



# Higgs Recoil Mass and Cross Section Analysis at ILD\_00

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# Introductory Remarks

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## ZH Recoil Ana. Group:

(EU) Hengne Li, Roman Poeschl, Francois Richard, Manqi Ruan, Zhiqing Zhang

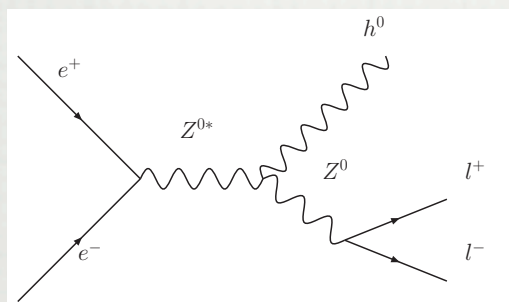
(JP) Kazutoshi Ito, Yosuke Takubo, Hitoshi Yamamoto

## Reviewers:

(EU) Klaus Desch, (JP) Akiya Miyamoto

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### - Higgs-Strahlung Process:



### - Higgs Recoil Mass:

$$m_{h^0}^2 = s + m_{Z^0}^2 - 2E_{Z^0} \sqrt{s}$$

### - Cross Section and Coupling Strength Measurement:

$$g^2 \propto \sigma = N/\mathcal{L}\epsilon$$

- $M_H = 120 \text{ GeV}$
- $E_{cm} = 250 \text{ GeV}$
- Beam Energy Spread: 0.3% for each beam
- Beamstrahlung: N/A <sup>(a)</sup>
- Luminosity: 250 fb<sup>-1</sup>
- Polarization:
  - $e^-_R e^+_L$ : ( $e^-$ : +80%,  $e^+$ : -30%)
  - $e^-_L e^+_R$ : ( $e^-$ : -80%,  $e^+$ : +80%)
- Detector Model: ILD\_00
- Event Generation:
  - WIZARD v1.40 (by SLAC)
- Simulation & Reconstruction:
  - ILCSOFT v01-06 (by DESY & KEK)

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<sup>(a)</sup> Discussed in the conclusions

# Introductory Remarks

**$e^-_R e^+_L$**

**$\mu\mu X$**

Reactions	Cross-Section
$\mu\mu X$	<b>7.02 fb</b>
$\mu\mu$	10.44 pb (137.71 fb)
$\tau\tau$	8117.53 fb
$\mu\mu\nu\nu$	56.10 fb
$\mu\mu ff$	1194.20 fb

**$eeX$**

Final State	Cross-Section
$eeX$	<b>7.48 fb</b>
$ee$	17.30 nb (650.894fb)
$\tau\tau$	8117.53 fb
$ee\nu\nu$	105.49 fb
$eeff$	4148.93 fb

**$e^-_L e^+_R$**

**$\mu\mu X$**

Final State	Cross-Section
$\mu\mu X$	<b>10.40 fb</b>
$\mu\mu$	8.12 pb (200.85 fb)
$\tau\tau$	10454.80 fb
$\mu\mu\nu\nu$	498.28 fb
$\mu\mu ff$	1282.22 fb

**$eeX$**

Final State	Cross-Section
$eeX$	<b>11.11 fb</b>
$ee$	17.30 nb (692.53 fb)
$\tau\tau$	10454.80 fb
$ee\nu\nu$	625.45 fb
$eeff$	4283.07 fb

**Pre-cuts for  $ee$  and  $\mu\mu$ :  
(cross-sections after pre-cuts  
are in blankets)**

Pre-cuts for  $\mu\mu$ :

- $M_{\mu^+\mu^-} \in (71.18, 111.18) \text{ GeV}$
- $P_{T\mu^+\mu^-} > 10 \text{ GeV}$
- $M_{recoil} \in (105, 165) \text{ GeV}$

Pre-cuts for  $ee$ :

- $|\cos\theta_{e^+e^-}| < 0.95$
- $M_{e^+e^-} \in (71.18, 111.18) \text{ GeV}$
- $P_{Te^+e^-} > 10 \text{ GeV}$
- $M_{recoil} \in (105, 165) \text{ GeV}$

(1)  $\mu\mu\nu\nu$  and  $ee\nu\nu$  have major contribution from WW, but also from ZZ.

(2)  $\mu\mu ff$  refers to  $\mu\mu ee + \mu\mu\mu\mu + \mu\mu\tau\tau + \mu\mu qq$ ,  
 $eeff$  refers to  $ee\mu\mu + eeee + ee\tau\tau + eeqq$



# Preparations

## 1) Cuts for lepton ID:

Efficiency of lepton pair ID:  
(pair selection according to  $Z^0$  Mass)

	$\mu$ -Identification	$e$ -Identification
$E_{ECAL}/E_{total}$	$< 0.5$	$> 0.6$
$E_{total}/P_{track}$	$< 0.3$	$> 0.9$

$\mu\mu X$  (muon ID) : 95.4%  
 $eeX$  (electron ID) : 98.8%

## 2) $\Delta P/P^2$ criterion on tracks in the selection of lepton candidates

- Parameterize  $\Delta P/P^2$  for central region

$$\Delta P/P^2 = a \oplus b/P;$$

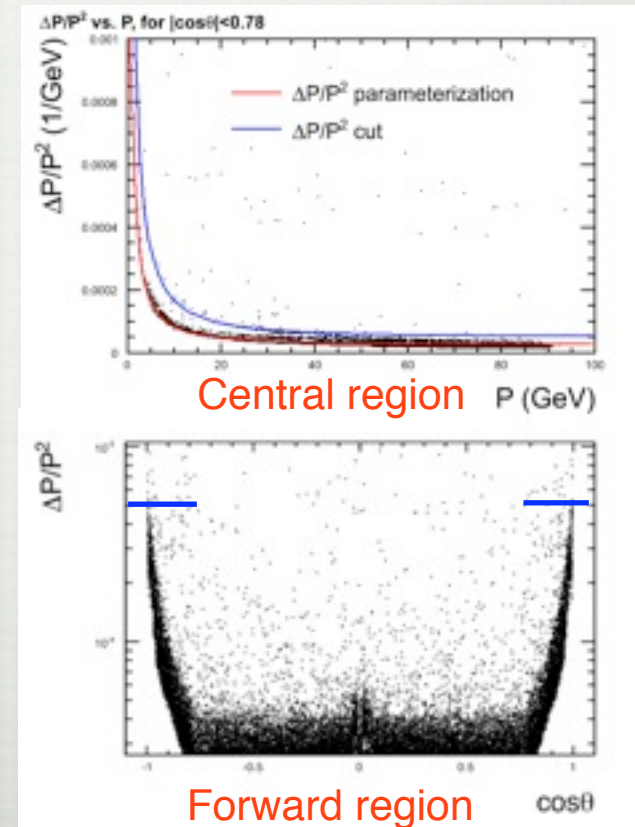
where  $a = 2.5 \times 10^{-5}$ ;  $b = 8 \times 10^{-4}$

- The criterion  $\Delta P/P^2$  applied

$$|\cos\theta| < 0.78 : \quad \Delta P/P^2 < 2 \times (2.5 \times 10^{-5} \oplus 8 \times 10^{-4}/P)$$

$$|\cos\theta| > 0.78 : \quad \Delta P/P^2 < 5 \times 10^{-4}$$

$\Delta P$  is propagated from tracking error matrix



# Analysis Procedures

Higgs Decay Model	Model Independent (MI)	SM Higgs Decay (SM)
Background Rejection	MI Cut-chain	SM Cut-chain
	Likelihood Further Rejection	
Fitting and Results		

- Background Rejection
  - Rejection by Cuts
    - MI Cut-Chain: Independent of Higgs Decay Modes
    - SM Cut-Chain: Assume SM Higgs Decay
  - Further Rejection by Likelihood with Model Independent variables
- Fitting and Results



# Background Rejection by Cuts: MI Cut-Chain

Pol.  $e^-_{\text{RE}} e^+_L$   
for illustration

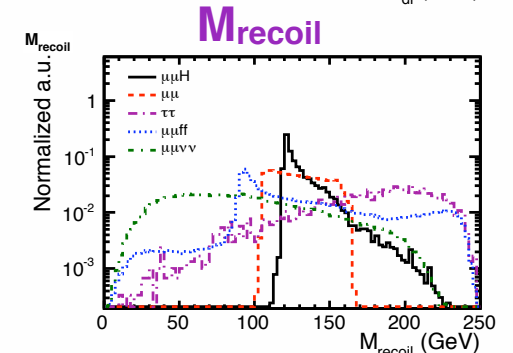
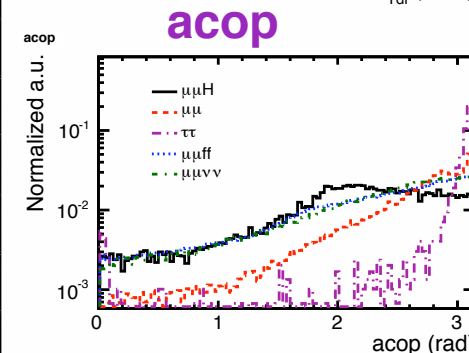
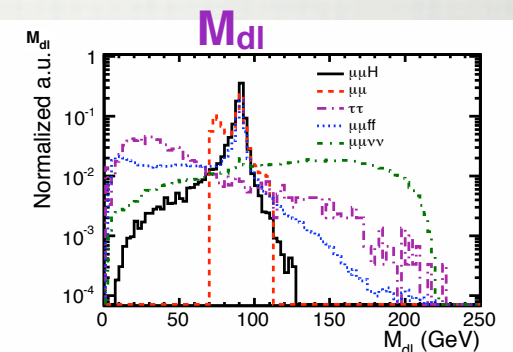
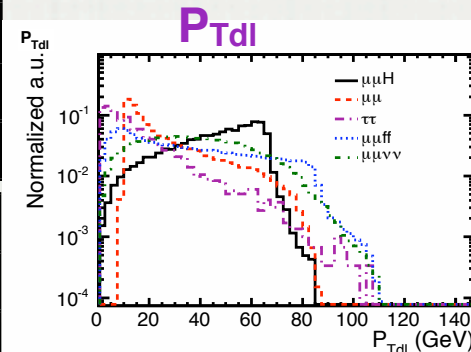
## MI Cut-Chain & Nevts after each cuts:

Nevts remained:	$\mu\mu X$	$\mu\mu$	$\tau\tau$	$\mu\mu\nu\nu$	$\mu\mu\text{ff}$
before any restriction:	1754	2.0M	2.0M	14k	299k
Both $\mu$ id + pre-cuts	1478(84.27%)	30k	4528	2481	10k
+ $P_{Tdl} > 20$ GeV	1402(79.97%)	15k	3139	2223	7390
+ $M_{dl} \in (80, 100)$ GeV	1299(74.10%)	11k	1750	1633	5257
+ $acop \in (0.2, 3.0)$	1211(69.05%)	9402	0	1505	4741
+ $\Delta P_{Tbal.} > 10$ GeV	1188(67.75%)	529	0	1464	4367
+ $ \Delta\theta_{2tk}  > 0.01$	1186(67.65%)	226	0	1448	4340
+ $M_{recoil} \in (115, 150)$ GeV	1156(65.93%)	165	0	900	2729

Nevts remained:	$eeX$	$ee$	$\tau\tau$	$ee\nu\nu$	$ee\text{ff}$
before any restriction:	1869	4.3G	2.0M	26k	1.0M
Both $e$ id + pre-cuts	1172(62.71%)	119k	6778	3155	9430
+ $P_{Tdl} > 20$ GeV	1100(58.86%)	90k	4694	2808	7909
+ $M_{dl} \in (80, 100)$ GeV	937(50.13%)	48k	2556	1929	5317
+ $acop \in (0.2, 3.0)$	879(47.06%)	44k	222	1807	4823
+ $\Delta P_{Tbal.} > 10$ GeV	857(45.88%)	2962	139	1712	4389
+ $ \Delta\theta_{2tk}  > 0.01$	856(45.80%)	1653	111	1692	4365
+ $M_{recoil} \in (115, 150)$ GeV	828 (44.29%)	1230	28	1043	2675

## Cuts based on lepton pair properties:

- $P_{Tdl} > 20$  GeV
- $M_{dl} \in (80, 100)$  GeV
- $acop \in (0.2, 3.0)$
- muon channel with pol.  $e^-_{\text{RE}} e^+_L$  for illustration
- $\mu\mu$  are pre-cutted



# Background Rejection by Cuts: Independent of Higgs Decay Model

## ISR $P_T$ balance for $\mu\mu$ and $ee$ rejection

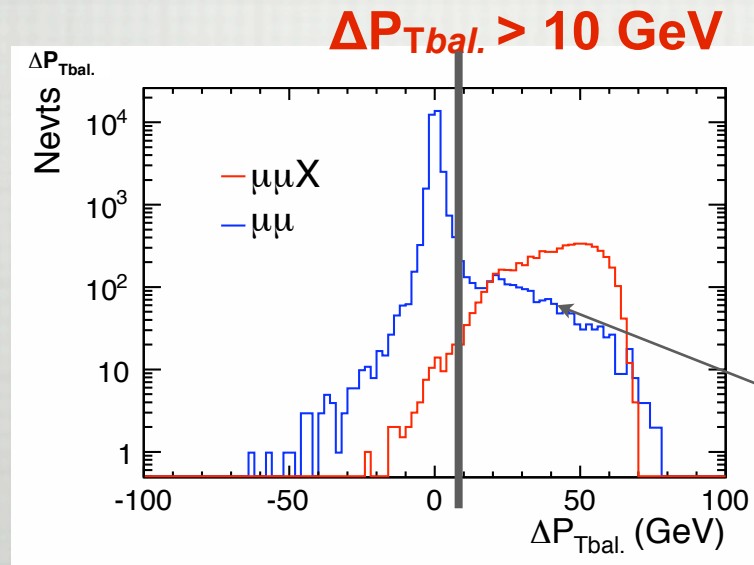
**Idea:** (Thanks to Francois' idea)

- **For  $\mu\mu$  and  $ee$ :**  $P_T$  of ISR photon should balance the  $P_T$  of di-lepton system;
- **For signal:** Impossible to have ISR to balance  $Z$   $P_T$ , independent of Higgs decay model.

**Requirements:**

- **$M_{dl} \in (80, 100)$  GeV:** large FSR events are removed
- **$P_{Tdl} > 20$  GeV:** Large  $P_T$  ISR photon can be detected

**Define  $\Delta P_{Tbal.} = P_{Tdl} - P_{Ty}$**

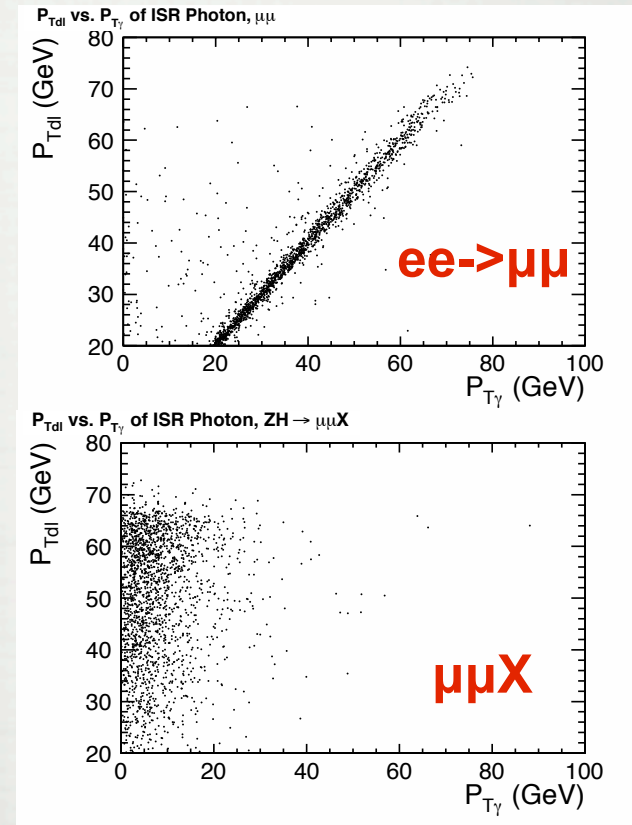


**Reduces  $\mu\mu$  and  $ee$  further by 1 to 2 orders of magnitude**  
**Signal lost:  $\sim 1\%$**

**ISR photon conversions**

**To reject the ISR Photon conversions:**

- **Cut  $|\Delta\theta_{2tk}| > 0.01$  :** Only apply on events with 2 additional tracks
- **Reject  $\mu\mu$  and  $ee$  Further by a factor of 2.**





# Background Rejection by Cuts:

## SM Cut-Chain

Pol. ( $e^-e^+L$ )  
for illustration

### SM Cut-Chain & Nevts after each cuts:

Nevts remained:	$\mu\mu X$	$\mu\mu$	$\tau\tau$	$\mu\mu\nu\nu$	$\mu\mu f f$
before any restriction:	1754	2.0M	2.0M	14k	299k
Both $\mu$ id + pre-cuts	1478(84.27%)	30k	4528	2481	10k
+ $N_{tks}>1$ :	1469(83.78%)	1813	472	31	8537
+ $ \Delta\theta_{2tk} >0.01$	1467(83.63%)	162	361	3	8423
+ $ \Delta\theta_{min} >0.01$	1444(82.36%)	105	111	0	7487
+ acop (0.2, 3.0)	1336(76.16%)	0	0	0	6635
+ $M_{recoil}\in(115, 150)$ GeV	1263(72.00%)	0	0	0	4119

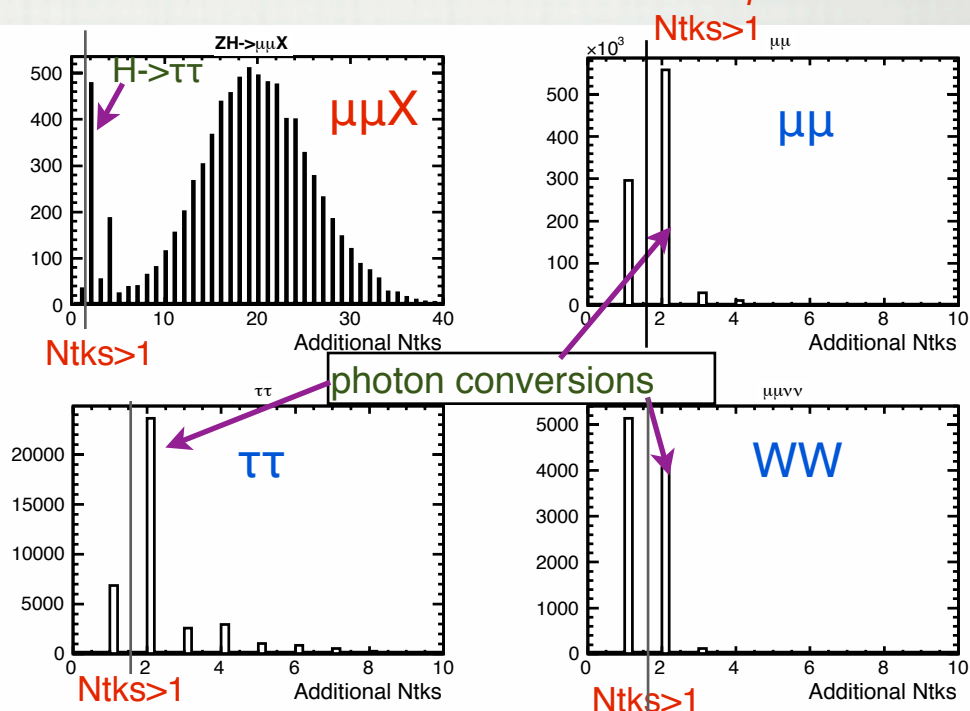
Nevts remained:	$eeX$	$ee$	$\tau\tau$	$ee\nu\nu$	$eeff$
before any restriction:	1869	4.3G	2.0M	26k	1.0M
Both $e$ id + pre-cuts	1172(62.71%)	119k	6778	3155	9430
+ $N_{tks}>1$ :	1160(62.10%)	7215	1889	50	8455
+ $ \Delta\theta_{2tk} >0.01$	1158(61.99%)	1114	1361	5	8397
+ $ \Delta\theta_{min} >0.01$	1140(61.01%)	324	278	0	7905
+ acop (0.2, 3.0)	1058(56.61%)	275	0	0	7060
+ $M_{recoil}\in(115, 150)$ GeV	969(51.87%)	172	0	0	4367

For SM Higgs decay, multiplicity in the final states is the most efficient criterion to reject the  $2f$  and  $WW$

• In order to keep the  $H\rightarrow\tau\tau$  in the signals :

- At most:  $N_{tks}>1$
- How to reject evts with  $N_{tks}=2$  in  $\mu\mu$ ,  $\tau\tau$  and  $WW$  ?

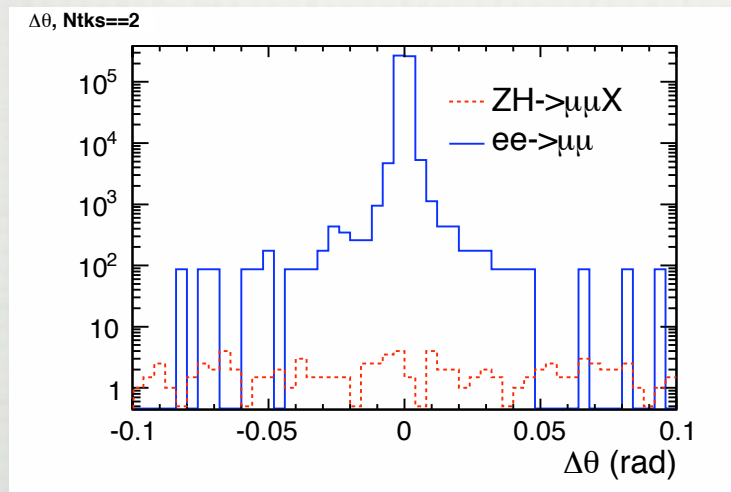
Additional Number of Tracks besides the two lepton candidates



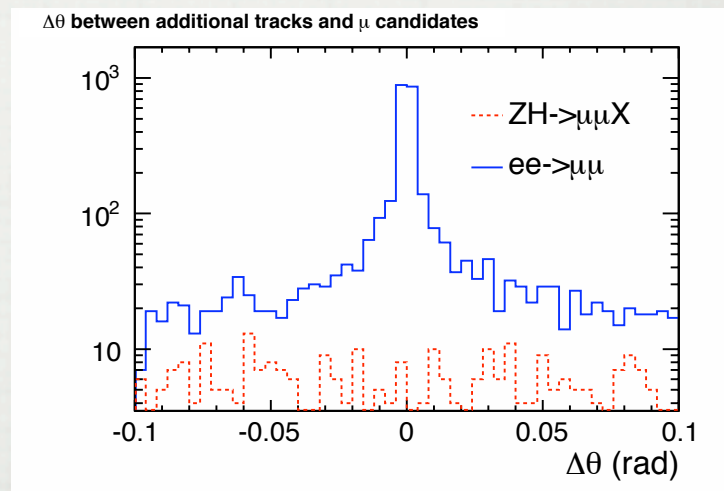
# Background Rejection by Cuts: SM Cut-Chain

To reject evts with  $N_{\text{tks}}==2$  in  $\mu\mu$ ,  $\tau\tau$  and  $WW$

- 1)
  - Define  $\Delta\theta_{2\text{tk}}$  :  $\Delta\theta$  between these two additional tracks for  $N_{\text{tks}}==2$ .
  - Apply  $|\Delta\theta_{2\text{tk}}| > 0.01$  to reject photon conversions
- 2)
  - Define  $\Delta\theta_{\text{min}}$  : the smallest  $\Delta\theta$  between the additional tracks and the lepton candidates



- Reduced the  $\mu\mu/ee$  and  $WW$  further by  $\sim 1$  order of magnitude, with a signal lost of only  $\sim 0.2\%$



- Because mis-identification of photon conversions to be lepton candidates



# BK Further Rejection by Likelihood

After Cuts Rejection, Apply Further Rejection using Likelihood Method

Likelihood:

$$L = \prod_i P_i$$

Probability

$i$  th Variable

Likelihood Fraction:

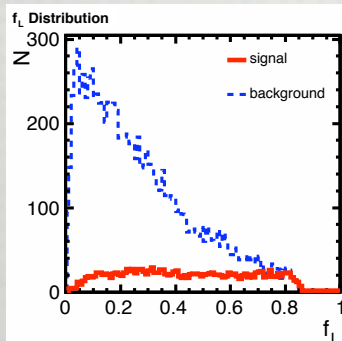
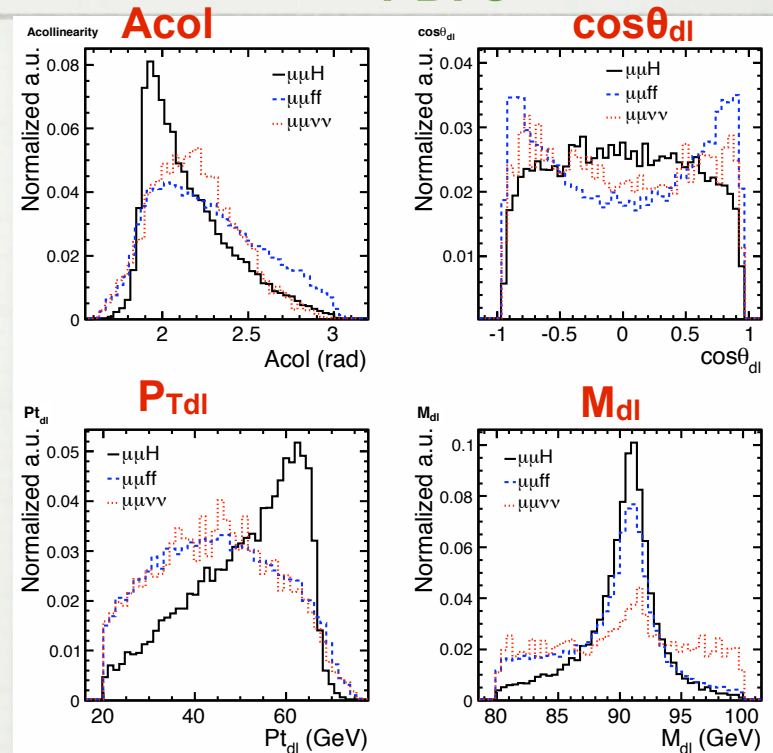
$$f_L = L_S / (L_S + L_B)$$

within (0, 1)

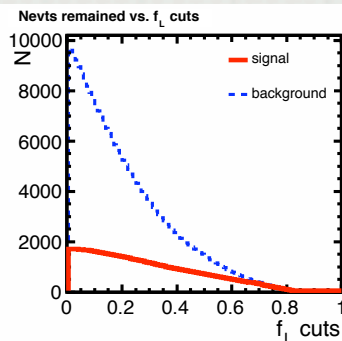
Decide the  $f_L$  cut by the maximum significance

$$f_L > 0.22$$

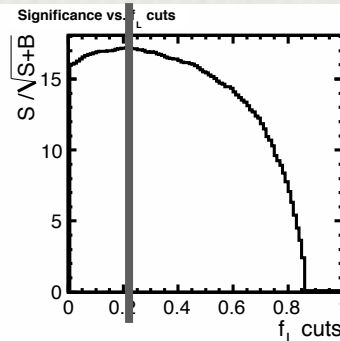
PDFs



$f_L$  Distribution



Nevt vs.  $f_L$



Significance

Taken:

Pol.  $e^-e^+$   
muon channel  
MI Analysis

For illustration

# Background Rejection Summary Table

Ana	Pol.	Ch.	Cuts	$\mu\mu X/eeX$		$\mu\mu/ee$	$\tau\tau$	$\mu\mu\nu\nu/ee\nu\nu$	$\mu\mu ff/eeff$	B	S/B	$S/\sqrt{(S+B)}$
MI	$e^-_R$ $e^+_L$	$\mu$	MI cut-chain:	1156	(65.93%)	165	0	900	2729			
			+ $f_L > 0.26$	849	(48.40%)	84	0	437	1140	1661	0.51	16.9
		$e$	MI cut-chain:	828	(44.29%)	1230	28	1043	2675			
			+ $f_L > 0.16$	715	(38.28%)	684	0	665	1587	2936	0.24	11.8
	$e^-_L$ $e^+_R$	$\mu$	MI cut-chain:	1709	(65.71%)	245	0	5482	4175			
			+ $f_L > 0.22$	1368	(52.60%)	141	0	2654	2157	4952	0.28	17.2
		$e$	MI cut-chain:	1235	(44.47%)	1313	56	5488	3665			
			+ $f_L > 0.19$	1025	(36.90%)	655	0	3041	2048	5744	0.18	12.5
SM	$e^-_R$ $e^+_L$	$\mu$	SM cut-chain:	1263	(72.00%)	49	0	0	4119			
			+ $f_L > 0.33$	1054	(60.09%)	10	0	0	1743	1753	0.60	19.9
		$e$	SM cut-chain:	969	(51.87%)	172	0	0	4367			
			+ $f_L > 0.39$	769	(41.16%)	49	0	0	1799	1848	0.42	15.0
	$e^-_L$ $e^+_R$	$\mu$	SM cut-chain:	1872	(71.96%)	68	0	0	6189			
			+ $f_L > 0.32$	1568	(60.28%)	13	0	0	2824	2837	0.55	23.6
		$e$	SM cut-chain:	1444	(52.00%)	184	0	5	5913			
			+ $f_L > 0.36$	1183	(42.62%)	56	0	1	2680	2737	0.43	18.9



# Fitting Methods

## Functions:

**Signal:** { **Gaussian Peak Exponential Tail (GPET):**

$$f(x) = N \begin{cases} e^{-\frac{(x-x_0)^2}{2\sigma^2}} & : \frac{x-x_0}{\sigma} \leq k \\ \beta e^{-\frac{(x-x_0)^2}{2\sigma^2}} + (1-\beta)e^{-(x-x_0)\frac{k}{\sigma}} e^{\frac{k^2}{2}} & : \frac{x-x_0}{\sigma} > k \end{cases}$$

**Convolution of Empirical with Gaussian (CEG): (K. Ito, / Tohoku U.)**

$$F(x) = N e^{-Ax} \int_{x_0-x}^{\sqrt{s}-x} F_H(x+t) e^{-\frac{t^2}{2\sigma^2}} dt;$$

$$F_H(x) = \left( \frac{x-x_0}{\sqrt{s}-x_0} \right)^{\beta-1}$$

**Background:** Polynomial with 3 coefficients

**Build Composite Model:**  $F(x) = N_S f_S(x) + N_B f_B(x)$

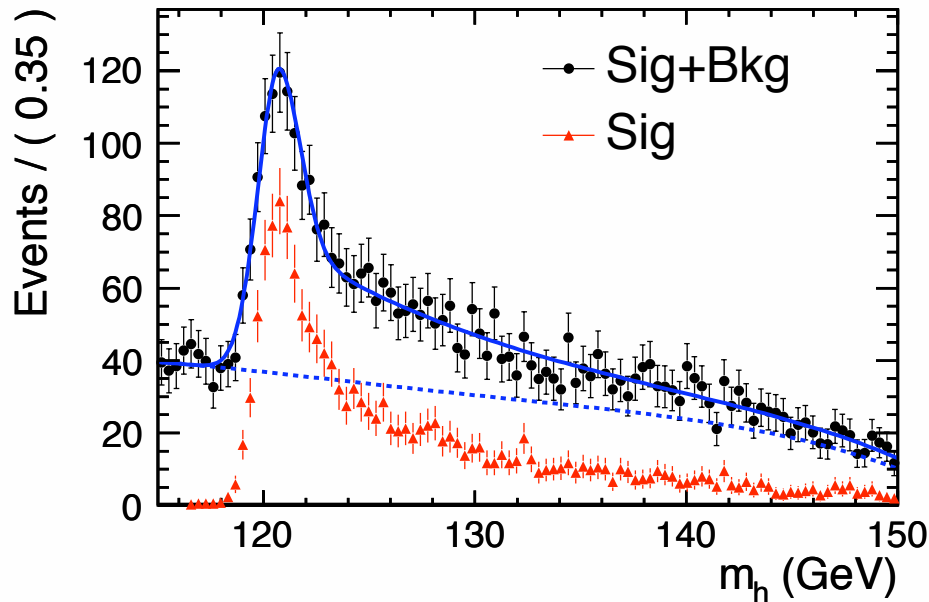
- Fitting:** {
- 1) Determine fitting parameters from MC (a separate data set)
  - 2) Fix all the parameters except the  $N_S$ ,  $(N_B)^*$  and  $M_H$
  - 3) Fit to the “Sig+Bkg” to get the results

**\*Note:** The results reported in ILD LOI has the  $N_B$  free, I also report the the results with  $N_B$  fixed, in order to be comparable with SiD

# Example Fitting I: (GPET)

$\mu\mu X$

Higgs Recoil Mass Spectrum,  $\mu$  channel,  $\sqrt{s}=250\text{GeV}$ , ILD\_00



**M Higgs :**

**$119.905 \pm 0.077 \text{ GeV}$**

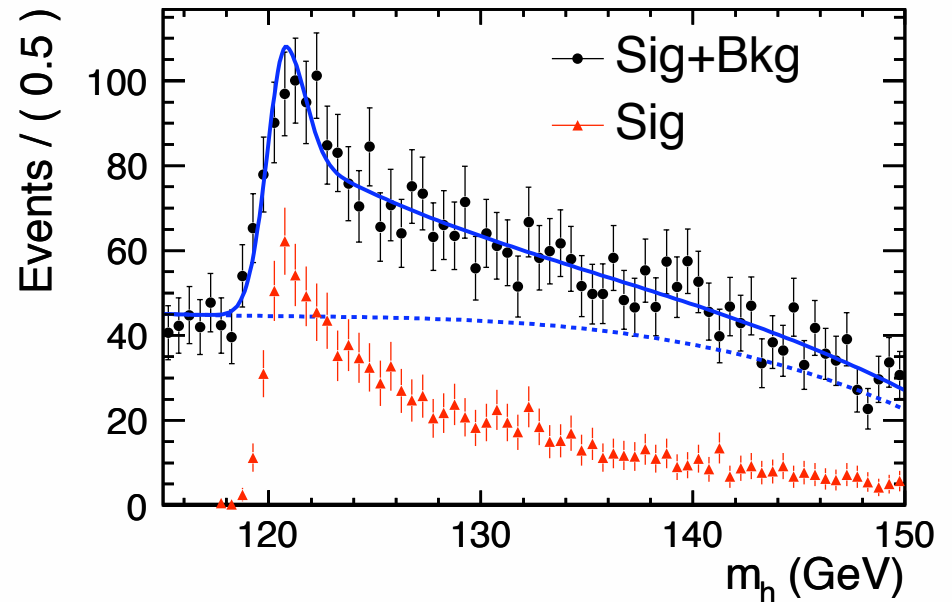
**Cross-Section:**

**$10.11 \pm 0.38 \text{ fb (3.76\%)}$**

Pol.  $e^-_L e^+_R$ , SM analysis for illustration

$eeX$

Higgs Recoil Mass Spectrum,  $e$  channel,  $\sqrt{s}=250\text{GeV}$ , ILD\_00



**M Higgs :**

**$119.871 \pm 0.135 \text{ GeV}$**

**Cross-Section:**

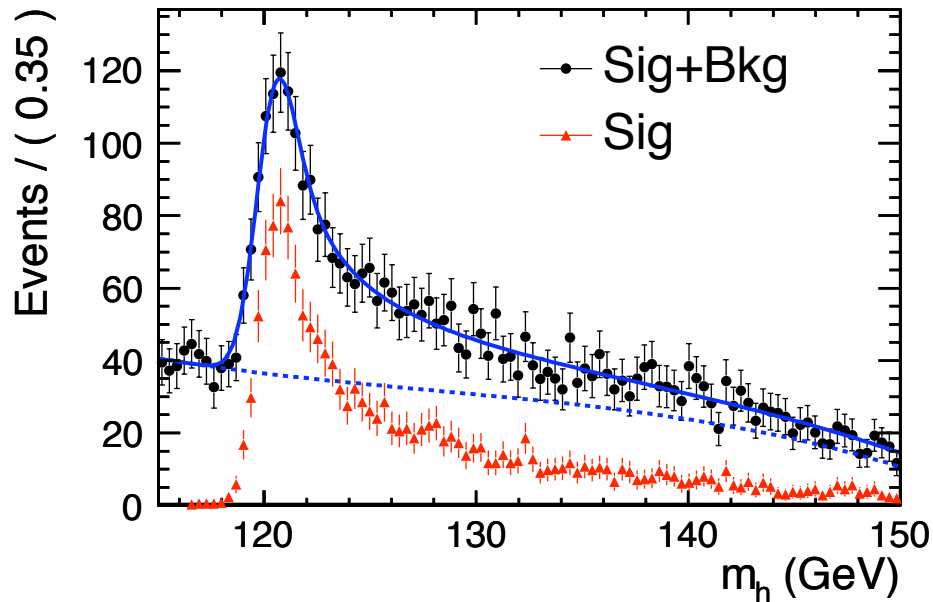
**$10.98 \pm 0.53 \text{ fb (4.83\%)}$**



# Example Fitting II: (CEG)

$\mu\mu X$

Higgs Recoil Mass Spectrum,  $\mu$  channel,  $\sqrt{s}=250\text{GeV}$ , ILD\_00



**M Higgs :**

$120.177 \pm 0.080 \text{ GeV}$

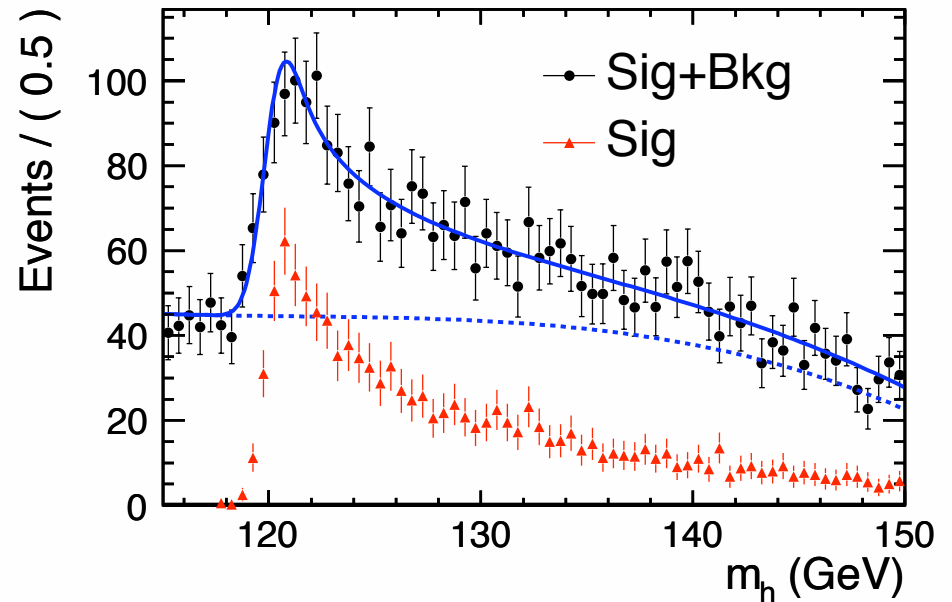
**Cross-Section:**

$10.48 \pm 0.39 \text{ fb (3.72\%)}$

Pol.  $e^-_L e^+_R$  , SM analysis for illustration

$eeX$

Higgs Recoil Mass Spectrum,  $e$  channel,  $\sqrt{s}=250\text{GeV}$ , ILD\_00



**M Higgs :**

$120.053 \pm 0.149 \text{ GeV}$

**Cross-Section:**

$10.98 \pm 0.53 \text{ fb (4.83\%)}$

# Results (a)

Ana.	Pol.	Ch.	$\delta M_H$ (MeV)	$\delta\sigma$ (fb) <sup>(d)</sup>	
MI	$e^-RE^+_L$	$\mu\mu X$	$90\pm 7$	0.50 (7.0%)	0.36 (5.1%)
		eeX	$182\pm 24$	0.87 (12.2%)	0.54 (7.3%)
		merged <sup>(c)</sup>	$81\pm 5$	0.43 (6.1%)	0.30 (4.2%)
	$e^-LE^+_R$	$\mu\mu X$	$85\pm 6$	0.70 (6.6%)	0.49 (4.8%)
		eeX	$150\pm 16$	1.15 (9.8%)	0.74 (6.5%)
		merged	$74\pm 4$	0.60 (5.5%)	0.41 (3.9%)
	Joint <sup>(b)</sup>	$\mu\mu X$	$87\pm 6$		
		eeX	$164\pm 20$		
		merged	$77\pm 5$		

Ana.	Pol.	Ch.	$\delta M_H$ (MeV)	$\delta\sigma$ (fb)	
SM	$e^-RE^+_L$	$\mu\mu X$	$93\pm 6$	0.45 (6.5%)	0.31 (4.4%)
		eeX	$204\pm 20$	0.74 (10.3%)	0.45 (6.1%)
		merged	$85\pm 8$	0.38 (5.5%)	0.26 (3.6%)
	$e^-LE^+_R$	$\mu\mu X$	$80\pm 8$	0.55 (5.4%)	0.38 (3.8%)
		eeX	$149\pm 14$	0.85 (8.0%)	0.53 (4.8%)
		merged	$70\pm 7$	0.46 (4.5%)	0.31 (3.0%)
	Joint	$\mu\mu X$	$86\pm 8$		
		eeX	$170\pm 16$		
		merged	$77\pm 7$		

(a) Results from GPET fitting function, see the backup slides for all the results.

(b) Joint: Taken  $125\text{fb}^{-1}$  Luminosity from each Pol., with a total Luminosity of  $250\text{fb}^{-1}$

(c) Merged: Results with merged statistics of  $\mu\mu X$  and eeX.

(d) Cross-Sections, **in Red**: free parameters  $N_S$  and  $M_H$ .

**in Blue**: free parameters  $N_S$ ,  $N_B$  and  $M_H$ , the results in ILD LOI



# Conclusions

- Realistic Methods and Techniques are developed for the Higgs Recoil Mass and Higgs-strahlung Cross-section measurement

- Measurements Precision achieved: (a)

- Higgs Mass: merged result:  
 $\pm 70 \text{ MeV}$
- Cross-Section: merged result:  
 $\pm 0.46 \text{ fb}^{-1} (4.5\%)$  (b)  
 $\pm 0.31 \text{ fb}^{-1} (3.0\%)$  (c)

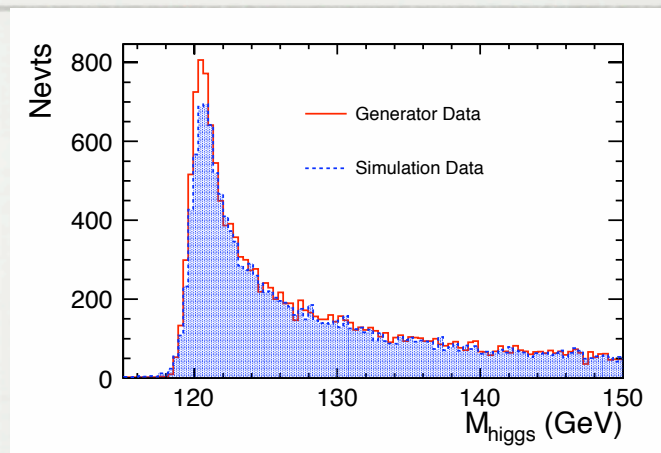
- The Higgs Recoil Mass measurement is very sensitive to several issues beside the detector uncertainty:

- **Beam Energy Spread:** Increases the width of recoil mass peak, thus reduce the accuracy of the measurement.
- **Beamstrahlung:** Largely reduces the effective statistics on the recoil mass peak

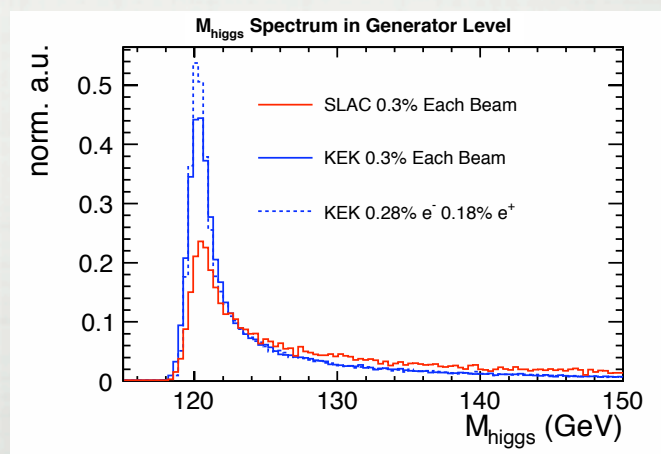
(a) SM,  $e^-_L e^+_R$  results.

(b) Fitting with free parameters  $N_S$ ,  $N_B$  and  $M_H$

(c) Fitting with free parameters  $N_S$  and  $M_H$



Comparisons of recoil mass spectra in generator level and after full simulation, with 0.3% beam energy spread for each beam, (of  $\mu\mu X$ )



Comparisons of recoil mass spectra in generator level of SLAC and KEK versions, where, the SLAC version is used in the all the 3 LOIs, and the KEK version is produced by Akiya Miyamoto with Andrei Seryi's beam parameters

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Thanks!



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# Backup Slides

# Mass Resolution

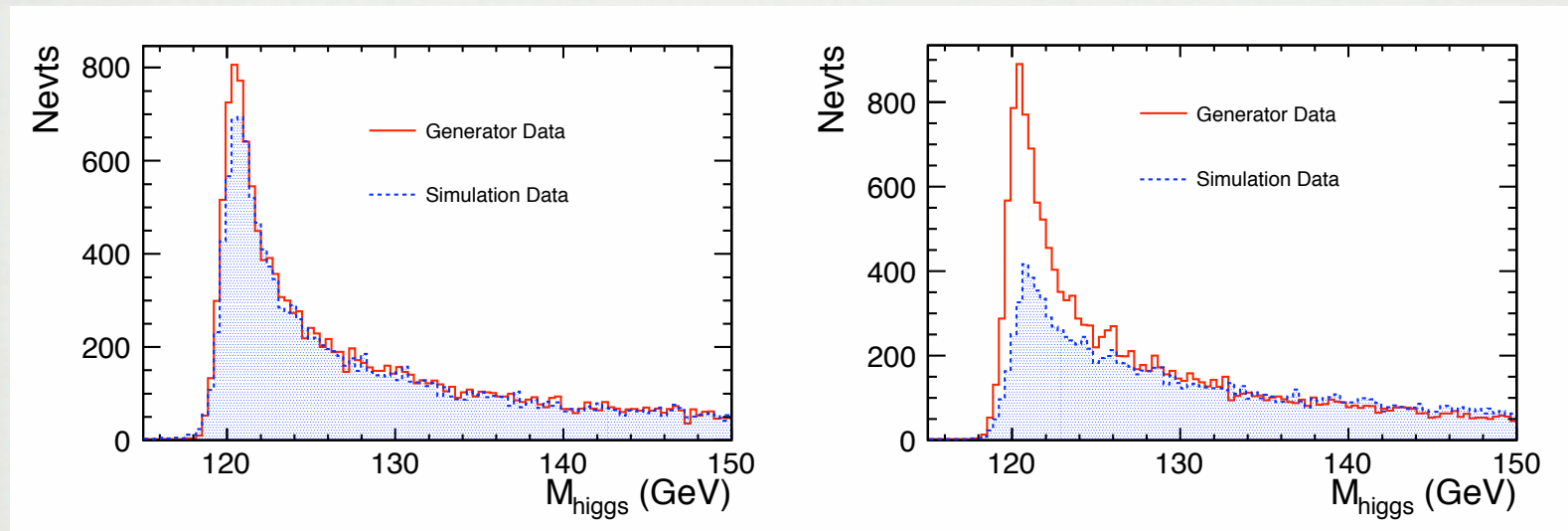
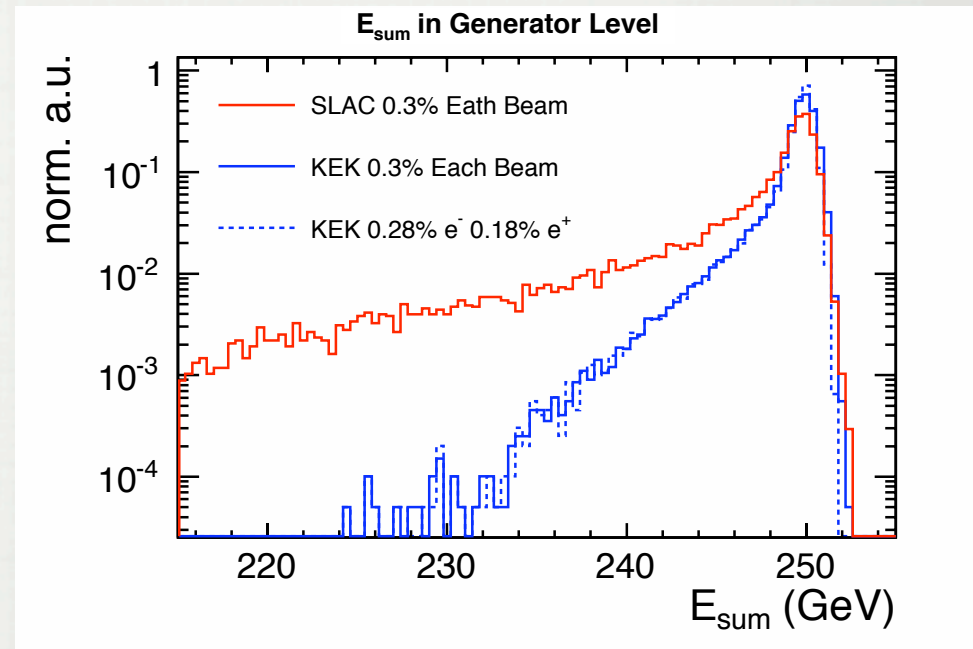
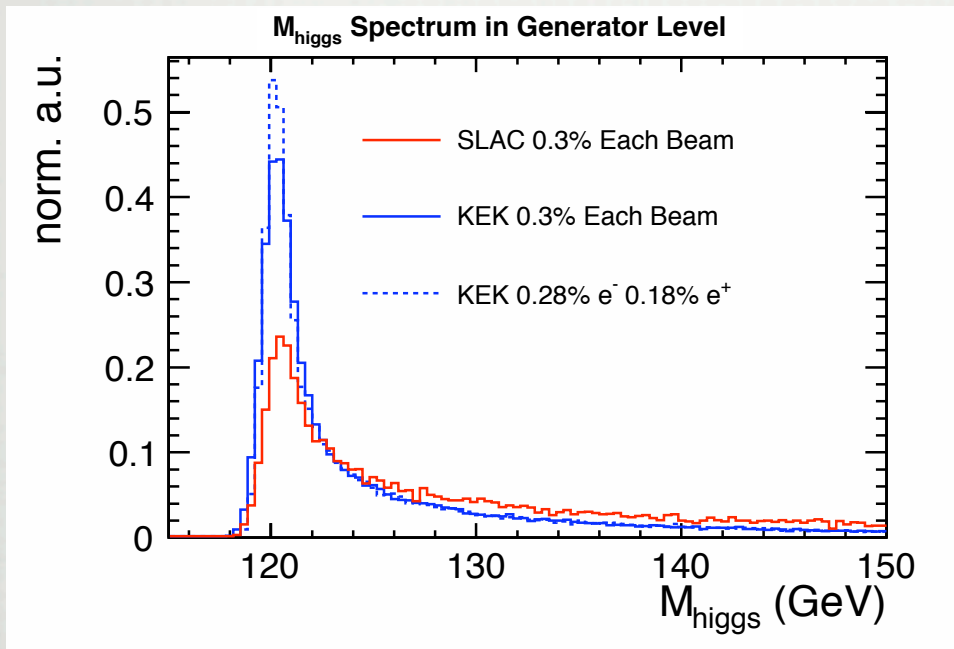


Figure 25: Comparisons of recoil mass spectra in generator level and after full simulation, for the  $\mu\mu X$ -channel (left) and the  $eeX$ -channel (right).

	$\Delta M_{tot.}$ (MeV)	$\Delta M_{mac.}$ (MeV)	$\Delta M_{dec.}$ (MeV)
$\mu\mu X$	870	730	470
$eeX$	970	730	640

Table 22: Mass Resolution with contributions by machine ( $\Delta M_{mac.}$ ) and detector ( $\Delta M_{det.}$ ) separated.

# Beam Affects



- Comparisons of recoil mass spectra in generator level of SLAC and KEK versions, where,
  - the SLAC version is used in the all the 3 LOIs, and
  - the KEK version is produced by Akiya Miyamoto with Andrei Seryi's beam parameters
- The SLAC version has larger beamstrahlung than expected.



# Results: MI , Free Pars: N<sub>S</sub>, M<sub>H</sub>

Fit.	Pol.	Ch.	$M_H$ (GeV)	$\sigma$ (fb)
GPET	$e_R^- e_L^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$119.984 \pm (0.090 \pm 0.0066)$	$7.05 \pm 0.36$ ( 5.11 %)
		$eeX$	$120.042 \pm (0.179 \pm 0.0234)$	$7.37 \pm 0.54$ ( 7.33 %)
		merged	$119.996 \pm (0.080 \pm 0.0051)$	$7.15 \pm 0.30$ ( 4.19 %)
	$e_L^- e_R^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$119.854 \pm (0.086 \pm 0.0060)$	$10.24 \pm 0.49$ ( 4.79 %)
		$eeX$	$119.924 \pm (0.152 \pm 0.0168)$	$11.32 \pm 0.74$ ( 6.54 %)
		merged	$119.871 \pm (0.075 \pm 0.0044)$	$10.57 \pm 0.41$ ( 3.87 %)
	Joint $\mathcal{L} = 125 \text{ fb}^{-1}(e_R^- e_L^+)$ $+125 \text{ fb}^{-1}(e_L^- e_R^+)$	$\mu\mu X$	$119.916 \pm (0.088 \pm 0.0063)$	
		$eeX$	$119.973 \pm (0.164 \pm 0.0196)$	
		merged	$119.929 \pm (0.077 \pm 0.0048)$	
CEG	$e_R^- e_L^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$120.085 \pm (0.099 \pm 0.0080)$	$6.97 \pm 0.36$ ( 5.16 %)
		$eeX$	$119.953 \pm (0.240 \pm 0.0420)$	$7.37 \pm 0.54$ ( 7.33 %)
		merged	$120.066 \pm (0.092 \pm 0.0067)$	$7.09 \pm 0.30$ ( 4.22 %)
	$e_L^- e_R^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$120.079 \pm (0.096 \pm 0.0075)$	$10.57 \pm 0.50$ ( 4.73 %)
		$eeX$	$120.010 \pm (0.188 \pm 0.0258)$	$11.34 \pm 0.74$ ( 6.53 %)
		merged	$120.065 \pm (0.085 \pm 0.0058)$	$10.81 \pm 0.41$ ( 3.83 %)
	Joint $\mathcal{L} = 125 \text{ fb}^{-1}(e_R^- e_L^+)$ $+125 \text{ fb}^{-1}(e_L^- e_R^+)$	$\mu\mu X$	$120.082 \pm (0.097 \pm 0.0077)$	
		$eeX$	$119.988 \pm (0.209 \pm 0.0319)$	
		merged	$120.065 \pm (0.088 \pm 0.0062)$	

# Results: SM , Free Pars: $N_S$ , $M_H$

Fit.	Pol.	Ch.	$M_H$ (GeV)	$\sigma$ (fb)
GPET	$e_R^- e_L^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$119.951 \pm (0.084 \pm 0.0057)$	$7.00 \pm 0.31$ ( 4.43 %)
		$eeX$	$119.704 \pm (0.200 \pm 0.0292)$	$7.39 \pm 0.45$ ( 6.09 %)
		merged	$119.914 \pm (0.077 \pm 0.0048)$	$7.13 \pm 0.26$ ( 3.58 %)
	$e_L^- e_R^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$119.906 \pm (0.078 \pm 0.0049)$	$10.11 \pm 0.38$ ( 3.76 %)
		$eeX$	$119.866 \pm (0.131 \pm 0.0125)$	$10.98 \pm 0.53$ ( 4.83 %)
		merged	$119.896 \pm (0.067 \pm 0.0035)$	$10.41 \pm 0.31$ ( 2.97 %)
	Joint $\mathcal{L} = 125 \text{ fb}^{-1}(e_R^- e_L^+)$ $+125 \text{ fb}^{-1}(e_L^- e_R^+)$	$\mu\mu X$	$119.927 \pm (0.081 \pm 0.0053)$	
		$eeX$	$119.817 \pm (0.155 \pm 0.0175)$	
		merged	$119.903 \pm (0.072 \pm 0.0041)$	
CEG	$e_R^- e_L^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$120.123 \pm (0.093 \pm 0.0070)$	$7.02 \pm 0.31$ ( 4.42 %)
		$eeX$	$119.684 \pm (0.201 \pm 0.0295)$	$7.40 \pm 0.45$ ( 6.08 %)
		merged	$120.046 \pm (0.084 \pm 0.0057)$	$7.14 \pm 0.26$ ( 3.57 %)
	$e_L^- e_R^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$120.178 \pm (0.081 \pm 0.0053)$	$10.48 \pm 0.39$ ( 3.72 %)
		$eeX$	$120.047 \pm (0.146 \pm 0.0155)$	$10.98 \pm 0.53$ ( 4.83 %)
		merged	$120.147 \pm (0.071 \pm 0.0040)$	$10.66 \pm 0.31$ ( 2.95 %)
	Joint $\mathcal{L} = 125 \text{ fb}^{-1}(e_R^- e_L^+)$ $+125 \text{ fb}^{-1}(e_L^- e_R^+)$	$\mu\mu X$	$120.154 \pm (0.086 \pm 0.0061)$	
		$eeX$	$119.922 \pm (0.167 \pm 0.0203)$	
		merged	$120.105 \pm (0.077 \pm 0.0047)$	



# Results: MI , Free Pars: N<sub>S</sub>, N<sub>B</sub> and M<sub>H</sub>

Fit.	Pol.	Ch.	$M_H$ (GeV)	$\sigma$ (fb)
GPET	$e_R^- e_L^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$119.984 \pm (0.090 \pm 0.0066)$	$7.11 \pm 0.50$ ( 7.03 %)
		$eeX$	$120.046 \pm (0.182 \pm 0.0241)$	$7.15 \pm 0.87$ ( 12.17 %)
		merged	$119.996 \pm (0.081 \pm 0.0052)$	$7.12 \pm 0.43$ ( 6.09 %)
	$e_L^- e_R^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$119.854 \pm (0.085 \pm 0.0059)$	$10.54 \pm 0.70$ ( 6.64 %)
		$eeX$	$119.922 \pm (0.150 \pm 0.0164)$	$11.72 \pm 1.15$ ( 9.81 %)
		merged	$119.871 \pm (0.074 \pm 0.0043)$	$10.86 \pm 0.60$ ( 5.51 %)
	Joint $\mathcal{L} = 125 \text{ fb}^{-1}(e_R^- e_L^+)$ $+125 \text{ fb}^{-1}(e_L^- e_R^+)$	$\mu\mu X$	$119.915 \pm (0.087 \pm 0.0062)$	
		$eeX$	$119.972 \pm (0.164 \pm 0.0195)$	
		merged	$119.928 \pm (0.077 \pm 0.0047)$	
CEG	$e_R^- e_L^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$120.086 \pm (0.100 \pm 0.0081)$	$6.91 \pm 0.50$ ( 7.24 %)
		$eeX$	$119.961 \pm (0.244 \pm 0.0434)$	$7.15 \pm 0.87$ ( 12.17 %)
		merged	$120.068 \pm (0.093 \pm 0.0068)$	$6.97 \pm 0.43$ ( 6.22 %)
	$e_L^- e_R^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$120.078 \pm (0.095 \pm 0.0073)$	$10.83 \pm 0.72$ ( 6.65 %)
		$eeX$	$120.007 \pm (0.185 \pm 0.0249)$	$11.75 \pm 1.15$ ( 9.79 %)
		merged	$120.063 \pm (0.085 \pm 0.0057)$	$11.09 \pm 0.61$ ( 5.50 %)
	Joint $\mathcal{L} = 125 \text{ fb}^{-1}(e_R^- e_L^+)$ $+125 \text{ fb}^{-1}(e_L^- e_R^+)$	$\mu\mu X$	$120.082 \pm (0.097 \pm 0.0077)$	
		$eeX$	$119.990 \pm (0.208 \pm 0.0317)$	
		merged	$120.065 \pm (0.088 \pm 0.0062)$	



# Results: SM , Free Pars: N<sub>S</sub>, N<sub>B</sub> and M<sub>H</sub>

Fit.	Pol.	Ch.	M <sub>H</sub> (GeV)	σ (fb)
GPET	$e_R^- e_L^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$119.951 \pm (0.084 \pm 0.0057)$	$6.98 \pm 0.45 (6.45 \%)$
		$eeX$	$119.713 \pm (0.204 \pm 0.0303)$	$7.18 \pm 0.74 (10.31 \%)$
		merged	$119.916 \pm (0.078 \pm 0.0048)$	$7.03 \pm 0.38 (5.47 \%)$
	$e_L^- e_R^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$119.905 \pm (0.077 \pm 0.0048)$	$10.26 \pm 0.55 (5.36 \%)$
		$eeX$	$119.871 \pm (0.135 \pm 0.0133)$	$10.67 \pm 0.85 (7.97 \%)$
		merged	$119.897 \pm (0.067 \pm 0.0035)$	$10.38 \pm 0.46 (4.45 \%)$
	Joint $\mathcal{L} = 125 \text{ fb}^{-1}(e_R^- e_L^+)$ $+125 \text{ fb}^{-1}(e_L^- e_R^+)$	$\mu\mu X$	$119.926 \pm (0.080 \pm 0.0052)$	
		$eeX$	$119.823 \pm (0.159 \pm 0.0185)$	
		merged	$119.905 \pm (0.072 \pm 0.0041)$	
CEG	$e_R^- e_L^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$120.122 \pm (0.093 \pm 0.0070)$	$7.03 \pm 0.44 (6.26 \%)$
		$eeX$	$119.689 \pm (0.204 \pm 0.0303)$	$7.23 \pm 0.74 (10.24 \%)$
		merged	$120.047 \pm (0.085 \pm 0.0057)$	$7.08 \pm 0.38 (5.34 \%)$
	$e_L^- e_R^+$ $\mathcal{L} = 250 \text{ fb}^{-1}$	$\mu\mu X$	$120.177 \pm (0.080 \pm 0.0052)$	$10.64 \pm 0.57 (5.36 \%)$
		$eeX$	$120.053 \pm (0.149 \pm 0.0162)$	$10.67 \pm 0.85 (7.97 \%)$
		merged	$120.149 \pm (0.070 \pm 0.0039)$	$10.65 \pm 0.47 (4.45 \%)$
	Joint $\mathcal{L} = 125 \text{ fb}^{-1}(e_R^- e_L^+)$ $+125 \text{ fb}^{-1}(e_L^- e_R^+)$	$\mu\mu X$	$120.154 \pm (0.086 \pm 0.0060)$	
		$eeX$	$119.926 \pm (0.170 \pm 0.0211)$	
		merged	$120.108 \pm (0.077 \pm 0.0047)$	

# MI vs. SM Rejection, LR, Muon

## MI

$N_{evts}$ left:	$\mu\mu X$	$\mu\mu$	$\tau\tau$	$\mu\mu\nu\nu$	$\mu\mu f f$
Before any restriction	2601	2.6M	2.6M	125k	321k
+ Both $\mu$ identified	2488 (95.65%)	44k (1.7%)	79k (3.0%)	108k (86.6%)	186k (57.9%)
+ Pre-cuts	2193 (84.33%)		5639 (0.2%)	17k (13.6%)	15k (4.5%)
+ $P_{Tdl} > 20$ GeV	2078 (79.91%)	22k (0.8%)	3806 (0.15%)	15k (11.8%)	11k (3.4%)
+ $M_{dl} \in (80, 100)$ GeV	1919 (73.79%)	17k (0.6%)	2111 (0.08%)	9124 (7.3%)	8005 (2.5%)
+ $acop \in (0.2, 3.0)$	1787 (68.72%)	14k (0.5%)	28	8548 (6.8%)	7213 (2.2%)
+ $\Delta P_{Tbal.} > 10$ GeV	1752 (67.38%)	796 (0.03%)	0	7969 (6.4%)	6747 (2.1%)
+ $ \Delta\theta_{2tk}  > 0.01$	1750 (67.28%)	335 (0.01%)	0	7871 (6.3%)	6719 (2.1%)
+ $M_{recoil} \in (115, 150)$ GeV	1709 (65.71%)	245	0	5284 (4.2%)	4175 (1.3%)

## SM

$N_{evts}$ left:	$\mu\mu X$	$\mu\mu$	$\tau\tau$	$\mu\mu\nu\nu$	$\mu\mu f f$
Before any restriction:	2601	2.61M	2.61M	125k	321k
Both $\mu$ identified	2488 (95.66%)	44k (1.7%)	79k (3.0%)	108k (86.6%)	186k (57.9%)
+ Pre-cuts	2193 (84.33%)		5639 (0.22%)	17k (13.62%)	15k (4.5%)
+ $N_{add.TK} > 1$	2179 (83.8%)	2643 (0.1%)	667 (0.03%)	290 (0.23%)	13k (4.0%)
+ $\Delta\theta_{2tk} > 0.01$	2176 (83.66%)	244	500 (0.02%)	34 (0.03%)	12.5k (3.9%)
+ $\Delta\theta_{min} > 0.01$	2140 (82.29%)	155	111	2	11k (3.5%)
+ $acop \in (0.2, 3.0)$	1977 (76.03%)	114	0	2	10k (3.1%)
+ $M_{recoil} \in (115, 150)$ GeV	1872 (71.96%)	68	0	0	6189 (1.9%)



# MI vs. SM Rejection, LR, Electron

MI

$N_{evts}$ left:	$eeX$	$ee$	$\tau\tau$	$ee\nu\nu$	$eeff$
Before any restriction	2777	4.3G	2.6M	156k	1.0M
+ Both $\mu$ identified	2728 (98.24%)	127k	294k (11.3%)	120k (77.1%)	404k (40.4%)
+ Pre-cuts	1739 (62.64%)		8972 (0.34%)	19k (12.2%)	12k (1.2%)
+ $P_{Tdl} > 20 \text{ GeV}$	1641 (59.10%)	96k	6195 (0.24%)	16k (10.6%)	10k (1.0%)
+ $M_{dl} \in (80, 100) \text{ GeV}$	1399 (50.38%)	51k	3500 (0.13%)	9784 (6.3%)	7186 (0.72%)
+ $acop \in (0.2, 3.0)$	1314 (47.33%)	46k	278 (0.01%)	9168 (5.9%)	6564 (0.66%)
+ $\Delta P_{Tbal.} > 10 \text{ GeV}$	1281 (46.15%)	3156	194	8222 (5.3%)	6066 (0.61%)
+ $ \Delta\theta_{2tk}  > 0.01$	1279 (46.07%)	1764	167	8069 (5.2%)	6041 (0.6%)
+ $M_{recoil} \in (115, 150) \text{ GeV}$	1235 (44.47%)	1313	56	5488 (3.5%)	3665 (0.37%)

SM

$N_{evts}$ left:	$eeX$	$ee$	$\tau\tau$	$ee\nu\nu$	$eeff$
Before any restriction:	2777	4.3G	2.61M	156k	1.0M
Both e identified	2728 (98.24%)	127k	294k (11.3%)	120k (77.1%)	404k (40.4%)
+ Pre-cuts	1739 (62.64%)		8972 (0.34%)	19k (12.21%)	12k (1.23%)
+ $N_{add.TK} > 1$	1724 (62.08%)	7660	2528 (0.10%)	463 (0.30%)	11k (1.13%)
+ $\Delta\theta_{2tk} > 0.01$	1721 (61.98%)	1190	1806 (0.07%)	76 (0.05%)	11k (1.13%)
+ $\Delta\theta_{min} > 0.01$	1696 (61.06%)	344	361 (0.01%)	10	10.7k (1.07%)
+ $acop \in (0.2, 3.0)$	1579 (56.86%)	293	0	10	9589 (0.96%)
+ $M_{recoil} \in (115, 150) \text{ GeV}$	1444 (52.00%)	184	0	5	5913 (0.59%)



# Lepton ID

## Cuts for lepton ID:

muon ID

$$E_{ecal}/E_{total} < 0.5$$

$$E_{cal}/P_{track} < 0.3$$

electron ID

$$E_{ecal}/E_{total} > 0.6$$

$$E_{cal}/P_{track} > 0.9$$

Cuts (for P>15GeV): single particle	$\mu\mu$ X (muon ID)	eeX (electron ID)
Efficiency ( $N_{trueiden}/N_{true}$ )	97.6%	96.3%
Purity ( $N_{trueiden}/N_{iden}$ )	91.4%	96.1%
<b>Efficiency lepton pair ID: (no P request, select according to Mz)</b>	<b>95.4%</b>	<b>98.8%</b>