Towards an update of the ILD ZHH analysis

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Agenda

- Introduction
- Part I: State-of-the-art (SOTA) Analysis Tools
- Part II: Future Analysis Tools
- Conclusion

Introduction

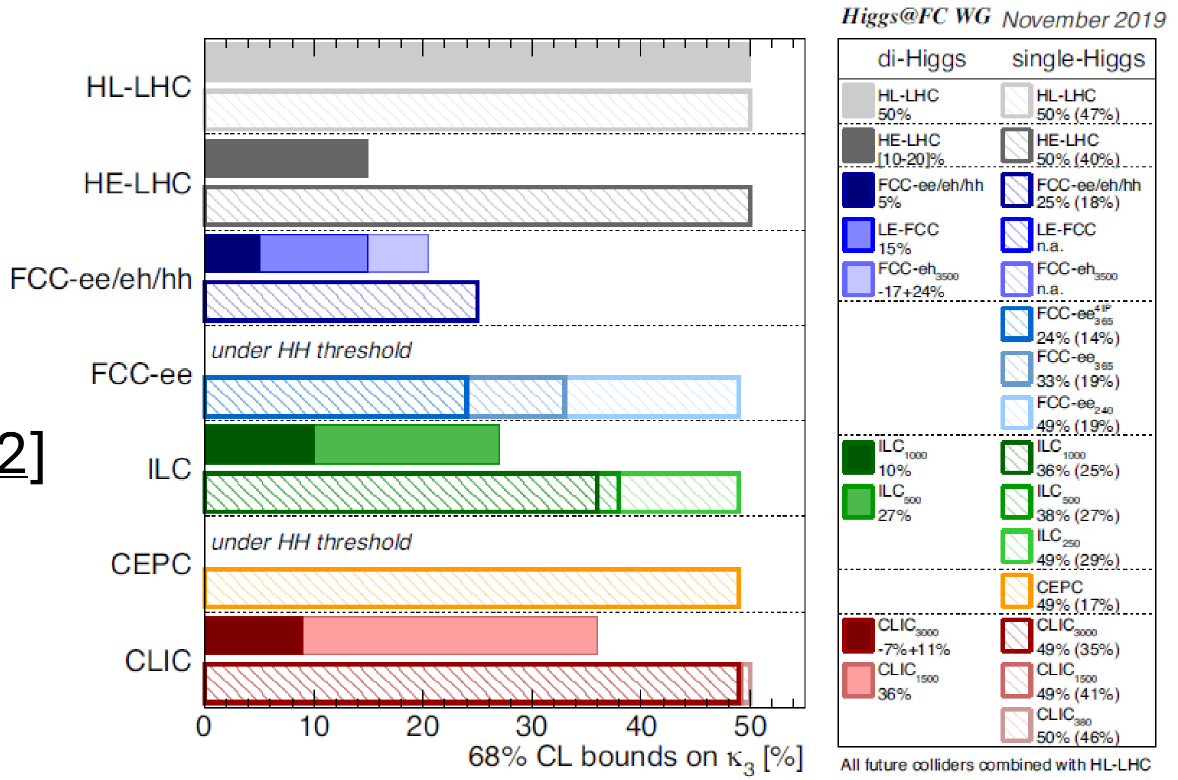
Physical fundamentals and methods for direct measurements of the Higgs self-coupling at future Higgs factories

The Higgs self-coupling λ in the SM

$$V(h) = \frac{1}{2} m_H^2 h^2 + \lambda v h^3 + o(h^4); \lambda_{SM} = \frac{m_H^2}{2v^2}$$

v	vacuum expectation value (vev) of Higgs field h
m_H	mass of Higgs boson

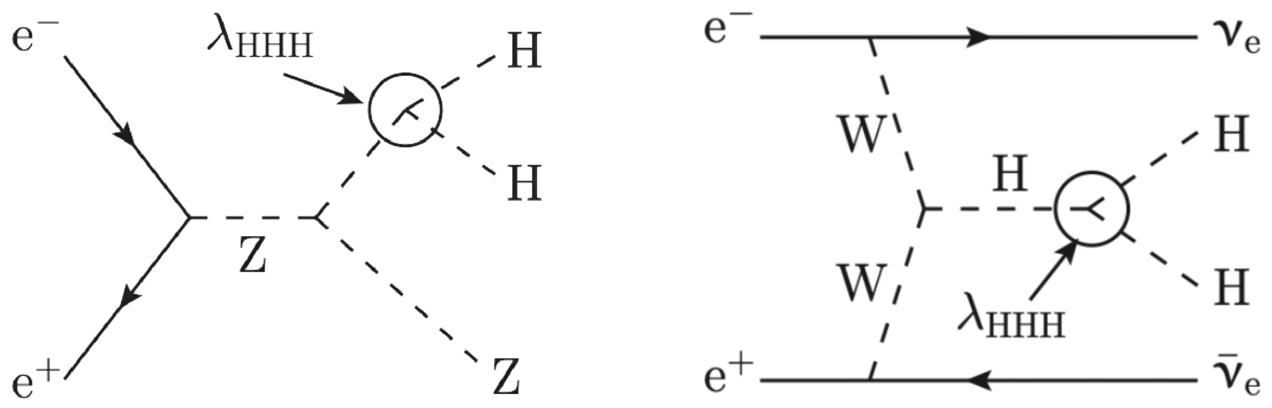
- in SM: λ_{SM} fixed since m_H is known [At/Cm12]
  - deviation from $\lambda = \lambda_{SM}$ hints at BSM physics
  - beyond SM, many values are possible
  - most projections assume $\lambda = \lambda_{SM}$

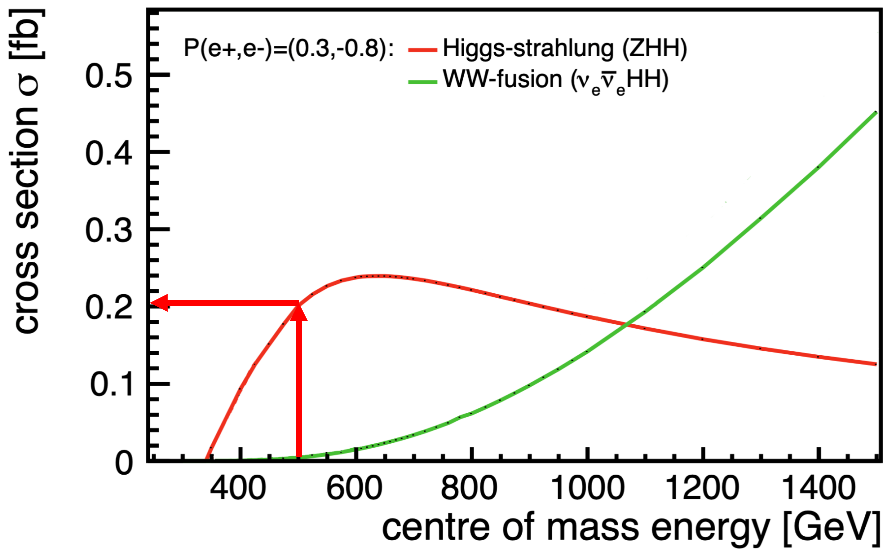


Projected sensitivity at 68% probability for k_3.
From [Db20]

Measuring the Higgs self-coupling at e+e- colliders

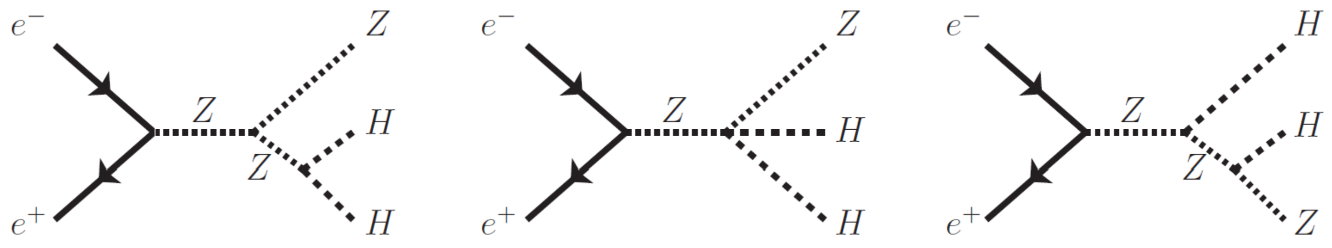
- *direct access* to λ through double-Higgs production
  - Di-Higgs strahlung (**ZHH**; dominant < 1 TeV)
  - vector boson fusion (**$\nu\bar{\nu}$HH**; dominant > 1 TeV)





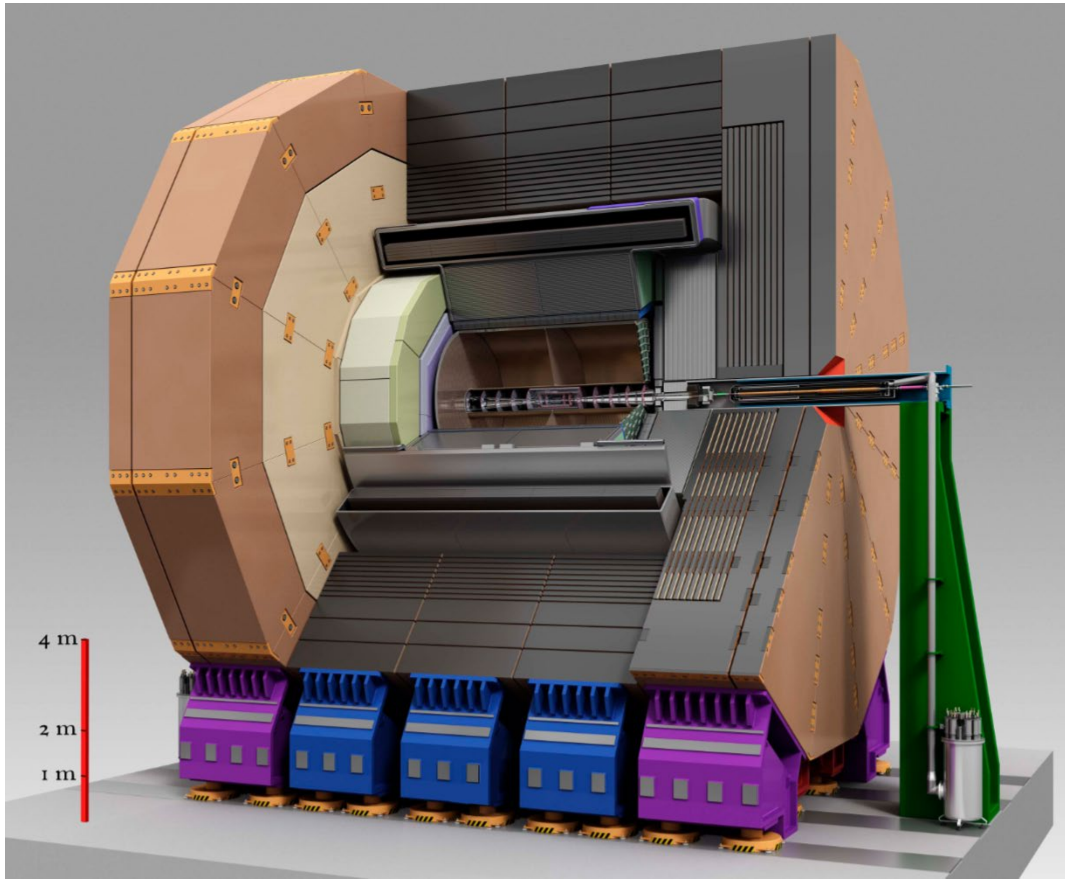
Cross-section of Di-Higgs production processes. From [Du16]

- degredation of sensitivity in ZHH by diagrams without λ



The International Large Detector (ILD)

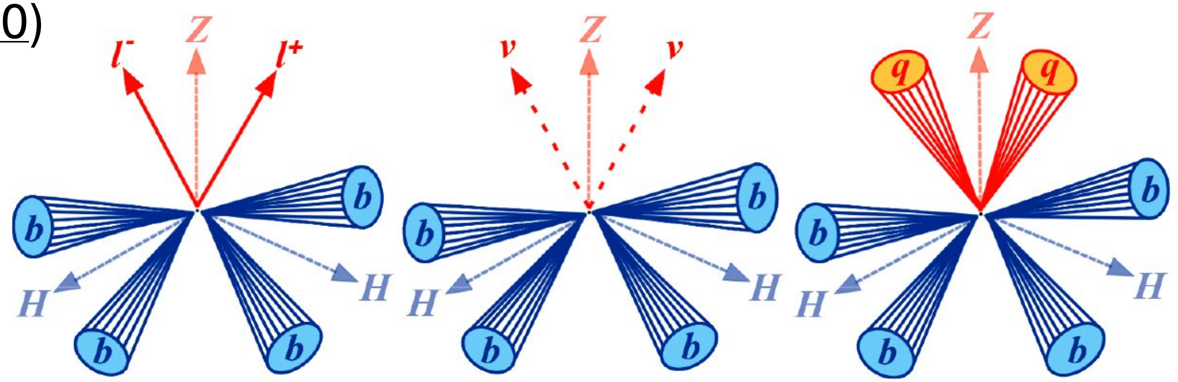
- well charatecterized, highly granular detector concept [IDR]
- designed around particle flow concept
  - allows reconstruction of individual physics objects (Particle Flow Objects, PFOs)
- full Geant4-based simulation available
  - including links between truth/reconstructed particles
- in the following: assuming ILD @ ILC500



Rendering of the ILD detector. From [Ba19]

The ZHH Analysis

- extensive projections at ILC500 (DESY-Thesis-16-027)
  - based on ILD detector concept (DBD2013, IDR2020) and *fully simulated* event samples
  - 17 background and 3 signal channels considered
  - multivariate (MVA) tools for multiple steps
    e.g. lepton and flavor tagging, background rejection etc.
  - event counting weighted by m_{HH}^2
    for further sensitivity enhancement



Lepton, neutrino and hadron channel of the signal process ZHH.
From [Du16]

- precision reach after running $4\mathrm{ab}^{-1}$ at $500\ \mathrm{GeV}$ $\left(\mathrm{HH} \to \mathrm{b\bar{b}b\bar{b}} + \mathrm{HH} \to \mathrm{b\bar{b}W^{\pm}W^{\mp}}\right)$

$$\Delta\sigma_{\mathrm{ZHH}}/\sigma_{\mathrm{ZHH}} = 16.8\%$$

$$\Delta\lambda_{\mathrm{SM}}/\lambda_{\mathrm{SM}} = 26.6\%$$ (10% with additional upgrade to 1 TeV)

Bottlenecks in the ZHH analysis

- jet pairing and jet misclustering: “perfect“ jet clustering → 40% improvement
  improve di-jet mass resolution
- removal of $\gamma\gamma$ overlay: 15% improvement expected
  important to tackle initial state radiation (ISR)
- flavor tagging: 11% improvement expected from 5% eff. increase with newer LCFIPlus
  important as $H \rightarrow b\bar{b}$ is the dominant Higgs decay channel
- adding $Z \rightarrow \tau\tau$ channel: 8% improvement expected
  include a yet unaccounted decay channel
- more modern ML architectures for signal/background selection
  improvement expected when transitioning from BDTs to (e.g.) transformer-based models etc.
- separation of ZHH diagrams with/without the self-coupling
  would directly improve the sensitivity on λ (lower sensitivity factor)

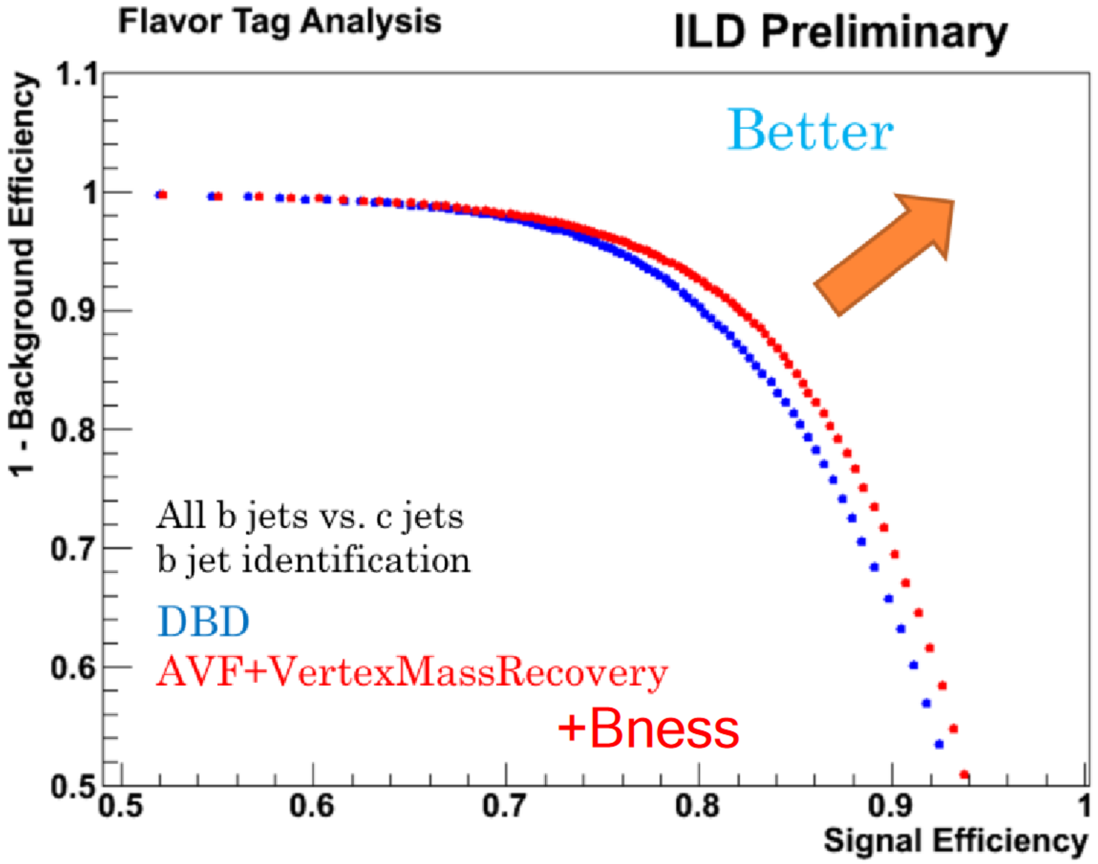
Expected relative improvements from DESY-Thesis-16-027

Tools of Today

State-of-the-art (SOTA) tools for reconstruction and analysis expected to improve the sensitivity on λ

Flavor tagging with LCFIPlus

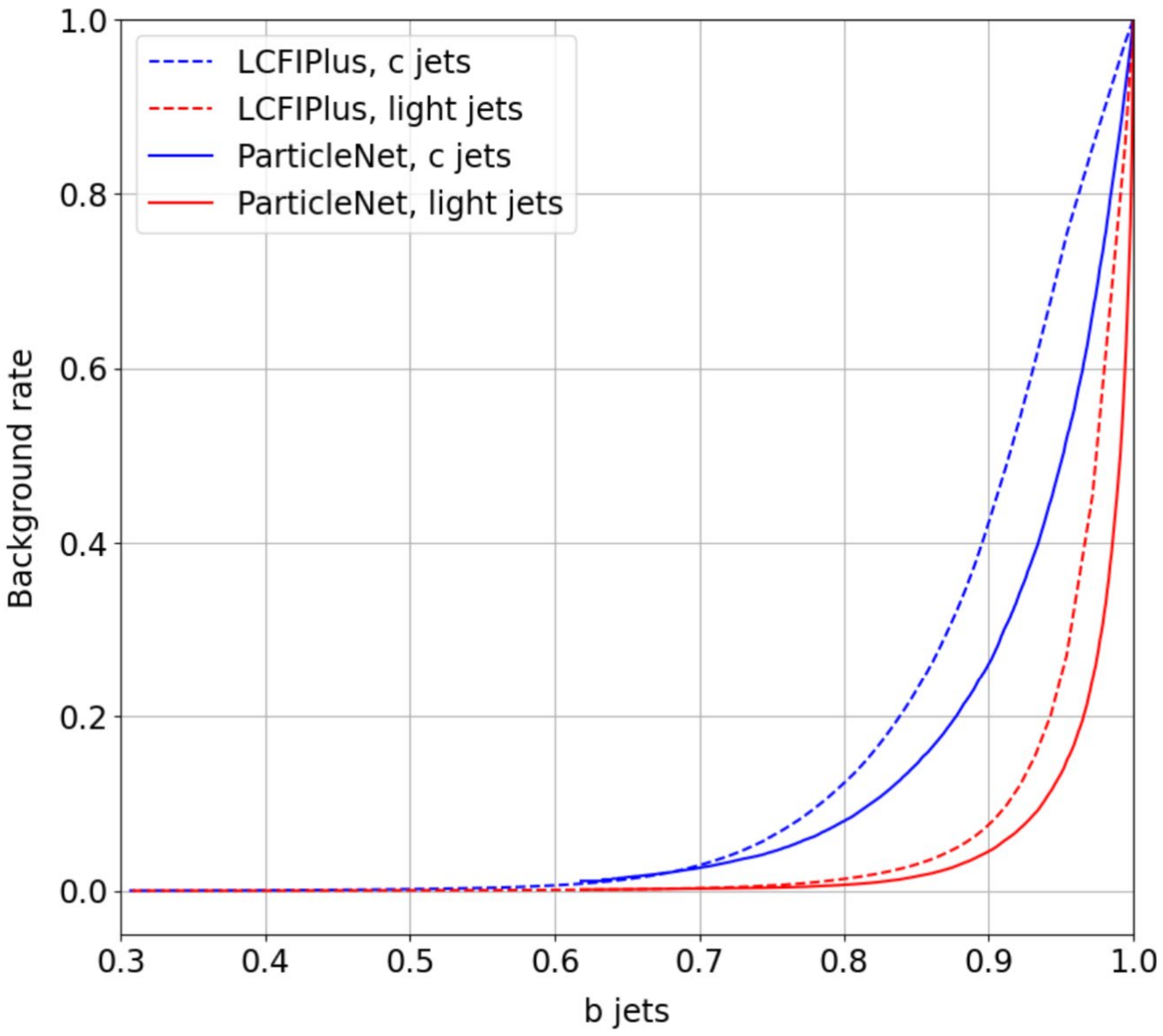
- improved b-tagging efficiency in current ILD standard LCFIPlus since SOTA projections from 2016
  - 5% relative improvement in ϵ_{b-tag} at same purity
  - 11% expected improvement in $\Delta\sigma_{\mathrm{ZHH}}/\sigma_{\mathrm{ZHH}}$



T. Suehara [2017]

Flavor tagging with ML (ParticleNet)

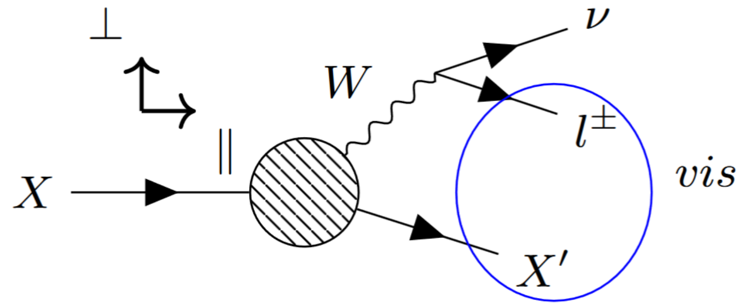
- improved b-tagging efficiency since state-of-the-art projections from 2016
- ML models (DeepJet, ParticleNet, ParT) show highly improved rejection compared to LCFIPlus
- status: ready for use (in MarlinML)



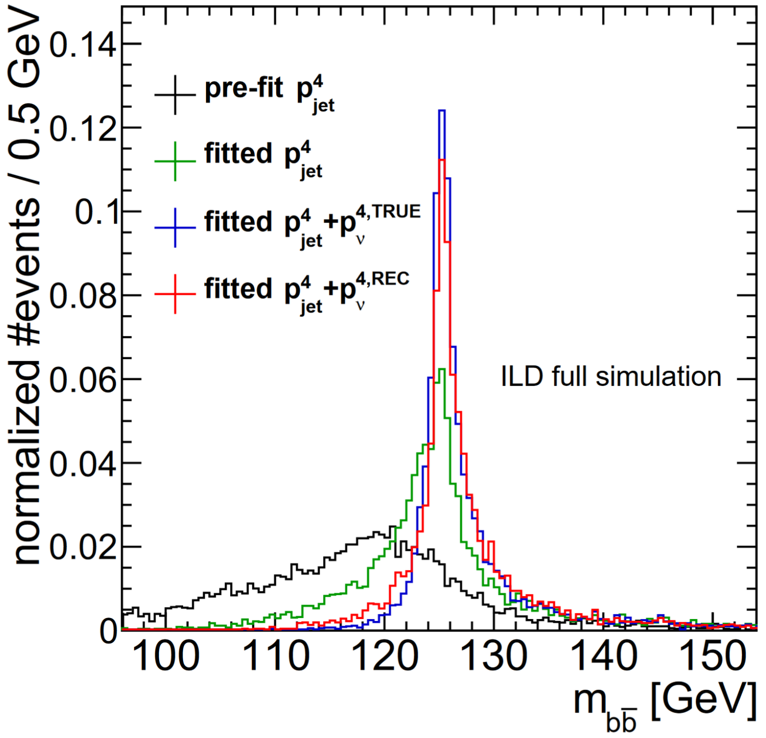
Flavor tagging performance of LCFIPlus vs. ParticleNet using ILD full simulation. M. Meyer [2023]

Neutrino correction with kinematic fitting

- for semileptonic decay (SLD) processes
  - already in $\mathrm{ZH} \rightarrow b\bar{b}/c\bar{c}$, 66% of events include at least one SLD
- procedure:
  - identify/tag heavy quark jet
  - identify lepton in jet
  - calculate neutrino four momentum from kinematics with kinematic fitting, the best solution is selected
- status: in production (in MarlinReco)



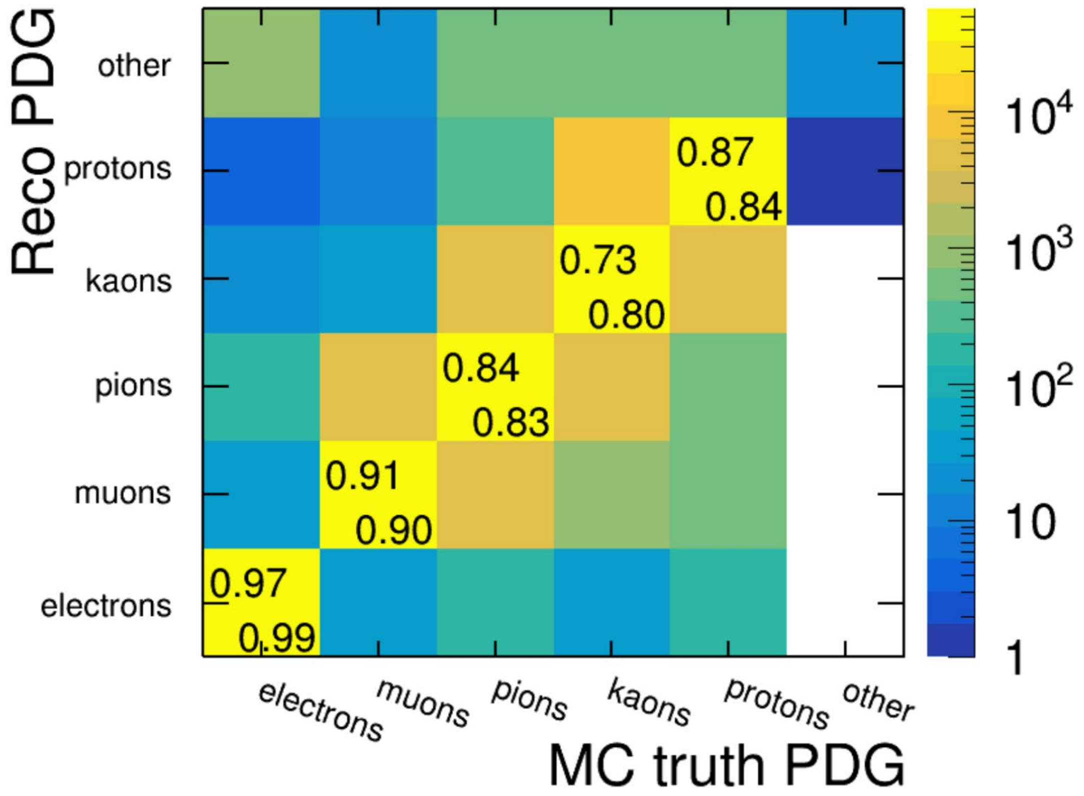
Recovering the neutrino kinematics. Y. Radkhorrami [2022]



Improved di-jet mass reconstruction. Y. Radkhorrami [2022]

Comprehensive Particle Identification (CPID)

- modular and highly configurable PID toolkit
  - "plug-and-play" of multiple data sources e.g. at ILD: dE/dx, TOF, cluster shape
  - extension through custom inference modules e.g. MVA/ML models etc.
- includes default weights for BDT model
- status: in production (in MarlinReco)



Confusion matrix for single charged partilces at ILD.
U. Einhaus (2023)

Conclusion I: The ZHH Analysis with SOTA-Tools

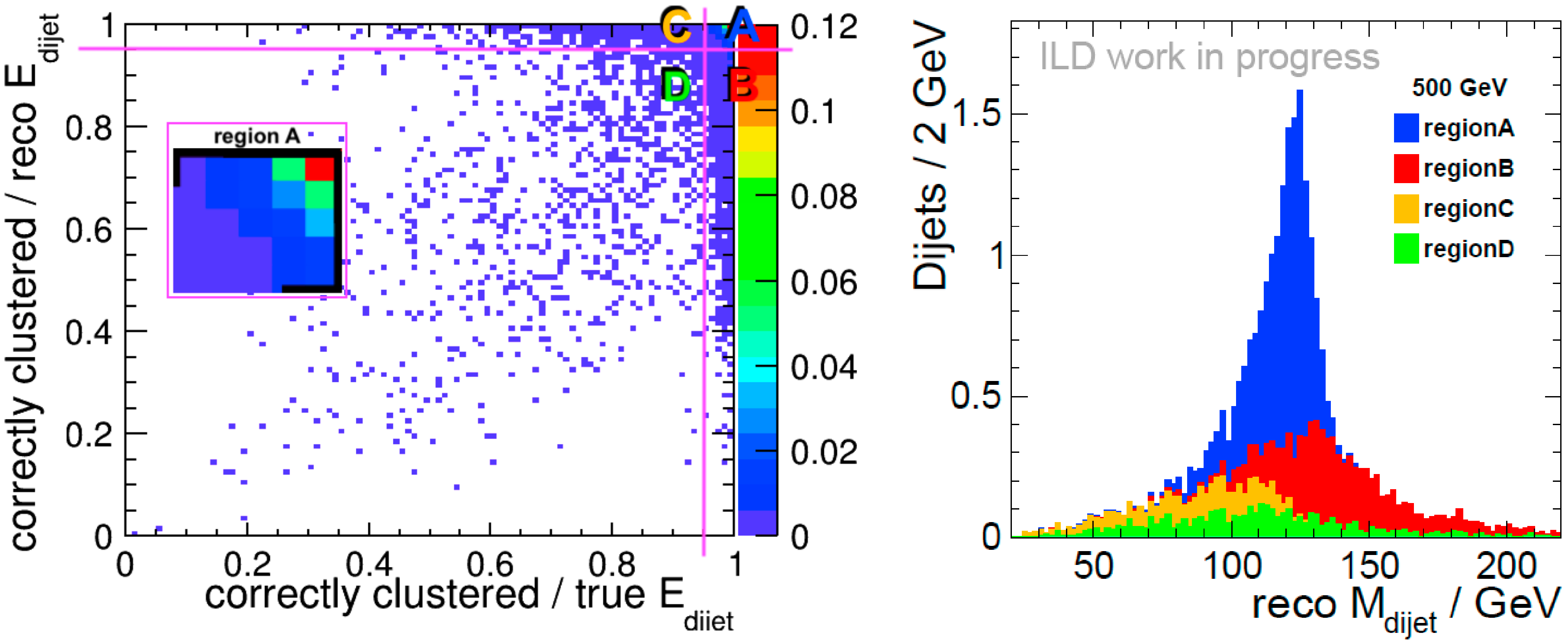
- major advancements in key aspects since last ZHH analysis [Du16]
  - flavor tagging efficiency improved by at least 5% ($\approx 10\%$ with ML tools)
  - kinematic fits benefit substantially from full ErrorFlow paramterization
  - neutrino correction has greatly improved di-jet mass resolution in events with SLDs
  - CPID improves particle ID performance by separating detector data and inference
- **better than 20% sensitivity of $\Delta\lambda_{SM}$ / λ_{SM}** expected with SOTA tools [To24b]

Tools of Tomorrow

Potential future tools for reconstruction and analysis

Motivation: Misclustering in the ZHH analysis

- misclustering of PFOs to jets deteriorates the sensitivity to λ by ≈ 2 [Du16]
- quantification: purity vs efficiency of energy in reconstructed di-jets
- classify di-jets into 4 regions (A, B, C, D) based on threshold: $> 95\%$ on both axes
  - e.g. 45.5% of dijets in region A

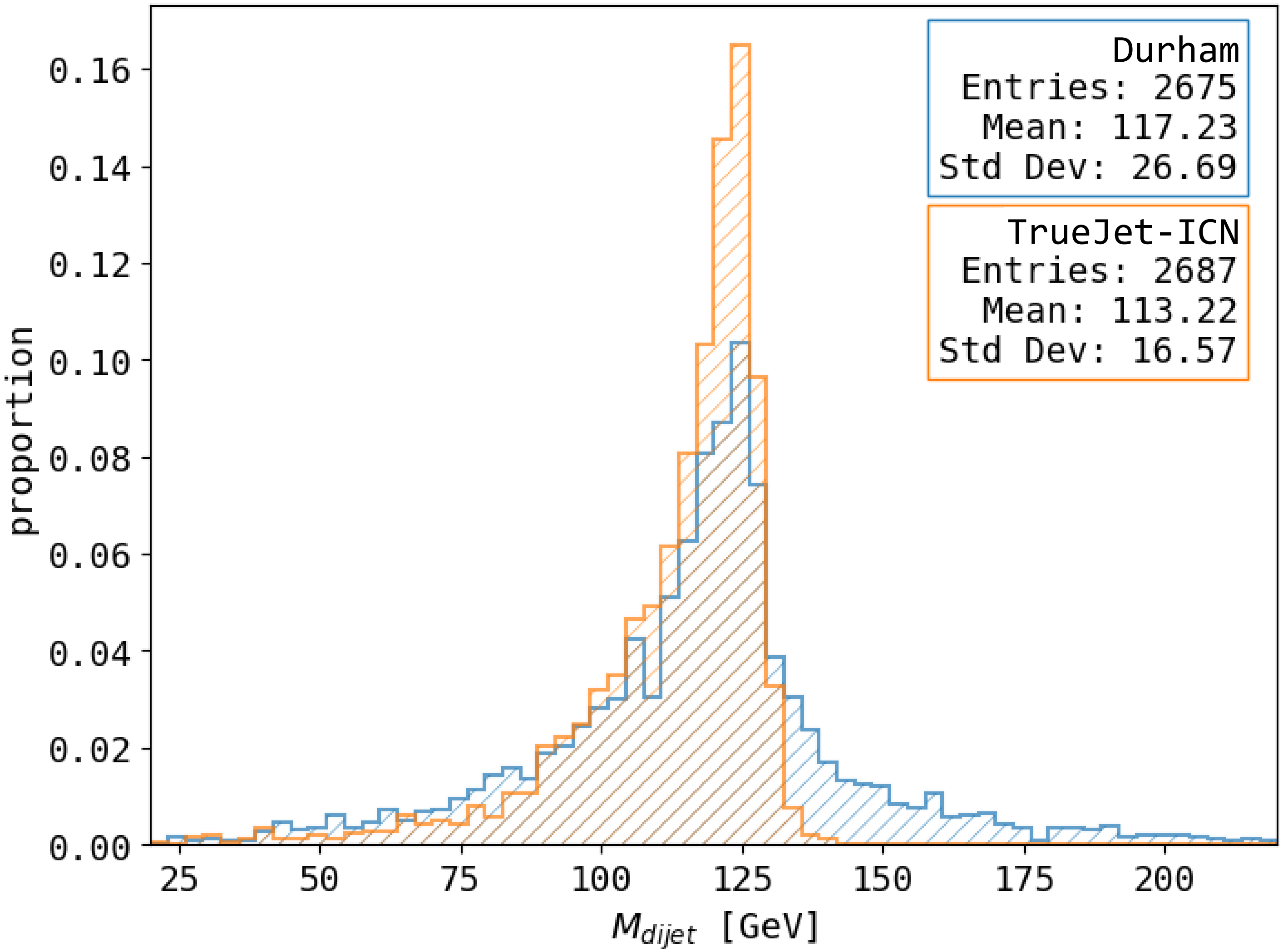


Misclustering in ZHH events at ILC500. From [To23b]

Misclustering in the ZHH analysis
J. Torndal, J. List (2023)

Supervised Jet Clustering

- idea: learn from truth-reco links to cluster PFOs into jets
  - upper performance bar given by TrueJet-ICN jet clustering
  - realistic target performance bounded by Durham and TrueJet



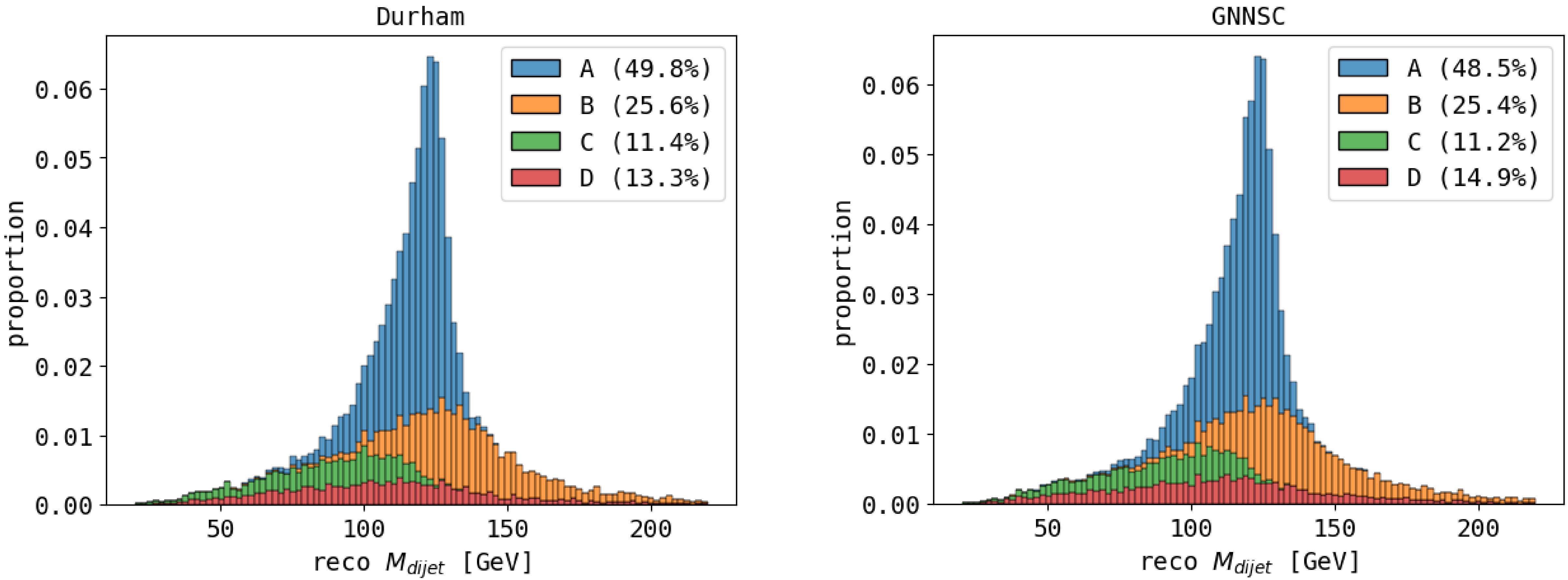
Di-jet mass reconstruction using Durham algorithm and TrueJet

Inspired by: *Supervised jet clustering with graph neural networks for Lorentz boosted bosons*. Nachman et al. [Na20]

TrueJet: M. Berggren (2018)

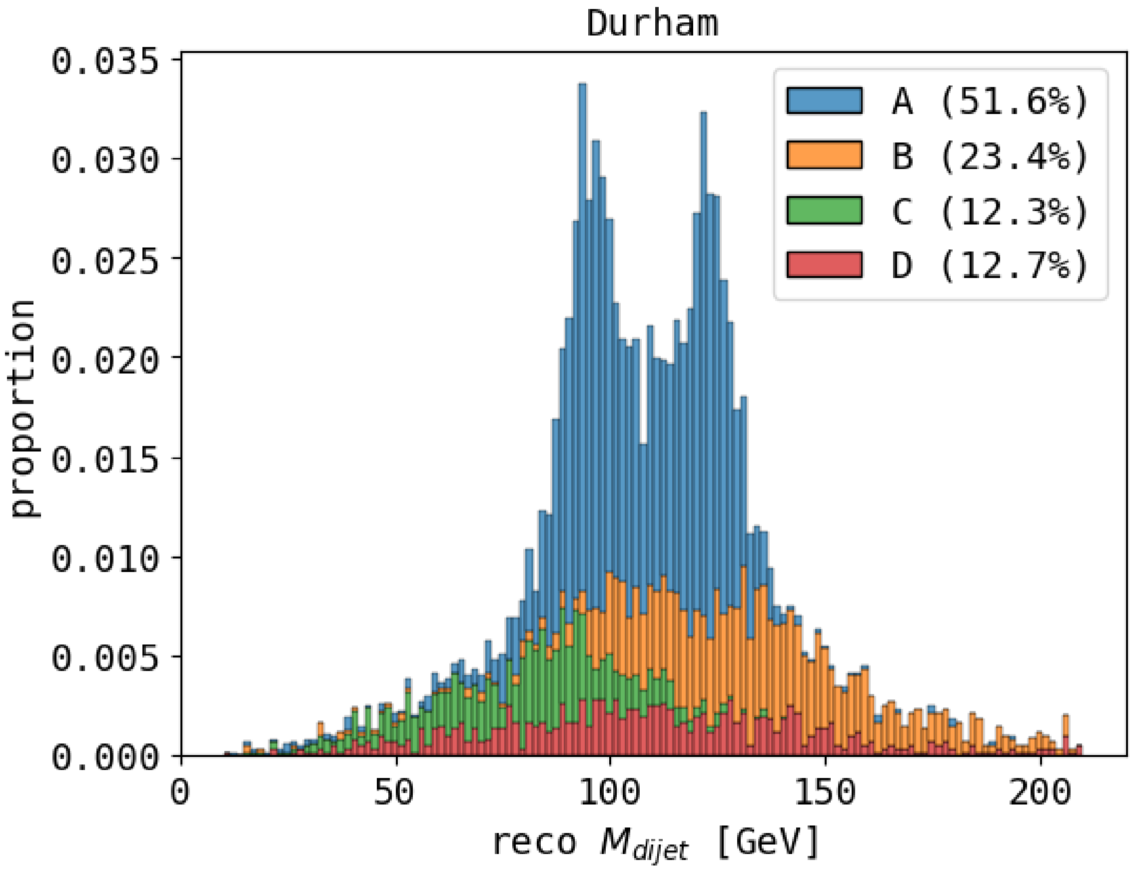
Supervised Jet Clustering

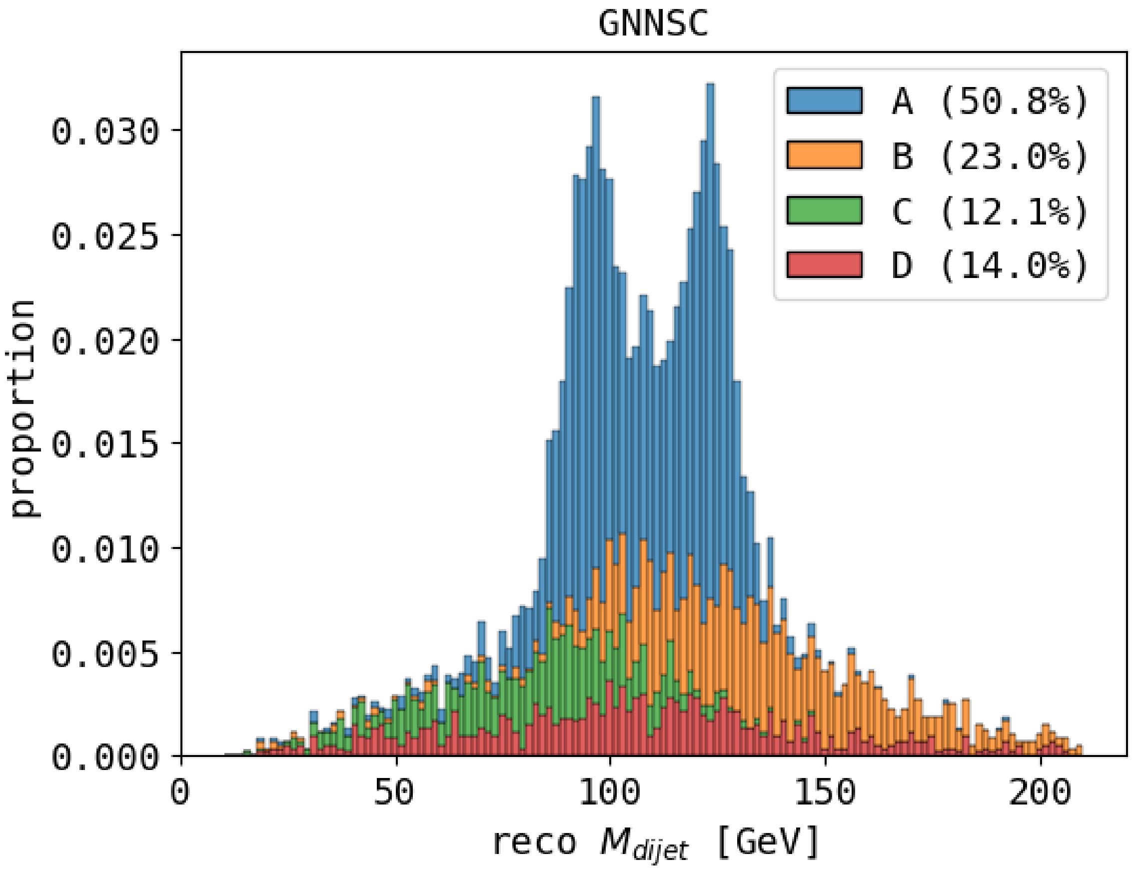
- proof-of-concept ML model (GNNSC) shows performance on par with Durham
  - status: proof-of-concept (Marlin processor available)
  - in the future: investigate more powerful architectures



Jet Clustering on ZZH events

- model was learned on ZHH events; how well does it generalize to ZZH events?
  - again, nearly identical performance of Durham and GNNSC model



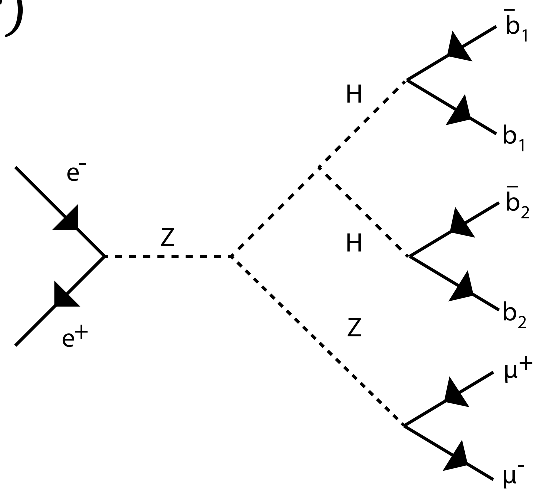


The Matrix Element Method (MEM)

- method for calculating event-likelihoods, i.e. $p(\text{event } \boldsymbol{x}|\text{channel i}) = p_i(\boldsymbol{x})$
  - example use case: separate ZHH vs. ZZH $\rightarrow \mu^-\mu^+ b\bar{b}b\bar{b}$ using likelihood ratio lr

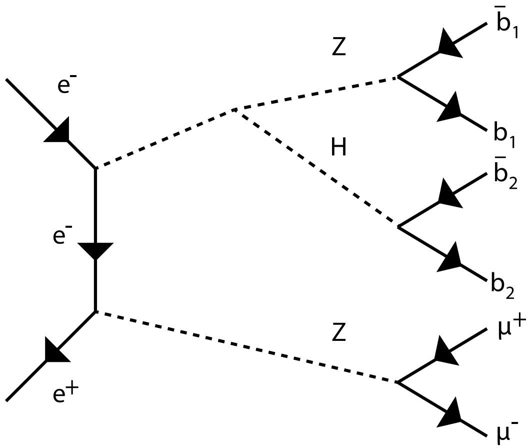
$$\text{lr} = \frac{p_{ZHH}}{p_{ZZH}}$$

  - binary classification by cutting on lr



- for each event $\boldsymbol{y}$ and process i (ZHH, ZZH), solve integral

$$p_i\,(\boldsymbol{y}\,) = \frac{1}{\sigma_i \cdot A_i} \int |M_i(\boldsymbol{x})|^2 W_i(\boldsymbol{y} \mid \boldsymbol{x}) \epsilon_i(\boldsymbol{x}) d\boldsymbol{\Phi}_n(\boldsymbol{x})$$



  - $M_i(\boldsymbol{x})$ LO matrix element
  - $W_i(\boldsymbol{y}|\boldsymbol{x})$ transfer function (TF): PDF for measuring $\boldsymbol{y}$ given $\boldsymbol{x}$; fit from ILD full-simulation samples

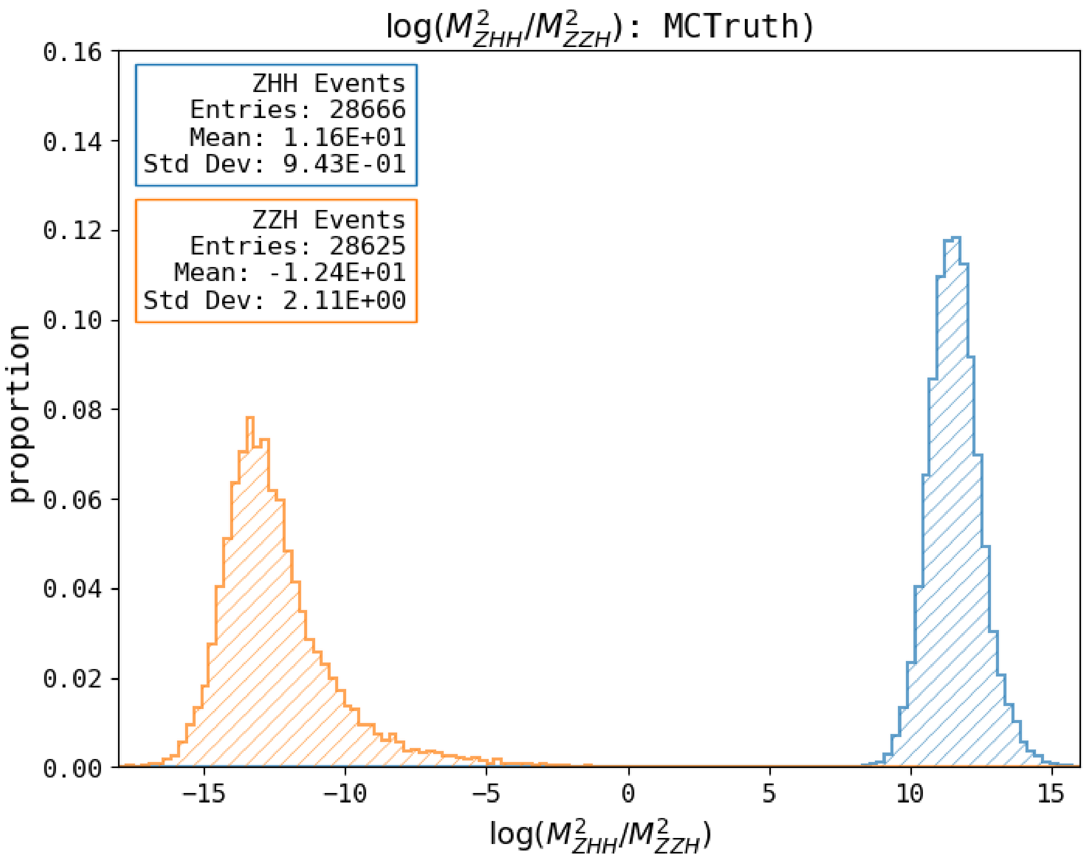
A_i : acceptance of channel i
$\epsilon_i(\boldsymbol{x})$: detector efficiency

MEM Introduction with Examples

generator level check

Event data / MEM type	MC truth	Reco
ME only		
ME+DTF	-	

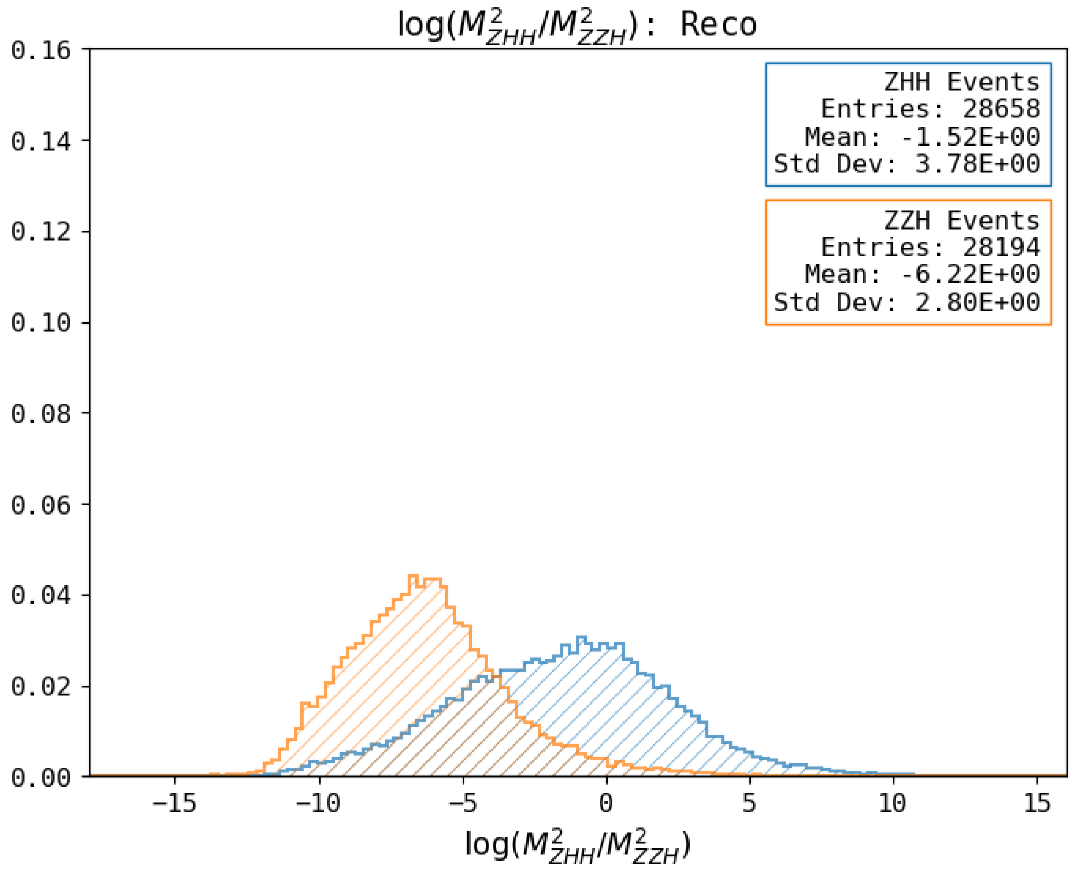
- excellent separation



naive MEM

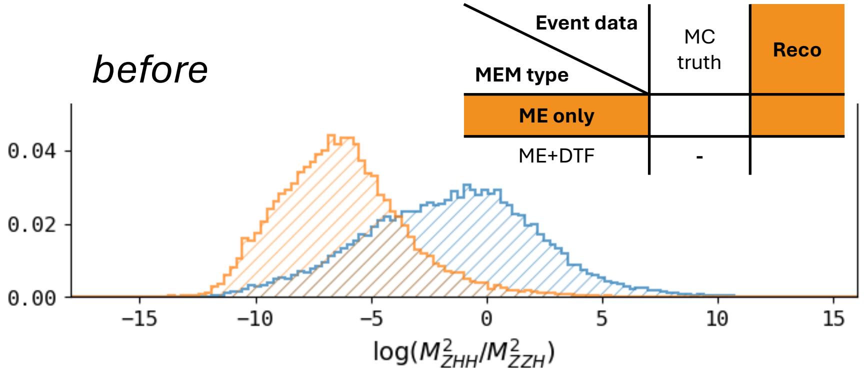
Event data / MEM type	MC truth	Reco
ME only		
ME+DTF	-	

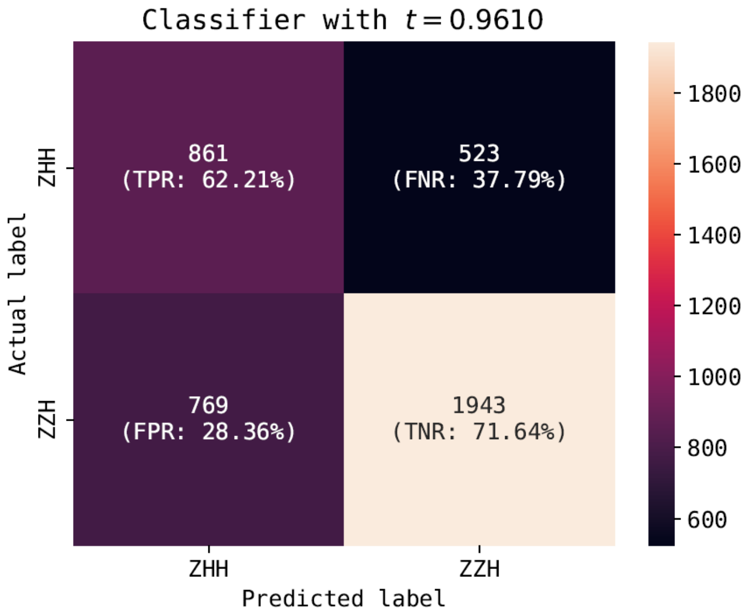
- separation power lost
  ➔ need to describe smearing with TFs

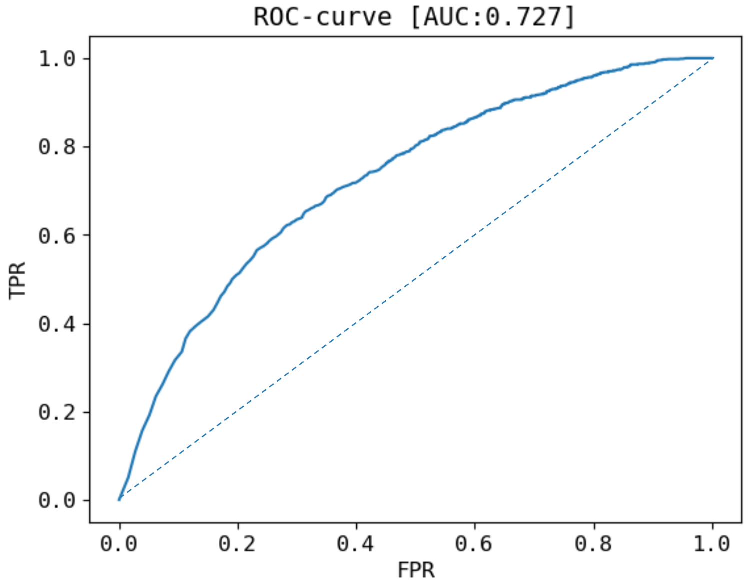


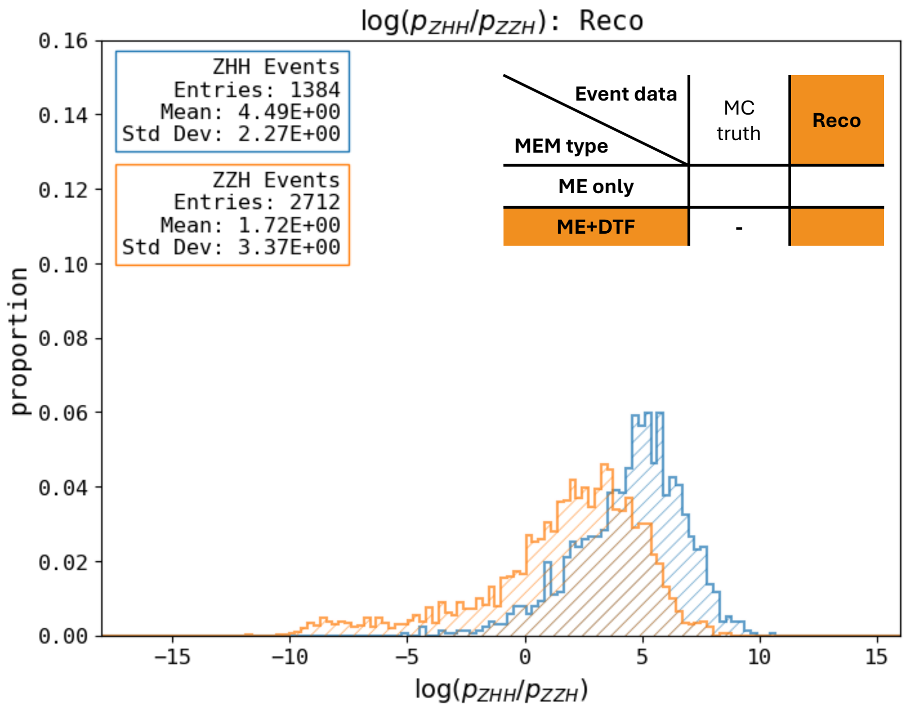
MEM Results

- obtained using VEGAS algorithm
- by including integration over transfer functions, some separation power is regained; $\mathrm{AUROC} = 0.73$





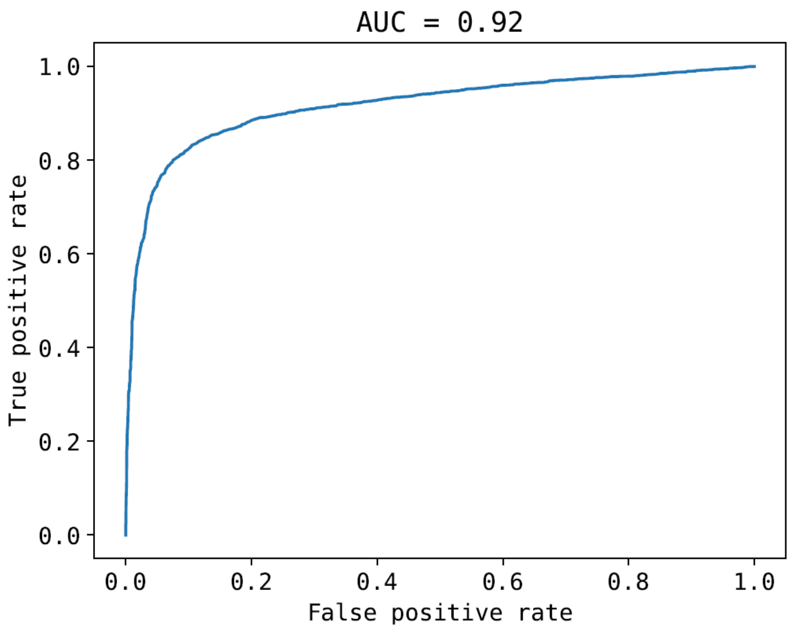




Direct S/B Separation with ML models

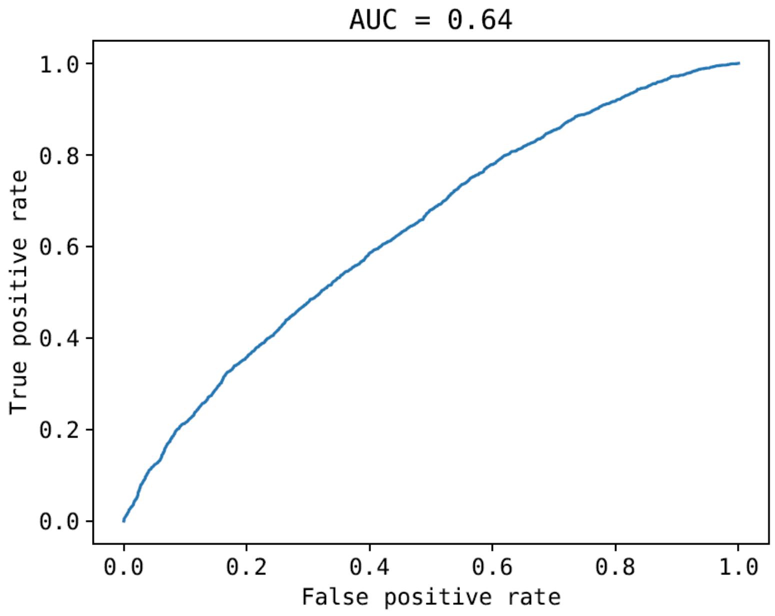
- using different architectures, a binary classifier is learned to again separate ZHH/ZZH
- input data: sets of four-momenta of the muons and b-jets; train/test ratio: 80/20

Benchmark



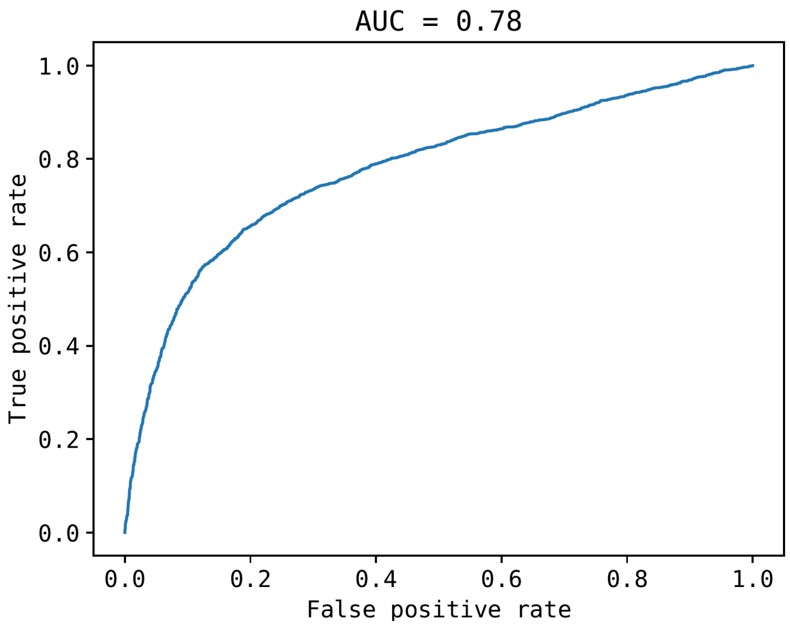
- model: transformer encoder
- data : cheated jet-parton matching

Realistic Model I



- model: permutation invariant (DeepSet)
- data : jets randomly permuted

Realistic Model II



- model: transformer encoder
- data : jets sorted by energy

Conclusion II: The ZHH Analysis with potential future tools

- in existing ZHH analysis: jet clustering as one leading source of uncertainty [Du16]
  - "proof-of-concept" supervised ML model for jet clustering implemented
  - performance approximately on par with current reconstruction (Durham algorithm)
- MEM implemented with example use case of process separation
  - time-complexity remains an issue due to phase space integration
  - in theory, gives access to perfect discriminator
- ML models for direct separation of ZHH/ZZH:
  - demonstrated that jet-parton matching is key information for separation power
  - best separation ($\text{AUROC} = 0.78,\ \text{AvgPrecision} = 67\%$)

General Conclusion

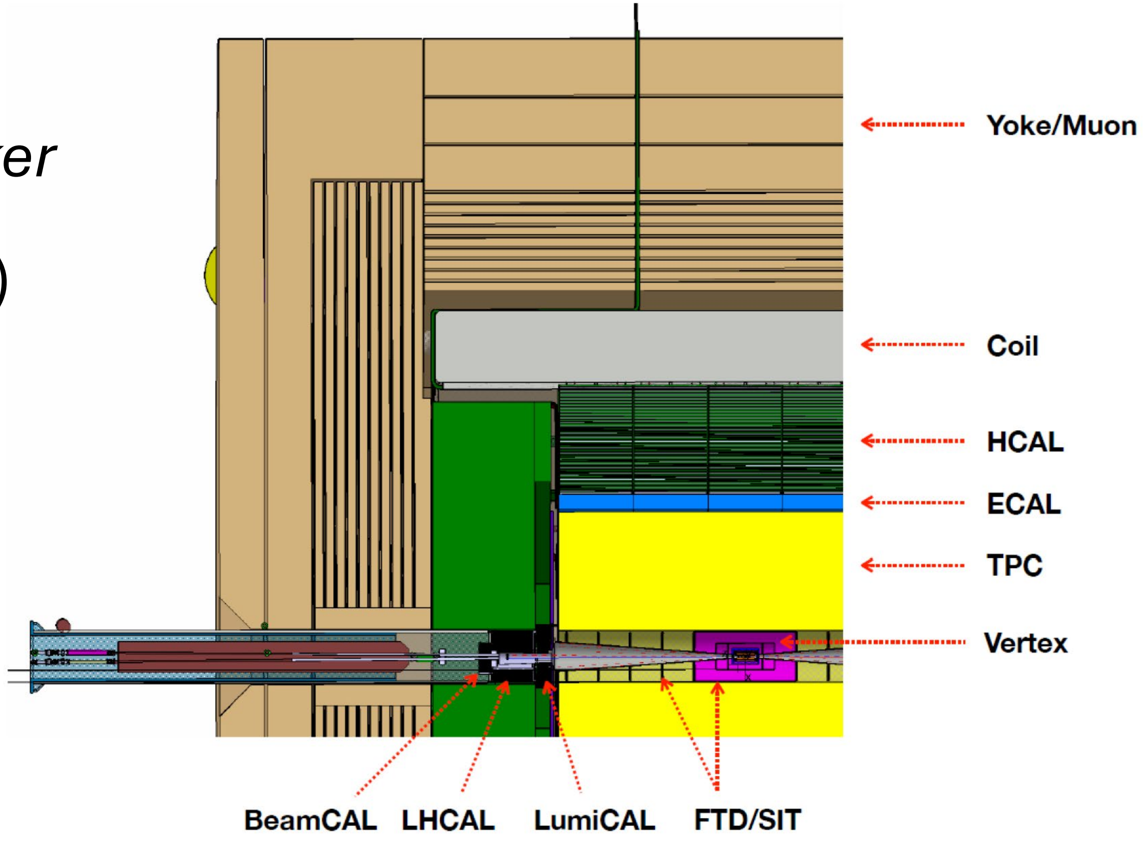
- major improvements in key analysis tools since last ZHH study [Du16]
  - existing SOTA tools are expected to improve the sensitivity on $\Delta\lambda_{SM}$ / λ_{SM} to **better than 20%**
- jet clustering and process separation identified as leading sources of error [Du16]
  - proof-of-concept ML jet clustering on par with Durham
  - MEM implementation and ML models shown to improve channel separation
  - true/reco links from ILD full sim allow unique possibilities for supervised ML
- outlook:
  - new estimates on $\Delta\lambda/\lambda$ with SOTA reconstruction and analysis underway
  - plan for new MC production at $\sqrt{s} = 550\ \text{GeV}$ with SLAC
    currently investigating relevant samples (2f irrelevant?; check 6f, 4f backgrounds)

Thank you for listening!

Backup

The International Large Detector (ILD)

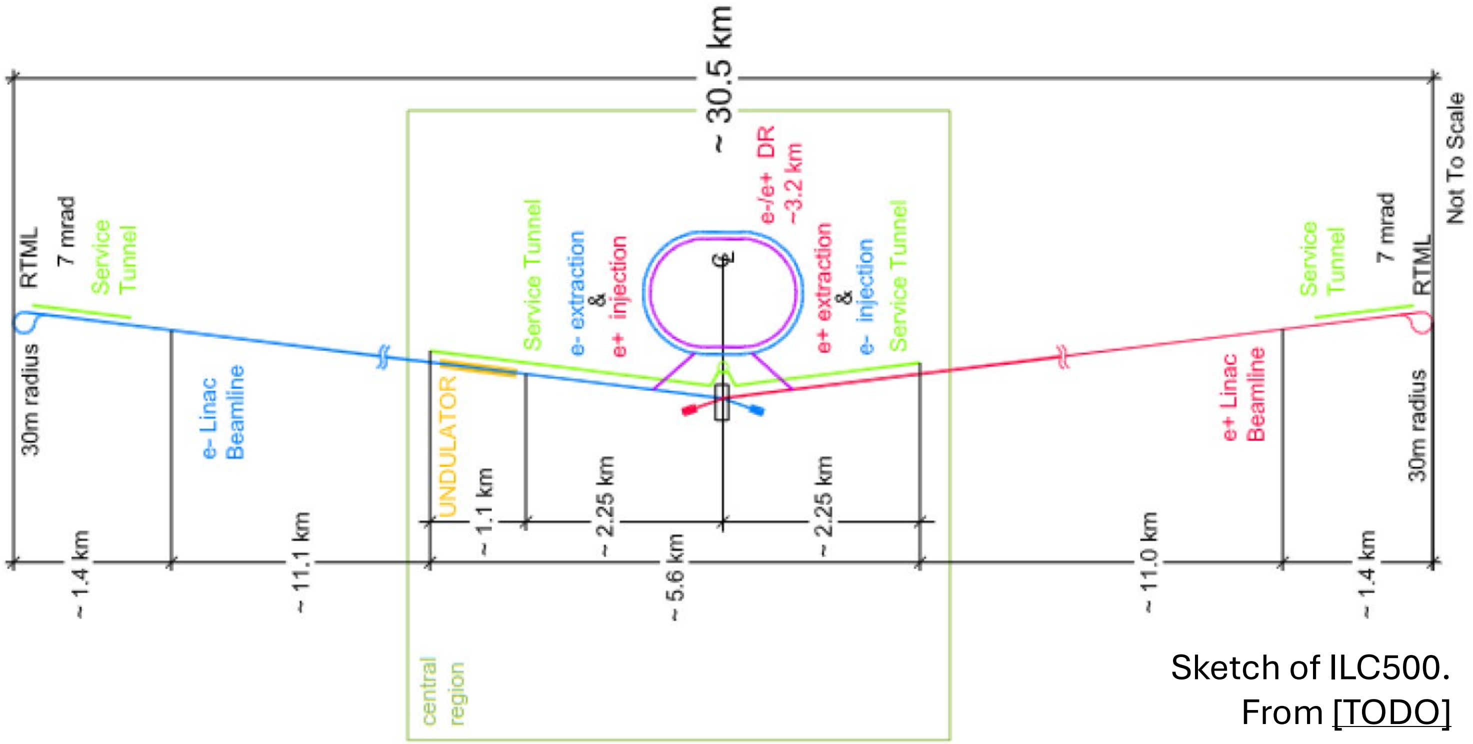
- inner and forward tracker (**SiT, FTD**)
  - precise identification of decay vertices
- time-projection chamber (**TPC**) as main *tracker*
- electromagnetic (**ECAL**) and hadronic (**HCAL**) calorimeters inside magnetic coil to reduce material budget



Quarter-slice through the ILD detector. From [TODO]

The International Linear Collider (ILC)

- linear collider concept with multiple energy stages $\left(\frac{\sqrt{s}}{\text{GeV}} = 250, \mathbf{500}, 1000\right)$
  - $500\ \text{GeV}$ stage allows direct measurements of λ through di-Higgs production
- mature concept (TDR), technologies available (superconducting RF-cavities etc.)



Sketch of ILC500.
From [TODO]

Future Higgs Factories

- goal: high production of Higgs bosons
- e^+e^- colliders for precision measurements
- different concepts proposed:
  - linear (ILC, CLIC, C^3):
    - maximum energy constrained by length
    - *direct* measurements of λ possible
    - measurements with polarized beams possible
  - circular (FCC-ee, CEPC):
    - maximum energy limited by synchrotron radiation
    - higher luminosities through beam reuse

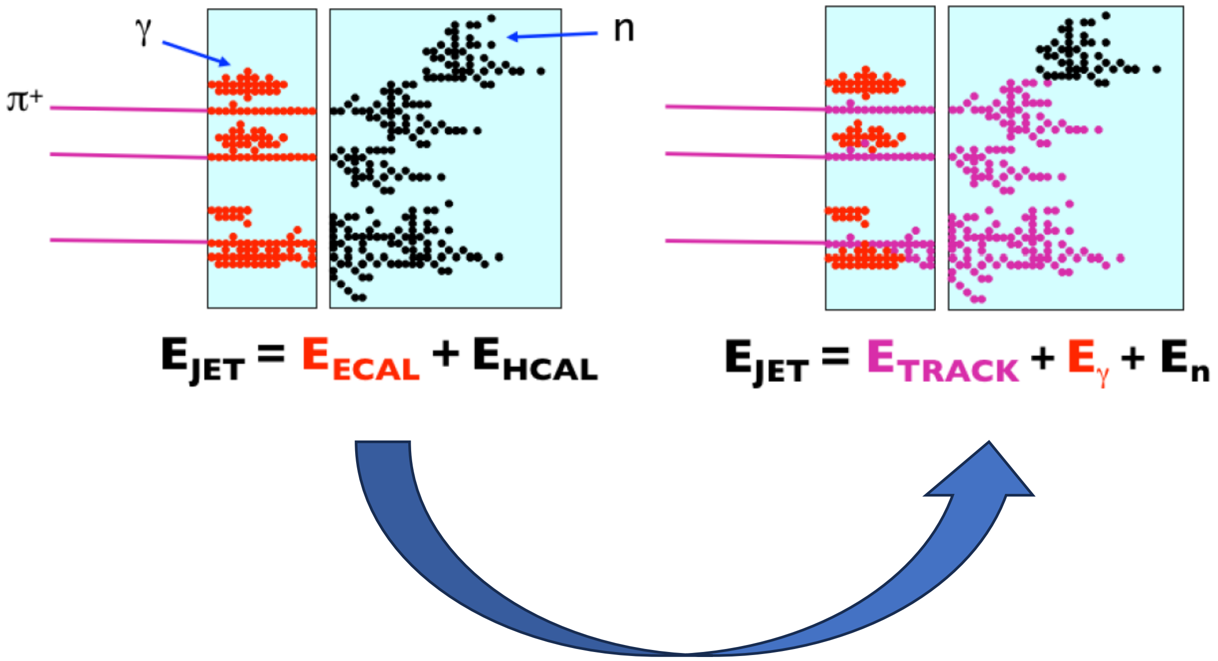
Collider	$\sqrt{s}$	$\mathcal{P}(e^-/e^+)[\%]$	N_{det}	$\mathcal{L}[\text{abarn}^{-1}\text{s}^{-1}]$
ILC	250 GeV	$\pm80/\pm30$	1	2.0
	500 GeV	$\pm80/\pm30$	1	4.0
	1000 GeV	$\pm80/\pm30$	1	8.0
CLIC	380 GeV	$\pm80/0$	1	1.0
	1.5 TeV	$\pm80/0$	1	2.5
	3.0 TeV	$\pm80/0$	1	5.0
C^3	250 GeV	$\pm x/0$	?	1.3
	550 GeV	$\pm x/0$	?	2.4
FCC-ee	M_Z	$0/0$	2	150
	$2M_W$	$0/0$	2	10
	240 GeV	$0/0$	2	5
	$2m_{top}$	$0/0$	2	1.5
CEPC	M_Z	$0/0$	2	16
	$2M_W$	$0/0$	2	2.6
	240 GeV	$0/0$	2	5.6
HALHF	250 GeV	$0/0$	1	≈ 2

Comparison of selected physics programs at the proposed accelerators ILC, CLIC, FCCee, CEPC, C^3 and HALHF. From [Db20]

Particle Flow

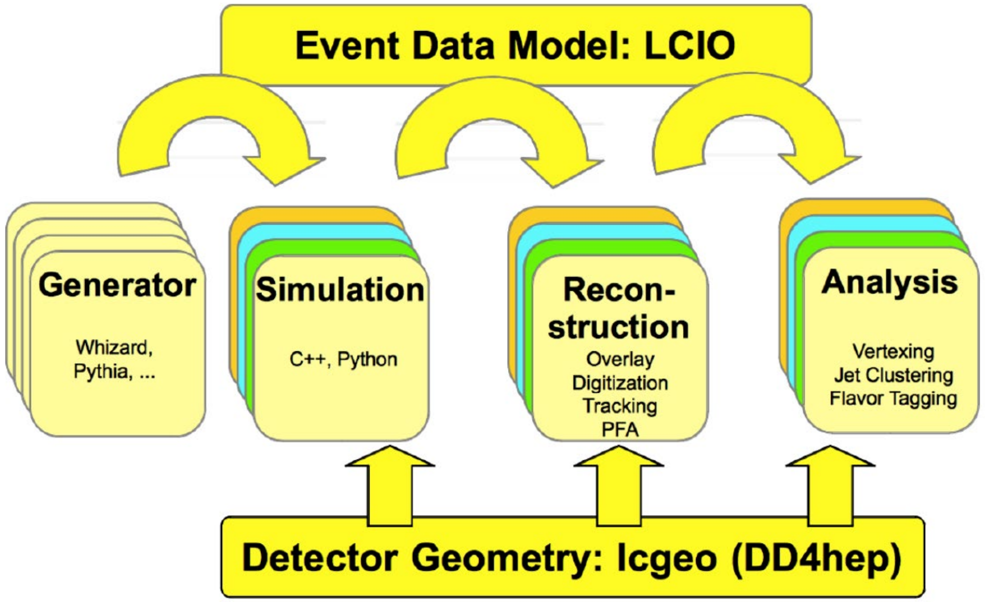
- use best combined information between detectors for highest energy resolution (**Particle Flow objects, PFOs**)
- goal: best jet energy resolution

From traditional to particle flow calorimetry. From [Du16]



Software

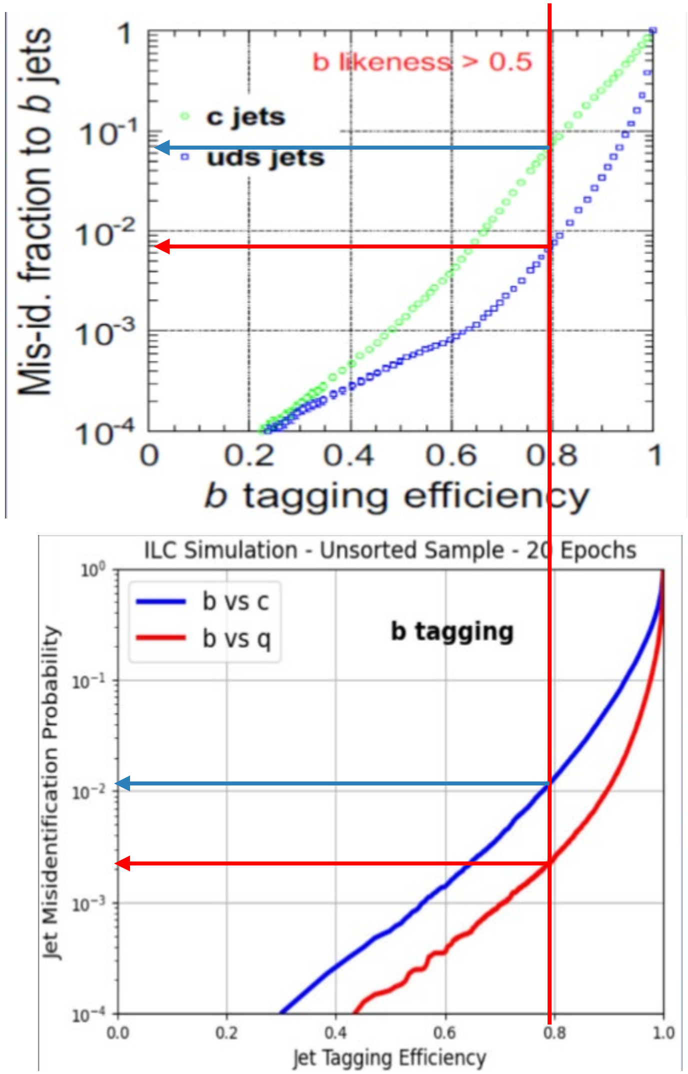
- iLCSoft software stack
- Marlin for reconstruction; important in existing ZHH-analysis:
  - TrueJet: jet-clustering of PFOs using truth information
  - isolated lepton tagging: decision trees for tagging leptons



Event flow in the iLCSoft stack. From [TODO]

Flavor tagging with ML (ParT)

- improved b-tagging efficiency since state-of-the-art projections from 2016
- ML models (DeepJet, ParticleNet, ParT) show highly improved rejection compared to LCFIPlus
- status: ready for use (in MarlinML)



Flavor tagging performance of LCFIPlus (top) vs. ParT (bottom) at ILD full simulation. T. Suehara [2023]

ErrorFlow

- assume full parameterization of errors for individual jets

$$\sigma_{E_{jet}} = \sigma_{Det} \oplus \sigma_{Conf} \oplus \sigma_{\nu} \oplus \sigma_{Clus} \oplus \sigma_{Had} \oplus \sigma_{\gamma\gamma}$$

  - σ_{Det}: detector resolution — Y. Radkhorrami [2022]
  - σ_{Conf}: particle confusion in particle flow algorithm
  - σ_{ν}: neutrino correction
- status: in production (in MarlinReco)

Durham jet clustering

- Durham algorithm: common jet-clustering method at e^+e^--colliders
  - sequential algorithm: cluster objects (here: PFOs) i and j together by lowest test variable y_{ij} until either a cut $y_{ij} > y_{cut}$ or a number of jets is reached; in Durham:

$$y_{ij} = \frac{M_{ij}^2}{Q^2}$$

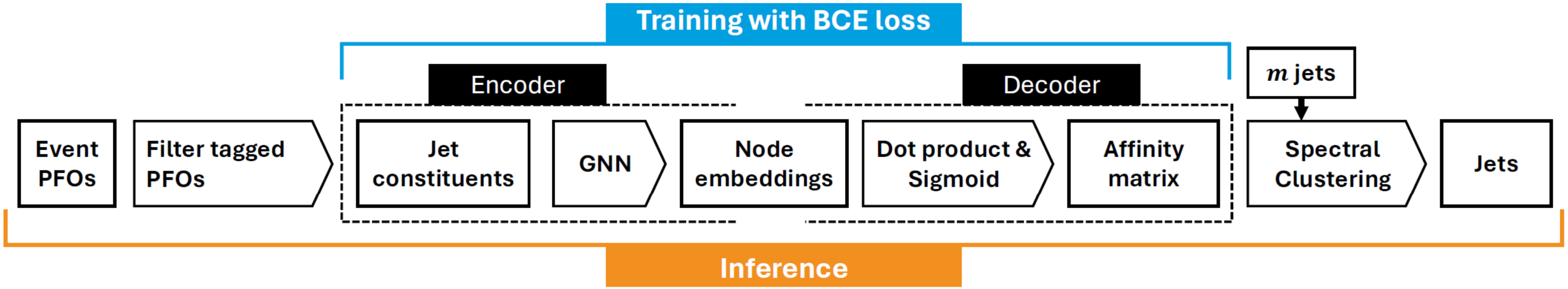
$$M_{ij}^2 = k_\perp^2 = 2\min\left(E_i, E_j\right)^2 \cdot \left(1 - \cos\theta_{ij}\right)$$

  - is **IRC-safe**: same result when arbitrarily soft/colinear input objects are added

Architecture: Supervised Jet Clustering with GNNs

TransformerConv operator from the paper *Masked Label Prediction: Unified Message Passing Model for Semi-Supervised Classification* [Sh20].

- here: implemented as hybrid model (**GNNSC**)
  - training a GNN in supervised manner to calculate edge scores
    here: using TransformerConv layer (implements message-passing and graph attention)
  - spectral clustering (SC) to build "jets"

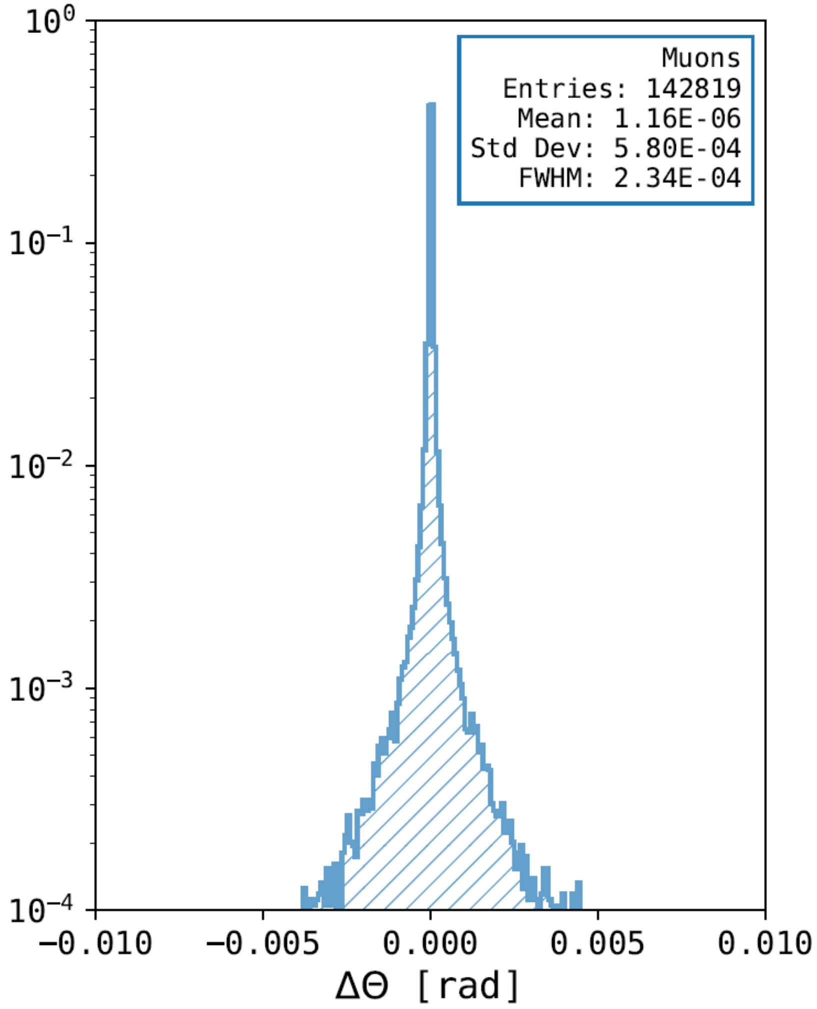


- advantages:
  - permutation invariant by construction
  - straightforward implementation
- disadvantages:
  - not fully differentiable
  - no inherent IRC-safety

Assumptions for the MEM

- assumptions:
  - same acceptance A_i for $i = \mathrm{ZHH}, \mathrm{ZZH}$ hypotheses
  - ignore efficiency $\epsilon_i(\boldsymbol{x})$
  - TF factorizes: $W_i(\boldsymbol{y}|\boldsymbol{x}) = \prod_{j=\text{final state particles}} W_{ij}(\boldsymbol{y_j}|\boldsymbol{x_j})$
  - components of TF can be parameterized in differences e.g. $W_{ij}(\boldsymbol{E^{reco}}|\boldsymbol{E^{true}}) = \widehat{W}(\Delta E = \boldsymbol{E^{reco}} - \boldsymbol{E^{true}})$
  - muon kinematics (energy + angles) perfectly measured
  - narrow width approximation (NWA): Higgs boson width is small w.r.t. mass <-> propagator delta peaked
- dimensionality of integral reduced from 18 to 11
  - further reduction to 7 by integrating out four momentum conserv.

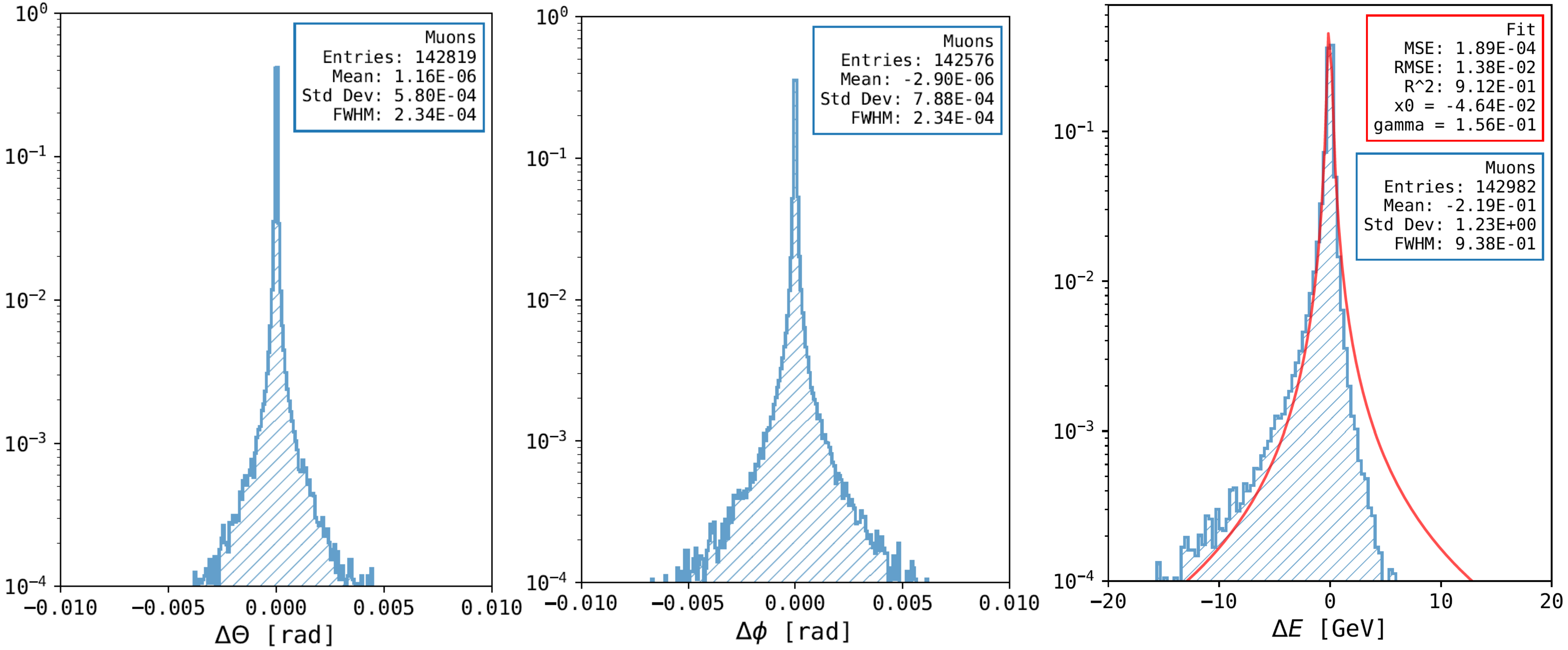
Example TF : $W_{\mu^\pm,(\theta,\phi)} = \theta^{Reco}_{\mu^\pm} - \theta^{True}_{\mu^\pm}$



MEM Transfer Functions – Muons

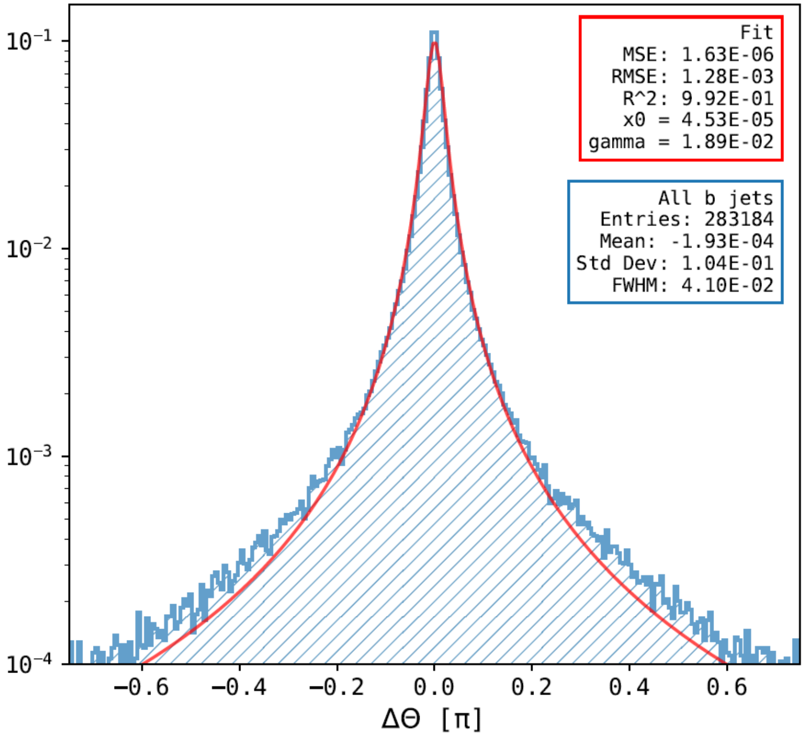
Angles $W_{\mu^\pm,(\theta,\phi)} = (\theta,\phi)^{Reco}_{\mu^\pm} - (\theta,\phi)^{True}_{\mu^\pm}$

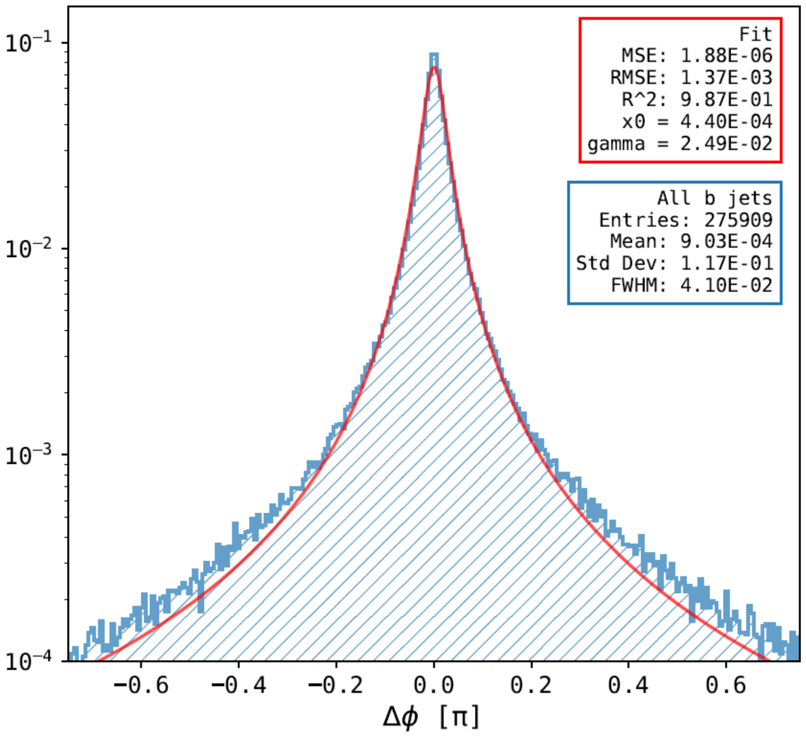
Energy: $W_{\mu^\pm,E} = E^{Reco}_{\mu^\pm} - E^{True}_{\mu^\pm}$



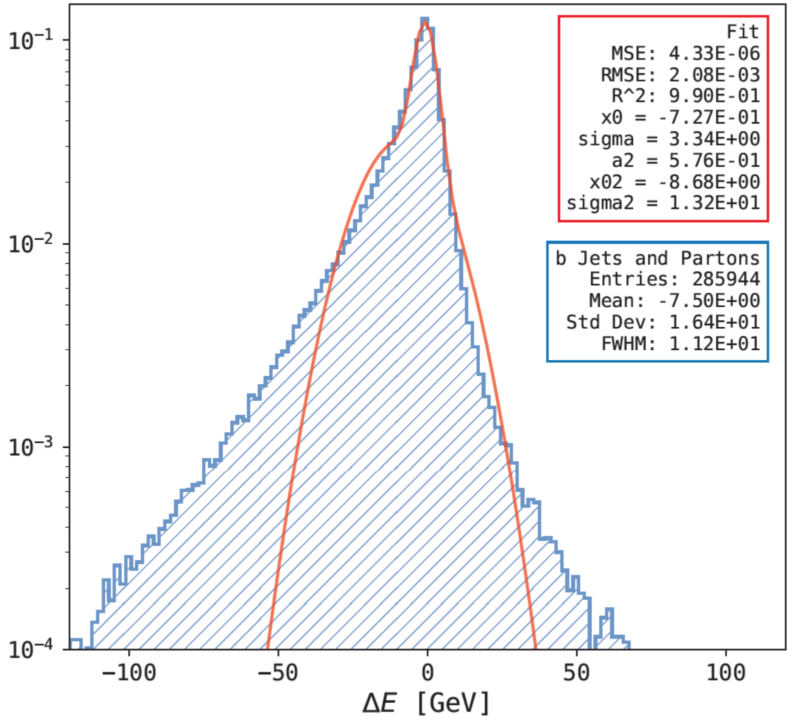
MEM Transfer Functions – Jets/b and $\bar{b}$ quarks

Angles $W_{b,(\theta,\phi)} = (\theta,\phi)_b^{Reco} - (\theta,\phi)_b^{True}$





Energy: $W_{b,E} = E_b^{Reco} - E_b^{True}$

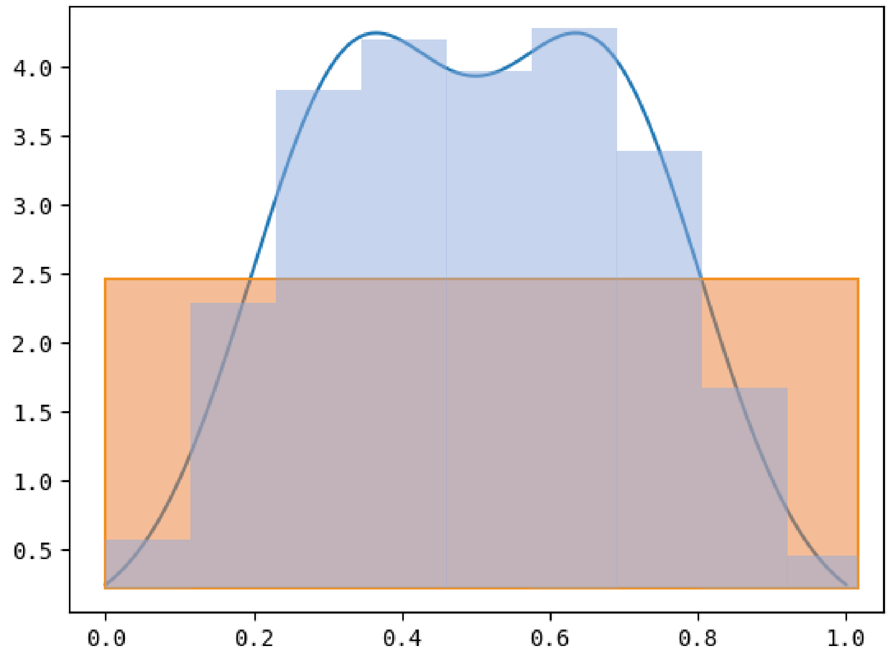


Solving the MEM integral

- problem: the chosen phase space parametrization is 7-dim.: efficient evaluation?
- solution: Monte Carlo (MC) integration

$$E_{p(x)}[I(f)] = \frac{1}{n}\sum_{i}^{n} f(x_i);\; x \sim p(X)$$

$$\sigma = \frac{\sqrt{E[(f - E[f])^2]}}{\sqrt{n}}$$



  - crude MC: uniform sampling; in every dim: $p(x) = \frac{1}{a-b}$
  - importance sampling: sample from proposal $x \sim q(x)$
    - need to find proposal dist. $q(x)$ that fits integrand without knowing integral
    - the "better" q, the faster the variance decreases
    - many approaches: e.g. VEGAS algorithm, neural importance sampling (NIS)

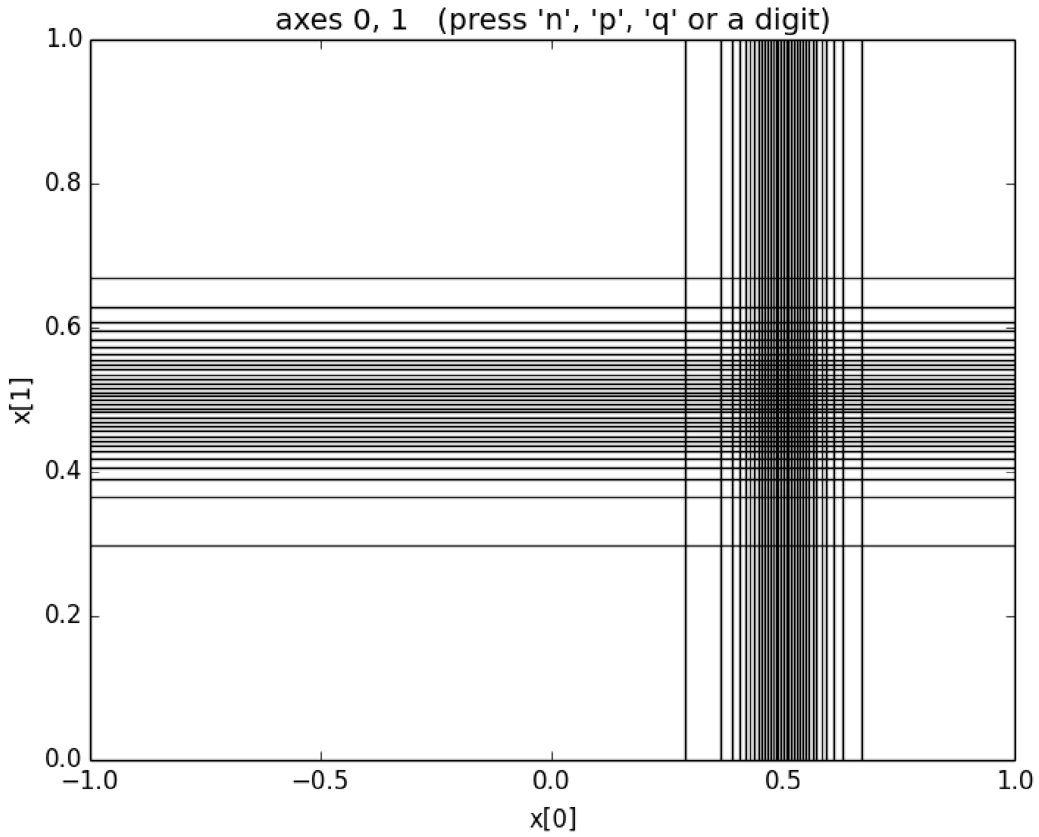
VEGAS Importance Sampling MC

- assume the integrand factorizes

$$f(x) = \prod_{i}^{n} f_i(x_i)$$

- divide each dimension into n bins with equal probability
- adjust the **bin widths** to sample more often in the more important regions

Example of a VEGAS grid after adaption



Source

Neural Importance Sampling MC

- principle
  - from a known base distribution u $\sim \pi(u)$
  - use ML to learn a **bijective and differentiable function** g to transform u to a more complex distribution

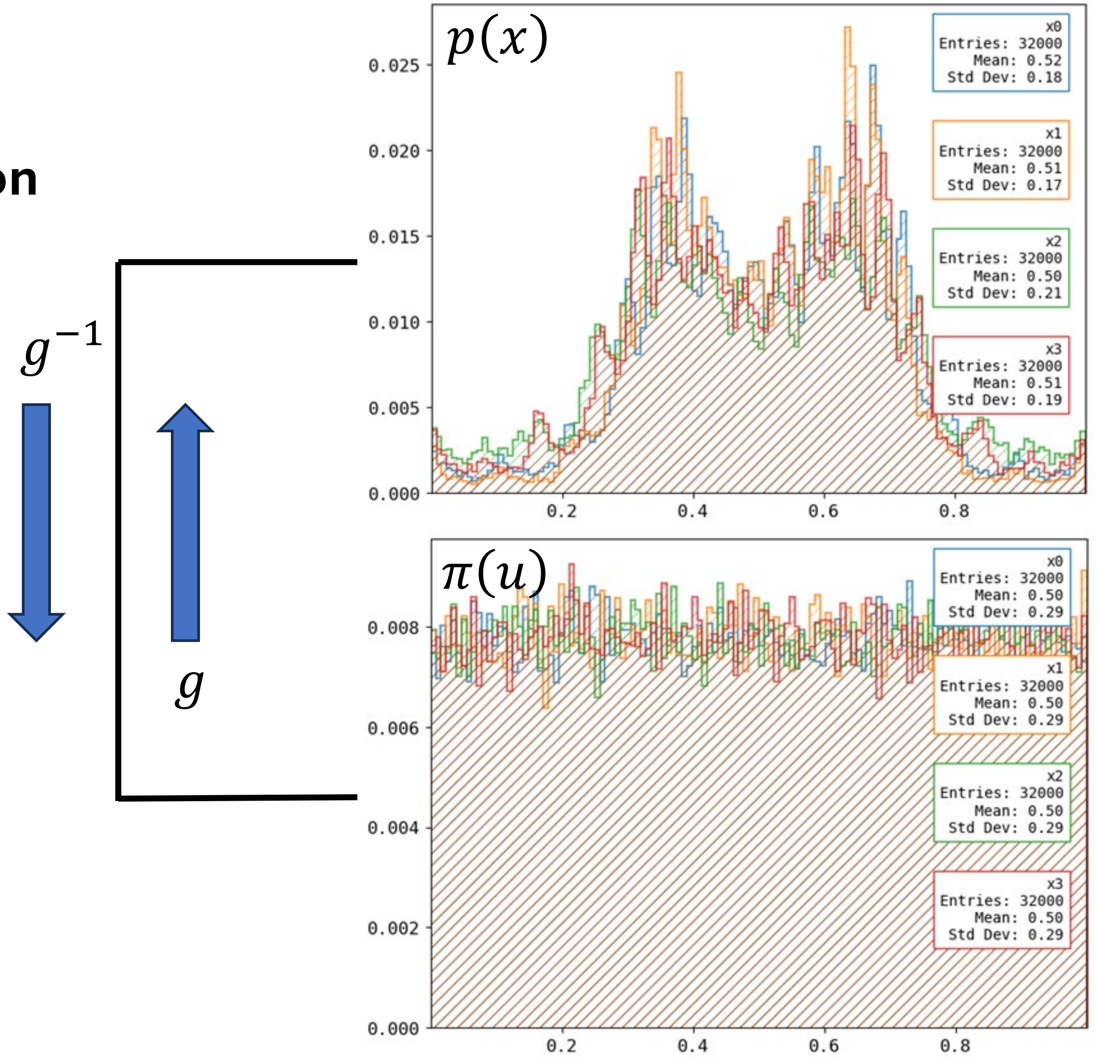
$$x = g(u)$$

- PDF of x given by change of variables formula

$$p(x) = \pi(g^{-1}(x)) \left|\det\left(\frac{\partial g^{-1}}{\partial x}\right)\right|$$

- here: transformation using piecewise rational quadratic spline

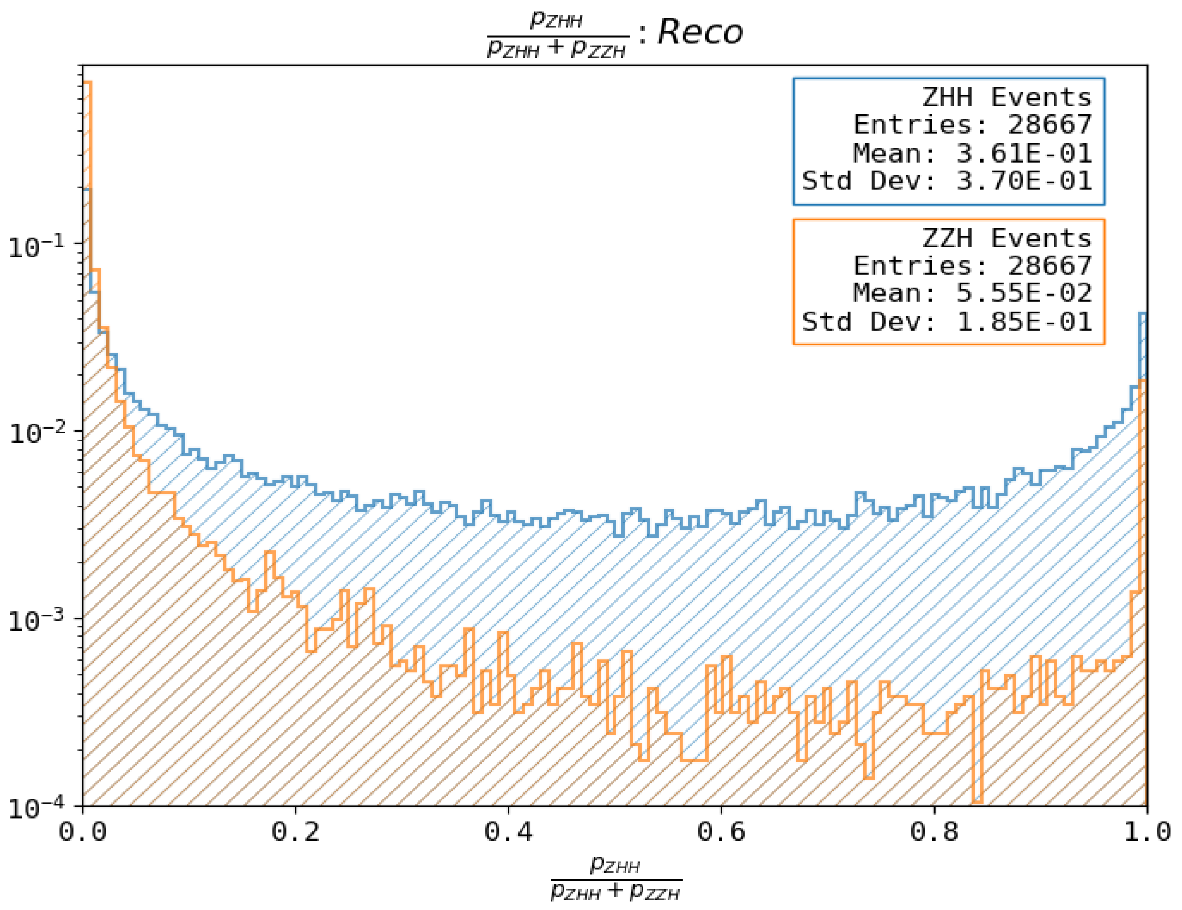
Before/after the flow: Example marginal distribution



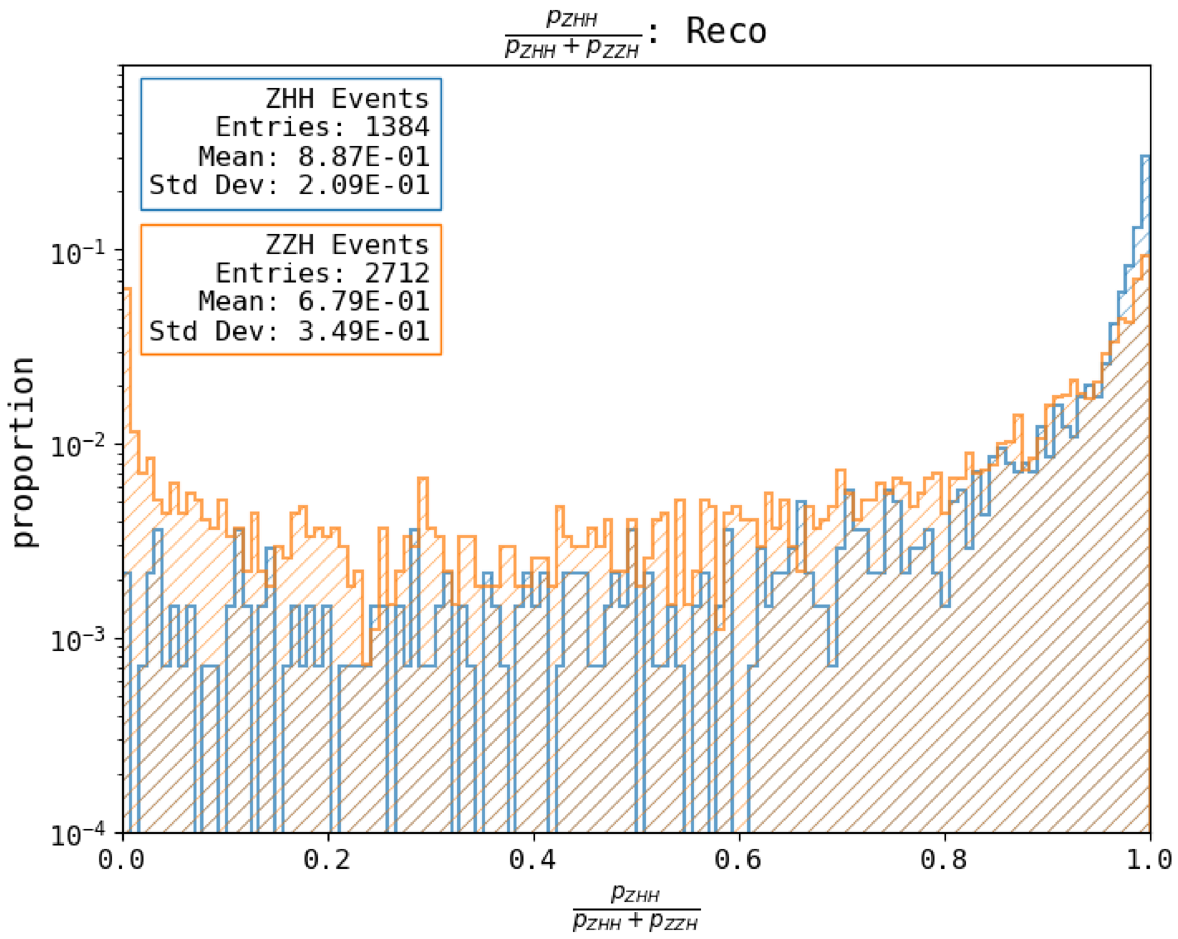
[arXiv:1410.8516] : NICE: Non-linear Independent Components Estimation
[arXiv:1808.03856] :Neural Importance Sampling
[arXiv:1906.04032] : Neural Spline Flows
[arXiv:2001.05486] : i-flow

MEM Results

Generator level: cross-x normalized ME only



VEGAS full MEM



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