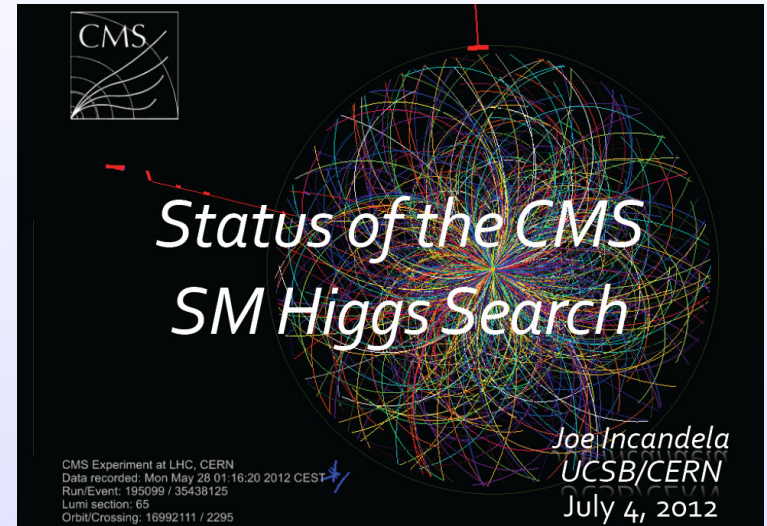
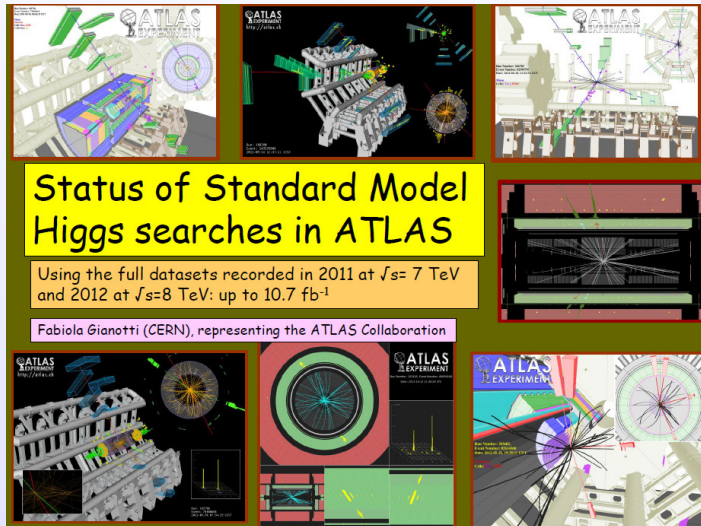
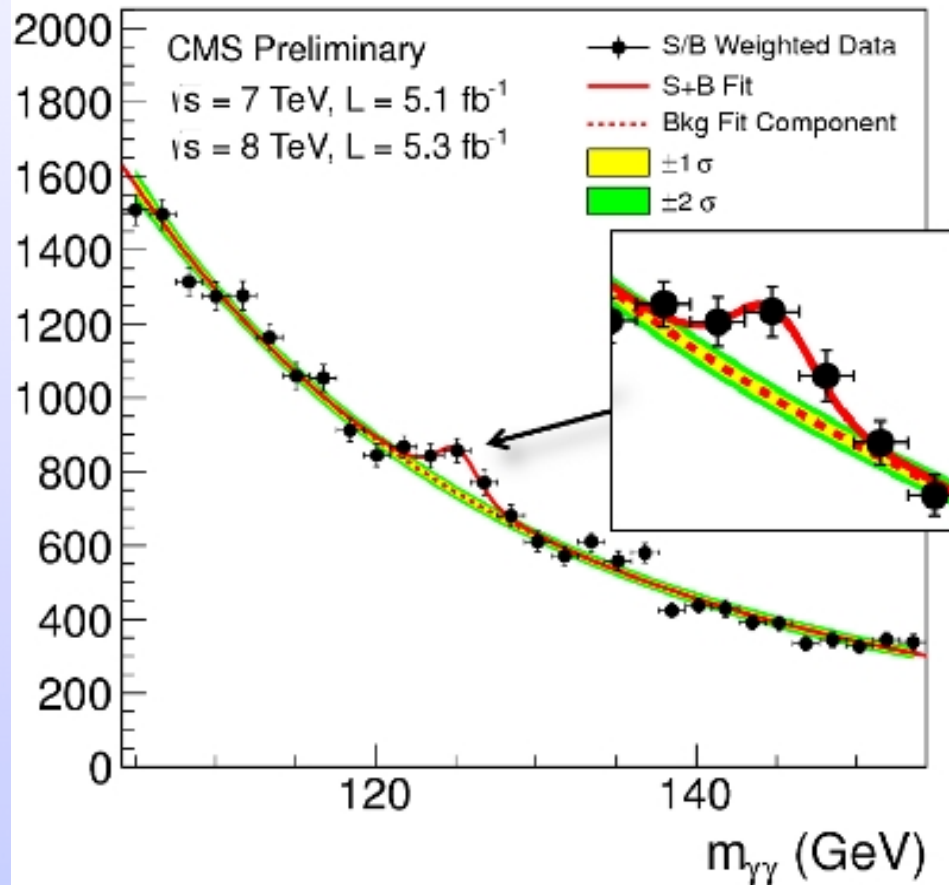
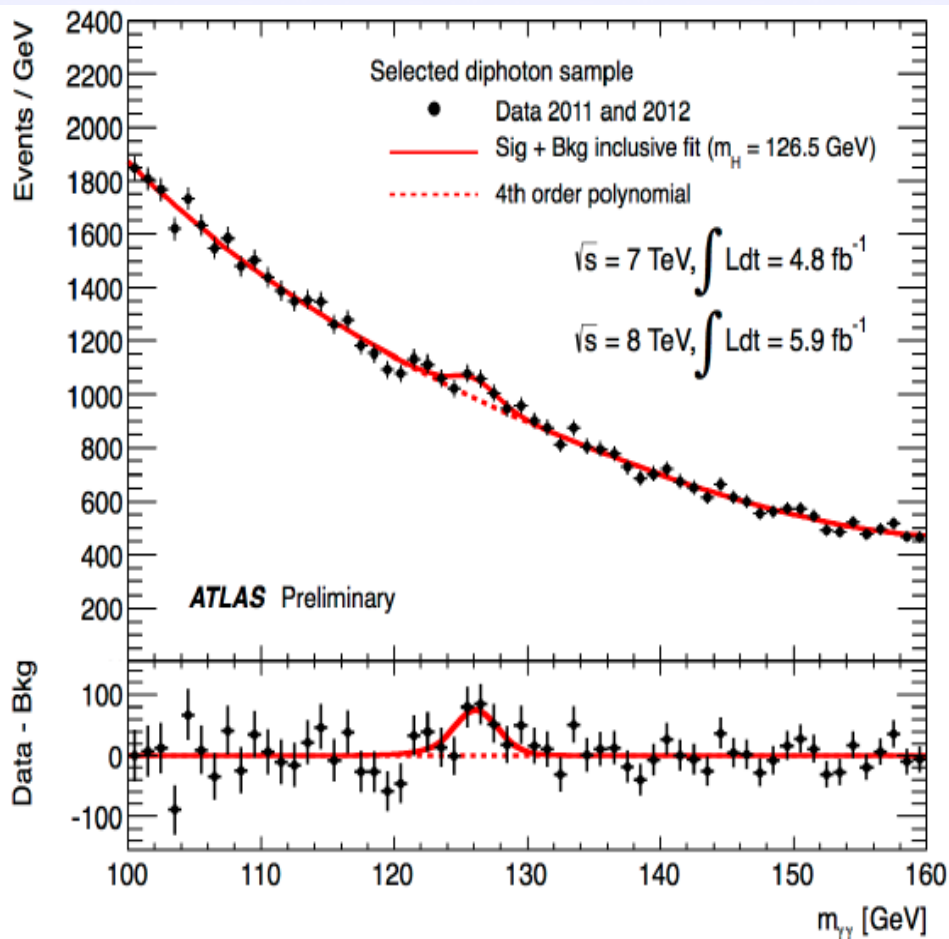


# Higgs Properties in the pMSSM

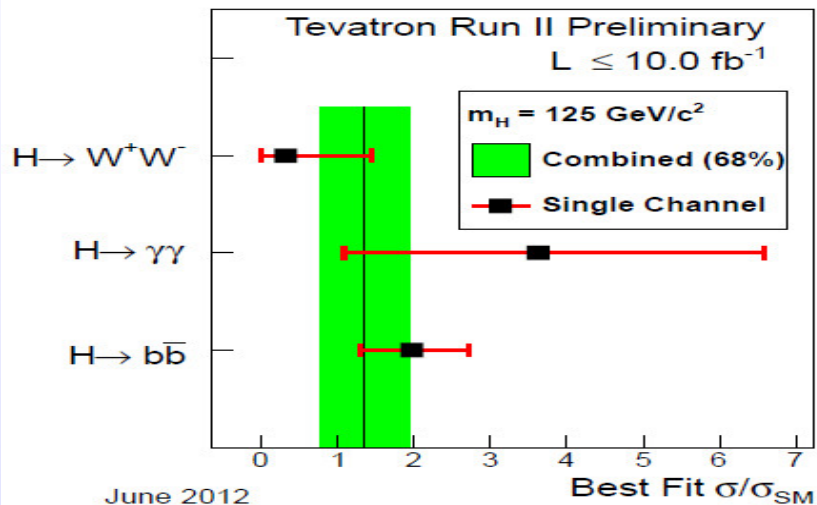


Cahill-Rowley, JLH, Hoeche, Ismail, Rizzo 1206.4321, 1206.5800, 1210.ASAP

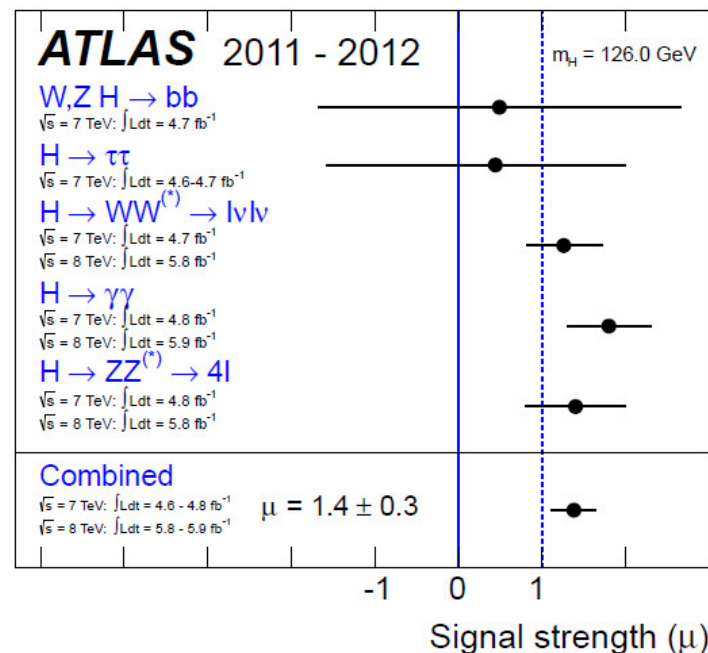
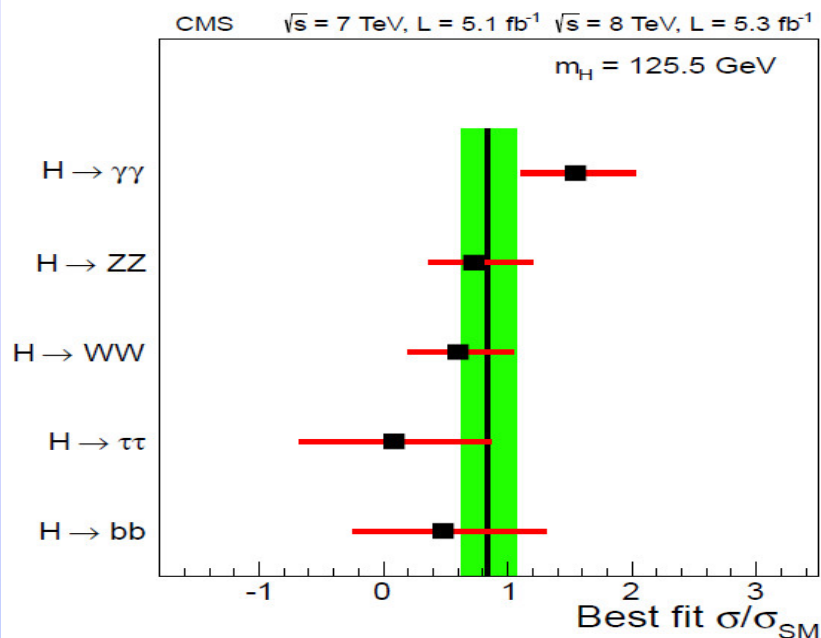
# Our Shiny-New Higgs-like Boson!



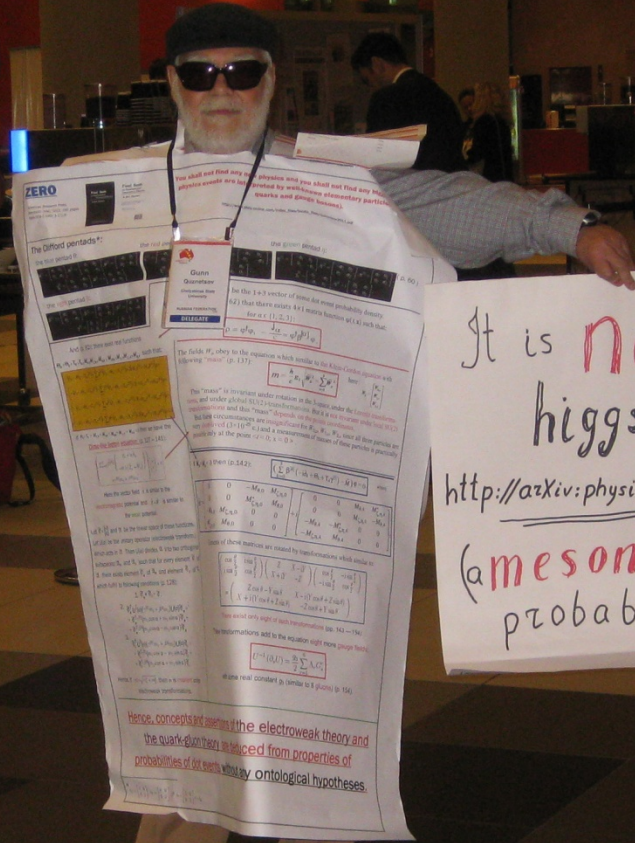
# Generally the Higgs is SM-like...so far...



Maybe the  $\gamma\gamma(bb)$  mode is a bit high(low) but, overall, things do look roughly right ...in a few months we'll know better.







It is **not**  
higgs.

<http://arxiv:physics/030201>

(**a**meson,  
probably).

Hence, concepts and assertions of the electroweak theory and  
the quantum theory are deduced from properties of  
probabilities of occurrence of events by ontological hypotheses.



# The pMSSM Model Framework

- The phenomenological MSSM (pMSSM)
  - Most general CP-conserving MSSM
  - Minimal Flavor Violation, First 2 sfermion generations are degenerate w/ negligible Yukawas
  - No GUT, SUSY-breaking assumptions!
  - 19 real, weak-scale parameters

scalars:

$m_{Q_1}, m_{Q_3}, m_{u_1}, m_{d_1}, m_{u_3}, m_{d_3}, m_{L_1}, m_{L_3}, m_{e_1}, m_{e_3}$

gauginos:  $M_1, M_2, M_3$

tri-linear couplings:  $A_b, A_t, A_\tau$

Higgs/Higgsino:  $\mu, M_A, \tan\beta$



# Study of the pMSSM (Neutralino/Gravitino LSP)

## Scan with Linear Priors

Perform large scan over  
Parameters

$$100 \text{ GeV} \leq m_{\text{sfermions}} \leq 4 \text{ TeV}$$

$$50 \text{ GeV} \leq |M_1, M_2, \mu| \leq 4 \text{ TeV}$$

$$400 \text{ GeV} \leq M_3 \leq 4 \text{ TeV}$$

$$100 \text{ GeV} \leq M_A \leq 4 \text{ TeV}$$

$$1 \leq \tan\beta \leq 60$$

$$|A_{t,b,\tau}| \leq 4 \text{ TeV}$$

$$(1 \text{ eV} \leq m_G \leq 1 \text{ GeV}) \text{ (log prior)}$$

Subject these points to  
Constraints from:

- Flavor physics
- EW precision measurements
- Collider searches
- Cosmology

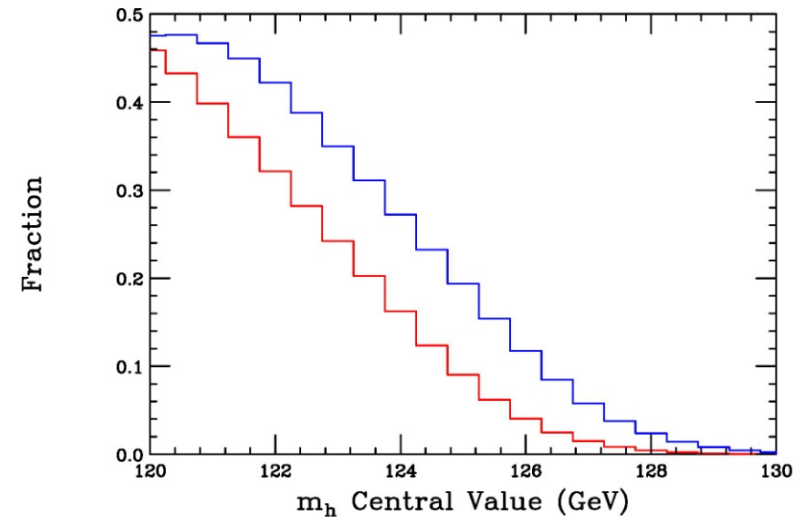
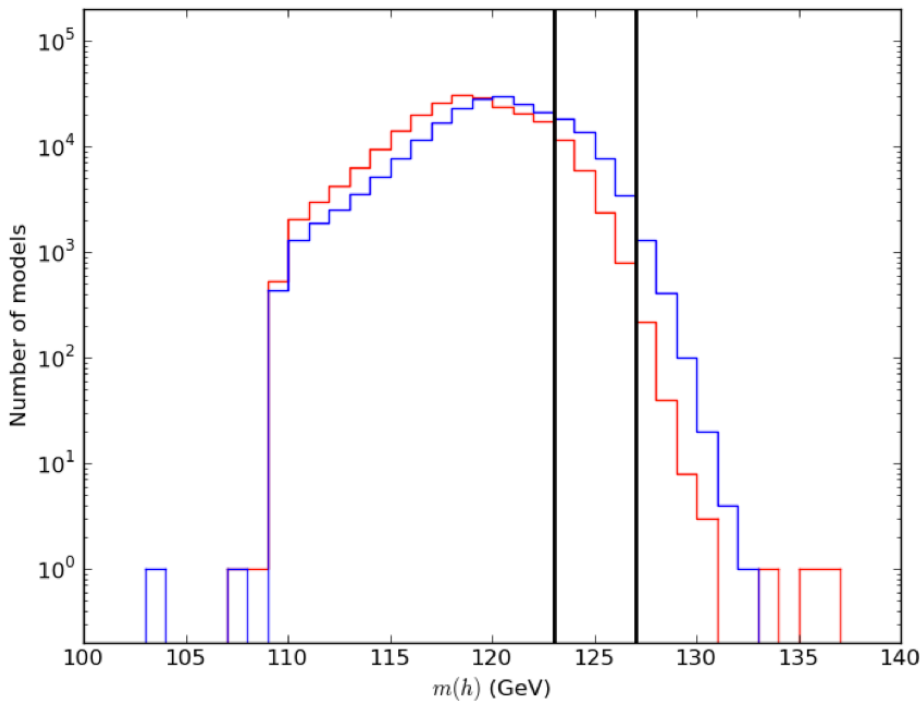
~225,000 models survive constraints for each LSP type!



# Predictions for Lightest Higgs Mass in the pMSSM

Models consistent with EW Precision, B Physics, Cosmology,  
and Collider data

Neutralino LSP  
Gravitino LSP



# The SUSY Higgs Sector

- SUSY Higgs sector:  $h^0, H^0, H^\pm, A^0$
- 2 free parameters in the Higgs potential: very predictive at tree-level!

$$M_Z^2 = -2\mu^2 + 2 \frac{m_{H_d}^2 - t_\beta^2 m_{H_u}^2}{t_\beta^2 - 1}$$

$$m_{h^0} < m_Z |\cos(2\beta)|$$

- Radiative corrections are important!

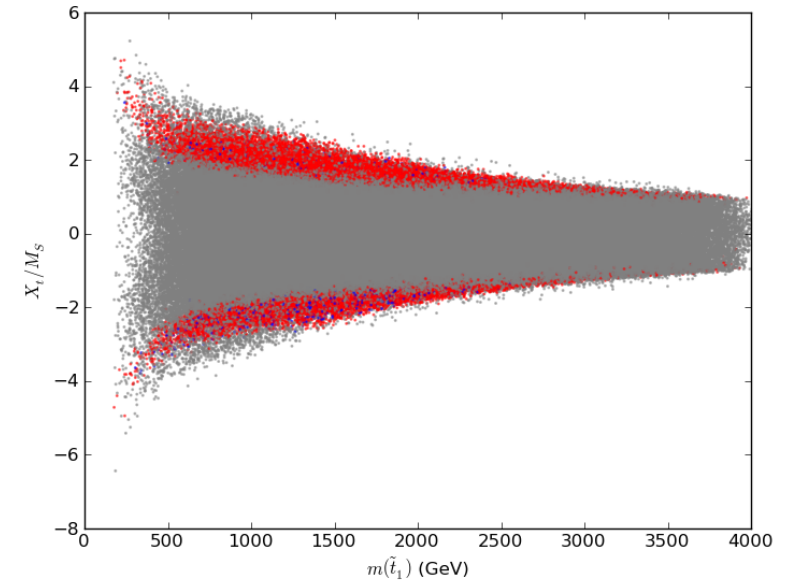
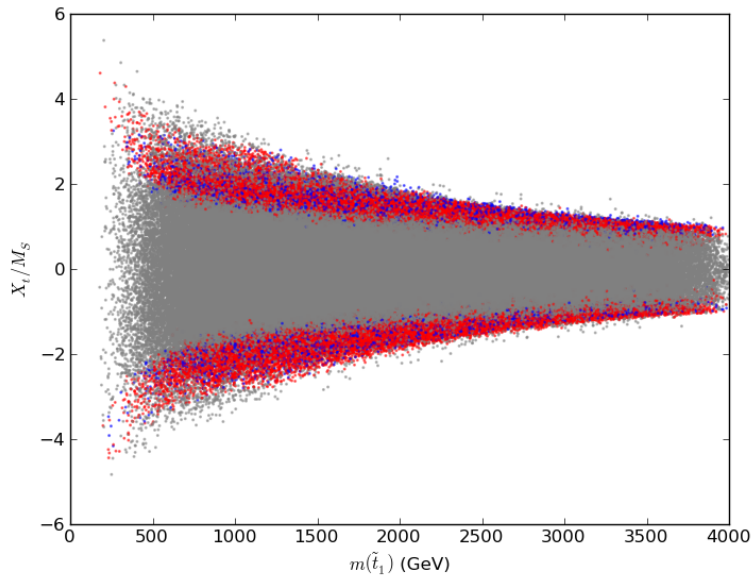
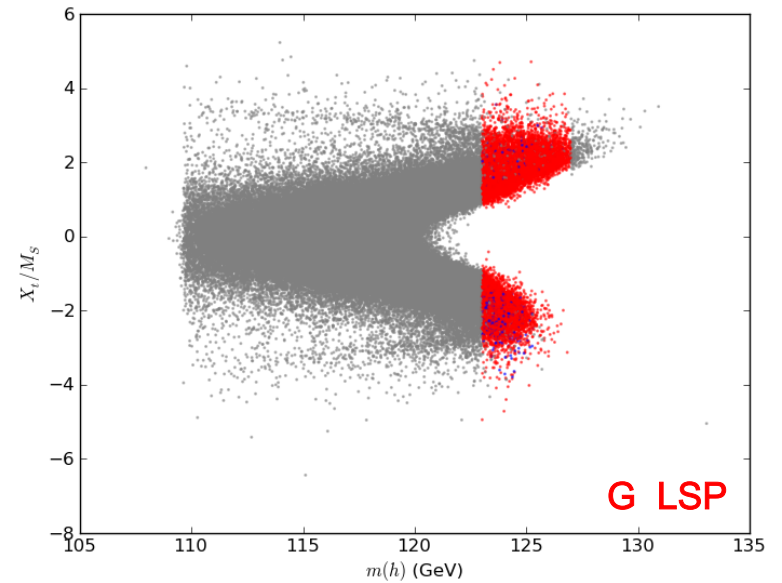
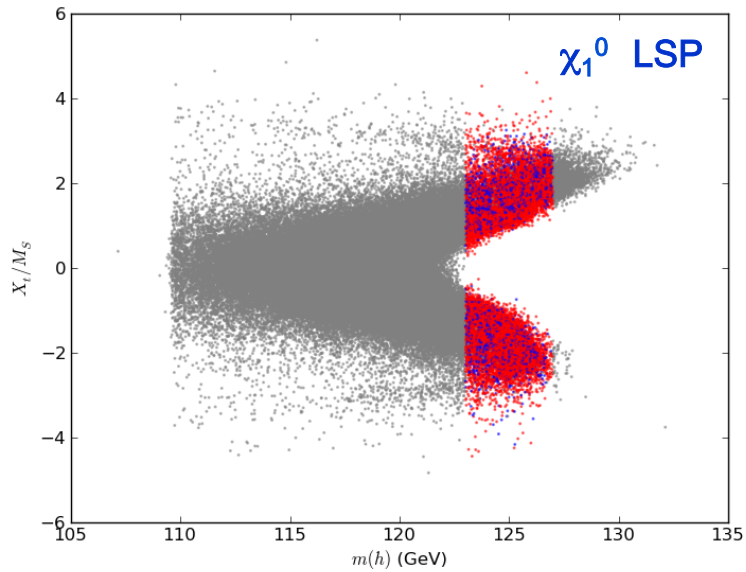
$$\Delta(m_{h^0}^2) = \text{[Solid Loop]} + \text{[Dashed Loop]} + \text{[Dashed Loop]}$$

Higgs mass  
is very sensitive  
in particular to  
the lightest  
stop mass

$$m_{h^0}^2 = m_Z^2 \cos^2(2\beta) + \frac{3}{4\pi^2} \sin^2\beta y_t^2 \left[ m_t^2 \ln(m_{\tilde{t}_1} m_{\tilde{t}_2} / m_t^2) + c_t^2 s_t^2 (m_{\tilde{t}_2}^2 - m_{\tilde{t}_1}^2) \ln(m_{\tilde{t}_2}^2 / m_{\tilde{t}_1}^2) \right. \\ \left. + c_t^4 s_t^4 \left\{ (m_{\tilde{t}_2}^2 - m_{\tilde{t}_1}^2)^2 - \frac{1}{2} (m_{\tilde{t}_2}^4 - m_{\tilde{t}_1}^4) \ln(m_{\tilde{t}_2}^2 / m_{\tilde{t}_1}^2) \right\} / m_t^2 \right].$$



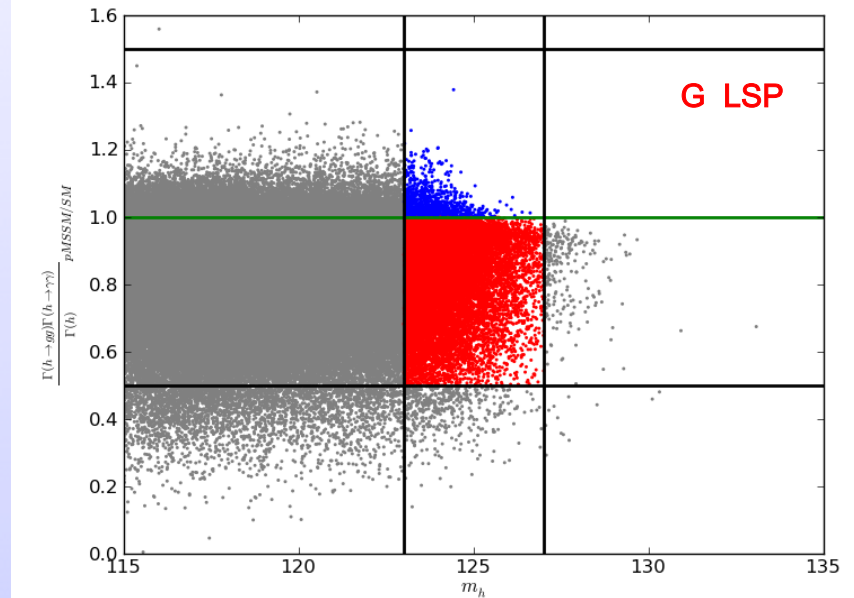
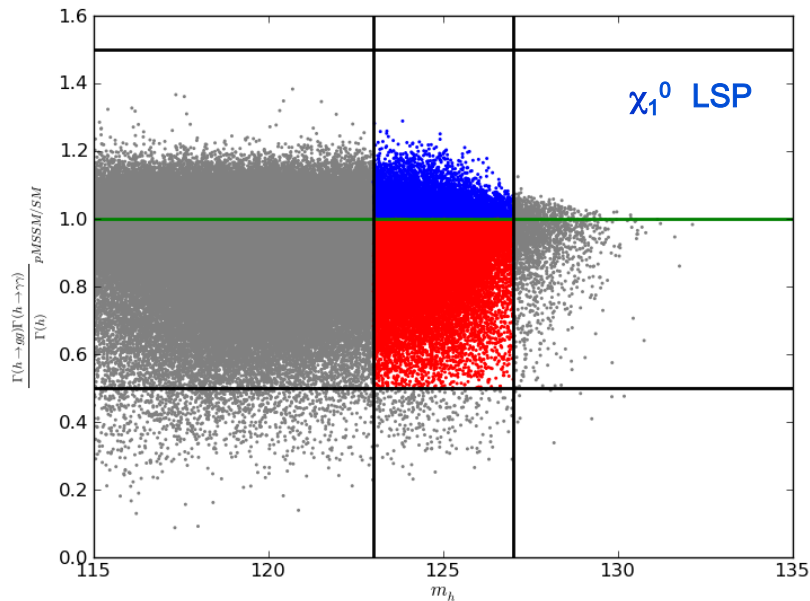
# Special parameter regions needed for the 126 GeV Higgs



# Higgs Properties

$$R_{XX} = \sigma(gg \rightarrow h) B(h \rightarrow XX)|_{p\text{MSSM/SM}}$$

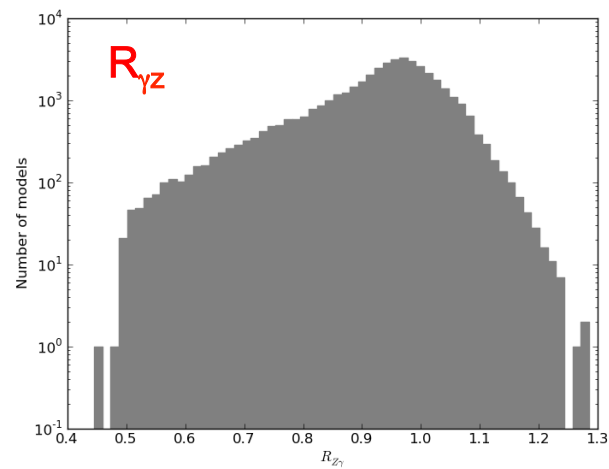
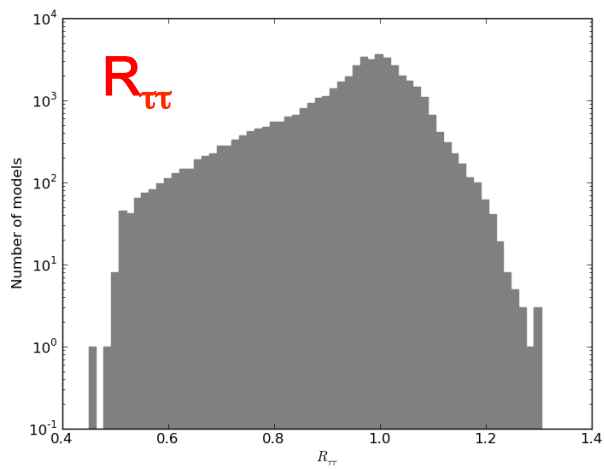
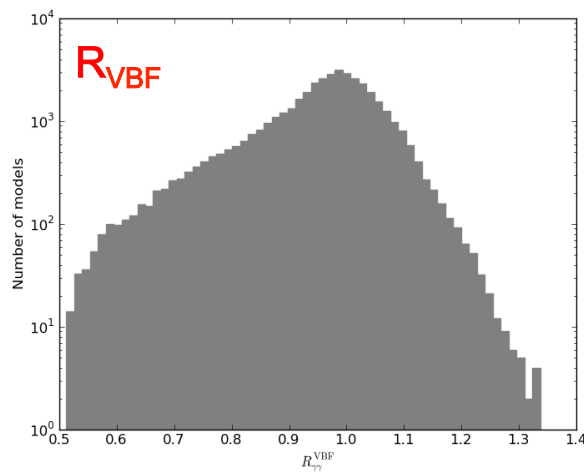
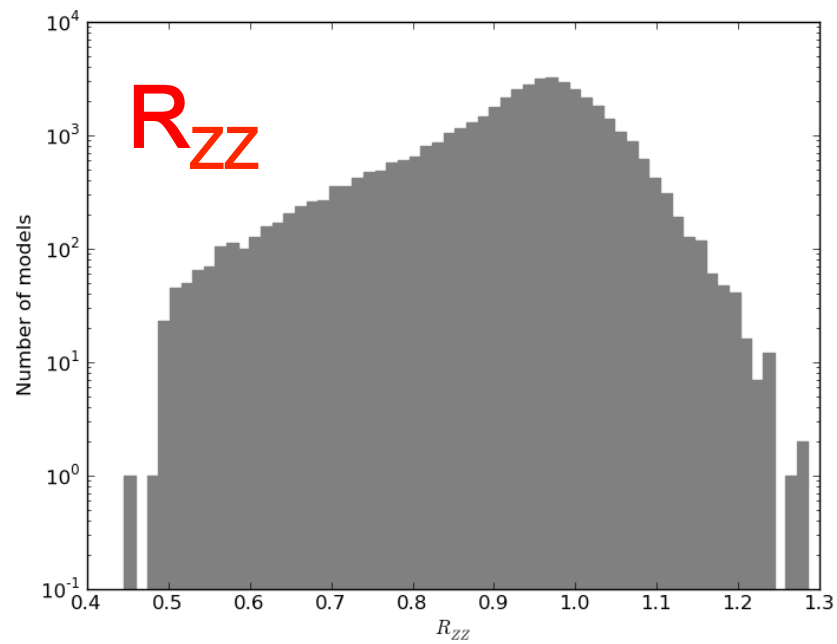
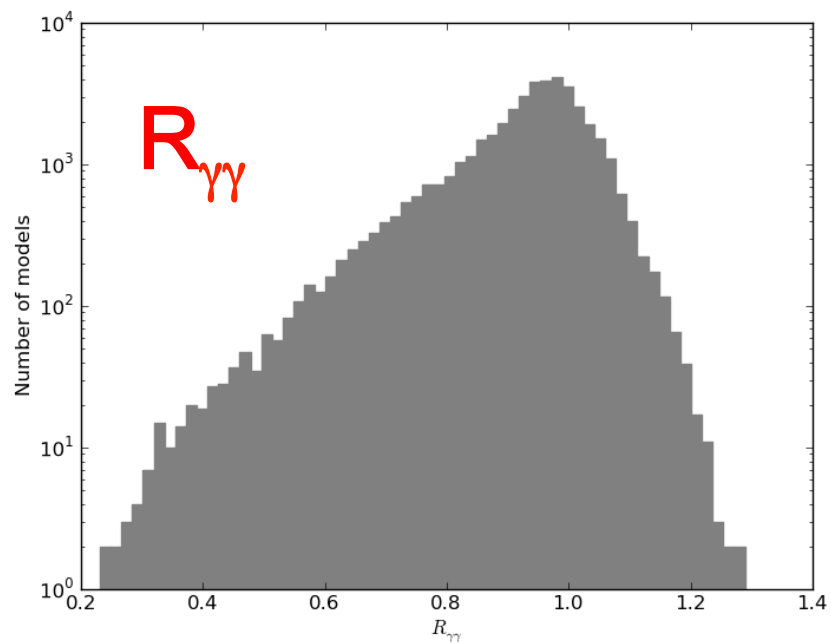
$R_{\gamma\gamma}$



The two different model sets lead to qualitatively similar yet quantitatively very different predictions...

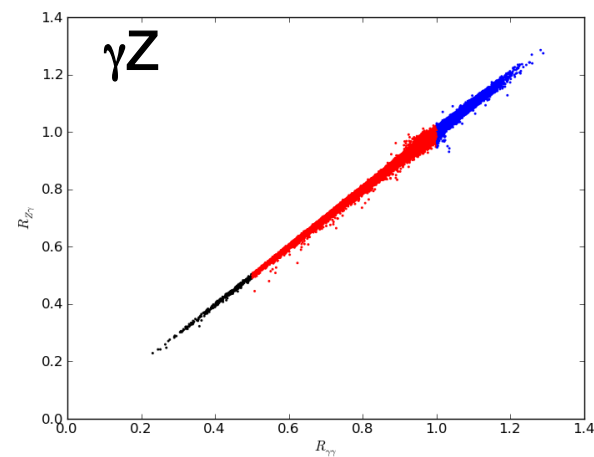
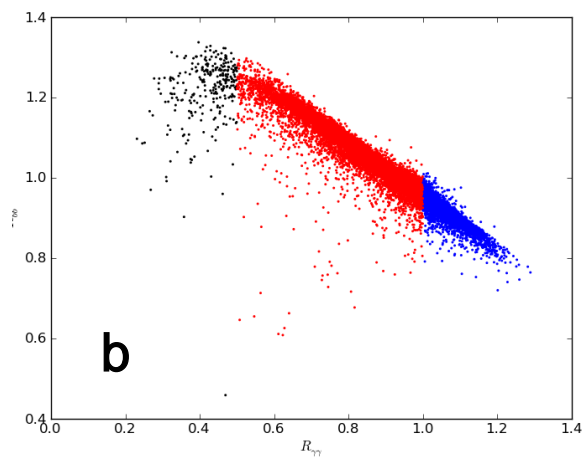
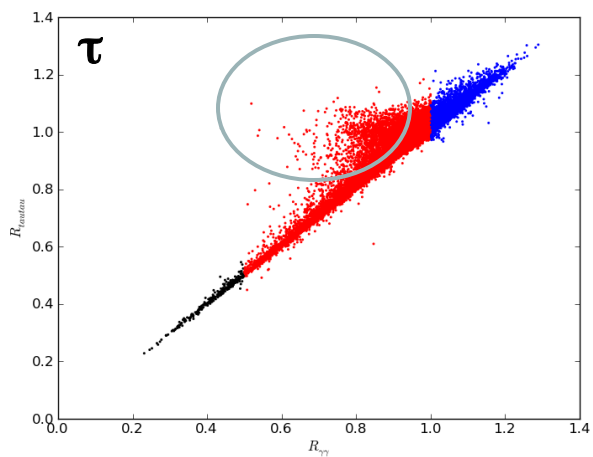
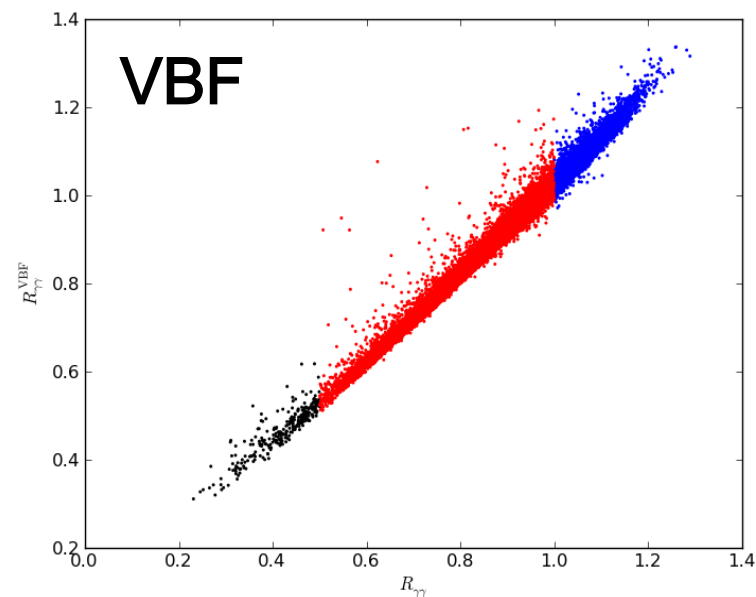
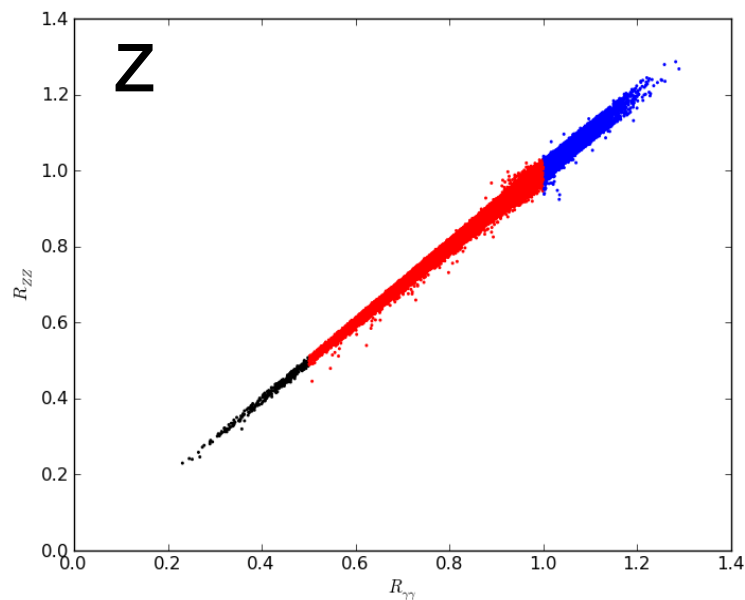


# $\chi_1^0$ LSP



# $\chi_1^0$ LSP

Very Highly Correlated !

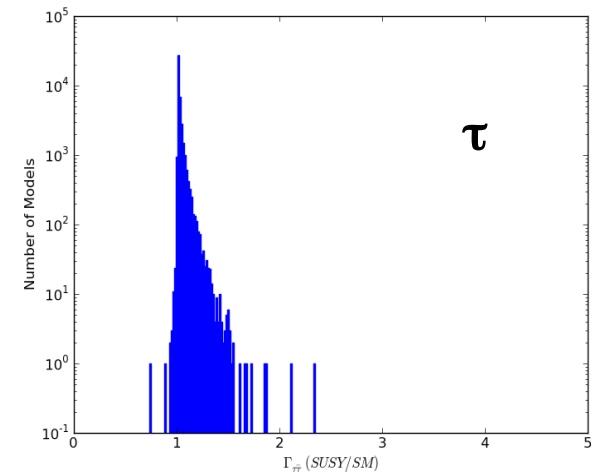
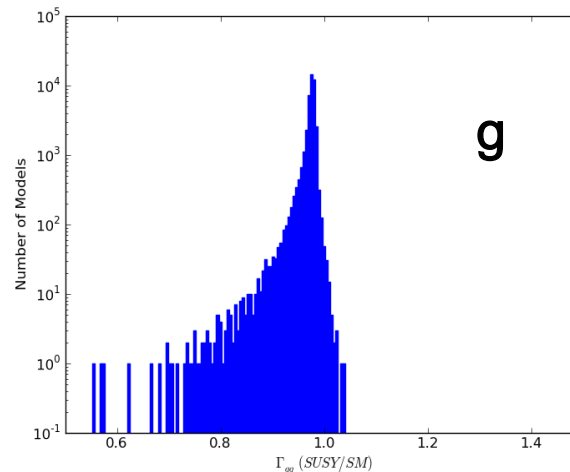
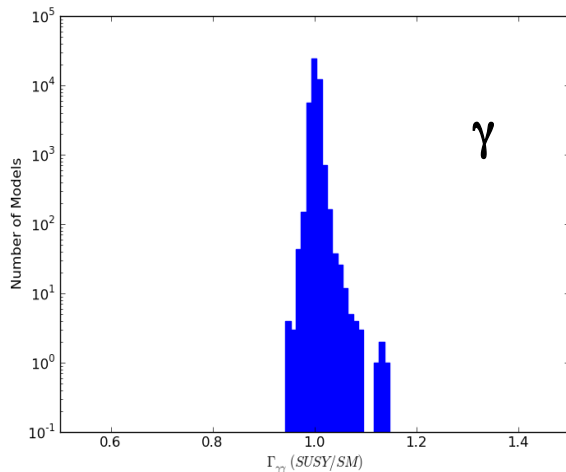
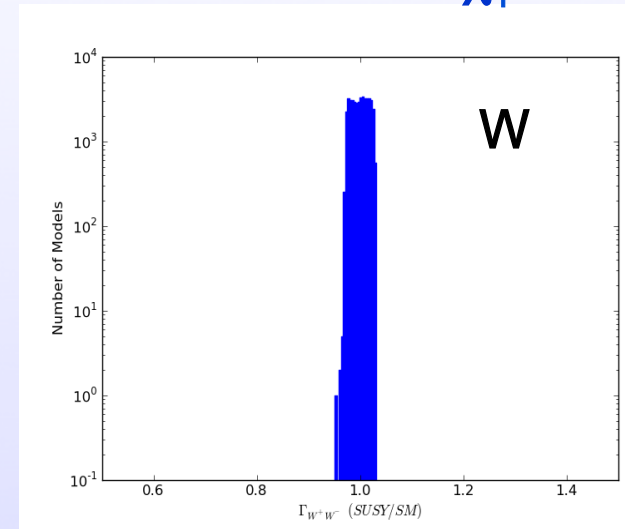




# Examination of Partial Widths

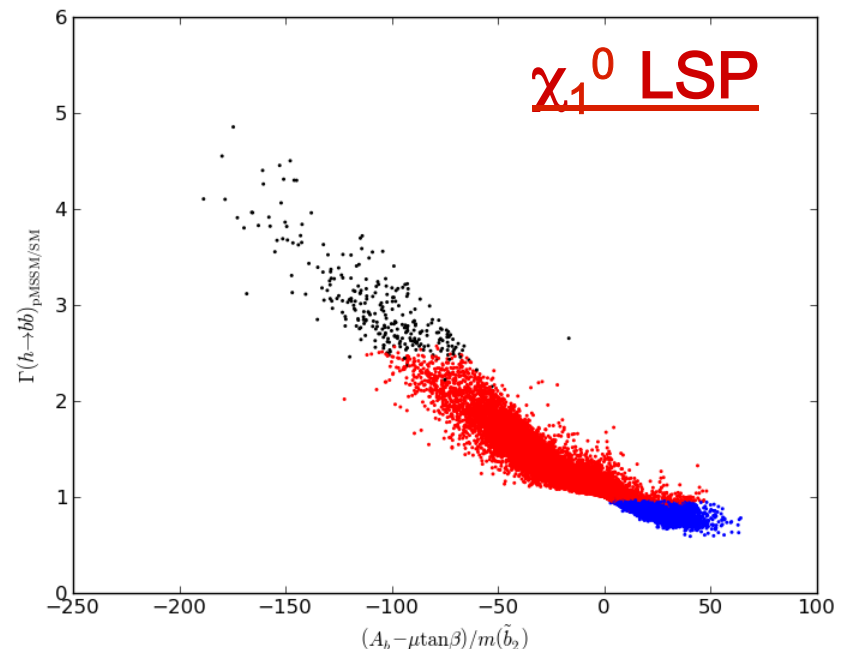
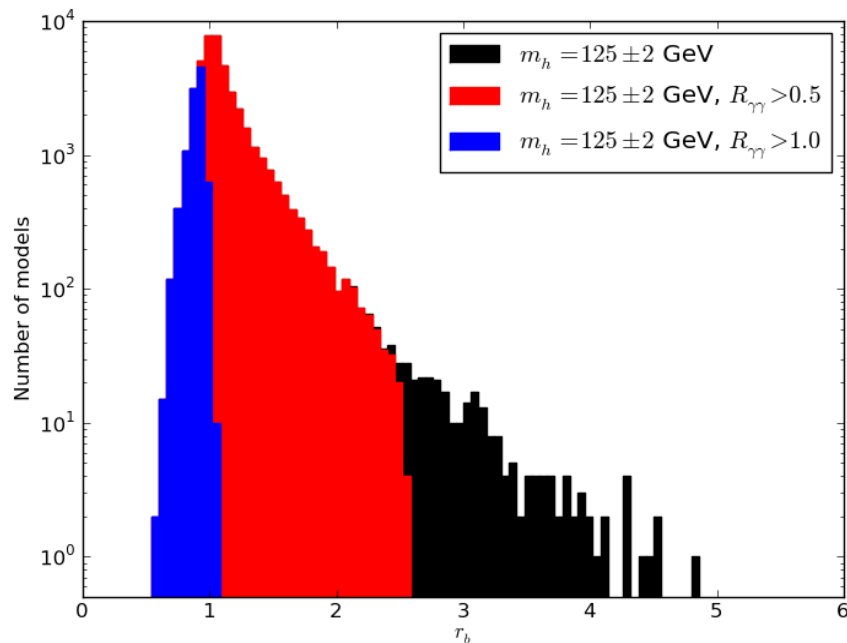
- Most partial widths are close to their SM values due to decoupling
- for both LSP model sets we get highly peaked  $r = \Gamma / \Gamma_{\text{SM}}$  distributions (here for the neutralino model set)
- Precision ILC measurements could Select pMSSM parameters

$\chi_1^0$  LSP



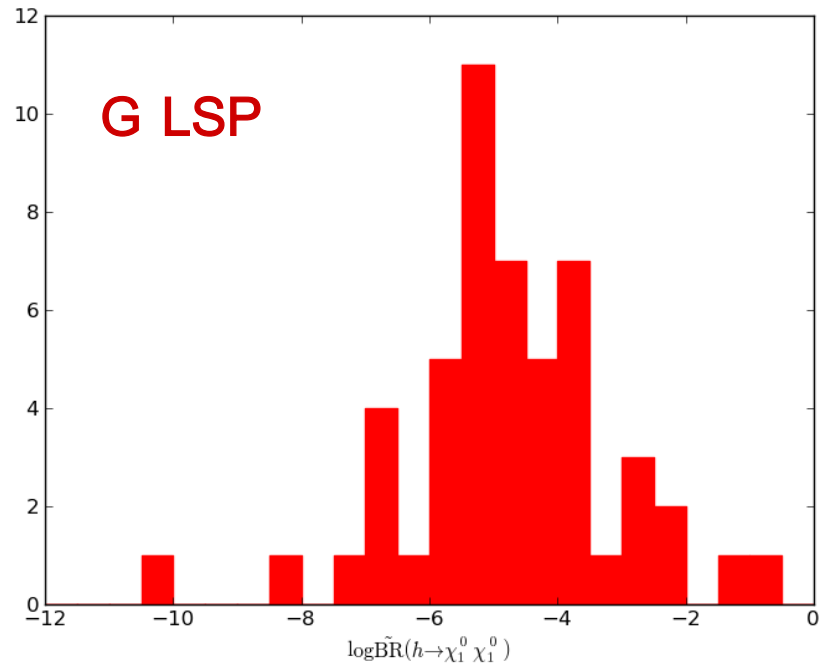
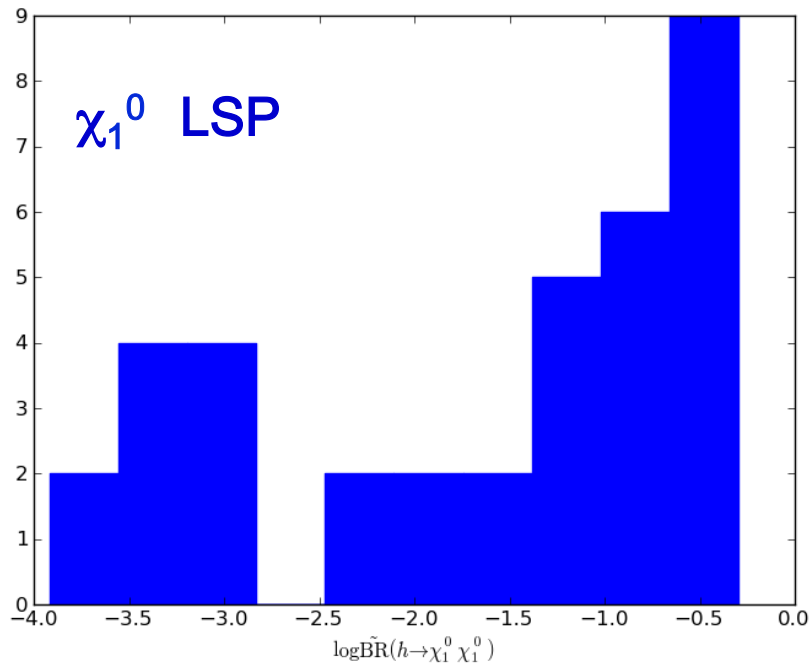
$h \rightarrow b\bar{b}$  is quite different...

- Large  $hbb$  coupling loop corrections decouple very slowly especially if there is large sbottom mixing (Haber et al.)
- These lead to a significant Higgs width increase/decrease since it is the dominant decay mode



## Non-SM Higgs decays

- In the **neutralino** (**gravitino**) model set **36** (**51**) models have kinematically accessible  $h$  ( $=125 \pm 2$  GeV) decays to pairs of neutralinos which are mostly **bino** w/ a small **Higgsino** admixture. (There are a higher fraction of **bino**  $\chi_1^0$ s in the gravitino set but there are fewer Higgs in this mass range.) The rate scales  $\sim$  as the product of the bino & Higgsino fractions.
- In the neutralino set this is the usual '**invisible Higgs decay**'. 15/36 have  $h \rightarrow$  invisible BF > 10% & in one case it's  $\approx$  50%
- In the gravitino set the NLSP neutralino will decay to  $\gamma$  + **gravitino** producing a  $\gamma\gamma$  + (small ?) MET signature. The neutralinos in this set have high bino purity & thus we expect a lower BF in this mode. Only 1/51 models lead to a BF > 1% (19%).



As expected the BF for this mode is higher in the neutralino set due to the high bino purity of the neutralino NLSP in the gravitino set

It will be important to continue to search for unusual Higgs decay modes as further tests of new physics beyond just measuring couplings to the SM fields.



# Naturalness Criterion

Standard prescription to compute fine-tuning:

- Take mass relation w/ radiative corrections

$$M_Z^2 = -2\mu^2 + 2 \frac{m_{H_d}^2 - t_\beta^2 m_{H_u}^2}{t_\beta^2 - 1} + \text{higher order}$$

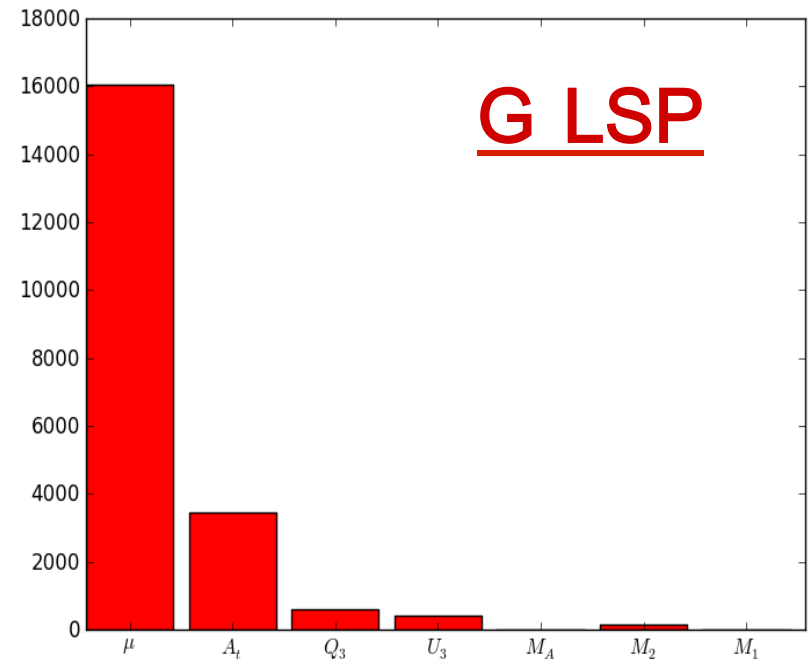
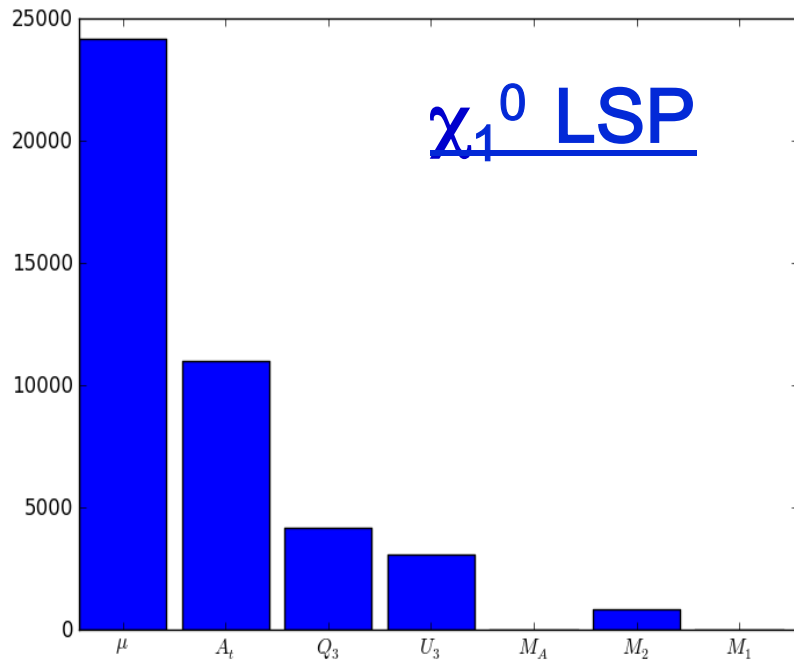
- Compute dependence on each SUSY parameter,  $p_i$

$$Z_i = \frac{\partial(\log M_Z^2)}{\partial(\log p_i)} = \frac{p_i}{M_Z^2} \frac{\partial M_Z^2}{\partial p_i}$$

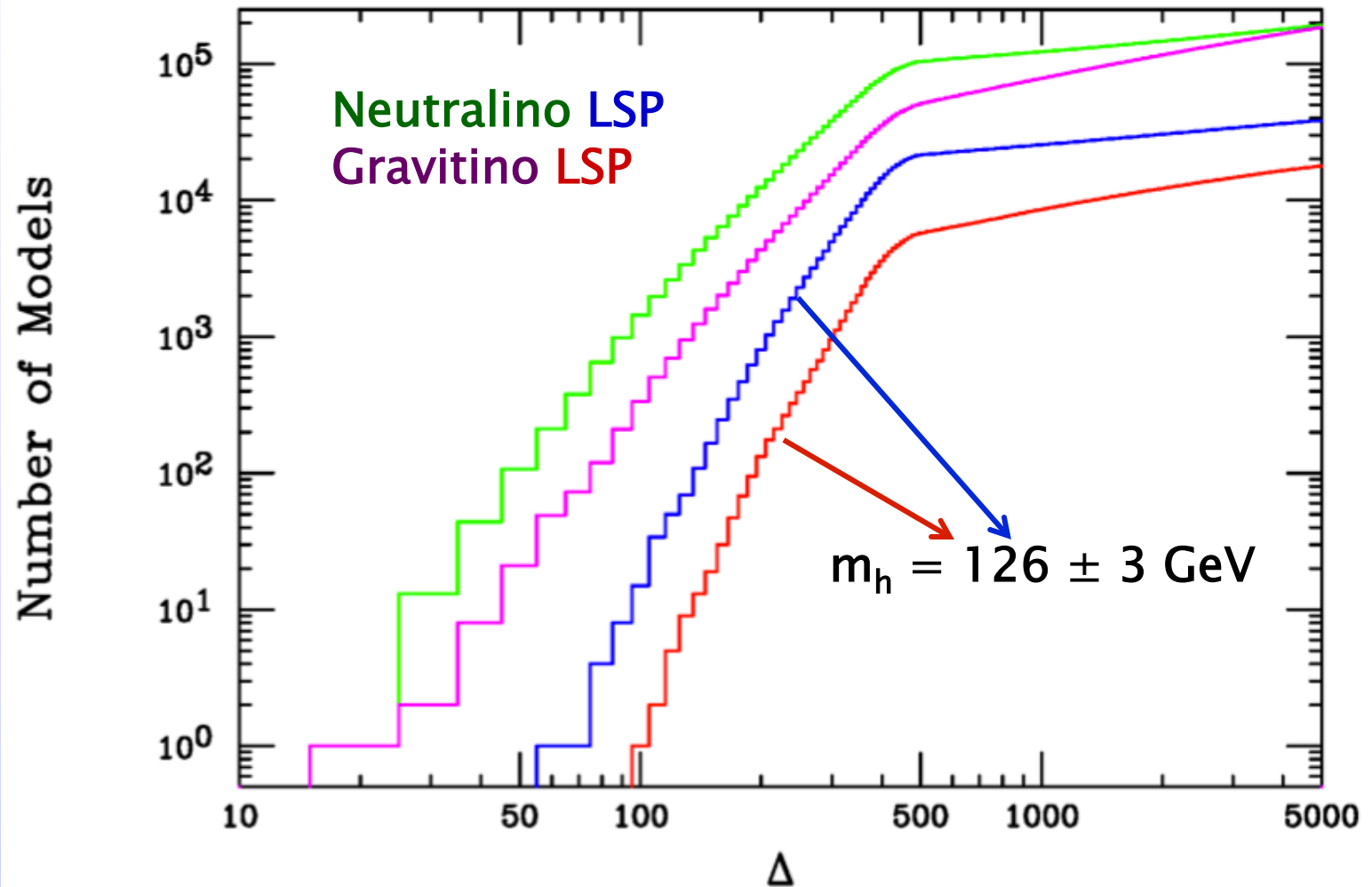
- Overall fine-tuning of model given by

$$\Delta = \max |Z_i|$$

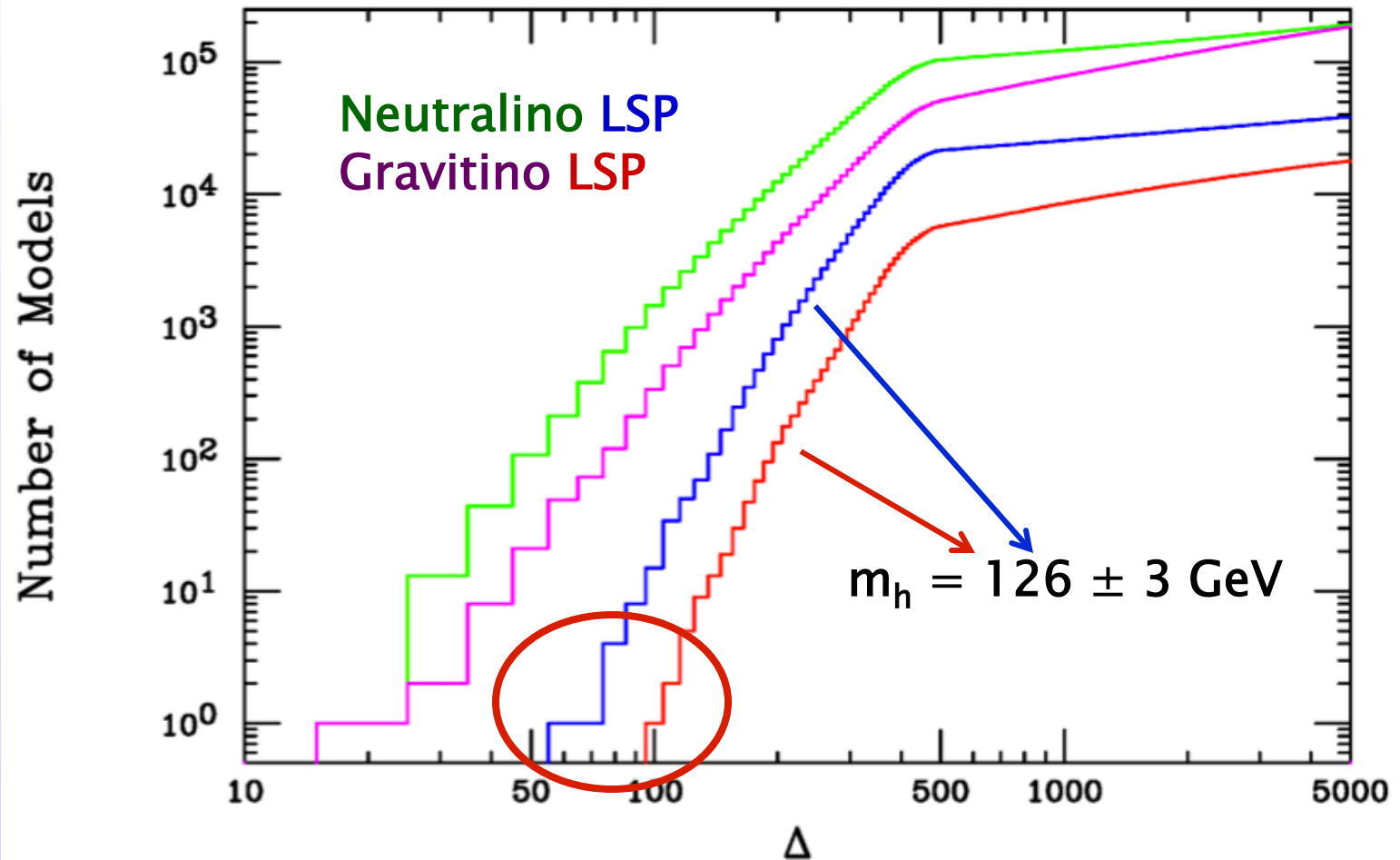
# Dominant FT Contributors



# Fine-Tuning in the pMSSM



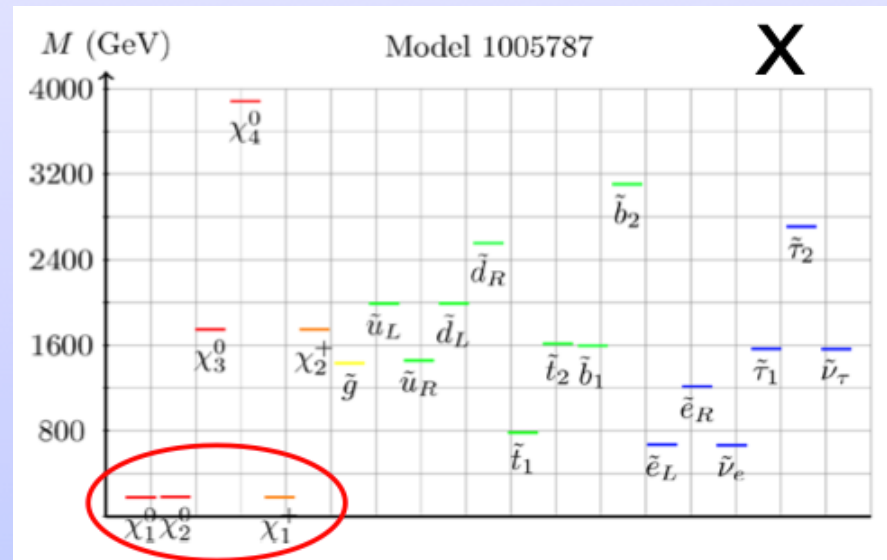
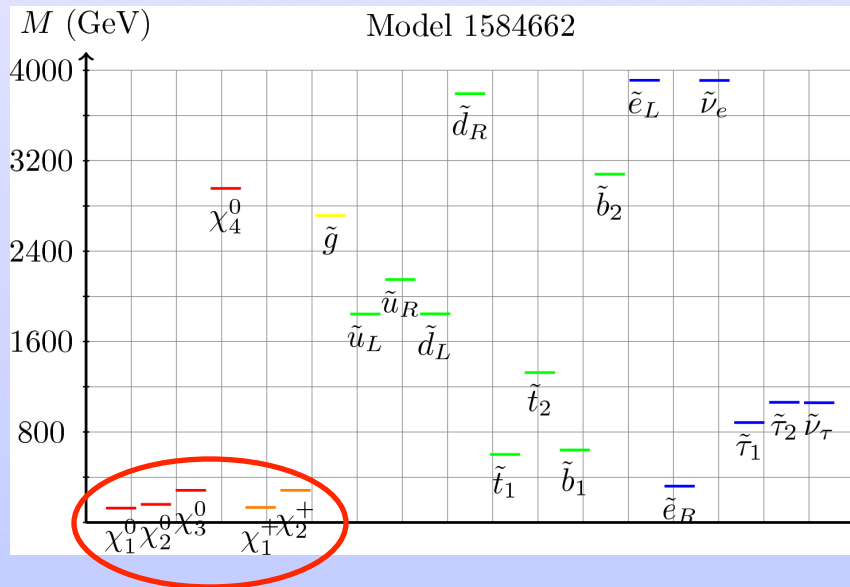
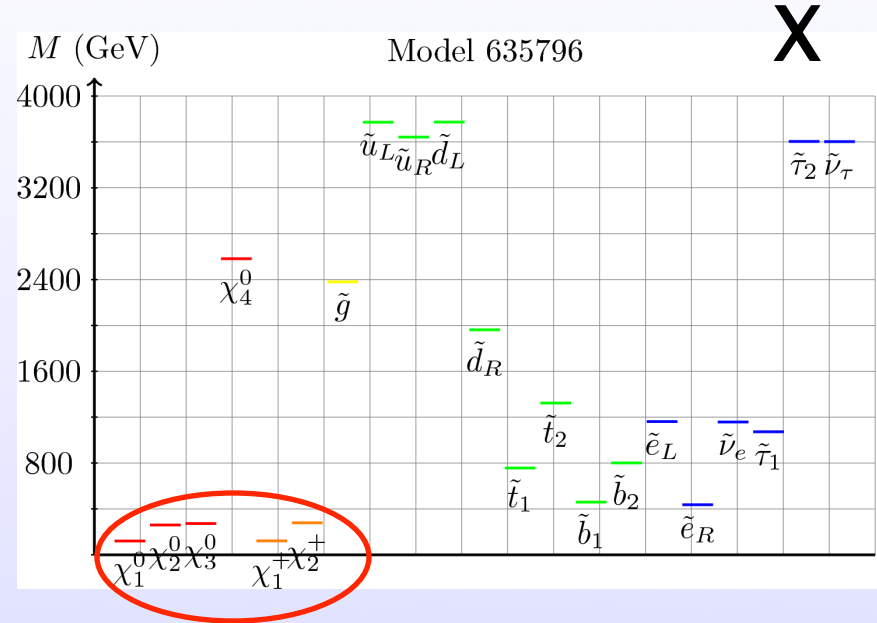
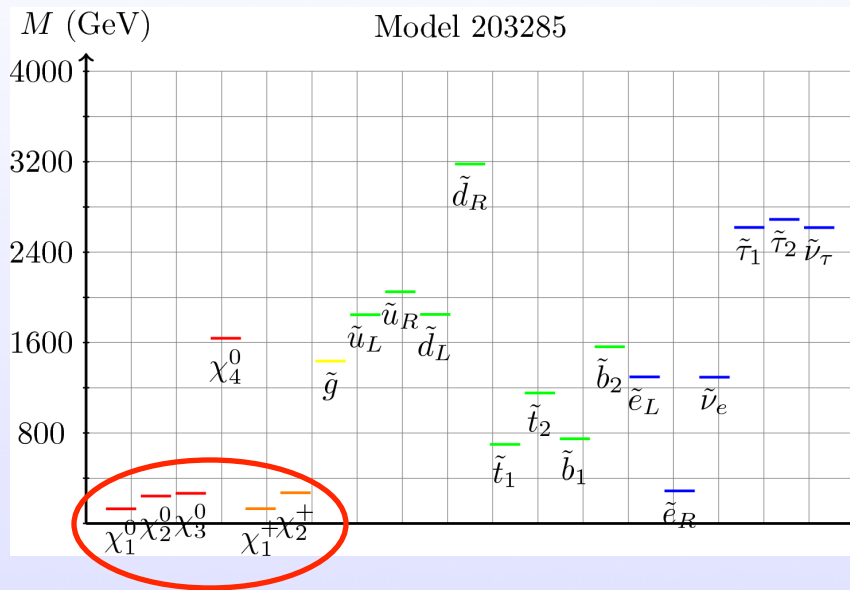
# Fine-Tuning in the pMSSM



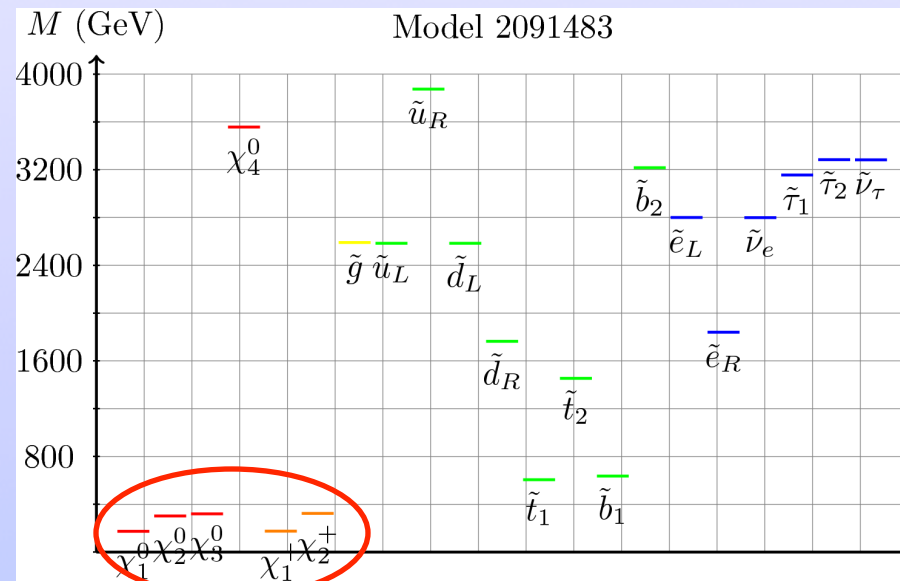
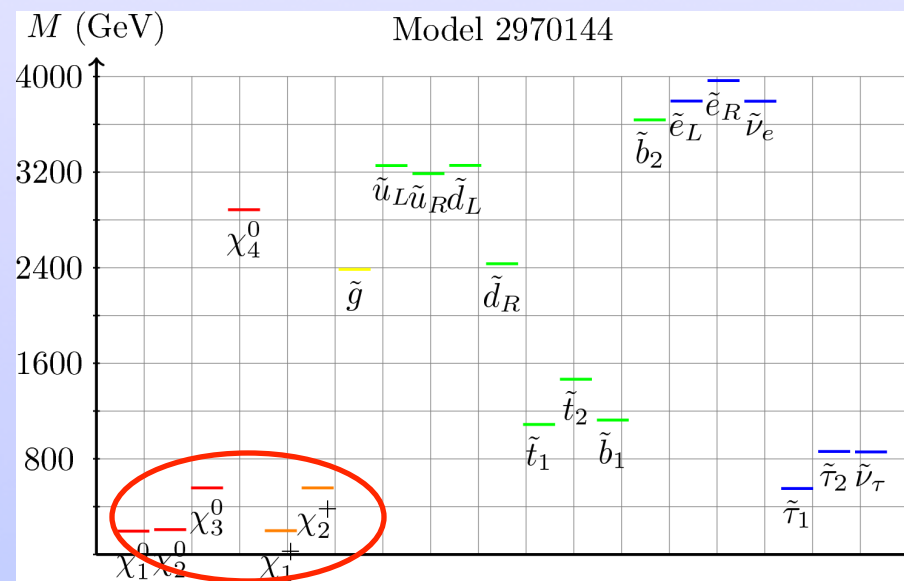
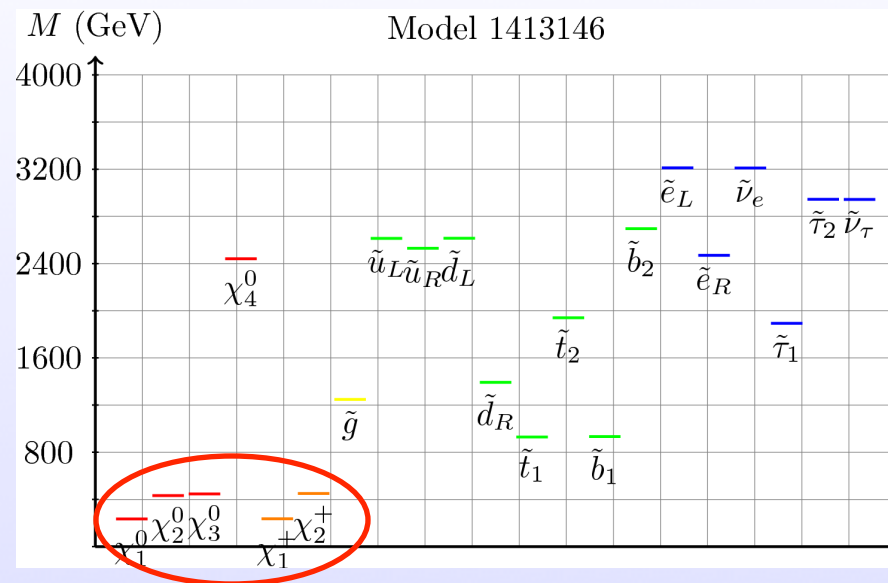
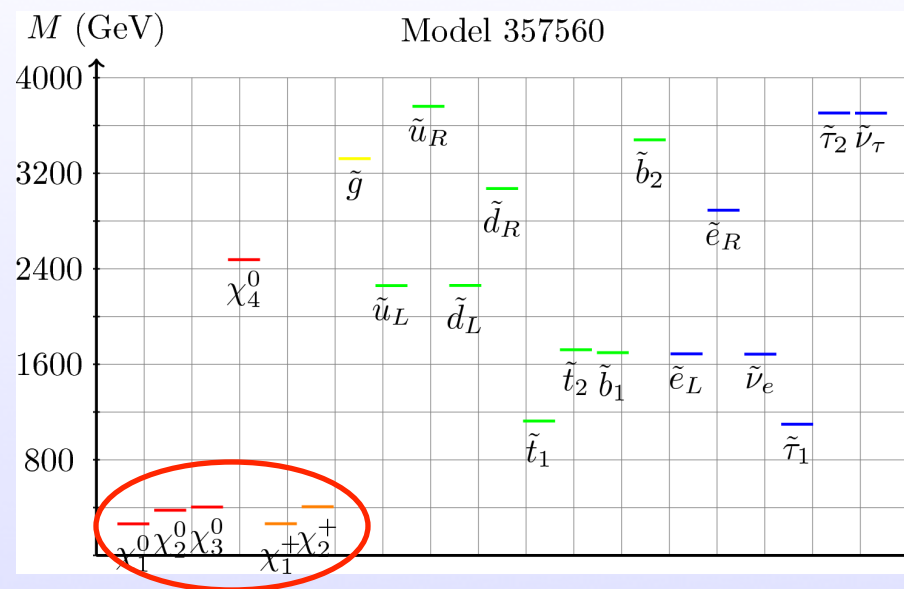
13 + 1 models with  $\Delta < 100$ ,  
4+1 of these are excluded by the LHC



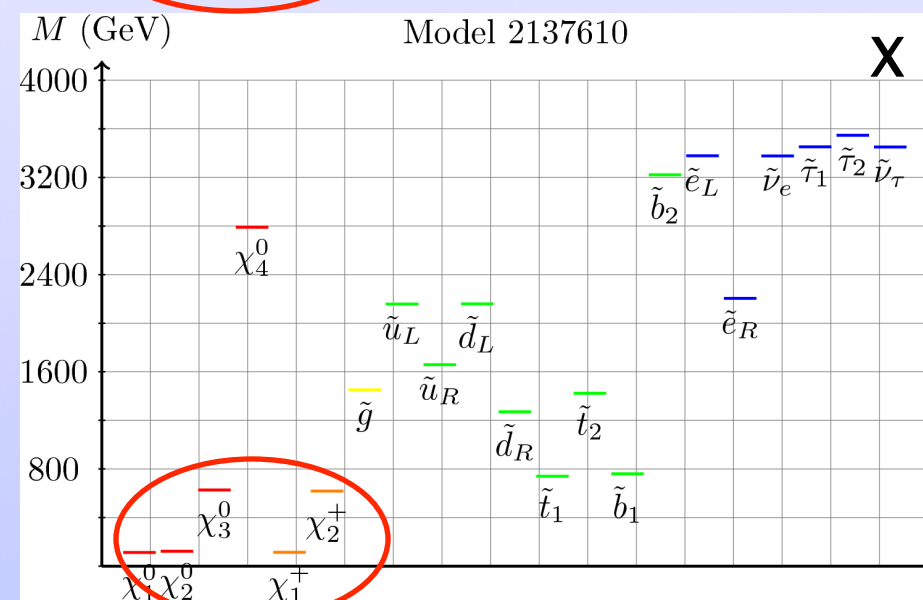
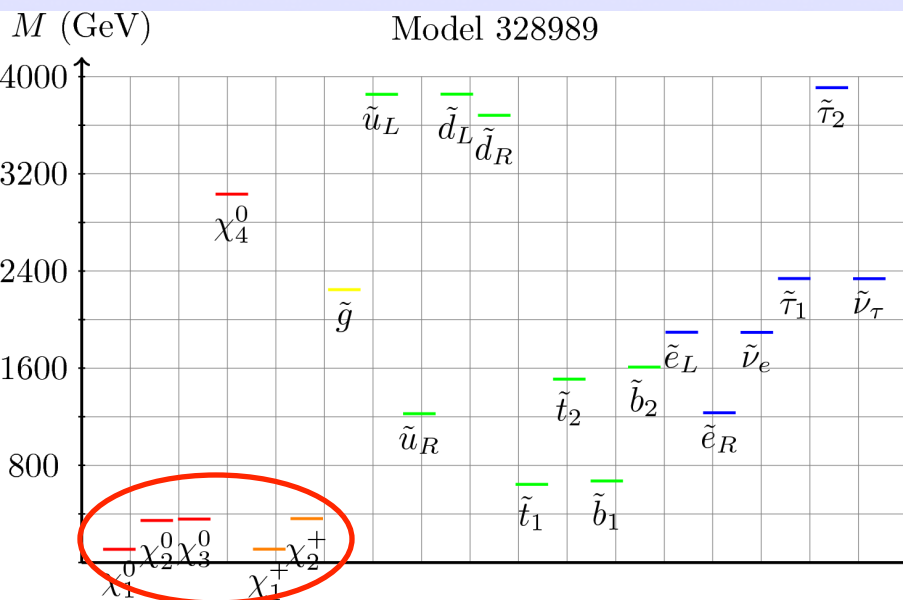
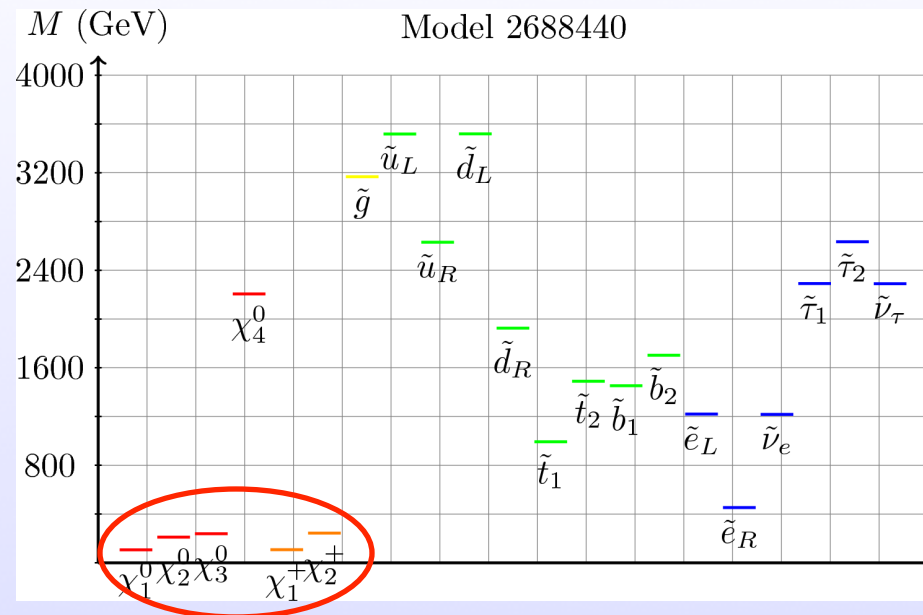
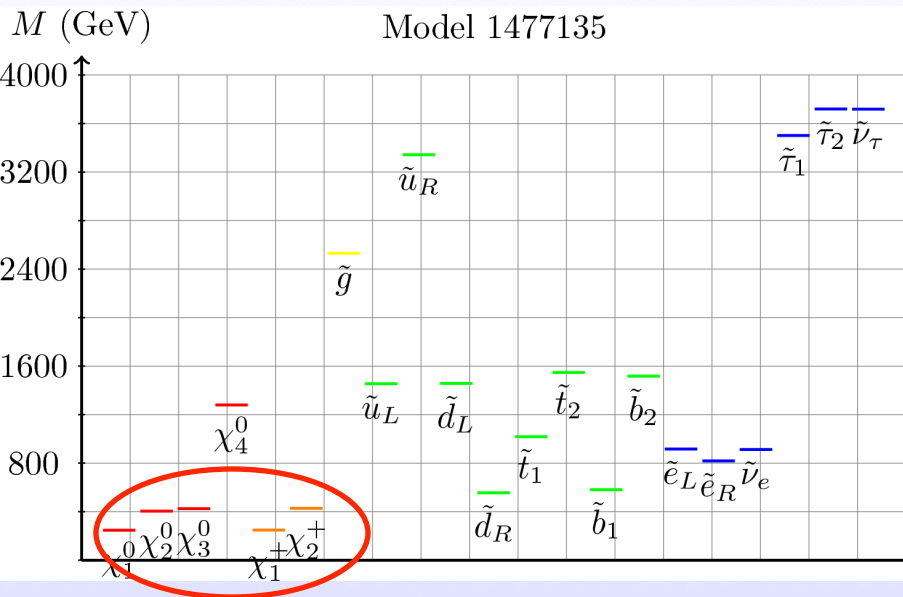
# Low Fine-Tuning Model Spectra I



# Low Fine-Tuning Model Spectra II



# Low Fine-Tuning Model Spectra III



$t_1$  (601 GeV)

Model 1584662  
FT=74.8

$t$  (18%)

$\chi_3^0$  (284 GeV)

$b$  (24%)

$\chi_2^+$  (284 GeV)

$t$  (23%)

$\chi_2^0$  (160 GeV)

$b$  (18%)

$\chi_1^+$  (134 GeV)

$t$  (17%)

$\chi_1^0$  (127 GeV)

$Z$  (12%)

$W$  (77%)

$W$  (24%)

$Z$  (29%)

$h$  (12%)

$h$  (8%)

$Z$  (2%)

$W$  (36%)

$W^*$  (37%)

$Z^*$  (59%)

$\gamma$  (4%)

$W^*$  (100%)



$b_1$  (641 GeV)

Model 1584662  
FT=74.8

$b$  (10%)

$\chi_3^0$  (284 GeV)

$t$  (34%)

$Z$  (12%)

$\chi_2^-$  (284 GeV)

$b$  (8%)

$W$  (77%)

$W$  (24%)

$\chi_2^0$  (160 GeV)

$Z$  (29%)

$t$  (36%)

$h$  (8%)  
 $Z$  (2%)

$h$  (12%)

$W$  (36%)

$W^*$  (37%)

$\chi_1^-$  (134 GeV)

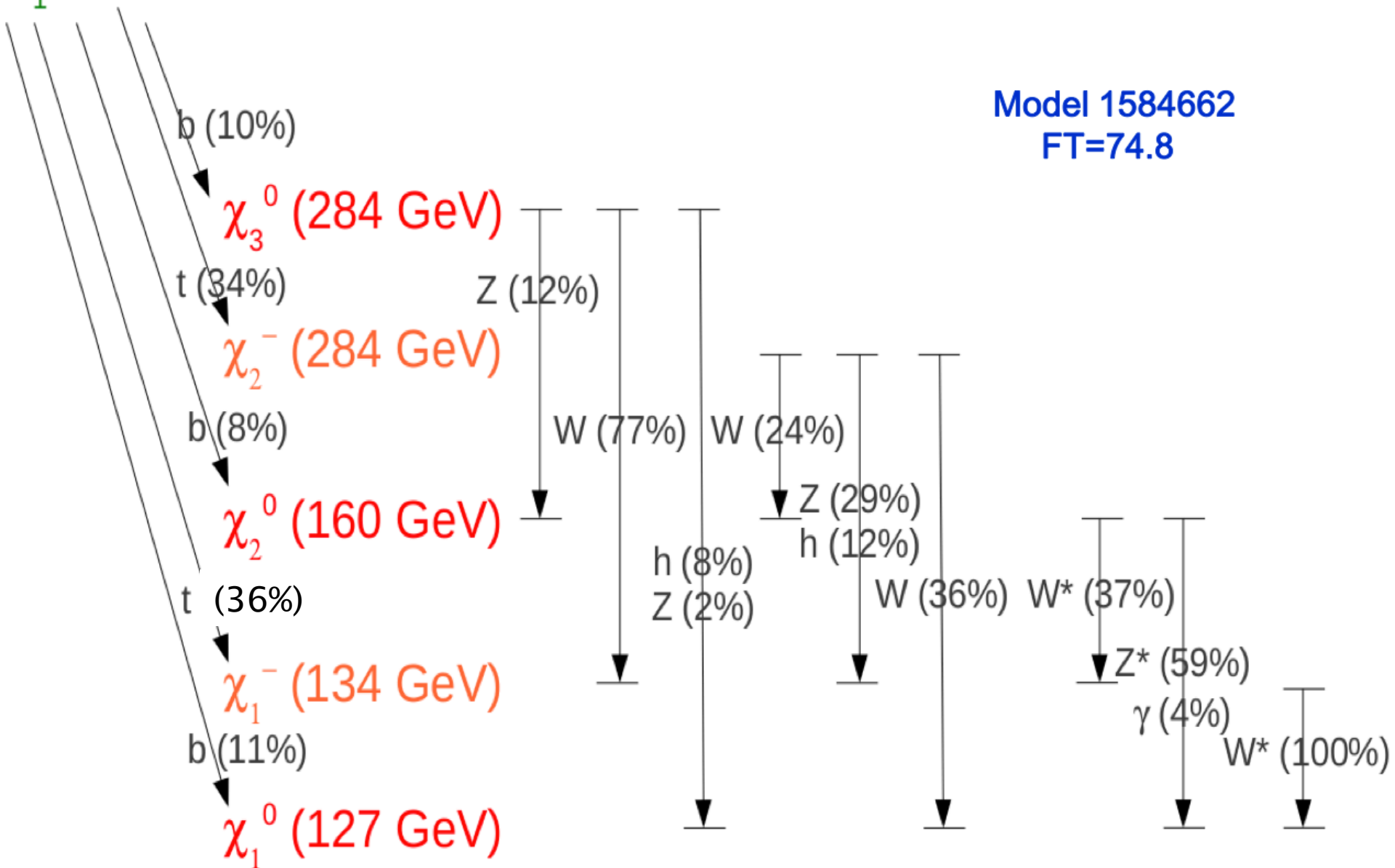
$Z^*$  (59%)

$b$  (11%)

$\gamma$  (4%)

$W^*$  (100%)

$\chi_1^0$  (127 GeV)

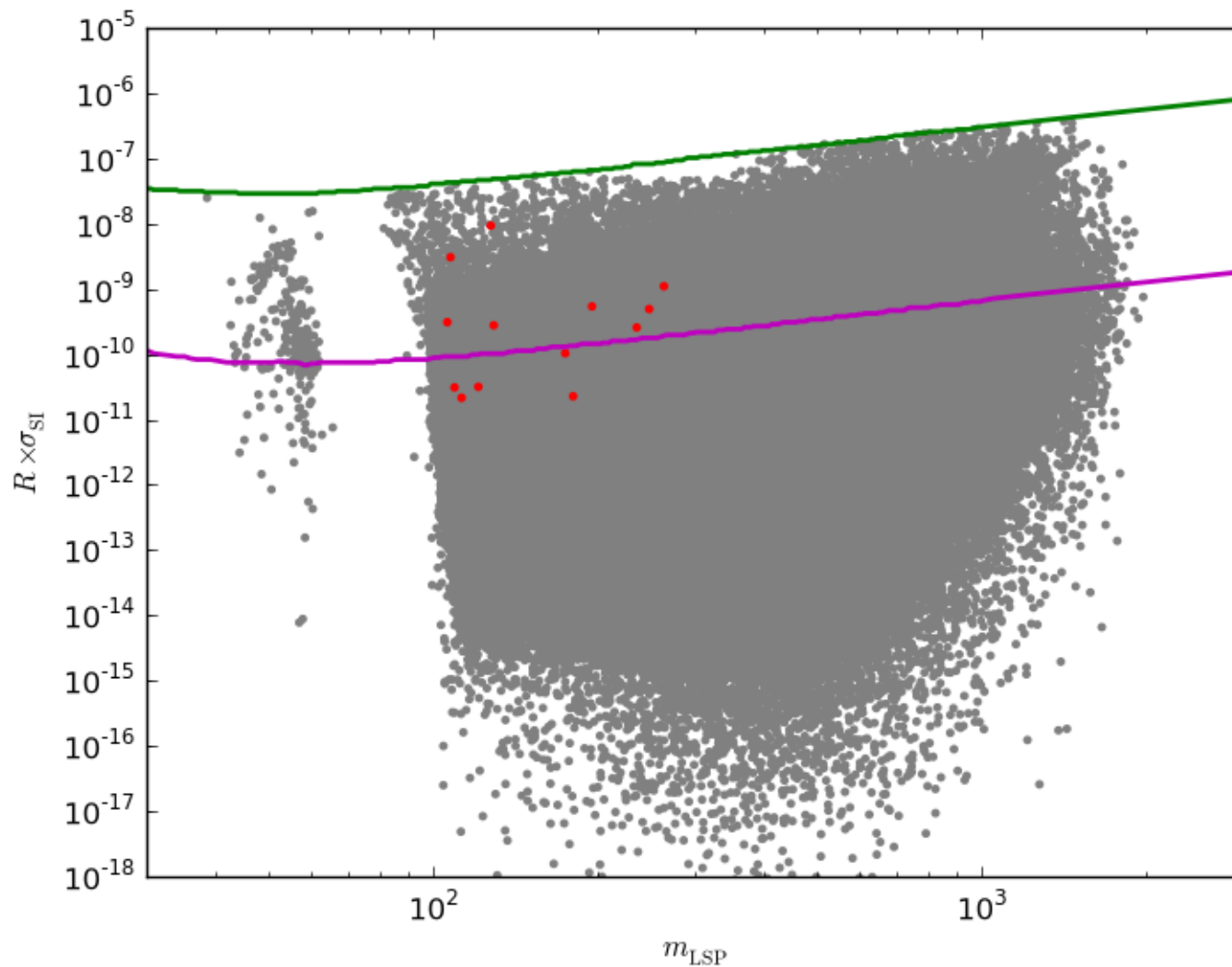


# Conclusions

- Relatively easy to accommodate 125/6 Higgs in the pMSSM
  - Selects region of stop mixing
- Higgs branching fractions are correlated
  - Lower  $b\bar{b}$  predicted
  - Lower  $\tau\tau$  difficult
- Reasonable fine-tuning  $\sim 1\%$  is possible
  - Selects region of parameter space
  - Light stop/sbottom
  - Very light and compressed EW-ino sector: Tailor-made for the ILC!

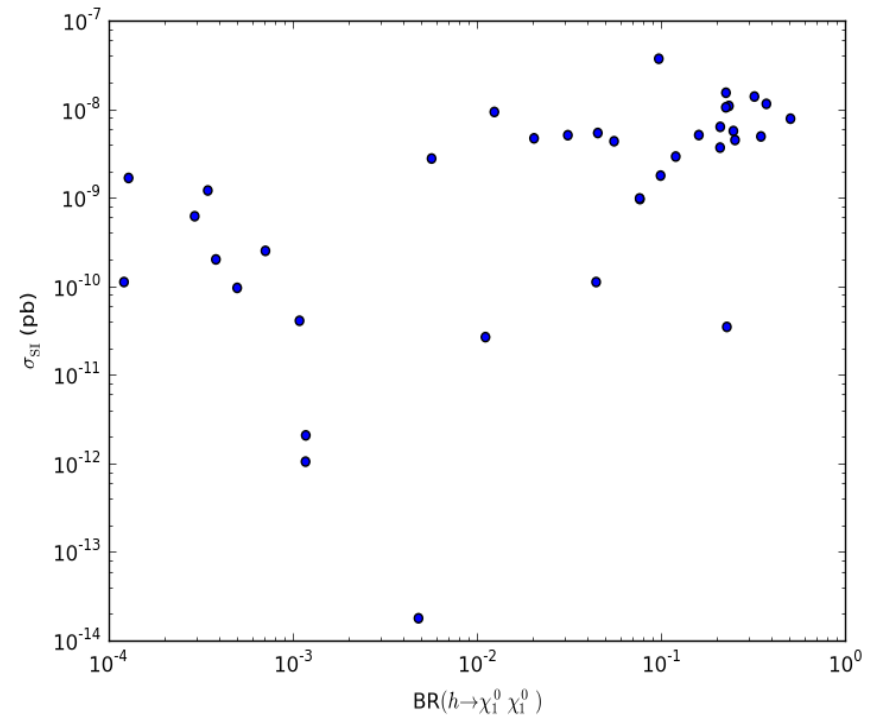
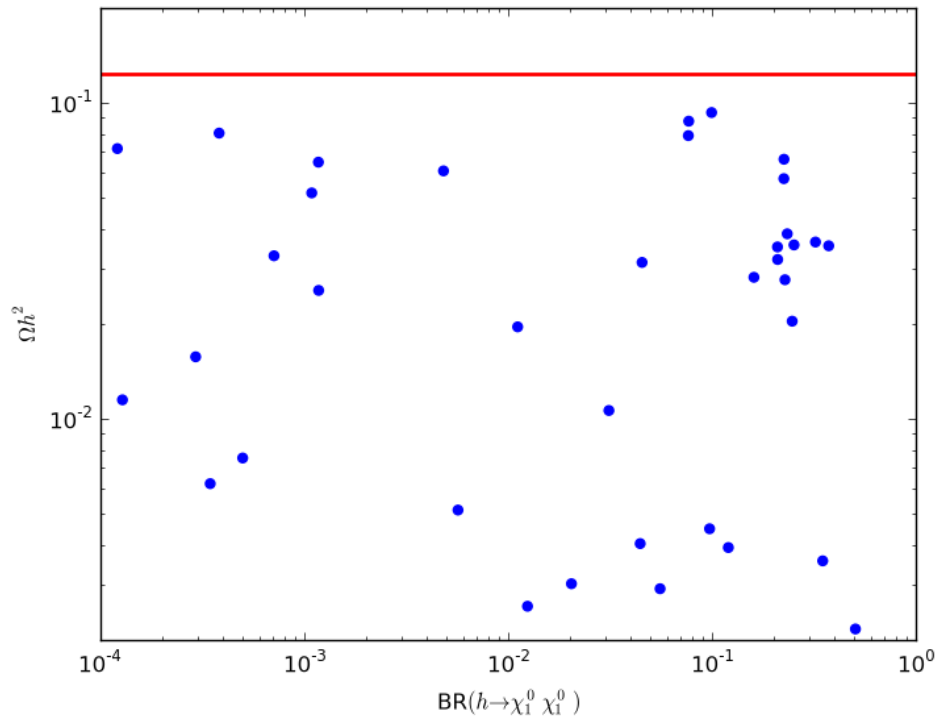
# Backup

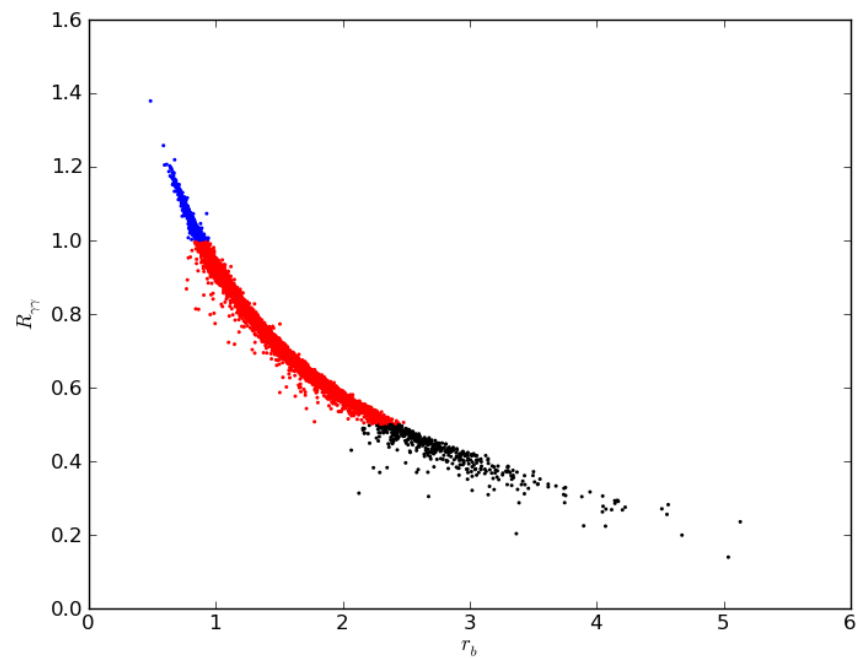
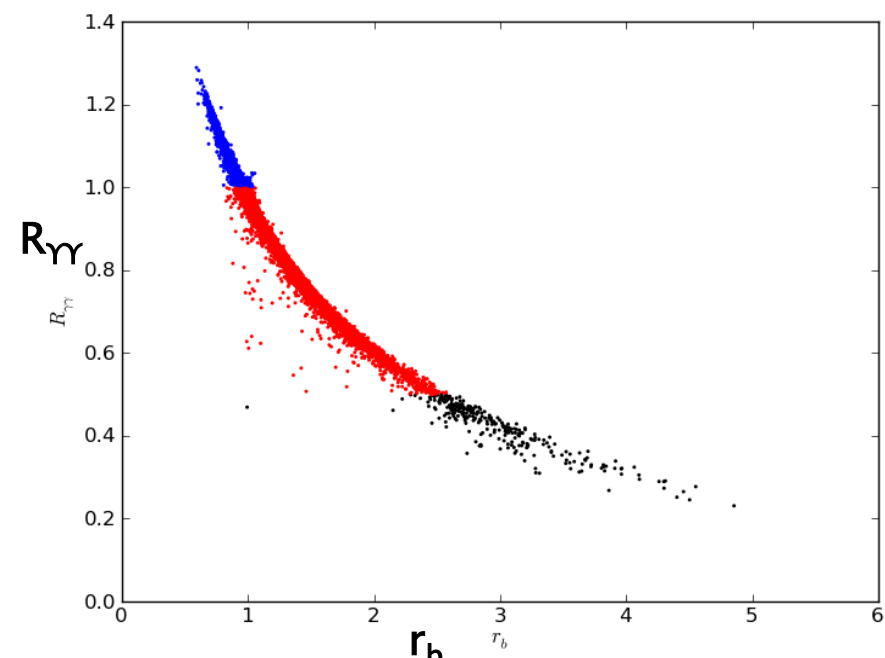
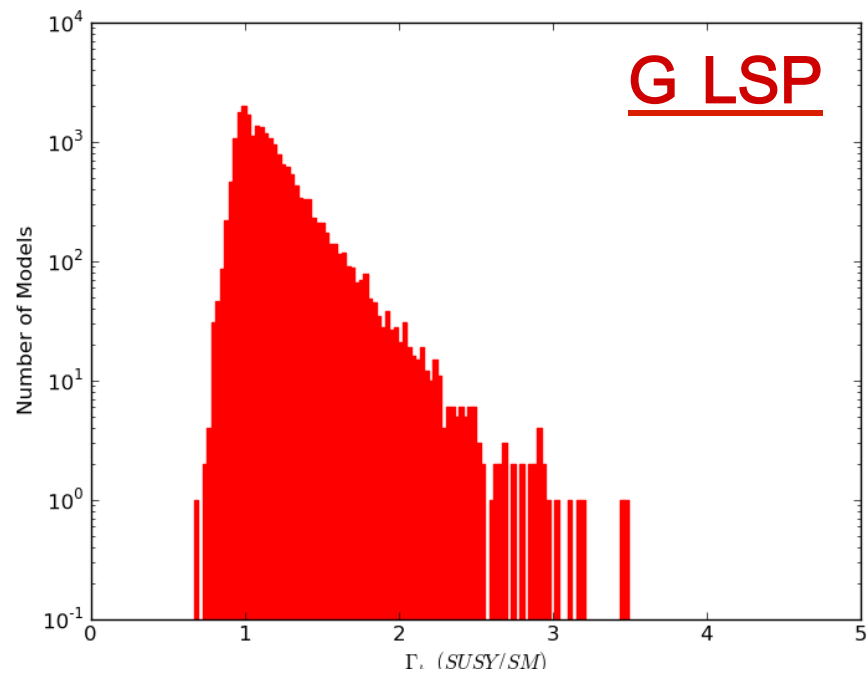
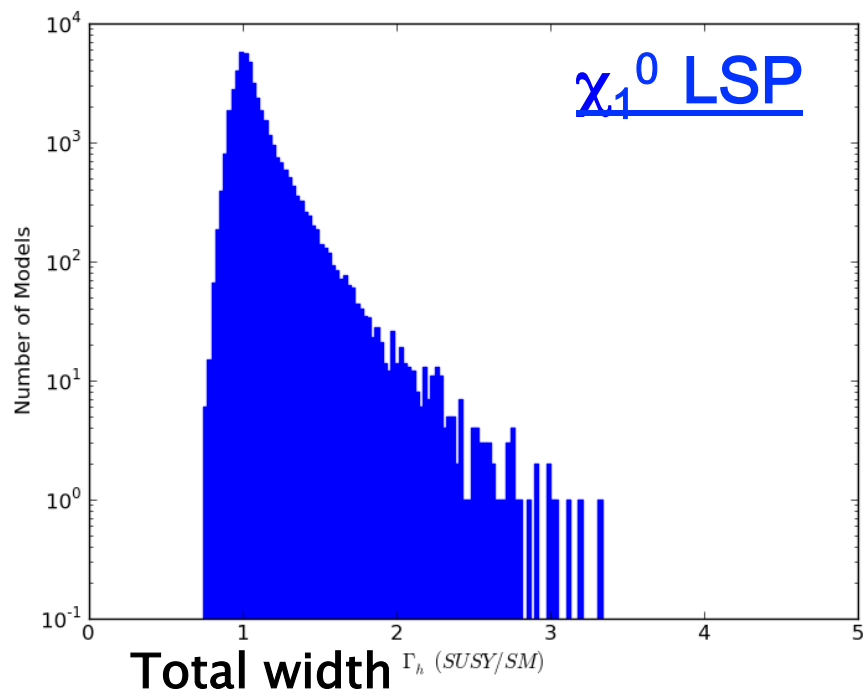
# Direct Detection of Dark Matter



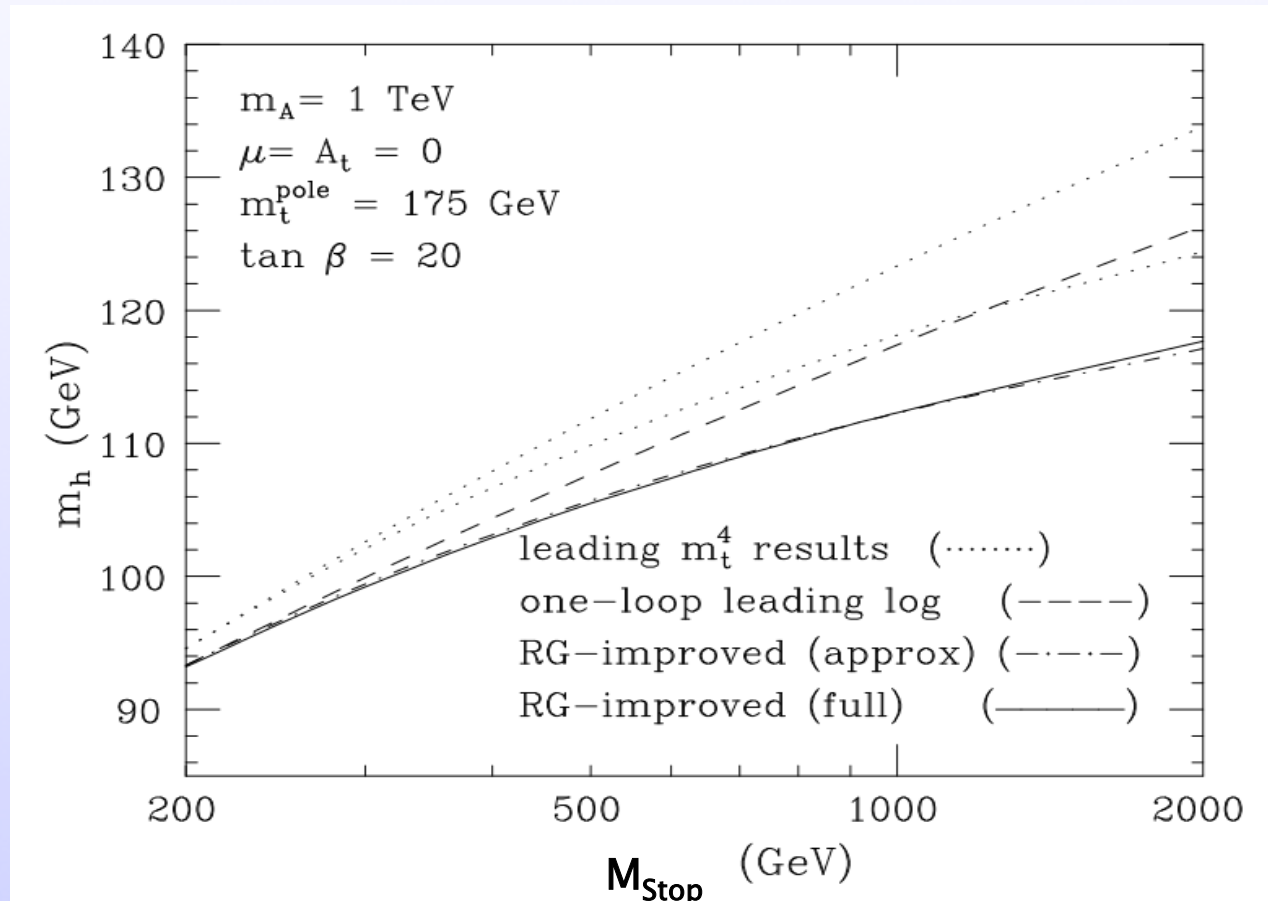


# Astrophysical Properties of Invisible Higgs Models





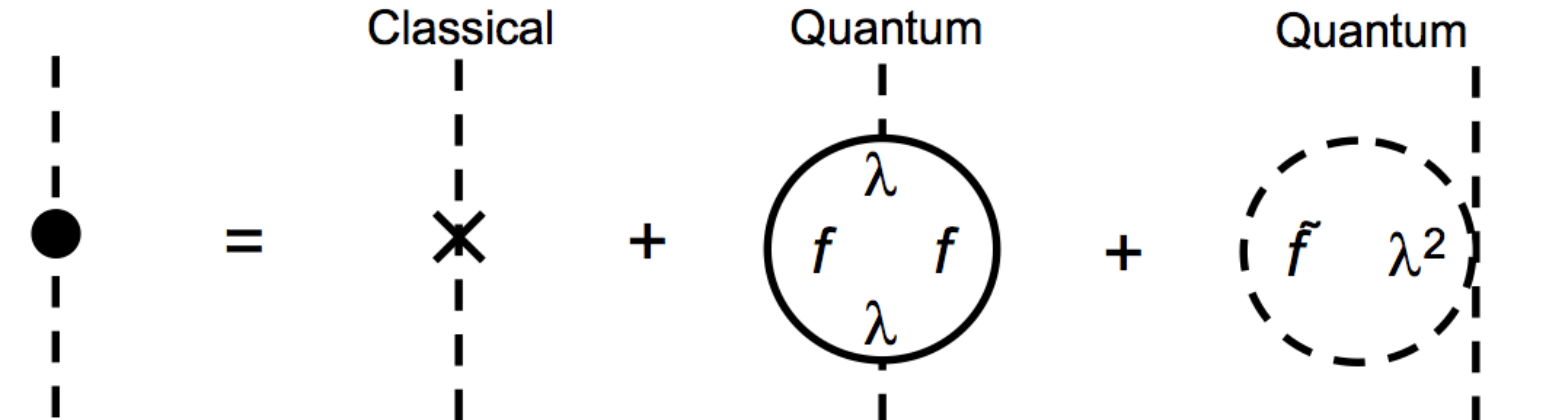
# The SUSY Higgs Sector



Haber, Hempfling

**A heavy  $h^0$  needs a heavy stop-squark  $\tilde{t}_1$**

# Supersymmetry and Naturalness



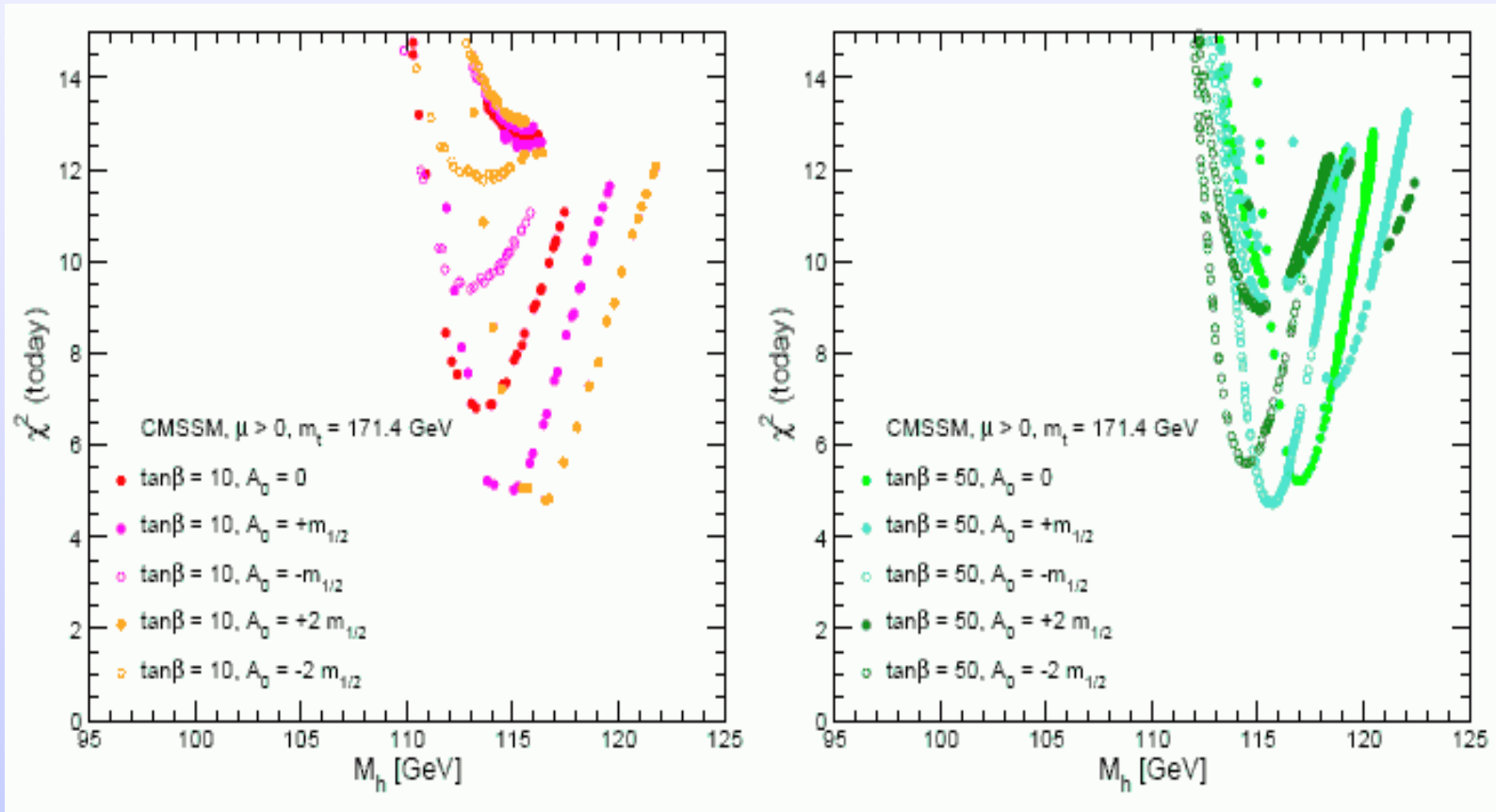
The diagram shows the renormalization of the Higgs mass. On the left, a vertical dashed line with a solid black dot represents the Higgs mass. This is equal to the sum of three terms: a 'Classical' term represented by a vertical dashed line with an 'X', and two 'Quantum' terms. The first quantum term is a solid circle with four external dashed lines and internal labels  $\lambda$  at the top and bottom, and  $f$  on the left and right. The second quantum term is a dashed circle with four external dashed lines and internal labels  $\tilde{f}$  on the left and  $\lambda^2$  on the right.

$$m_h^2 = (m_h^2)_0 - \underbrace{\frac{1}{16\pi^2}\lambda^2\Lambda^2 + \frac{1}{16\pi^2}\lambda^2\Lambda^2}_{\text{Quadratically divergent}} + \frac{1}{16\pi^2}\lambda^2(m_{\tilde{f}}^2 - m_f^2)\ln(\Lambda/m_h)$$

The hierarchy problem needs a light stop-squark  $\tilde{t}_1$

# Predictions for Lightest Higgs Mass in the CMSSM

- $\chi^2$  fit to EW, Flavor, Collider, Cosmology global data set



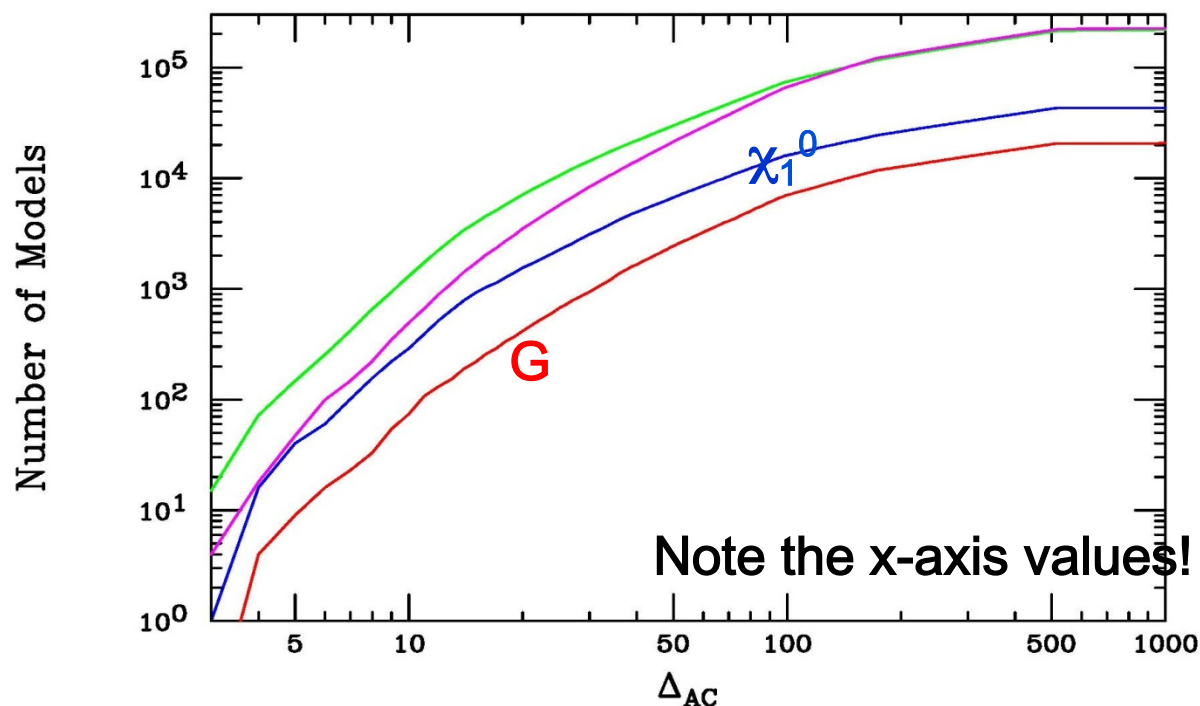
FT from parameter  $a$  is  $\gamma = c/\bar{c}$ .

This definition of  $\bar{c}$  corresponds to

$$\bar{c}^{-1} = \frac{\int da a f(a) c(X; a)^{-1}}{a f(a) \int da}$$

How sensitive is, e.g.,  $M_Z$  to variations of parameter,  $a$ , in a given model  $M$  compared to the entire set of models from which  $M$  was drawn?

where  $c$  is the usual BG result &  $f$  is the distribution of the parameter  $a$  within the full model set (here taken to be flat as generated)

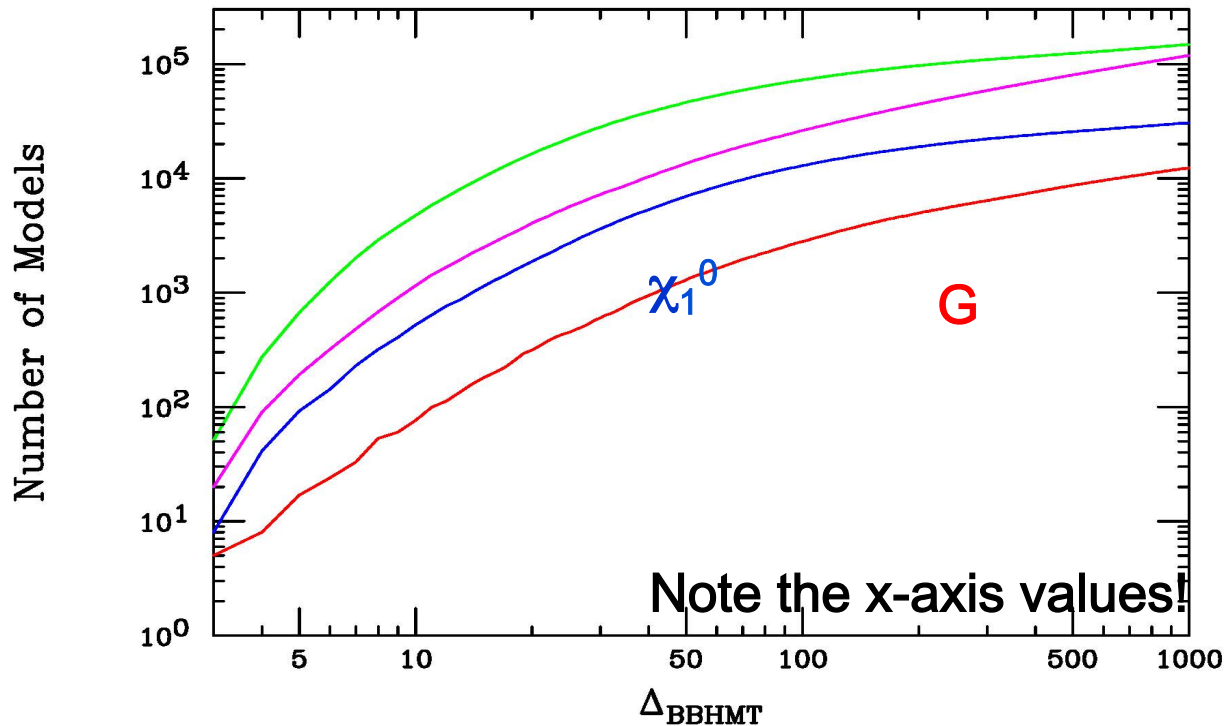




Caveat: there are other possible measures of EW FT...

$$\frac{m_Z^2}{2} = \frac{(m_{H_d}^2 + \Sigma_d^d) - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{(\tan^2 \beta - 1)} + \mu^2$$

Just require RC's (the  $\Sigma$ 's) to be smaller than the LHS ..this is the so-called minimal or 'vanilla' constraints. Then



Baer et al,  
1207.3343

An Example :  
#146314G w/ FT=95.9

## Light Stop Decays

$t_1$  (669)

$b$   
3  
 $\chi_2^+$  (620)

$t$   
22

$W$

23

$t$   
52

$\chi_2^0$  (399)

$Z, h$

26,  
24

$W$

21

$W^*$

$Z^*$

$\gamma$

16,6

$b$   
23

$\chi_1^0$  (384)

$W^*$

100

78

$\chi_1^+$  (381)

$W G$

An Example :  
 #2592398 w/  $FT_{\text{BBHMT}} = 6.6$

## Light Stop Decays

