

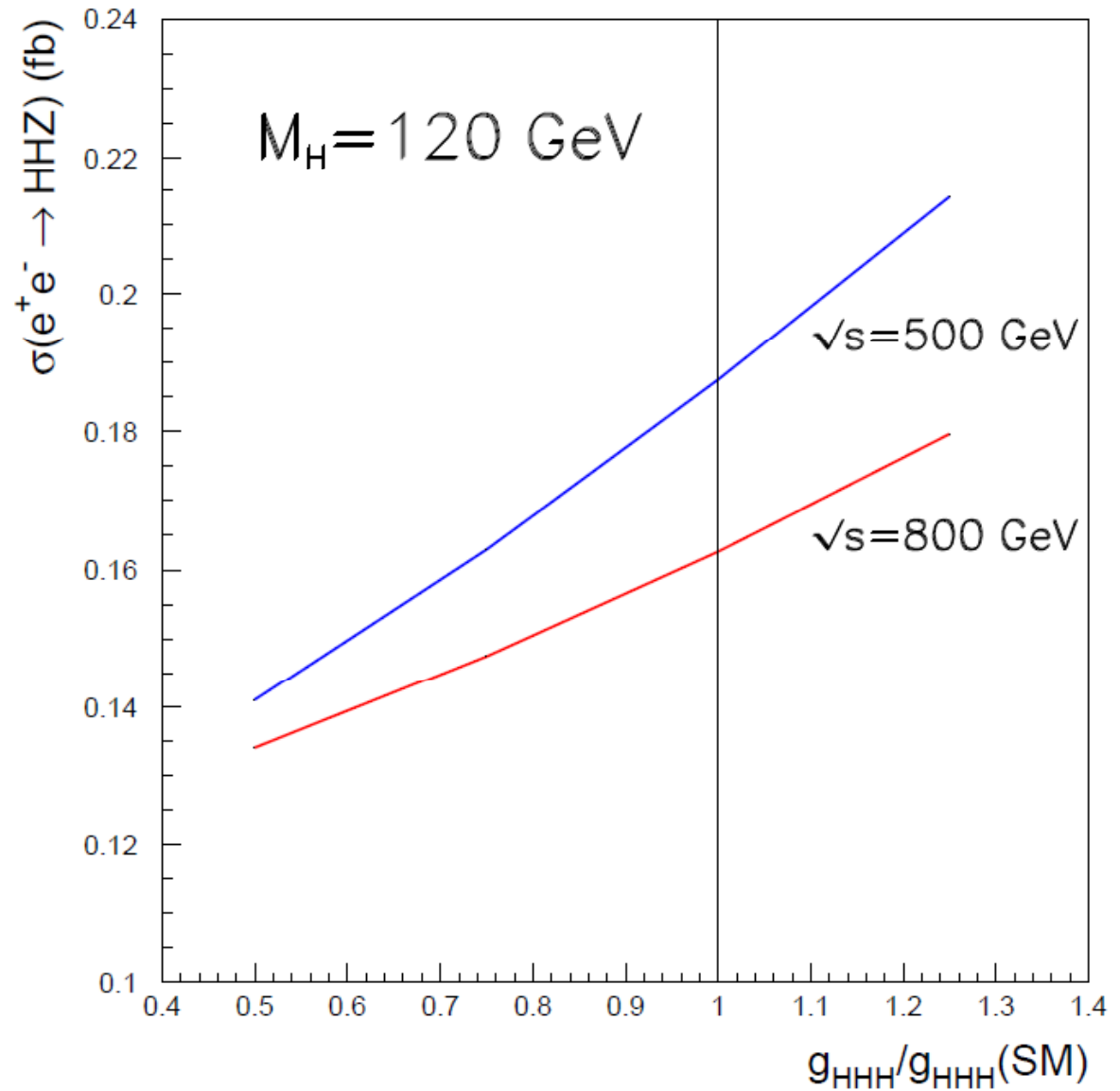
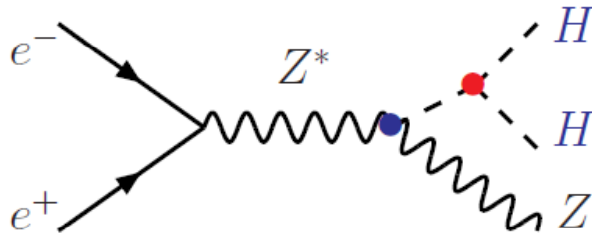
Higgs Self Coupling Measurement

Tim Barklow

SLAC

June 1, 2007

$$e^+e^- \rightarrow ZHH \rightarrow q\bar{q}b\bar{b}b\bar{b}$$



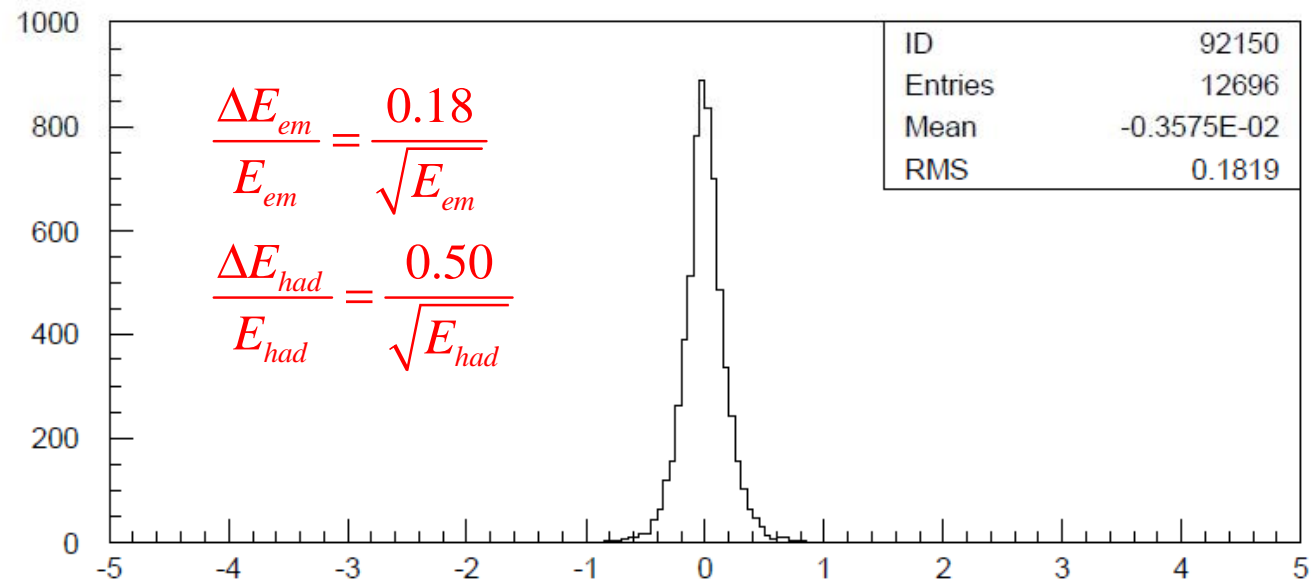
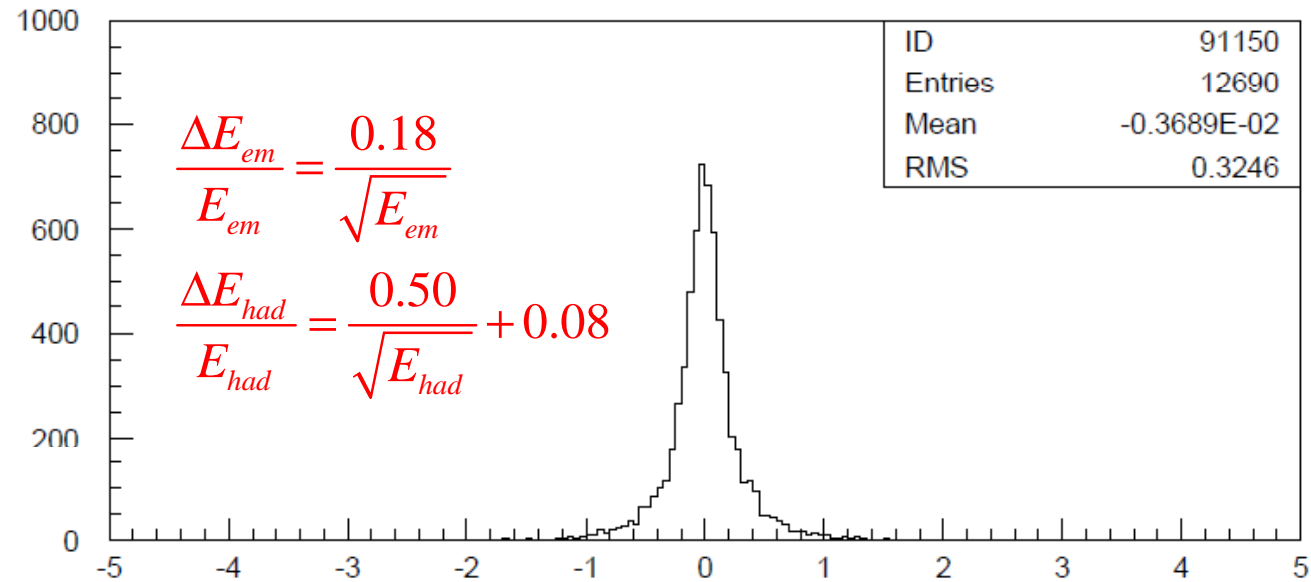
Plan for Analysis

- Perform analysis on qqbbbb channel only at $E_{\text{cm}}=500$ GeV assuming 0% electron polarization. Use org.lcsim Fast MC simulation of baseline SiD. This MC includes a reasonable algorithm for smearing charged track angles, curvature and impact parameters. Calorimeter simulation consists of simple single neutral particle smearing with EM resolution for photons and HAD res for n, $K0_L$.
- Scale single particle calorimeter resolutions to get a particular ΔE_{jet} .
- Use org.lcsim ZVTOP for b-tagging
- Perform analysis both with and without final state gluon radiation in signal and background evt generators.

$$\sqrt{s} = 500 \text{ GeV}$$

$$e^+ e^- \rightarrow u\bar{u}$$

E_{true} is adjusted
for neutrinos and
particles outside
detector acceptance



$$\Delta E_{jet} = (E_{rec} - E_{true}) / \sqrt{E_{true}}$$

Drop constant term in single particle resolution for now. Assume negligible contribution from charged particles to jet energy resolution and write

$$\sigma^2 = (1 + \lambda(1 - r))A_\gamma^2 w_\gamma E_{jet} + (1 + \lambda r)A_h^2 w_h E_{jet} = c^2 E_{jet}$$

where $c = 0.3, 0.4, 0.5, 0.6$

$r =$ hadronic resolution degradation fraction

($r = 1$ to only degrade hadronic resolution

$r = 0$ to only degrade em resolution)

$$A_\gamma = 0.18 \quad A_h = 0.50 \quad w_\gamma = 0.28 \quad w_h = 0.10$$

Given a desired jet energy resolution c the parameter λ is given by

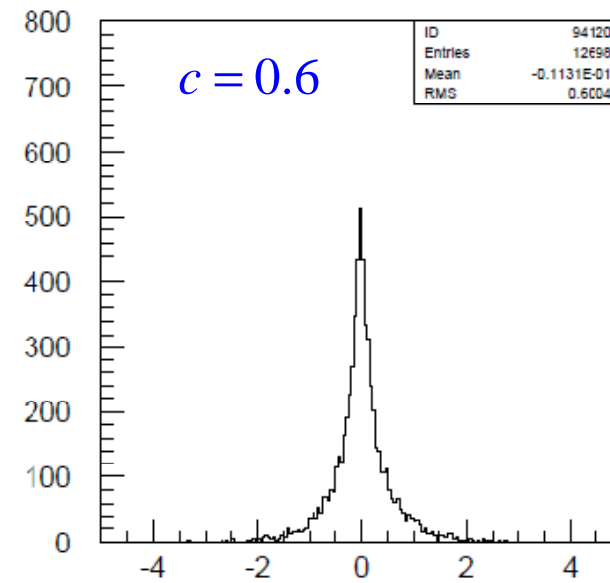
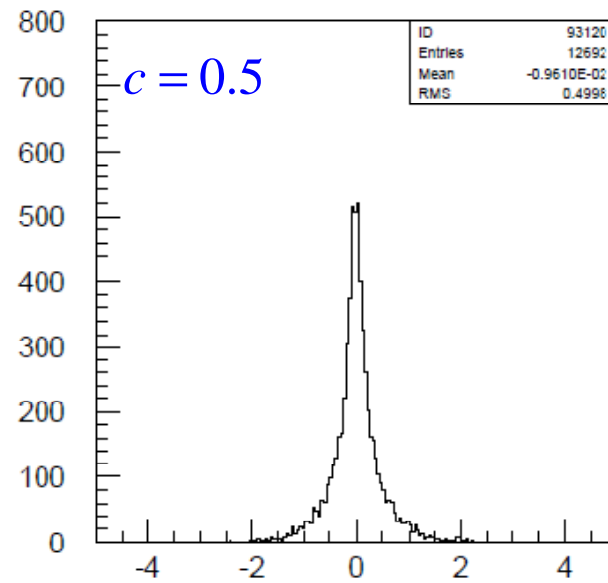
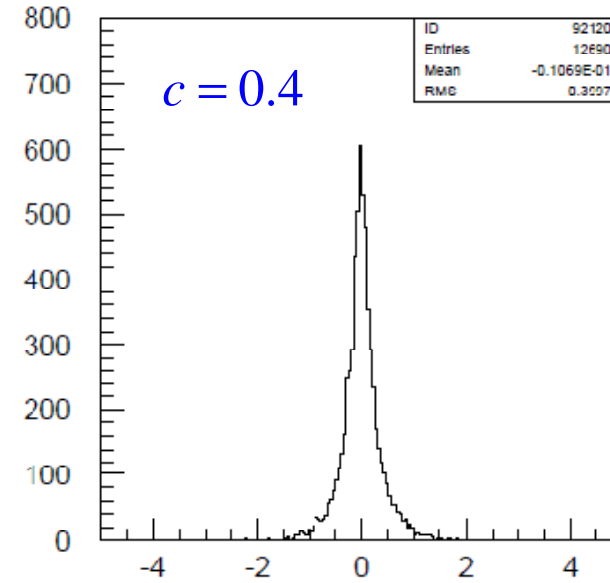
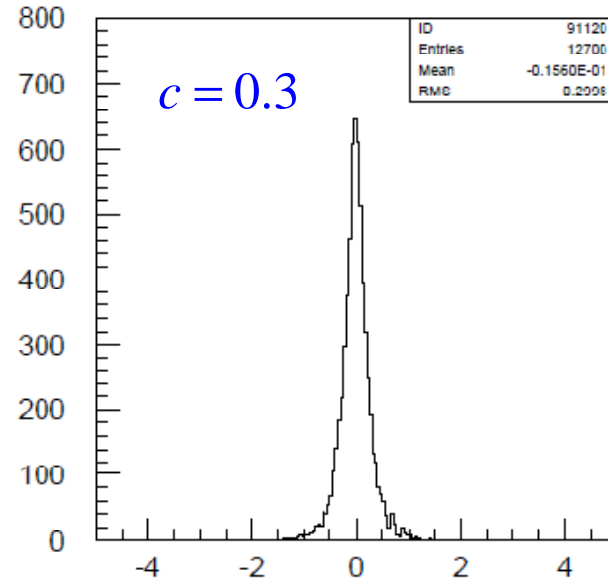
$$\lambda = \frac{c^2 - A_\gamma^2 w_\gamma - A_h^2 w_h}{(1 - r)A_\gamma^2 w_\gamma + rA_h^2 w_h}$$

$$e^+e^- \rightarrow u\bar{u}$$

$$\sqrt{s} = 500 \text{ GeV}$$

$$r = 1.0$$

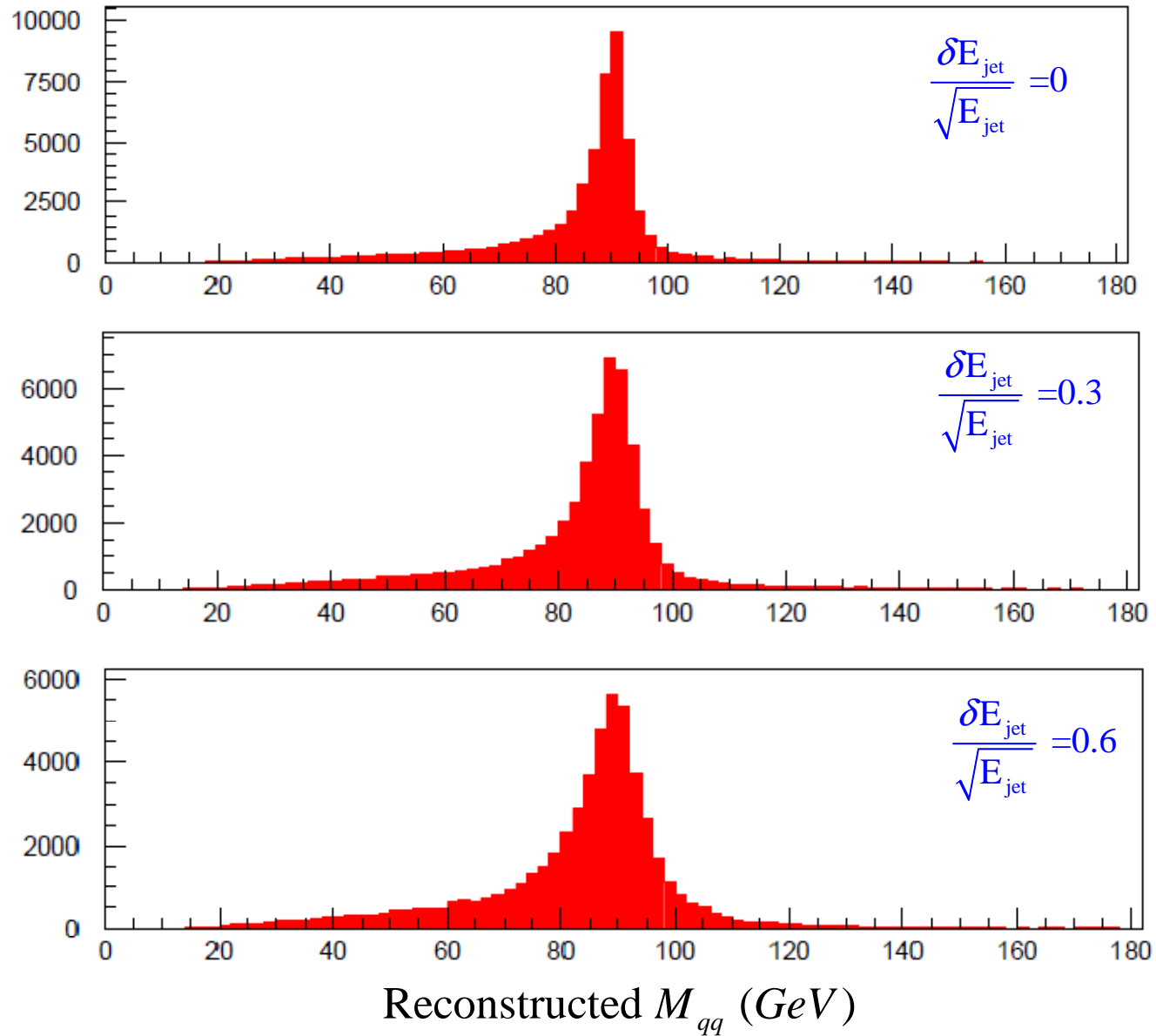
(only degrade
had resolution)



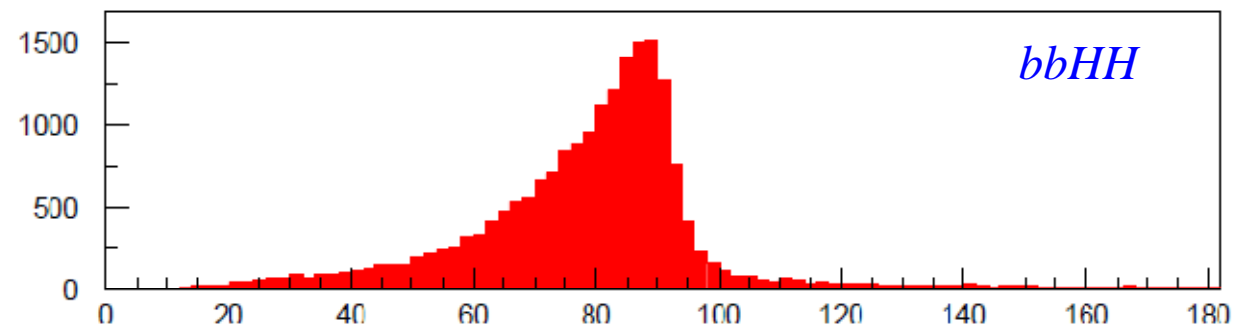
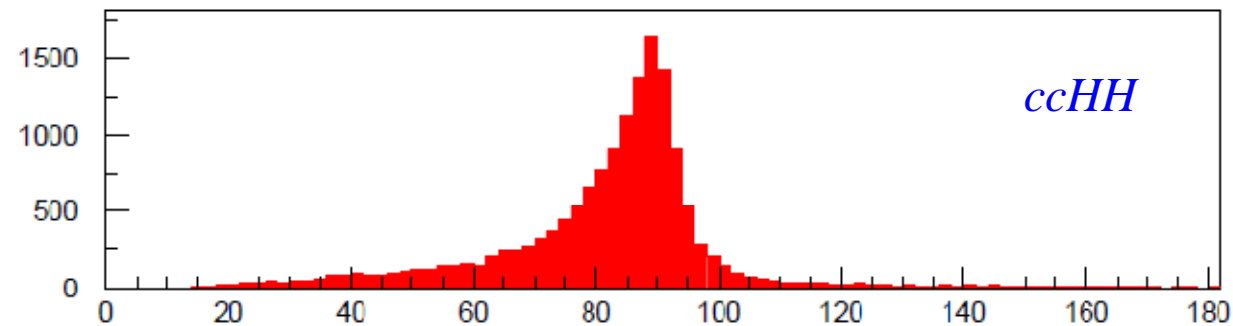
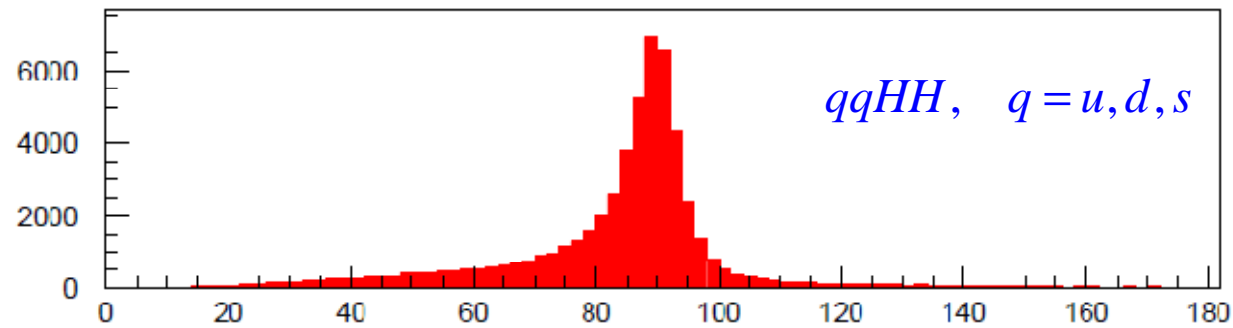
$$\Delta E_{jet} = (E_{rec} - E_{true}) / \sqrt{E_{true}}$$

$$\Delta E_{jet} = (E_{rec} - E_{true}) / \sqrt{E_{true}}$$

$e^+e^- \rightarrow qqHH$, $q = u, d, s$ non-Gaussian Parameterization



$$e^+e^- \rightarrow qqHH, \quad \frac{\delta E_{\text{jet}}}{\sqrt{E_{\text{jet}}}} = 0.3, \quad \text{non-Gaussian Parameterization}$$



Reconstructed M_{qq} (GeV)

ZHH Preselection

Require:

$$|\cos \theta_{thrust}| < 0.95$$

$$thrust < 0.85$$

$$P_{tot}(z) < 50 \text{ GeV}$$

$$M_{thrust_hemisphere} > 110 \text{ GeV for at least 1 thrust hemisphere}$$

$$N_{isolated\ leptons} = 0$$

$$6 \leq N_{jets} \leq 8$$

$$N_{chrg\ tracks} \geq 35$$

$$E_{jet}(photons) / E_{jet}(total) < 0.8 \text{ for all 6 jets}$$

NN_{btag}

- Use udsbc jets in ZHH events to train NN_{btag}
- Perform jet analysis on charged and neutral objects allowing number of jets to vary; for each jet perform ZVTOP analysis as implemented in org.lcsim
- Use the following variables in the btag neural net:

E_{jet}

E_{vtx}

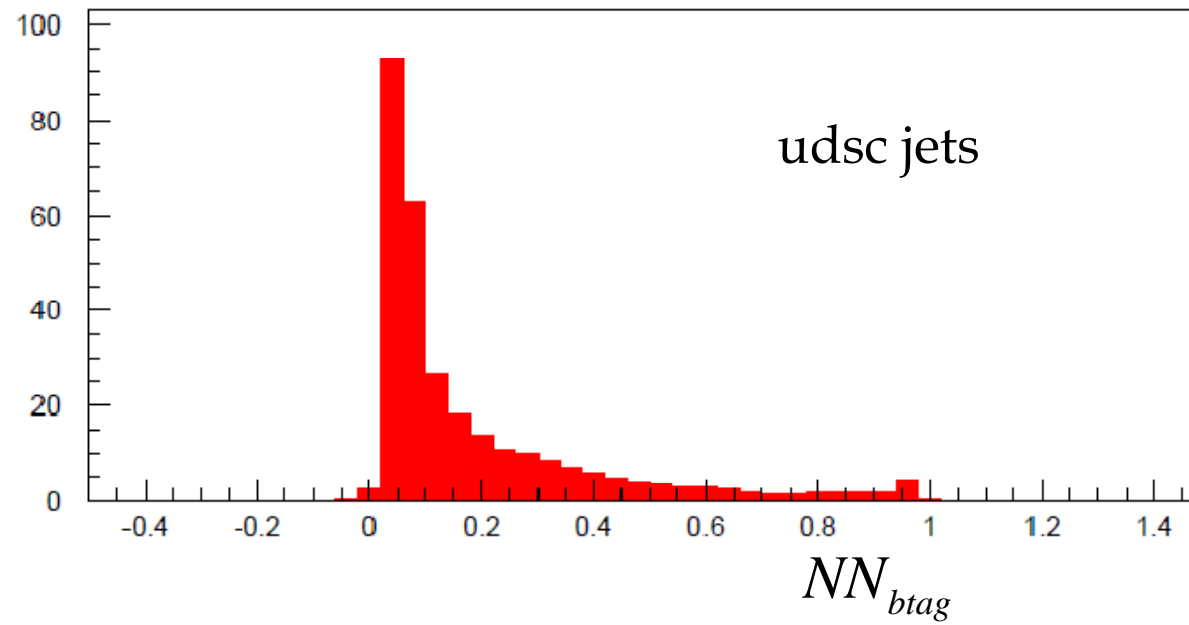
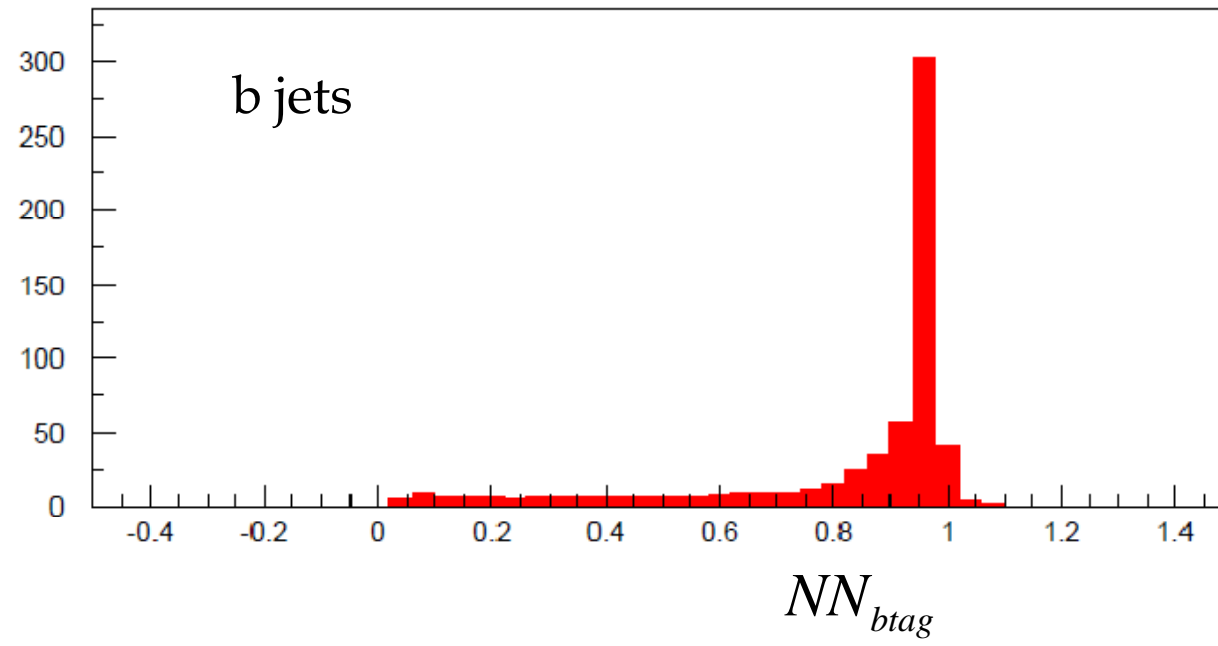
M_{vtx}

Pt-Corrected M_{vtx}

Secondary Vertices

Unassociated Large Impact Parameter Tracks

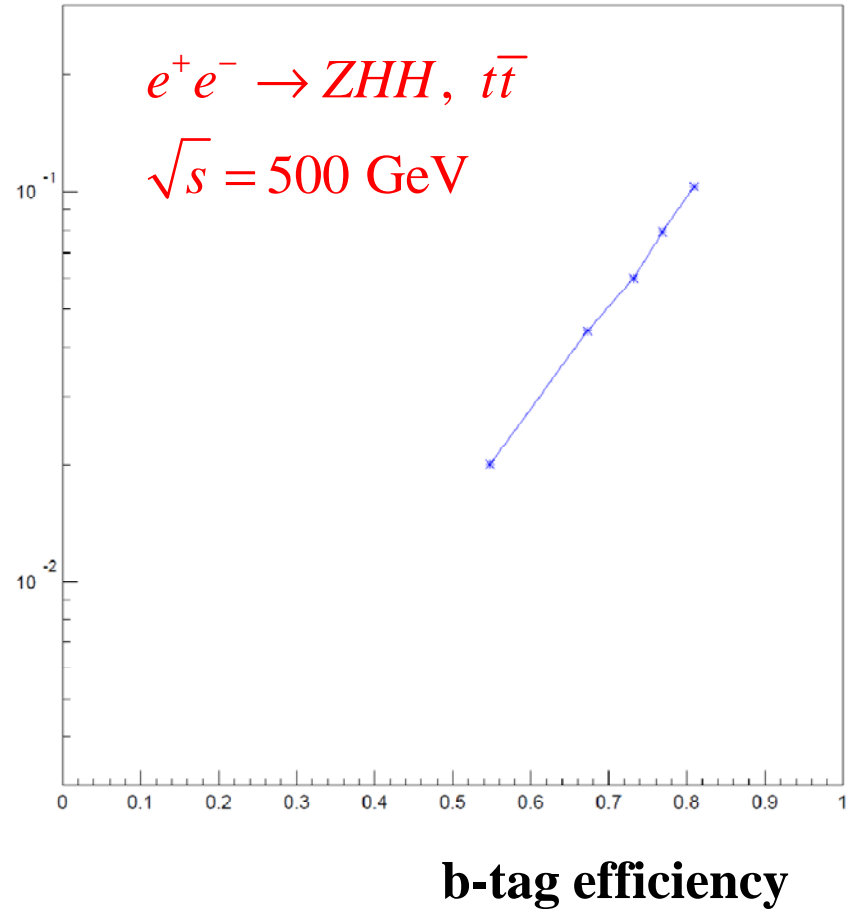
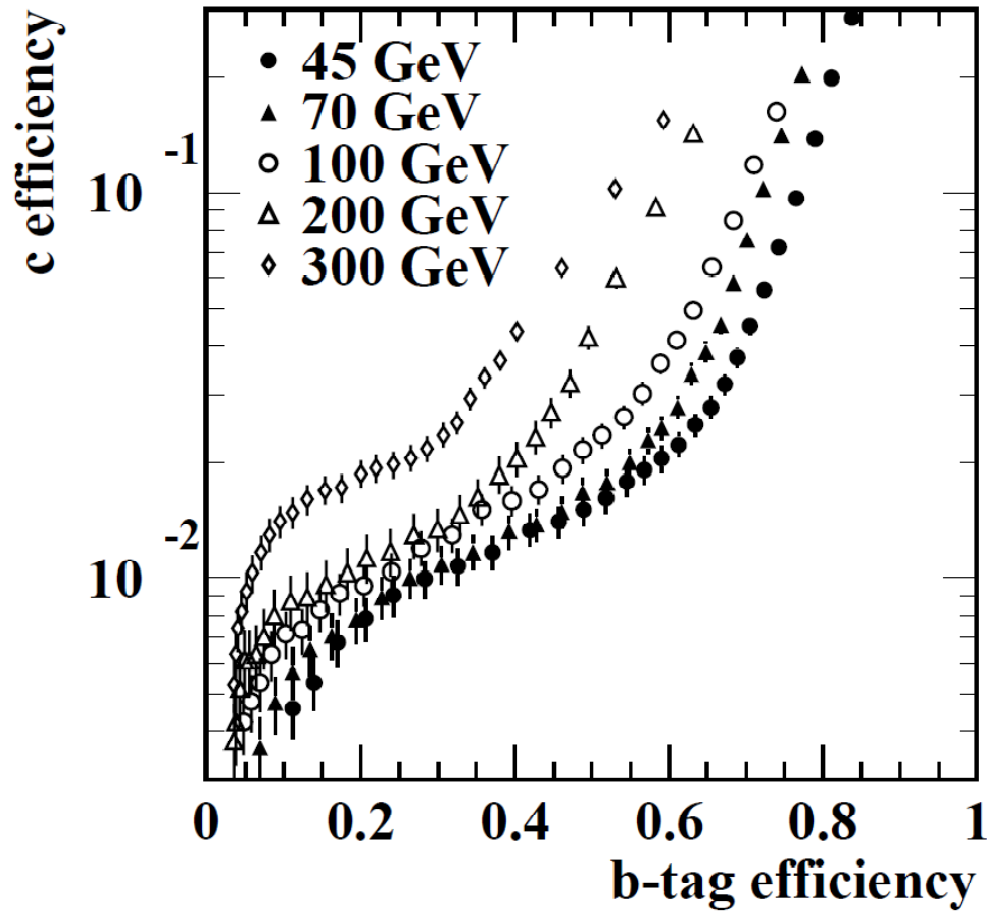
ZHH events



charm mis-id efficiency versus b-tag efficiency

R. Hawkings, LC-PHSM-2000-021

SiD ZHH Analysis



OLD Neural Net NN_{ZHH}

- Use signal and background events that pass preselection to train NN_{ZHH}
- Use the following variables in the ZHH neural net:

$$\chi_{ZHH}^2 \quad \chi_{ZHH_HHmass}^2 \quad \chi_{ZHH_ZHHmass}^2$$

$$\chi_{TT}^2 \quad \chi_{TT_WWmass}^2 \quad \chi_{TT_TTmass}^2$$

$$\chi_{ZZ}^2 \quad \chi_{ZZH_ZZHmass}^2$$

$$\chi_{ZZ}^2 \quad \chi_{ZH_ZHmass}^2$$

$$NNbtag_j, j = 1, 2, 3, 4, 5, 6$$

$$\min(M_{jet}(k), k = 1, 2, 3, 4, 5, 6)$$

$$|\cos \theta_{thrust}|$$

jets

Old definition χ_{ZHH}^2

- Force charged and neutral objects into 6 jets
- Loop over 45 jet-pair combinations & minimize χ_{ZHH}^2

$$\chi_{ZHH}^2 = \chi_{ZHH_ZHHmass}^2 + \sum_{j=3}^6 \frac{(NNbtag_j - 1)^2}{\sigma_{NNbtag}^2}$$

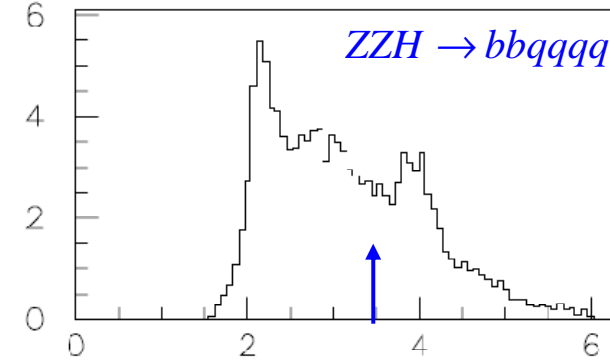
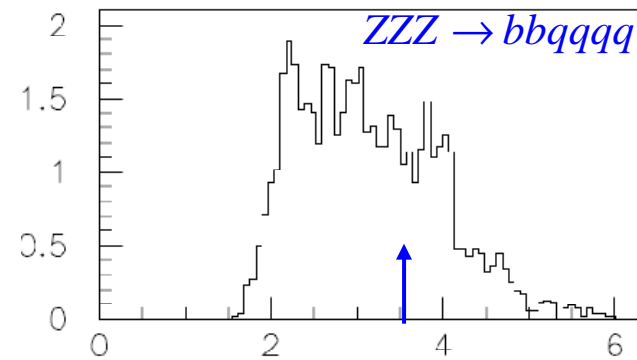
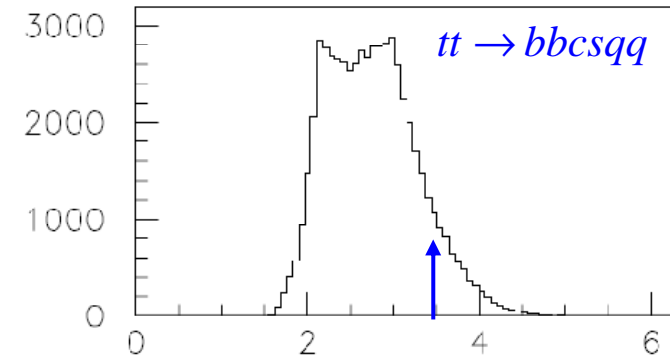
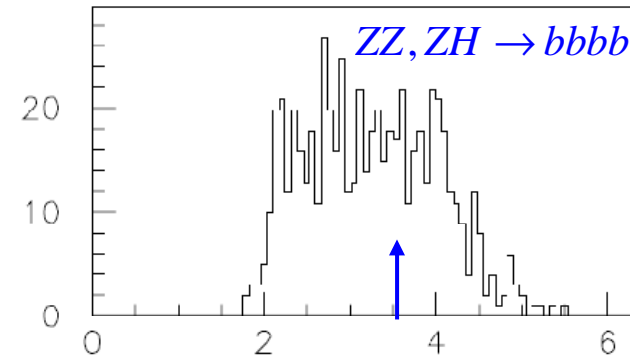
$$\chi_{ZHH_ZHHmass}^2 = \chi_{ZHH_HHmass}^2 + \frac{(M_{12} - M_Z)^2}{\sigma_{M_Z}^2}$$

$$\chi_{ZHH_HHmass}^2 = \frac{(M_{34} - M_H)^2}{\sigma_{M_H}^2} + \frac{(M_{56} - M_H)^2}{\sigma_{M_H}^2}$$

M_{ij} = Mass for jet-pair combination ij

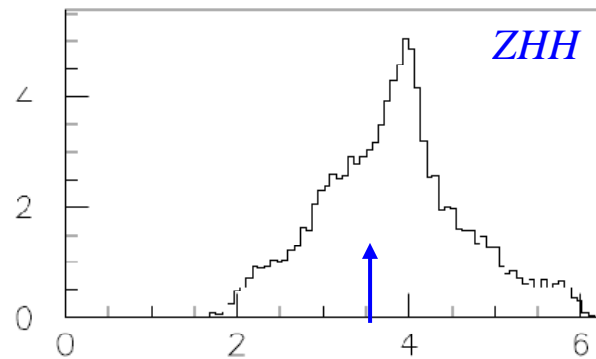
$NNbtag_j$ = btag neural net variable for jet j

New approach:
 Instead of variables
 such as χ^2_{ZH} , which
 contain kinematic info
 for 1 of 45 combinations,
 feed neural net all jet pair
 masses where jets are
 ordered according to jet
 btag neural net value
 (jet 1 is the most b-like,
 jet 2 is 2nd most b-like,
 etc.)



Require

$$\sum_{j=1}^6 NN_{btag}(j) > 3.5$$

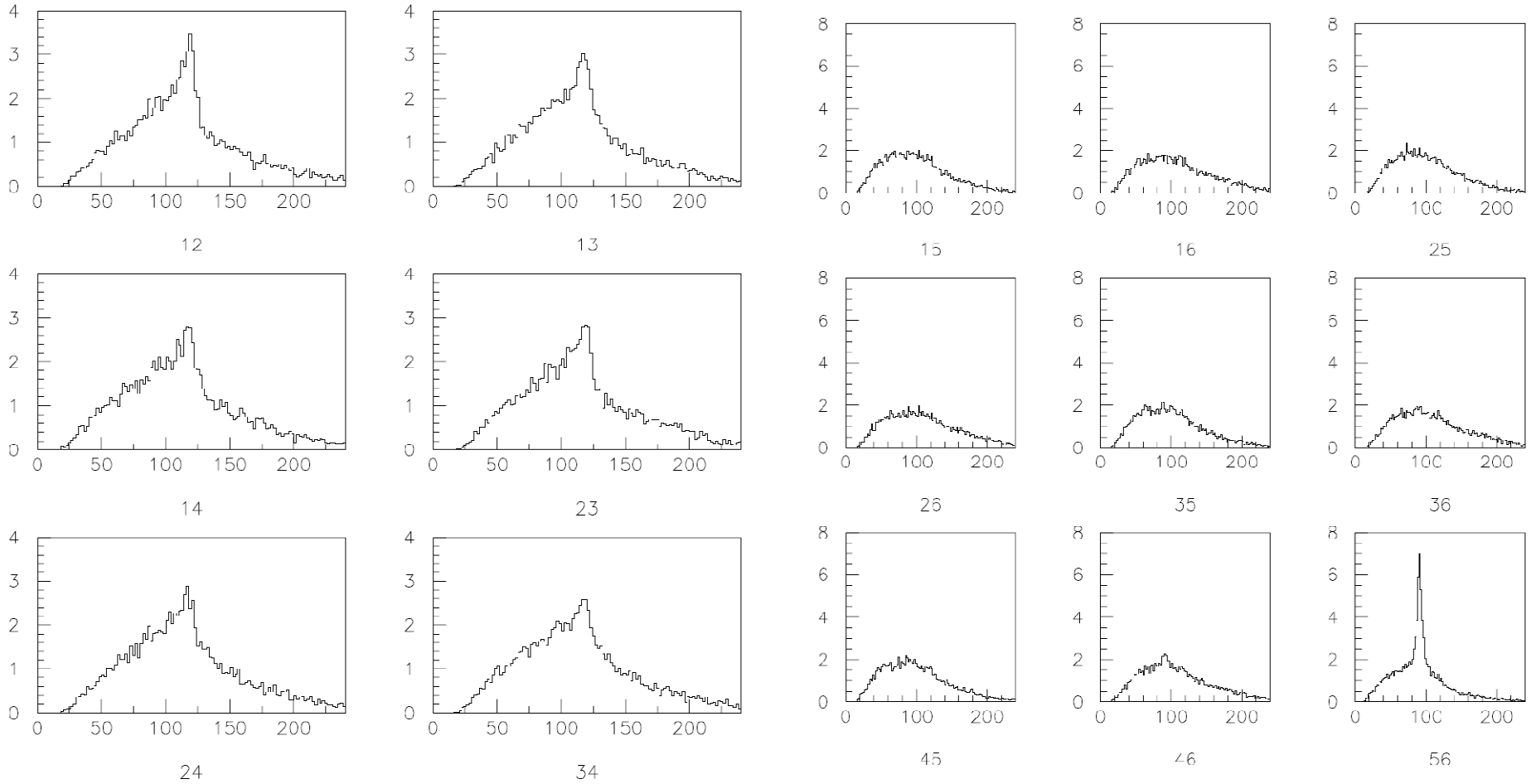


$$\sum_{j=1}^6 NN_{btag}(j)$$

Jet pair masses where jets are ordered according to jet btag neural net value

(jet 1 is the most b-like, jet 2 is 2nd most b-like, etc.) Require $\sum_{j=1}^6 NN_{btag}(j) > 3.5$

ZHH

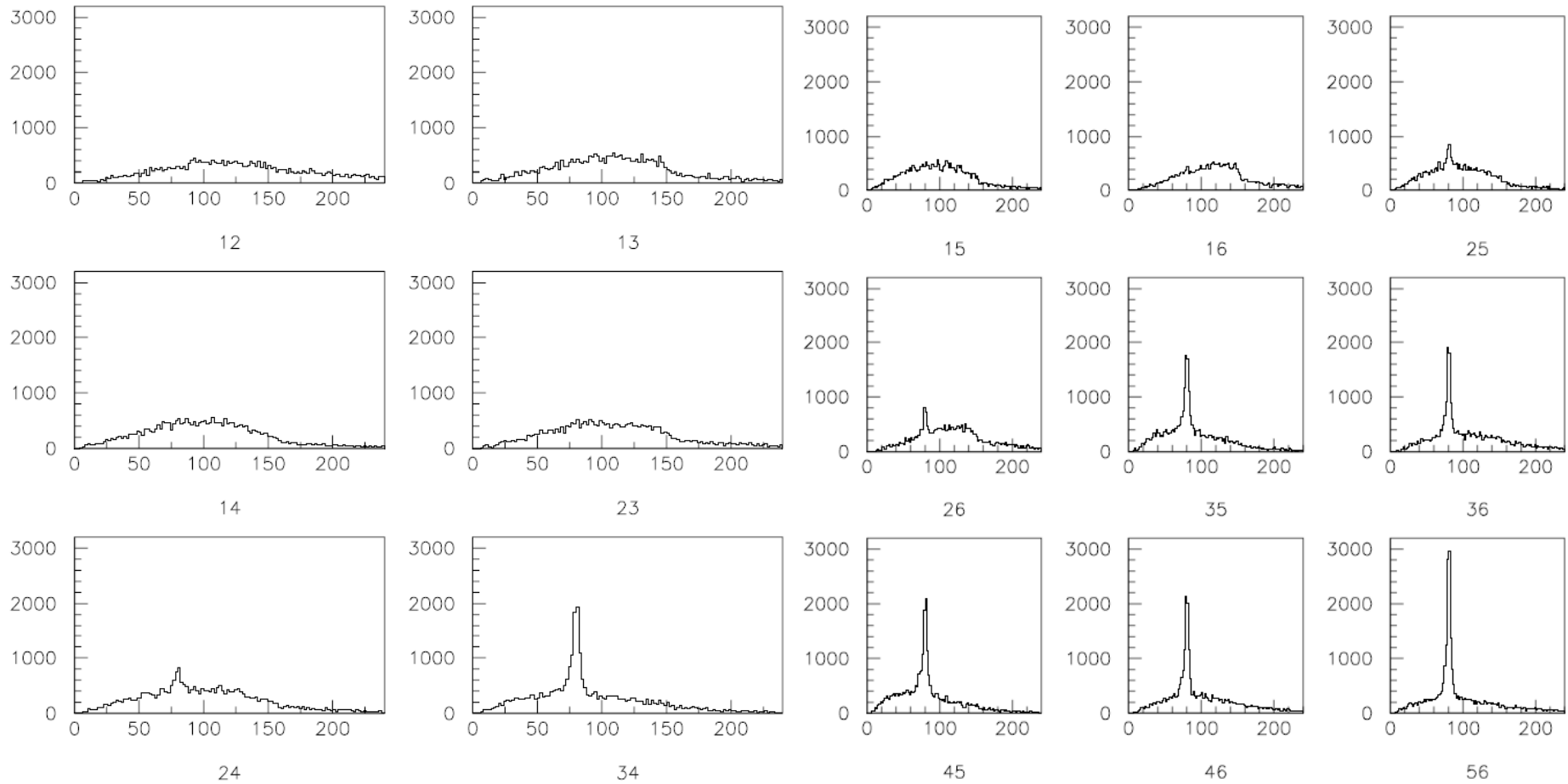


M_{jk} (GeV)

Jet pair masses where jets are ordered according to jet btag neural net value

(jet 1 is the most b-like, jet 2 is 2nd most b-like, etc.) Require $\sum_{j=1}^6 NN_{btag}(j) > 3.5$

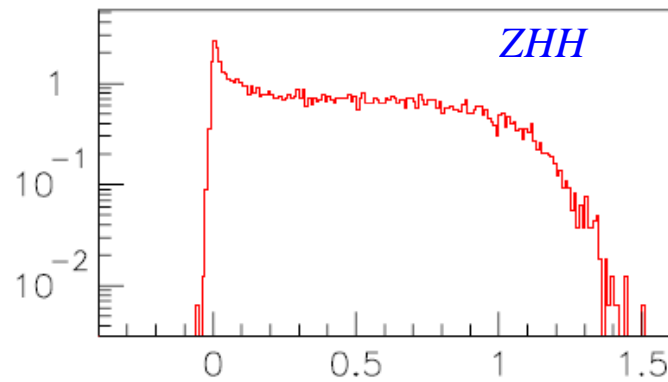
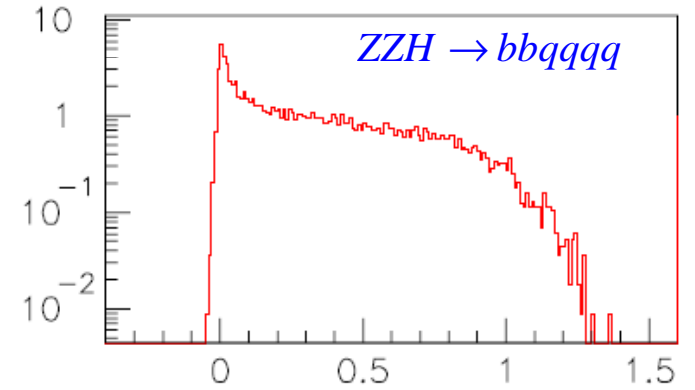
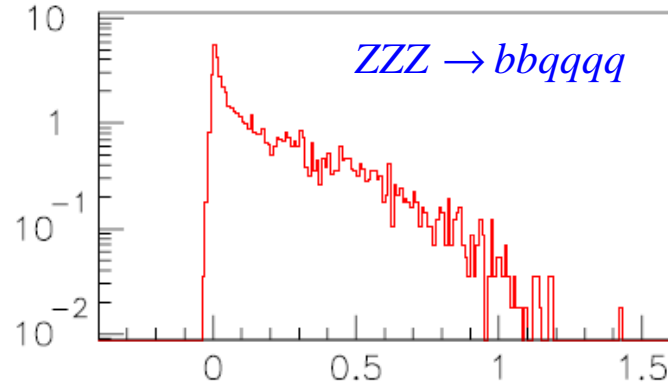
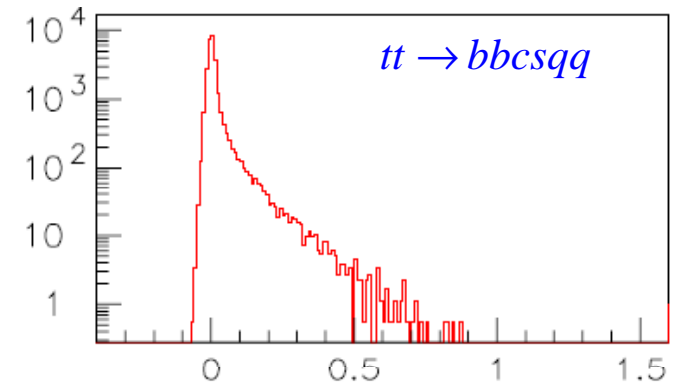
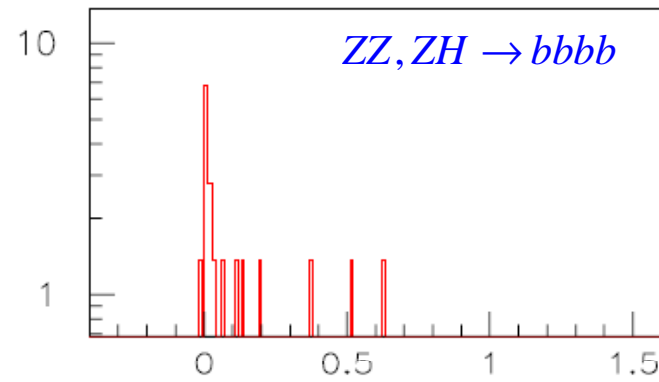
$t\bar{t}$



$M_{jk} (GeV)$

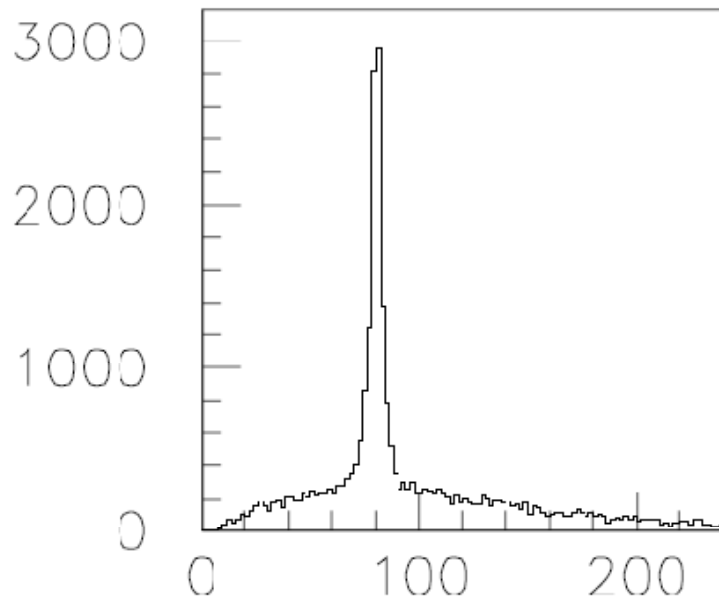
Neural net based on
 b-tag ordered jet pair
 masses and χ_{HH}^2 , χ_{tt}^2 ,
 χ_{ZZH}^2 , χ_{ZZZ}^2 (only 3
 comb. for $\chi_{HH}^2, \chi_{ZZZ}^2$
 only 6 comb. for $\chi_{tt}^2, \chi_{ZZH}^2$)

QCD rad turned off



NN_{final}

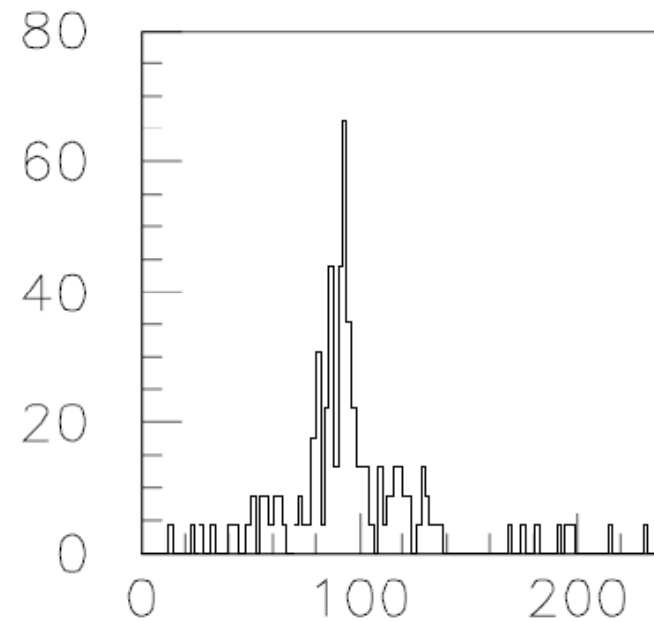
all $t\bar{t}$ with $\sum_{j=1}^6 NN_{btag}(j) > 3.5$



M_{56} (GeV)

all $t\bar{t}$ with $\sum_{j=1}^6 NN_{btag}(j) > 3.5$

and $NN_{final} > 0.1$



M_{56} (GeV)

w/o gluon rad

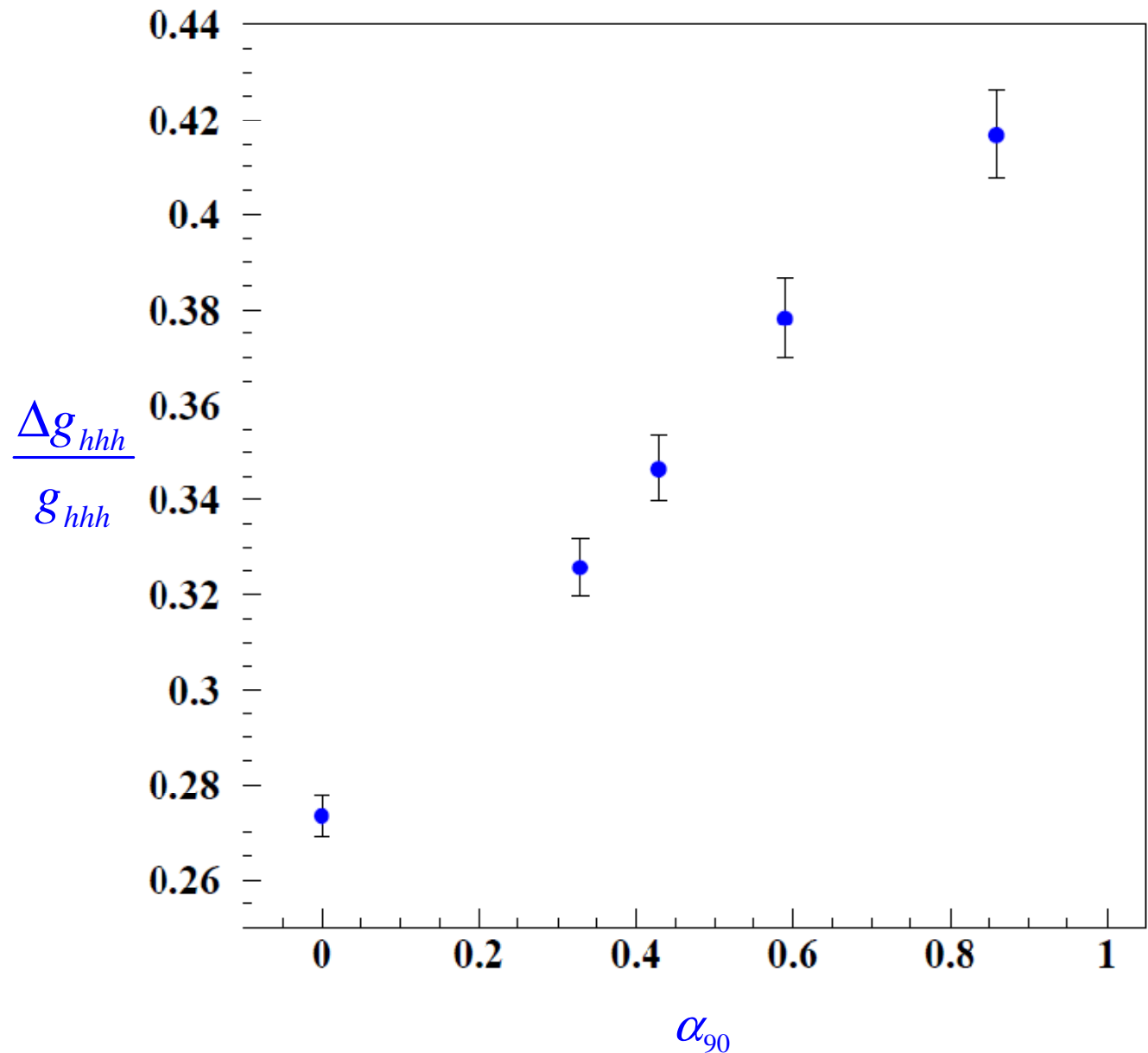
$$\text{BR}(H \rightarrow b\bar{b})=0.678$$

$$e^+e^- \rightarrow ZHH \\ \rightarrow qq\bar{b}\bar{b}$$

$$\sqrt{s} = 500 \text{ GeV}$$

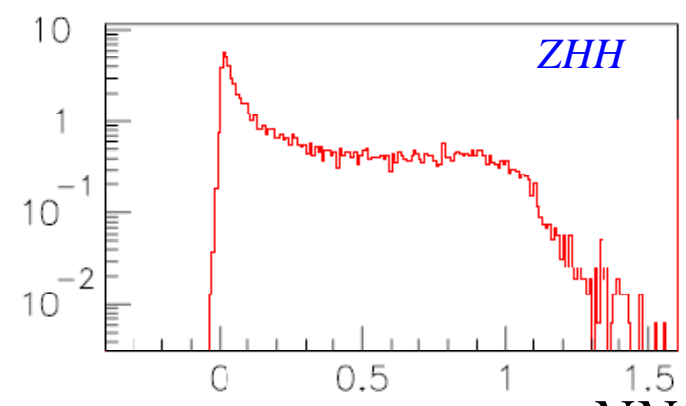
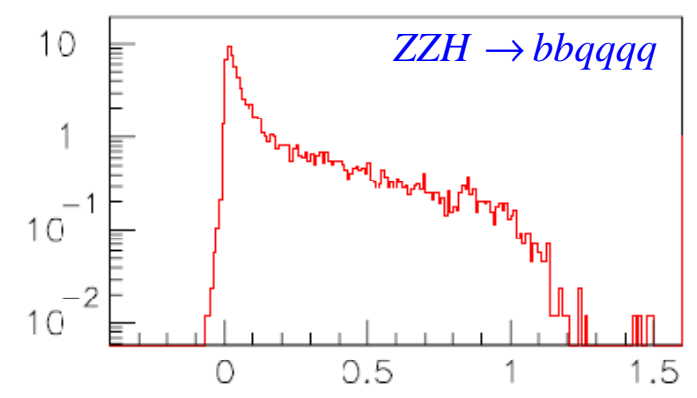
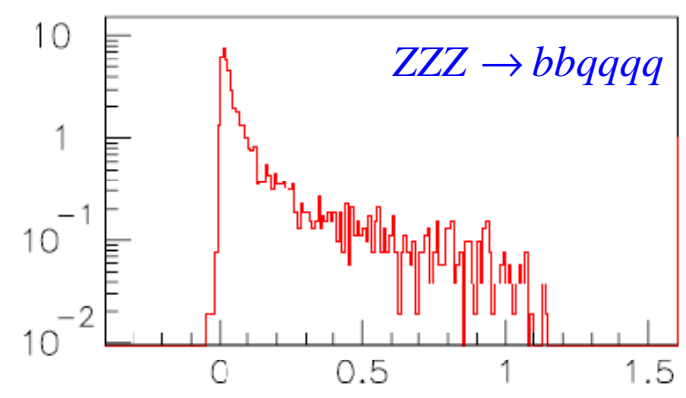
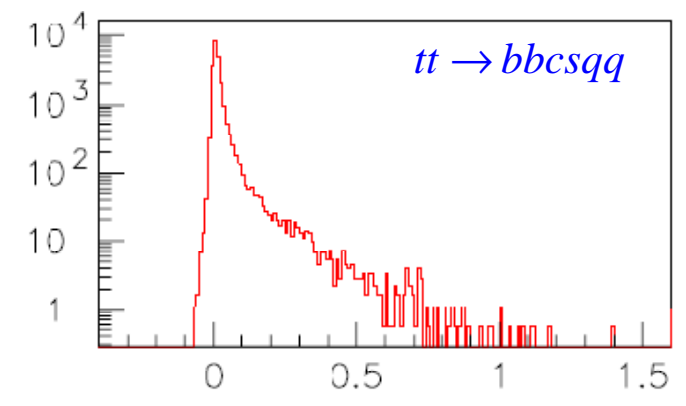
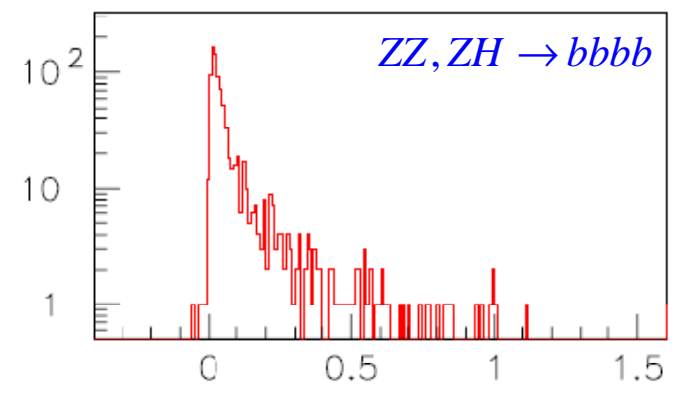
$$L = 2000 \text{ fb}^{-1}$$

$\Delta E/\sqrt{E} = 60\% \rightarrow 30\%$
equiv to $1.4 \times \text{Lumi}$



Neural net based on
 b-tag ordered jet pair
 masses and χ_{HH}^2 , χ_{tt}^2 ,
 χ_{ZZH}^2 , χ_{ZZZ}^2 (only 3
 comb. for $\chi_{HH}^2, \chi_{ZZZ}^2$
 only 6 comb. for $\chi_{tt}^2, \chi_{ZZH}^2$)

QCD rad turned on



NN_{ZHH}

with gluon rad

$$\text{BR}(H \rightarrow b\bar{b})=0.678$$

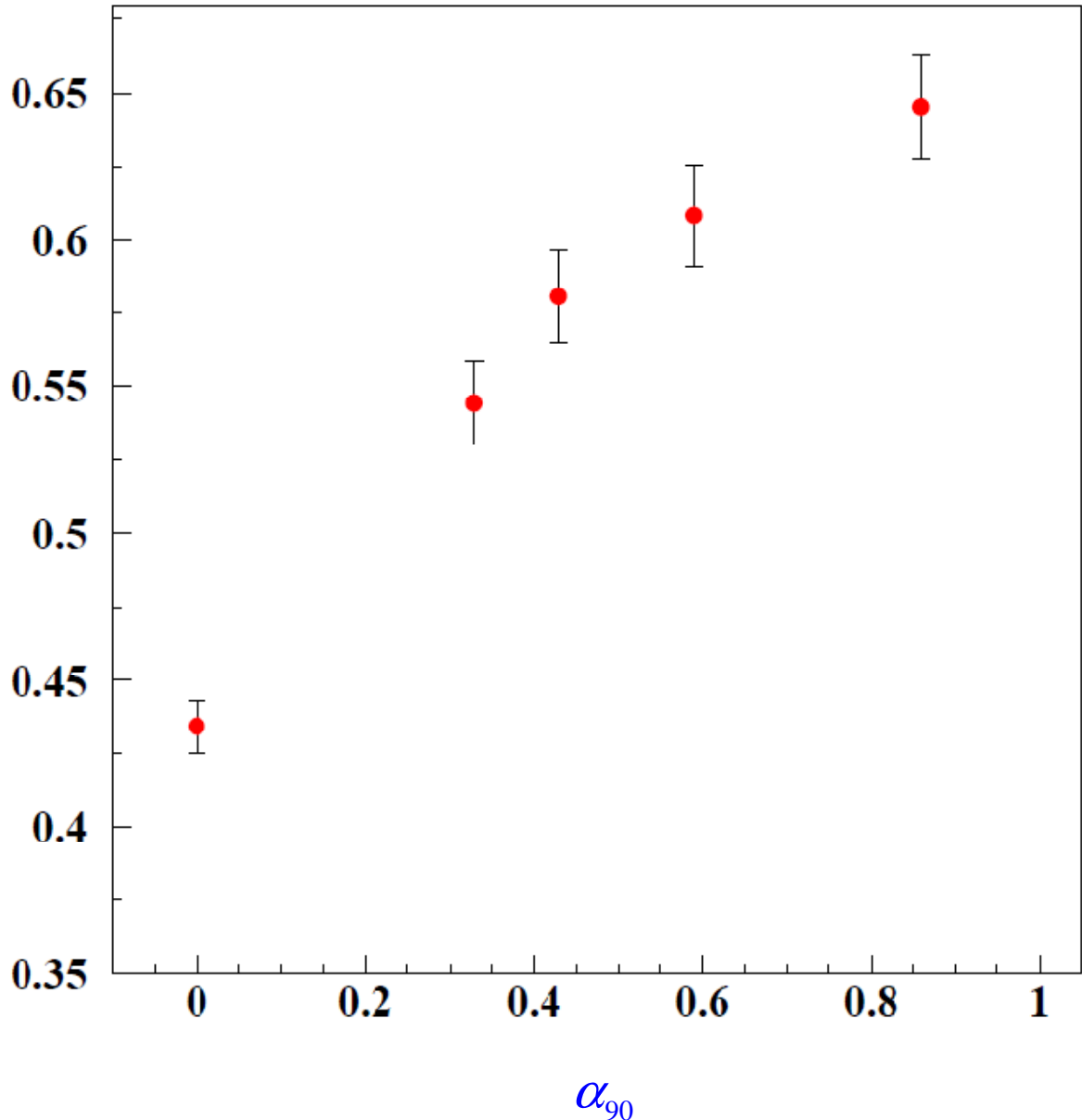
$$e^+e^- \rightarrow ZHH \\ \rightarrow qq\bar{b}\bar{b}\bar{b}\bar{b}$$

$$\sqrt{s} = 500 \text{ GeV}$$

$$L = 2000 \text{ fb}^{-1}$$

$\Delta E/\sqrt{E} = 60\% \rightarrow 30\%$
equiv to $1.35 \times \text{Lumi}$

$$\frac{\Delta g_{hhh}}{g_{hhh}}$$

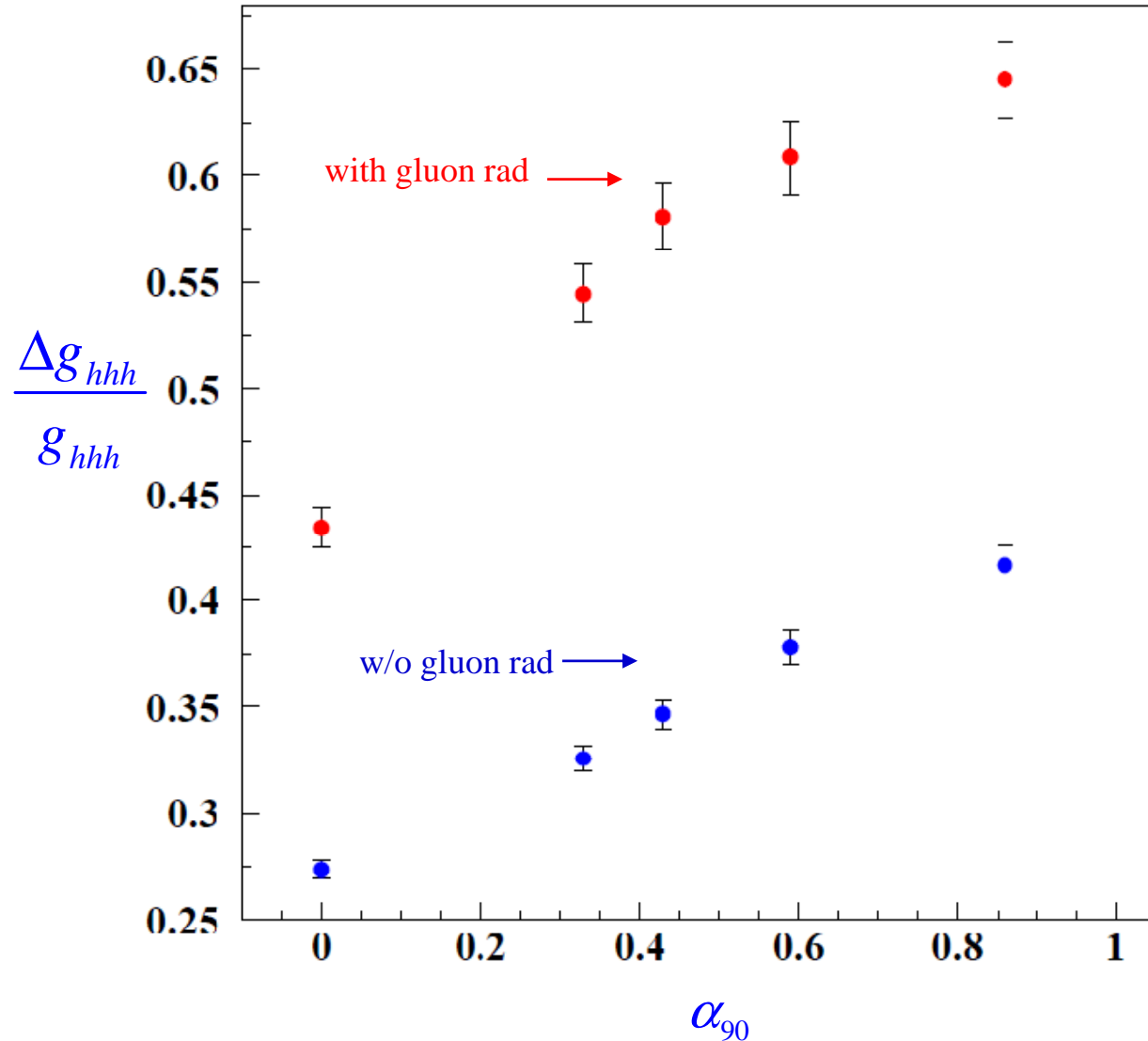


$$\text{BR}(H \rightarrow b\bar{b})=0.678$$

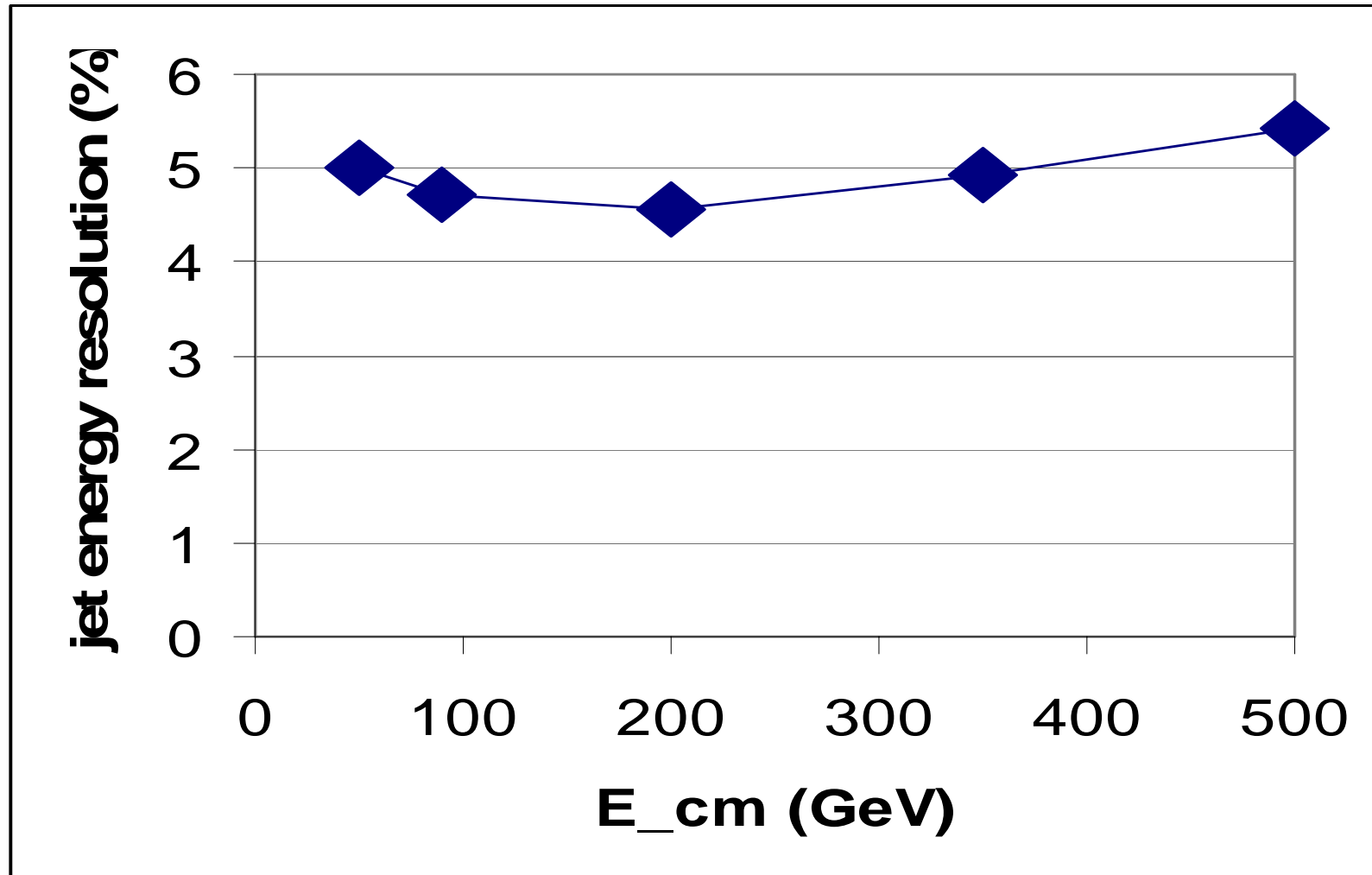
$$e^+e^- \rightarrow ZHH \\ \rightarrow qq\bar{b}\bar{b}\bar{b}\bar{b}$$

$$\sqrt{s} = 500 \text{ GeV} \\ L = 2000 \text{ fb}^{-1}$$

$$\Delta E/\sqrt{E} = 60\% \rightarrow 30\% \\ \text{equiv to } 1.4 \times \text{Lumi}$$



Light quark jets $ee \rightarrow qq$ GLD-PFA



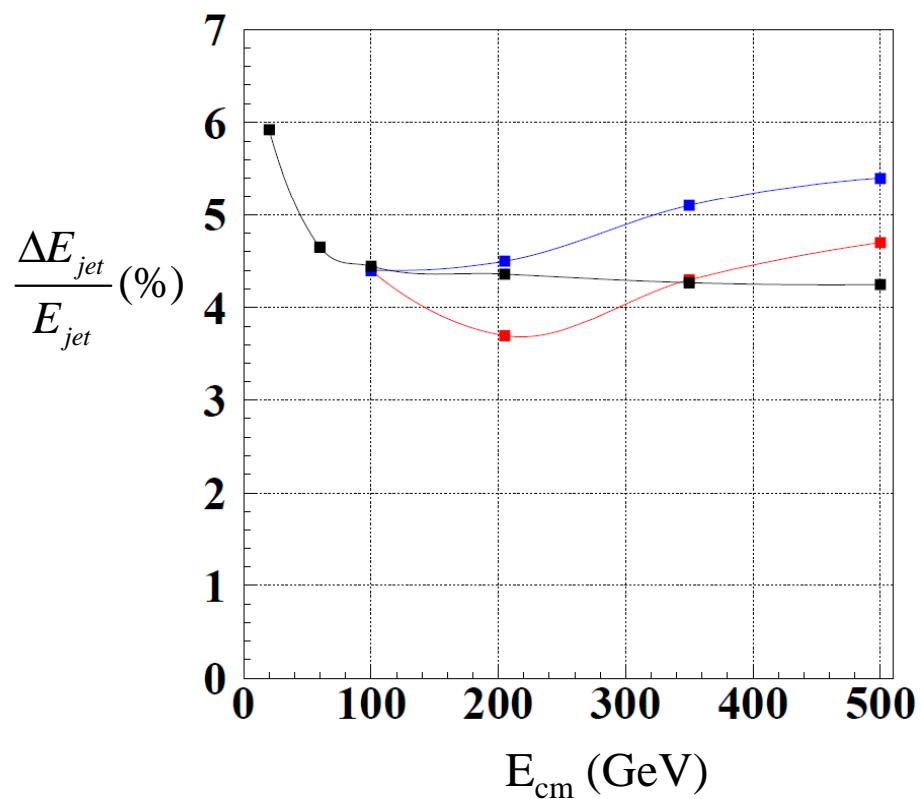
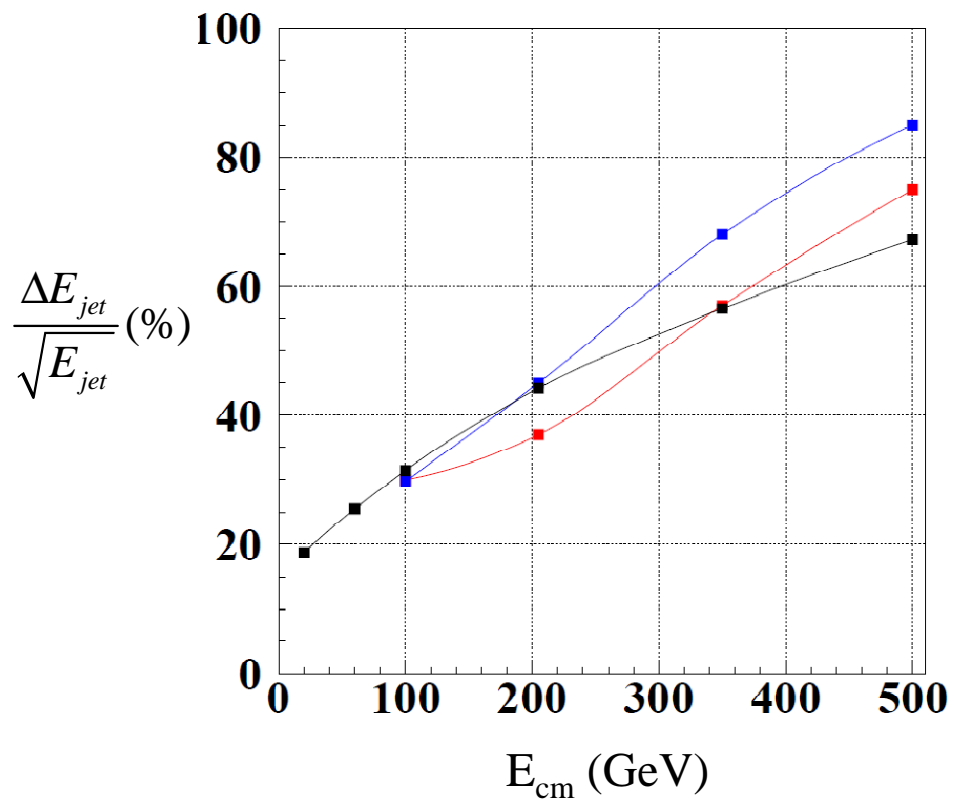
Light quark jets $ee \rightarrow qq$

— GLD PFA

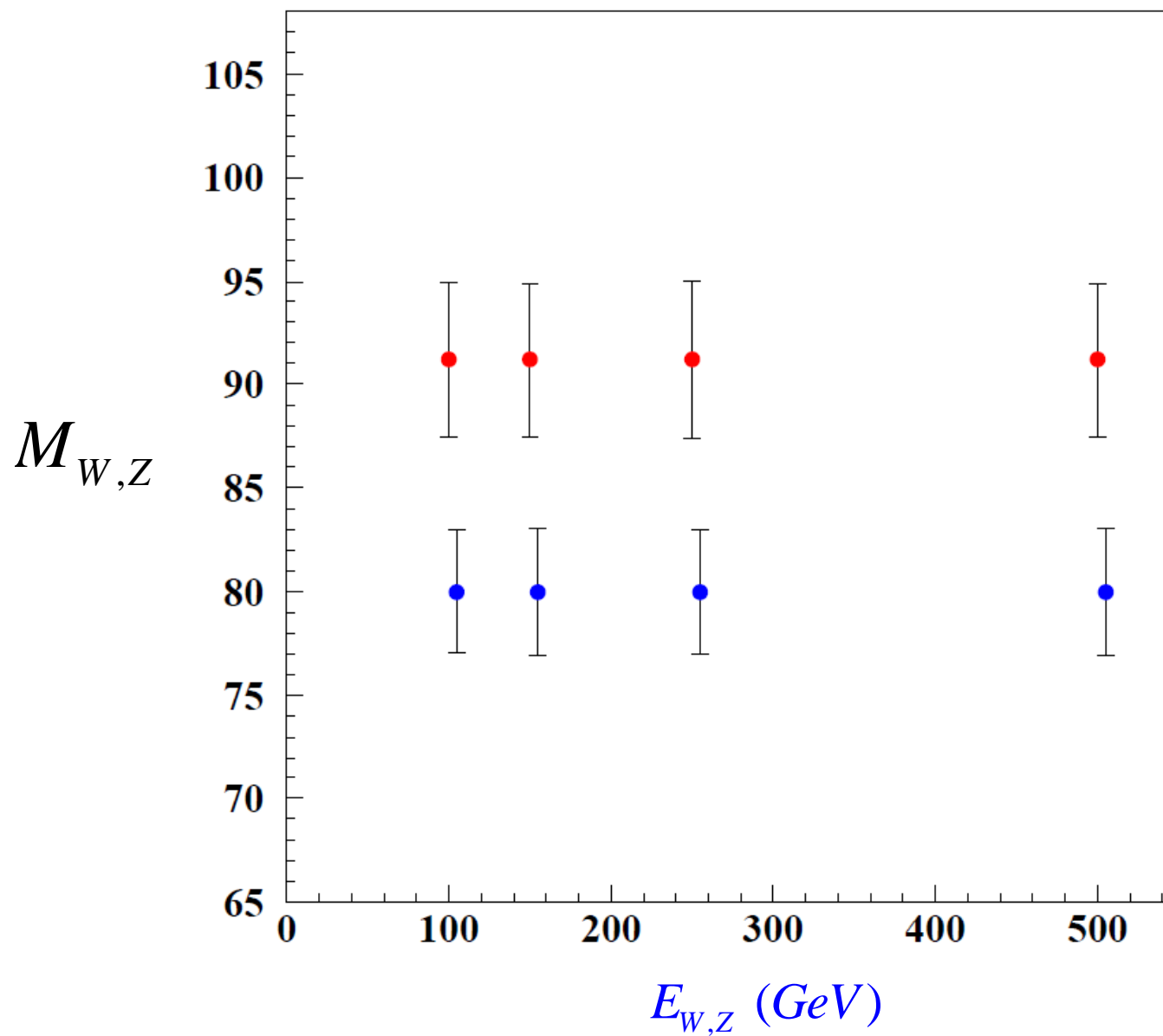
— LDC PFA

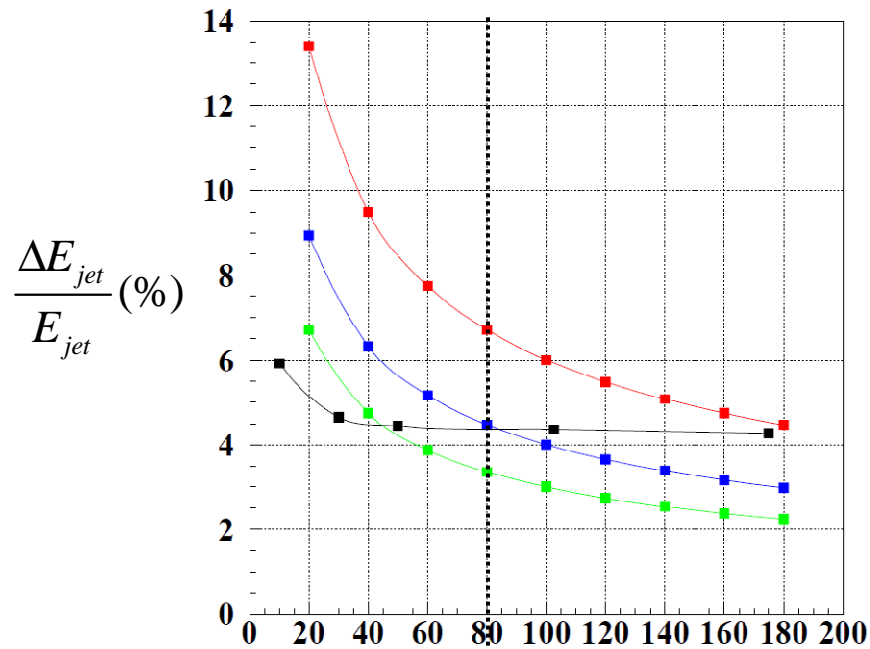
— FASTMC with

$$\frac{\Delta E_\gamma}{E_\gamma} = \frac{0.18}{\sqrt{E_\gamma}} \quad \frac{\Delta E_{n,K_L^0}}{E_{n,K_L^0}} = 0.28$$



$$\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}} \approx 0.043 \quad (\text{see FASTMC plot on previous page})$$



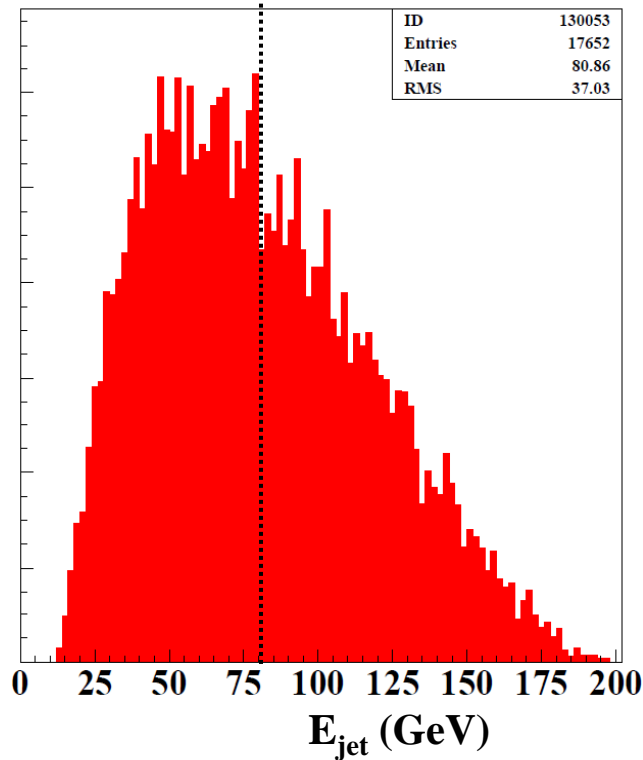


$$\frac{\Delta E_{jet}}{E_{jet}} = \frac{0.6}{\sqrt{E_{jet}}}$$

$$\frac{\Delta E_{jet}}{E_{jet}} = \frac{0.4}{\sqrt{E_{jet}}}$$

$$\frac{\Delta E_{jet}}{E_{jet}} = \frac{0.3}{\sqrt{E_{jet}}}$$

$$\frac{\Delta E_{jet}}{E_{jet}} \approx \text{PFA Current Status}$$



True Jet Energy Distribution for
 $e^+e^- \rightarrow ZHH \rightarrow q\bar{q}b\bar{b}b\bar{b}$
 at $\sqrt{s} = 500$ GeV

Analysis must be redone with $\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}}$ that reflects current PFA status.

For now replot triple Higgs coupling error vs. $\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}}$ using existing results with $\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}} \equiv \frac{\alpha_{90}}{\sqrt{80}}$

$$\text{BR}(H \rightarrow b\bar{b}) = 0.678$$

$$e^+e^- \rightarrow ZHH$$

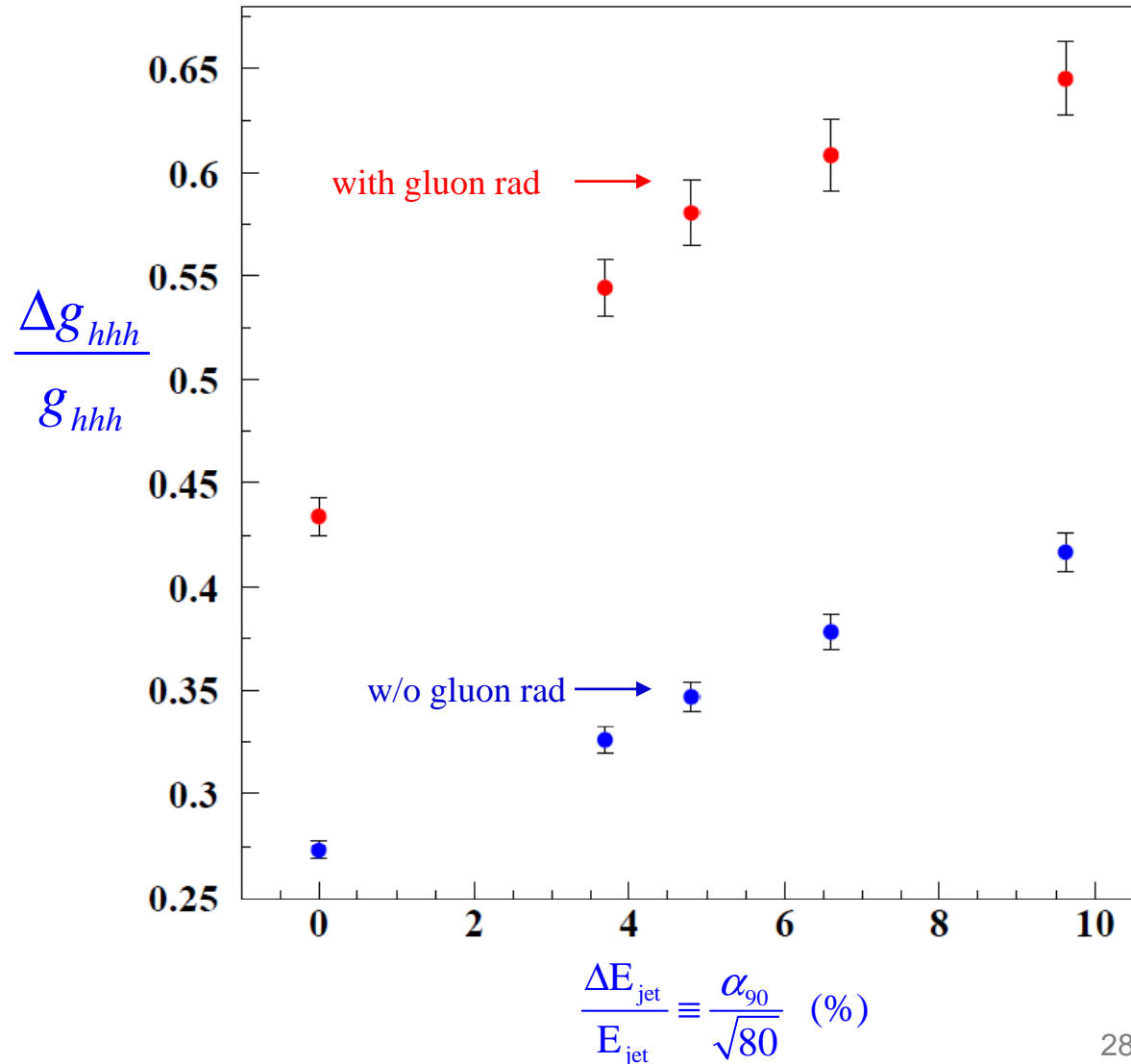
$$\rightarrow qqbb\bar{b}\bar{b}$$

$$\sqrt{s} = 500 \text{ GeV}$$

$$L = 2000 \text{ fb}^{-1}$$

$$\frac{\Delta E}{\sqrt{E}} = 60\% \rightarrow 30\%$$

equiv to $1.4 \times \text{Lumi}$



Conclusions

- The error on the coupling g_{HHH} varies between 32 % and 38% as the jet energy resolution is varied between 30% to 60% over \sqrt{E} assuming no gluon radiation, $E_{cm}=500$ GeV, $L=2000$ fb⁻¹, and the final state $ZHH \rightarrow qqbbbbb$. This corresponds to an effective luminosity gain of 40% as the jet energy resolution is improved from 60% to 30% over \sqrt{E} . By increasing $BR(H \rightarrow bb)$ from 0.687 to 0.853, and adding the contribution from $ZHH \rightarrow llbbbbb$, this particular result replicates the TESLA TDR result.
- When final state gluon radiation is switched on, the error on g_{HHH} deteriorates to a range of 53 % to 62% for jet energy resolutions between 30% to 60% over \sqrt{E} . This problem may be solved with a more sophisticated jet algorithm and better b/c tagging. Note that we currently force reconstructed particles into 6 jets, which may not be the best approach in the presence of hard gluon radiation. Better b/c tagging, as well as b/\bar{b} discrimination, can reduce combinatorics and provide b/c weighted jet energy corrections.

Conclusions (cont.)

- Results from the study of the Higgs self coupling error versus jet energy resolution at $E_{\text{cm}}=500$ GeV do not reflect the ultimate precision on the Higgs self coupling. In addition to improvement to the analysis of $ZHH \rightarrow qqbbbb$, methods have and will be developed to exploit other Higgs decay modes. Also, analysis at $E_{\text{cm}}=1000$ GeV will lead to a significant improvement. A precision of 10% can eventually be achieved when data at $E_{\text{cm}}=500$ GeV and 1000 GeV are combined.