

Exploring new physics by loop-corrected decays of additional Higgs bosons

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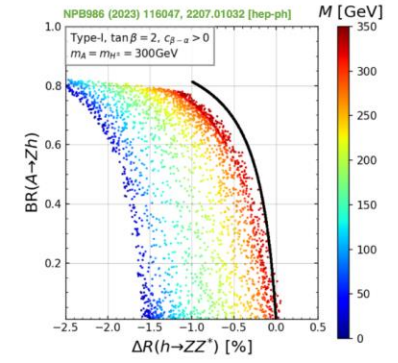
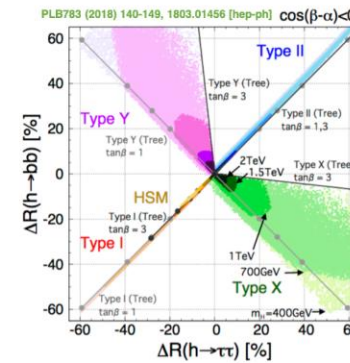
Kei Yagyu (Osaka U.)

Comput.Phys.Commun. 301 (2024) 109231



H-COUP

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<http://www-het.phys.sci.osaka-u.ac.jp/~hcoup/>

What do we want to know?

What kinds of Higgs fields are in the Higgs sector?

Decoupling?
or
non-decoupling?

Additional symmetries

$\rho_{EW} = 1 ?$

Why is FCNC suppressed?

Additional CP phases

- How much is “alignmentness” ?

$$g_{hXX} = \kappa_X g_{hXX}^{\text{SM}}$$

$\kappa_X \rightarrow 1$ (Alignment limit)

- The mass scale of the 2nd Higgs boson
Decoupling ? or Non-decoupling?

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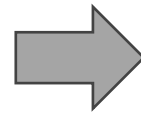
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Additional CP phases

- How much is “alignmentness” ?

$$g_{hXX} = \kappa_X g_{hXX}^{\text{SM}}$$

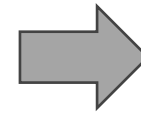
$\kappa_X \rightarrow 1$ (Alignment limit)



LHC results are consistent with SM predictions.

$\kappa_X \simeq 1$ (Nearly alignment)

- The mass scale of the 2nd Higgs boson
Decoupling ? or Non-decoupling?



Unknown.

No new particle has been discovered.

It does not mean decoupling scenario.

⇒ Direct search of additional Higgs bosons remains an important exploring method.

Two Higgs doublet models

We investigate additional Higgs boson decays for direct searches.

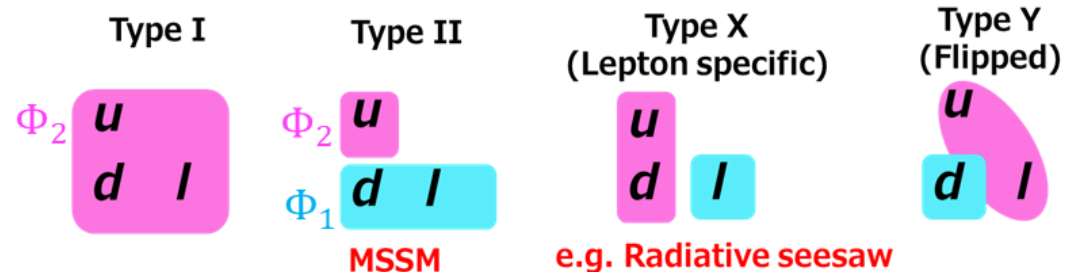
- We show analyses of THDM with the softly broken Z_2 symmetry as an example.

$$\Phi_1 \rightarrow + \Phi_1$$

$$\Phi_2 \rightarrow - \Phi_2$$

Can avoid FCNC.

4 types of Yukawa interactions \Rightarrow



- We focus on the CP-conserving case.
- Mass eigenstates

Higgs basis

$$\Phi = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(h'_1 + v + iG^0) \end{pmatrix} \quad \Phi' = \begin{pmatrix} h_{125}, H, A, H^\pm \\ \frac{1}{\sqrt{2}}(h'_2 + iA) \end{pmatrix} \quad \begin{pmatrix} h'_1 \\ h'_2 \end{pmatrix} = \begin{pmatrix} \cos(\beta - \alpha) & \sin(\beta - \alpha) \\ -\sin(\beta - \alpha) & \cos(\beta - \alpha) \end{pmatrix} \begin{pmatrix} H \\ h \end{pmatrix}$$

- h_{125} couplings

h_{WW}, h_{ZZ}

$$\kappa_V^h = \frac{g_{hVV}^{\text{THDM}}}{g_{hVV}^{\text{SM}}} = \sin(\beta - \alpha) \quad \text{Alignment limit} \rightarrow 1$$

How to Search Additional Higgs

In nearly alignment case, additional Higgs bosons' decays are very interesting !!

- Additional Higgs couplings with SM particles

THDM
Type-I

HWW, HZZ

$$\kappa_V^H = \frac{g_{HVV}^{NP}}{g_{hVV}^{SM}} = \cos(\beta - \alpha)$$

Alignment limit

$\rightarrow 0$

Hhh

$$\lambda_{Hhh} = -\frac{\cos(\beta - \alpha)}{2v \sin 2\beta} \{ (2m_h^2 + m_H^2 - 3M^2) \sin 2\alpha + M^2 \sin 2\beta \} \rightarrow 0$$

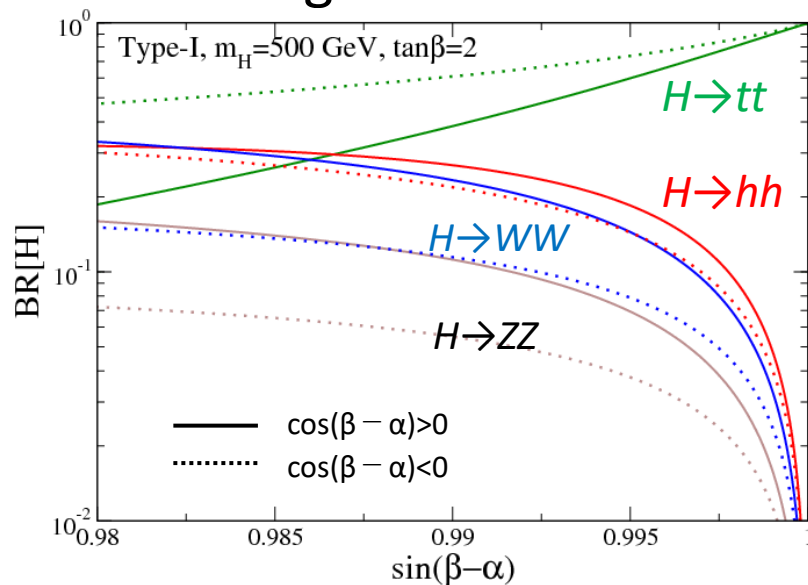
In the nearly-alignment case they play important roles

Hff

Type-I THDM

$$\kappa_f^H = \cos(\beta - \alpha) - \cot \beta \sin(\beta - \alpha) \rightarrow -\cot \beta$$

- Branching ratio of H



H decays are very sensitive to $\kappa_V^{\text{tree}} = \sin(\beta - \alpha)$.

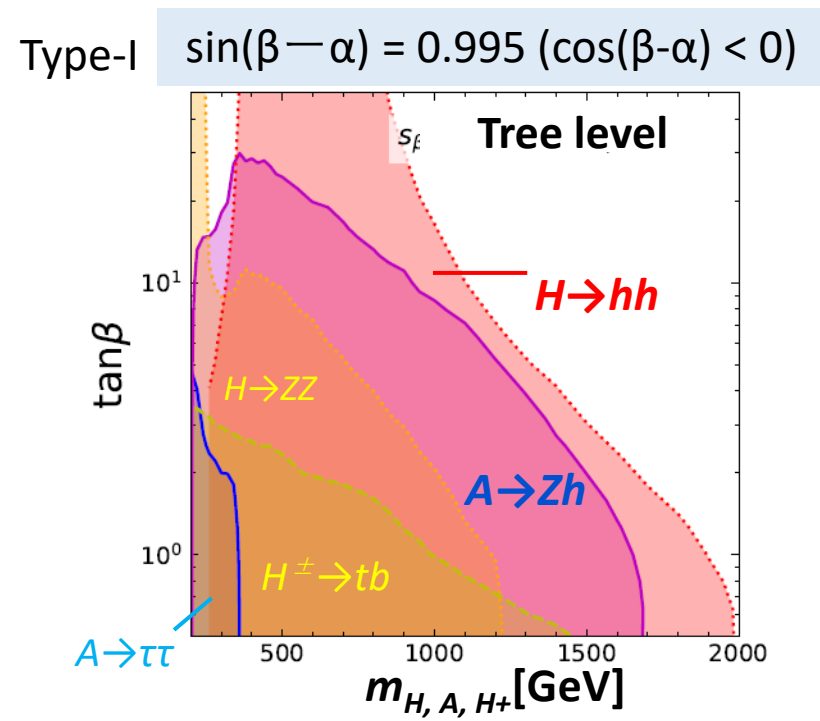
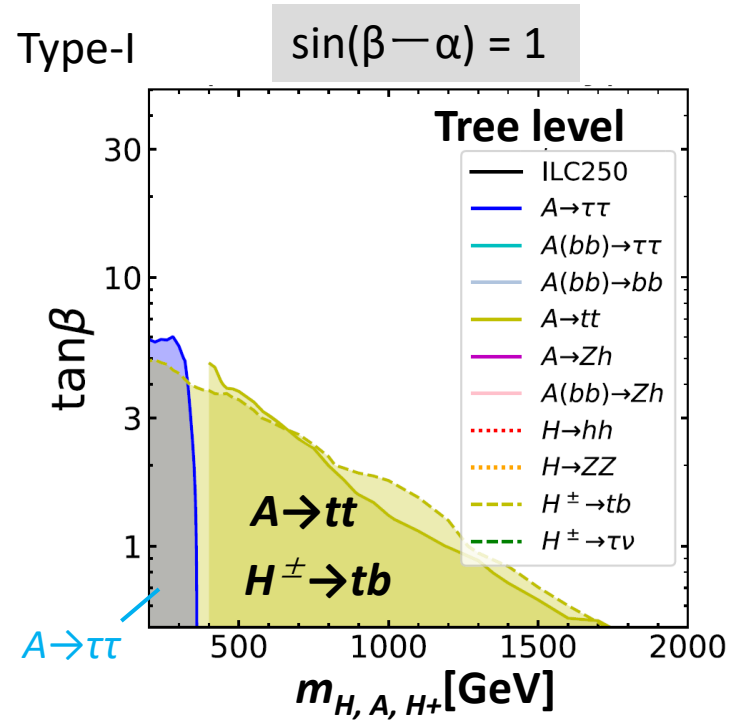


Roughly, $\sin(\beta - \alpha)$ can be determined by h_{125} -coupling measurements.

It is important to evaluate h_{125} -couplings and/or decays at the same time.

Searchable regions in nearly-alignment

Expected excluded parameter region by direct searches @HL-LHC(3000fb⁻¹) (95%CL)



Aiko, Kanemura, MK, Mawatari,
Sakurai, Yagyu
[NPB966(2021)115375]

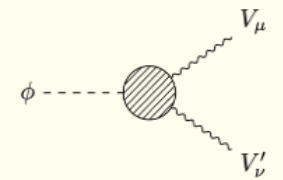
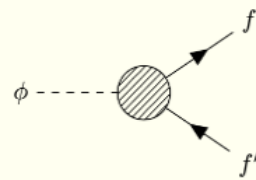
- Wide parameter region is expected to be surveyed by “Higgs to Higgs decays”.
- Additional Higgs decays are very sensitive to $\sin(\beta - \alpha)$.

They are results at tree level.

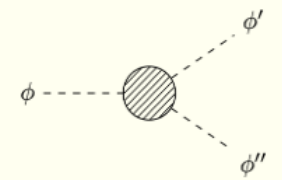
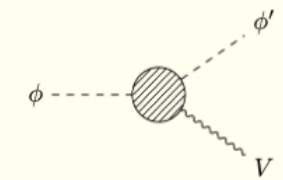


Precise calculation is necessary for both h_{125} -decays and additional Higgs decays.

We evaluate the correlations with loop corrections by using H-COUP!



H-COUP



Fortran program for **decay BRs** of **Higgs bosons** with **loop corrections** in **extended Higgs models**.

You can obtain H-COUP at \Rightarrow <http://www-het.phys.sci.osaka-u.ac.jp/~hcoup/>

【Characteristics of H-COUP】

- **Various extended Higgs models** : Higgs singlet model, THDMs (Type-I, II, X, Y) , Inert doublet model

- **Full set of decay processes** of **all Higgs bosons**:

Ver.1 (2017) : Renormalized vertices of h_{125} .

Kanemura, MK, Sakurai, Yagyu, CPC.233(2018)134

Ver.2 (2019) : Two- and Three-body decays of h_{125} .

Kanemura, MK, Mawatari, Sakurai, Yagyu, CPC 257(2020) 107512

Ver.3 (2023) : **Two-body decays of additional Higgs bosons (H, A, H^\pm)**

Aiko, Kanemura, MK, Sakurai, Yagyu, CPC 301 (2024) 109231

\Rightarrow Evaluate correlations between behavior of various decay processes.

- **Loop corrections** : EW and scalar-NLO

*New renormalization scheme
Yagyu's talk (Wed.)*

- UV div. \rightarrow On-shell renormalizations
- Gauge dependence \rightarrow Remove by Pinch technique
- IR div. via photon loop \rightarrow Cancel by real photon emission

QCD (NNLO, NLO) corrections (\overline{MS} -bar scheme).

A. Djouadi, Phys. Rept., 457, 1 (2008),
B. M. Spira, Prog. Part. Nucl. Phys., 95, 98 (2017),
K. G. Chetyrkin, A. Kwiatkowski, Nucl. Phys., B461, 3 (1996)

- **Constraints** : Vacuum stability(tree level, RGE improved), Tree-level unitarity, Triviality, True vacuum, ST parameters

Processes in THDMs

CP-even	CP-odd	Charged
$H \rightarrow VV$	$A \rightarrow ff$	$H^\pm \rightarrow ff'$
$H \rightarrow ff$	$A \rightarrow Zh, ZH$	$H^\pm \rightarrow AW$
$H \rightarrow hh$	$A \rightarrow H^\pm W$	$H^\pm \rightarrow HW, hW$
$H \rightarrow AA, H^+H^-$	$A \rightarrow ZZ, WW, \gamma\gamma, \gamma Z$	$H^\pm \rightarrow W\gamma, WZ$
$H \rightarrow AZ, H^\pm W$		
$H \rightarrow \gamma\gamma, \gamma Z, gg$		

NPB 973 (2021) 115581, Aiko, Kanemura, Sakurai

NPB 983(2022)115906 Kanemura, MK, Yagyu

NPB 986 (2023) 116047 Aiko, Kanemura, Sakurai,

IDM

CP-even	CP-odd	Charged
$H \rightarrow AZ$	$A \rightarrow ZH$	$H^\pm \rightarrow AW$
$H \rightarrow H^\pm W$	$A \rightarrow H^\pm W$	$H^\pm \rightarrow HW$

HSM

CP-even
$H \rightarrow VV$
$H \rightarrow ff$
$H \rightarrow hh$
$H \rightarrow \gamma\gamma, \gamma Z, gg$

We show results for decays of $H \rightarrow hh, A \rightarrow Zh, h \rightarrow VV^*$ in Type-I THDM.

Loop corrections to $\Gamma[H \rightarrow hh]$

- NLO contributions works constructively or destructively
 $\cos(\beta - \alpha) > 0$ · · · constructively, $\cos(\beta - \alpha) < 0$ · · · destructively

$$\Gamma_{\text{NLO}}[H \rightarrow hh] = \left| \begin{array}{c} \cos(\beta - \alpha) \\ \text{---} \bullet \text{---} \\ \text{---} \end{array} \right|^2 + 2\text{Re} \left[\text{---} \bigcirc \text{---} \times \begin{array}{c} \cos(\beta - \alpha) \\ \text{---} \bullet \text{---} \\ \text{---} \end{array} \right]$$

- Decoupling? Or Non-decoupling?

$$M^2 \gg \lambda_{\Phi} v^2 \quad (m_{\Phi}^2 \simeq M^2) \quad \cdot \cdot \cdot \quad \text{Decoupling}$$

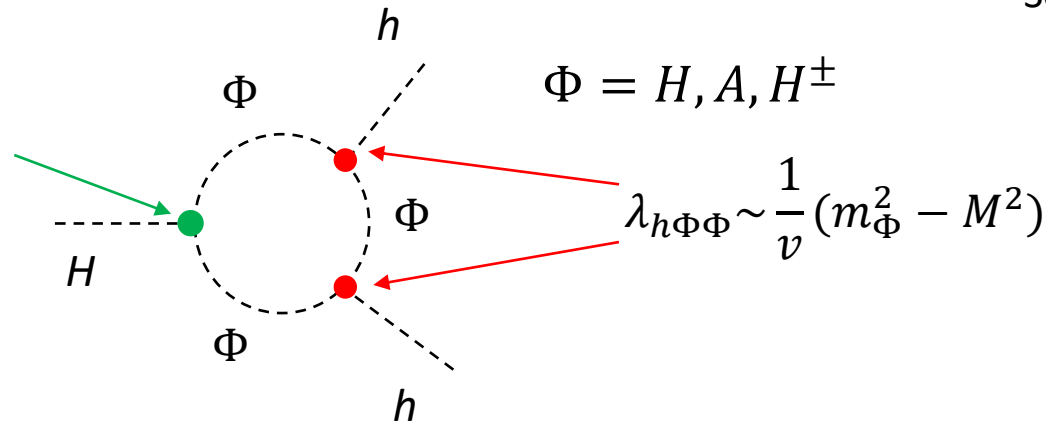
$$M^2 \simeq \lambda_{\Phi} v^2 \quad \cdot \cdot \cdot \quad \text{Non-decoupling}$$

$$m_{\Phi}^2 \simeq \lambda_{\Phi} v^2 + M^2$$

↑
Scalar self couplings

$\cos(\beta - \alpha) \ll 1$ case

$$\lambda_{H\Phi\Phi} \sim \frac{1}{v} (m_H^2 - M^2)$$



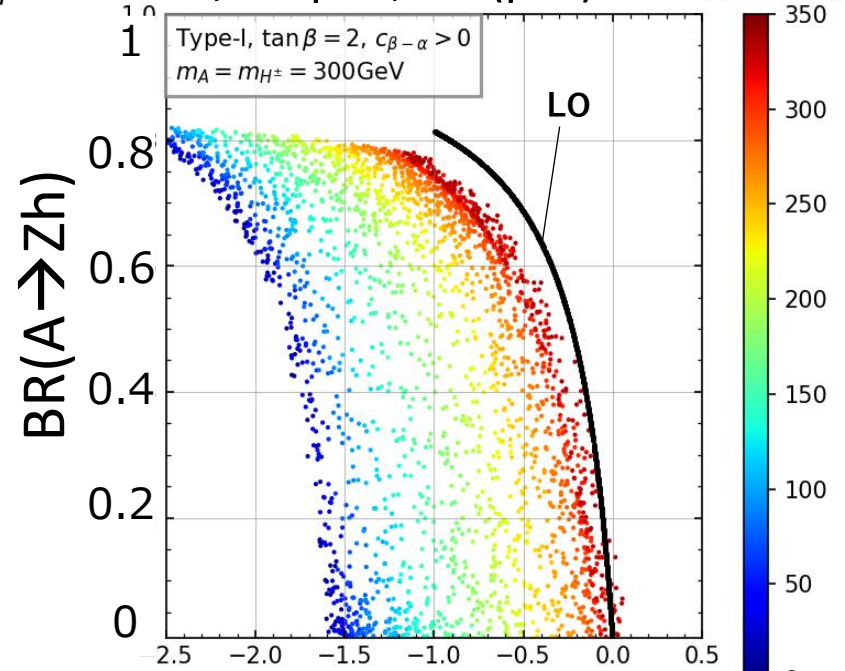
$(m_{A, H^{\pm}} - m_H \neq 0)$ case

Even if $m_H^2 \simeq M^2$, corrections of H^{\pm}, A loop diagrams are not suppressed.

Correlation between “Higgs to Higgs decays” and $h_{125} \rightarrow VV^*$

Type-I

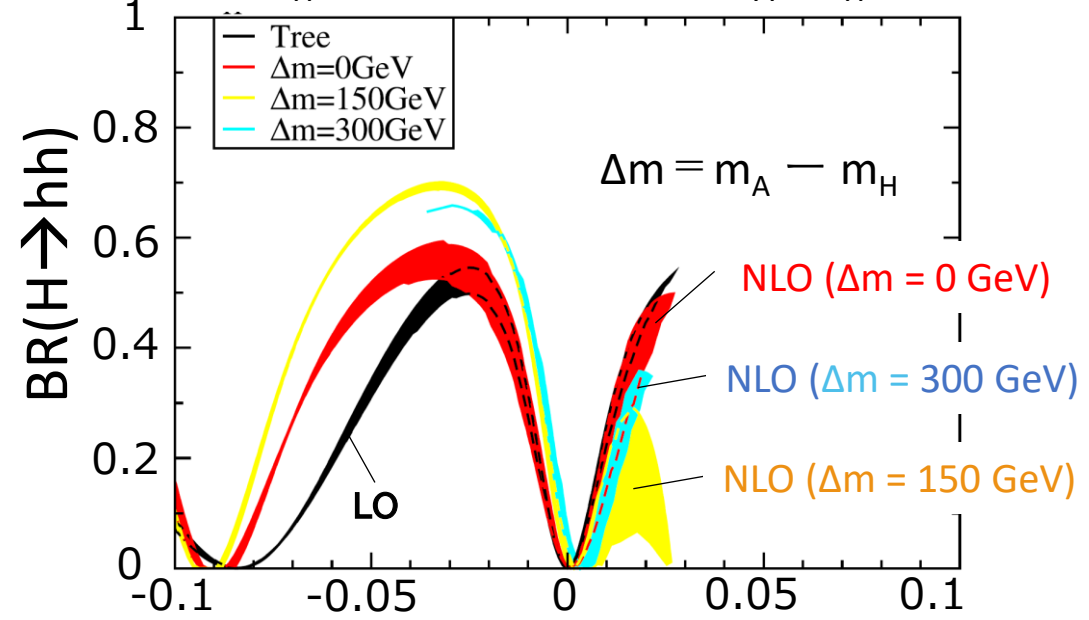
$m_A = m_{H^\pm} = 300 \text{ GeV}, \tan\beta = 2, \cos(\beta - \alpha) > 0$ $M [\text{GeV}]$



$$\Delta R[h_{125} \rightarrow ZZ^*] = \frac{\Gamma_{\text{NLO}}^{\text{THDM}}[h_{125} \rightarrow ZZ^*]}{\Gamma_{\text{NLO}}^{\text{SM}}[h_{125} \rightarrow ZZ^*]} - 1$$

NPB 986 (2023) 116047
Aiko, Kanemura, Sakurai

$m_H = 500 \text{ GeV}, \tan\beta = 5, m_A = m_{H^\pm}$



$$\Delta\mu[h_{125} \rightarrow WW^*] = \frac{\text{BR}_{\text{NLO}}^{\text{THDM}}[h_{125} \rightarrow WW^*]}{\text{BR}_{\text{NLO}}^{\text{SM}}[h_{125} \rightarrow WW^*]} - 1$$

NPB 983(2022)115906
Kanemura, MK, Yagyu

Correlations between “Higgs to Higgs decays” and $h_{125} \rightarrow VV^*$ are significantly changed from LO ($\sim O(10)\%$).

It is necessary to evaluate both h_{125} -decays and Heavy Higgs decays with loop corrections simultaneously.

Summary

- H-COUP is a good tool for determining the Higgs sector by comparing precise predictions of various processes in some extended Higgs models and future precision measurement.
- h_{125} measurements indicate “nearly alignment”.
 ⇒ “Higgs to Higgs decays” can be main search modes.
- We show results of BR[Higgs to Higgs decays] and BR[h_{125}] including radiative corrections in Type-I THDM.
 - BR[$H \rightarrow hh$] with NLO correction can change LO prediction by O(10)%.
 - BR[$A \rightarrow Zh$] also receives O(10)% correction if $\tan\beta \simeq 2$.
- Correlations between $A \rightarrow Zh / H \rightarrow hh$ and $h \rightarrow VV^*$ significantly change from LO.

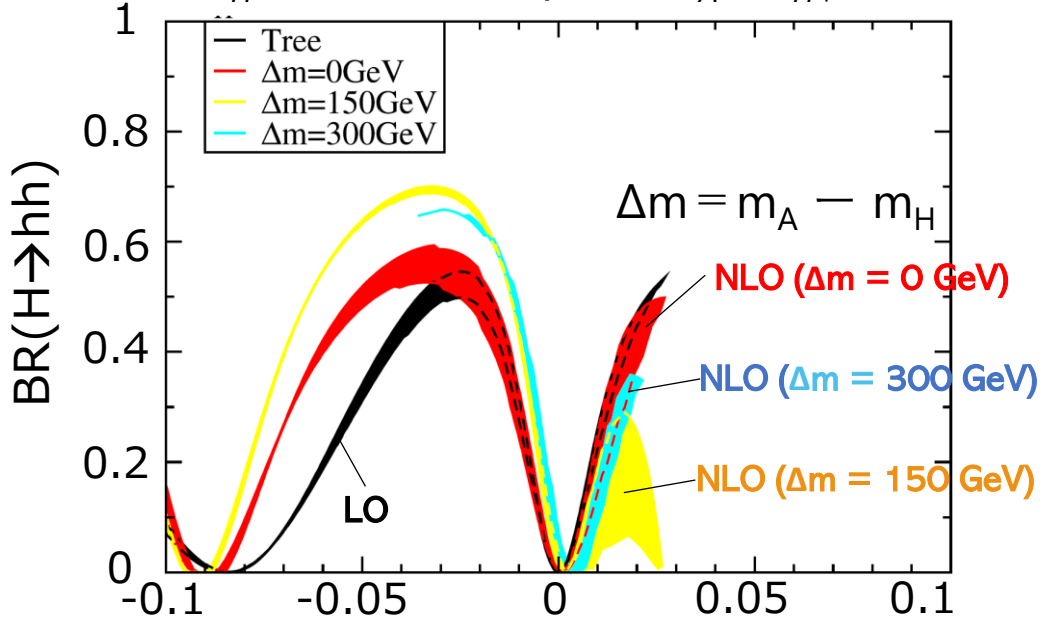


Correlation between $H \rightarrow hh$ and $h \rightarrow WW^*$

NPB 983(2022)115906
Kanemura, MK, Yagyu

Type-I

$m_H = 500 \text{ GeV}, \tan\beta = 5, m_A = m_{H^\pm}$



$$\Delta\mu[h \rightarrow WW^*] = \frac{\text{BR}_{\text{NLO}}^{\text{THDM}}[h \rightarrow WW^*]}{\text{BR}_{\text{NLO}}^{\text{SM}}[h \rightarrow WW^*]} - 1$$

$$\Gamma_{\text{LO}}^{\text{THDM}}[h \rightarrow WW^*] \propto \sin^2(\beta - \alpha)$$

$$\Rightarrow \Gamma^{\text{THDM}}[h \rightarrow WW^*] \lesssim \Gamma^{\text{SM}}[h \rightarrow WW^*]$$

$$\text{If } \cos(\beta - \alpha) > 0 \dots \Gamma_{h,\text{total}}^{\text{THDM}} > \Gamma_{h,\text{total}}^{\text{SM}}$$

$$\text{If } \cos(\beta - \alpha) < 0 \dots \Gamma_{h,\text{total}}^{\text{THDM}} < \Gamma_{h,\text{total}}^{\text{SM}}$$

\Rightarrow Decrease in $\Gamma_{\text{partial}}^{\text{THDM}}$ is canceled by decrease in $\Gamma_{h,\text{total}}^{\text{THDM}}$.

Correlation between $\text{BR}(H \rightarrow hh)$ and $\text{BR}(h \rightarrow WW^*)$ is changed from LO by $O(10)\%$.

It is important to evaluate both h -decays and H -decays with loop corrections simultaneously.

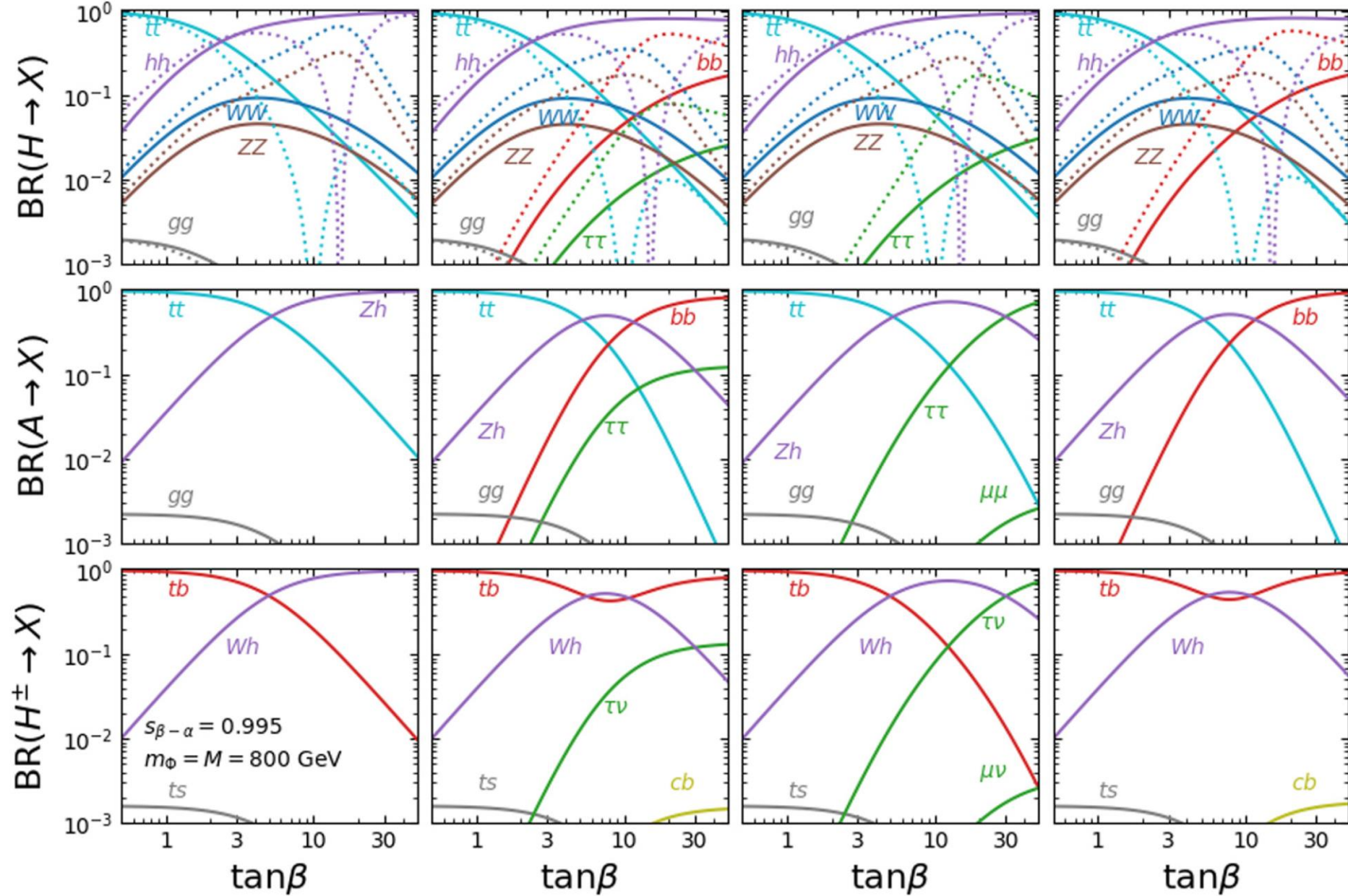


Fig. 5. Decay branching ratios for h , H , A and H^\pm as a function of $\tan\beta$ in the case of $m_\Phi = M = 800$ GeV and $s_{\beta-\alpha} = 0.995$. Solid lines show results of $c_{\beta-\alpha} < 0$ and dotted lines are those of $c_{\beta-\alpha} > 0$. Results for Type-I, Type-II, Type-X and Type-Y of the THDM are shown from the left panels to the right panels.

Expected uncertainties of $\sigma \times BR$ at ILC

ILC250 with 2 at⁻¹ total integrated luminosity

[arXiv:2203.07622](https://arxiv.org/abs/2203.07622) (Snowmass report2021)

$\sigma_{Zh} \times BR(h \rightarrow bb)$	0.7%
$\sigma_{Zh} \times BR(h \rightarrow cc, gg)$	4%
$\sigma_{Zh} \times BR(h \rightarrow \tau\tau)$	2%
$\sigma_{Zh} \times BR(h \rightarrow \mu\mu)$	38%
$\sigma_{Zh} \times BR(h \rightarrow ZZ)$	8%
$\sigma_{Zh} \times BR(h \rightarrow WW)$	2.4%

Table 2.4. Expected accuracies for cross section times branching ratio measurements for the 125 GeV h boson.

ILC TDR (2013)

\sqrt{s} and \mathcal{L} (P_{e-}, P_{e+})	$\Delta(\sigma \cdot BR)/(\sigma \cdot BR)$				
	250 fb ⁻¹ at 250 GeV (-0.8, +0.3)		500 fb ⁻¹ at 500 GeV (-0.8, +0.3)		1 ab ⁻¹ at 1 TeV (-0.8, +0.2)
mode	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$	$\nu\bar{\nu}h$
$h \rightarrow b\bar{b}$	1.1%	10.5%	1.8%	0.66%	0.47%
$h \rightarrow c\bar{c}$	7.4%	-	12%	6.2%	7.6%
$h \rightarrow gg$	9.1%	-	14%	4.1%	3.1%
$h \rightarrow WW^*$	6.4%	-	9.2%	2.6%	3.3%
$h \rightarrow \tau^+\tau^-$	4.2%	-	5.4%	14%	3.5%
$h \rightarrow ZZ^*$	19%	-	25%	8.2%	4.4%
$h \rightarrow \gamma\gamma$	29-38%	-	29-38%	20-26%	7-10%
$h \rightarrow \mu^+\mu^-$	100%	-	-	-	32%

coupling	ILC250		ILC500		ILC1000	
	full	no BSM	full	no BSM	full	no BSM
hZZ	0.49	0.38	0.35	0.20	0.34	0.16
hWW	0.48	0.38	0.35	0.20	0.34	0.16
hbb	0.99	0.80	0.58	0.43	0.47	0.31
$h\tau\tau$	1.1	0.95	0.75	0.63	0.63	0.52
hgg	1.6	1.6	0.96	0.91	0.67	0.59
hcc	1.8	1.7	1.2	1.1	0.79	0.72
$h\gamma\gamma$	1.1	1.0	1.0	0.96	0.94	0.89
$h\gamma Z$	8.9	8.9	6.5	6.5	6.4	6.4
$h\mu\mu$	4.0	4.0	3.8	3.7	3.4	3.4
htt	—	—	6.3	6.3	1.0	1.0
hhh	—	—	20	20	10	10
Γ_{tot}	2.3	1.3	1.6	0.70	1.4	0.50
Γ_{inv}	0.36	—	0.32	—	0.32	—

Table 12.2: Projected uncertainties in the Higgs boson couplings for the ILC250, ILC500, and ILC1000, with precision LHC input. All values are *relative* errors, given in percent (%). The columns labelled “full” refer to a 22-parameter fit including the possibility of invisible and exotic Higgs boson decays. The columns labelled “no BSM” refer to a 20-parameter fit including only decays modes present in the SM.

Renormalization in potential (1)

Parameters in Higgs potential (8)

$$m_h^2, \quad m_H^2, \quad m_A^2, \quad m_{H^\pm}^2, \quad M^2(m_{12}^2), \quad v, \quad \alpha, \quad \beta$$

Parameter shift ;

$$m_\phi^2 \rightarrow m_\phi^2 + \delta m_\phi^2 \quad M^2 \rightarrow M^2 + \delta M^2 \quad v \rightarrow v + \delta v \quad \alpha \rightarrow \alpha + \delta\alpha \quad \beta \rightarrow \beta + \delta\beta$$

Field shift ;

$$\begin{pmatrix} H \\ h \end{pmatrix} \rightarrow \begin{pmatrix} 1 + \delta Z_H & \delta C_{Hh} + \delta\alpha \\ \delta C_{hH} - \delta\alpha & 1 + \delta Z_h \end{pmatrix} \begin{pmatrix} H \\ h \end{pmatrix}$$

$$\begin{pmatrix} G^0 \\ A \end{pmatrix} \rightarrow \begin{pmatrix} 1 + \delta Z_G & \delta C_{GA} + \delta\beta \\ \delta C_{AG} - \delta\beta & 1 + \delta Z_A \end{pmatrix} \begin{pmatrix} G^0 \\ A \end{pmatrix}$$

$$\begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix} \rightarrow \begin{pmatrix} 1 + \delta Z_{G^\pm} & \delta C_{G^\pm H^\mp} + \delta\beta \\ \delta C_{H^\pm G^\mp} - \delta\beta & 1 + \delta Z_{H^\pm} \end{pmatrix} \begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix}$$

8 counterterms
via parameter shifts

12 counterterms
via field shifts

Total : 20 counterterms

Renormalization in potential (2)

■ On shell conditions

δm_ϕ^2	$\times 4$	$\hat{\Pi}_{\phi\phi}[m_\phi^2] = 0.$	$\times 4$	$\delta m_i^2 = \tilde{\Pi}_{ii}^{1PI}[m_i^2]$	$\times 6$
δZ_ϕ	$\times 6$	$\frac{d}{dp^2} \hat{\Pi}_{\phi\phi}[p^2] _{p^2=m_\phi^2} = 0,$	$\times 6$	$\delta Z_i = -\frac{d}{dp^2} \Pi_{ii}^{1PI}[p^2] _{p^2=m_i^2}$	$\times 6$
δC_{Hh}	δC_{hH}	$\delta C_{hH} = \delta C_{Hh}$		$\delta C_{hH} = \delta C_{Hh} = \frac{1}{m_H^2 - m_h^2} (\Pi_{hH}^{1PI}[m_h^2] - \Pi_{hH}^{1PI}[m_H^2])$	
$\delta\alpha$	3	$\hat{\Pi}_{hH}[m_h^2] = \hat{\Pi}_{hH}[m_H^2] = 0,$	3	$\delta\alpha = \frac{1}{2(m_H^2 - m_h^2)} (\tilde{\Pi}_{Hh}^{1PI}[m_h^2] + \tilde{\Pi}_{Hh}^{1PI}[m_H^2])$	
δC_{GA}	δC_{AG}	$\delta C_{GA} = \delta C_{AG}$		$\delta C_{AG} = \delta C_{GA} = -\frac{1}{2m_A^2} (\Pi_{AG^0}^{1PI}[m_A^2] - \Pi_{AG^0}^{1PI}[0])$	
$\delta\beta$	3	$\hat{\Pi}_{AG^0}[m_A^2] = \hat{\Pi}_{AG^0}[0] = 0$	3	$\delta\beta = \frac{1}{2m_A^2} (\tilde{\Pi}_{AG}^{1PI}[m_A^2] + \tilde{\Pi}_{AG}^{1PI}[0])$	
$\delta C_{H^\pm G^\mp}$	$\delta C_{G^\pm H^\mp}$	$\hat{\Pi}_{H^\pm G^\mp}[m_{H^\pm}^2] = \hat{\Pi}_{H^\pm G^\mp}[0] = 0$		$\delta C_{H^\pm G^\mp} = \delta C_{G^\pm H^\mp} = \delta\beta + \frac{1}{m_{H^\pm}^2} \tilde{\Pi}_{H^\pm G^\mp}^{1PI}[0]$	
	2	$\delta C_{GA} = \delta C_{AG}$	2		

δv is determined by EW renormalization. 1

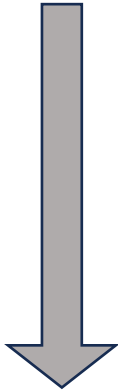
Total : 19

Renormalization in potential (3)

δM^2 is determined by the MS-bar scheme, which absorb only the divergent part in the hhh vertex at the one-loop level.

$$\hat{\Gamma}_{hhh} = 6\lambda_{hhh} + \delta\Gamma_{hhh} + \Gamma_{hhh}^{1PI} \quad \longrightarrow$$

Remove only
divergent part

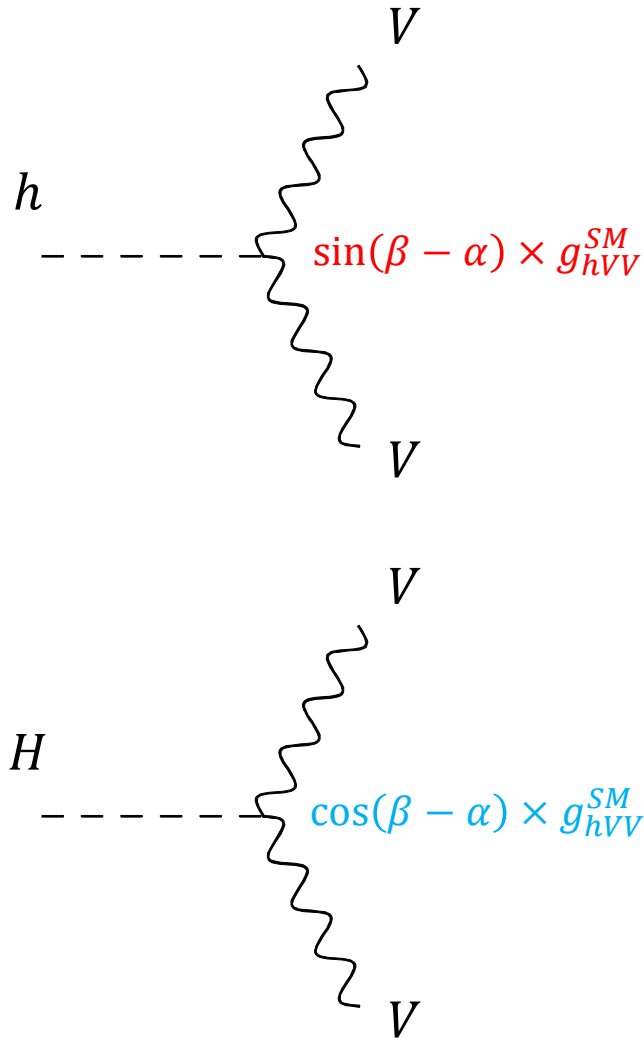


$$\delta\Gamma_{hhh} = 6\delta\lambda_{hhh} + 9\lambda_{hhh}\delta Z_h + 6\lambda_{Hhh}(\delta C_{Hh} + \delta\alpha)$$

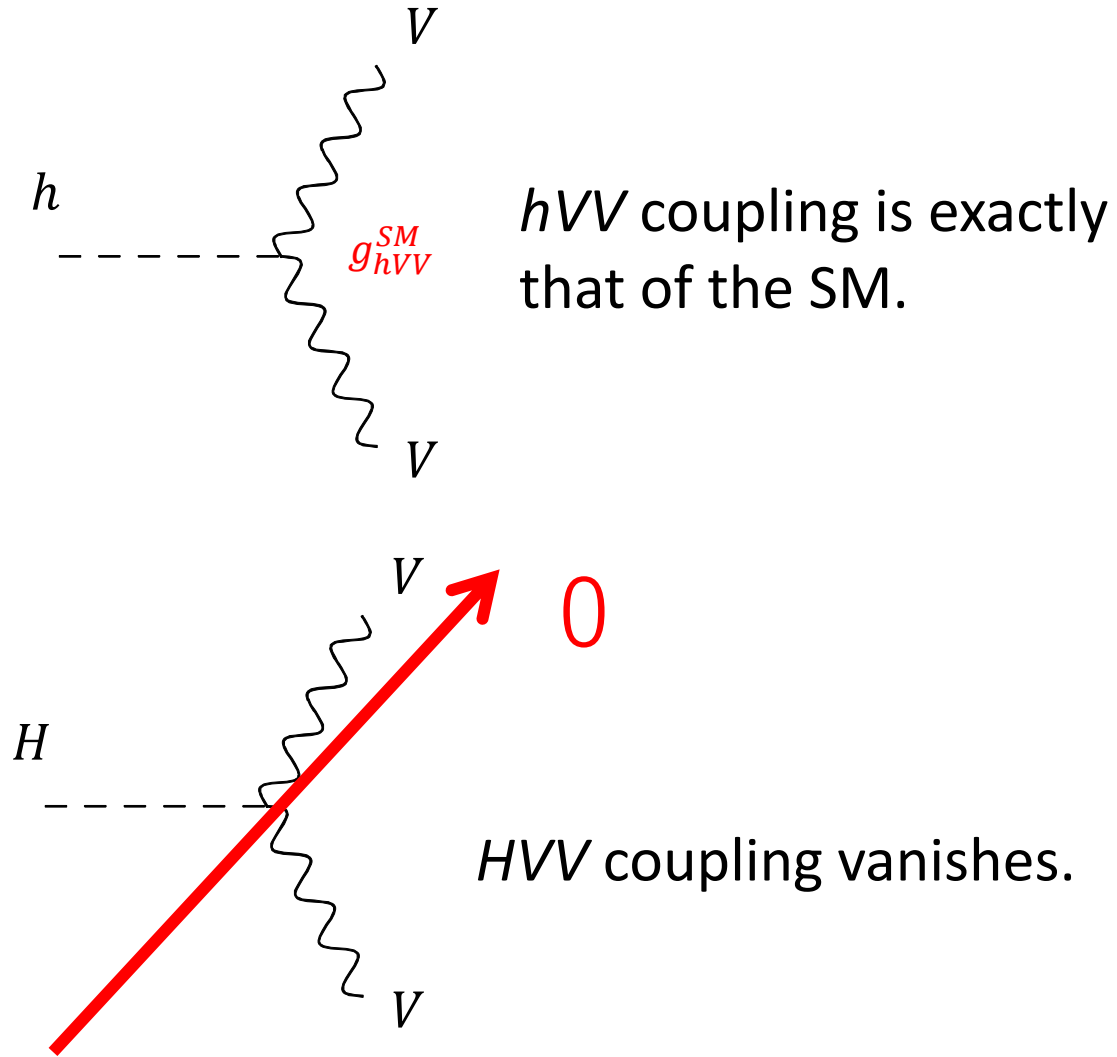
$$\delta\lambda_{hhh} = -\lambda_{hhh}\frac{\delta v}{v} - \frac{c_{3\alpha-\beta} + 3c_{\alpha+\beta}}{4vs_{2\beta}}\delta m_h^2 + F_\alpha\delta\alpha + F_\beta\delta\beta + \frac{c_{\beta-\alpha}^2 c_{\alpha+\beta}}{vs_{2\beta}}\delta M^2$$

$$\delta M^2 = \frac{M^2}{16\pi^2 v^2} \left[2 \sum_f N_c^f m_f^2 \kappa_f^2 + 4M^2 - 2m_{H^\pm}^2 - m_A^2 + \frac{s_{2\alpha}}{s_{2\beta}}(m_H^2 - m_h^2) - 3(2m_W^2 + m_Z^2) \right] \Delta_{\text{Div}} + \frac{2c_{2\beta}}{s_{2\beta}} \frac{M^2}{v} \left(\frac{c_{\beta-\alpha}}{m_h^2} \text{Div}(T_h^{1PI}) - \frac{s_{\beta-\alpha}}{m_H^2} \text{Div}(T_H^{1PI}) \right)$$

Alignment limit at tree level



Alignment limit



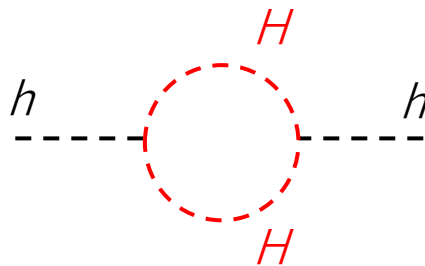
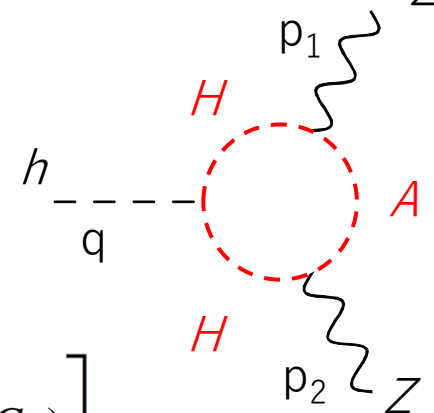
Alignment limit at loop level (hVV)

At loop level, $\sin(\beta-\alpha)$ is no longer a parameter that represents "alignmentness".
One cannot take the exact alignment limit at loop level.

Since the renormalized hVV vertex cannot take the on-shell momentum, we have to calculate not the renormalized vertex but the three-body decay or the four-body decay.

$$\hat{\Gamma}_{hVV}^i(p_1^2, p_2^2, q^2) = \Gamma_{hVV}^{i,\text{tree}} + \delta\Gamma_{hVV}^i + \Gamma_{hVV}^{i,1\text{PI}}(p_1^2, p_2^2, q^2)$$

$$\delta\Gamma_{hVV}^1 = \frac{2m_V^2}{v} \left[\sin(\beta - \alpha) \left(\frac{\delta m_V^2}{m_V^2} + \delta Z_V + \frac{1}{2} \delta Z_h - \frac{\delta v}{v} \right) + \cos(\beta - \alpha) (\delta\beta + \delta C_h) \right]$$



Alignment limit at loop level (HVV)

Renormalized HVV vertex

$$\hat{\Gamma}_{HVV}^i(p_1^2, p_2^2, q^2) = \Gamma_{HVV}^{1.Tree} + \delta\Gamma_{HVV}^i + \Gamma_{HVV}^{i,1PI}(p_1^2, p_2^2, q^2)$$

Renormalized HVV vertex

$$\delta\Gamma_{HVV}^1 = \frac{2m_V^2}{v} \left[\cos(\beta - \alpha) \left(\frac{\delta m_V^2}{m_V^2} - \frac{\delta v}{v} + \delta Z_V + \frac{1}{2} \delta Z_H \right) + \sin(\beta - \alpha) (\delta C_{hH} - \delta\beta) \right]$$

In the case with $\sin(\beta - \alpha) = 1$

$$\delta\Gamma_{HVV}^1 = \frac{2m_V^2}{v} [(\delta C_{hH} - \delta\beta)] \neq 0$$

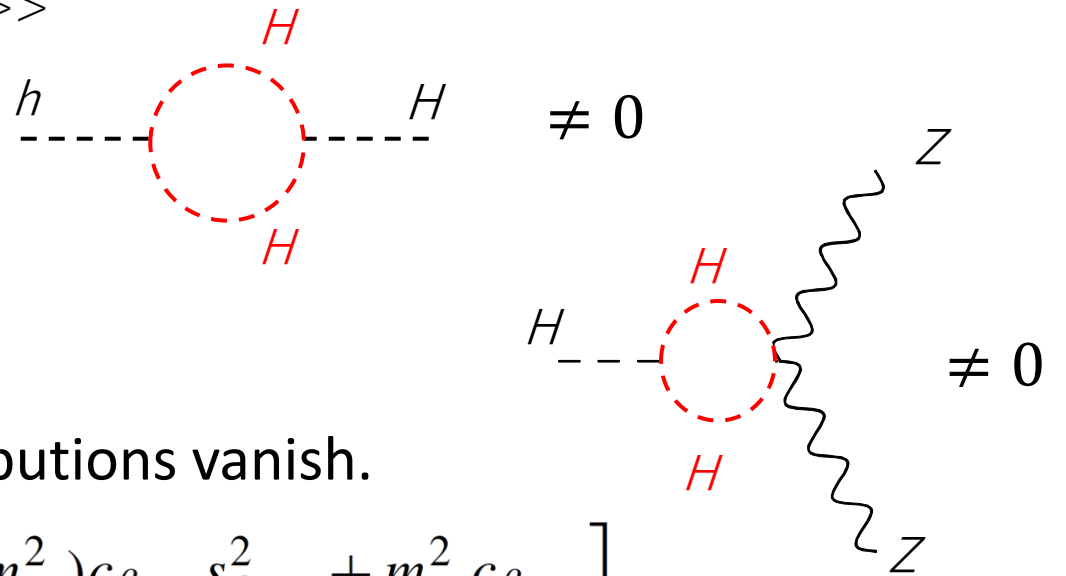
$$\Gamma_{HVV}^{i,1PI}(p_1^2, p_2^2, q^2) \neq 0$$

Only taking $\sin(\beta - \alpha) = 1$ does not realize $HVV = 0$.

In the case with $m_{H,A,H^\pm}^2 = M^2$, these loop contributions vanish.

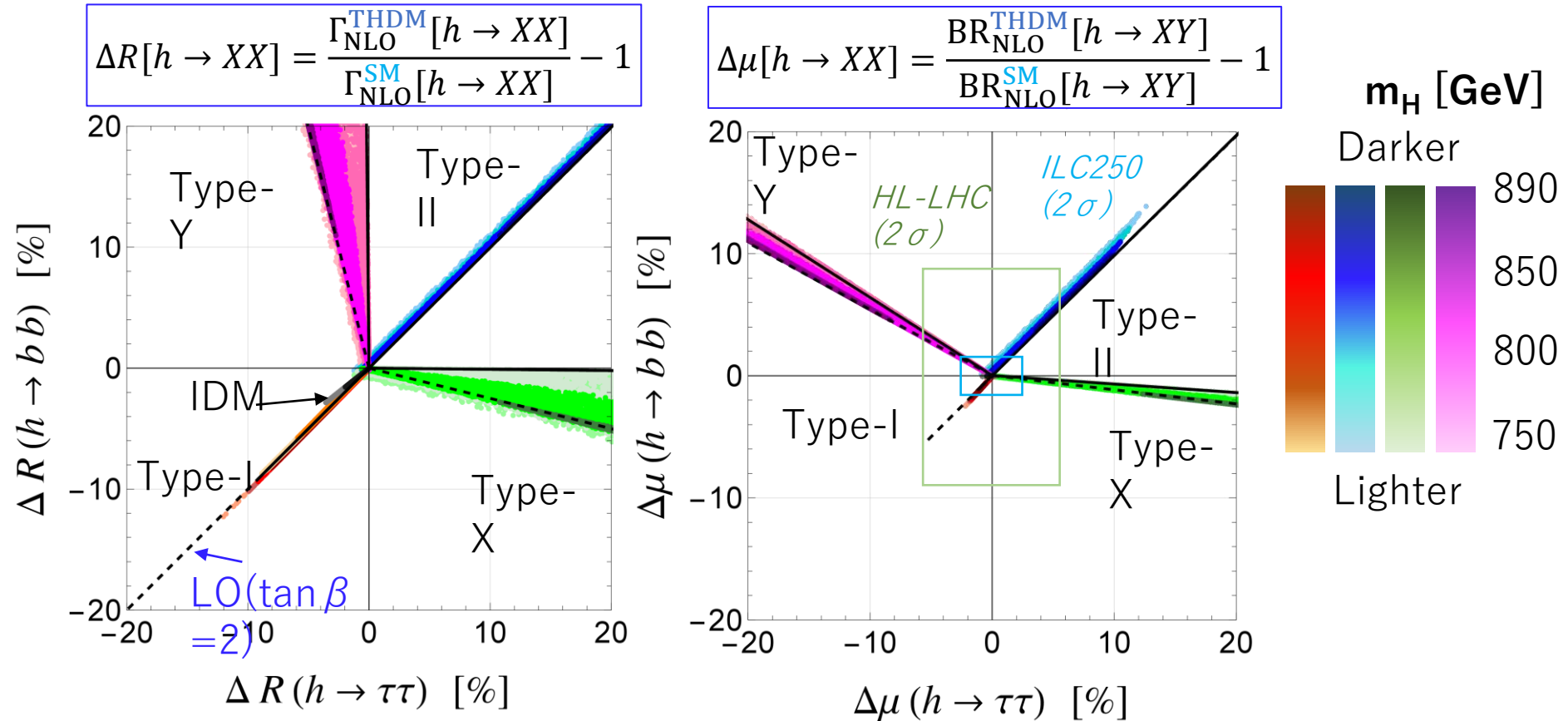
$$\lambda_{HHH} = -\frac{1}{2v} \left[2(M^2 - m_H^2) \cot 2\beta s_{\beta-\alpha}^3 - 2(M^2 - m_H^2) c_{\beta-\alpha} s_{\beta-\alpha}^2 + m_H^2 c_{\beta-\alpha} \right]$$

ex.>>



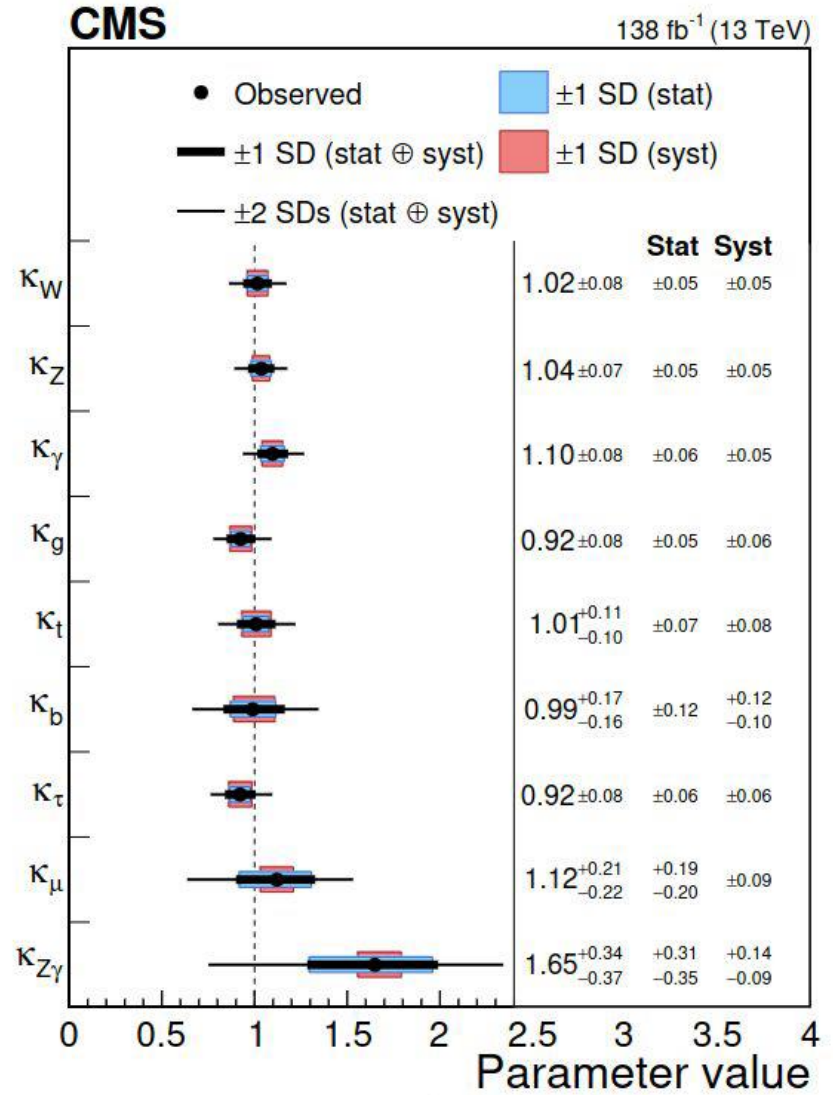
$h \rightarrow bb, h \rightarrow \tau\tau$

$$m_A = m_{H^\pm} = 800 \text{ GeV}, \cos(\beta - \alpha) < 0$$

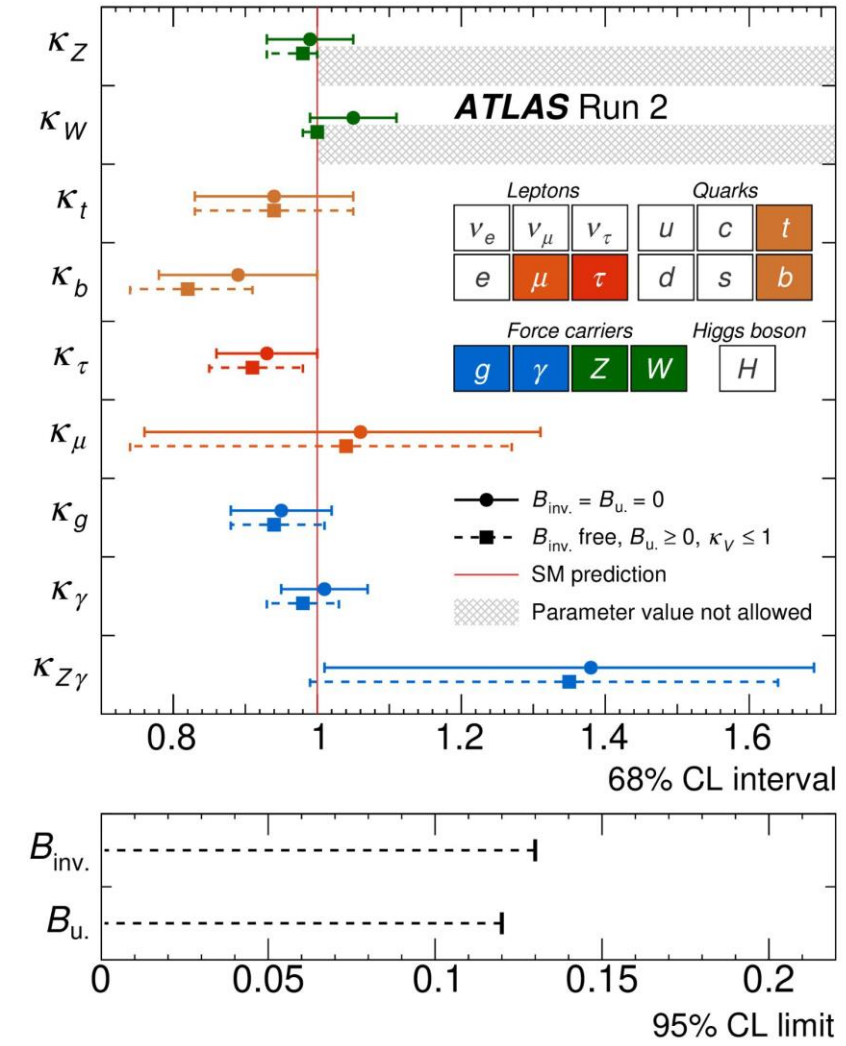


If $|\Delta R[h \rightarrow bb/\tau\tau]| > \text{several } \%$, prediction of each Type does not overlap

Combined scale factor results

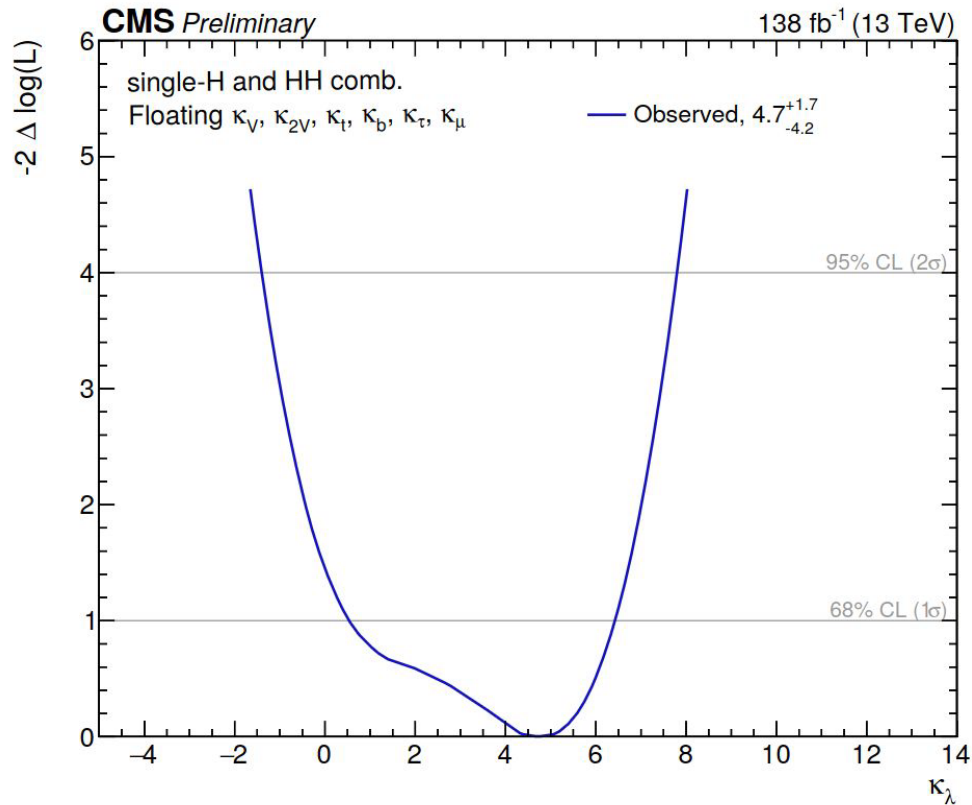


Nature 607 (2022) 60



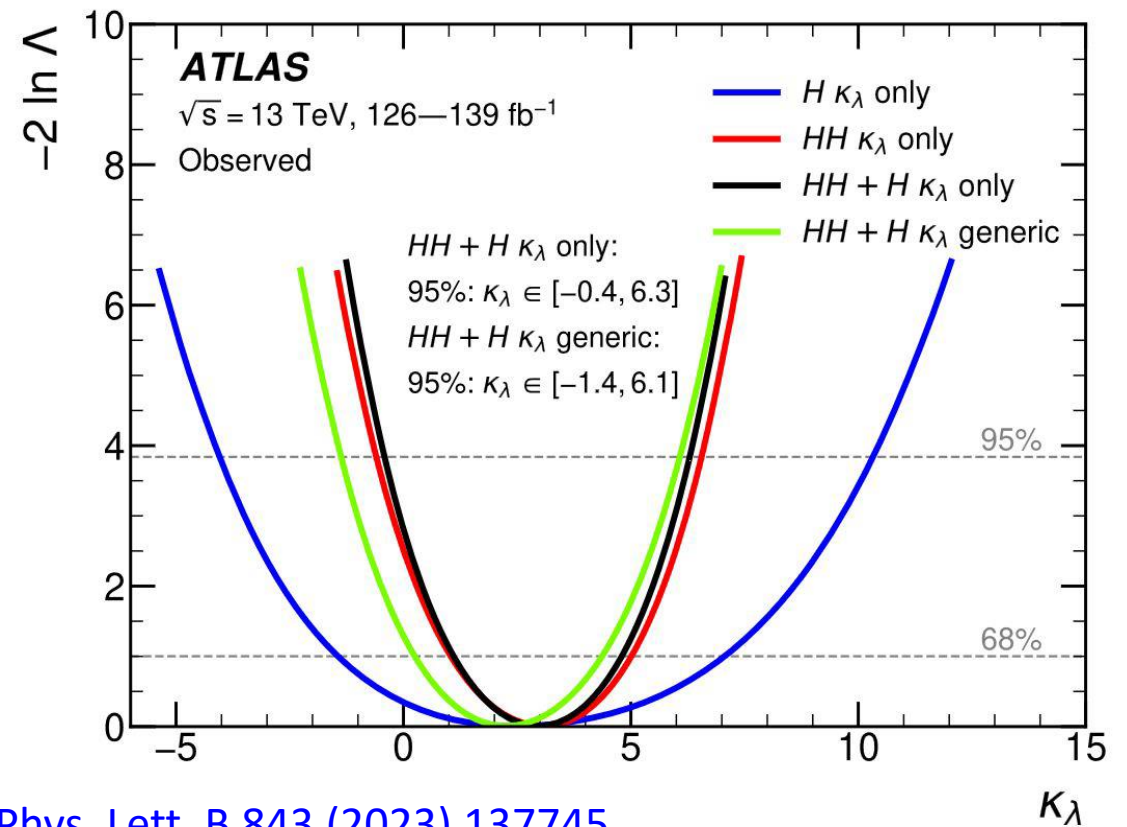
Nature 607 (2022) 52

hhh coupling measurement



CMS-HIG-23-006

$$-1.2 < \kappa_\lambda < 7.5 \text{ at 95\% CL}$$



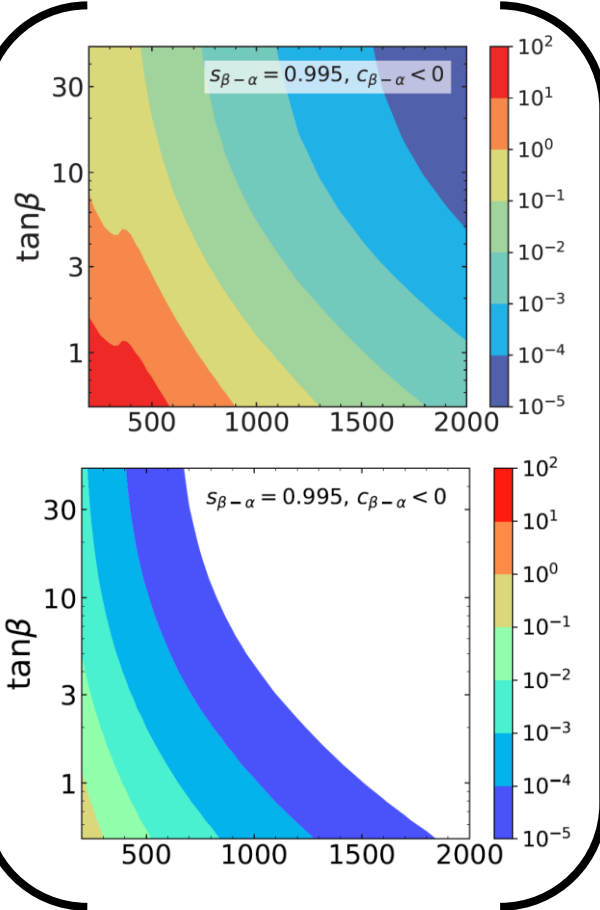
Phys. Lett. B 843 (2023) 137745

$$-1.4 < \kappa_\lambda < 6.1 \text{ at 95\% CL}$$

Constraint from direct searches (Run2)

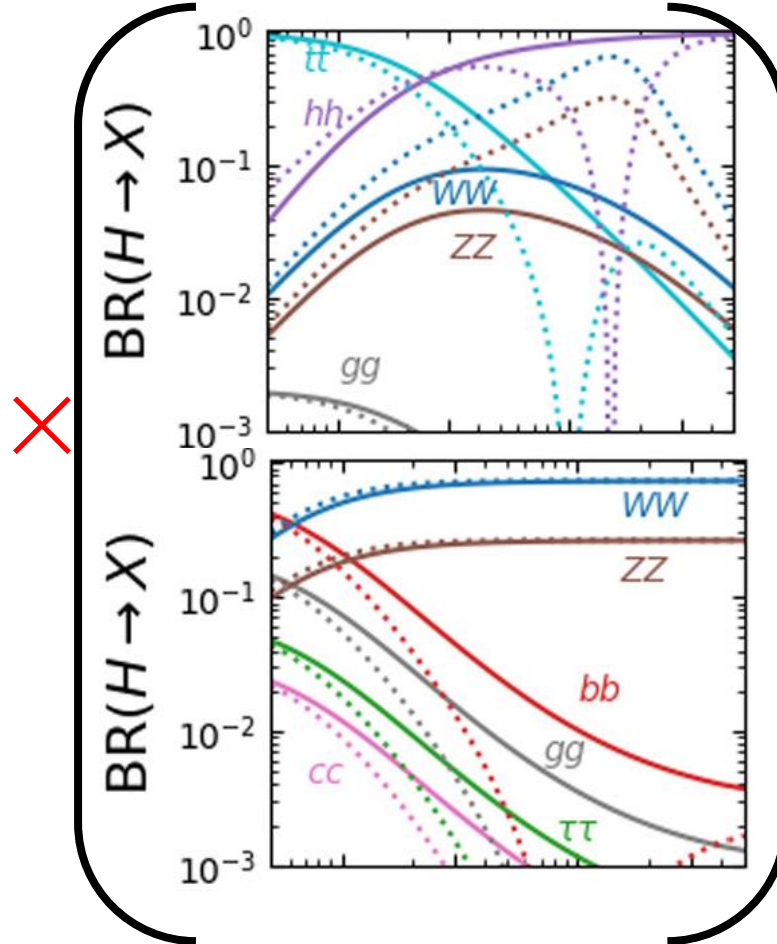
gluon-fusion process
($pp \rightarrow H$)

Production cross section



bottom associated
process ($pp \rightarrow H(bb)$)

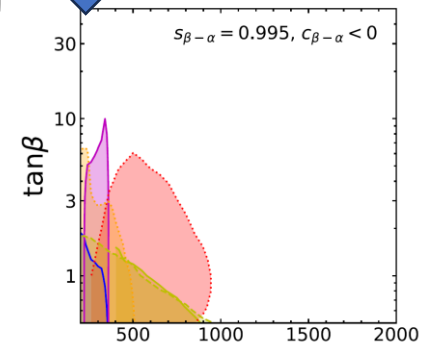
BR



Compare

Upper limits at
95% CL with
 36fb^{-1} data

obtain
Constraints



Correlation between $A \rightarrow Zh$ and $h \rightarrow ZZ^*$

