

ILC beam-parameters and the $\tilde{\tau}$ channel in SPS1a'

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LCWS, Beijing, 28 Mar 2010

Outline

- $\tilde{\tau}$:s in SPS1a'
- RDR \rightarrow SB2009.
- Conclusions.

$\tilde{\tau}$ in SPS1a'

Pure mSUGRA model:

$$M_{1/2} = 250 \text{ GeV}, M_0 = 70 \text{ GeV}, A_0 = -300 \text{ GeV}, \\ \tan \beta = 10, \text{sign}(\mu) = +1$$

Just outside what is excluded by LEP and low-energy observations.
Compatible with WMAP, with $\tilde{\chi}_1^0$ Dark Matter.

- All sleptons available.
- No squarks.
- Lighter bosinos, up to $\tilde{\chi}_3^0$ (in $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_3^0$)

Features of $\tilde{\tau}$:s in SPS1a'

- In SPS1a', the $\tilde{\tau}_1$ is the NLSP.
- $M_{\tilde{\tau}_1} = 107.9 \text{ GeV}$, $M_{\tilde{\tau}_2} = 194.9 \text{ GeV}$, $M_{\tilde{\chi}_1^0} = 97.7 \text{ GeV}/c^2$
- $E_{\tilde{\tau}_1, \min} = 2.6 \text{ GeV}$, $E_{\tilde{\tau}_1, \max} = 42.5 \text{ GeV}$: $\gamma\gamma$ background.
- $E_{\tilde{\tau}_2, \min} = 35.0 \text{ GeV}$, $E_{\tilde{\tau}_2, \max} = 152.2 \text{ GeV}$: $WW \rightarrow l\nu l\nu$ background.
- The $\tilde{\tau}$ mass-eigen states \neq chiral-eigen states. Off-diagonal term of mass-matrix: $-M_\tau(A_{\tilde{\tau}} - \mu \tan \beta)$.
- $\tilde{\tau}$ NLSP $\rightarrow \tau$:s in most SUSY decays \rightarrow SUSY is background to SUSY.
- For pol=(-1,1): $\sigma(\tilde{\chi}_2^0 \tilde{\chi}_2^0)$ and $\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)$ = several hundred fb and BR($X \rightarrow \tilde{\tau}$) > 50 %. For pol=(1,-1): $\sigma(\tilde{\chi}_2^0 \tilde{\chi}_2^0)$ and $\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-) \approx 0$.

Polarisation = (0.8, -0.3) assumed.

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Extracting the $\tilde{\tau}$ properties

From decay kinematics:

- $M_{\tilde{\tau}}$ from $M_{\tilde{\chi}_1^0}$ and end-point of spectrum = $E_{\tau,max}$.
- Need to measure end-point of spectrum.
- In principle: $M_{\tilde{\chi}_1^0}$ turn-over of spectrum = $P_{\tau,min}$, but hidden in $\gamma\gamma$ background.
- Must get $M_{\tilde{\chi}_1^0}$ from other sources. ($\tilde{\mu}$, \tilde{e} , not yet done)

From cross-section:

- $\sigma_{\tilde{\tau}} = A(\theta_{\tilde{\tau}}, \mathcal{P}_{beam}) \times \beta^3 / s$, so
- $M_{\tilde{\tau}} = E_{beam} \sqrt{1 - (\sigma s / A)^{2/3}}$: no $M_{\tilde{\chi}_1^0}$!

Topology selection

$\tilde{\tau}$ properties:

- Only two τ :s in the final state.
- Large missing energy and momentum.
- High acollinearity, with little correlation to the energy of the τ decay-products.
- Central production.
- No forward-backward asymmetry.

Select this by:

- Exactly two jets.
- $N_{ch} < 10$
- Vanishing total charge.
- Charge of each jet = ± 1 ,
- $M_{jet} < 2.5 \text{ GeV}/c^2$,
- $E_{vis} < 300 \text{ GeV}$,
- $M_{miss} > 250 \text{ GeV}/c^2$,
- No particle with momentum above $180 \text{ GeV}/c$ in the event.

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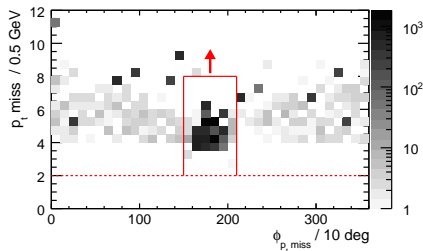
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$\gamma\gamma$ suppression

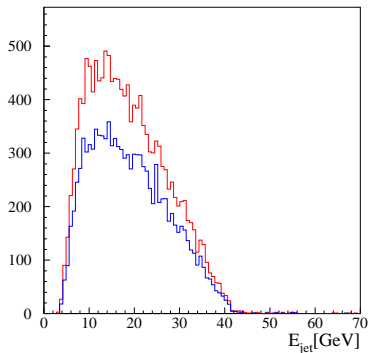
$\Delta(M) = 10.2 \text{ GeV}/c^2 \rightarrow \gamma\gamma$ background ...

- Correlated cut in ρ and θ_{acop} :
 $\rho > 2.7 \sin \theta_{acop} + 1.8$.
- no significant activity in the BeamCal
- $\phi_{p_{miss}}$ not in the direction of the incoming beam-pipe.



Finding τ :s

In particular in the presence of beam-background, general jet-finders perform poorly when used to find τ :s Use the **DELPHI τ -finder**: Performs **better than Durham** forced to two jets **already without background**:



BLUE: Durham, RED: DELPHI

End-point and cross-section

Additional cuts against $\gamma\gamma$

- $|\cos \theta_{\text{missing momentum}}| < 0.8$
- Low fraction of “Rest-of-Event” energy at low angles.
- Good agreement $p_{\text{track}} - E_{\text{calo}}$

From now on: Different cuts for $\tilde{\tau}_1$ ($\gamma\gamma$ background), and $\tilde{\tau}_2$ (WW background).

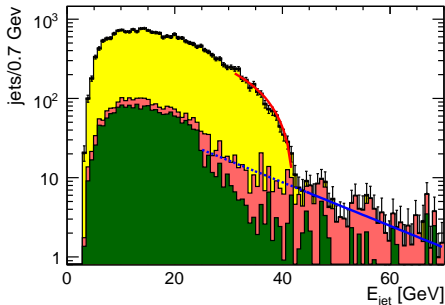
- | | |
|---|--|
| • $E_{\text{vis}} < 120$ GeV, | • $E_{\text{vis}} > 50$ GeV. |
| • $ \cos \theta_{\text{jet}} < 0.9$ for both jets, | • $\theta_{\text{acop}} < 155^\circ$. |
| • $\theta_{\text{acop}} > 85^\circ$, | • Other side jet not e or μ |
| • $(E_{\text{jet1}} + E_{\text{jet2}}) \sin \theta_{\text{acop}} < 30$ GeV. | • Most energetic jet not e or μ |
| • $M_{\text{vis}} > 20$ GeV/ c^2 . | • Cut on Signal-SM LR of $f(q_{\text{jet1}} \cos \theta_{\text{jet1}}, q_{\text{jet2}} \cos \theta_{\text{jet2}})$ |

Fitting the $\tilde{\tau}$ mass: Endpoint

- Only the upper end-point is relevant.
- Background subtraction:
 - $\tilde{\tau}_1$: Important SUSY background, but region above 45 GeV is signal free. Fit exponential and extrapolate.
 - $\tilde{\tau}_2$: \sim no SUSY background above 45 GeV. Take background from SM-only simulation and fit exponential.
- Fit line to (data-background fit).

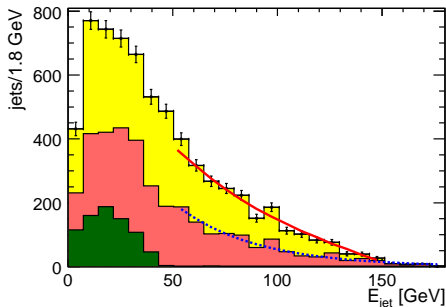
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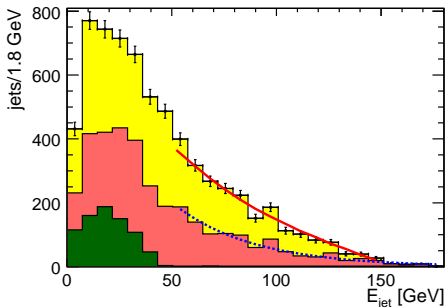
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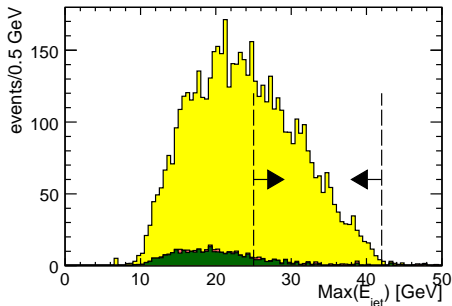


Fitting the $\tilde{\tau}$ mass: Cross-section

- Poorly known SUSY background is most important contribution to uncertainty.
- Select region where it is as low as possible.

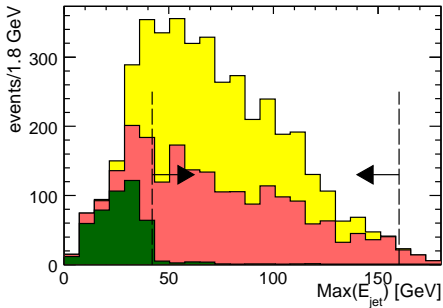
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RDR , SB2009 and $\tilde{\tau}$:s

Main items for physics

- Half RF power:
 - The free parameter is N_{bunch} . Fringe benefit: Allows for smaller damping rings
 - To keep L : decrease beam-size.
 - But: . \rightarrow **increases** δ_{BS}
 - Doubled luminosity/BX \rightarrow doubled probability for a $\gamma\gamma$ event *in the same BX*.
- Undulator move :
 - Higher energy-spread at 500 GeV.
 - Lower positron polarisation at 500 GeV.
 - Also: Lower lumi below 250 GeV, not relevant here.

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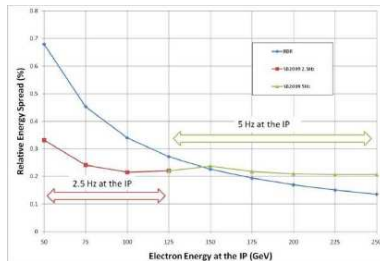
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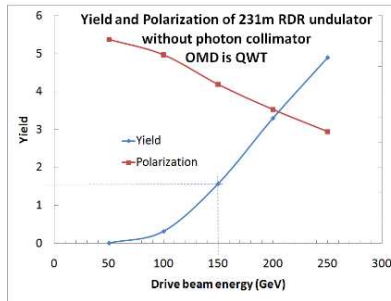
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Specifically:

- Twice as much beam-strahlung:
 - more overlaid tracks (real or fake)
 - Twice as much energy in BeamCal
- Total luminosity unchanged RDR→SB2009 w TF, but reduced by %25 for SB2009 w/o TF.
- $P(e^+)$ goes from 33 % to 22 %.
- Incoming energy-spread grows from 0.16 to 0.21 %.
- Luminosity within 1 % of nominal reduced from 0.83 to 0.72.

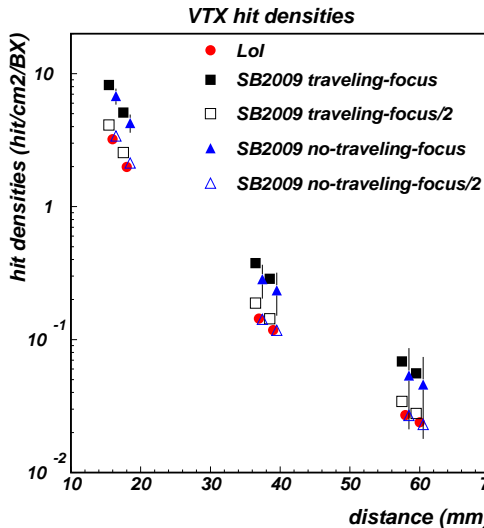
RDR , SB2009 and $\tilde{\tau}$:s

Potential effects on the $\tilde{\tau}$ -channels:

- Total **luminosity decrease** for SB2009 w/o TF.
- Decrease of $P(e^+)$: **More background, less-signal** for $\tilde{\tau}_1$.
- Incoming energy-spread grows: **end-point blurred**.
- Luminosity within 1 % of nominal reduced: **lower signal**.
- Twice as much beam-strahlung:
 - more overlaid tracks (real or fake): **Destroys τ topology**.
 - Twice as much energy in BeamCal: **More $\gamma\gamma$** .
- Higher probability for a $\gamma\gamma$ event *in the same BX* as the physics event (this effect has not yet been studied).

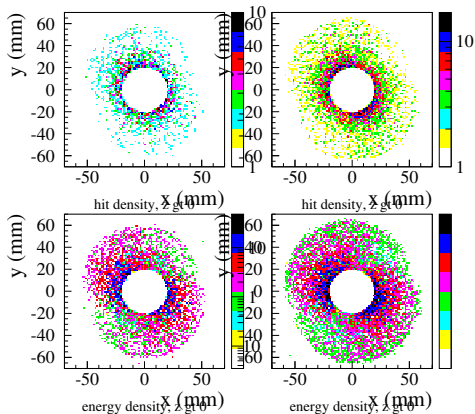
Beam-strahlung: Hits in Vertex detector

- Full simulation (Mokka), with crossing-angle and anti-DID field.
- No reconstruction yet, just count hits.
- The ILD VTX integrates of a certain time-window \rightarrow Many BX:es overlaid.



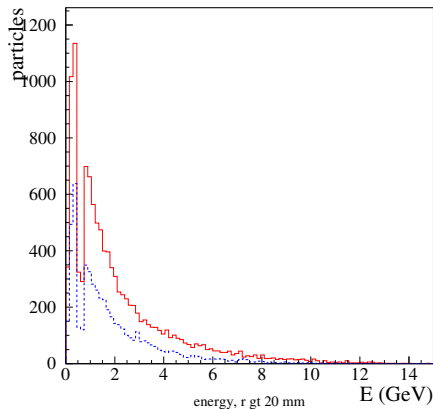
Beam-strahlung: BeamCal

- Only GP, but with crossing-angle and anti-DID.
- Both hit-densities (top) and energy-density (bottom) matters.
- The issue: can one still see a ≈ 250 GeV electron from a $\gamma\gamma$ process over the pairs-background?



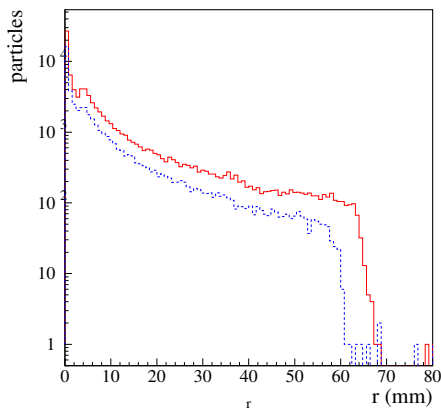
Beam-strahlung: BeamCal

- Distribution of particle energy for $r > 20$ mm.
- Total energy in BeamCal per BX: 24 TeV for SB2009TF, 10 TeV for RDR nom.
- Number of particles per BX: 11500 for SB2009TF, 5400 for RDR nom.
- Energy density vs Radius. SB2009TF has about twice at any given radius, and extends 5 mm further.
- All the relevant numbers double



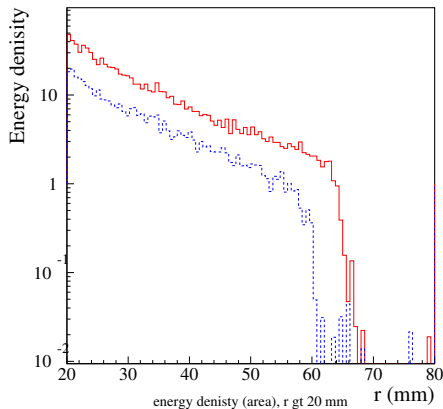
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Beam-background

- Generate 1000 bunch-crossings with **GuineaPig**.
- Reconstruct these with full ILD reconstruction.
- Add **simulated and reconstructed beam-background only events** on beam-background free, fully simulated and reconstructed physics events → **under-estimate pattern rec. problems.**

RDR, SB2009 and $\tilde{\tau}$:s

RDR \rightarrow SB2009 procedure

- **BeamCal:** From our studies: $SB2009(TF) \approx SB2009(noTF) \approx 2 \times$ RDR. \rightarrow Multiply BeamCal Energy-density map(RDR) by 2. Use same function $p([E_e atx, y], [pairsenergydensityatx, y])$ as the probability to detect an electron of energy E entering the BeamCal at (x,y) would be seen.
- **Tracking** Fully simulated and reconstructed BX:es available both for RDR and SB2009 (no TF). Use method outlined above. NB: optimistic when applied to SB2009 with TF !
- **Beam-spectrum** Lumi distributions from GP (A. Hartin, T Barklow) for RDR and SB2009 and $E_{beam1,2}$ used to calculate even-by-event weights, to modify the existing fully simulated sample to an RDR one.
- **Polarisation:** Straight-forward relative weighting of generated samples with $P=(-1,1)$ and $P=(1,-1)$.

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RDR, SB2009 and $\tilde{\tau}$'s: Signal and background

Events after cuts, end-point analysis

case	$\tilde{\tau}_1$			$\tilde{\tau}_2$		
	SM	SUSY	signal	SM	SUSY	signal
RDR	317	998	10466	1518	241	1983
SB09(TF)	814	956	8410	1346	223	1555
SB09(nTF)	611	717	6308	1009	167	1166

Events after cuts, cross-section analysis

case	$\tilde{\tau}_1$			$\tilde{\tau}_2$		
	SM	SUSY	signal	SM	SUSY	signal
RDR	17.6	47.7	2377	1362	33.7	1775
SB09(TF)	17.6	45.7	1784	1194	32.4	1366
SB09(nTF)	13.2	34.3	1337	895	24.3	1025

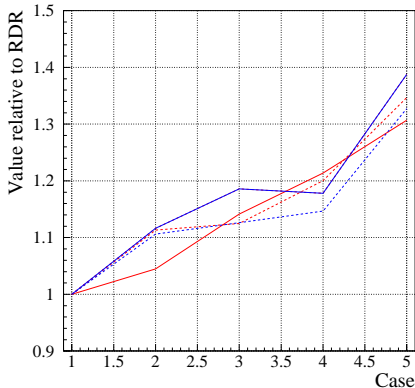
RDR, SB2009 and $\tilde{\tau}$'s: Effect on end-results

Errors on end-point (GeV)

case	#	$\tilde{\tau}_1$	$\tilde{\tau}_2$
RDR	1	0.129	1.83
+SB bck	2	0.144	2.02
+SB ppol	3	0.153	2.06
+SB spect	4	0.152	2.10
+SB noTF	5	0.179	2.42

Errors on cross-section (%)

case	#	$\tilde{\tau}_1$	$\tilde{\tau}_2$
RDR	1	2.90	4.24
+SB bck	2	3.03	4.72
+SB ppol	3	3.31	4.77
+SB spect	4	3.52	5.09
+SB noTF	5	3.79	5.71



Red: cross-section, Blue: end-point,
Solid : $\tilde{\tau}_1$, Dashed: $\tilde{\tau}_2$.

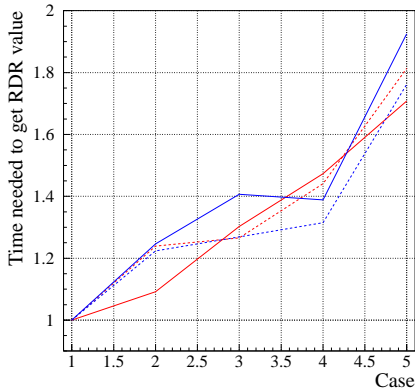
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Conclusions

- The effect of the transition RDR \rightarrow SB2009 of the $\tilde{\tau}$ channels in SPS1a' was studied.
 - Less favourable beam spectrum and positron polarisation treated by re-weighting the existing samples with RDR parameters.
 - Increased pairs-background in BeamCal treated by scaling up the RDR energy densities.
 - New GP-generated pairs were fully simulated and reconstructed, and over-layed on the physics events (background and signal).
- 15-20 % degradation both on end-point and cross-section determination, both for $\tilde{\tau}_1$ and $\tilde{\tau}_2$. Increases to 20-30 % if TF scheme would turn out not to be feasible.
- Corresponds to increasing the in running time by 40 % (80 % for noTF) to achieve the same results.
- Half of degradation from the modifications of the positron source: Wider incoming beam-spectrum and lower positron polarisation.