

# Measurements of the model parameter in the Littlest Higgs Model with T-parity

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(ICRR, Univ. of Tokyo)

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LHT

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**Littlest Higgs model with T-parity (LHT)** is one of attractive models for TeV new physics. LHT could solve the **little hierarchy problem**, and contains a **dark matter candidate**.

In LHT,

	Gauge boson				fermion		Higgs
SM	g	W	Z	A	q	l	H
NEW	$W_H$	$Z_H$	$A_H$	$q_H$	$l_H$	$\Phi_H$	

- Particles & these partners are same spin.
  - New particles get mass by VEV  $f \sim 1$  TeV.
- (New gauge boson masses depend only on VEV  $f$ .)**



In this study, we estimate...

- measurement accuracy of new gauge boson masses
- determination of VEV  $f$
- determination of new particle spins

@ ILC.

# Plan

- Introduction
- What is the LHT?
- How to measure the LHT at ILC?
- Simulation results
- Summary


What is the LHT?

The SM is the successful model describing physics below  $\sim 100$  GeV.  
But ...

**Hierarchy problem**  
(related to quadratic divergence to the Higgs mass term)

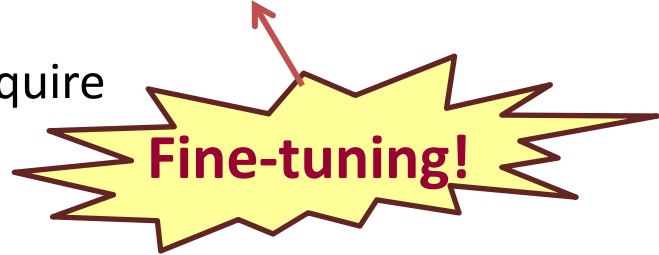
If we assume that

SM is valid all the way up to the GUTs scale,  $\Lambda \sim 10^{15}$  GeV,


$$m_h^2 = m_0^2 + \Lambda^2$$

$100^2 \Leftrightarrow 10000000000000000^2$

EW scale higgs mass require




The SM is the successful model describing physics below  $\sim 100$  GeV.  
But ...

## Hierarchy problem

(related to quadratic divergence to the Higgs mass term)

If we require that

there are no fine-tuning for Higgs mass  $m_h$ ,


$$m_h^2 = m_0^2 + \Lambda^2$$

$100^2 \Leftrightarrow 1000^2$

No fine-tuning



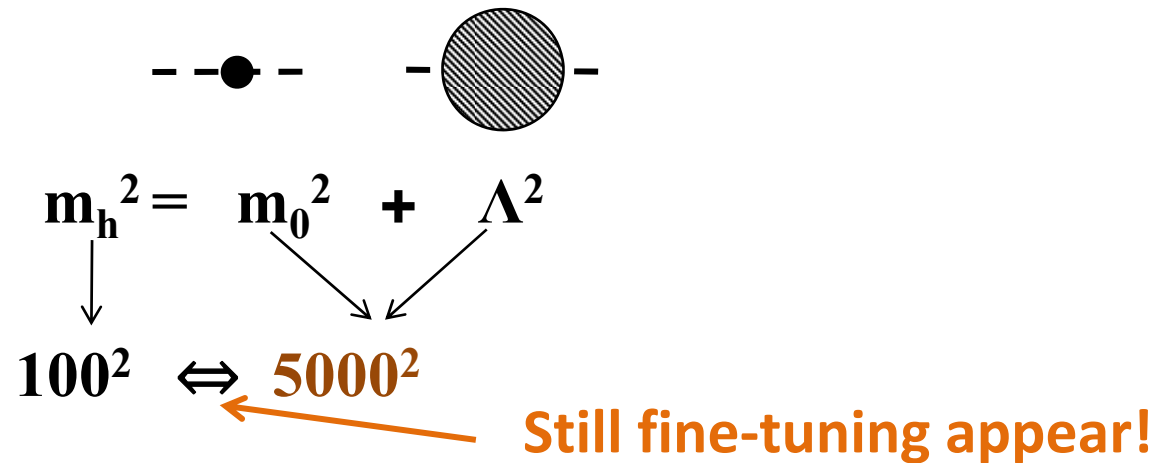
Cut off scale  $\Lambda \sim 1$  TeV

The SM is the successful model describing physics below  $\sim 100$  GeV.  
But ...

**Hierarchy problem**  
(related to quadratic divergence to the Higgs mass term)

However...

**LEP experiments require that the cut off scale is larger than 5 TeV!**



**Little Hierarchy problem!**



No fine-tuning  $\rightarrow$  Cut off scale  $\Lambda \sim 1$  TeV

LEP experiments  $\rightarrow$   $\Lambda \gtrsim 5$  TeV

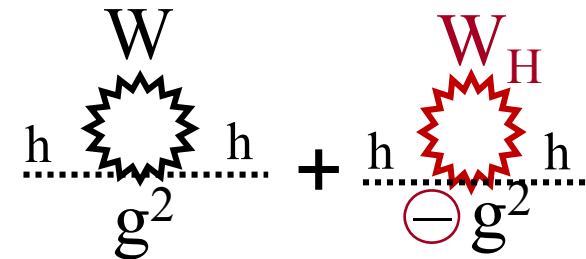


Little Higgs model with T-parity is solution of little hierarchy problem!  
 Even if  $\Lambda \sim 10\text{TeV}$ , there are still no fine-tuning,

Because of ...

• **Collective symmetry breaking (VEV  $f$ )** N. Arkani-Hamed, A. G. Cohen, H. Georgi ('01)

- Higgs boson is regarded as **Pseudo NG boson** of a global symmetry at some higher scale.
- Explicit breaking of the global symmetry is specially arranged to **cancel quadratic divergent corrections to  $m_h$**  at 1-loop level by new gauge bosons and fermions.

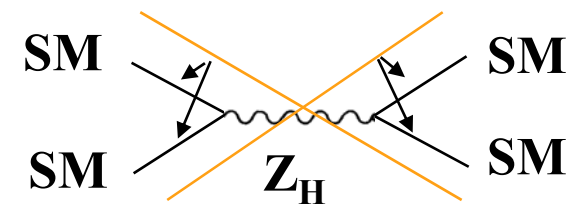


➔ **Little Higgs mechanism**

• **T-parity** H. C. Cheng, I. Low ('03)

In order to avoid constraints from EWPM,  $Z_2$  symmetry called T-parity are introduced.

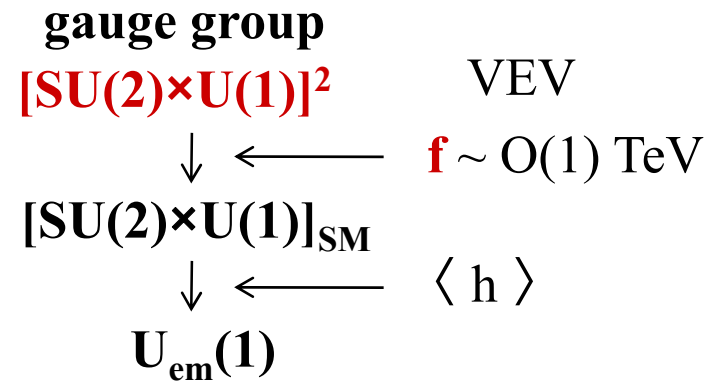
$$\text{SM} \Leftrightarrow \text{SM}, \quad \text{New} \Leftrightarrow -\text{New}$$



**The model contains dark matter candidate! (Heavy photon  $A_H$ )**

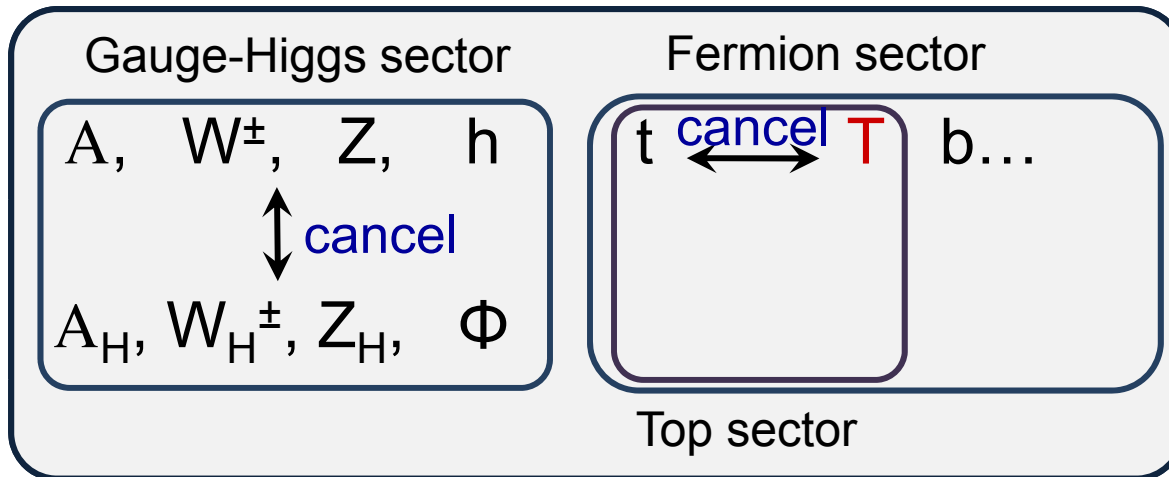
# In order to Implement the Little Higgs Mechanism...

- LHT is based on the non-linear sigma model breaking **SU(5)/SO(5)** symmetry breaking.
- The subgroup **[SU(2)×U(1)]<sup>2</sup>** in SU(5) is gauged, which is broken down to the SM gauge group by vev **f**.

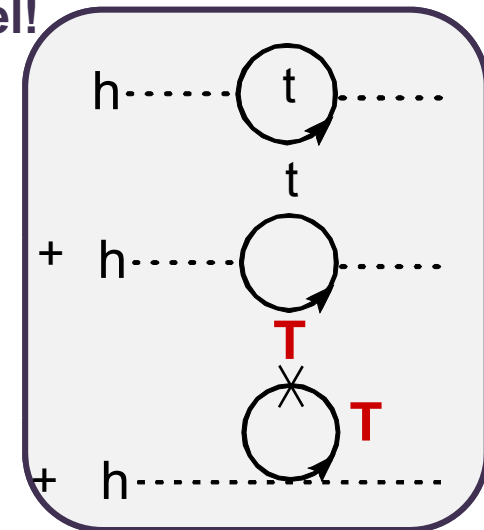


[Arkani-Hamed, Cohen, Katz and Nelson (2002)]

## Particle contents



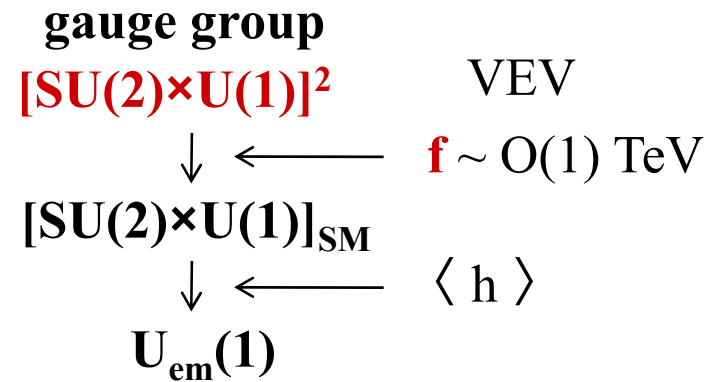
## Cancel!



Due to the cancelation of quadratic divergences, partners are introduced. In the fermion sector, only top partner is required to cancel the quadratic divergences because other fermion Yukawa couplings are small.

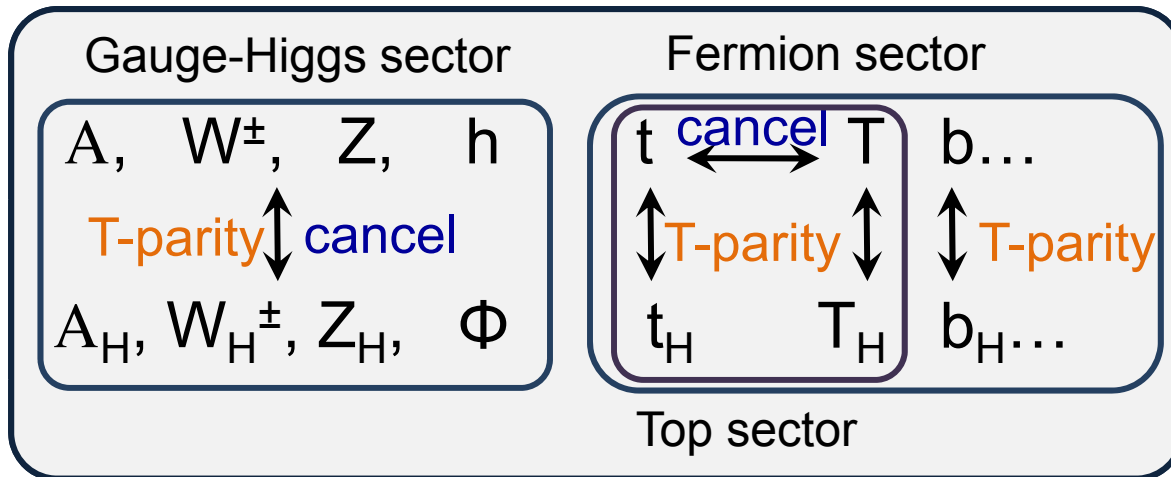
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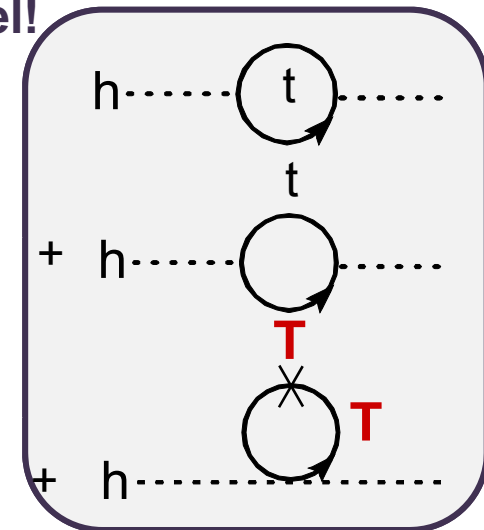


[Arkani-Hamed, Cohen, Katz and Nelson (2002)]

## Particle contents



## Cancel!

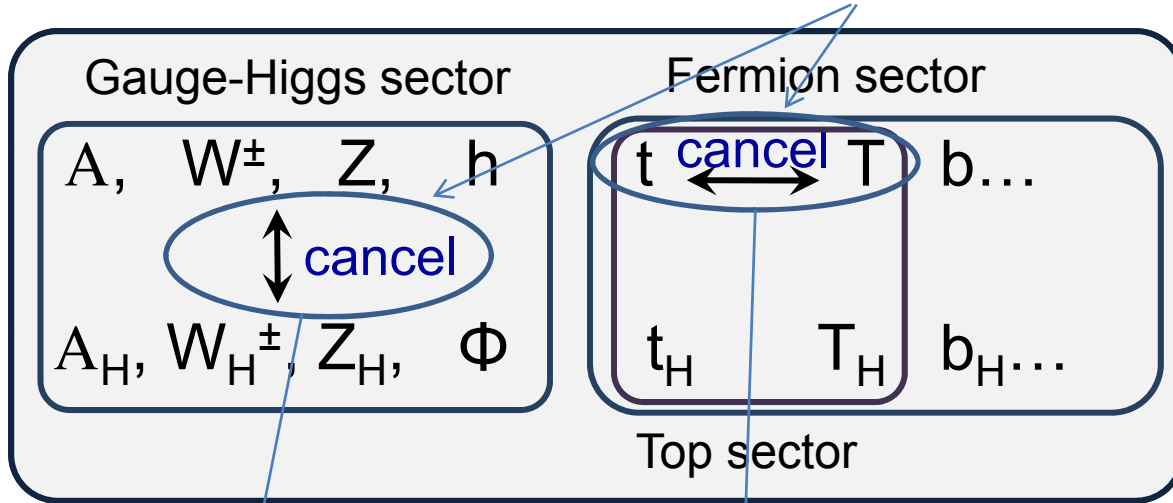


## In order to implement the T-parity...

T-odd partners are introduced for each fermions.

# How to measure the LHT at ILC?

In order to verify the LHT,  
we should measure the **Little Higgs mechanism!**



Top sector

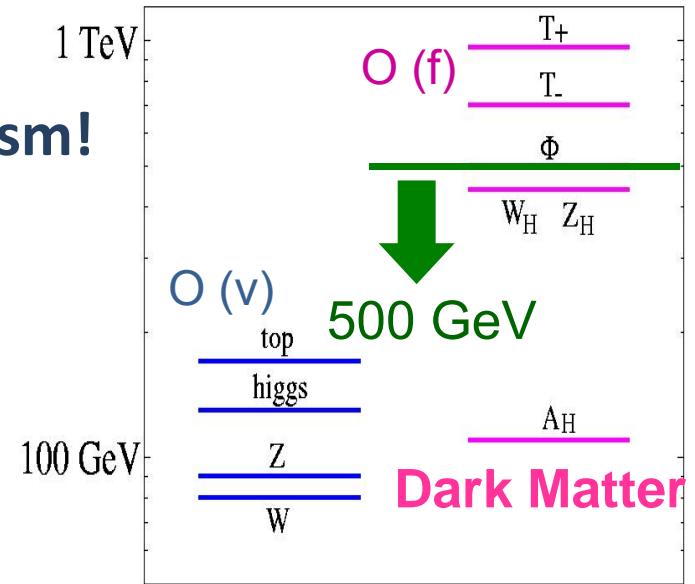
- can be measured at LHC.
- too heavy to produced at ILC.

Gauge sector

Q. H. Cao, C. R. Chen (07)

- can be produced at ILC!
- cannot measure masses at LHC
- with good accuracy at ILC

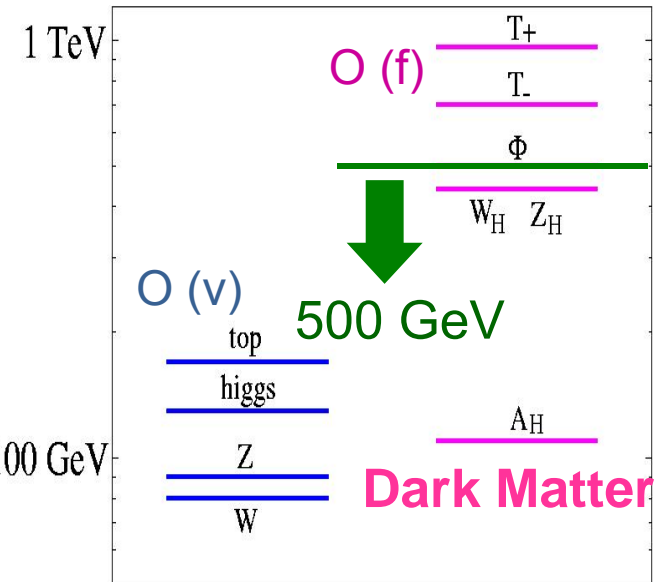
**We should measure the gauge sector in the LHT at ILC.**



S. Matsumoto, T. Moroi, K. Tobe (08)  
and .....

In the gauge sector,

Which mode can be measured at the ILC ?



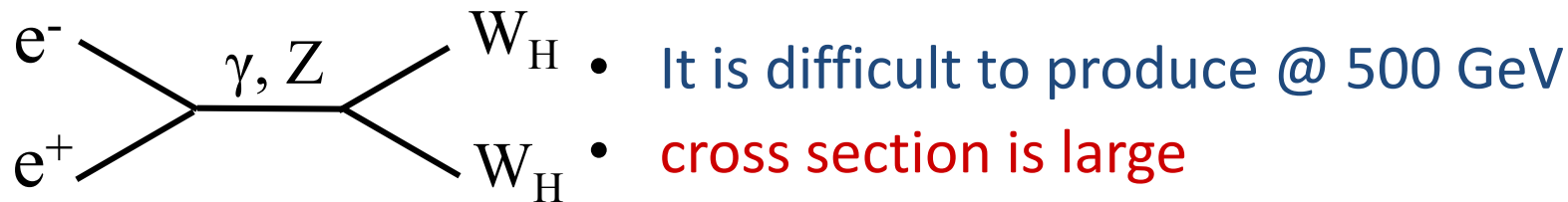
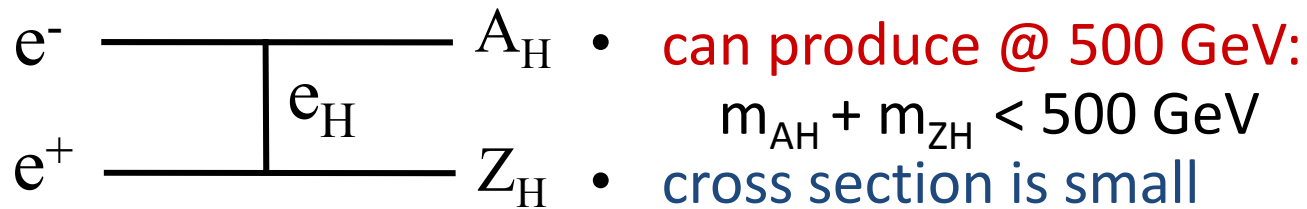
$e^-$  —————  $A_H$  • can produce easily  
 $e^+$  —————  $A_H$  •  $m_{A_H} + m_{A_H} < 500 \text{ GeV}$  100 GeV  
 $e_H$  • No signal

$e^-$  —————  $A_H$  • can produce @ 500 GeV:  
 $e^+$  —————  $Z_H$  •  $m_{A_H} + m_{Z_H} < 500 \text{ GeV}$   
 $e_H$  • cross section is small

$e^-$  \ /  $\gamma, Z$  /  $W_H$  • It is difficult to produce @ 500 GeV  
 $e^+$  / \  $W_H$  \ • cross section is large

## Our strategy

1. @ 500 GeV ILC,  
we estimate the measurement of gauge boson masses &  
vev  $f$  using  $e^+e^- \rightarrow A_H Z_H$
2. Using  $e^+e^- \rightarrow W_H W_H$ ,  
we estimate the improvement of gauge boson masses &  
vev  $f$  measurement @ 1 TeV ILC.



Representative point  
of our simulation



# Mode & Representative point

Which particle can produced at the ILC ? → It depends on VEV **f** .

Because heavy gauge boson masses depend only on vev f.

$$e^+e^- \rightarrow A_H Z_H$$

$$e^+e^- \rightarrow W_H W_H$$

↓ dark matter relic abundance in this model ↓

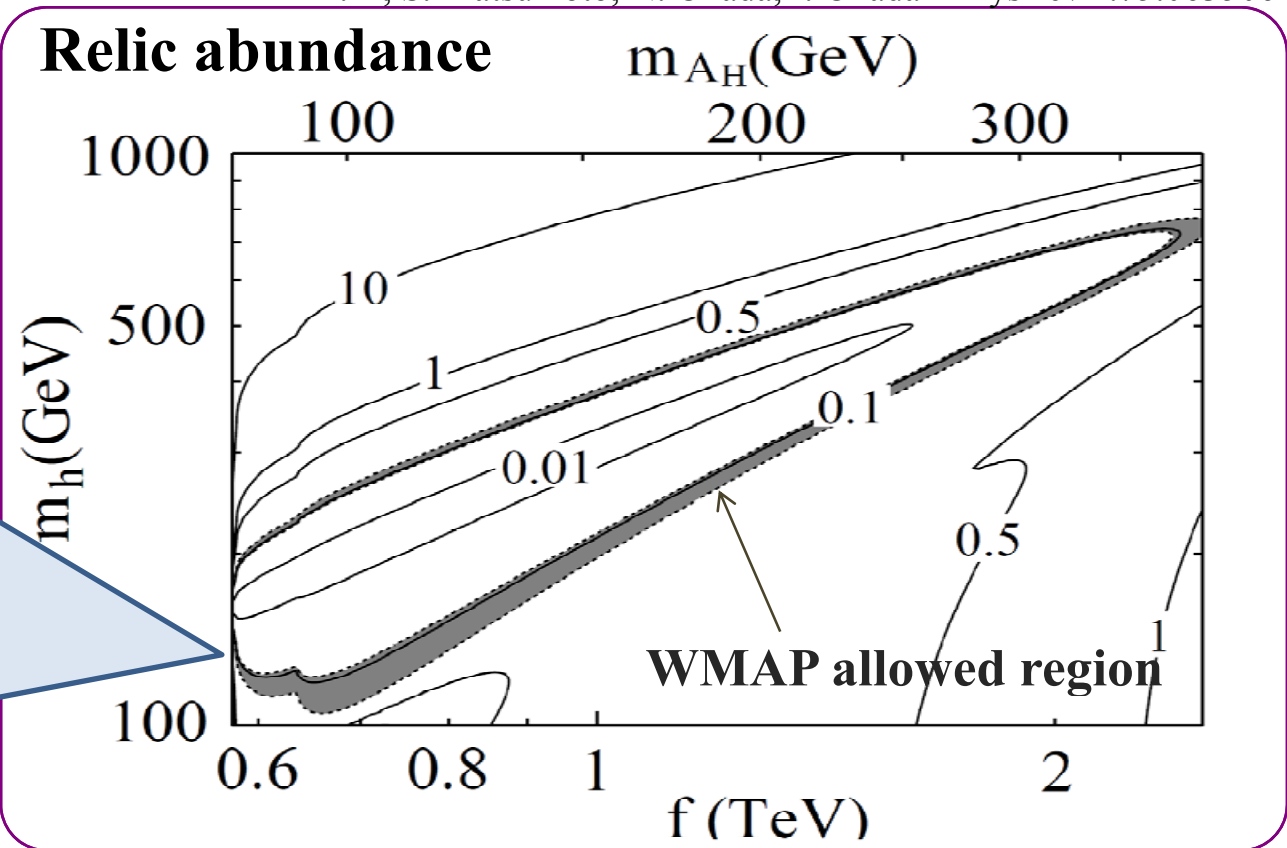
M. A, S. Matsumoto, N. Okada, Y. Okada PhysRevD.75.063506

**Dark matter ( $A_H$ )**

Shaded area is WMAP allowed region .

DM abundance is determined by the Higgs mass & vev f.

**At this WMAP allowed region, the model also satisfies other experimental constraints!**



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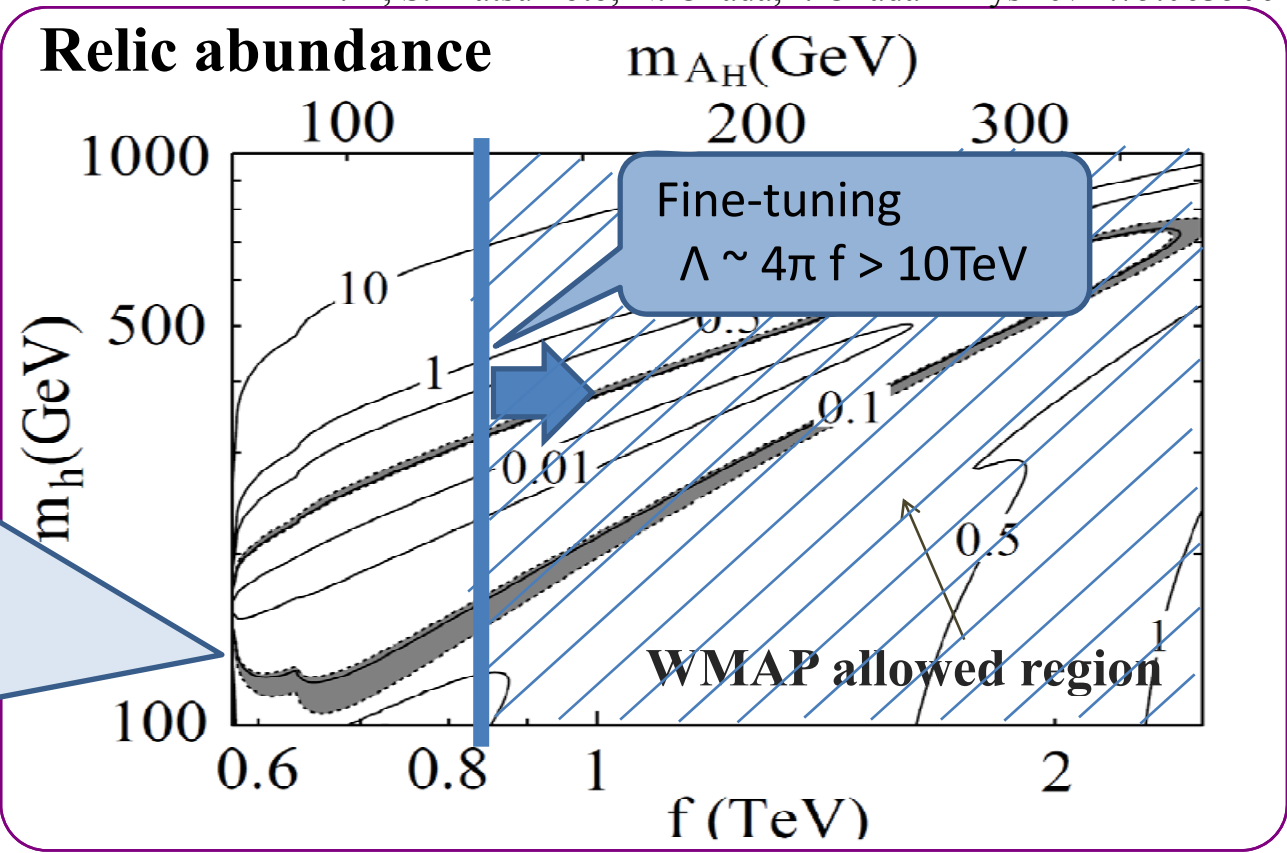
$$e^+e^- \rightarrow A_H Z_H$$

$$e^+e^- \rightarrow W_H W_H$$

If f is larger than ~800GeV, the hierarchy problem appears again.

M. A, S. Matsumoto, N. Okada, Y. Okada PhysRevD.75.063506

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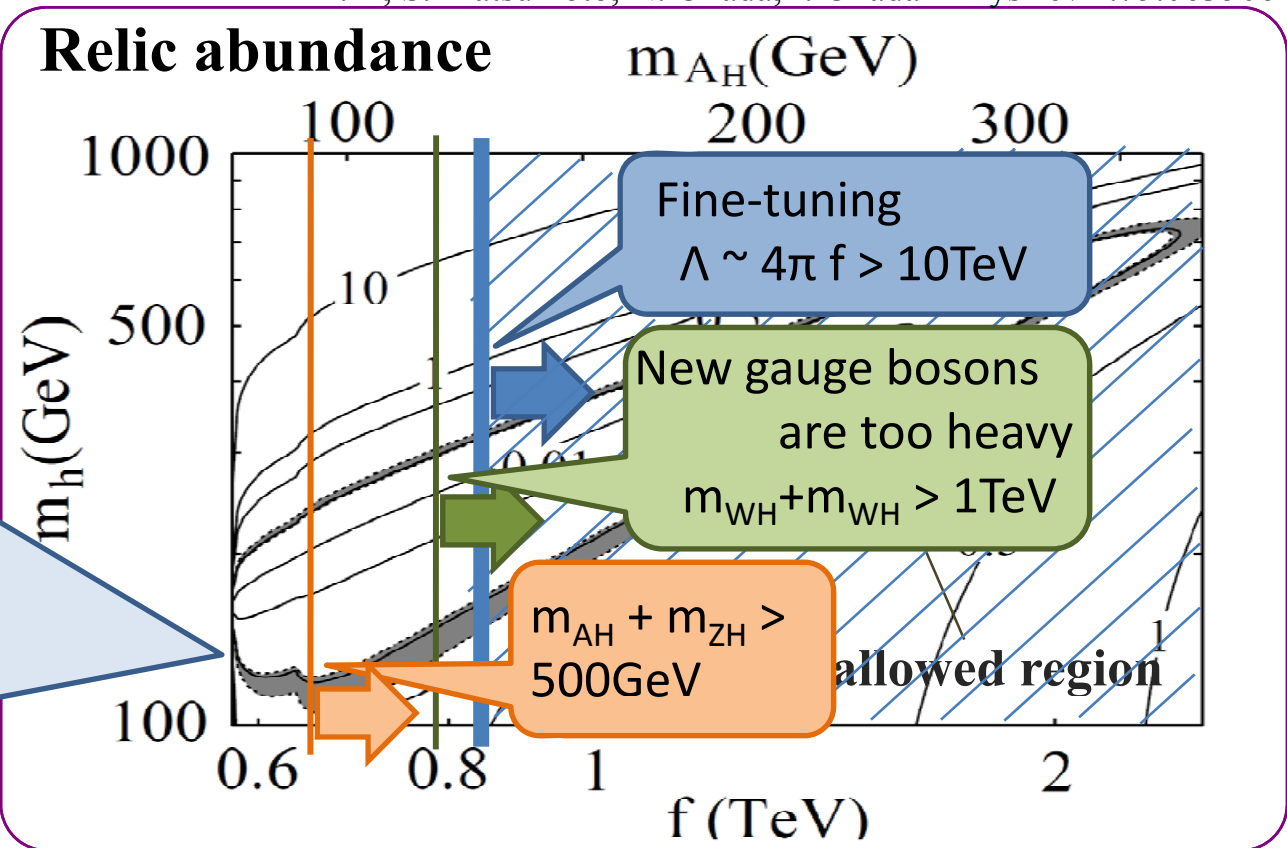
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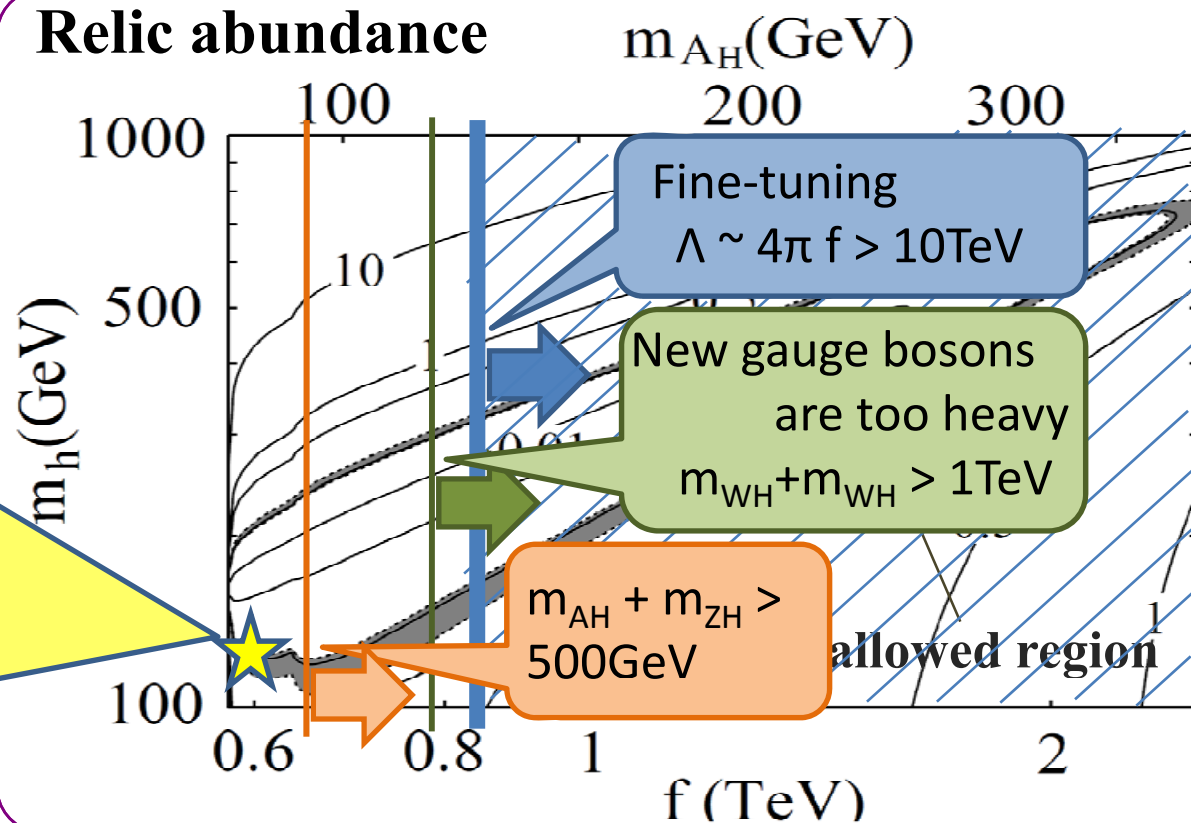
## Mass spectrum

f	580
$e_H$	410
$Z_H$	369
$W_H$	368
$A_H$	82
Higgs	134

### Point I (GeV)

Sample points satisfy all experimental & cosmological constraints.

## Relic abundance



# Simulation results

# Simulation

We simulate using **Physsim & PYTHIA** for generating BG,  
**MadGraph** for generating signal,  
**JSFQuickSimulator** for simulating detector.

@ 500 GeV ILC

$$e^+e^- \rightarrow A_H Z_H \rightarrow A_H A_H h$$

We determine heavy gauge masses  
from edges of higgs energy distribution.

- Integrated luminosity 500 fb<sup>-1</sup>
- Cross section
  - **Signal  $A_H Z_H$  1.9 fb**
  - BG  $\nu\nu Z \rightarrow \nu\nu b\bar{b}$  44.3 fb
  - $\nu\nu Z \rightarrow \nu\nu c\bar{c}$  34.8 fb
  - $\nu\nu h \rightarrow \nu\nu b\bar{b}$  34.0 fb
  - .....

@ 1 TeV ILC

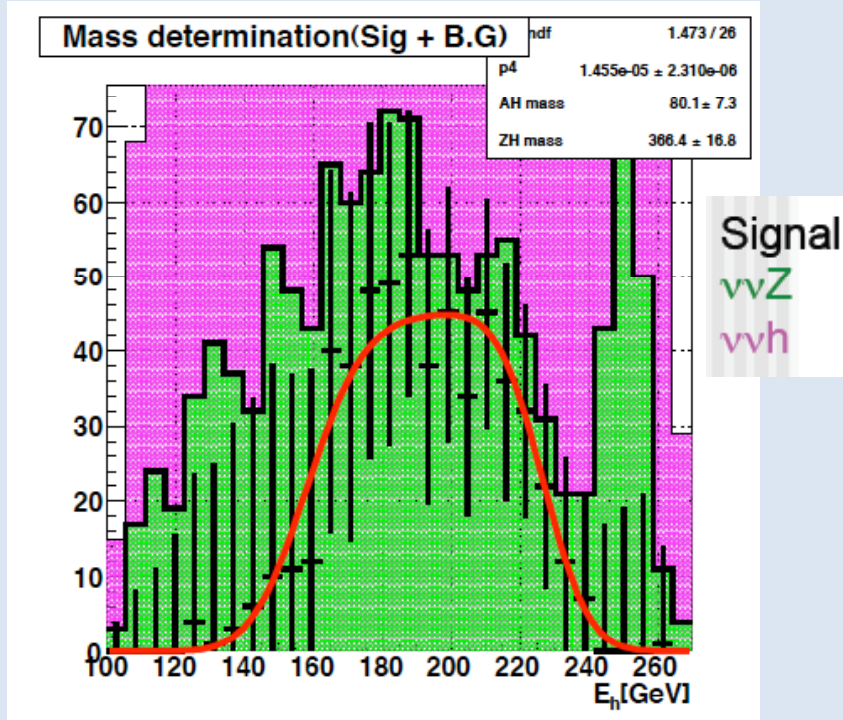
$$e^+e^- \rightarrow W_H W_H \rightarrow A_H A_H W W$$

from edges of  $W_{\pm}$  energy distribution.

- Integrated luminosity 500 fb<sup>-1</sup>
- Cross section
  - **Signal  $W_H^+ W_H^-$  121 fb**
  - BG  $W^+ W^-$  1308 fb
  - $e^+e^- W^+ W^-$  491 fb
  - .....

@ 500 GeV ILC

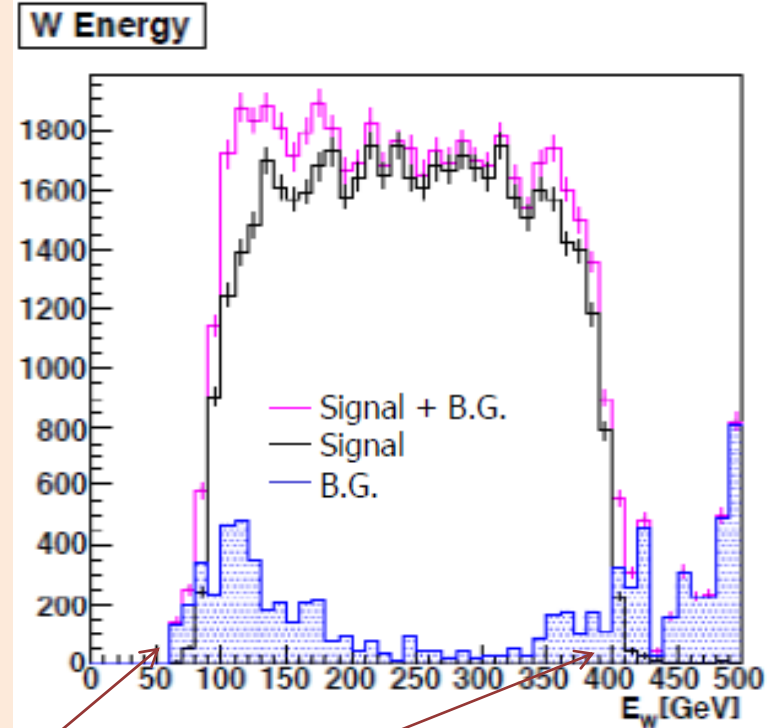
$$e^+e^- \rightarrow A_H Z_H \rightarrow A_H A_H h$$



➔ For details, see next talk (T. Kusano).

@ 1 TeV ILC

$$e^+e^- \rightarrow W_H W_H \rightarrow A_H A_H WW$$

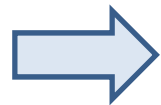
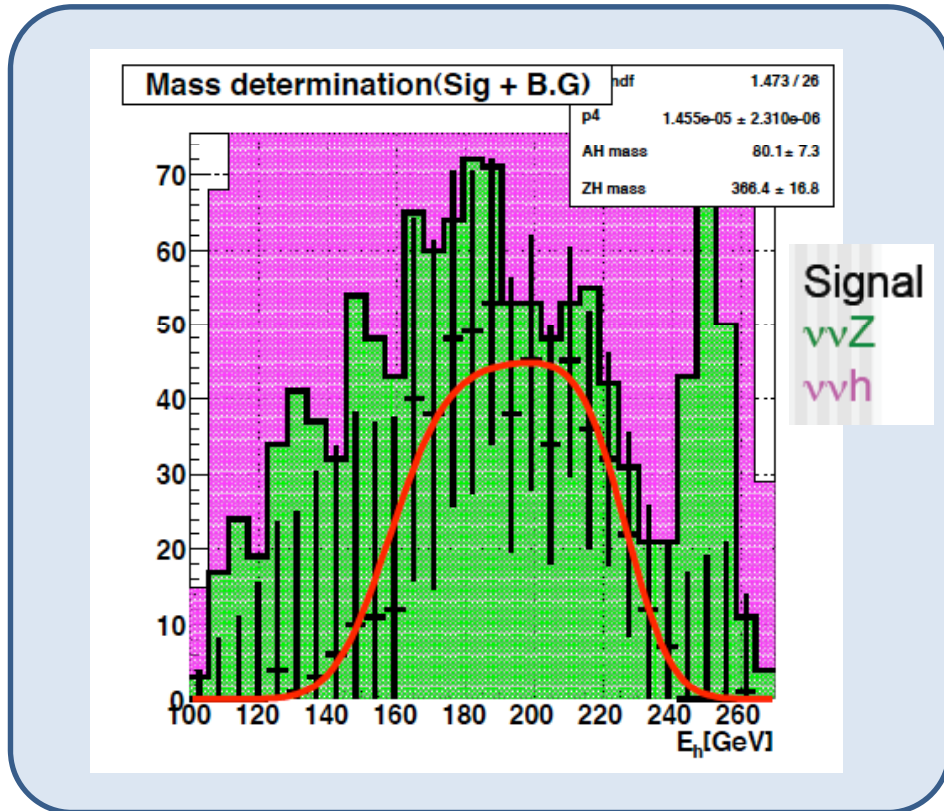


➔ For details, see next next talk (R. Sasaki).

Because the **simulation shows end points clearly**,  
It allow us to extract the property of heavy gauge bosons and DM!

@ 500 GeV ILC

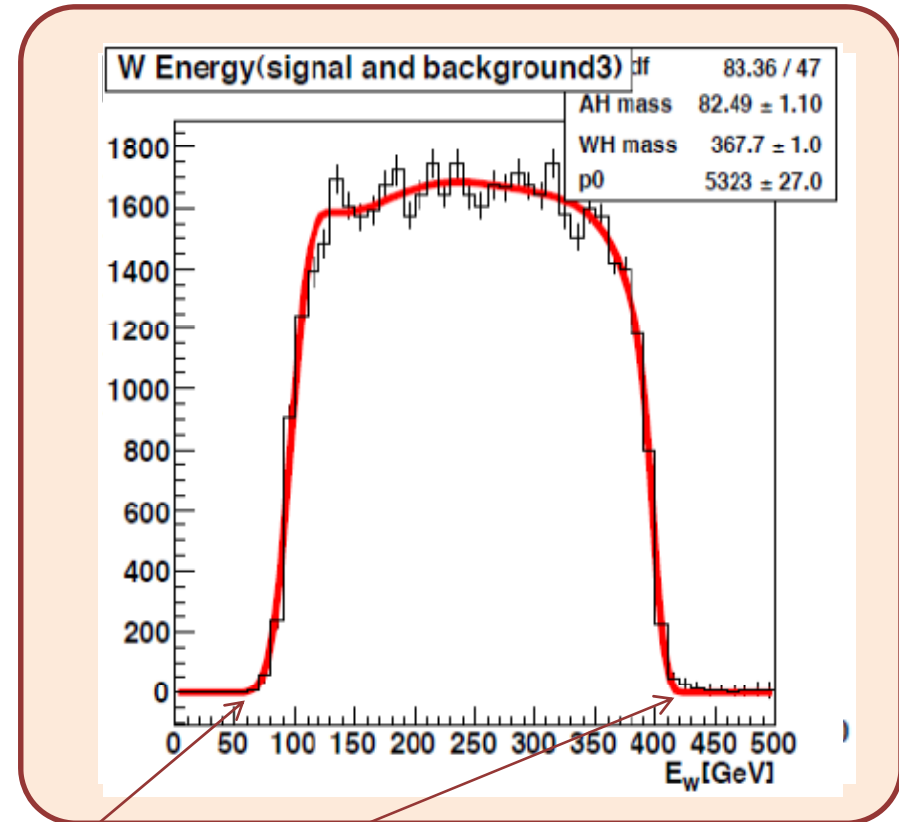
$$e^+e^- \rightarrow A_H Z_H \rightarrow A_H A_H h$$



For details,  
see next talk (T. Kusano).

@ 1 TeV ILC

$$e^+e^- \rightarrow W_H W_H \rightarrow A_H A_H WW$$



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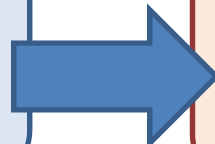


# Simulation results

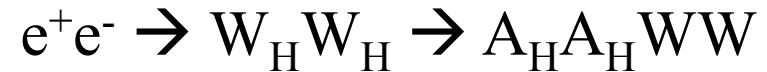
@ 500 GeV ILC



- Mass determination
  - Fit results
    - $m_{A_H} = 80.1 \pm 7.3 \text{ GeV}$   
true(81.85)
    - $m_{Z_H} = 366 \pm 17 \text{ GeV}$   
true(368.1)
- f determination
  - $f = 580 \pm 22 \text{ GeV}$   
true(580)



@ 1 TeV ILC



- Mass determination
  - Fit results
    - $m_{A_H} = 82.42 \pm 1.09 \text{ GeV}$   
true(81.85)
    - $m_{W_H} = 368.0 \pm 0.9 \text{ GeV}$   
true(368.1)
- f determination
  - $f = 580 \pm 1.3 \text{ GeV}$   
true(580)

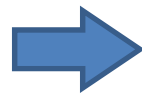


We can also determine

- $W_H$  spin using production angle of  $W_H^+$ .
- $W$  helicity using angular distribution of jets.

# Summary

- **Littest Higgs model with T-parity (LHT)** is one of attractive models for physics beyond the SM.
- Important model parameter ( $f$ ) can be determined by gauge boson sector with good accuracy.
  - @ 500 GeV ILC, we can measure LHT using  $e^+e^- \rightarrow A_H Z_H$ .
  - @ 1 TeV ILC, we can measure LHT using  $e^+e^- \rightarrow W_H W_H$  with very high accuracy.
- Our simulation shows **the clear edge** in signal events, which allow us to extract the model parameters precisely.
- Results obtained from the collider experiments will be compared to those from astrophysical experiments



Cosmological impact will be talked by S. Matsumoto in today's cosmological session.