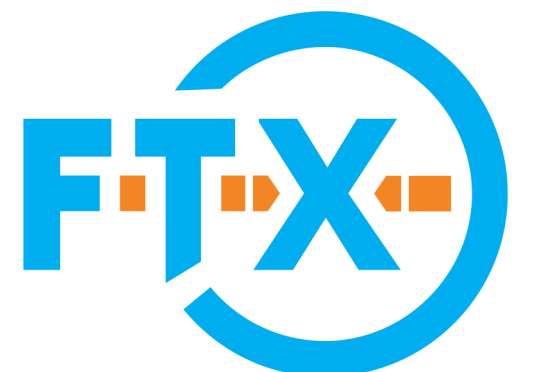
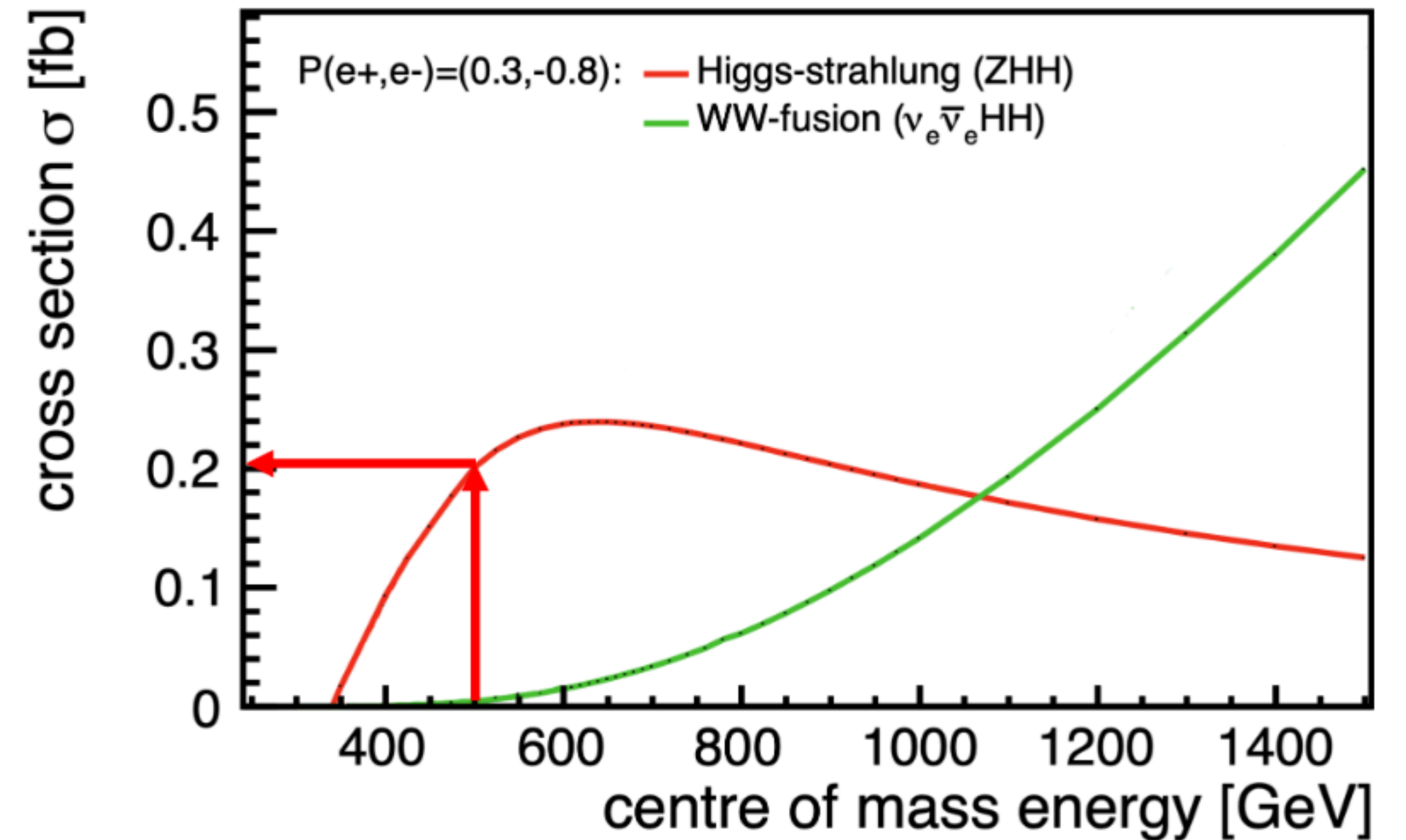


Update on new Higgs self-coupling study

For the ECFA Higgs Factory Report

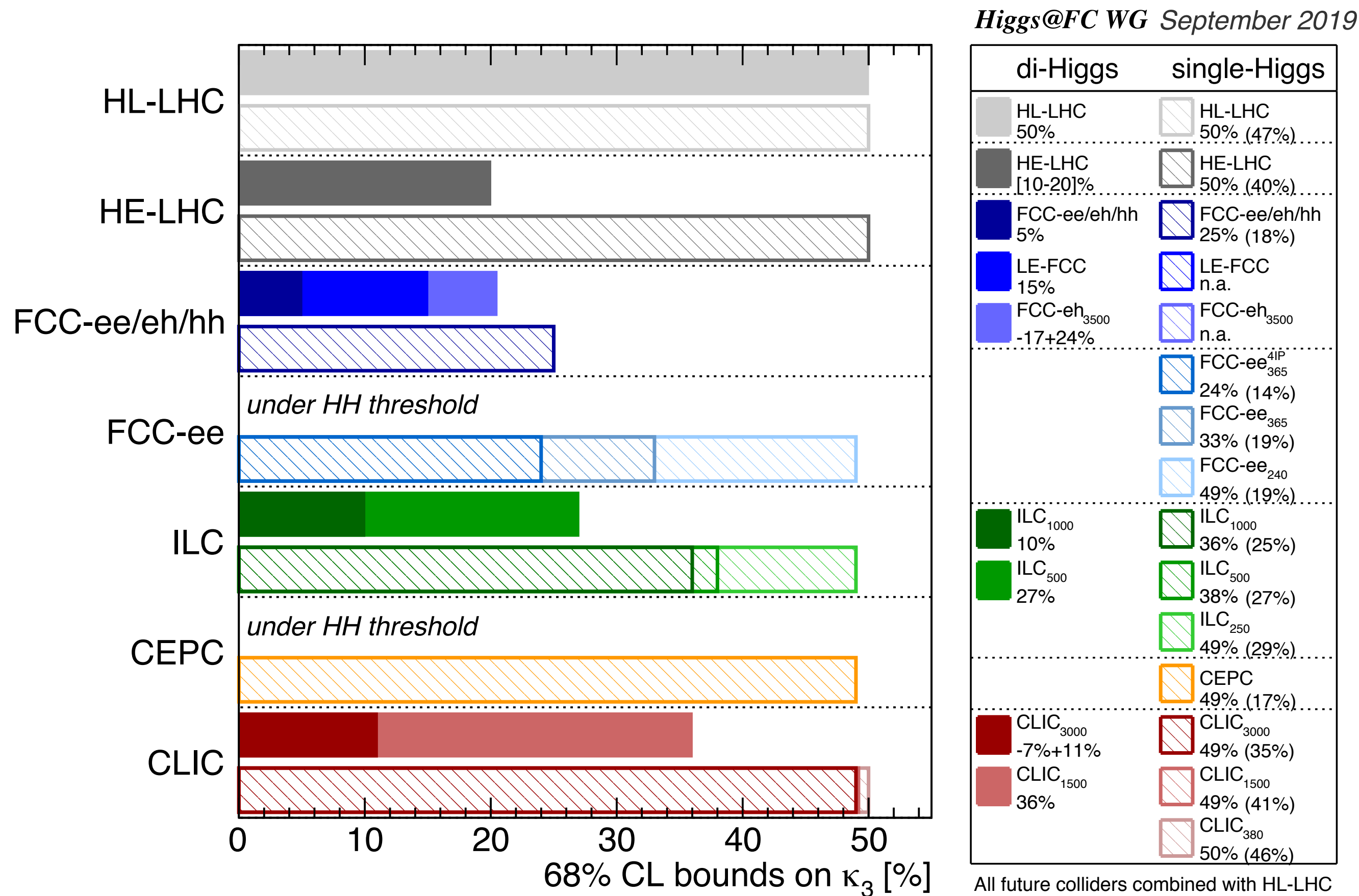
Bryan Bliewert (DESY/UHH), Jenny List (DESY),
Dimitris Ntounis (SLAC), Taikan Suehara (U Tokyo),
Junping Tian (U Tokyo), Julie Torndal (DESY/UHH),
Caterina Vernieri (SLAC)

ILD Software & Analysis Meeting, Jan 21 2025



Motivation I

Higgs self-coupling as key part of physics case for e+e- collisions at ≥ 500 GeV



Key question of the community in the upcoming EPPSU: **Will a Linear Collider do any better than the HL-LHC ?**

HL-LHC update will only be known from their strategy submission, but we should not be surprised if from the previous 50% \rightarrow 25%

– for the SM case!

Apples - Oranges - Pears

A slide from Marcel's talk at the LC Vision Community Event

Top Yukawa coupling comparison

M. L. Mangano et al., *Measuring the Top Yukawa Coupling at 100 TeV*,
 J. Phys. G **43** (2016) 035001, DOI: [10.1088/0954-3899/43/3/035001](https://doi.org/10.1088/0954-3899/43/3/035001),
 arXiv: [1507.08169](https://arxiv.org/abs/1507.08169) [hep-ph].

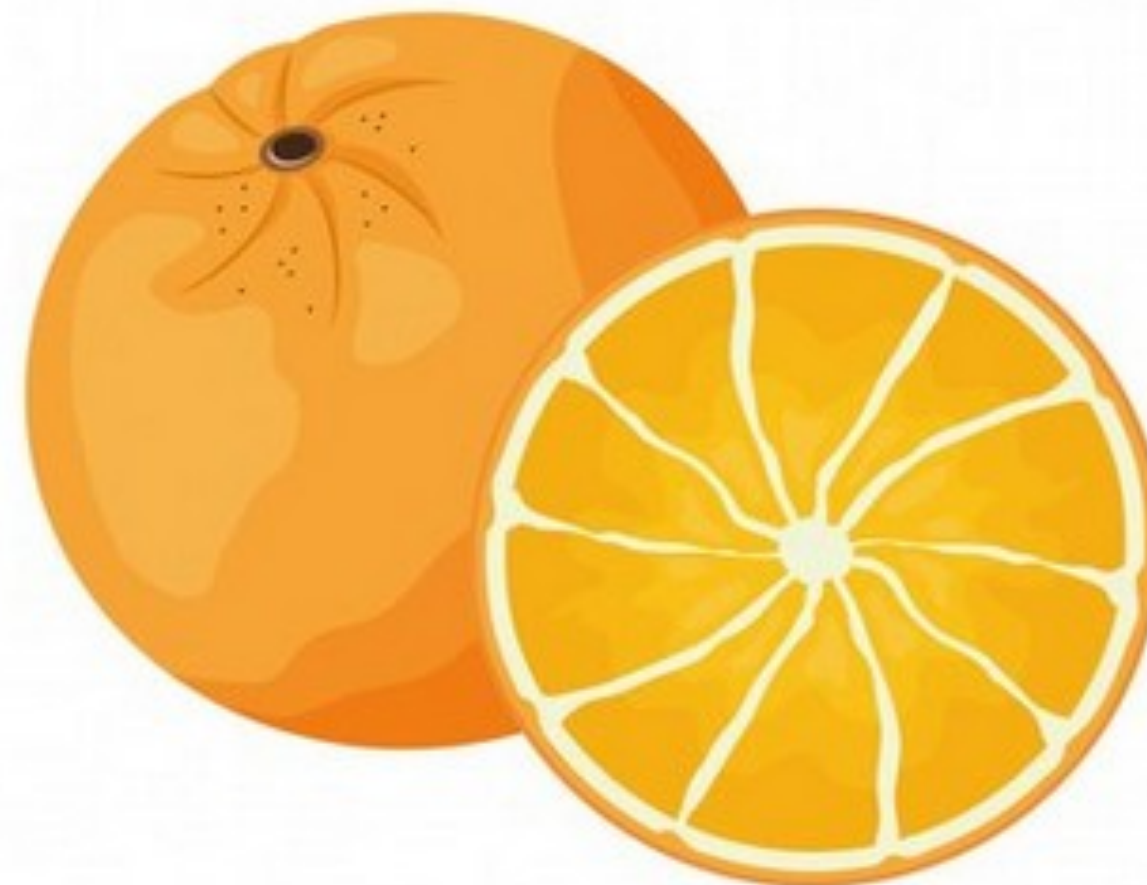
Z. Liu et al., *Top Yukawa coupling determination at high energy muon collider*,
 Phys. Rev. D **109** (2024) 035021, DOI: [10.1103/PhysRevD.109.035021](https://doi.org/10.1103/PhysRevD.109.035021),
 arXiv: [2308.06323](https://arxiv.org/abs/2308.06323) [hep-ph].

S2 projection: “apples”

LC prospects: “oranges”

Theory studies: “pears”

Values in % units		LHC	HL-LHC	ILC500	ILC550	ILC1000	CLIC	FCChh	μ -coll
δy_t	Global fit	12%	5.1%	3.1%	2.6%	1.5%	3.0%	-	-
	Indiv. fit	10%	3.7%	2.8%	2.3%	1.4%	2.5%	1%	1.5%

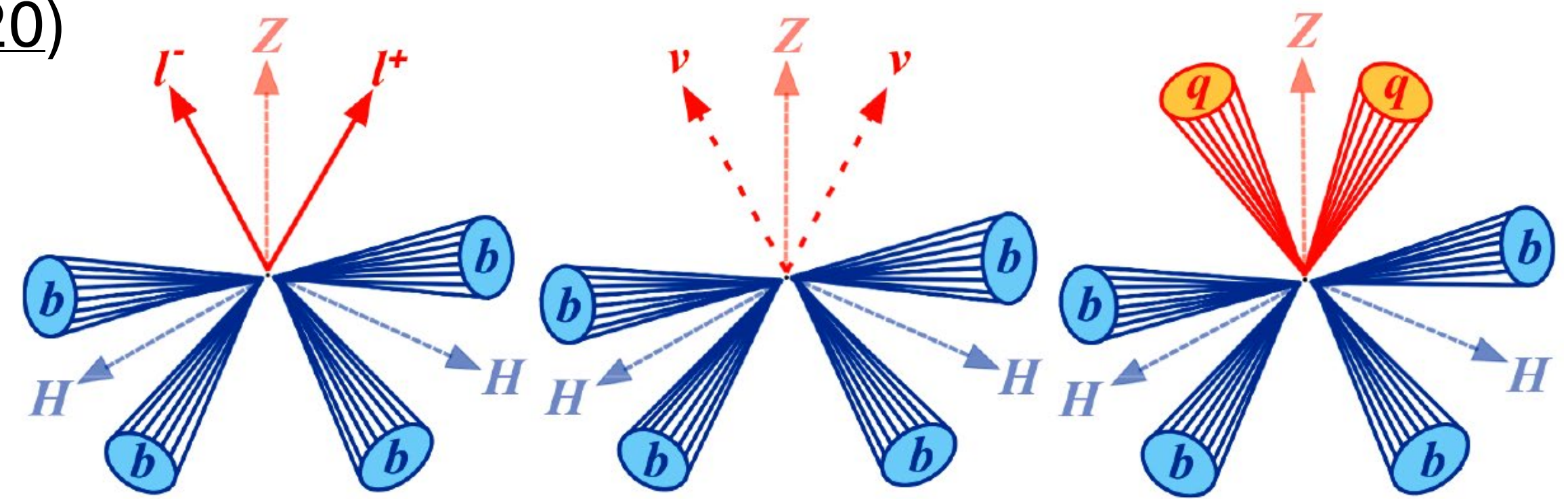


The previous ZHH Analysis

ILC500 based on ILD DBD2013

➤ extensive projections at ILC500 ([DESY-Thesis-16-027](#))

- based on ILD detector concept ([DBD2013](#), [IDR2020](#)) and *fully simulated* event samples
- 17 background and 3 signal channels considered
- multivariate (MVA) tools for multiple steps e.g. lepton and flavor tagging, background rejection etc.
- event counting weighted by m_{HH}^2 for further sensitivity enhancement



Lepton, neutrino and hadron channel of the signal process ZHH.
From [Du16]

➤ precision reach after running $4ab^{-1}$ at 500 GeV ($HH \rightarrow b\bar{b}b\bar{b} + HH \rightarrow b\bar{b}W^\pm W^\mp$)

$$\frac{\Delta\sigma_{ZHH}}{\sigma_{ZHH}} = 16.8\%$$

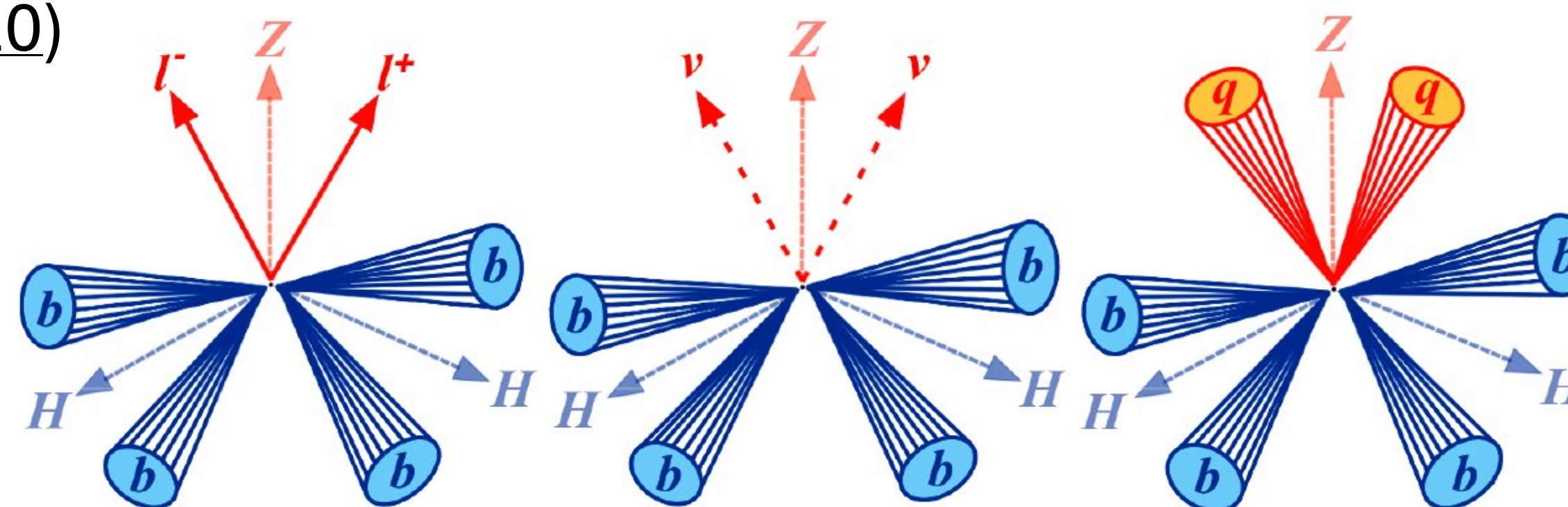
$$\frac{\Delta\lambda_{SM}}{\lambda_{SM}} = 26.6\% \quad (10\% \text{ with additional upgrade to 1 TeV})$$

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8 σ observation of ee -> ZHH

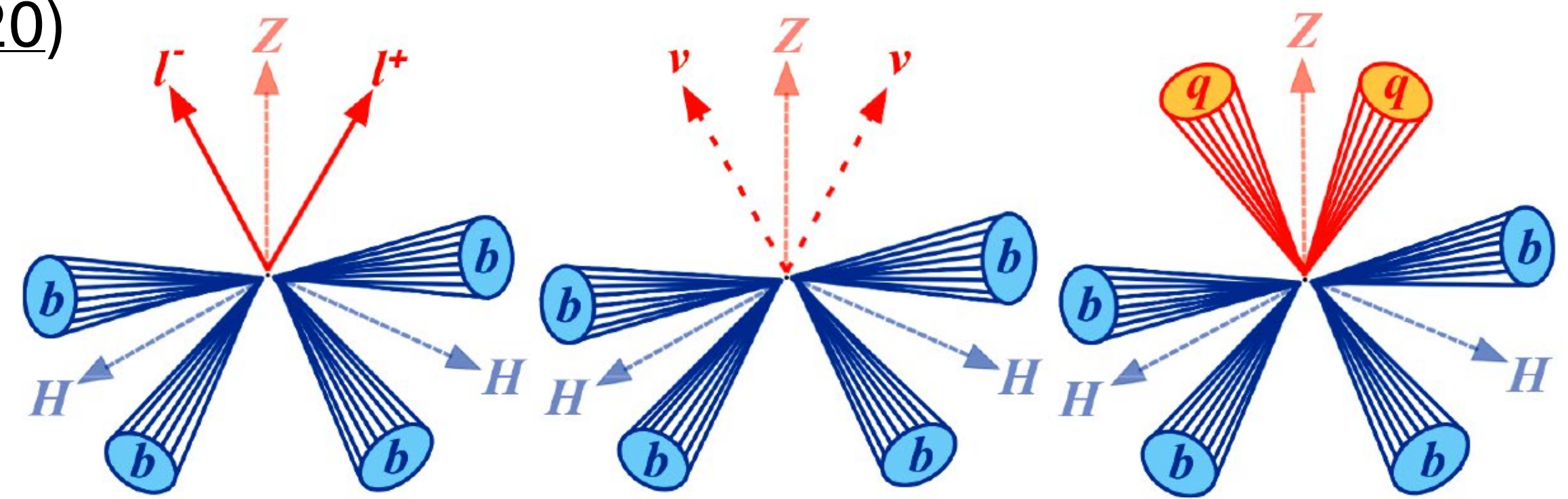
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8 σ observation of ee -> ZHH

$$\Delta\lambda_{SM}/\lambda_{SM} = 26.6\% \quad (10\% \text{ with additional upgrade to 1 TeV})$$

only 3.x σ observation of λ_{SM}

Bottlenecks of the ZHH analysis

As identified during 2014 analysis and (relative) improvement impact

- jet pairing and jet misclustering: “perfect“ jet clustering → 40% improvement
improve di-jet mass resolution
- removal of $\gamma\gamma$ overlay: 15% improvement expected
also: improve ISR reconstruction
- flavor tagging: 11% improvement expected from 5% eff. increase with newer LCFIPlus
important as $H \rightarrow b\bar{b}$ is the dominant Higgs decay channel
- adding $Z \rightarrow \tau\tau$ channel: 8% improvement expected
include a yet unaccounted decay channel
- more modern ML architectures for signal/background selection
improvement expected when transitioning from BDTs to (e.g.) transformer-based models etc.
- separation of ZHH diagrams with/without the self-coupling
would directly improve the sensitivity on λ (lower sensitivity factor)

Expected relative
improvements from
[DESY-Thesis-16-027](#)

Bottlenecks of the ZHH analysis

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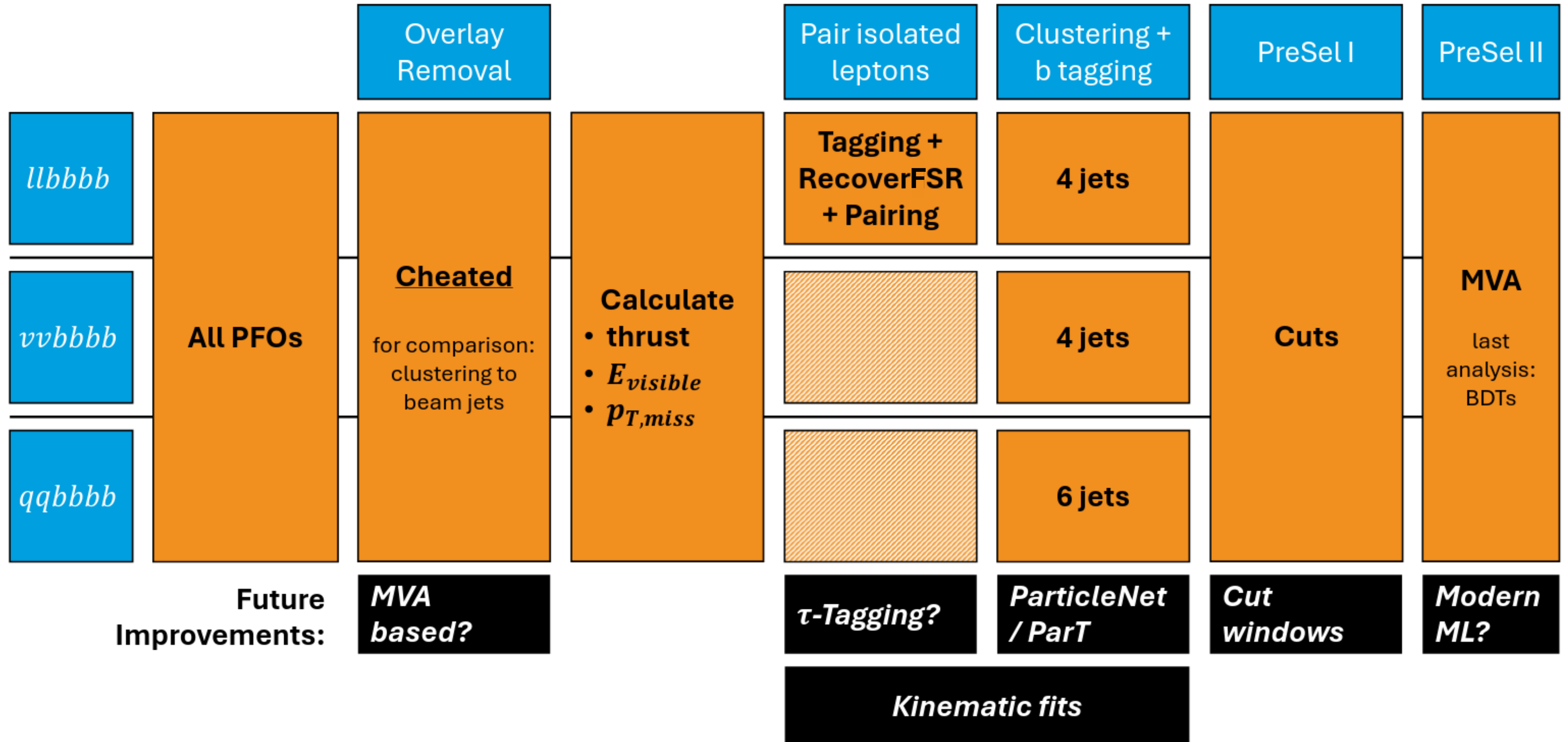
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**if 25% (rel.) improvement out of (a combination) of these
=> 5 σ discovery of λ_{SM}**

Expected relative
improvements from
[DESY-Thesis-16-027](#)

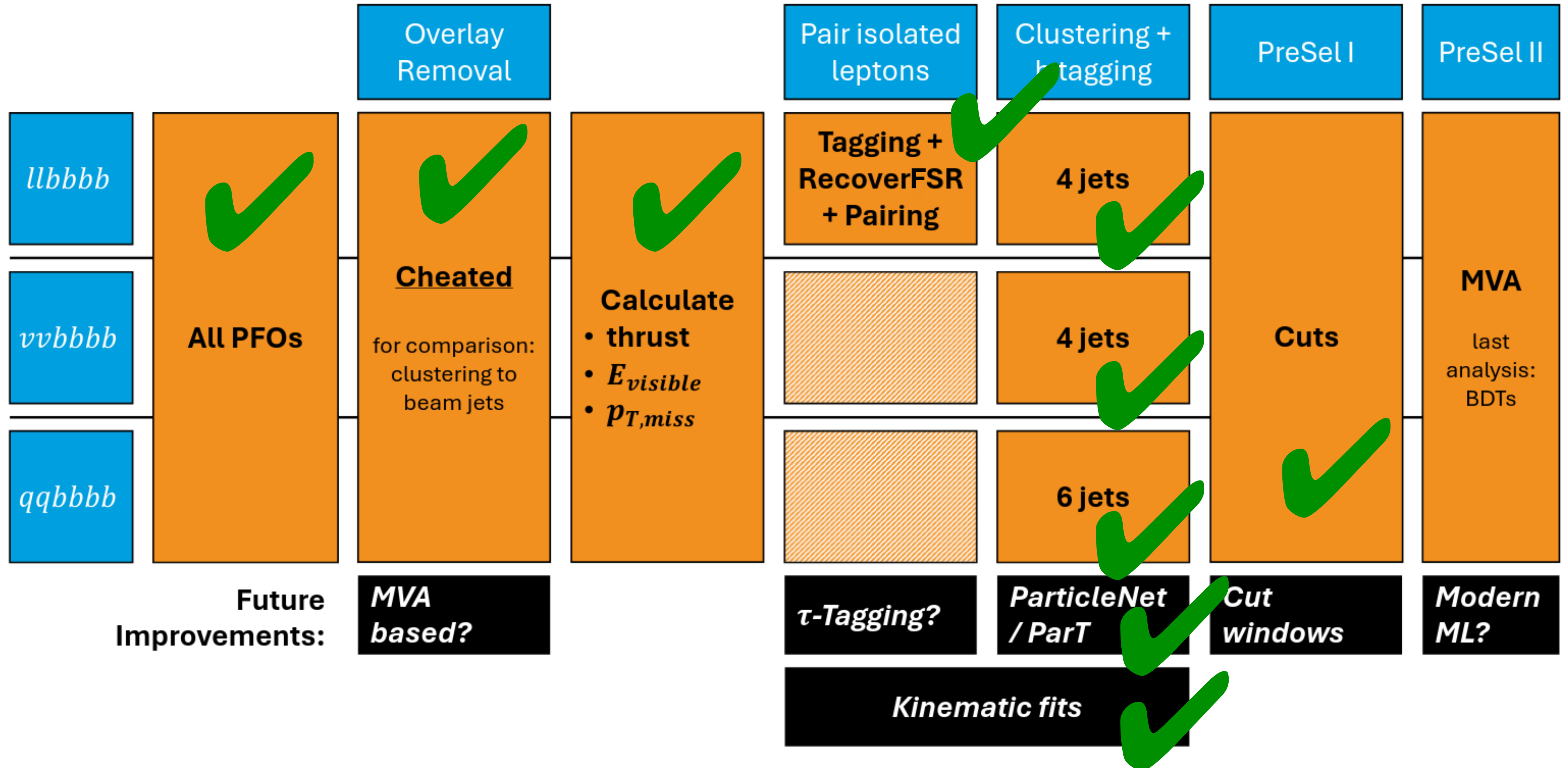
Towards a full update of the di-Higgs analysis

Analysis Flow — set up and working to a large extent



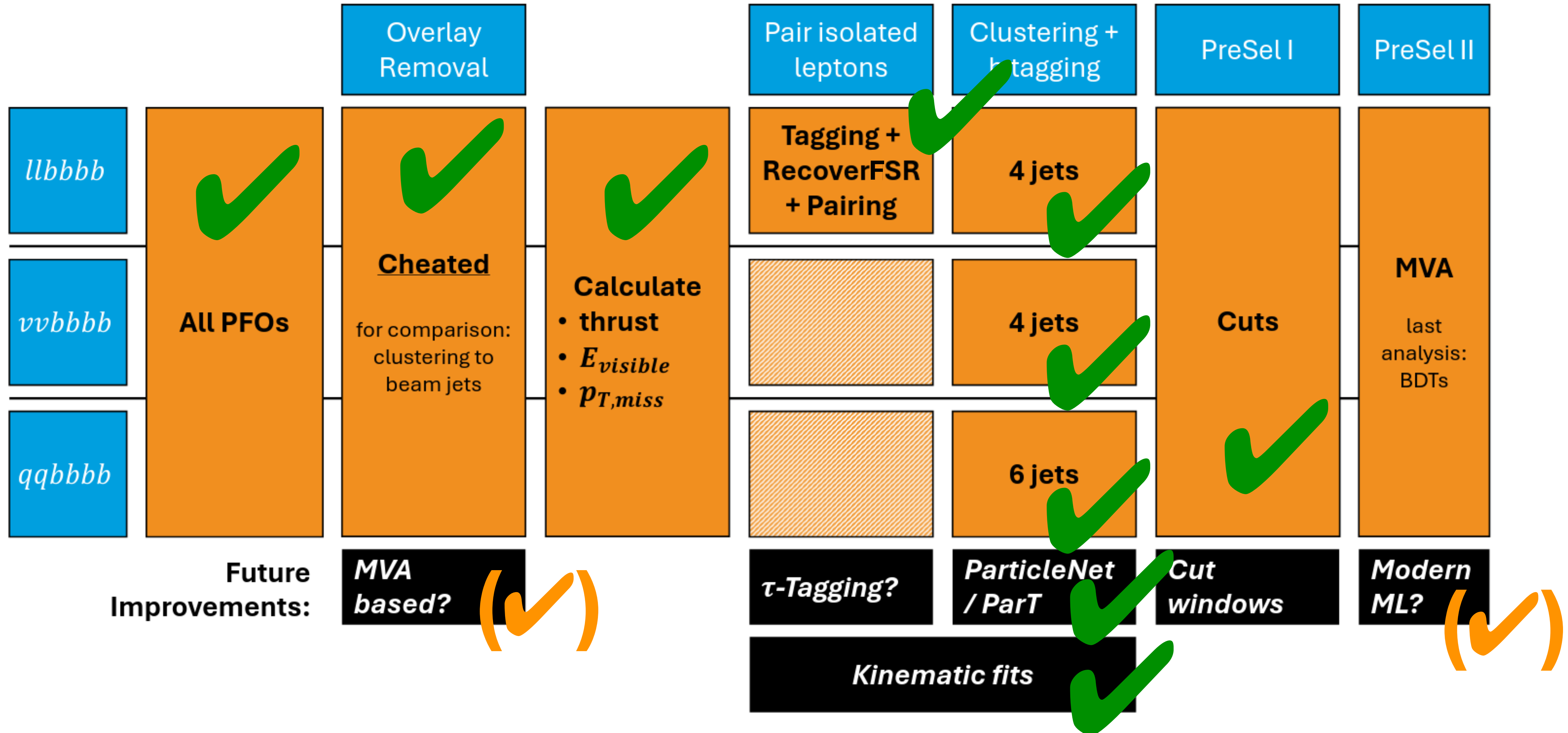
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Towards a full update of the di-Higgs analysis

Analysis Flow — set up and working to a large extent



And in addition...

... and some missing things

- **MC samples**
 - “ZHH” and “ZZH” generated, simulated, reconstructed in 2022/23
 - SM backgrounds at 500 GeV from IDR production — modern PID not available
 - would like to move full analysis to 550 GeV
 - new production at 550 GeV underway, 2f / 4f generated, 6f / 8f wip
 - SGV / full sim comparison very successful => can use SGV for evaluating bulk background rejection
- **Flavour tagging**
 - major progress with actually applying ML in analysis
 - ML tools require huge training samples => SGV, wip
- **kinematic reconstruction and general event selection**
 - major progress in porting semi-leptonic decay correction / kinematic fitting / matrix-elements ...
 - even more expected from full ML selection
c.f. talk by Manqi last week
- **we're not quite there yet to run the whole analysis chain — but not far away either!**

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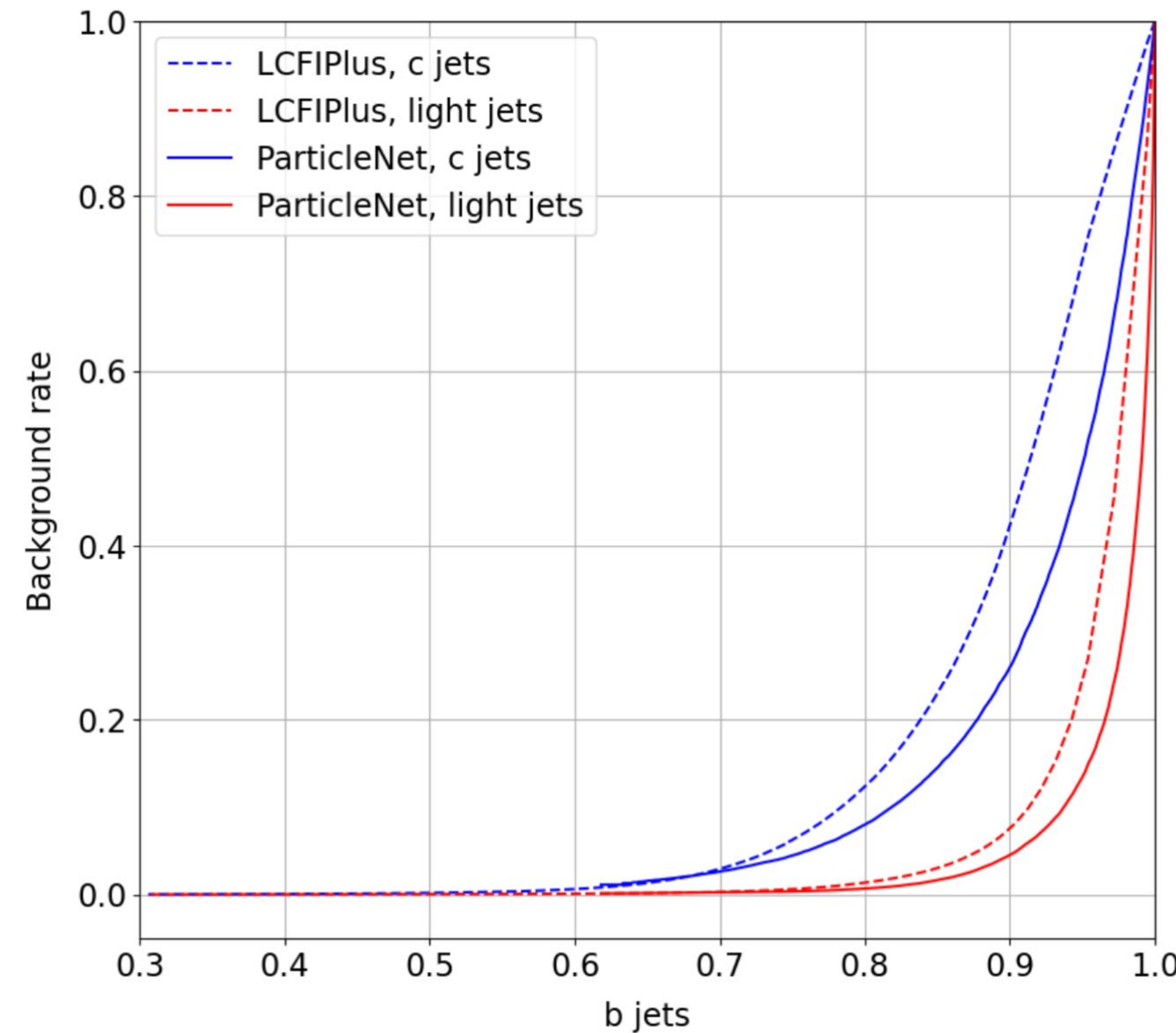
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Flavour-Tagging with ML

ParticleNet and ParticleTransformer (ParT)

- significant improvements wrt LCFIPlus achieved
- NEW: recipe to perform inference from Marlin MarlinMLFlavorTagging
=> essential for application in full reconstruction & analysis chain!

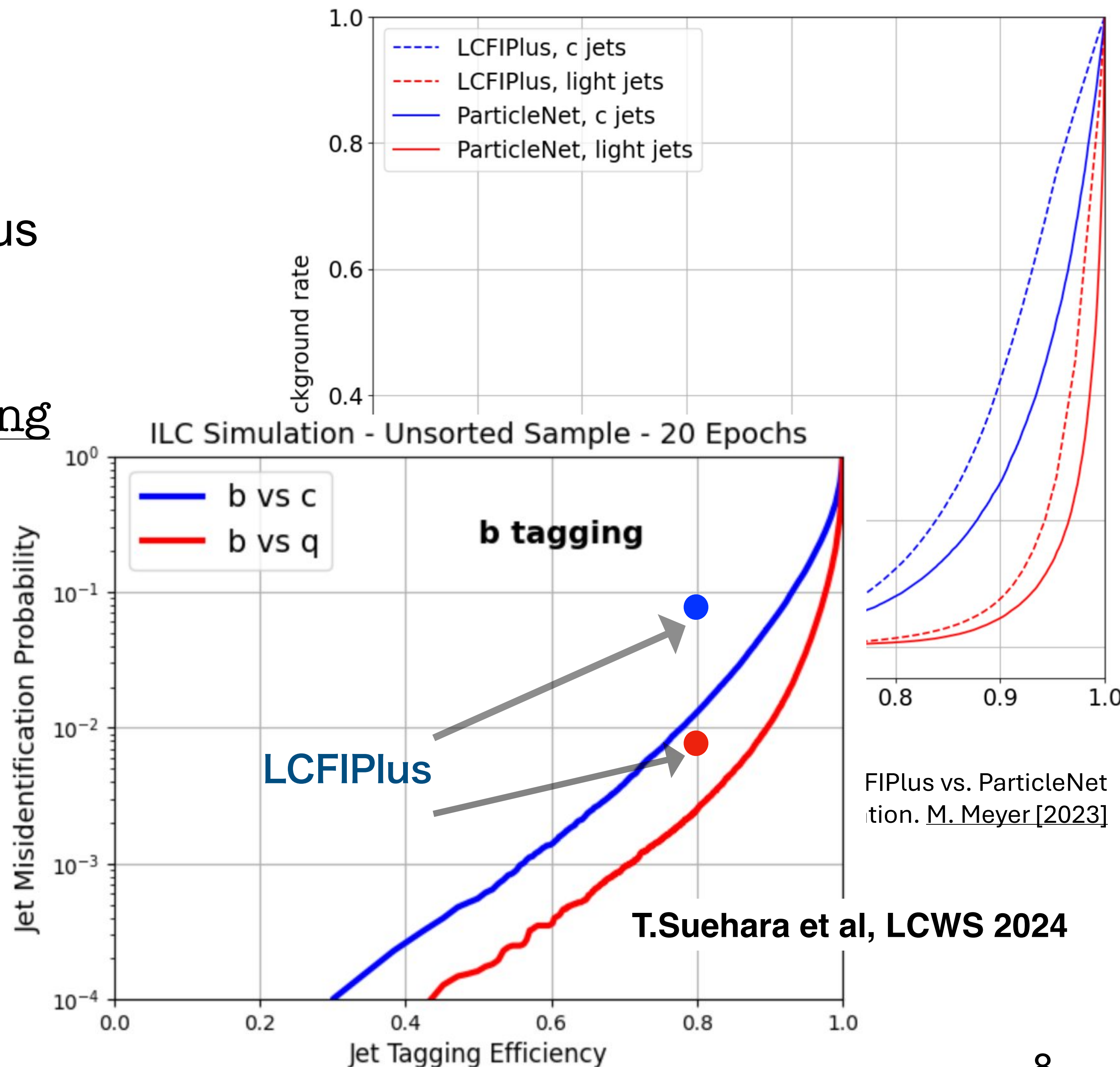


Flavor tagging performance of LCFIPlus vs. ParticleNet using ILD full simulation. [M. Meyer \[2023\]](#)

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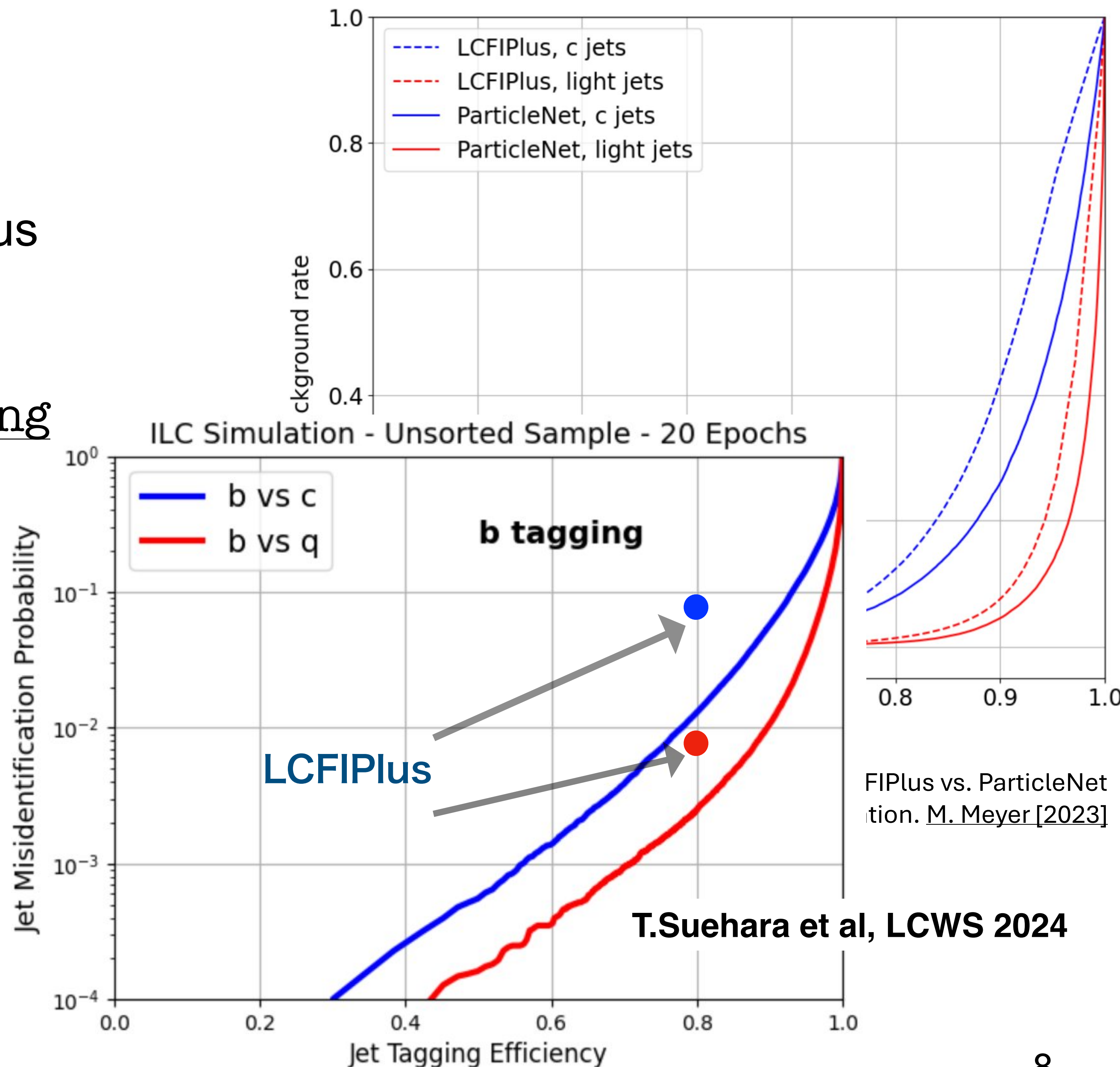


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Evaluation of impact in ZHH analysis ongoing, potential improvement even larger than conceivable in 2016...



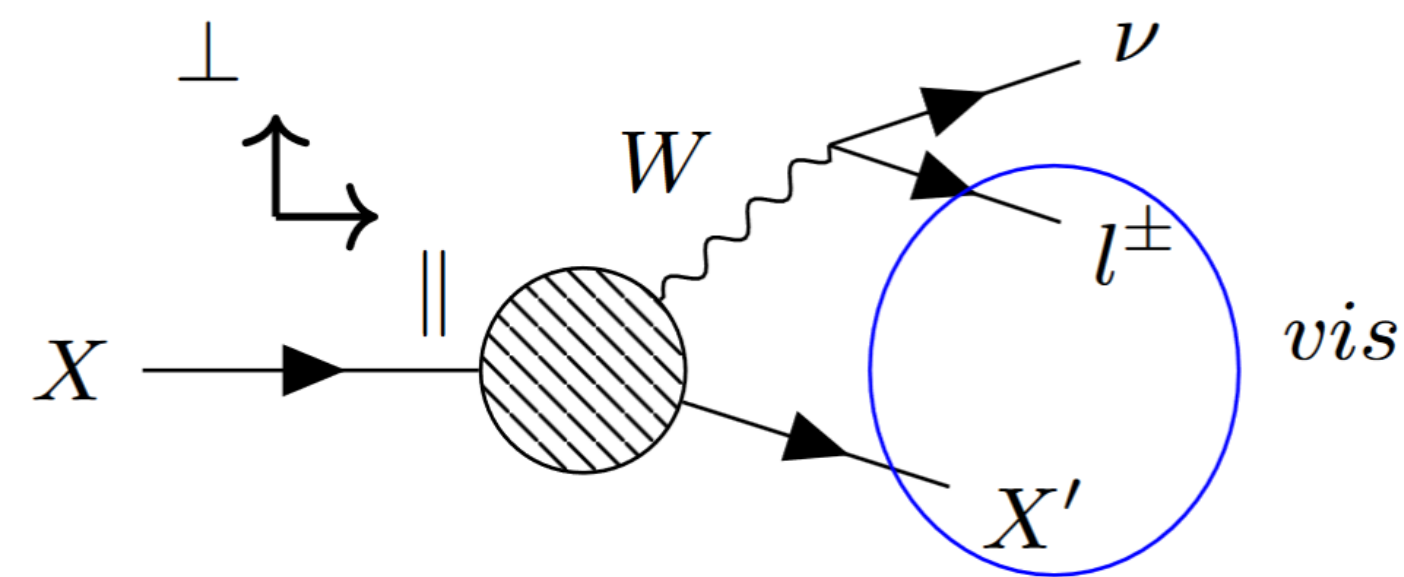
Flavour Tagging with ML

Final status for now, motivate ~10% higher efficiency at same background level

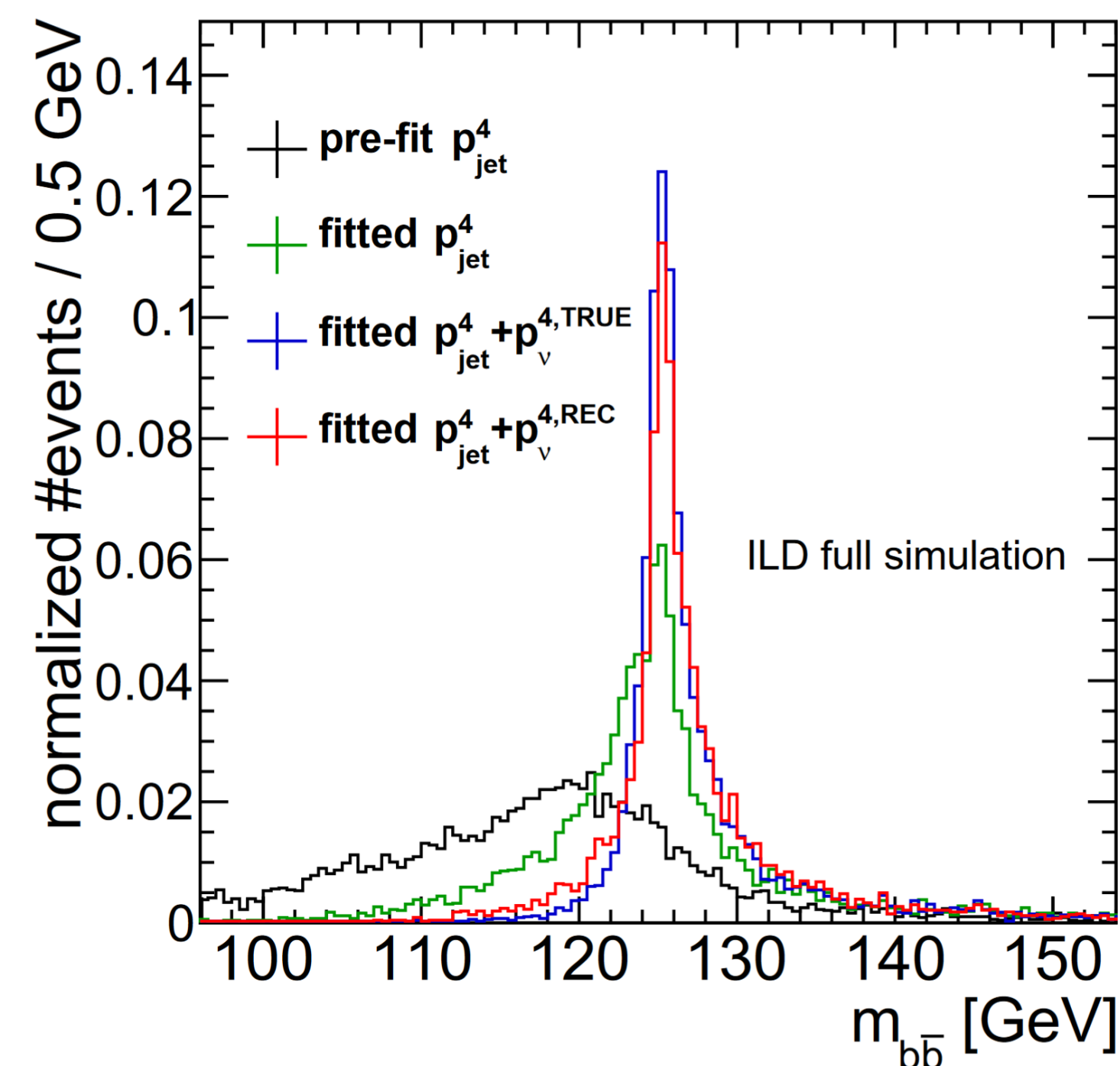
Neutrino Correction with Vertexing, PFlow and Kinematic Fit

Improved $m(bb)$ invariant mass reconstruction

- for semileptonic decay (SLD) processes
 - already in $ZH \rightarrow b\bar{b}/c\bar{c}$, 66% of events include at least one SLD
- procedure:
 - identify/tag heavy quark jet
 - identify lepton in jet
 - calculate neutrino four momentum from kinematics with kinematic fitting, the best solution is selected
- status: in production (in MarlinReco)



Recovering the neutrino kinematics. Y. Radkhorrani [2022]

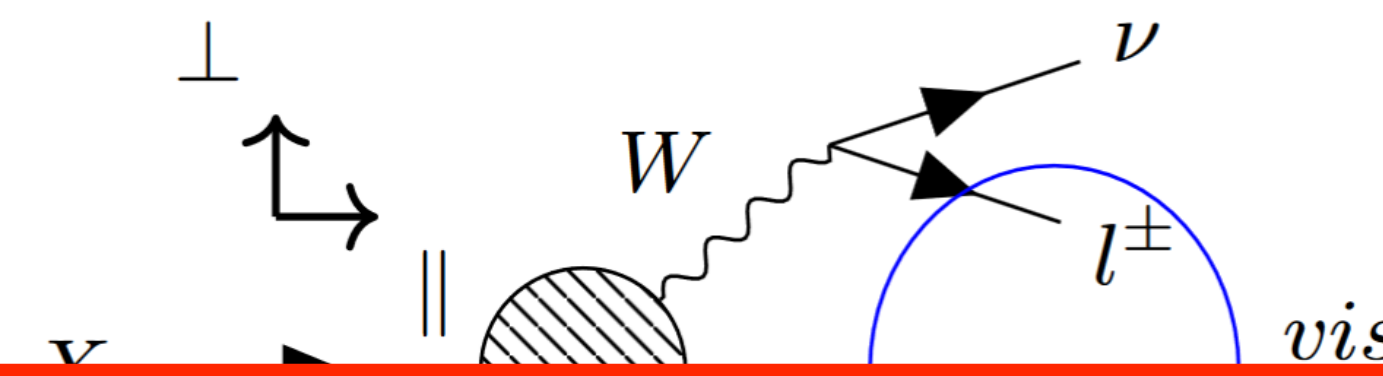


Improved di-jet mass reconstruction. Y. Radkhorrani [2022]

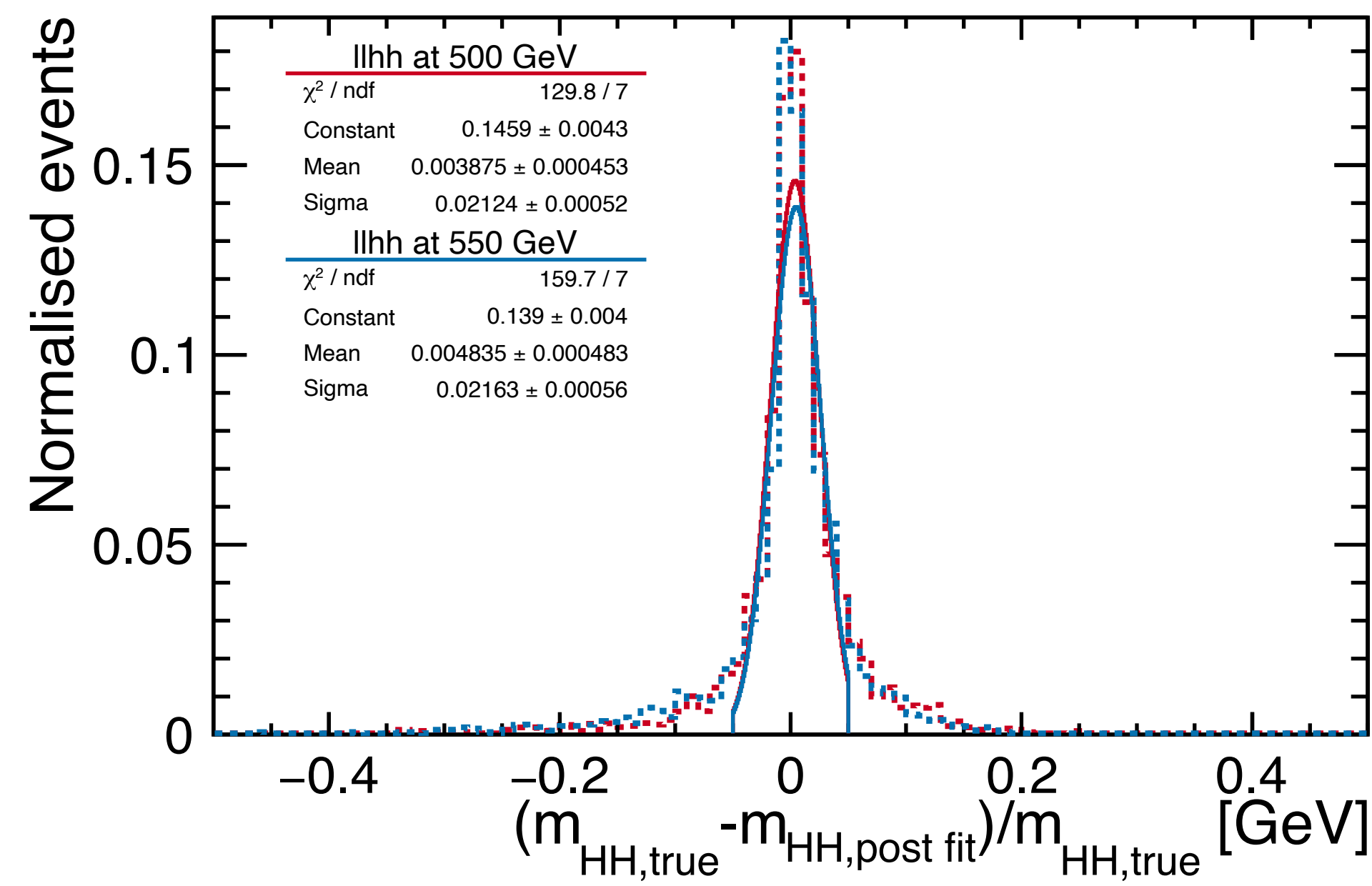
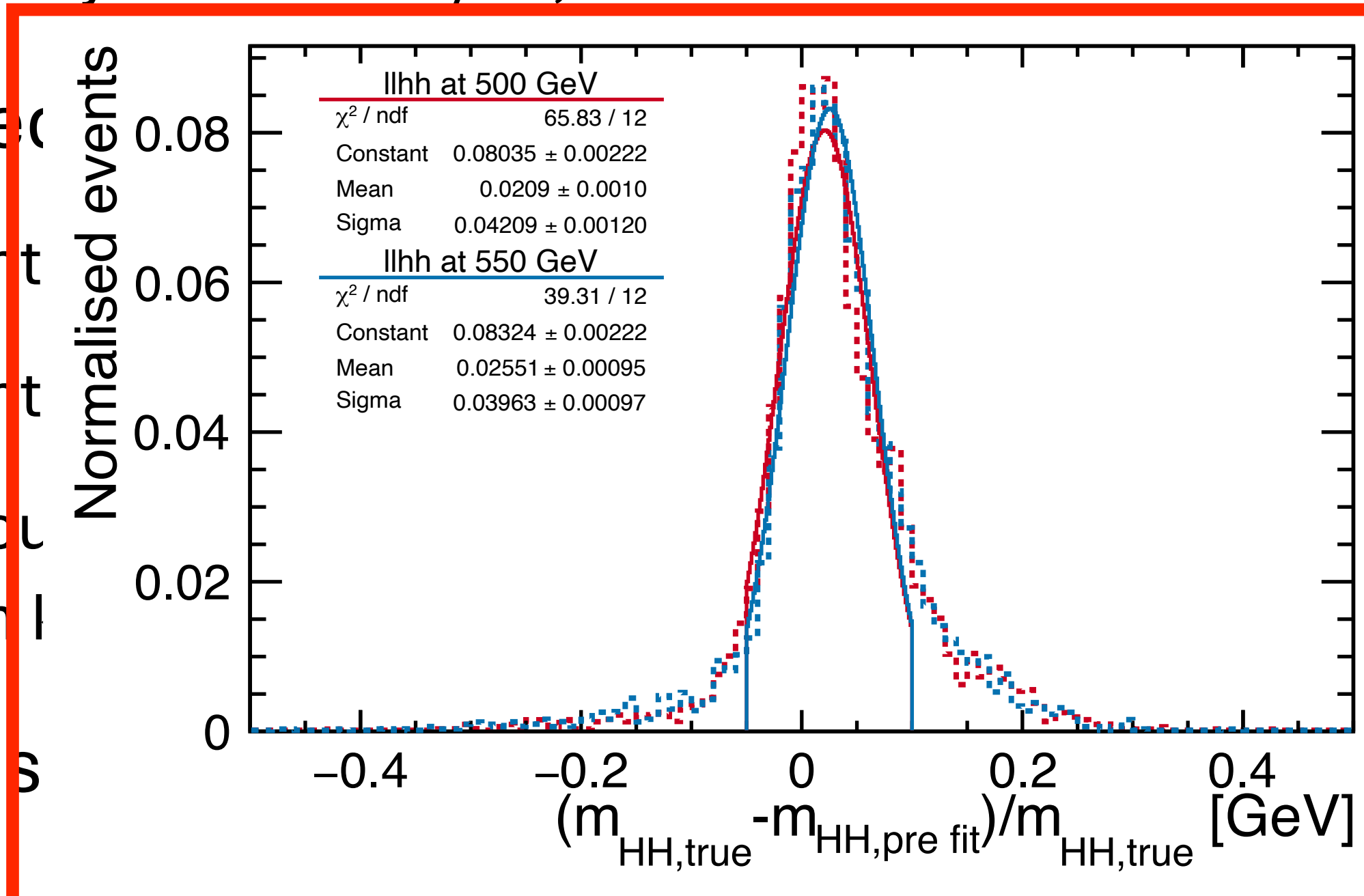
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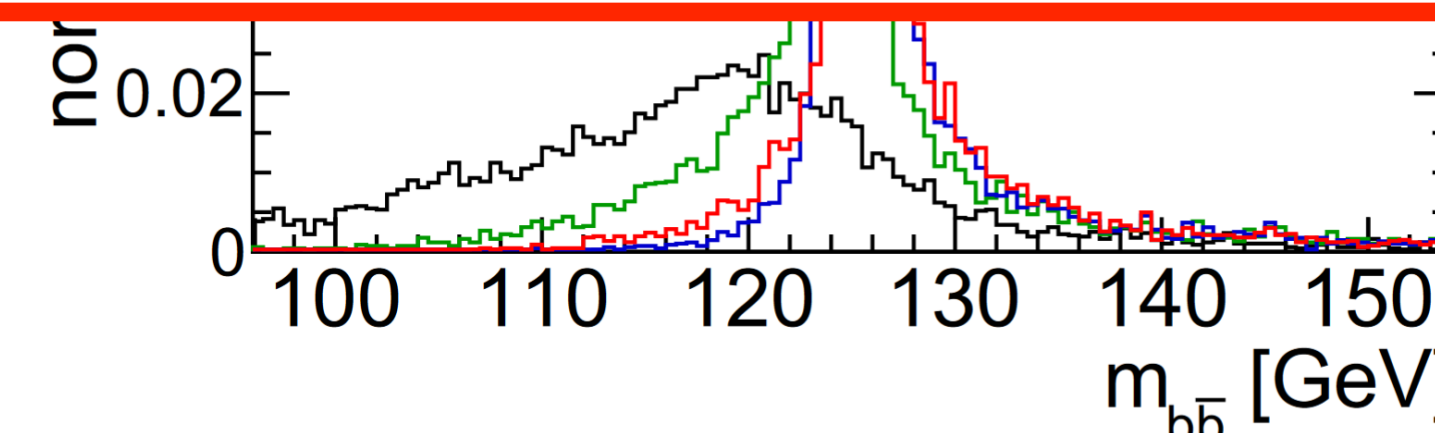
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- process
- ident
- ident
- calc
- with
- status



Shown to work on ZHH, twice better resolution of $m(HH)$ cf talk by Julie Dec 4



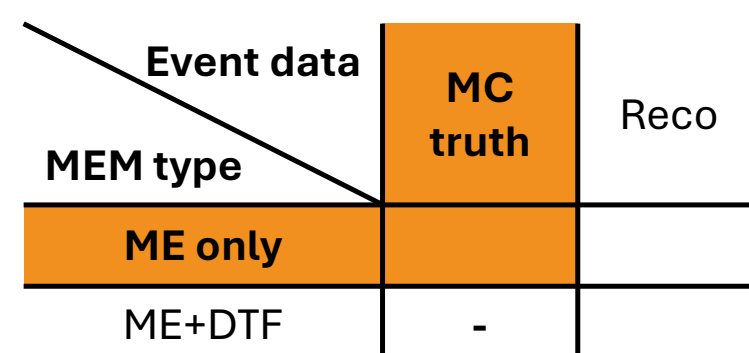
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Matrixelements for ZZH / ZHH discrimination

In theory the optimal observable...

generator level check

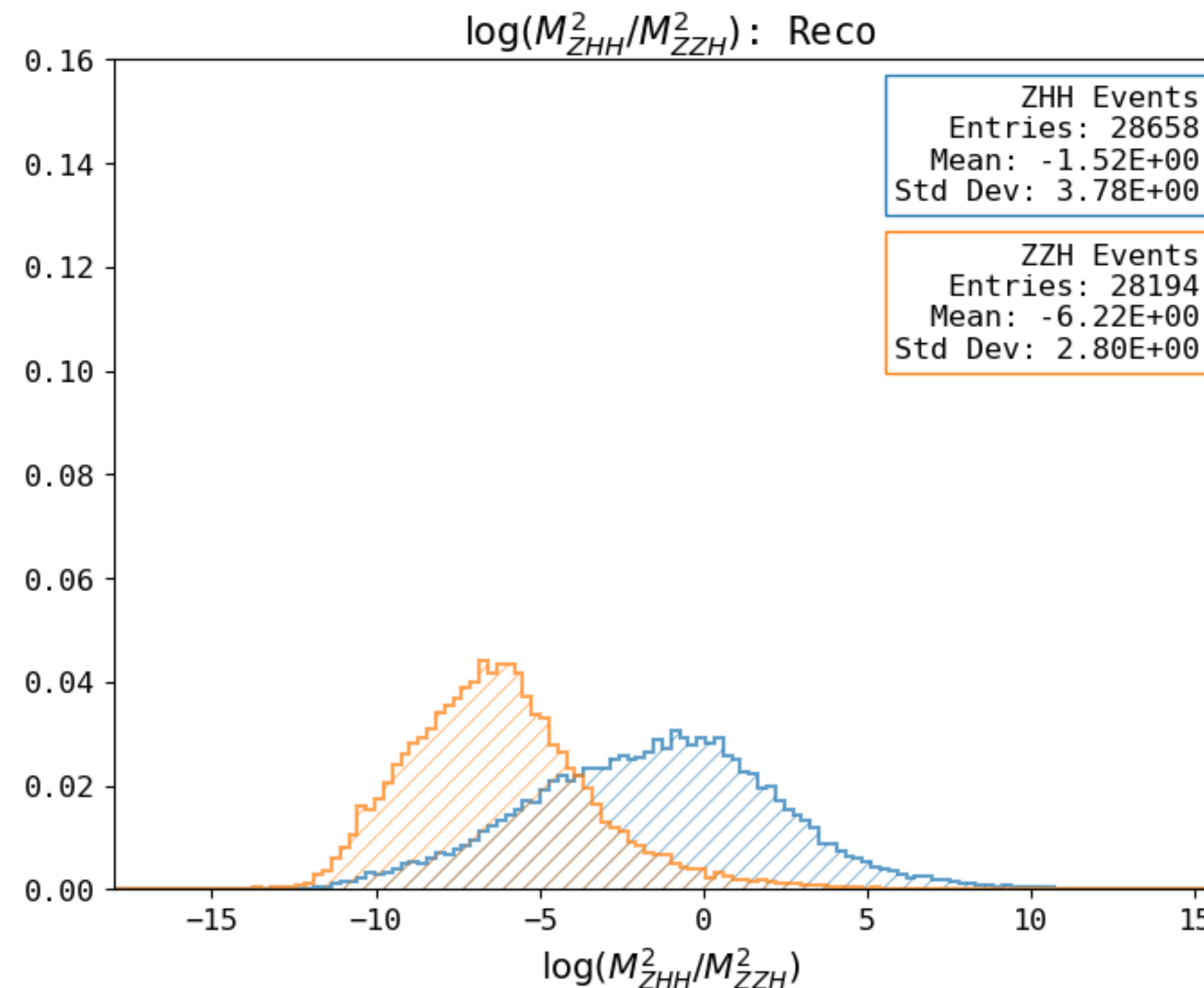
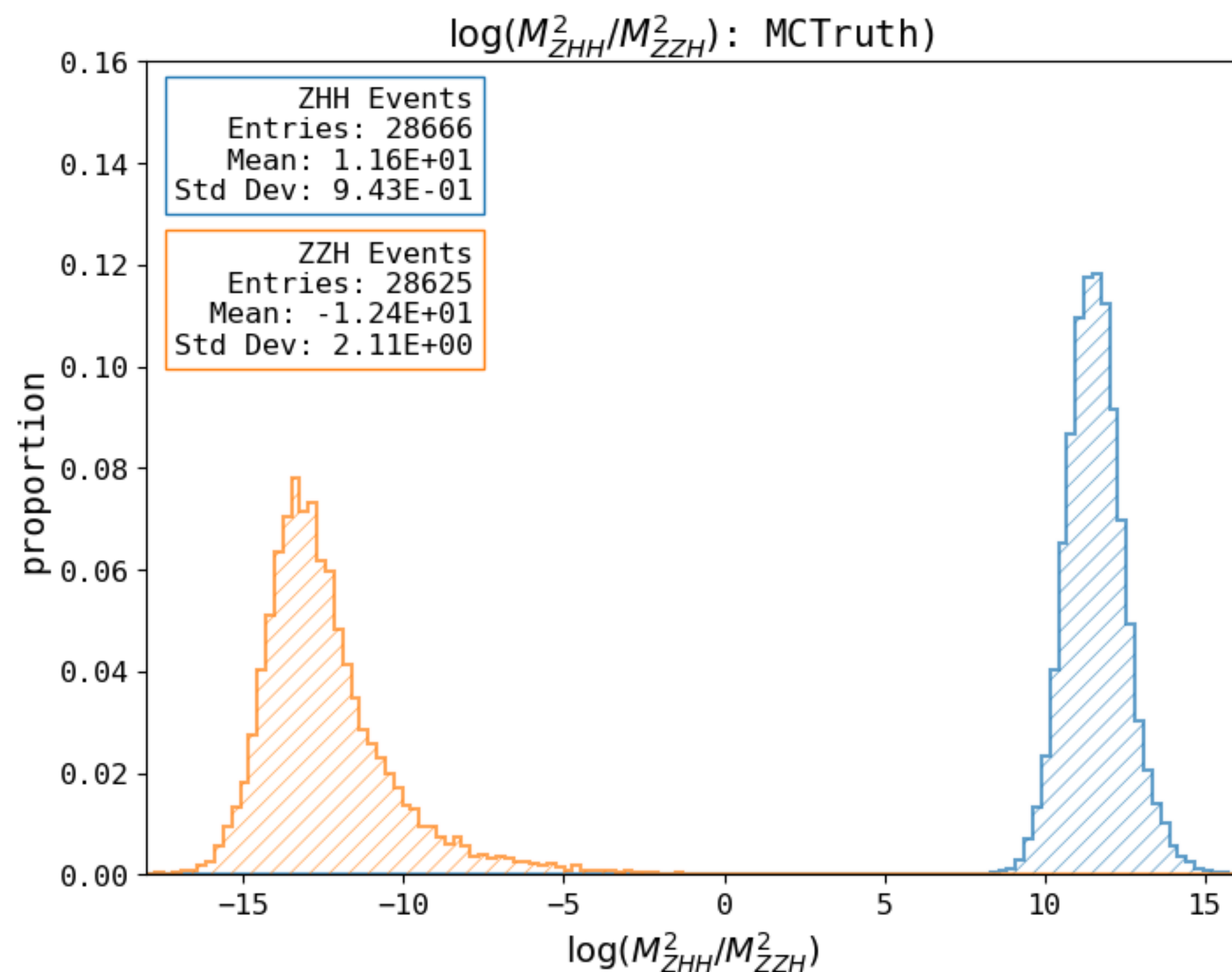
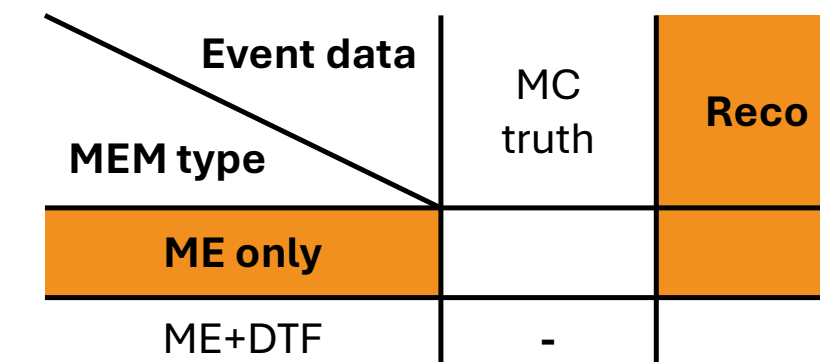
➤ excellent separation



naive MEM

➤ separation power lost

➔ need to describe smearing with TFs

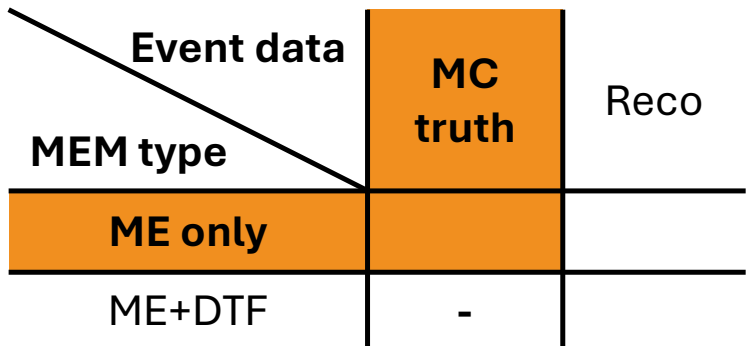


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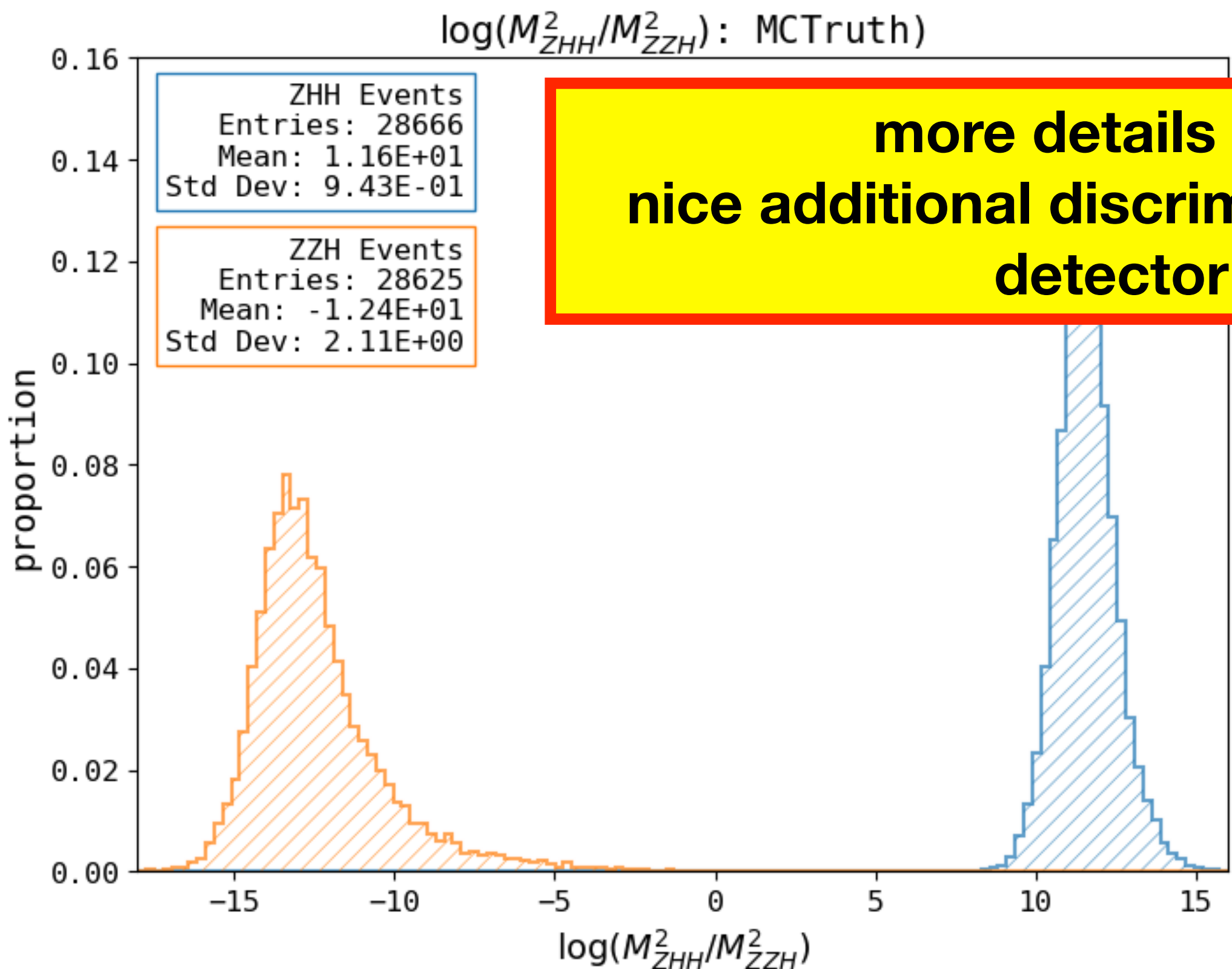
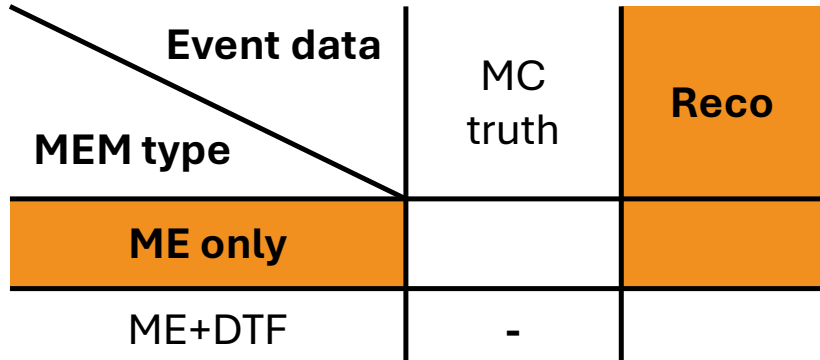
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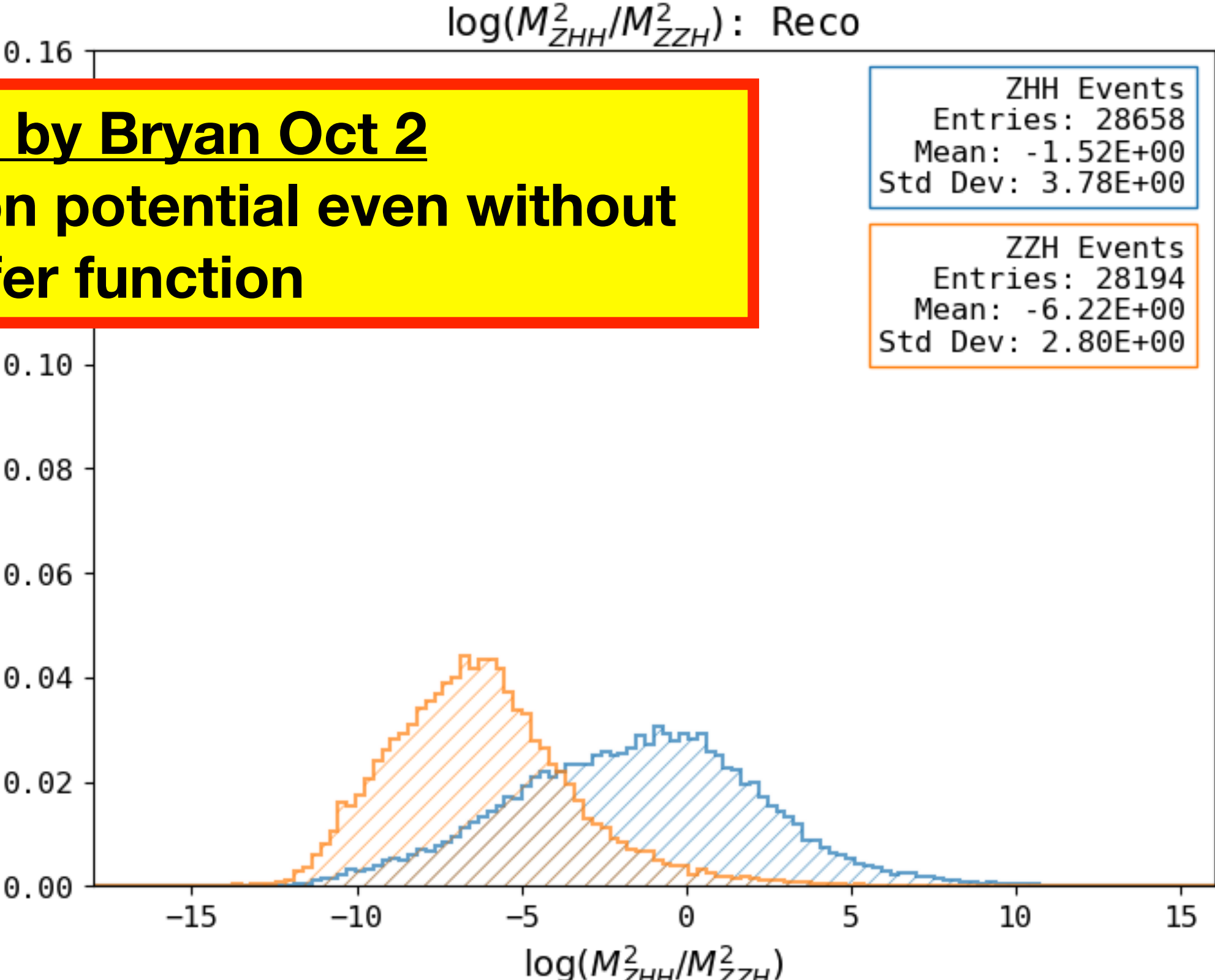
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➤ separation power lost

➔ need to describe smearing with TFs



more details cf talk by Bryan Oct 2
nice additional discrimination potential even without detector transfer function



Extrapolation scheme

Incorporating the shown flavour tag and kinematic reconstruction/selection improvements

- starting point: Table 9.1 Thesis Claude Dürig with S, B and significances for both polarisations

Pol	eebbbb		mumubbbb		nunubbbb		bbbbbb		qqbbbb		comb sig	comb. X-sec. uncert
	-80,+30	+80,-30	-80,+30	+80,-30	-80,+30	+80,-30	-80,+30	+80,-30	-80,+30	+80,-30		
Significance (meas.) Claude	1.07	0.92	1.26	1.1	1.5	1.54	1.57	1.58	1.55	1.64	4.41	0.227
x ²	1.14	0.85	1.59	1.21	2.25	2.37	2.46	2.50	2.40	2.69	19.46	
s Claude (Tab 9.1)	3.9	2.9	5.1	3.8	5.6	3.6	8.5	5.9	12.6	8.3		
b Claude (Tab 9.1)	7	4.2	8.9	5.3	6.9	1.1	21.9	7	55	16		
s/sqrt(s+b)	1.18	1.09	1.36	1.26	1.58	1.66	1.54	1.64	1.53	1.68	4.39	0.228
x ²	1.40	1.18	1.86	1.59	2.51	2.76	2.38	2.70	2.35	2.83	19.29	

- apply changes to signal s per channel and polarisation, re-calculate combined cross-section significance

- flavour tag improvement: 22.8% -> 17.2%
- kin. sel. improvement: 17.2% -> 16%

- include additional channels (also done for the good old 26.6% ~27%): 16% -> 11.2%

- Z-> tautau
- HH->bbWW
- HH->bb tautau and "other"

- convert to dlamba/lambda with sensitivity factor incl. mHH weighting (1.62):

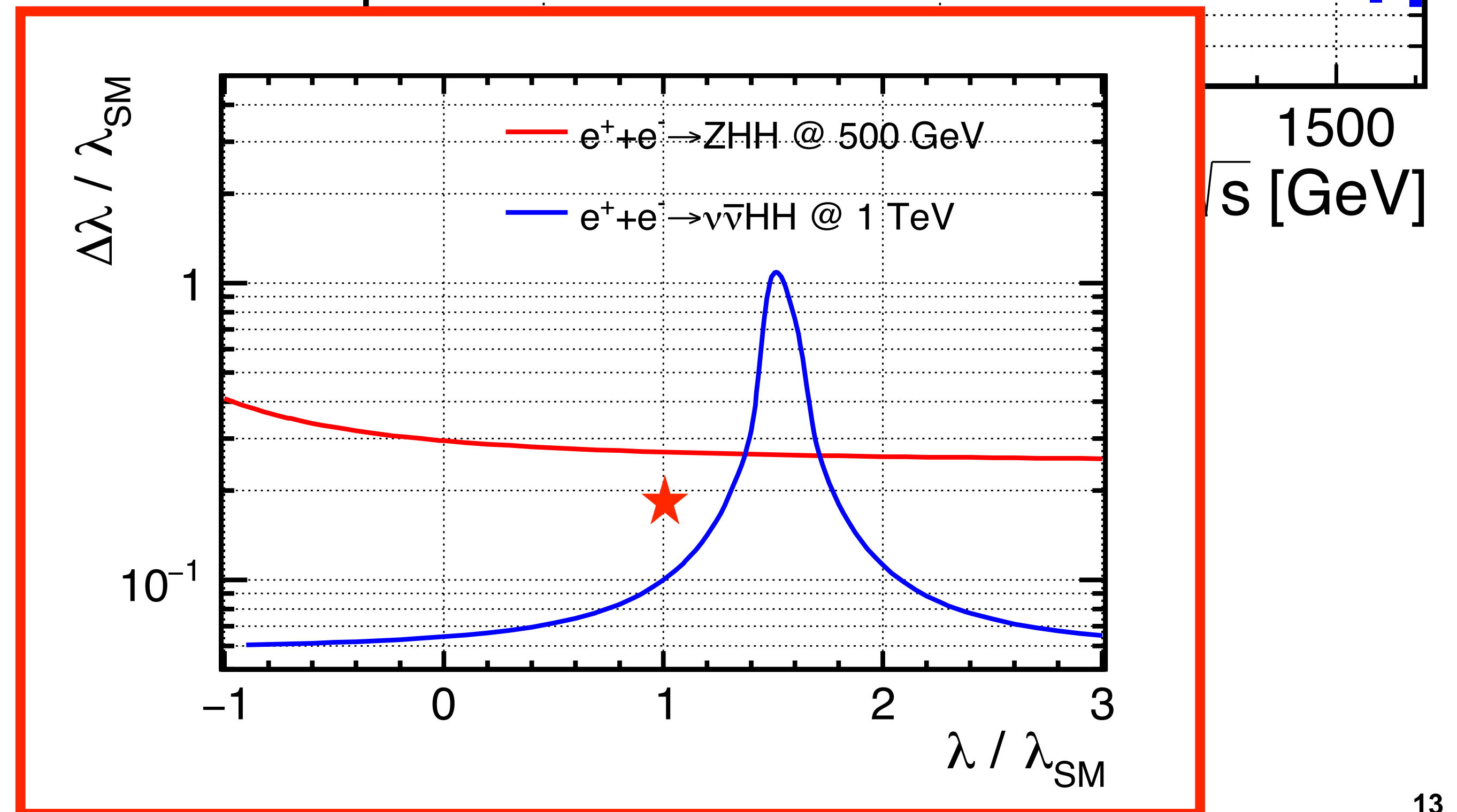
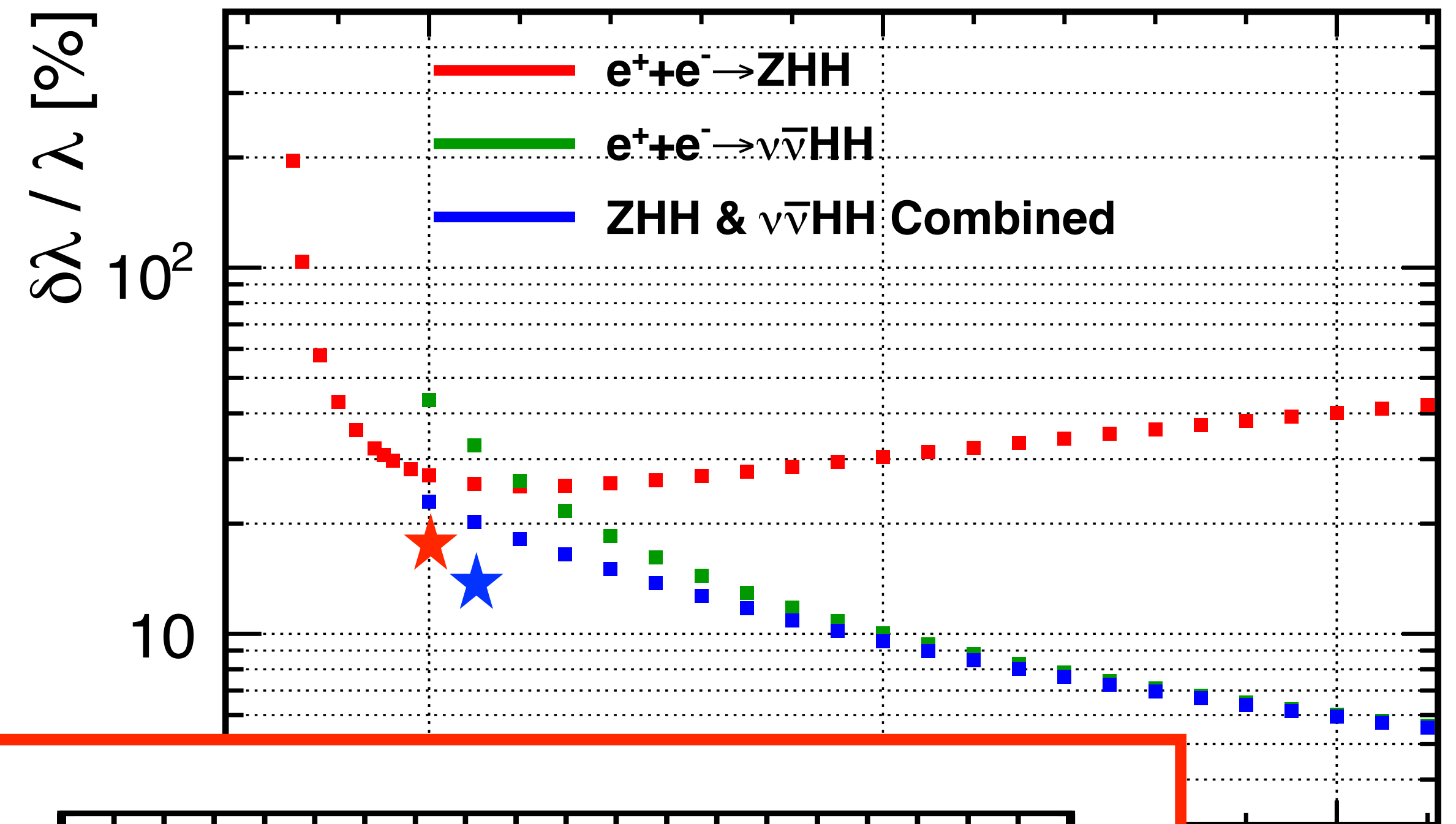
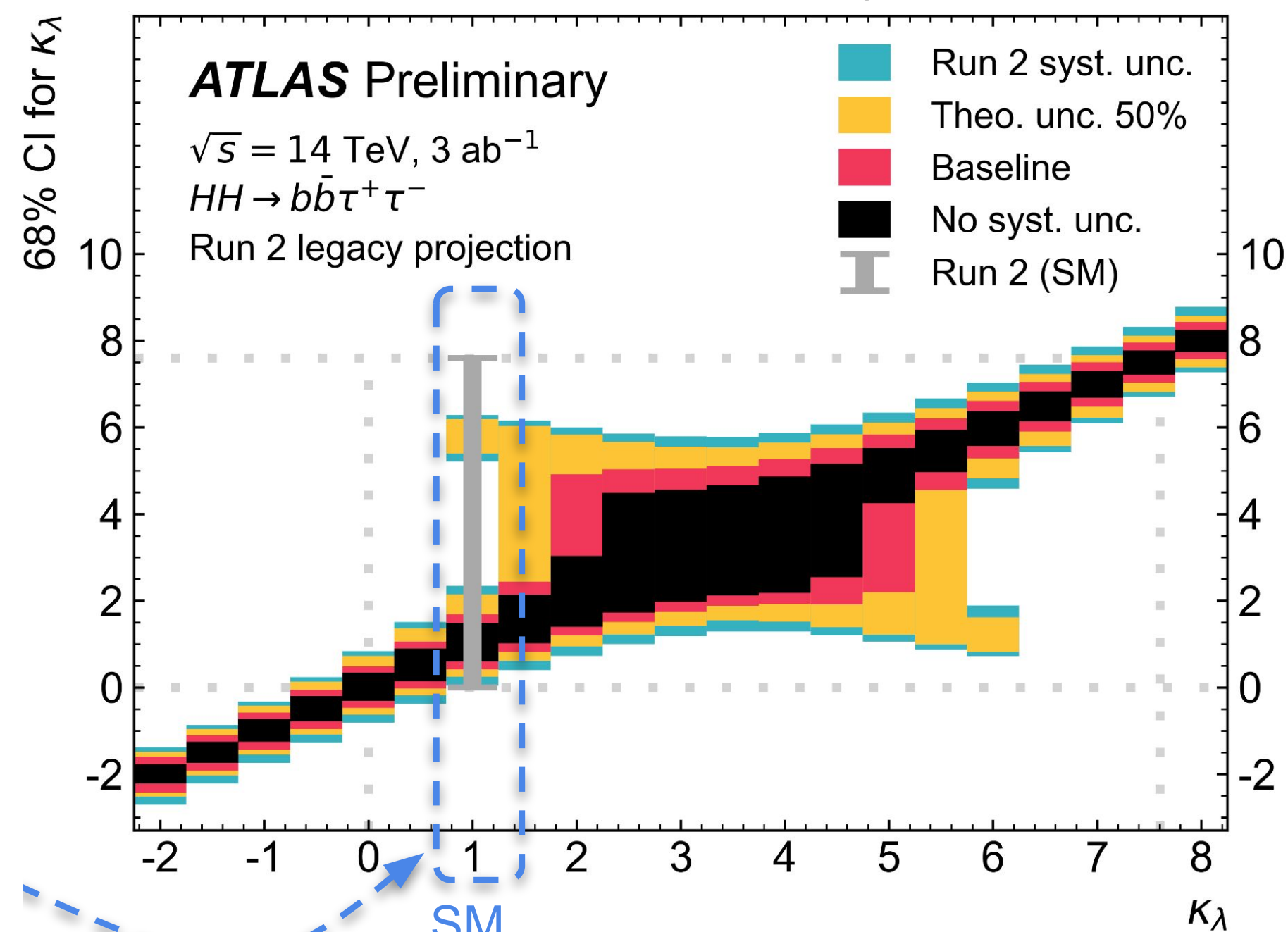
$$d\lambda/\lambda \text{ (SM)} = 18 \%$$

“flavour tag and kinematic reconstruction improvements demonstrated in detailed simulations of the ILD detector concept, propagated to the ZHH analysis based on [cite PhD Claude Dürig]”

BSM / ECM dependency

as before....

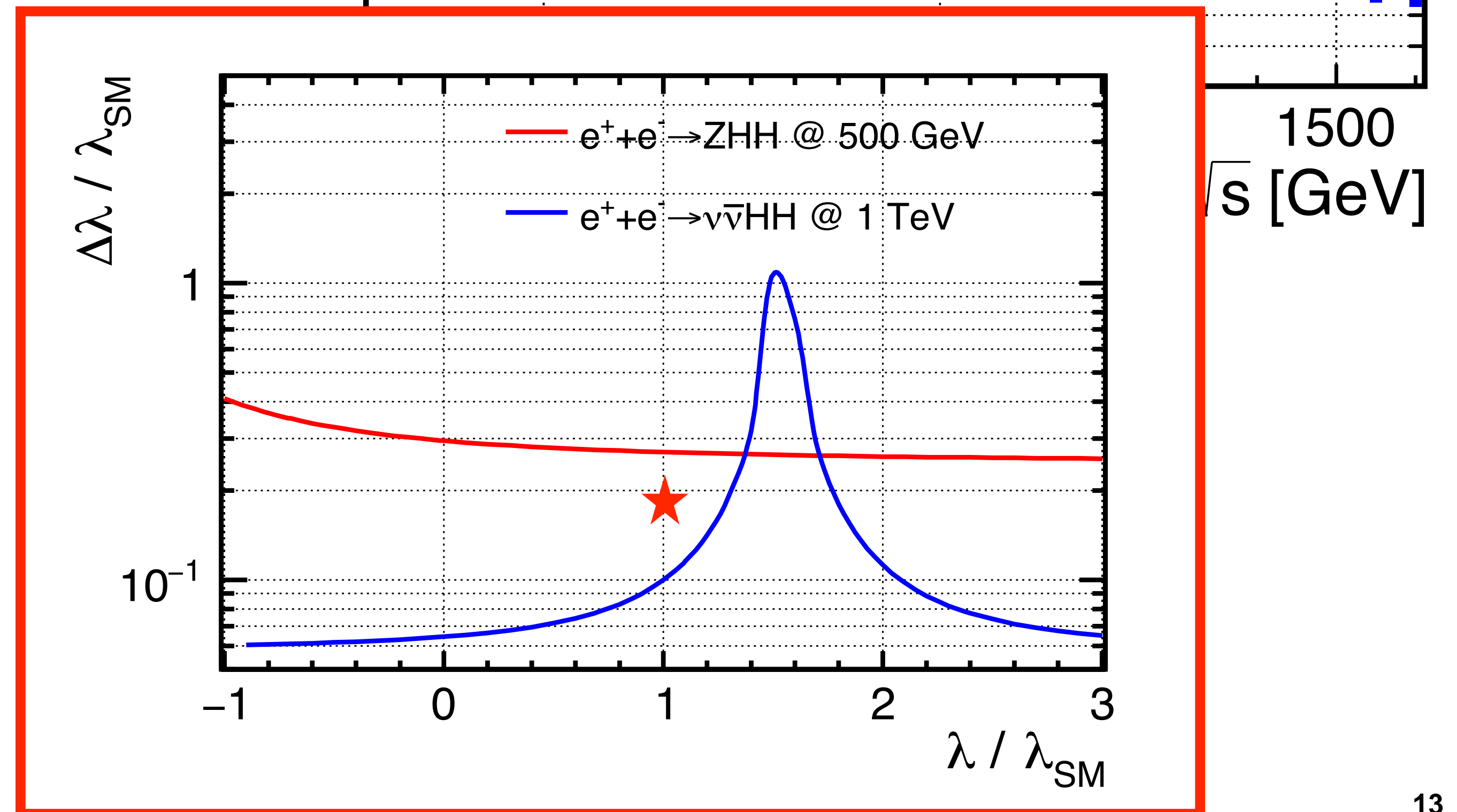
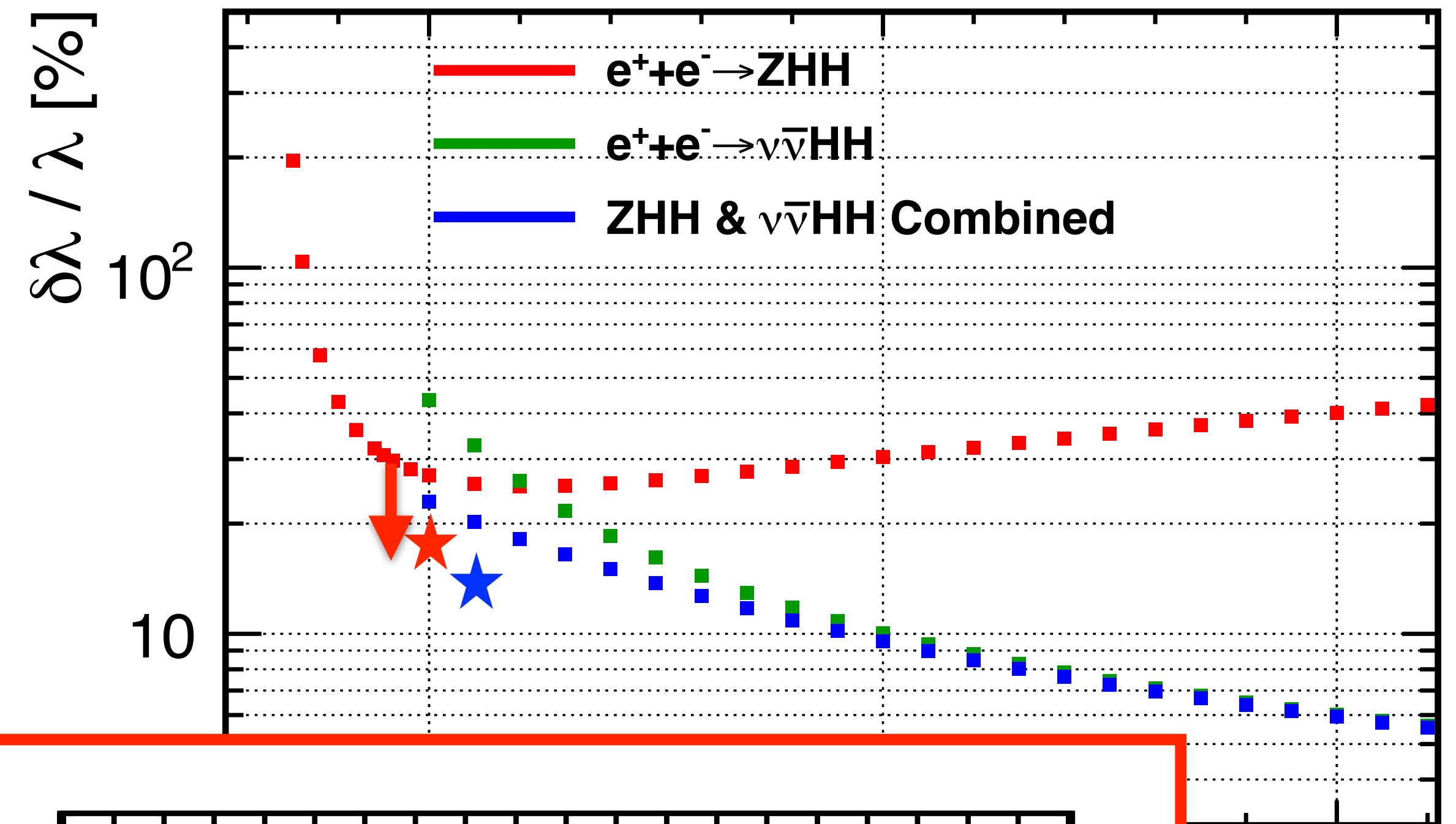
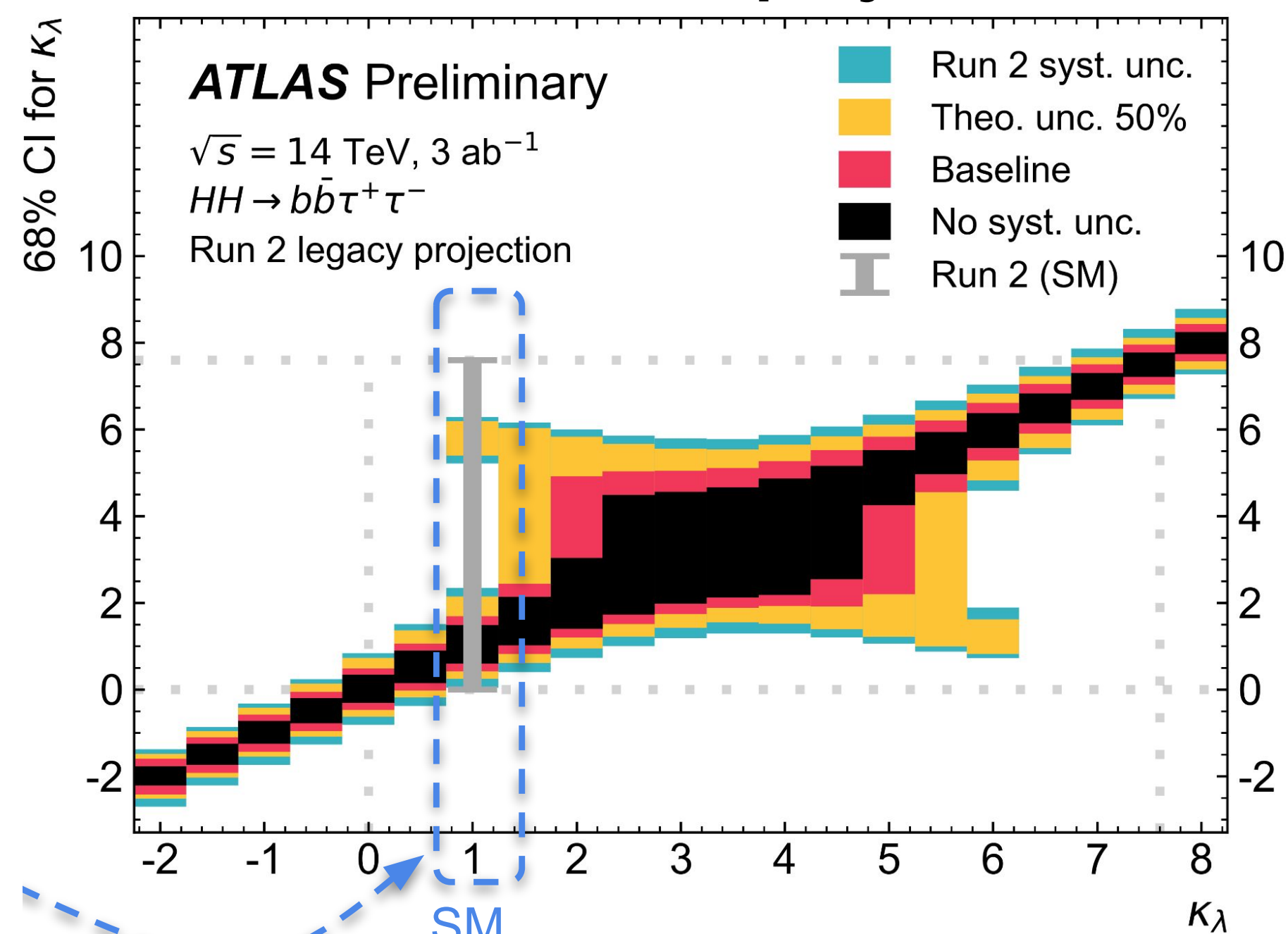
- use the “usual” cross-section-level extrapolation to project the dependency on
- ECM: 550 GeV incl $\nu\nu HH \rightarrow 13\%$
- value of λ
- draw in style / scale comparable to ATLAS HH- \rightarrow b \bar{b} tau τ projection



BSM / ECM dependency

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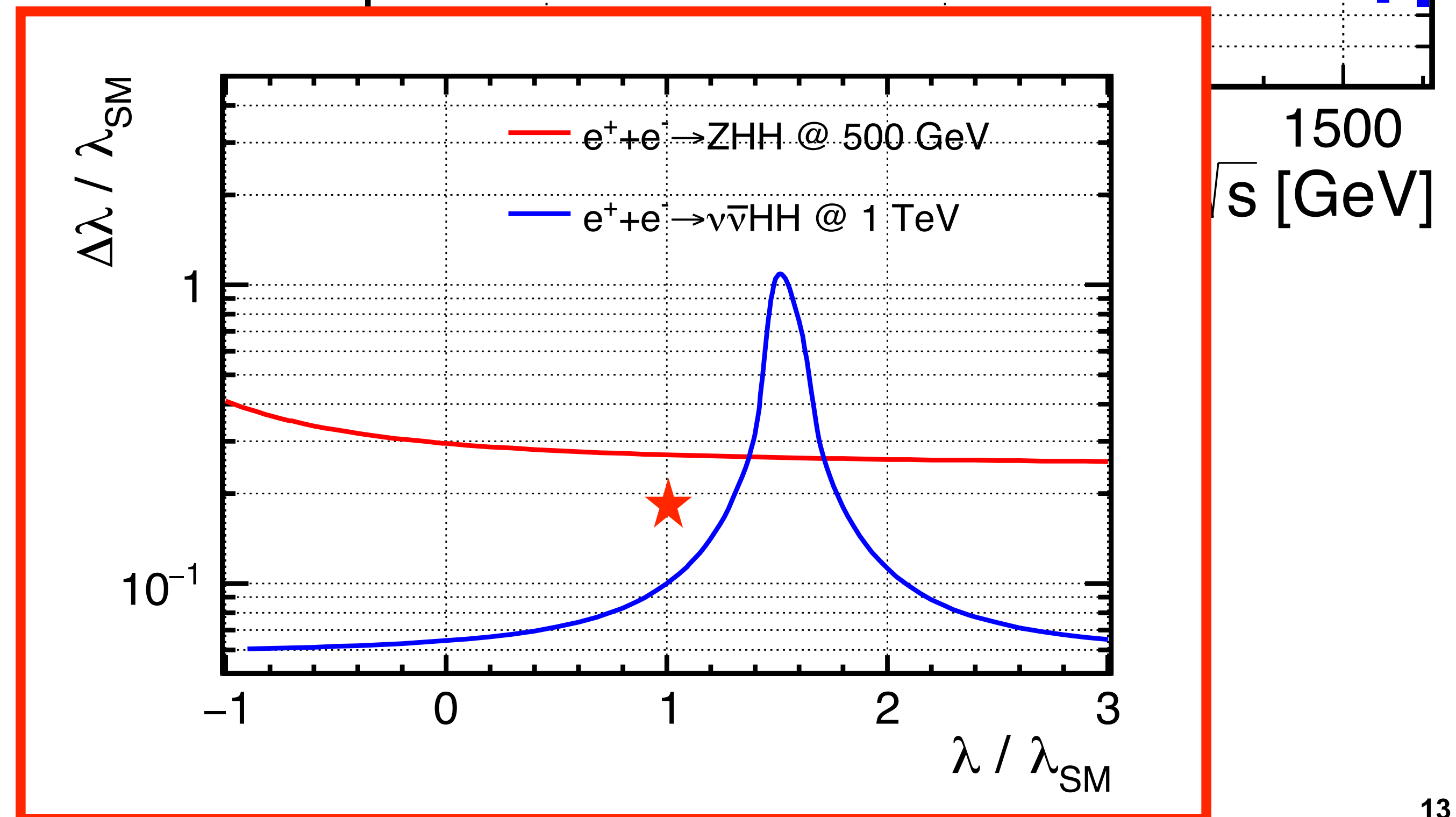
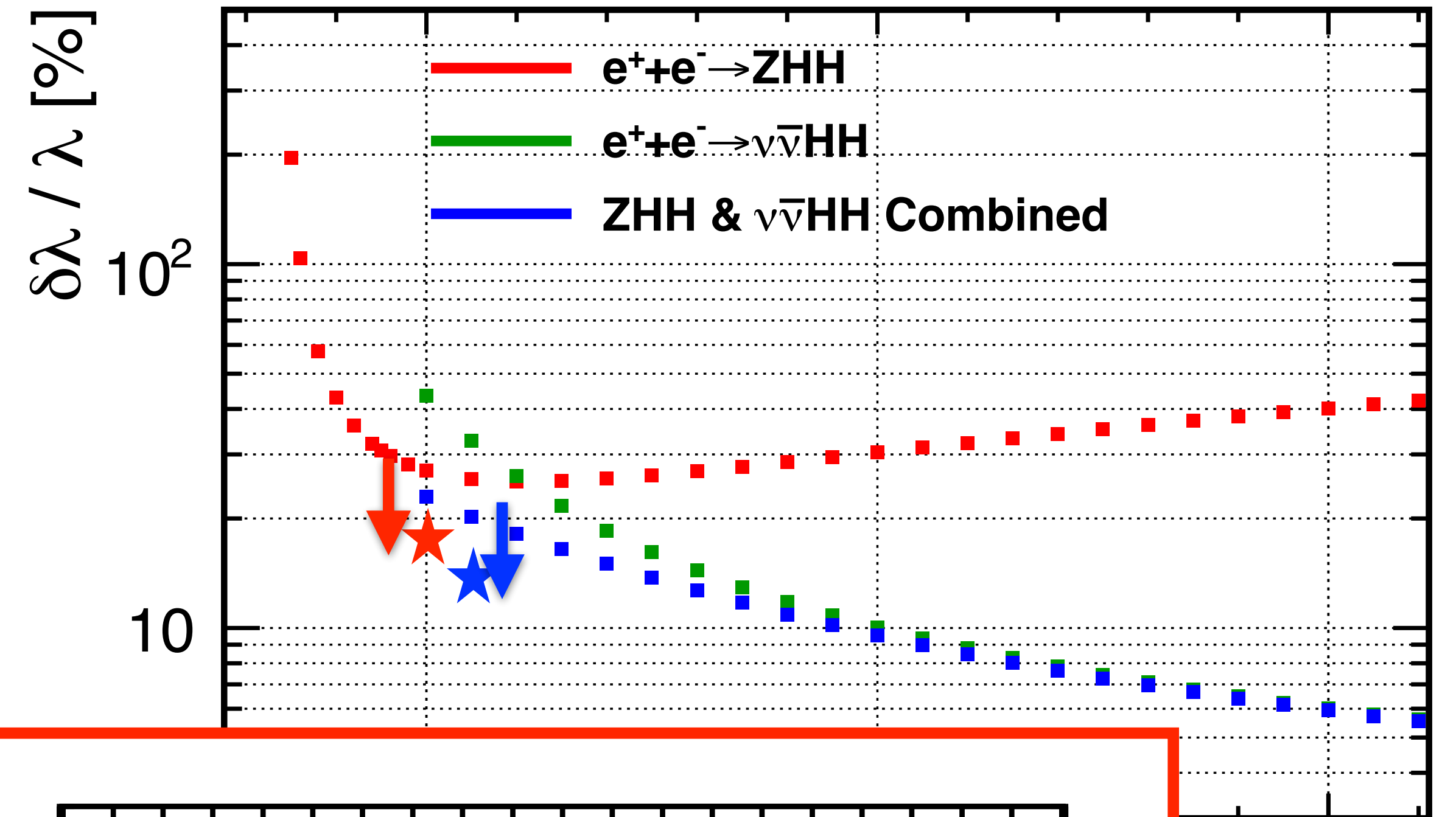
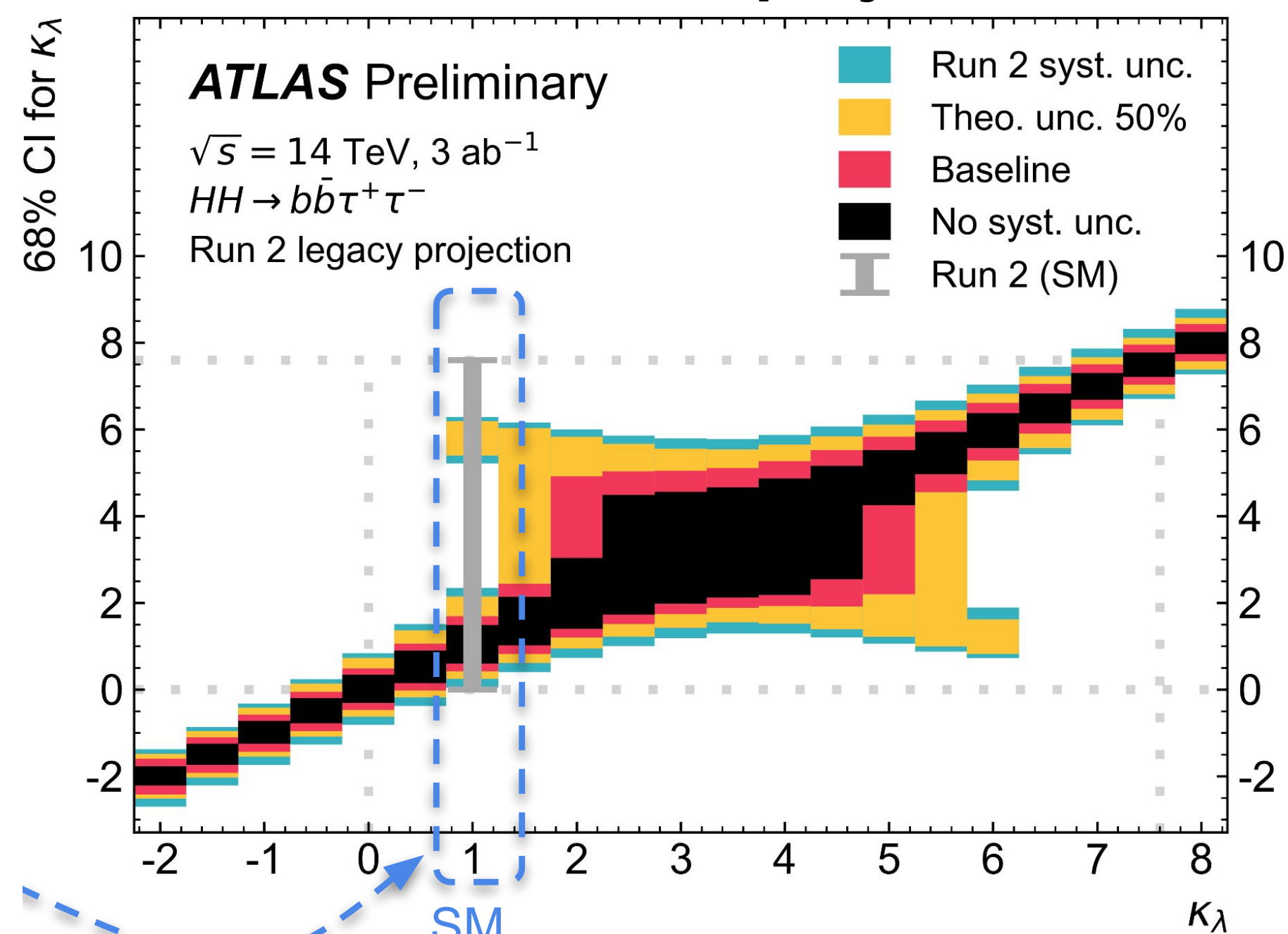
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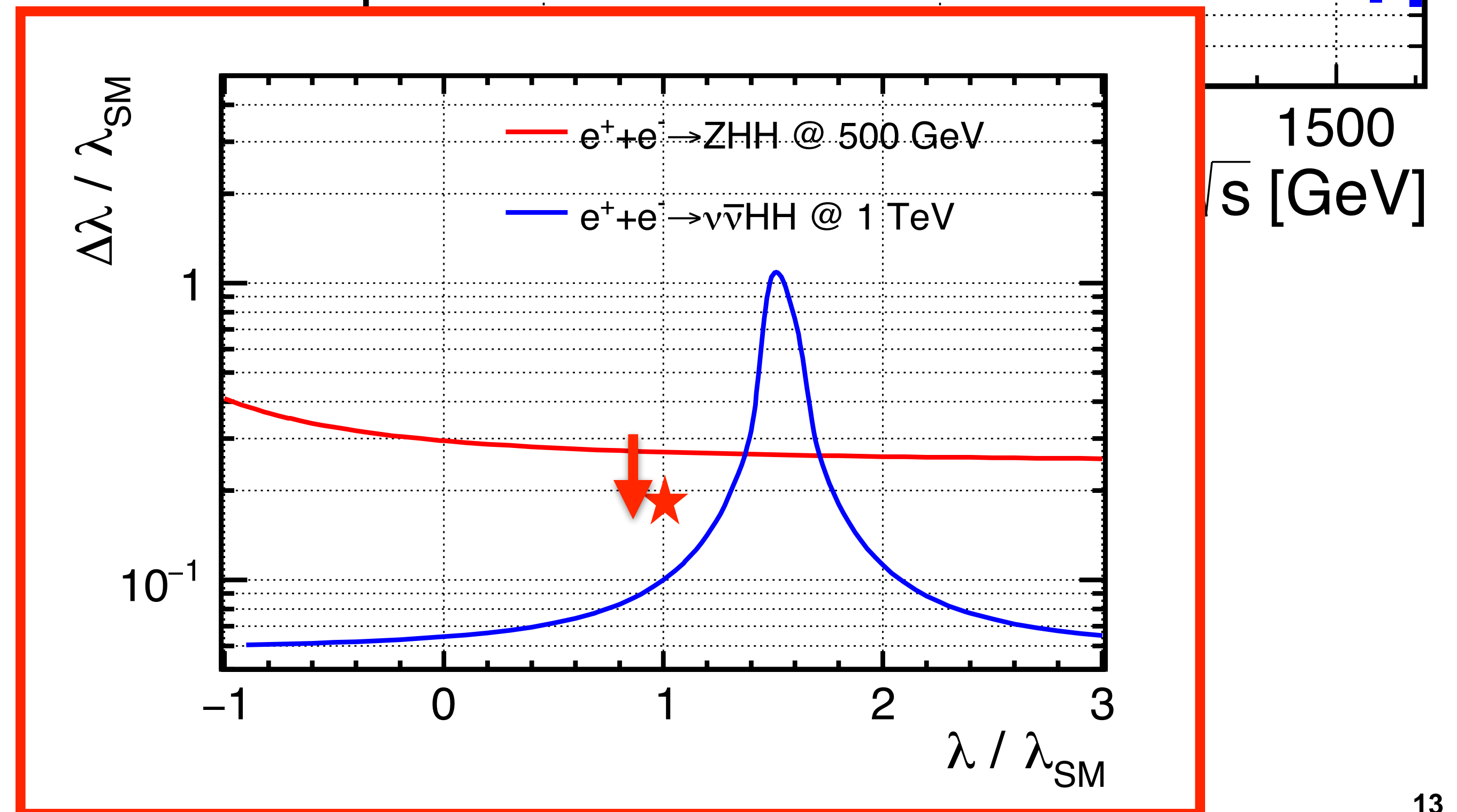
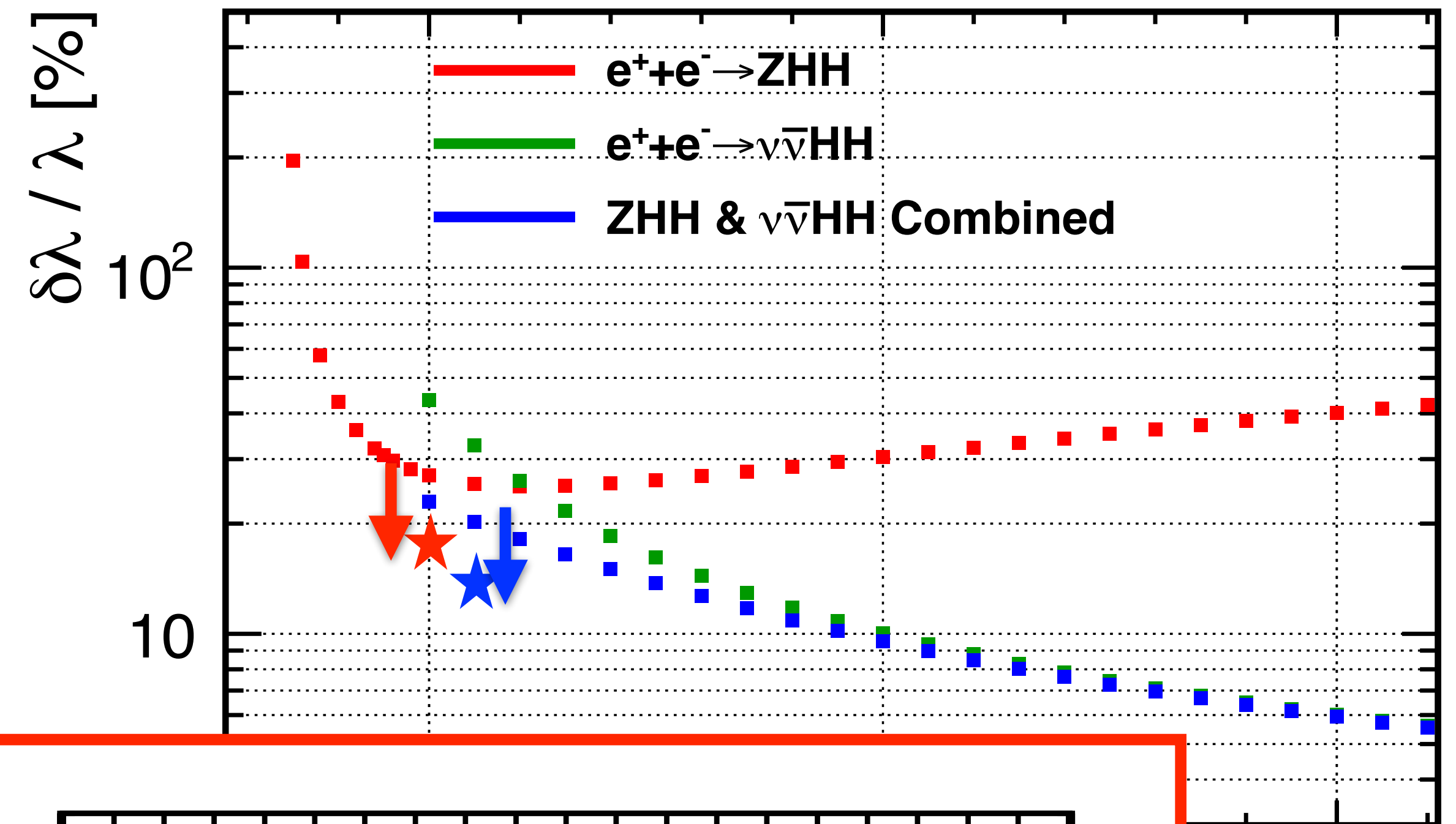
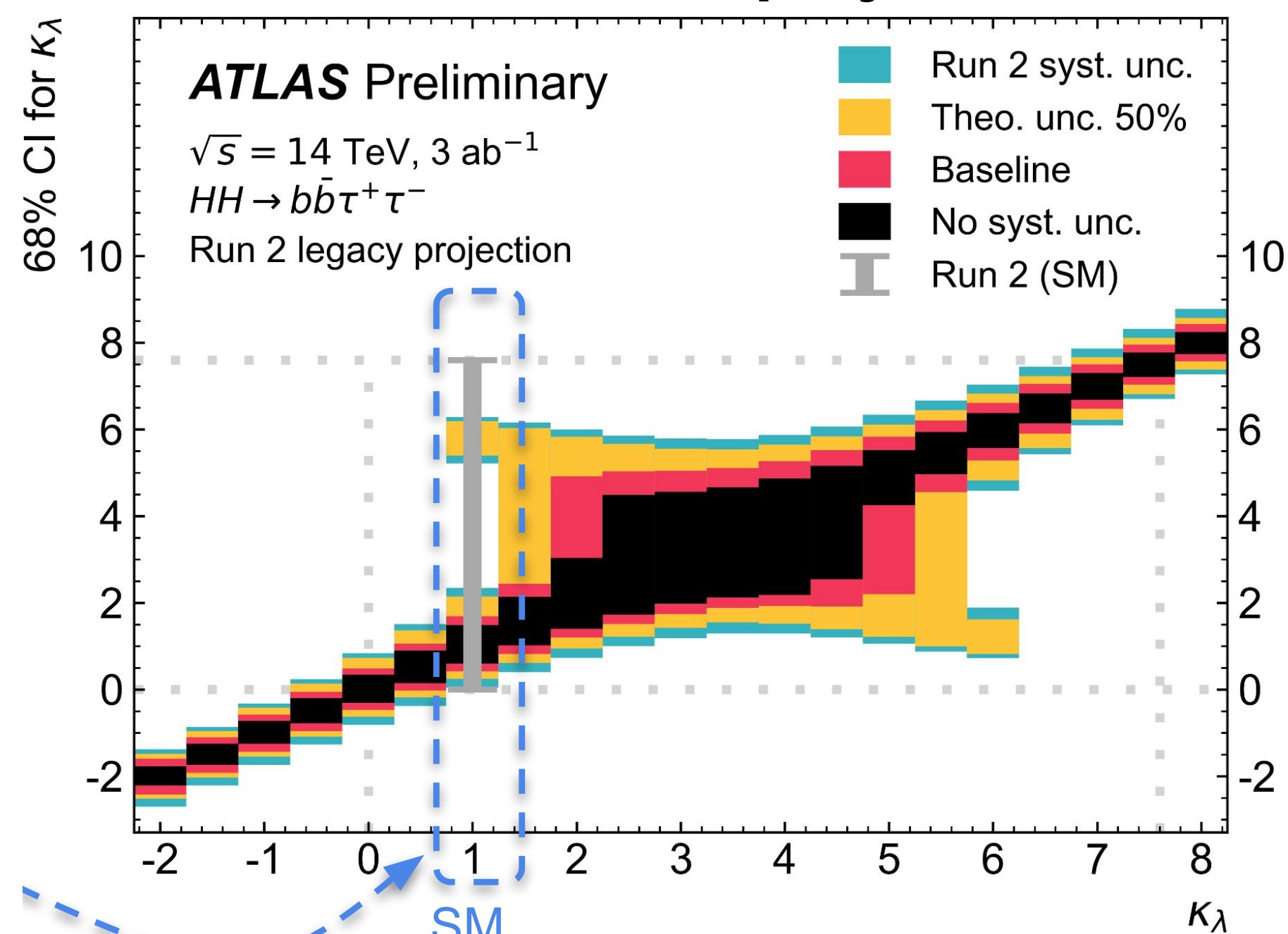
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Conclusions / Next steps

Overview

Conclusions / Next steps

Overview

Outlook on mid-term schedule

-