

# Correlation studies for likelihood variables

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# Introduction

- Correlation factor:

- Defined as:

$$\rho_{x,y} = \frac{\langle (x - \bar{x}) \times (y - \bar{y}) \rangle}{\sqrt{\langle (x - \bar{x})^2 \rangle \times \langle (y - \bar{y})^2 \rangle}} = \frac{\mathbf{COV}_{x,y}}{\sigma_x \times \sigma_y}$$

- Measures the degree of correlation:

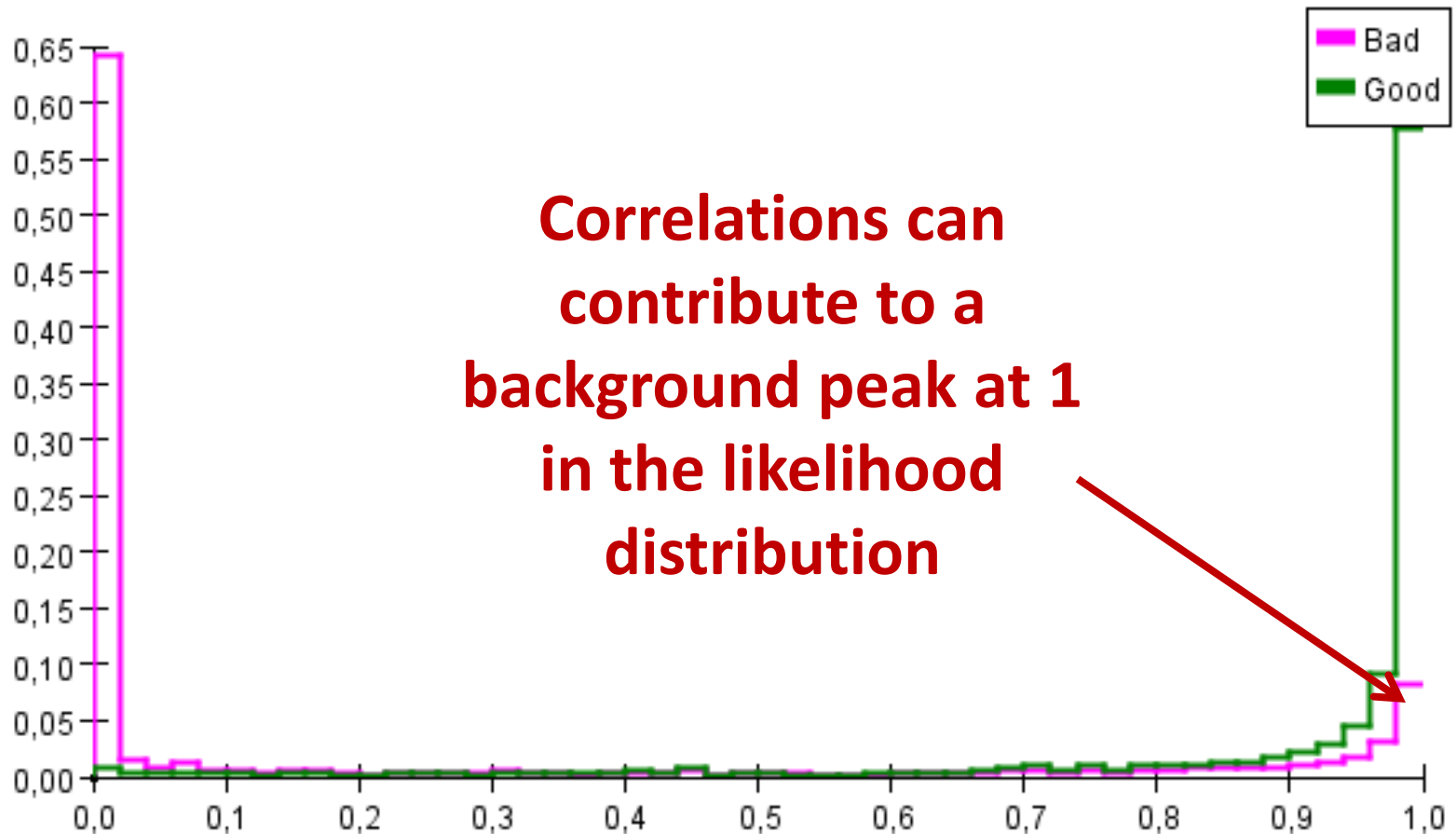
$$-1 \leq \rho_{x,y} \leq 1$$

- Likelihood function assumes independent variables:

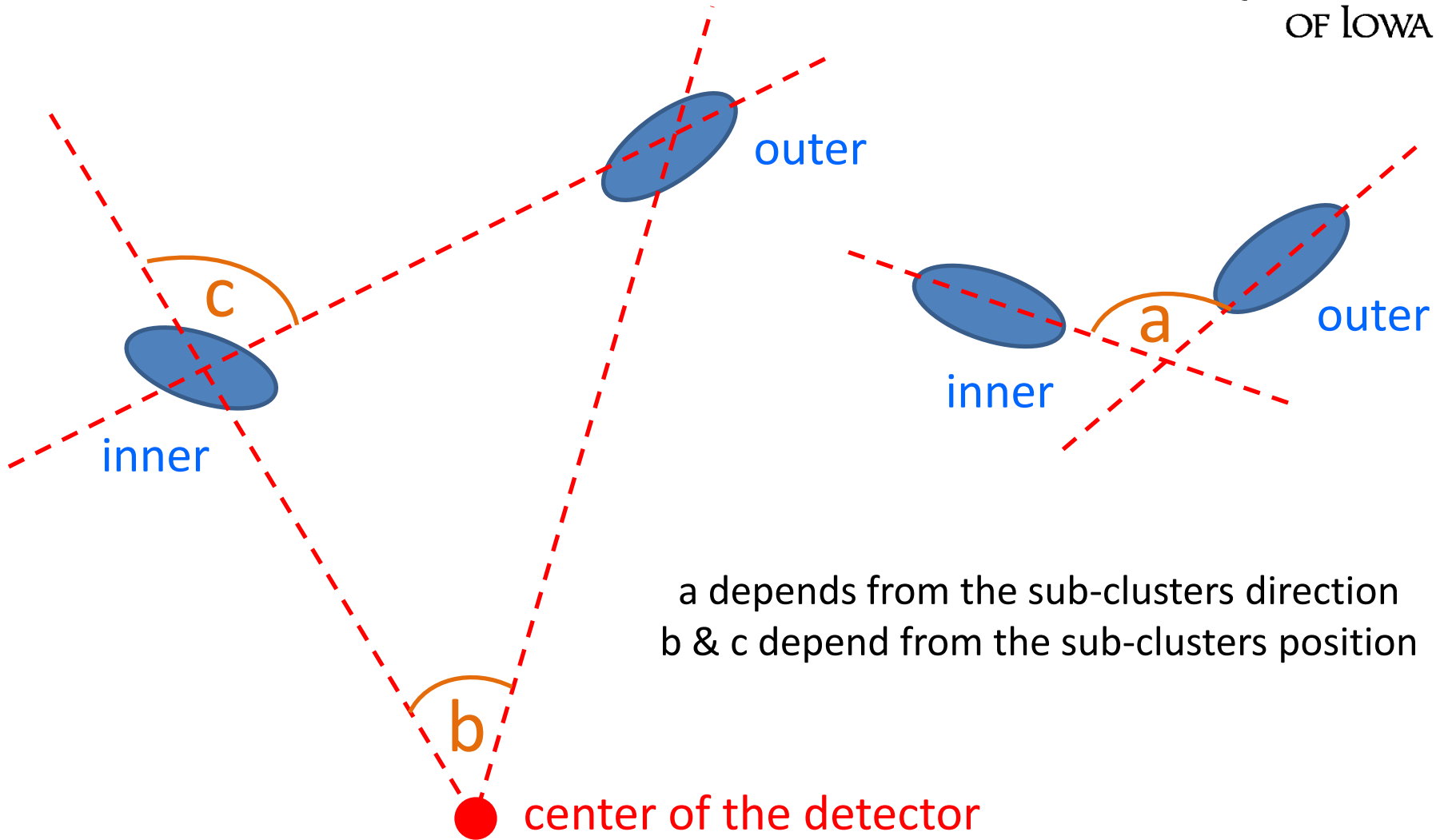
- Correlations between variables may cause peaks in the likelihood distribution for background in the signal region and vice versa.

# Introduction

Likelihood - AnyCluster AnyCluster

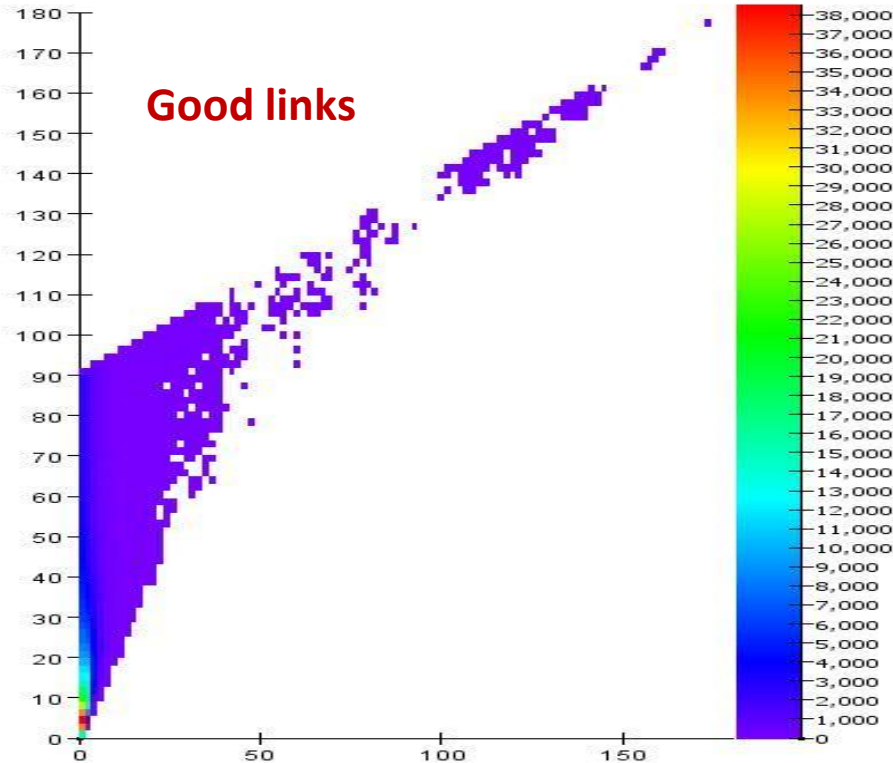


# Introduction

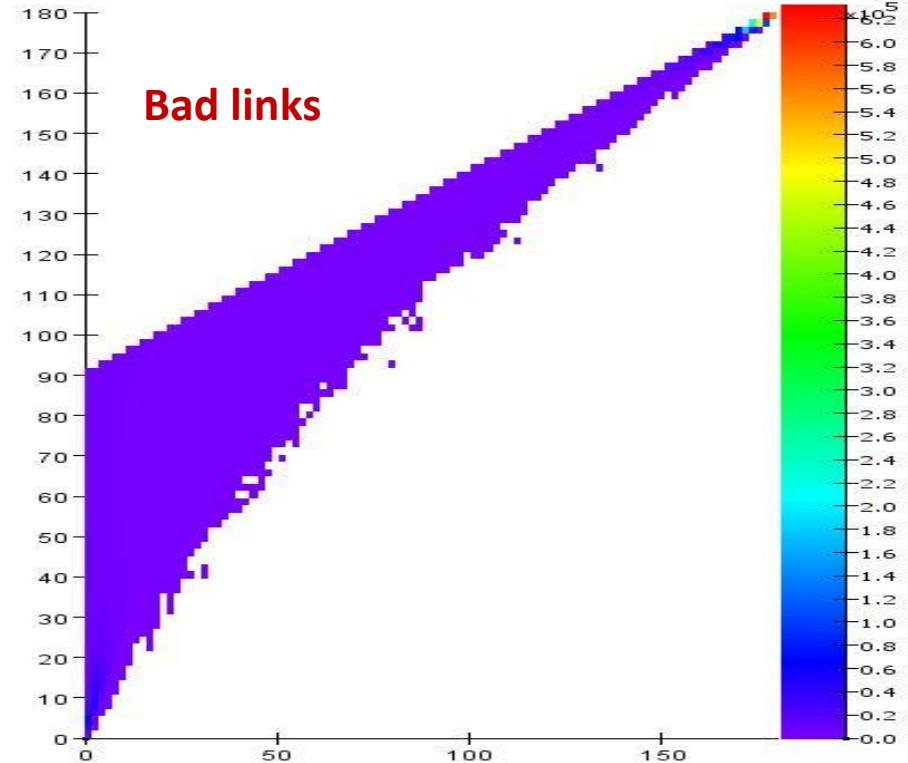


# Any Cluster to Any Cluster: angle 'c' vs angle 'b'

ClusterAngleFromCenter\_vs\_ClusterAngleWithCenter

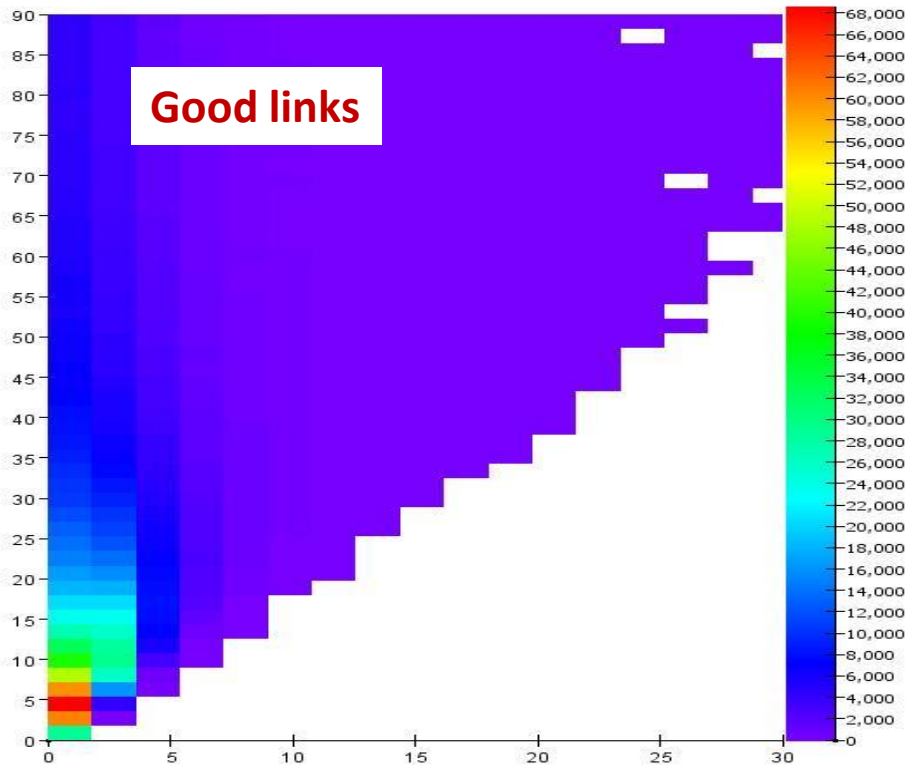


ClusterAngleFromCenter\_vs\_ClusterAngleWithCenter

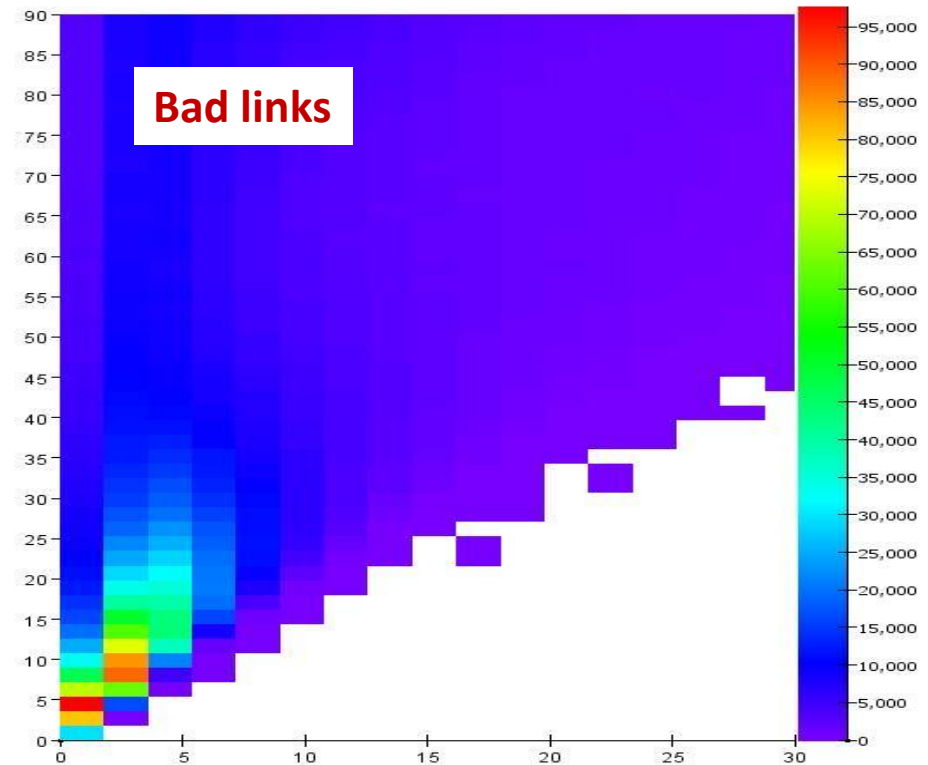


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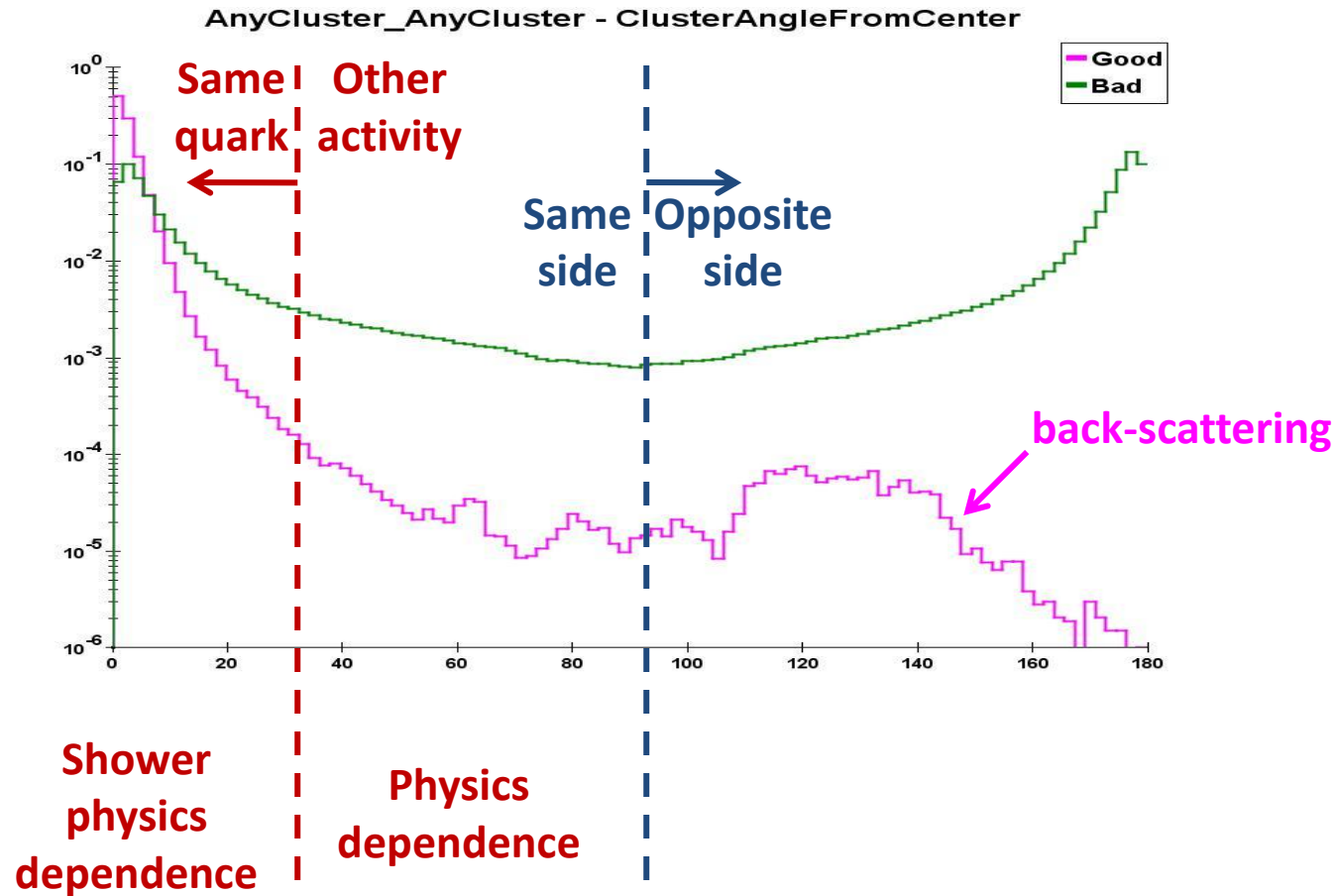


ClusterAngleFromCenter\_vs\_ClusterAngleWithCenter

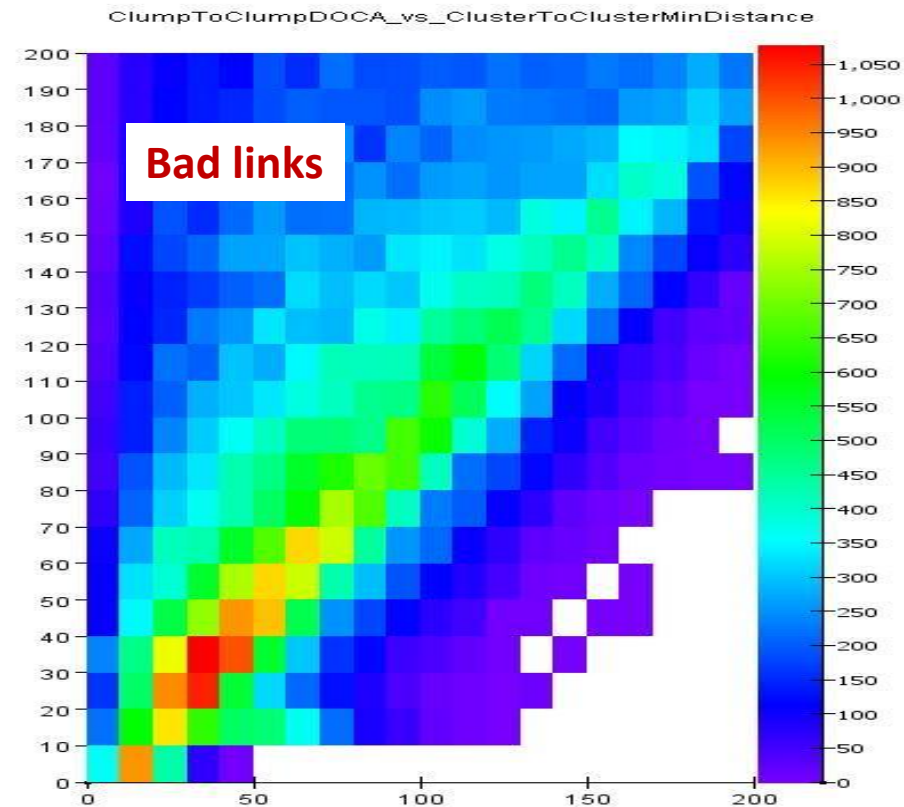
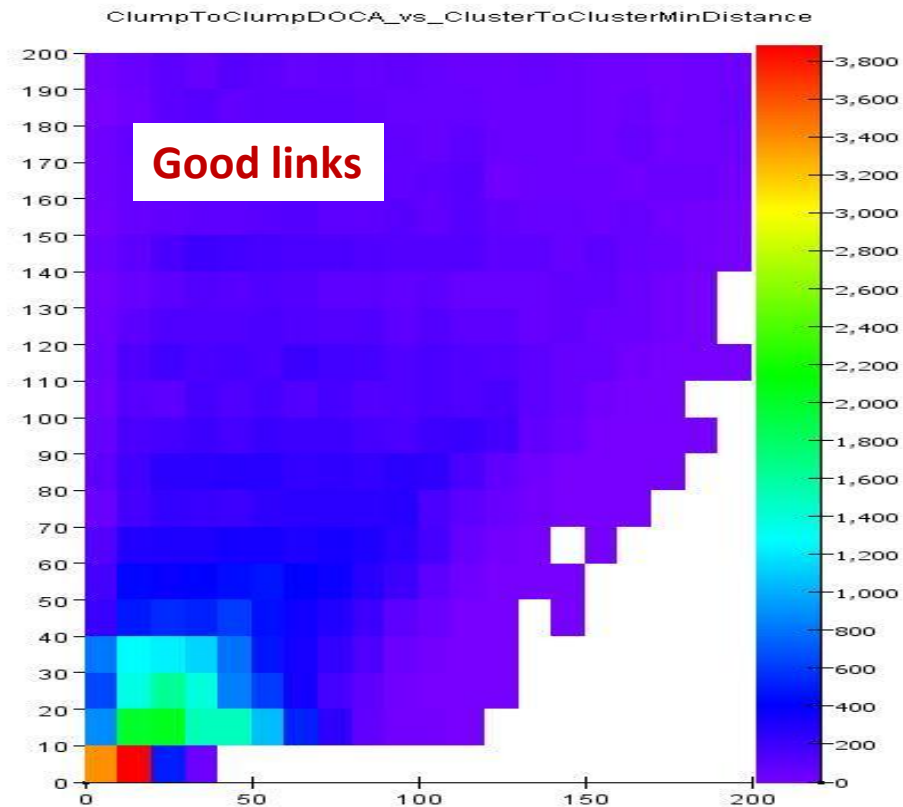


# We should cut on angle 'b'.

to reduce  
combinatorics  
but also to  
eliminate  
physics  
dependence.



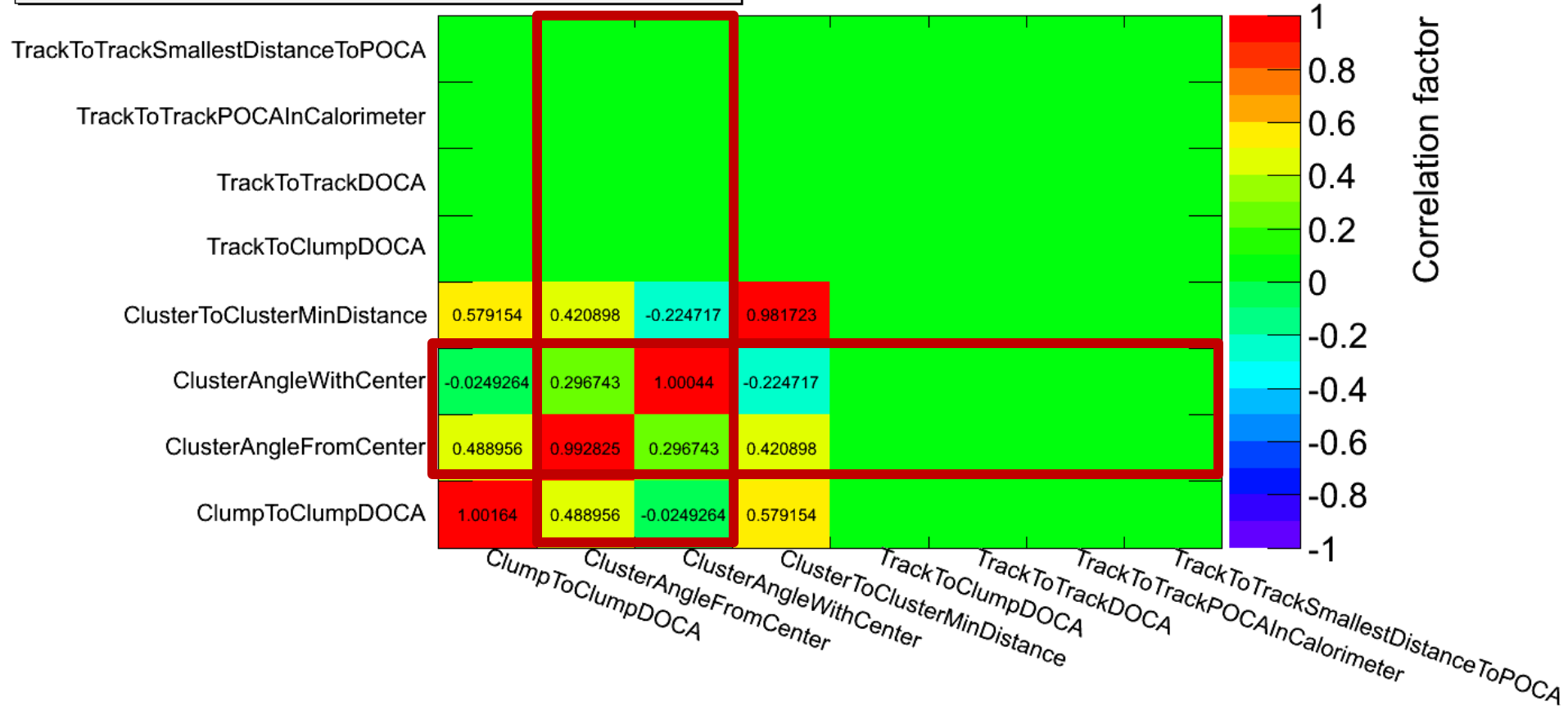
# Clump to Clump: DOCA vs. MinDistance





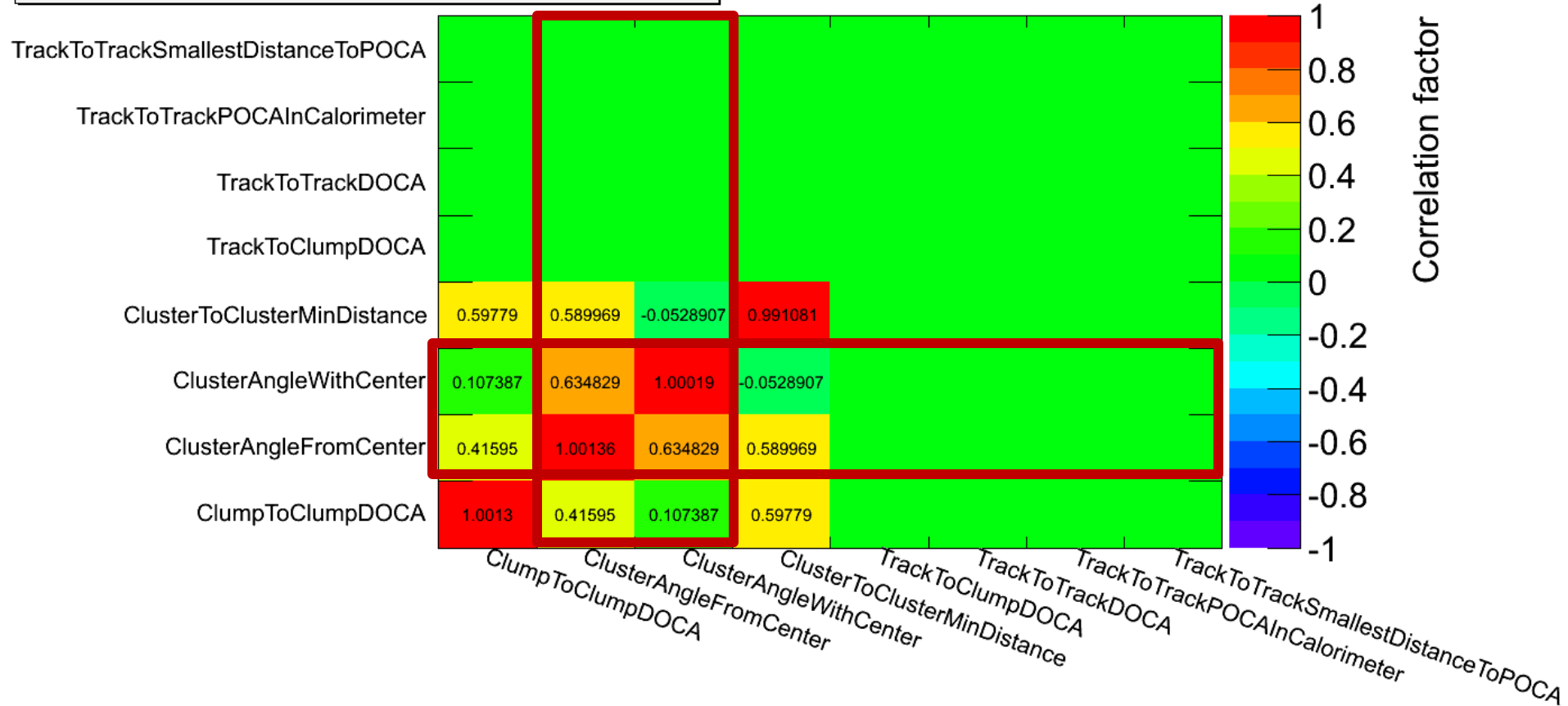
# Clump to Clump: good links

H\_\_BeforeFirstCone\_Good\_Clumps\_Clumps



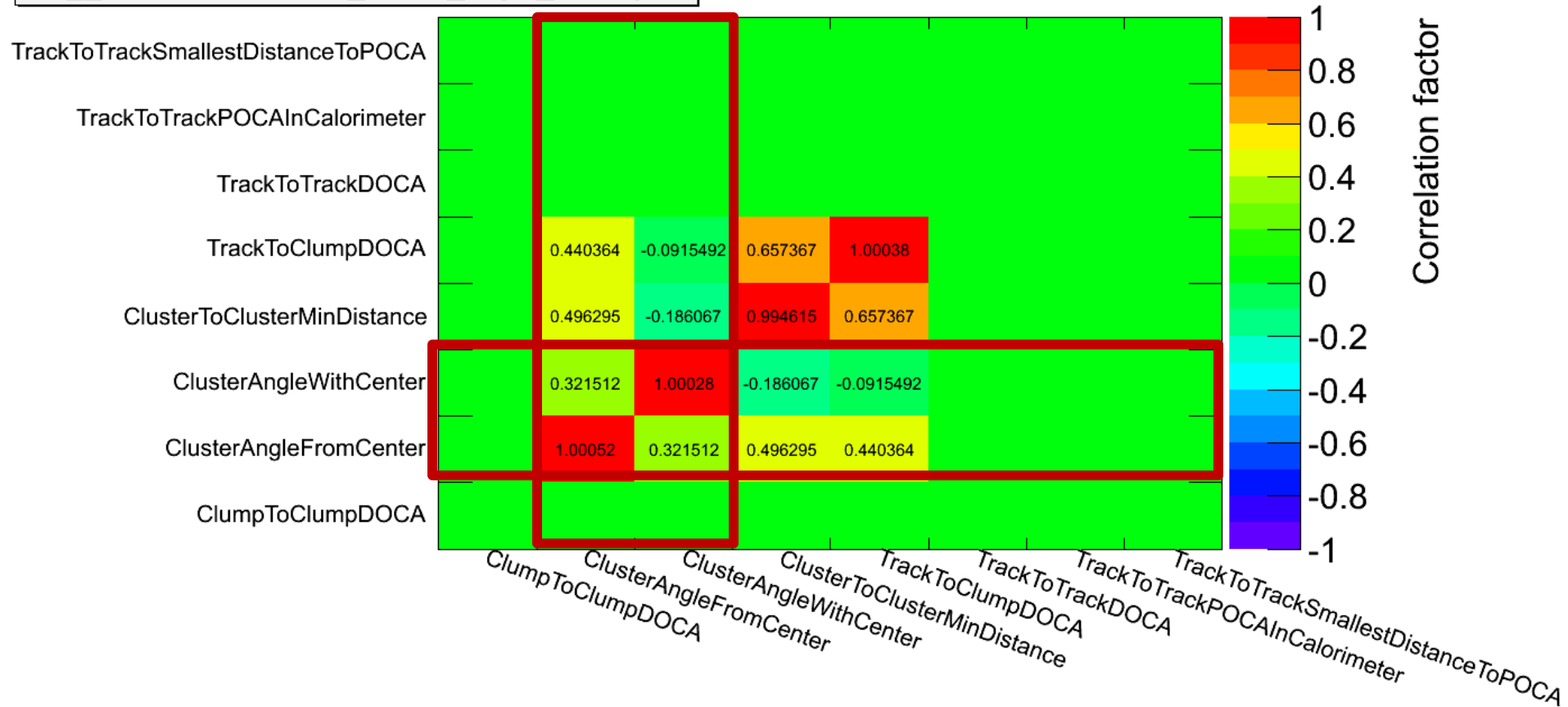
# Clump to Clump: bad links

H\_\_BeforeFirstCone\_Bad\_Clumps\_Clumps



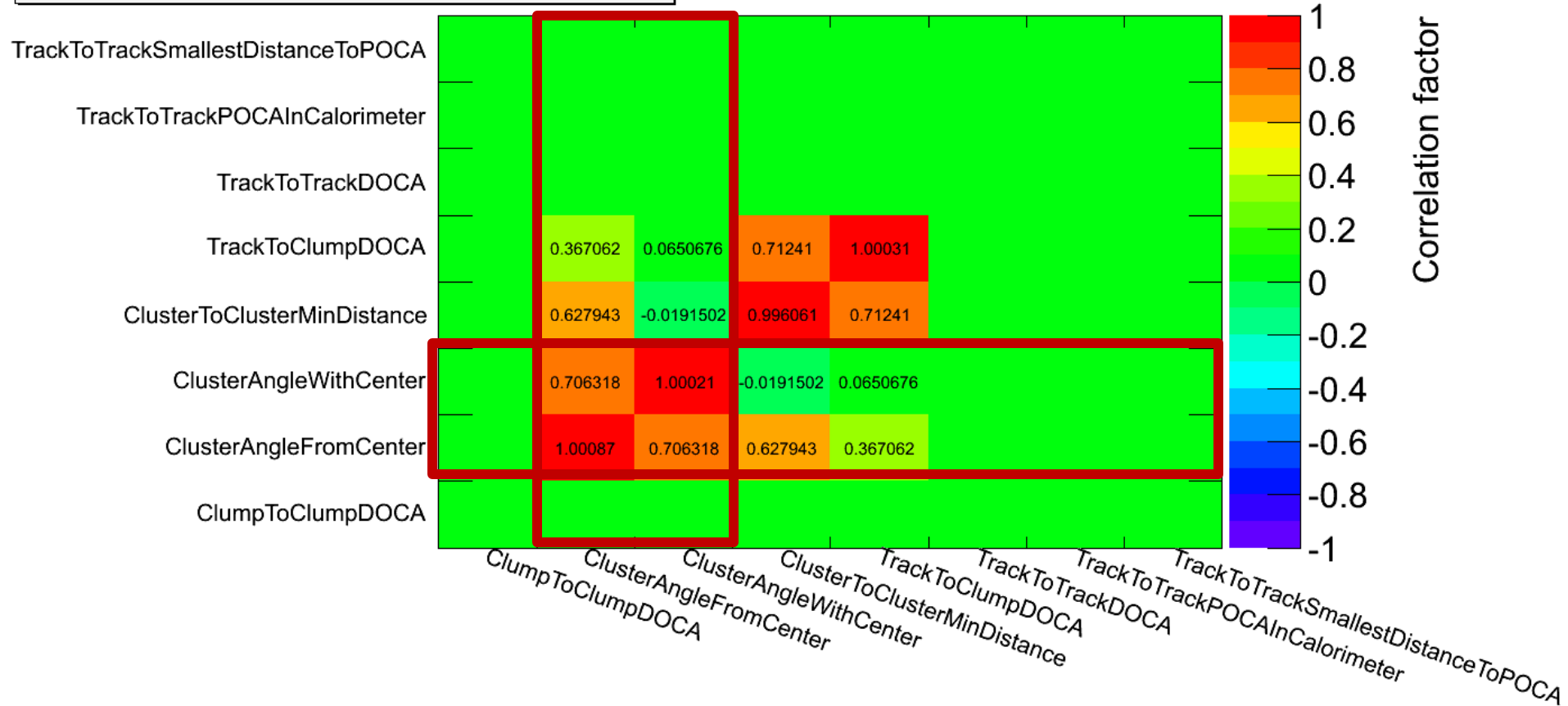
# MIP to Clump: good links

H\_\_BeforeFirstCone\_Good\_Mips\_Clumps



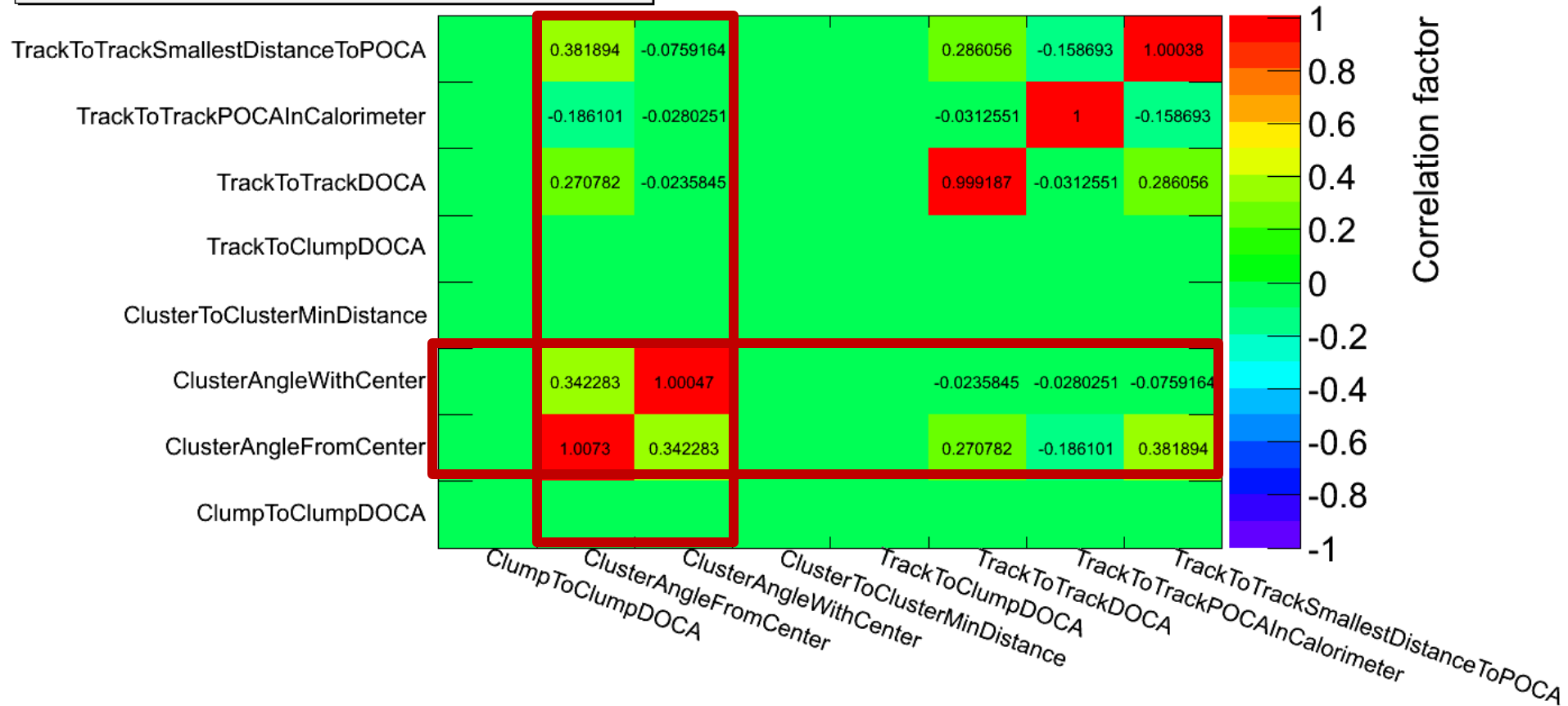
# MIP to Clump: bad links

H\_\_BeforeFirstCone\_Bad\_Mips\_Clumps



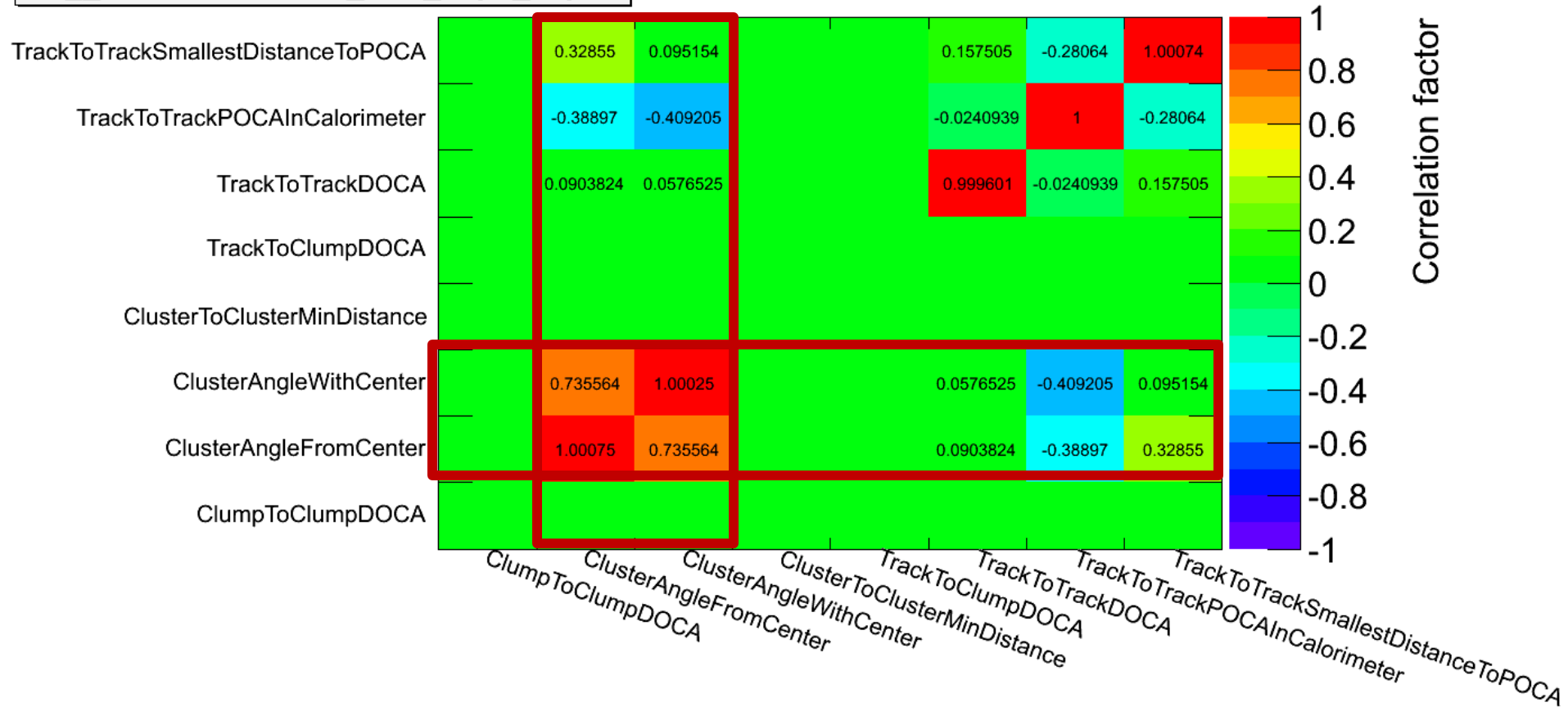
# MIP to MIP: good links

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# MIP to MIP: bad links

H\_\_BeforeFirstCone\_Bad\_Mips\_Mips



# Conclusion

- Should use multi-dimensional PDFs in some cases:
  - This would take correlations into account in the likelihood definition.
  - Code is ready for this.
- Should not be dependent on what happens outside the jet region:
  - Impose a cut on angular separation.