

Enhanced multi-Higgs boson production in the general 2HDM

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- RNH, D. Lopez-Val, J. Sola : Phys. Lett. B **673** (2009) 47;
arXiv:0901.2257

Outline

- 1 The two Higgs doublet model (2HDM)
- 2 Enhanced Higgs trilinear couplings
- 3 Double Higgs Production in Gauge Boson Fusion
- 4 Conclusions

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What is the Higgs Sector?

$$SU(2)_L \times U(1)_Y \rightarrow U(1)_\gamma$$

The masses and other properties of the W^\pm and Z^0 bosons are accurately described by a spontaneously broken gauge theory

A Higgs boson?

The nature of the so-called Higgs sector, responsible for the breaking, remains experimentally unconfirmed

Standard Model or Beyond?

- Simplest model of a single scalar doublet (the Standard Model) is not excluded
- It is not the only possibility, e.g. 2HDM, SUSY, Composite Higgs ...

Standard Model Higgs Potential

SM Higgs boson

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} G^+ \\ v + H + iG^0 \end{pmatrix}$$

SM Higgs Potential

$$\begin{aligned} V_{\text{SM}} &= \lambda \left(\Phi^2 - \frac{v^2}{2} \right)^2 \\ &= \lambda v^2 H^2 + \lambda v H^3 + \frac{\lambda}{4} H^4 \end{aligned}$$

Trilinear Coupling

$$\lambda_{HHH} = \frac{3}{2} \frac{eM_H^2}{s_W M_W}$$

- small for a light Higgs

Two Higgs-Doublet Model

EW Eigenstates

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ v_1 + \phi_1 + ia_1 \end{pmatrix}$$

$$\Phi_2 = \begin{pmatrix} \phi_2^+ \\ v_2 + \phi_2 + ia_2 \end{pmatrix}$$

Coupling to Fermions?

Type-I 2HDM: $\Phi_1 (u, d, e)$

Type-II 2HDM: $\Phi_1 (d, e)$

$\Phi_2 (u)$

Mass Eigenstates

$$\begin{pmatrix} h^0 \\ H^0 \end{pmatrix} = \begin{pmatrix} c_\alpha & s_\alpha \\ -s_\alpha & c_\alpha \end{pmatrix} \begin{pmatrix} \phi_1 \\ \phi_2 \end{pmatrix}$$

$$\begin{pmatrix} G^0 \\ A^0 \end{pmatrix} = \begin{pmatrix} c_\beta & s_\beta \\ -s_\beta & c_\beta \end{pmatrix} \begin{pmatrix} a_1 \\ a_2 \end{pmatrix}$$

$$\begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix} = \begin{pmatrix} c_\beta & s_\beta \\ -s_\beta & c_\beta \end{pmatrix} \begin{pmatrix} \phi_1^\pm \\ \phi_2^\pm \end{pmatrix}$$

$$v^2 = v_1^2 + v_2^2, \quad \tan \beta = \frac{v_2}{v_1}$$

2HDM Potential

General (CP-conserving) 2HDM potential

$$\begin{aligned}
 V(\Phi_1, \Phi_2) = & \lambda_1 \left(\Phi_1^\dagger \Phi_1 - v_1^2 \right)^2 + \lambda_2 \left(\Phi_2^\dagger \Phi_2 - v_2^2 \right)^2 \\
 & + \lambda_3 \left[\left(\Phi_1^\dagger \Phi_1 - v_1^2 \right) + \left(\Phi_2^\dagger \Phi_2 - v_2^2 \right) \right] \\
 & + \lambda_4 \left[\left(\Phi_1^\dagger \Phi_1 \right) \left(\Phi_2^\dagger \Phi_2 \right) - \left(\Phi_1^\dagger \Phi_2 \right) \left(\Phi_2^\dagger \Phi_1 \right) \right] \\
 & + \lambda_5 \left[\Re \left(\Phi_1^\dagger \Phi_2 \right) - v_1 v_2 \right]^2 + \lambda_6 \left[\Im \left(\Phi_1^\dagger \Phi_2 \right) \right]^2
 \end{aligned}$$

Softly broken Z_2 symmetry to prevent FCNCs.

Parameters

MSSM case

Imposing SUSY severely constrains the Higgs potential

- Find $\lambda_5 = \lambda_6$
- All quartic couplings are given in terms of the electroweak gauge couplings g, g'

Two free parameters, $M_A, \tan \beta$

General 2HDM- Our analysis

- We impose $\lambda_5 = \lambda_6$.
- 6 free parameters

We can choose $M_{H^0}, M_{A^0}, M_{H^\pm}, \tan \beta, \tan \alpha$

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3H Couplings

Higgs self-interactions

$$\lambda_{H^0 H^0 H^0} = -\frac{ie c_{\beta-\alpha}}{2M_W s_W s_{2\beta}} \left[\left(2M_{h^0}^2 + M_{H^0}^2 \right) s_{2\alpha} - M_{A^0}^2 (3s_{2\alpha} - s_{2\beta}) \right]$$

$$\xrightarrow{\text{MSSM}} \frac{ieM_Z}{2c_W s_W} \left[c_{2\alpha} c_{\alpha+\beta} - 2s_{2\alpha} s_{\alpha+\beta} \right]$$

Restrictions

- 2HDM couplings enhanced for large (small) values of $\tan \beta$ or large Higgs mass splittings
- Maximum enhancement limited by phenomenological and theoretical constraints

Theoretical Constraints

Perturbativity

We restrict $0.1 \lesssim \tan \beta \lesssim 60$

Unitarity

Bound all $3H$ couplings by the SM value at $M_H = 1 \text{ TeV}$

$$|\lambda_{HHH}| \leq \frac{3}{2} \frac{eM_H^2}{s_W M_W} \Big|_{M_H=1\text{TeV}}$$

Approximates well the range excluded by more sophisticated calculations

- Kanemura, Kubota, Takasugi; hep-ph/9303263
- Akeroyd, Arhrib, Naimi; hep-ph/0006035
- Horejsi, Kladiva; hep-ph/0510154

Phenomenological Constraints

$b \rightarrow s\gamma$

- Restricts charged Higgs mass

$M_{H^\pm} \gtrsim 350 \text{ GeV}$ for $\tan \beta \geq 1$ in the Type-II model

Ciuchini, Degrossi, Gambino, Giudice;
hep-ph/9710335

Borzumati, Greub; hep-ph/9802391

- No constraint for the Type-I model as $H^\pm \bar{f}f$ couplings suppressed by $\cot \beta$

Gambino, Misiak; hep-ph/0104034

Custodial $SU(2)$

- 2HDM contributions to $\delta\rho$ vanish as $M_{A^0} \rightarrow M_{H^\pm}$

Barbieri, Maiani; *Nucl. Phys.***B224** (1983) 32

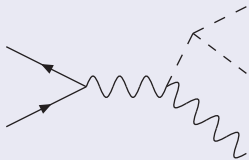
- $|\delta\rho| \leq 10^{-3}$ constrains A^0 to also be heavy in the Type-II model

Outline

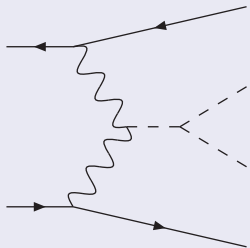
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Multi-Higgs processes

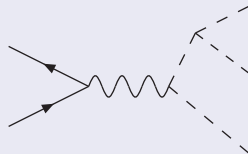
Double Higgs-strahlung



Gauge-boson fusion



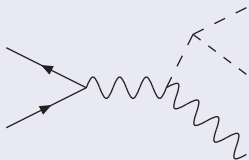
Triple Higgs production



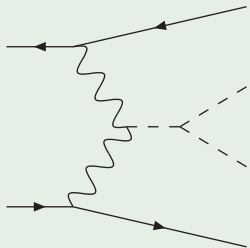
- $3H$ production in Ferrera, Guasch, López-Val and Solà, arXiv:0707.3162
- ZHH in Arhrib, Benbrik and Chiang, arXiv:0802.0319

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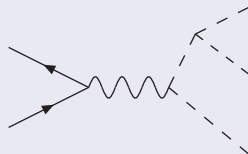
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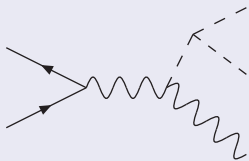
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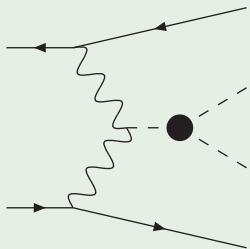
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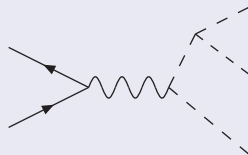
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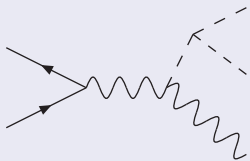
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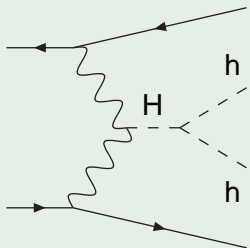
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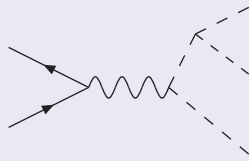
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Parameter Sets

We consider four distinct scenarios

Heavy Higgs Spectrum (Type-I and Type-II)

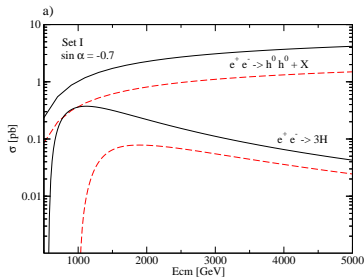
- 1 Non-Resonant Production
- 2 Resonant Production

Light Higgs Spectrum (Type-I only)

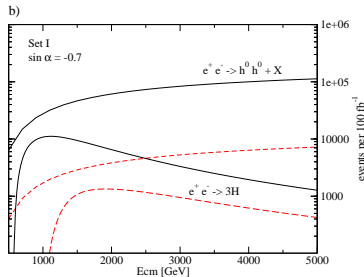
- 1 Non-Resonant Production
- 2 Resonant Production

Focus on production of light Higgs states
Numerical results using *CompHep*

Non-Resonant; Heavy Charged Higgs I



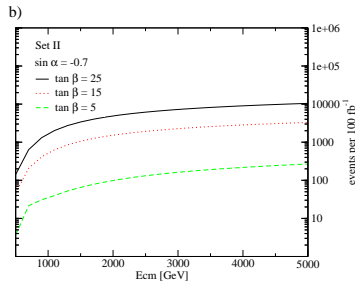
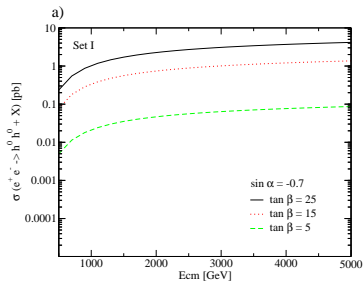
$$\tan \beta \simeq 25(4)$$



$$\tan \beta \simeq 14(2)$$

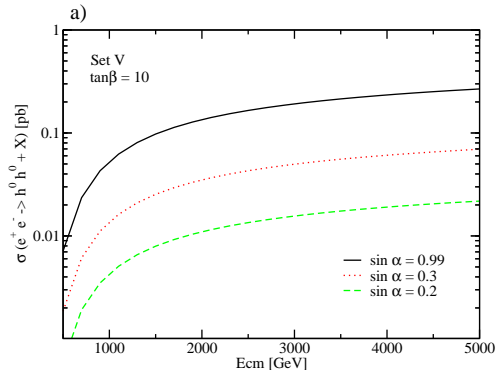
	M_{h^0} [/GeV]	M_{H^0} [/GeV]	M_{A^0} [/GeV]	M_{H^\pm} [/GeV]
Set I (solid)	100	190	360	350
Set I' (dash)	100	190	800	800

Non-Resonant; Heavy Charged Higgs II



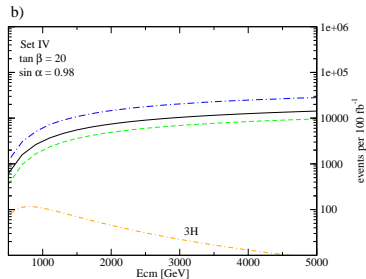
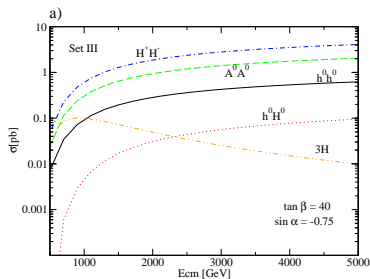
	M_{h^0} [/GeV]	M_{H^0} [/GeV]	M_{A^0} [/GeV]	M_{H^\pm} [/GeV]
Set I	100	190	360	350
Set II	150	250	360	350

Resonant; Heavy Charged Higgs



	M_{h^0} [/GeV]	M_{H^0} [/GeV]	M_{A^0} [/GeV]	M_{H^\pm} [/GeV]
Set V	125	280	300	350

Light Charged Higgs



	M_{h^0} [GeV]	M_{H^0} [GeV]	M_{A^0} [GeV]	M_{H^\pm} [GeV]
Set III	150	290	150	150
Set IV	100	225	110	105

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Summary and Outlook

- Even after discovery of the Higgs it will be necessary to measure its self-interactions in order to reconstruct the EW symmetry breaking potential
- If nature is described by a 2HDM the ILC or CLIC may have access to prodigious production of two-Higgs final states through gauge boson fusion
- Double Higgs-strahlung and triple Higgs production are also enhanced and give complementary measurements of the triple-Higgs vertices