

Higgs boson pair production at a photon-photon collision in the two Higgs doublet model

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Introduction

The Higgs sector is the last unknown part of the standard model.

Higgs potential

$$V = \frac{1}{2}m_h^2 h^2 + \frac{1}{3!}\lambda_{hhh} h^3 + \frac{1}{4!}\lambda_{hhhh} h^4 + \dots$$

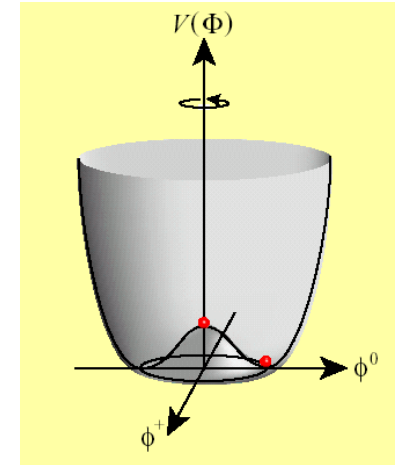
In the SM, tree level hhh coupling is given by

$$\lambda_{hhh}^{\text{SM}} = \frac{3m_h^2}{v}$$

It is important to measure the Higgs mass and the Higgs self-coupling.

- Test for the Higgs potential
- Search for New Physics effect

Higgs self coupling measurement is one of main purposes at the ILC.



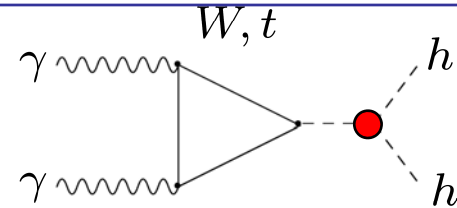
Measurement of hhh coupling

Measurement at collider experiment

LHC (SLHC) $gg \rightarrow hh$

ILC $e^+e^- \rightarrow Zhh$ $e^+e^- \rightarrow hh\bar{\nu}\nu$

PLC $\gamma\gamma \rightarrow hh$
My talk focus on this process.



Photon Linear Collider (PLC) is optional experiment for ILC

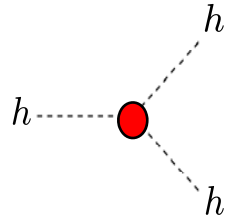
We estimate sensitivity of hhh coupling at the PLC.

We calculate $\gamma\gamma \rightarrow hh$ in THDM

$\gamma\gamma \rightarrow hh$ process

We consider anomalous hhh coupling

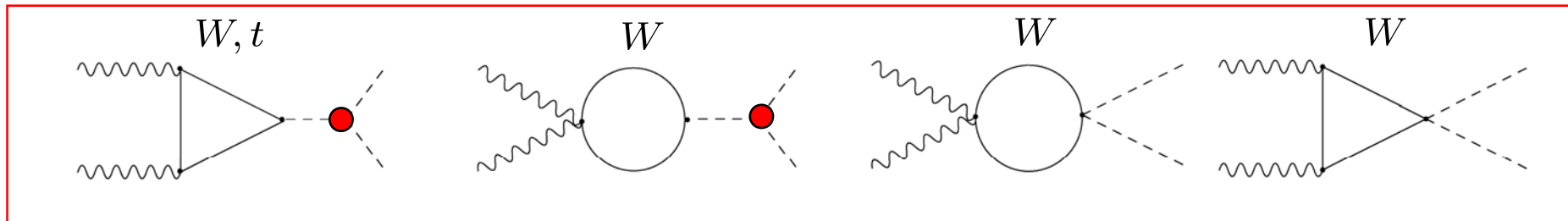
$$\lambda_{hhh}^{\text{SM}} = \frac{3m_h^2}{v}$$



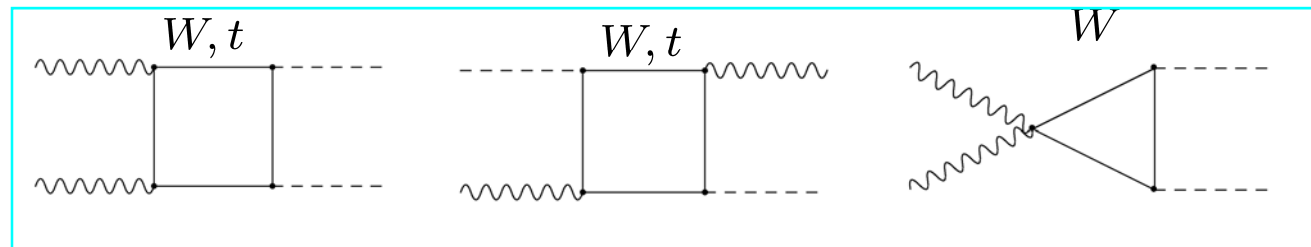
$$\lambda_{hhh} = \lambda_{hhh}^{\text{SM}} + \delta\lambda = \lambda_{hhh}^{\text{SM}}(1 + \delta\kappa)$$

SM diagrams

pole



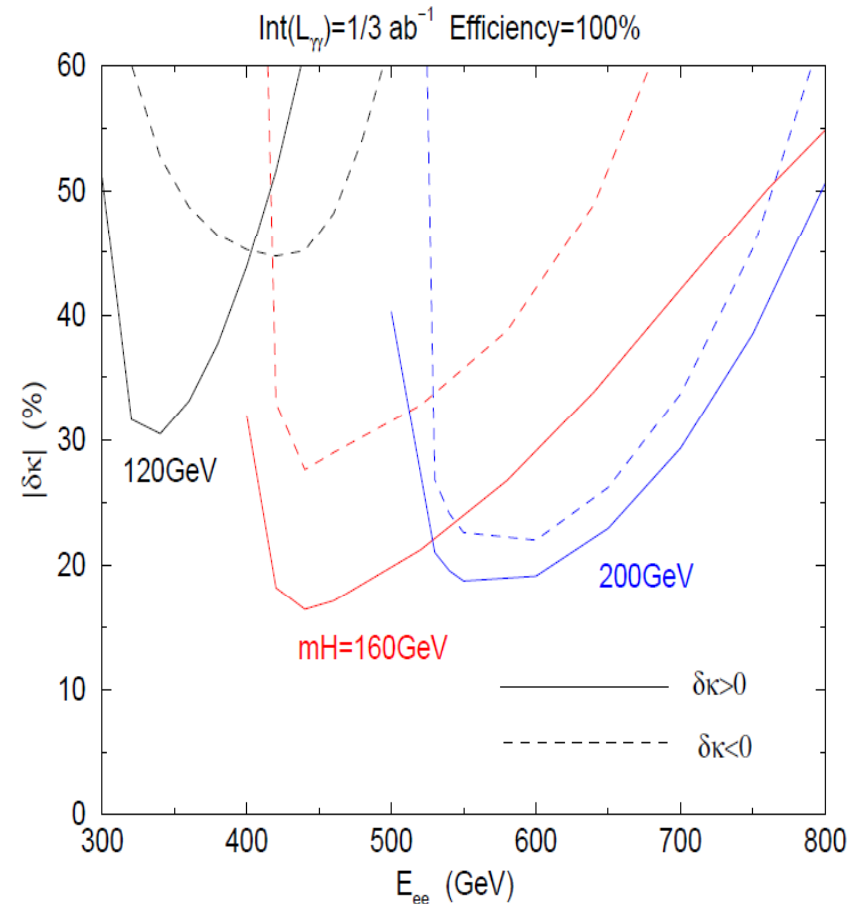
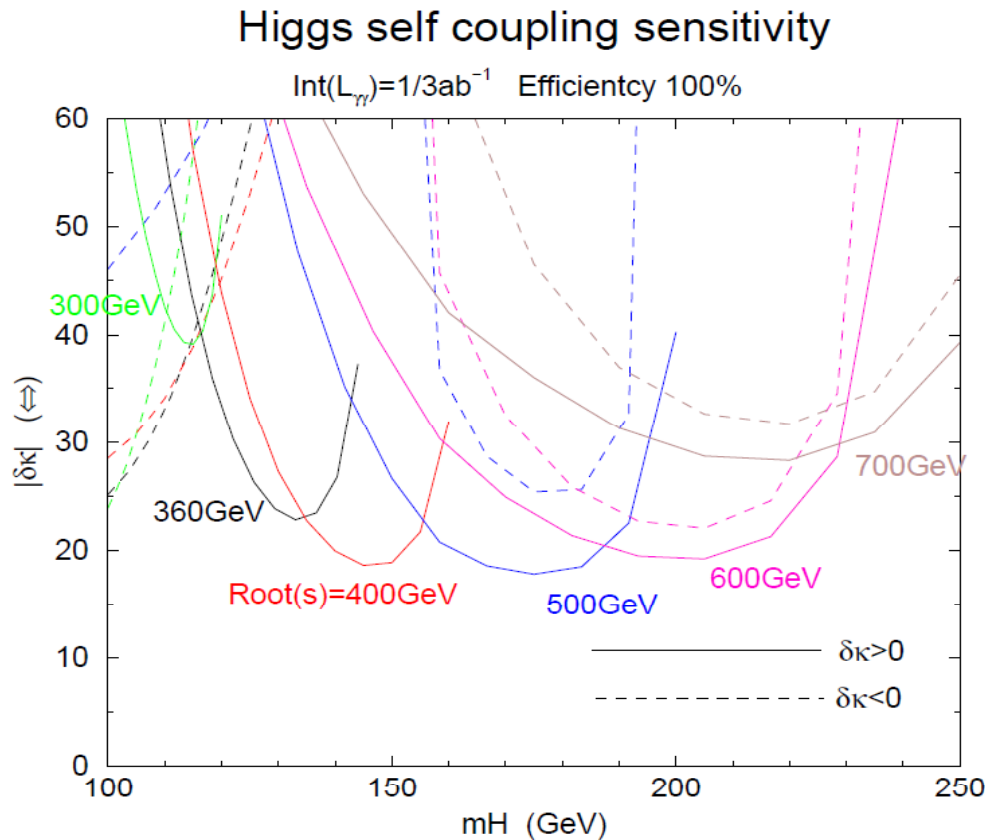
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Estimation of hhh sensitivity

E.Asakawa, D. Harada, S. Kanemura, Y. Okada, K. Tsumura at TILC 08

Higgs Self Coupling Sensitivity



Photon linear collider ($E_{ee} < 500\text{GeV}$) is useful to measure the HHH coupling for $m_H = 150\text{-}200$.

$\gamma\gamma \rightarrow hh$ in the THDM

We calculated $\gamma\gamma \rightarrow hh$ process in THDM with SM-like limit

- Non-decoupling effects
- Charged Higgs loop effects

Two Higgs Doublet Model

Higgs potential

$$V_{\text{THDM}} = \mu_1^2 |\Phi_1|^2 + \mu_2^2 |\Phi_2|^2 - (\mu_3^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ + \lambda_1 |\Phi_1|^4 + \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{\lambda_5}{2} \{(\Phi_1^\dagger \Phi_2)^2 + \text{h.c.}\}$$

Higgs doublets

$$\Phi_i = \begin{pmatrix} \omega_i^+ \\ \frac{1}{\sqrt{2}}(v_i + h_i + iz_i) \end{pmatrix} \quad (i = 1, 2)$$

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = R(\alpha) \begin{pmatrix} H \\ h \end{pmatrix} \\ \begin{pmatrix} z_1 \\ z_2 \end{pmatrix} = R(\beta) \begin{pmatrix} z \\ A \end{pmatrix} \\ \begin{pmatrix} \omega_1^+ \\ \omega_2^+ \end{pmatrix} = R(\beta) \begin{pmatrix} \omega^+ \\ H^+ \end{pmatrix} \quad R(\theta) = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$

$$\tan \beta = \frac{v_2}{v_1} \quad v^2 = v_1^2 + v_2^2 \simeq (246 \text{ GeV})^2$$

CP-even h, H CP-odd A Charged bosons H^\pm

$$m_h^2 = \{\lambda_1 \cos^4 \beta + \lambda_2 \sin^4 \beta + 2(\lambda_3 + \lambda_4 + \lambda_5) \cos^2 \beta \sin^2 \beta\} v^2$$

$$m_H^2 = M^2 + \frac{1}{8} \{\lambda_1 + \lambda_2 - 2(\lambda_3 + \lambda_4 + \lambda_5)\} (1 - \cos 4\beta) v^2$$

$$m_A^2 = M^2 - \lambda_5 v^2$$

$$m_{H^\pm}^2 = M^2 - \frac{\lambda_4 + \lambda_5}{2} v^2$$

$$M = \frac{|\mu_3|}{\sqrt{\sin \beta \cos \beta}}$$

We consider following parameters

- SM-like limit $\sin(\alpha - \beta) = -1$

Lightest Higgs has the same tree-level coupling as the SM Higgs boson and the other Higgs bosons do not couple to gauge bosons.

- Non-decoupling limit $M = 0$

In the THDM, extra Higgs boson loop correction is known as non-decoupling effect.

- rho parameter constrain $m_H \simeq m_A \simeq m_{H^\pm}$

$$m_H = m_A = m_{H^\pm}$$

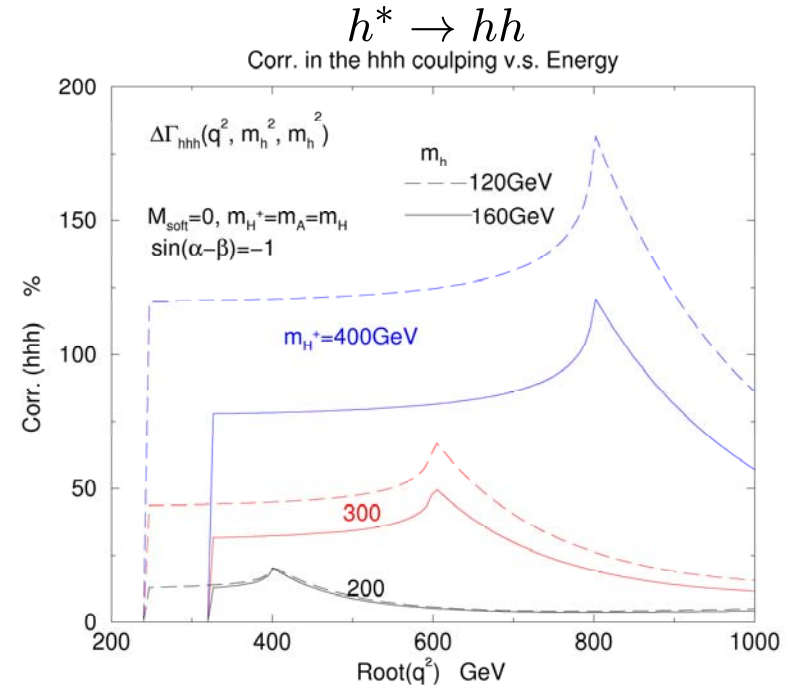
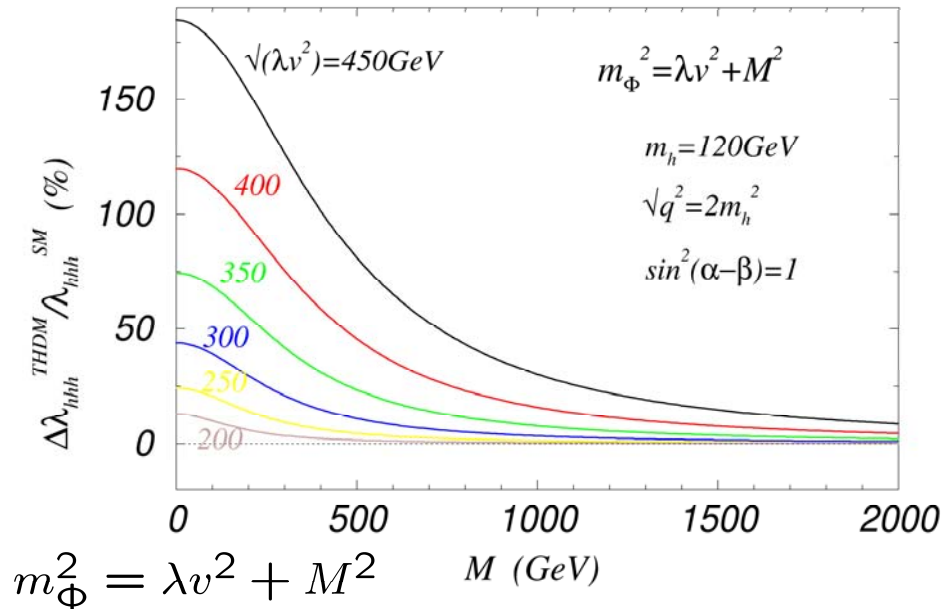
We assume that the masses of the extra Higgs bosons degenerate.

New Physics effect on hhh coupling

S. Kanemura, Y. Okada, E. Senaha, C. P. Yuan

$M \sim 0$
non-decoupling

$M \gg v$
decoupling



Effective hhh coupling

$$\Gamma_{hhh}^{\text{THDM}} \simeq -\frac{3m_h^2}{v} \left[1 + \sum_{\Phi} \frac{m_{\Phi}^4}{12\pi^2 v^2 m_h^2} \left(1 - \frac{M^2}{m_{\Phi}^2} \right)^3 - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} \right]$$

m_{Φ}^4 term appear in 1-loop correction

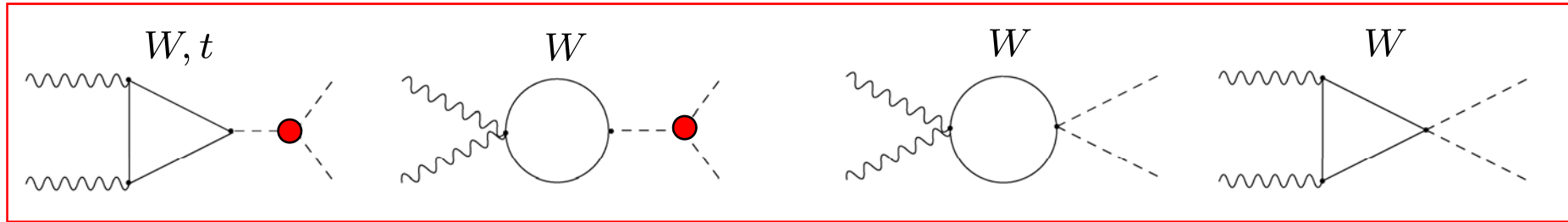
$$\frac{\Delta\Gamma_{hhh}^{\text{THDM}}}{\Gamma_{hhh}^{\text{SM}}} \equiv \frac{\Gamma_{hhh}^{\text{THDM}} - \Gamma_{hhh}^{\text{SM}}}{\Gamma_{hhh}^{\text{SM}}}$$

We set $M=0$. H, A, H^{\pm} receive their masses from the VEV.

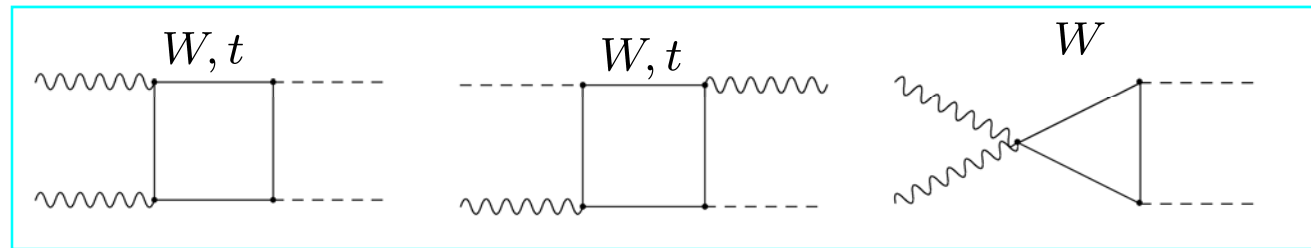
heavier Higgs boson loop effect $\sim 100\%$ non-decoupling

Effective hhh coupling

$$\begin{array}{c}
 \begin{array}{c} h \\ \diagup \\ \text{---} \bullet \text{---} \\ \diagdown \\ h \end{array} = \begin{array}{c} h \\ \diagup \\ \text{---} \\ \diagdown \\ h \end{array} + \text{"extra Higgs boson / top" loop effect} \\
 \mathcal{M}(l_1, l_2) \quad \text{W boson and top loop diagrams} \quad \gamma\gamma \rightarrow hh \quad \text{pole}
 \end{array}$$

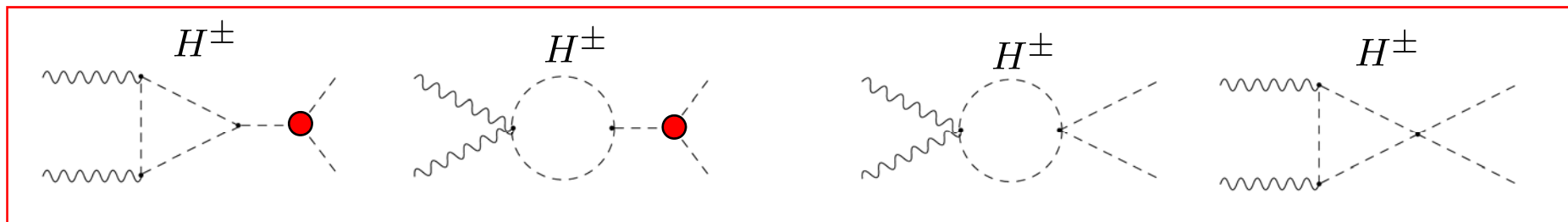


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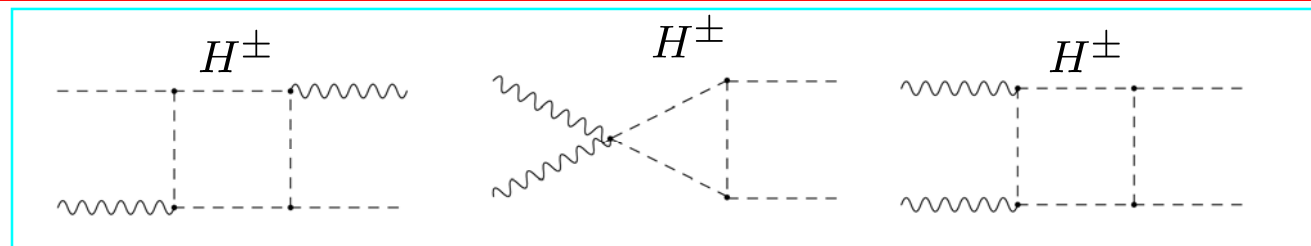


$\Delta\mathcal{M}(l_1, l_2)$ Additional one-loop diagrams (charged Higgs boson loop)

pole



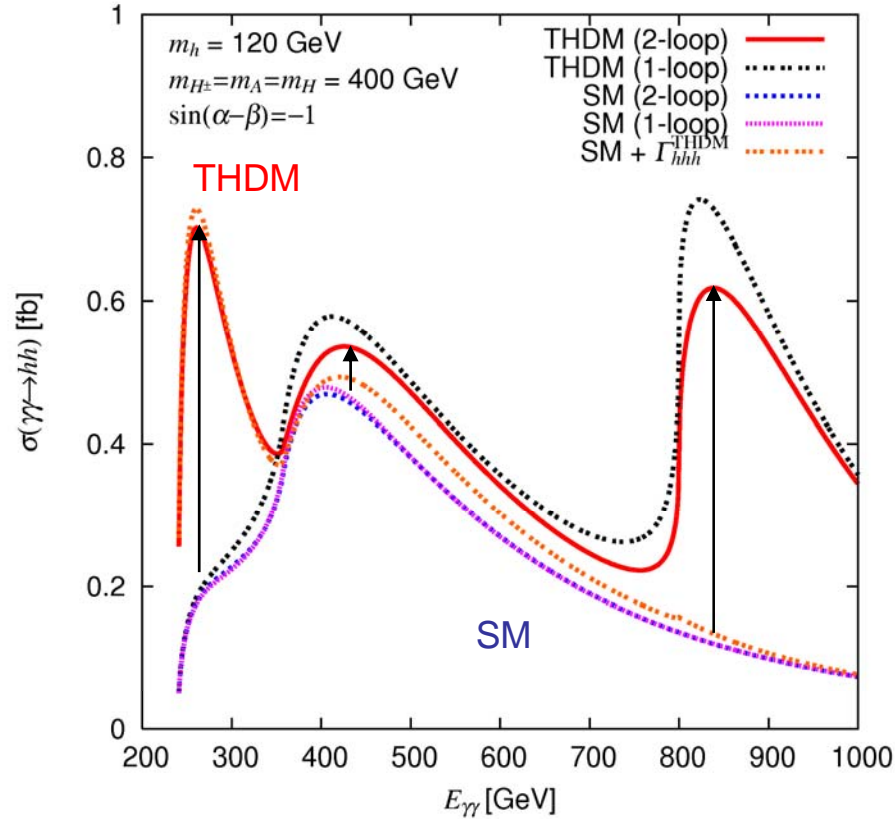
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$$m_H = m_A = m_{H^\pm} = 400 \text{ GeV}$$

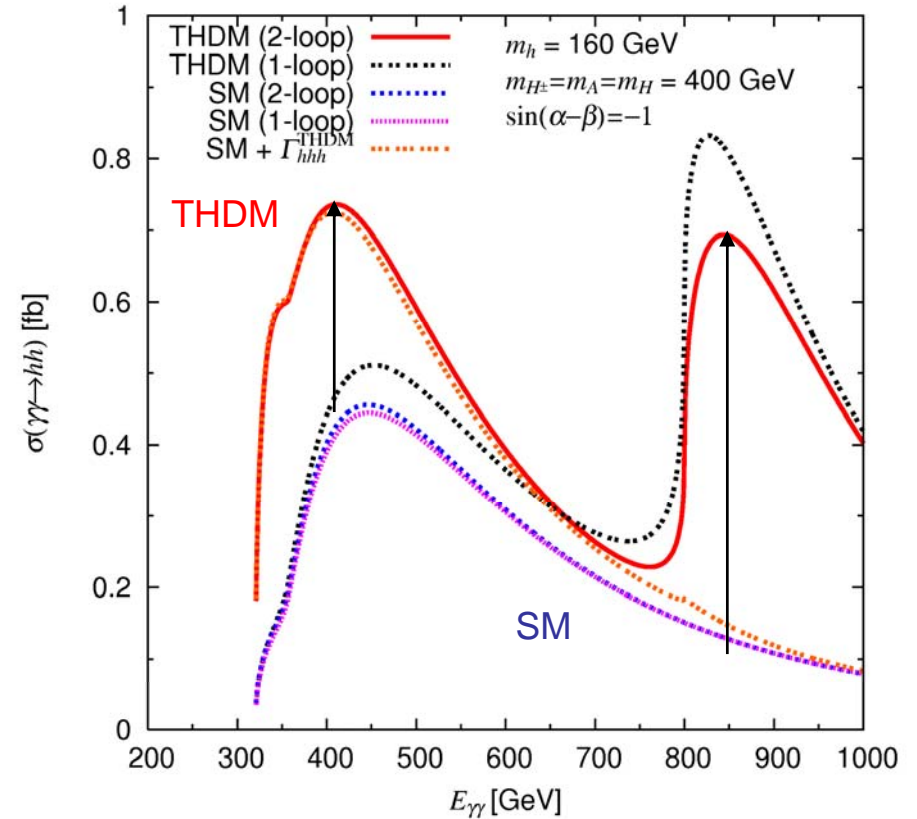
$$m_h = 120 \text{ GeV}$$

Sub cross section (++)



$$m_h = 160 \text{ GeV}$$

Sub cross section (++)



$E_{\gamma\gamma} \sim 250 \text{ GeV}$ Cross section is enhanced by the effect of $\frac{\Delta\Gamma_{hhh}^{\text{THDM}}}{\Gamma_{hhh}^{\text{SM}}} \sim 120\%$

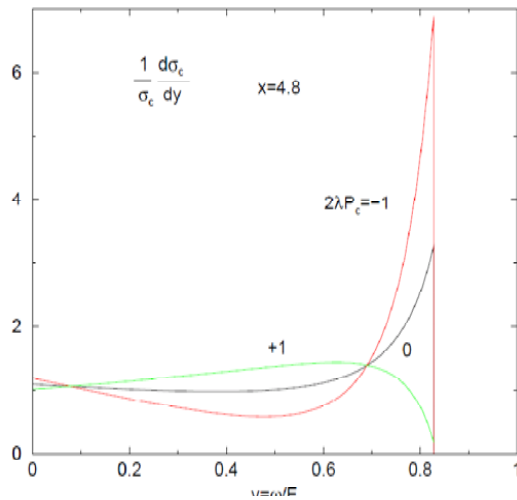
$E_{\gamma\gamma} \sim 400 \text{ GeV}$ Threshold enhancement of top pair production

$E_{\gamma\gamma} \sim 850 \text{ GeV}$ Threshold enhancement of charged Higgs pair production

Full Cross Section

Photon luminosity spectrum

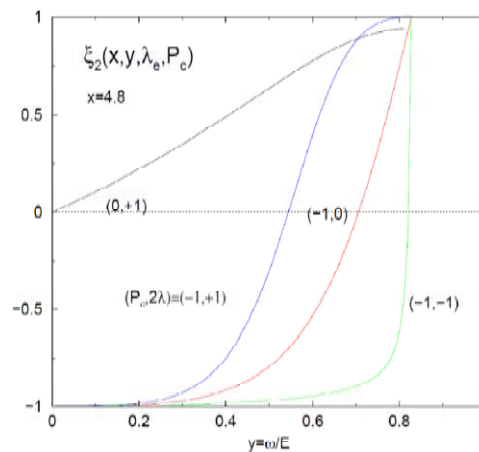
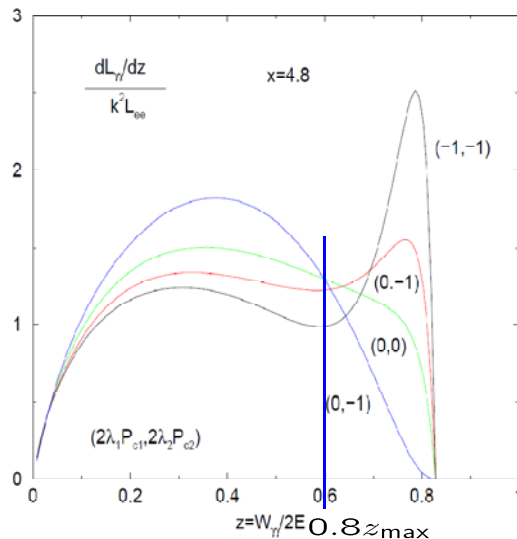
Ginzburg, et. al



$$d\sigma = \int_{\tau/y_m}^{y_m} d\tau \frac{dL_{\gamma\gamma}}{d\tau} \left(\frac{1 + \langle \xi_2^{(1)} \xi_2^{(2)} \rangle}{2} d\hat{\sigma}(+,+) + \frac{1 - \langle \xi_2^{(1)} \xi_2^{(2)} \rangle}{2} d\hat{\sigma}(+,-) \right)$$

$$\frac{L_{\gamma\gamma}}{d\tau} = \int_{\tau/y_m}^{y_m} \frac{dy}{y} f_\gamma(x, y) f_\gamma(x, \tau/y)$$

$$\tau = \hat{s}/s, y = E_\gamma/E_e \quad y_m = \frac{x}{1+x}, x = \frac{4E_e\omega_0}{m_e^2}$$



$\langle \xi_2 \rangle$: mean polarization
of the γ beam

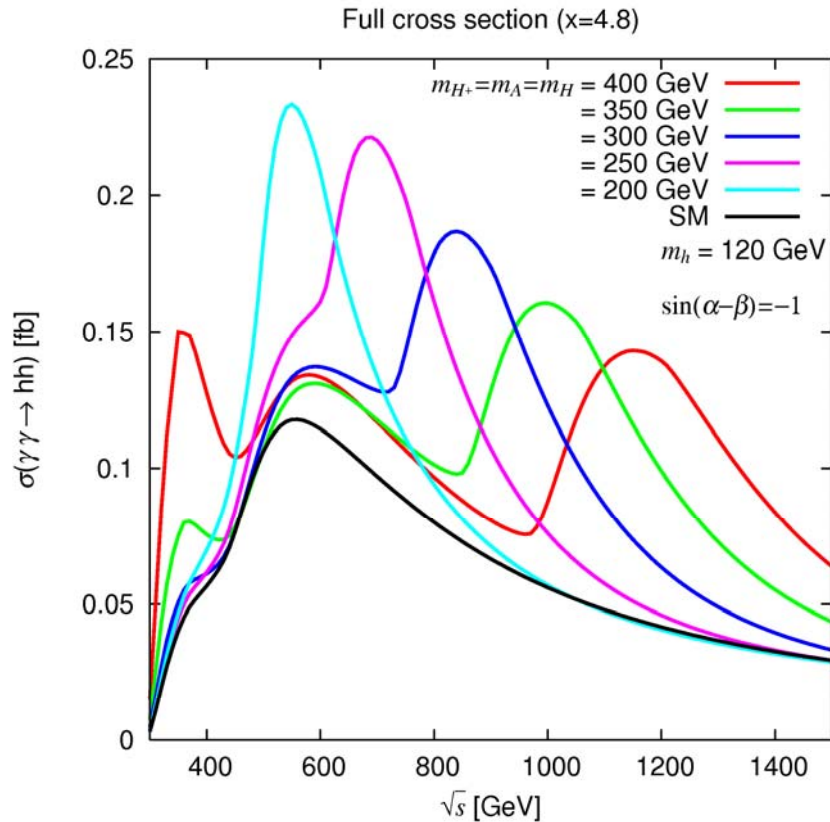
λ_e : electron helicity

P_c : laser photon

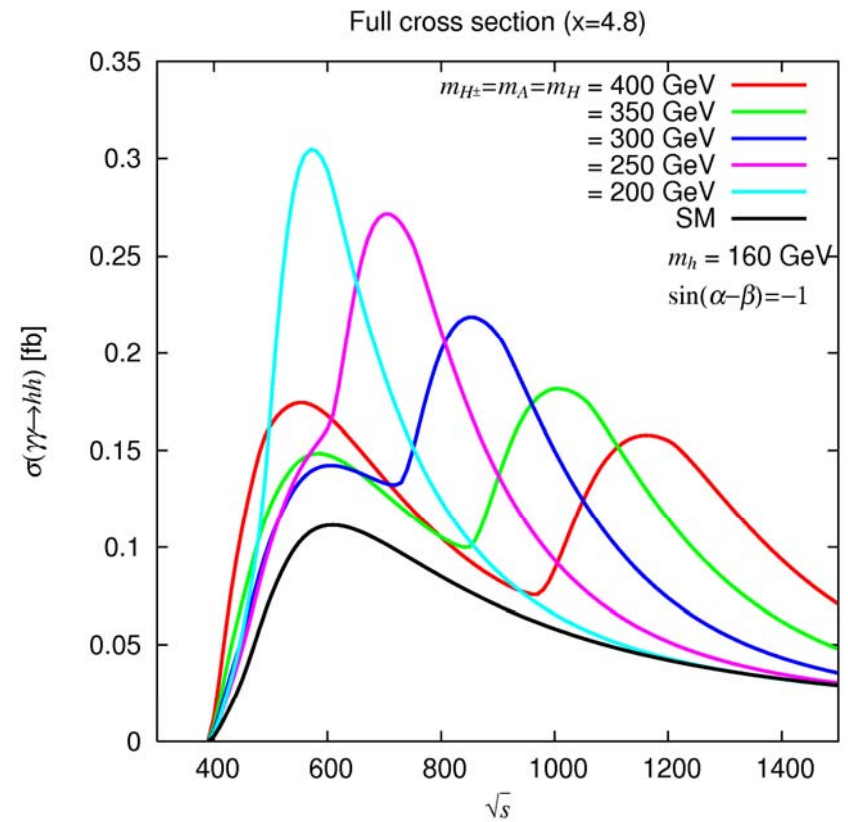
mean helicity¹²

$$e^-e^- \rightarrow \gamma\gamma \rightarrow hh$$

$$m_h = 120 \text{ GeV}$$



$$m_h = 160 \text{ GeV}$$

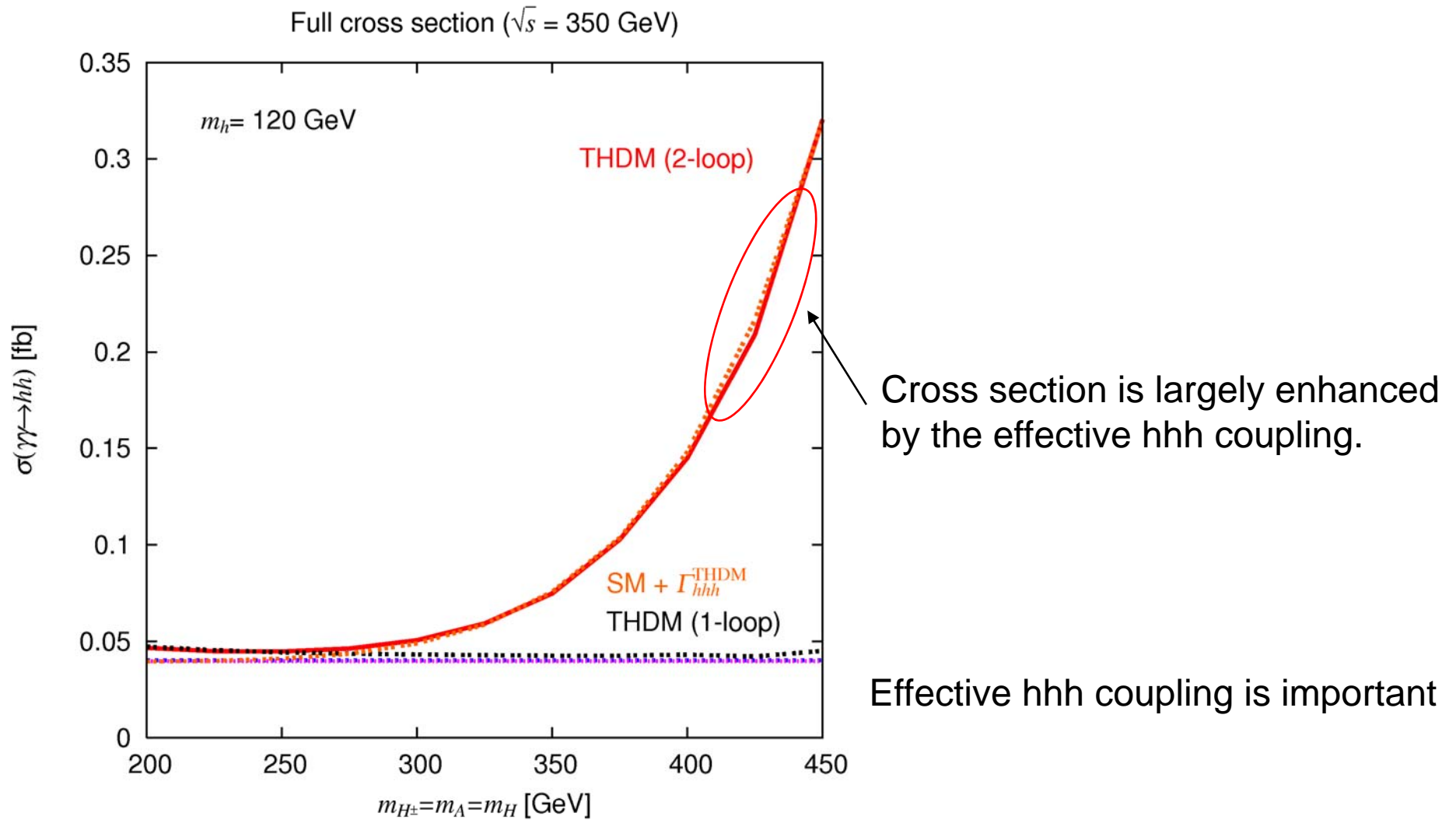


The full cross section is given from the sub cross section by convoluting the photon luminosity spectrum.

We use following values

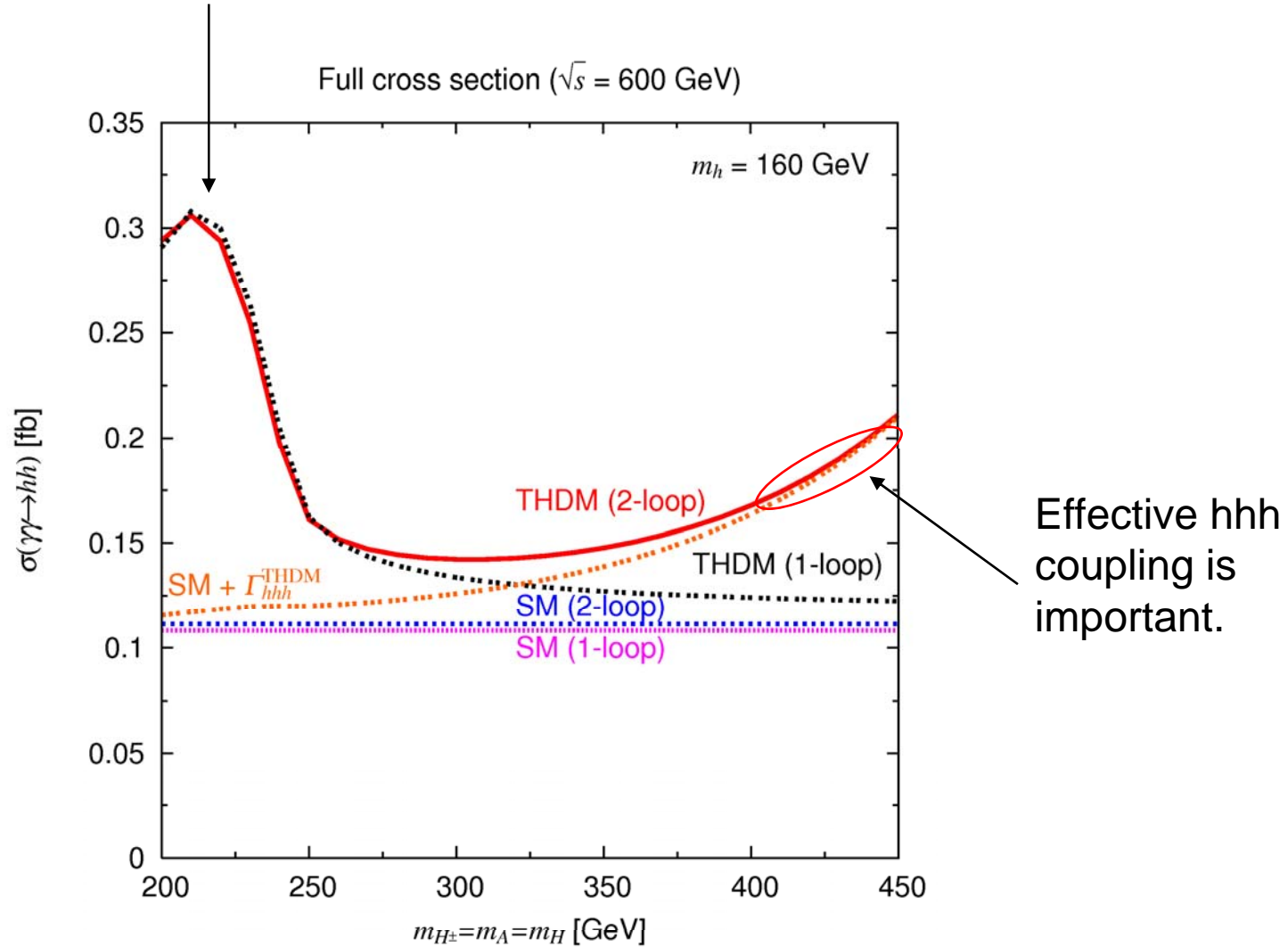
Initial laser beam mean helicity $P_c = -1$ Initial electron helicity $\lambda_e = +0.45$

$$\sqrt{s} = 350 \text{ GeV} \quad m_h = 120 \text{ GeV}$$



$$\sqrt{s} = 600 \text{ GeV} \quad m_h = 160 \text{ GeV}$$

Threshold enhancement of charged Higgs pair production



For 250-400 GeV, charged Higgs boson loop contribution and the effective hhh coupling are important.

Conclusion

We calculate $\gamma\gamma \rightarrow hh$ in THDM with SM-like limit

- The cross section can be largely changed from the SM.
 - additional contribution of charged Higgs boson loop
 - Effective 1-loop hhh vertex enhanced by the non-decoupling effect
- The cross section strongly depend on m_h m_Φ \sqrt{s}

	THDM $m_\Phi = 450\text{GeV}$ 200GeV		SM
$\sqrt{s} = 350\text{GeV}$ $m_h = 120\text{GeV}$	$\sigma \sim 0.3\text{fb}$	$\sigma \sim 0.05\text{fb}$	$\sigma \sim 0.05\text{fb}$
$\sqrt{s} = 600\text{GeV}$ $m_h = 160\text{GeV}$	$\sigma \sim 0.2\text{fb}$	$\sigma \sim 0.3\text{fb}$	$\sigma \sim 0.1\text{fb}$

In the region between threshold of top pair production and that of charged Higgs boson pair production, both the contributions are important. 16

Backup Slide

(a) THDM 2-loop THDM with additional one-loop corrections to the hhh coupling

$$\mathcal{M}_{\text{THDM}}^{2\text{-loop}}(l_1, l_2) = \mathcal{M}(l_1, l_2, \Gamma_{hhh}^{\text{THDM}}) + \Delta\mathcal{M}(l_1, l_2, \Gamma_{hhh}^{\text{THDM}})$$

(b) THDM 1-loop THDM with the tree level hhh coupling

$$\mathcal{M}_{\text{THDM}}^{1\text{-loop}}(l_1, l_2) = \mathcal{M}(l_1, l_2, \lambda_{hhh}) + \Delta\mathcal{M}(l_1, l_2, \lambda_{hhh}) \quad \lambda_{hhh} = -\frac{3m_h^2}{v}$$

(c) SM 2-loop SM with additional top loop correction to the hhh coupling

$$\mathcal{M}_{\text{SM}}^{2\text{-loop}}(l_1, l_2) = \mathcal{M}(l_1, l_2, \Gamma_{hhh}^{\text{SM}})$$

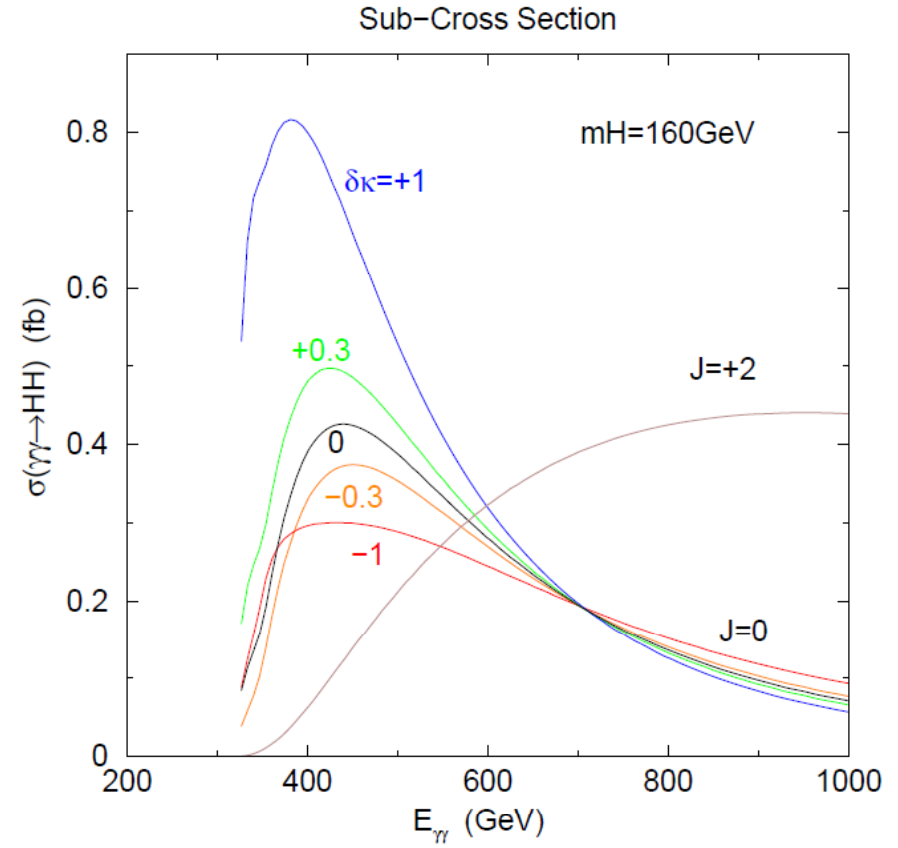
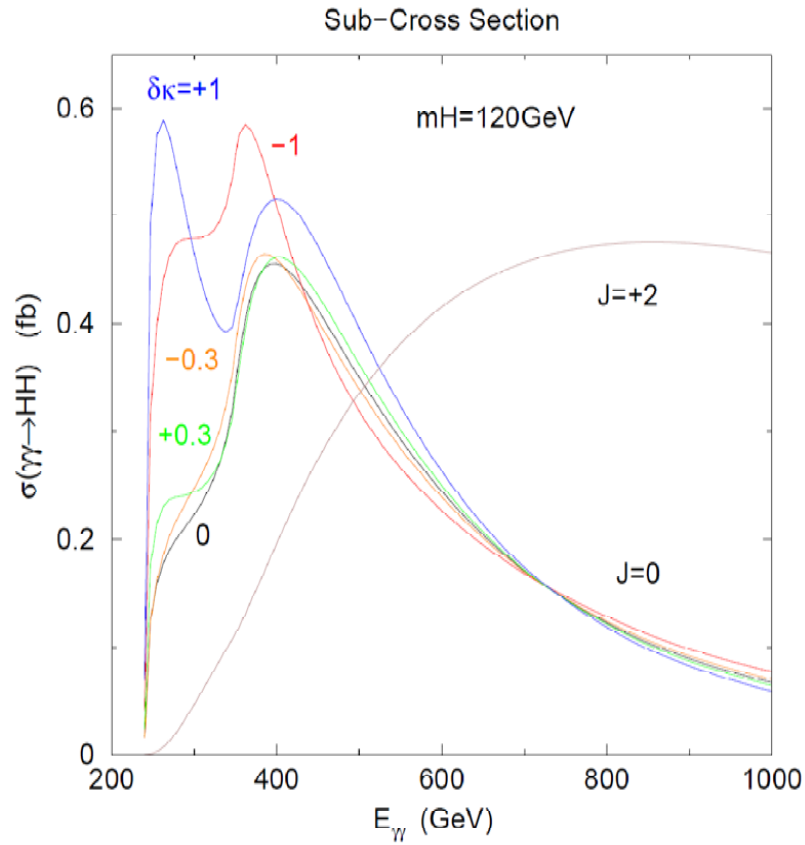
(d) SM 1-loop SM with the tree level hhh coupling

$$\mathcal{M}_{\text{SM}}^{1\text{-loop}}(l_1, l_2) = \mathcal{M}(l_1, l_2, \lambda_{hhh})$$

(e) $\text{SM} + \Gamma_{hhh}^{\text{THDM}}$ SM with additional one-loop corrections (THDM) to the hhh coupling

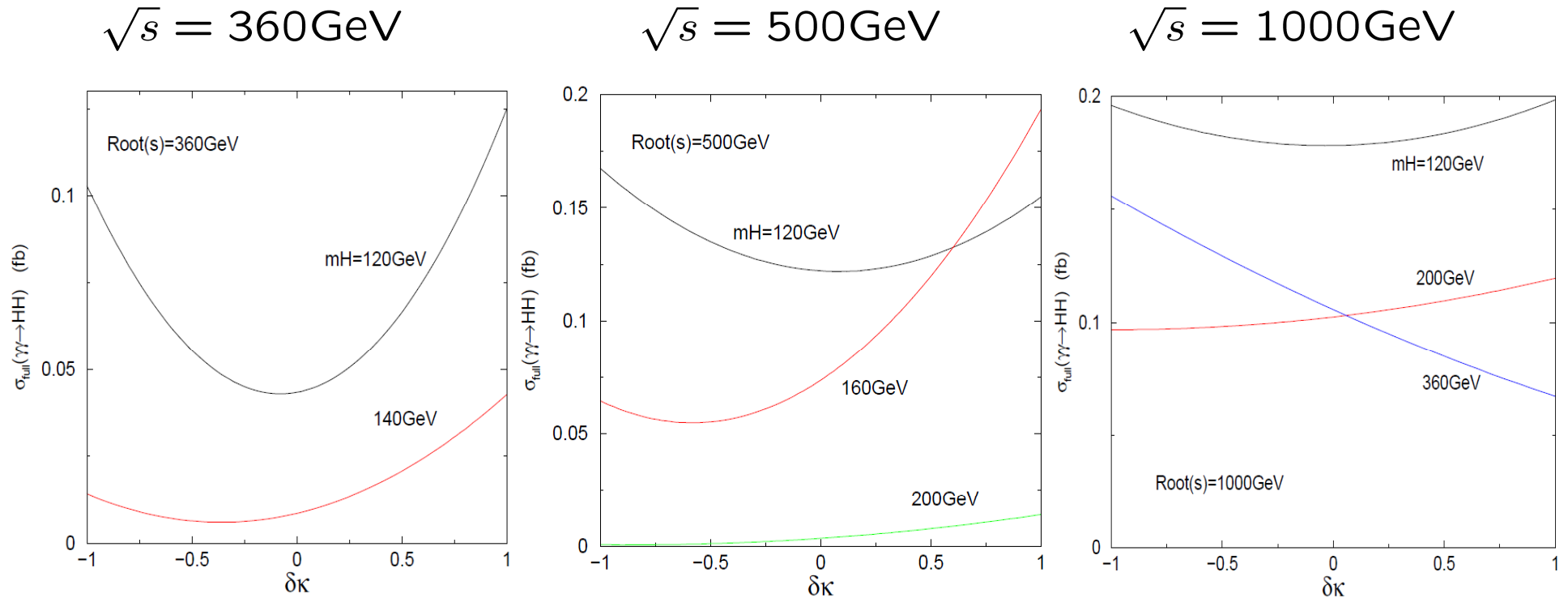
$$\mathcal{M}_{\text{SM} + \Gamma_{hhh}^{\text{THDM}}}(l_1, l_2) = \mathcal{M}(l_1, l_2, \Gamma_{hhh}^{\text{THDM}})$$

Anomalous hhh coupling



$$\lambda_{hhh} = \lambda_{hhh}^{\text{SM}} (1 + \delta\kappa)$$

Full Cross Section ($\delta\kappa$ dependences)



$$\lambda_{hhh} = \lambda_{hhh}^{\text{SM}}(1 + \delta\kappa)$$