



Impact of beam-beam effects on precision luminosity measurements at the ILC

LCWS07, May 30th - June 3rd 2007, Hamburg



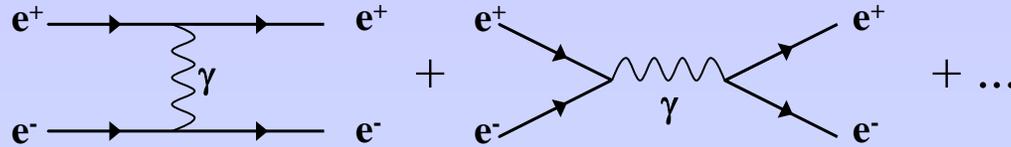
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Impact of beam-beam effects on precision luminosity measurements at the ILC

- Principle of luminosity measurement using Bhabha scattering
- Modifications due to beam-beam effects
- Consequences on reachable luminosity precision
- Dependence with the bunch parameters and energy
- Summary and conclusions

Luminosity measurement in the LumiCal using Bhabha scattering at small angles



- Bhabha particles are detected in coincidence in the LumiCal covering a range of 26.2 to 82 mrad.

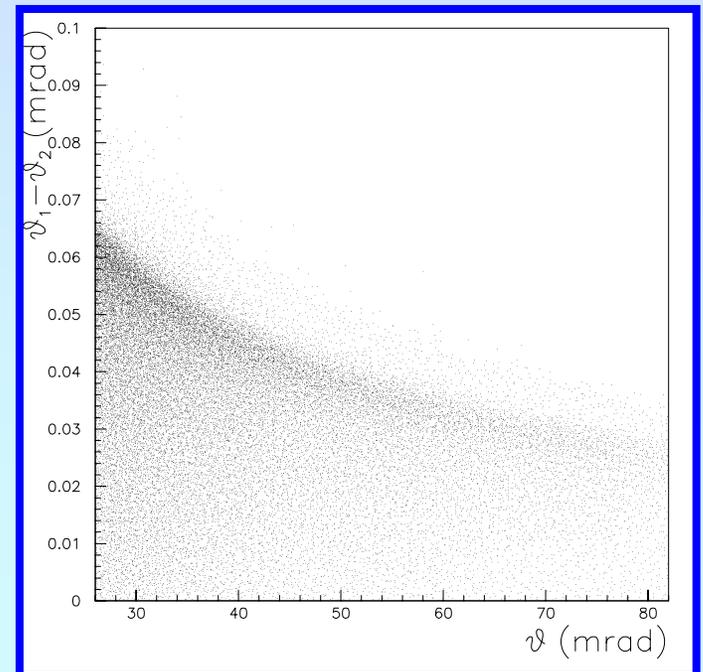
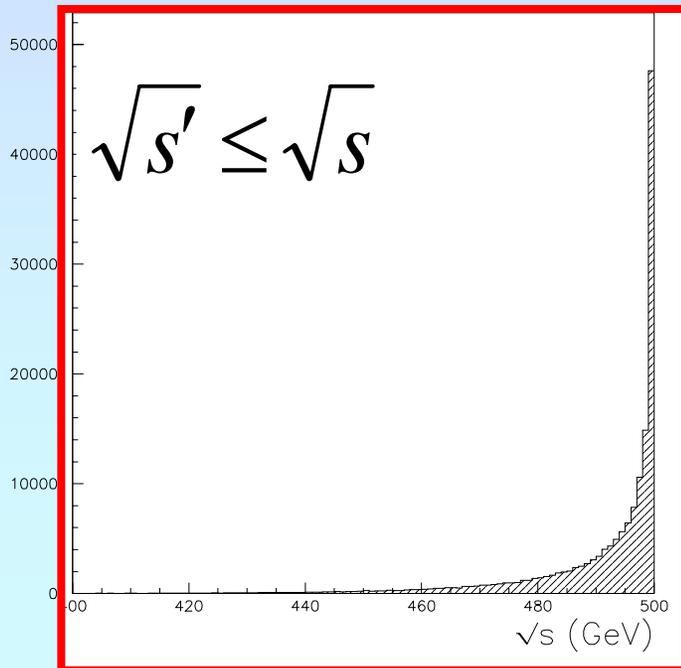
- $\mathcal{L} = N_{\text{Bh}} / \sigma_{\text{Bh}}$ from counting rate \rightarrow **integrated luminosity** ($\Delta\mathcal{L}/\mathcal{L}$: 10^{-3} - 10^{-4})

$$\frac{d\sigma_{\text{Bhabha}}}{d\mathcal{G}} \approx \frac{32\pi\alpha^2}{s} \frac{1}{\mathcal{G}^3}$$

- Measurement of energy and scattering angle of the Bhabhas \rightarrow **luminosity spectrum reconstruction**

Beam-Beam effects on Bhabha scattering

- Bhabhas are produced with BHLUMI, $\sqrt{s} = 500$ GeV, $25 < \theta < 90$ mrad, **ISR included**
- Beam-Beam effect treatment with GUINEA-PIG (Nominal beam param. used for simul.)
 - **Modification of initial state: Beamstrahlung** $\rightarrow \sqrt{s}' \leq \sqrt{s}$, $\Delta\theta_{\text{ini}} \neq 0$, $E_{\text{elec}} \neq E_{\text{posit}}$
 - **Modification of final state: Electromagnetic deflections** \rightarrow bhabha angle reduction ($\sim 10^{-2}$ mrad) + small energy losses



Consequences on integrated luminosity measurement:

Reduction of Bhabha counting rate

First study with the following selection cuts :

$$30 < \theta_{\text{bhabha}} < 75 \text{ mrad} \quad \text{and} \quad E_{\text{bhabha}} > 0.8 E_{\text{beam}}$$

→ **Suppression of Bhabha particles**

Due to modification of initial state = beamstrahlung: $(-3.78 \pm 0.04)\%$

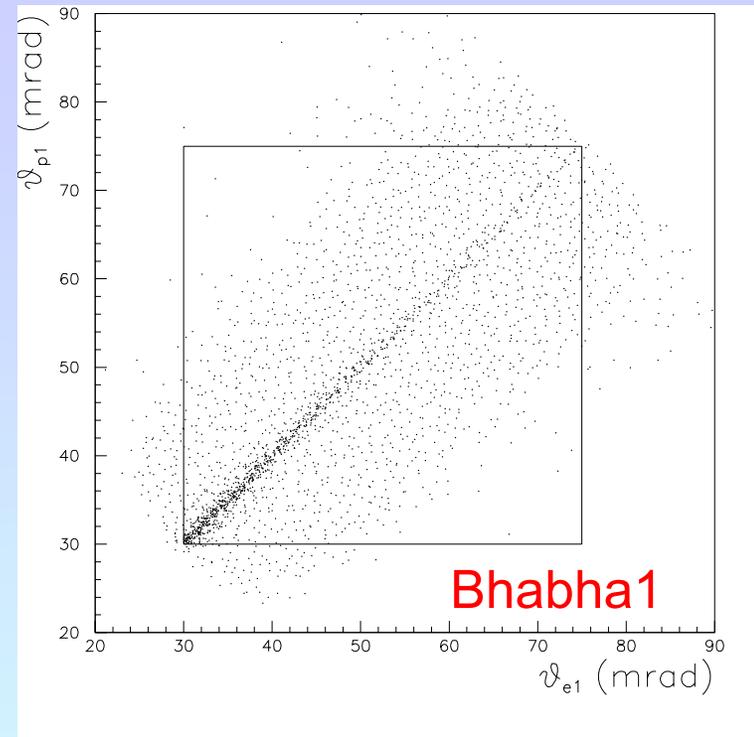
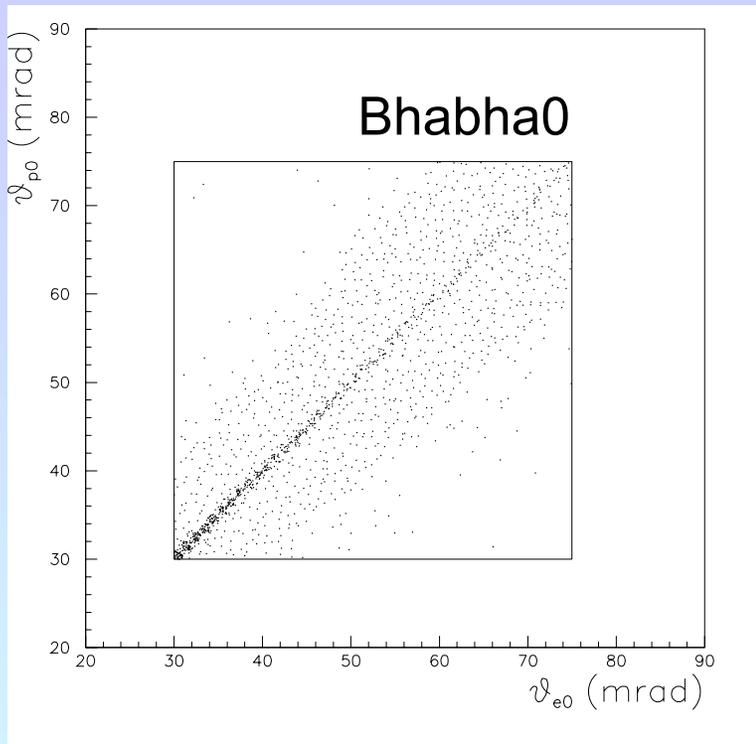
Due to modification of final state = EM deflections: $(-0.65 \pm 0.02)\%$

Total BHabha Suppression Effect : $(-4.41 \pm 0.05)\%$

Why is there such an important BHSE ?

Reduction of Bhabha counting rate

Angular cuts optimization



Beamstrahlung → enhancement of acollinearity:

$$\langle \Delta\theta_0 \rangle = 1.27 \text{ mrad}$$

$$\langle \Delta\theta_1 \rangle = 2.00 \text{ mrad}$$

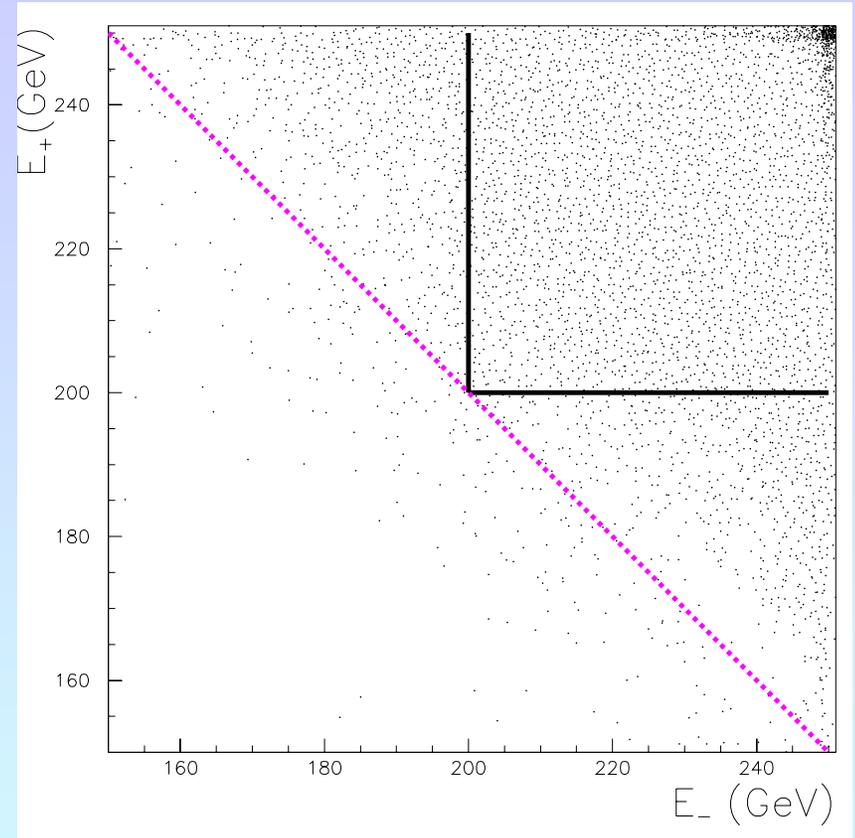
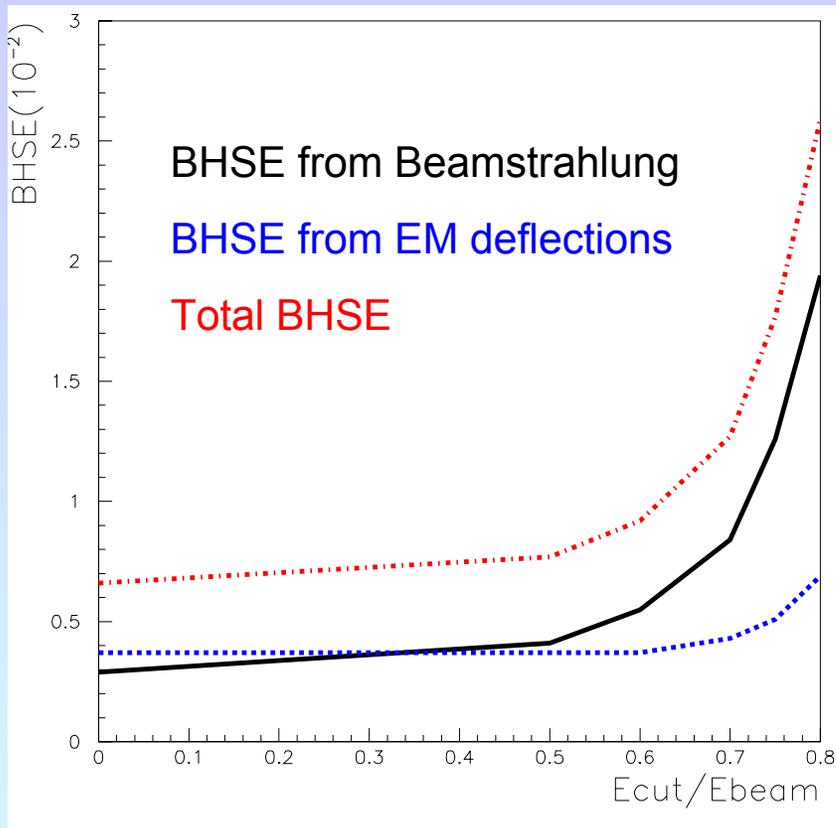
The angular cut should not be symmetric: new **asymmetrical** cuts

$$30 \text{ mrad} < \theta_{-+} < 75 \text{ mrad} \ \& \ 26.2 \text{ mrad} < \theta_{+-} < 82 \text{ mrad}$$

ref. A. Stahl LC-DET-2005-004

Reduction of Bhabha counting rate

Energy cuts optimization



Beamstrahlung & EM deflections: Bhabha energy reduction + energy asymmetry enhancement → use global energy cut: $E_+ + E_- > 0.8\sqrt{s}$

Consequences on integrated luminosity measurement:

Reduction of Bhabha counting rate

Suppression of Bhabha particles inside the selection cuts $30 < \theta_{\text{bhabha}} < 75$ mrad and $E_{\text{bhabha}} > 0.8 E_{\text{beam}}$:

Due to modification of initial state = beamstrahlung: $(-3.78 \pm 0.04)\%$

Due to modification of final state = EM deflections: $(-0.65 \pm 0.02)\%$

Total BHabha Suppression Effect : $(-4.41 \pm 0.05)\%$

Suppression of Bhabha particles inside the optimized selection cuts

$30 \text{ mrad} < \theta_{1,2} < 75 \text{ mrad}$ & $26.2 \text{ mrad} < \theta_{2,1} < 82 \text{ mrad}$ and $E_+ + E_- > 0.8 \sqrt{s}$:

Due to modification of initial state = beamstrahlung: $(-1.03 \pm 0.04)\%$

Due to modification of final state = EM deflections: $(-0.48 \pm 0.02)\%$

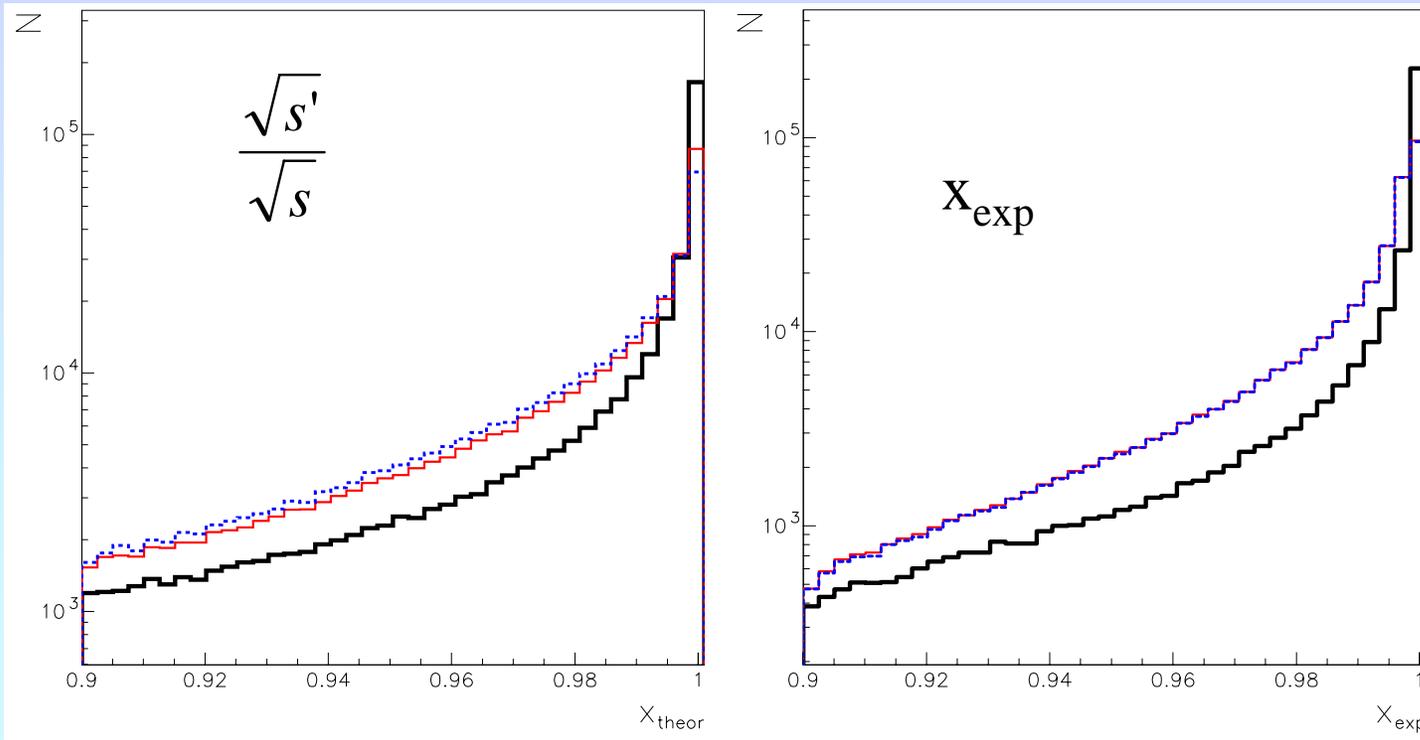
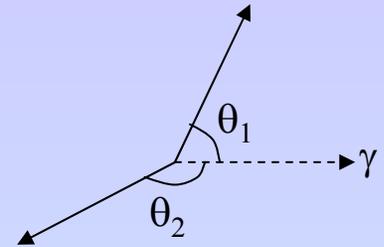
Total BHabha Suppression Effect : $(-1.51 \pm 0.05)\%$

→ The bias on integrated luminosity measurement is reduced about a factor 3 with asymmetric angular cuts and global energy cut

Reconstruction of luminosity spectrum from lumical - 1

from K. Mönig ref. LC-PHSM-2000-60-TESLA

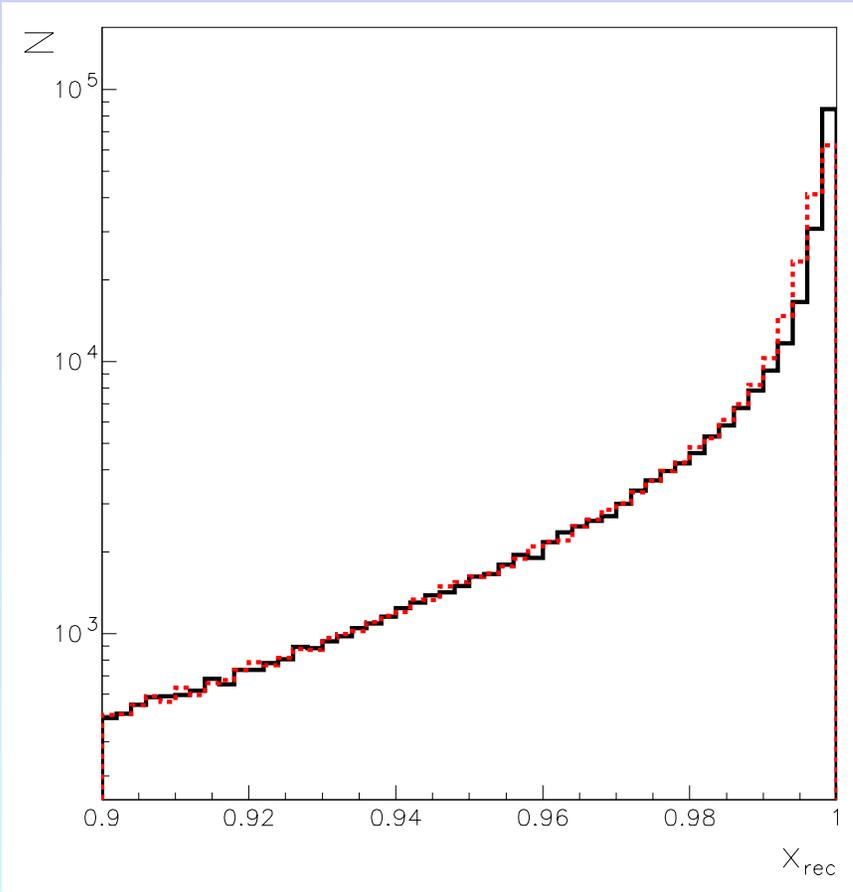
$$x_{theor} = \frac{\sqrt{s'}}{\sqrt{s}} \approx \sqrt{1 - 2 \frac{\sin(\theta_1 + \theta_2)}{\sin(\theta_1 + \theta_2) - \sin \theta_1 - \sin \theta_2}} = x_{exp}$$



ISR
 ISR+BS
 ISR+BS+EMdef

Experimentally EM deflections have no impact on the reconstructed lumi spectrum

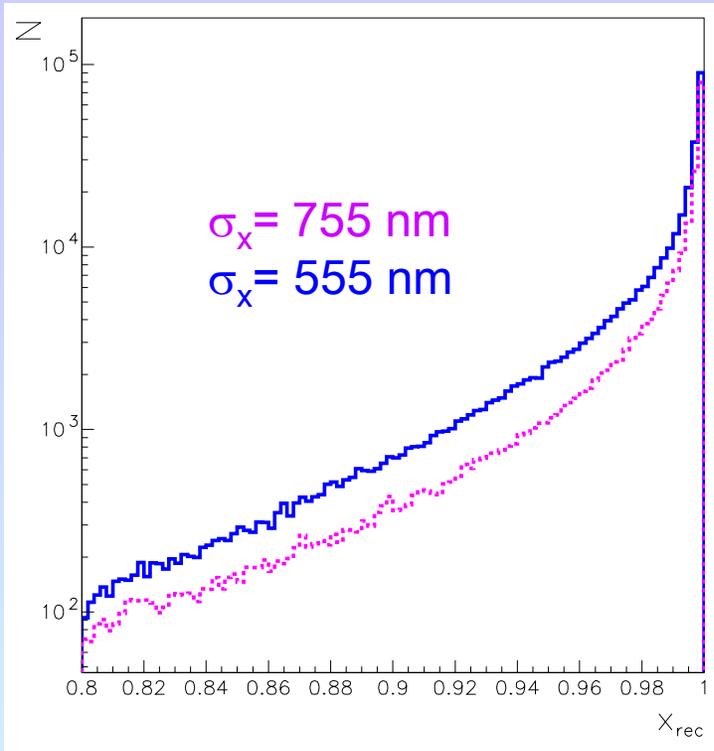
Reconstruction of luminosity spectrum from lumical - 2



reconstructed lumi spectrum
reconstructed lumi spectrum with error on
angular reconstruction: $\sigma_\theta = 0.13$ mrad

Experimental angle resolution $\rightarrow \Delta \langle x_{\text{rec}} \rangle / \langle x_{\text{rec}} \rangle \approx 5 \cdot 10^{-4}$

Required reconstruction accuracy to control the BHSE

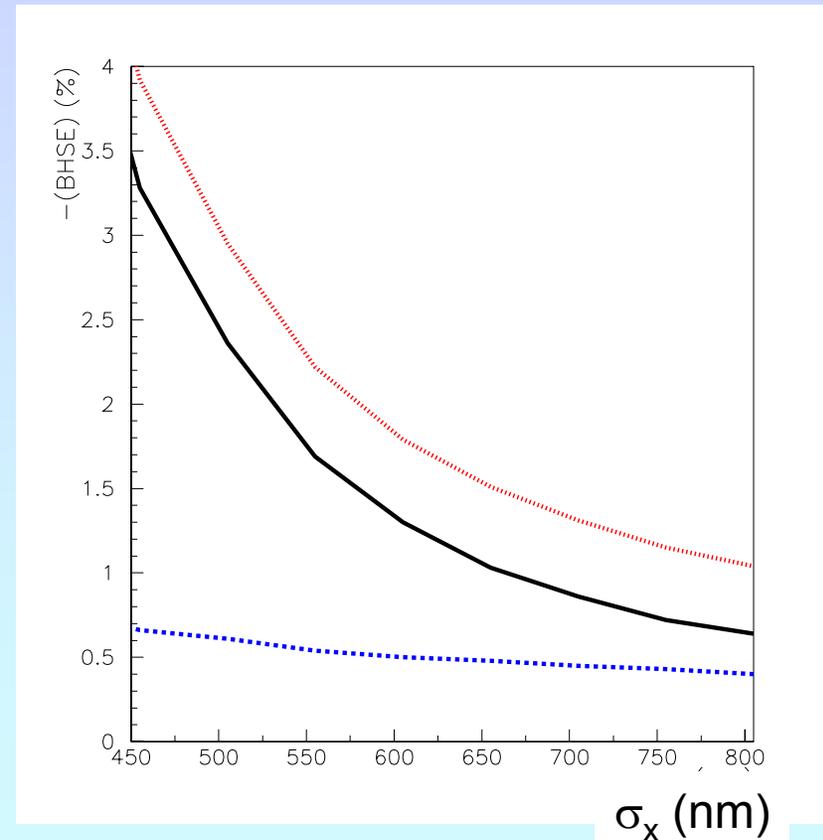
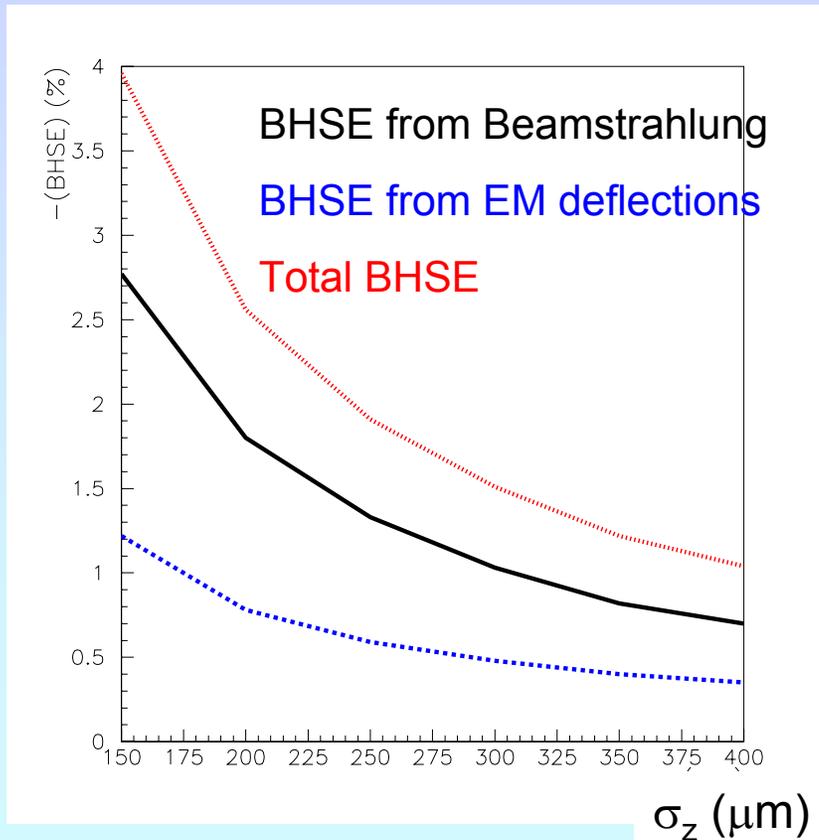


σ_x [nm]	\mathcal{L} [μb^{-1}]	$\langle X_{\text{rec}} \rangle$	BHSE [%]
555	1.8	0.976	-2.22
755	1.2	0.980	-1.14
Δ		$4 \cdot 10^{-3}$	$1 \cdot 10^{-2}$

- Modification of beamstrahlung with beam parameters
 - modification in luminosity spectrum and mean value
 - modification in BHSE
- To control the bias on integrated lumi at 10^{-3} , variations in the rec lumi spectrum need to be known with a precision of $4 \cdot 10^{-4}$
- Fitting the shapes of the lumi spectra → improvement of sensitivity to beam parameter variation

Sensitivity of BHSE to beam parameters

- BHSE is insensitive to beam offsets, Δ_x and Δ_y , and to longitudinal shifts of the bunch waist
- BHSE is insensitive to the vertical size of the bunch
- BHSE has strong dependence on bunch length, σ_z , and horizontal size, σ_x

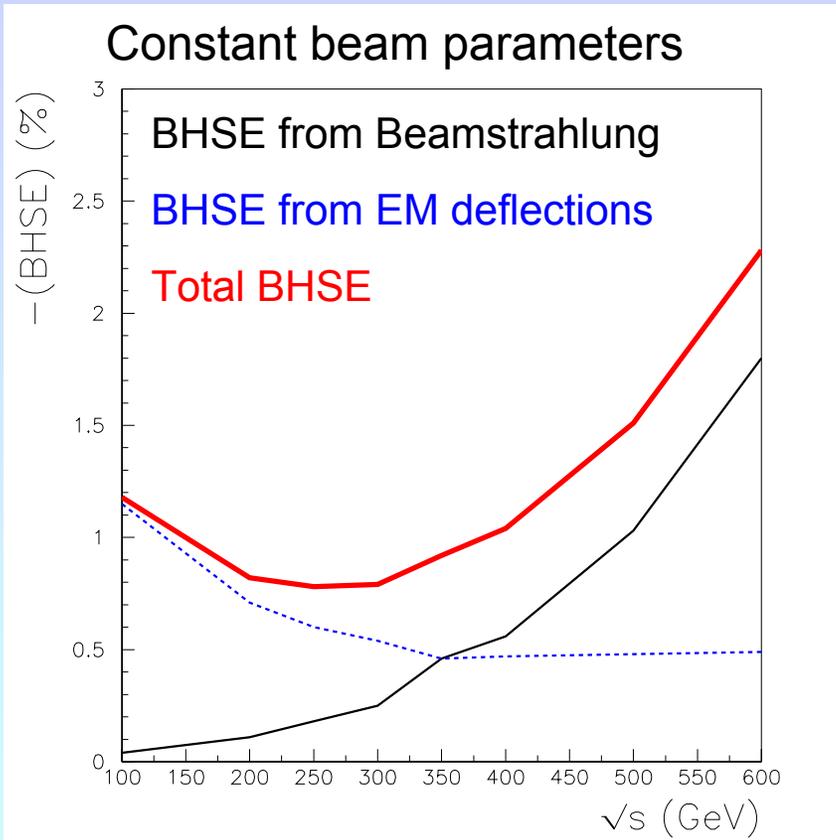


Sensitivity of BHSE to beam sizes

$\frac{\Delta\sigma_z}{\sigma_z}$	$\Delta BHSE_{b\text{slung}}[\%]$	$\Delta BHSE_{EM\text{def}}[\%]$	$\Delta BHSE[\%]$
20%	-0.40 +0.25	-0.15 +0.10	-0.50 +0.30
10%	-0.20 +0.15	-0.07 +0.05	-0.25 +0.15
5%	-0.10 +0.05	-0.03 +0.02	-0.15 +0.05
$\frac{\Delta\sigma_x}{\sigma_x}$	$\Delta BHSE_{b\text{slung}}[\%]$	$\Delta BHSE_{EM\text{def}}[\%]$	$\Delta BHSE[\%]$
20%	-1.10 +0.35	-0.10 +0.08	-1.20 +0.40
10%	-0.40 +0.20	-0.04 +0.04	-0.45 +0.25
5%	-0.20 +0.10	-0.02 +0.02	-0.20 +0.10

Sensitivity of BHSE to energy

ILC should enable physics runs initially for energies from the Z boson mass to 500 GeV
 → In this energy range beam-beam effects are strongly modified



Relative Energy lost by Beamstrahlung :

$$\delta \propto \frac{N^2 \gamma}{\sigma_x^2 \sigma_z} \propto \frac{N^2 \gamma^2}{\epsilon_x^* \beta_x \sigma_z}$$

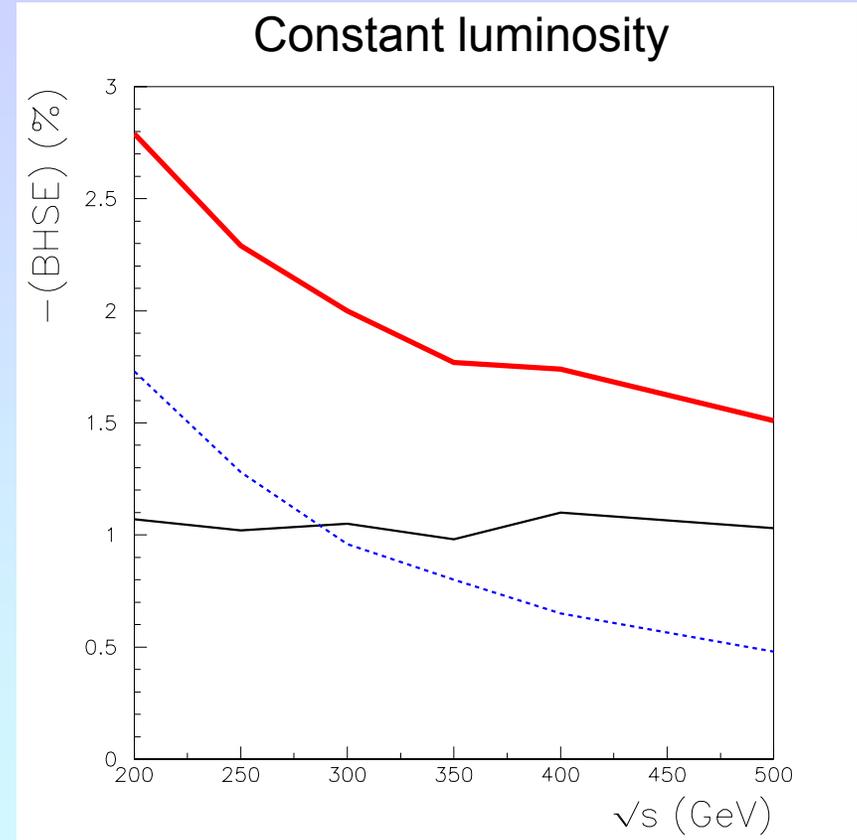
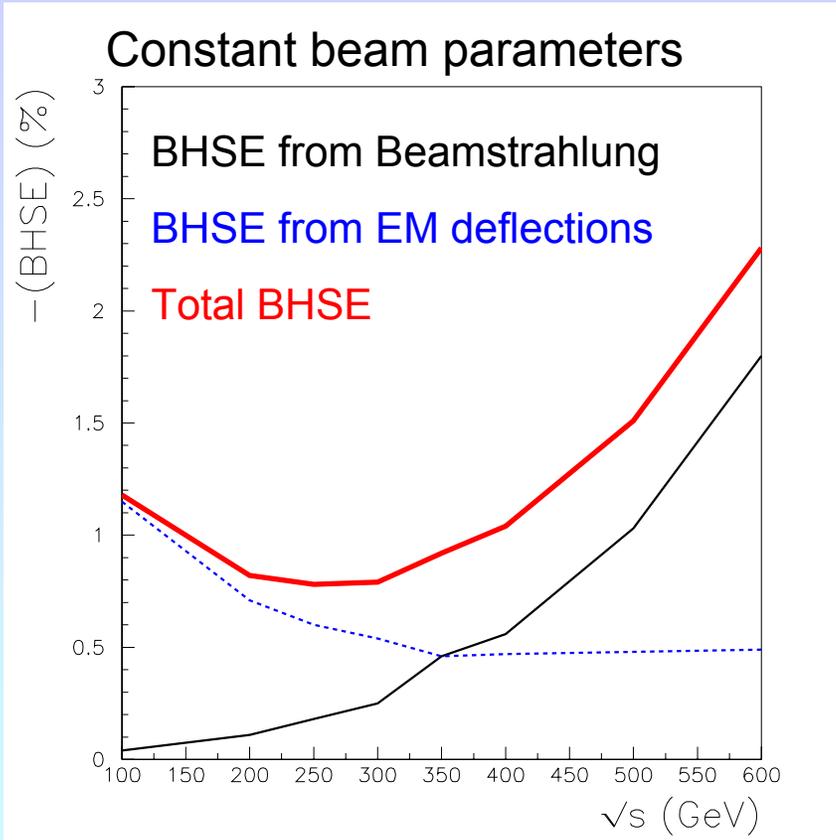
$$\mathcal{L} = \frac{N^2}{4\pi \sigma_x \sigma_y} H_D = \frac{N^2 \gamma}{4\pi \sqrt{\epsilon_x^* \beta_x \epsilon_y^* \beta_y}} H_D$$

$$\mathcal{L} \propto \sqrt{\frac{\delta}{\epsilon_y}} \frac{P_{beam}}{E} H_D$$

At low energy, EM contribution of BHSE becomes dominant

Sensitivity of BHSE to energy

ILC should enable physics runs initially for energies from the Z boson mass to 500 GeV
→ In this energy range beam-beam effects are strongly modified



At low energy, EM contribution of BHSE becomes dominant, reaching few $100 \cdot 10^{-4}$

Summary & Conclusions - 1

- Beam-beam effects on Bhabha scattering increase acollinearity (+0.7 mrad) and energy asymmetry on the Bhabha particles → Need to find a compromise with background suppression cuts
- This leads to a **bias on the integrated luminosity measurement of few 10^{-2}**
- This BHSE mainly arises from beamstrahlung (for Nominal ILC)
- The reconstructed luminosity spectrum in the LumiCal is almost not modified by EM deflections → beamstrahlung can be measured from the lumi spectrum reconstruction
- Angular resolution induces a relative error of $5 \cdot 10^{-4}$ in the Luminosity spectrum reconstruction
- To control the bias on luminosity measurement at 10^{-3} , we would need to reconstruct luminosity spectrum mean value with a precision of $4 \cdot 10^{-4}$. But a fitting procedure of the lumi spectrum would enable to reach better precision.

Summary & Conclusions - 2

- Main dependences are from the horizontal and longitudinal sizes of the bunch. A precision of 20% is needed on their knowledge to limit the error on BHSE from EM deflections to about 10^{-3} .
- No direct way to control experimentally the bias from EM deflections → Need to use a simulation tool as GUINEA-PIG for further studies.
<http://flc.web.lal.in2p3.fr/mdi/BBSIM/bbsim.html>
- For the GigaZ option, a precision of 10^{-4} is needed for the luminosity, while the bias from EM deflections is $>100 \times 10^{-4}$... → need more complete studies.
- “Impact of beam-beam effects on precision luminosity measurements at ILC”, C. Rimbault, P. Bambade, K. Mönig, D. Schulte, EuroTeV-Report-2007-017. To be published.