

Requirements for Jet Energy Resolution

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Simple study of $\Delta M_{W,Z}$ versus $E_{W,Z}$ & ΔE_{jet} using FASTMC

$$e^- \gamma \rightarrow \nu_e W^- \rightarrow \nu_e \bar{u} d$$

$$\nu_e H \rightarrow \nu_e Z \rightarrow \nu_e u \bar{u}$$

No resolution loss from jet-finding, neutrinos,
or particles outside fid. vol.

Use the following single particle calorimeter resolutions in FASTMC to mimick PFA jet energy resolution versus jet energy for jet energies $50 \text{ GeV} < E_{\text{jet}} < 250 \text{ GeV}$:

$$\frac{\Delta E_{\gamma}}{E_{\gamma}} = \frac{0.18}{\sqrt{E_{\gamma}}} \quad \frac{\Delta E_{n,K_L^0}}{E_{n,K_L^0}} = 0.28$$

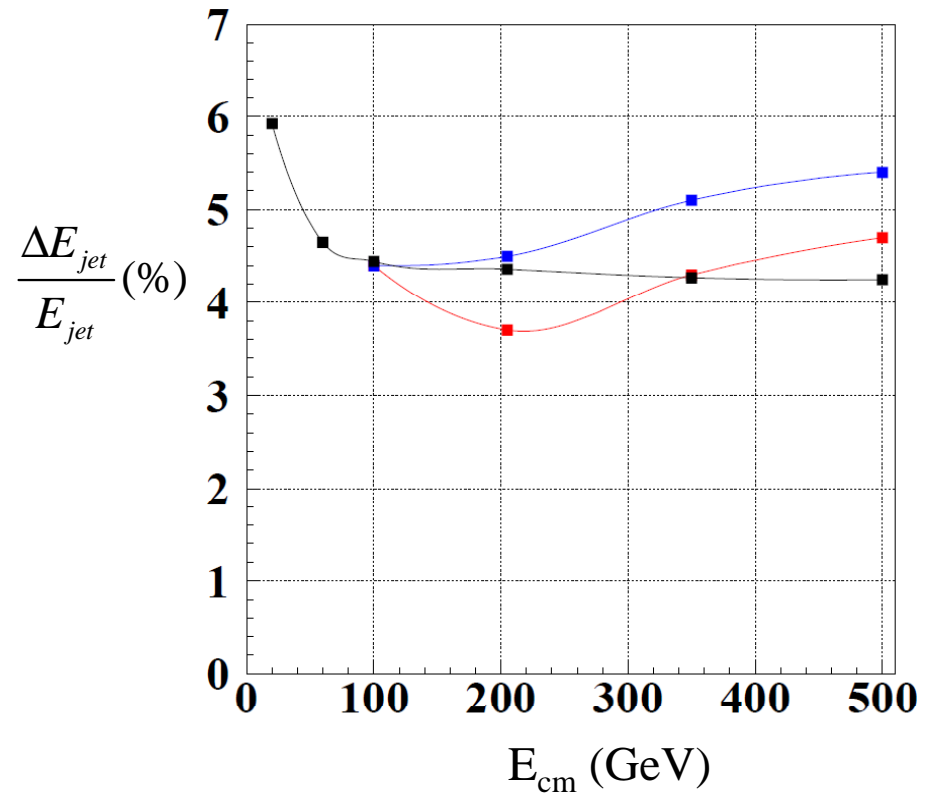
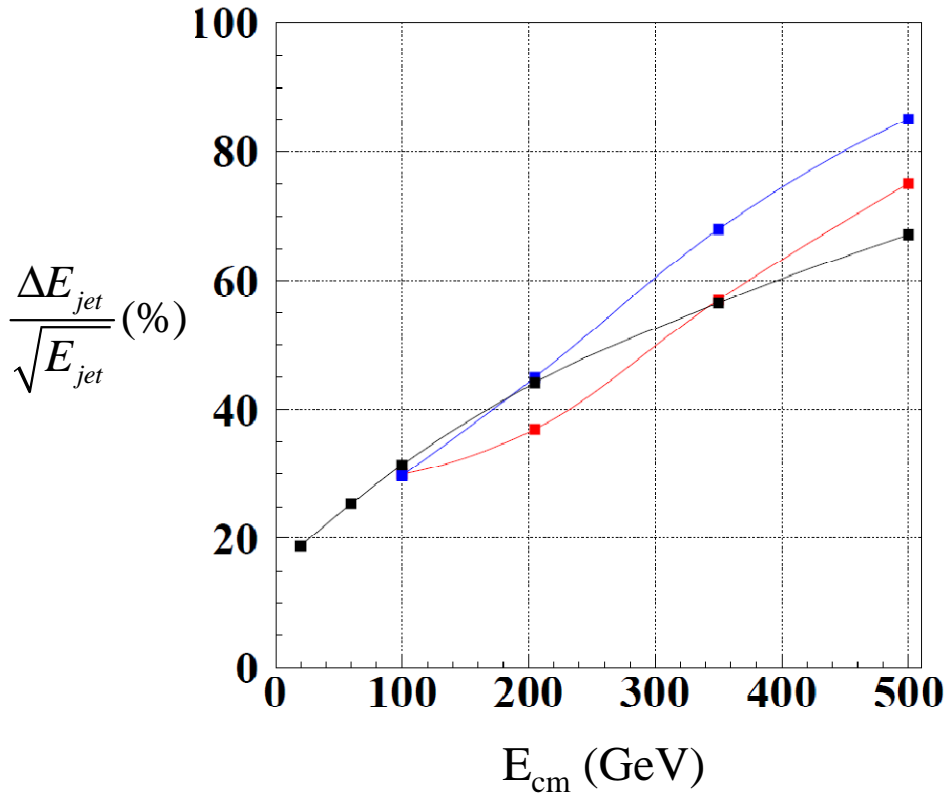
Light quark jets $ee \rightarrow qq$

— GLD PFA

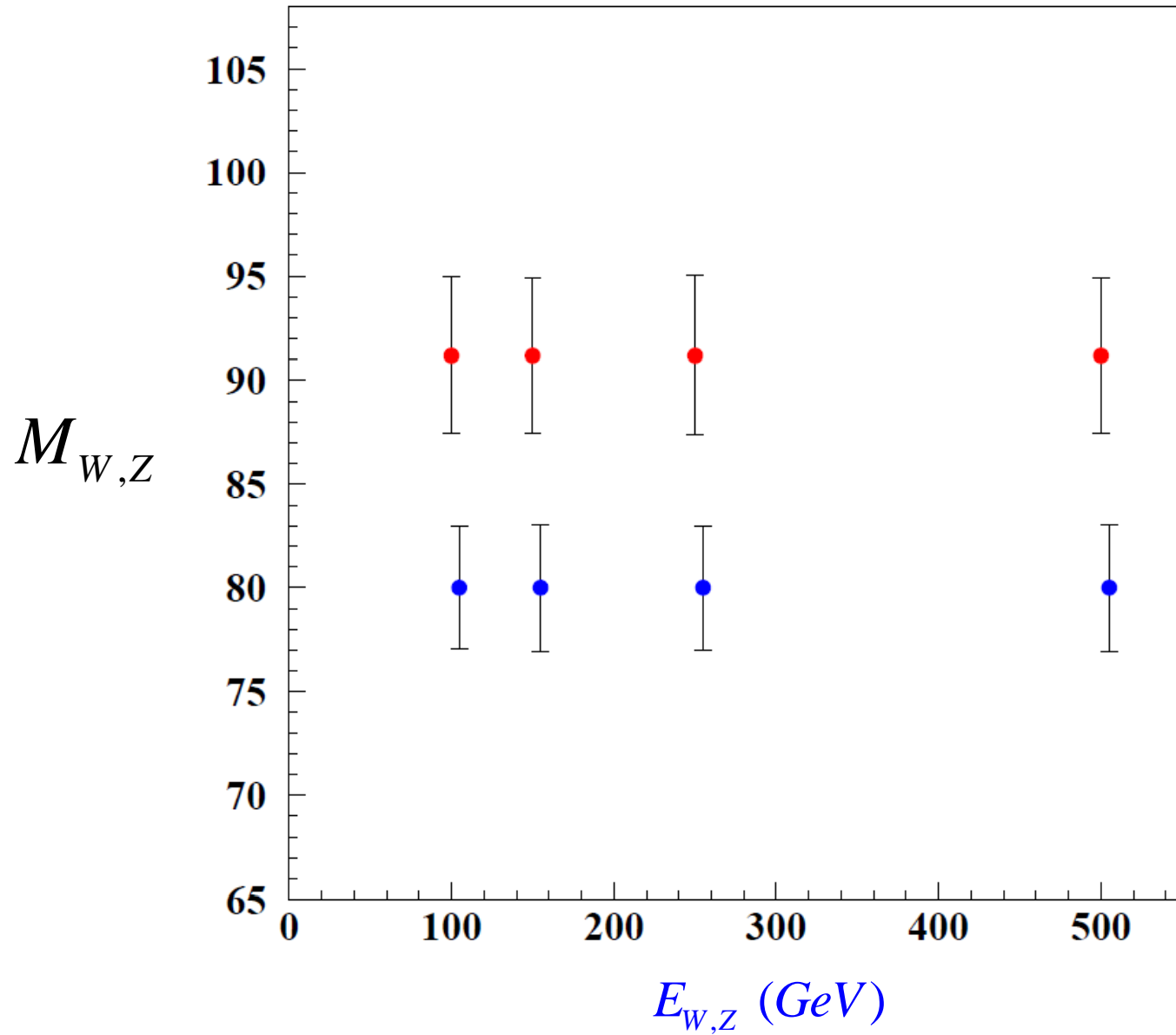
— LDC PFA

— FASTMC with

$$\frac{\Delta E_\gamma}{E_\gamma} = \frac{0.18}{\sqrt{E_\gamma}} \quad \frac{\Delta E_{n,K_L^0}}{E_{n,K_L^0}} = 0.28$$



$$\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}} \approx 0.043 \quad (\text{see FASTMC plot on previous page})$$



The approximate expression for the two-jet mass M is

$$M \approx 2E_1E_2(1 - \cos \theta)$$

$$\frac{\Delta M}{M} \approx \frac{1}{2} \left[\frac{\Delta E_1}{E_1} \oplus \frac{\Delta E_2}{E_2} \right]$$

but the full expression is

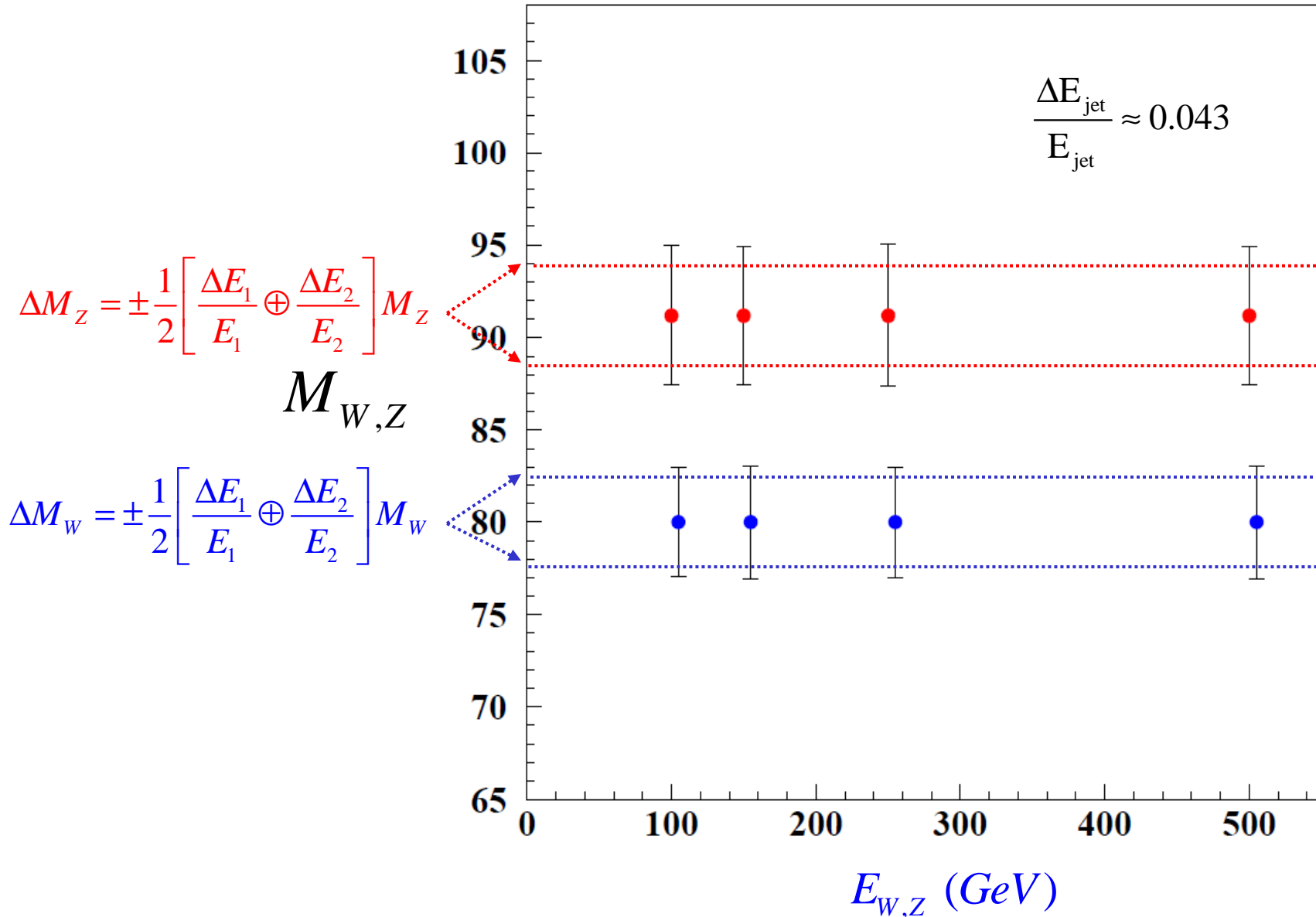
$$M = m_1^2 + m_2^2 + 2E_1E_2(1 - \beta_1\beta_2 \cos \theta) \quad , \quad \beta_j = \left(1 - \frac{m_j^2}{E_j^2} \right)^{\frac{1}{2}}$$

$$\frac{\Delta M}{M} \approx \frac{1}{2} \left[\frac{\Delta E_1}{E_1} \oplus \frac{\Delta E_2}{E_2} \oplus \frac{\theta \sin \theta}{1 - \cos \theta} \frac{\Delta \theta}{\theta} \oplus \frac{1 + r^{-1} \cos \theta}{1 - \cos \theta} \frac{m_1^2}{E_1E_2} \frac{\Delta m_1}{m_1} \oplus \frac{1 + r \cos \theta}{1 - \cos \theta} \frac{m_2^2}{E_1E_2} \frac{\Delta m_2}{m_2} \right]$$

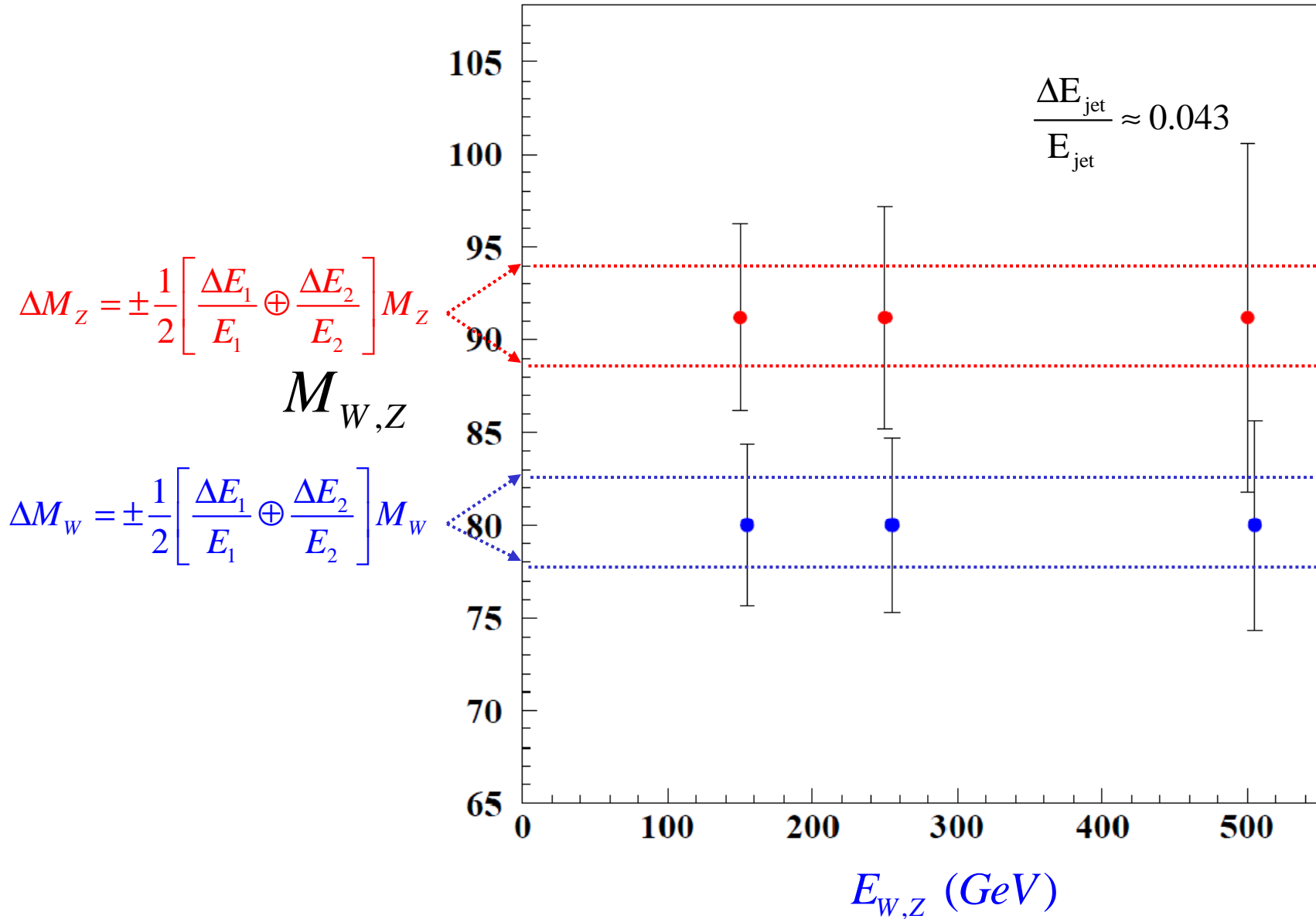
$$r = \frac{E_1}{E_2}$$

How important are the $\frac{\Delta \theta}{\theta}$, $\frac{\Delta m_1}{m_1}$, $\frac{\Delta m_2}{m_2}$ terms?

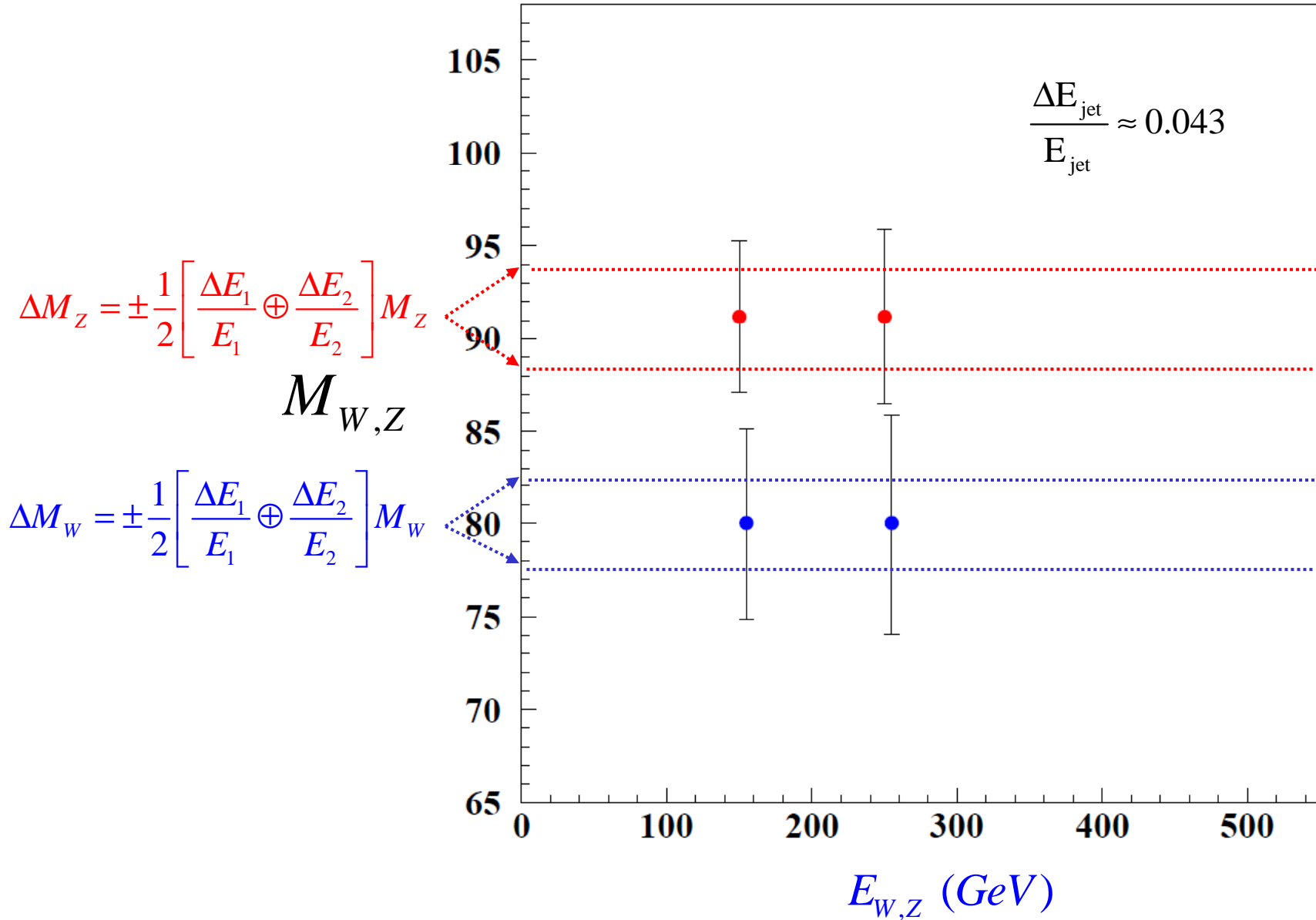
At least in the FASTMC, the $\frac{\Delta\theta}{\theta}$, $\frac{\Delta m_1}{m_1}$, $\frac{\Delta m_2}{m_2}$ terms are as important:



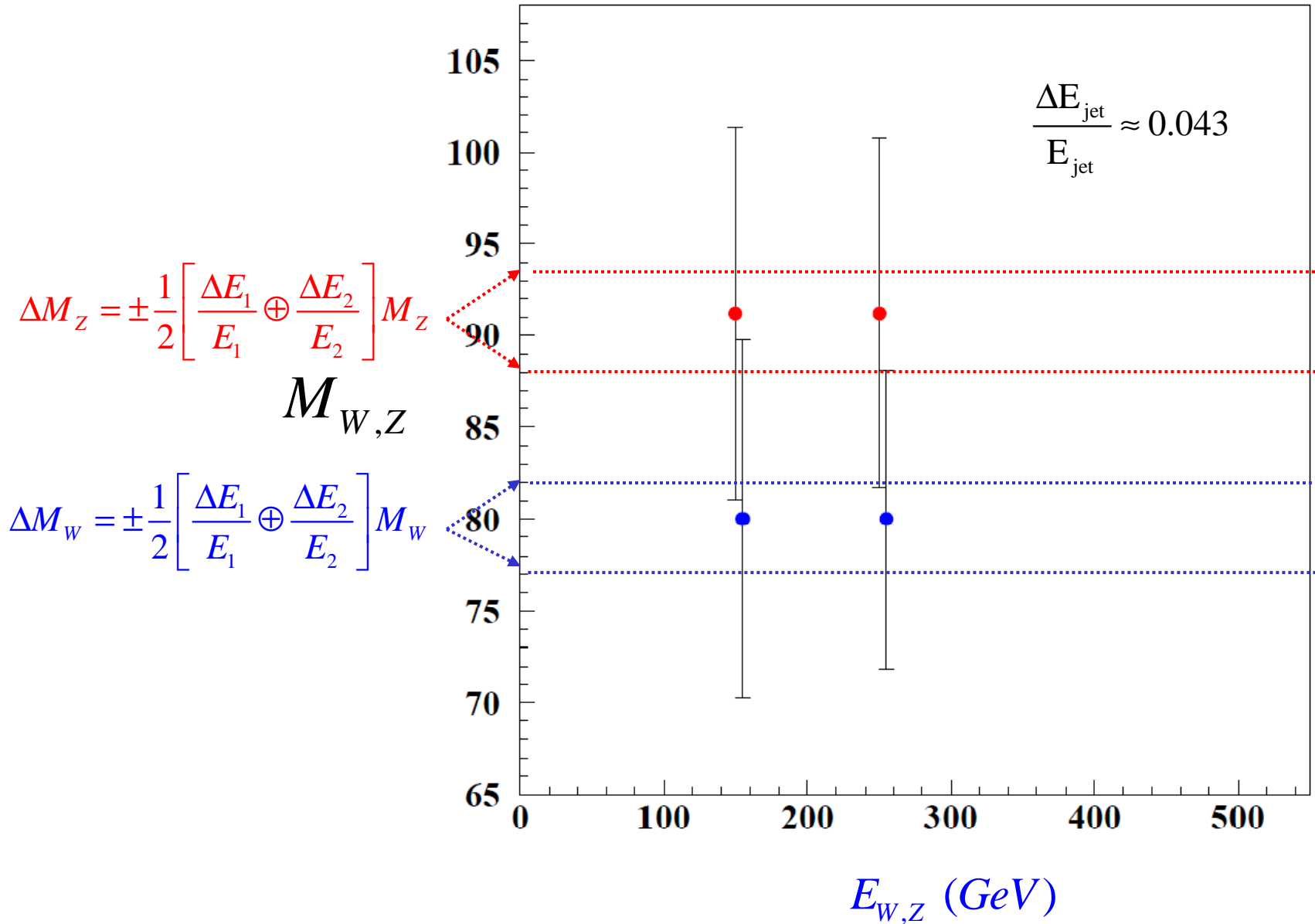
Back to back W Z \rightarrow 4 jets no gluon radiation



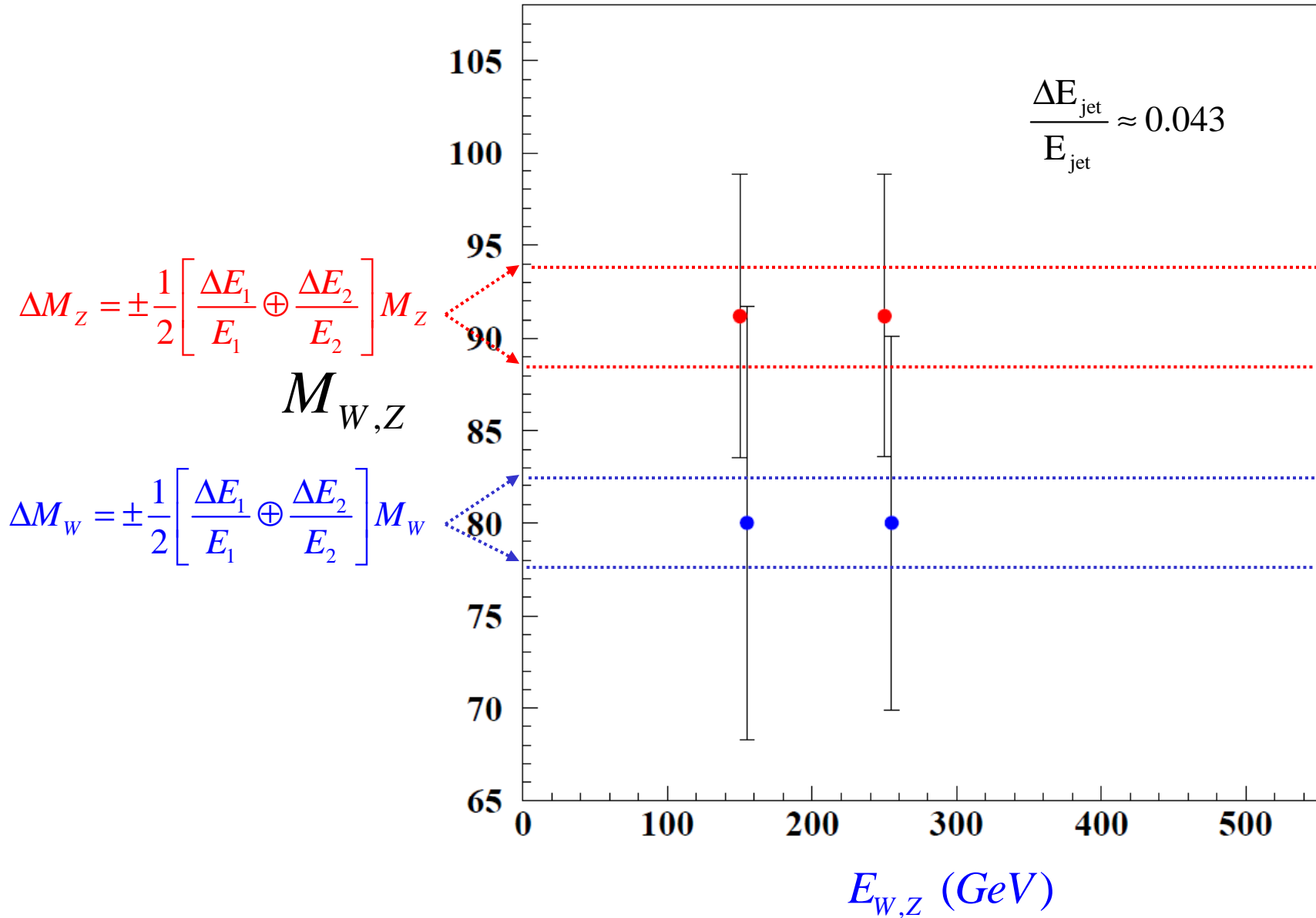
Collinear W Z \rightarrow 4 jets no gluon radiation



Back to back W Z \rightarrow 4 jets yes gluon radiation



Collinear W Z \rightarrow 4 jets yes gluon radiation

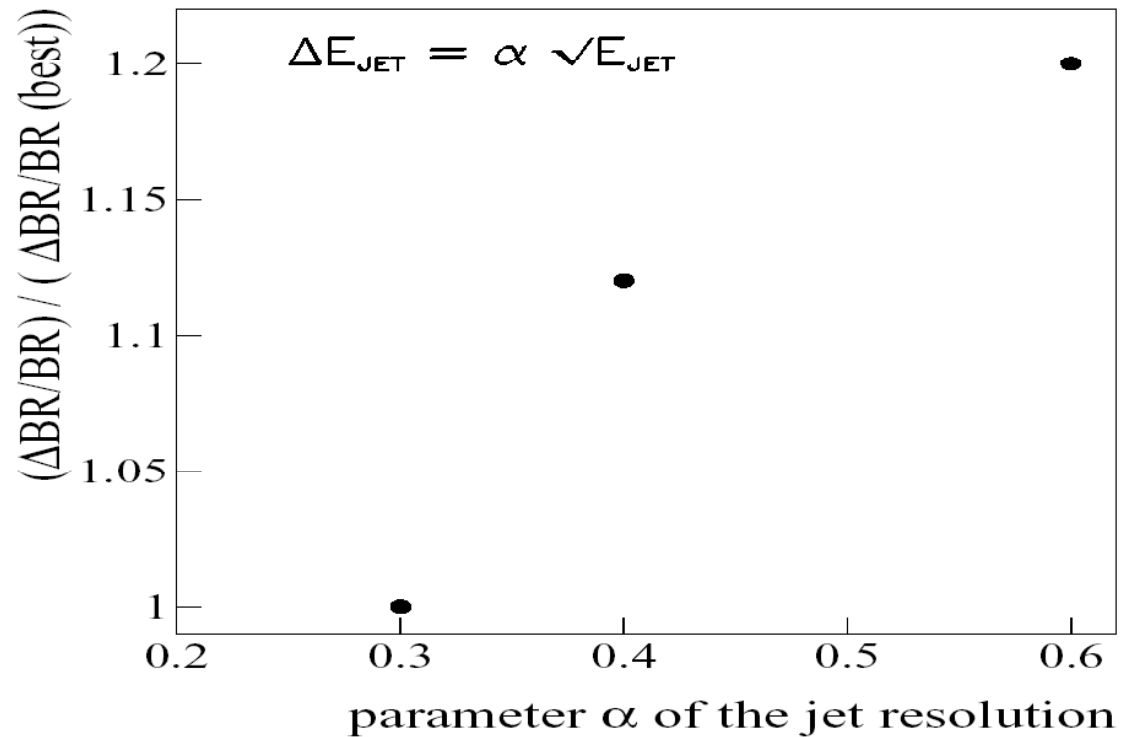


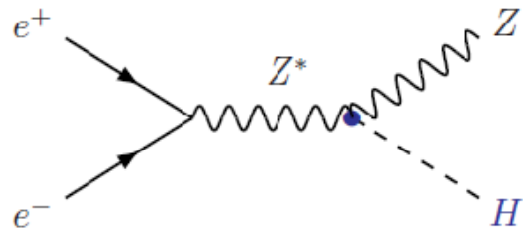
Error on $BR(H \rightarrow WW^*)$ from measurement of

$e^+e^- \rightarrow ZH \rightarrow q\bar{q}WW^* \rightarrow q\bar{q}q\bar{q}l\nu$ at $\sqrt{s} = 360$ GeV, $L=500$ fb $^{-1}$

J.-C. Brient, LC-PHSM-2004-001

$\Delta E/\sqrt{E} = 60\% \rightarrow 30\%$
equiv to $1.4 \times$ Lumi





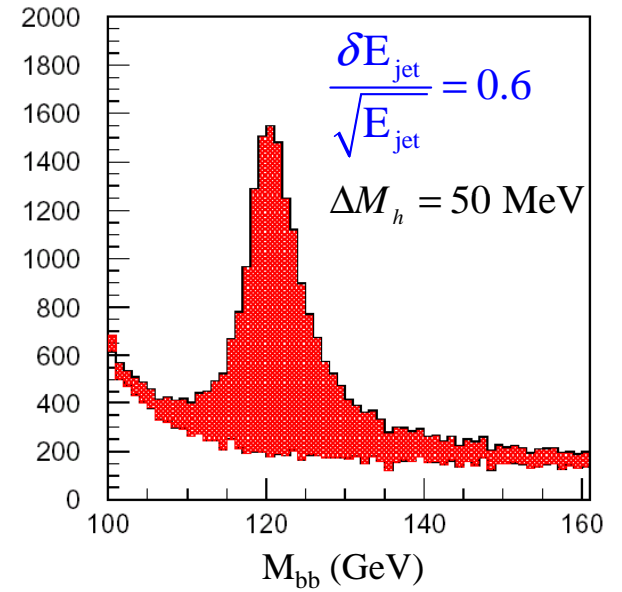
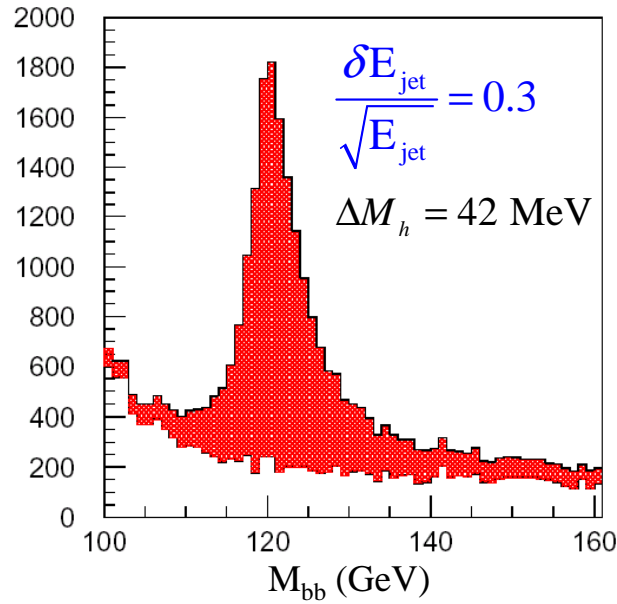
$$e^+ e^- \rightarrow ZH$$

$$\rightarrow qq b \bar{b}$$

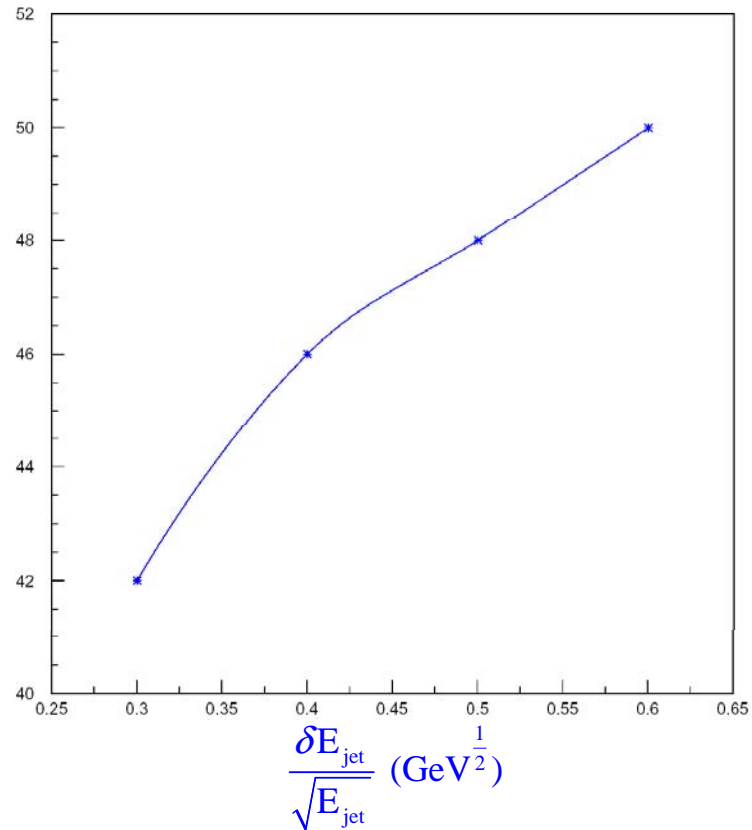
$$\sqrt{s} = 350 \text{ GeV}$$

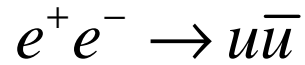
$$L = 500 \text{ fb}^{-1}$$

$\Delta E/\sqrt{E} = 60\% \rightarrow 30\%$
equiv to $1.4 \times \text{Lumi}$



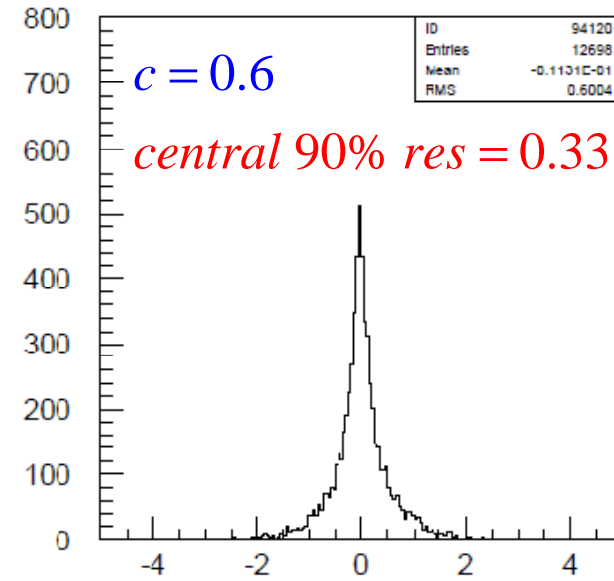
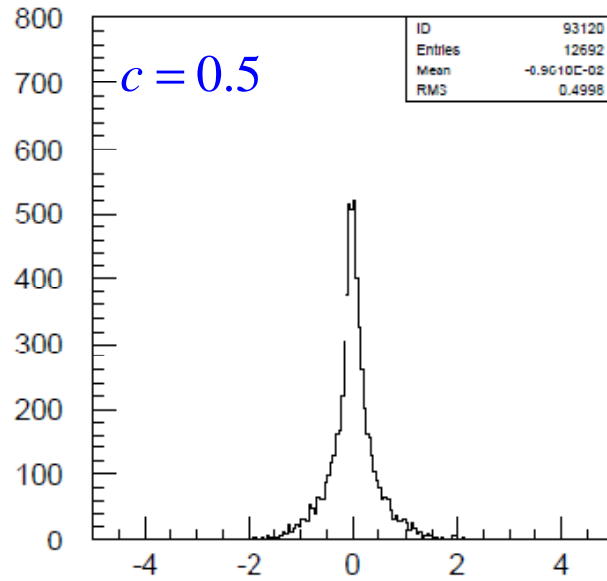
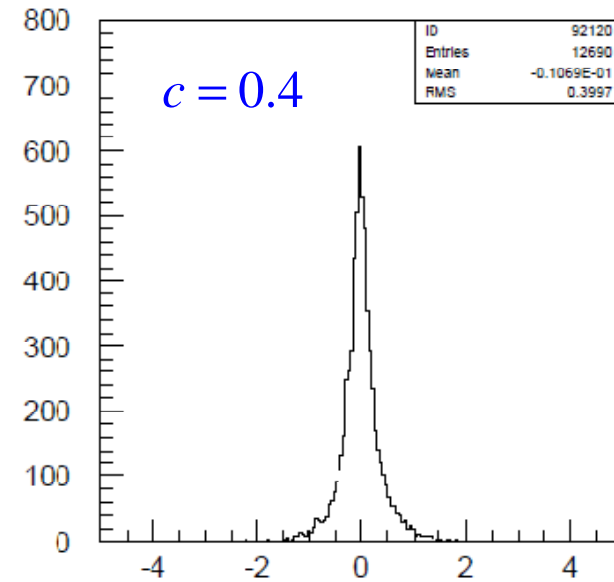
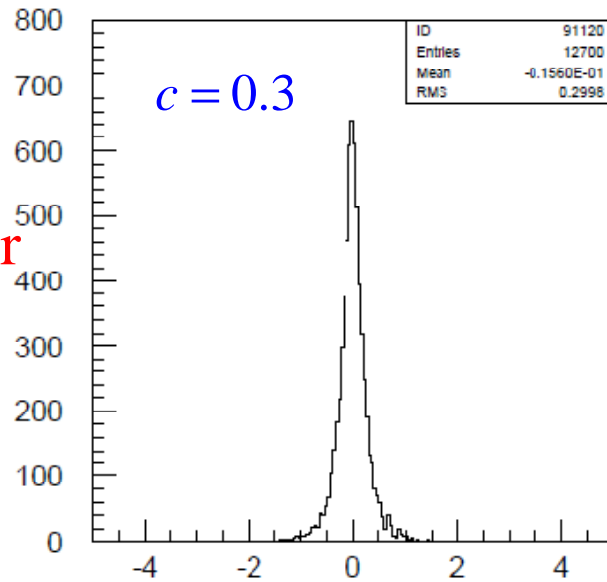
ΔM_h (MeV)





$\sqrt{s} = 500 \text{ GeV}$

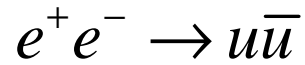
Always use tracker
momentum for
chrg had.



org.lcsim Fast MC

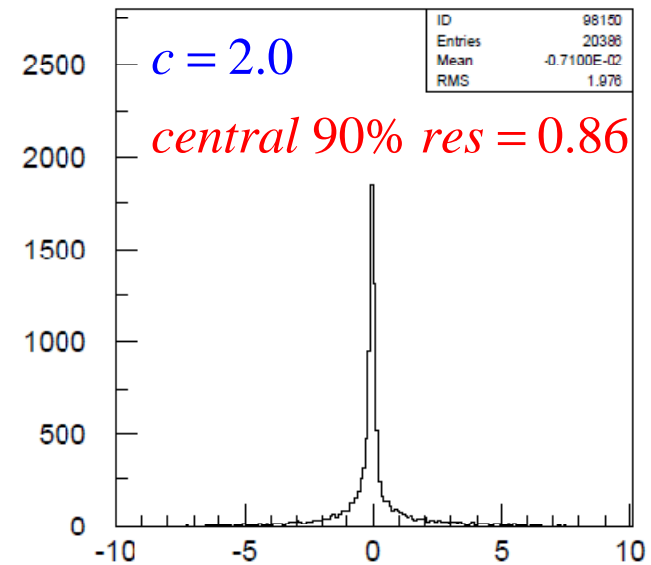
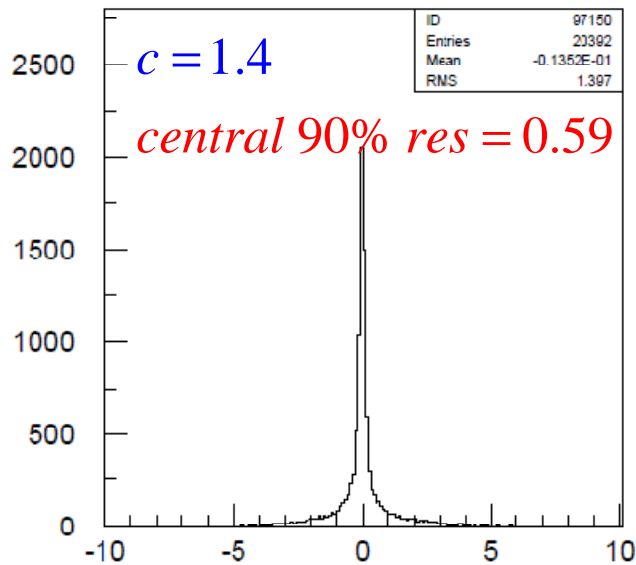
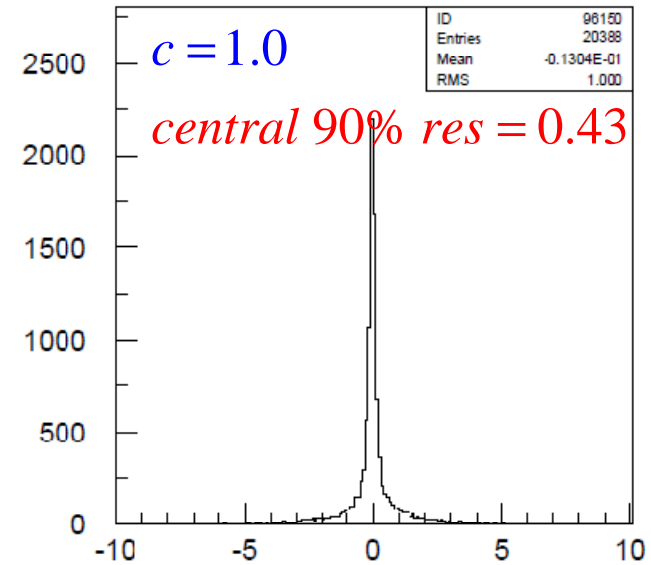
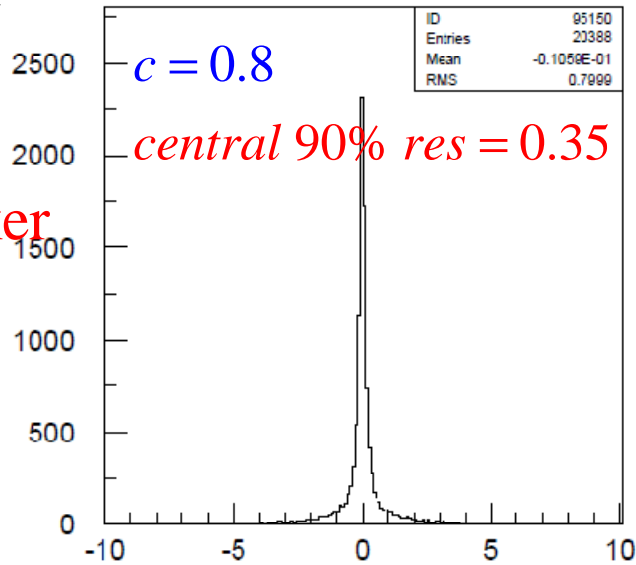
$$\Delta E_{jet} = (E_{rec} - E_{true}) / \sqrt{E_{true}}$$

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$\sqrt{s} = 500 \text{ GeV}$

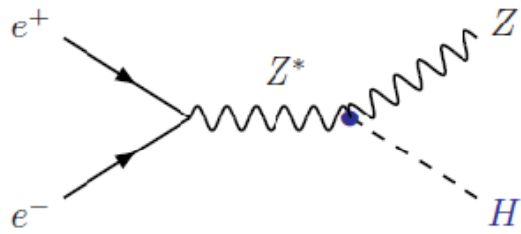
Always use tracker
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$$\Delta E_{jet} = (E_{rec} - E_{true}) / \sqrt{E_{true}}$$

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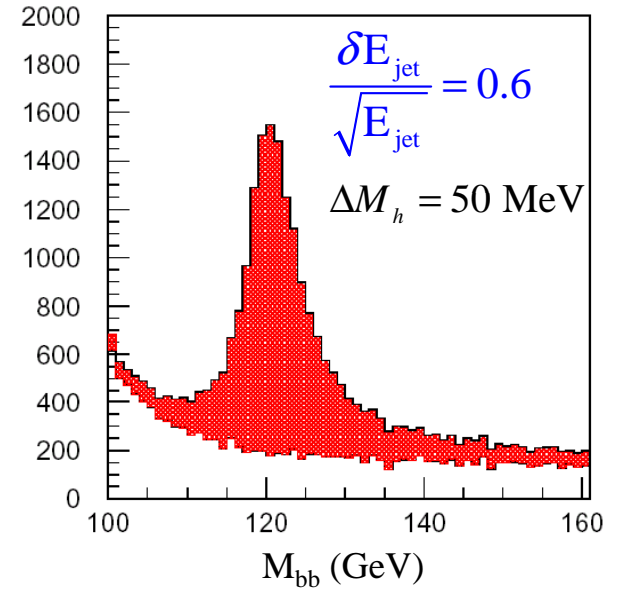
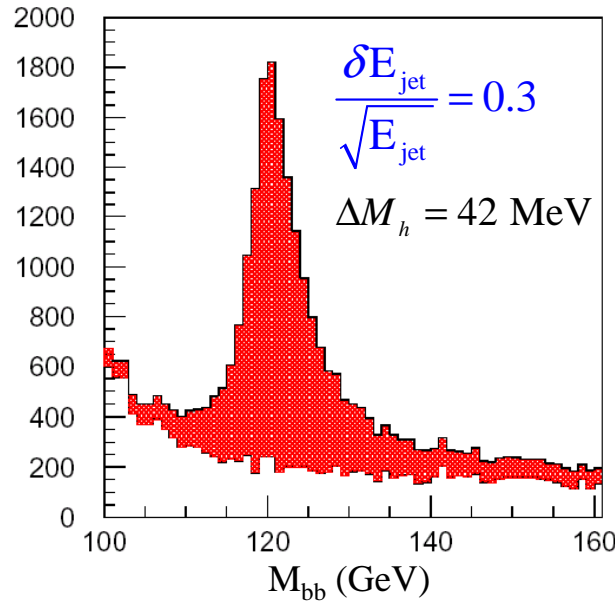


$$e^+ e^- \rightarrow ZH$$

$$\rightarrow qq b \bar{b}$$

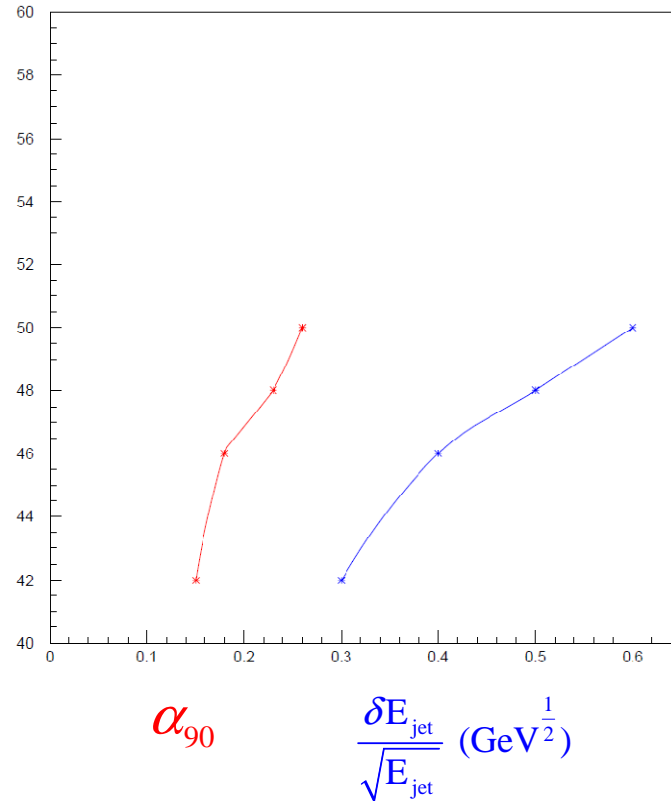
$$\sqrt{s} = 350 \text{ GeV}$$

$$L = 500 \text{ fb}^{-1}$$

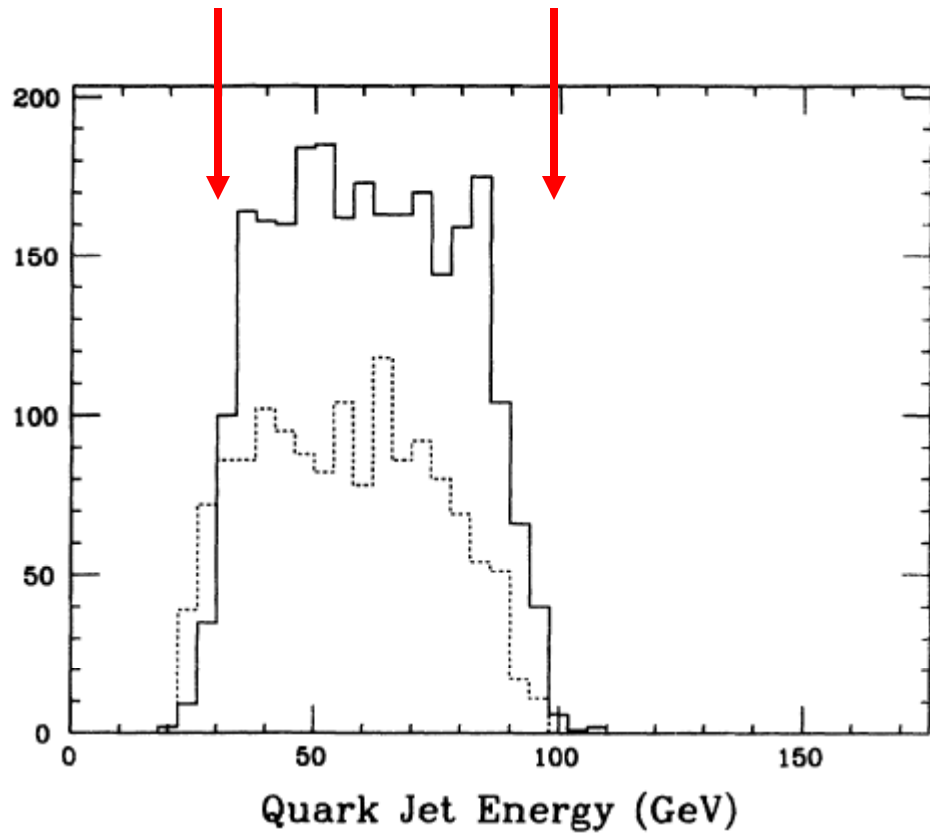


ΔM_h (MeV)

$\Delta E/\sqrt{E} = 60\% \rightarrow 30\%$
equiv to $1.4 \times \text{Lumi}$



E.g., the simple squark $\rightarrow q \chi$ two-body decay leads to the familiar 'table' structure. The rate depends on the specifics of the mass spectrum and the beam polarization.



$$\delta m/m \sim 0.5 \delta E/E$$

For $m \sim 400$ GeV
and $\delta E/E = 5\%$,
 $\delta m \sim 10$ GeV??
which is not too
much of an
improvement !!

Problem ???

The end points tell us the squark mass

Feng & Finnell '93

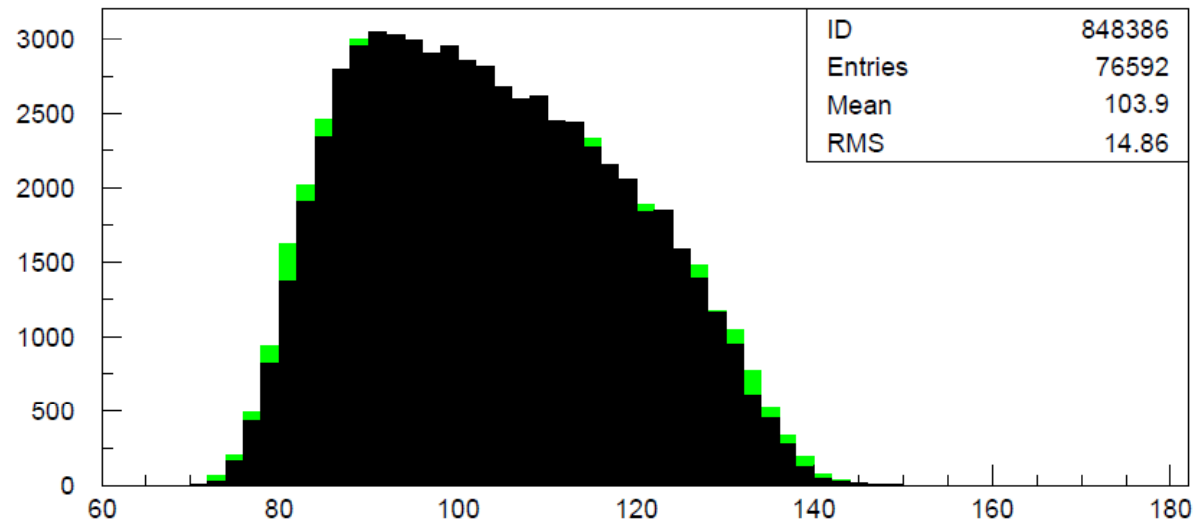
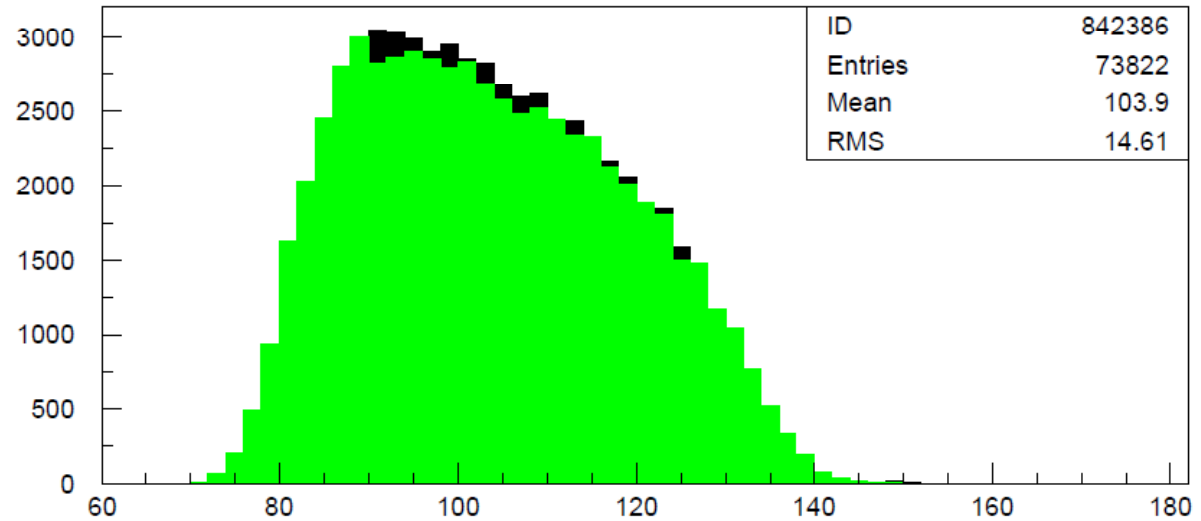
$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 W^+ W^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qqqq$$

$$M_{\tilde{\chi}_1^0} = 106.2 \text{ GeV}$$

$$\sqrt{s} = 500 \text{ GeV}$$

■ $M_{\tilde{\chi}_1^+} = 198.4 \text{ GeV}$

■ $M_{\tilde{\chi}_1^+} = 200.4 \text{ GeV}$



E_W (GeV)

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 W^+ W^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qqqq$$

$$M_{\tilde{\chi}_1^+} = 199.4 \text{ GeV}$$

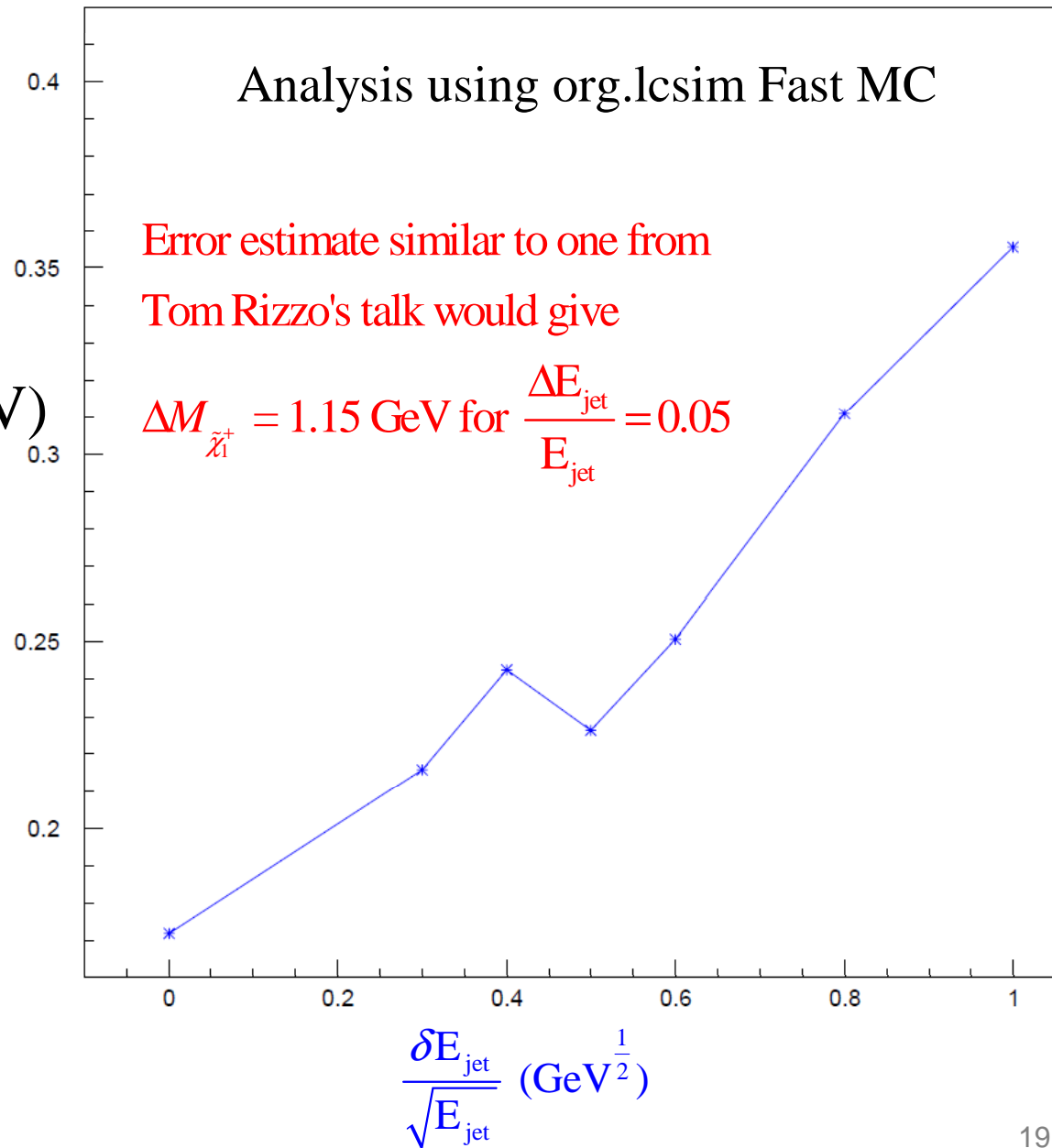
$$M_{\tilde{\chi}_1^0} = 106.2 \text{ GeV}$$

$$\sqrt{s} = 500 \text{ GeV}$$

$$L = 500 \text{ fb}^{-1}$$

$$\Delta M_{\tilde{\chi}_1^+} \text{ (GeV)}$$

$\Delta E/\sqrt{E} = 60\% \rightarrow 30\%$
equiv to $1.4 \times \text{Lumi}$



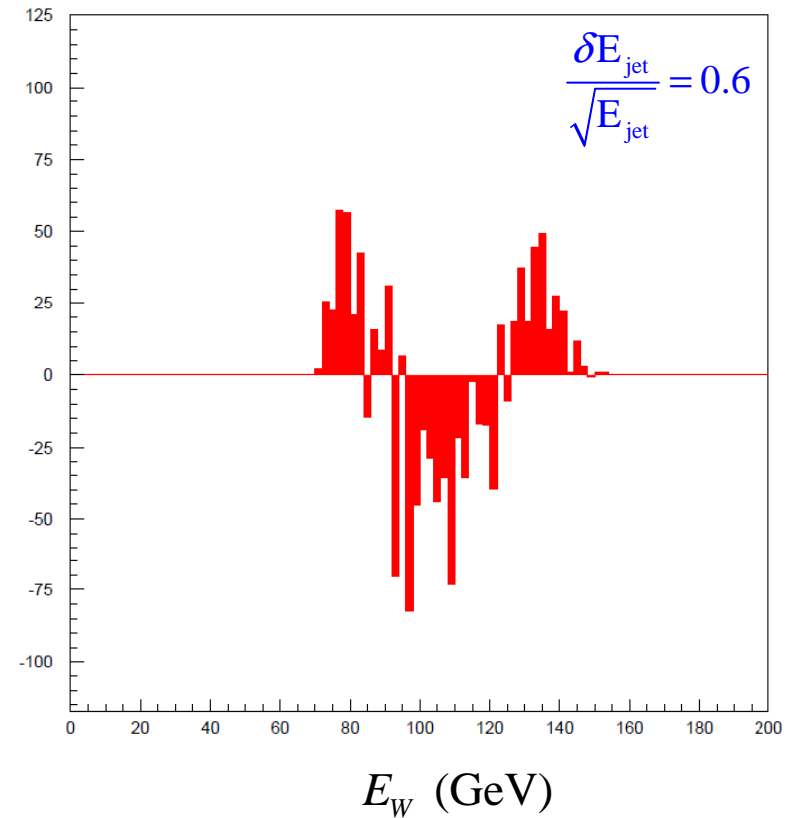
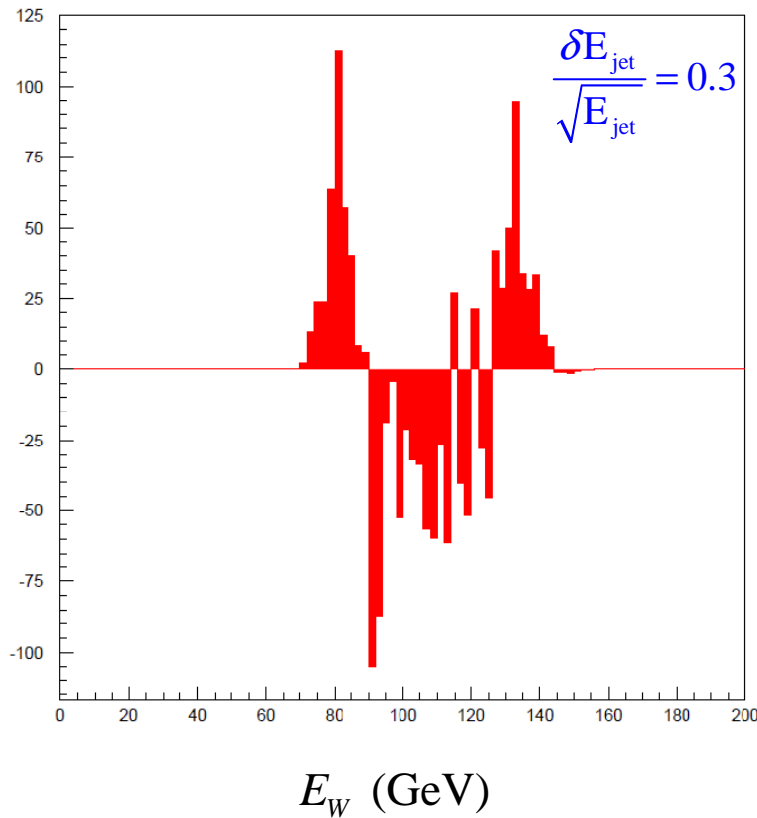
$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 W^+ W^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qqqq$$

$$M_{\tilde{\chi}_1^+} = 199.4 \text{ GeV}$$

$$M_{\tilde{\chi}_1^0} = 106.2 \text{ GeV}$$

$$\sqrt{s} = 500 \text{ GeV}$$

$$\frac{dN_{bin}}{dM_{\tilde{\chi}_1^+}}$$



$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 W^+ W^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qqqq$$

$$M_{\tilde{\chi}_1^+} = 199.4 \text{ GeV}$$

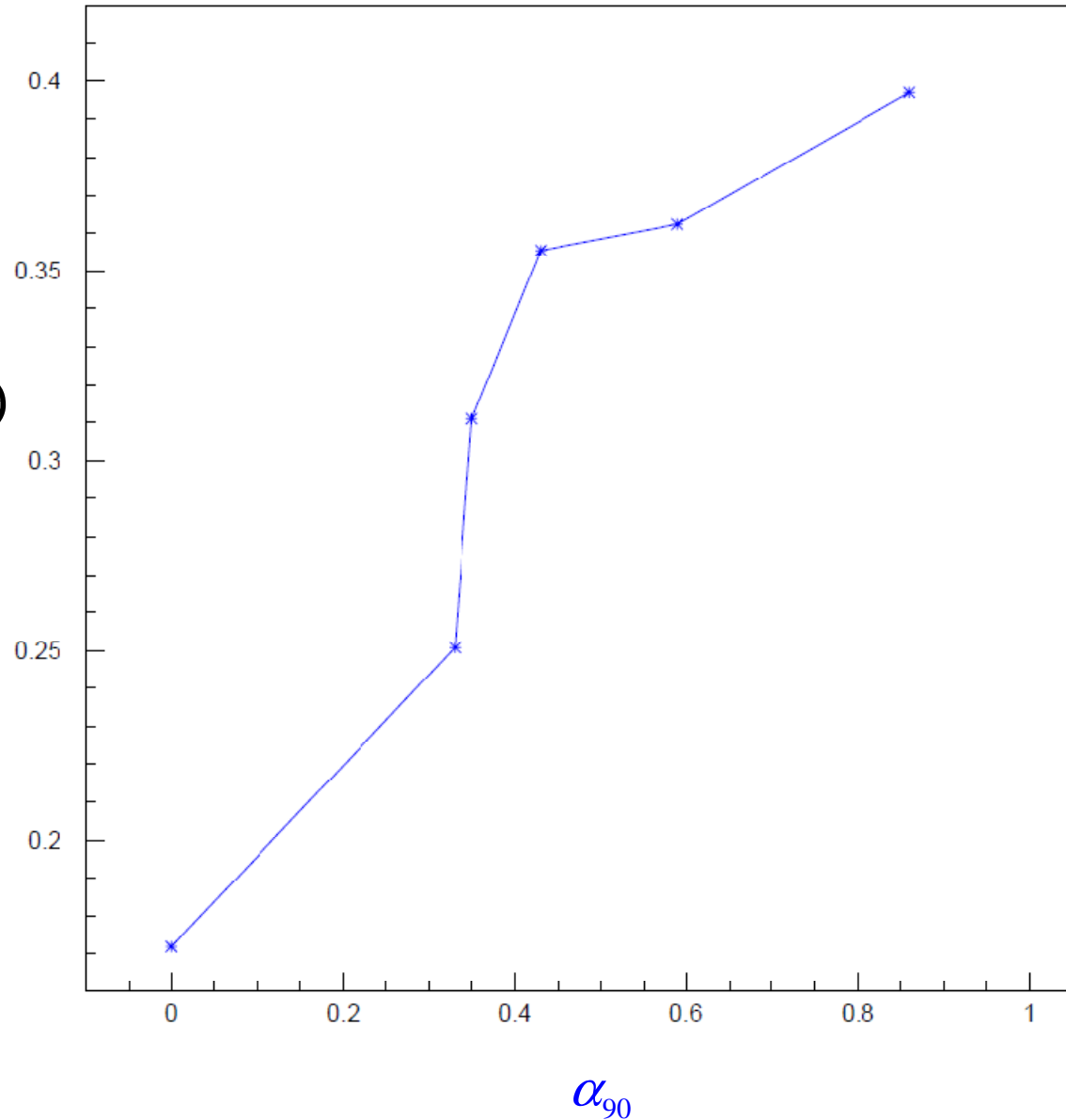
$$M_{\tilde{\chi}_1^0} = 106.2 \text{ GeV}$$

$$\sqrt{s} = 500 \text{ GeV}$$

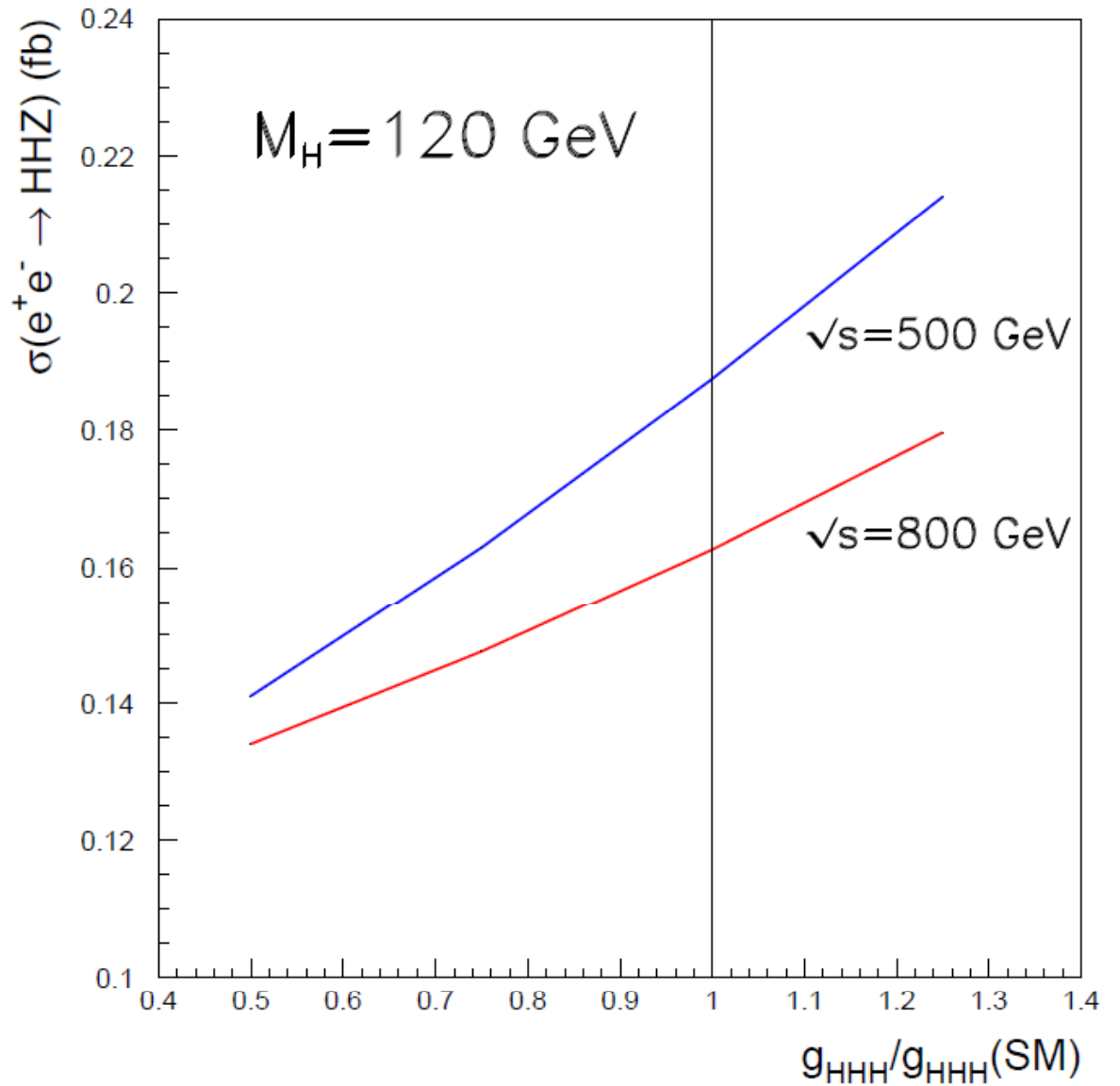
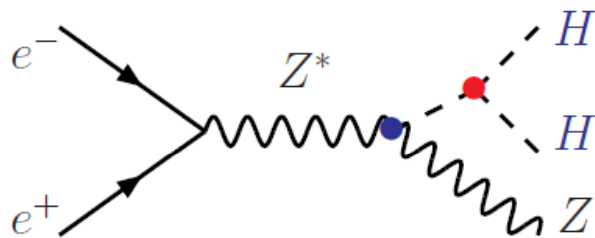
$$L = 500 \text{ fb}^{-1}$$

$$\Delta M_{\tilde{\chi}_1^+} \text{ (GeV)}$$

$\Delta E/\sqrt{E} = 60\% \rightarrow 30\%$
equiv to $2.1 \times \text{Lumi}$

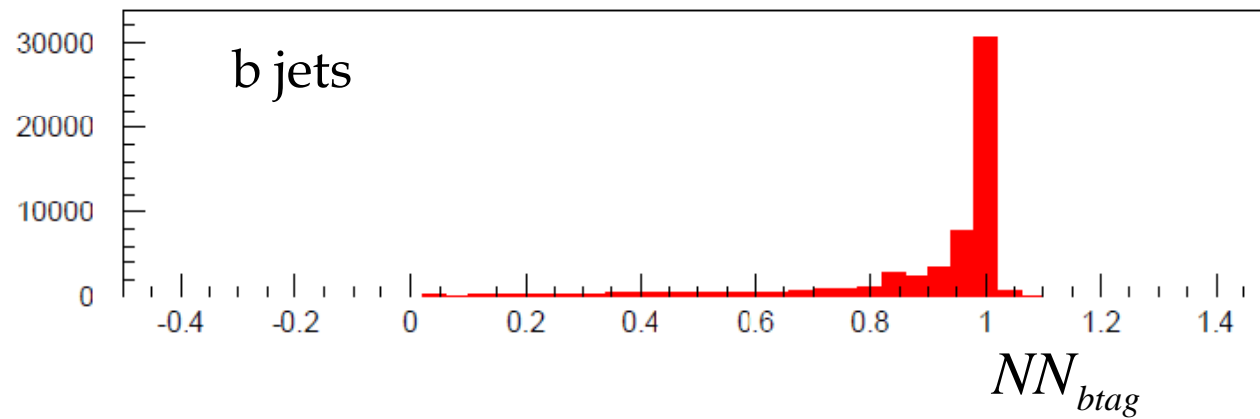
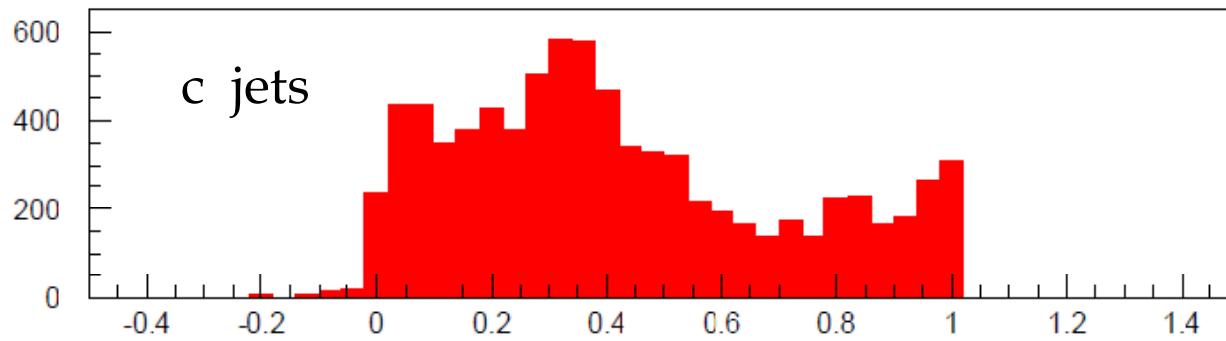
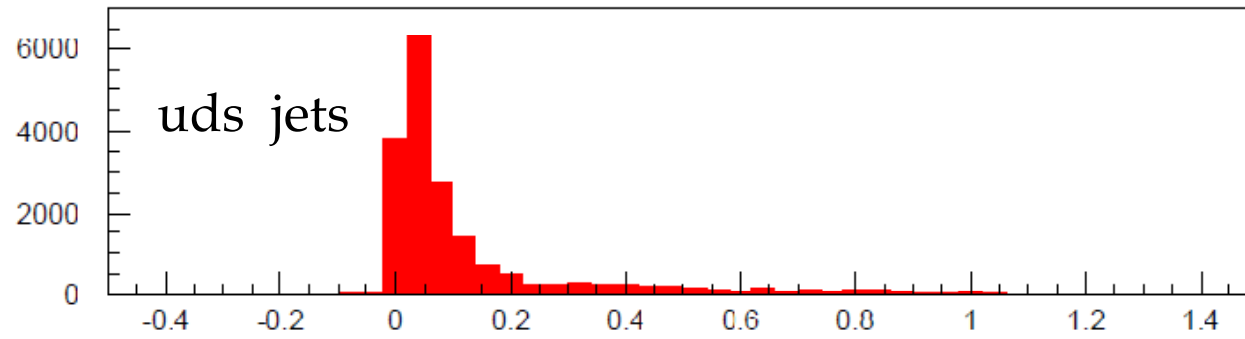


$$e^+e^- \rightarrow ZHH \rightarrow q\bar{q}b\bar{b}b\bar{b}$$



ZHH events

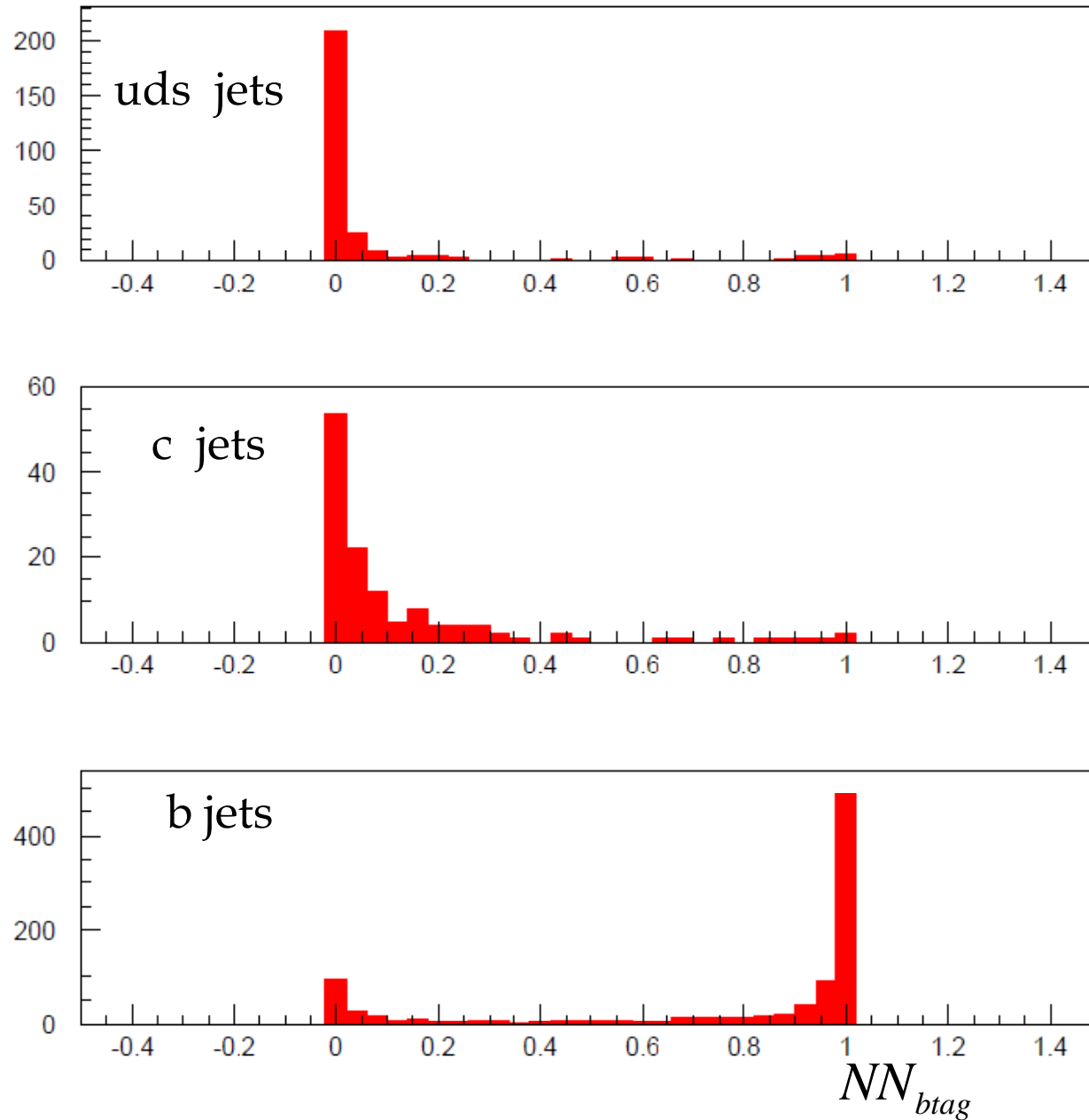
My btag NN



ZHH events

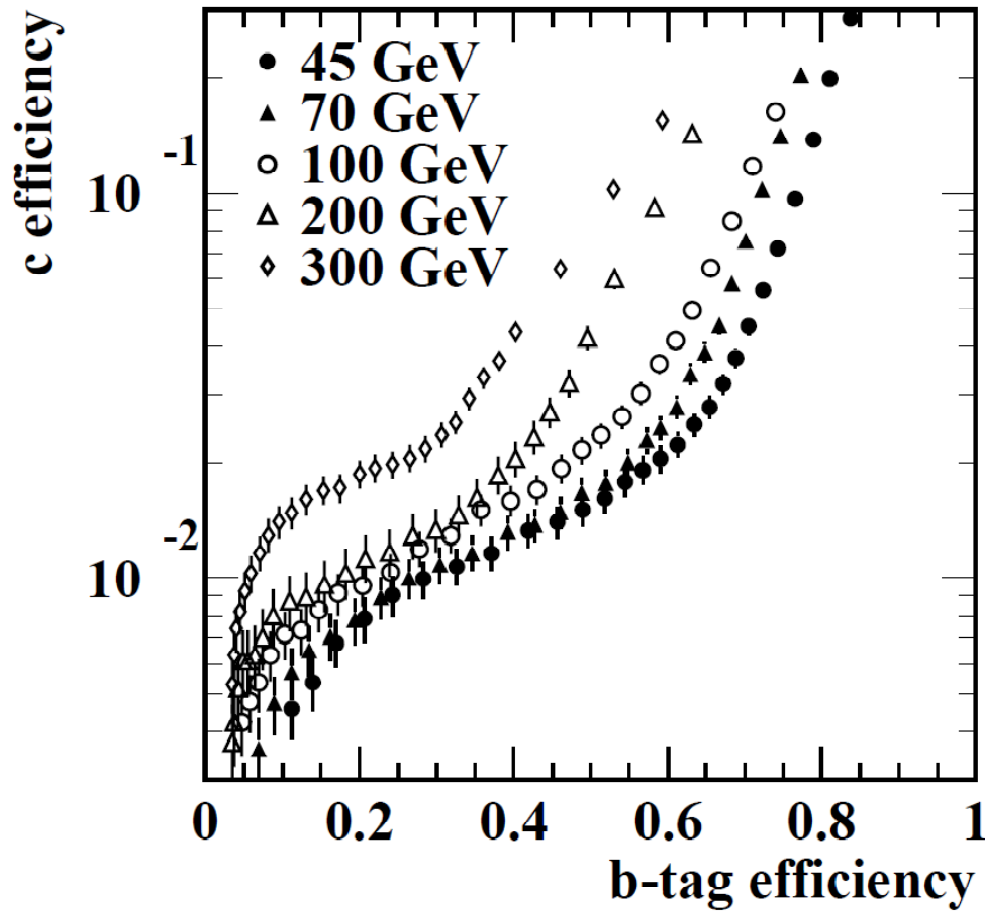
LCFI btag NN

much improved performance but 5s/ev

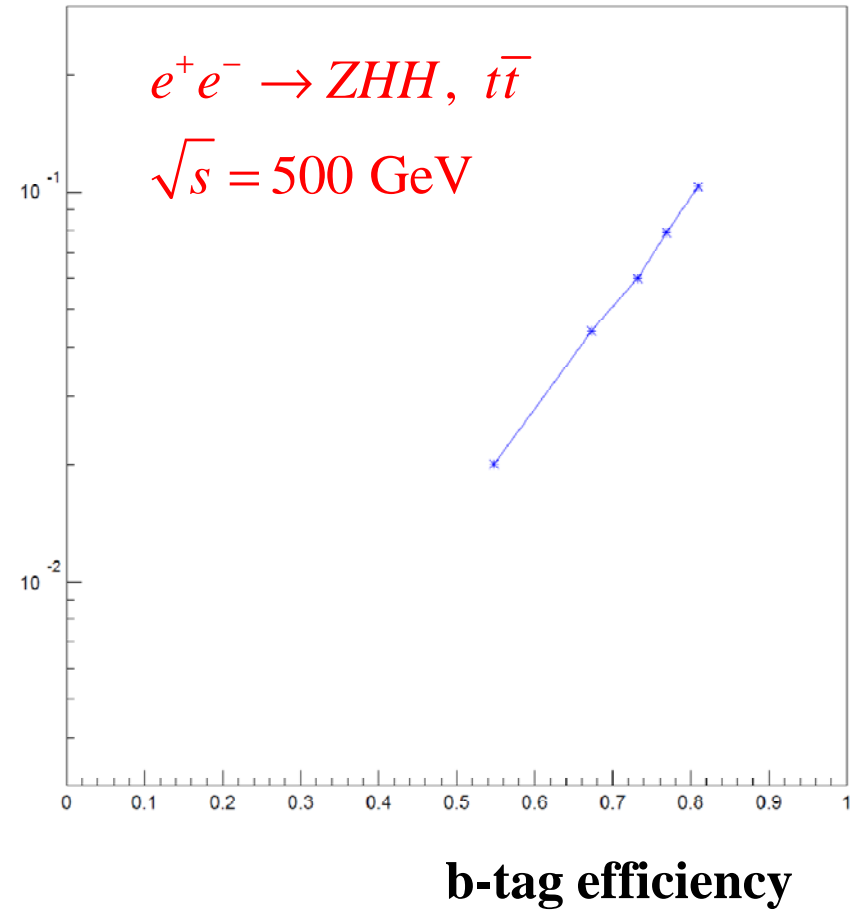


charm mis-id efficiency versus b-tag efficiency

R. Hawkings, LC-PHSM-2000-021



SiD ZHH Analysis



$$\text{BR}(H \rightarrow b\bar{b})=0.678$$

$$e^+e^- \rightarrow ZHH$$

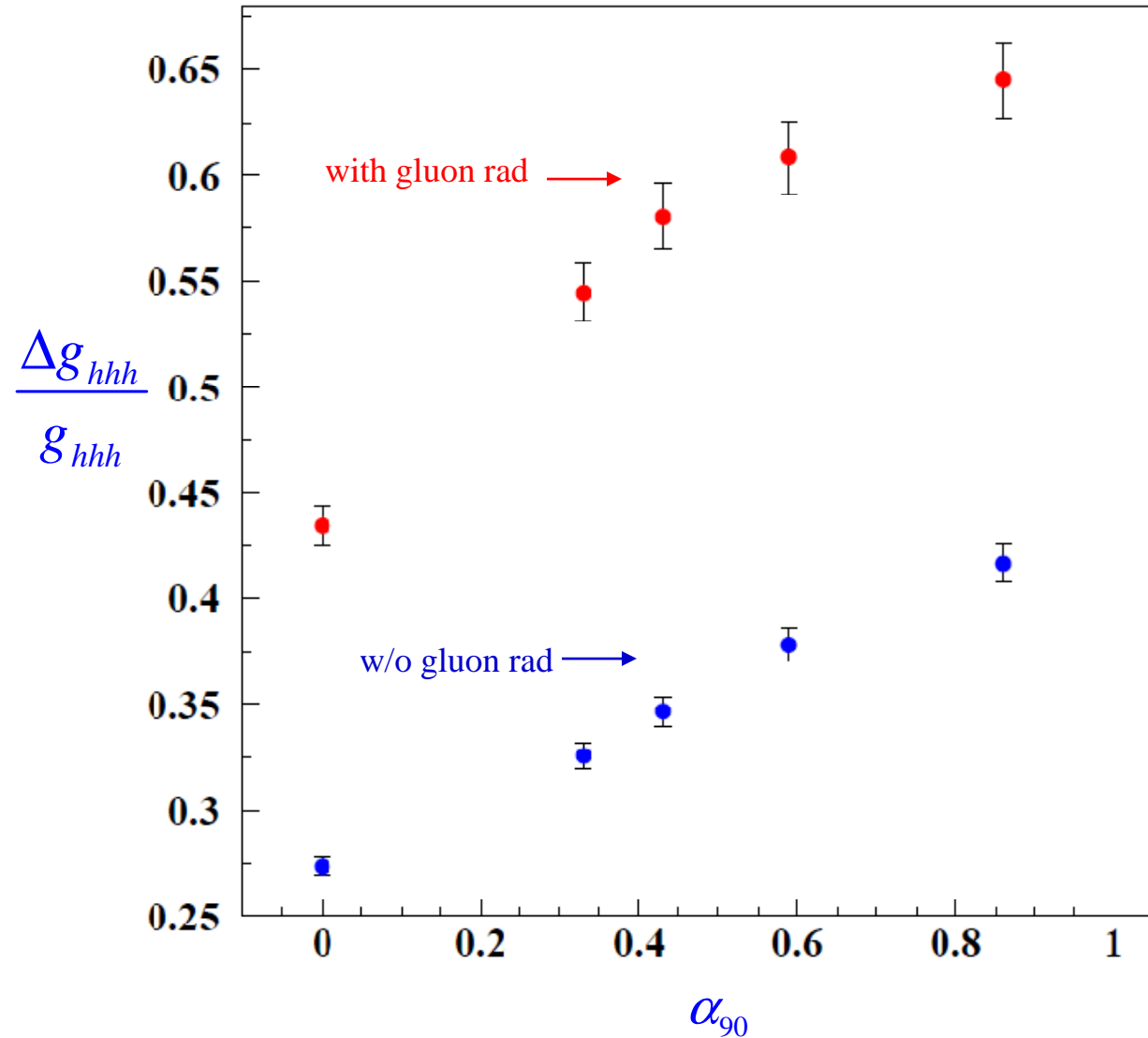
$$\rightarrow qq\bar{b}b\bar{b}\bar{b}$$

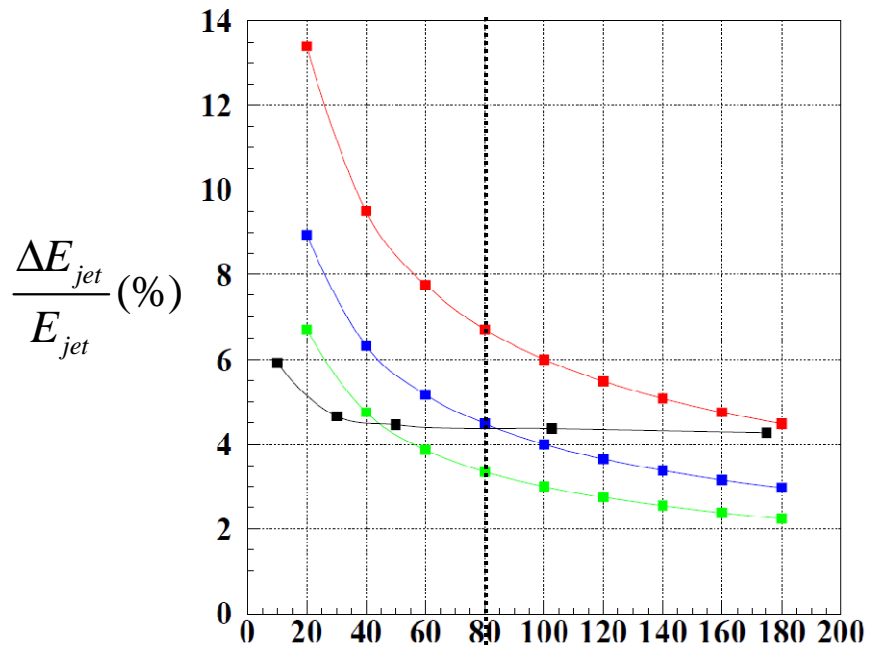
$$\sqrt{s} = 500 \text{ GeV}$$

$$L = 2000 \text{ fb}^{-1}$$

$$\Delta E/\sqrt{E} = 60\% \rightarrow 30\%$$

equiv to $1.4 \times \text{Lumi}$



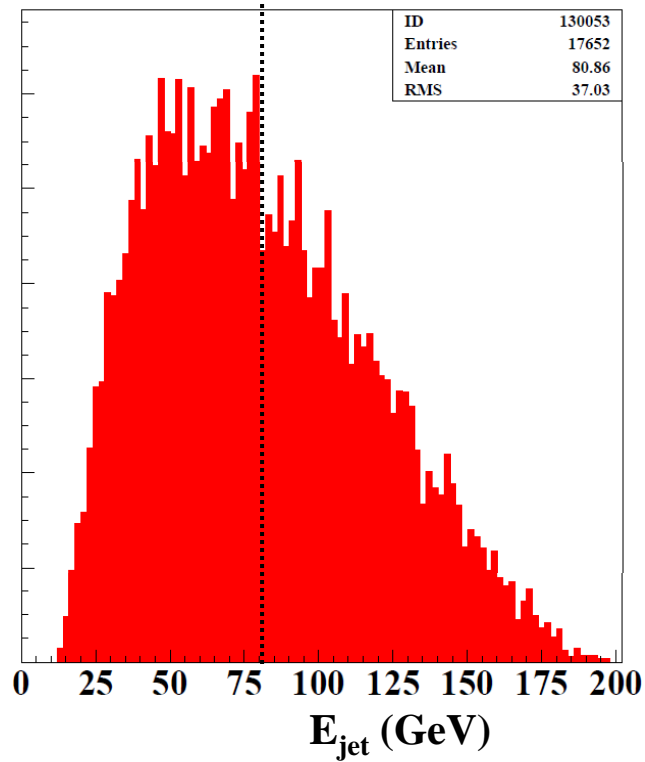


$$\frac{\Delta E_{jet}}{E_{jet}} = \frac{0.6}{\sqrt{E_{jet}}}$$

$$\frac{\Delta E_{jet}}{E_{jet}} = \frac{0.4}{\sqrt{E_{jet}}}$$

$$\frac{\Delta E_{jet}}{E_{jet}} = \frac{0.3}{\sqrt{E_{jet}}}$$

$$\frac{\Delta E_{jet}}{E_{jet}} \approx \text{PFA Current Status}$$



True Jet Energy Distribution for
 $e^+e^- \rightarrow ZHH \rightarrow q\bar{q}b\bar{b}b\bar{b}$
 at $\sqrt{s} = 500$ GeV

Analysis must be redone with $\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}}$ that reflects current PFA status.

For now replot triple Higgs coupling error vs. $\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}}$ using existing results with $\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}} \equiv \frac{\alpha_{90}}{\sqrt{80}}$

$$\text{BR}(H \rightarrow b\bar{b}) = 0.678$$

$$e^+e^- \rightarrow ZHH$$

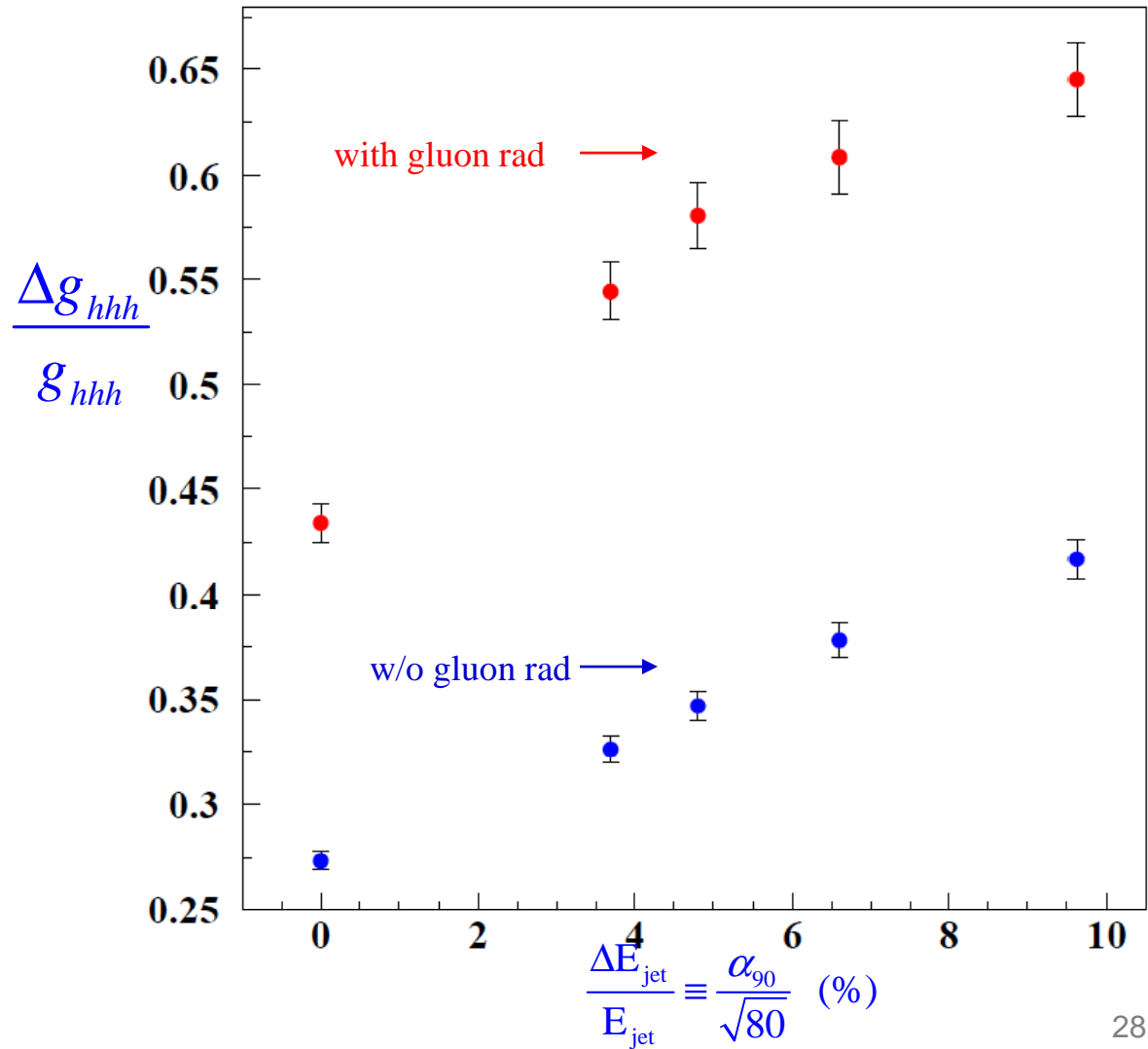
$$\rightarrow qqbb\bar{b}\bar{b}$$

$$\sqrt{s} = 500 \text{ GeV}$$

$$L = 2000 \text{ fb}^{-1}$$

$$\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}} = .067 \rightarrow .033$$

equiv to $1.4 \times \text{Lumi}$



Analysis has now been redone with $\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}}$ that reflects current PFA status

triple Higgs coupling error vs. genuine $\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}}$ is plotted in BLACK

$$\text{BR}(H \rightarrow b\bar{b})=0.678$$

$$e^+e^- \rightarrow ZHH \\ \rightarrow qq b\bar{b} b\bar{b}$$

$$\sqrt{s} = 500 \text{ GeV} \\ L = 2000 \text{ fb}^{-1}$$

$$\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}} = .067 \rightarrow .033 \\ \text{equiv to } 1.4 \times \text{Lumi}$$

$$\frac{\Delta g_{hhh}}{g_{hhh}}$$

