

# Developing KinkFinder at ILC

*Work in progress*

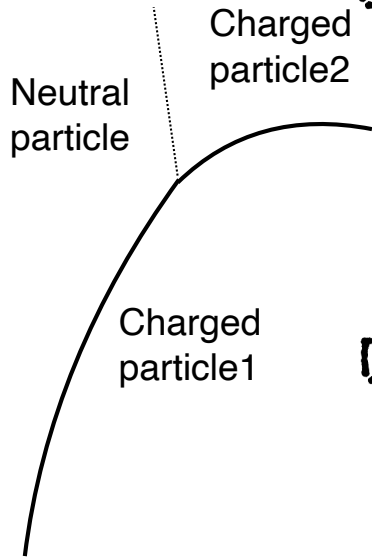
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# The motivation and aim of my study



## □ What is kink?

A charged particle decays and produces another charged particle.

Then the track bends abruptly and it is called “**kink**”.

## □ Why do I focus on kinks?

**The kink is a signature of Long Lived Particles (LLPs) for New physics.**

Ex. Chargino decays into a SM charged particle and a neutralino (Lightest SUSY Particle) etc...



I focus on kinks decayed inside a tracking detector, I'd like to identify kinks efficiently and accurately.

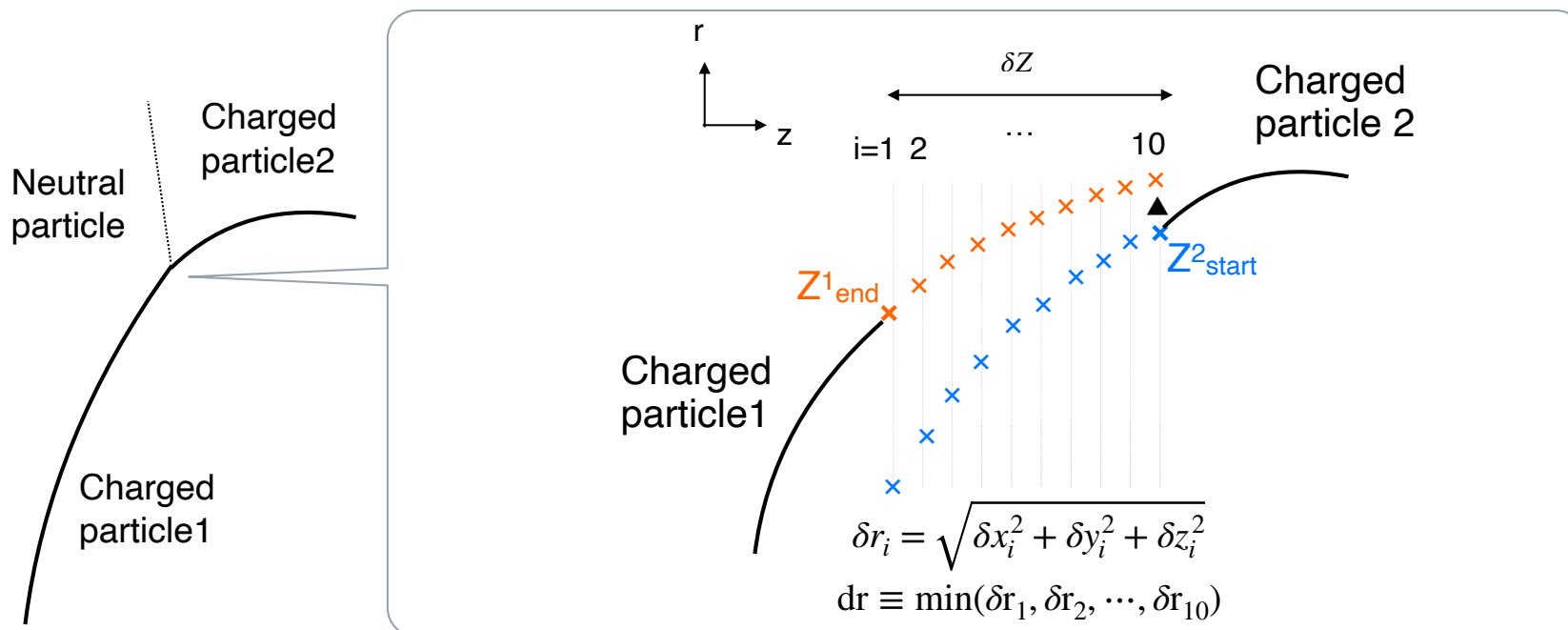
# How do I identify kinks? - KinkFinder

in MarlinReco/Tracking/KinkFinder

I want to study kinks from LLPs but firstly I try to check “standard kinks” from **SM particles (eg. Kaon...)**

2 tracks with

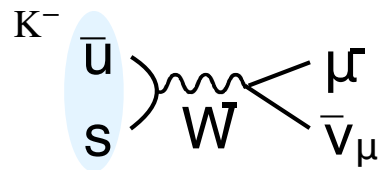
- ▶ Same sign
- ▶ Different momenta
- ▶ Small distance of closest approach



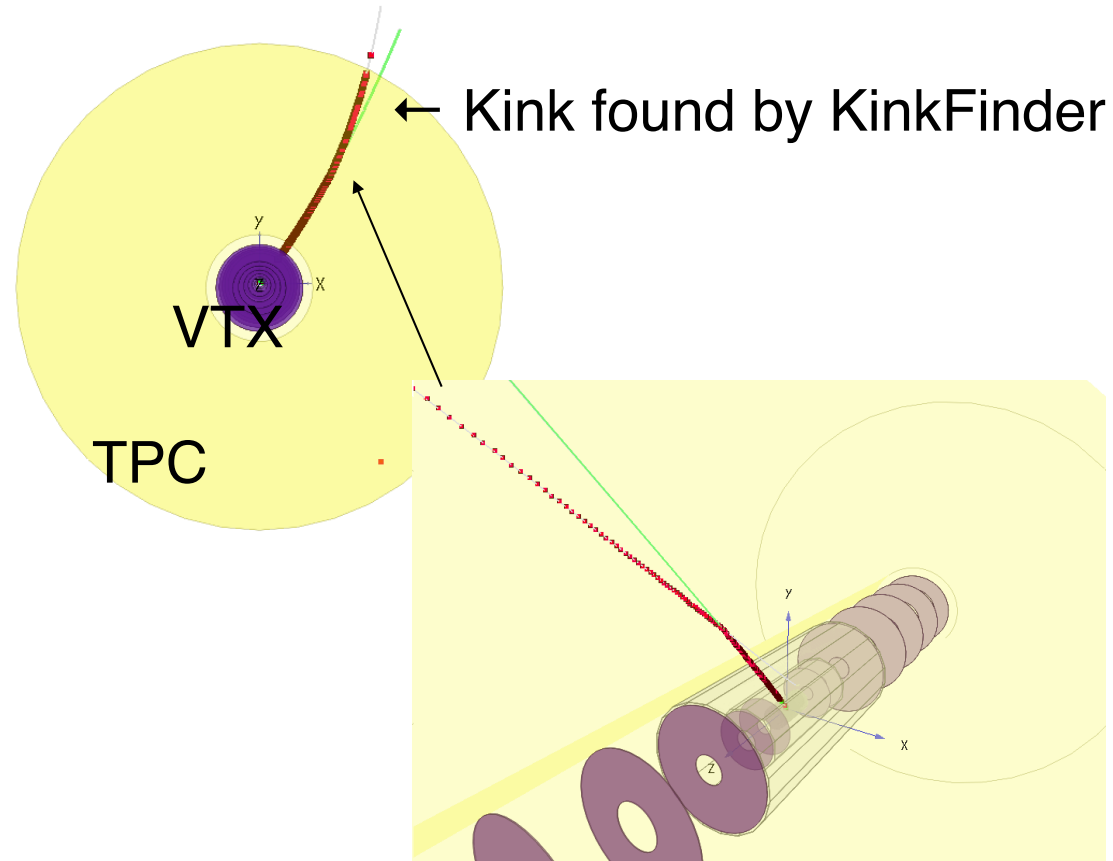
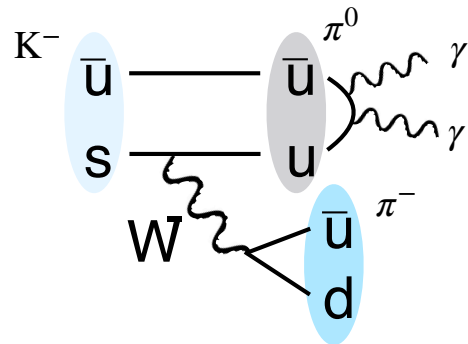
# Kaon

10GeV Kaons simulated and reconstructed in ILD\_I5\_v02 (CALOS removed)

1.  $K^- \rightarrow \mu^- \nu_\mu$



2.  $K^- \rightarrow \pi^- \pi^0$

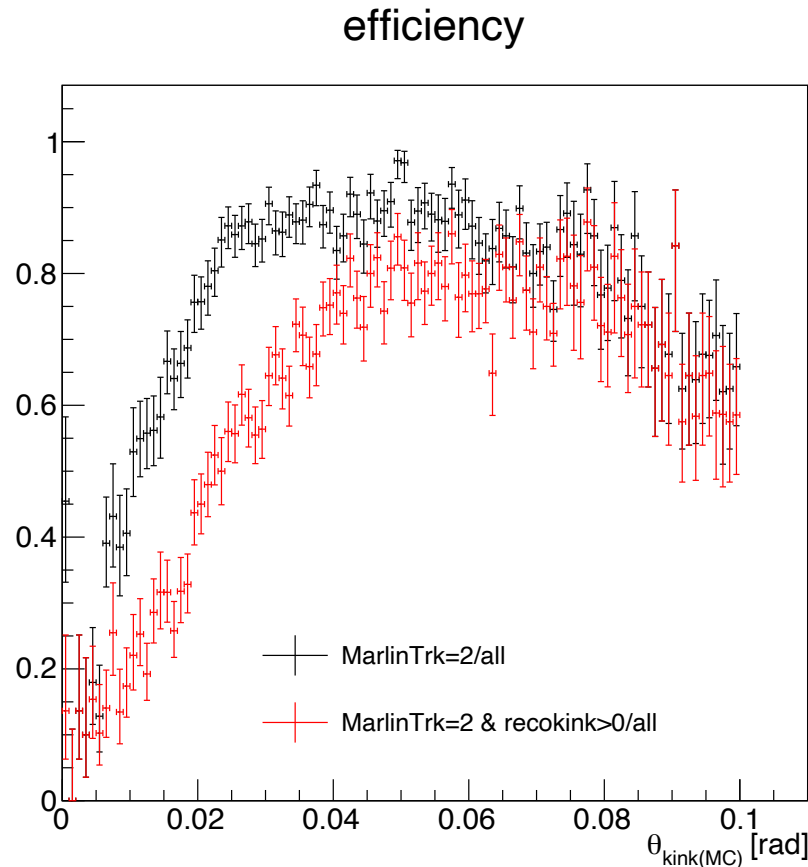
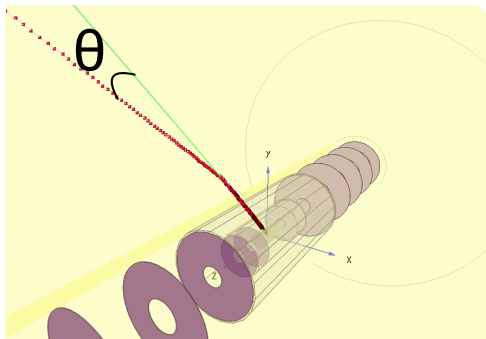
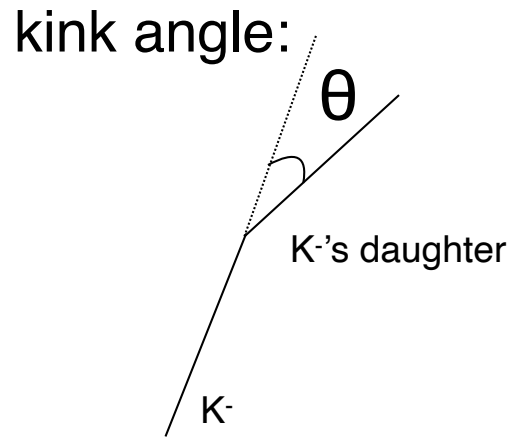


I checked the efficiency of KinkFinder.

# Efficiency dependence on the kink angle

## Prerequisites made from MCparticles

- Produced Kaon:  $P_K = 10$  [GeV]
- Endpoint(MC) inside TPC:  $329 + 100 < r < 1770 - 100$  [mm],  $|z_{max}| < 2350 - 250$  [mm]
- (MC) # of charged daughter of Kaon = 1



all: imposing only prerequisites

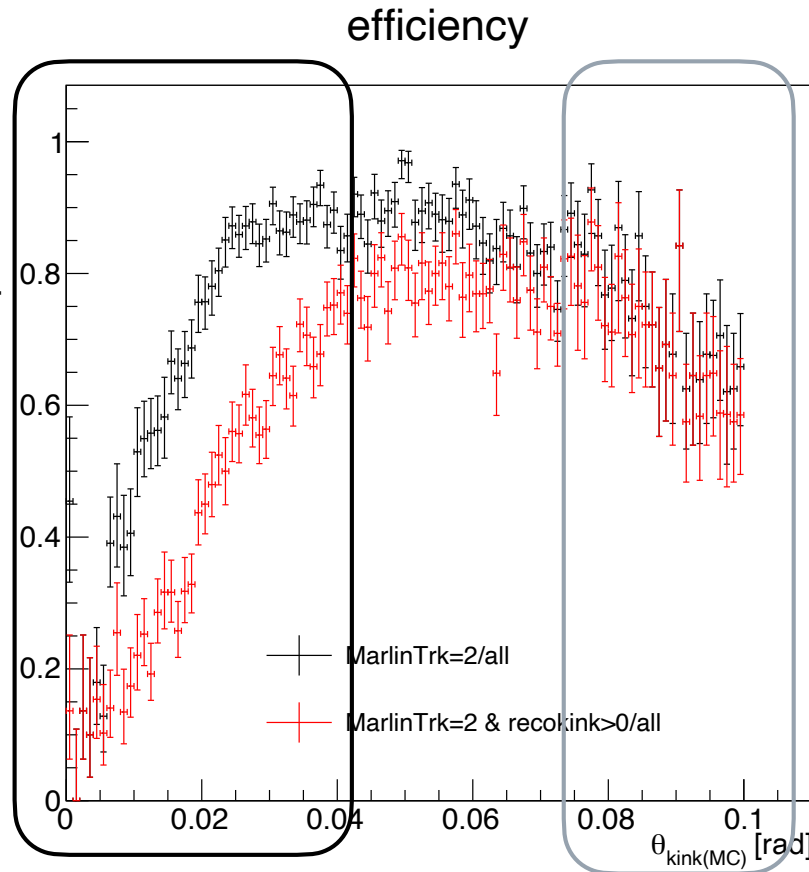
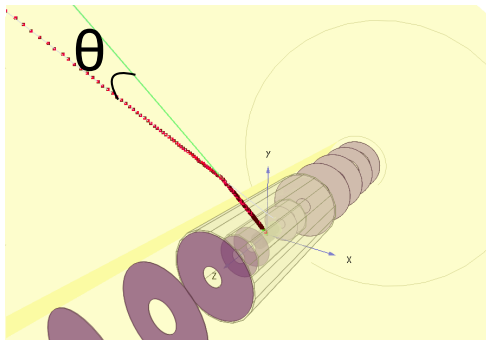
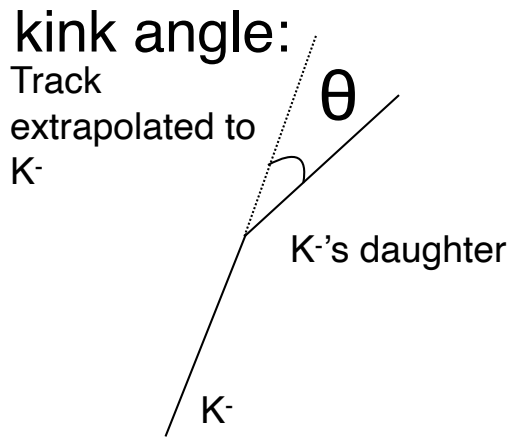
Black: nTrack = 2 (tracking efficiency)  
Red: nTrack = 2 and Kink > 0 (tracking and KinkFinding efficiency)

KinkFinder efficiency  $\sim 80\%$  ( $0.04 < \theta_{\text{kink(MC)}} < 0.08$ )

# Efficiency dependence on the kink angle

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all: imposing only prerequisites

Black: nTrack = 2 (tracking efficiency)

Red: nTrack = 2 and Kink > 0 (tracking and KinkFinding efficiency)

Reconstructed as **single** track?

Tracking for very displaced 2nd track?

# More particles - Kaon, Pion, Sigma, Xi

10GeV particles simulated and reconstructed in ILD\_I5\_v02  
(CALOS removed)

Estimated **kinkmass**

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# What is kink mass? which particle produced kink?

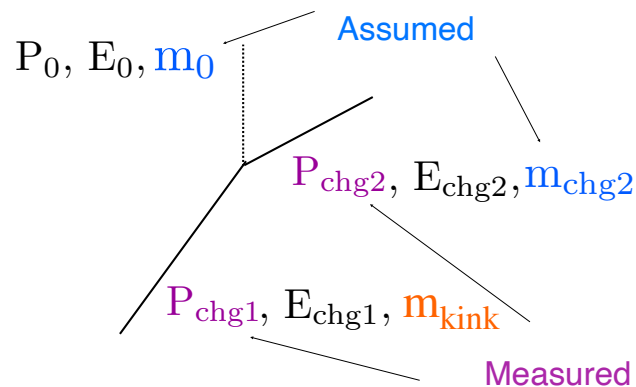


fig.Schematic of kink

Using  $P_0 = P_{\text{chg1}} - P_{\text{chg2}}$ , (Momentum conservation)

$$E_0 = \sqrt{P_0^2 + m_0^2} = \sqrt{(P_{\text{chg1}} - P_{\text{chg2}})^2 + m_0^2}$$

$$E_{\text{chg2}} = \sqrt{P_{\text{chg2}}^2 + m_{\text{chg2}}^2} \quad \text{(Energy conservation)}$$



$$m_{\text{kink}} \equiv \sqrt{(E_{\text{chg2}} + E_0)^2 - P_{\text{chg1}}^2}$$

Table 1. Tested kink decay in standard kinkfinder

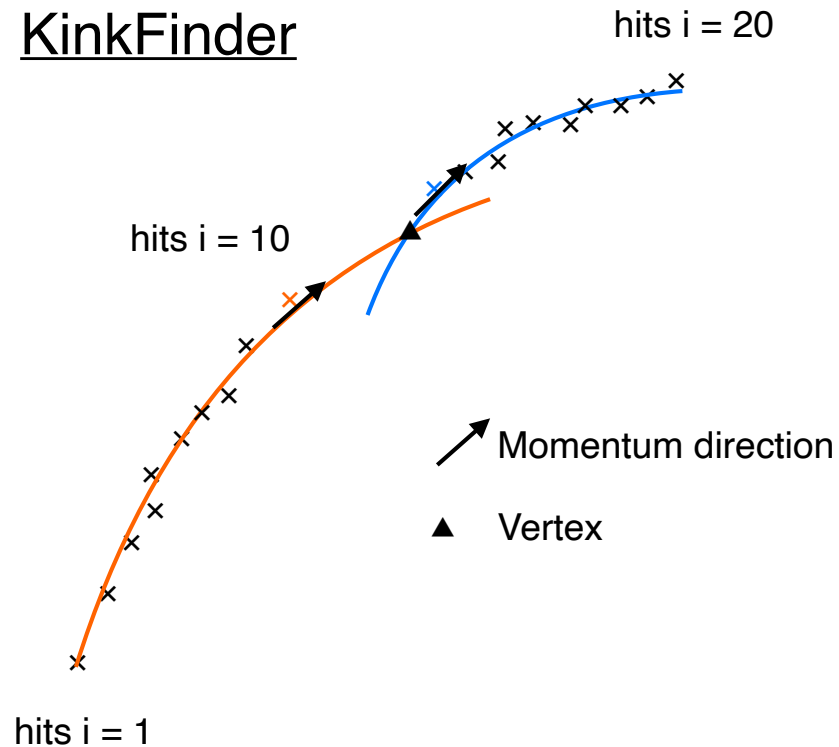
	$m_{\text{chg2}}$	$m_0$
$\pi^\pm / K^\pm \rightarrow \mu^\pm \nu$	$m_\mu$	0
$K^\pm \rightarrow \pi\pi$	$m_\pi$	$m_\pi$
$\Sigma^+ / \Sigma^- \rightarrow \pi n$	$m_\pi$	$m_n$
$\Sigma^+ \rightarrow p\pi_0$	$m_p$	$m_\pi$
$\Xi^- \rightarrow \pi\Lambda$	$m_\pi$	$m_\Lambda$

Choose best decay hypothesis using kink mass



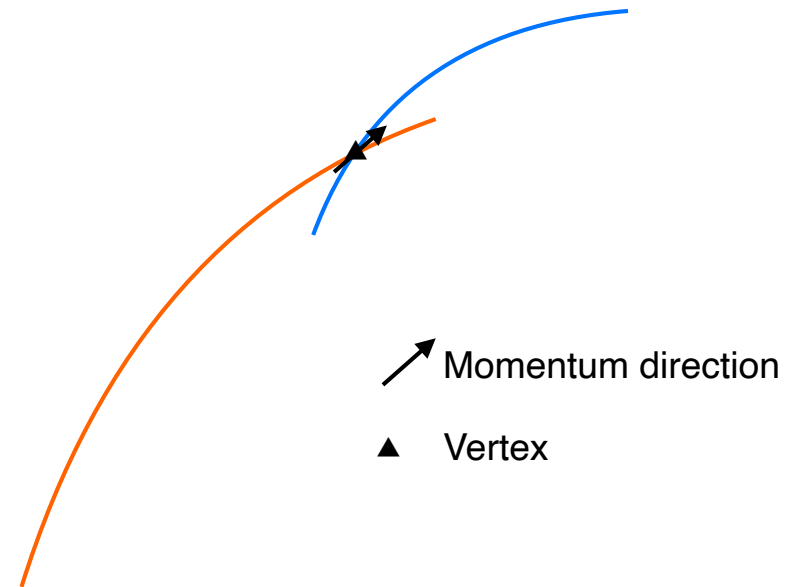
# How to get momentum information

## KinkFinder



Fit first / last 10 hits to helix  
Helix momentum at last/first hits

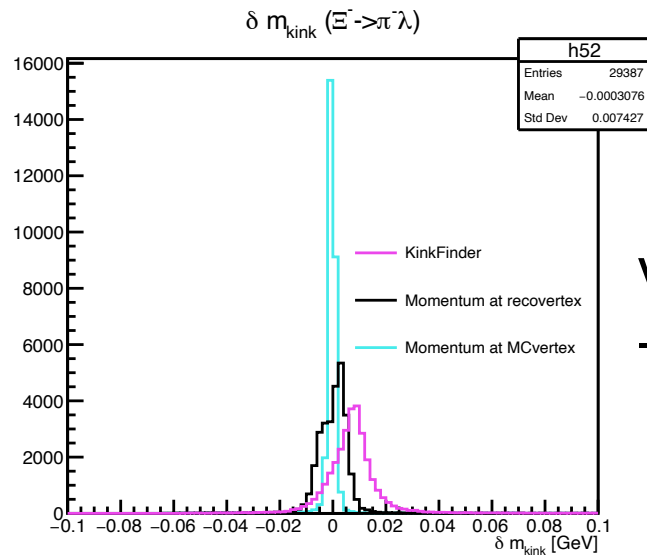
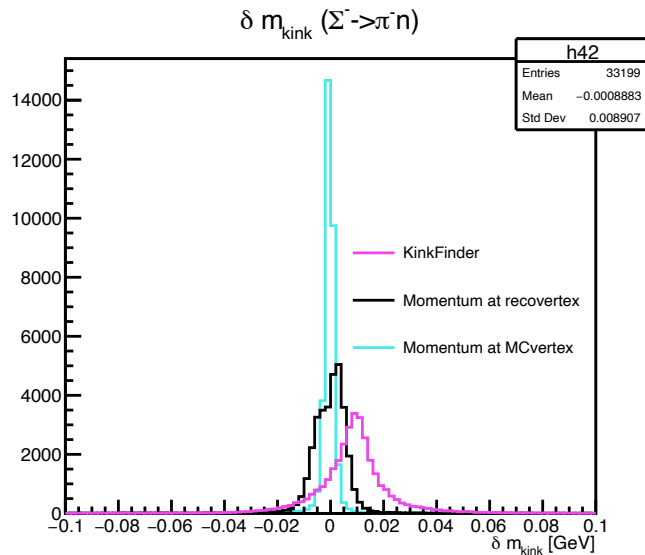
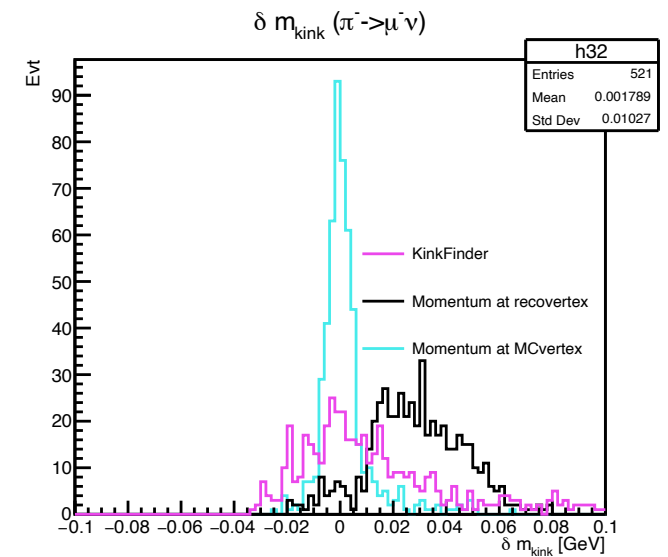
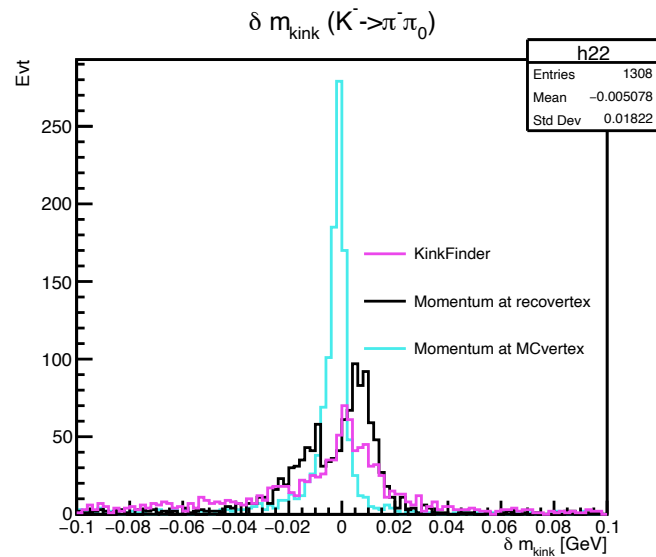
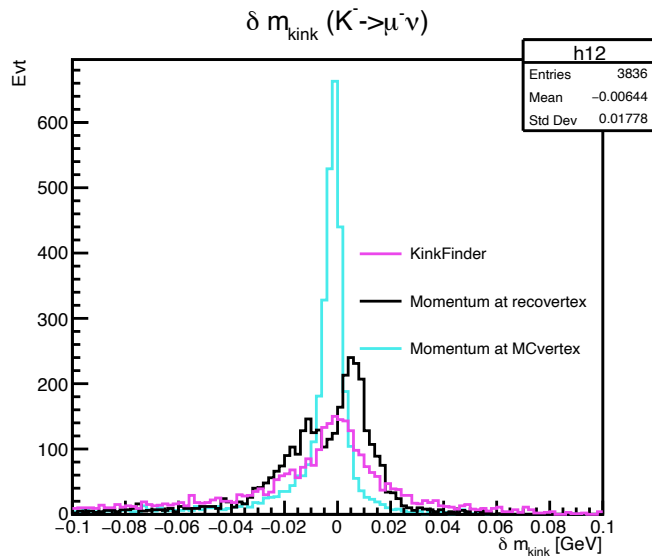
## Momentum at vertex



Use full track fits  
trackstate momentum at  
reconstructed vertex

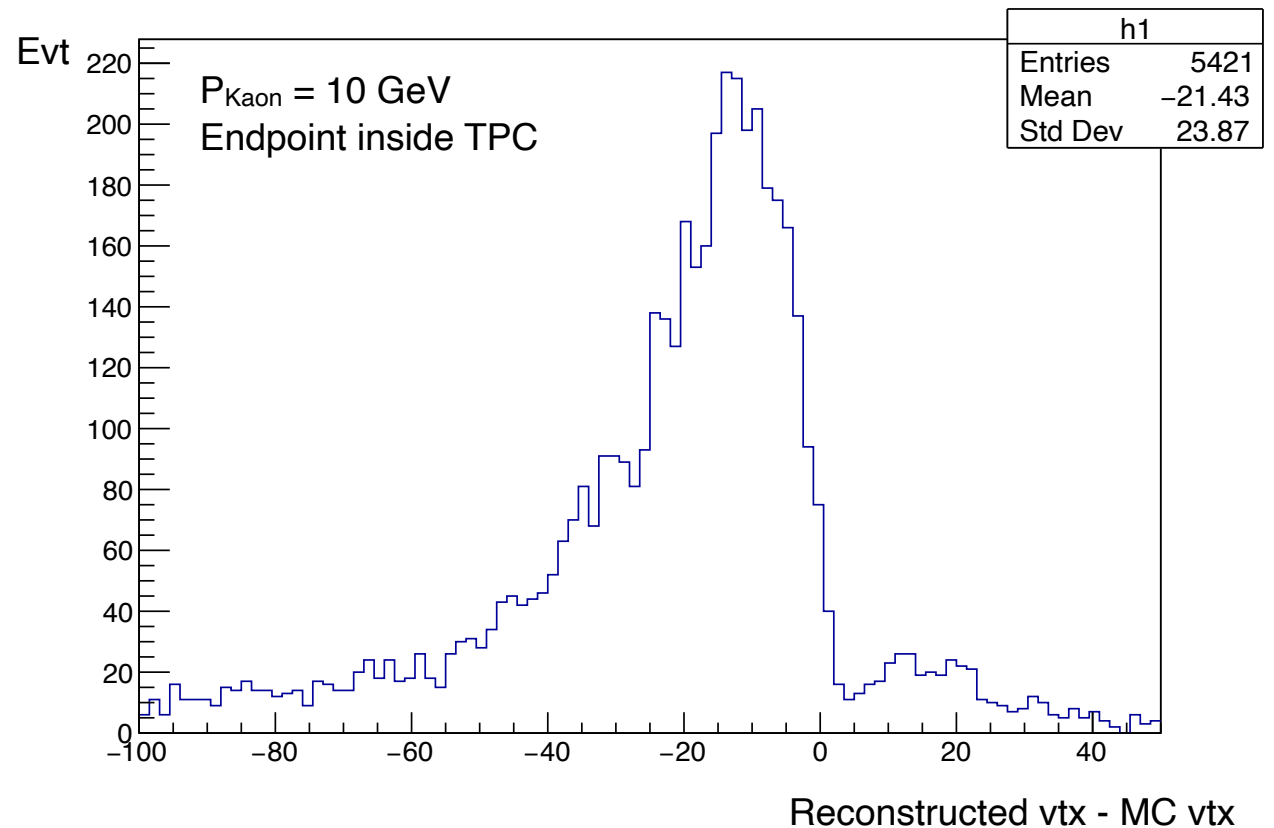
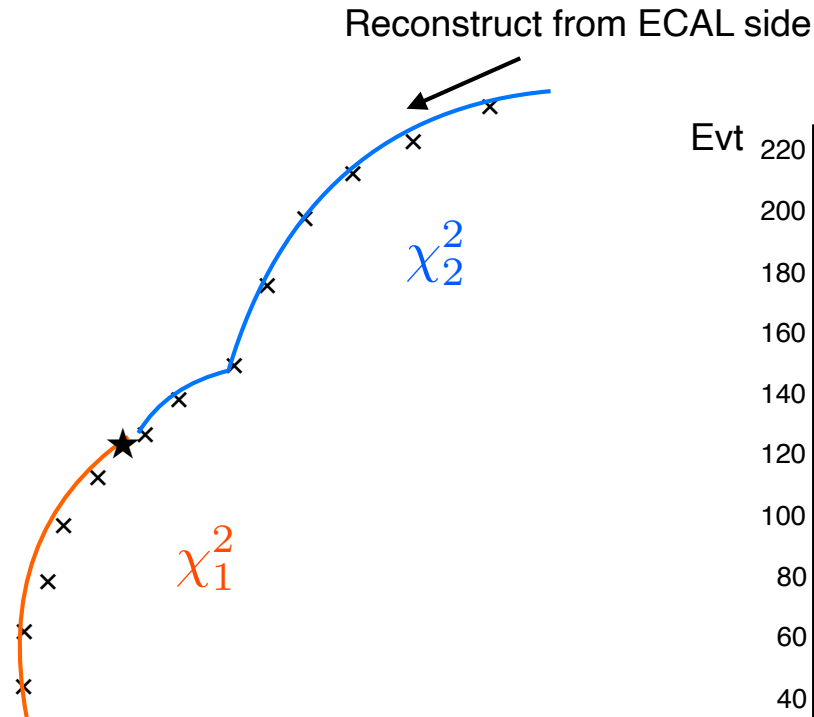
# Comparison of $\delta m$ distribution

$$\delta m_{\text{kink}} \equiv m_{\text{reco}_K} - m_{\text{true}_K}$$



Vertex reconstruction improved  
 $\rightarrow$   $\delta m$  distribution is improved

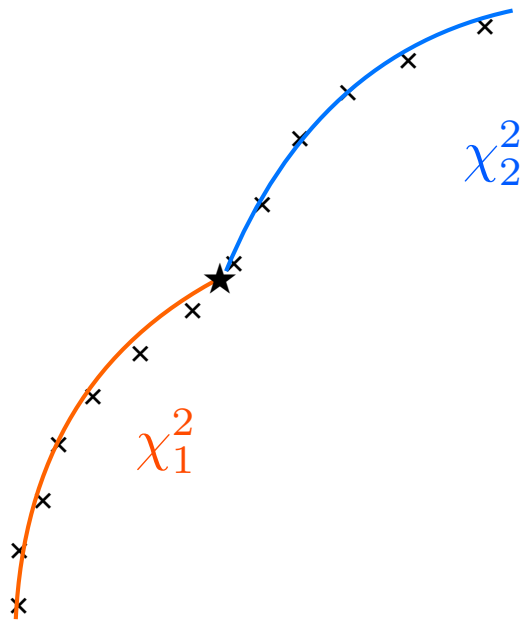
# Marlintrk bias at vertex



In Marlin track reconstruction, when chisq is bad, tracking is stopped.  
-> vertex is bias to smaller radius.

# How to get vertex information

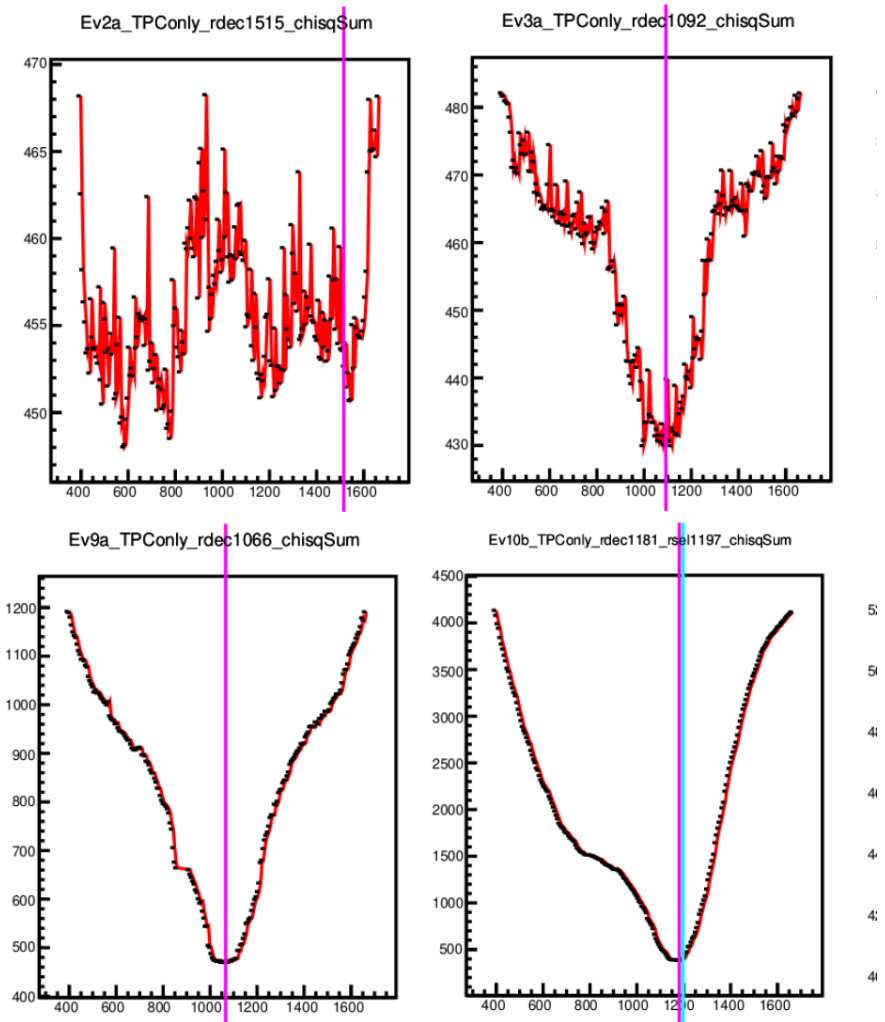
## New version



chiSq-trk1  
+  
chisq-trk2

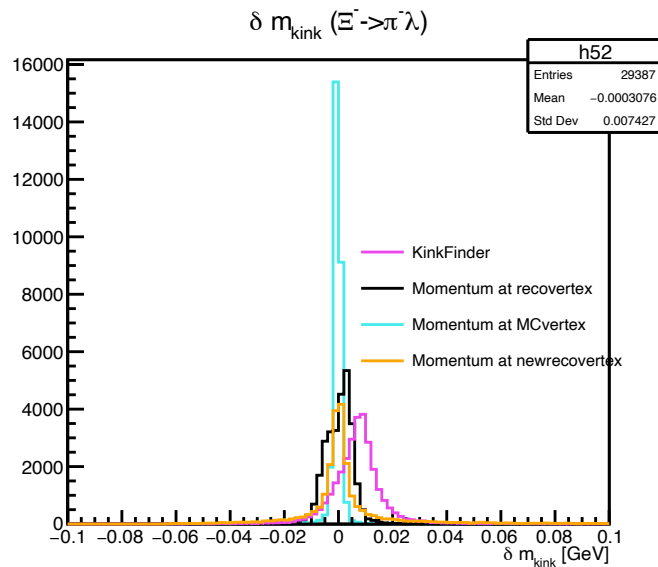
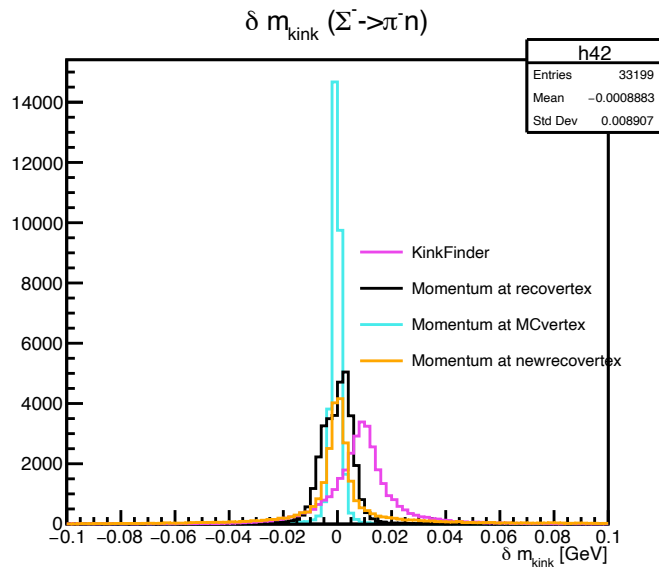
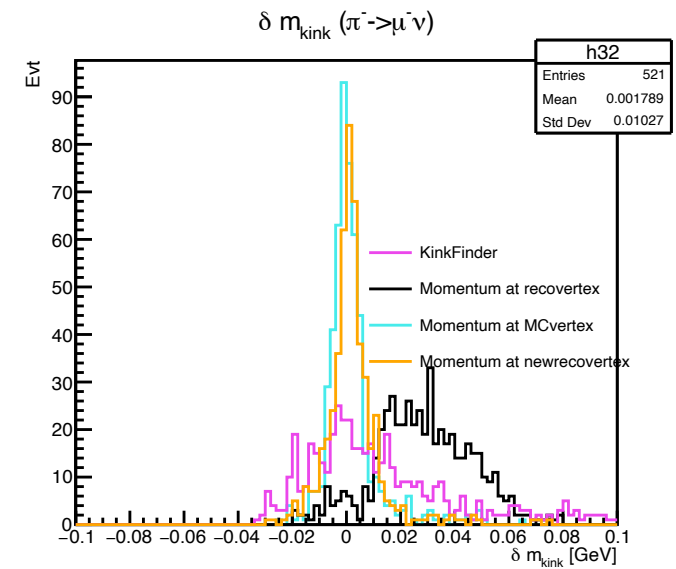
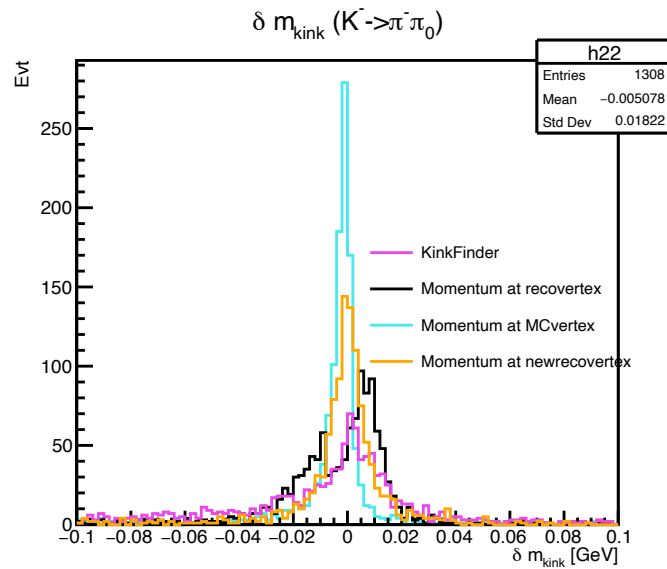
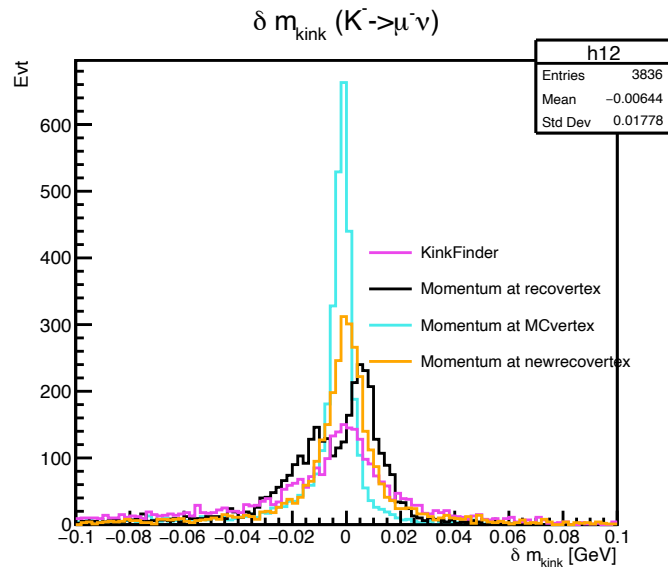
I try to cut track at every hits position,  
calculate  $\chi_1^2 + \chi_2^2$

a hit corresponded to minimum  
 $\chi_1^2 + \chi_2^2$  is assumed as a kink vertex.



Figures by Daniel

# Comparison of $\delta m$ distribution - new!



Improving mass resolution!

# Summary

Kink is useful for LLP search!

KinkFinder efficiency is about 80% ( $0.04 < \theta_{\text{kink(MC)}} < 0.08$ )

Improving mass resolution

<- better vertex position

<- better track momentum at vertex

Next steps

- Fix likelihood function
- vertex fitting
- Improving efficiency at small and large kink angle

# New likelihood function - try1

KinkFinder

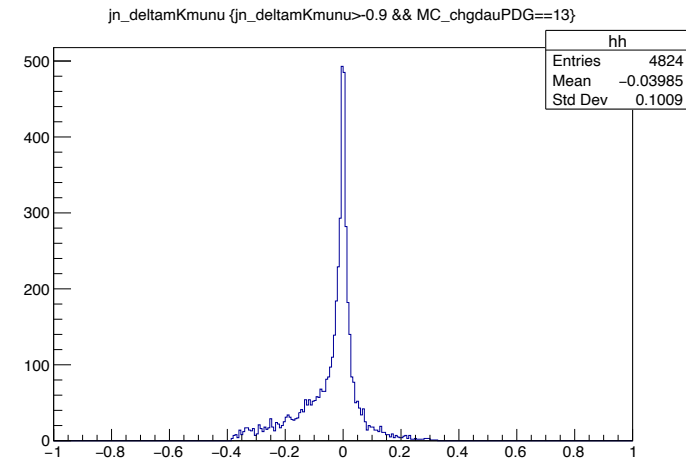
$$\text{likelihood } K \equiv 3.125 \times \delta K \times \delta K + tK \quad \delta K \equiv \frac{|m_{kink} - m_K|}{\text{K mass resolution (0.075 [GeV])}}$$

$$L_K \equiv \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{1}{2} \left( \frac{\delta m_K}{\sigma} \right)^2} \times e^{-tK}$$

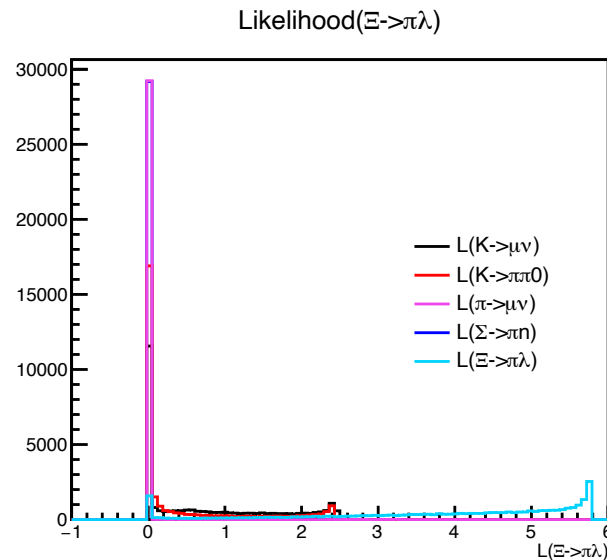
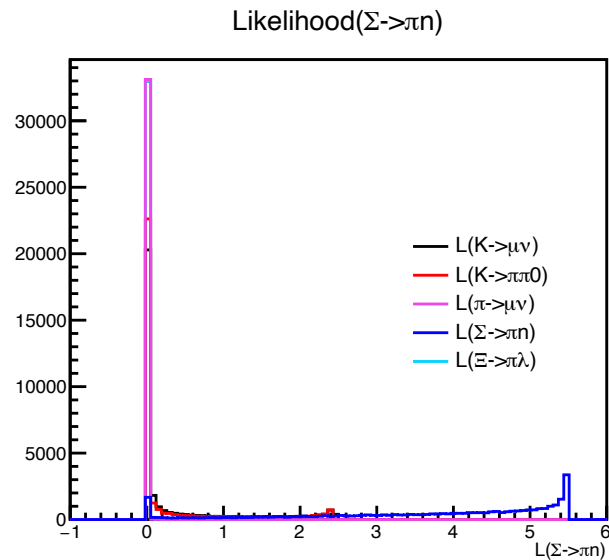
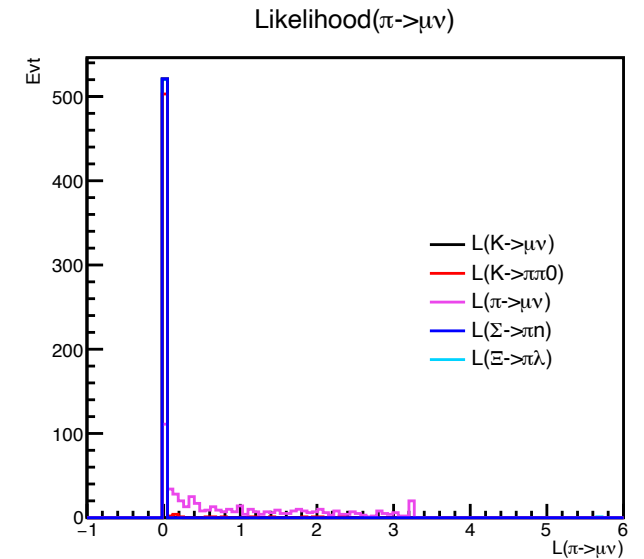
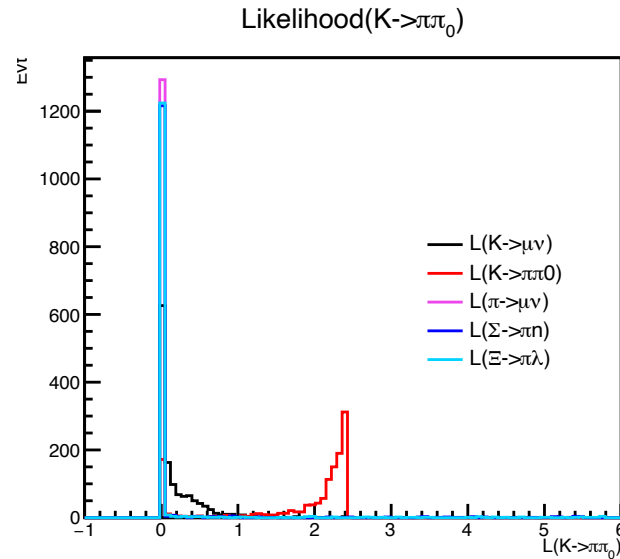
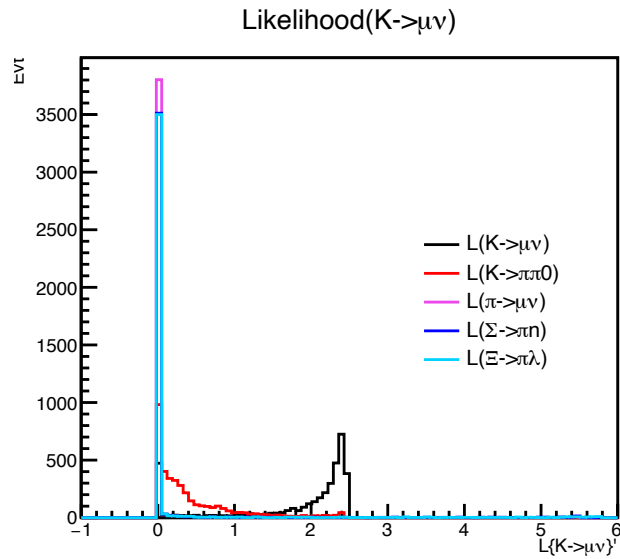
Ignoring

$$\delta m_K \equiv m_{\text{reco}K} - m_{\text{true}K}$$

I find  $\sigma$  from  $\delta K'$ ,  $\delta \pi'$ ,  $\delta \Sigma'$  and  $\delta \Xi'$  distribution.  
I used "RMS90".



# Distribution of new likelihood function

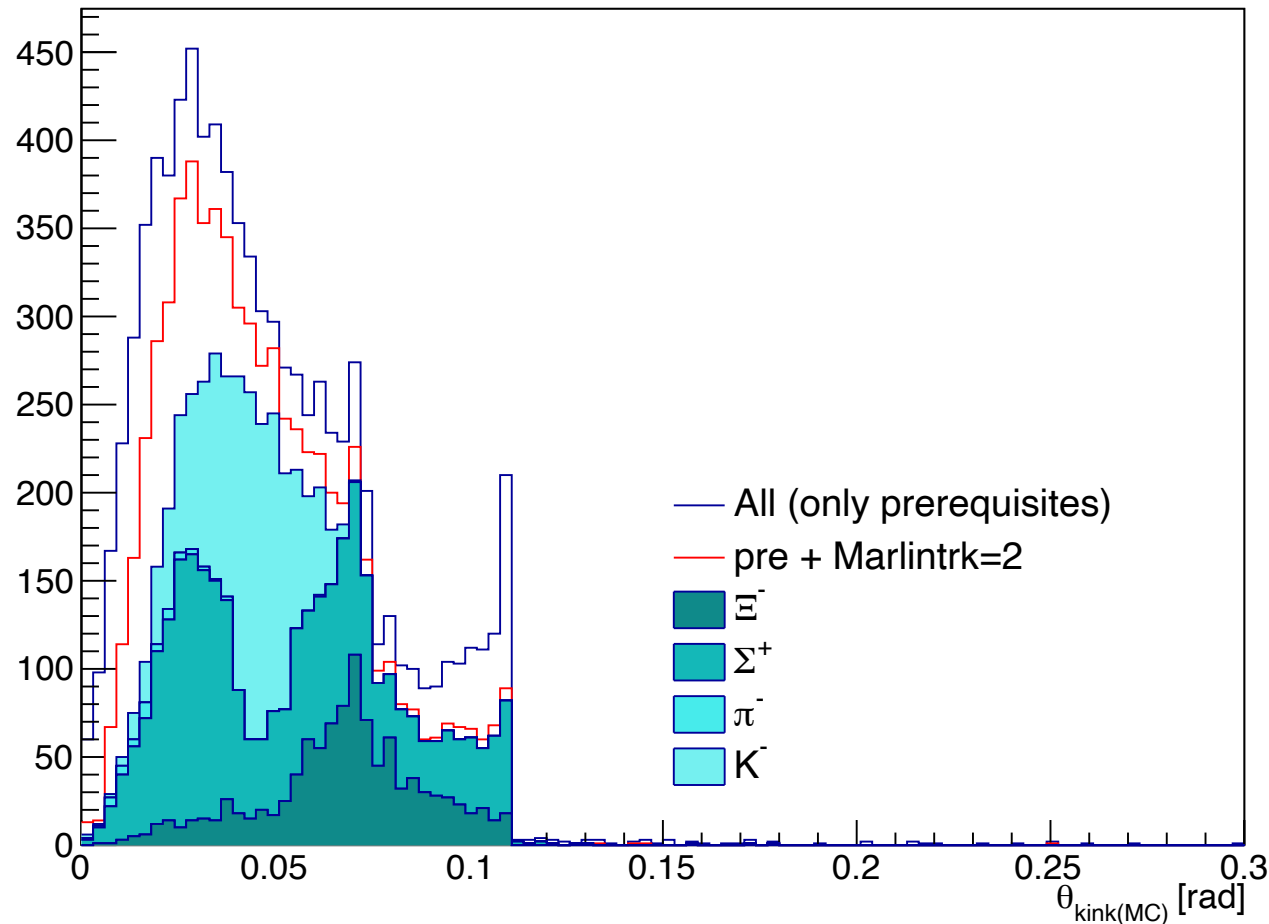




# Kink angle on each pdgs - KinkFinder

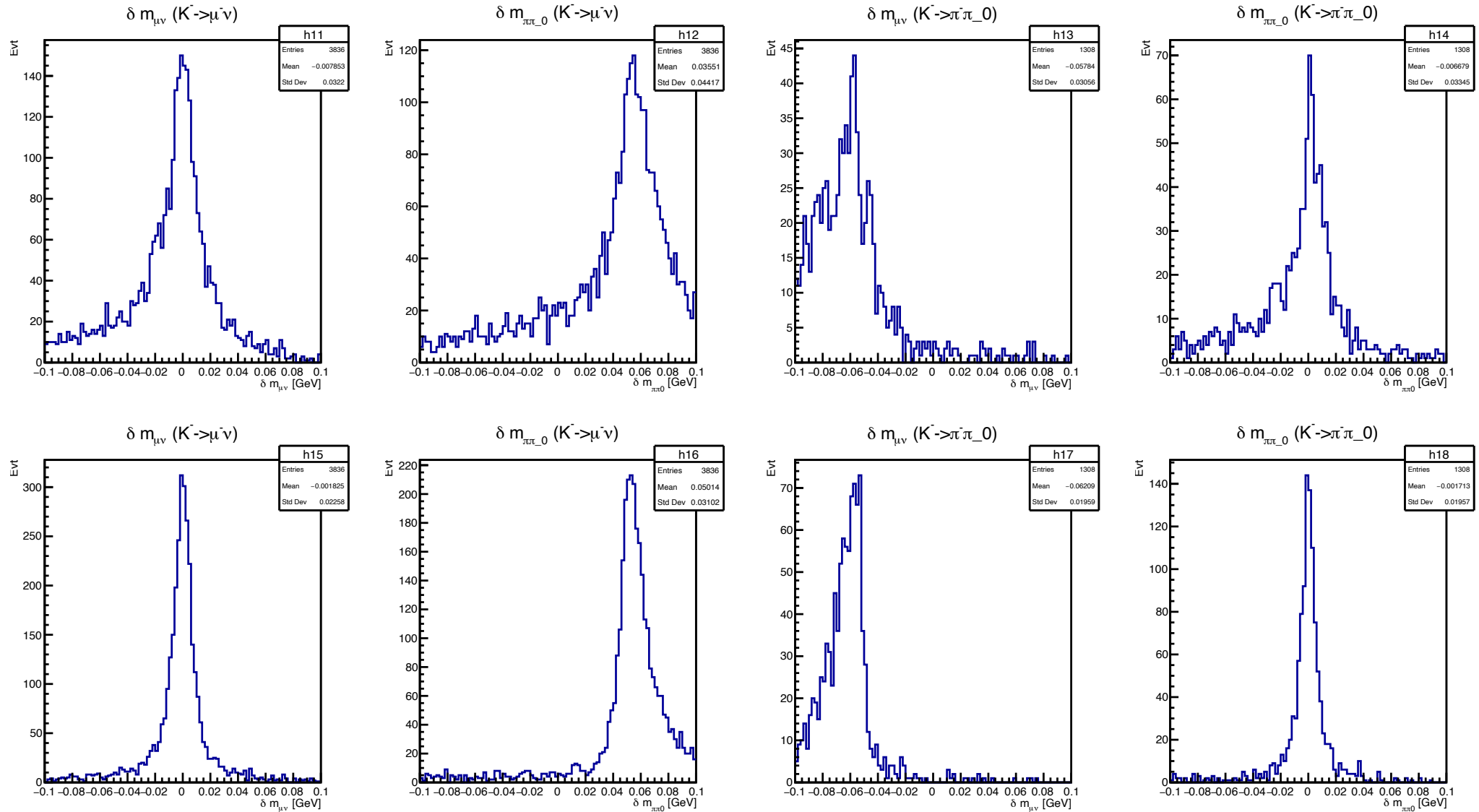
## Prerequisites made from MCparticles

- Endpoint(MC) inside TPC:  $329 + 100 < r < 1770 - 100$  [mm]  $|z_{max}| < 2350 - 250$  [mm]
  - (MC) # of charged daughter of Kaon = 1
- Each pdg plots are imposed Marlintrk = 2 and reconstructed kink exists



In Kaon samples, many kinks are misidentified

# KinkFinder vs New - $\delta m$ distribution (Kaon)



# Table: sigma by RMS 90 - New

	Sigma	Error of sigma
K->munu	0.012136338	0.00015802845
K->pipi0	0.0088005273	0.00019342986
Pi->munu	0.0057965286	0.00019430008
Si->pin	0.0093852586	4.3146168E-05
Xi->pilamda	0.0078814737	3.9757787E-05