

IFQED processes in CAIN

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Advanced QED for future colliders Workshop

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Synopsis

- ▶ CAIN IFQED processes and approximations.
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 - ▶ order of magnitude estimation of the cross-section

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- ▶ **However** Precision physics eg. polarization studies require precise spin tracking (cf. Gudi et al The Power Report)
- ▶ Pertinent to look at higher order IFQED and radiative corrections

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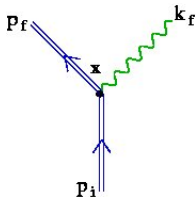


Figure: The beamsstrahlung process.

Spin tracking in CAIN - precession

- ▶ Spin precession in the bunch field is given by the T-BMT equation

$$\frac{d\vec{S}}{dt} = -\frac{e}{m\gamma} \left[(\gamma + 1)\vec{B}_T + (a + 1)\vec{B}_L - \gamma\left(a + \frac{1}{\gamma + 1}\right)\frac{1}{c^2}\vec{v} \times \vec{E} \right] \times \vec{S}$$

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$$W \propto e F^{\mu\nu} p_\mu s_\nu \int_0^\infty \frac{du}{(1+u)^3} 3x K_{1/3}(x)$$
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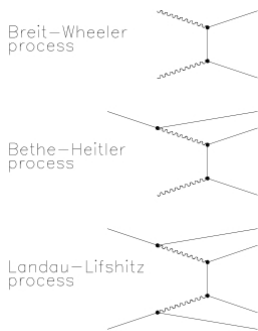
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- ▶ This pole corresponds to the IR divergence $\omega_f \rightarrow 0$
- ▶ Uncorrected in CAIN/G-P, so uncertainty in the spin-flip rate
- ▶ Has to be corrected with the corrected vertex in the external field
- ▶ But I wont discuss it further here

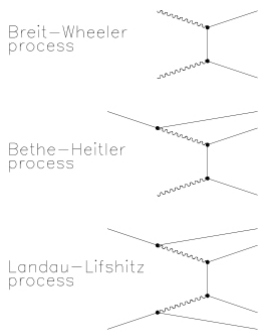
CAIN pair production processes



- ▶ Real beamstrahlung photons and/or virtual photons give the three pair production processes
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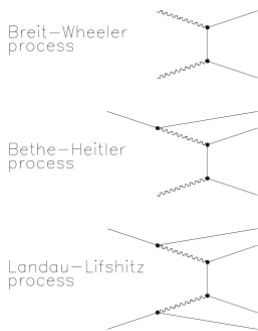


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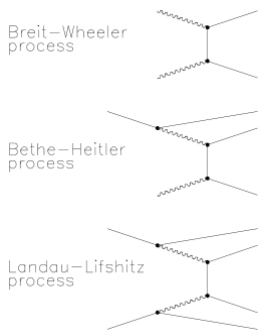


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- ▶ The poles of the Dressed propagator are particularly interesting
- ▶ Furthermore assume EPA in the external field is still valid
- ▶ We need the Second order IFQED processes in the Furry picture

2 vertex pair production in an external field I

- ▶ Use the method of Nikishov and Ritus - we need only the modified vertex

$$\Gamma_{\mu}^e = \int d^4x \bar{E}_{p_-}(x) \gamma_{\mu} E_{p_+}(x) \exp(-i(k_1 x))$$

$$E_p(x) = \left(1 + \frac{e k A}{2(k p)} \right) \exp(iS(x))$$

- ▶ We need a product of 4 of these, 2 projection operators and propagator numerators - 2000 terms in the trace!
- ▶ We can reduce using the usual rules but still its in our interest to simplify the matrix element as much as possible

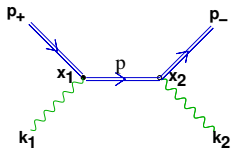


Figure: The 2 vertex IFQED pair production.

2 vertex pair production in an external field II

$$S_{fi} = \int dr ds dp \bar{u}(p_f) \bar{E}(p_-) \gamma_\mu E(p) \frac{\not{p} + m}{p^2 - m^2} \bar{E}(p) \gamma_\nu E(p_+) \cdot \delta(p_- - p - k_1 - rk) \delta(p - p_+ - k_2 - sk)$$

- ▶ Use the delta function to integrate over the propagator momentum p to get one delta function

$$\delta(p_- - p_+ - k_1 - k_2 - (r + s)k)$$

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- ▶ Shift the integration $\int ds \rightarrow \int dl$
- ▶ Try and do the integration over dr before squaring the matrix element

Two vertex Auxillary functions I

- ▶ The two vertex auxillary function is an integration of an Airy function product

$$A \equiv \int_{-\infty}^{\infty} \frac{dr}{(p - k_1) + r(kp)} \text{Ai}(r - Q_1) \text{Ai}(l - r - Q_2) \exp(-irQ_3)$$

- ▶ These type of calculations always occur, for circularly polarised field its an infinite summation over Bessel function products
- ▶ Add an imaginary component to the denominator $\frac{1}{(p - k_1) + r(kp) + i\epsilon}$

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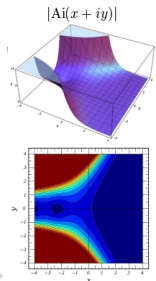
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 $\int \frac{dr}{p-k_1 + r(kp) + i\epsilon} \exp(-ir(t + Q_3)) =$
 $\exp(-\epsilon|t + Q_3|)$
- ▶ Result: Airy function product with a complex argument



Two vertex Auxillary functions II

- ▶ An alternative for constant crossed field is to use the limit $\omega \rightarrow 0$
- ▶ Actually this was discussed by Nikishov-Ritus in regards to a decay process (JETP 19,5(1964))

$$\begin{aligned}\sum_{r=-\infty}^{+\infty} \int dr A^2 \delta(p_i + rk - p_f + k_f) &\approx \sum_{-r_{eff}}^{+r_{eff}} A^2 \delta(p_i - p_f + k_f) \\ &\approx \delta(p_i - p_f + k_f)\end{aligned}$$

- ▶ so in constant crossed field reduces to the field free process
- ▶ only for processes which occur also in absence of the external field
- ▶ Can I do the same thing for my auxillary function?

$$\frac{1}{(p_- k_1)} \text{Ai}\left(-l + \frac{\lambda^2}{2}\right) \exp\left[i\left(\frac{\lambda^3}{6} - \frac{\lambda l}{2}\right)\right]$$

The Volkov propagator poles

- ▶ The propagator denominator is a function of r

$$\frac{1}{(p_- k_1) + r(k p_-) - (k k_1)}$$

- ▶ The pole can be expressed as

$$r = -\frac{\omega_1}{\omega} \frac{\epsilon_-}{\epsilon_- - \omega_1}$$

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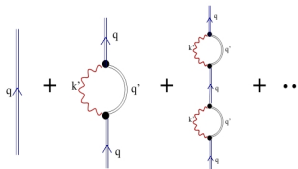
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- ▶ For bunch collisions we idealised the bunch field
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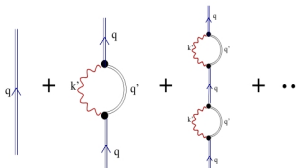
Volkov propagator radiative corrections



$$\begin{aligned} G_{SE}^e(x_2, x_1) &= \int d^4p E_p(x_2) \frac{1}{\not{p} - m} \bar{E}_p(x_1) \\ &+ \int d^4p E_p(x_2) \frac{1}{\not{p} - m} \Sigma^e(p) \frac{1}{\not{p} - m} \bar{E}_p(x_1) \\ &+ \dots \end{aligned}$$

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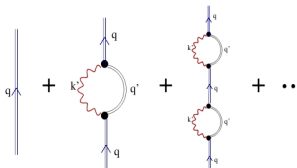
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- ▶ Inclusion of electron self energy is straightforward if we consider a self energy sandwiched between E functions
- ▶ Becker and Mitter argue that the divergence in the dressed self energy only occurs in the field free parts, therefore the regularization procedure is the same as for the non-external field case

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$$\begin{aligned}
 G_{SE}^e(x_2, x_1) &= \int d^4p E_p(x_2) \frac{1}{\not{p} - m} \bar{E}_p(x_1) \\
 &+ \int d^4p E_p(x_2) \frac{1}{\not{p} - m} \Sigma^e(p) \frac{1}{\not{p} - m} \bar{E}_p(x_1) \\
 &+ \dots
 \end{aligned}$$

- ▶ Inclusion of electron self energy is straightforward if we consider a self energy sandwiched between E functions
- ▶ Becker and Mitter argue that the divergence in the dressed self energy only occurs in the field free parts, therefore the regularization procedure is the same as for the non-external field case
- ▶ Actually we already saw this: since the Optical theorem relates the dressed self energy to beamstrahlung in

$$W \propto \int_0^\infty \frac{du}{(1+u)^2} \left[\int_x^\infty K_{5/3}(y) dy - \frac{u^2}{1+u} K_{2/3}(x) \right]$$

- ▶ Its better to say that the IR divergence in the dressed self energy coincides with that of the ordinary self energy

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- ▶ Work in progress - expect some numerical results!