# NLO electroweak corrections to Higgs production in $\gamma\gamma$ fusion

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#### Outline



2 Method for NLO EW (thresholds)

3 Numerical results



# Higgs branching ratios

Branching ratios of the SM Higgs for 100 GeV  $< M_H < 200$  GeV obtained using HDECAY [Djouadi, Kalinowski, Mühlleitner, Spira]



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for 
$$M_H = 120 \text{ GeV} \quad \Rightarrow \quad \Gamma_{H \to \gamma \gamma} \text{Br}_{H \to b\overline{b}} \to 1.8\%$$

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Theory side: SM radiative corrections to  $\Gamma_{H\to\gamma\gamma}$  needed to match the % experimental accuracy, to distinguish between standard/non standard Higgs, to reveal possible unknown charged particles in loops

# LO decay width

Ellis, Gaillard, Nanopoulos'76, Vainshtein, Voloshin, Zakharov, Shifman'79



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1) computed below the  $t\bar{t}$  threshold, for  $M_H < 2M_t$ 

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⇒ improved including 3 loops Steinhauser'96

#### 2) result extended to the complete Higgs-mass range

Melnikov,Yakovlev'93,Djouadi,Spira,Zerwas'93,Inoue,Najima, Oka,Saito'94 ⇒ analytic form Fleischer,Tarasov,Tarasov'04, Harlander,Kant'05,Aglietti,Bonciani,Degrassi,Vicini'06

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 $M_H < 170 \,\text{GeV}$   $\delta^{\text{QCD}} > 0$ , monotonically decreasing,  $\delta^{\text{QCD}} < 2 \,\%$ 

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Each result <u>matches the size of QCD corrections</u>, and should be taken into account when comparing with experiment for a % accuracy

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- Threshold singularities show up at the amplitude level

$$\mathcal{A}_{\rm NLO}(H \to \gamma \gamma) = \ldots + \underbrace{\frac{f(4M_W^2/M_H^2)}{\sqrt{4M_W^2 - M_H^2}}}_{M_H = 2M_W \to \infty} + \ldots$$

\* Minimal solution in known results:  $M_W^2 \Rightarrow M_W^2 - i\Gamma_W M_W$  only in the square root to cure the divergent behaviour

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What does it happen if complex poles instead of real masses

are used everywhere?

# Steps of the computation

Computation of all NLO EW corrections through 6 standard steps

- **1** Generate all Feynman diagrams contributing to  $H \rightarrow \gamma \gamma$
- **2** Projection of  $A_{\text{NLO}}$  on <u>form factors</u>  $F_i$  (Ward identity  $\Rightarrow$  1 FF)
- **3** Reduce  $F_i$  to basis integrals  $M_i$  ( $\neq$  math. sense, no IBPIs)
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- 4  $\mathcal{A}_{\text{NLO}}$  shows UV poles  $\Rightarrow$  <u>renormalized</u>, bare  $\Leftrightarrow$  input data
- **5**  $M_j$  divergent for  $m_f \rightarrow 0$ ;  $A_{\rm NLO}$  finite for  $m_f \rightarrow 0$

$$\Rightarrow M_j = \underbrace{c_j \ln(m_f^2/s)}_{\text{analytically}} + M_j^{\text{fin}} \Rightarrow \underbrace{\sum c_j \ln(m_f^2/s) = 0}_{\text{amplitude}} \Rightarrow m_f = 0$$

**6** Renormalized  $A^{\text{NLO}} = \sum a_j M_j^{\text{fin}}$  evaluated <u>numerically</u>

- FORM/FORTRAN [SA, Ferroglia, Passarino, Passera, Sturm, Uccirati]
- No special conceptual problems appear before crossing the WW threshold

#### EW corrections below 150 GeV

Anatomy of EW corrections to  $\Gamma(H \rightarrow \gamma \gamma)$  for 110 GeV <  $M_H$  < 150 GeV



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- Agreement with lep and lq Aglietti, Bonciani, Degrassi, Vicini'04; corrected (renormalization) 3rd gen. quarks and YM Degrassi, Maltoni'05
- 'Dominant' contributions ∝ G<sub>F</sub>m<sup>2</sup><sub>t</sub> Liao, Li'96, Djouadi, Gambino Kniehl'97, Fugel, Kniehl, Steinhauser'04 large but not dominant

#### Around the *WW* threshold: WI

1st problem with crossing of WW: WI violation for  $H \rightarrow \gamma \gamma$ 

• WI  $\rightarrow p_1^{\mu} \mathcal{A}_{\mu\nu} p_2^{\nu} = 0$  explicitly  $\Rightarrow p_1^{\mu} \mathcal{A}_{\mu\nu} p_2^{\nu} \neq 0 \ (M_H^2 > 4 M_W^2)$ 

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- Due to *H* mass renormalization  $\Rightarrow \underbrace{\mathcal{M}_{H}^{2}}_{\text{bare}} = \underbrace{\mathcal{M}_{H}^{2}}_{\text{exp.}} \left[ 1 + \frac{G_{F}\mathcal{M}_{W}^{2}}{2\sqrt{2}\pi^{2}} \operatorname{Re}\Sigma_{H}^{(1)}(\mathcal{M}_{H}^{2}) \right]$
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- Below WW ⇒ both diagrams are real, and the Ward id. is fulfilled
- Above  $WW \Rightarrow$  mismatch imaginary parts (Re), and the Ward id.  $\neq 0$

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1) (H WFR factor)  $\otimes$  (1-loop diagrams) (also Kniehl, Palisoc, Sirlin'00)



2) (W mass renormalization)  $\otimes$  (derivatives 1-loop diagrams)



divergent for  $\beta_W = 0$ 

divergent for  $\beta_{W,Z} \rightarrow 0$ 

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3) (irr. 2-loop diagrams div.)  $\Rightarrow$  sum 2) + 3) finite for  $\beta_W = 0$   $\Rightarrow$  H WFR divergent



#### Logarithmic singularity at the WW threshold

3rd problem with crossing of WW: logarithmic singularity

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- same config. with *t* loop finite, In multiplied by  $\beta_t^2$  (spin structure)
- well known problem, studied beyond perturbation theory (resummation of Coulomb photons) Melnikov, Spira, Yakovlev'94

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Cure problems with crossing of thresholds through complex poles:

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Decompose  $A = A_{\text{div}}^{1,W}/\beta_W + A_{\text{div}}^{1,Z}/\beta_Z + A_{\text{div}}^2 \ln(-\beta_W^2 - i0) + A_{\text{fin}}$ 

Replace  $M_V^2$  with  $s_V = \mu_V (\mu_V - i\gamma_V)$  in both  $A_{div}^{1,2}$  and threshold factor  $\beta_V$ 

$$\mu_V^2 = M_V^2 - \Gamma_V^2 \qquad \qquad \gamma_V = \Gamma_V \left( 1 - \frac{\Gamma_V^2}{2M_V^2} \right)$$

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Replace  $M_V^2$  with  $s_V = \mu_V (\mu_V - i\gamma_V)$  in all divergent and <u>finite</u> terms

Replacement also at the level of the couplings in order to preserve gauge invariance <u>CMS</u> Denner, Dittmaier, Roth, Wackeroth, Wieders'99-'05

### Threshold behaviour for $H \rightarrow \gamma \gamma$

Comparison of EW corrections to  $\underline{H} \rightarrow \gamma \gamma$  around the *WW* threshold, obtained using different schemes for treating unstable particles



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Comparison of EW corrections to  $\underline{H} \rightarrow \gamma \gamma$  around the *WW* threshold, obtained using different schemes for treating unstable particles



- Result obtained with <u>real masses</u> divergent at WW; good approx. below; completely off above threshold, since no cancellation mechanism occurs
- Result in MCM setup finite, shows cusp; result in CM setup is smooth
- At threshold, result in <u>MCM setup</u>  $\rightarrow$  3.5%; result in <u>CM setup</u>  $\rightarrow$  2.7%  $\Rightarrow$  prediction at the % level requires complete CMS implementation

## Threshold behaviour for $gg \rightarrow H$

Threshold effects can be even artificially larger for other processes

Comparison of EW corrections to  $gg \rightarrow H$  around the WW threshold, obtained using different schemes for treating unstable particles



- Result obtained with <u>real masses</u> divergent at WW; good approx. below/above
- MCM setup gives finite result at WW; large effect 9.6 % associated with cusp
- CM setup smoothens singular behaviour; effects at threshold reduced to 4.6 %

# EW/QCD corrections to $H \rightarrow \gamma \gamma$

Summary of EW/QCD corrections to  $H \rightarrow \gamma \gamma$  for 100 GeV  $< M_H <$  170 GeV



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- <u>Heavier</u> Higgs, <u>enhancement</u> between QCD and EW NLO effects:  $M_H = 170 \text{ GeV} \Rightarrow \delta = +4.4\%$