
Chargino and Neutralino Masses

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Outline

- Introduction
- Samples
- Analysis methods
 - Background suppression cuts
 - Chargino/Neutralino events separation
 - Kinematic fitting
- Chargino/Neutralino mass extraction
- Summary and plan

Introduction

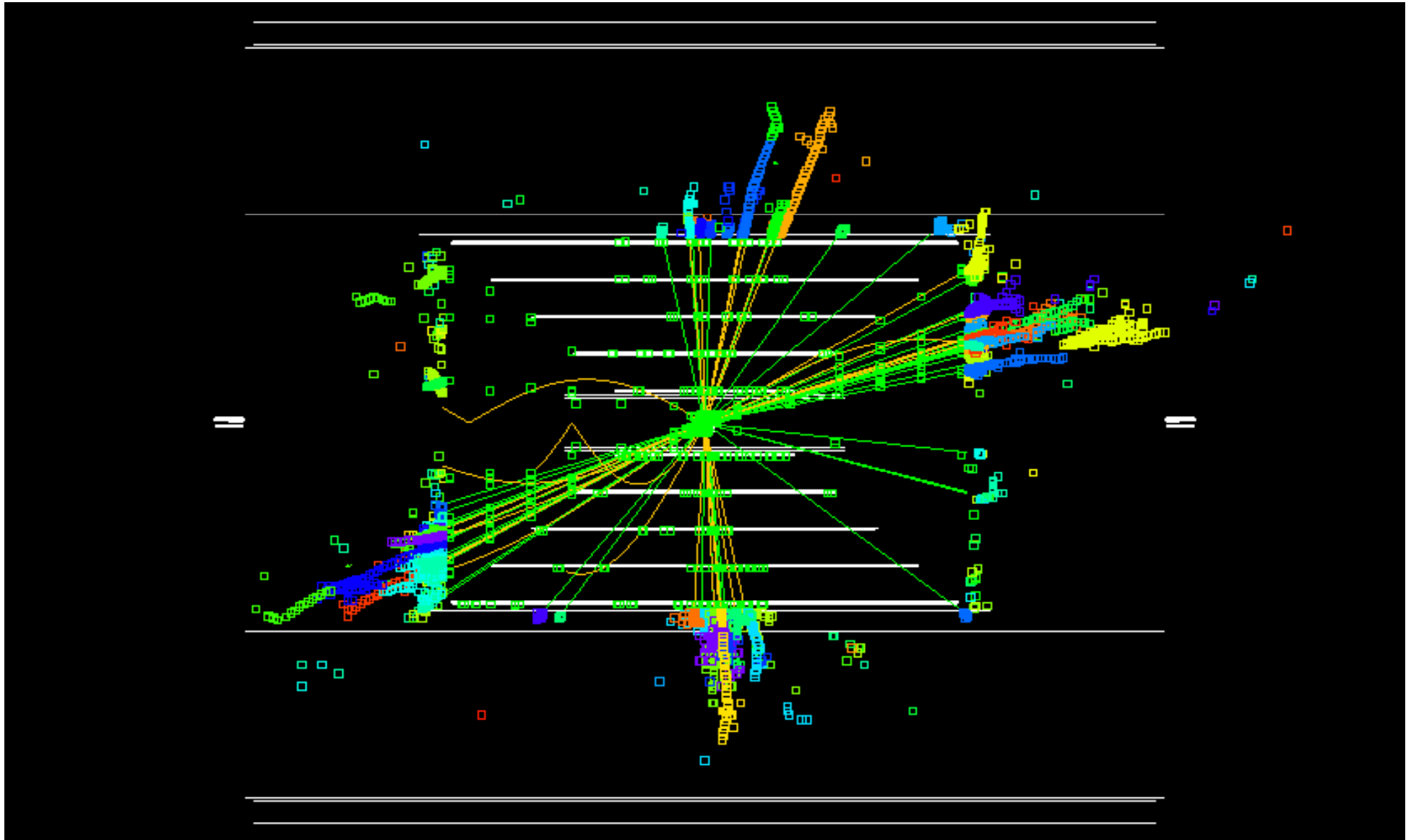
- Physics process:

$$\begin{aligned} e^+e^- &\rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 W^+ W^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q \bar{q} q \bar{q} \\ e^+e^- &\rightarrow \tilde{\chi}_2^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 Z^0 Z^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q \bar{q} q \bar{q} \end{aligned}$$

- Cross-section not too small
 - Chargino pair production: ~ 100 fb
 - Neutralino pair production: ~ 10 fb
- The gauge boson energy depends on the parent and LSP mass
- All hadronic decay channel of gauge boson
=> signature: 4 jets + missing energy

Introduction

$e^+e^- \rightarrow ne_2ne_2 \rightarrow ne_1ne_1ssdd$



Samples

- SUSY samples:
 - $\sqrt{s} = 500$ GeV; 500 fb⁻¹ luminosity; ~ 1.2 M events /sample
 - Polarization: 80% e⁻ L, 30% e⁺ R
 - Cross section (all boson decay channels included):
 - Chargino events: 132.0 fb
 - Neutralino events: 23.28 fb
 - Backgrounds: e⁺e⁻ \rightarrow ne1ne2, slepton pair production

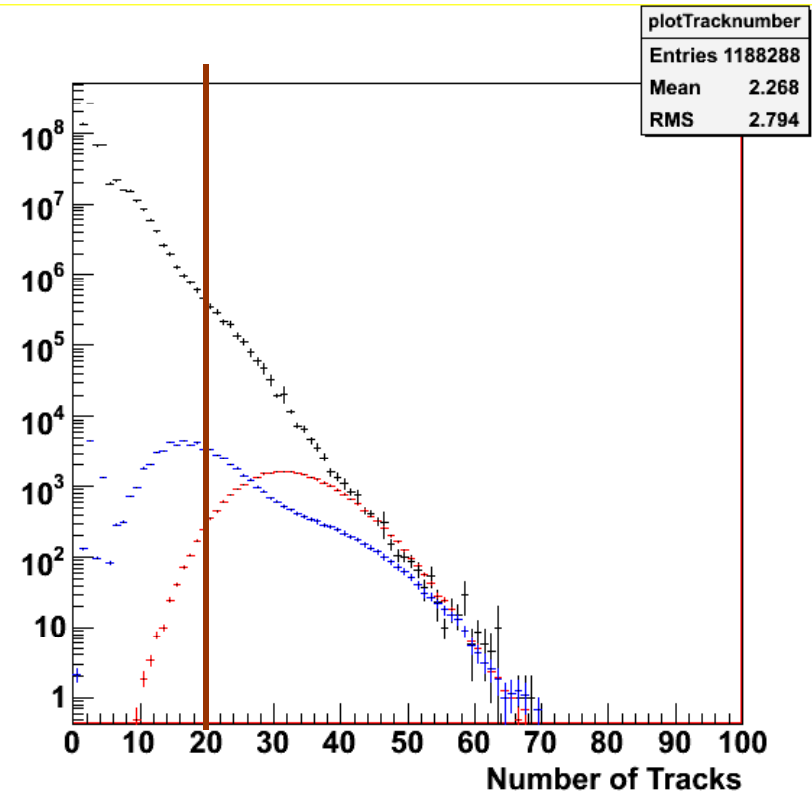
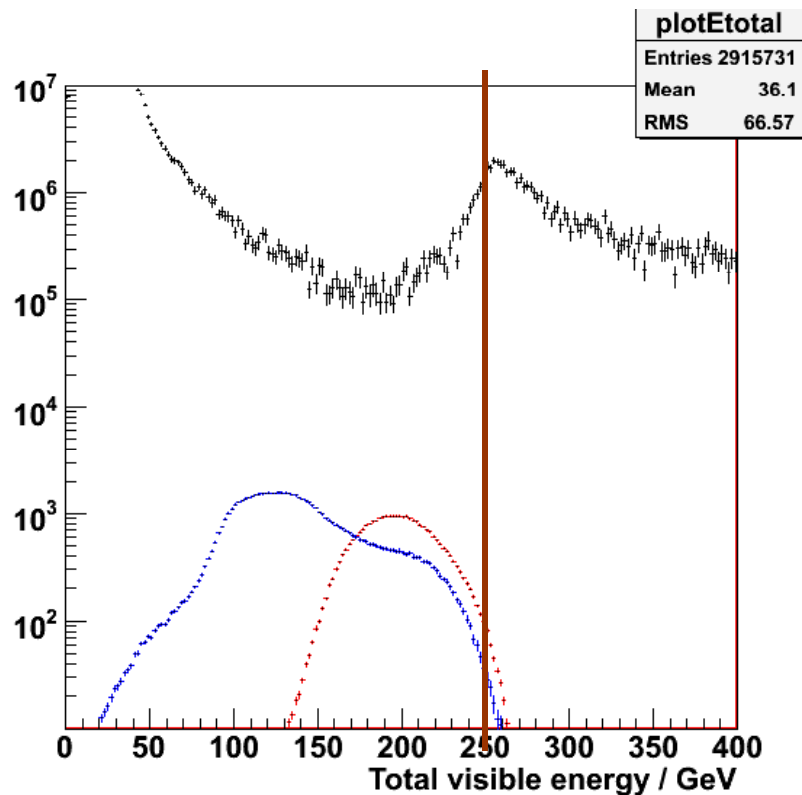
sample	$m_{\tilde{\chi}_1^0}$ (GeV)	$m_{\tilde{\chi}_1^\pm}$ (GeV)	$m_{\tilde{\chi}_2^0}$ (GeV)
Reference	115.7	216.7	216.5
$m_{\tilde{\chi}_1^0} + 0.5$	117.2	216.7	216.5
$m_{\tilde{\chi}_1^\pm} + 0.5$	115.7	217.2	216.5
$m_{\tilde{\chi}_2^0} + 0.5$	115.7	216.7	217.0

- SM background: 500 GeV, ~ 4.7 M events

Selection cuts

Number of jets	4
Total visible energy	$< 250 \text{ GeV}$
Number of tracks	> 20
Thrust	< 0.85
$\text{Cos } \theta_{\text{thrust}}$	< 0.9
$E(\text{jet})$	$> 10 \text{ GeV}$
No isolated lepton	
$E_{\text{lepton}}(\text{in jet } i)$	$E_{\text{lepton}, 1} < 40 \text{ GeV}, E_{\text{lepton}, 2} < 40 \text{ GeV},$ $E_{\text{lepton}, 3} < 40 \text{ GeV}, E_{\text{lepton}, 4} < 40 \text{ GeV}$
$f(\text{EM})$	$< 80\%$
Angle between jets	$\theta_{12} < 60^\circ; \theta_{13}, \theta_{14}, \theta_{23} < 40^\circ;$ $\theta_{24}, \theta_{34} < 20^\circ$
Acollinearity of two reco bosons	$> 10 \text{ degree}$

Selection cuts – visible energy, multiplicity

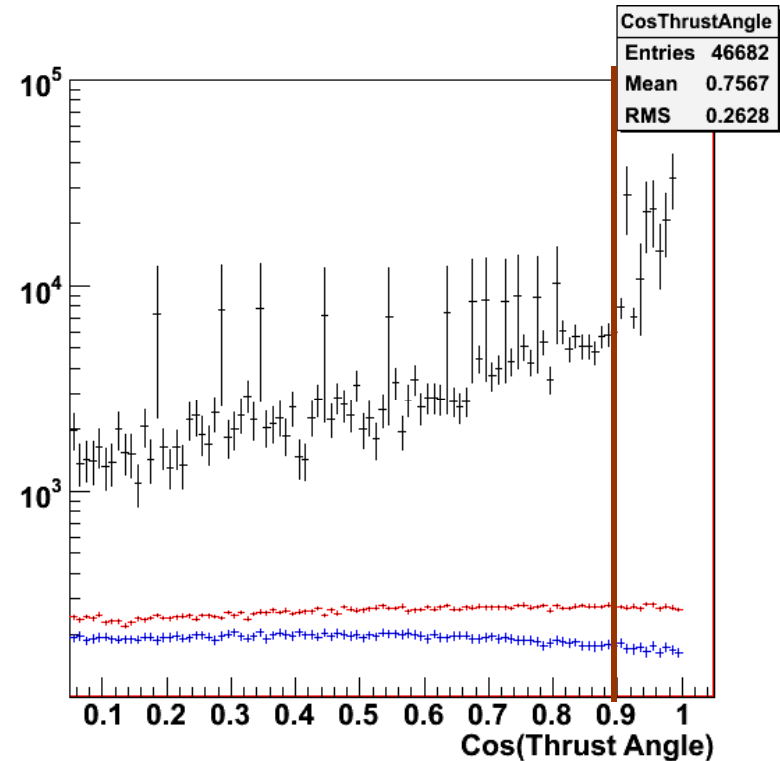
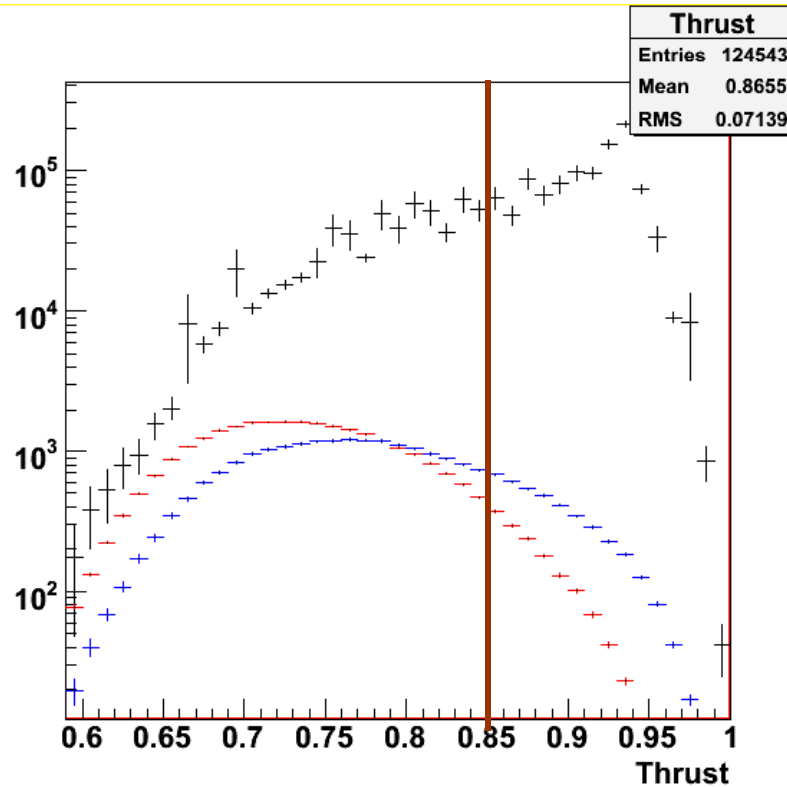


Red: Chargino signal (all hadronic channel)

Blue: SUSY background

Black: SM background

Selection cuts - thrust, thrust angle



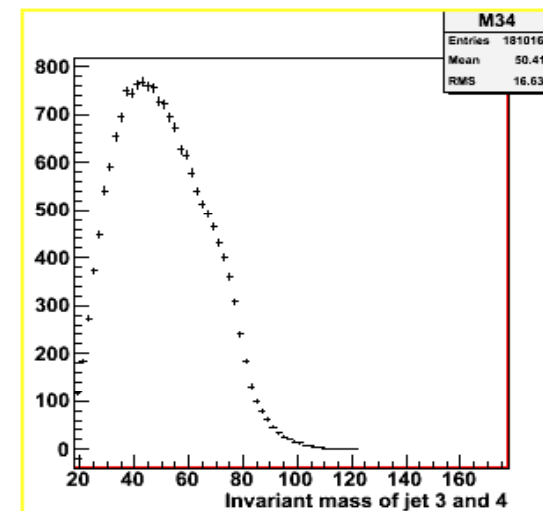
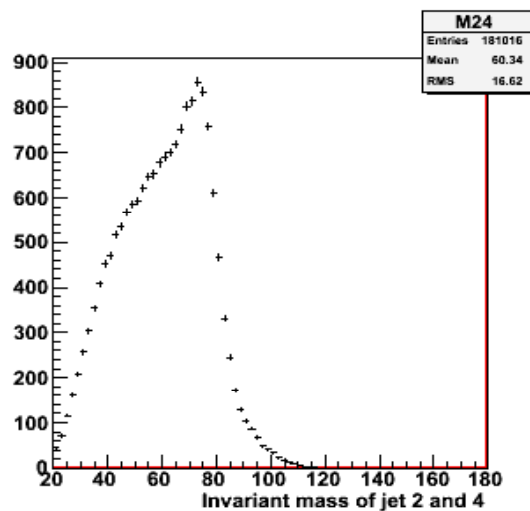
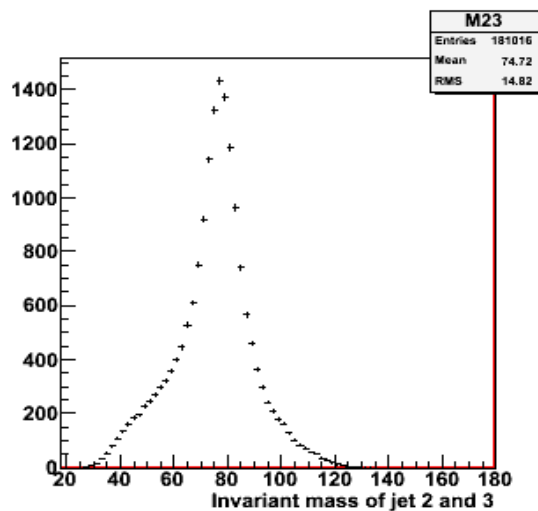
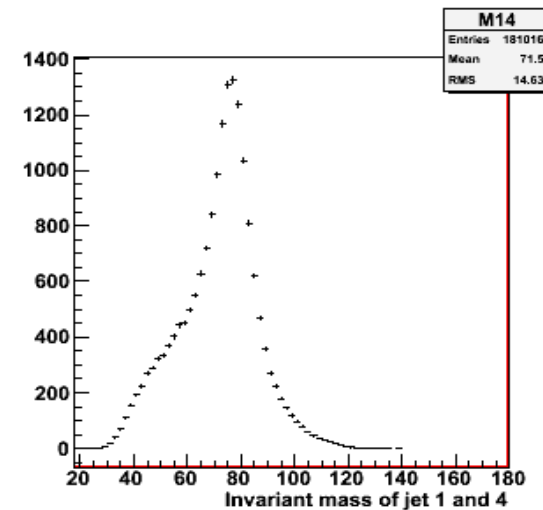
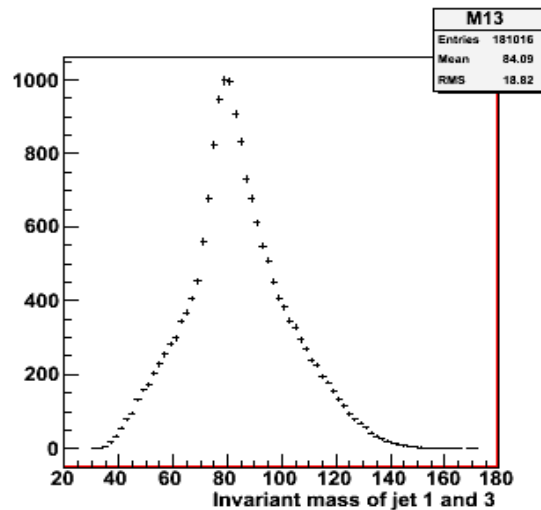
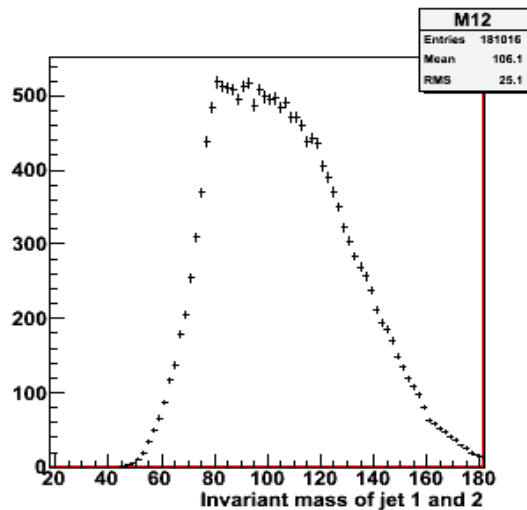
Red: Chargino signal (all hadronic channel)

Blue: SUSY background

Black: SM background

Chargino/ Neutralino Separation

- Based on the two reconstructed boson mass: W or Z
- Need to pair jets correctly
- All jet combinations for chargino selection:

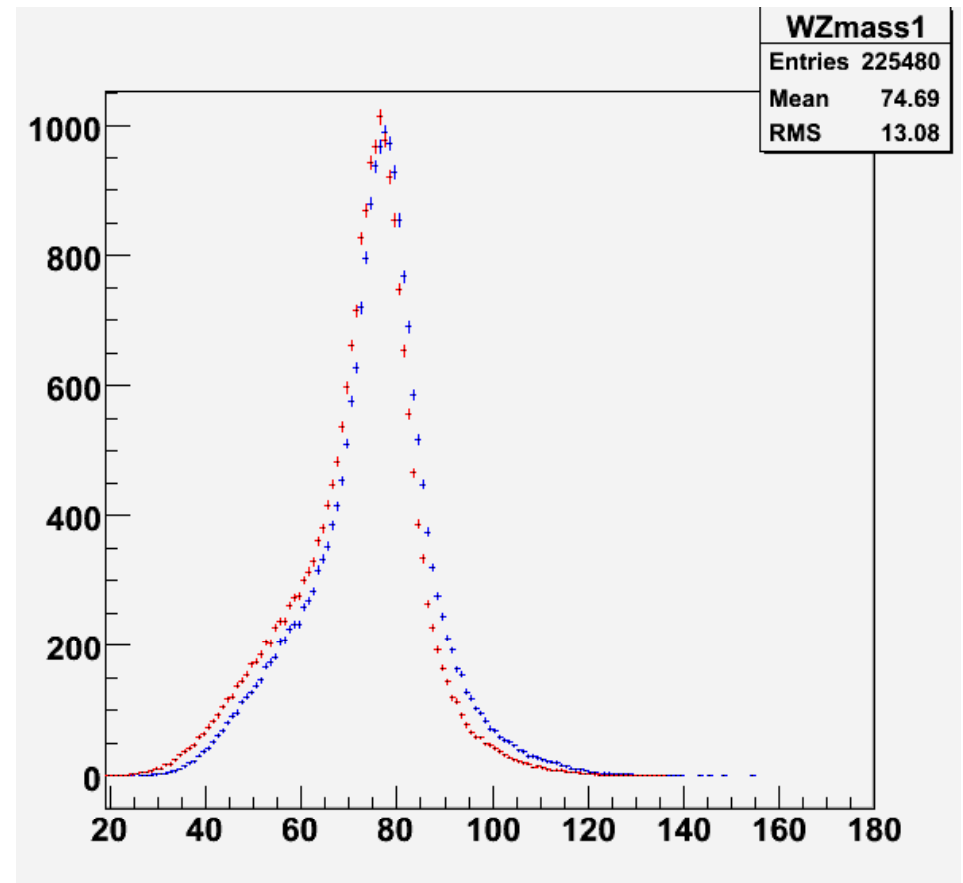


Chargino/ Neutralino Separation

- Jet pairing optimization:
- Choose the combination minimizing:
 - $(m_{j_1,j_2} - m_W)^2 + (m_{j_3,j_4} - m_W)^2$

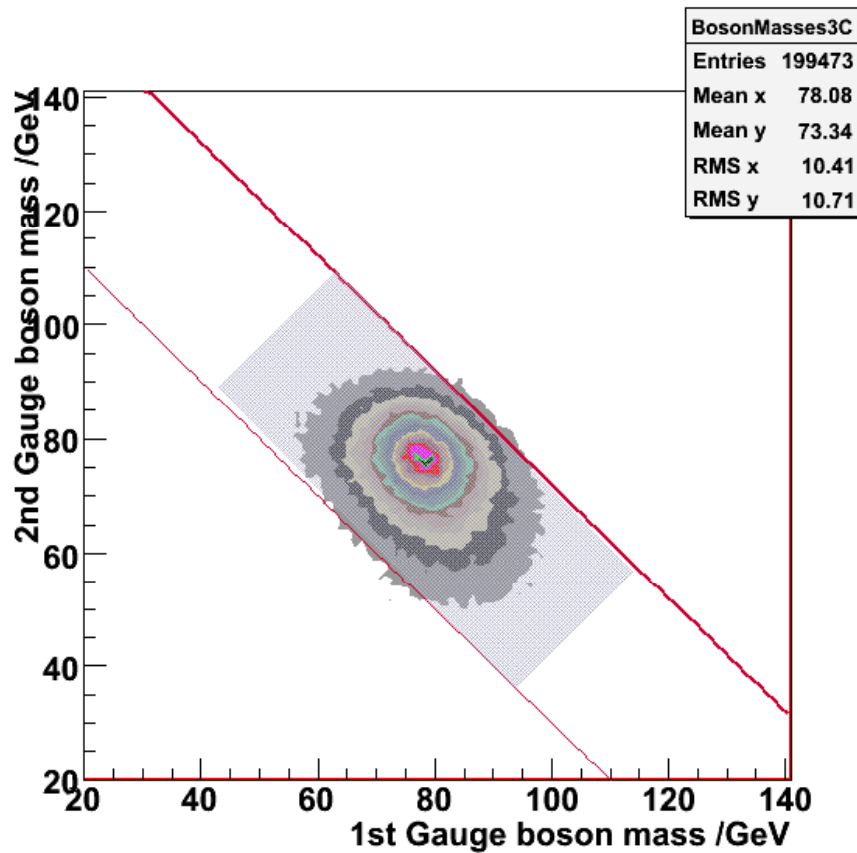
Blue: Reco'd mass of 1st W

Red: Reco'd mass of 2nd W



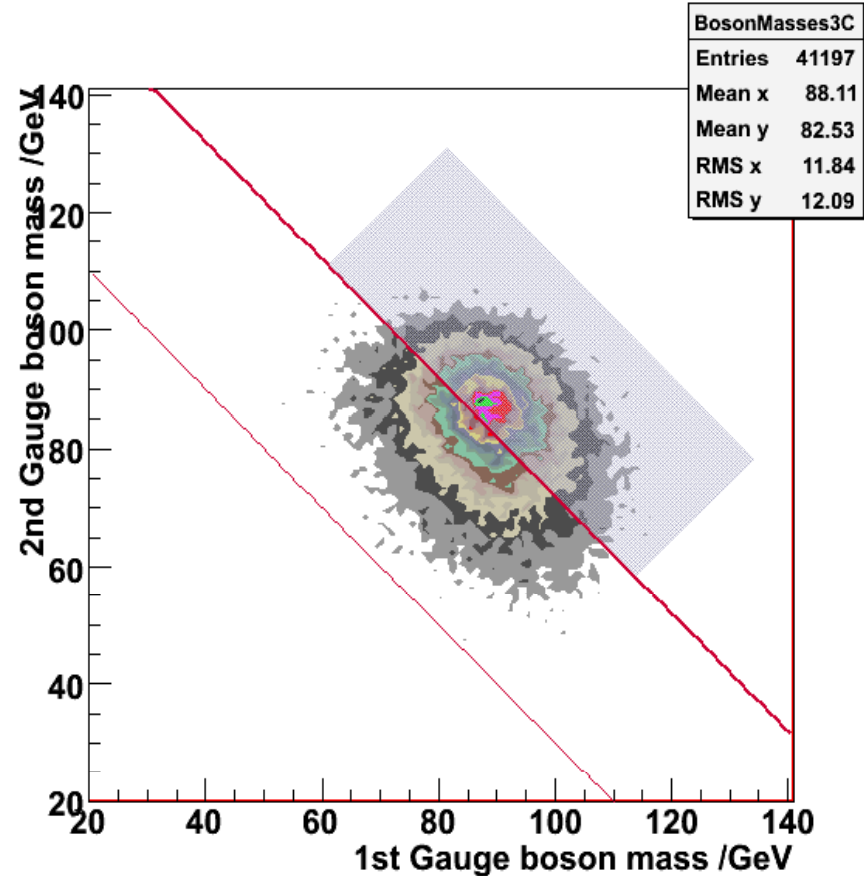
Chargino/ Neutralino Separation

Correlation of two di-jet masses is a powerful selection criteria



Chargino events signal

$$130 \text{ GeV} < M(W1) + M(W2) < 172 \text{ GeV}$$

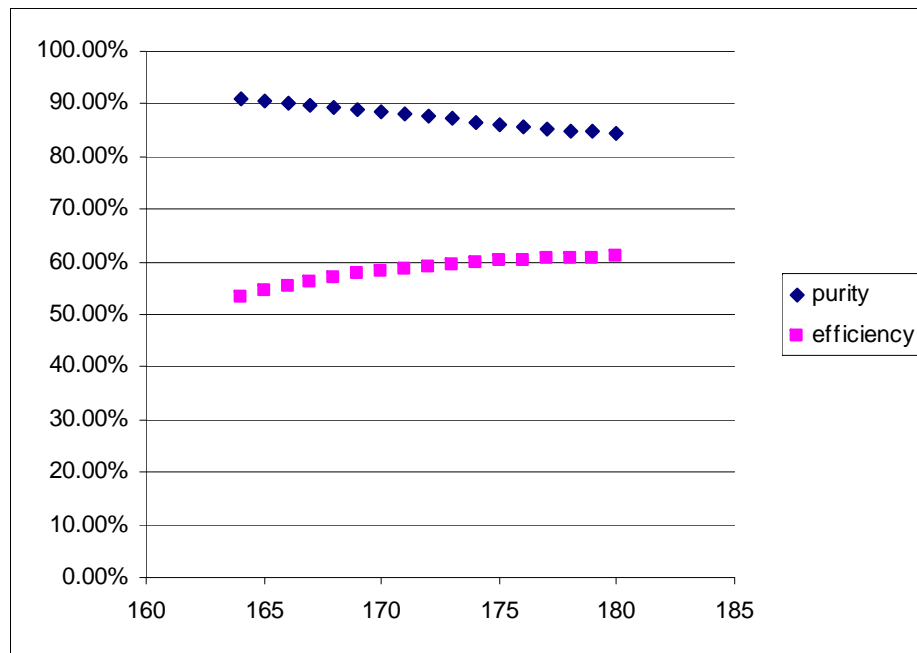


Neutralino events signal

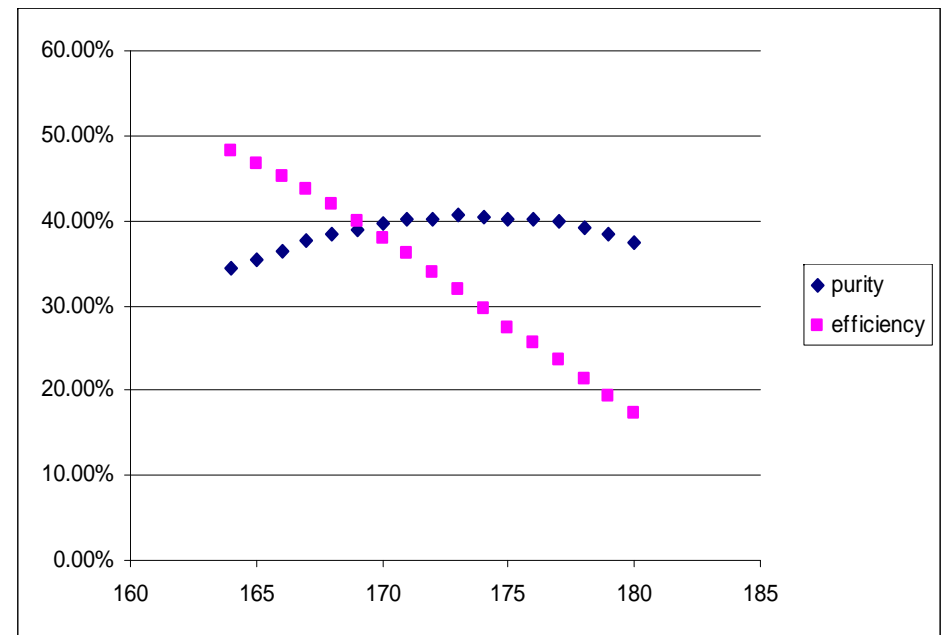
$$M(Z1) + M(Z2) > 172 \text{ GeV}$$

Chargino/ Neutralino Separation

Di-jet mass correlation cut



Chargino



Neutralino

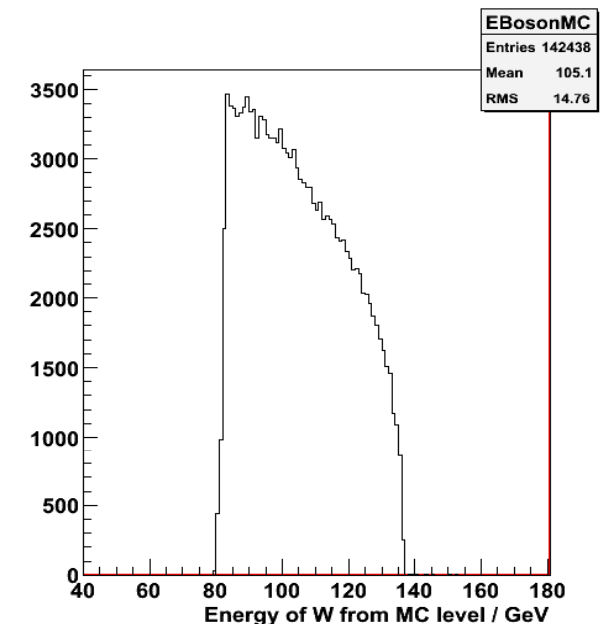
Boson energy & Chargino/Neutralino mass

- When $\chi_1(\nu_2) \rightarrow \nu_1 + W(Z)$, in χ_1 rest frame, the W is monochromatic

$$E_W = \frac{|(m_{\chi}^2 + m_W^2 - m_{\nu}^2)|}{2m_{\chi}}$$

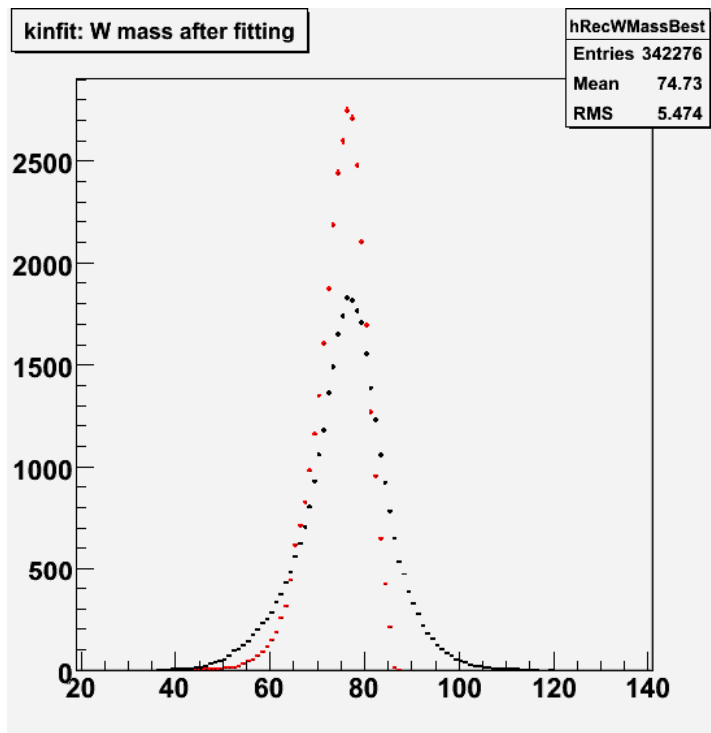
- In lab frame the W energy is boosted but still depends on the mass of chargino and neutralino.

- Therefore we can extract the chargino/neutralino energy (or their difference wrt MC sample) by comparing the W/Z energy spectrum with the template.

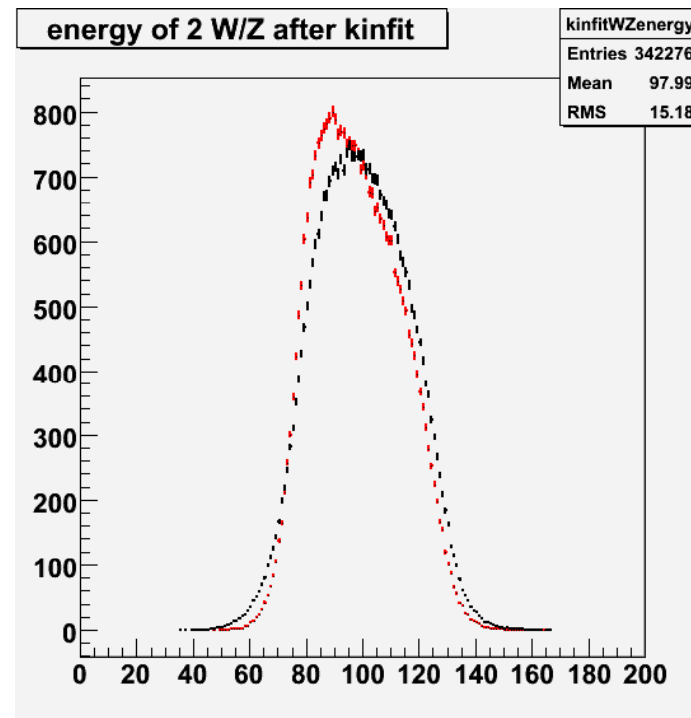


Kinematic fitting

- Kinematic fitting with one constraint ($M_{\text{boson1}} = M_{\text{boson2}}$) can help improve the boson energy distribution
- Kinfit in Marlinreco package is used.
- The parameters used:
 - $dE = 50\%/\sqrt{E}$; $d\theta = 0.1$ rad; $d\phi = 0.1$ rad



Reco'd W mass



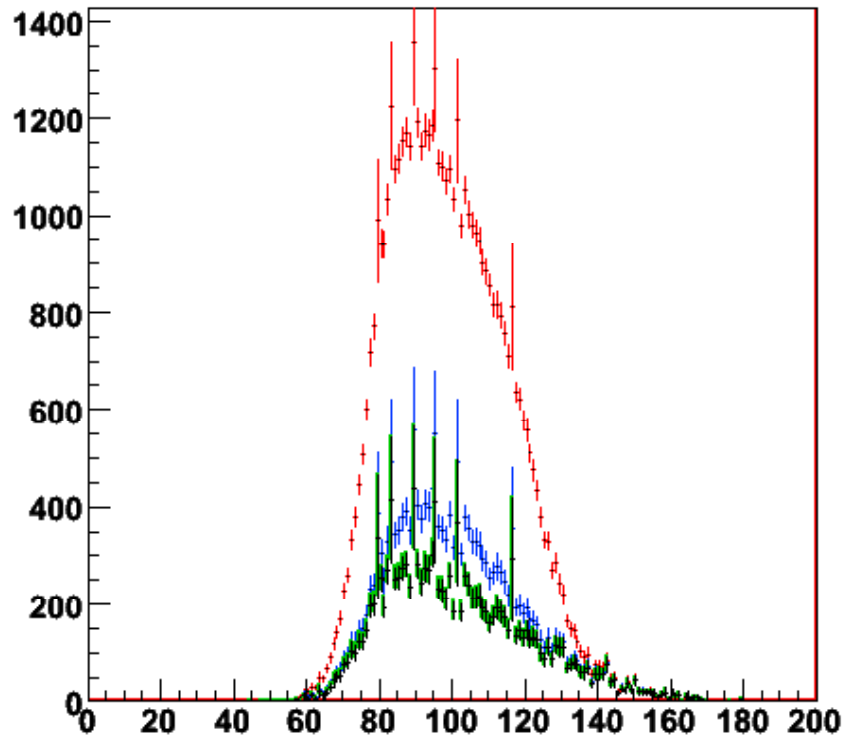
Reco'd W energy

Chargino
selection:
Before/ **After**
Kinfit

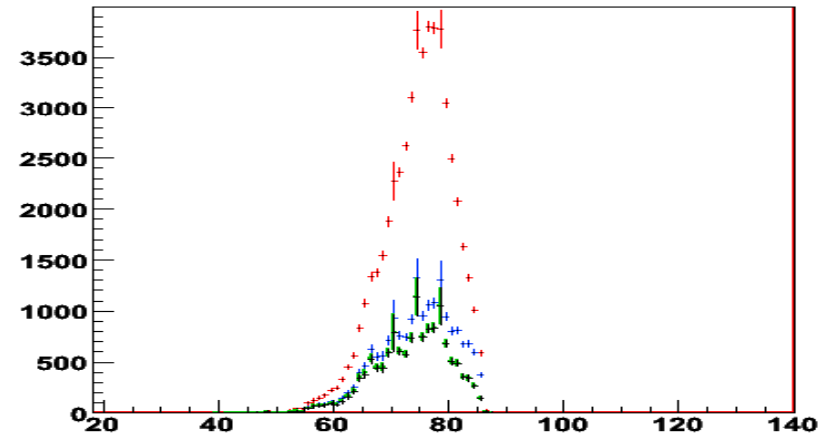
Results

Chargino selection

- (all hadronic) Chargino signal
- Neutralino events as bkg
- Other SUSY bkg
- SM bkg



Reco'd W energy /GeV



Reco'd W mass /GeV

Purity: 63.05%

Efficiency: 59.58%

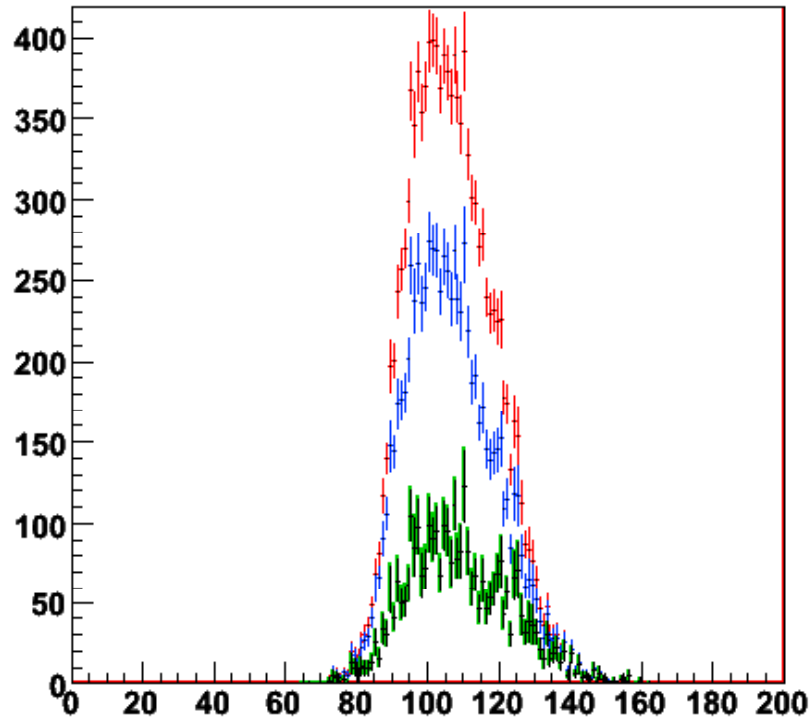
Background:

- SM 75.46%, neu2neu2 23.82%, other SUSY bkg 0.27%

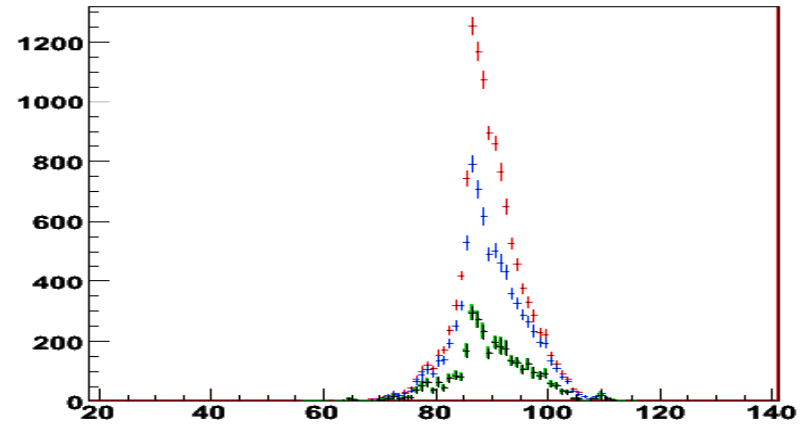
Results

Neutralino selection

- (all hadronic) Neutralino signal
- Chargino events as bkg
- Other SUSY bkg
- SM bkg



Reco'd Z energy / GeV



Reco'd Z mass / GeV

Purity: 30.77%

Efficiency: 35.68%

Background:

- SM 40.29%, chichi 59.48%, other SUSY bkg 0.24%

Template fitting

- When comparing the real data with the template, the change in *ith* bin content $\Delta y_i \sim \Delta m(\text{SUSY})$

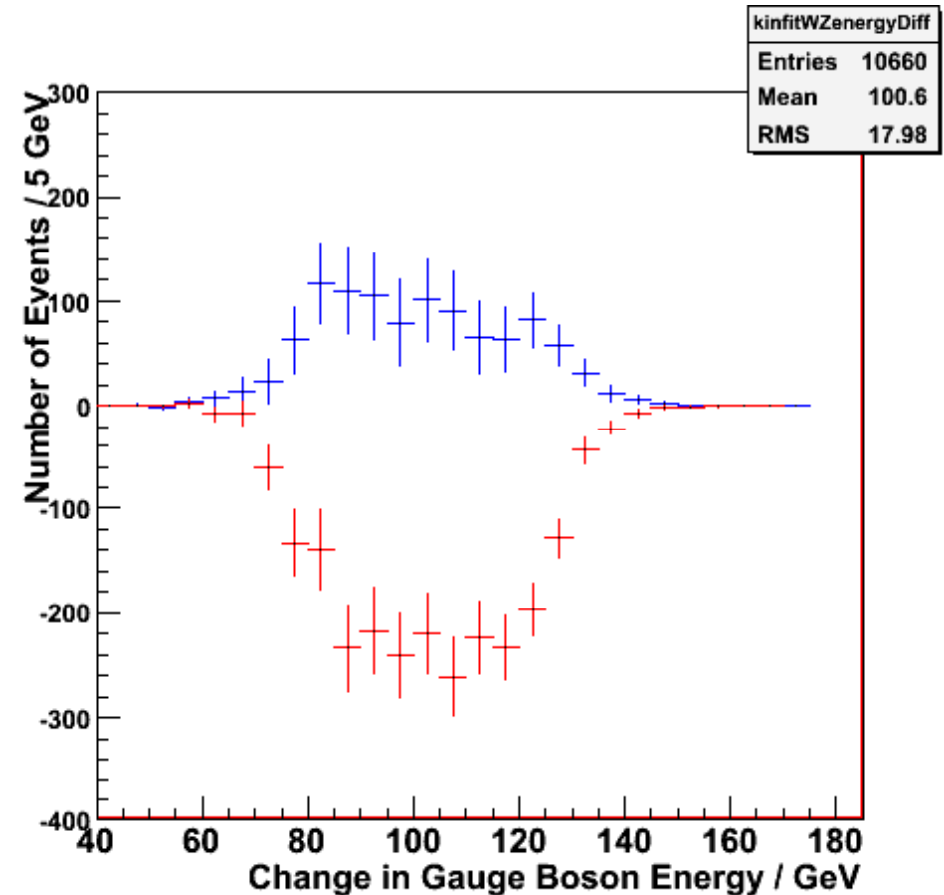
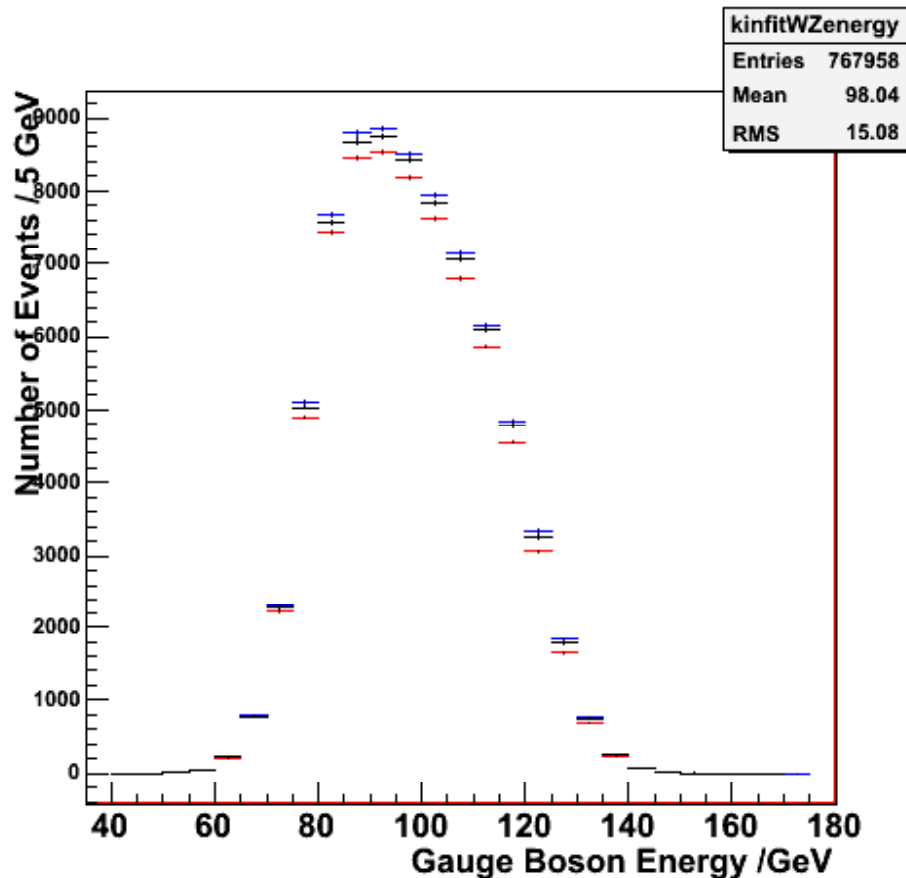
$$\Delta y_i = \left(\frac{\partial y}{\partial m_{\tilde{\chi}_1^\pm}} \right)_i \Delta m_{\tilde{\chi}_1^\pm} + \left(\frac{\partial y}{\partial m_{\tilde{\chi}_1^0}} \right)_i \Delta m_{\tilde{\chi}_1^0}$$

- Each derivative in the formula above is obtained by generating another sample with eg. $m(\text{chi})$ shifted. The mass difference from the template value can be extracted by doing least linear square fit for Δy_i wrt the derivatives.

Template fitting

Error on $\Delta m(\text{ch})$: 281 MeV

Error on $\Delta m(\text{neu1})$: 123 MeV



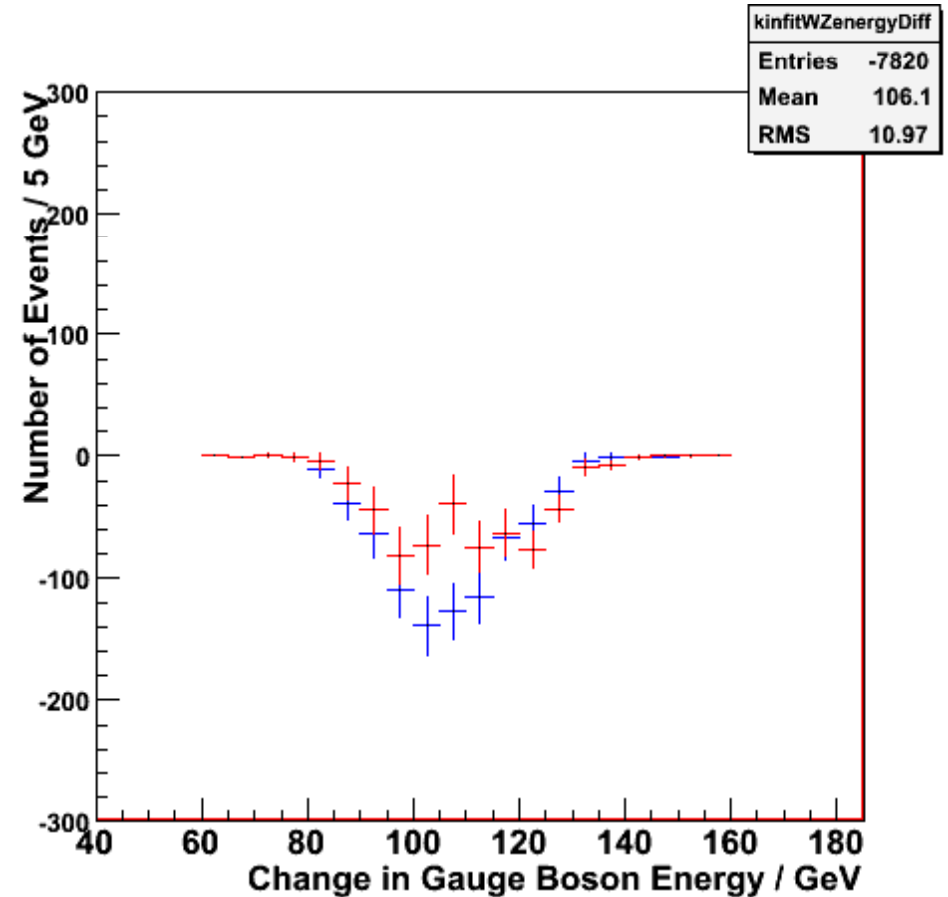
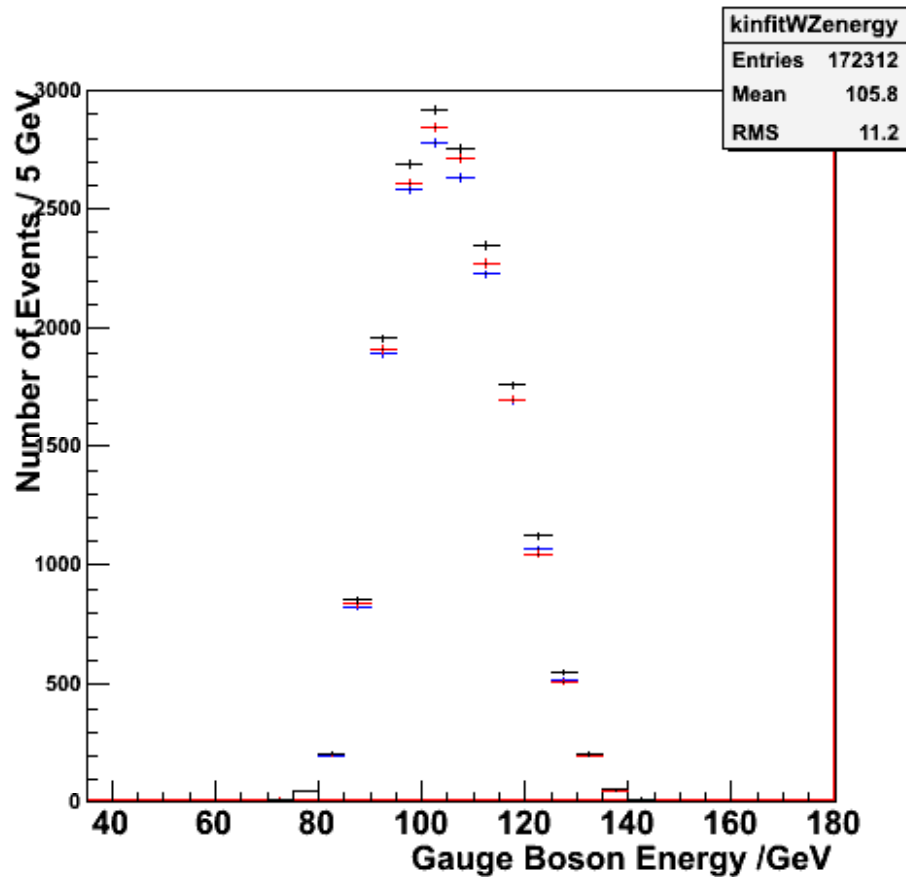
Reco'd W energy incl. all backgrounds(left) and its difference wrt the templates (right).

Red: $m(\text{neutrolino1}) + 0.5 \text{ GeV}$; **Blue:** $m(\text{chargino}) + 0.5 \text{ GeV}$

Template fitting

Error on $\Delta m(\text{neu}2)$: 161 MeV

Error on $\Delta m(\text{neu}1)$: 214 MeV



Reco'd Z energy incl. all backgrounds (left) and its difference wrt the templates (right).

Red: $m(\text{neutrolino}1) + 0.5 \text{ GeV}$; **Blue:** $m(\text{neutrolino}2) + 0.5 \text{ GeV}$

Template fitting

$\Delta m(\text{ch})$
/ GeV

for the binning on previous slides:

Chargino selection:

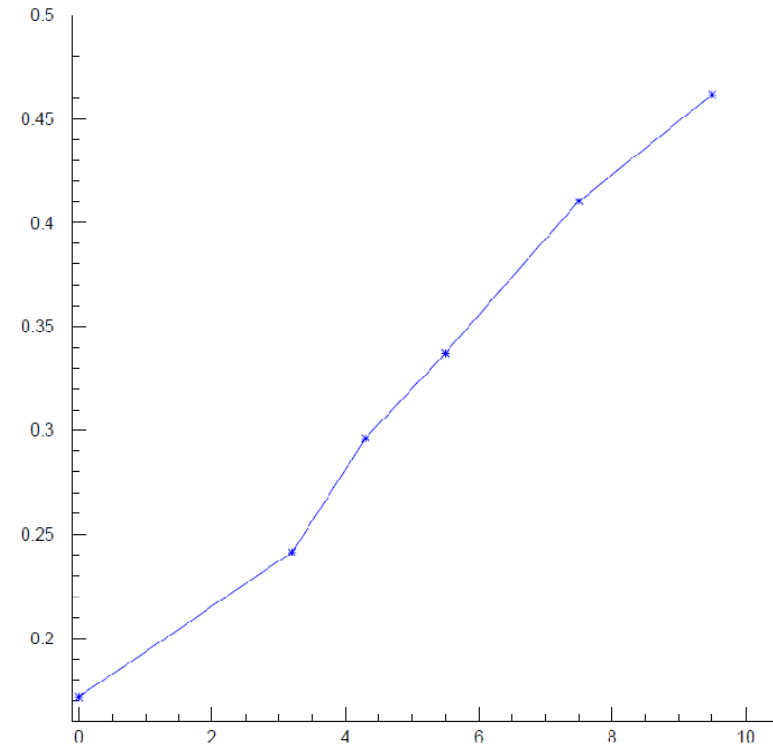
Error on $\Delta m(\text{ch})$: 281 MeV

Error on $\Delta m(\text{neu1})$: 123 MeV

Neutralino selection:

Error on $\Delta m(\text{neu2})$: 161 MeV

Error on $\Delta m(\text{neu1})$: 214 MeV



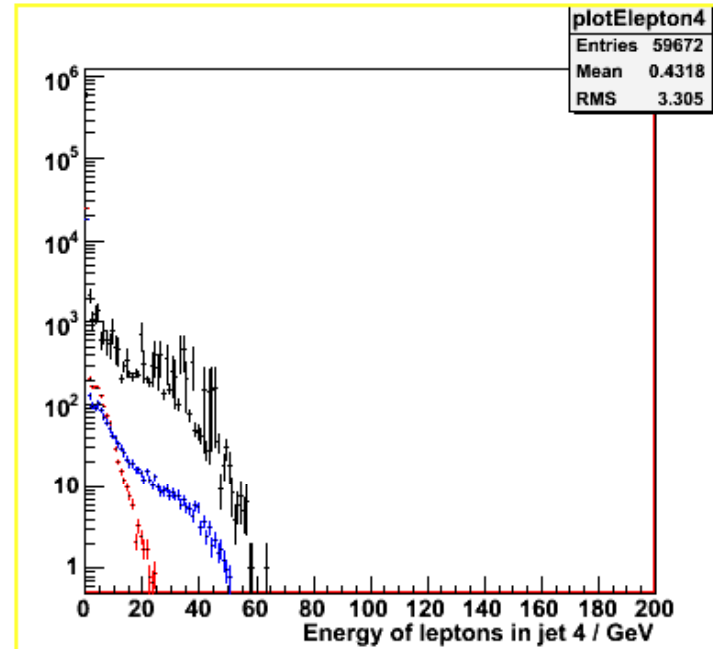
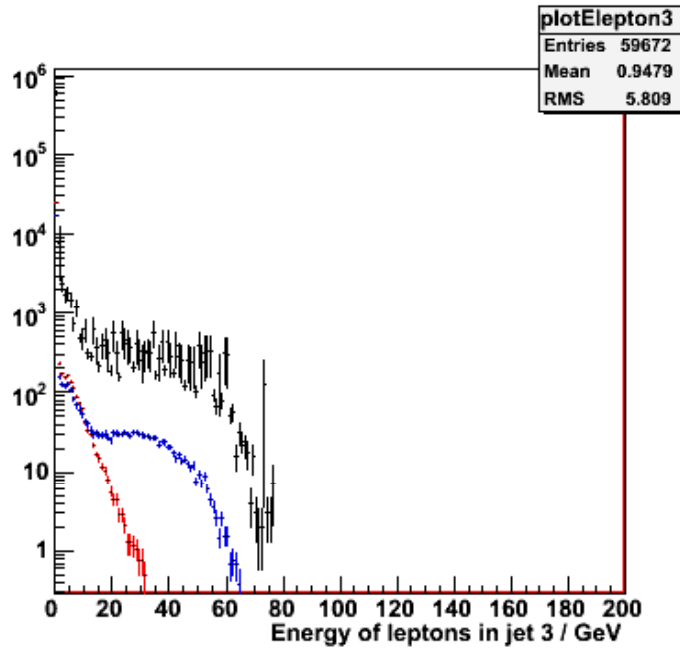
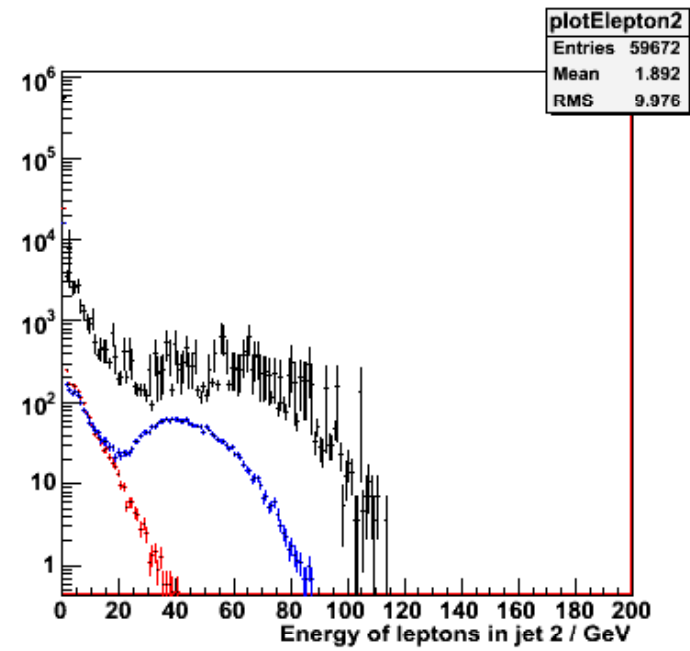
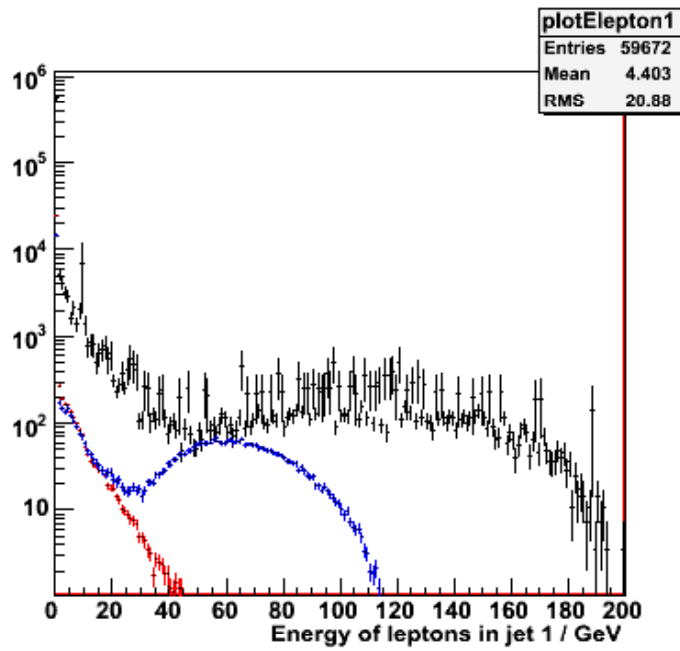
$$\left(\frac{\Delta E_{\text{jet}}}{E_{\text{jet}}} \right)_{90} (\%)$$

Study of error on chargino mass based on fastmc.
(Tim Barklow)

Summary and plan

- Chargino / neutralino events can be identified at the presence of SM bkg, and separated from each other.
 - Chargino selection has much better performance
- More efforts could be made to further suppress SM background.
- Cuts have to be optimized to achieve the best purity * efficiency.
- Template fitting has provided a framework for chargino/neutralino mass extraction, but more understanding on the error estimation is needed.

Backups

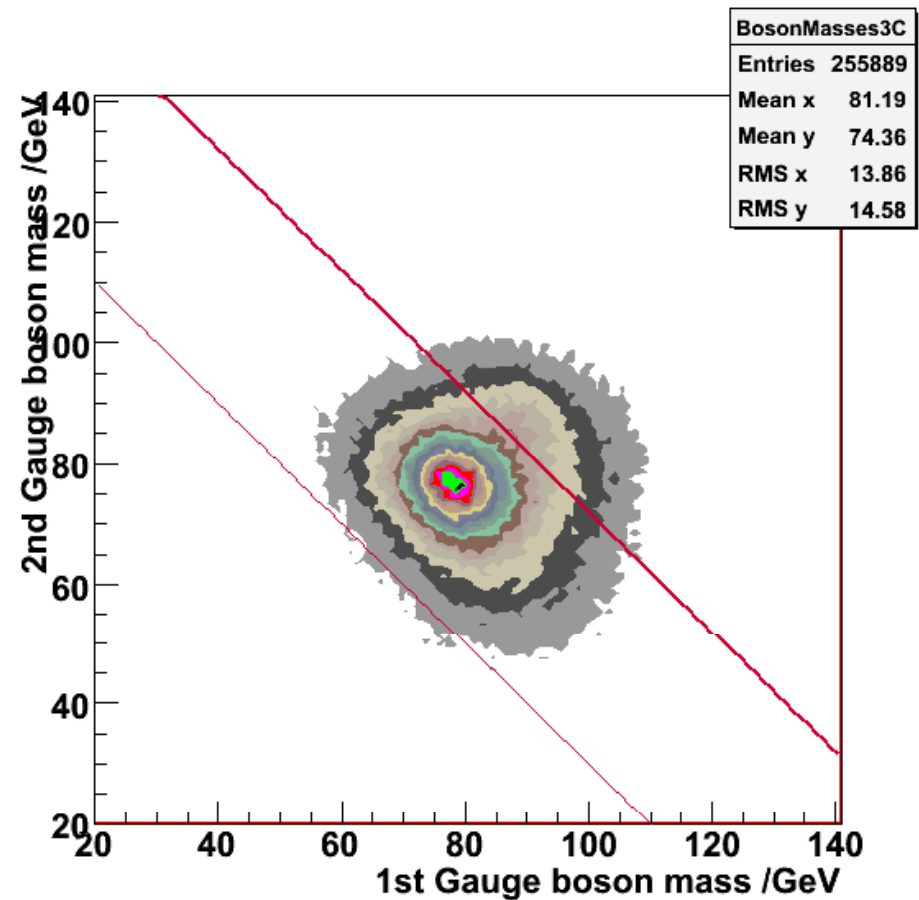
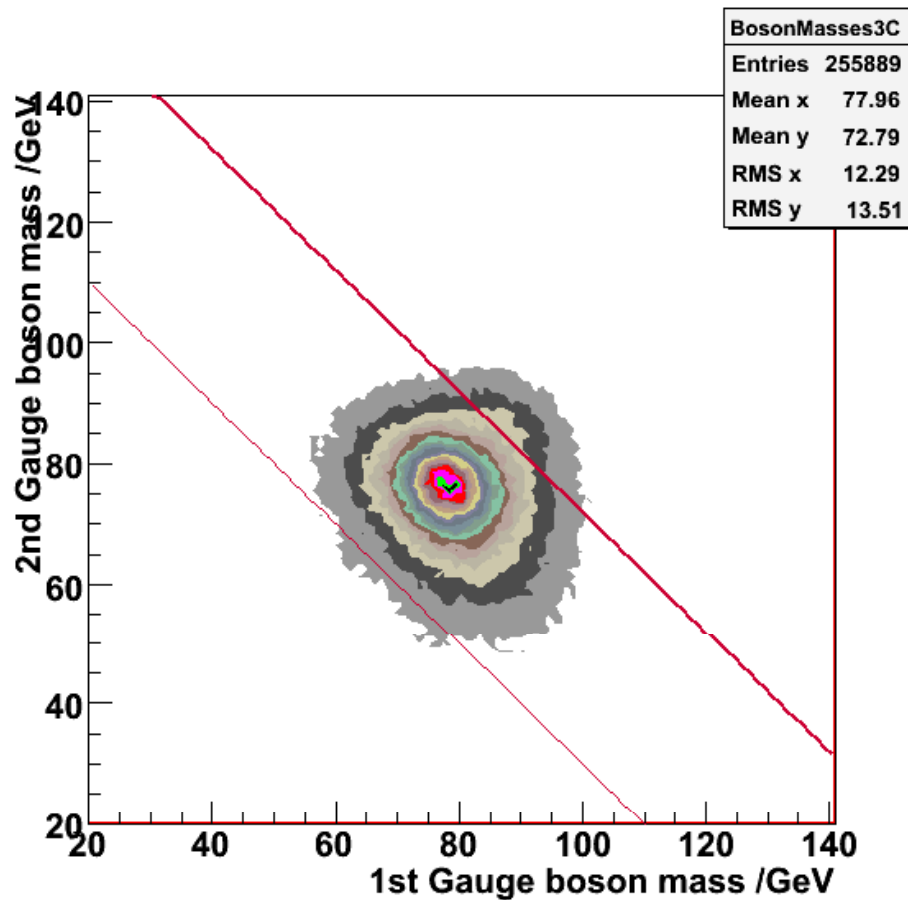


Chargino selection cuts

	ChiChi signal		Neu2Neu2 bkg		SM background	
nBeforecut Jet Number	28506	100%	11648.1	100%	6.12E+09	100%
nBeforecut E Total	28506	100%	10855.9	93.20%	1.07E+09	17.50%
nBeforecut Track Number	28189.7	98.89%	10752.2	92.31%	9.61E+08	15.70%
nBeforecut Thrust	27506	96.49%	7322.06	62.86%	1.70E+06	0.03%
nBeforecut CosThrustAngle	26038.1	91.34%	6428.18	55.19%	607485	0.01%
nBeforecut IsolatedLepton	23303.8	81.75%	5852.54	50.24%	330098	0.01%
nBeforecut fEM	23303.5	81.75%	5633.26	48.36%	324119	0.01%
nBeforecut Lepton energy	22584.1	79.23%	5318.33	45.66%	300008	0.00%
nBeforecut Jet Energy	22566.2	79.16%	5176.57	44.44%	297471	0.00%
nBeforecut Jet Angles	22360.2	78.44%	4794.56	41.16%	131883	0.00%
nBeforecut Acollinearity	19412.1	68.10%	4218.05	36.21%	38135.6	0.00%
nBeforecut 2BosonMassMax	18975.7	66.57%	3998.48	34.33%	36916.6	0.00%
nBeforecut 2BosonMassMin	18171.1	63.74%	2608.71	22.40%	36091	0.00%
nAftercut 2BosonMassMin	16983.3	59.58%	2371.4	20.36%	7511.14	0.00%

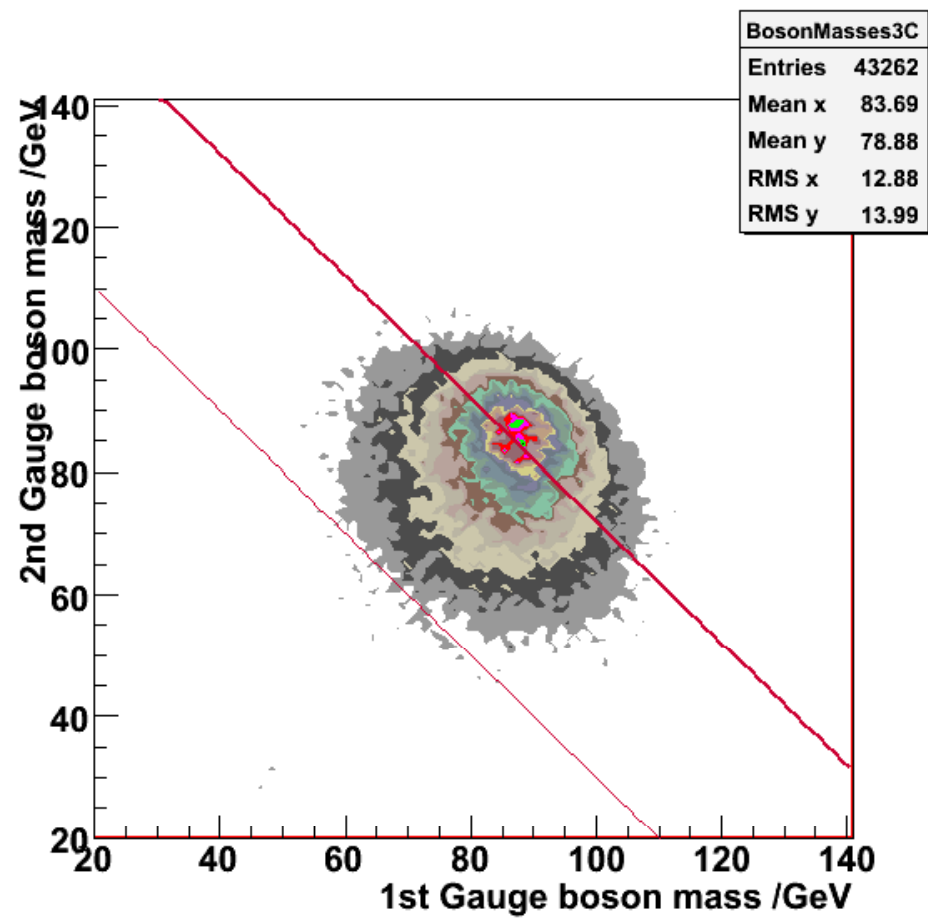
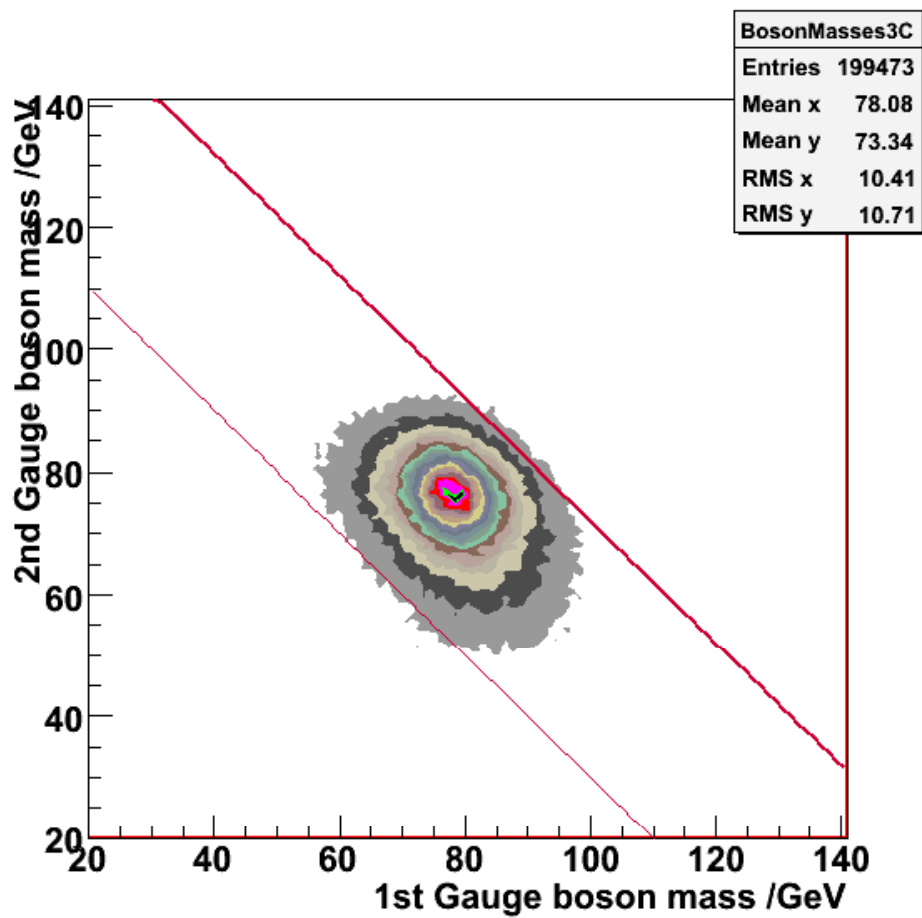
Neutralino selection cuts

	Neu2Neu2 signal		ChiChi bkg		SM background	
nBeforecut Jet Number	5478.23	100%	66060.1	100%	6.12E+09	100%
nBeforecut E Total	5478.23	100%	61875.6	93.67%	1.07E+09	17.50%
nBeforecut Track Number	5410.57	98.76%	61536.4	93.15%	9.61E+08	15.70%
nBeforecut Thrust	5349.34	97.65%	36470.7	55.21%	1.70E+06	0.03%
nBeforecut CosThrustAngle	4929.11	89.98%	33505	50.72%	607485	0.01%
nBeforecut IsolatedLepton	4480.71	81.79%	30079.6	45.53%	330098	0.01%
nBeforecut fEM	4480.71	81.79%	28746.8	43.52%	324119	0.01%
nBeforecut Lepton energy	4373.56	79.84%	26235.3	39.71%	300008	0.00%
nBeforecut Jet Energy	4355.91	79.51%	25064.9	37.94%	297471	0.00%
nBeforecut Jet Angles	4330.46	79.05%	24140.5	36.54%	131883	0.00%
nBeforecut Acollinearity	4251.2	77.60%	22808.5	34.53%	98988.5	0.00%
nBeforecut 2BosonMassMax	4212.39	76.89%	22176	33.57%	70174.7	0.00%
nBeforecut 2BosonMassMin	4113.23	75.08%	21274.5	32.20%	56676	0.00%
nAftercut 2BosonMassMin	4043.62	73.81%	20559.4	31.12%	40959	0.00%



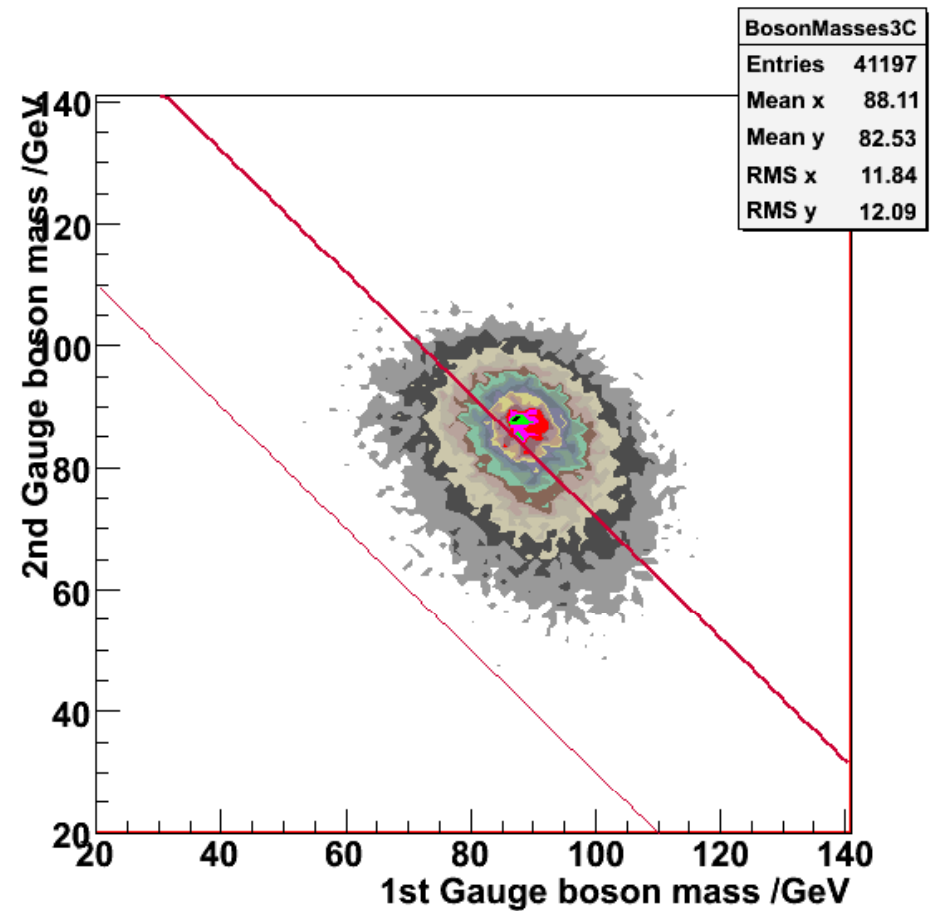
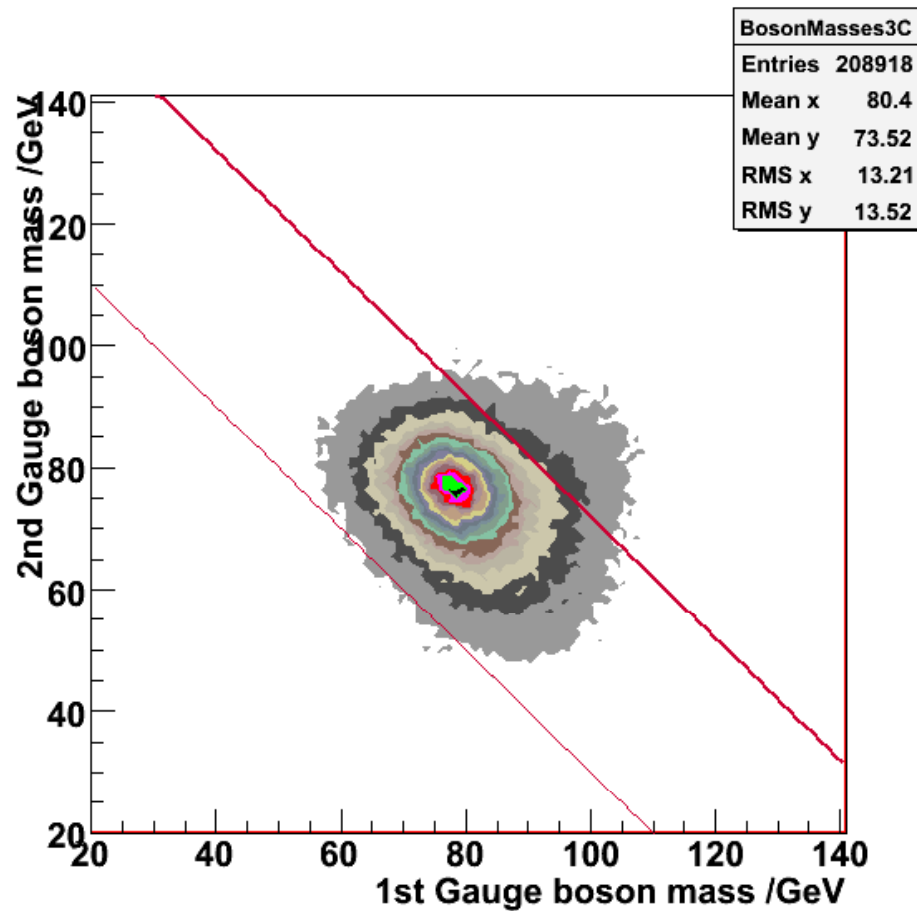
The two boson masses of all SUSY events

Left: chargino events selection; right: neutralino events selection



Chargino events selection:

Left: true chargino events; right: true neutralino events



Neutralino events selection:

Left: true chargino events; right: true neutralino events