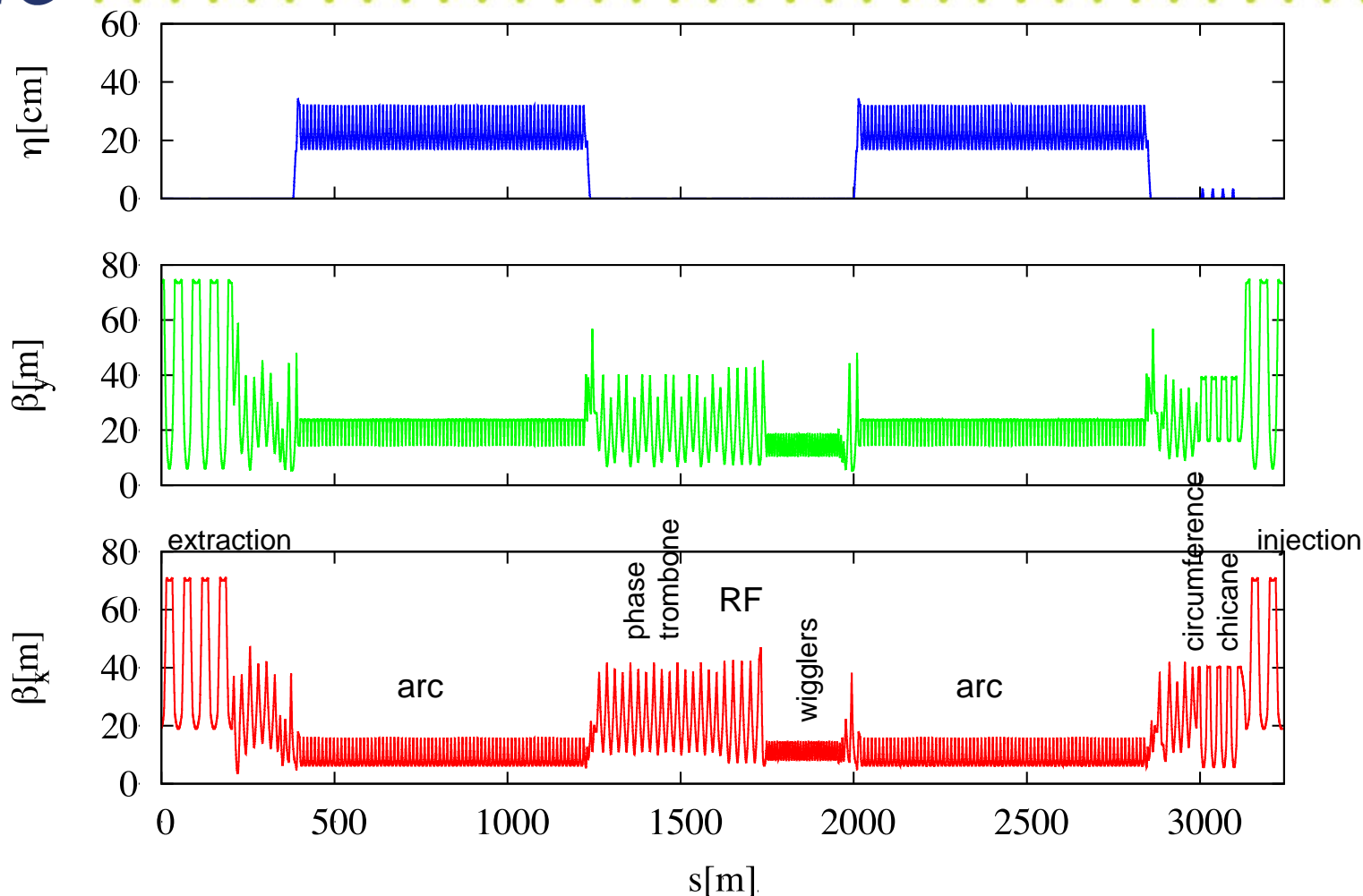
2 beam position monitors

75-cells/arc





# Lattice – Optics Functions - Reminder



DTC04 straights are based on their counterparts in the 6.4km DCO4 lattice created by Andy Wolski and Maxim Kostelev

# Parameter Table

Parameter	10 Hz(Low)	5 Hz (Low)	5 Hz (High)	10 Hz (electrons)
Circumference	3.238 km	3.238 km	3.238 km	3.238 km
RF frequency	650 MHz	650MHz	650 MHz	650 MHz
$\tau_x/\tau_y$ [ms]	12.86	23.95	23.95	17.5
$T_z$ [ms]	6.4	12.0	12.0	8.7
$\sigma_s$ [mm]	6.02	6.02	6.02	6.01
$\sigma_\delta$	0.137%	0.11%	0.11%	0.12%
$\alpha_p$	$3.3 \times 10^{-4}$	$3.3 \times 10^{-4}$	$3.3 \times 10^{-4}$	$3.3 \times 10^{-4}$
$\gamma\epsilon_x$ [ $\mu\text{m}$ ]	6.4	5.7	5.7	5.6
RF [MV] Total/Per cav(12)	22.4/1.9	14.2 /1.2	14.2/1.2	17.9/1.5
RF – synchronous phase[deg]	21.9	18.5	18.5	20.3
$\xi_x/\xi_y$	-50.9/-44.1	-51.3/-43.3	-51.3/-43.3	-51.3/-43.3
Wigglers- $N_{\text{cells}}@B[\text{T}]$	27@2.16	27@1.51	27@1.51	27@1.81
Energy loss/turn [MeV]	8.4	4.5	4.5	6.19
sextupoles	3.34/-4.34	3.34/-4.23	3.34/-4.23	3.34/-4.23
Number of bunches	1312	1312	2450	1312
Particles/bunch [ $\times 10^{10}$ ]	2	2	1.74	2
Power/RF coupler [kW]*	272 (389mA)	146 (389mA)	237 (632mA)	200 (389mA)

\*Power/coupler is computed as (Current) X (Energy loss/turn)/(Number of cavities)

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# Characterization – Dynamic Aperture

- Focus on **5Hz low-power lattice**
  - Previous studies have shown minimal difference for the 10Hz lattice
- 2-family sextupole distribution
  - Chromaticity  $\sim 1$  (horizontal and vertical)
- Track for 1000 turns; if particle lost, record amplitude
- Overlay phase space amplitude of injected bunch:
  - $A_x + A_y < 0.07$  m-rad (normalized)



# Guide field multipole errors

## Dipole multipoles, r=3cm

Multipole	Systematic		Random	
	$a_n(\times 10^{-4})$	$b_n(\times 10^{-4})$	$a_n(\times 10^{-4})$	$b_n(\times 10^{-4})$
3	1.60	0.0	0.8	0.0
4	-0.16	0.0	0.08	0.0
5	0.76	0	0.38	0.0

## Quadrupole multipoles, r=5cm

Multipole	Systematic		Random	
	$a_n(\times 10^{-4})$	$b_n(\times 10^{-4})$	$a_n(\times 10^{-4})$	$b_n(\times 10^{-4})$
3	-0.124	-0.115	0.761	0.725
4	0.023	0.141	1.32	1.27
5	-0.043	0.0062	0.15	0.162
6	3.40	-0.493	1.65	3.63
7	0.003	-0.0102	0.067	0.066
8	0.006	0.0038	0.089	0.066
9	0.006	-0.0028	0.046	0.049
10	-0.617	-0.577	2.46	2.33
11	-0.002	-0.0038	0.042	0.035
12	0.036	-0.0653	0.348	0.366
13	0.006	0.012	0.092	0.086
14	0.01	-0.0074	0.476	0.446

$$(B_y + iB_x) = B(r) \sum_{n=1} (b_n + ia_n) \left( \frac{x}{r} + i\frac{y}{r} \right)^{n-1}$$

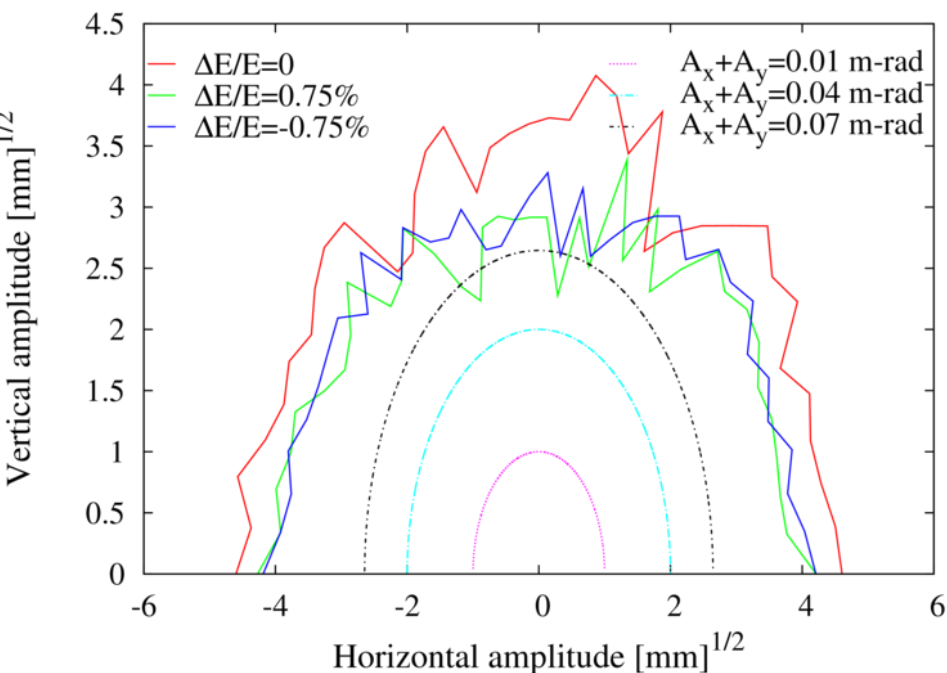
## Sextupole multipoles, r=3.2cm

Multipole	Systematic		Random	
	$a_n(\times 10^{-4})$	$b_n(\times 10^{-4})$	$a_n(\times 10^{-4})$	$b_n(\times 10^{-4})$
4	2	0	1	0
5	1	0	0.3	0
6	7	0	1	0
7	1	0	0.3	0
8	1	0	0.3	0
9	1	0	0.3	0
10	1	0	0.3	0
11	1	0	0.3	0
12	32	0	1	0
13	1	0	0.3	0
14	1	0	0.3	0

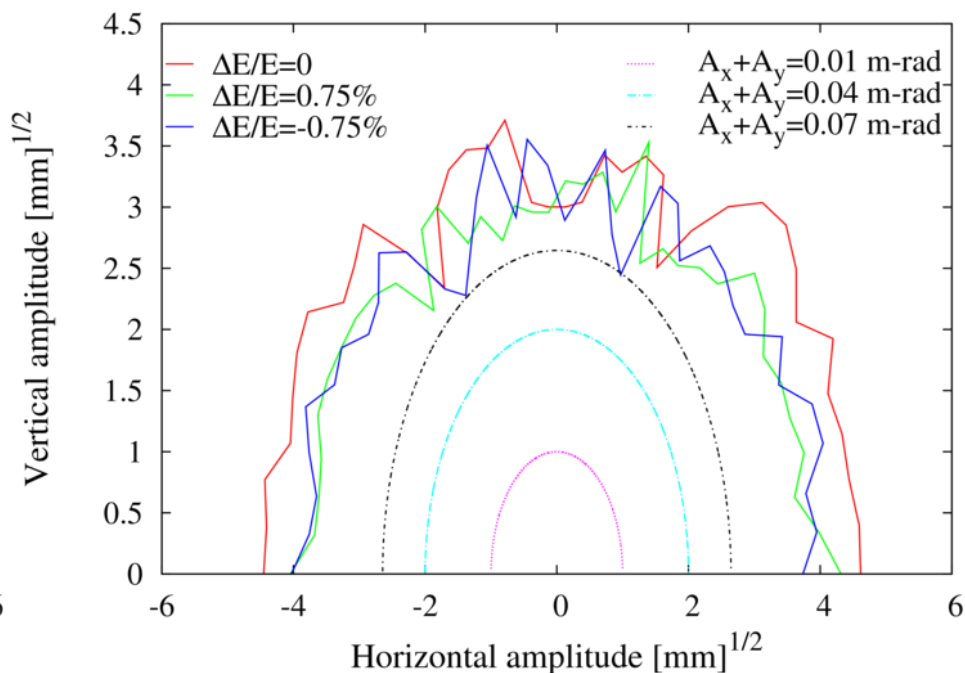
SPEAR3 and PEP-II

Measured multipoles – Y. Cai

**Use 2x these values  
in simulations**

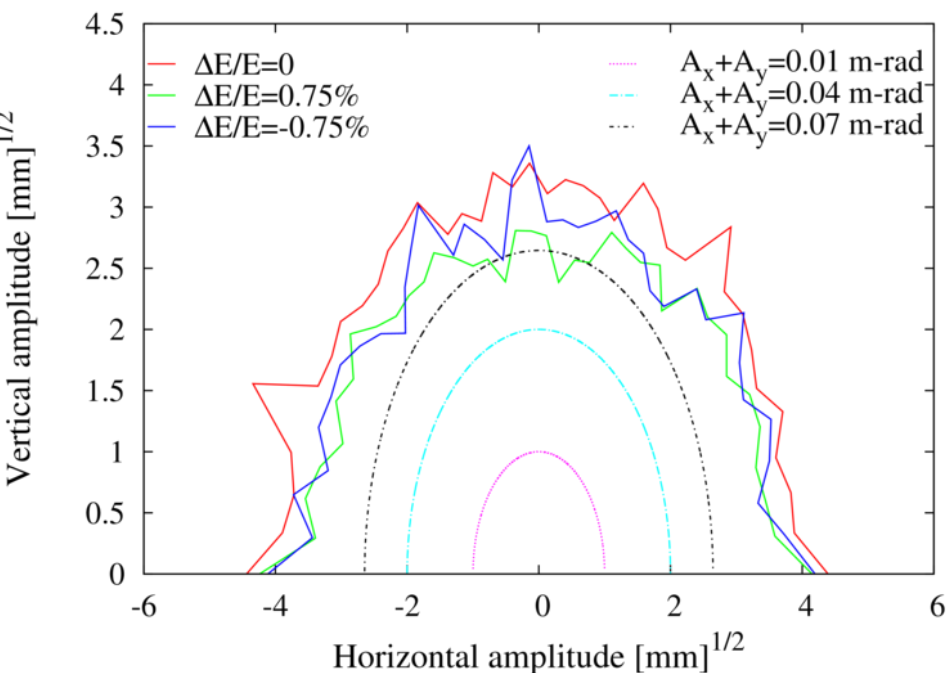


No multipoles

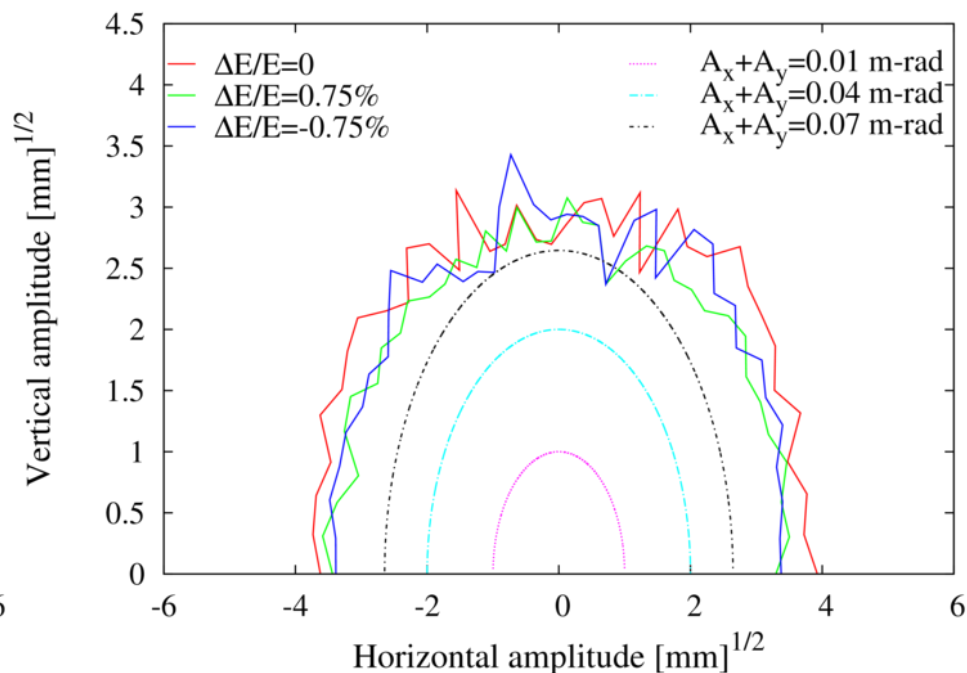


Systematic + random multipoles

- Using MAD-style wiggler model
- DA improves slightly when including multipoles



No multipoles



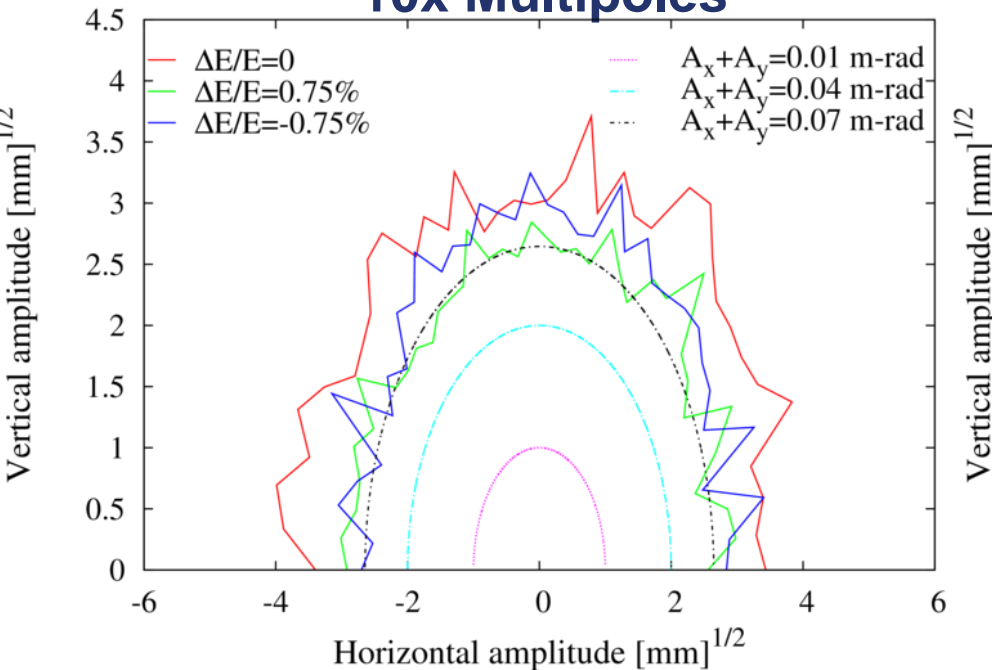
Systematic + random multipoles

- DA much reduced by including full wiggler map, but is still sufficient for ideal lattice

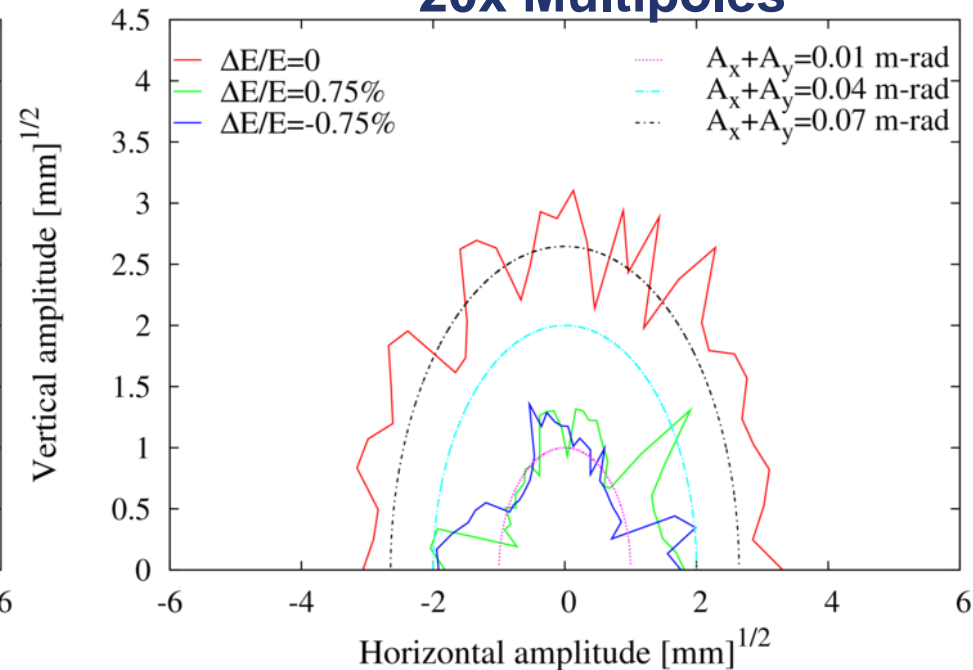
**From this point on, only consider Taylor map wigglers for DA**

# Increased Multipoles

## 10x Multipoles



## 20x Multipoles



- Using Taylor map for wigglers
- Increase multipoles from Y. Cai's table until dynamic aperture is impaired
- For ideal lattice, ~10x multipoles (systematic + random) may be acceptable
  - However, tolerance must be a balance between multipoles, misalignments, and number of BPMs; can't just consider multipoles by themselves

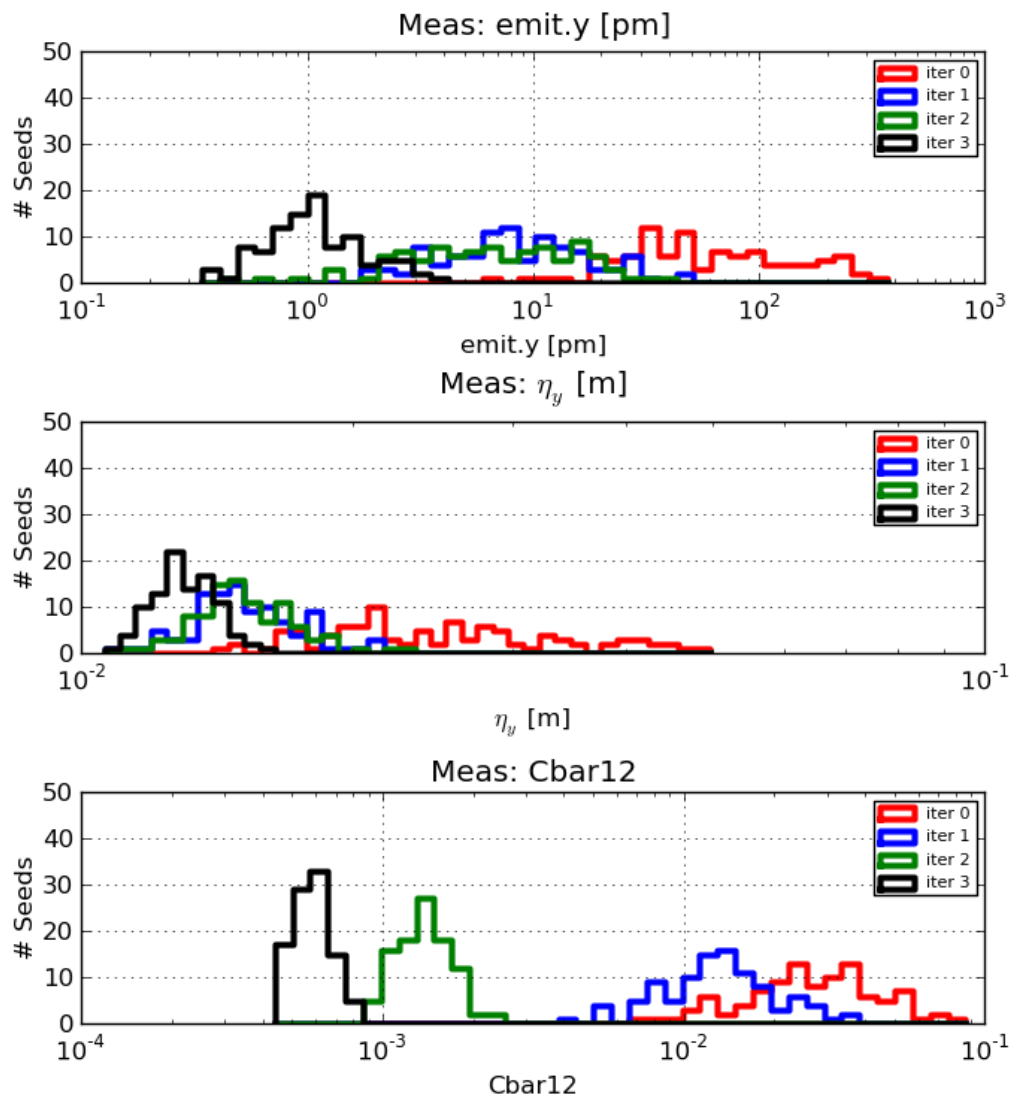


# Error Tolerance – ring\_ma

- Built on Bmad library
- Capable of introducing errors to any parameter for any element described by Bmad
  - Examples: offset (x,y,z), roll, pitch, k1, k2, arbitrary multipoles, corrector calibrations, ...
- Thorough characterization of BPM errors
  - Offset with respect to nearest quad; BPM tilt; relative button-to-button gain error; shot-to-shot repeatability
  - All simulated measurements used for corrections have BPM errors
- Multi-stage corrections
  - Simulate new measurements after each level of correction

# Example: Emittance Tuning at CESR/TA

- Model emittance correction procedure at CESR/TA
- Typical 95%CL correction levels:
  - $\eta_y = 15\text{mm}$
  - $\text{Cbar12} = 1 \times 10^{-3}$
- Consistent with measurements
- Confidence in ring\_ma for describing correction levels for coupling, dispersion





# Misalignments and BPM Resolution

Parameter	RMS	Affected by multiplier?
BPM – Differential resolution	1 $\mu\text{m}$	No
BPM – Absolute resolution	50 $\mu\text{m}$	No
BPM – Tilt	5 mrad	No
BPM button – Gain variation	0.5%	No
Quads + Sexts – Offset (H+V)	25 $\mu\text{m}$	Yes
Quads – Tilt	50 $\mu\text{rad}$	Yes
Dipole – Roll	50 $\mu\text{rad}$	Yes
Wiggler – Offset (V only)	100 $\mu\text{m}$	Yes
Wiggler - Roll	100 $\mu\text{rad}$	Yes
Multipoles (sys+rand)	2x PEP-II tables	Yes (random only)

Nominal misalignments and BPM  
tolerances for ring\_ma studies





# Emittance Tuning Procedure

- 1) Measure and correct orbit using all steerings
- 2) Measure betatron phase advance and coupling (by resonant excitation)
  - Correct using quadrupoles and skew quadrupoles
- 3) Measure orbit, coupling, and vertical dispersion
  - Simultaneously correct with vertical steerings and skew quadrupoles

# DTC04 – Error Tolerance

- Misaligned as per misalignment table
- Optics correction assuming BPM accuracy as tabulated and
  - 1 skew quad in each arc cell
  - 2 skew quads in each dispersion suppressor line
  - 1 H and V steering in each arc cell
  - 1 H&V steering adjacent to each quad in straights
  - BPM at every quadrupole

**Vertical emittance, dispersion and coupling (actual, not observed)  
after emittance tuning for 95%CL of 100 seeds**

	1x Errors		2x Errors	
Parameter	No Multipoles	Systematic+Random Multipoles	No Multipoles	Systematic+Random Multipoles
$\epsilon_y$	0.20 pm	0.20 pm	0.33 pm	0.41 pm
$\eta_y$	0.54 mm	0.53 pm	0.98 mm	1.07 mm
$C_{12}$	$3.86 \times 10^{-4}$	$3.83 \times 10^{-4}$	$7.76 \times 10^{-4}$	$8.71 \times 10^{-4}$

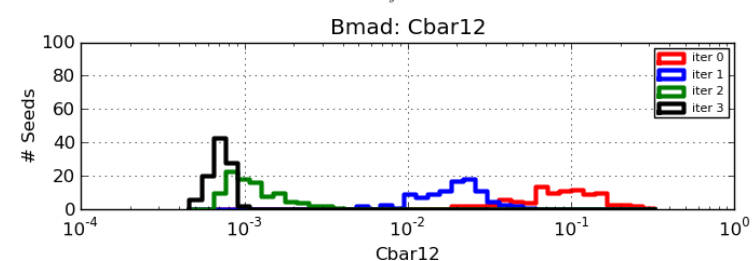
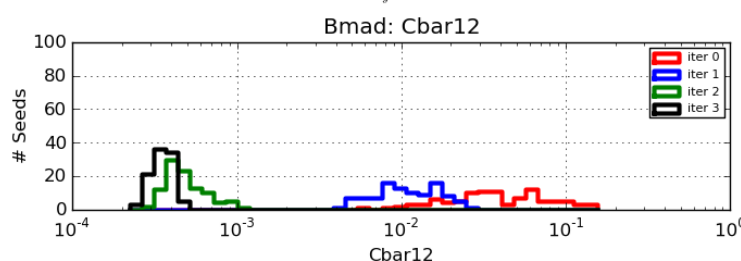
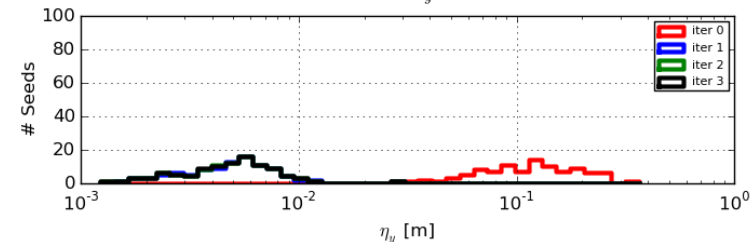
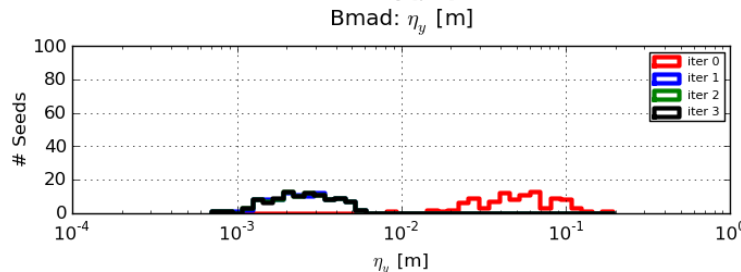
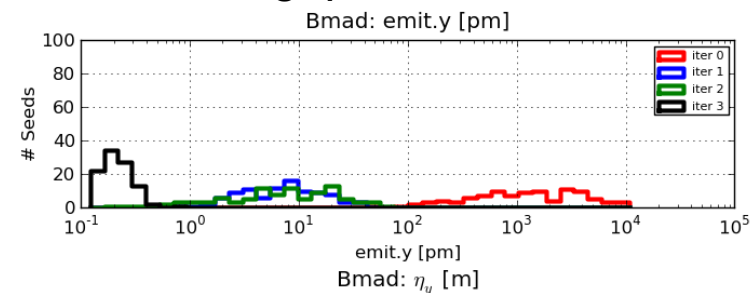
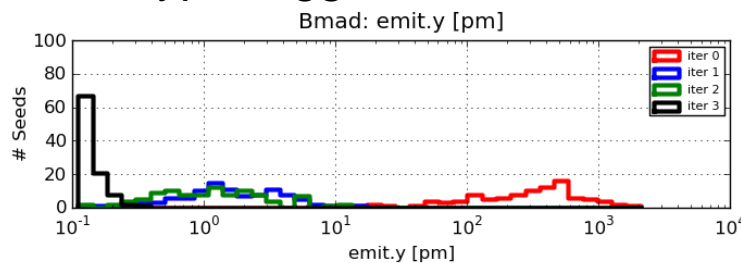
# Error Tolerance – MAD Wigglers

- Multipoles do not have a significant effect on optics correction
  - Will have a bigger effect on dynamic aperture, after misalignments and corrections
- Optics corrections are more or less unaffected by wiggler model
  - Opt to use MAD-type wigglers to increase simulation throughput

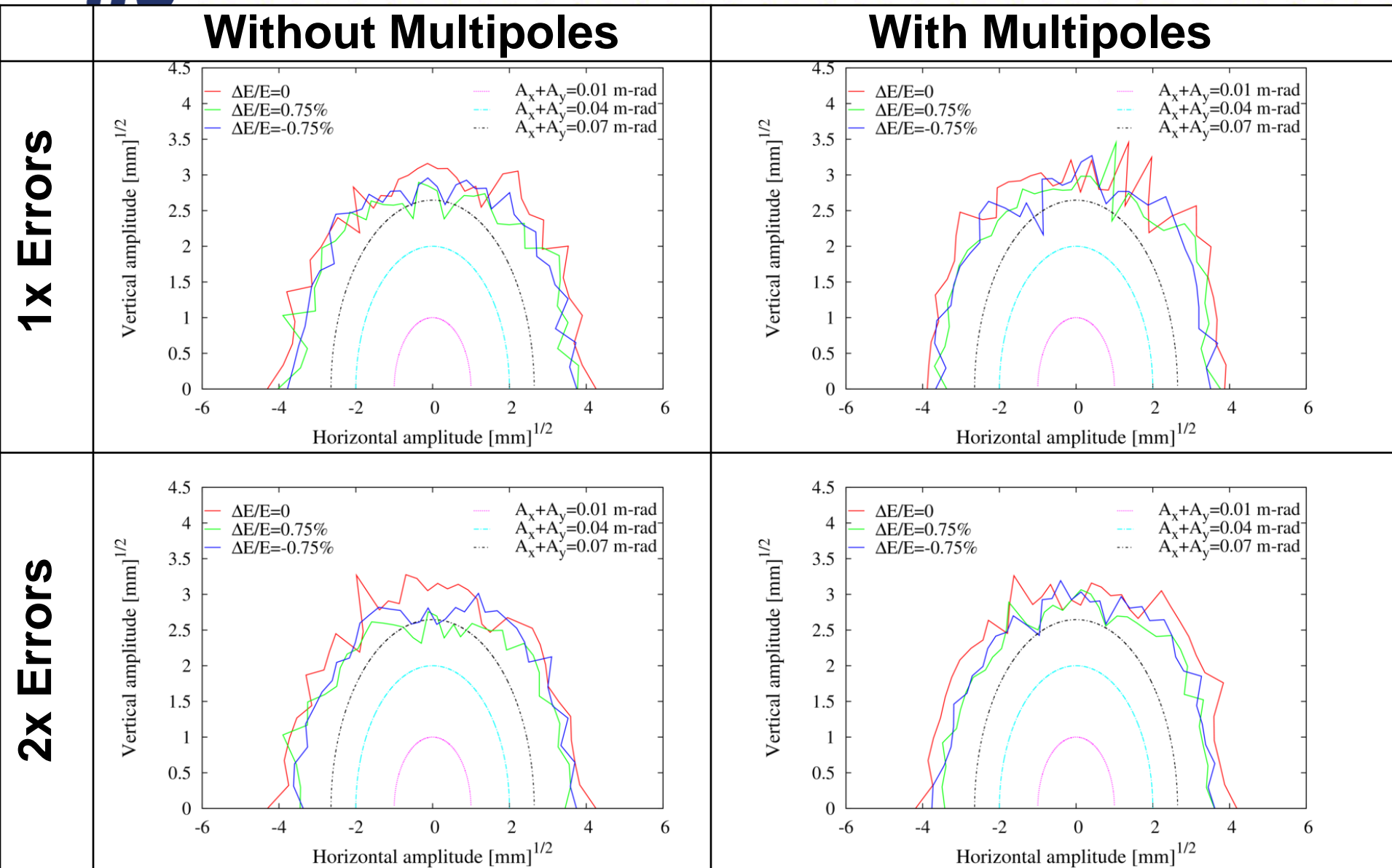
## Plots:

MAD wigglers  
No multipoles

Left: 1x errors  
Right: 2x errors

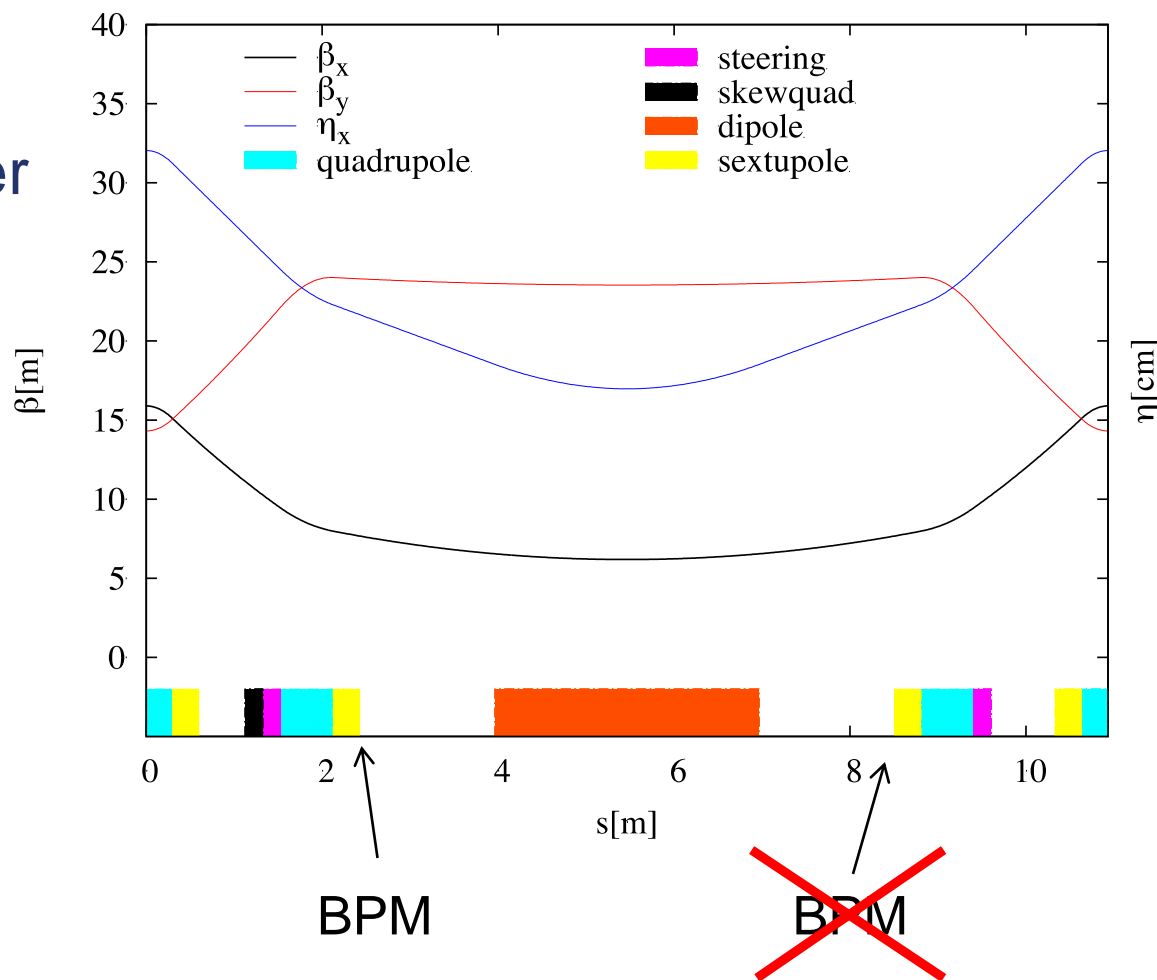


# Error Tolerance – Taylor Map W wigglers



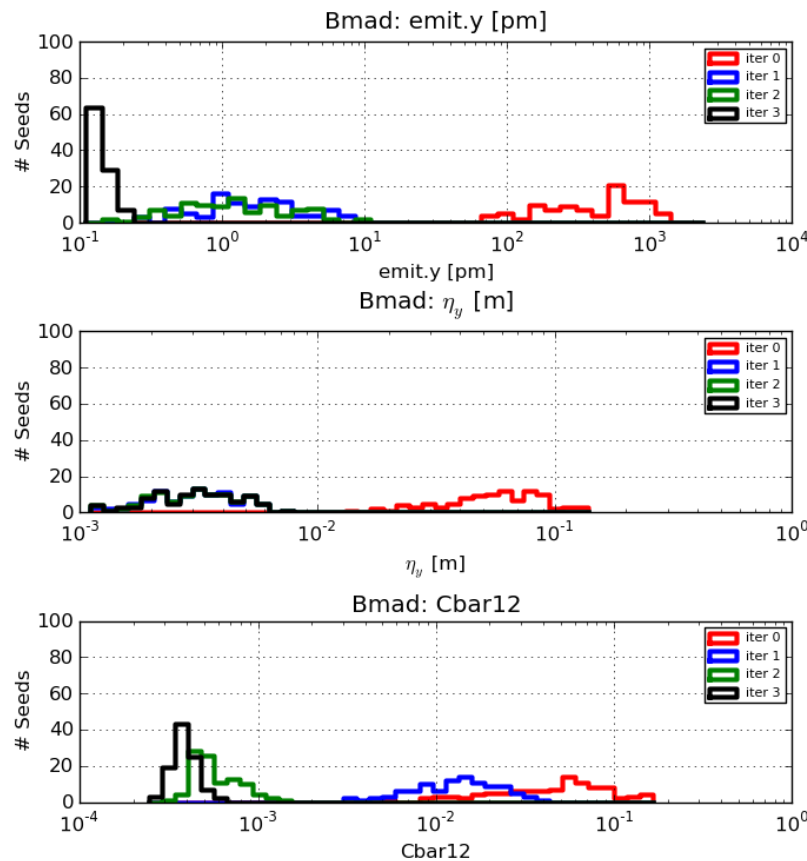
# Reduced Number of BPMs

- Reduce the total number of BPMs in the arcs by 50% (from 2/cell to 1/cell)

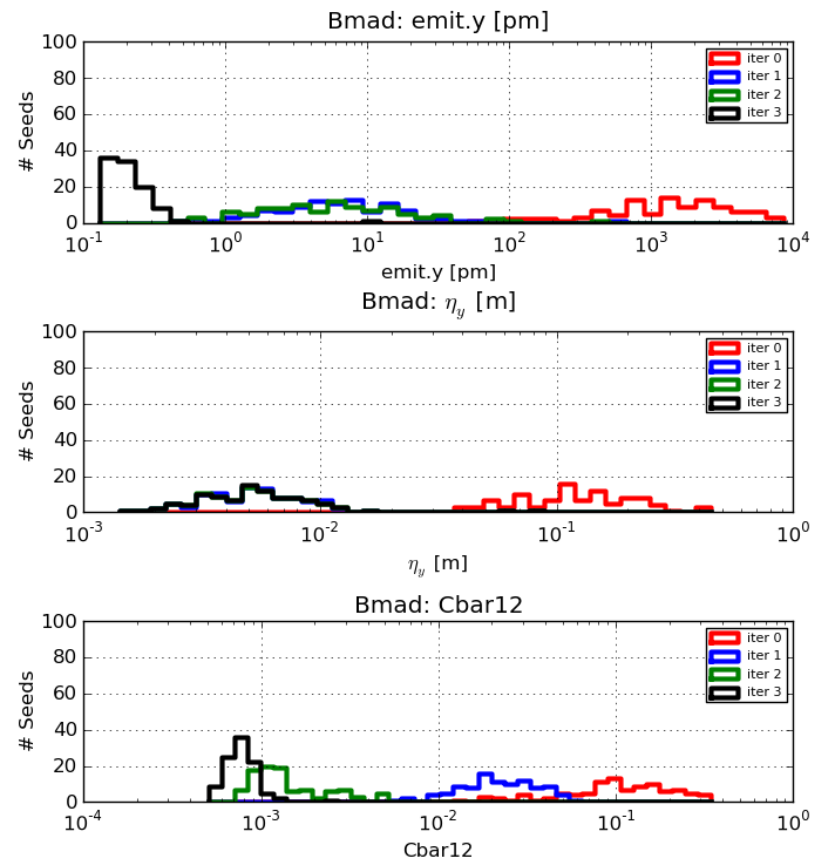


# Error Tolerance – Reduce BPMs in Arcs

- With reduced number of BPMs in arcs, still achieve emittance target
- Significant cost savings (511 BPMs  $\rightarrow$  361 BPMs = 30% reduction in BPMs)



MAD-type wigglers, 1x errors



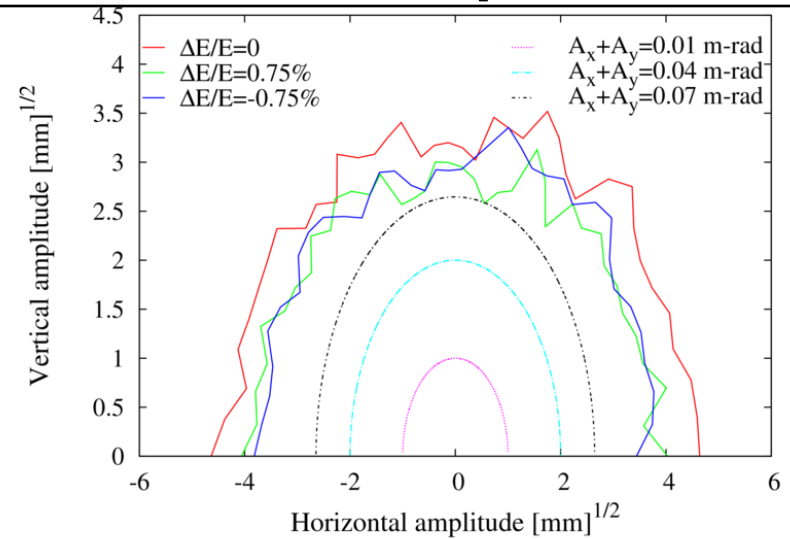
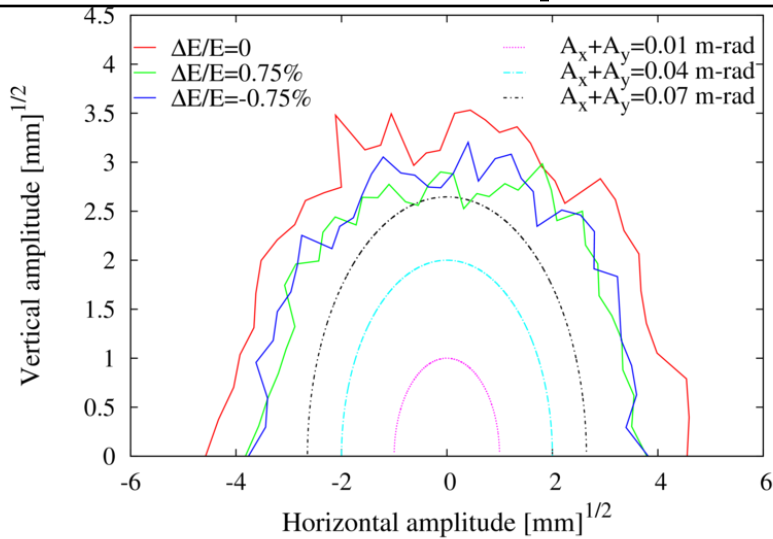
MAD-type wigglers 2x errors

# 50% Arc BPMs, 100% Straight BPMs

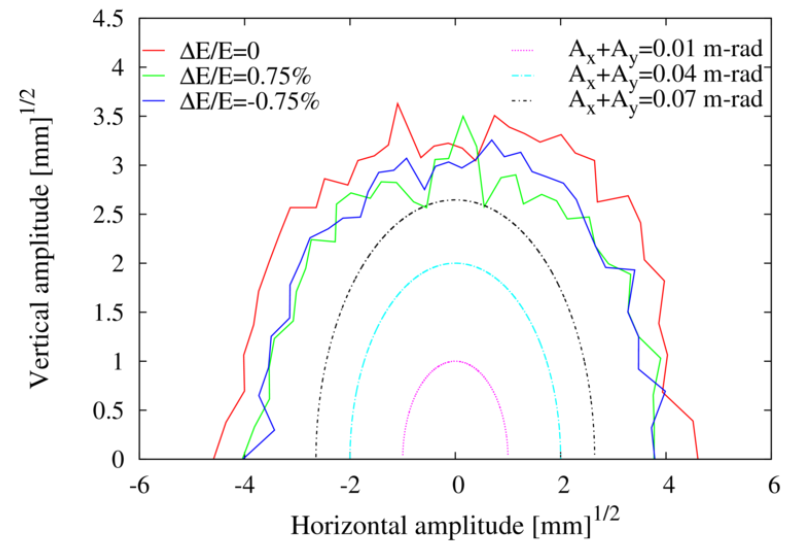
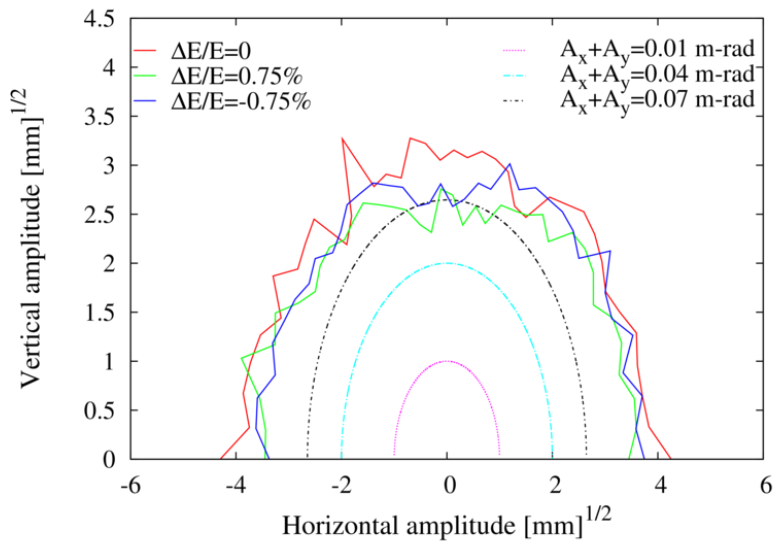
## Without Multipoles

## With Multipoles

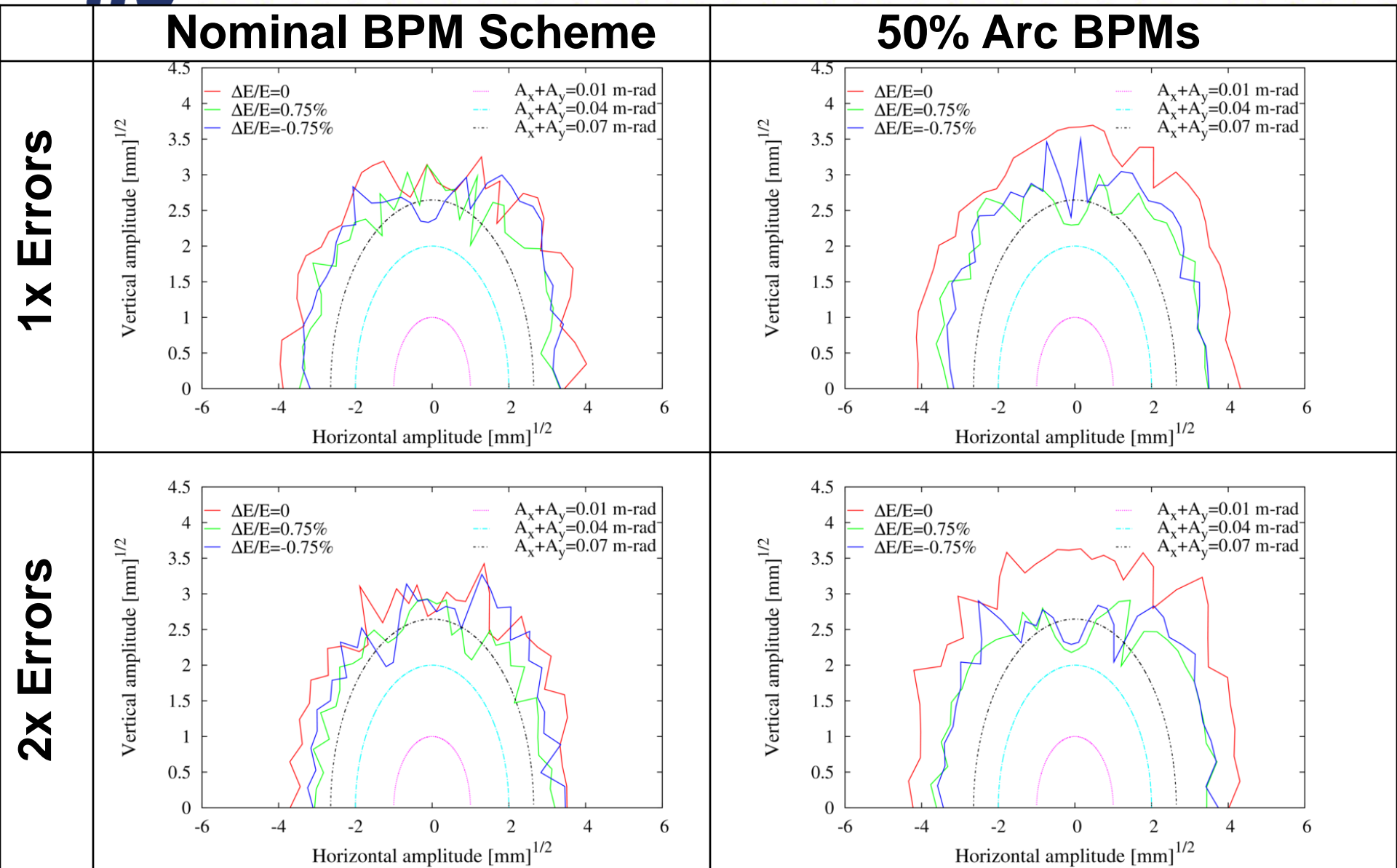
1x Errors



2x Errors



# Increase to 5x Multipoles







# Misalignment and BPM Resolution Tolerance

Updated to reflect maximum tolerance for  $\varepsilon_y < 2\text{pm-rad}$   
**and** sufficient dynamic aperture

Parameter	RMS
# of BPMs	361 (50% in arcs, 100% in straights)
BPM – Differential resolution	1 $\mu\text{m}$
BPM – Absolute resolution	50 $\mu\text{m}$
BPM – Tilt	5 mrad
BPM button – Gain variation	0.5%
Quads + Sexts – Offset (H+V)	50 $\mu\text{m}$
Quads – Tilt	100 $\mu\text{rad}$
Dipole – Roll	100 $\mu\text{rad}$
Wiggler – Offset (V only)	200 $\mu\text{m}$
Wiggler - Roll	200 $\mu\text{rad}$
Multipoles	2x PEP-II (systematic) 4x PEP-II (random)

## Status

- Updated constraints on magnet multipole and misalignment tolerances, consistent with  $\varepsilon_y = 2\text{pm-rad}$  and  $DA > 0.07\text{m-rad}$ :
  - Systematic multipoles: 2x PEP-II multipoles
  - Random multipoles: 4x PEP-II multipoles
  - Misalignments and BPM errors as per previous slide
- Reduced BPM count by 30% (511  $\rightarrow$  361)
  - 50% BPMs in arcs; maintain all BPMs in straights
- Sufficient dynamic aperture confirmed with reduced BPM count, full wiggler map, misalignments and corrections, and multipoles

## Ongoing effort

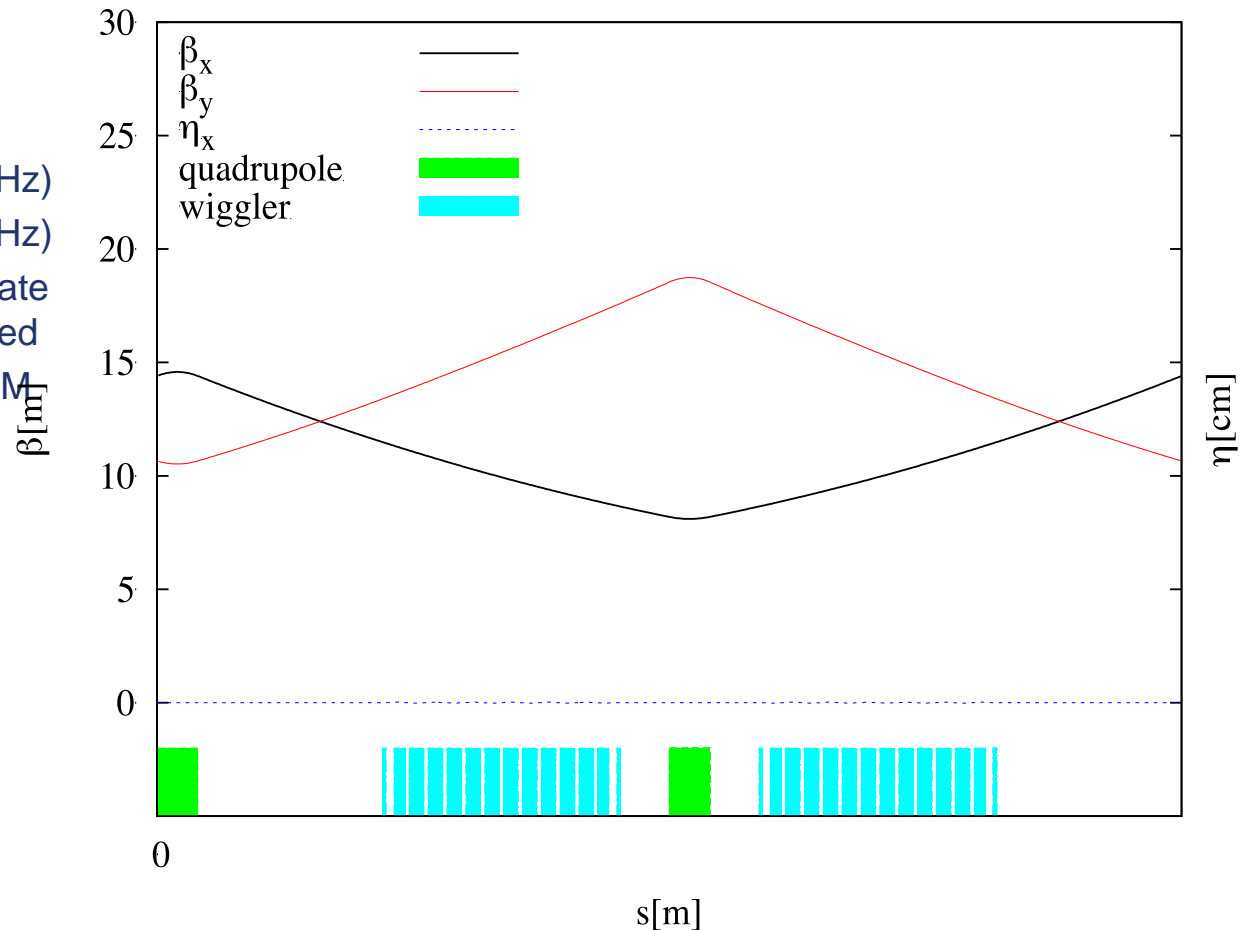
- Investigate increasing misalignment tolerances beyond 2x nominal values
  - Include dipole strength, quad k1, sextupole k2 errors
- Emittance tuning with fewer correctors; reduced number of BPMs in straights
- Explore tune plane for better dynamic aperture
- Alternate sextupole distributions for more DA



# Backup Slides

# Damping Wigglers

- Wiggler straight
  - 2 wigglers/cell
  - 30 cells
  - 2.1 m wiggler
  - $1.5\text{T} < B_{\text{peak}} < 2.2\text{T}$
  - 54 @  $2.16\text{T} \Rightarrow \tau_x = 13\text{ms}$  (10Hz)
  - 54 @  $1.51\text{T} \Rightarrow \tau_x = 25\text{ms}$  (5Hz)
  - 3 empty cells will accommodate 6 additional wigglers if required
  - H&V dipole corrector and BPM adjacent to each quad



## • RF

- 2 cavities/cell
- 22.4 MV  $\Rightarrow$  6mm bunch length @  $\tau_x = 13\text{ms}$
- $\Rightarrow$  for 12 cavities

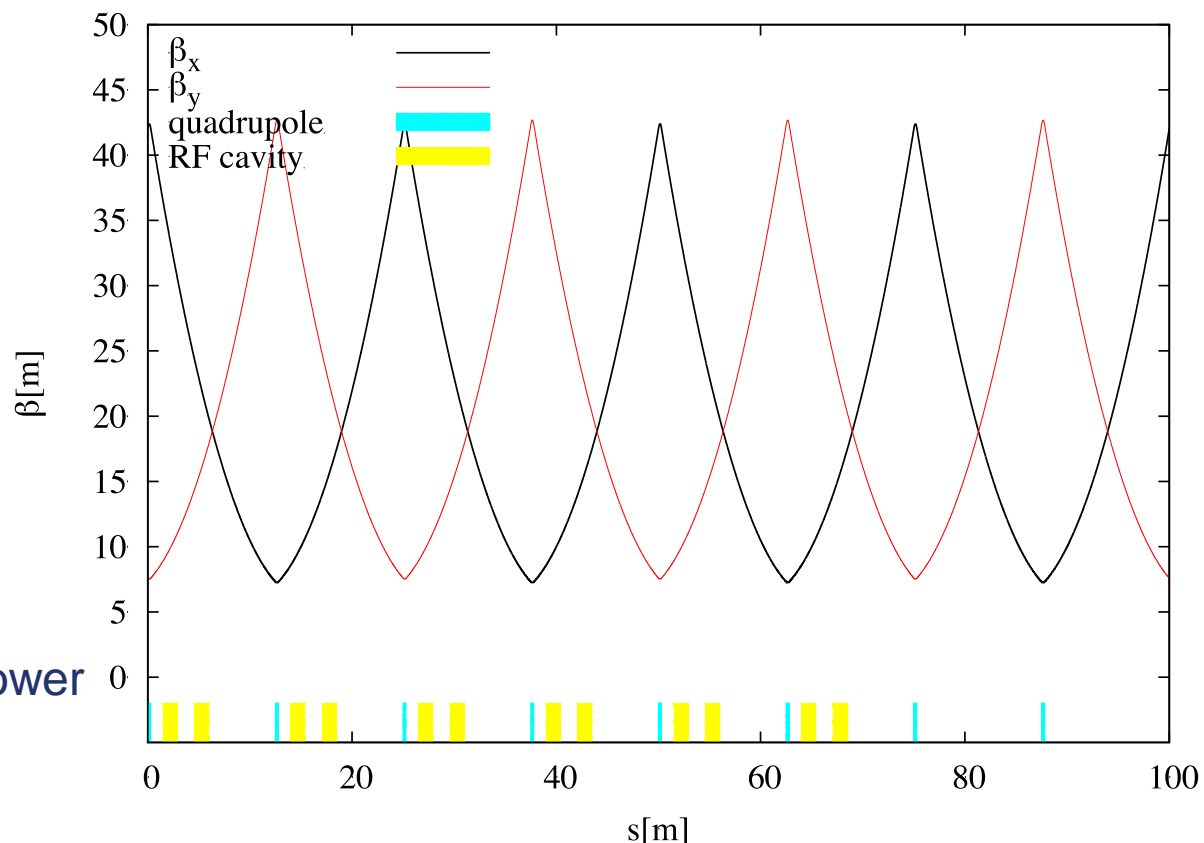
1.9MV/cavity

272kW/coupler

Lattice can accommodate  
16 cavities if required

Cavities offset so that  
waveguides of upper and lower  
rings are interleaved

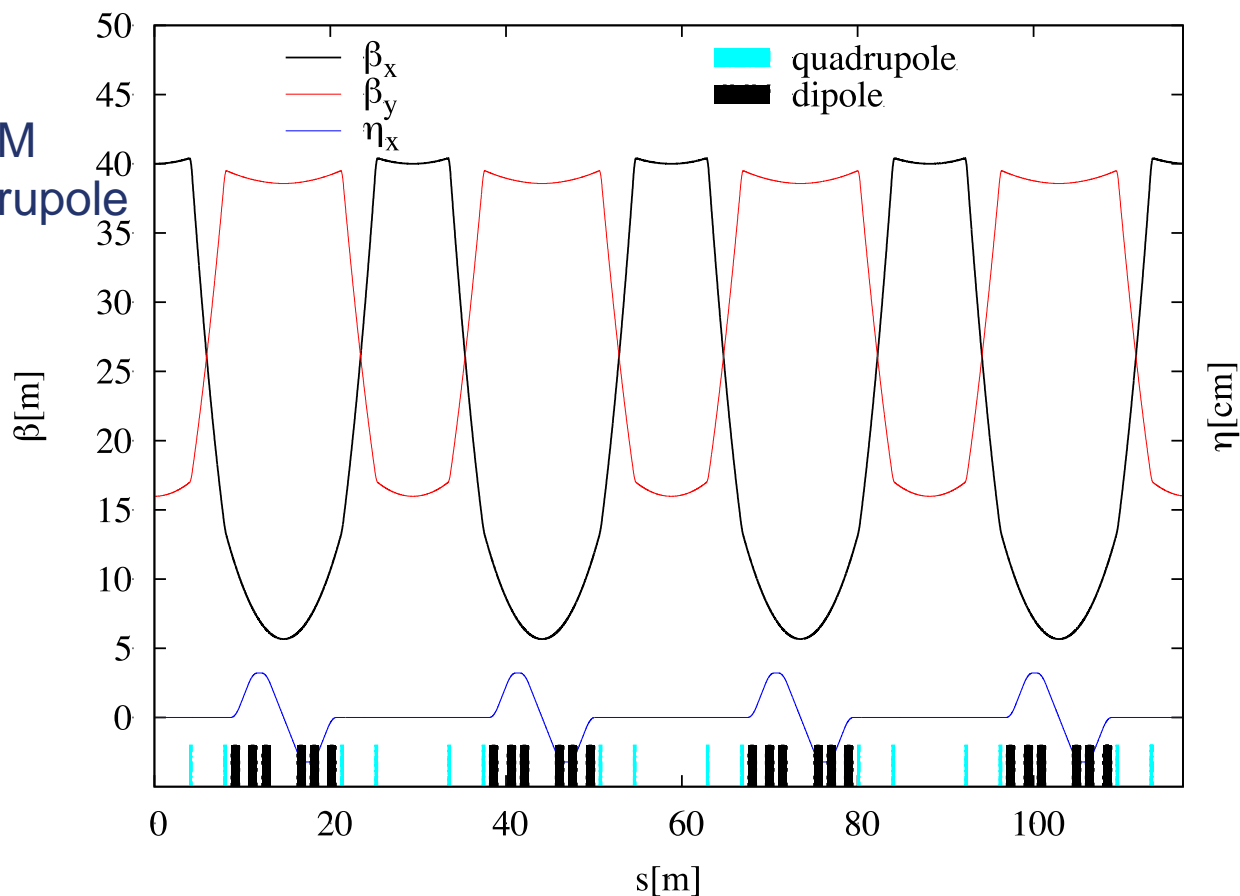
H&V corrector and BPM  
adjacent to each quadrupole



# Circumference chicane

- Chicane

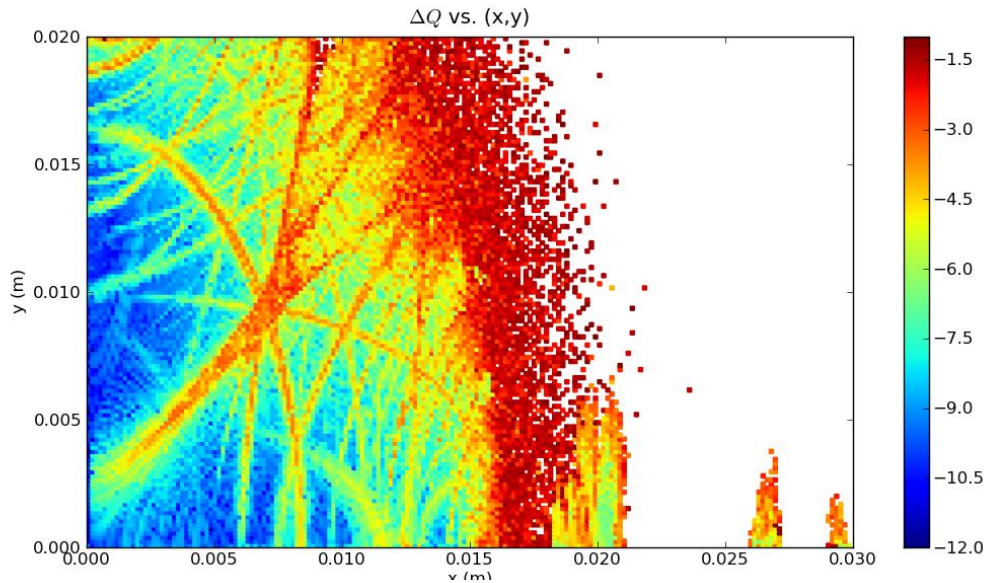
- $\Delta C = \pm 4\text{mm}$
- $\Delta\epsilon_y < 3\%$
- H&V corrector and BPM adjacent to each quadrupole



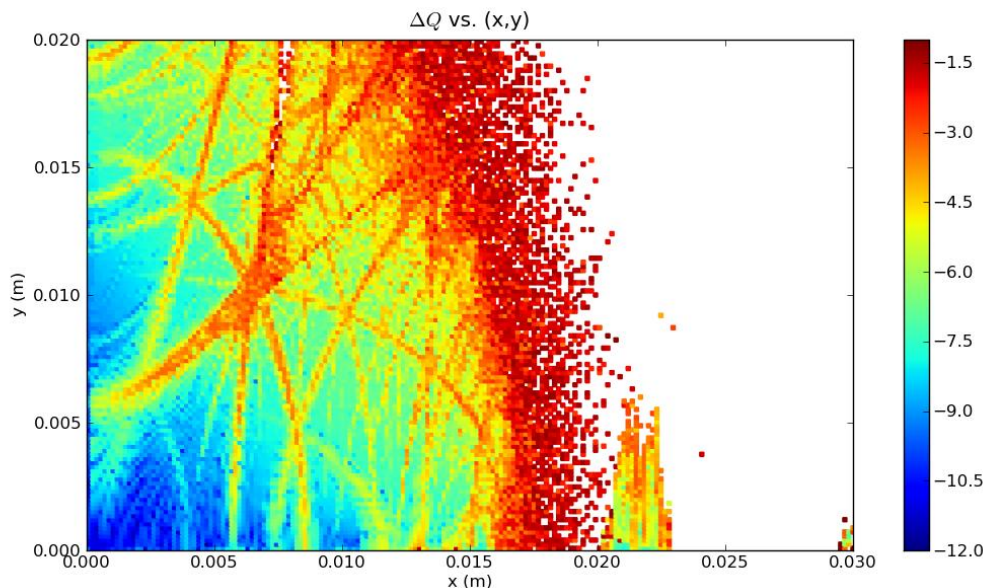
# Frequency maps

- With and without multipoles
  - (static + random) vs. no multipoles
  - Scan amplitudes (0:30mm)x(0:20mm)
  - Track 2048 turns; FFT first and last 1024 turns
  - Plot:
    - $\Delta Q$  vs. (x,y)
    - $\Delta Q$  vs. (Qx, Qy) [tunes from first 1024 turns]
- Maps for a single seed (with misalignments and corrections) per scenario

# DTC04-5Hz Frequency maps



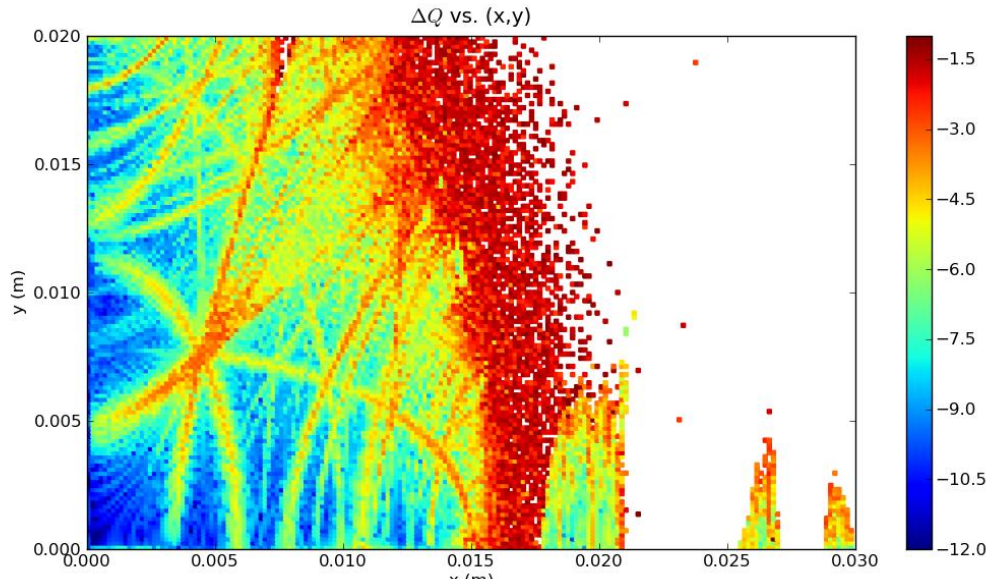
- No Multipoles
- Random misalignments
- Corrections



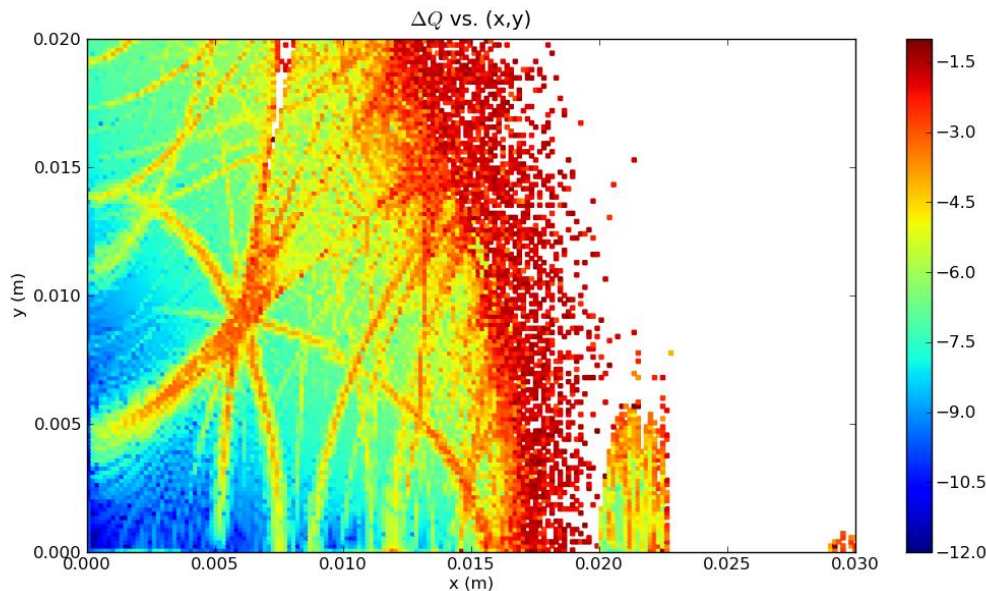
- Static + Random Multipoles
- Random misalignments
- Corrections



# DTC04-10Hz Frequency maps



- No Multipoles
- Random misalignments
- Corrections



- Static + Random Multipoles
- Random misalignments
- Corrections

$\Delta Q$  vs.  $(Q_x, Q_y)$

- No Multipoles
- Random misalignments
- Corrections

- Static + Random Multipoles
- Random misalignments
- Corrections

