



Simulation and theoretical studies towards HEP applications of plasma accelerators

Maxence Thévenet – DESY

10.07.2024, LCWS24

The University of Tokyo, Japan

- A plasma injector for Petra IV
- Flat beams in plasma accelerators

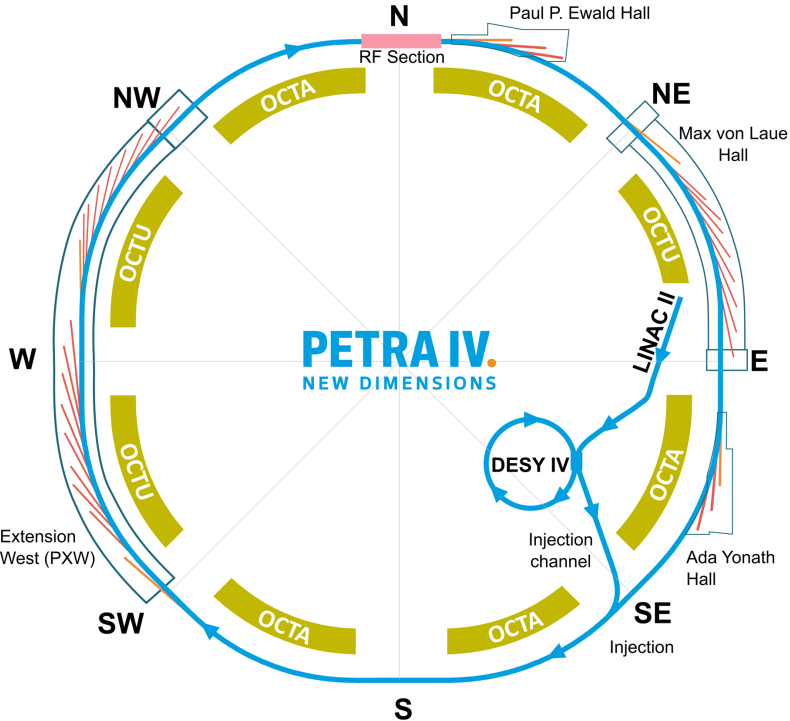


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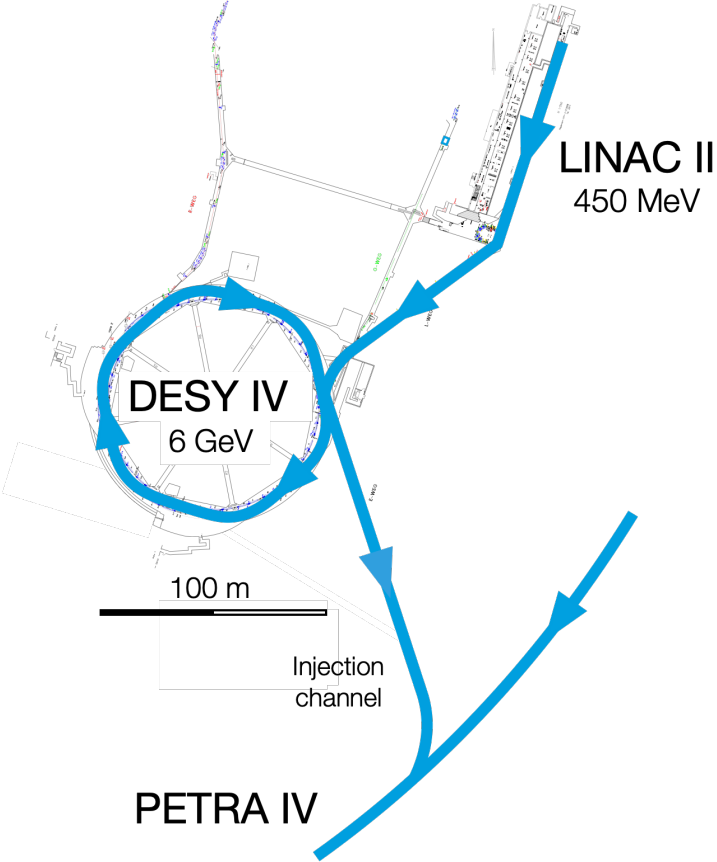
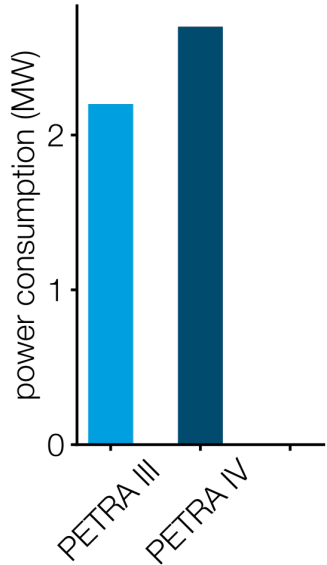
I. Agapov, S. Antipov, R. Brinkmann, A. Ferran Pousa, S. Jalas, L. Jeppe, M. Kirchen, W. P. Leemans, A. R. Maier, **A. Martinez de la Ossa**, J. Osterhoff, R. Shaloo, M. Thévenet, P. Winkler

Petra IV: record brightness for 6 GeV storage ring

Petra IV [1] is the upgrade of the Petra III storage ring for synchrotron radiation (2.3 km, 6 GeV), proposing orders-of-magnitude increase in x-ray brightness.



Injector power usage (during injection)



[1] https://www.desy.de/research/facilities_projects/petra_iv

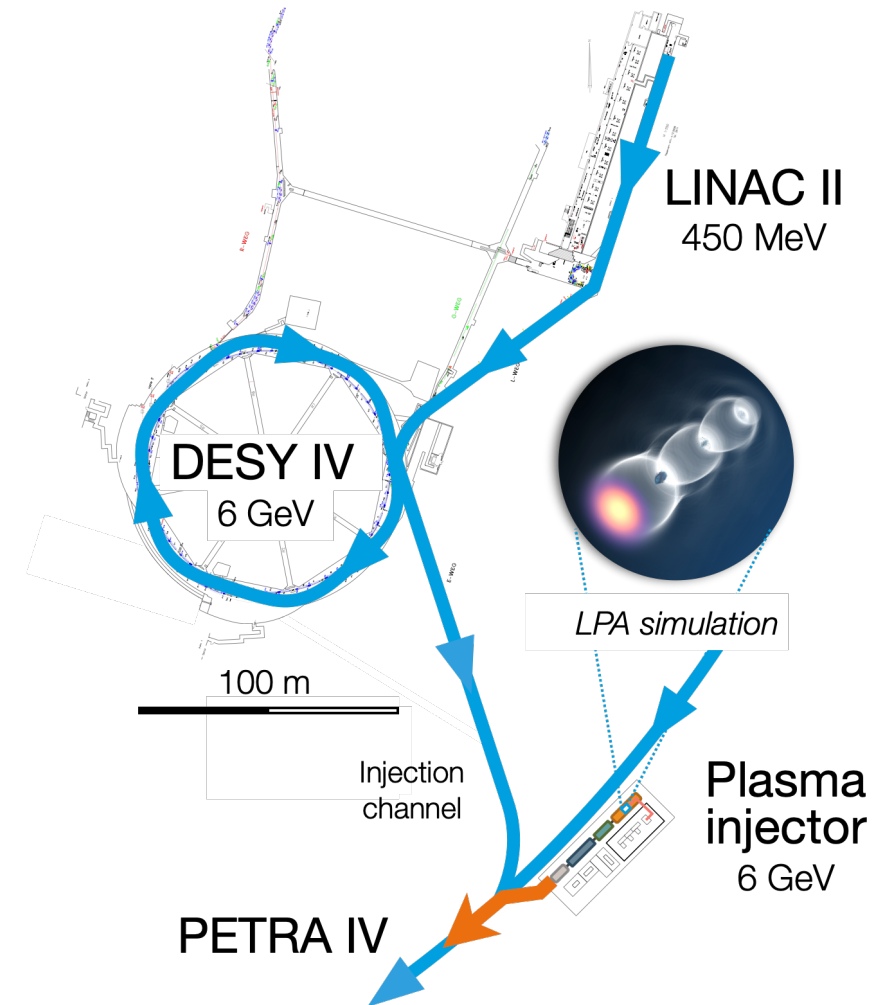
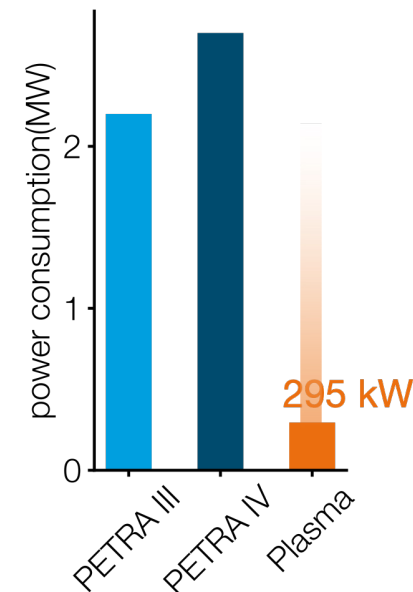
A plasma-based solution could be compact and energy efficient

- **Compact** – Laser-plasma acc. + beamline: < 50 m
- **Cost-effective** – Power consumption: < 500 kW
- **Competitive** – Full PETRA IV operation (fill + top-up)

Key challenges

- Energy gain **6 GeV**
- Energy spread and jitter: **< 0.3 %**
to maximize charge throughput and stability
- Charge injection rate: **≥ 2.6 nC/s**
to fill the ring in < 10 minutes
- Availability: **≥ 98%**
for users' satisfaction

Injector power usage
(during injection)



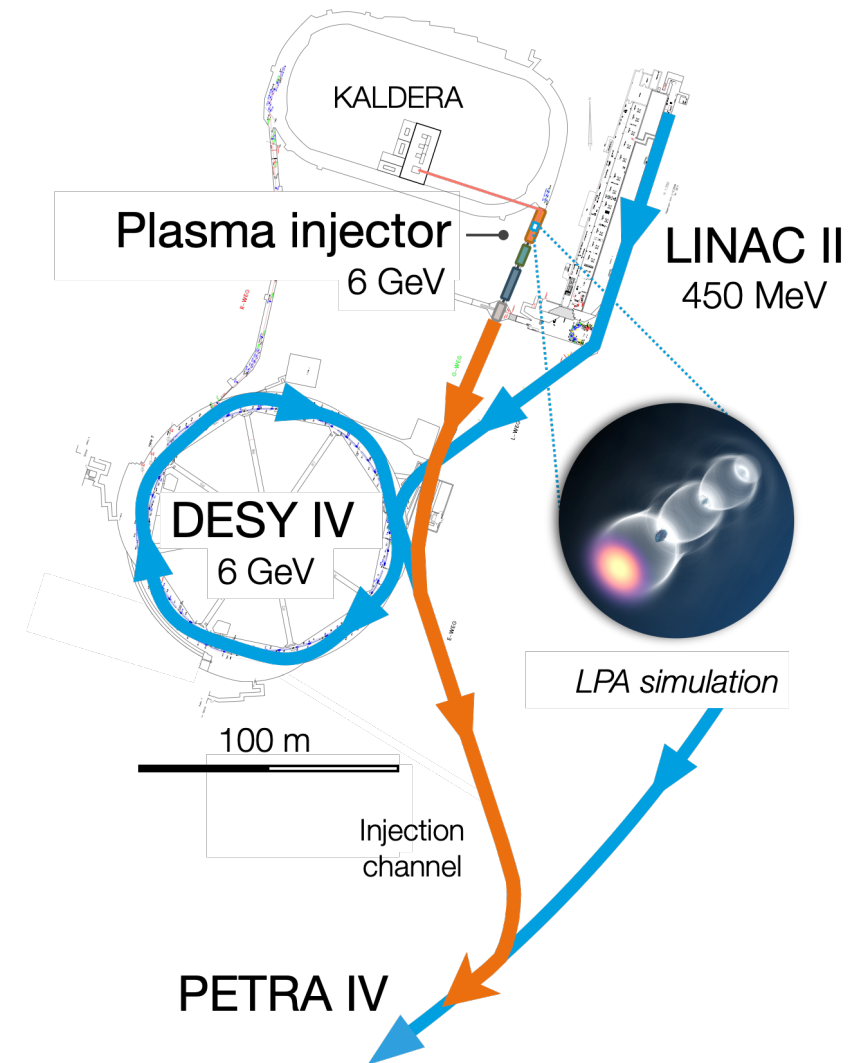
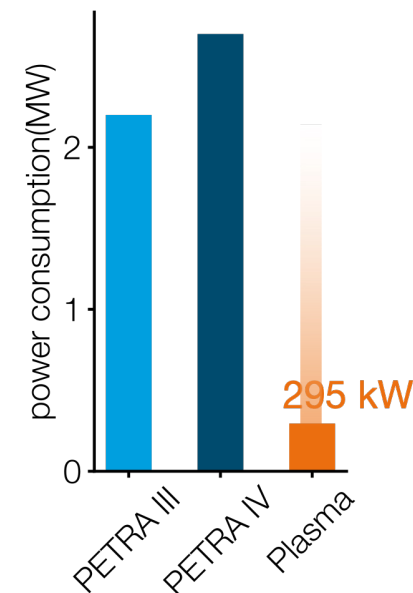
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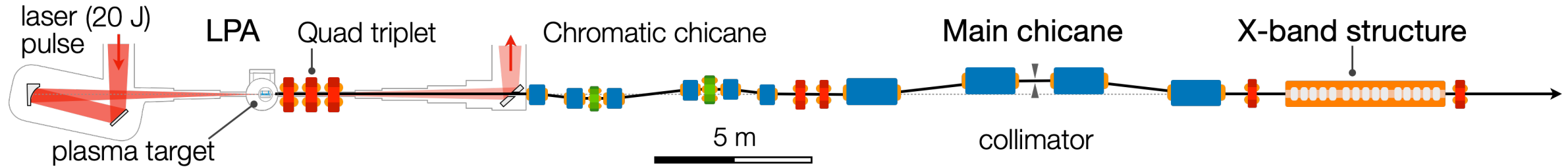
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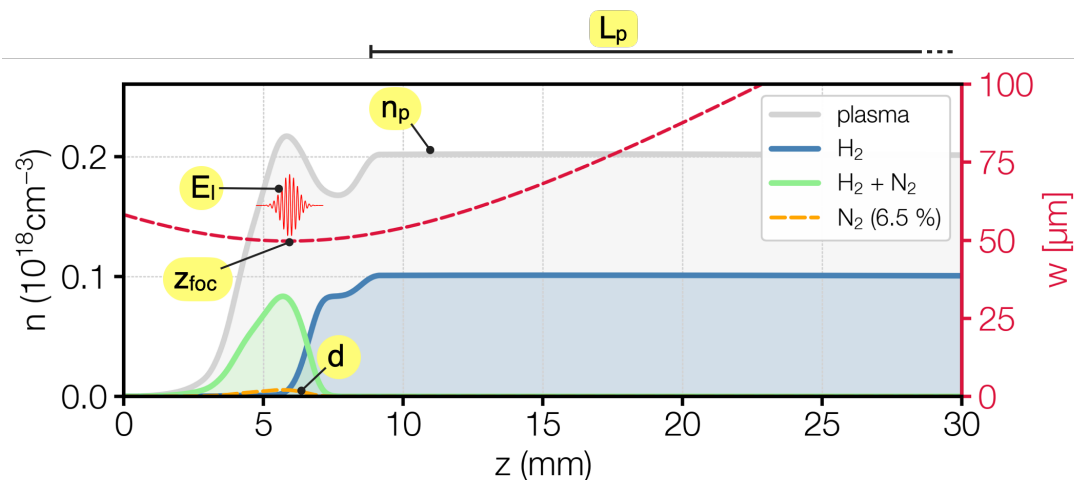
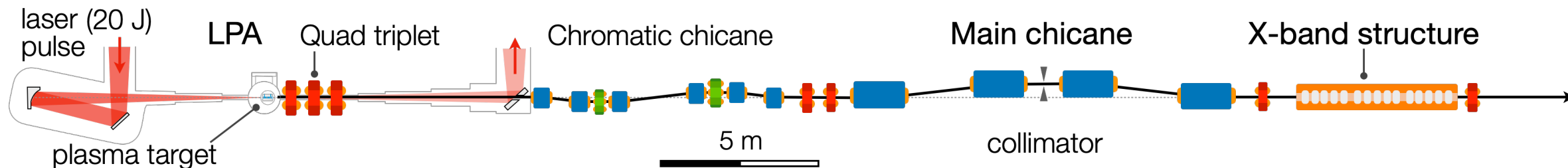


The plasma injector design: reliable LPA + energy compression



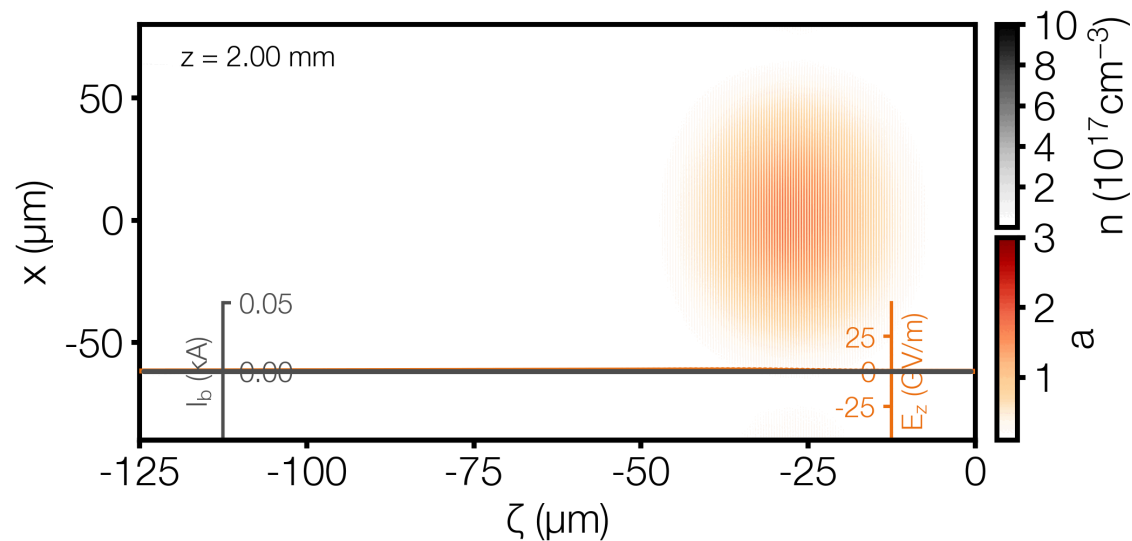
- Combines successful LPA development at DESY (LUX) and laser guiding.
- Energy compression beamline (ECB) to improve energy bandwidth and stability.
- State-of-the-art numerical tools and advanced optimization.

The LPA: controlled injection and guiding in stable operation (LUX)

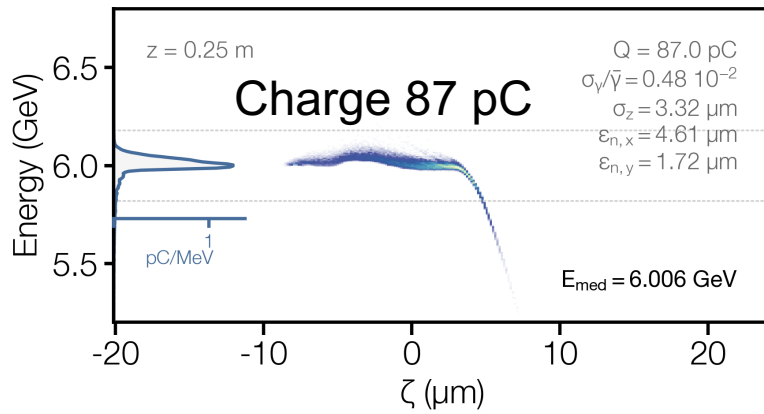
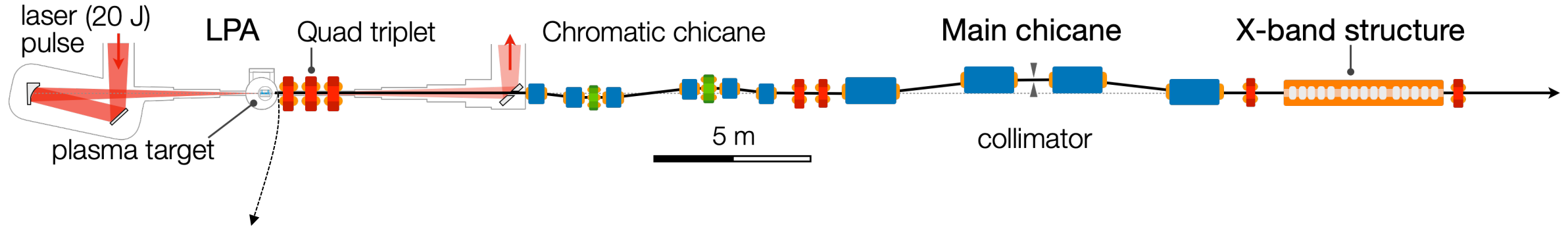


Laser pulse: Flattened Gaussian $a_0 = 2.0$, $w_0 = 50 \mu\text{m}$, 345 TW, 53 fs, 19.6 J.

Plasma target: LUX-type profile $n_p = 2 \times 10^{17} \text{cm}^{-3}$, 22 cm plateau. Transversely parabolic (HOPI) $w_m = 50 \mu\text{m}$



The ECB: controlling/correcting the beam's energy spectrum

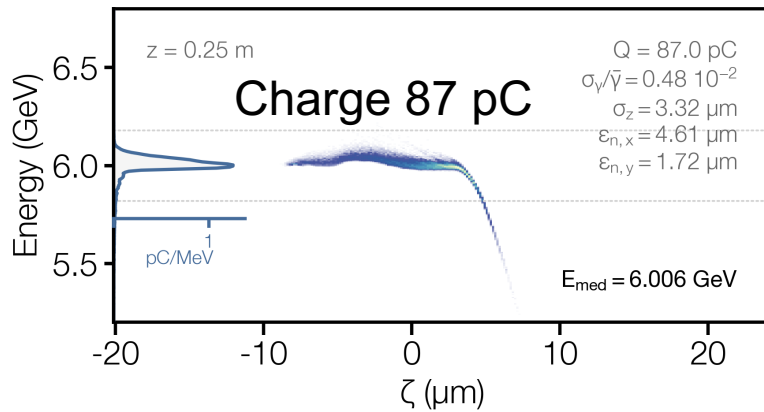
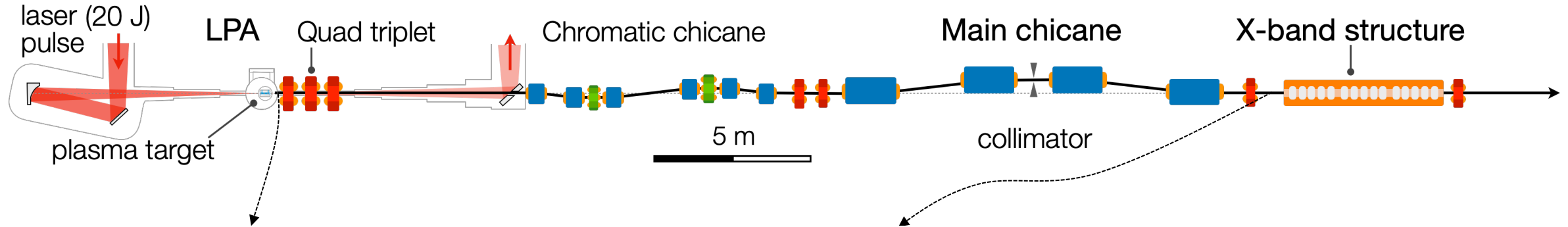


After LPA

$$\Delta\mathcal{E}/\mathcal{E} = 0.5\% \quad L = 3 \mu\text{m}$$

Norm. emittance: 4.6 μm and 1.7 μm .
 Divergence: 0.22 mrad and 0.12 mrad.
 Efficiency: 2.7 %

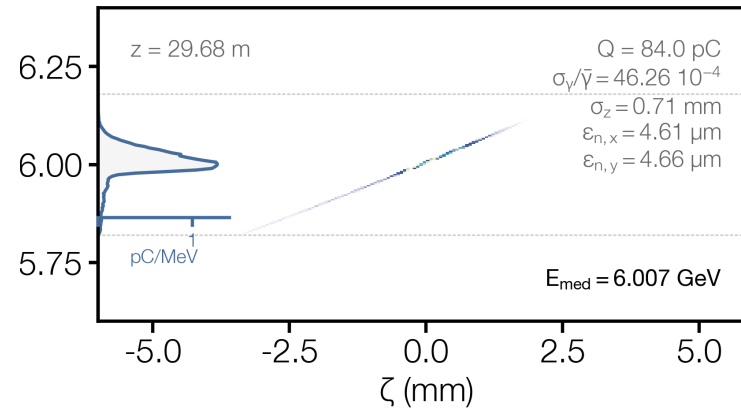
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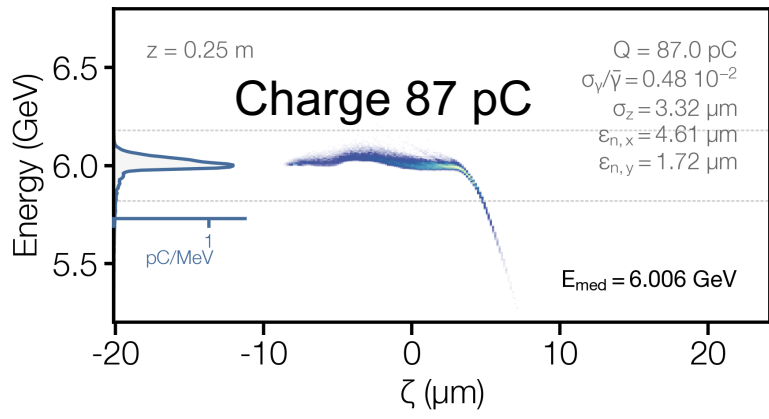
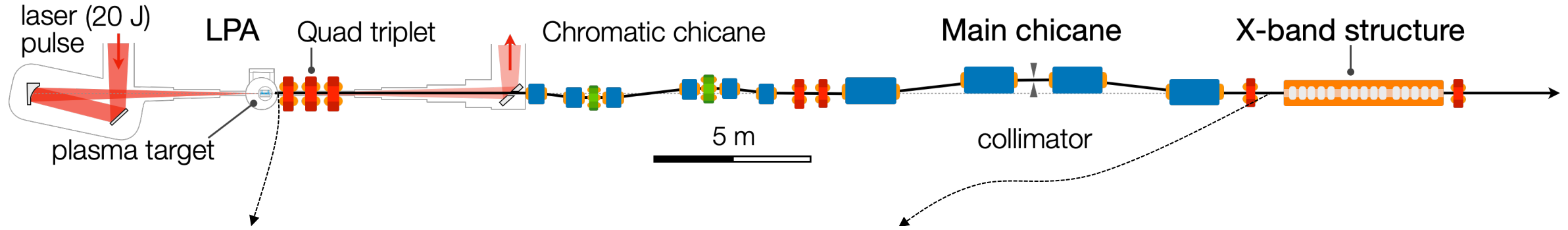
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After chicanes

$$\Delta\mathcal{E}/\mathcal{E} = 0.5\% \quad L = 710 \mu\text{m}$$

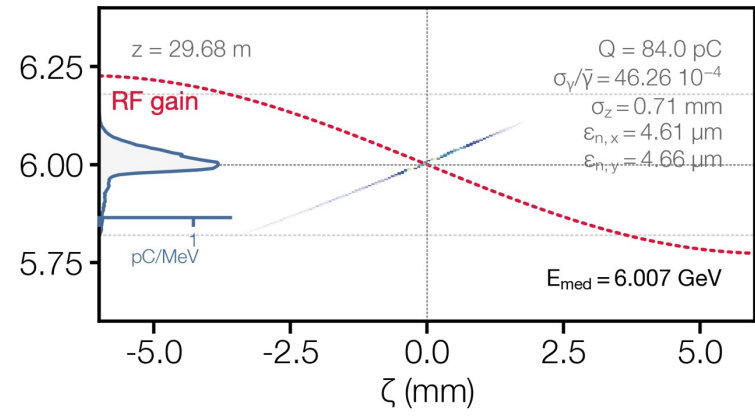
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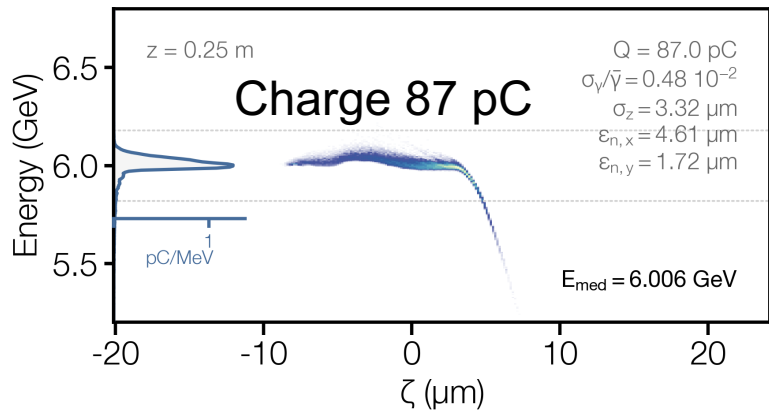
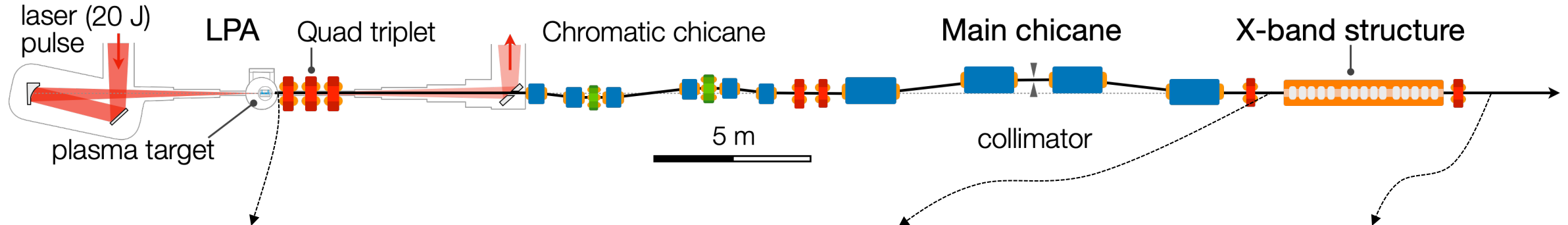
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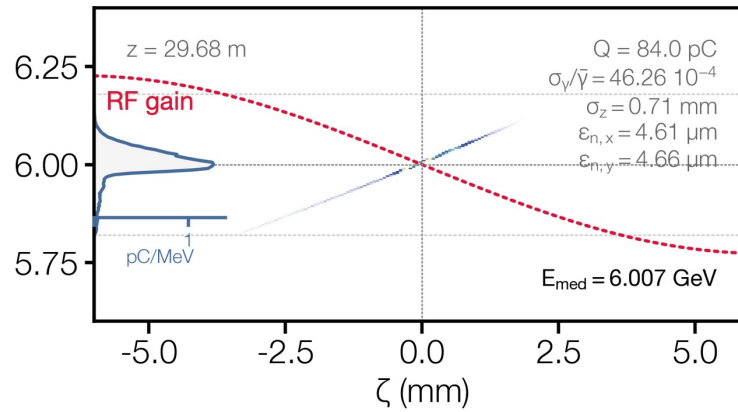
The ECB: controlling/correcting the beam's energy spectrum



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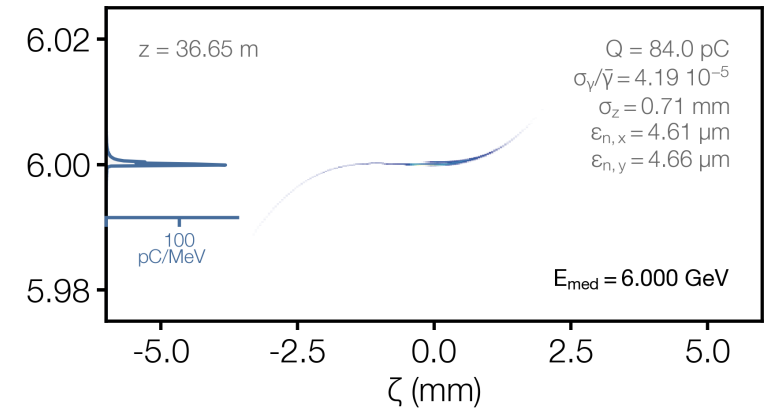
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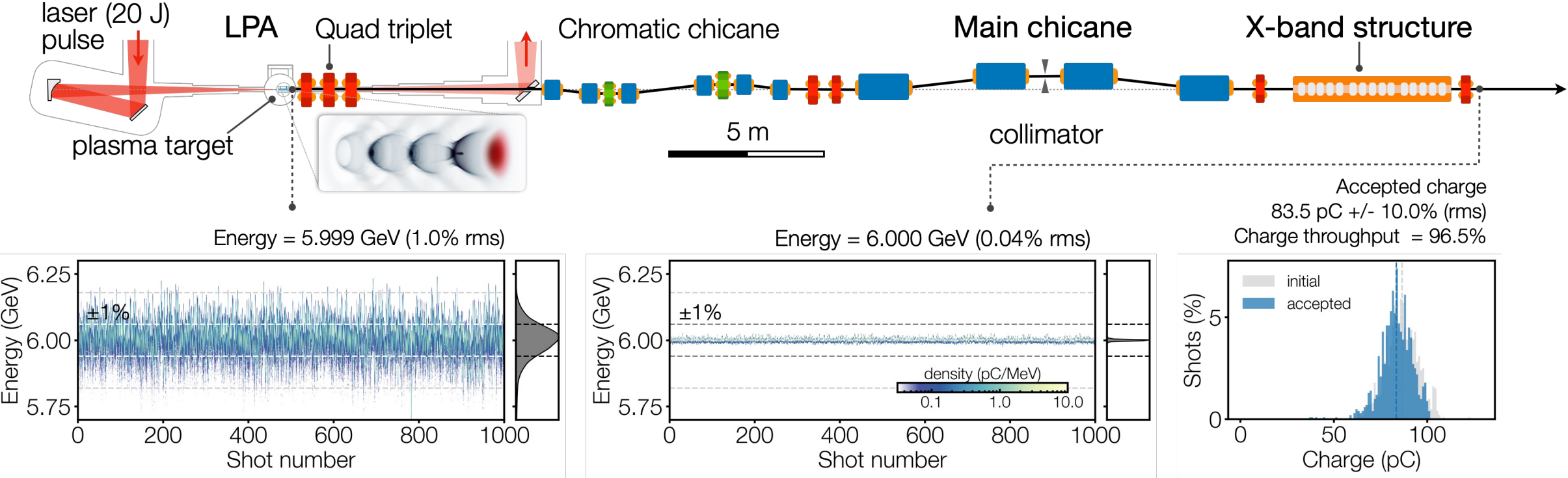
$$\Delta\mathcal{E}/\mathcal{E} = 0.5\% \quad L = 710 \mu\text{m}$$



After X-band structure

$$\frac{\Delta\mathcal{E}}{\mathcal{E}} < 0.1\% \quad L = 710 \mu\text{m}$$

Operational considerations and implementation plans



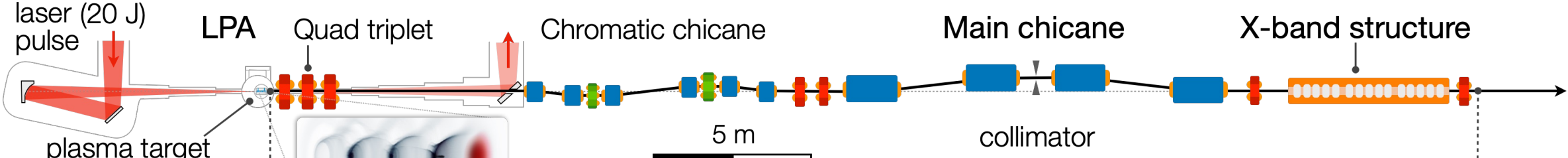
Jitters : {0.75 mm in z_f , 0.75% in E_L , 0.75% in n_p , 0.2 mrad in θ_x , 0.1 mrad in θ_y , 100 fs in RF timing}

Introduced in FBPIC

Introduced in OCELOT

Overall energy deviations reduced by factor 25 → 0.04%
Charge throughput 96.5%

Operational considerations and implementation plans



Parameter	After LPA	After ECB
Charge	87 pC	84 pC
Charge spread	9.8 %	10.0 %
Energy	5.999 GeV	6.000 GeV
Energy spread	1.0 %	0.04%
Emittance (x, y)	0.4, 0.2 nm	0.4, 0.6 nm

Operation requirements and performance

- Filling the ring in 10 min: 80 pC @ 32 Hz.
- Top-up 1% of charge: 6 s every 6 min.
- Power during filling: 300 kW.

Accepted charge
83.5 pC +/- 10.0% (rms)
Charge throughput = 96.5%

Energy = 6.000 GeV (0.04% rms)

Introduced in FBPIC

Introduced in OCELOT

Overall energy deviations reduced by factor 25 → 0.04%
Charge throughput 96.5%

DESY makes steps towards prototyping the plasma injector



Andreas R. Maier



Guido Palmer

KALDERA laser



Manuel Kirchen



Rob Shalloo

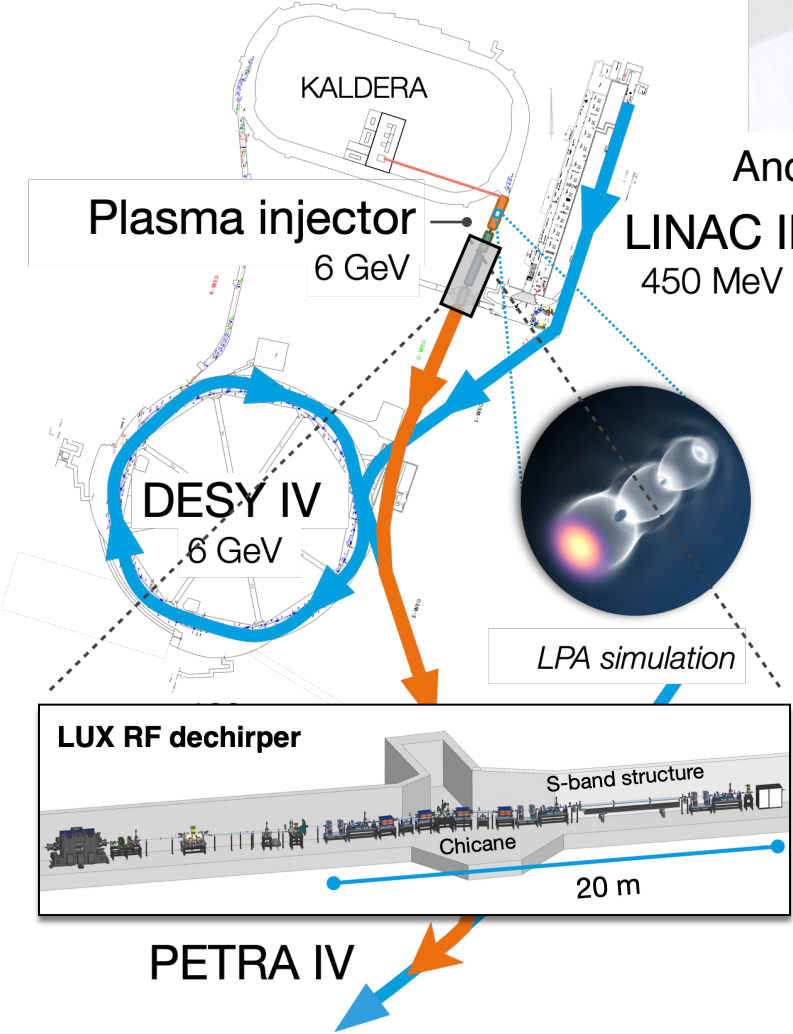
Emmy Noether Junior Research Group

Plasma source



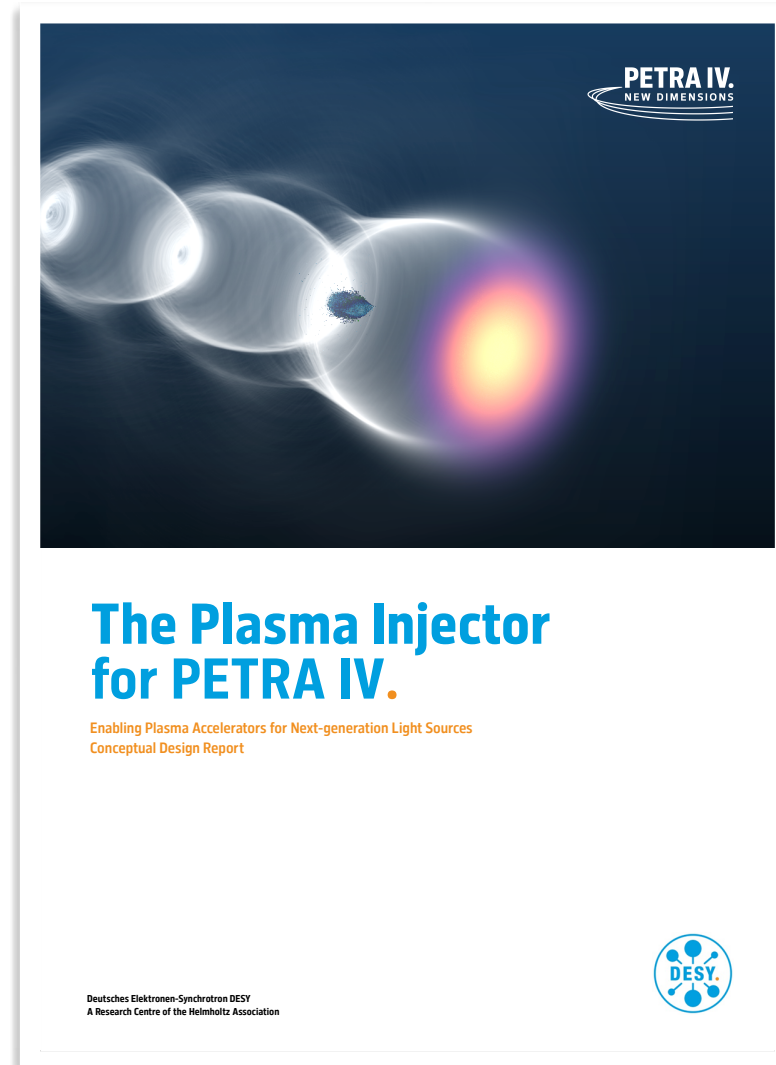
Paul Winkler

Energy compression beamline



One goal is to demonstrate the full technology chain: laser, guiding, ECB, transport to inject into DESY II (500 MeV)

Conceptual Design Report to be published (58 p., internal review)

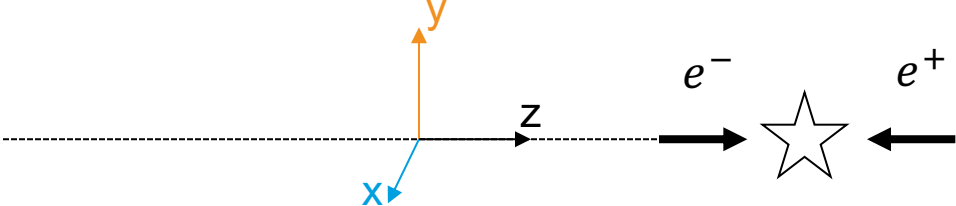




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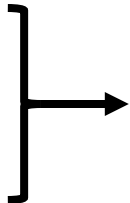
S. Diederichs, C. Benedetti, A. Ferran Pousa, A. Sinn,
J. Osterhoff, C. B. Schroeder, and M. Thévenet

Flat beams are preferred at the interaction point



Beamstrahlung scales with¹ $\sim 1/(\sigma_x + \sigma_y)$

Luminosity scales with² $\sim 1/(\sigma_x \sigma_y)$ or $\sim 1/\sqrt{\epsilon_x \epsilon_y}$



Flat beams with $\sigma_x \gg \sigma_y$ ($\epsilon_x \gg \epsilon_y$) minimize beamstrahlung and maximize luminosity

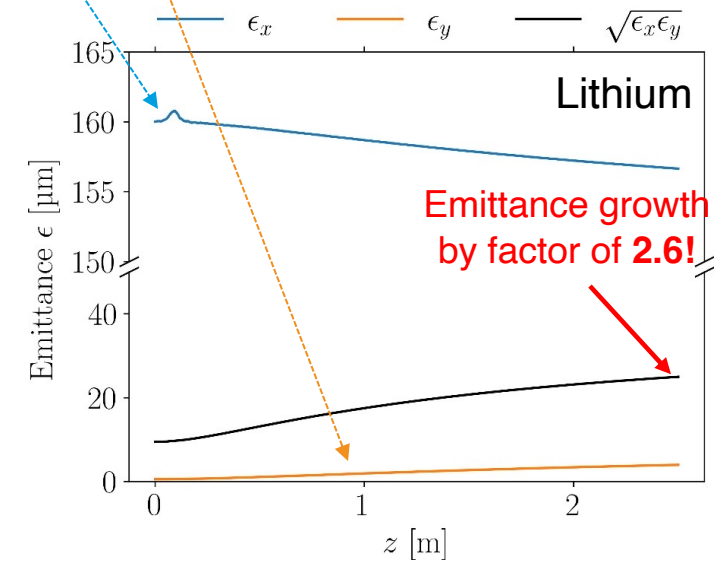
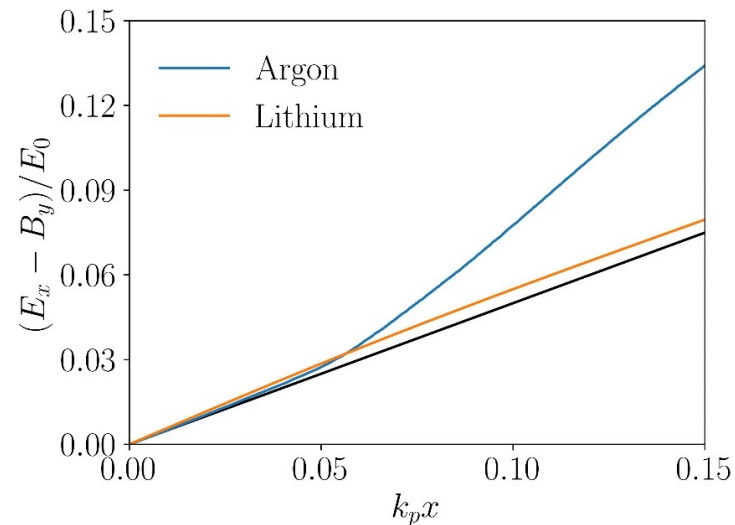
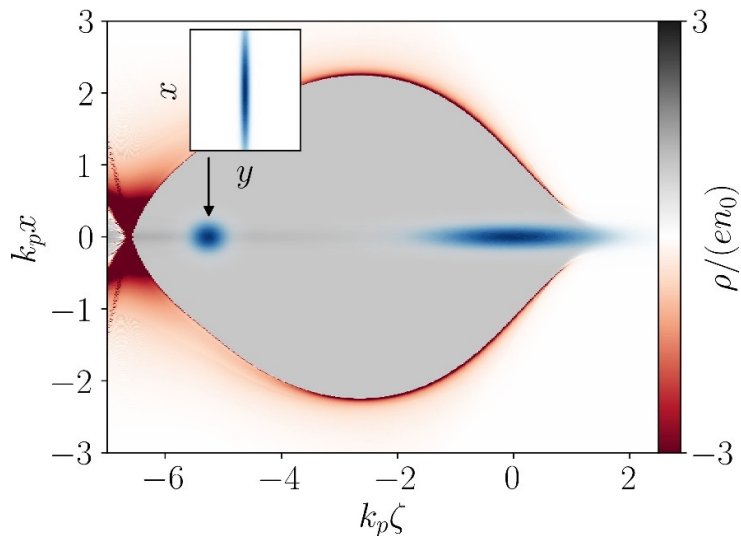
Acceleration of flat beams not mentioned as a key R&D challenge in ESPP



[1] Schroeder et al, JINST 2022
[2] Schulte, RAST 2016
[3] Raubenheimer, SLAC PUB 1993

Realistic plasma stage sees considerable emittance exchange

- **Drive bunch:** Charge: 4.28 nC, Length (rms): $42 \mu\text{m}$, $\epsilon_{[x,y]} = [60, 60] \mu\text{m}$.
- **Witness bunch:** Charge: 1.6 nC, Length (rms): $18 \mu\text{m}$, $\epsilon_{[x,y]} = [160, 0.54] \mu\text{m}$.
- **Plasma:** $n_0 = 7 \times 10^{15} \text{ cm}^{-3}$, Length: 2.5 m, Lithium.



- Mild ion motion or ionization causes considerable emittance exchange

Mechanism: coupled wakefields give coupled x & y orbits

Consider the dynamics of a single beam electron in wakefield $W = E + ce_z \times B$

Ideal blowout regime
Axisymmetric and linear

$$W_r = E_0 \frac{k_p r}{2}$$

$$W_x = E_0 \frac{k_p x}{2}$$

$$W_y = E_0 \frac{k_p y}{2}$$

$$r = \sqrt{x^2 + y^2}$$

→ The x and y orbits are fully decoupled

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Example Axisymmetric non-linear wakefields

$$W_r = E_0 \frac{k_p r}{2} + \alpha r^2$$

$$W_x = E_0 \frac{k_p x}{2} + \alpha r x$$

$$W_y = E_0 \frac{k_p y}{2} + \alpha r y$$

- Ion motion/ionization/... caused by an axisymmetric drive beam
- Guiding channel for LPA

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- Ion motion/ionization/... caused by an axisymmetric drive beam
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→ The x and y orbits are coupled

General non-axisymmetric, non-linear fields

$$W_x = f(x, y)$$

$$W_y = g(x, y)$$

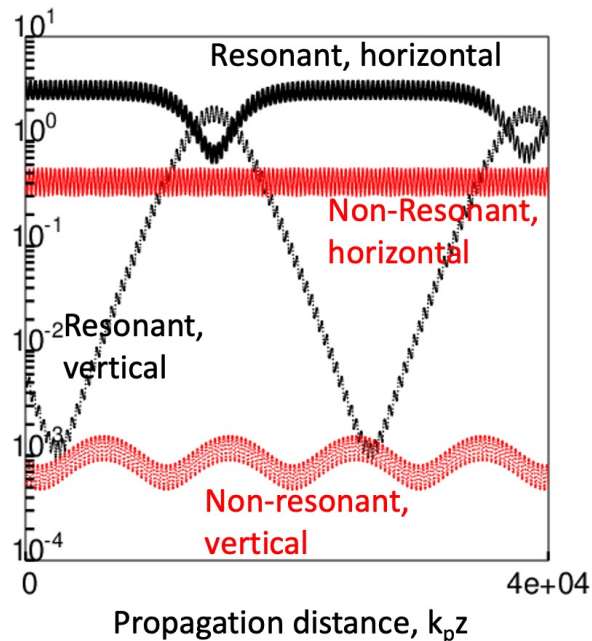
- Ion motion/ionization/... caused by a flat witness beam
- Laser misalignment in guiding channel for LPA

→ The x and y orbits are coupled

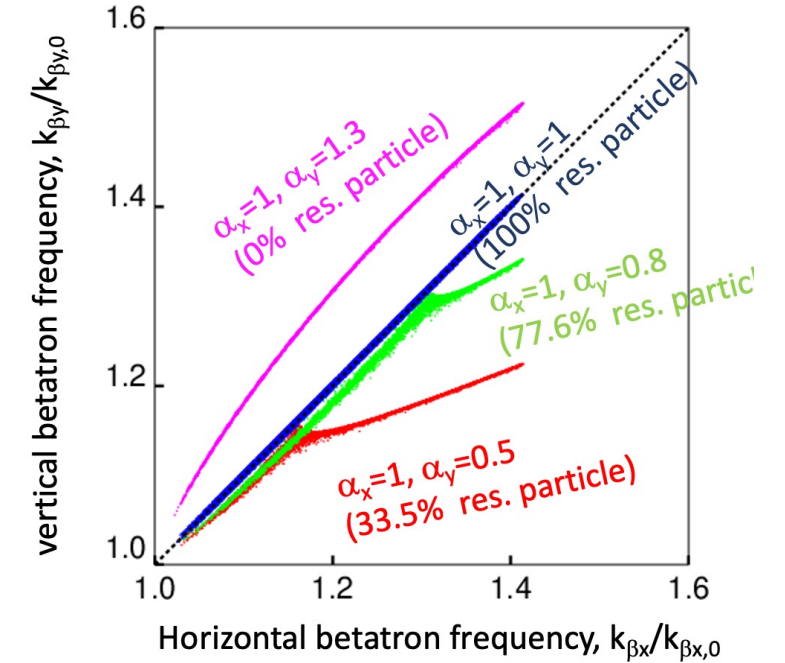
A fraction of beam particles are trapped in a resonance

- Each electron has a different $k_{\beta x}$ and $k_{\beta y}$ depending on initial conditions.
- The resonance is located on the diagonal $k_{\beta x} = k_{\beta y}$.
- Electrons in a specific area are trapped in the resonance.
- These resonant electrons see periodic exchange in x and y orbits.
- They are responsible for the emittance exchange.

Single particle betatron amplitudes



Map of betatron frequencies



- Well-known (complex) phenomenon in RF accelerators
- Axisymmetric + non-linear is the worst case
all particles are resonant → **full emittance exchange**

No clear solution yet for a dense flat witness beam causing ion motion

Ion motion caused by the driver only (6 HALHF stages)

Driver: 4.28 nC, 42 μm , $\epsilon_{[x,y]} = [60, 60] \mu\text{m}, [24, 150] \mu\text{m}$

Witness: 1.6 nC, 18 μm , $\epsilon_{[x,y]} = [160, 0.54] \mu\text{m}$

Plasma: Sodium 1+, $n_0 = 7 \times 10^{15} \text{ cm}^{-3}$, 2.5 + 5*5 m.

→ A flat driver breaks the resonance and mitigates emittance exchange

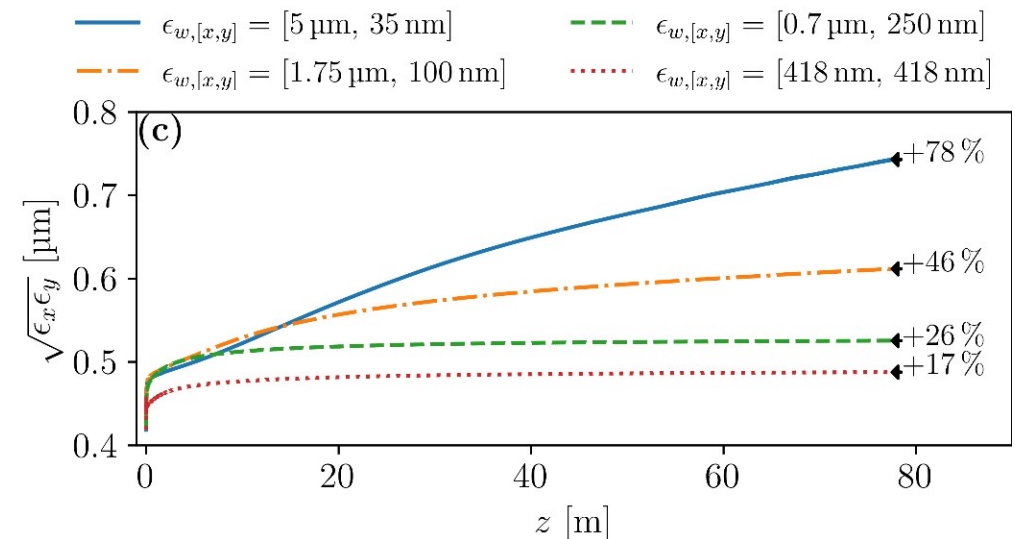
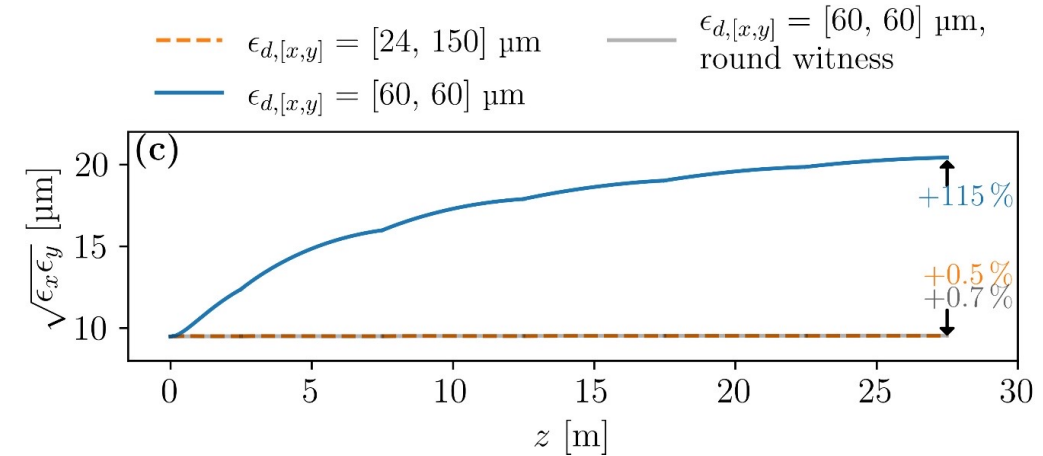
Ion motion caused by the witness beam only

Driver: 4.28 nC, 42 μm , $\epsilon_{[x,y]} = [2.8, 2.8] \text{ mm}$, rigid

Witness: 1.6 nC, 18 μm , $\epsilon_{[x,y]} = [5, 0.035] \mu\text{m}$

Plasma: Hydrogen, $n_0 = 7 \times 10^{15} \text{ cm}^{-3}$, length 77.5 m

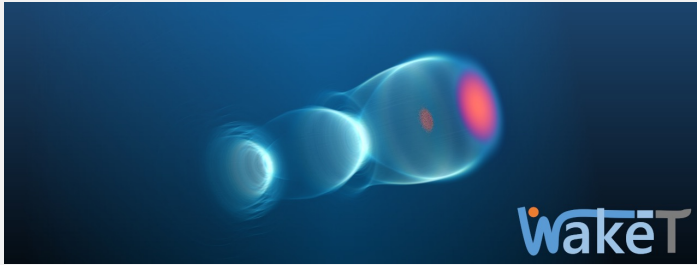
→ A flatter beam causes larger emittance exchange



Studies made possible thanks to recent progress in simulations

➤ Wake-T

Quick simulations (benchmarked vs. FBPIC)

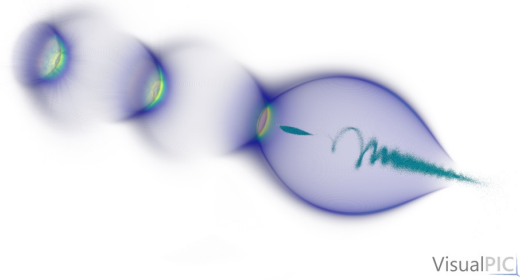


- 2D (axisymmetric) quasistatic
- Laser-driven or beam-driven
- Python, second/minutes on a laptop
- **Recent:** Adaptive grid & ion motion

Open-source <https://github.com/AngelFP/Wake-T>

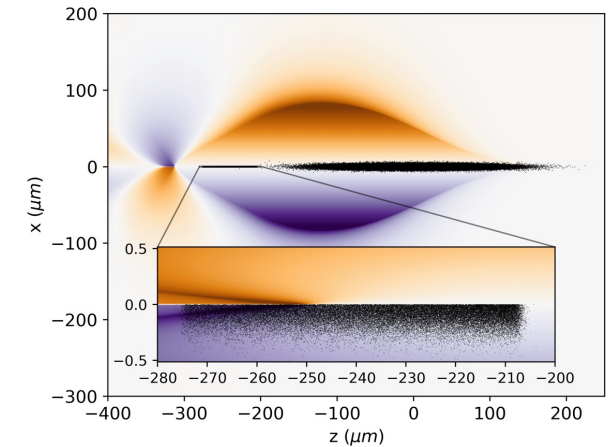
➤ HiPACE++

Optimized for large 3D simulations



- 3D quasistatic particle-in-cell
- Multi-physics
- C++, on top supercomputers
- **Recent:** Mesh refinement

Open-source <https://github.com/Hi-PACE/hipace>



And others

- With mesh refinement, 3D simulations of a 20 GeV stage from 175 GeV, emittance 135 nm, are very affordable
Numerical convergence with transverse resolution of 5 nanometers to fully resolve ion motion effects

- Multi-stage simulation studies done routinely

A. Ferran Pousa et al. Proc. IPAC'23 14: 1533-1536. ; S. Diederichs et al. arXiv:2403.05871 (2024).

- A collection of tools enables start-to-end multi-physics studies

COMSOL-plasma for hydrodynamics simulations of HOFI, Optimas for scalable Bayesian optimization, LASY for laser manipulations

Conclusion

- **We propose a plasma injector for Petra IV.**

6 GeV, < 0.3% energy deviation, 2.6 nC/s

Reliable 6 GeV LPA + energy compression beamline for energy spread & jitter reduction

CDR to be published soon

- **Accelerating a flat beam in a plasma accelerator poses significant challenges.**

Emittance is transferred from the large to the small direction, degrading quality

This is caused by particles falling in a resonance

Avoiding the resonance might mitigate this effect

- **Full-physics realistic simulations are very affordable.**

Progress in numerical methods makes most scenarios doable and cheap, even in 3D



Resonant emittance mixing of flat beams in plasma accelerators

S. Diederichs,^{1,2} C. Benedetti,³ A. Ferran Pousa,¹ A. Sinn,¹ J. Osterhoff,^{1,3} C. B. Schroeder,^{3,4} and M. Thévenet^{1,*}

¹Deutsches Elektronen-Synchrotron DESY, Notkestr. 85, 22607 Hamburg, Germany

²CERN, Espl. des Particules 1, 1211 Geneva, Switzerland

³Lawrence Berkeley National Laboratory, 1 Cyclotron Rd, Berkeley, California 94720, USA

arXiv ⁴Department of Nuclear Engineering, University of California, Berkeley, California 94720, USA
(Dated: March 12, 2024)

Thank you for your attention

Conceptual Design Report to be published (58 p., internal review)

Conceptual design

- State-of-the-art LPA: 6 GeV — <1% spread and deviations.
- Energy compression beamline with X-band RF: 6 GeV — 0.04%.
- Compact solution: < 50 m.

Performance demonstrated through full S2E simulations

- Operation with 80 pC (10% rms) similar to conventional.
- 32 Hz with diode-pumped Ti:Sa laser: 295 kW.

Outlook

- First prototyping under consideration at DESY.

