

Introduction to Higgs physics at future e^+e^- — focused on single Higgs

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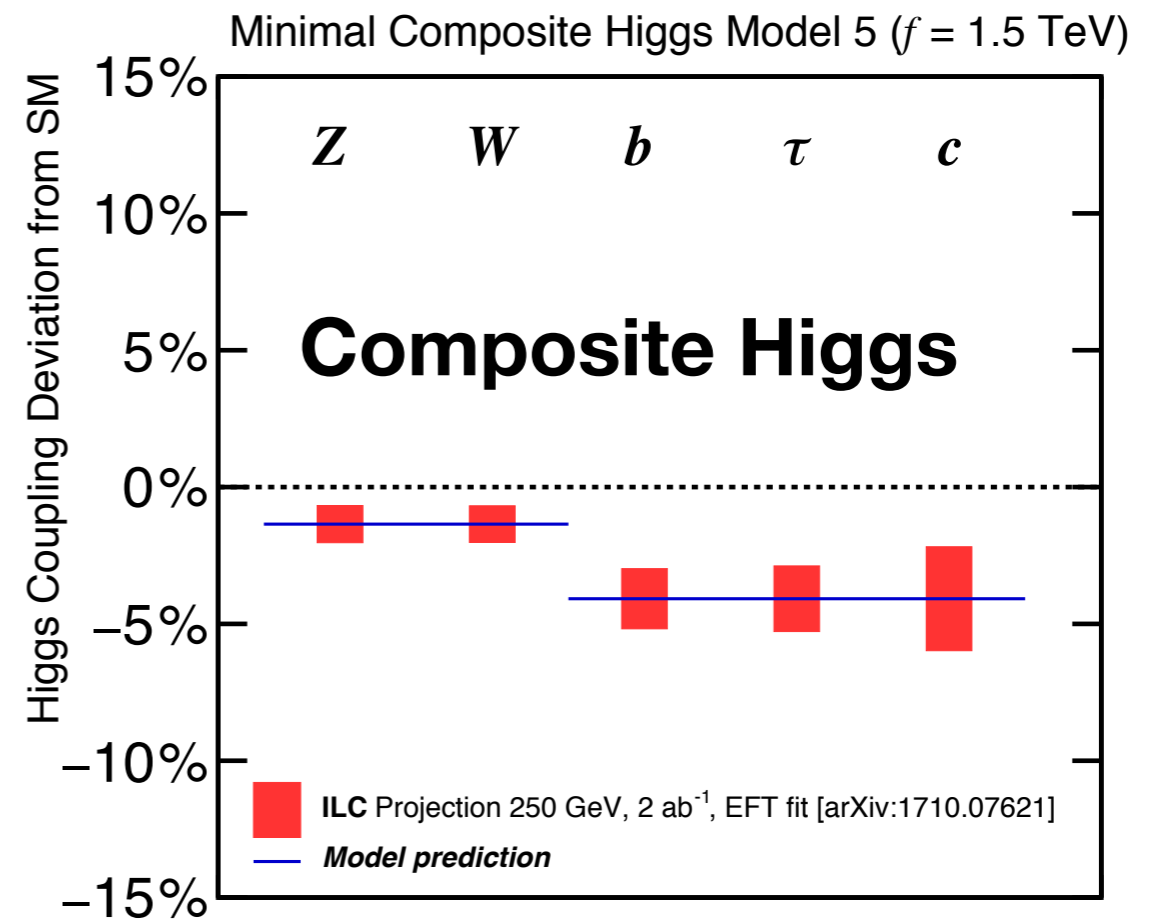
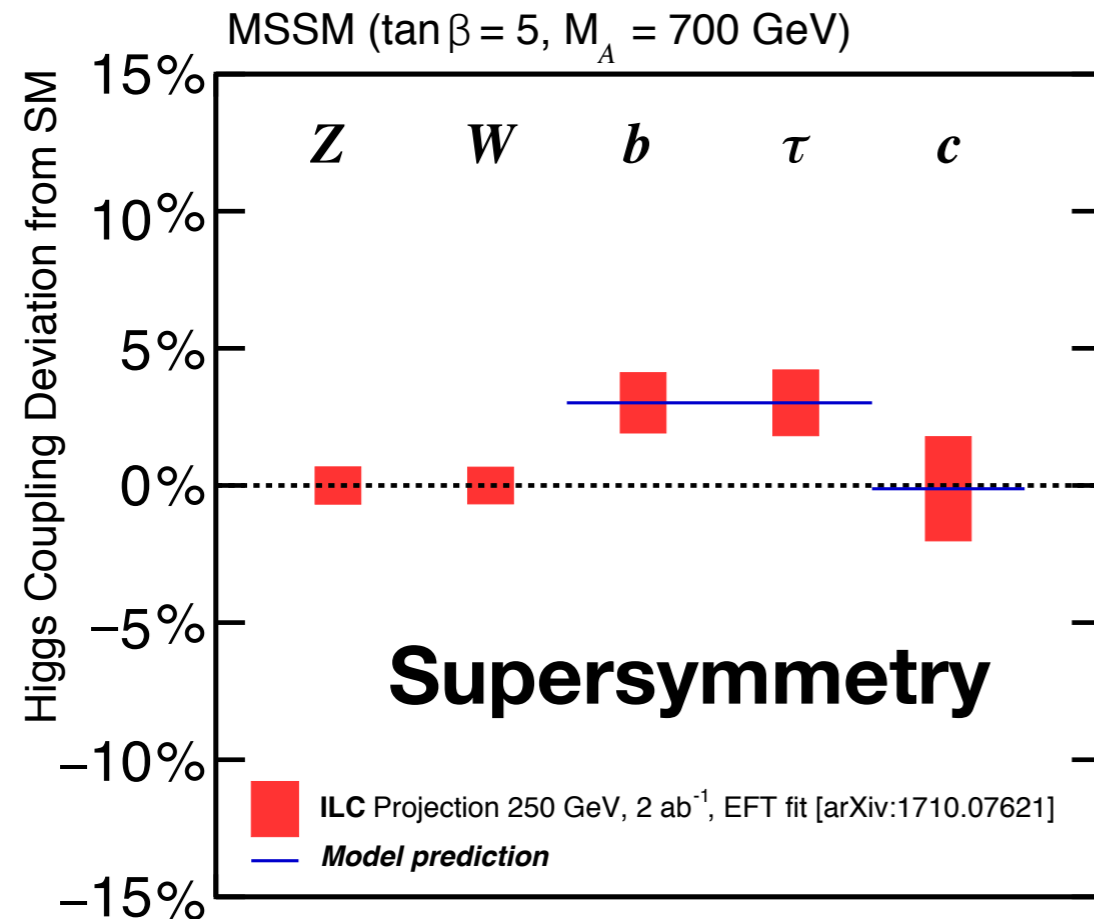
for comprehensive review, arXiv:1903.01629; 2203.07622

outline

- Introduction
- Single-Higgs cross section
- Differential cross section & CP
- Interplay between Higgs/EW/Top
- summary

opportunities from precision Higgs couplings

— another way towards discovery



arXiv: 1306.6352

- measuring deviation pattern of Higgs couplings will reveal the nature of BSM physics

general guidelines for Higgs coupling meas. @ future e+e-

—in light of what have been found at LHC

- new particles are heavy, deviation is small, 1-10% for $m_{\text{BSM}} \sim 1\text{TeV}$: need measurement with **1% precision** or below so that deviations with SM can be discovered
- measurement needs to be as **model-independent** as possible: so that the true BSM model can be discriminated from others, future HEP direction hence can be decided

proposals of future e+e- colliders

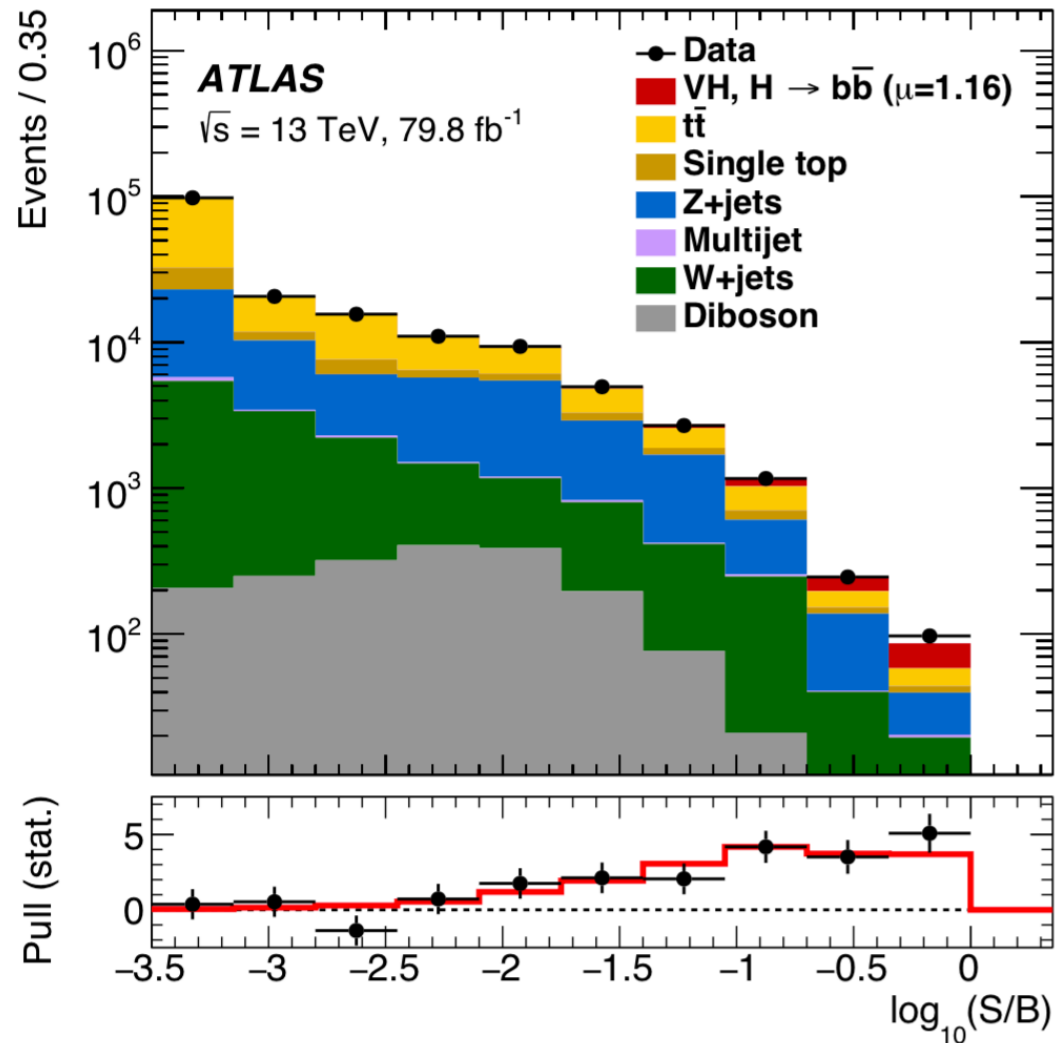
	\sqrt{s}	beam polarisation	$\int L dt$ (baseline)	R&D phase
ILC	0.1 - 1 TeV	e-: 80% e+: 30% (20%)	2 ab ⁻¹ @ 250 GeV 0.2 ab ⁻¹ @ 350 GeV 4 ab ⁻¹ @ 500 GeV 8 ab ⁻¹ @ 1 TeV	TDR 2013
CLIC	0.35 - 3 TeV	e-: (80%) e+: 0%	1 ab ⁻¹ @ 380 GeV 2.5 ab ⁻¹ @ 1.5 TeV 5 ab ⁻¹ @ 3 TeV	CDR 2012
CEPC	90 - 240 GeV	e-: 0% e+: 0%	20 ab ⁻¹ @ 240 GeV 100 ab ⁻¹ @ M _Z 6 ab ⁻¹ @ 2M _w	TDR 2022
FCC-ee	90 - 350 GeV	e-: 0% e+: 0%	150 ab ⁻¹ @ M _Z 10 ab ⁻¹ @ 2M _w 5 ab ⁻¹ @ 240 GeV 1.7 ab ⁻¹ @ 365 GeV	CDR 2018

common: Higgs factory with O(10⁶) Higgs events

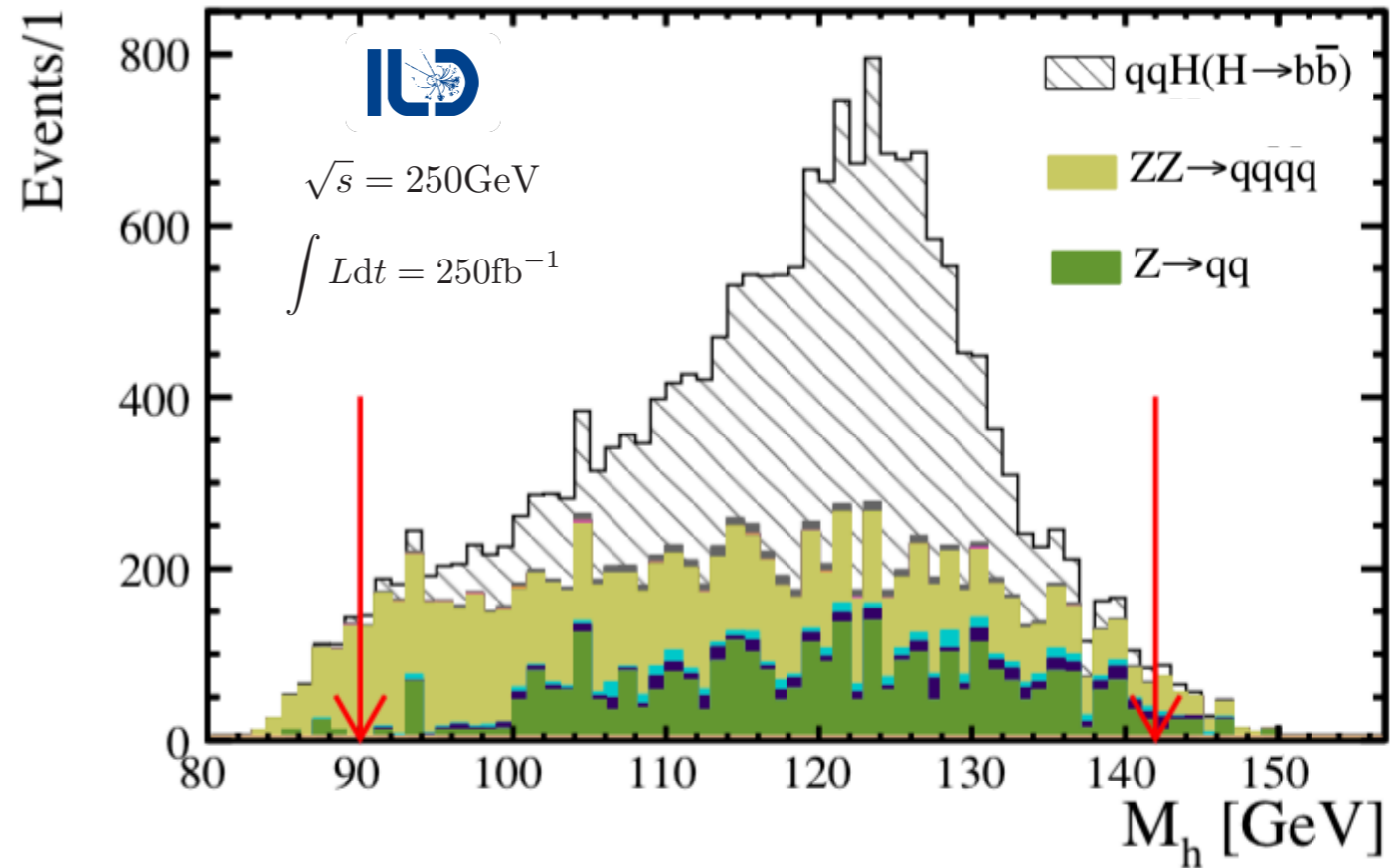
differ in energy reach, luminosity, polarization, project readiness

statistics vs S/B: example on $H \rightarrow bb$ discovery

LHC (super Higgs factory # 10^8)



e^+e^- (Higgs factory # 10^6)



full detector simulation

of Higgs produced: $\sim 4,000,000$

~ 400

significance: 5.4σ

5.2σ

[ATLAS, 1808.08238; CMS, 1808.08242]

[Ogawa, PhD Thesis (Sokendai)]

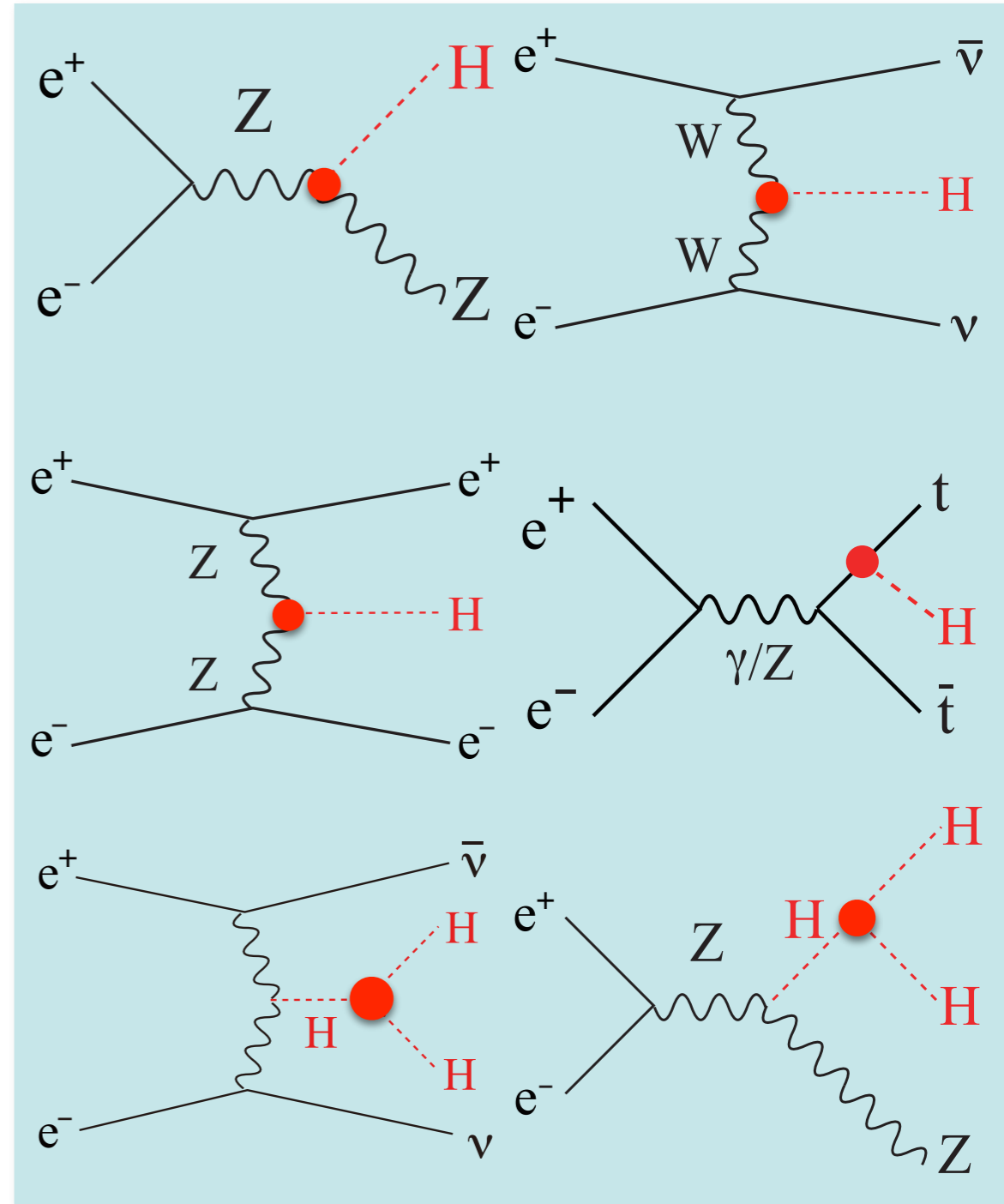
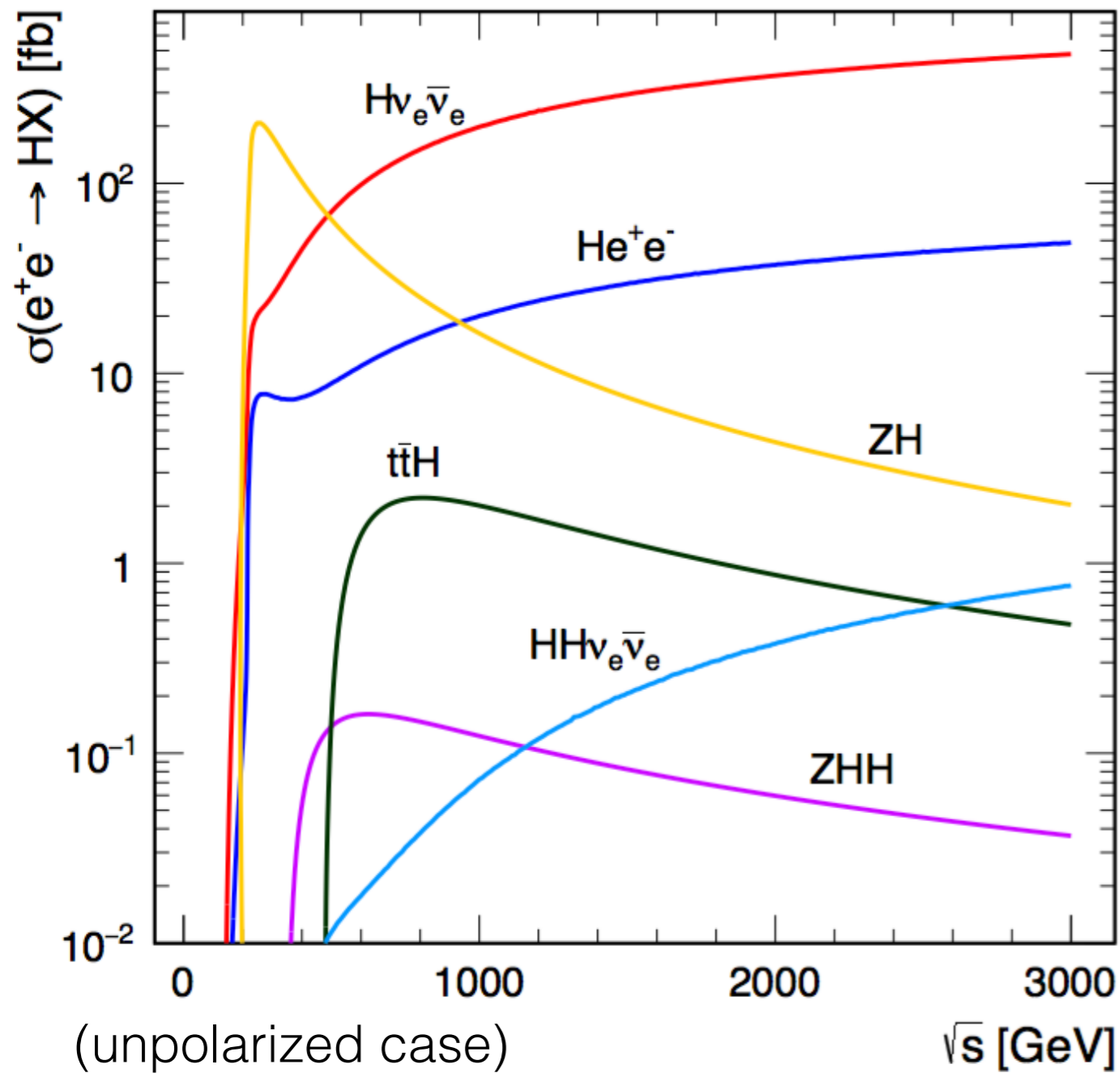
(precision meas.)

“that is much much easier, infinitely easier,
on a e^+e^- machine than on a proton machine”



youtube: Burton Richter #mylinearcollider, 2015

(ii) Higgs productions at e^+e^-



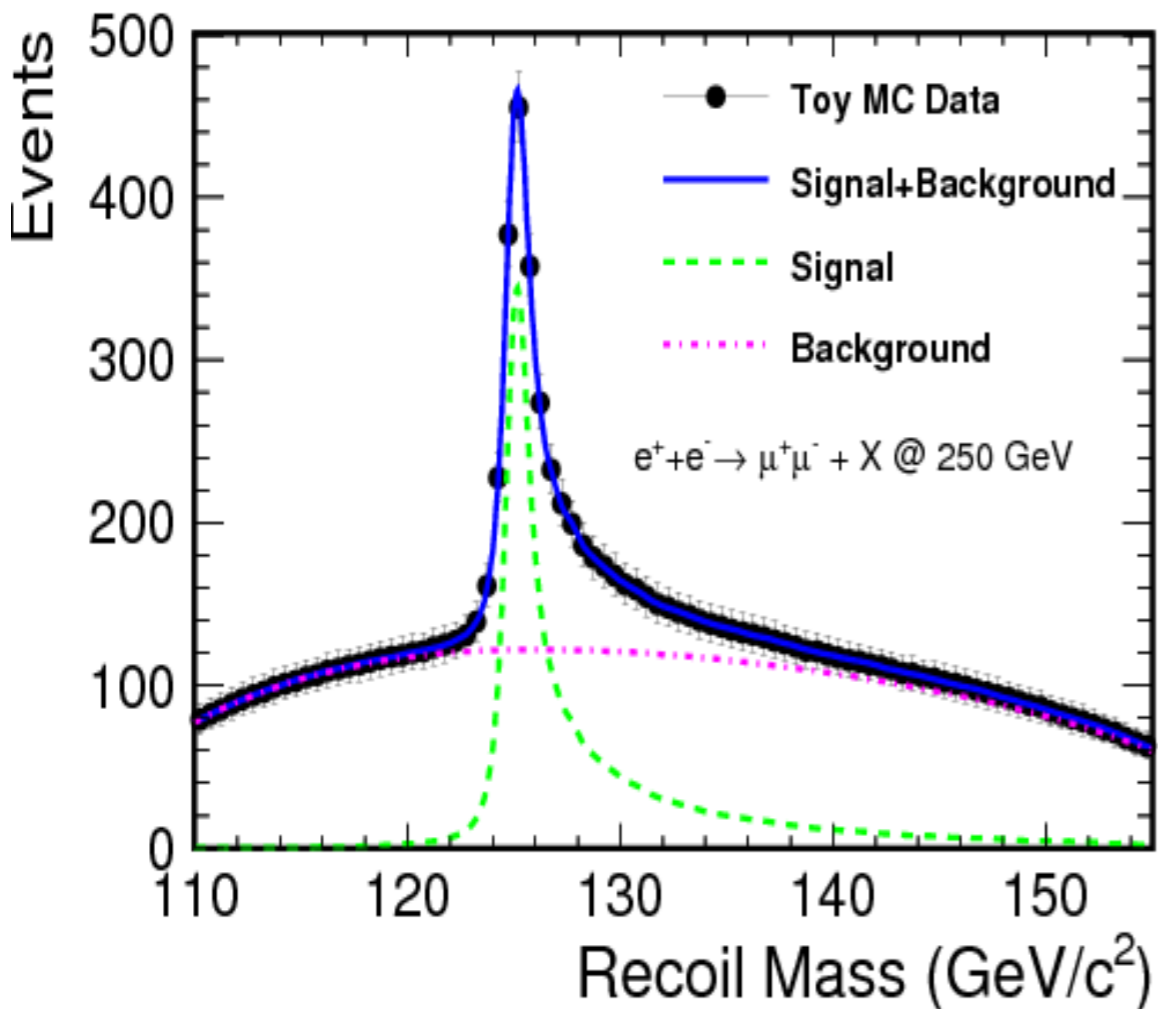
- two apparent important thresholds: $\sqrt{s} \sim 250$ GeV for **ZH**, ~ 500 - 600 GeV for **ZHH** and **ttH**
- + another threshold for **t t-bar**, important for Higgs physics as well

direct experimental observables: some are unique @ e+e-

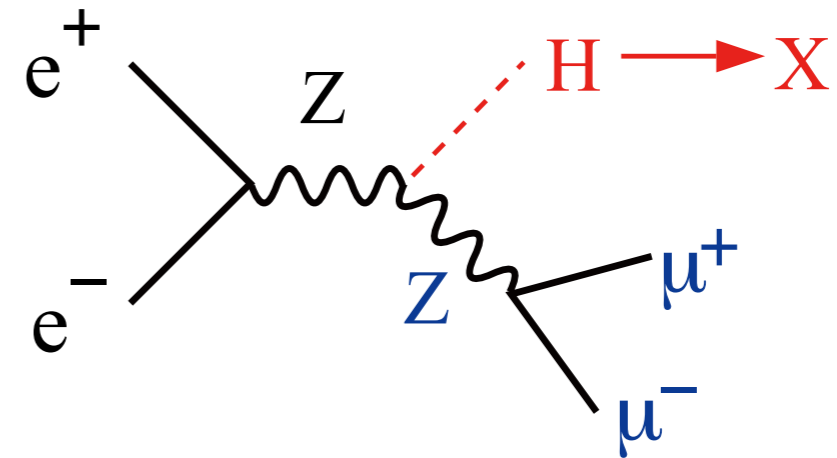
- ☑ σ_{ZH}
- ☑ $\sigma_{ZH} \times \text{Br}(H \rightarrow bb), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow bb)$
- ☑ $\sigma_{ZH} \times \text{Br}(H \rightarrow cc), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow cc)$
- ☑ $\sigma_{ZH} \times \text{Br}(H \rightarrow gg), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow gg)$
- ☑ $\sigma_{ZH} \times \text{Br}(H \rightarrow WW^*), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow WW^*)$
- ☑ $\sigma_{ZH} \times \text{Br}(H \rightarrow ZZ^*), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow ZZ^*)$
- ☑ $\sigma_{ZH} \times \text{Br}(H \rightarrow \tau\tau), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \tau\tau)$
- ☑ $\sigma_{ZH} \times \text{Br}(H \rightarrow \gamma\gamma), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \gamma\gamma)$
- ☑ $\sigma_{ZH} \times \text{Br}(H \rightarrow \mu\mu), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \mu\mu)$
- ☑ $\sigma_{ZH} \times \text{Br}(H \rightarrow \text{Invisible} / \text{Exotic})$
- ☑ $\sigma_{ttH} \times \text{Br}(H \rightarrow bb)$
- ☑ $\sigma_{ZH\text{HH}} \times \text{Br}^2(H \rightarrow bb), \sigma_{\nu\nu\text{HH}} \times \text{Br}^2(H \rightarrow bb)$

note the important synergy with LHC: $H \rightarrow \gamma\gamma / \gamma Z / \mu\mu$

(ii-1) inclusive σ_{ZH} : the key for model independence



for $Z \rightarrow ll$, Yan et al, arXiv:1604.07524;
 for $Z \rightarrow qq$, Thomson, arXiv:1509.02853



$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

- well defined initial states at e^+e^-
- recoil mass technique \rightarrow tag Z only
- Higgs is tagged without looking into H decay
- absolute cross section of $e^+e^- \rightarrow ZH$

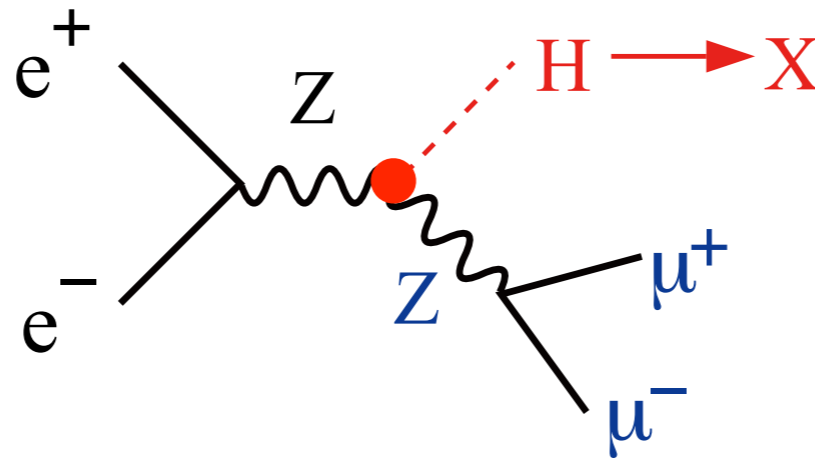
same technique can be used to search for $H \rightarrow$ invisible / exotic decays

independent of H decay modes?

$$e^+ + e^- \rightarrow ZH \rightarrow l^+ l^- / q\bar{q} + X$$

- this question is almost equivalent to whether we can tag the Z decay products unambiguously
- might be easy in Z->ll, certainly not trivial in Z->qq
- even in Z->ll mode, we know there can be isolated leptons from Higgs decay, e.g. H->WW*/τ τ/ZZ, which get mis-identified as leptons from Z decay
- keep in mind we are targeting 0.1-1% precision measurement

independent of HZZ vertex?



- different HZZ vertex might change angular distributions of Z
- hence, this question is equivalent to whether the selections cuts are democratic for all production angles of Z
- open question, this is not sufficiently studied yet

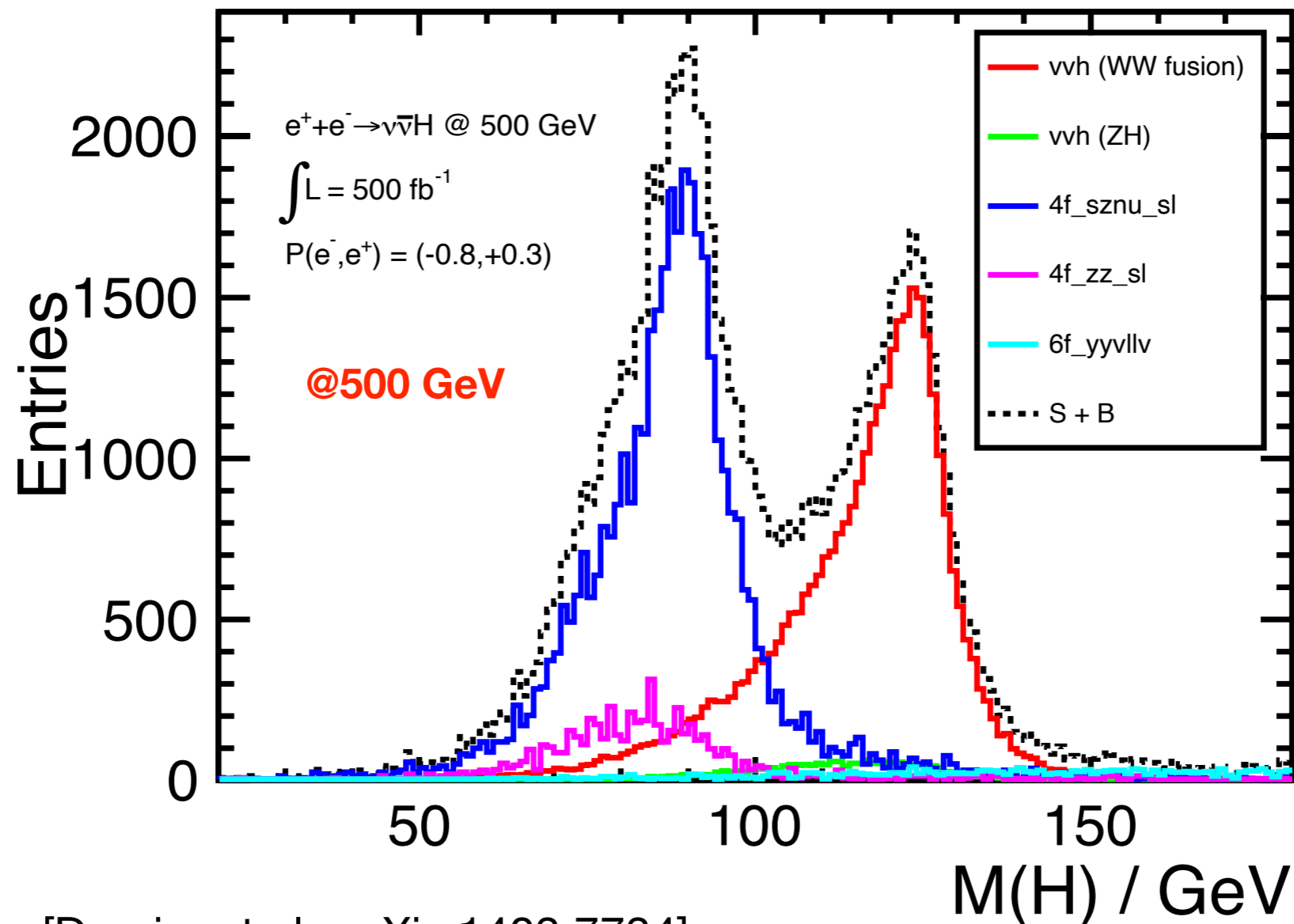
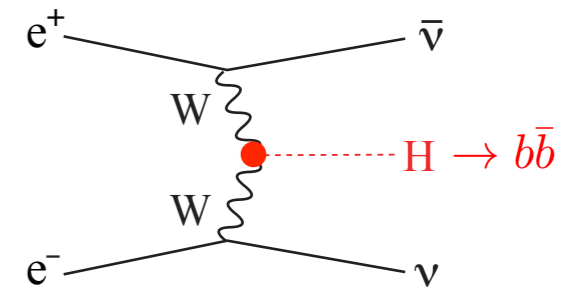
(ii-2) WW-fusion channel & Higgs total width Γ_H

$$\Gamma_H = \frac{\Gamma_{HZZ}}{\text{Br}(H \rightarrow ZZ^*)} \propto \frac{g_{HZZ}^2}{\text{Br}(H \rightarrow ZZ^*)}$$

—> Br(H->ZZ*) very small

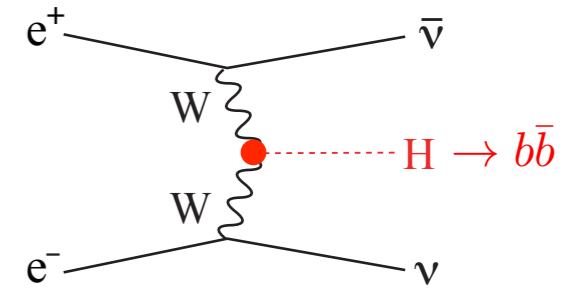
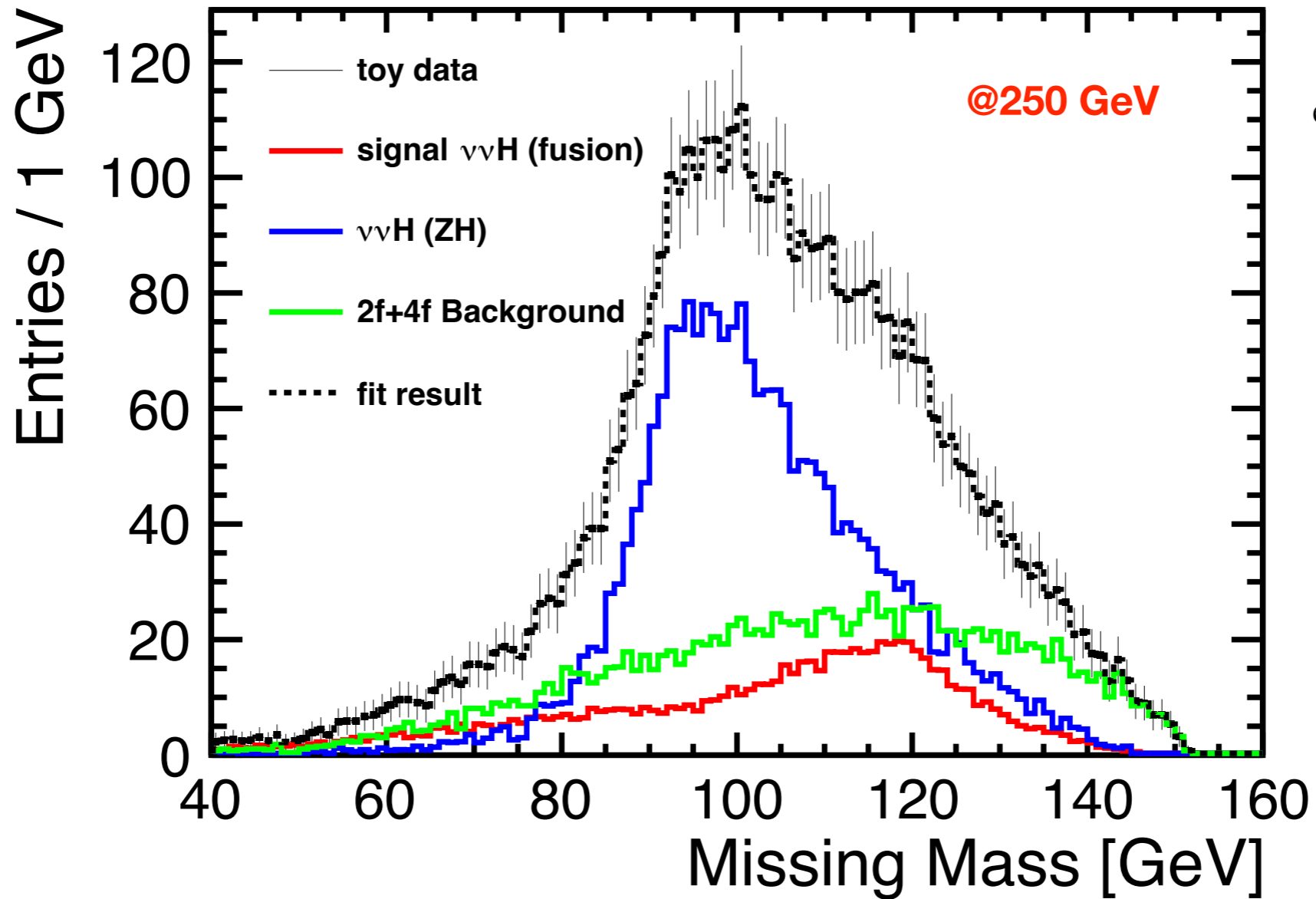
★
$$\Gamma_H = \frac{\Gamma_{HWW}}{\text{Br}(H \rightarrow WW^*)} \propto \frac{g_{HWW}^2}{\text{Br}(H \rightarrow WW^*)}$$

—> better option!



[Duerig, et al., arXiv:1403.7734]

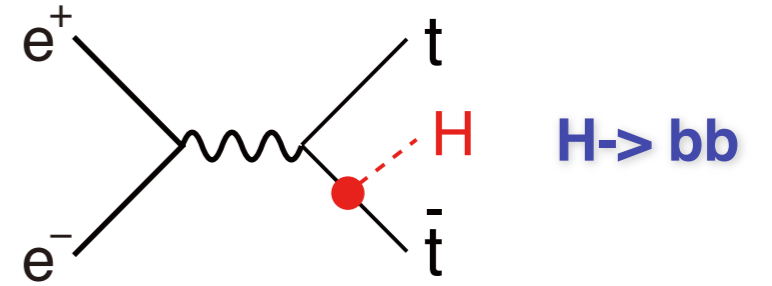
very different at $\sqrt{s}=250$ GeV



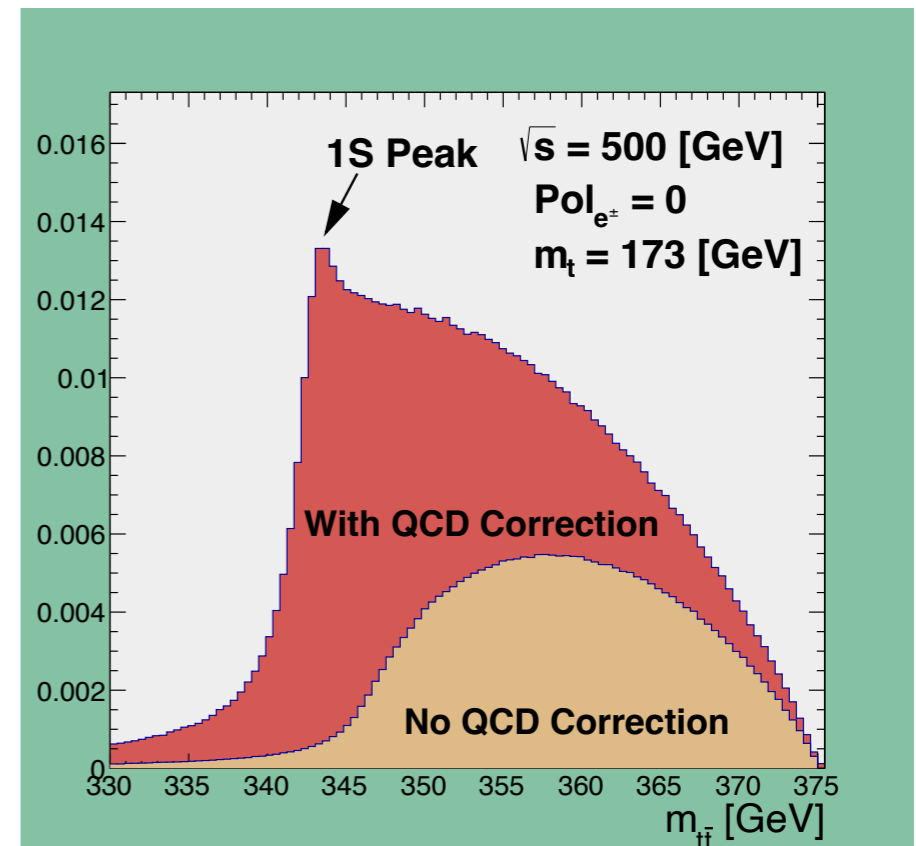
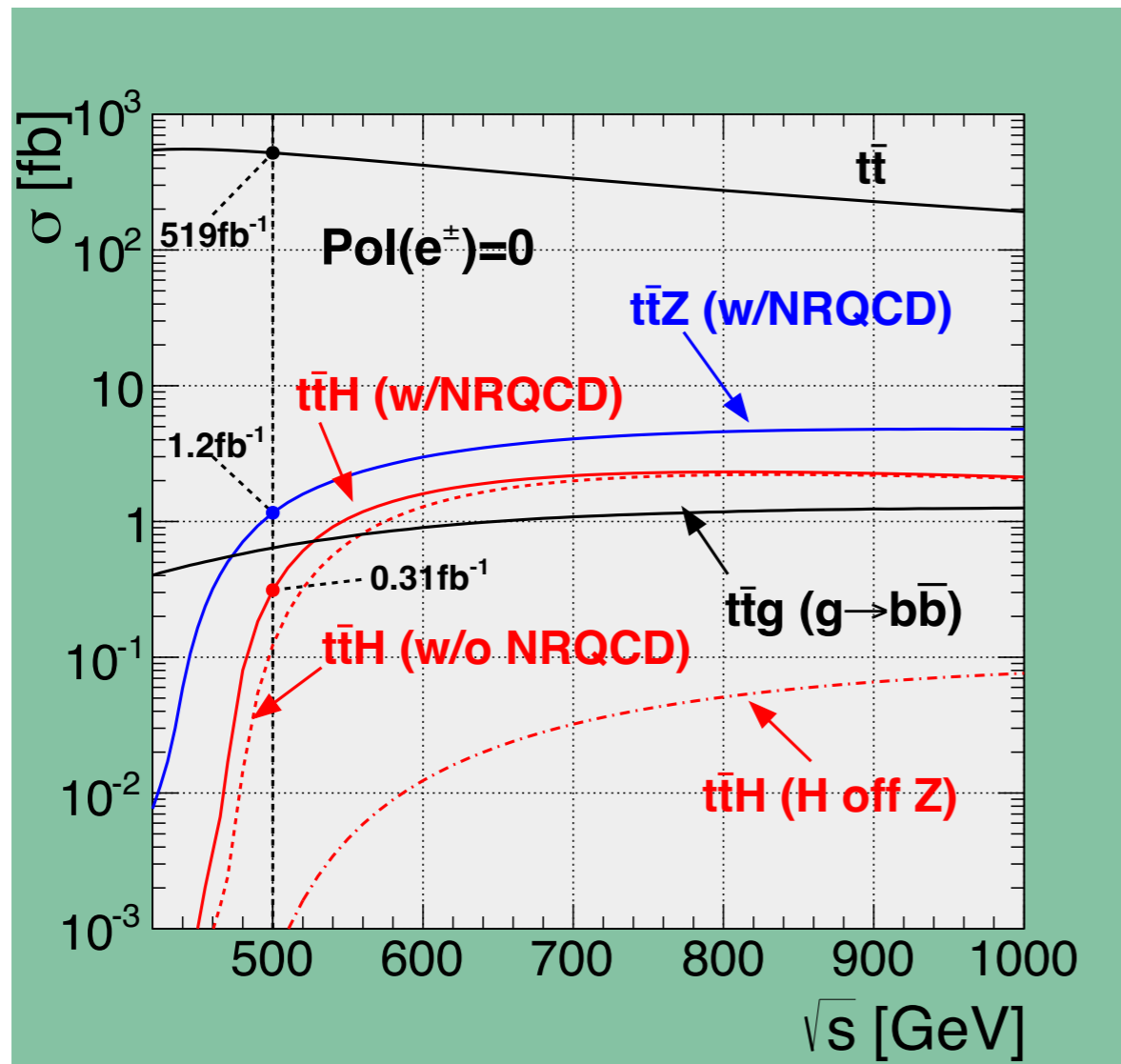
$\rho = -34\%$ correlation between
 $\sigma_{\nu\nu H} \times BR(H \rightarrow b\bar{b})$ and $\sigma_{ZH} \times BR(H \rightarrow b\bar{b})$

(ii-3) Top-Yukawa coupling

- ▶ largest Yukawa coupling; crucial role
- ▶ non-relativistic $t\bar{t}$ bound state correction: enhancement by ~ 2 at 500 GeV
- ▶ Higgs CP measurement



$\Delta g_{ttH} / g_{ttH}$	500 GeV	+ 1 TeV
ILC	6.3%	1.5%

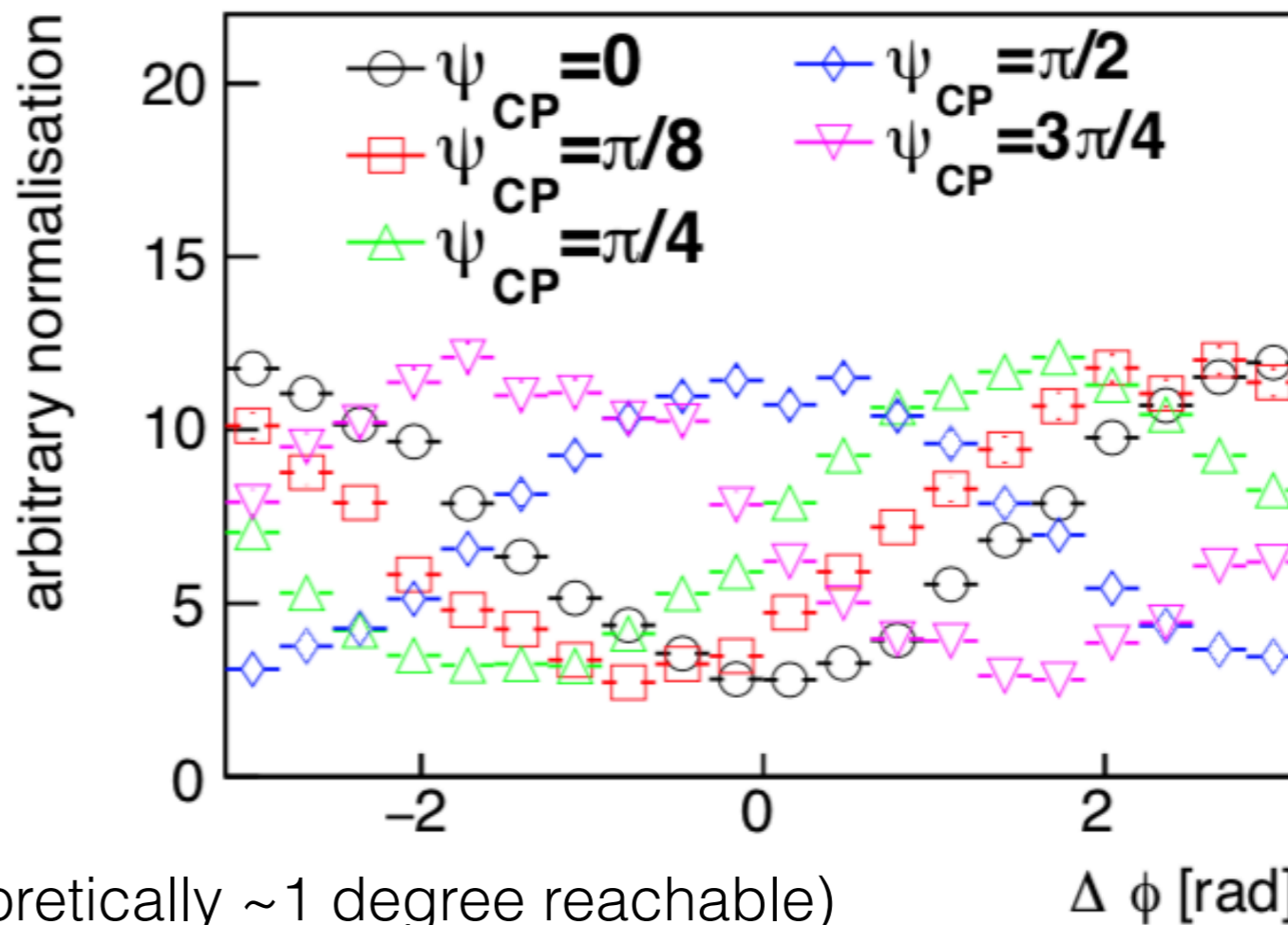
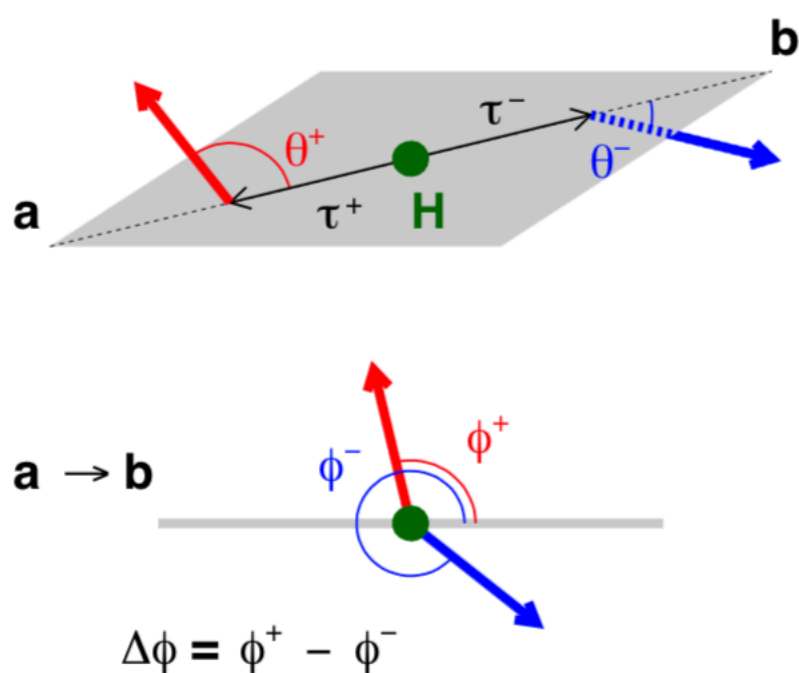


Yonamine, et al., PRD84, 014033;
Price, et al., Eur. Phys. J. C75 (2015) 309

(iii-1) Higgs CP in $H \rightarrow \tau^+ \tau^-$

○ CP is essential to understand structures of all Higgs couplings

$$L_{Hff} = -\frac{m_f}{v} H \bar{f} (\cos \Phi_{CP} + i \gamma^5 \sin \Phi_{CP}) f$$



$$\Delta \Phi_{CP} \sim 4.3^\circ$$

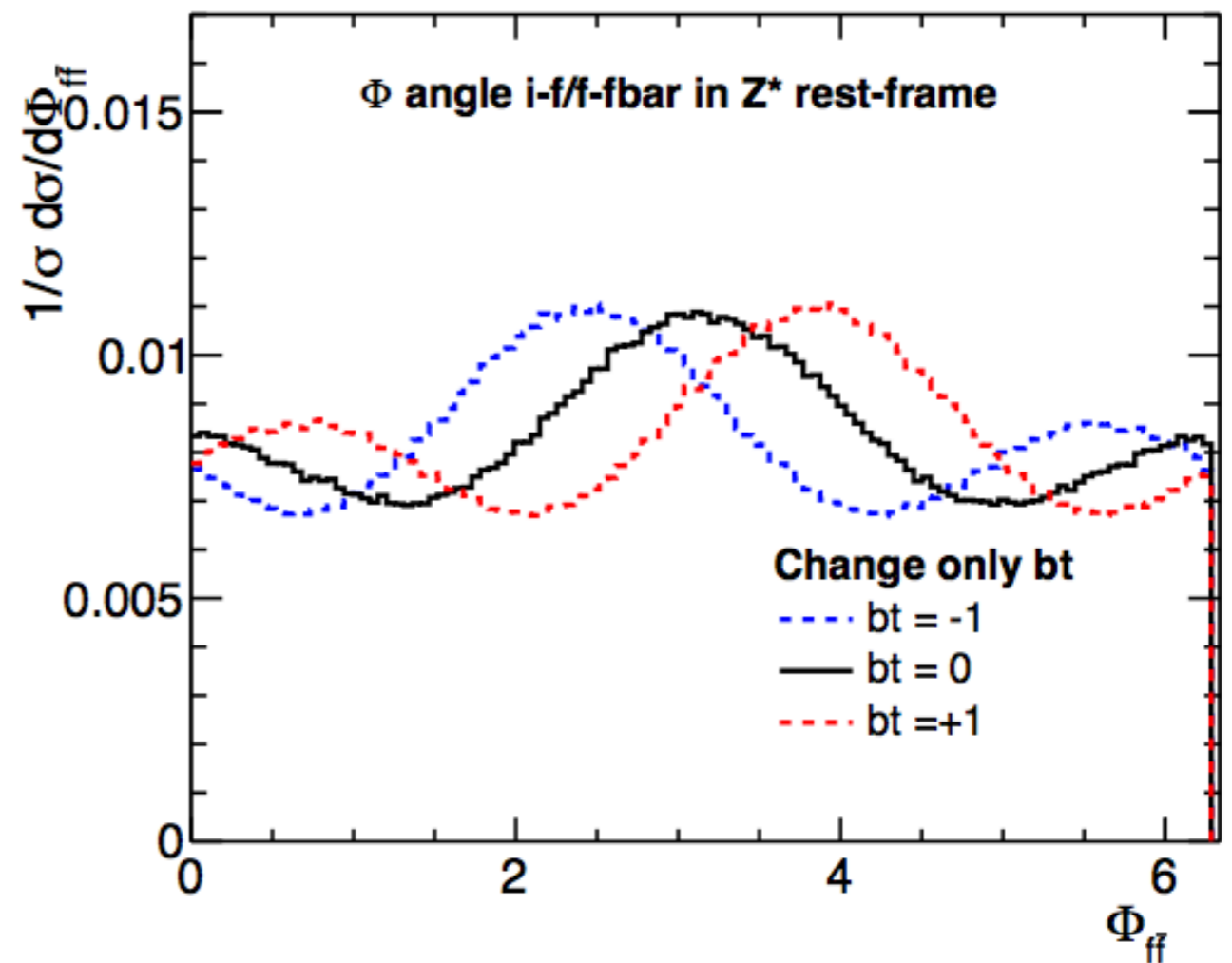
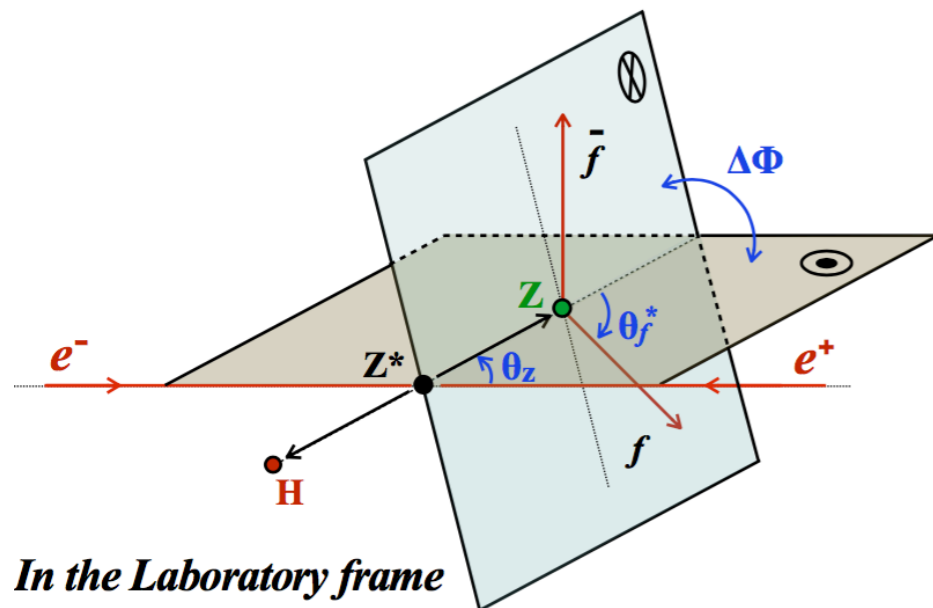
(theoretically ~ 1 degree reachable)

Jeans et al, arXiv:1804.01241

(iii-2) Higgs CP in HZZ coupling

$$L_{hZZ} = M_Z^2 \left(\frac{1}{v} + \frac{a}{\Lambda} \right) h Z_\mu Z^\mu + \underbrace{\frac{b}{2\Lambda} h Z_{\mu\nu} Z^{\mu\nu}}_{\text{(CP-even)}} + \underbrace{\frac{\tilde{b}}{2\Lambda} h Z_{\mu\nu} \tilde{Z}_{\mu\nu}}_{\text{(CP-odd)}}$$

$$e^+ + e^- \rightarrow Zh \rightarrow f \bar{f} h$$



@ $\sqrt{s} = 250\text{GeV}$

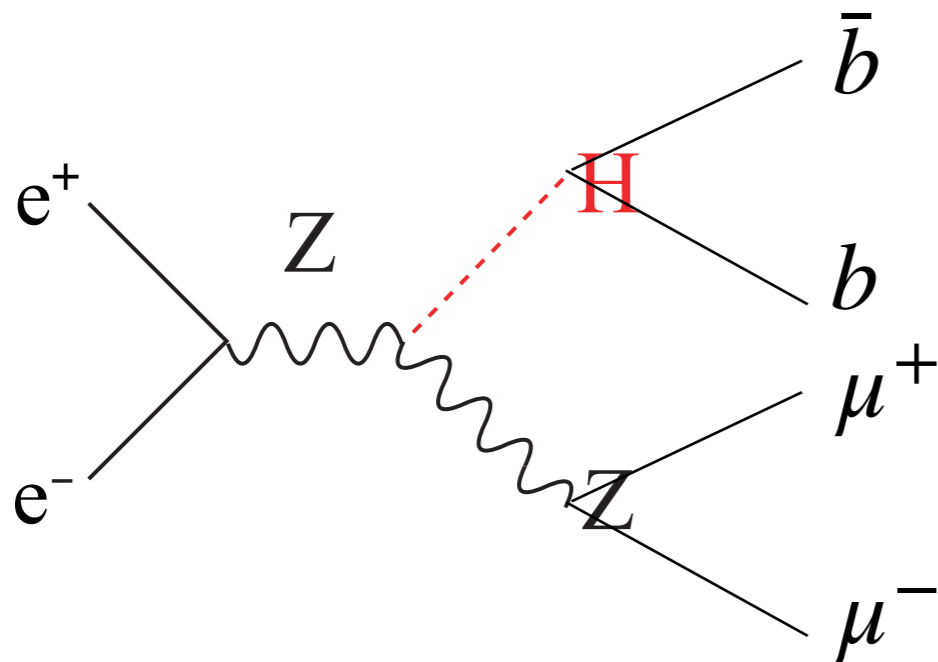
$$\Delta \tilde{b} \sim 0.016 \quad (\text{for } \Lambda = 1\text{TeV})$$

(iv) Global interpretation: why do we need it?

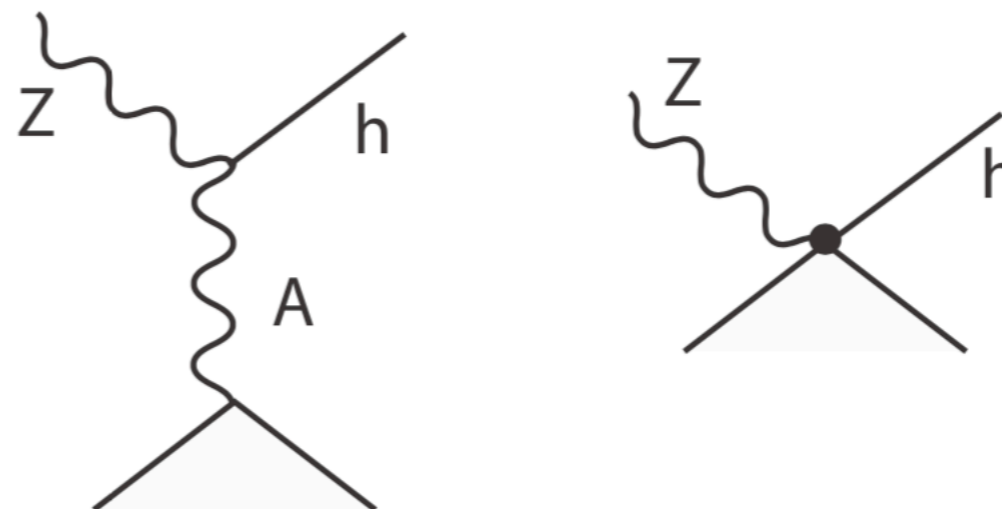
suppose we discover a deviation in, e.g. cross section of

$$e^+e^- \rightarrow ZH \rightarrow (\mu\mu) (bb)$$

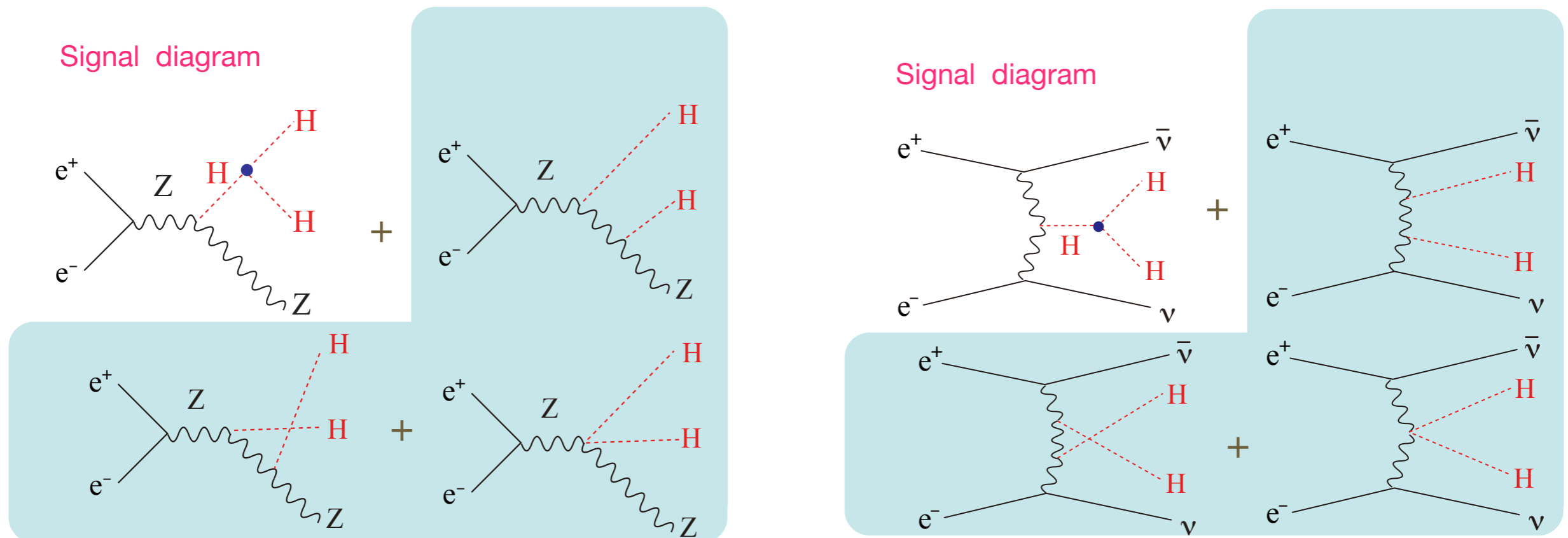
then we would like to know which coupling is deviated:



- hbb coupling?
- hZZ coupling?
- $Z\mu\mu$ coupling?
- Zee coupling?
- new diagrams?

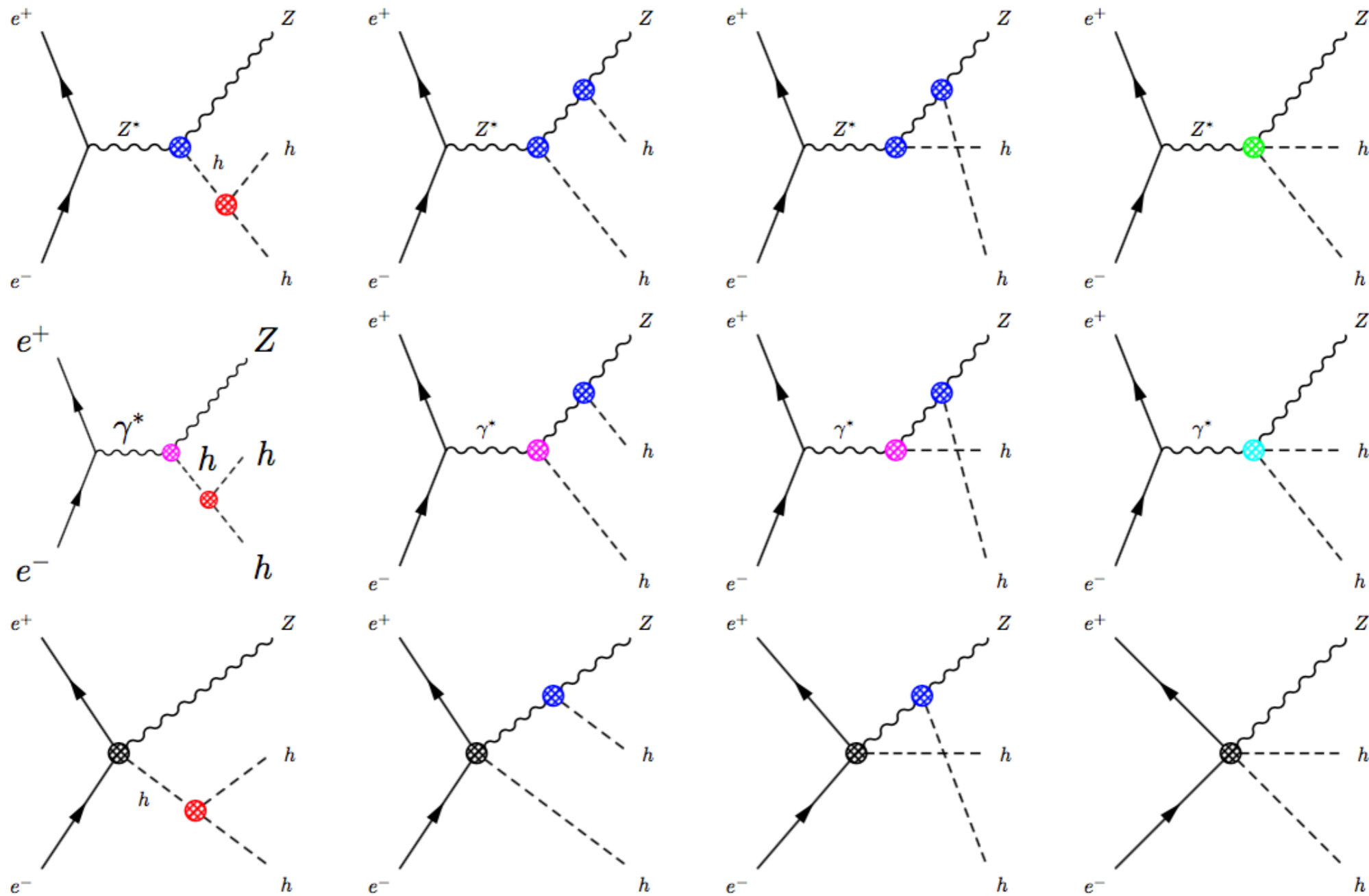


Higgs self-coupling determination in HH processes



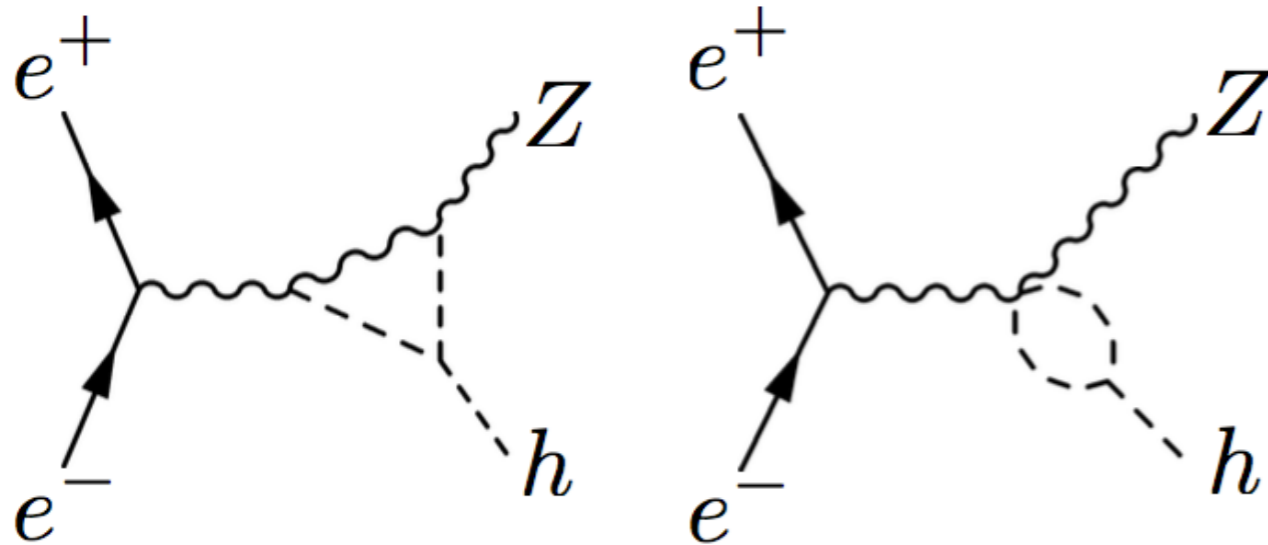
- classic studies always assume all the coupling except λ_{hhh} in these processes are fixed
- might be OK for many of the couplings, but definitely not obvious for $ZZHH$ / $WWHH$ couplings

more general interactions in HH processes



- what we are measuring if only σ_{ZH} is determined?

λ_{hhhh} determination in single-Higgs process



McCullough, arXiv:1312.3322

$$\delta_{\sigma}^{240} = 100 (2\delta_Z + 0.014\delta_h) \%$$

- $\delta\sigma$ could receive contributions from many other sources
 - > **$\delta h \sim 500\%$** at 250GeV only; Gu, et al, arXiv:1711.03978
 - > **$\delta h \sim 50\%$** + 350/500GeV; Jung, Peskin, JT, paper in preparation
- open: what if we include other NLO effects as well?

From observables to couplings — Global Fit

$$\chi^2 = \sum_{i=1}^n \left(\frac{Y_i - Y'_i}{\Delta Y_i} \right)^2$$

Y_i : measured values by experiments

Y'_i : predicted values by underlying theory

ΔY_i : measurement uncertainty

n : number of independent observables

○ kappa formalism

$$Y'_i = F_i \cdot \frac{g_{HA_i A_i}^2 \cdot g_{HB_i B_i}^2}{\Gamma_0} \quad \begin{array}{l} (A_i = Z, W, t) \\ (B_i = b, c, \tau, \mu, g, \gamma, Z, W : \text{decay}) \end{array}$$

$$g_{HXX} = \kappa_X \cdot g_{HXX}^{SM}$$

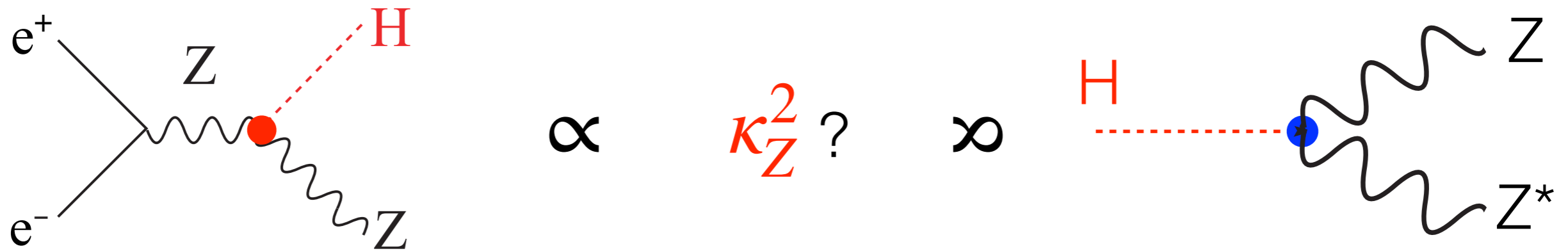
○ SM Effective Field Theory formalism

Higgs coupling determination — kappa formalism

- 1) recoil mass technique \longrightarrow inclusive σ_{Zh}
- 2) $\sigma_{Zh} \longrightarrow \mathbf{K_Z} \longrightarrow \Gamma(h \rightarrow ZZ^*)$
- 3) W-fusion $\nu_e \nu_e h \longrightarrow \mathbf{K_W} \longrightarrow \Gamma(h \rightarrow WW^*)$
- 4) total width $\mathbf{\Gamma_h} = \Gamma(h \rightarrow ZZ^*) / \text{BR}(h \rightarrow ZZ^*)$
- 5) or $\mathbf{\Gamma_h} = \Gamma(h \rightarrow WW^*) / \text{BR}(h \rightarrow WW^*)$
- 6) then all other couplings $\text{BR}(h \rightarrow XX) * \mathbf{\Gamma_h} \longrightarrow \mathbf{K_X}$

one question in kappa formalism:

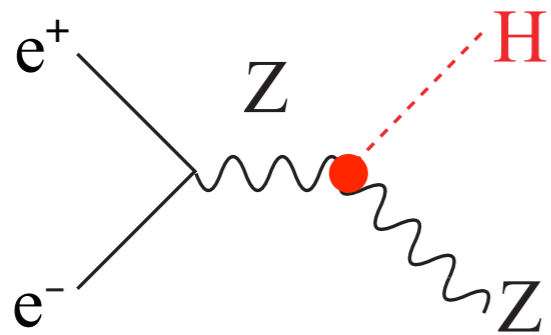
$$\frac{\sigma(e^+e^- \rightarrow Zh)}{SM} = \frac{\Gamma(h \rightarrow ZZ^*)}{SM} = \kappa_Z^2 \quad ?$$



BSM territory: can deviations be represented by single κ_Z ?

the answer is model dependent

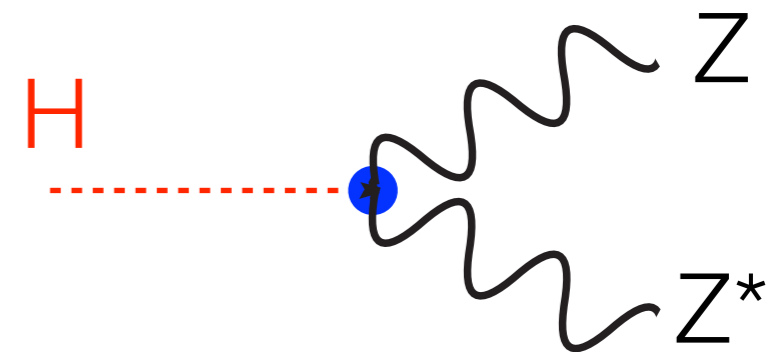
$$\delta\mathcal{L} = (1 + \eta_Z) \frac{m_Z^2}{v} h Z_\mu Z^\mu + \zeta_Z \frac{h}{2v} Z_{\mu\nu} Z^{\mu\nu}$$



$$\sigma(e^+e^- \rightarrow Zh) = (SM) \cdot$$

$$(1 + 2\eta_Z + (5.5)\zeta_Z)$$

\neq



$$\Gamma(h \rightarrow ZZ^*) = (SM) \cdot$$

$$(1 + 2\eta_Z - (0.50)\zeta_Z)$$

- BSM can induce new Lorentz structures in hZZ
- need a better, more theoretical sound framework

new strategy: SM Effective Field Theory

$$\begin{aligned}\mathcal{L}_{\text{eff}} &= \mathcal{L}_{\text{SM}} + \Delta\mathcal{L} \\ &= \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^{d_i-4}} O_i\end{aligned}$$

- most general BSM effects represented by $d_i > 4$ operators
 - ▶ more model-independent formalism
- well-defined quantum field theory respecting SM $SU(3) \times SU(2) \times U(1)$ gauge symmetries
 - ▶ can include radiative corrections consistently
- unifying BSM effects in Higgs, W/Z, top, 2-fermion physics
 - ▶ global view in searching for BSM

global SMEFT fit @ e+e-

(Barklow, Fujii, Jung, Peskin, JT, arXiv:1708.09079)

$$\begin{aligned} \Delta\mathcal{L} = & \frac{c_H}{2v^2} \partial^\mu (\Phi^\dagger \Phi) \partial_\mu (\Phi^\dagger \Phi) + \frac{c_T}{2v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\Phi^\dagger \overleftrightarrow{D}_\mu \Phi) - \frac{c_6 \lambda}{v^2} (\Phi^\dagger \Phi)^3 \\ & + \frac{g^2 c_{WW}}{m_W^2} \Phi^\dagger \Phi W_{\mu\nu}^a W^{a\mu\nu} + \frac{4gg' c_{WB}}{m_W^2} \Phi^\dagger t^a \Phi W_{\mu\nu}^a B^{\mu\nu} \\ & + \frac{g'^2 c_{BB}}{m_W^2} \Phi^\dagger \Phi B_{\mu\nu} B^{\mu\nu} + \frac{g^3 c_{3W}}{m_W^2} \epsilon_{abc} W_{\mu\nu}^a W^{b\nu\rho} W^{c\rho\mu} \\ & + i \frac{c_{HL}}{v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\bar{L} \gamma_\mu L) + 4i \frac{c'_{HL}}{v^2} (\Phi^\dagger t^a \overleftrightarrow{D}^\mu \Phi) (\bar{L} \gamma_\mu t^a L) \\ & + i \frac{c_{HE}}{v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\bar{e} \gamma_\mu e) . \end{aligned}$$

“Warsaw” basis,
Grzadkowski et al,
arXiv:1008.4884

Φ : higgs field
W, B: SU(2), U(1) gauge
L, e: left/right electron

- 10 operators modifying couplings for h/Z/W/ γ
- in total, 23 parameters (see backup slides)

next: highlight a few important implications

(iv-1) Higgs couplings are related to themselves (hWW/hZZ)

$$\Gamma(h \rightarrow ZZ^*) = (SM) \cdot (1 + 2\eta_Z - (0.50)\zeta_Z) ,$$

$$\Gamma(h \rightarrow WW^*) = (SM) \cdot (1 + 2\eta_W - (0.78)\zeta_W)$$

SM-like hVV

$$\eta_W = -\frac{1}{2}c_H$$

$$\eta_Z = -\frac{1}{2}c_H - c_T$$

custodial symmetry is broken by
 $c_T \rightarrow$ constrained by EWPOs

anomalous hVV

$$\zeta_W = (8c_{WW})$$

$$\zeta_Z = c_w^2(8c_{WW}) + 2s_w^2(8c_{WB}) + (s_w^4/c_w^2)(8c_{BB})$$

$c_i \sim O(10^{-4}-10^{-3})$

- hWW/hZZ ratio can be determined to <0.1%
- very important for physics case of any 250 GeV e+e-
- hWW can be determined as precisely as hZZ at 250 GeV; hence precision total width & other couplings

(iv-1) Higgs couplings are related to themselves (synergy w/ LHC)

two measurements from LHC (model independent)

$$R_{\gamma\gamma} = \frac{BR(h \rightarrow \gamma\gamma)}{BR(h \rightarrow ZZ^*)} \quad R_{\gamma Z} = \frac{BR(h \rightarrow \gamma Z)}{BR(h \rightarrow ZZ^*)}$$

$$\delta\Gamma(h \rightarrow \gamma\gamma) = \mathbf{528} \delta Z_A - c_H + \dots$$

$$\delta\Gamma(h \rightarrow Z\gamma) = \mathbf{290} \delta Z_{AZ} - c_H + \dots$$

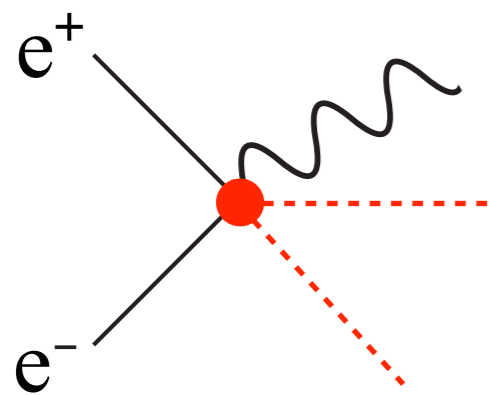
$$\delta\Gamma(h \rightarrow ZZ^*) = -0.50\delta Z_Z - c_H + \dots$$

- loop induced $h \rightarrow \gamma\gamma/\gamma Z$ depend strongly on $c_{WW}/c_{WB}/c_{BB}$
- $h \rightarrow \gamma\gamma/\gamma Z$ at LHC can help higgs couplings at $e+e-$

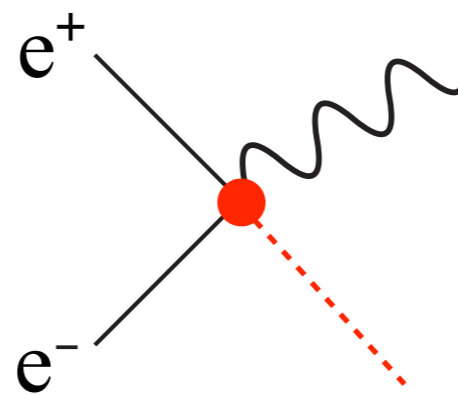
(iii-2) Higgs couplings are related to W-/Z- couplings (EWPOs)

$$i \frac{c_{HL}}{v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\bar{L} \gamma_\mu L)$$

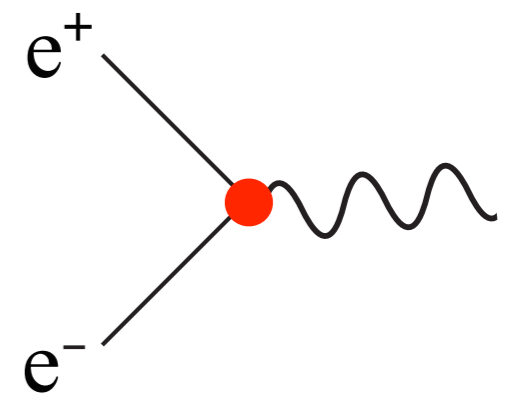
+ (c'_{HL}, c_{HE})



$e^+e^- \rightarrow Zhh$



$e^+e^- \rightarrow Zh$

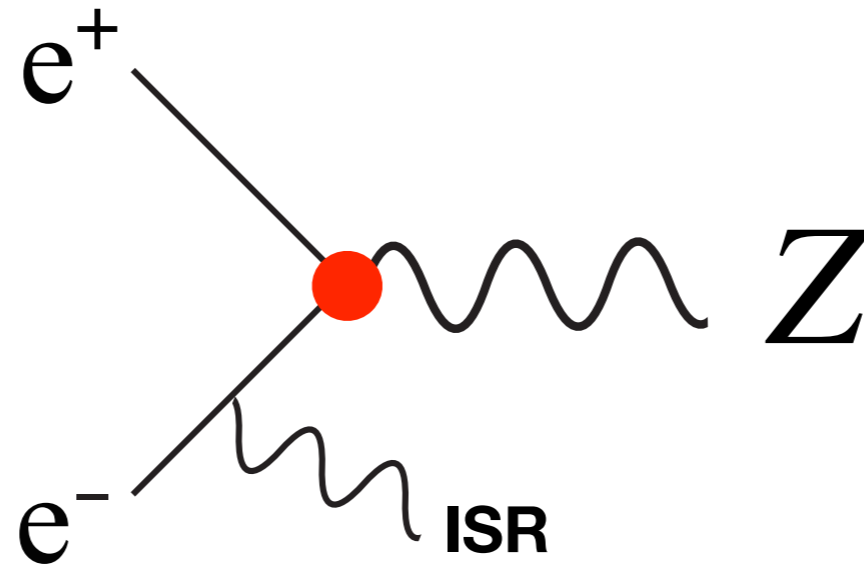


Z-pole

- Higgs coupling encoded in EWPOs at Z-pole: $\mathbf{A}_{LR}, \mathbf{\Gamma}_I$
- Z coupling helped by Higgs meas. at high \sqrt{s} : $\delta\sigma \sim \mathbf{s}/\mathbf{m}^2_Z$

new ideas: improving EWPOs @ ILC250

radiative return



[Mizuno, PhD thesis]

- a free gift by ISR: Higgs factory is meantime a Z factory
- $\sim 10^8$ Z events by ILC250, without any change of accelerator
- more over, **polarized beams**

$$\text{ILC250} = \text{ILC250} + 100\times\text{LEP/SLC}$$

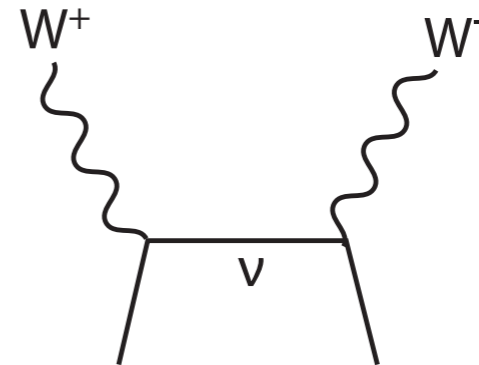
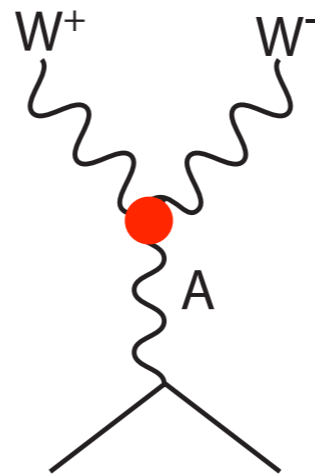
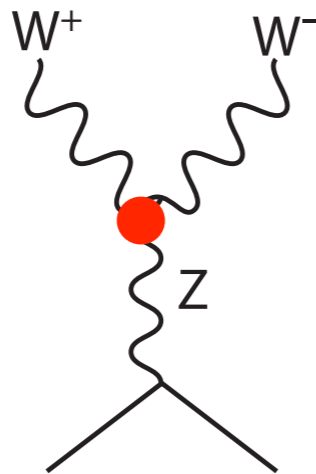
see more in
arXiv:1908.11299

- expect a factor of 10 improvement on A_{LR}

(iv-2) Higgs couplings are related to W-/Z- couplings (TGCs)

$$\boxed{\frac{4gg'c_{WB}}{m_W^2} \Phi^\dagger t^a \Phi W_{\mu\nu}^a B^{\mu\nu}} + (c_{WW}, c_{BB})$$

$e^+e^- \rightarrow WW$



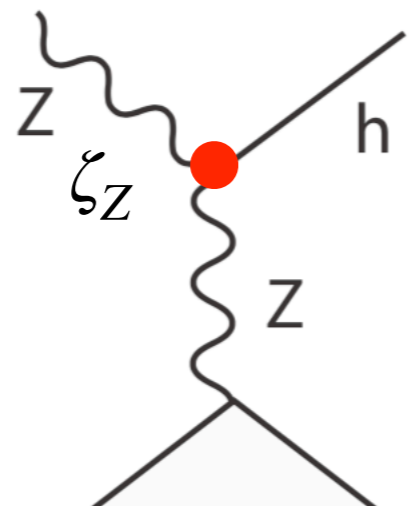
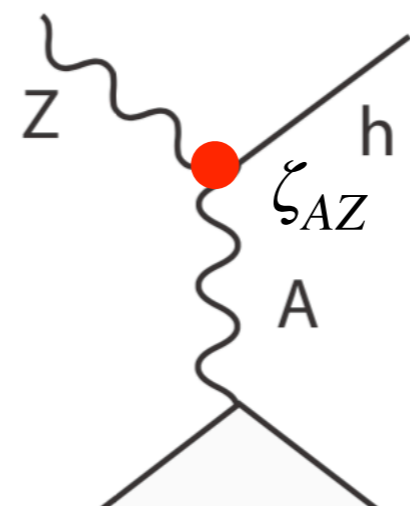
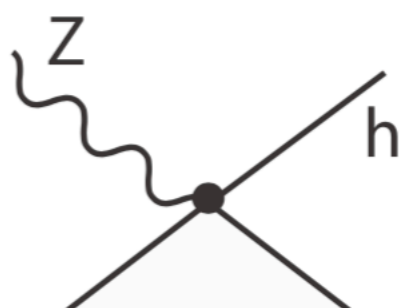
$h \rightarrow ZZ$

$$\zeta_Z \frac{h}{2v} Z_{\mu\nu} Z^{\mu\nu}$$

$$\zeta_Z = c_w^2(8c_{WW}) + 2s_w^2(8c_{WB}) + s_w^4/c_w^2(8c_{BB})$$

- longitudinal modes of W/Z are from Higgs fields
- higgs coupling helped by meas. of TGCs in $e^+e^- \rightarrow WW$

(iv-3) role of beam polarizations ($e^+e^- \rightarrow Zh$)

			
$P(e^-, e^+)$			
$(-1, +1)$	$\frac{g}{\cos \theta_w} \left(\frac{1}{2} - \sin^2 \theta_w \right)$	$g \sin \theta_w$	$\frac{g}{\cos \theta_w} (c_{HL} + c'_{HL})$
$(+1, -1)$	$\frac{g}{\cos \theta_w} (-\sin^2 \theta_w)$	$g \sin \theta_w$	$\frac{g}{\cos \theta_w} (c_{HE})$

- sensitive to different couplings \rightarrow lift degeneracy
- A_{LR} in σ_{ZH} \rightarrow improve c_{WW} , $c_{HL} + c'_{HL}$ and c_{HE}
- large cancellation in **(+1,-1)** \rightarrow weaker dependence on c_{WW}

(iv-3) role of beam polarizations ($e^+e^- \rightarrow Zh$)

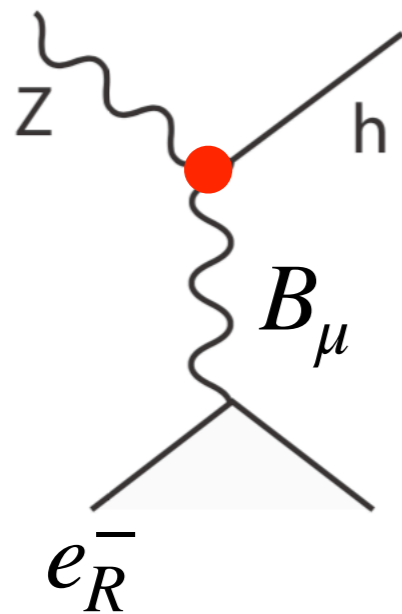
$\sqrt{s}=250$ GeV

$$\delta\sigma_L = -c_H + 7.7(8c_{WW}) + \dots$$

$$\delta\sigma_R = -c_H + 0.6(8c_{WW}) + \dots \quad \text{why?}$$

$$\delta\sigma_0 = -c_H + 4.6(8c_{WW}) + \dots$$

$(8c_{WW}) \sim 0.16\%$ from other meas.



contribution from
almost cancels out

$$\frac{g^2 c_{WW}}{m_W^2} \Phi^\dagger \Phi W_{\mu\nu}^a W^{a\mu\nu}$$

up to a difference in Z/ γ propagator suppressed by $\frac{m_Z^2}{s}$

(iv-3) role of beam polarizations (overall effects)

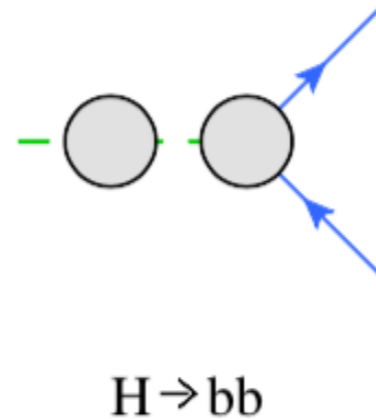
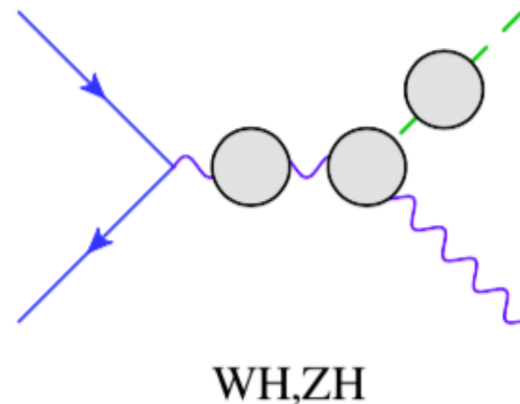
ILC250: 2 ab⁻¹

FCCee240: 5 ab⁻¹

coupling	2/ab-250	+4/ab-500	5/ab-250	+ 1.5/ab-350
	pol.	pol.	unpol.	unpol
<i>HZZ</i>	0.50	0.35	0.41	0.34
<i>HWW</i>	0.50	0.35	0.42	0.35
<i>Hbb</i>	0.99	0.59	0.72	0.62
<i>Hττ</i>	1.1	0.75	0.81	0.71
<i>Hgg</i>	1.6	0.96	1.1	0.96
<i>Hcc</i>	1.8	1.2	1.2	1.1
<i>Hγγ</i>	1.1	1.0	1.0	1.0
<i>HγZ</i>	9.1	6.6	9.5	8.1
<i>Hμμ</i>	4.0	3.8	3.8	3.7
<i>Htt</i>	-	6.3	-	-
<i>HHH</i>	-	27	-	-
Γ_{tot}	2.3	1.6	1.6	1.4
Γ_{inv}	0.36	0.32	0.34	0.30
Γ_{other}	1.6	1.2	1.1	0.94

- 250 GeV e⁺e⁻: power of 2 ab⁻¹ polarized \approx 5 ab⁻¹ unpolarized

(iv-4) what happens at next leading order for SMEFT



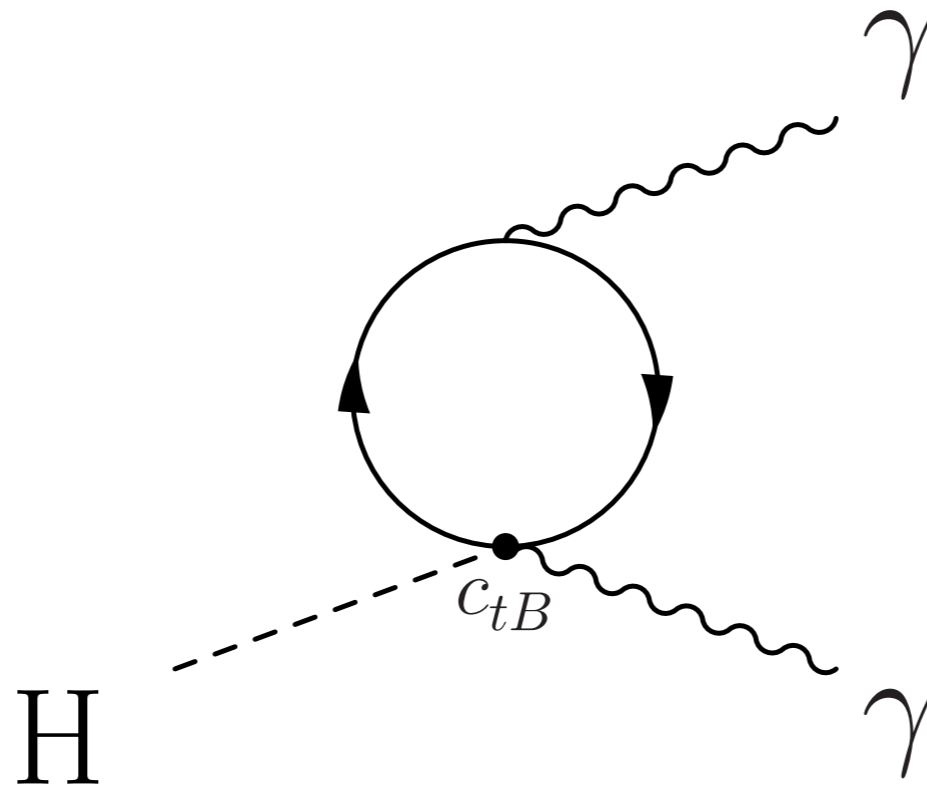
Zhang, et al,
arXiv:1804.09766,
1807.02121

- at e^+e^- , NLO $\sim O(\alpha)$, 1% level
- for NLO from $W/Z/\gamma/H$, operators constrained to $\sim <0.01$, overall effect will be $< 0.1\%$
- for NLO from top, operators would be much less constrained, currently $\sim O(1)$ \rightarrow overall effect 1% \rightarrow potential impact in global fit on Higgs coupling precision

some detailed understandings

$$\delta\Gamma(h \rightarrow \gamma\gamma) : + = -0.56c_{tH} + 1.2c_{HQ}^{(3)} - 0.04c_{Htb} + 33c_{tW} + \underline{61c_{tB}}$$

HL-LHC ~600%

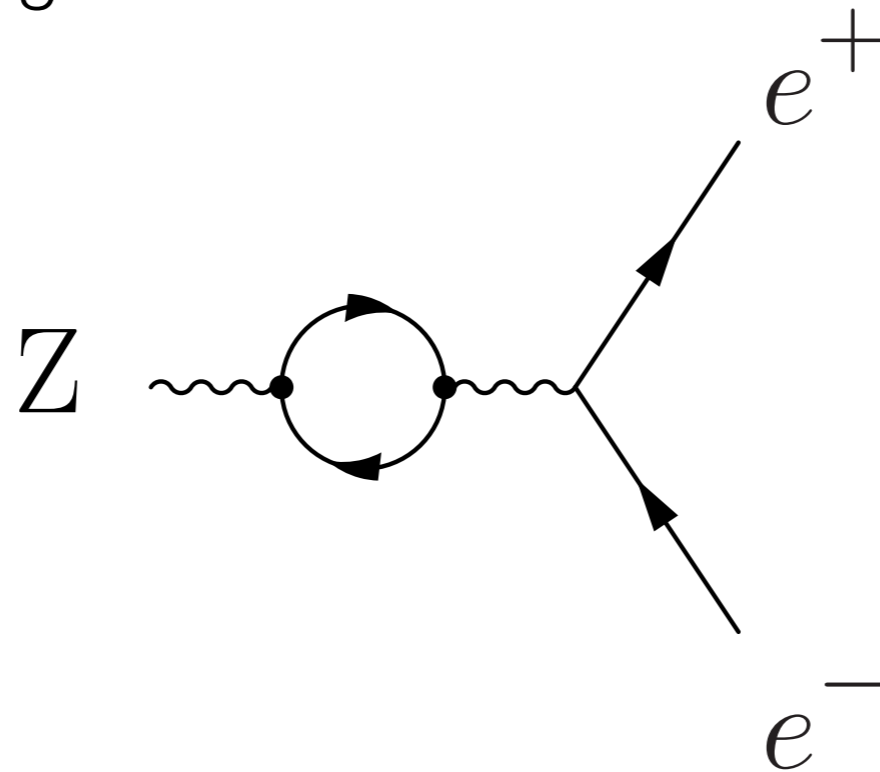


some detailed understandings

$$\delta A_l : + = 0.05c_{HQ}^{(1)} - 0.2c_{HQ}^{(3)} + 0.1c_{Ht} + 1.8c_{tW} - \underline{0.3c_{tB}}$$

A_{LR} : left-right asymmetry
in Z-e-e coupling

$\sim 1\%$



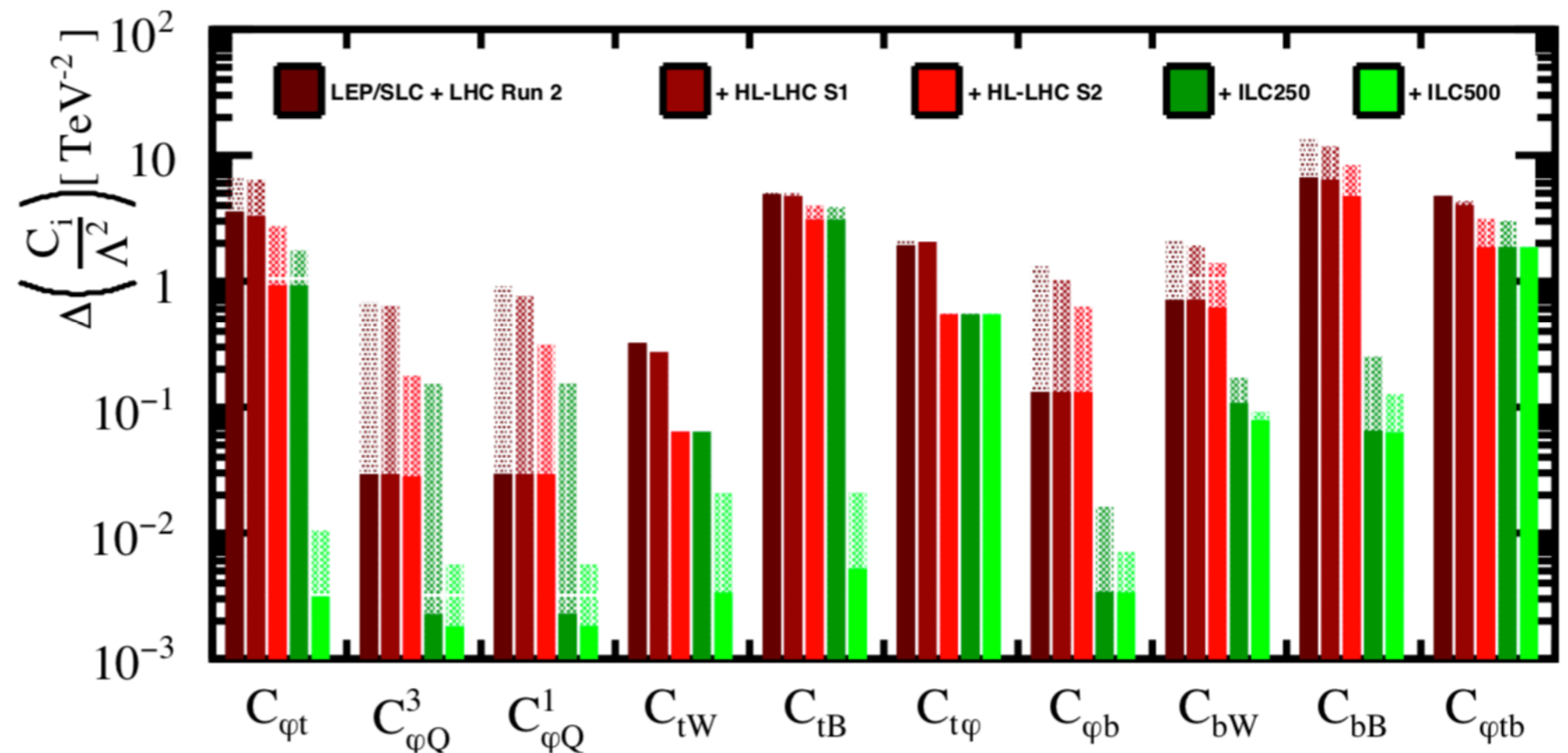
impact from top-EW operators: $\sqrt{s} = 250 \text{ GeV } e^+e^-$

- with the same set of observables (as previous global fit), at 250 GeV running only, the global fit will not converge at any of the Higgs factories
- e.g. Higgs couplings could not be determined unambiguously

impact from top-EW operators: ILC250 + LHC

- LHC will provide us valuable top data sets
- top operators will be constrained to some extent at (HL-)LHC

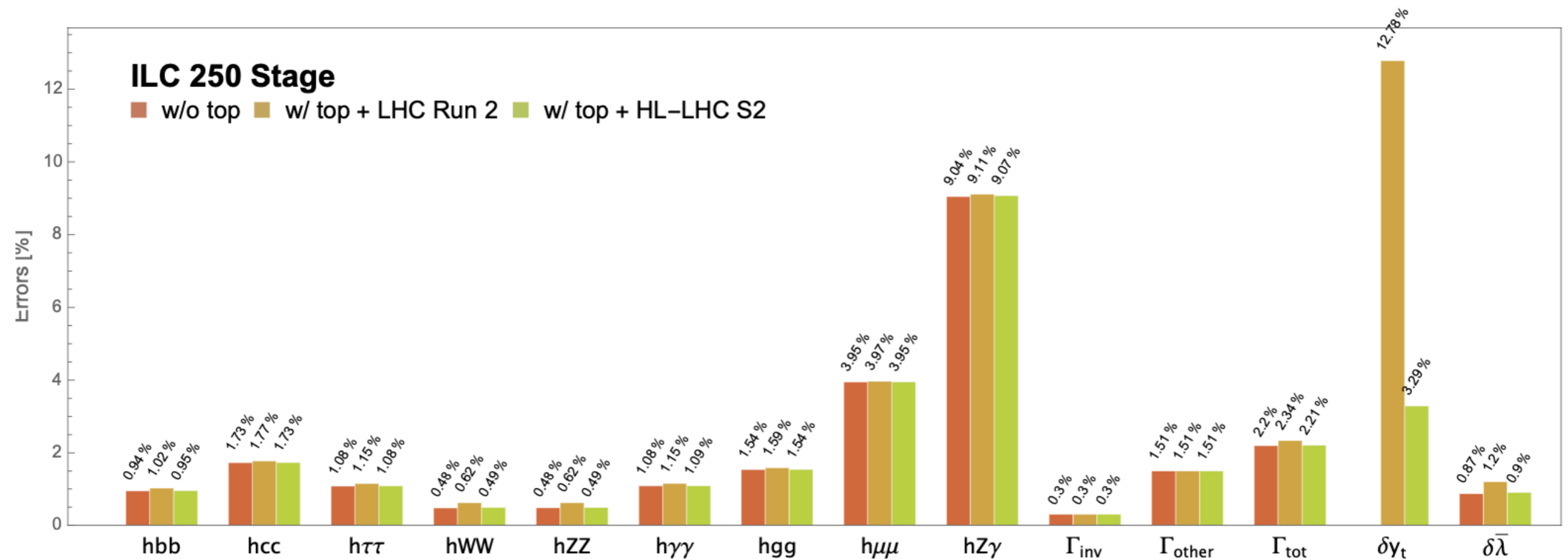
Process	observable
$pp \rightarrow t\bar{t}H$	cross section
$pp \rightarrow t\bar{t}Z/W$	cross section
$pp \rightarrow t\bar{t}\gamma$	fid. x-sec.
single-top (t-ch)	cross section
single-top (Wt)	cross section
single-top (tZq)	cross section
$t \rightarrow W^+b$	F_0, F_L
$e^-e^+ \rightarrow b\bar{b}$	R_b, A_{FBLR}^{bb}



[Durieux, et al, arXiv:1907.10619]

impact from top-EW operators: ILC250 + LHC

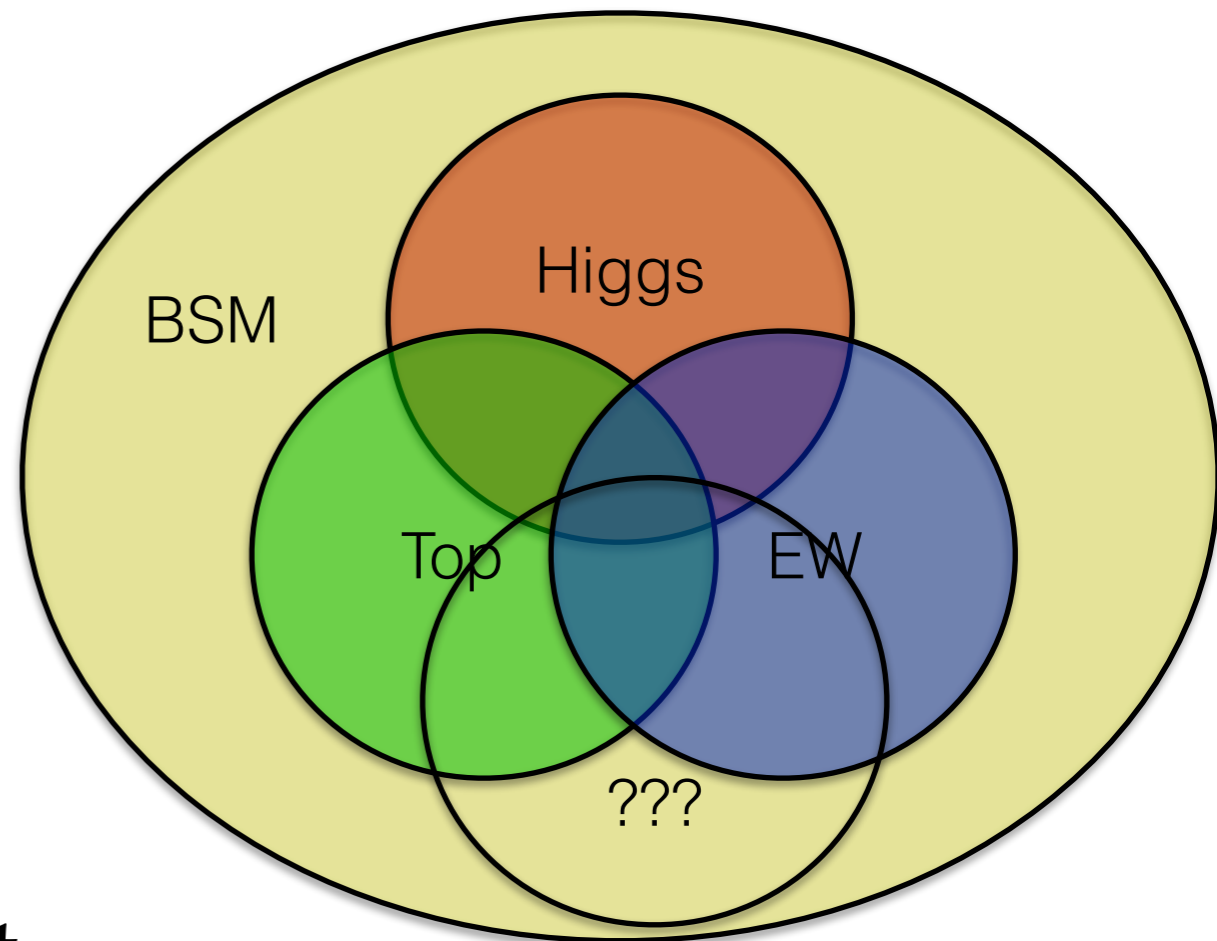
- with the help of LHC top data, Higgs coupling precisions @ ILC250 are almost restored
- note: top data from LHC Run 2 is not constraining enough



S.Jung, J.Lee, M.Perello, JT, M.Vos, [arXiv:2006.14631](https://arxiv.org/abs/2006.14631)

summary

- Higgs provides a unique window into BSM physics
- Many couplings can be measured to 1% or below using single-Higgs
- Differential cross section can be also measured precisely, important for CP, to be explored for self-coupling
- Room for new ideas & improvement
- Higgs is not alone in probing BSM, tightly connected with other EW and top-quark measurement & direct searches: global interpretation important

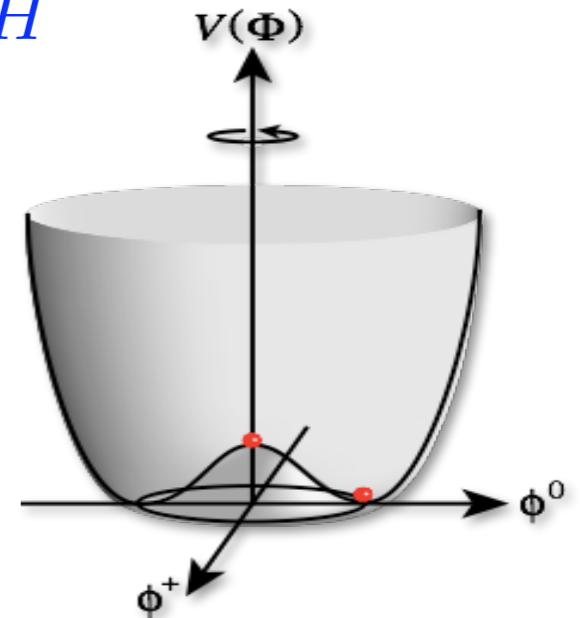


backup

(ii-3) Higgs self-coupling

$$V(\eta_H) = \frac{1}{2}m_H^2\eta_H^2 + \lambda v\eta_H^3 + \frac{1}{4}\lambda\eta_H^4$$

- direct probe of the Higgs potential
- large deviation (> 20%) motivated by electroweak baryogenesis, could be ~100%
- $\sqrt{s} \geq 500$ GeV, $e^+e^- \rightarrow ZHH$
- $\sqrt{s} \geq 1$ TeV, $e^+e^- \rightarrow \nu\nu HH$ (WW-fusion)

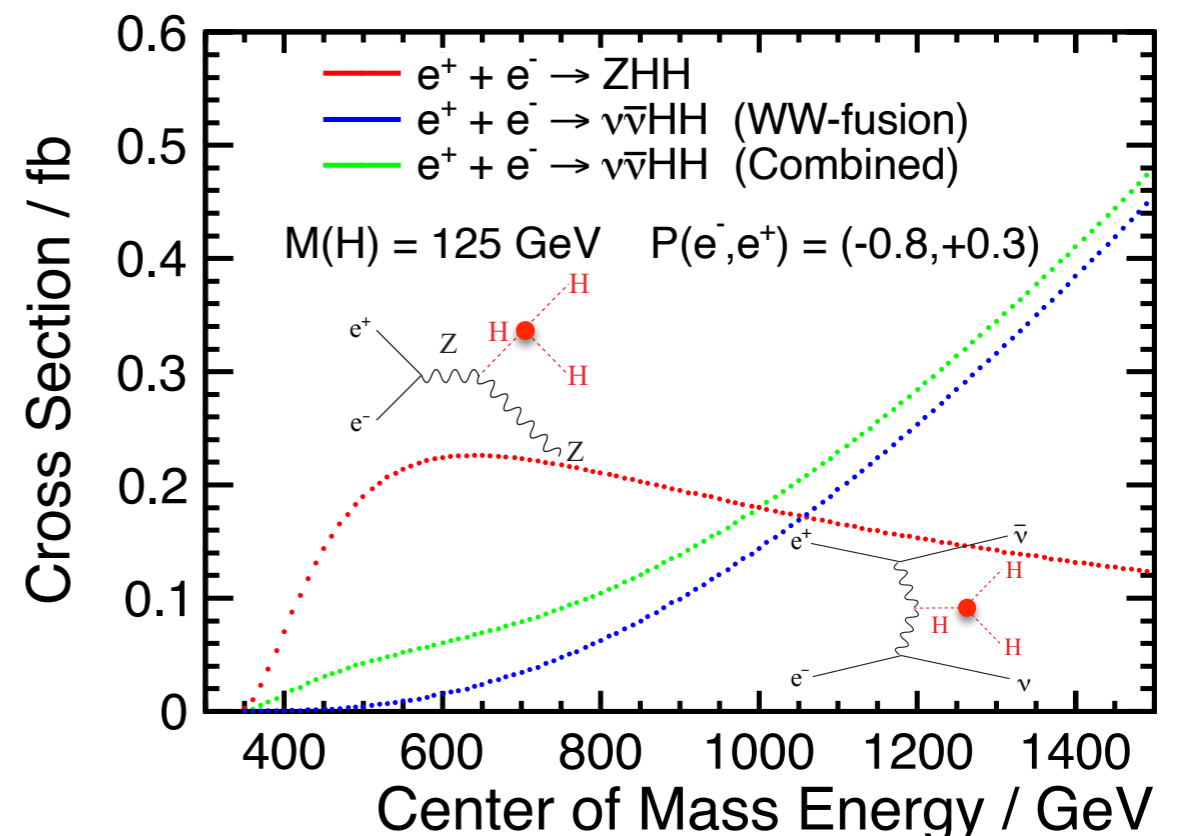


ILC

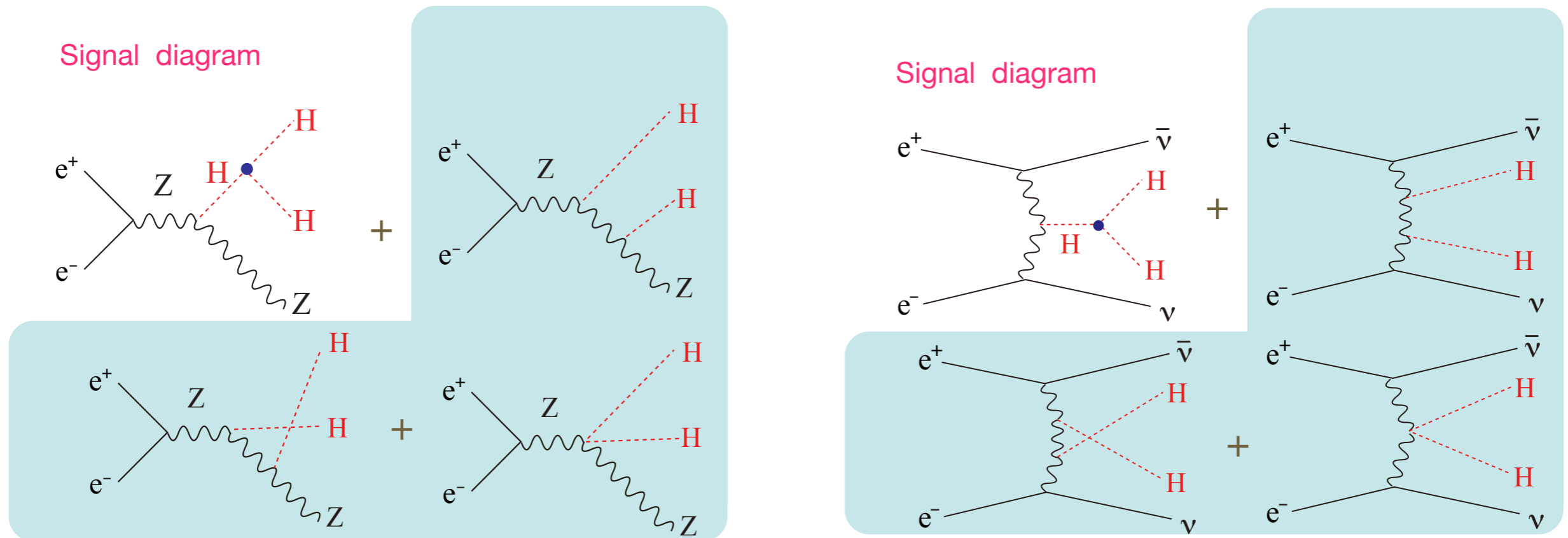
$\Delta\lambda_{HHH}/\lambda_{HHH}$	500 GeV	+ 1 TeV
H20	27%	10%

CLIC

1.5 TeV	+3 TeV
36%	10%



physics issues: diagrams for double Higgs production



$$\sigma = S\lambda^2 + I\lambda + B$$

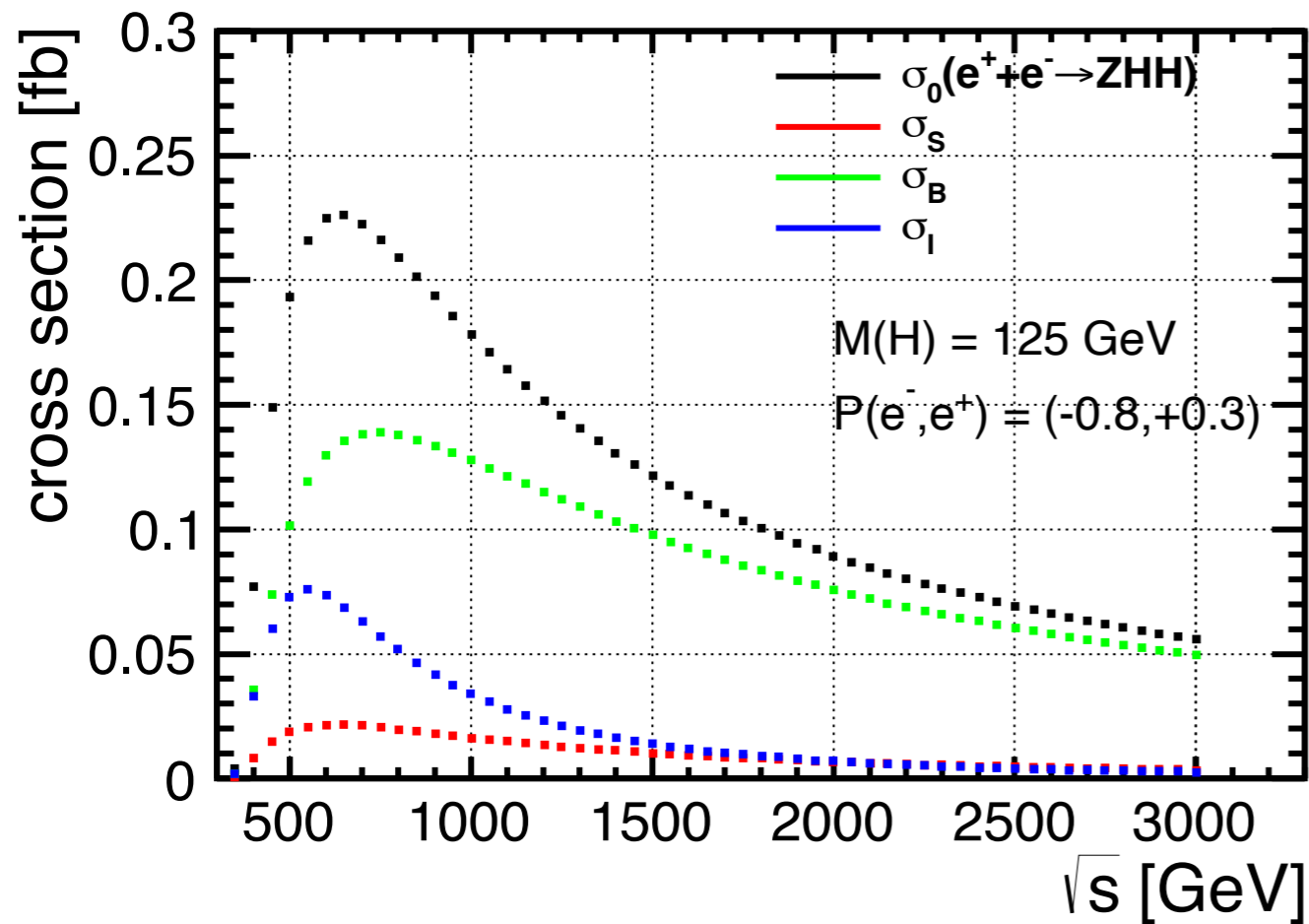
(signal diagram) (interference) (background diagram)

- the sensitivity of λ is determined not just by the apparent total cross section, in fact is determined by S and I term;
- if B term dominates, measurement would be very difficult

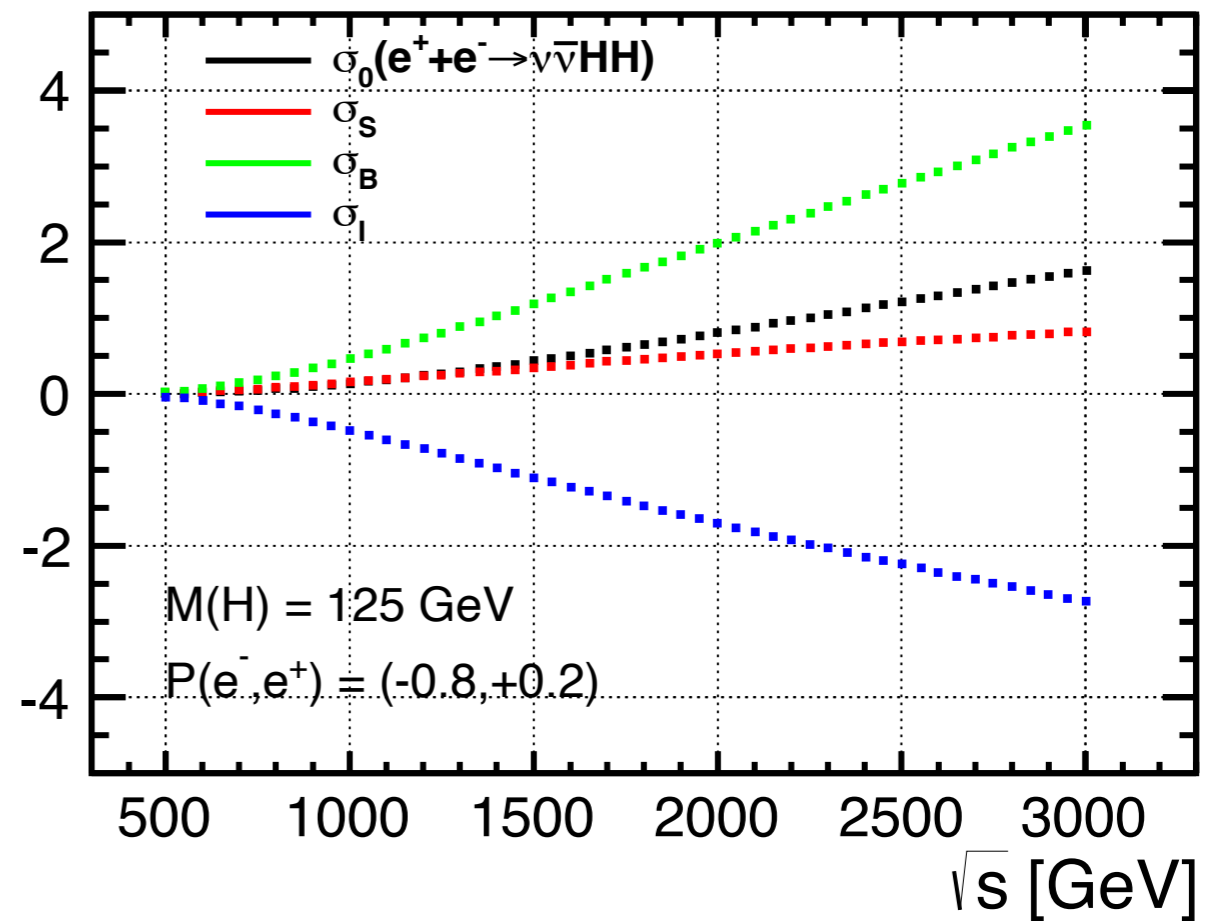
double Higgs x-section: breakdown for each diagram

$$\sigma = S\lambda^2 + I\lambda + B$$

ZHH



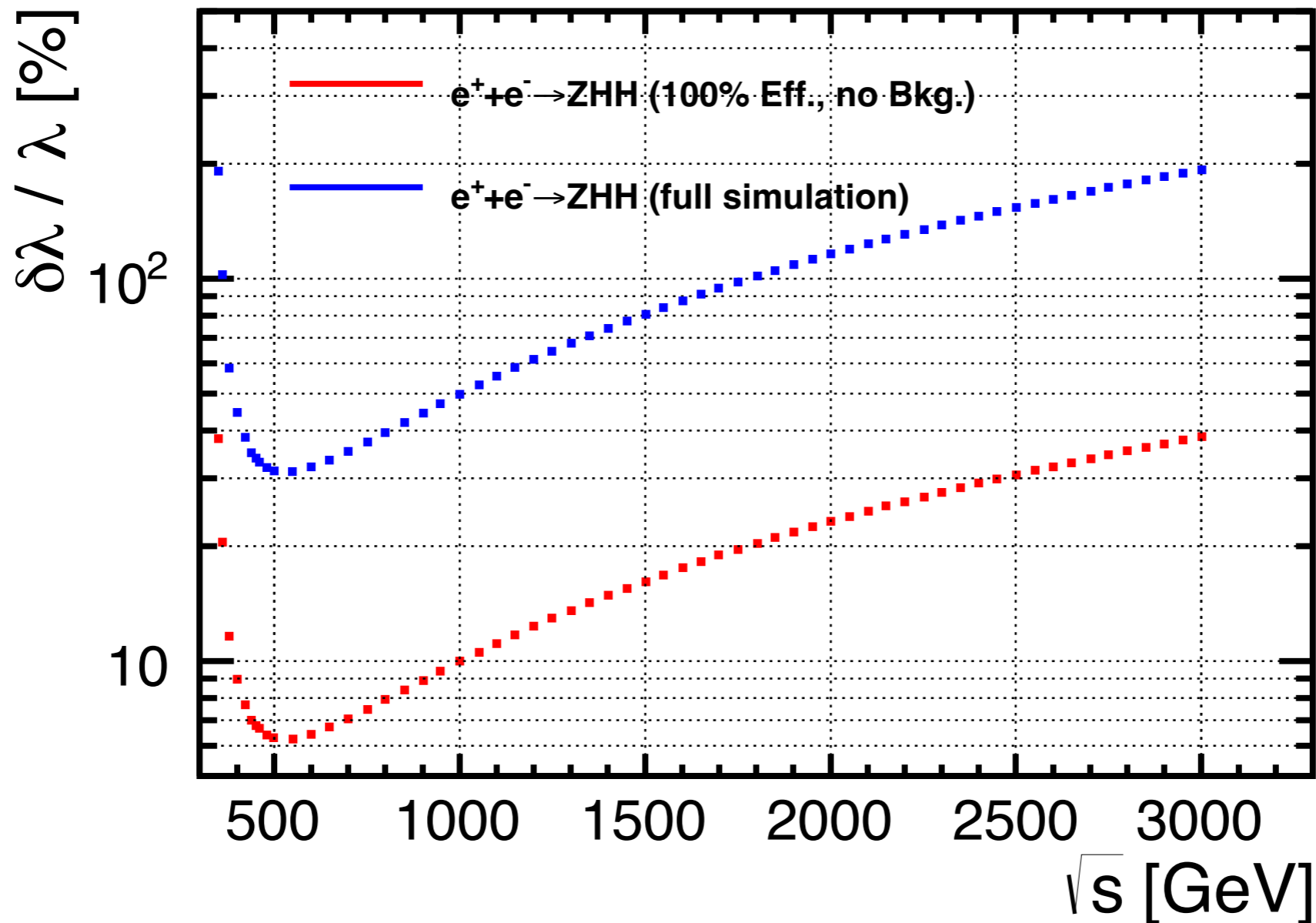
$\nu\nu HH$



- o very useful to understand the impact of ECM (more in backup)

expected precision of λ : impact from analysis & \sqrt{s}

ZHH

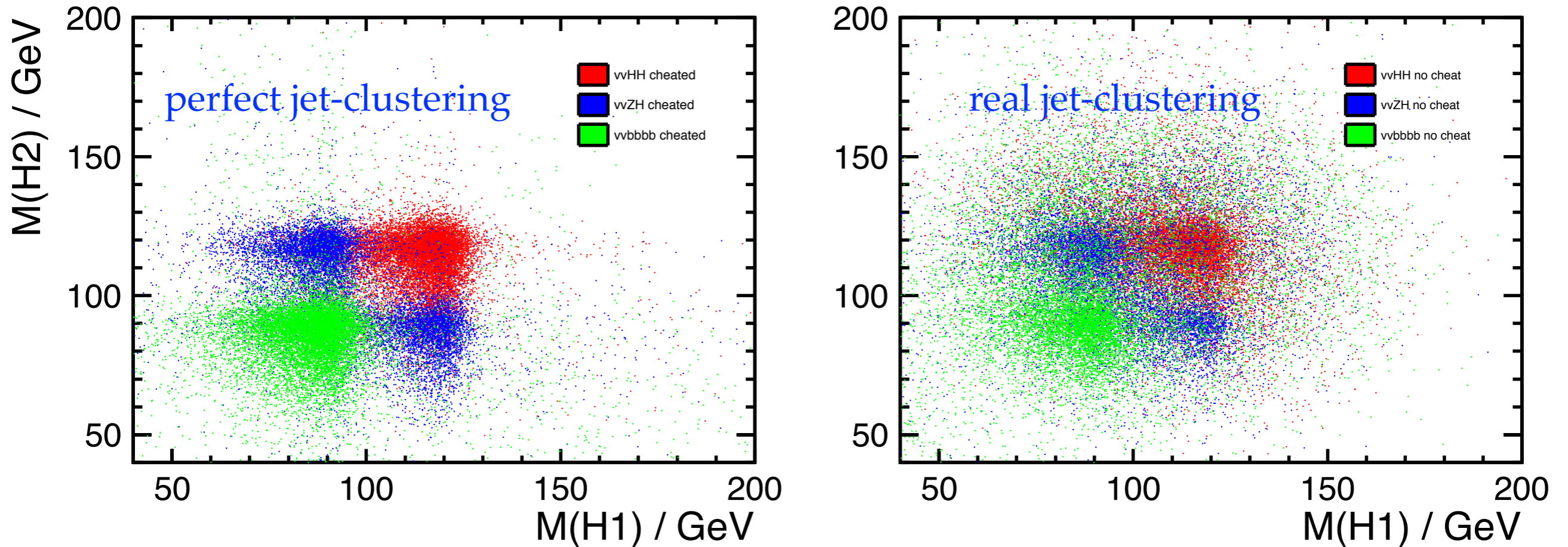


- huge gap of these two expectations \rightarrow room of improvement
- for ZHH: optimal at 500-600 GeV; significantly worse at higher \sqrt{s}

one limiting factor: jet-clustering algorithm

ZHH->vvbbbb (BG: ZZH and ZZZ)

scatter plot of two Higgs masses



- ♦ the mis-clustering of particles degrades significantly the separation between signal and BG.
- ♦ it is studied that using perfect color-singlet-jet-clustering can improve $\delta\lambda/\lambda$ by 40%!

SM Effective Field Theory: some simplifications

$$\begin{aligned}\mathcal{L}_{\text{eff}} &= \mathcal{L}_{\text{SM}} + \Delta\mathcal{L} \\ &= \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^{d_i-4}} O_i\end{aligned}$$

the new particle searches at LHC Run 2 suggest $\Lambda > 500$ GeV

simplify the analysis up to dimension-**6** operators

there are **84** of such operators for 1 fermion generation

assuming B / L conservation & CP even, there are **59**

- there exists a smaller but complete set relevant to Higgs coupling determination at e^+e^-

SM Effective Field Theory: full formalism (23 pars.)

(“Warsaw” basis by Grzadkowski et al)

$$\begin{aligned}
 \Delta\mathcal{L} = & \frac{c_H}{2v^2} \partial^\mu (\Phi^\dagger \Phi) \partial_\mu (\Phi^\dagger \Phi) + \frac{c_T}{2v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\Phi^\dagger \overleftrightarrow{D}_\mu \Phi) - \frac{c_6 \lambda}{v^2} (\Phi^\dagger \Phi)^3 \\
 & + \frac{g^2 c_{WW}}{m_W^2} \Phi^\dagger \Phi W_{\mu\nu}^a W^{a\mu\nu} + \frac{4gg' c_{WB}}{m_W^2} \Phi^\dagger t^a \Phi W_{\mu\nu}^a B^{\mu\nu} \\
 & + \frac{g'^2 c_{BB}}{m_W^2} \Phi^\dagger \Phi B_{\mu\nu} B^{\mu\nu} + \frac{g^3 c_{3W}}{m_W^2} \epsilon_{abc} W_{\mu\nu}^a W^{b\nu\rho} W^{c\rho\mu} \\
 & + i \frac{c_{HL}}{v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\bar{L} \gamma_\mu L) + 4i \frac{c'_{HL}}{v^2} (\Phi^\dagger t^a \overleftrightarrow{D}^\mu \Phi) (\bar{L} \gamma_\mu t^a L) \\
 & + i \frac{c_{HE}}{v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\bar{e} \gamma_\mu e) .
 \end{aligned}$$

10 operators (h,W,Z, γ): $c_H, c_T, c_6, c_{WW}, c_{WB}, c_{BB}, c_{3W}, c_{HL}, c'_{HL}, c_{HE}$

+ **4** SM parameters: g, g', v, λ

+ **5** operators modifying h couplings to b, c, τ, μ, g

+ **2** operators for contact interactions with quarks

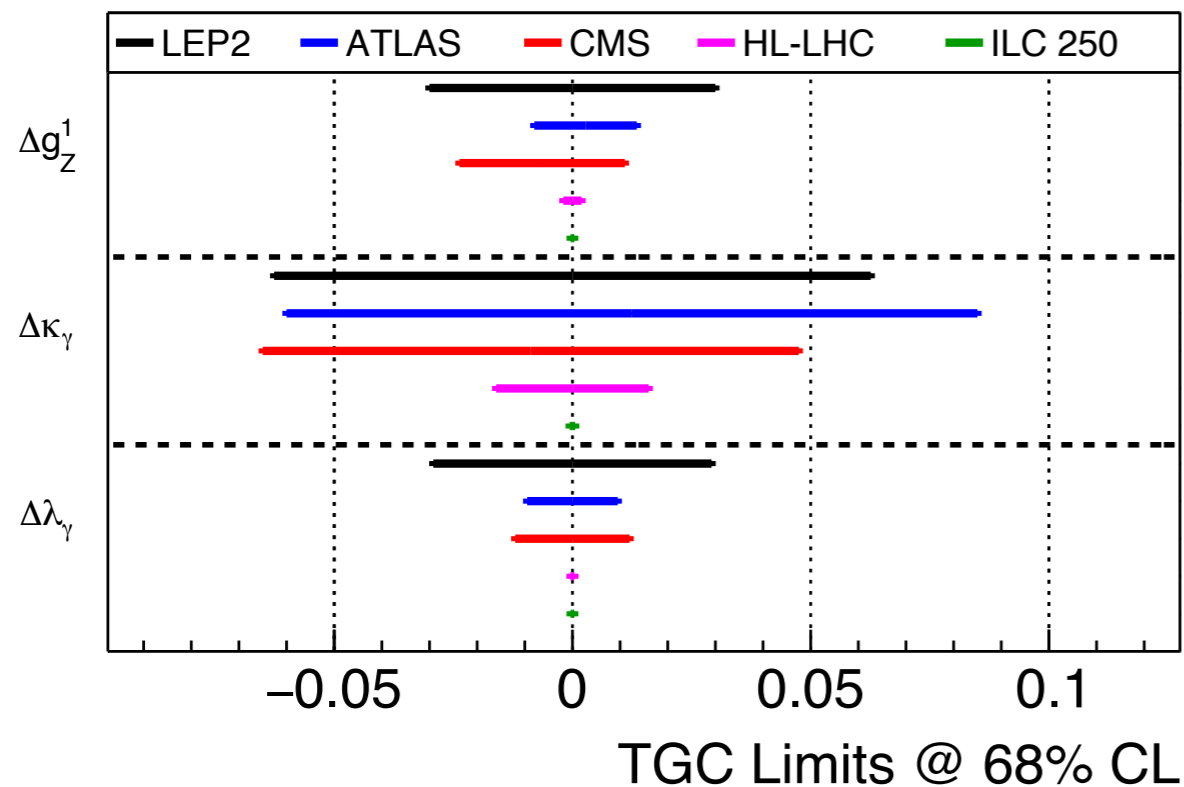
+ **2** parameters for h->invisible and exotic

expected improvement on TGCs at ILC250

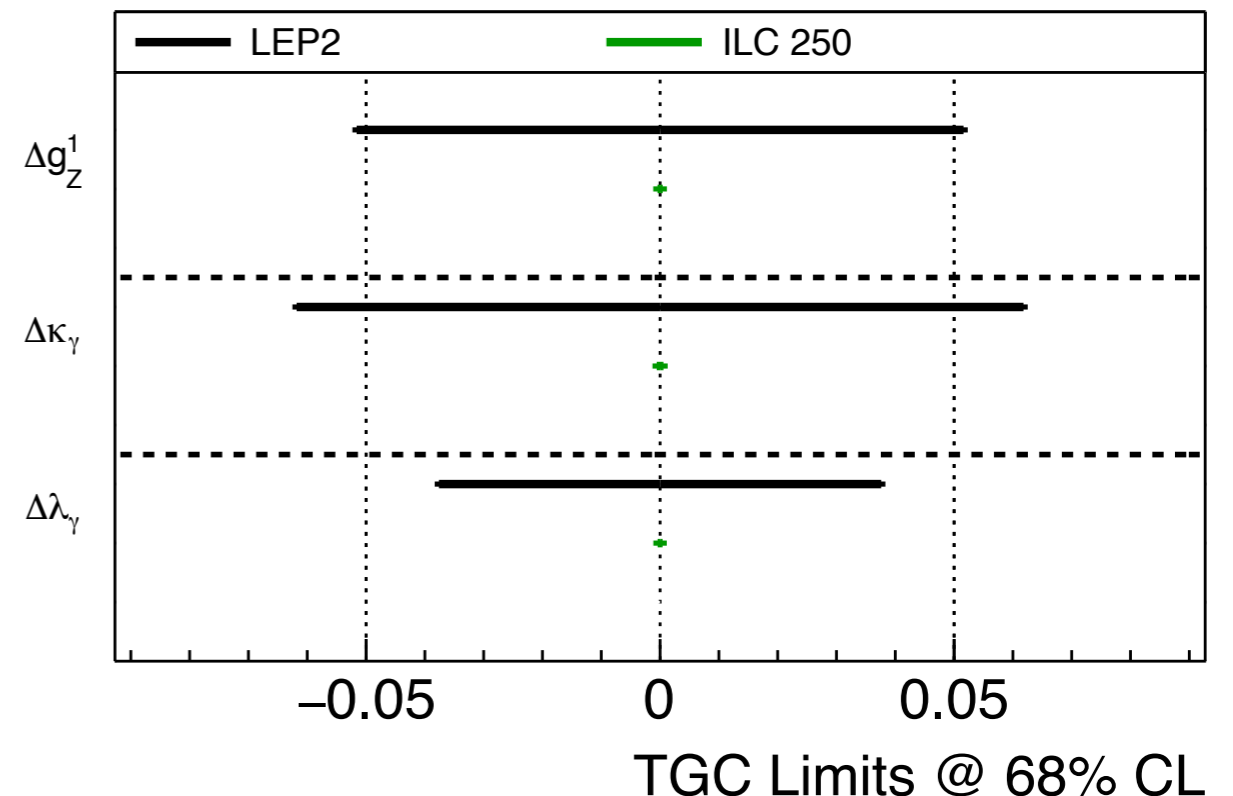
arXiv:1908.11299

$$\Delta\mathcal{L}_{TGC} = ig_V \left\{ V^\mu (\hat{W}_{\mu\nu}^- W^{+\nu} - \hat{W}_{\mu\nu}^+ W^{-\nu}) + \kappa_V W_\mu^+ W_\nu^- \hat{V}^{\mu\nu} + \frac{\lambda_V}{m_W^2} \hat{W}_\mu^{-\rho} \hat{W}_{\rho\nu}^+ \hat{V}^{\mu\nu} \right\}$$

1-par sensitivity



3-par sensitivity



○ statistically x2000 more WW events w.r.t. LEP2

(iii-3) Higgs couplings are related to themselves

$$\begin{aligned}
 \Delta\mathcal{L}_h = & \frac{1}{2}\partial_\mu h\partial^\mu h - \frac{1}{2}m_h^2 h^2 - (1 + \eta_h)\bar{\lambda}vh^3 + \frac{\theta_h}{v}h\partial_\mu h\partial^\mu h \\
 & + (1 + \eta_W)\frac{2m_W^2}{v}W_\mu^+W^{-\mu}h + (1 + \eta_{WW})\frac{m_W^2}{v^2}W_\mu^+W^{-\mu}h^2 \\
 & + (1 + \eta_Z)\frac{m_Z^2}{v}Z_\mu Z^\mu h + \frac{1}{2}(1 + \eta_{ZZ})\frac{m_Z^2}{v^2}Z_\mu Z^\mu h^2 \\
 & + \zeta_W\hat{W}_{\mu\nu}^+\hat{W}^{-\mu\nu}\left(\frac{h}{v} + \frac{1}{2}\frac{h^2}{v^2}\right) + \frac{1}{2}\zeta_Z\hat{Z}_{\mu\nu}\hat{Z}^{\mu\nu}\left(\frac{h}{v} + \frac{1}{2}\frac{h^2}{v^2}\right) \\
 & + \frac{1}{2}\zeta_A\hat{A}_{\mu\nu}\hat{A}^{\mu\nu}\left(\frac{h}{v} + \frac{1}{2}\frac{h^2}{v^2}\right) + \zeta_{AZ}\hat{A}_{\mu\nu}\hat{Z}^{\mu\nu}\left(\frac{h}{v} + \frac{1}{2}\frac{h^2}{v^2}\right).
 \end{aligned}$$

(SM structure: kappa like)

$$\eta_h = \delta\bar{\lambda} + \delta v - \frac{3}{2}c_H + c_6$$

$$\eta_W = 2\delta m_W - \delta v - \frac{1}{2}c_H$$

$$\eta_{WW} = 2\delta m_W - 2\delta v - c_H$$

$$\eta_Z = 2\delta m_Z - \delta v - \frac{1}{2}c_H - c_T$$

$$\eta_{ZZ} = 2\delta m_Z - 2\delta v - c_H - 5c_T$$

(Anomalous: new Lorentz structure)

$$\theta_h = c_H$$

$$\zeta_W = \delta Z_W = (8c_{WW})$$

$$\zeta_Z = \delta Z_Z = c_w^2(8c_{WW}) + 2s_w^2(8c_{WB}) + s_w^4/c_w^2(8c_{BB})$$

$$\zeta_A = \delta Z_A = s_w^2\left((8c_{WW}) - 2(8c_{WB}) + (8c_{BB})\right)$$

$$\zeta_{AZ} = \delta Z_{AZ} = s_w c_w \left((8c_{WW}) - \left(1 - \frac{s_w^2}{c_w^2}\right)(8c_{WB}) - \frac{s_w^2}{c_w^2}(8c_{BB}) \right)$$

- hZZ/hWW/hγZ/hγγ highly related: SU(2)xU(1) gauge symmetries

(iv-1) absolute Higgs couplings (unique role of inclusive σ_{Zh})

$$\frac{c_H}{2v^2} \partial^\mu (\Phi^\dagger \Phi) \partial_\mu (\Phi^\dagger \Phi)$$

$$\frac{c_H}{2} \partial^\mu h \partial_\mu h$$

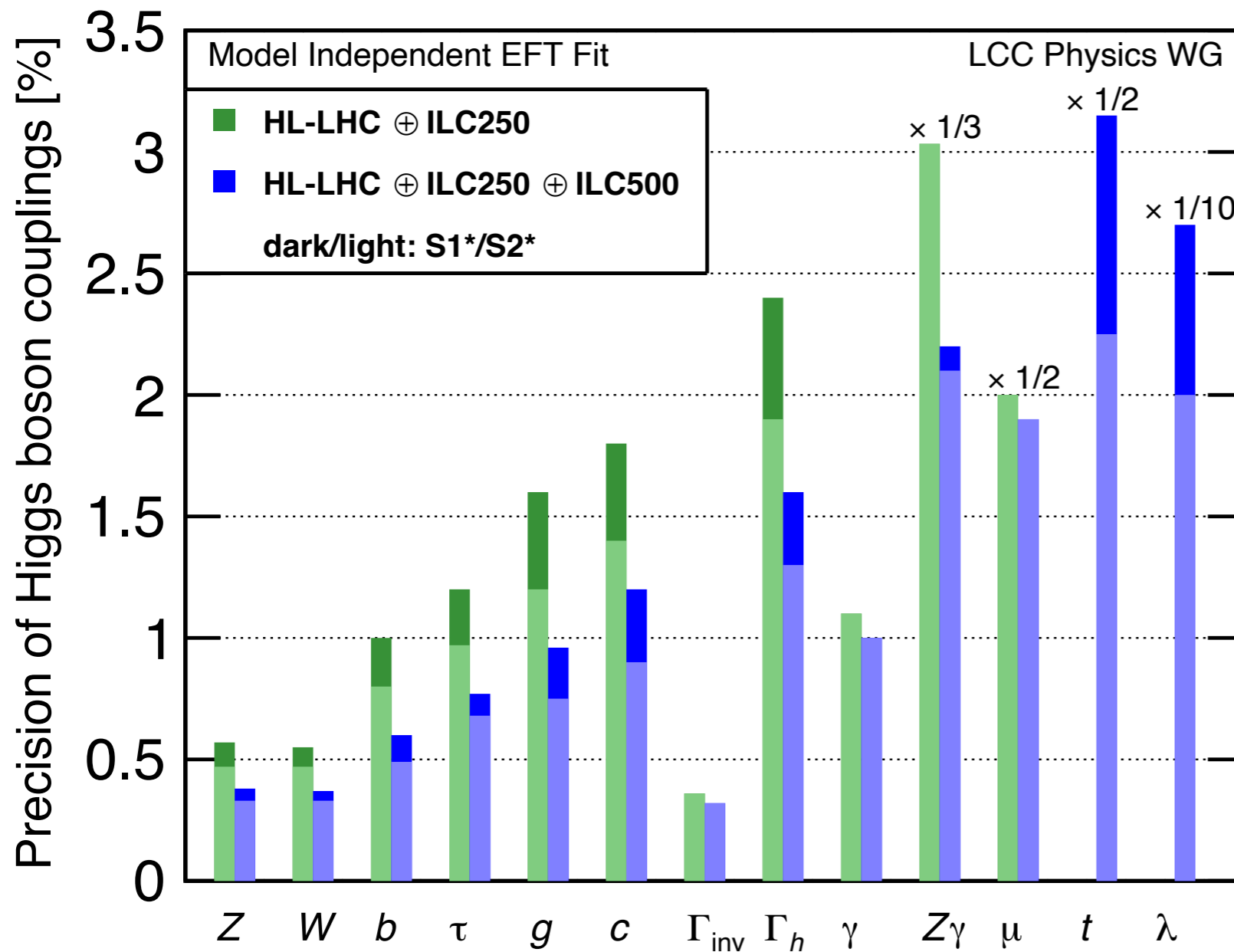
→ renormalize kinetic term
of SM Higgs field

$$h \longrightarrow (1 - c_H/2)h$$

→ **shift all SM Higgs couplings by $-c_H/2$**

- c_H can not be determined by any BR or ratio of couplings
- c_H has to rely on inclusive cross section of $e^+e^- \rightarrow Zh$, enabled by recoil mass technique at e^+e^-

precisions at Higgs factories: complementarity with LHC



(arXiv:1903.01629)

#qualitative:

model independence,
hcc coupling

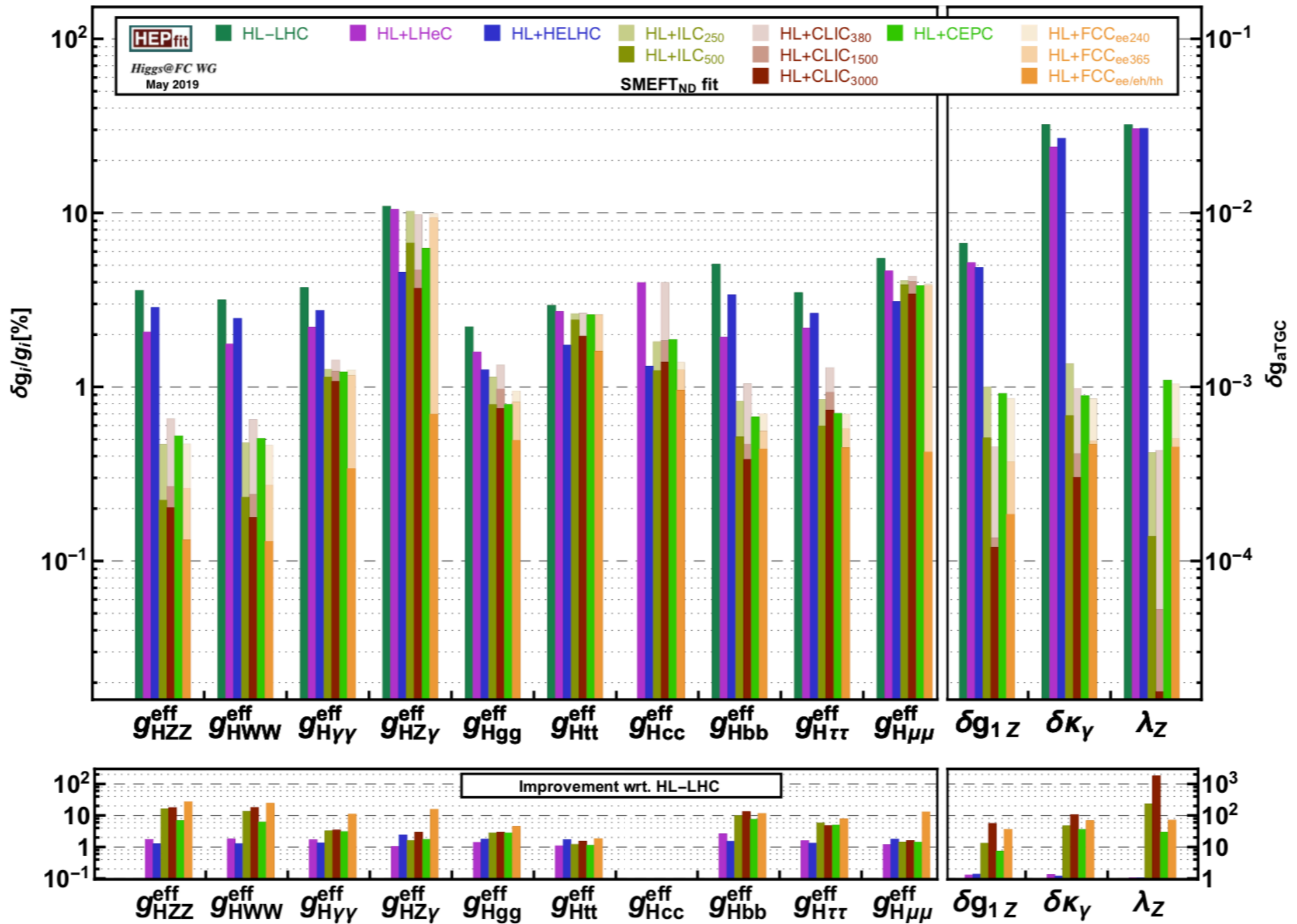
#quantitative (<~1%):

hZZ, hWW, hbb, hττ
h->invisible/exotic

#synergy:

hγγ, hγZ, hμμ, htt, λ

precision at Higgs factories: European Strategy Update



top-quark operators (added to previous SMEFT fit)

(no 4-fermion operators considered)

$$\mathcal{O}_{tH} = (\Phi^\dagger \Phi)(\bar{Q}t\tilde{\Phi}),$$

$$\mathcal{O}_{Hq}^{(1)} = (\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi)(\bar{Q}\gamma^\mu Q),$$

$$\mathcal{O}_{Hq}^{(3)} = (\Phi^\dagger i \overleftrightarrow{D}_\mu^a \Phi)(\bar{Q}\gamma^\mu \tau^a Q),$$

$$\mathcal{O}_{Ht} = (\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi)(\bar{t}\gamma^\mu t),$$

$$\mathcal{O}_{Htb} = i(\tilde{\Phi}^\dagger D_\mu \Phi)(\bar{t}\gamma^\mu b),$$

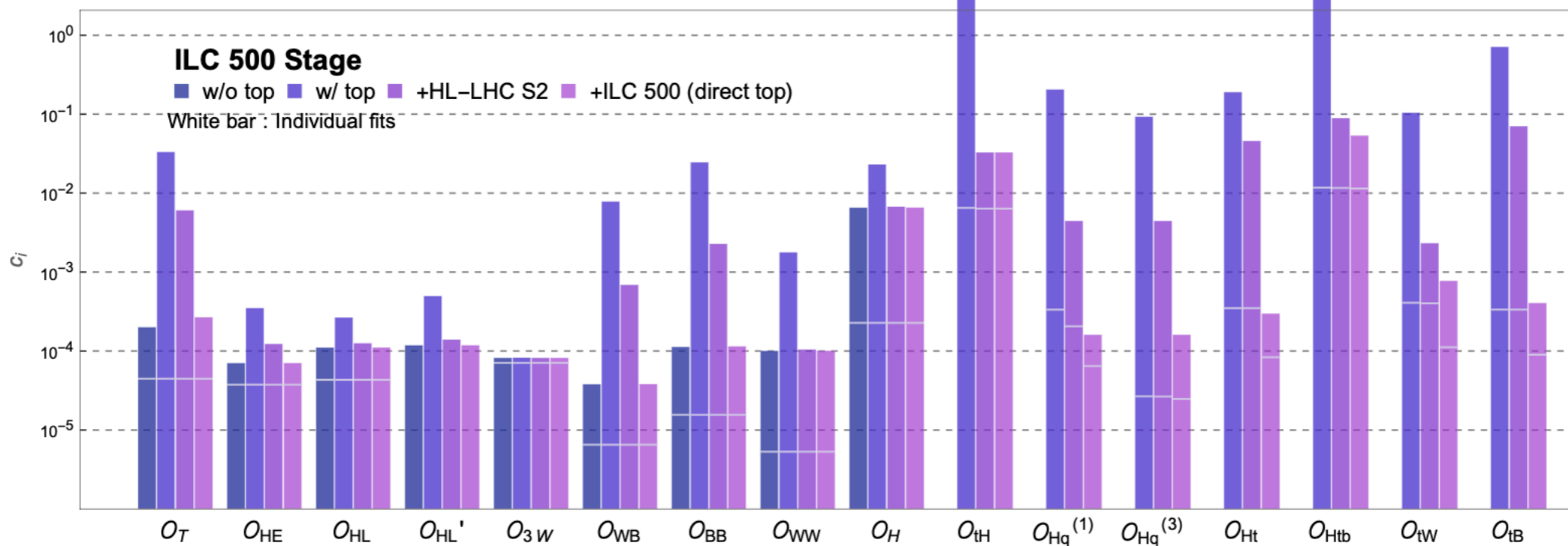
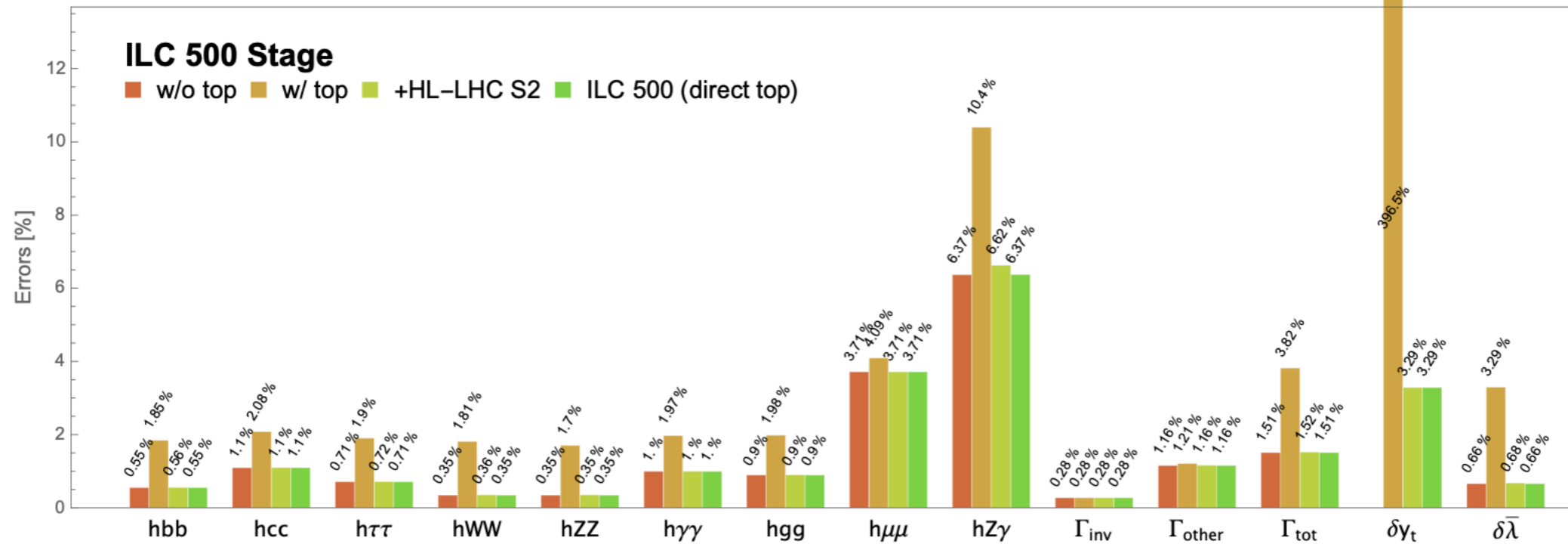
$$\mathcal{O}_{tW} = (\bar{Q}\sigma^{\mu\nu}t)\tau^a\tilde{\Phi}W_{\mu\nu}^a,$$

$$\mathcal{O}_{tB} = (\bar{Q}\sigma^{\mu\nu}t)\tilde{\Phi}B_{\mu\nu},$$

$$\Delta\mathcal{L}_{\text{top}} = y_t \frac{c_{tH}}{v^2} \mathcal{O}_{tH} + \frac{c_{Hq}^{(1)}}{v^2} \mathcal{O}_{Hq}^{(1)} + \frac{c_{Hq}^{(3)}}{v^2} \mathcal{O}_{Hq}^{(3)} + \frac{c_{Ht}}{v^2} \mathcal{O}_{Ht} + \frac{c_{Htb}}{v^2} \mathcal{O}_{Htb} + \frac{c_{tW}}{v^2} \mathcal{O}_{tW} + \frac{c_{tB}}{v^2} \mathcal{O}_{tB}.$$

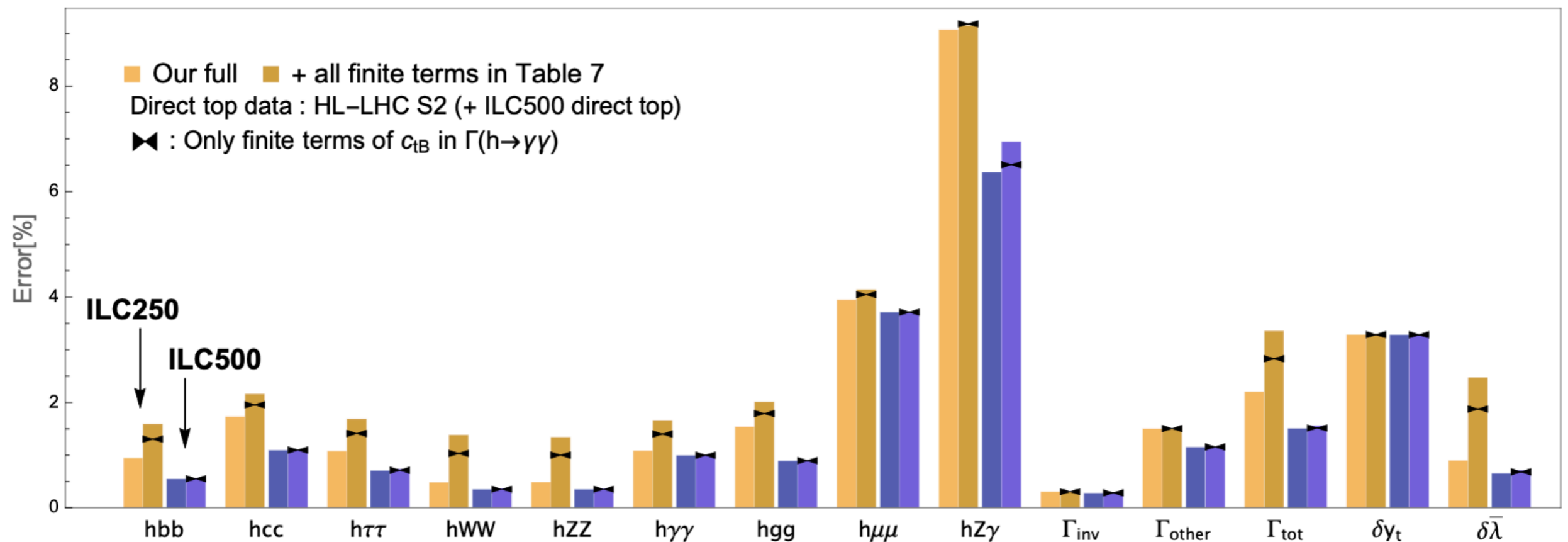
results (IV): ILC250+LHC+ILC500

- precisions of both Higgs couplings and operators restored

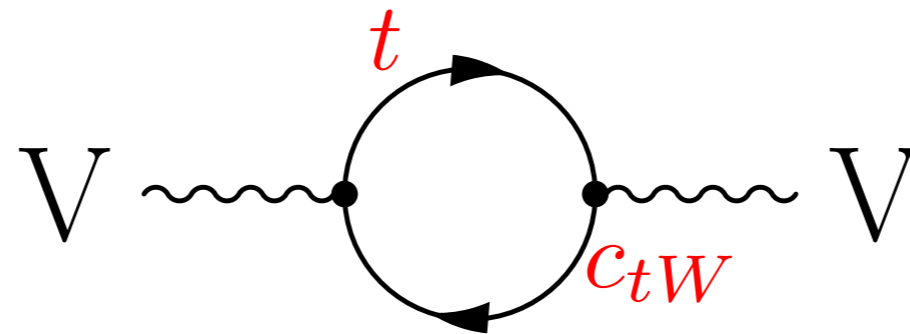


results (V): potential impact from finite one-loop effects

- could be significant @ 250 GeV, in particular for hZZ / hWW , x2-3 worse, though ~ 1 -2% precision
- almost no difference once direct $e^+e^- \rightarrow tt$ data is available



effect of top operators: example



log-dependence

higgs operator

$$\frac{g^2 c_{WW}}{m_W^2} \Phi^\dagger \Phi W_{\mu\nu}^a W^{a\mu\nu}$$

top operator

$$\frac{c_{tW}}{v^2} (\bar{Q} \sigma^{\mu\nu} t) \tau^a \tilde{\Phi} W_{\mu\nu}^a$$

$$\dot{c}_{WW} = \frac{1}{4} (-2g y_t N_c \underline{c_{tW}})$$

more detailed power-counting rule

	Higgs loop production/decay	other observables	top production
SM	finite 1-loop	tree-level	tree-level
Higgs operator	tree-level from $c_{WW,WB,BB}$ finite 1-loop from other operators	tree-level	none
top operator	log 1-loop via $\dot{c}_{WW,WB,BB}$ log 2-loop via other \dot{c} finite 1-loop via tree-shift of y_t, g_{Ztt}	log 1-loop via \dot{c}	tree-level

key: include leading contributions from top-quark operators

our approach to include NLO top effects

S.Jung, J.Lee, M.Perello, JT, M.Vos, [arXiv:2006.14631](https://arxiv.org/abs/2006.14631)

- we didn't try to include full NLO effects for all observables
- mainly include effects that have log-dependence on Q-scale
- captured by Renormalization Group Evolution (mixing)

$$\dot{c}_i \equiv 16\pi^2 \frac{dc_i}{d \ln \mu} = \gamma_{ij} c_j$$

[Alonso, Jenkins,
Manohar, Trott, 2013]

\mathbf{c}_i : Higgs operators; \mathbf{c}_j : Top operators; $\mathbf{\gamma}_{ij}$: anomalous dimensions

- convenient to include such top-quark effects in all Higgs/EWPO/
WW observables that have been considered previously

λ_{hhh} model-independent determination in SMEFT (c_6)

(arXiv:1708.09079)

$$\frac{\sigma_{Zh\bar{h}}}{\sigma_{SM}} - 1 = 0.565c_6 - 3.58c_H + 16.0(8c_{WW}) + 8.40(8c_{WB}) + 1.26(8c_{BB}) \\ - 6.48c_T - 65.1c'_{HL} + 61.1c_{HL} + 52.6c_{HE},$$

$$\Delta c_6 = \frac{1}{0.565} \left[\left(\frac{\Delta\sigma_{Zh\bar{h}}}{\sigma_{SM}} \right)^2 + \sum_{i,j} a_i a_j (V_c)_{ij} \right]^{\frac{1}{2}}$$

(statistical error) (systematic error)

16.8% >> 2.0%

- interesting to prove this in $e^+e^- \rightarrow \nu\bar{\nu}HH$ as well: still open
- another crucial question: can we do the same analysis to HH processes at hadron collider? can we still measure λ_{hhh} to 5% at FCC-hh?

SMEFT fit: typical difference with kappa fit

ILC250: $\int L dt = 2 \text{ ab}^{-1}$ @ 250 GeV

coupling $\Delta g/g$	kappa-fit	EFT-fit
hZZ	0.38%	0.50%
hWW	1.8%	0.50%
hbb	1.8%	0.99%
Γ_h	3.9%	2.3%

(definition for higgs coupling precision: 1/2 of partial width precision)

global SMEFT fit: full formalism (23 pars.)

$$\begin{aligned}
 \Delta\mathcal{L} = & \frac{c_H}{2v^2} \partial^\mu (\Phi^\dagger \Phi) \partial_\mu (\Phi^\dagger \Phi) + \frac{c_T}{2v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\Phi^\dagger \overleftrightarrow{D}_\mu \Phi) - \frac{c_6 \lambda}{v^2} (\Phi^\dagger \Phi)^3 \\
 & + \frac{g^2 c_{WW}}{m_W^2} \Phi^\dagger \Phi W_{\mu\nu}^a W^{a\mu\nu} + \frac{4gg' c_{WB}}{m_W^2} \Phi^\dagger t^a \Phi W_{\mu\nu}^a B^{\mu\nu} \\
 & + \frac{g'^2 c_{BB}}{m_W^2} \Phi^\dagger \Phi B_{\mu\nu} B^{\mu\nu} + \frac{g^3 c_{3W}}{m_W^2} \epsilon_{abc} W_{\mu\nu}^a W^{b\nu\rho} W^{c\rho\mu} \\
 & + i \frac{c_{HL}}{v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\bar{L} \gamma_\mu L) + 4i \frac{c'_{HL}}{v^2} (\Phi^\dagger t^a \overleftrightarrow{D}^\mu \Phi) (\bar{L} \gamma_\mu t^a L) \\
 & + i \frac{c_{HE}}{v^2} (\Phi^\dagger \overleftrightarrow{D}^\mu \Phi) (\bar{e} \gamma_\mu e) .
 \end{aligned}$$

10 operators (h,W,Z, γ): $c_H, c_T, c_6, c_{WW}, c_{WB}, c_{BB}, c_{3W}, c_{HL}, c'_{HL}, c_{HE}$

+ 4 SM parameters: g, g', v, λ

+ 5 operators modifying h couplings to b, c, τ, μ, g

+ 2 operators for contact interactions with quarks

+ 2 parameters for h->invisible and exotic

strategy to determine all the 23 parameters at e^+e^-

Electroweak Precision Observables (9)

+

Triple Gauge boson Couplings (3)

+

Higgs observables at LHC & e^+e^- (3+12x2)

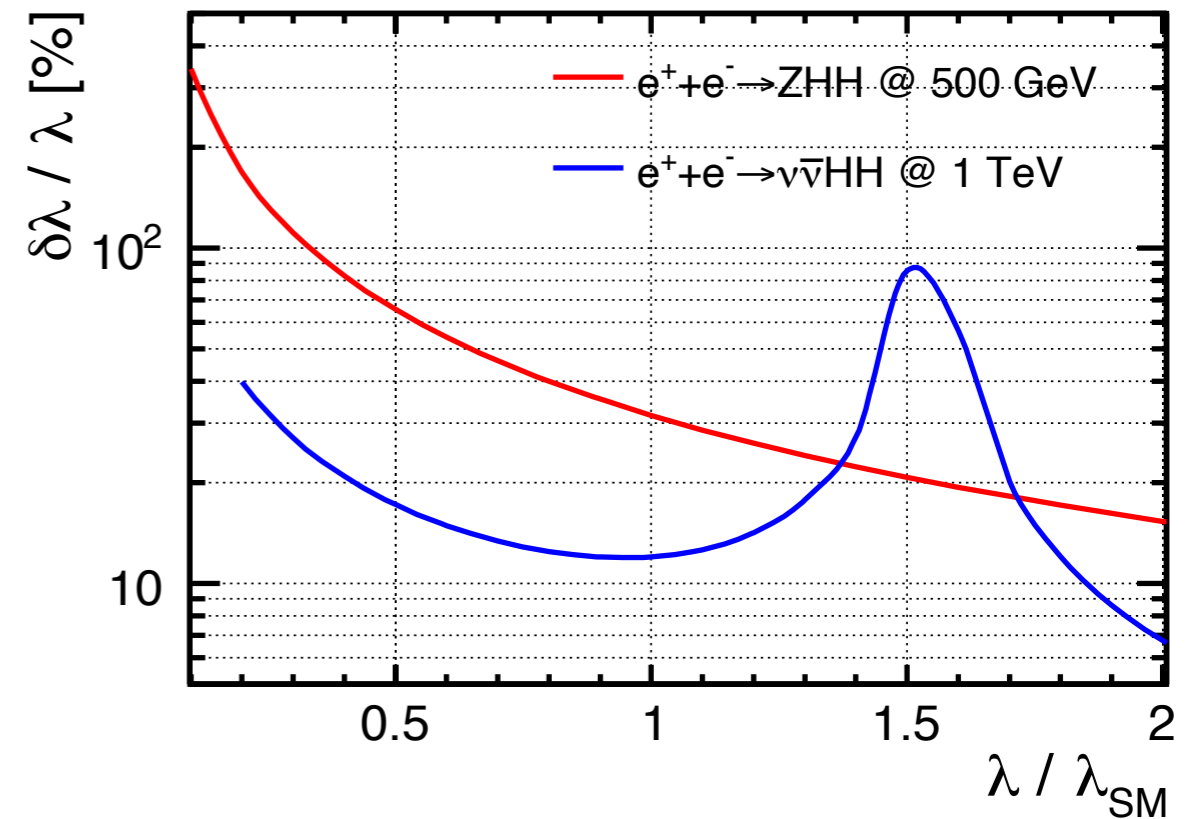
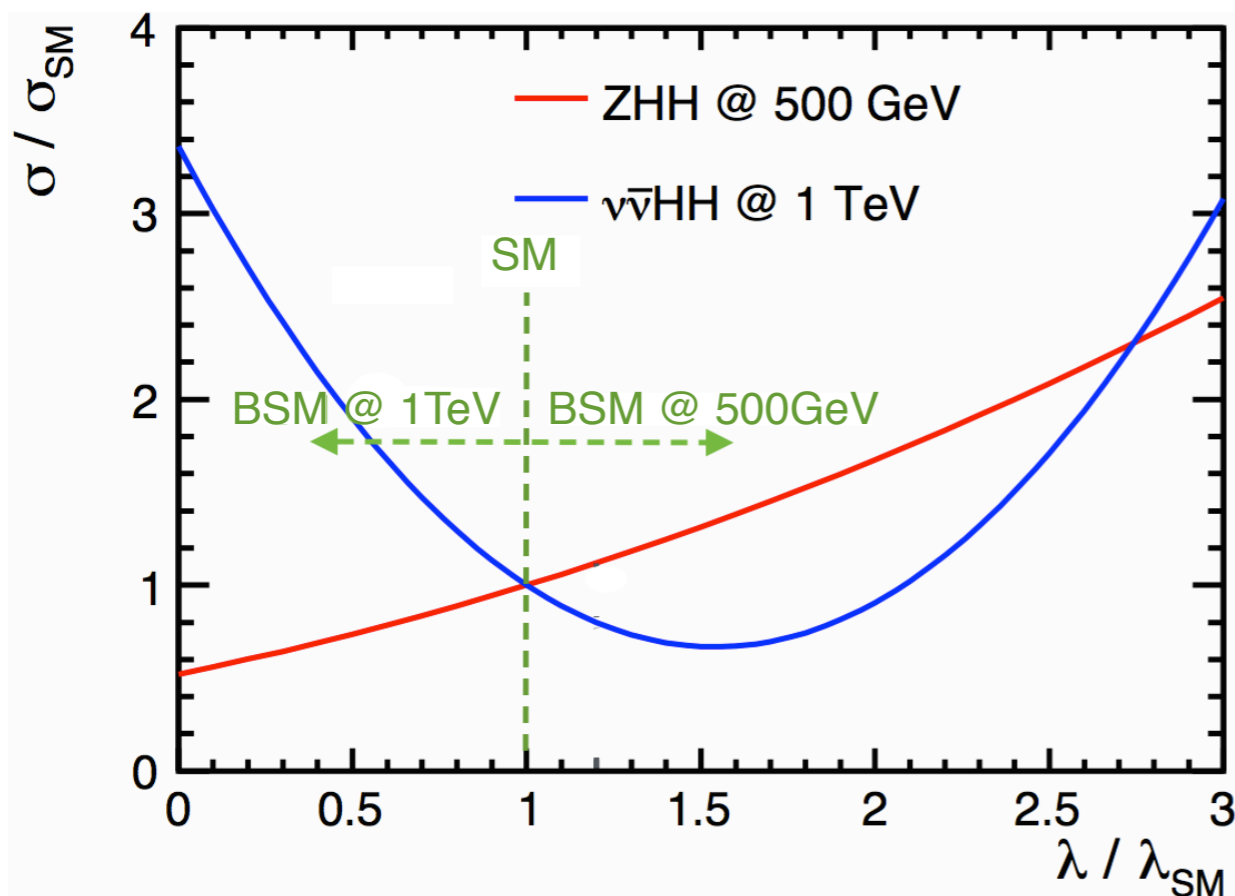
↑
2 for polarized

- all the 23 parameters can be determined ***simultaneously***

(details in backup)

Higgs self-coupling: when $\lambda_{HHH} \neq \lambda_{SM}$?

- λ_{HHH} can be enhanced significantly in BSM
- complementarity between ZHH & $\nu\bar{\nu}HH$ (& LHC): interference nature
- if $\lambda_{HHH} / \lambda_{SM} = 2$, λ_{HHH} be measured to $\sim 13\%$ using ZHH at 500 GeV e^+e^-



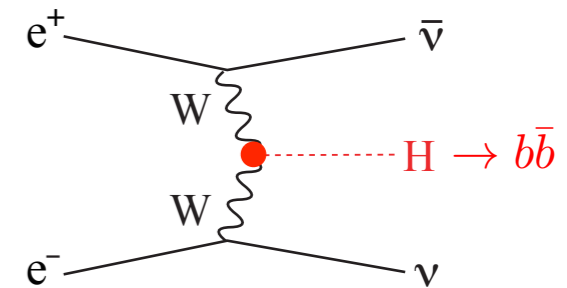
direct meas. of hWW coupling & impact of \sqrt{s}

$$\Gamma_H = \frac{\Gamma_{HZZ}}{\text{Br}(H \rightarrow ZZ^*)} \propto \frac{g_{HZZ}^2}{\text{Br}(H \rightarrow ZZ^*)}$$

→ Br(H→ZZ*) very small

★
$$\Gamma_H = \frac{\Gamma_{HWW}}{\text{Br}(H \rightarrow WW^*)} \propto \frac{g_{HWW}^2}{\text{Br}(H \rightarrow WW^*)}$$

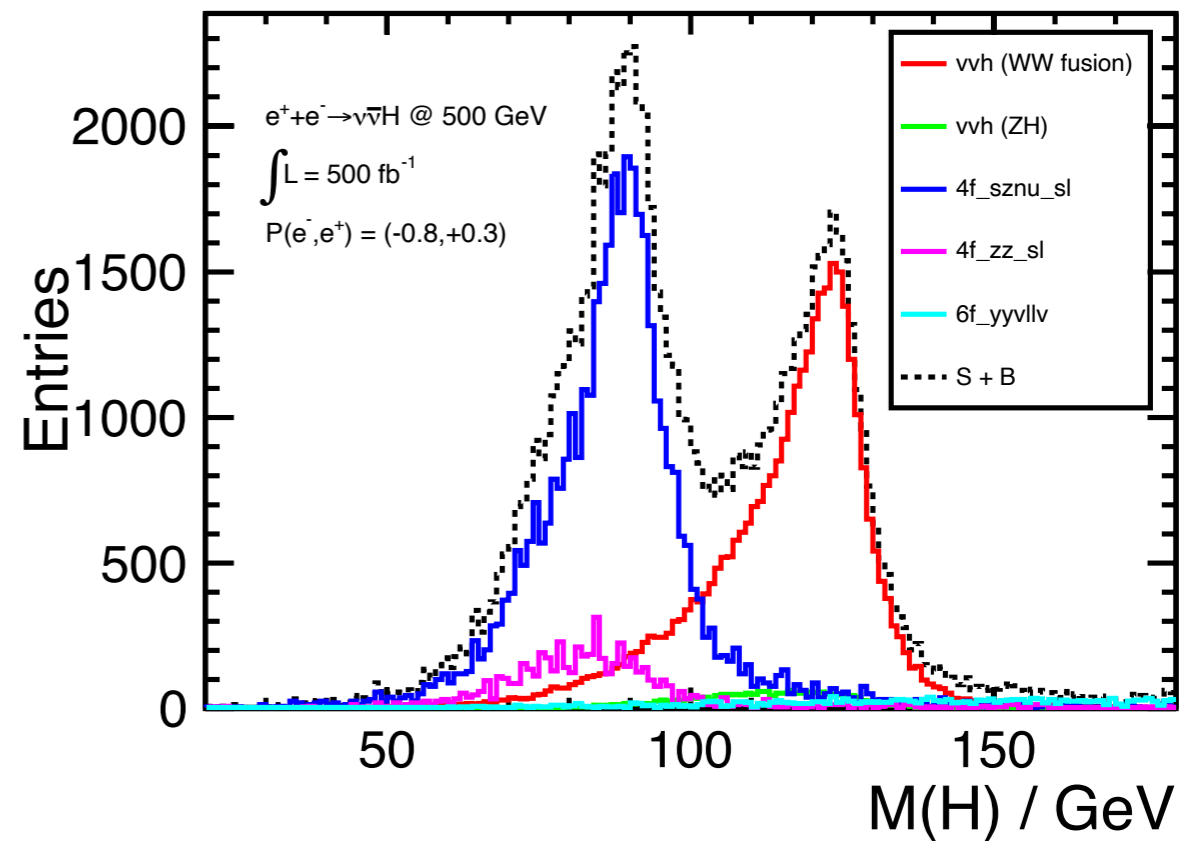
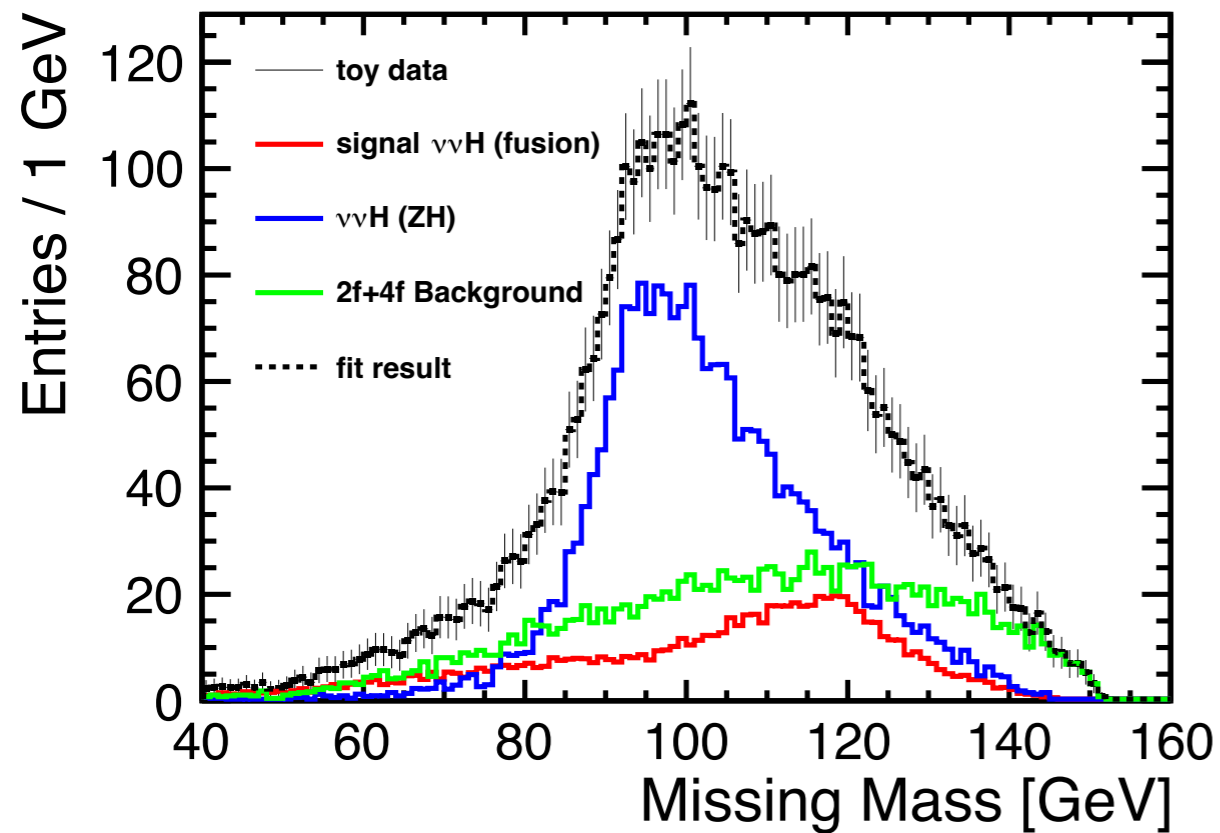
→ better option!



@250 GeV

Duerig, et al., arXiv:1403.7734

@500 GeV



- we used to think W-fusion production is crucial...

From observables to couplings — Global Fit

in case there are correlated observables

$$\chi^2 = \sum_{i=1}^n \left(\frac{Y_i - Y'_i}{\Delta Y_i} \right)^2 + (Y_j - Y'_j)^T C_j^{-1} (Y_j - Y'_j)$$

Y_j : column vector of correlated observables

C_j : covariance matrix for those observables

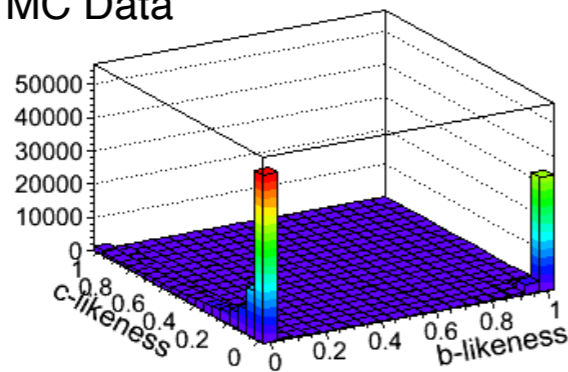
one example: TGCs in SMEFT fit

(ii-2) Higgs direct couplings to bb, cc and gg

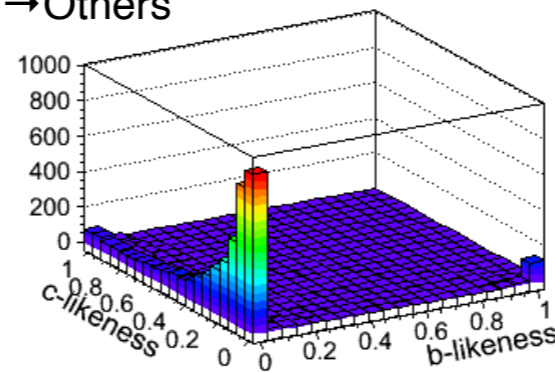
- clean environment at e^+e^- ; excellent b- and c-tagging performance
- bb/cc/gg modes can be separated simultaneously by template fitting

$e^+e^- \rightarrow ZH \rightarrow ff(jj)$: b-likeness .vs. c-likeness

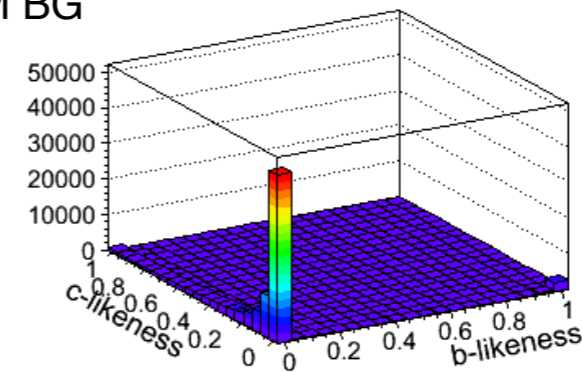
MC Data



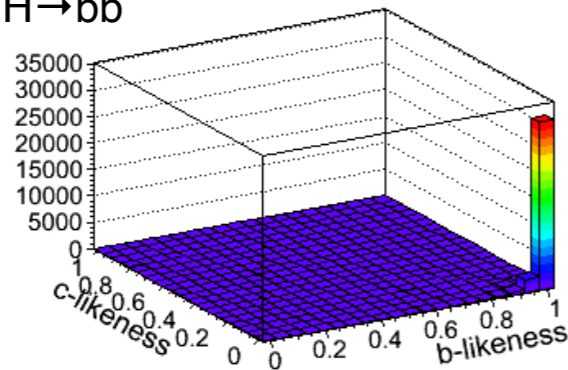
H→Others



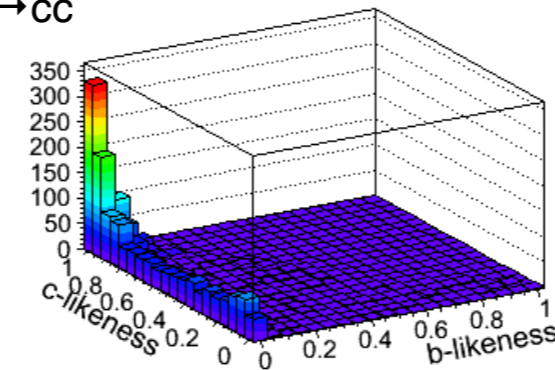
SM BG



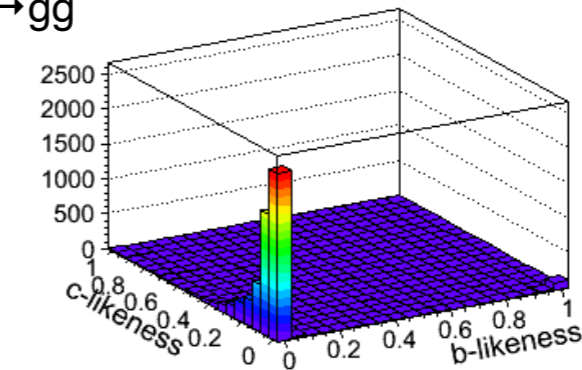
H→bb



H→cc



H→gg

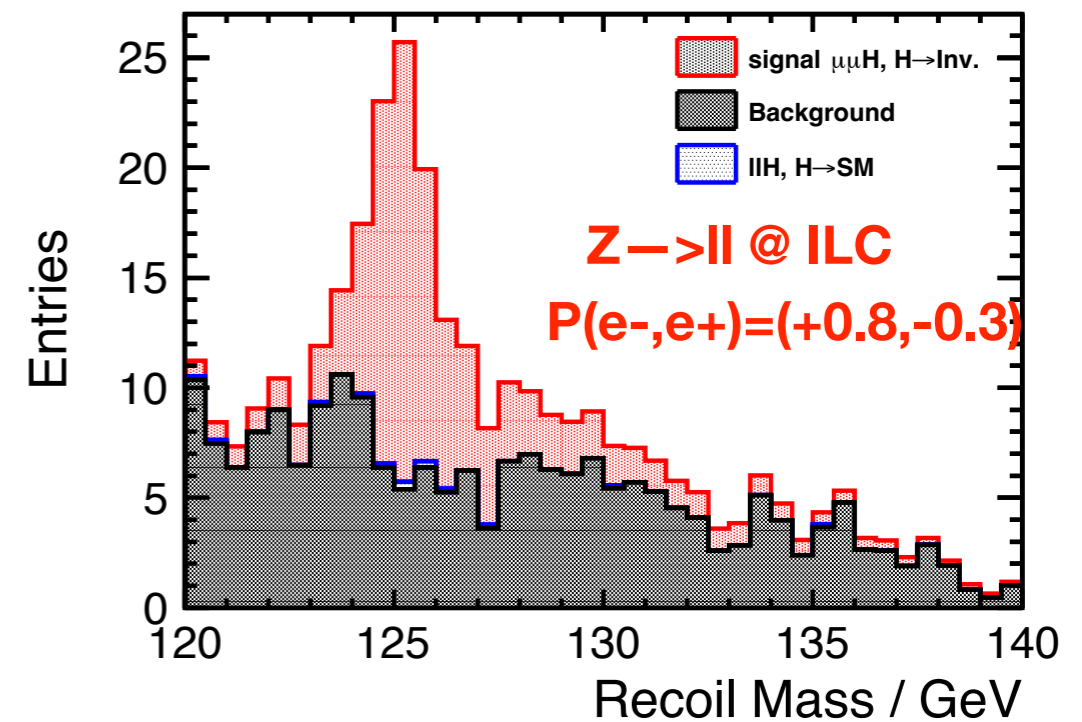
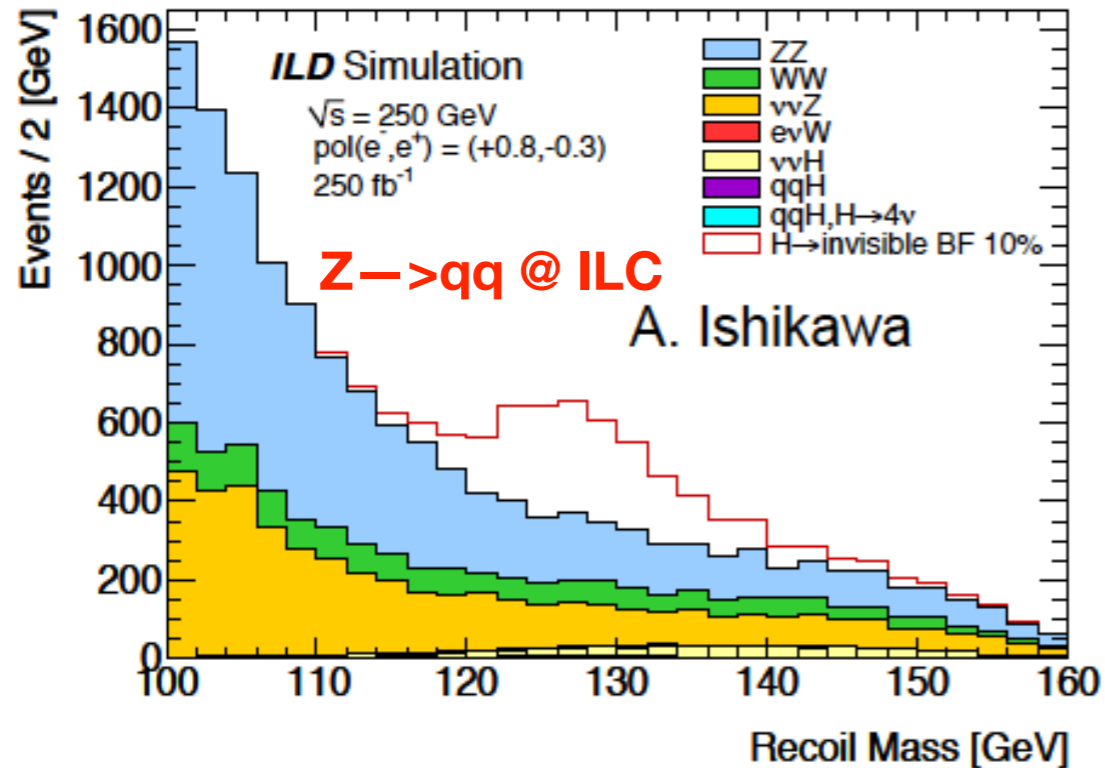


Ono, et. al, Euro. Phys. J. C73, 2343; F.Mueller, PhD thesis (DESY)

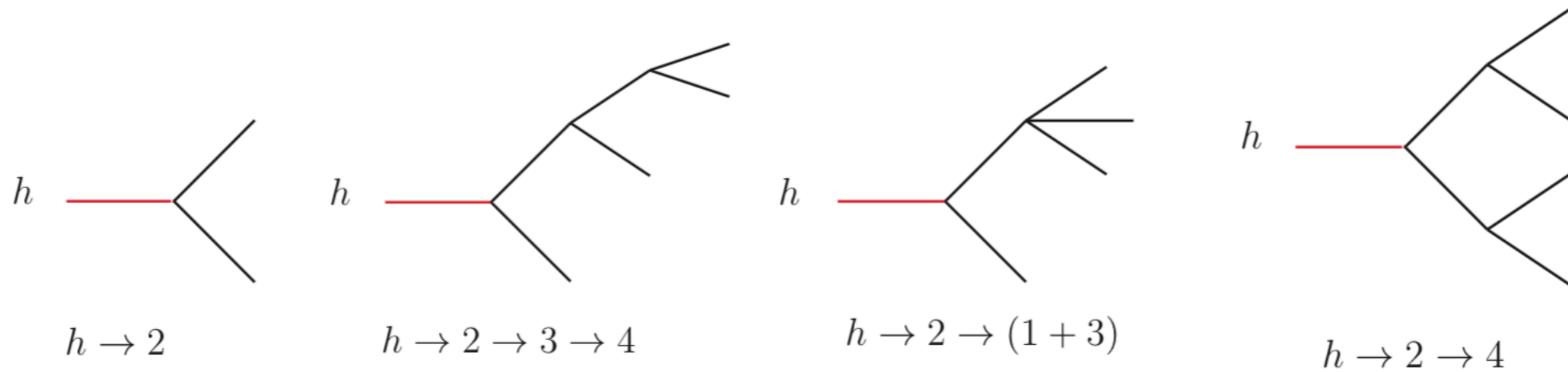
(ii-3) search of Higgs to invisible

- $BR(H \rightarrow \text{inv.}) < 0.3\%$ ($CL^{95\%}$)
- Higgs portal dark matter search
- right-handed beam polarization: much lower background

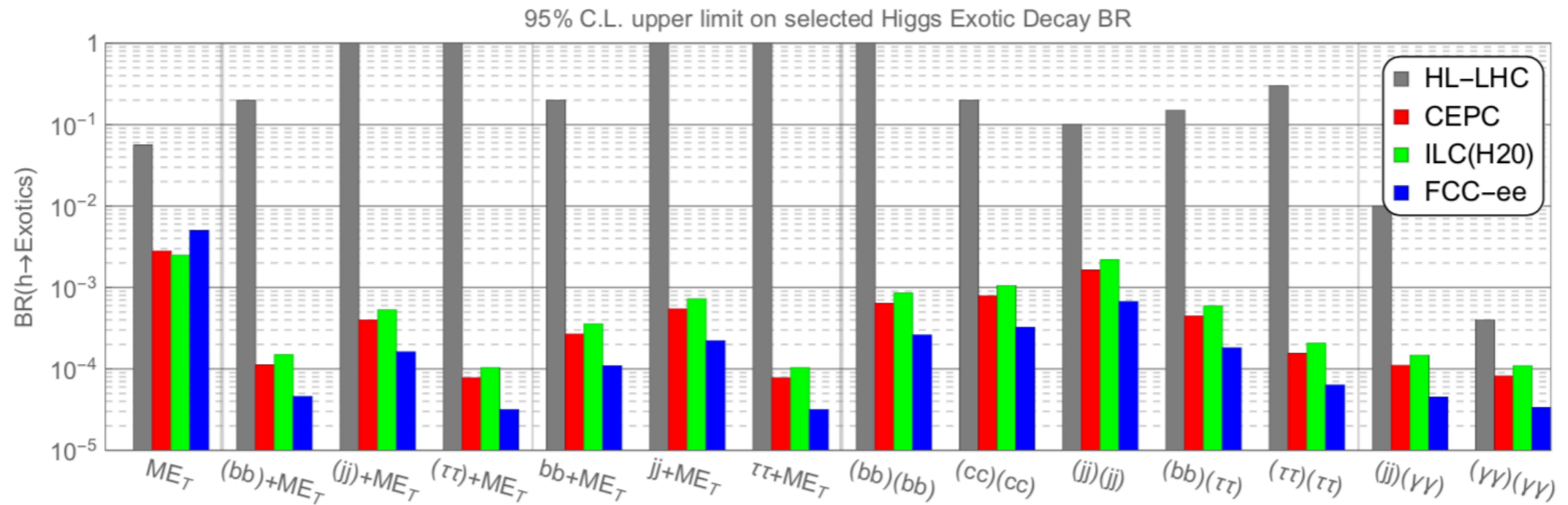
$$e^+ + e^- \rightarrow ZH \rightarrow l^+l^- / q\bar{q} + \text{Missing}$$



(ii-3) search of Higgs exotic decays



BR < 0.1-0.01% @ ILC, Liu et al, arXiv:1612.09284



efficiencies breakdown (leptonic recoil)

H \rightarrow XX	bb	cc	gg	$\tau\tau$	WW*	ZZ*	$\gamma\gamma$	γZ
BR (SM)	57.8%	2.7%	8.6%	6.4%	21.6%	2.7%	0.23%	0.16%
Lepton Finder	93.70%	93.69%	93.40%	94.02%	94.04%	94.36%	93.75%	94.08%
Lepton ID+Precut	93.68%	93.66%	93.37%	93.93%	93.94%	93.71%	93.63%	93.22%
$M_{l+l-} \in [73, 120]$ GeV	89.94%	91.74%	91.40%	91.90%	91.82%	91.81%	91.73%	91.47%
$p_T^{l+l-} \in [10, 70]$ GeV	89.94%	90.08%	89.68%	90.18%	90.04%	90.16%	89.99%	89.71%
$ \cos \theta_{\text{miss}} < 0.98$	89.94%	90.08%	89.68%	90.16%	90.04%	90.16%	89.91%	89.41%
BDT > -0.25	88.90%	89.04%	88.63%	89.12%	88.96%	89.11%	88.91%	88.28%
$M_{\text{rec}} \in [110, 155]$ GeV	88.25%	88.35%	87.98%	88.43%	88.33%	88.52%	88.21%	87.64%

- every cut is applied very carefully to avoid large bias, still $\sim 1\%$
- nevertheless, it becomes almost a paradox:
 - ☑ no cut, no bias; looser cuts, less bias
 - ☑ extremely tighter cuts, less bias;
 - ☑ too loose or too tight cuts \rightarrow remain too much background or too little signal \rightarrow bad precision measurement

efficiencies breakdown (hadronic recoil)

Decay mode	$\epsilon_{\mathcal{L}>0.65}^{\text{vis.}}$	$\epsilon_{\mathcal{L}>0.60}^{\text{invis.}}$	$\epsilon^{\text{vis.}} + \epsilon^{\text{invis.}}$
H \rightarrow invis.	<0.1 %	23.5 %	23.5 %
H \rightarrow q \bar{q} /gg	22.6 %	<0.1 %	22.6 %
H \rightarrow WW*	22.1 %	0.1 %	22.2 %
H \rightarrow ZZ*	20.6 %	1.1 %	21.7 %
H \rightarrow $\tau^+\tau^-$	25.3 %	0.2 %	25.5 %
H \rightarrow $\gamma\gamma$	25.7 %	<0.1 %	25.7 %
H \rightarrow Z γ	18.6 %	0.3 %	18.9 %
H \rightarrow WW* \rightarrow q \bar{q} q \bar{q}	20.8 %	<0.1 %	20.8 %
H \rightarrow WW* \rightarrow q \bar{q} l ν	23.3 %	<0.1 %	23.3 %
H \rightarrow WW* \rightarrow q \bar{q} $\tau\nu$	23.1 %	<0.1 %	23.1 %
H \rightarrow WW* \rightarrow l ν l ν	26.5 %	0.1 %	26.5 %
H \rightarrow WW* \rightarrow l ν $\tau\nu$	21.1 %	0.5 %	21.6 %
H \rightarrow WW* \rightarrow $\tau\nu$ $\tau\nu$	16.3 %	2.3 %	18.7 %

○ relative bias can be as large as ~15%

a nice trick: categorization

$$\sigma_{ZH} = \sigma^{cat1} + \sigma^{cat2} + \sigma^{cat3} + \sigma^{cat4} + \dots$$

- if we have a complete list of categories
- then we only need to keep all selection cuts independent of decay mode in each category;
- selections cuts among categories can be very different

for example

$$\sigma_{ZH} = \sigma^{H \rightarrow \text{invisible}} + \sigma^{H \rightarrow \text{visible}}$$

a realistic solution: make use of individual BR measurement

$$\sigma_{ZH} = \frac{N_S}{R_f L \bar{\epsilon}} \quad \bar{\epsilon} \equiv \sum_i B_i \epsilon_i$$

N_S : # of signal

R_f : BR of $Z \rightarrow ff$

L : int. luminosity

B_i : BR of H decay mode i

ϵ_i : efficiency of mode i

- if every ϵ_i is same $\rightarrow \sum B_i = 1$; no need for any knowledge about B_i
- nevertheless, we can measure many of the $\sigma \times B_i$; assume $i=1..n$ is known with ΔB_i ; $i=n+1, \dots$ is unknown, sum up to B_x ;

known modes

systematic error to σ_{ZH}

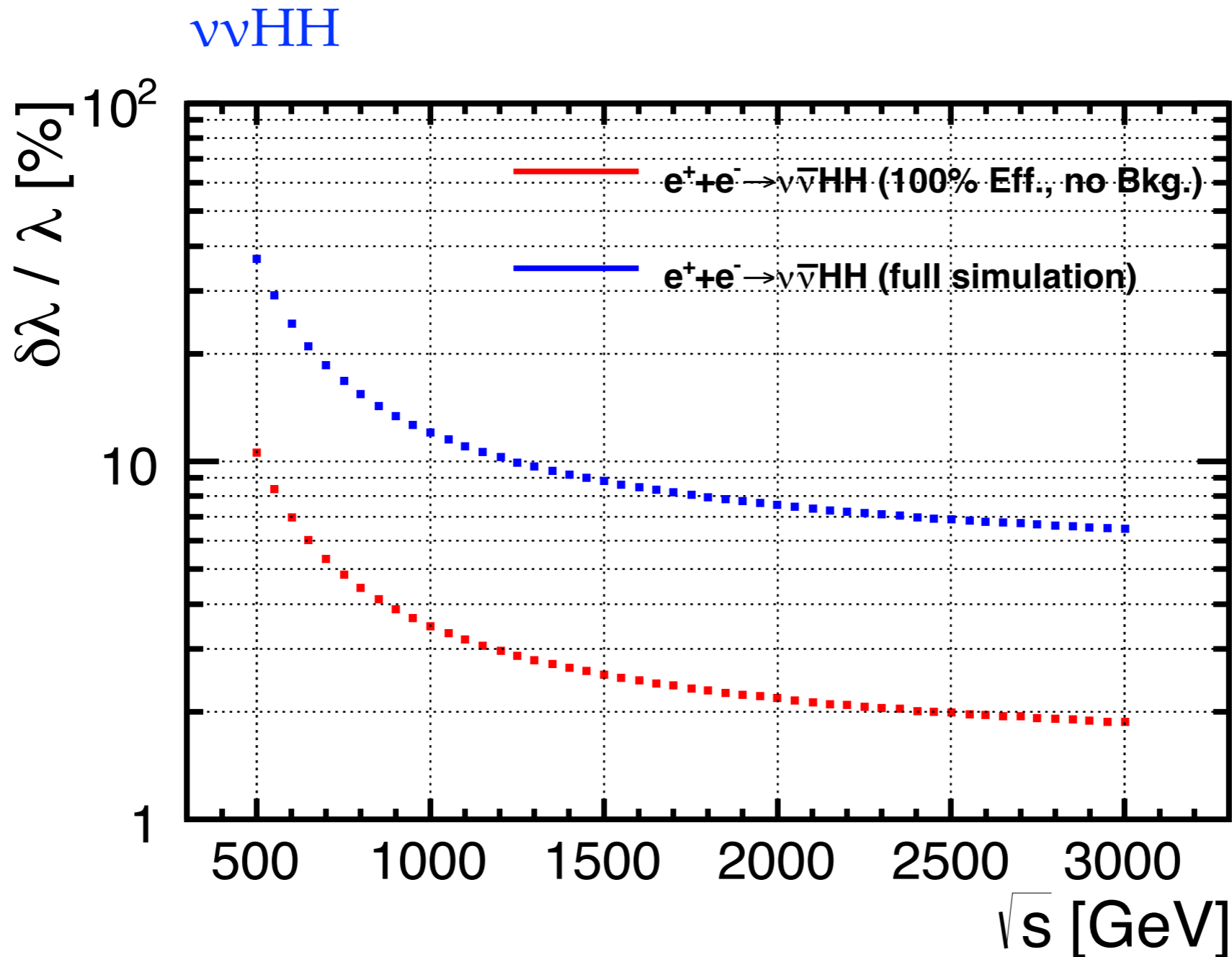
unknown modes

$$\frac{\Delta \sigma_{ZH}}{\sigma_{ZH}} = \frac{\Delta \bar{\epsilon}}{\bar{\epsilon}} = \sqrt{\sum_{i=1}^n \Delta B_i^2 \left(\frac{\epsilon_i}{\epsilon_0} - 1 \right)^2}$$

$$\frac{\Delta \sigma_{ZH}}{\sigma_{ZH}} = \frac{\Delta \bar{\epsilon}}{\bar{\epsilon}} < \sum_{i=n+1} B_i \frac{\delta \epsilon_{\max}}{\epsilon_0} = B_x \frac{\delta \epsilon_{\max}}{\epsilon_0}$$

- leptonic recoil, demonstrated possible $\delta \sigma_{ZH} \sim 0.1\%$ for $B_x < 10\%$
- hadronic recoil, still need more work for $\delta \sigma_{ZH} < 1\%$ for $B_x < 10\%$

expected precision of λ : impact from analysis & \sqrt{s}



- for $\nu\nu HH$: significantly better from 500 GeV to 1 TeV, $\delta\lambda / \lambda \sim 10\%$ achievable at ≥ 1 TeV; not drastically better, from 1 TeV to 3 TeV, improved by 50%

strategy to determine all the 23 parameters

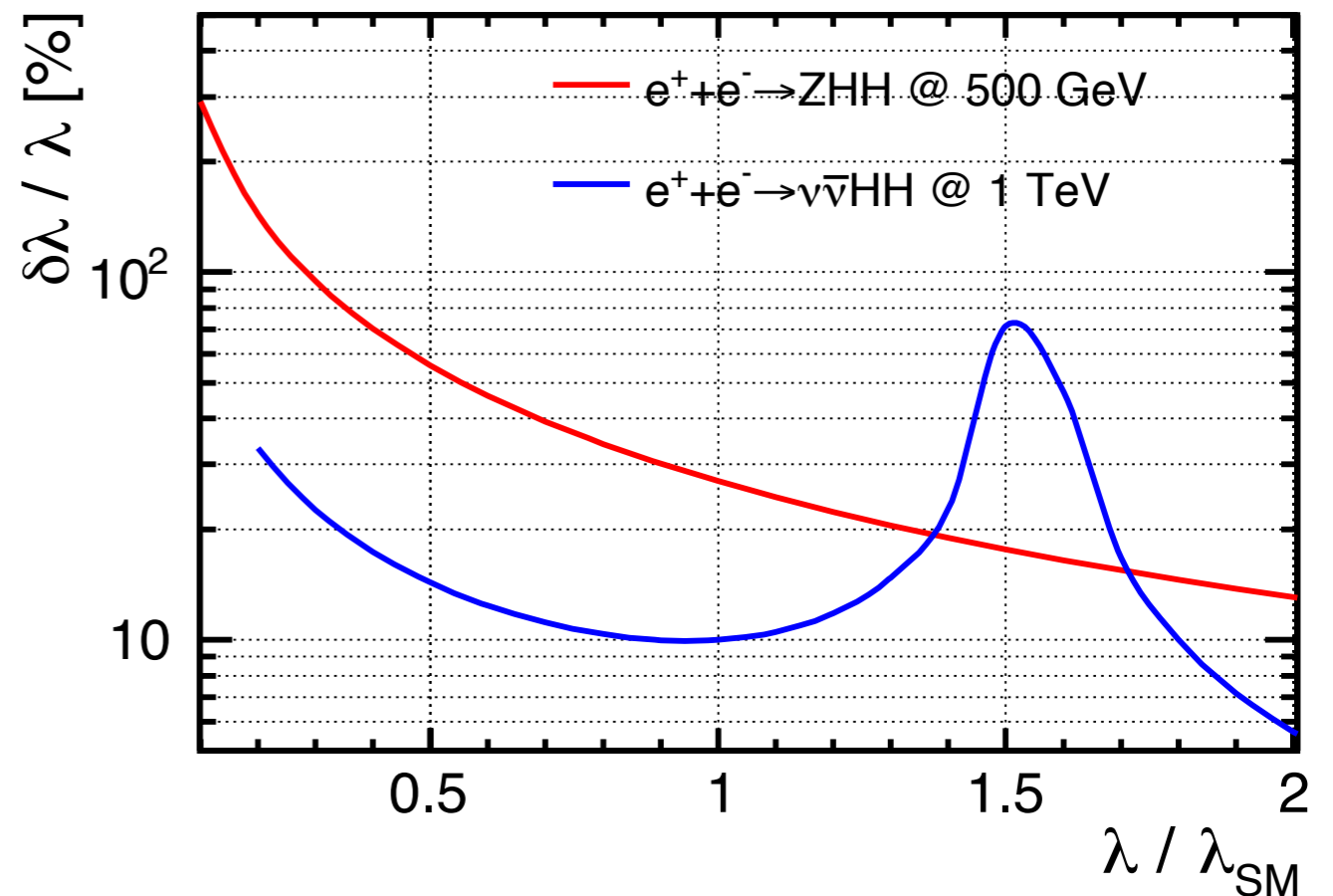
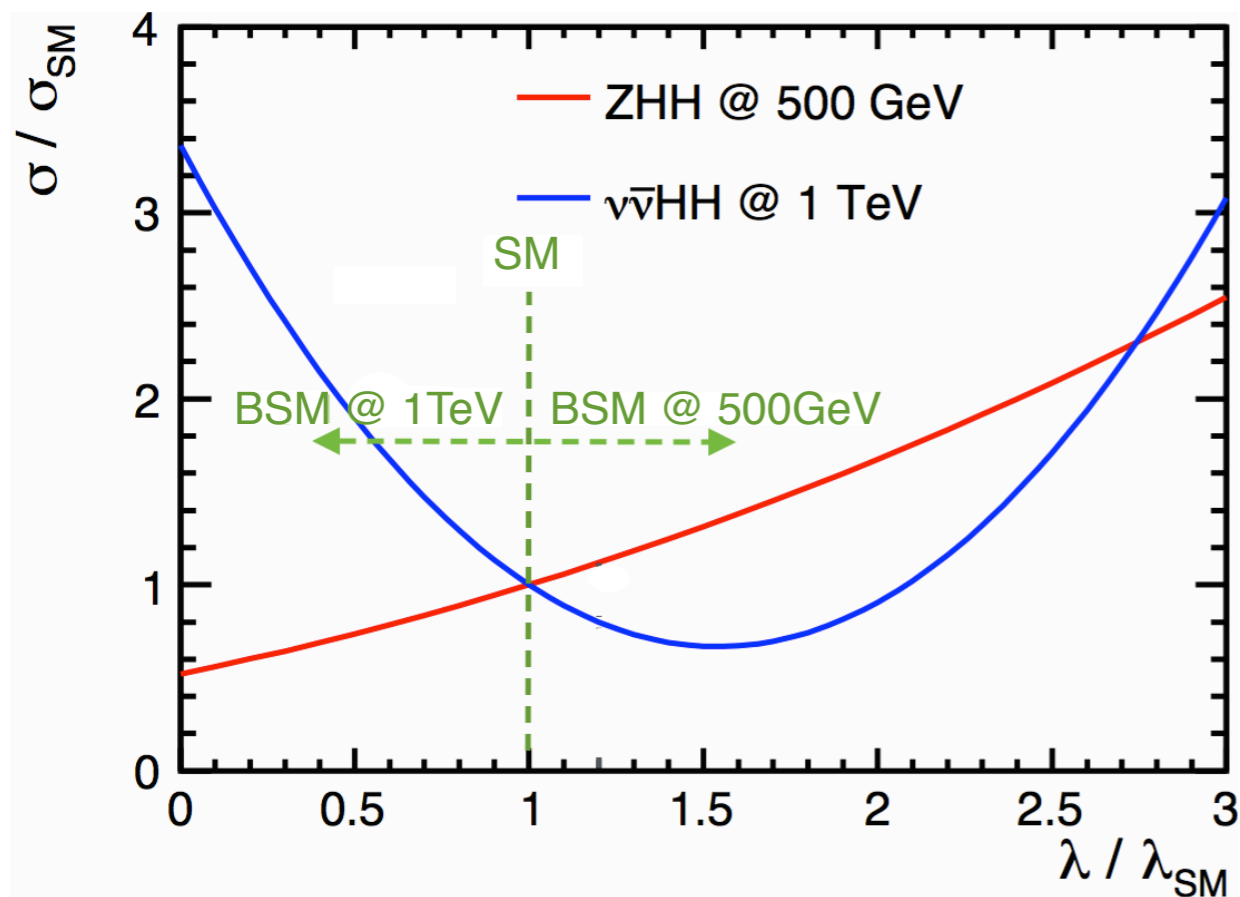
- m_W and $\alpha(m_Z) \rightarrow g, g'$;
- $G_F \rightarrow v; m_h \rightarrow \lambda; m_Z \rightarrow c_T$;
- A_l and $\Gamma_l \rightarrow c_{HL} + c_{HL}', c_{HE}$;
- Γ_W and $\Gamma_Z \rightarrow c_W, c_Z$;

- $g_{1Z} \rightarrow c_{HL}'; K_\gamma \rightarrow c_{WB}; K_\lambda \rightarrow c_{3W}$;

- $BR(h \rightarrow \gamma\gamma)$ and $BR(h \rightarrow \gamma Z) \rightarrow c_{BB}, c_{WW}$;
- $\sigma_{ZH} \rightarrow c_H; \sigma_{ZH H} \rightarrow c_6$;
- $BR(h \rightarrow bb/cc/gg/\mu\mu/\tau\tau) \rightarrow y_b, y_c, c_g, y_\mu, y_\tau$;
- $BR(h \rightarrow invisible)$ and $BR(h \rightarrow other)$;
- c_{WW} is helped by A_{LR} in σ_{ZH} , angular meas., W-fusion;
- $c_{HL}/c_{HL}'/c_{HE}$ are helped by A_{LR} in σ_{ZH}

Higgs self-coupling: when $\lambda_{HHH} \neq \lambda_{SM}$?

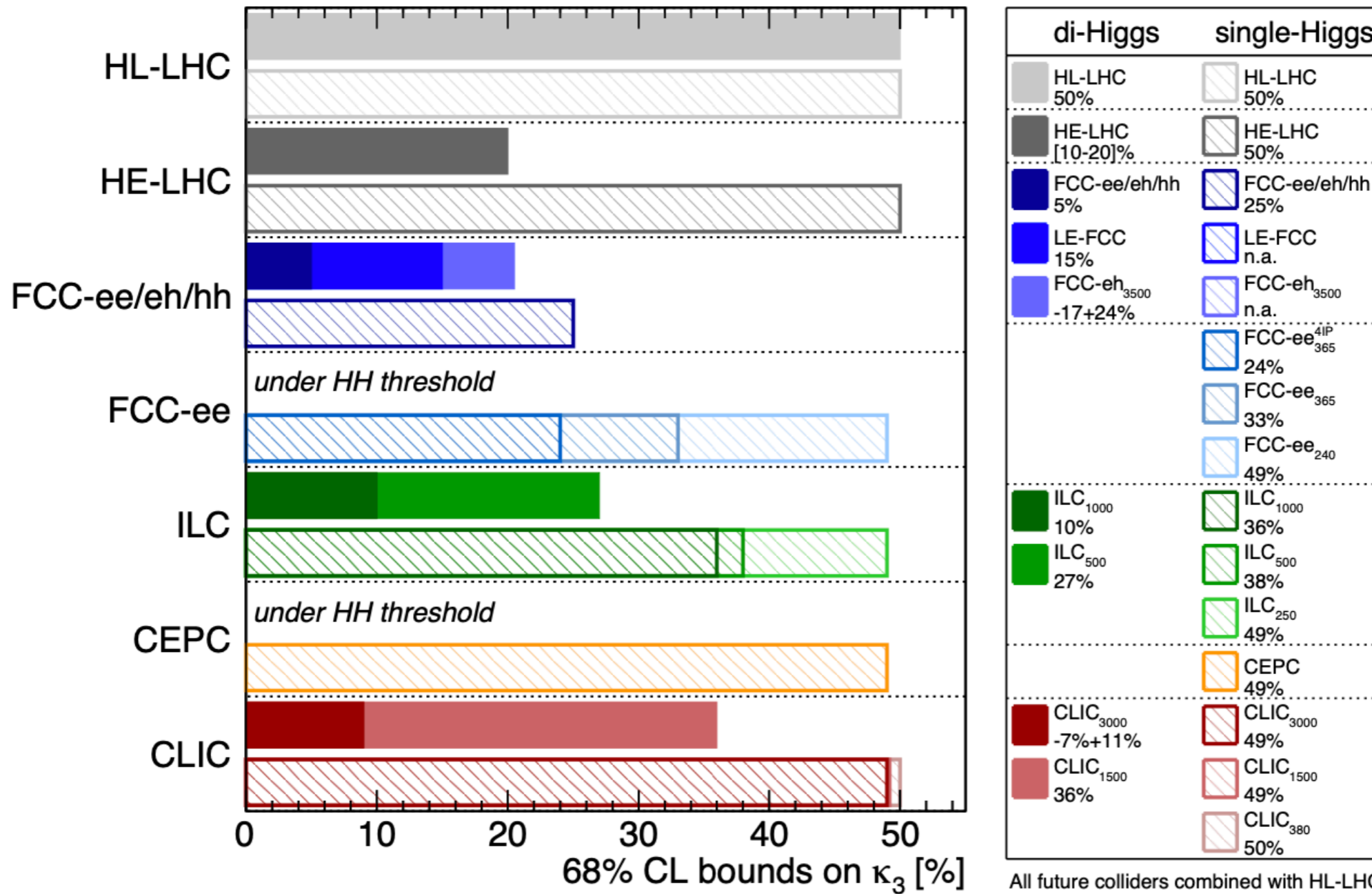
- constructive interference in ZHH, while destructive in $\nu\bar{\nu}HH$ (& LHC) \rightarrow complementarity between ILC & LHC, between $\sqrt{s} \sim 500$ GeV and >1 TeV
- if $\lambda_{HHH} / \lambda_{SM} = 2$, Higgs self-coupling can be measured to $\sim 15\%$ using ZHH at 500 GeV e^+e^-



Duerig, Tian, et al, paper in preparation

λ_{hhh} by double / single Higgs processes

Higgs@FC WG September 2019



(Physics Briefing Book, arXiv:1910.11775)

benchmark BSM models

Model	$b\bar{b}$	$c\bar{c}$	gg	WW	$\tau\tau$	ZZ	$\gamma\gamma$	$\mu\mu$
1 MSSM [34]	+4.8	-0.8	-0.8	-0.2	+0.4	-0.5	+0.1	+0.3
2 Type II 2HD [36]	+10.1	-0.2	-0.2	0.0	+9.8	0.0	+0.1	+9.8
3 Type X 2HD [36]	-0.2	-0.2	-0.2	0.0	+7.8	0.0	0.0	+7.8
4 Type Y 2HD [36]	+10.1	-0.2	-0.2	0.0	-0.2	0.0	0.1	-0.2
5 Composite Higgs [38]	-6.4	-6.4	-6.4	-2.1	-6.4	-2.1	-2.1	-6.4
6 Little Higgs w. T-parity [39]	0.0	0.0	-6.1	-2.5	0.0	-2.5	-1.5	0.0
7 Little Higgs w. T-parity [40]	-7.8	-4.6	-3.5	-1.5	-7.8	-1.5	-1.0	-7.8
8 Higgs-Radion [41]	-1.5	-1.5	10.	-1.5	-1.5	-1.5	-1.0	-1.5
9 Higgs Singlet [42]	-3.5	-3.5	-3.5	-3.5	-3.5	-3.5	-3.5	-3.5

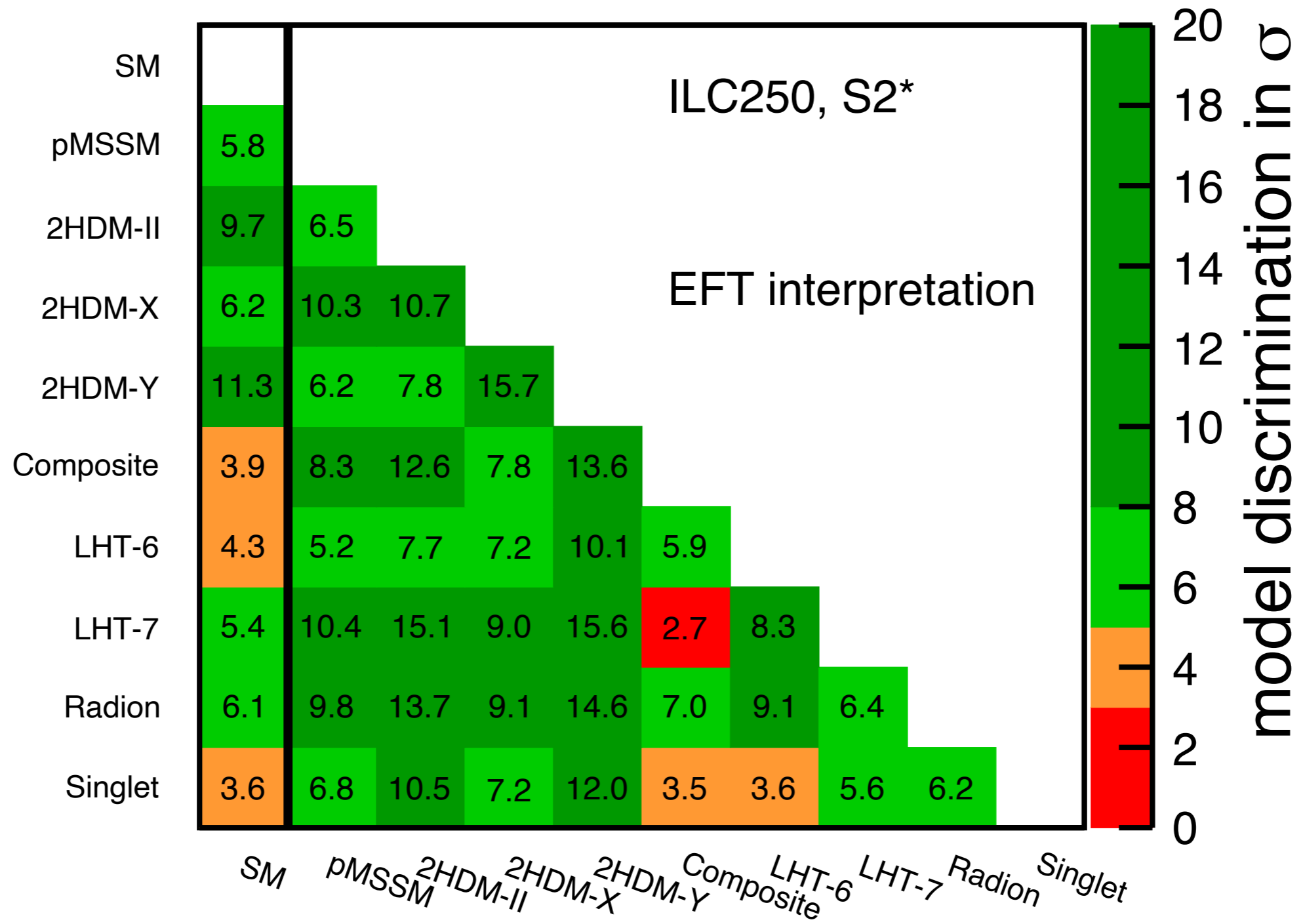
Table 4: Deviations from the Standard Model predictions for the Higgs boson couplings, in %, for the set of new physics models described in the text. As in Table 1, the effective couplings $g(hWW)$ and $g(hZZ)$ are defined as proportional to the square roots of the corresponding partial widths.

—> quantitative assessment for models discrimination

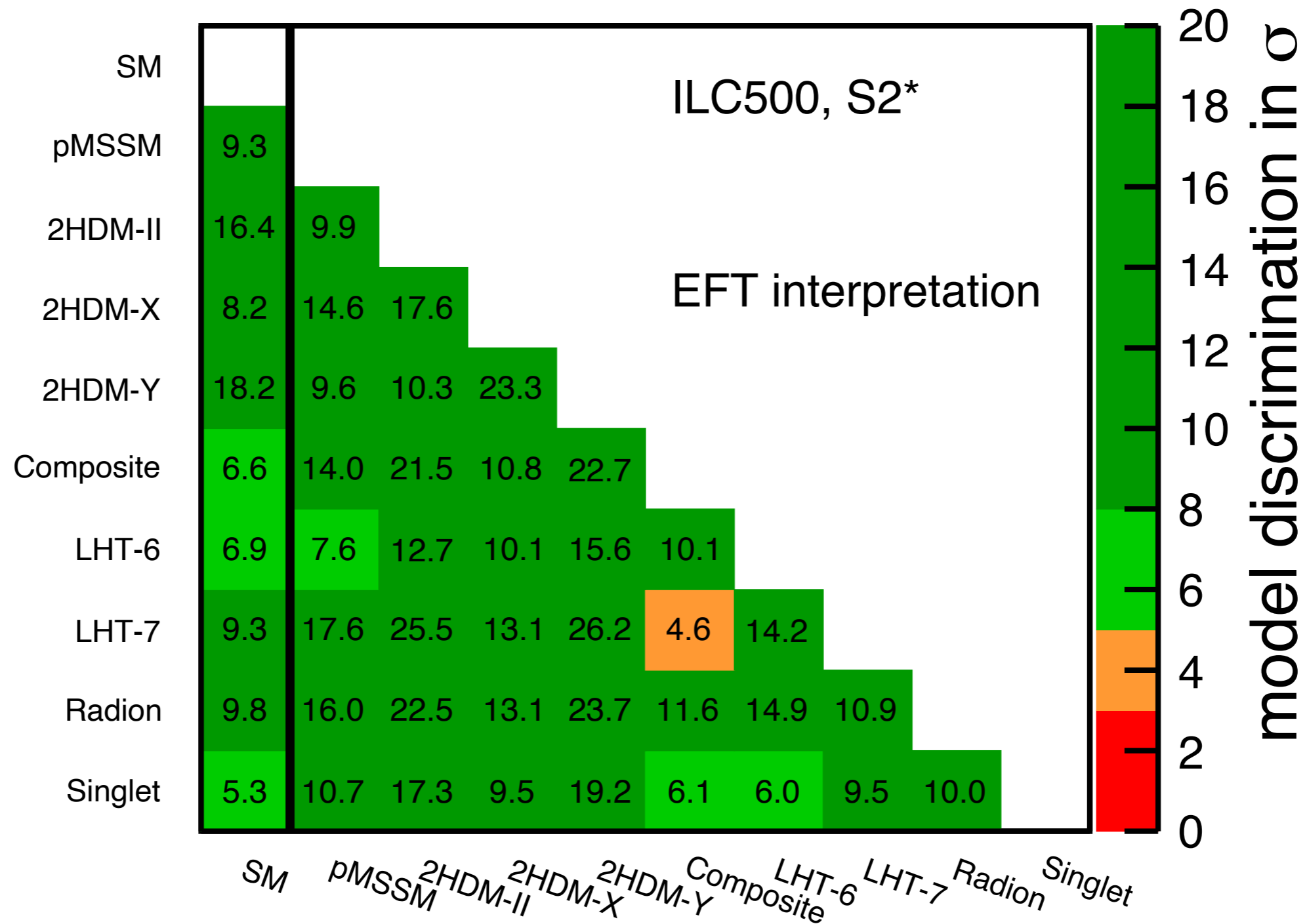
model parameters (chosen as escaping direct search at HL-LHC)

- a PMSSM model with b squarks at 3.4 TeV, gluino at 4 TeV
- a Type II 2 Higgs doublet model with $m_A = 600$ GeV, $\tan \beta = 7$
- a Type X 2 Higgs doublet model with $m_A = 450$ GeV, $\tan \beta = 6$
- a Type Y 2 Higgs doublet model with $m_A = 600$ GeV, $\tan \beta = 7$
- a composite Higgs model MCHM5 with $f = 1.2$ TeV, $m_T = 1.7$ TeV
- a Little Higgs model with T-parity with $f = 785$ GeV, $m_T = 2$ TeV
- A Little Higgs model with couplings to 1st and 2nd generation with $f = 1.2$ TeV, $m_T = 1.7$ TeV
- A Higgs-radion mixing model with $m_r = 500$ GeV
- a model with a Higgs singlet at 2.8 TeV creating a Higgs portal to dark matter and large λ for electroweak baryogenesis

BSM benchmark models discrimination at ILC250



effect of improvement from TGC, $\nu\nu H$, ZH at 500GeV



simplifications of our analysis

- at tree level, and to linear order in D-6 coefficients
- ignore some possible D-6 corrections involving light leptons, e.g. 4-fermion operators
- avoid using observables that involve contact interactions that include quark currents (see more later)
- ignore the effects of CP-violating operators

$$\begin{aligned}\Delta\mathcal{L}_{CP} = & +\frac{g^2\tilde{c}_{WW}}{m_W^2}\Phi^\dagger\Phi W_{\mu\nu}^a\tilde{W}^{a\mu\nu} + \frac{4gg'\tilde{c}_{WB}}{m_W^2}\Phi^\dagger t^a\Phi W_{\mu\nu}^a\tilde{B}^{\mu\nu} \\ & +\frac{g'^2\tilde{c}_{BB}}{m_W^2}\Phi^\dagger\Phi B_{\mu\nu}\tilde{B}^{\mu\nu} + \frac{g^3\tilde{c}_{3W}}{m_W^2}\epsilon_{abc}W_{\mu\nu}^aW^{b\nu}{}_{\rho}\tilde{W}^{c\rho\mu}\end{aligned}$$

on-shell renormalization

- D-6 operators modify the SM expressions for precision electroweak observables, thus shift the appropriate values for the SM couplings $\rightarrow g, g', v, \lambda$ free parameters
- D-6 operators also renormalize the kinetic terms of the SM fields \rightarrow rescale the boson fields

$$\mathcal{L} = -\frac{1}{2}W_{\mu\nu}^+W^{-\mu\nu} \cdot (1 - \delta Z_W) - \frac{1}{4}Z_{\mu\nu}Z^{\mu\nu} \cdot (1 - \delta Z_Z) \\ -\frac{1}{4}A_{\mu\nu}A^{\mu\nu} \cdot (1 - \delta Z_A) + \frac{1}{2}(\partial_\mu h)(\partial^\mu h) \cdot (1 - \delta Z_h) ,$$

with

$$\delta Z_W = (\delta c_{WW})$$

$$\delta Z_Z = c_w^2(\delta c_{WW}) + 2s_w^2(\delta c_{WB}) + s_w^4/c_w^2(\delta c_{BB})$$

$$\delta Z_A = s_w^2 \left((\delta c_{WW}) - 2(\delta c_{WB}) + (\delta c_{BB}) \right)$$

$$\delta Z_h = -c_H \quad .$$

$$\Delta\mathcal{L} = \frac{1}{2}\delta Z_{AZ} A_{\mu\nu}Z^{\mu\nu} , \quad \delta Z_{AZ} = s_w c_w \left((\delta c_{WW}) - \left(1 - \frac{s_w^2}{c_w^2}\right)(\delta c_{WB}) - \frac{s_w^2}{c_w^2}(\delta c_{BB}) \right)$$

systematic errors included in the global fit

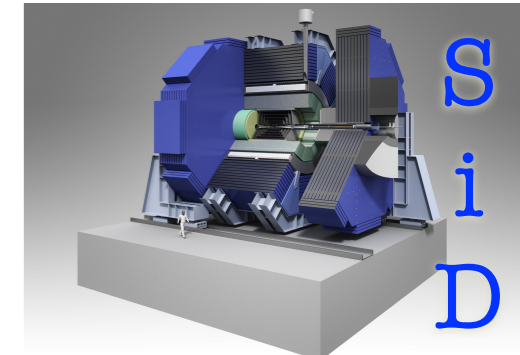
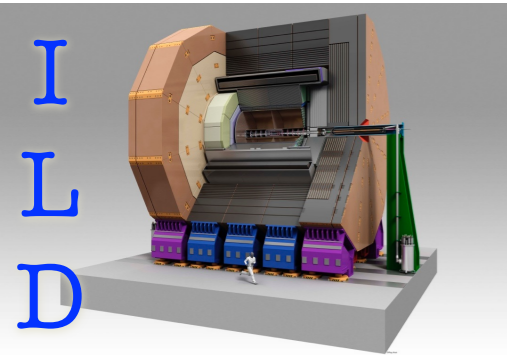
- 0.1% from theory computations
- 0.1% from luminosity
- 0.1% from beam polarizations
- $0.1\% \oplus 0.3\%/\sqrt{L/250}$ from b-tagging and analysis

improvement factors in S2

- 10% from better jet-clustering algorithm
- 20% from better flavor-tagging algorithm
- 20% from including more signal channels in $h \rightarrow WW^*$
- x10 better for A_{LR} using $e^+e^- \rightarrow \gamma Z$ at ILC250

expected meas. for direct observables

estimates at ILC by full simulation



-30% e^- , +30% e^+ polarization:

	250 GeV		350 GeV		500 GeV	
	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$
σ [50–53]	2.0		1.8		4.2	
$h \rightarrow invis.$ [54, 55]	0.86		1.4		3.4	
$h \rightarrow b\bar{b}$ [56–59]	1.3	8.1	1.5	1.8	2.5	0.93
$h \rightarrow c\bar{c}$ [56, 57]	8.3		11	19	18	8.8
$h \rightarrow gg$ [56, 57]	7.0		8.4	7.7	15	5.8
$h \rightarrow WW$ [59–61]	4.6		5.6 *	5.7 *	7.7	3.4
$h \rightarrow \tau\tau$ [63]	3.2		4.0 *	16 *	6.1	9.8
$h \rightarrow ZZ$ [2]	18		25 *	20 *	35 *	12 *
$h \rightarrow \gamma\gamma$ [64]	34 *		39 *	45 *	47	27
$h \rightarrow \mu\mu$ [65, 66]	72 *		87 *	160 *	120 *	100 *
a [27]	7.6		2.7 *		4.0	
b	2.7		0.69 *		0.70	
$\rho(a, b)$	-99.17		-95.6 *		-84.8	

(arXiv: 1708.08912; numbers are in %, for nominal $\int L dt = 250 \text{ fb}^{-1}$)

EFT input from TGCs in $e^+e^- \rightarrow W^+W^-$

	250 GeV W^+W^-	350 GeV W^+W^-	500 GeV W^+W^-
g_{1Z}	0.062 *	0.033 *	0.025
κ_A	0.096 *	0.049 *	0.034
λ_A	0.077 *	0.047 *	0.037
$\rho(g_{1Z}, \kappa_A)$	63.4 *	63.4 *	63.4
$\rho(g_{1Z}, \lambda_A)$	47.7 *	47.7 *	47.7
$\rho(\kappa_A, \lambda_A)$	35.4 *	35.4 *	35.4

(arXiv: 1708.08912; numbers are in %, for nominal $\int L dt = 500 \text{ fb}^{-1}$ shared equally by left-/right- polarized data)

EFT input: EWPOs

Observable	current value	current σ	future σ	SM best fit value
$\alpha^{-1}(m_Z^2)$	128.9220	0.0178		(same)
G_F (10^{-10} GeV $^{-2}$)	1166378.7	0.6		(same)
m_W (MeV)	80385	15	5	80361
m_Z (MeV)	91187.6	2.1		91188.0
m_h (MeV)	125090	240	15	125110
A_ℓ	0.14696	0.0013		0.147937
Γ_ℓ (MeV)	83.984	0.086		83.995
Γ_Z (MeV)	2495.2	2.3		2494.3
Γ_W (MeV)	2085	42	2	2088.8

EFT input: EWPOs (7)

$$\underline{\alpha(m_Z), G_F, m_W, m_Z, m_h, A_{LR}(\ell), \Gamma(Z \rightarrow \ell^+ \ell^-)}$$

$$\delta e = \delta(4\pi\alpha(m_Z^2))^{1/2} = s_w^2 \delta g + c_w^2 \delta g' + \frac{1}{2} \delta Z_A$$

$$\delta G_F = -2\delta v + 2c'_{HL}$$

$$\delta m_W = \delta g + \delta v + \frac{1}{2} \delta Z_W$$

$$\delta m_Z = c_w^2 \delta g + s_w^2 \delta g' + \delta v - \frac{1}{2} c_T + \frac{1}{2} \delta Z_Z$$

$$\delta m_h = \frac{1}{2} \delta \bar{\lambda} + \delta v + \frac{1}{2} \delta Z_h$$

$$(\delta X = \Delta X / X)$$

$$\bar{\lambda} = \lambda(1 + \frac{3}{2} c_6)$$

$$s_w^2 = \sin^2 \theta_w = \frac{g'^2}{g^2 + g'^2}$$

$$c_w^2 = \cos^2 \theta_w = \frac{g^2}{g^2 + g'^2}$$

$$\longrightarrow \delta g, \delta g', \delta v, \delta \lambda, c_T$$

EFT input: EWPOs (7)

$$\alpha(m_Z), G_F, m_W, m_Z, m_h, \underline{A_{LR}(\ell), \Gamma(Z \rightarrow \ell^+ \ell^-)}$$

$$\delta\Gamma_\ell = \delta m_Z + 2 \frac{g_L^2 \delta g_L + g_R^2 \delta g_R}{g_L^2 + g_R^2}$$

$$\delta A_\ell = \frac{4g_L^2 g_R^2 (\delta g_L - \delta g_R)}{g_L^4 - g_R^4}$$

$$g_L = \frac{g}{c_w} \left[\left(-\frac{1}{2} + s_w^2\right) \left(1 + \frac{1}{2} \delta Z_Z\right) - \frac{1}{2} (c_{HL} + c'_{HL}) - s_w c_w \delta Z_{AZ} \right]$$

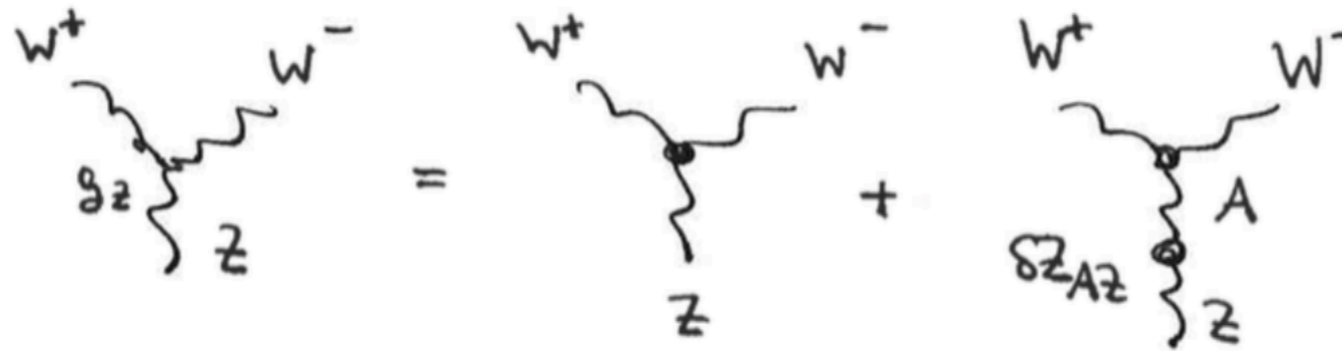
$$g_R = \frac{g}{c_w} \left[\left(+s_w^2\right) \left(1 + \frac{1}{2} \delta Z_Z\right) - \frac{1}{2} c_{HE} - s_w c_w \delta Z_{AZ} \right]$$



CHL + C'HL, CHE

EFT input: TGC (3)

$$\Delta\mathcal{L}_{TGC} = ig_V \left\{ V^\mu (\hat{W}_{\mu\nu}^- W^{+\nu} - \hat{W}_{\mu\nu}^+ W^{-\nu}) + \kappa_V W_\mu^+ W_\nu^- \hat{V}^{\mu\nu} + \frac{\lambda_V}{m_W^2} \hat{W}_\mu^-{}^\rho \hat{W}_\rho^+ \hat{V}^{\mu\nu} \right\}$$

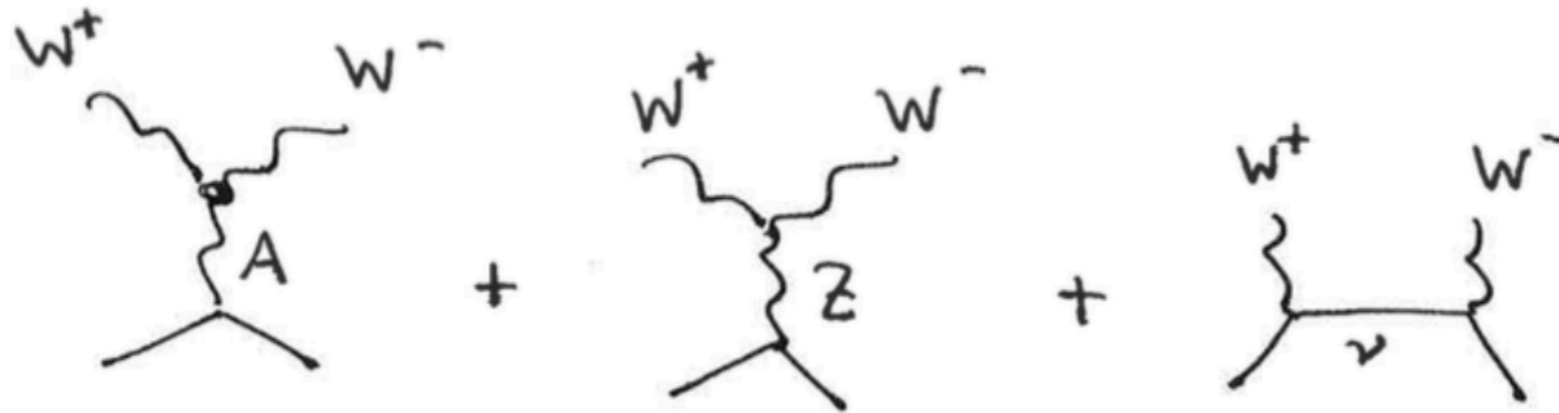


$$g_Z = g c_w \left(1 + \frac{1}{2} \delta Z_Z + \frac{s_w}{c_w} \delta Z_{AZ} \right)$$

$$\kappa_A = 1 + (\delta c_{WB})$$

$$\lambda_A = -6g^2 c_{3W}$$

EFT input: TGC (3)



$$\delta g_{Z,eff} = \delta g_Z + \frac{1}{c_w^2} ((c_w^2 - s_w^2) \delta g_L + s_w^2 \delta g_R - 2\delta g_W)$$

$$\delta \kappa_{A,eff} = (c_w^2 - s_w^2) (\delta g_L - \delta g_R) + 2(\delta e - \delta g_W) + (8c_{WB})$$

$$\delta \lambda_{A,eff} = -6g^2 c_{3W}$$

$$g_W = g \left(1 + c'_{HL} + \frac{1}{2} \delta Z_W \right)$$

EFT input: $\text{BR}(h \rightarrow \gamma\gamma)/\text{BR}(h \rightarrow ZZ^*)$, $\text{BR}(h \rightarrow \gamma Z)/\text{BR}(h \rightarrow ZZ^*)$

(2: HL-LHC)

$$\delta\Gamma(h \rightarrow \gamma\gamma) = 528 \delta Z_A - c_H + 4\delta e + 4.2 \delta m_h - 1.3 \delta m_W - 2\delta v$$

$$\begin{aligned} \delta\Gamma(h \rightarrow Z\gamma) = & 290 \delta Z_{AZ} - c_H - 2(1 - 3s_W^2)\delta g + 6c_w^2 \delta g' + \delta Z_A + \delta Z_Z \\ & + 9.6 \delta m_h - 6.5 \delta m_Z - 2\delta v \end{aligned}$$

$$\delta\Gamma(h \rightarrow ZZ^*) = 2\eta_Z - 2\delta v - 13.8\delta m_Z + 15.6\delta m_h - 0.50\delta Z_Z - 1.02C_Z + 1.18\delta\Gamma_Z$$

$$\delta Z_A = s_w^2 \left((\delta c_{WW}) - 2(\delta c_{WB}) + (\delta c_{BB}) \right) \quad \delta Z_{AZ} = s_w c_w \left((\delta c_{WW}) - \left(1 - \frac{s_w^2}{c_w^2}\right) (\delta c_{WB}) - \frac{s_w^2}{c_w^2} (\delta c_{BB}) \right)$$

EFT coefficients

10: $C_H, C_T, C_6, C_{WW}, C_{WB}, C_{BB}, C_{3W}, C_{HL}, C'_{HL}, C_{HE}$
+ 4: g, g', v, λ

can already be determined,
except C_6, C_H

—> Higgs observables @ e^+e^-

EFT input: $\sigma(e^+e^- \rightarrow Zh)$, $\sigma(e^+e^- \rightarrow Zhh)$

- c_H has to be determined by inclusive σ_{Zh} measurement
- c_6 has to be determined by double Higgs measurement

EFT input: $BR(h \rightarrow XX)$

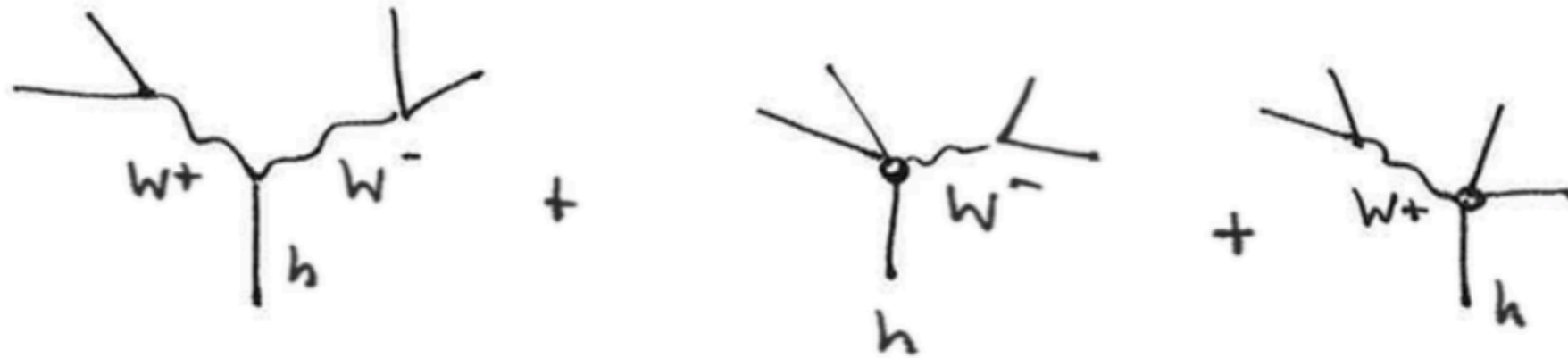
$$\Delta\mathcal{L} = -c_{\tau\Phi} \frac{y_\tau}{v^2} (\Phi^\dagger\Phi) \bar{L}_3 \cdot \Phi \tau_R + h.c.$$

- h couplings to b, c, τ, μ, g
- $\Gamma(h \rightarrow \text{invisible})$, total decay width

$$\delta\mathcal{L} = \mathcal{A} \frac{h}{v} G_{\mu\nu} G^{\mu\nu}$$

note: beam polarizations provide several independent (redundant) set of $\sigma, \sigma \times BR$ input, which are powerful to test EFT validity

two more parameters: C_W , C_Z for $\Gamma(h \rightarrow WW^*)$ and $\Gamma(h \rightarrow ZZ^*)$



$$\Gamma/(SM) = 1 + 2\eta_W - 2\delta v - 11.7\delta m_W + 13.6\delta m_h - 0.75\zeta_W - 0.88C_W + 1.06\delta\Gamma_W ,$$

$$C_W = \sum_X c'_X \mathcal{N}_X / \sum_X \mathcal{N}_X ,$$

(c'_X : contact interactions)

EFT input:
$$\Gamma_W = \frac{g^2 m_W}{48\pi} \left(\sum_X \mathcal{N}_X \right) \cdot (1 + 2\delta g + \delta m_W + \delta Z_W + 2C_W)$$

(similar for Z)