

Photons: Energy Resolution and Linearity

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Silicon Detector Calorimetry Meeting
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Analysis

- Can we use simulations to design a detector with good response to photons?
- Start by investigating the intrinsic detector characteristics:
 - Energy linearity
 - Energy resolution
- Analyze the response to single photons.

Simple Geant4 study

- Generate simple sampling calorimeters composed of tungsten-silicon sandwiches.
- Create stacks sufficiently large to contain the full particle showers.
- Vary thicknesses of tungsten and silicon to study the impact on the energy resolution.
- Simulate the response to single photons of varying energy.
- Plot resolution as a function of tungsten and silicon thickness.

Resolution as $fn(d_W, d_{Si})$

- Generate 400 points in 20 x 20 grid.

- Resolution fits well to the plane:

$$h(x,y) = a*x + b*y + c$$

x is the silicon thickness in microns

y is the tungsten thickness in mm

h is the energy resolution in %

- With parameters:

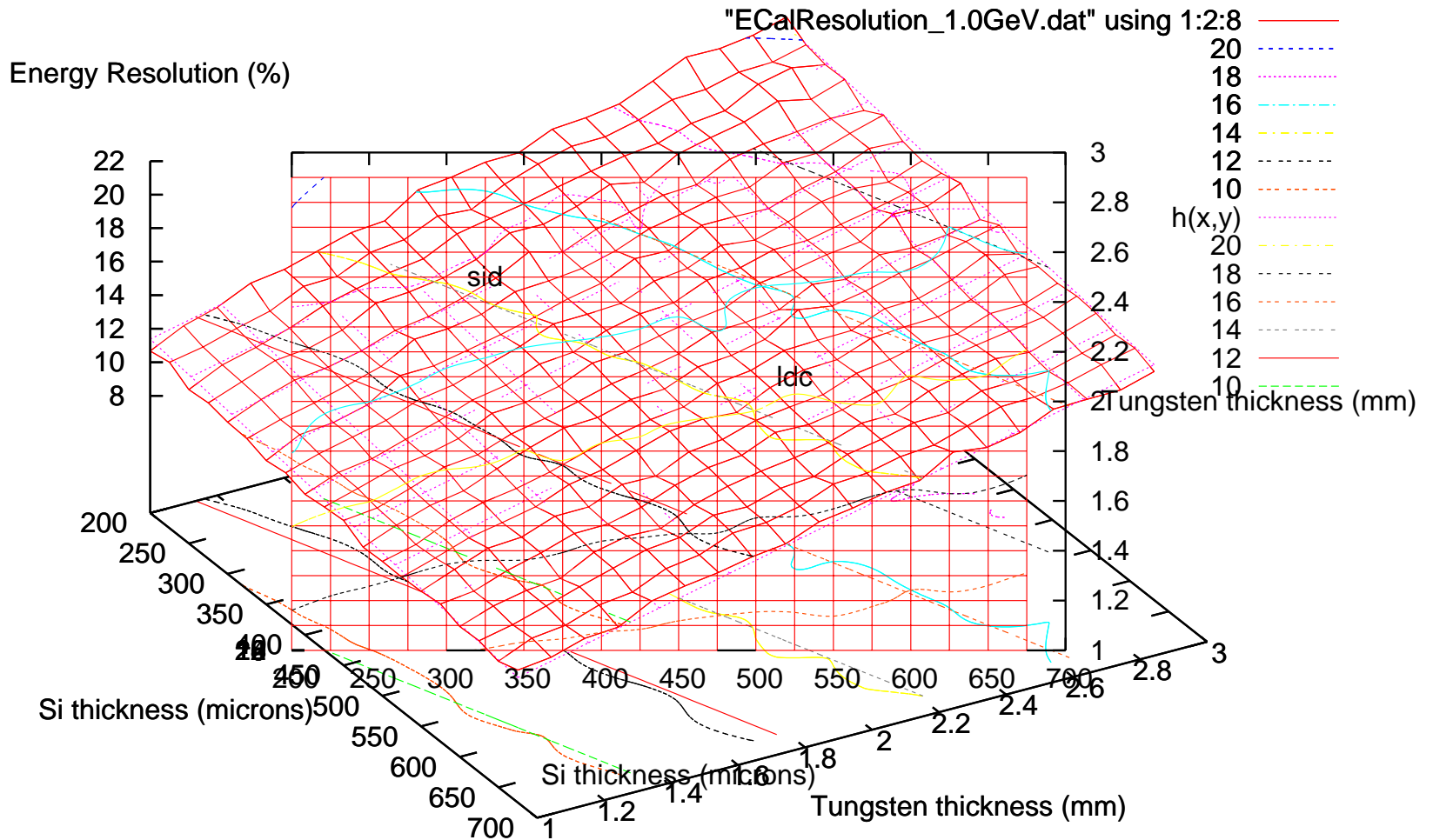
$$a = -0.00614792 \quad +/- 0.0001221 \quad (1.986\%)$$

$$b = 4.57985 \quad +/- 0.03052 \quad (0.6665\%)$$

$$c = 8.02729 \quad +/- 0.08189 \quad (1.02\%)$$

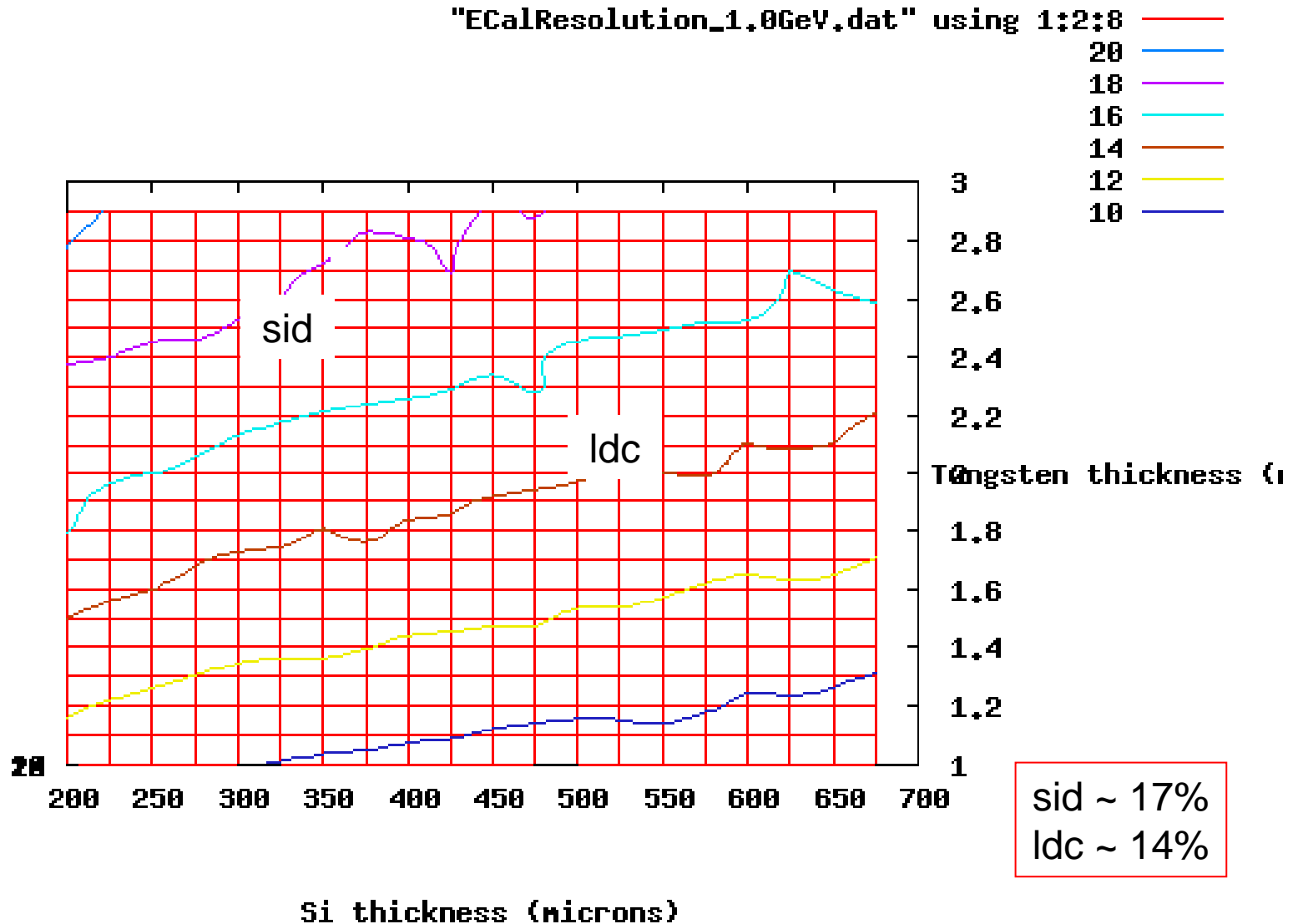
Resolution as $\text{fn}(d_W, d_{Si})$

Energy Resolution for 1GeV photons



Resolution as $\text{fn}(d_W, d_{Si})$

"ECalResolution_1.0GeV.dat" using 1:2:8



Full Simulation Detectors

■ acme0605

- 20 layers of .271cm W (Dens25), 320 μ m Si
- 10 layers of .543cm W (Dens25), 320 μ m Si
- HCal: .75cm W, .5cm scintillator

■ acme0605_30layerecal

- 30 layers of .271cm W (Dens25), 320 μ m Si

■ acme0605_40layerecal

- 40 layers of .271cm W (Dens25), 320 μ m Si

■ acme0605_steel_scint

- 20 layers of .271cm W (Dens25), 320 μ m Si
- 10 layers of .543cm W (Dens25), 320 μ m Si
- HCal: 2.0cm Steel, .5cm scintillator

Full Simulation Data Samples

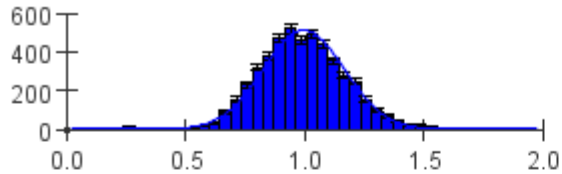
- Generated single particle events with photons at $\theta = 90^\circ$ to the beam line, $0 < \varphi < 2\pi$.
- Discrete energies: 1, 2, 5, 10, 20, 50, 100 GeV
- Also looked at 250 and 500 GeV samples.
- Apply conservative fixed-cone clustering algorithm to clean up obvious outliers.

Results

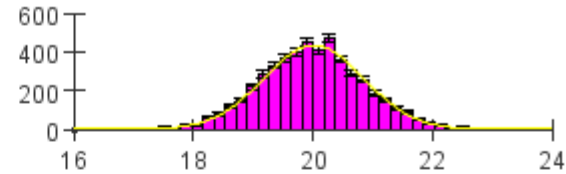
- Sampling fractions can be obtained for all the detector designs which provide a linear response for photons with energies between 1 and 100 GeV.
- The energy resolution is only slightly affected by the EM calorimeter designs:
 - acme0605: 17.1%
 - acme0605_40layerecal: 16.9%
 - acme0605_30layerecal: 17.2%
 - acme0605_steel_scint: 17.7%

Plots: acme0605 Raw

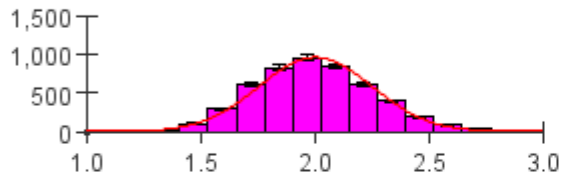
corrected cluster energy



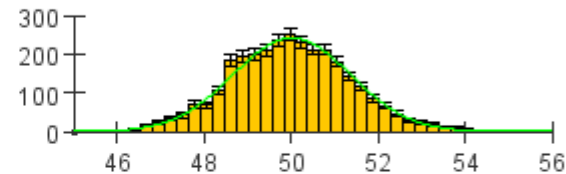
corrected cluster energy



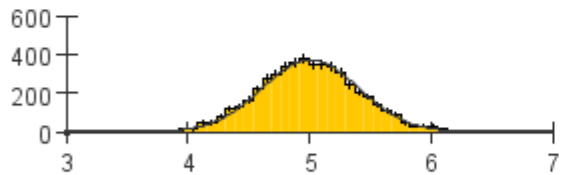
corrected cluster energy



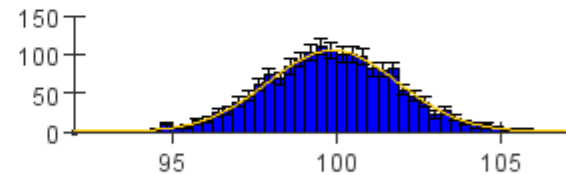
corrected cluster energy



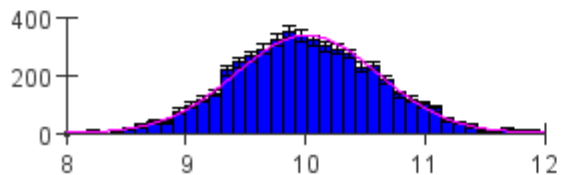
corrected cluster energy



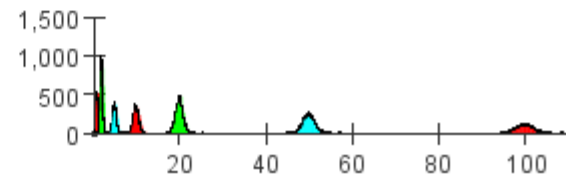
corrected cluster energy



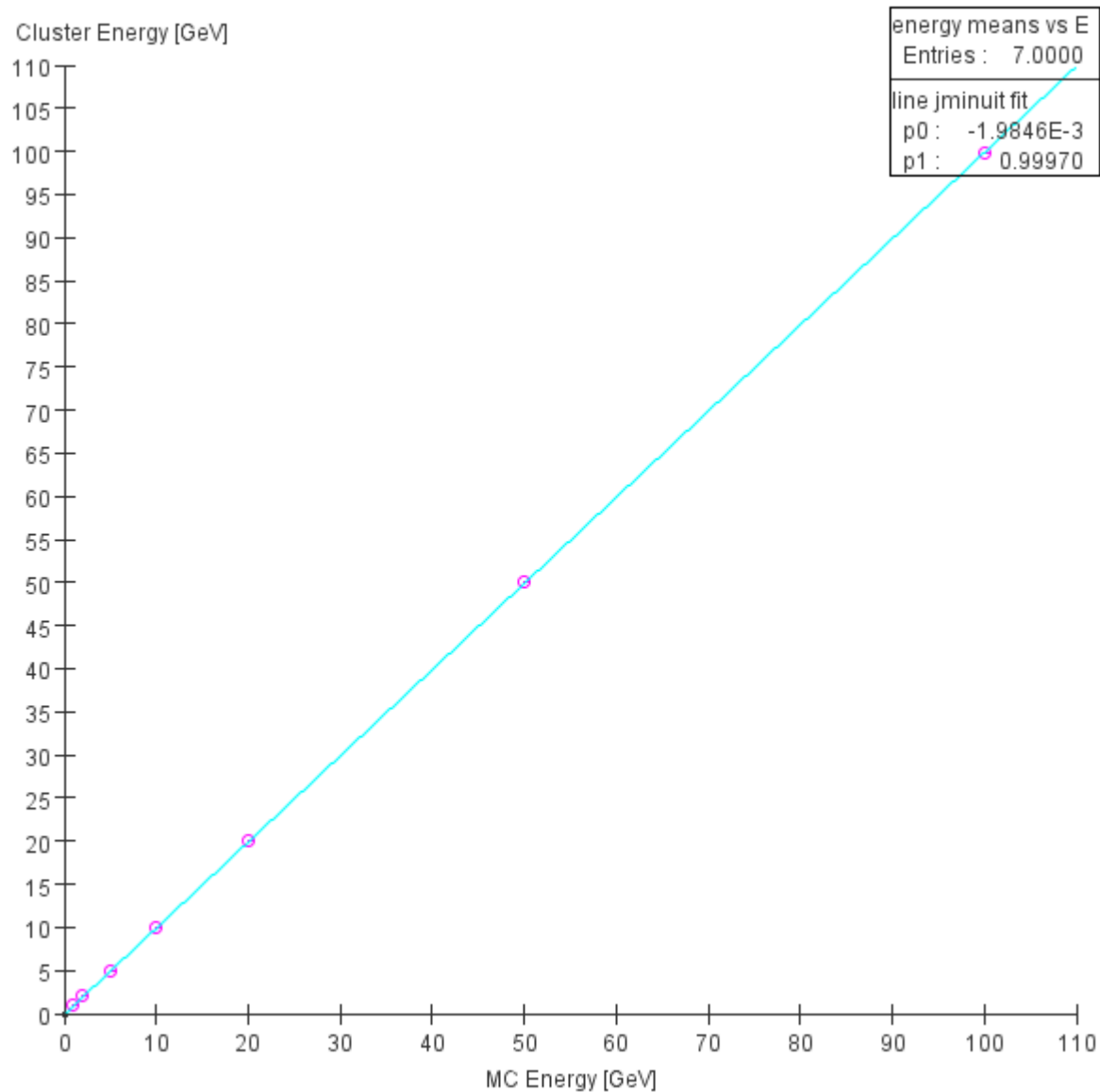
corrected cluster energy



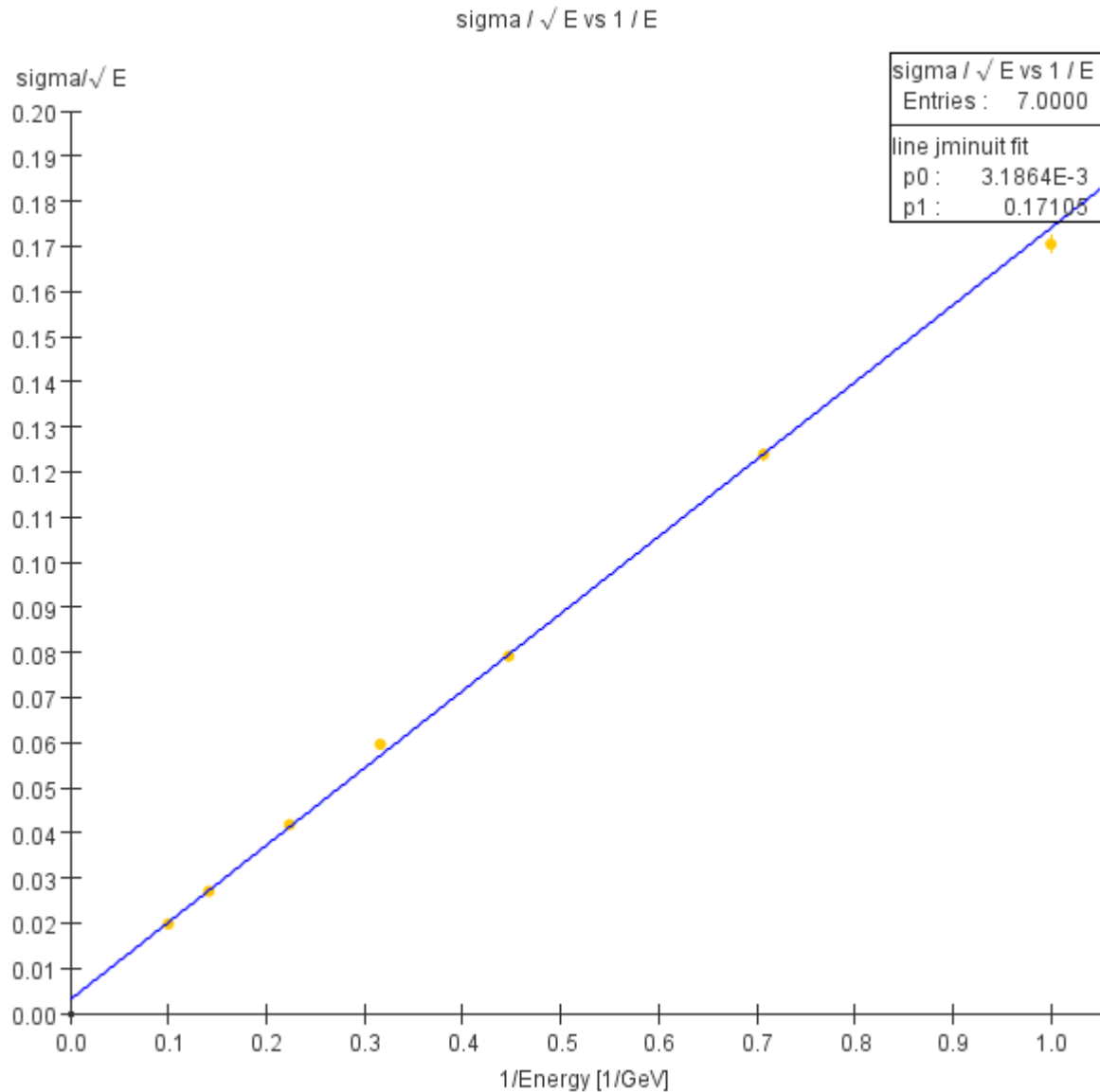
corrected cluster energy



Plots: acme0605 Linearity

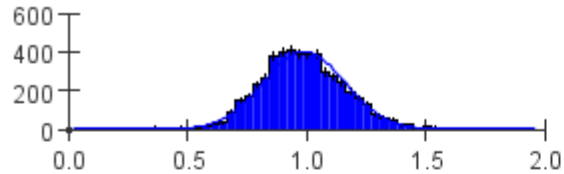


Plots: acme0605 Resolution

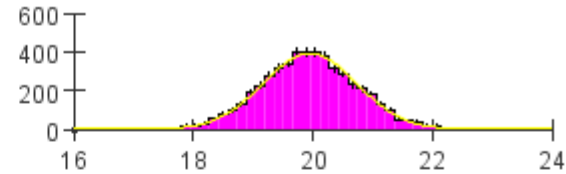


Plots: acme0605_30layerecal Raw

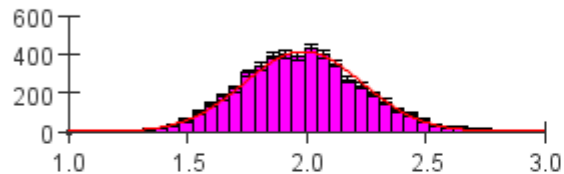
corrected cluster energy



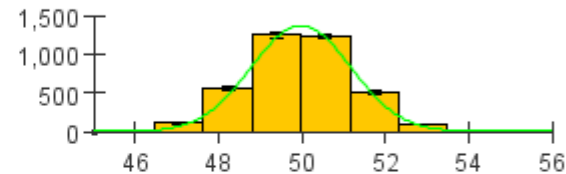
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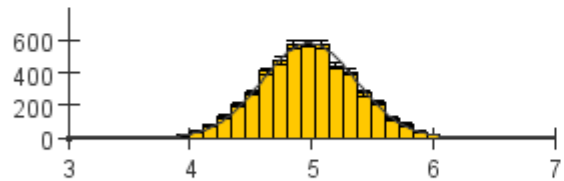
corrected cluster energy



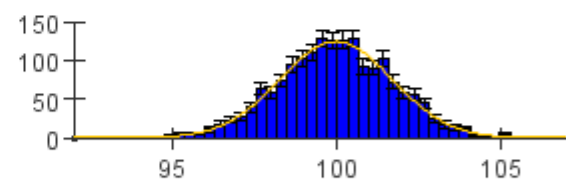
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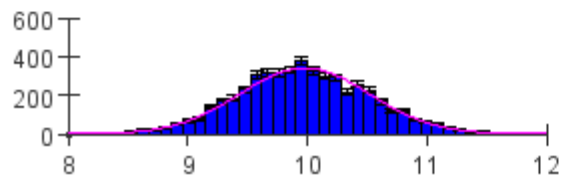
corrected cluster energy



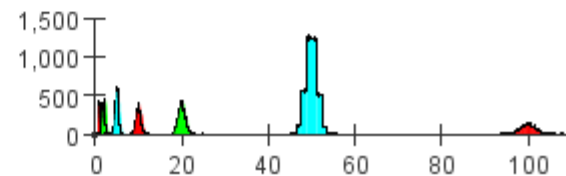
corrected cluster energy



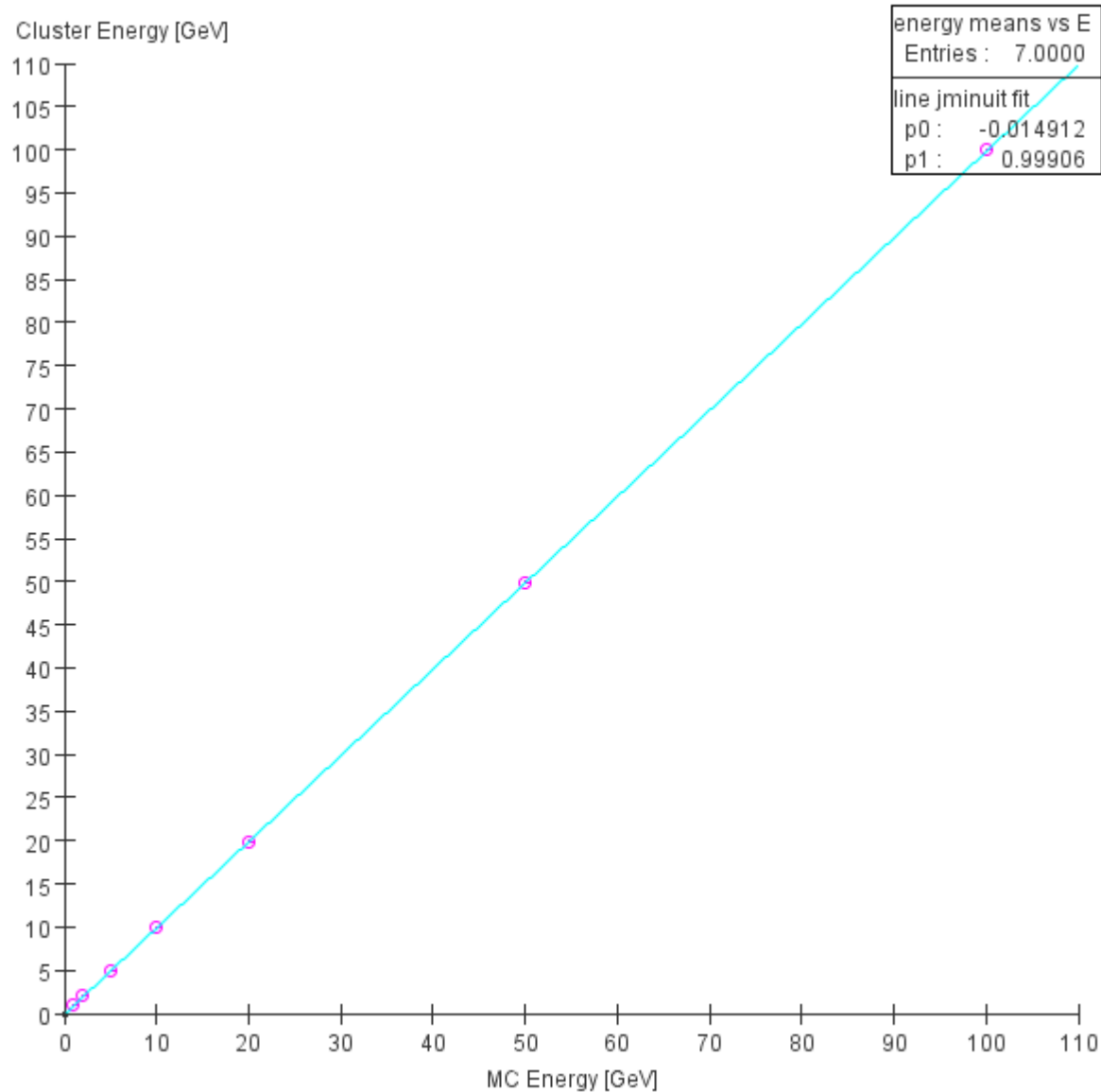
corrected cluster energy



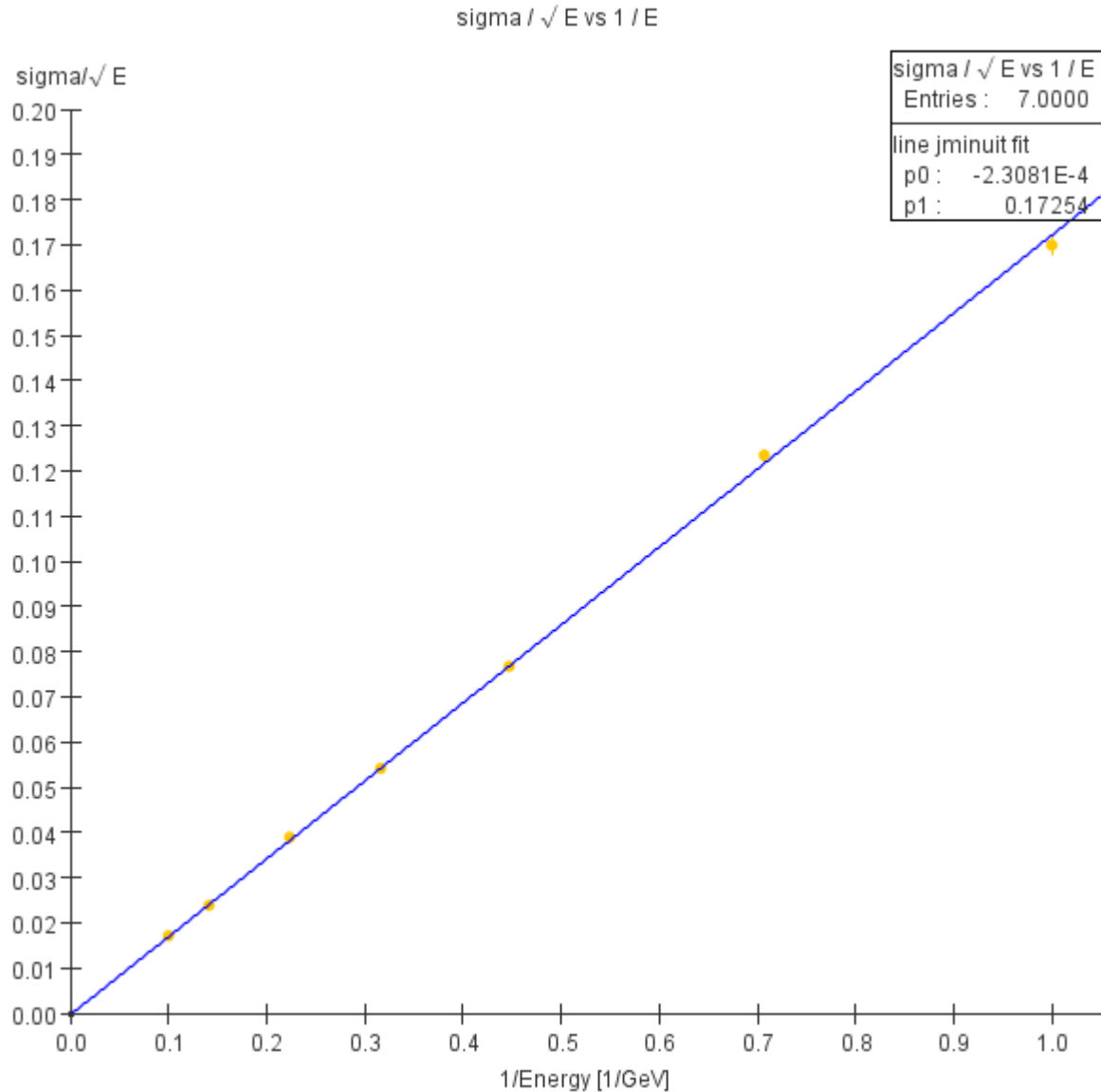
corrected cluster energy



Plots: acme0605_30layerecal Linearity

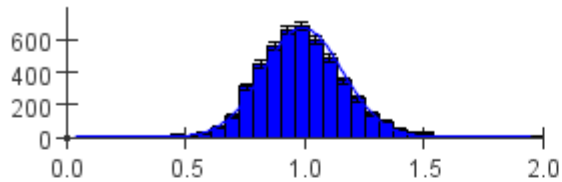


Plots: acme0605_30layerecal Resolution

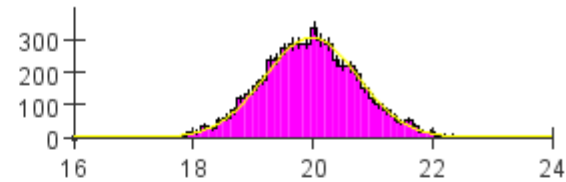


Plots: acme0605_40layerecal Raw

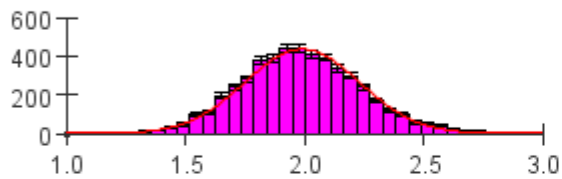
corrected cluster energy



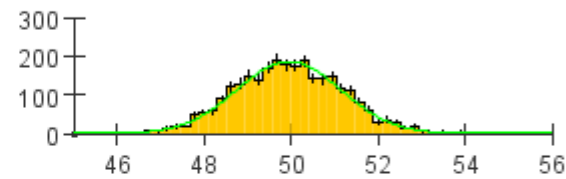
corrected cluster energy



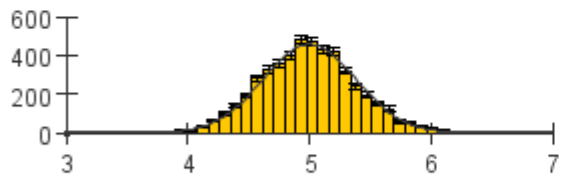
corrected cluster energy



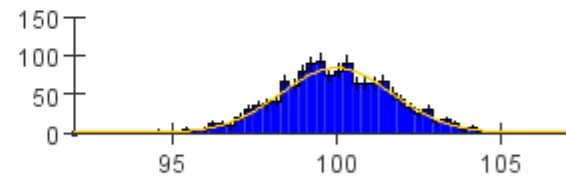
corrected cluster energy



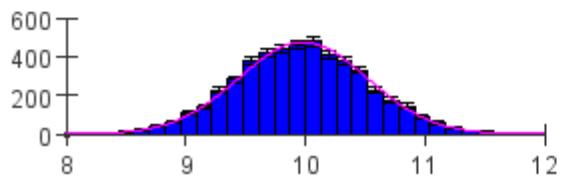
corrected cluster energy



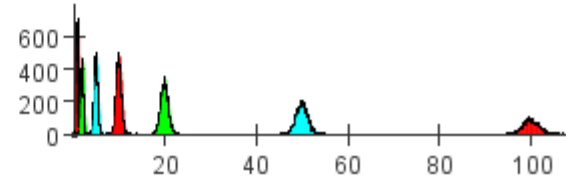
corrected cluster energy



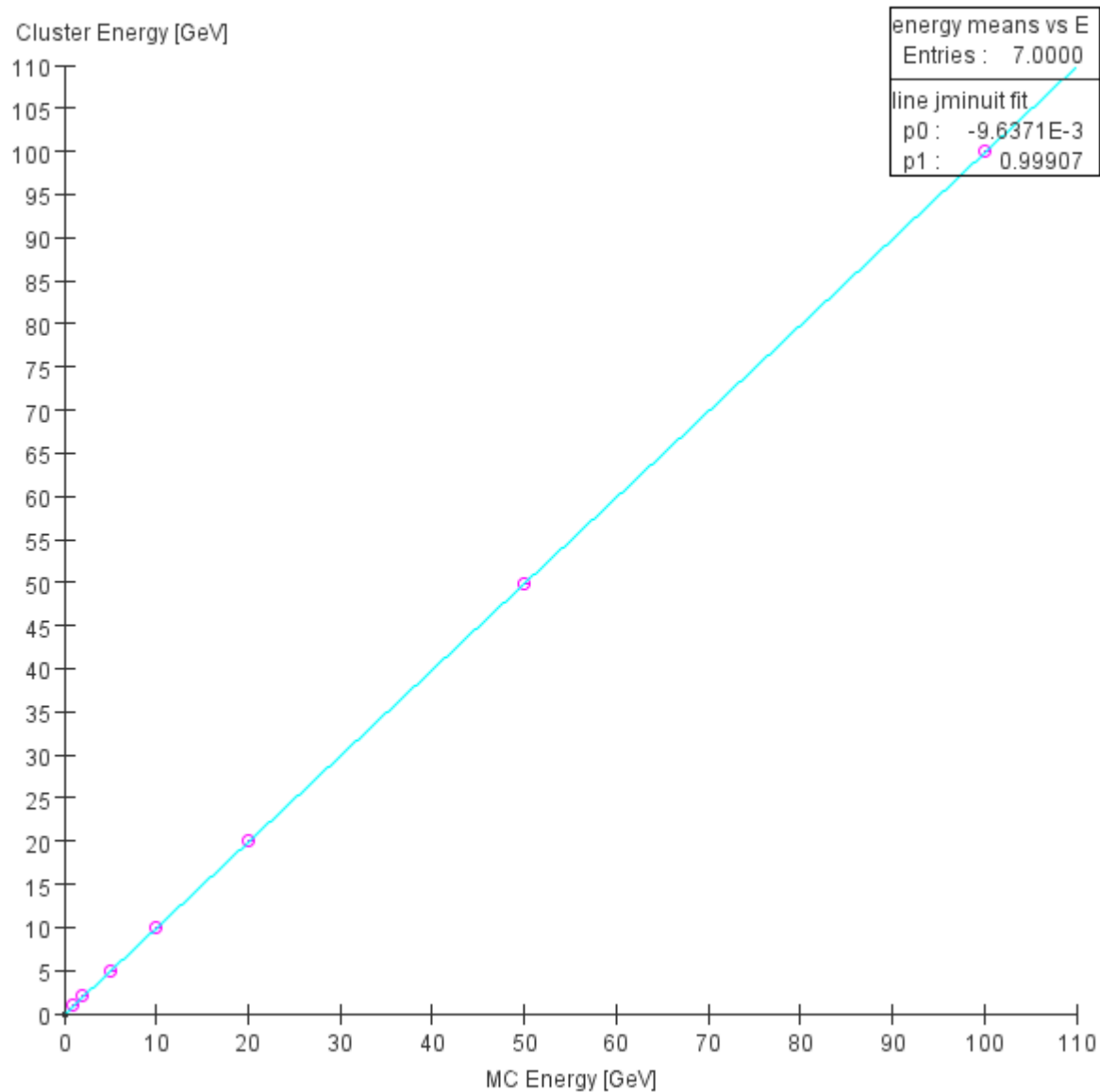
corrected cluster energy



corrected cluster energy

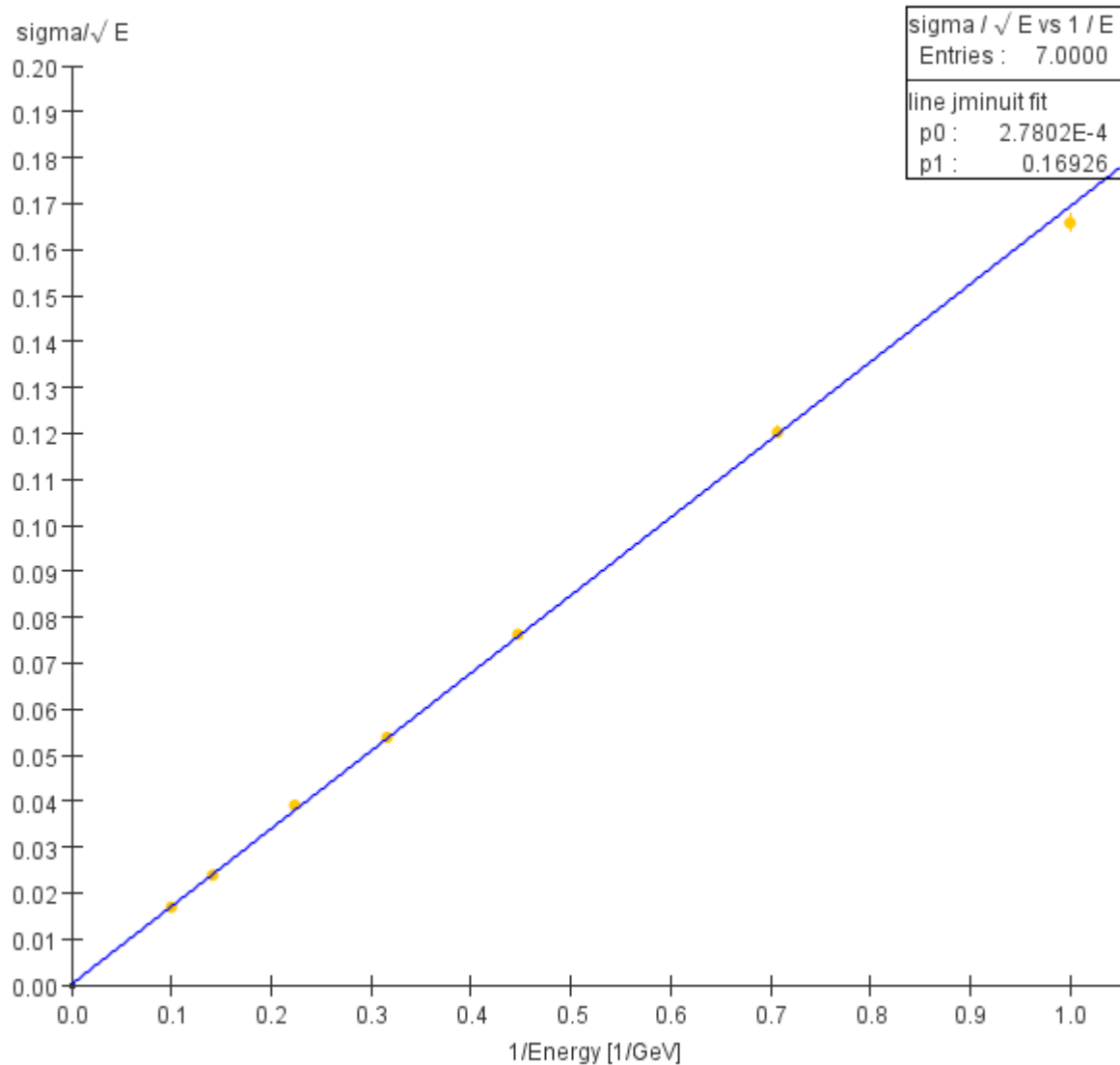


Plots: acme0605_40layerecal Linearity



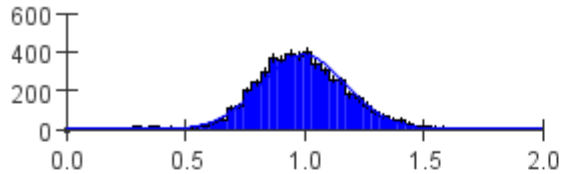
Plots: acme0605_40layerecal Resolution

sigma / \sqrt{E} vs 1 / E

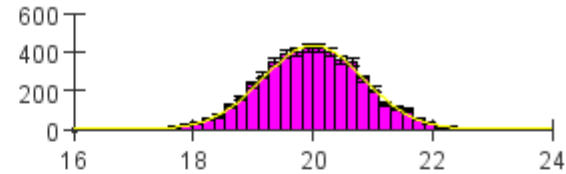


Plots: acme0605_steel_scint Raw

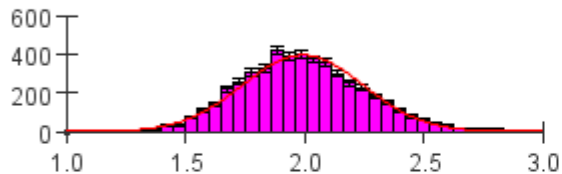
corrected cluster energy



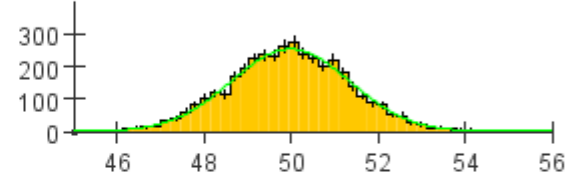
corrected cluster energy



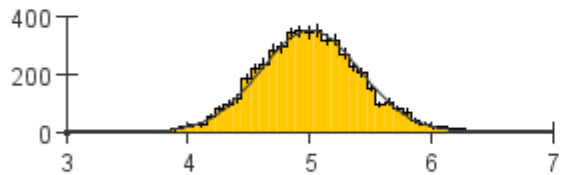
corrected cluster energy



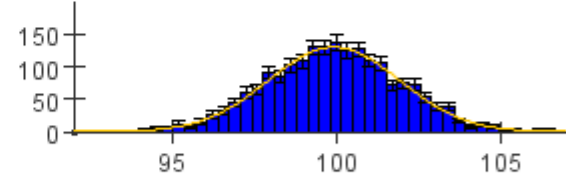
corrected cluster energy



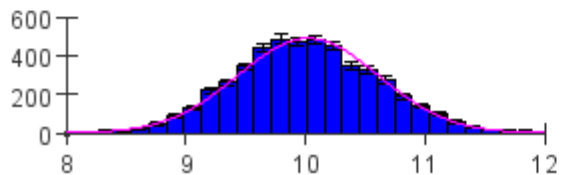
corrected cluster energy



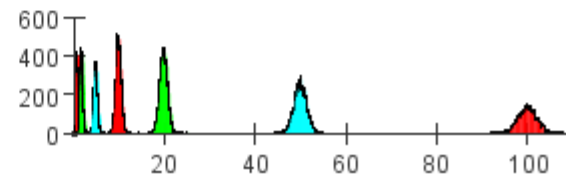
corrected cluster energy



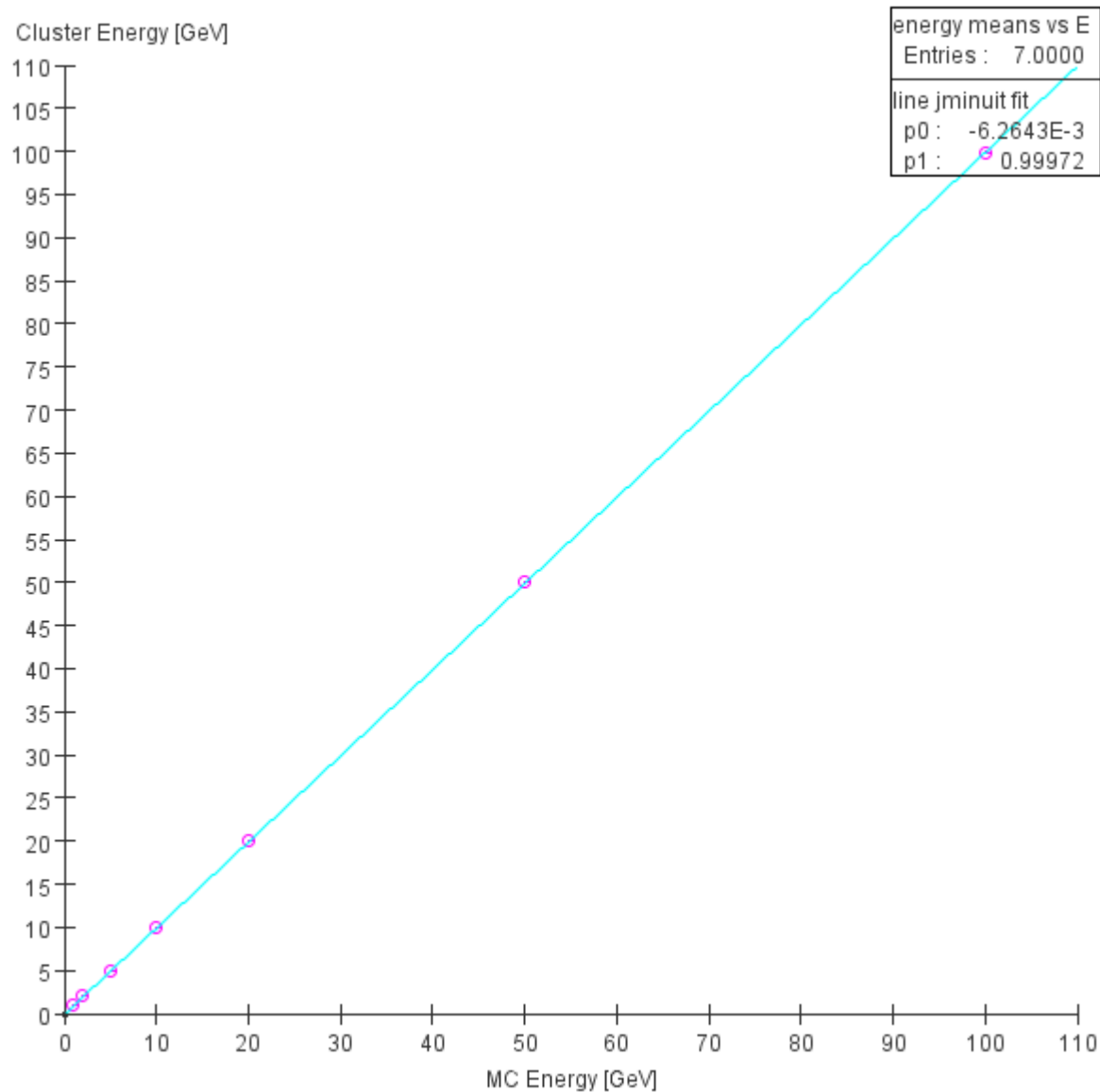
corrected cluster energy



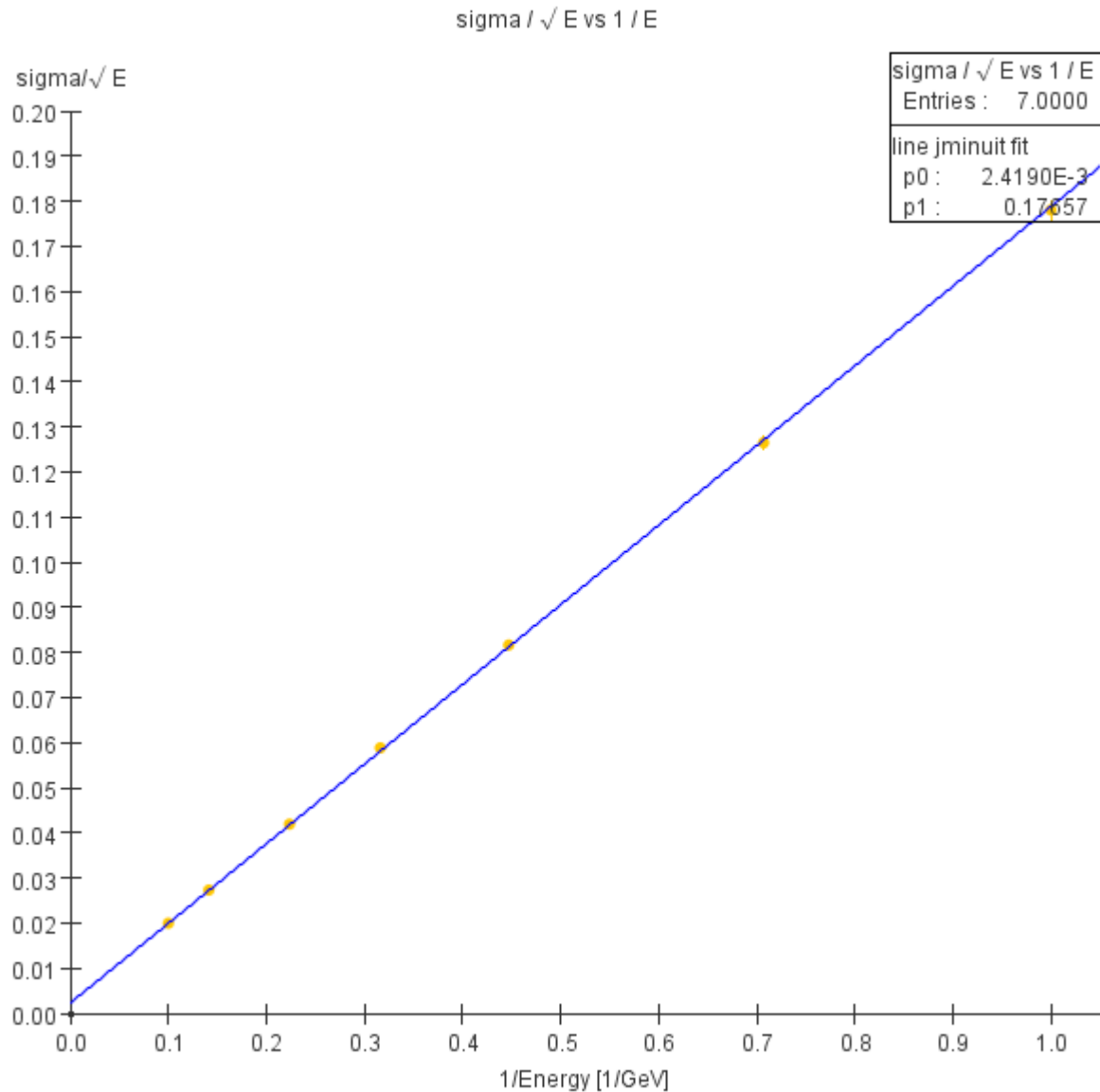
corrected cluster energy



Plots: acme0605_steel_scint Linearity



Plots: acme0605_steel_scint Linearity



Summary

- The tools are available to design a system of calorimeters with good energy resolution and linearity of response to photons.
- A default set of sampling fractions can be determined which gives excellent linearity for photons with energies between 1 and 100 GeV.
- The energy resolution and linearity can be improved by introducing energy-dependent sampling fractions.
 - Physical reason for this is that the electromagnetic shower composition changes as a function of energy and longitudinal depth of the shower.
- The baseline silicon detector calorimeters provide an energy resolution of:

$$\sigma/E \sim 17\%/\sqrt{E} \text{ with } \sim 0 \text{ constant term.}$$