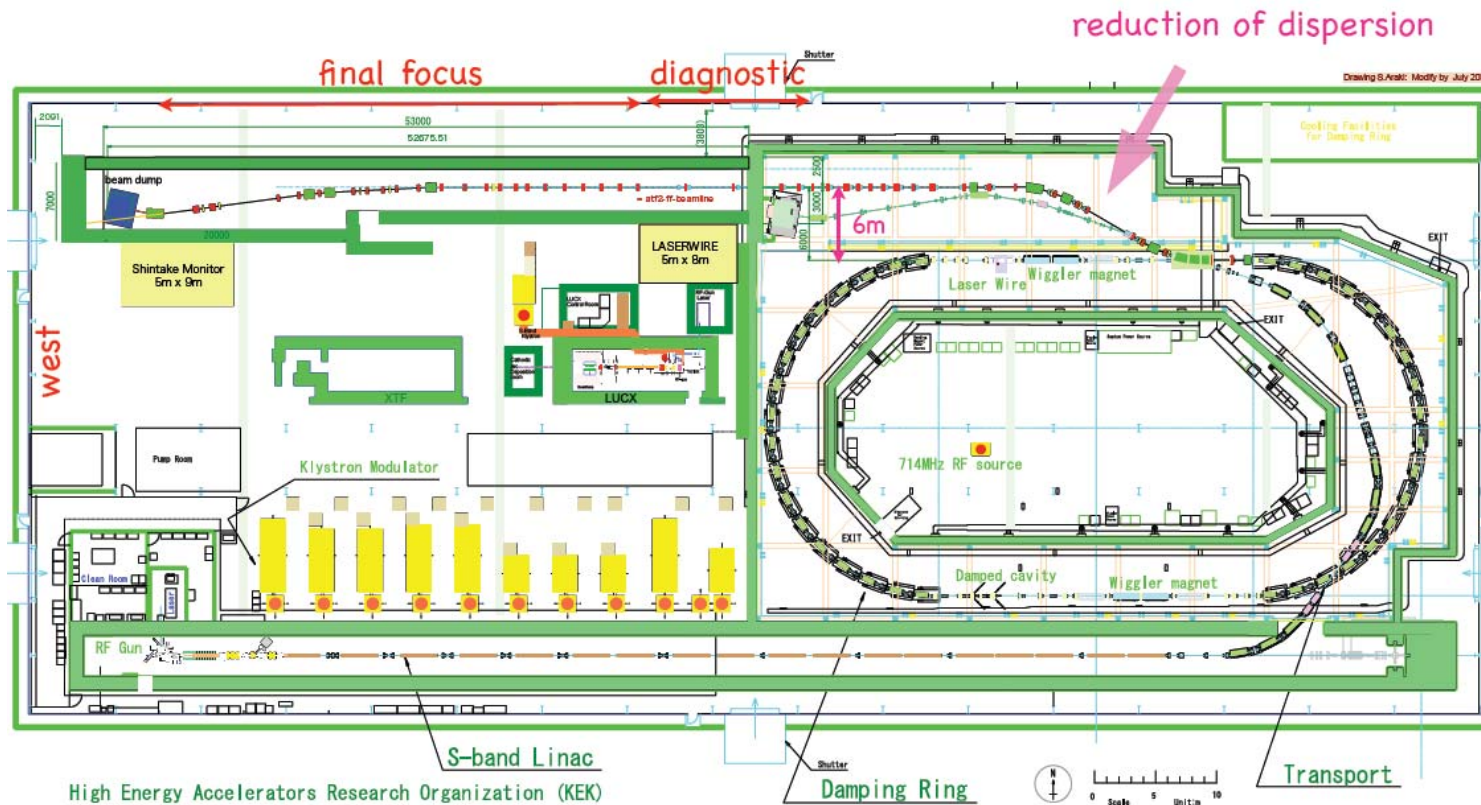
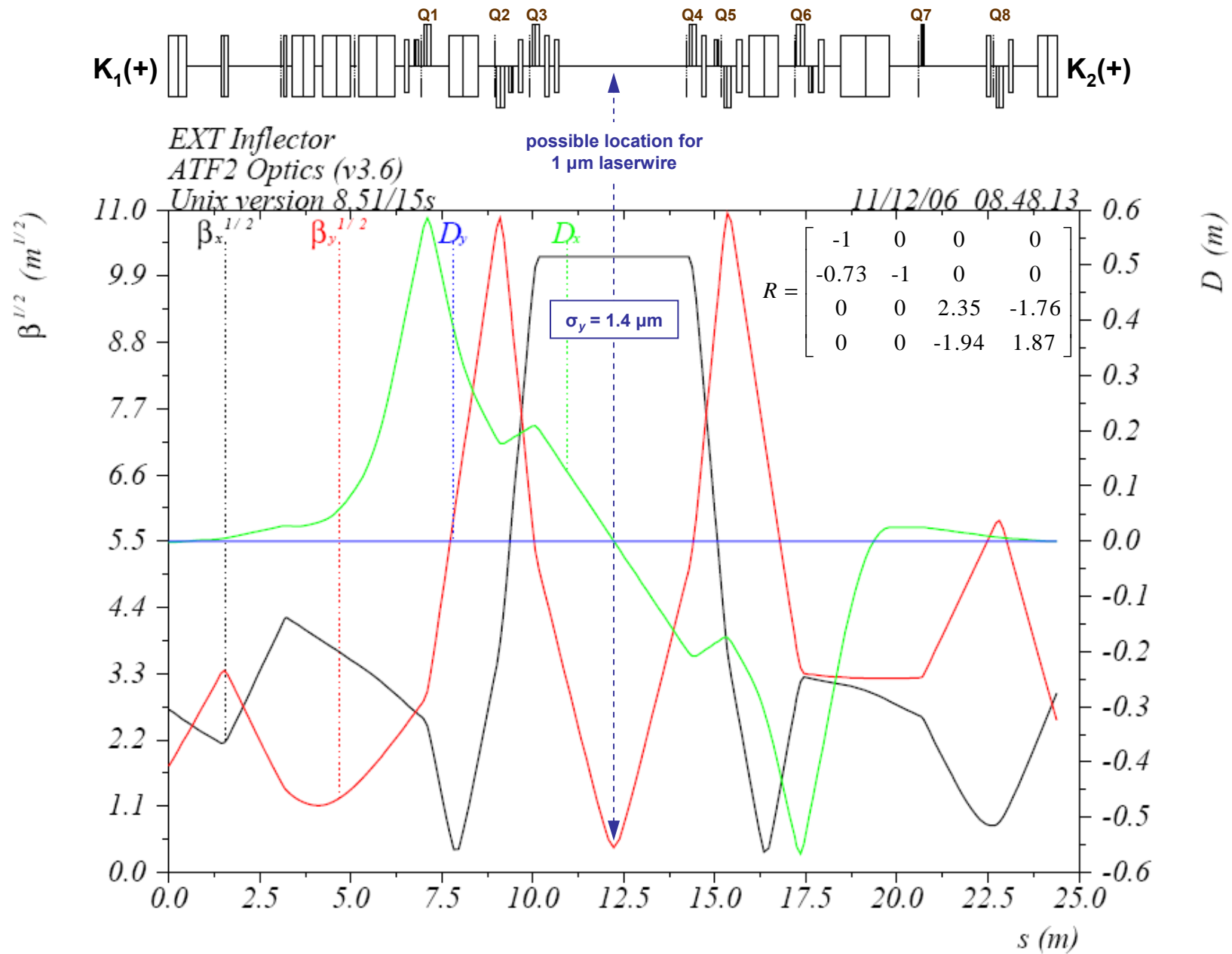




Correction of Anomalous Vertical Dispersion in the ATF2 EXT Line (v3.6)

Optics v3.5, 1 July 2006





For MAD files see <http://www.slac.stanford.edu/~mdw/ATF2/v3.6>

Simulation Parameters

- use Peter Tenenbaum's Lucretia¹ simulation code
- included
 - perfect beam from Damping Ring ($\epsilon_x=2\times 10^{-9}$ m, $\gamma\epsilon_y=3\times 10^{-8}$ m) ... errors begin after extraction septa, unless otherwise noted
 - perfect Final Focus
 - dipole errors²: $\Delta Y = 100 \mu\text{m}$ (rms)
 - quadrupole errors: $\Delta X = 50 \mu\text{m}$, $\Delta Y = 30 \mu\text{m}$, $\Delta\theta = 0.3 \text{ mrad}$ (rms)
 - sextupole errors: $\Delta X = 50 \mu\text{m}$, $\Delta Y = 30 \mu\text{m}$, $\Delta\theta = 0.3 \text{ mrad}$ (rms)
 - BPM resolution: $5 \mu\text{m}$ (rms)
- *not* included
 - wire scanner rolls: $|\theta| \leq 0.2^\circ$ (uniform)
 - wire scanner beam size errors: $\sigma = \sigma_0(1+\Delta\sigma_{\text{relative}})+\Delta\sigma_{\text{absolute}}$
 - quadrupole strength errors ($\Delta K/K$)
 - BPM offsets
 - BPM rolls
 - tuning in FF

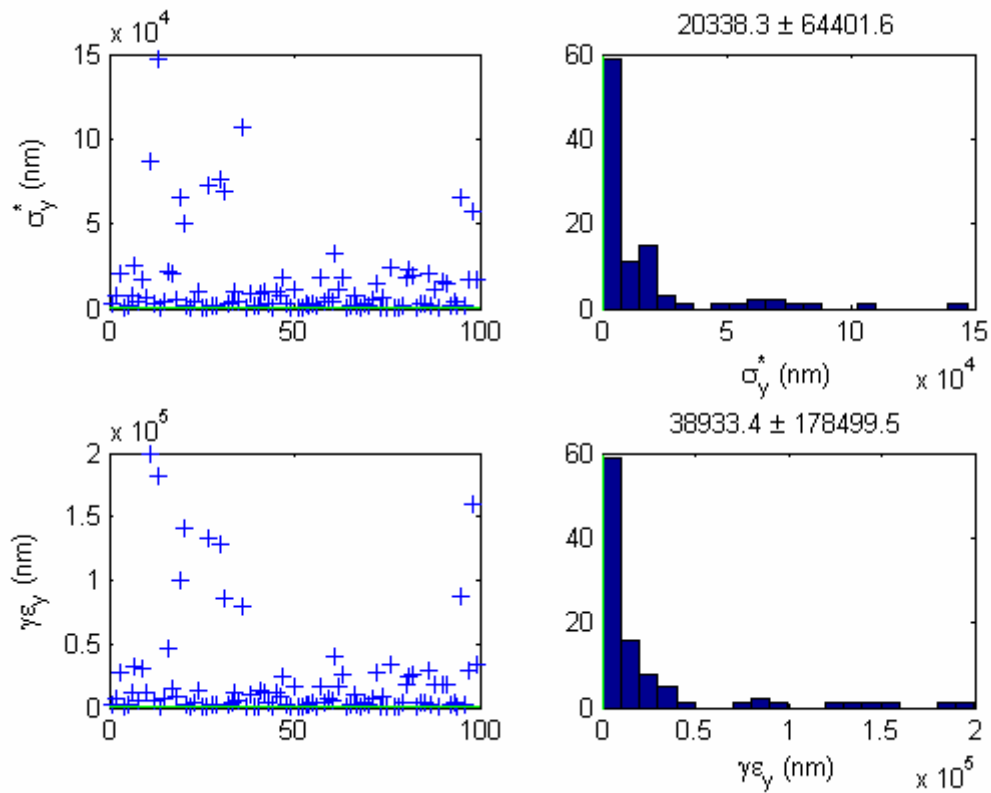
¹<http://www.slac.stanford.edu/accel/ilc/codes/Lucretia/>

²EXT dipoles BH1 and BH2 are assumed to have nonzero sextupole components

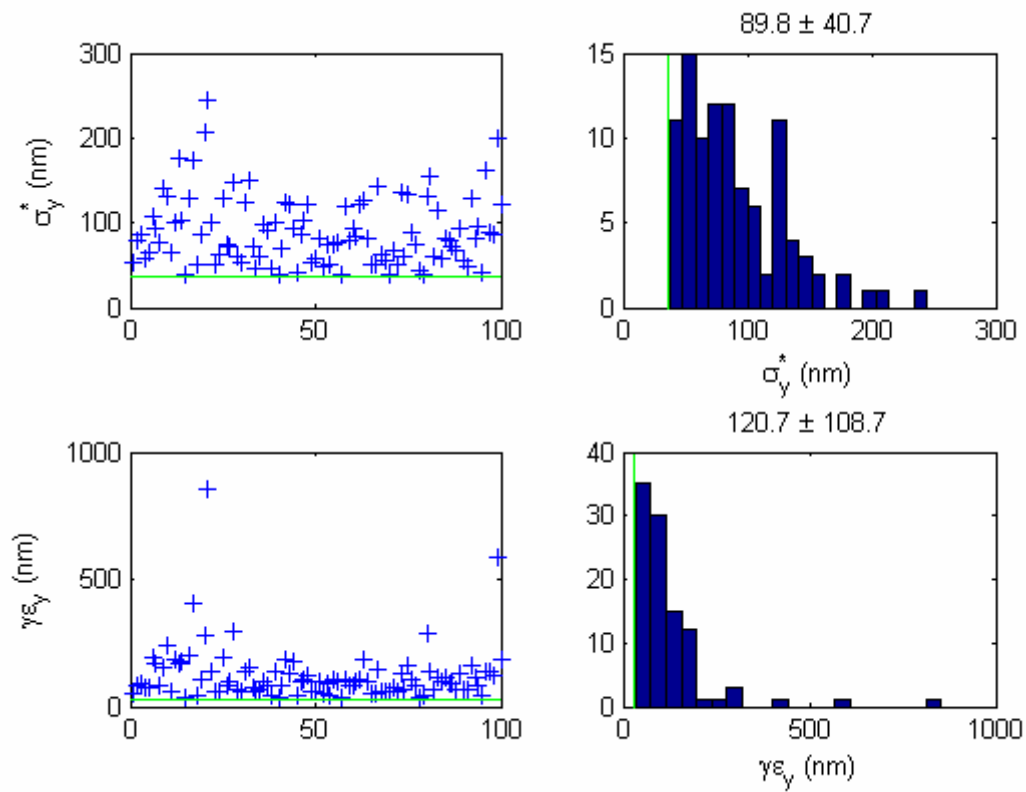
Simulation Procedure

1. apply errors
2. steer flat (EXT only)
3. launch into FF
 - use 2 virtual correctors
 - steer to 2 virtual BPMs (one at the IP and one 90° upstream)
 - virtual BPMs are perfect
4. measure dispersion in diagnostic section
 - scan input beam energy
 - measure orbits
 - fit position vs energy at each BPM
5. correct dispersion in diagnostic section
 - back-propagate measured η to start of diagnostic section to get η_0 and η'_0
 - use QF1X + QF6X multiknobs for η_x and η'_x
 - correct η_y and η'_y using skew quads in inflector (thin lenses at quad centers)
6. correct coupling
 - scan 4 skew quadrupoles sequentially
 - deduce projected ε_y from wire scanner measurements
 - set each skew quad to minimize projected ε_y

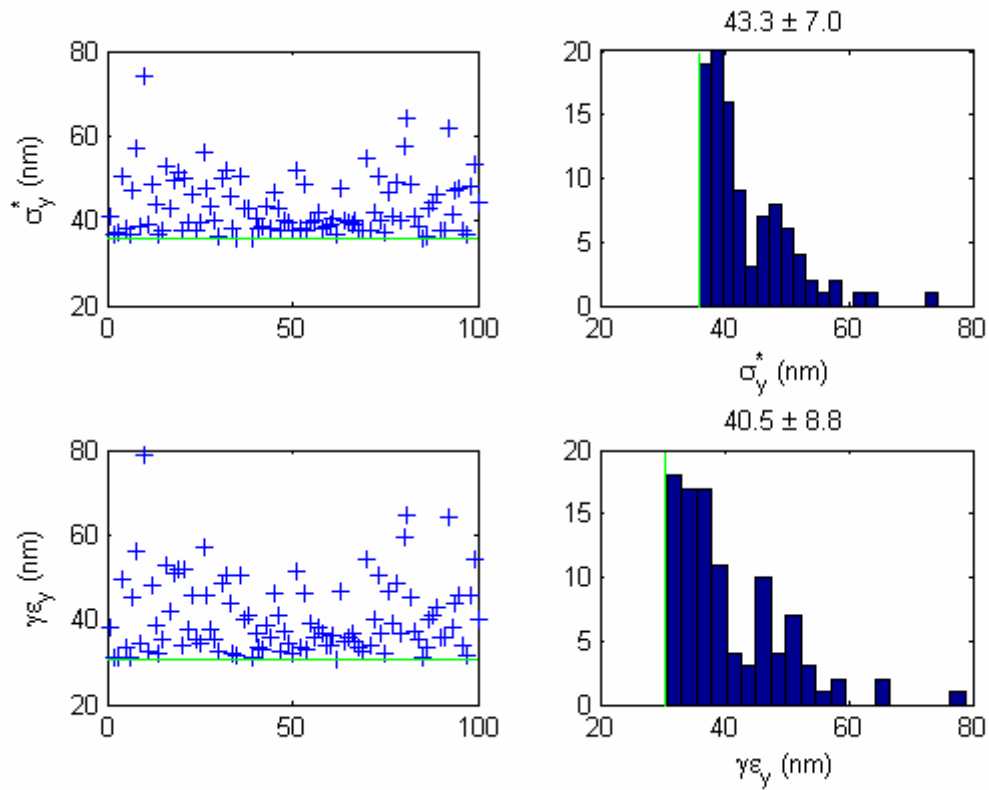
errors only (100 seeds)



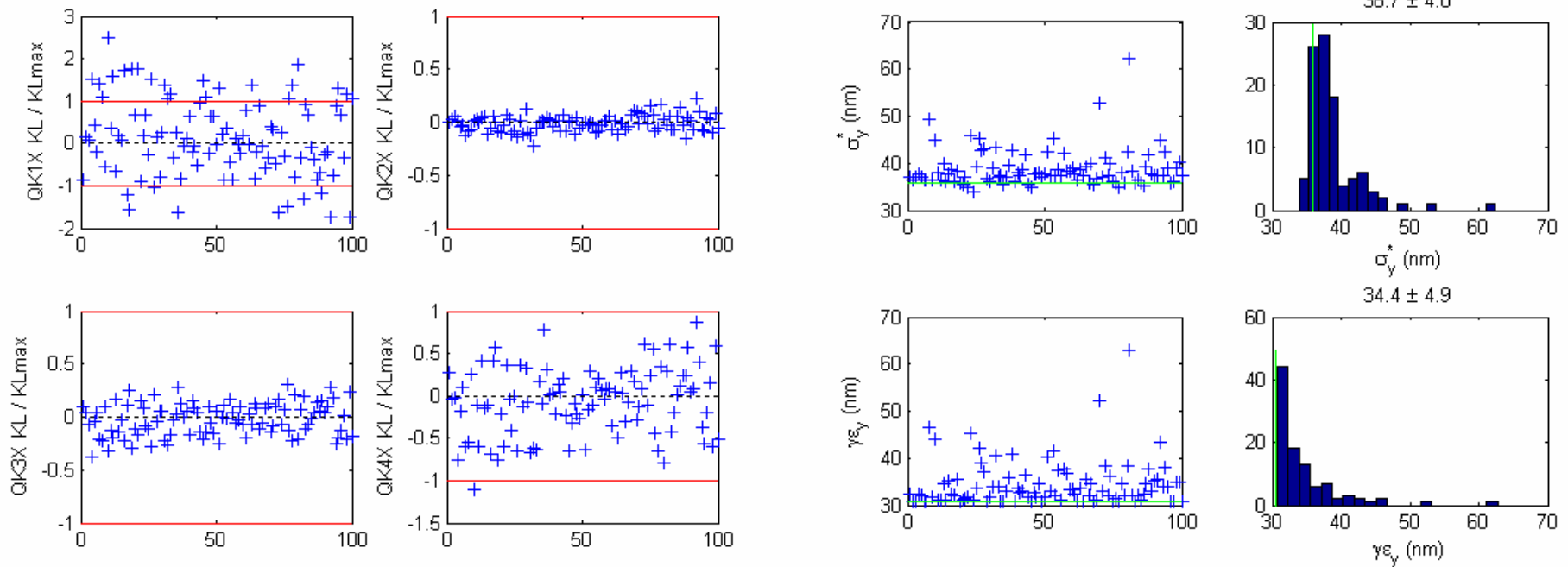
errors, FF launch



errors, steer flat, FF launch

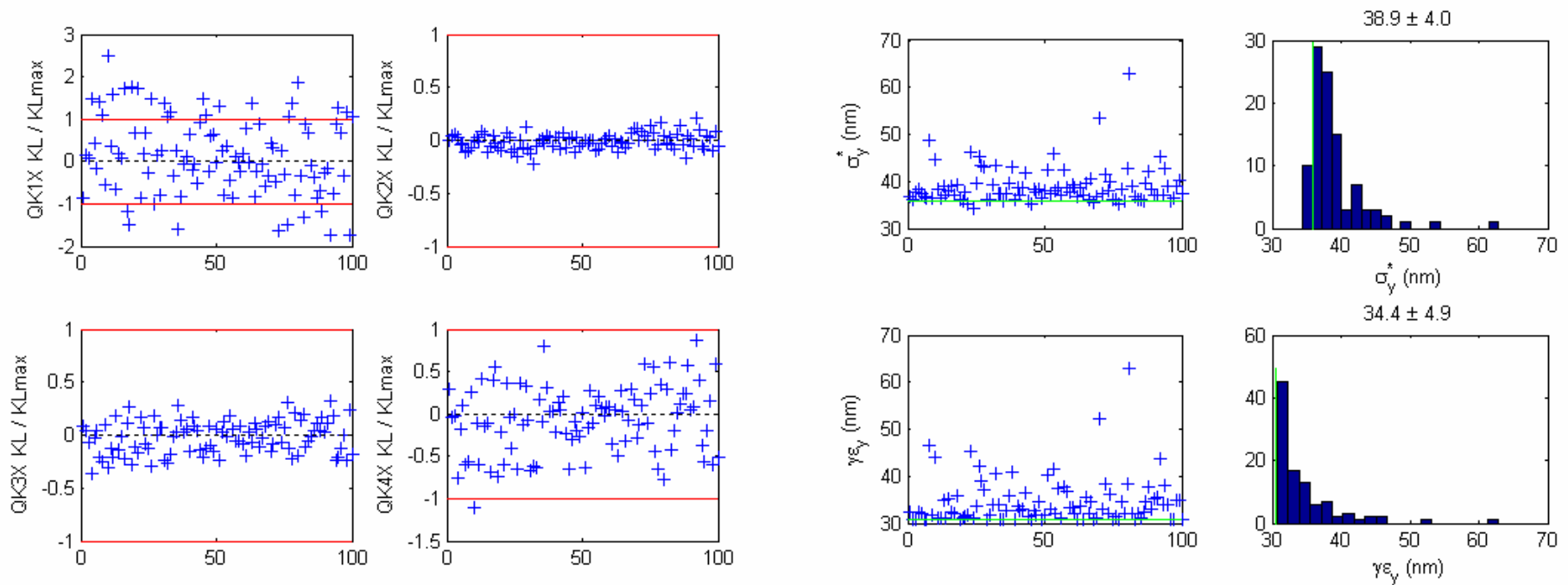


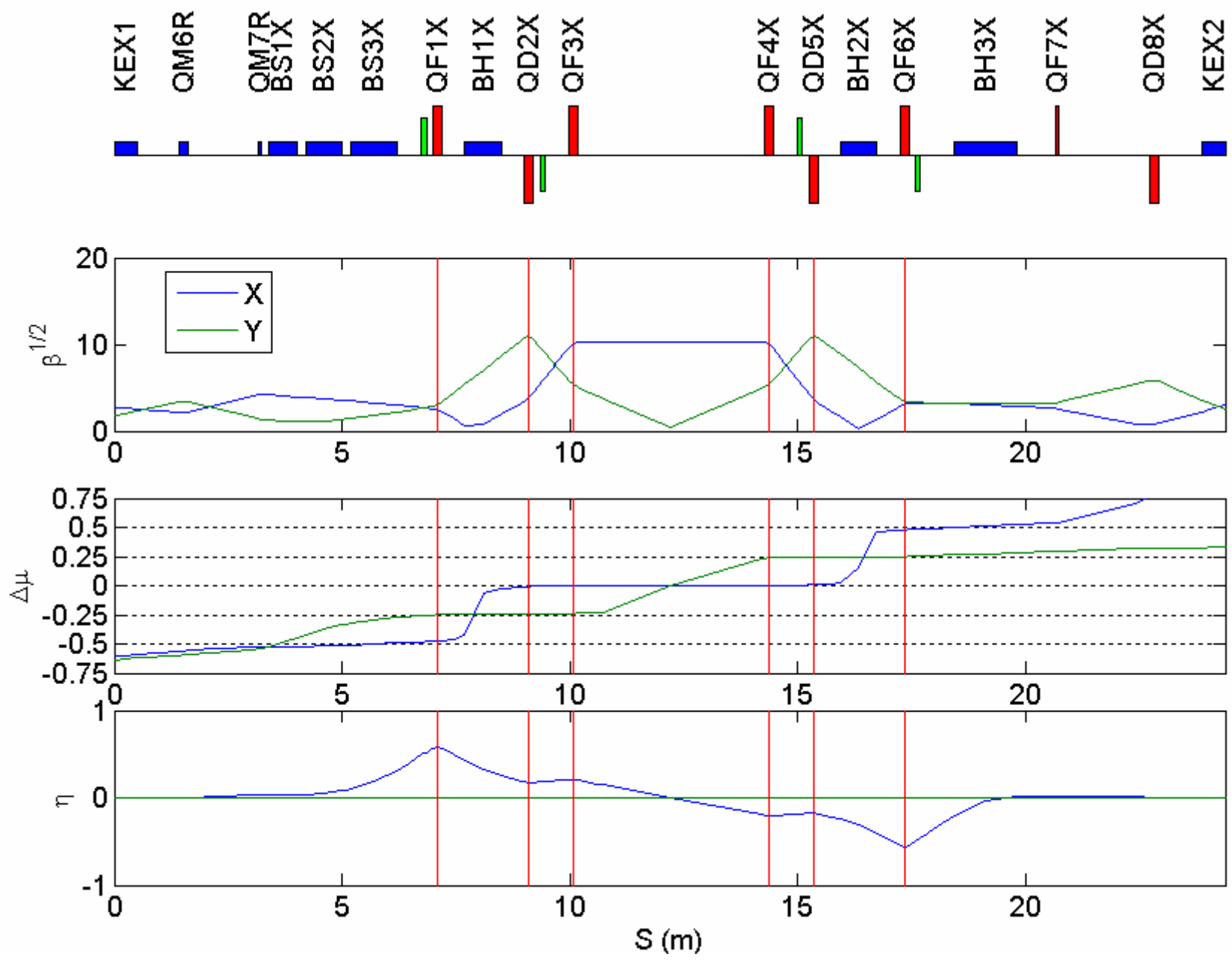
errors, steer flat, correct coupling, FF launch



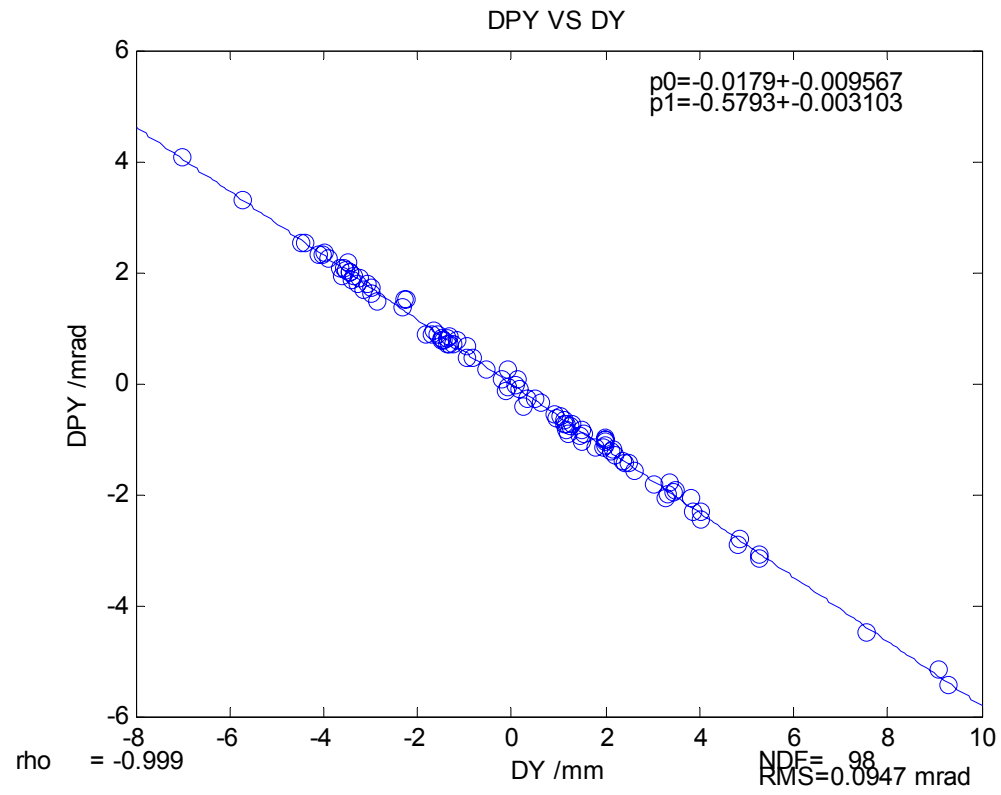
Note: red lines represent maximum integrated strength of IDX skew quad ($K_{Lmax} \approx 0.1$ T)

errors, steer flat, correct η_x , correct coupling, FF launch

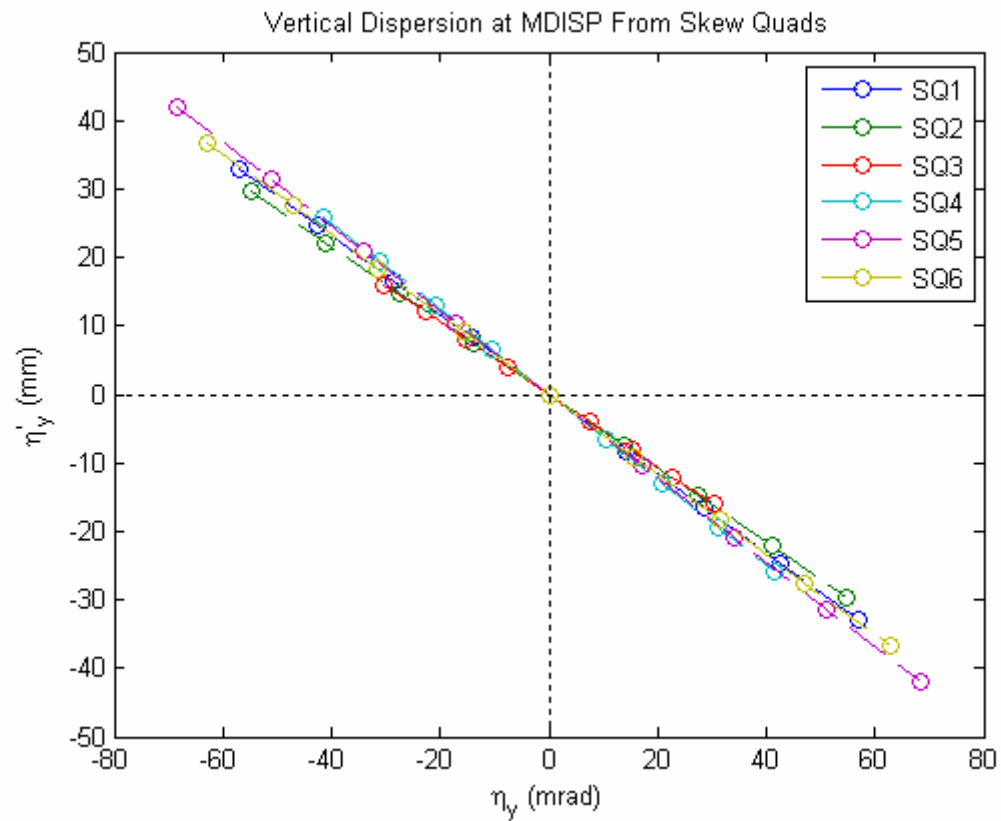




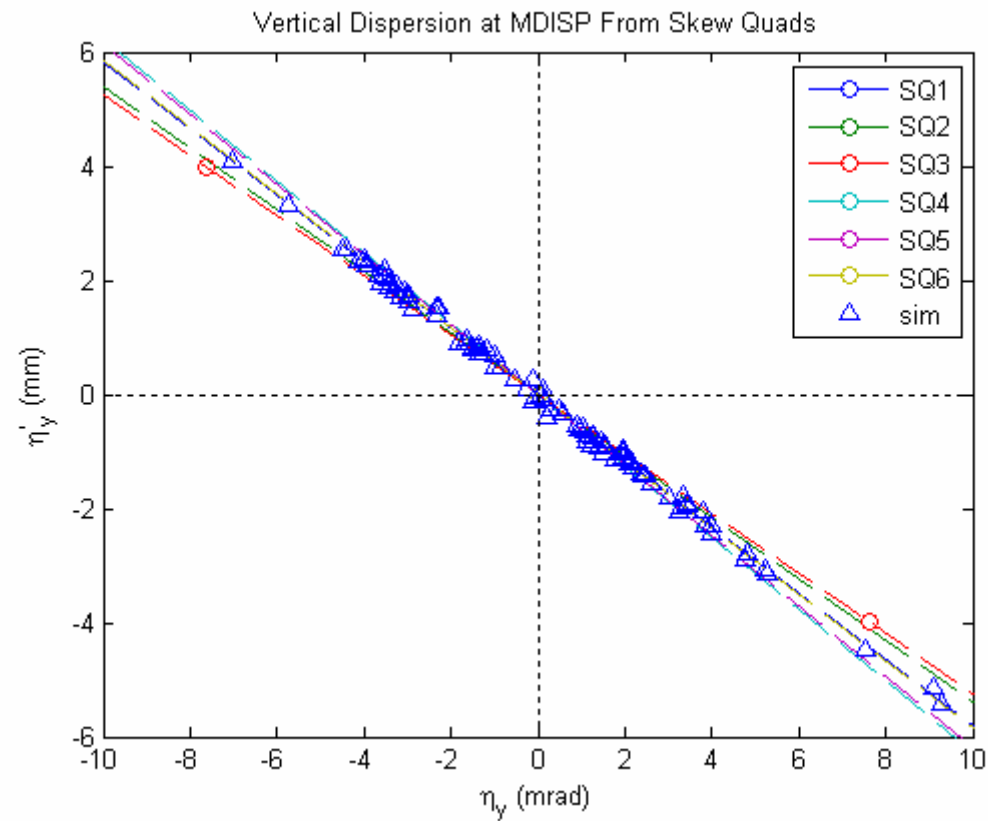
η_y vs η'_y at exit of KEX2 (start of diagnostic section)
100 seeds after steering EXT



η_y vs η'_y at exit of KEX2 (start of diagnostic section)
perfect EXT; scan each skew quad



both η_y and η'_y can be corrected with any single skew quad!



η_y correction: residual x-y coupling

$$R = \begin{bmatrix} R_{11} & R_{12} & R_{13} & R_{14} \\ R_{21} & R_{22} & R_{23} & R_{24} \\ R_{31} & R_{32} & R_{33} & R_{34} \\ R_{41} & R_{42} & R_{43} & R_{44} \end{bmatrix} \equiv \begin{bmatrix} A & B \\ C & D \end{bmatrix}$$

$$Q_{x,y} \equiv \frac{1}{\sqrt{\beta_{x,y}}} \begin{bmatrix} \beta_{x,y} & 0 \\ -\alpha_{x,y} & 1 \end{bmatrix}$$

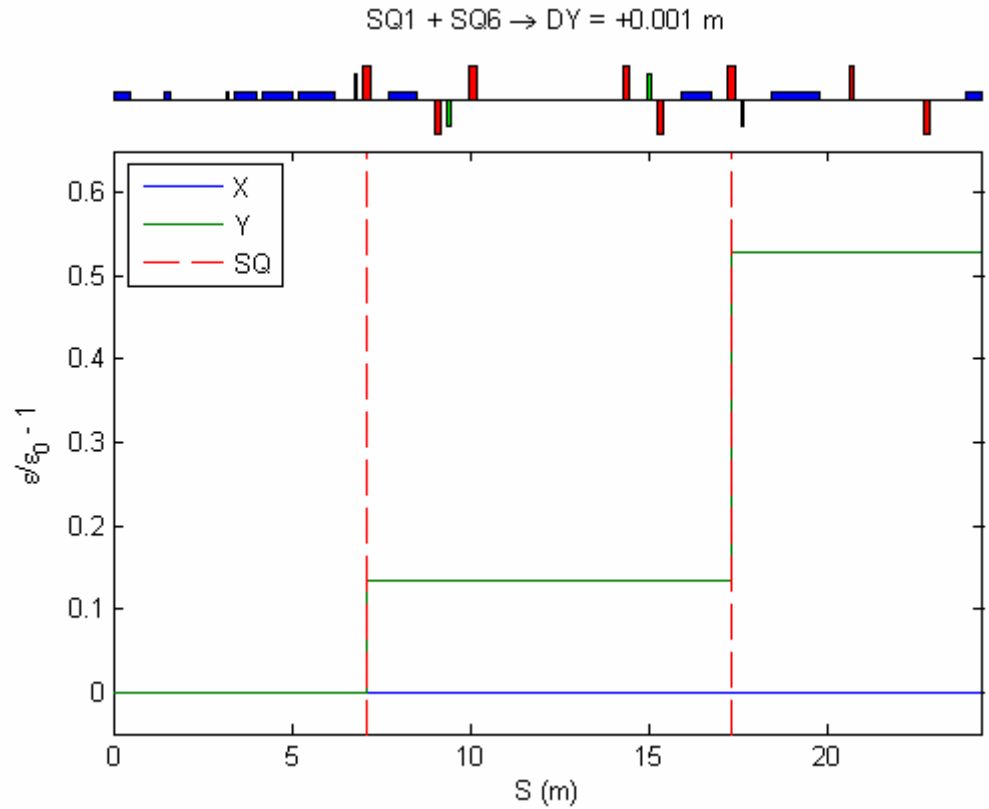
$$P \equiv Q_x^{-1} A^{-1} B Q_y$$

$$\lambda = \text{tr}(PP^T)$$

$$\epsilon_x^2 = |A|^2 \epsilon_{x0}^2 + |C|^2 \epsilon_{y0}^2 + |A|^2 \epsilon_{x0} \epsilon_{y0} \lambda$$

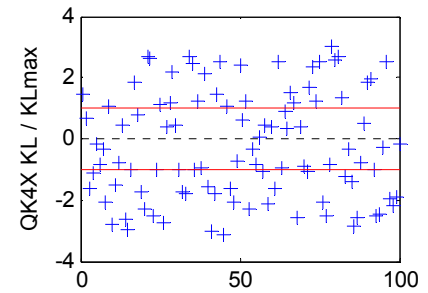
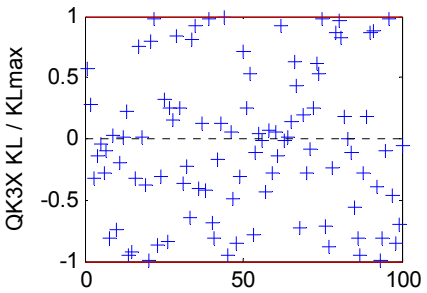
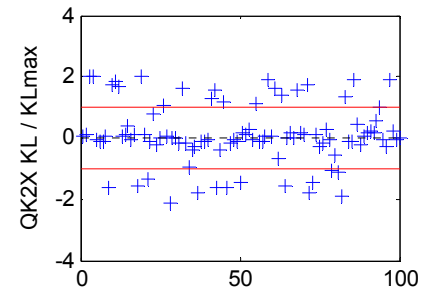
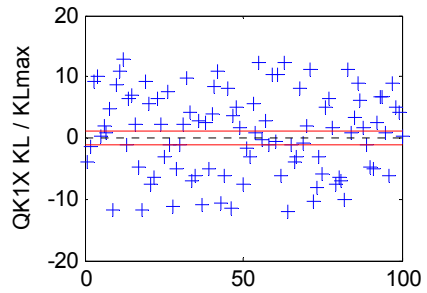
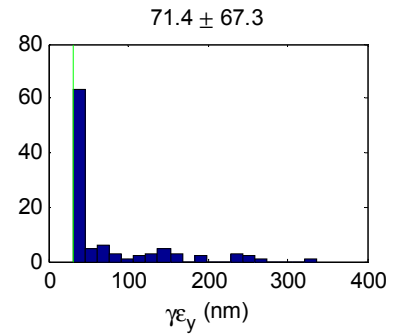
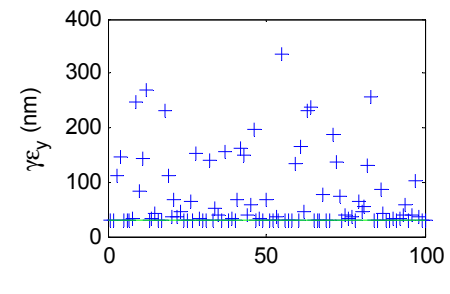
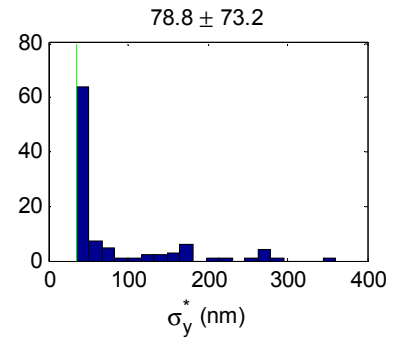
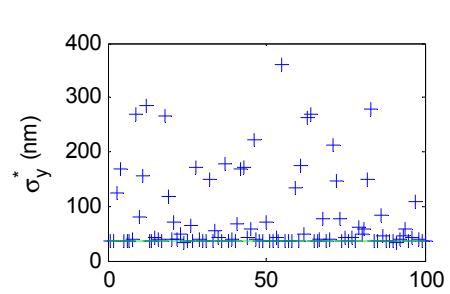
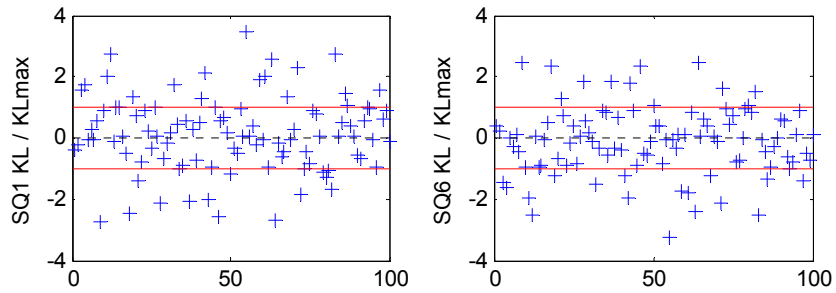
$$\epsilon_y^2 = |C|^2 \epsilon_{x0}^2 + |A|^2 \epsilon_{y0}^2 + |A|^2 \epsilon_{x0} \epsilon_{y0} \lambda$$

Scheme 1: 2 skew quads

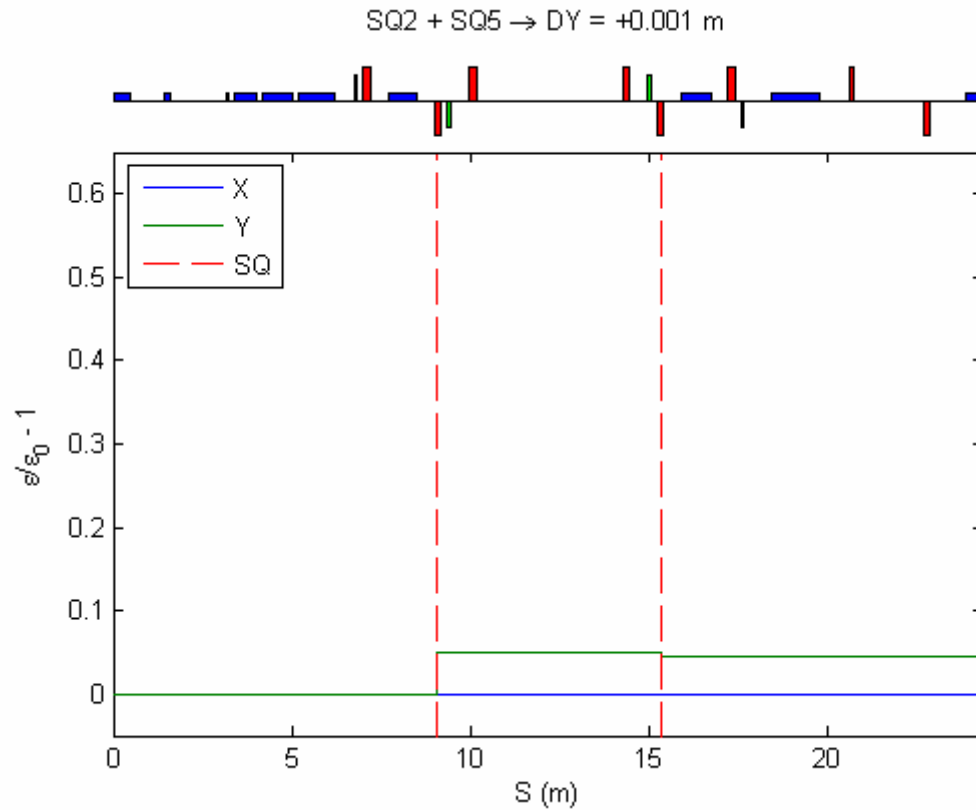


	SQ1	SQ6
β_x	= 5.920	10.036
α_x	= 4.480	-5.320
η_x	= 0.585	-0.566
β_y	= 9.053	11.557
α_y	= -7.212	6.631
$\Delta\mu_x$	= -	343.575
$\Delta\mu_y$	= -	179.568
k_l/k_{lmax}	= 0.221	-0.178
residual	= 0.5288	

Scheme 1

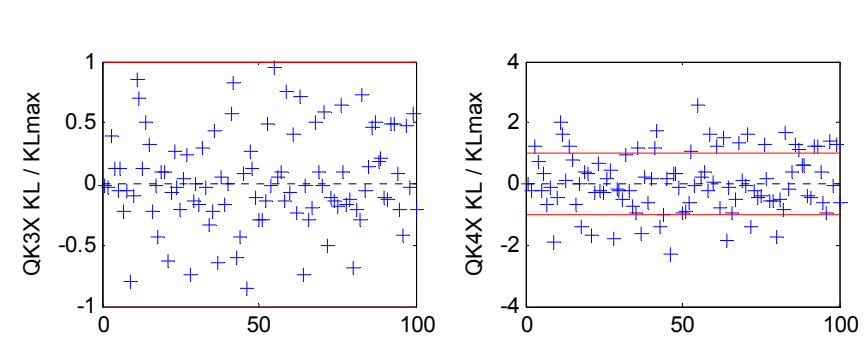
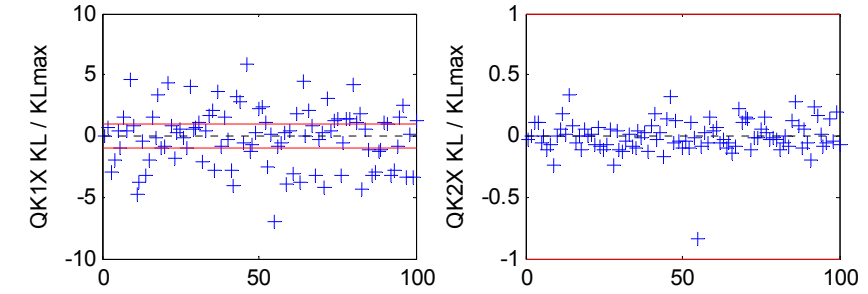
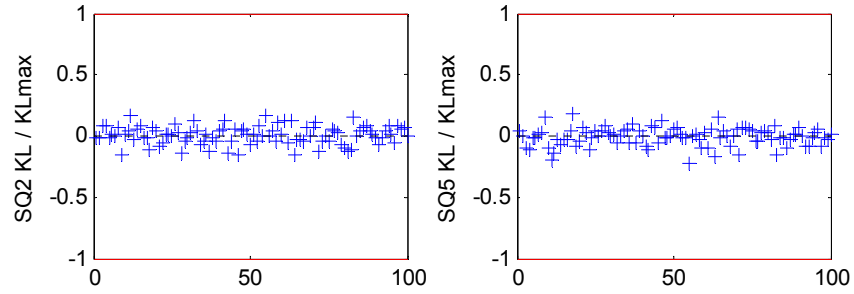
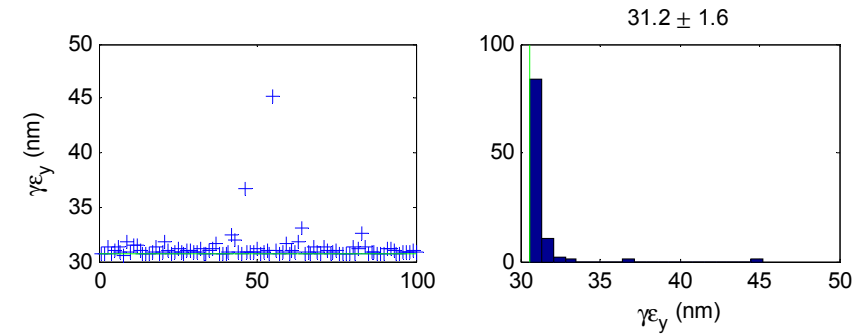
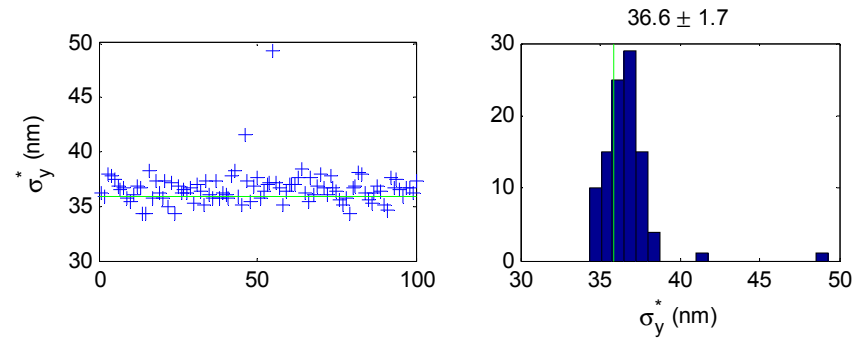


Scheme 2: 2 skew quads

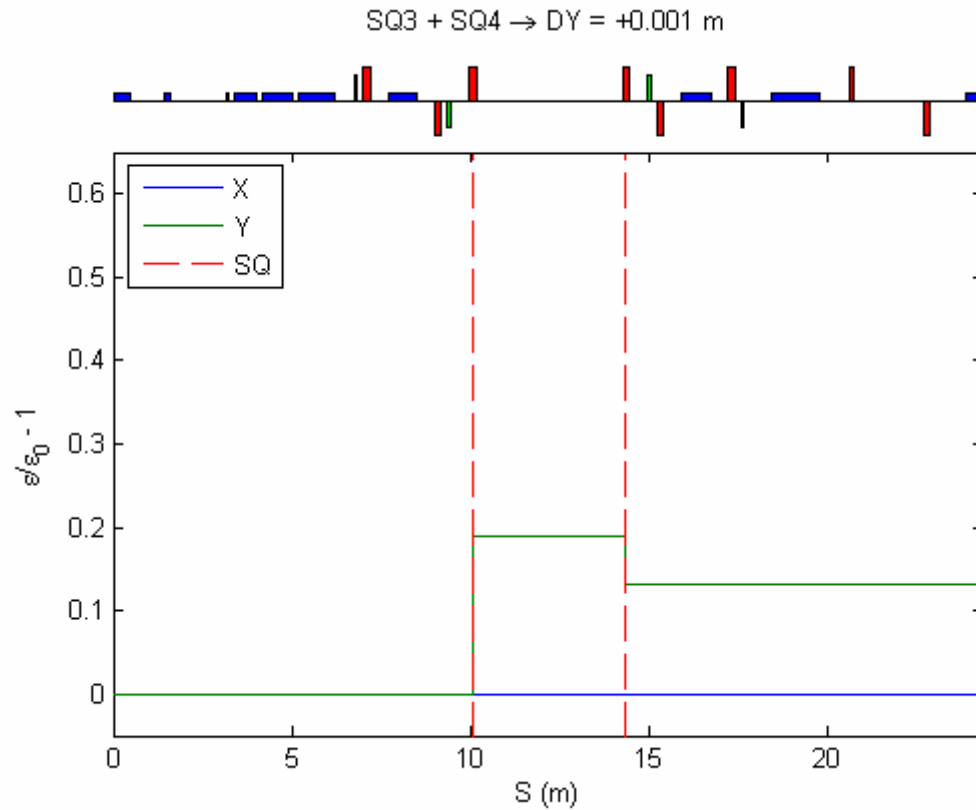


	SQ2	SQ5
β_x	= 14.557	13.494
α_x	= -18.187	18.354
η_x	= 0.177	-0.174
β_y	= 118.109	119.830
α_y	= 10.711	-12.069
$\Delta\mu_x$	= -	5.337
$\Delta\mu_y$	= -	172.957
kl/kl_{max}	= 0.023	0.001
residual	= 0.0442	

Scheme 2

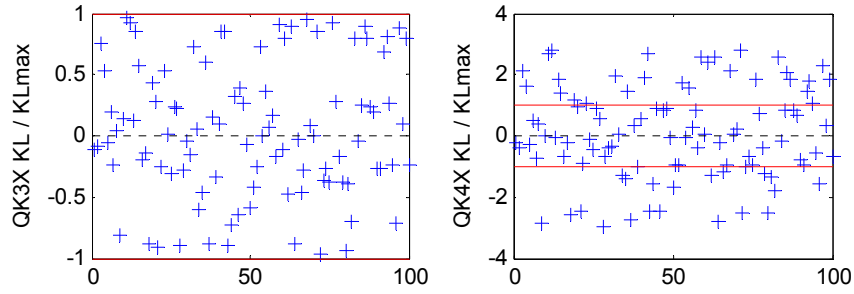
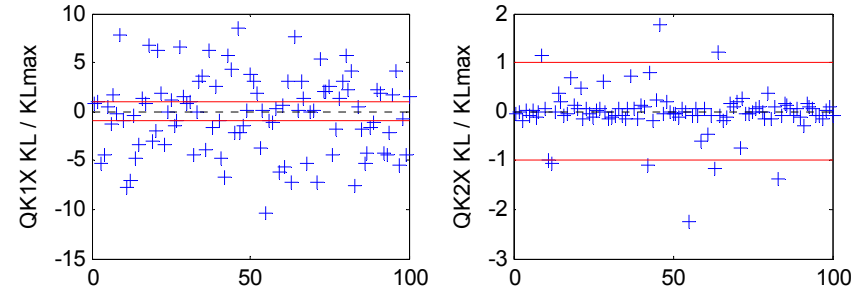
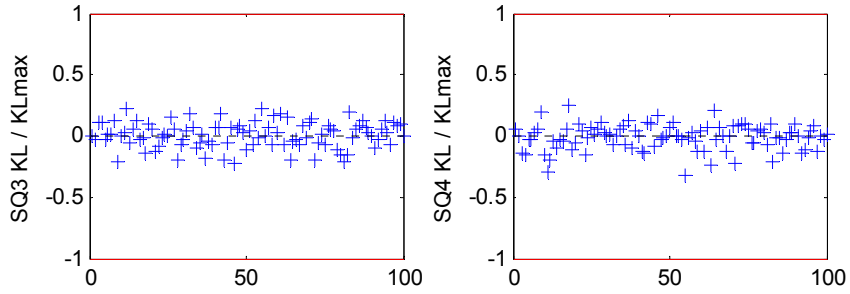
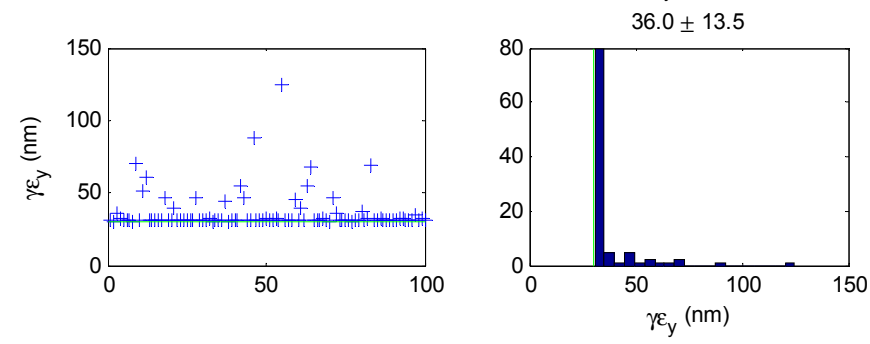
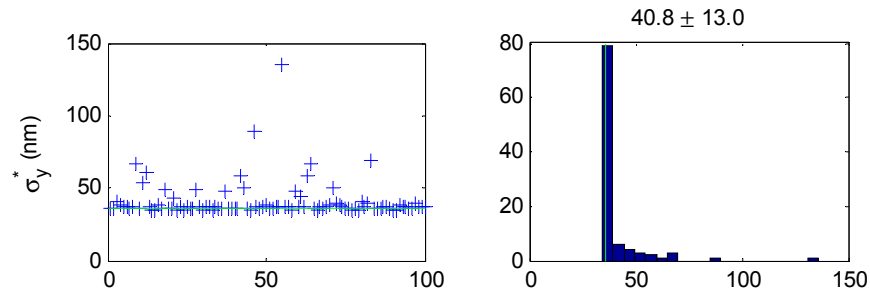


Scheme 3: 2 skew quads

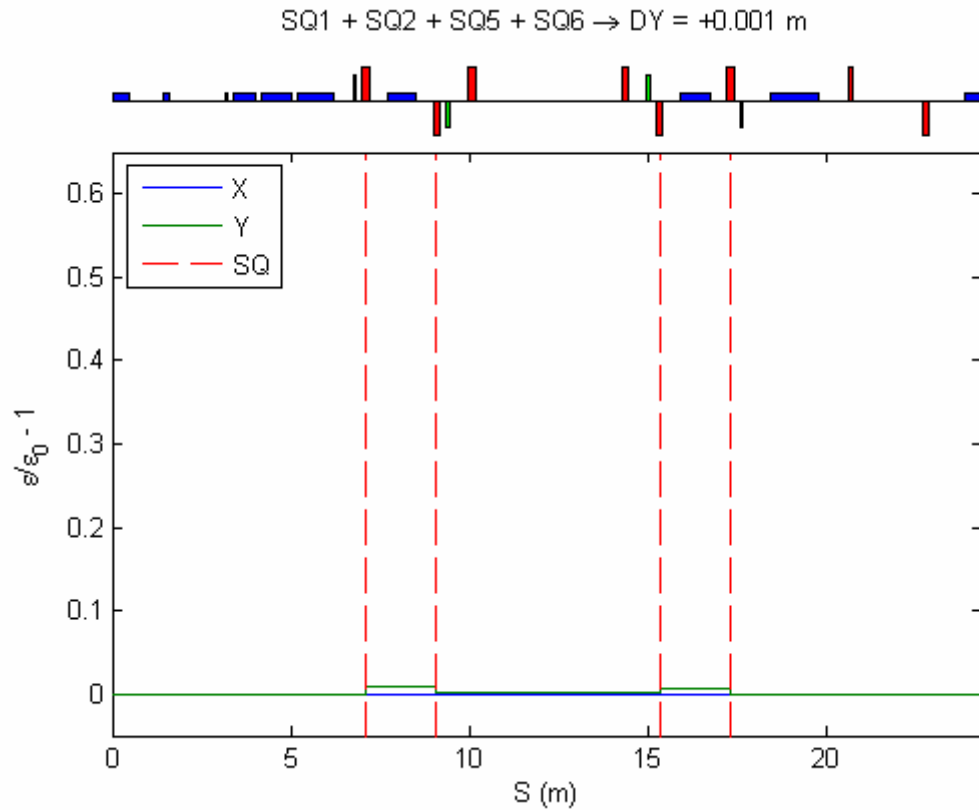


	SQ3	SQ4
β_x	= 101.073	101.000
α_x	= -34.197	34.920
η_x	= 0.209	-0.209
β_y	= 28.629	28.649
α_y	= 22.275	-22.484
$\Delta\mu_x$	= -	2.362
$\Delta\mu_y$	= -	171.062
kl/kl_{max}	= 0.036	0.006
residual	= 0.1318	

Scheme 3

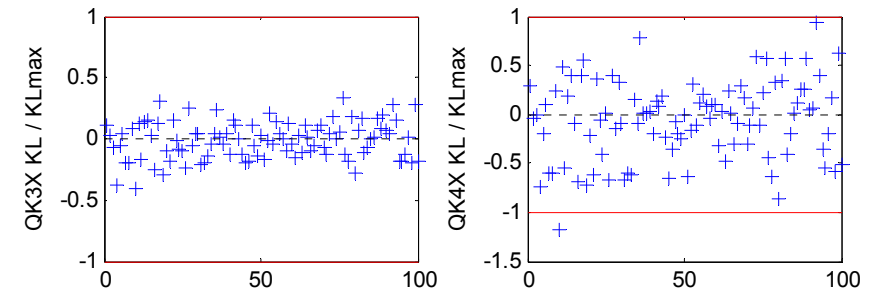
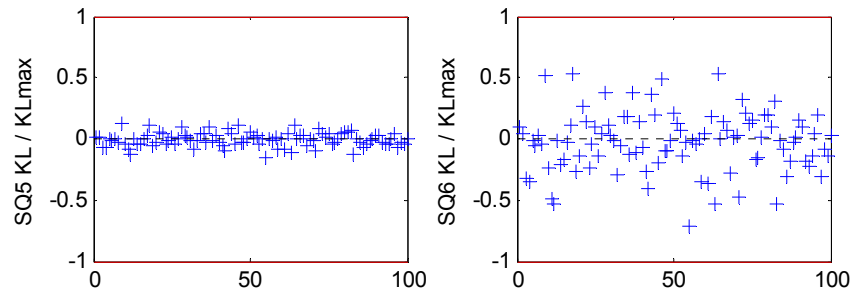
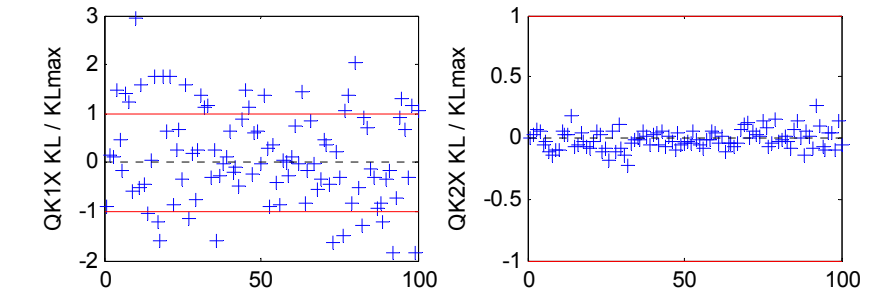
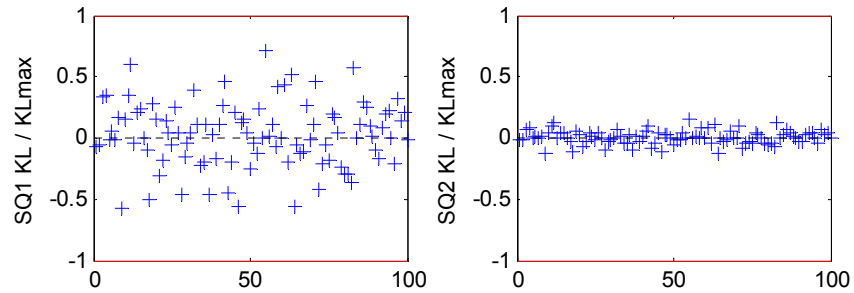
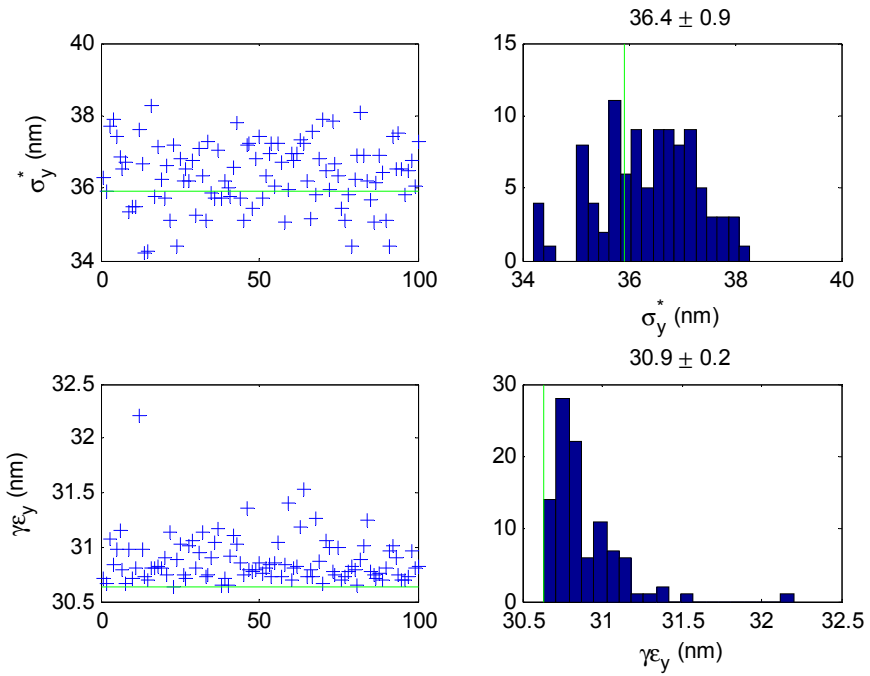


Scheme 4: 4 skew quads

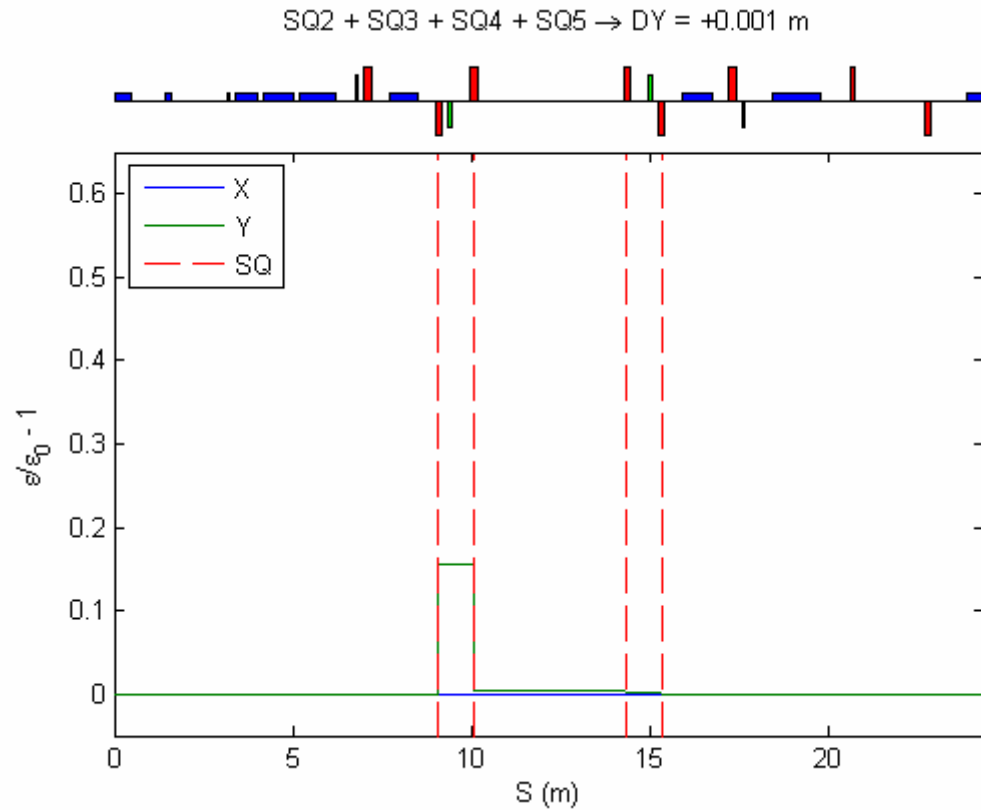


	SQ1	SQ2	SQ5	SQ6
β_x	= 5.920	14.557	13.494	10.036
α_x	= 4.480	-18.187	18.354	-5.320
η_x	= 0.585	0.177	-0.174	-0.566
β_y	= 9.053	118.109	119.830	11.557
α_y	= -7.212	10.711	-12.069	6.631
$\Delta\mu_x$	= -	167.871	173.208	343.575
$\Delta\mu_y$	= -	3.516	176.473	179.568
kl/kl_{max}	= 0.058	0.008	-0.010	-0.027
residual	= 1.8430e-004			

Scheme 4

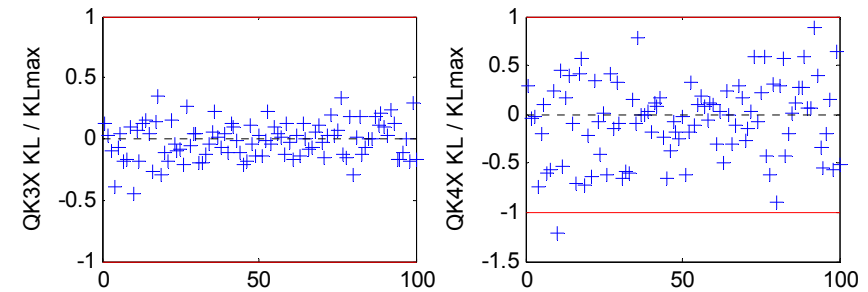
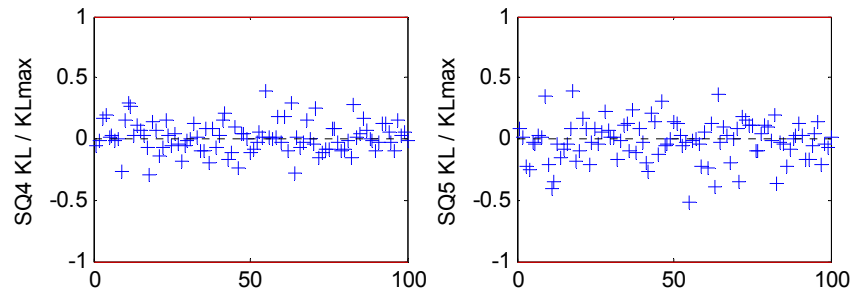
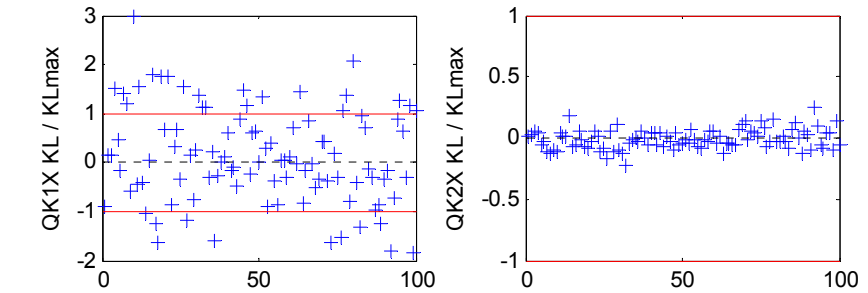
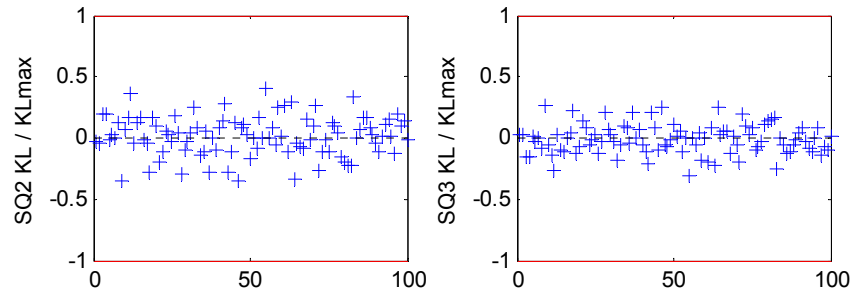
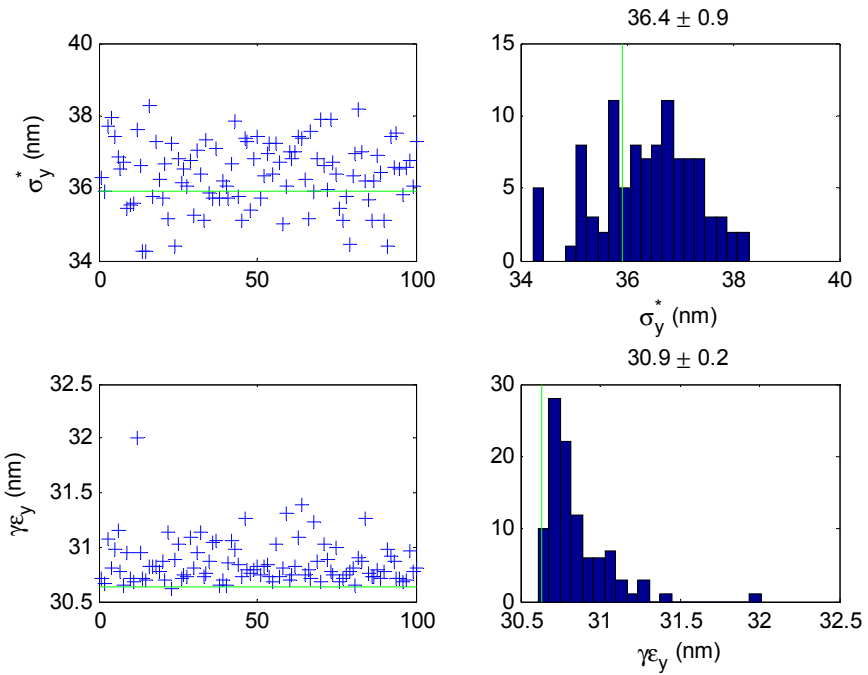


Scheme 5: 4 skew quads

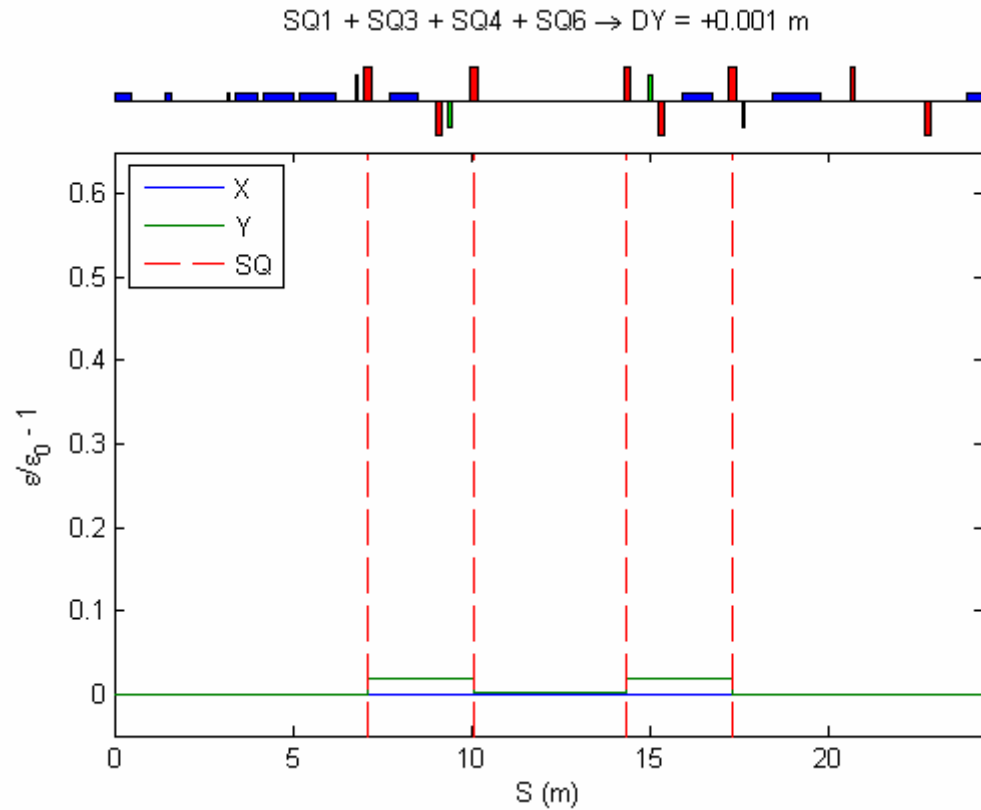


	SQ2	SQ3	SQ4	SQ5
β_x	= 14.557	101.073	101.000	13.494
α_x	= -18.187	-34.197	34.920	18.354
η_x	= 0.177	0.209	-0.209	-0.174
β_y	= 118.109	28.629	28.649	119.830
α_y	= 10.711	22.275	-22.484	-12.069
$\Delta\mu_x$	= -	1.460	3.822	5.337
$\Delta\mu_y$	= -	0.951	172.013	172.957
k_l/k_{lmax}	= 0.042	-0.028	0.007	-0.005
residual	=	4.3953e-004		

Scheme 5

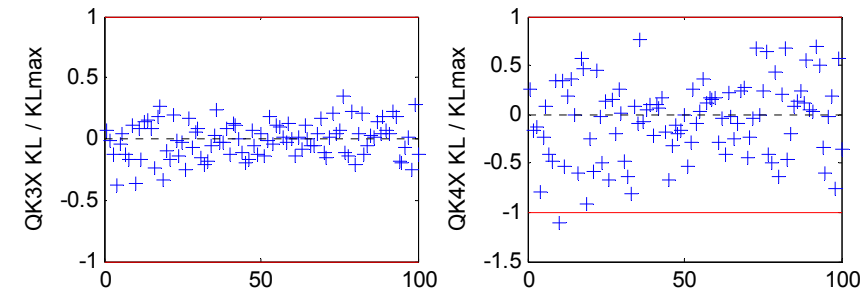
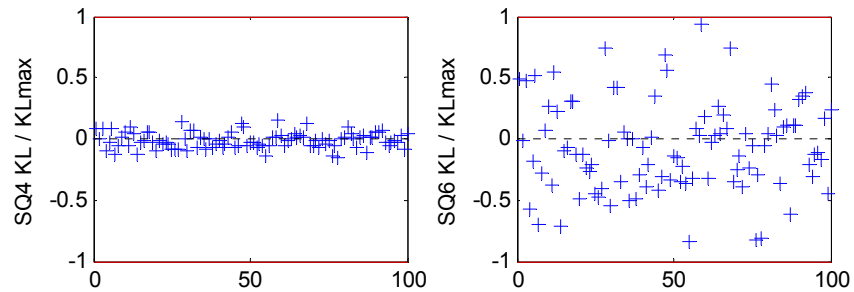
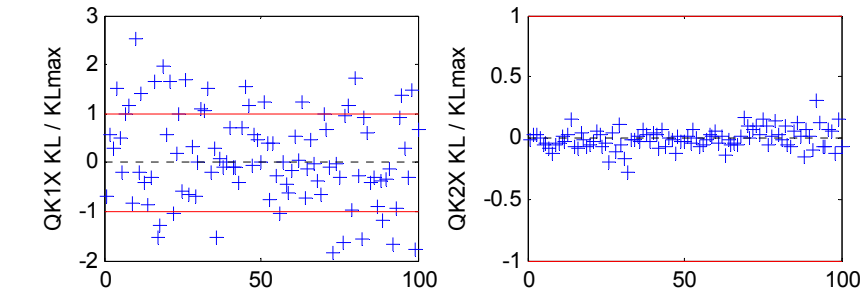
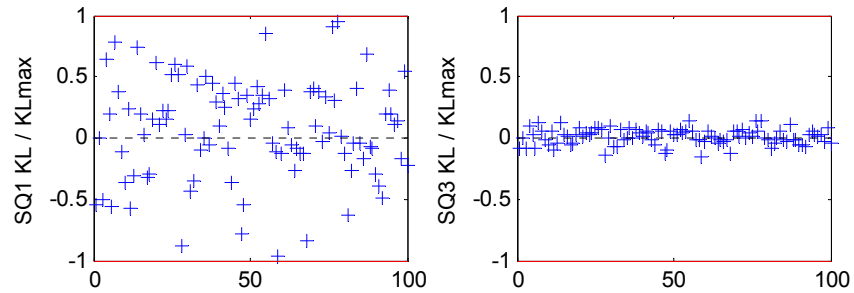
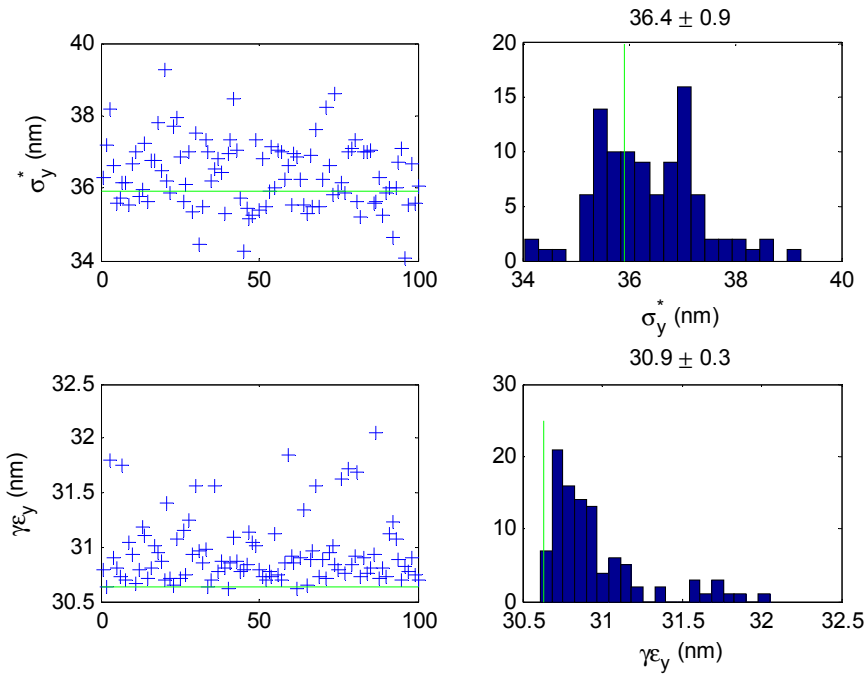


Scheme 6: 4 skew quads

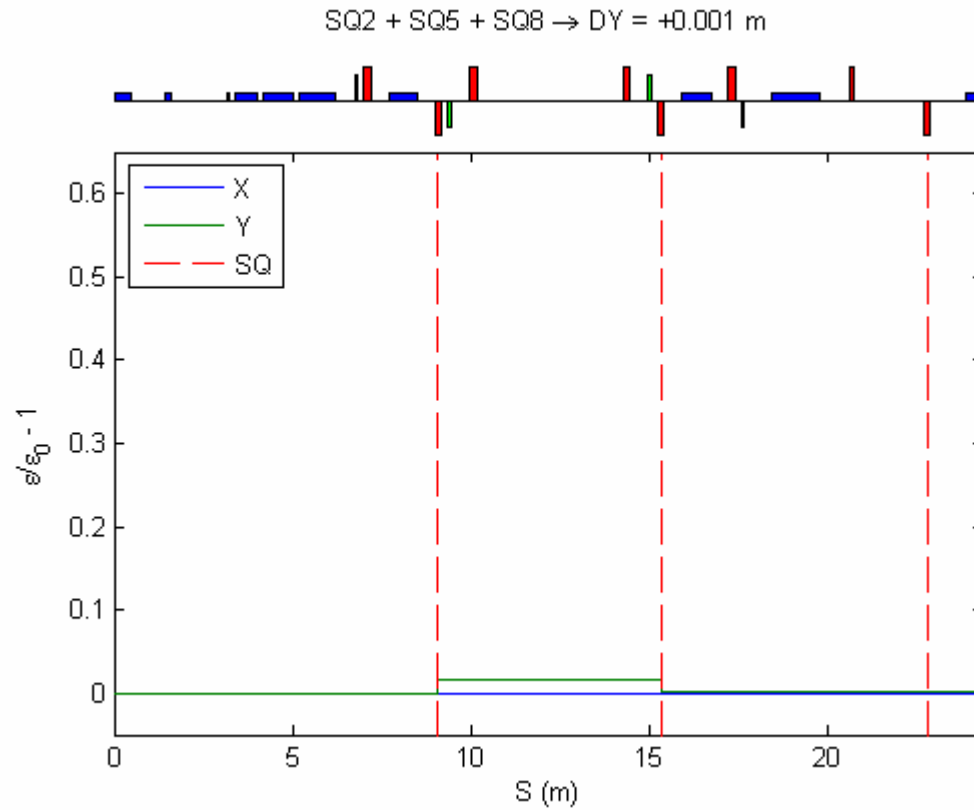


	SQ1	SQ3	SQ4	SQ6
β_x	= 5.920	101.073	101.000	10.036
α_x	= 4.480	-34.197	34.920	-5.320
η_x	= 0.585	0.209	-0.209	-0.566
β_y	= 9.053	28.629	28.649	11.557
α_y	= -7.212	22.275	-22.484	6.631
$\Delta\mu_x$	= -	169.330	171.693	343.575
$\Delta\mu_y$	= -	4.467	175.529	179.568
kl/klmax	= 0.080	0.010	-0.011	-0.048
residual	= 2.1308e-004			

Scheme 6

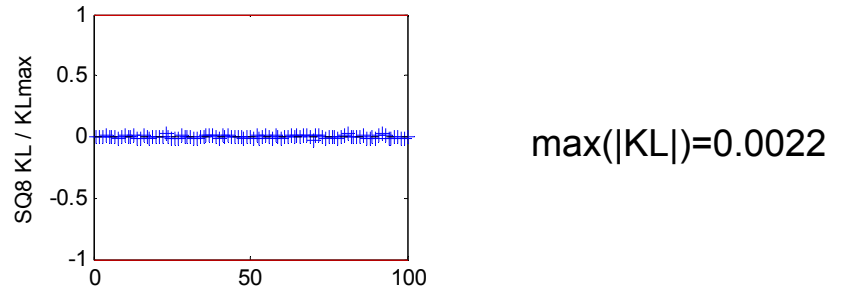
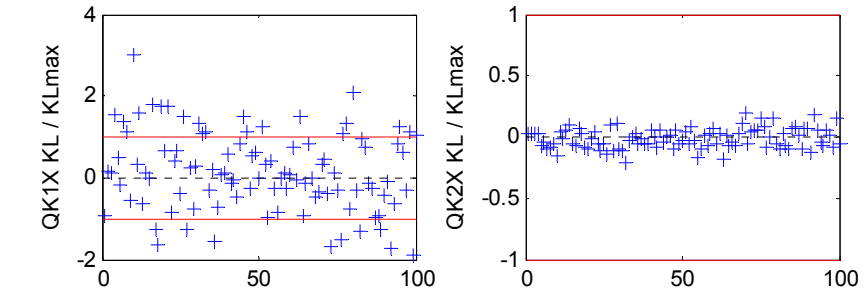
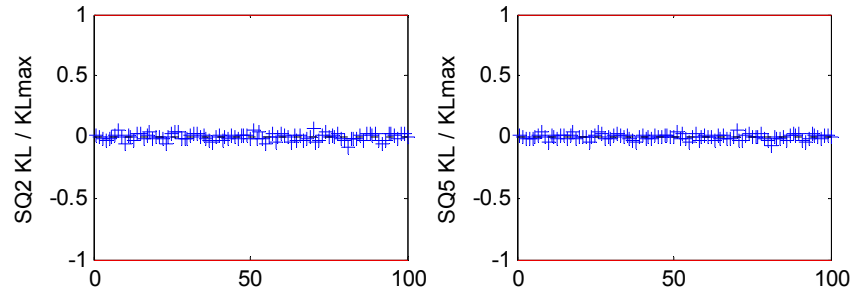
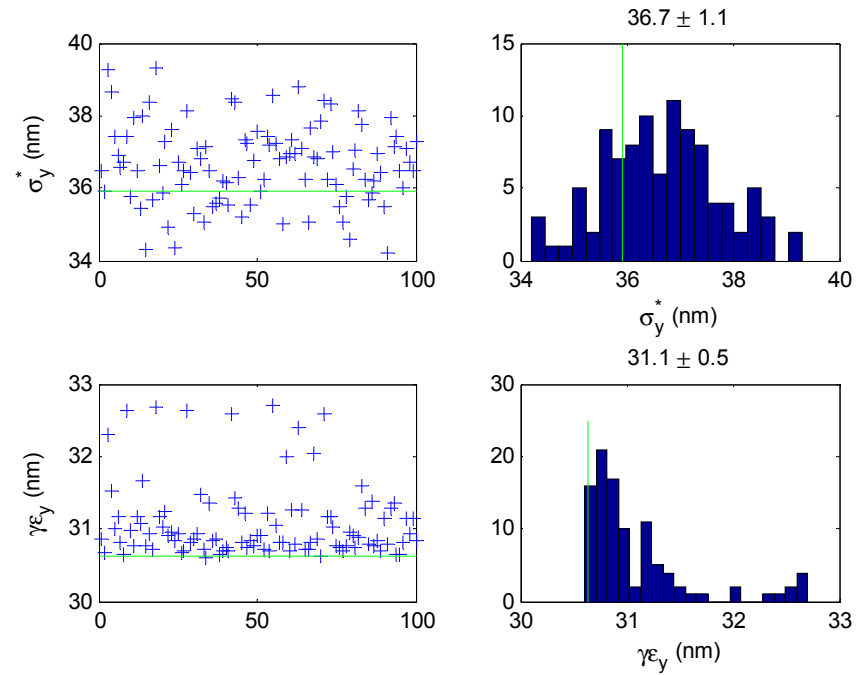


Scheme 7: 3 skew quads

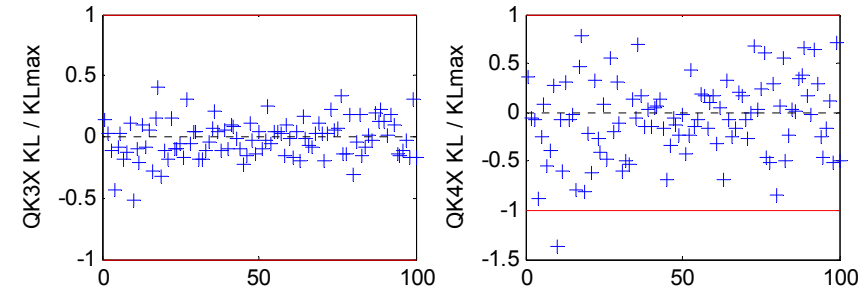


	SQ2	SQ5	SQ8
β_x	= 14.557	13.494	0.696
α_x	= -18.187	18.354	-0.561
η_x	= 0.177	-0.174	0.007
β_y	= 118.109	119.830	34.124
α_y	= 10.711	-12.069	2.668
$\Delta\mu_x$	= -	5.337	289.667
$\Delta\mu_y$	= -	172.957	200.657
k_l/k_{lmax}	= 0.013	0.010	-0.005
residual	= 0.0016		

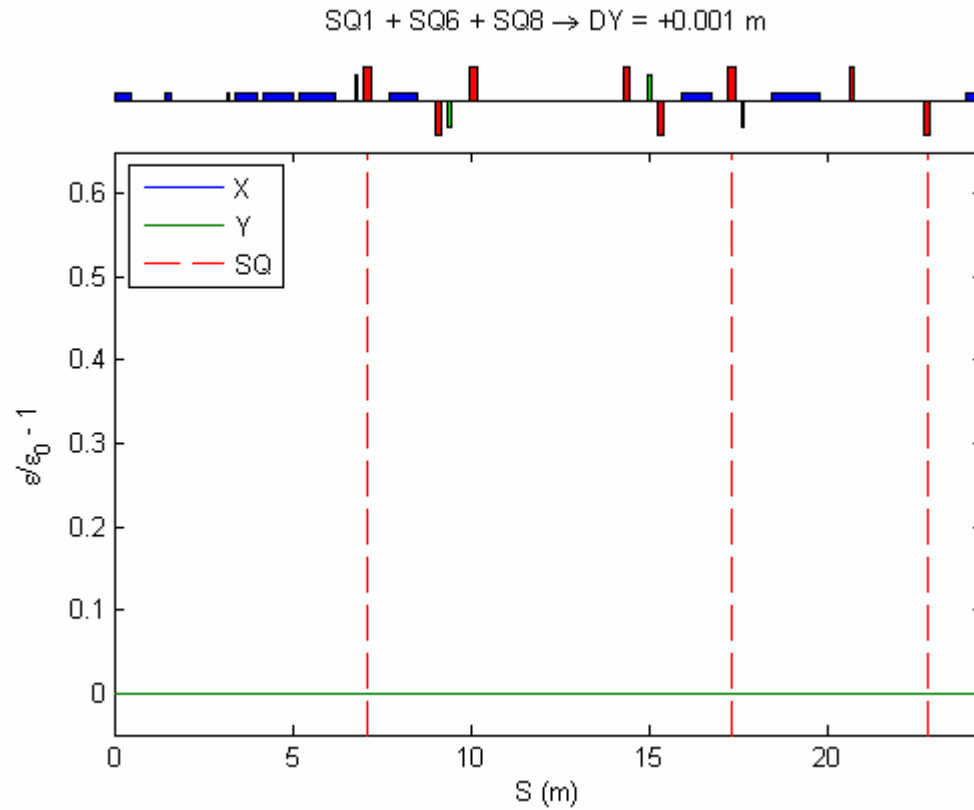
Scheme 7



$\max(|KL|)=0.0022$

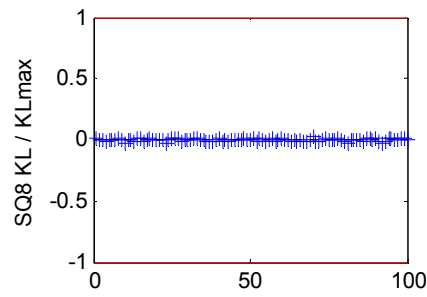
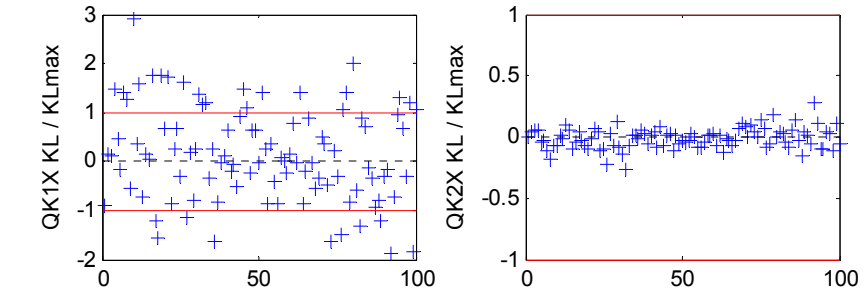
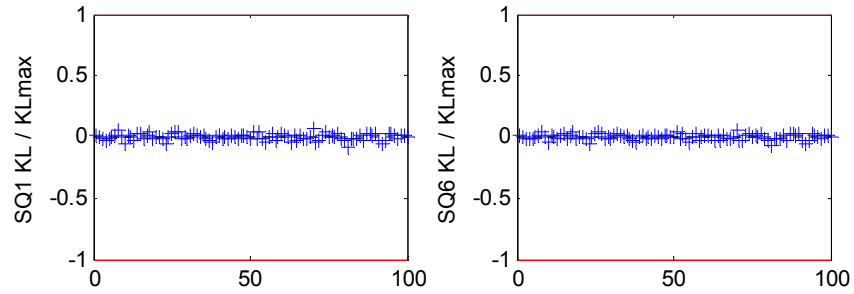
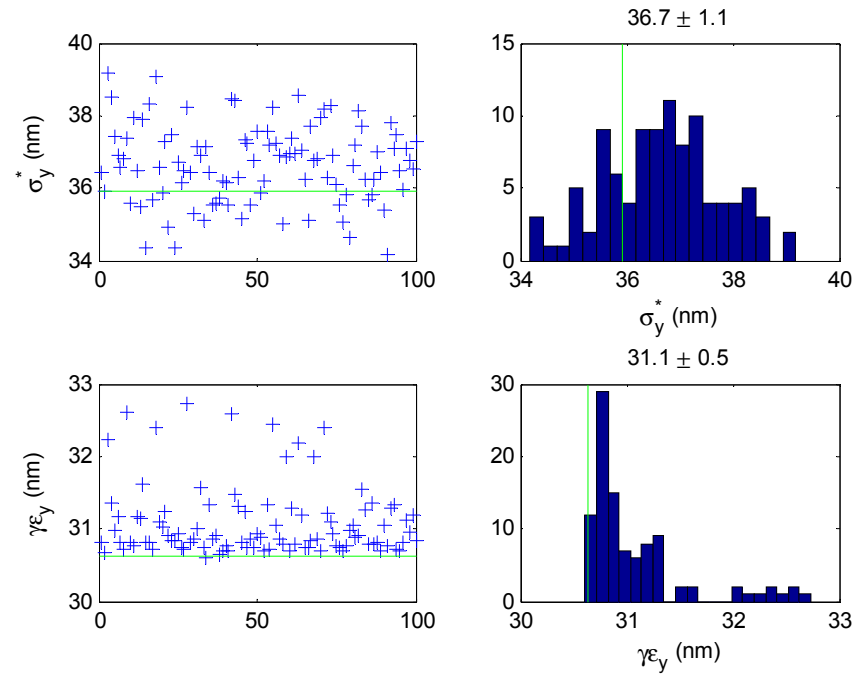


Scheme 8: 3 skew quads

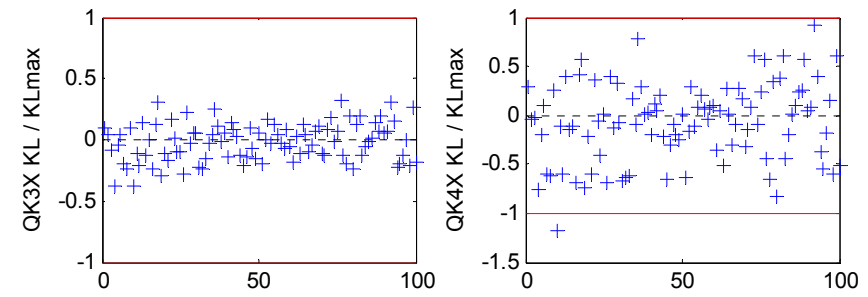


	SQ1	SQ6	SQ8
β_x	= 5.920	10.036	0.696
α_x	= 4.480	-5.320	-0.561
η_x	= 0.585	-0.566	0.007
β_y	= 9.053	11.557	34.124
α_y	= -7.212	6.631	2.668
$\Delta\mu_x$	= -	343.575	457.538
$\Delta\mu_y$	= -	179.568	204.174
k_l/k_{lmax}	= 0.013	0.011	0.005
residual	= 0.0000		

Scheme 8



$\max(|KL|)=0.0021$



Conclusions

- simulated system performance is adequate for the achievement of ATF2 goal “A” (35 nm IP σ_y)
- if small assumed quadrupole roll errors and vertical dipole misalignments are the only sources of coupling, skew correction seems unnecessary
- if quadrupole roll errors are increased by a factor of 10, coupling correction provides 20% improvement in IP σ_y