

Little Higgs with T-parity model at 1TeV using quick simulator

**ILD workshop,LAL
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Little Hierarchy problem

There are 2 predictions on where the energy scale of new physics should emerge.

1. Fine tuning of Higgs mass


$$\underline{m_{Higgs}^2} = \underline{m_0^2} + \underline{\delta m^2}$$

Measured Higgs mass Bare mass Correction term

$$\Lambda : \text{Energy scale} \quad \delta m^2 \approx (0.27\Lambda)^2$$

$\Lambda < 1 \text{ TeV}$

2. Electroweak precision measurement

$\Lambda > 10 \text{ TeV}$

→ Conflict between the 2 energy scales.

→ Little Higgs model was proposed!

Little Higgs model

<Little Higgs mechanism>

Global Symmetry : $SU(5)$ $f \sim 1 \text{ TeV}$ $SO(5)$ $v \sim \langle h \rangle$
subgroup : $[SU(2)_L \times U(1)_Y]^2 \rightarrow SU(2)_L \times U(1)_Y \rightarrow U(1)_Y$

<Higgs mass contribution>

$$\begin{aligned} -\bar{H} \text{---} \textcircled{t} \text{---} H + H \text{---} \textcircled{T_+} \text{---} H + -\bar{H} \text{---} \textcircled{t} \text{---} T = 0 \Lambda^2 \\ H \text{---} \textcircled{w,z} \text{---} H + H \text{---} \textcircled{w_H,z_H} \text{---} H = 0 \Lambda^2 \end{aligned}$$

Quadratic divergent terms cancel at 1-loop order

Solves Little hierarchy problem

Littlest Higgs with T-Parity model

Standard model

Quarks	u up	c charm	t top	γ photon
	d down	s strange	b bottom	Z Z boson
Leptons	V_e electron neutrino	V_μ muon neutrino	V_τ tau neutrino	W W boson
	e electron	μ muon	τ tau	g gluon

Higgs* boson

T₊

T-parity

Little Higgs partner

Quarks	u₋ up	c₋ charm	t₋ top	γ_H photon
	d₋ down	s₋ strange	b₋ bottom	Z_H Z boson
Leptons	V_{e-} electron neutrino	$V_{\mu-}$ muon neutrino	$V_{\tau-}$ tau neutrino	W_H W boson

Triplet* Higgs boson

T₋

A_H :DM candidate

$$m_{W_H} \sim m_{Z_H} \sim g f$$

$$m_{A_H} \sim g' f / \sqrt{5}$$

$$m_u^- \sim m_d^- \sim \sqrt{2k_q} f$$

$$m_{e^-} \sim m_{\nu^-} \sim \sqrt{2k_l} f$$

LHT masses in gauge & lepton sector can be described with 2 parameters

f(VEV): energy scale of global symmetry breaking

K : lepton Yukawa coupling

Important parameters which describe how LHT particles obtain masses & solve little hierarchy problem.

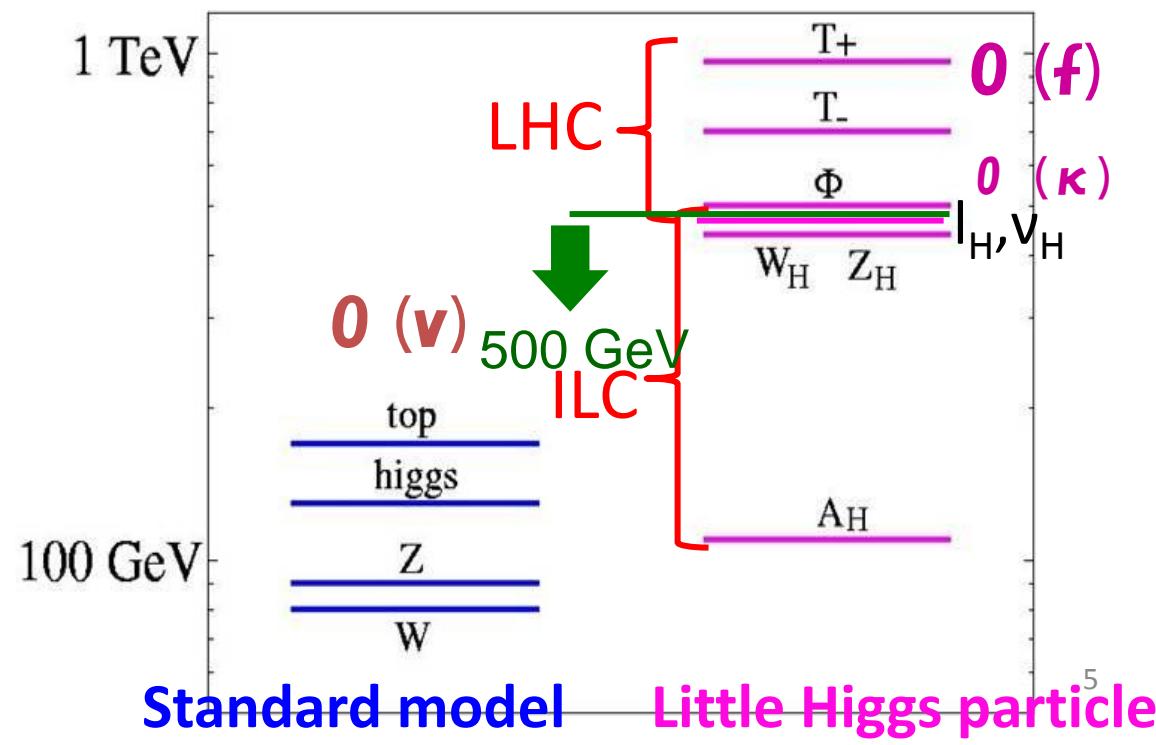
Aim of study

Evaluate ILC's sensitivity on ...

- 1st aim : extracting model parameters(f&kappa)
- 2nd aim: completing the mass spectrum and checking consistency with parameters

Strong proof that discovered particles are indeed LHT.

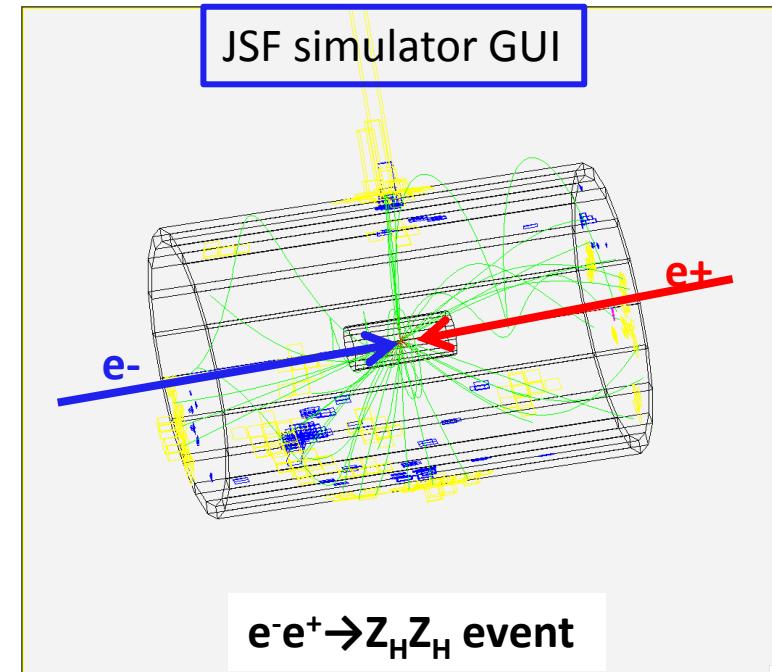
κ	f
0.5	580(GeV)



Simulation environment

■ Software for fast simulation

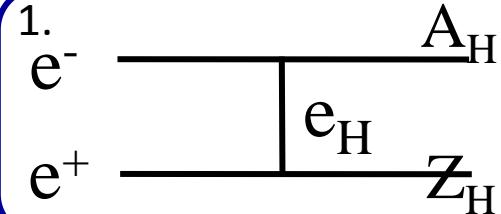
- Physsim(generate basic particles)
 - Helicity amplitude: HELAS
 - Numerical integration: BASES
 - Event generation: SPRING
- JSF hadronizer (time evolution)
 - Hadronization: Pythia
 - Tau decay : TAUOLA
- JSF Quick simulator(simulation)



■ Experiment environment

- CM energy: 1TeV
- luminosity : 500fb^{-1} (4 years)
- beam/bremstrahlung, beam energy spread are included.

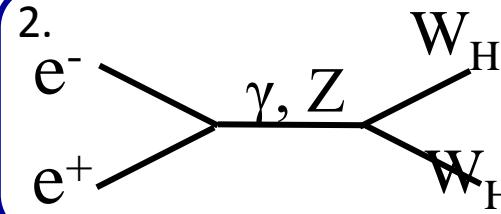
Analysis strategy



- $m_{AH} + m_{ZH} < 500 \text{ GeV}$
- producable @ 500 GeV
- **First signal of LHT!**

LOI

500 GeV

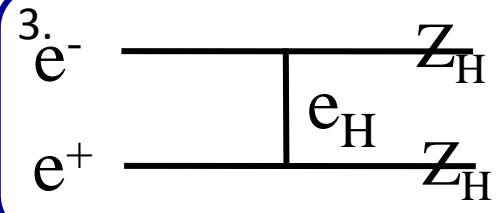


- Large cross section
- **Precision measurement on f.**

LOI

1 TeV

$$m_{WH} \sim m_{ZH} \sim g f$$



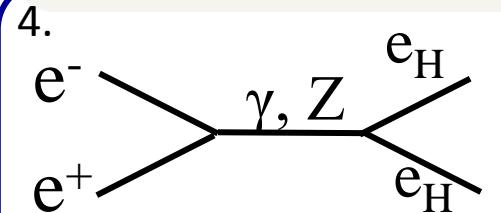
- Determine f.
- **complete mass spectrum in gauge sector**

New

1 TeV

$$m_{A_H} \sim g' f / \sqrt{5}$$

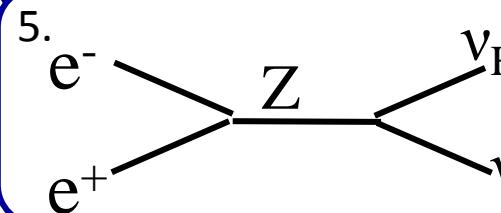
$$m_e \sim m_\nu \sim \sqrt{2} k_l f$$



- Determine I_H mass
- **Precision measurement on κ**

New

500 GeV



- **Complete mass spectrum in lepton sector**

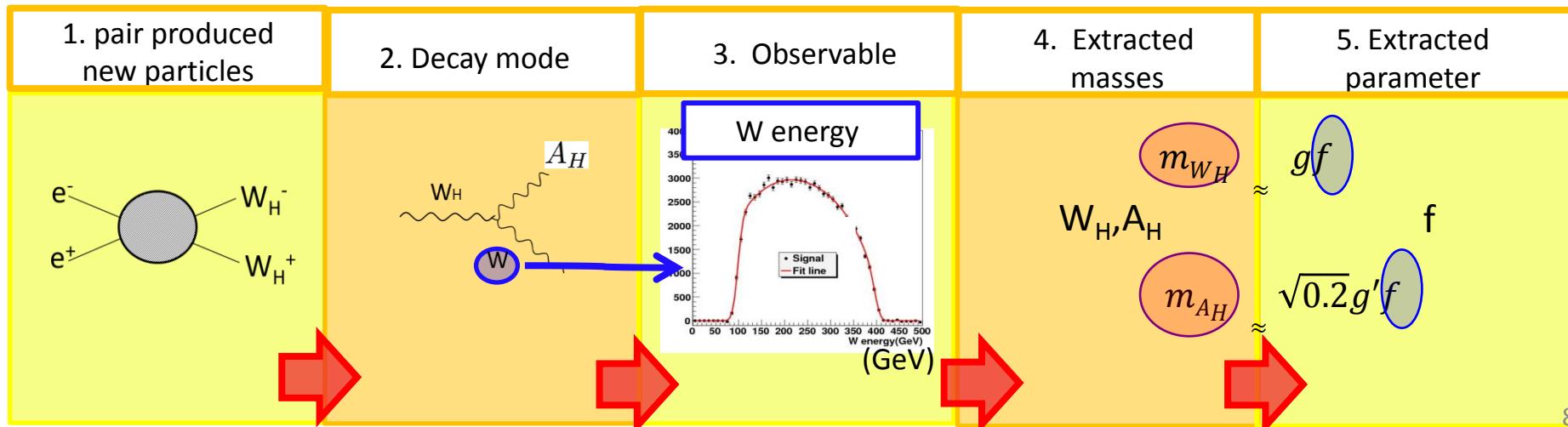
New

100 GeV

Dark Matter

Analysis procedure

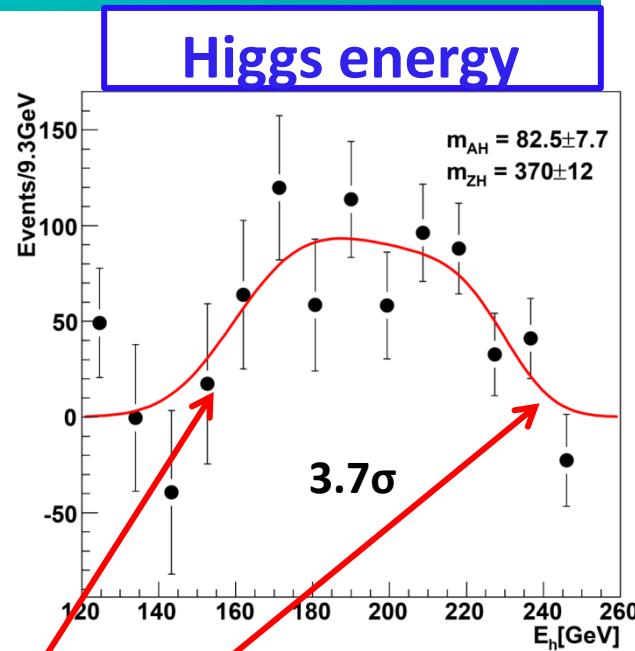
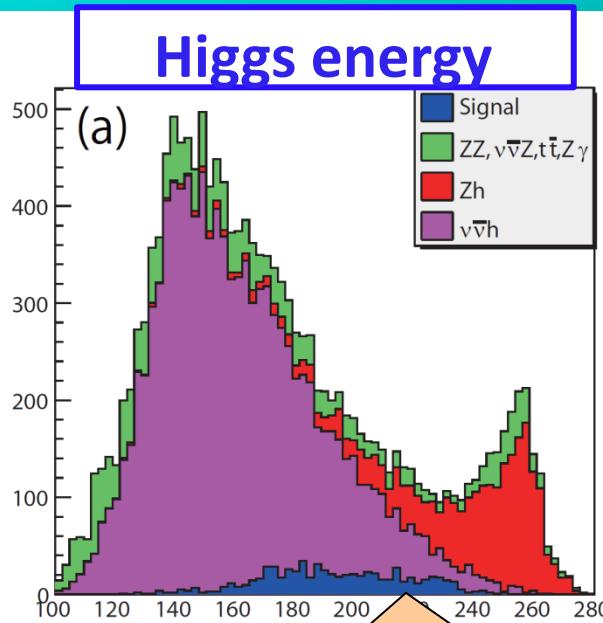
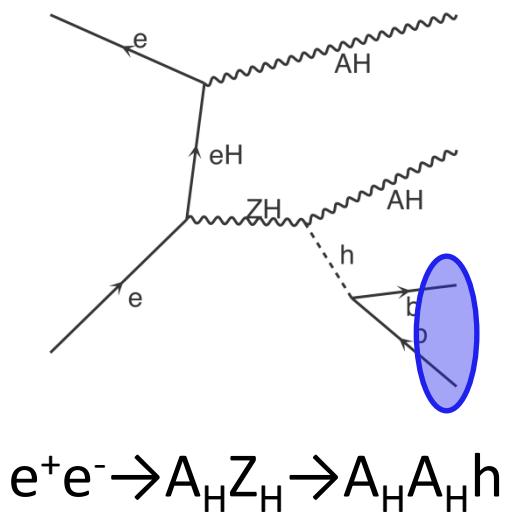
1. T-Parity  new particles are produced in pairs
2.  produced new particles decay into SM and LHT particles.
3. Extract LHT mass information by recognizing end point of SM energy.
4. LHT masses are expressed with model parameters.
5. Extract model parameters.



Heavy gauge boson sector
~mass & parameter f extraction ~

$Z_H A_H$ @500GeV

arXiv:0901.4873v1 [hep-ph]



Cross section small 1.05fb

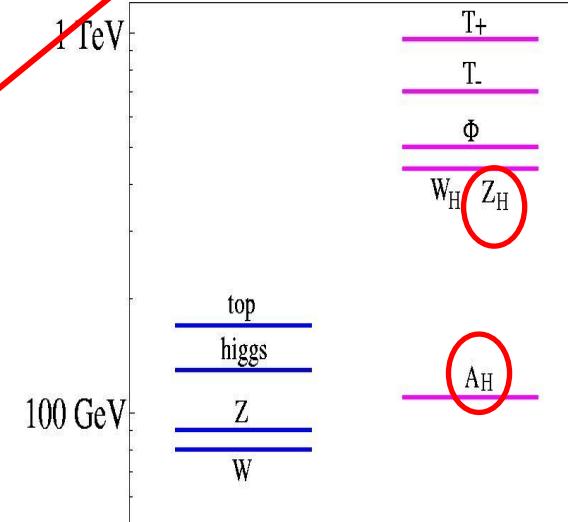
Signal: $A_H A_H bb$

- Mass determination
 - $m_{A_H} = 82.5 \pm 7.7$ GeV true(81.85)
 - $m_{Z_H} = 370. \pm 12.$ GeV true(368.2)
- f determination: $f = 581 \pm 17$ GeV true(580)

First signal of LHT

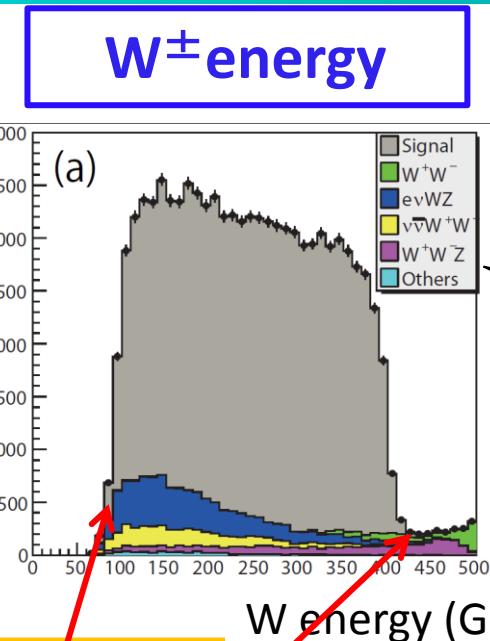
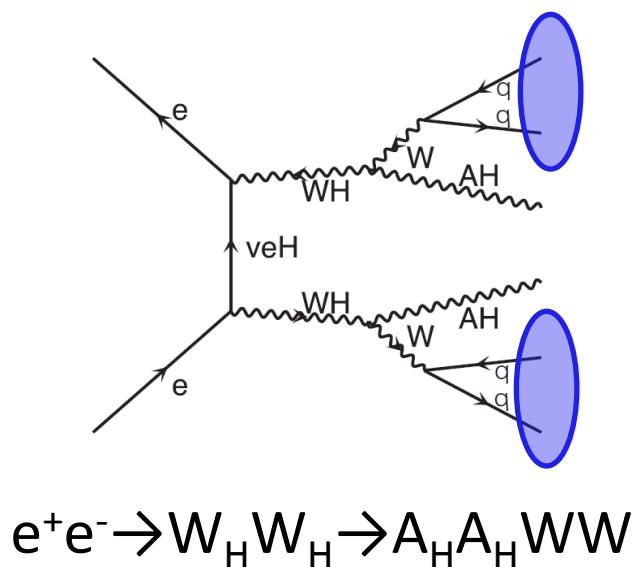
(event selection)

- Higgs mass
- miss Pt cut
- b-tagging



$W_H W_H @1\text{TeV}$

(phys. Rev D79.075013)



- (event selection)
- $W^\pm\text{energy}$
 - $W^\pm\text{mass}$
 - miss Pt

Large cross section : 120fb

Signal: $A_H A_H qqqq$

This analysis produces 2 mass solutions.

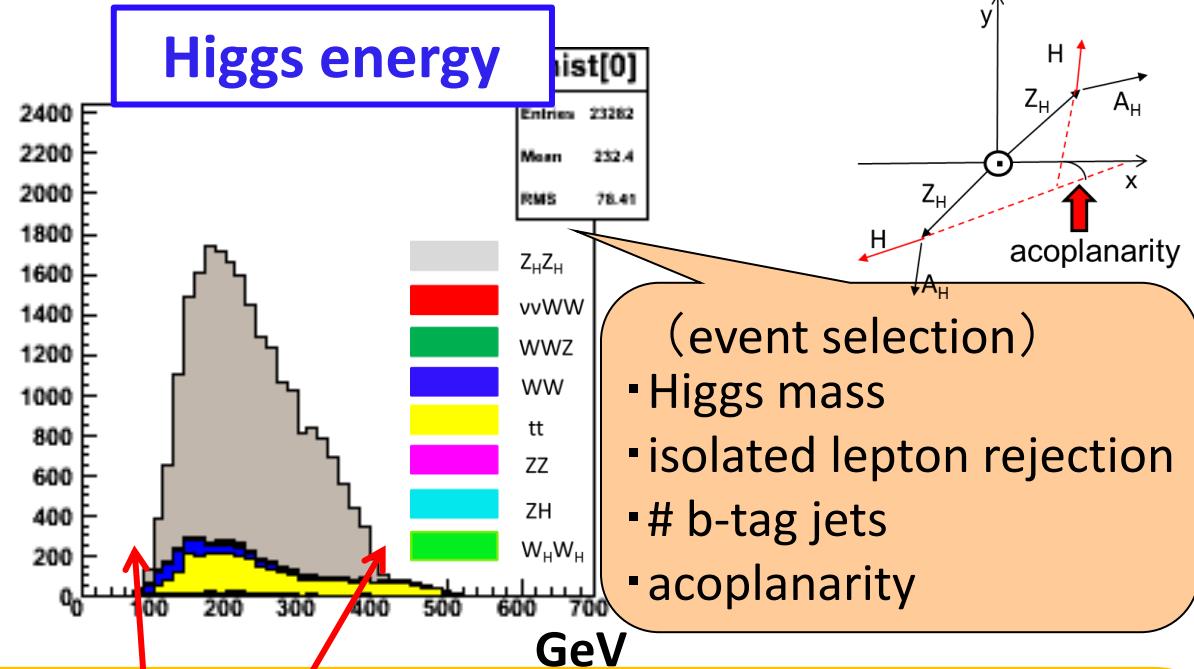
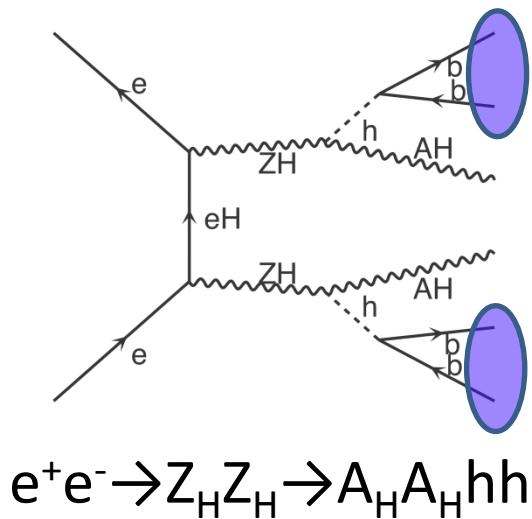
True solution

$$m_{AH} = 81.6 \text{ GeV}, \quad 81.0 \text{ GeV } 1.3\%$$

$$m_{WH} = 368.3 \text{ GeV}, \quad 218.0 \text{ GeV } 0.2\%$$

Highly accurate, however true solution needs to be selected

$Z_H Z_H @1\text{TeV}$



Large cross section : 99 fb

Signal: $A_H A_H qqqq$

This analysis also produces 2 mass solutions.

True solution

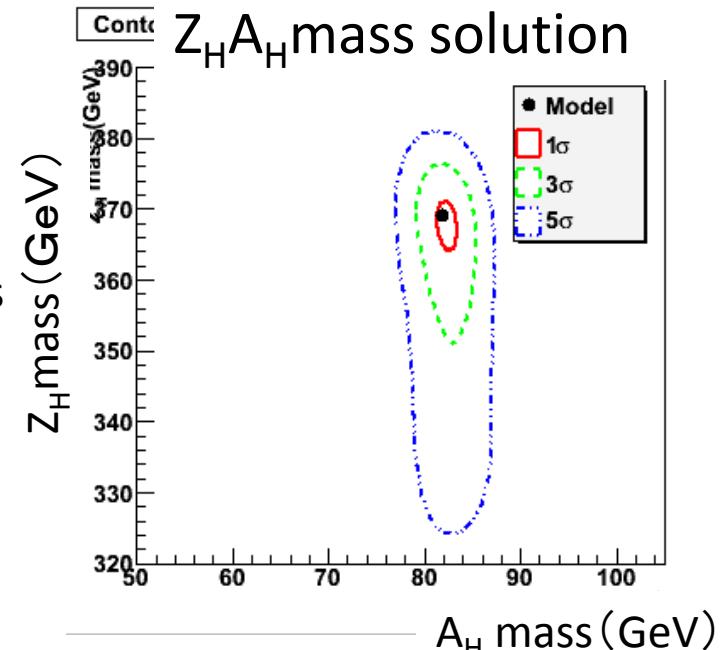
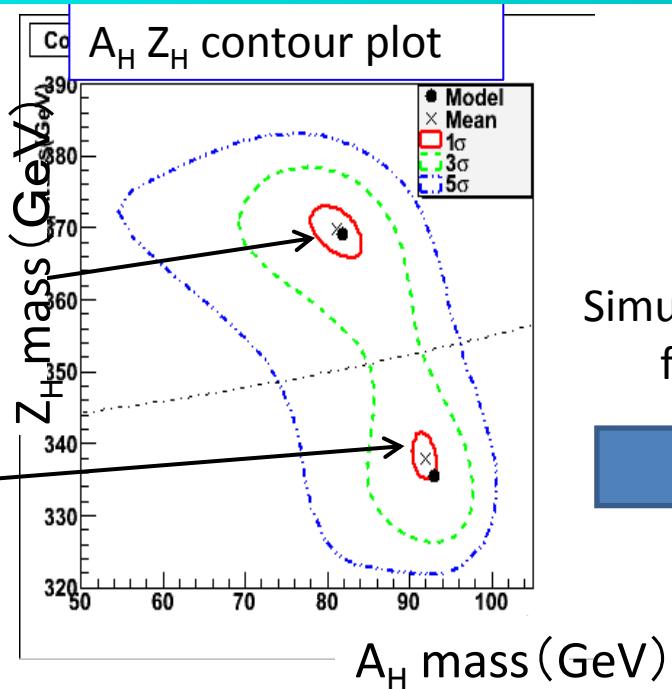
$$m_{A_H} = 82.7 \text{ GeV}, 93.1 \text{ GeV} \quad 4.2\%$$

$$m_{Z_H} = 366.1 \text{ GeV}, 335.4 \text{ GeV} \quad 1.3\%$$

Highly accurate, however true solution needs to be selected

Mass determination in gauge sector

True solution
False solution



Through simultaneous fitting W_HW_H&Z_HZ_H (both derive A_Hmass),we were able to derive a single mass solution.

- Mass measurement accuracy: A_H 1.3%, Z_H 1.1% W_H 0.20%
- parameter measurement accuracy: f 0.16%

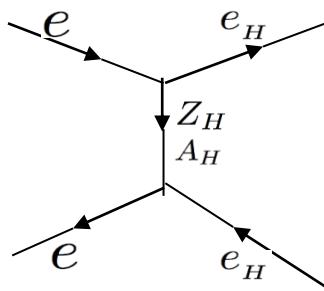
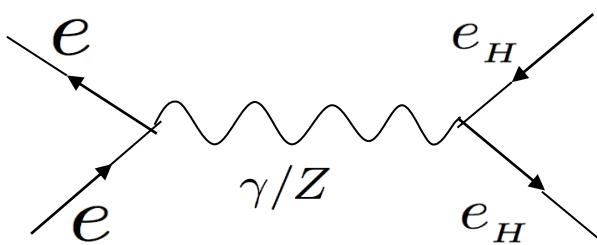
ILC is highly sensitive to f !

Heavy lepton sector
~mass¶meter κ extraction~

$e_H e_H @1\text{TeV}$

■ Aim: extract lepton Yukawa coupling κ by measuring e_H mass.

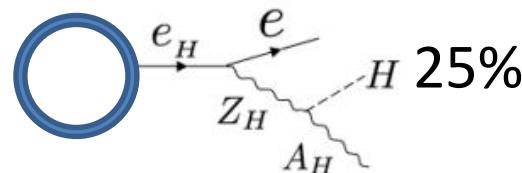
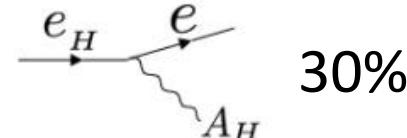
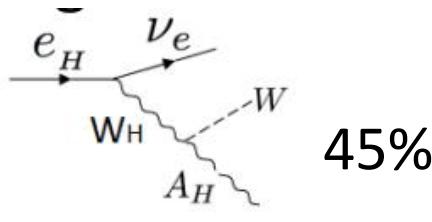
Extremely important in knowing lepton sector mass generation mechanism.



$$m_{eH} = \sqrt{2} \kappa f = 410 \text{ GeV}$$

Signal(4.56fb)

$e_H e_H \rightarrow e Z_H e Z_H \rightarrow ee qqqq$

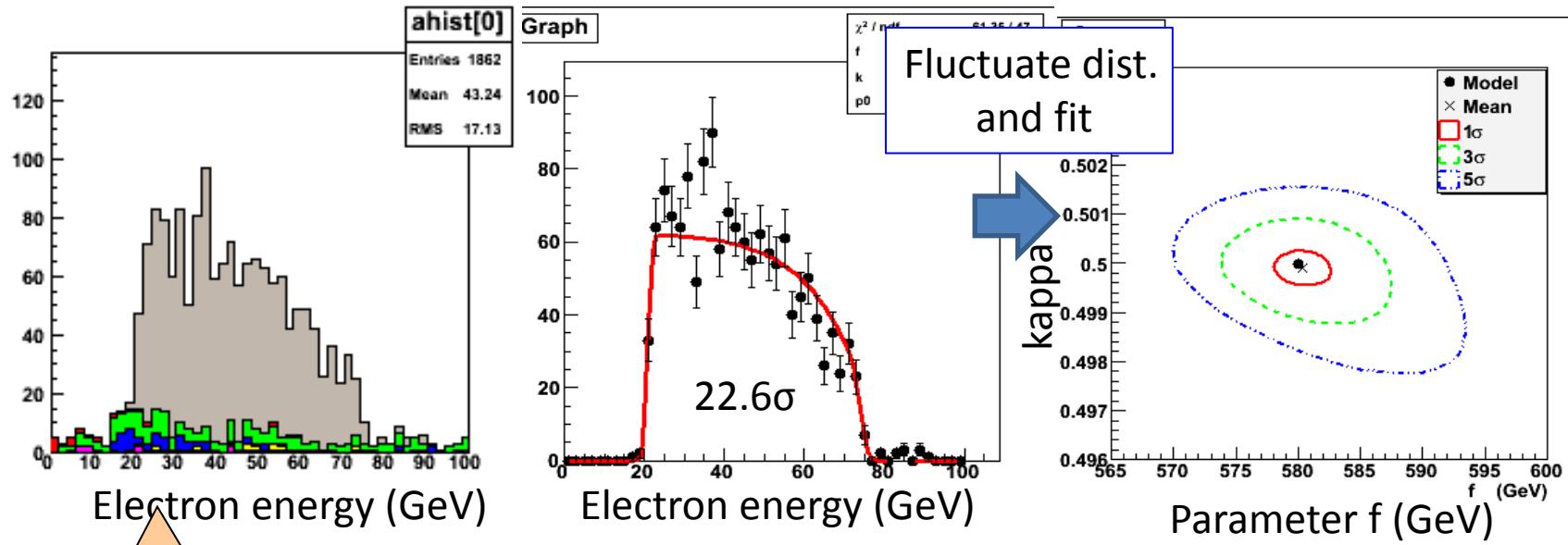


Same signal as $W_H W_H$.
 e_H access difficult

Charge suppressed.
Large SM & LHT background.

2 higgs characteristic final state
Small background.

e_H mass/parameter extraction



(event selection)

- #Isolated $e = 2$ with opp. charge
- h mass
- miss Pt

BG: $\tau_H\tau_H$,
 $t\bar{t}, t\bar{t}Z, t\bar{t}h$
 $e\nu WZ, eeWW, ZZZ$

■ No multiple solution.
 extracted value: $f=579.6 \pm 3.0(\text{GeV})$ $\kappa=0.5 \pm 4e-4$
 True value: $f=580(\text{GeV})$, $\kappa=0.5$
 mass accuracy: $e_H: 412.8 \pm 1.7(\text{GeV})$ $Z_H: 371.2 \pm 1.5(\text{GeV})$

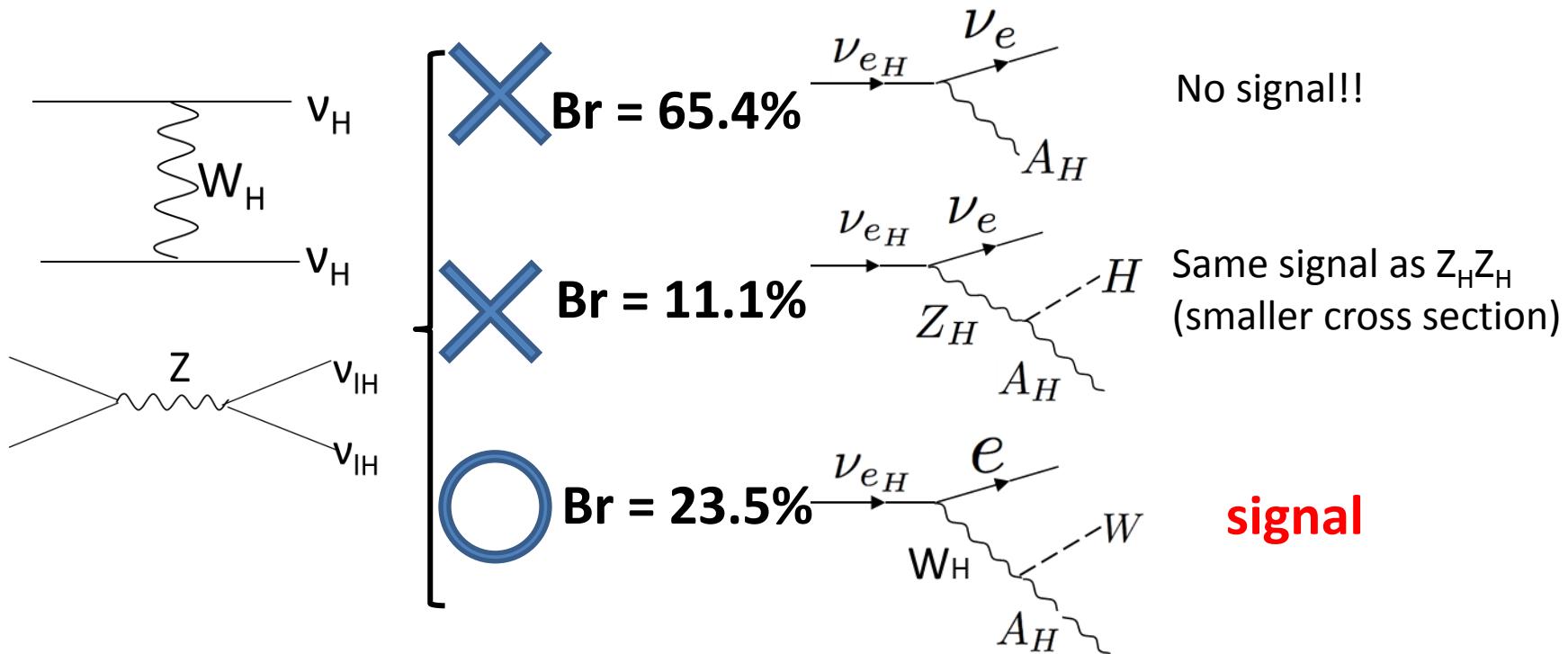
Successfully extract mass and parameters.

$\nu_H \nu_H @ 1\text{TeV}$

- AIM: extract ν_H mass and complete LHT mass spectrum
- $\nu_H \nu_H(eW_H eW_H)$ (tot xsec : 1036fb)

– Signal: eeqqqq(2W)A_HA_H (25.96fb)

$$M_{\nu_H} \doteq \sqrt{2\kappa f} = 400\text{GeV}$$



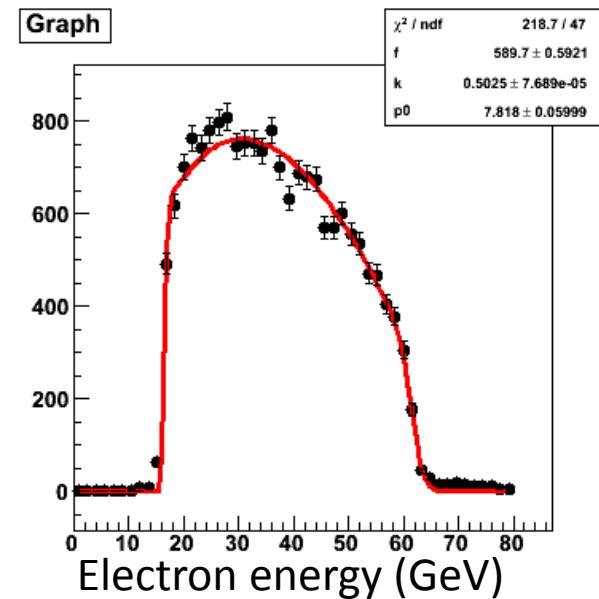
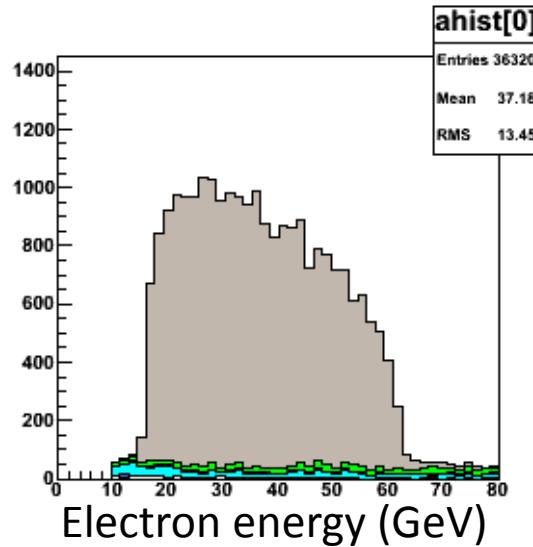
v_H mass/parameter extraction

SG: $eW_H eW_H (eeqqqq)$

BG: $v_{\tau H} v_{\tau H}, e_H e_H, \tau_H \tau_H,$
 $t\bar{t}, t\bar{t}Z, t\bar{t}h$
 $e\nu WZ, eeWW, ZZZ$

(event selection)

- #Isolated e = 2
- W mass



■ No multiple solution.

extracted value: $f=582.0 \pm 0.6(\text{GeV})$ $\kappa=0.5 \pm 1\text{e-}4$

True value: $f=580(\text{GeV})$, $\kappa=0.5$

mass accuracy: $v_H: 400.8 \pm 0.4(\text{GeV})$ $W_H: 369.6 \pm 0.4(\text{GeV})$

Successfully extract mass and parameters.

Summary

- Results show that ILC is capable of doing highly accurate precision measurements on LHT masses and parameters.
 - Parameter extraction is extremely important in studying LHT's mass generation mechanism.
 - Little Higgs model's characteristic mass spectrum (expressed with 2 parameters) can be confirmed by high precision mass measurement.

particle	mass	sensitivity
A _H	81.9(GeV)	1.3%
W _H	369(GeV)	0.20%
Z _H	368(GeV)	0.56%
e _H	410(GeV)	0.46%
v _H	400(GeV)	0.001%

parameter	True value	Measurement accuracy
f	580(GeV)	0.16%
K	0.5	0.0001%

plan

- Cross section can be measured when changing polarization.
- Coupling will be derived.

Cross section measurement		
Mode	σ @0%pol	σ meas. accuracy
$Z_H Z_H$	99fb	0.89%
$e_H e_H$	3.6fb	2.7%
$N_H N_H$	25fb	0.77%
$W_H W_H$	1 06fb	0.41%

backup

Selection of model parameters

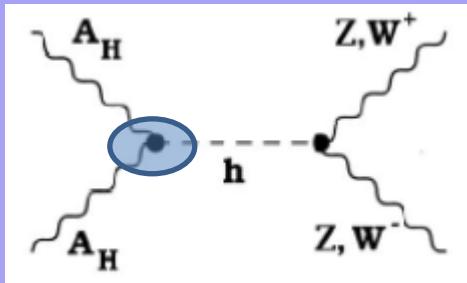
lepton and gauge sector are described with 2 model parameters

K	f	m_H
0.5	580(GeV)	134(GeV)

- * K small $\rightarrow l_H, v_H$ mass too small
- * K large \rightarrow 4 fermi interaction contribution increases and large discrepancy from SM.

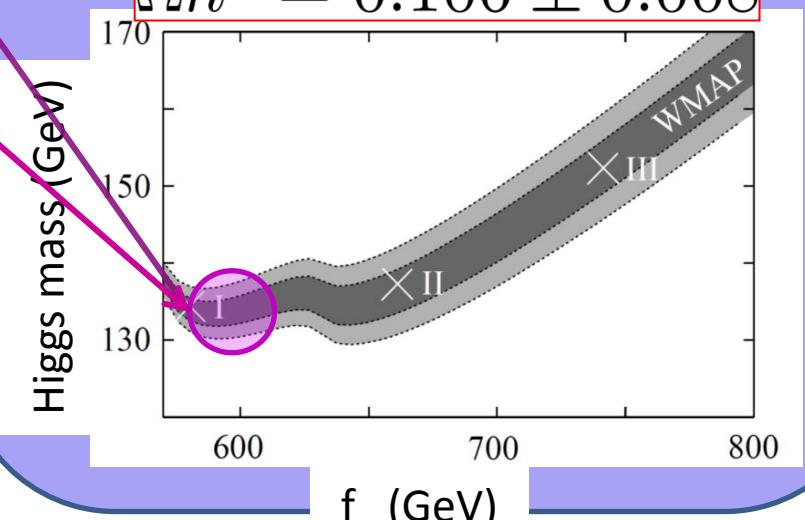
relic density measure from WMAP

Main annihilation mode



Cross section depends on m_{A_H} & m_H

$$\Omega h^2 = 0.106 \pm 0.008$$



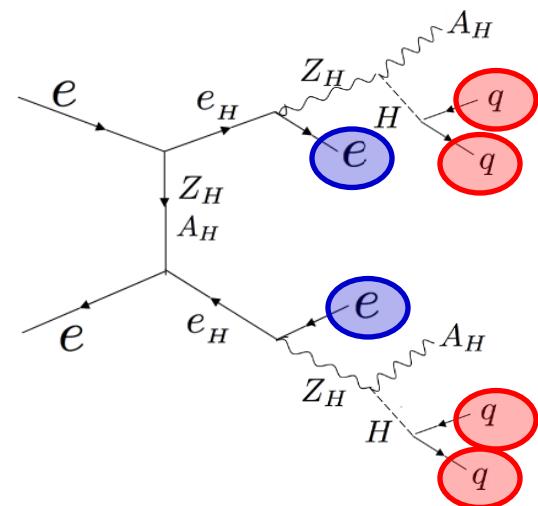
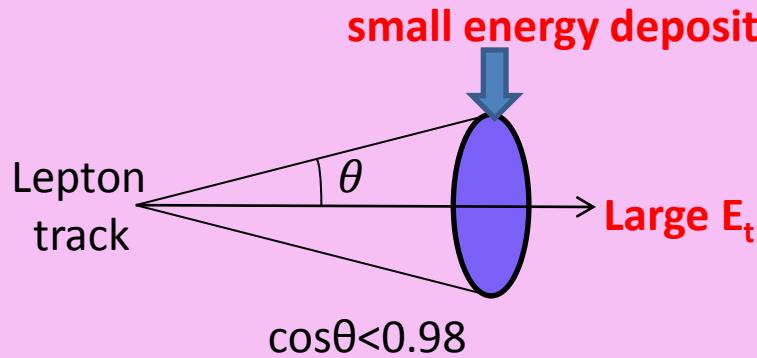
Event reconstruction

1. Select 2 Isolated lepton with maximum energy
2. Reconstruct and force the rest of the tracks as 4 jets.
3. Select reconstructed jet pair that minimizes χ^2 .

$$\chi_H^2 = \left(\frac{M_{H1} - M_H}{\sigma_{M_H}} \right)^2 + \left(\frac{M_{H2} - M_H}{\sigma_{M_H}} \right)^2$$

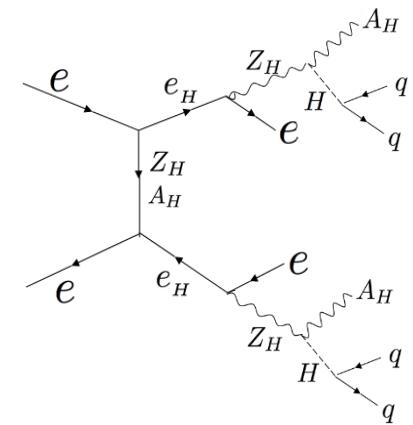
$$M_H = 134.0(GeV)$$

Isolated Lepton ID

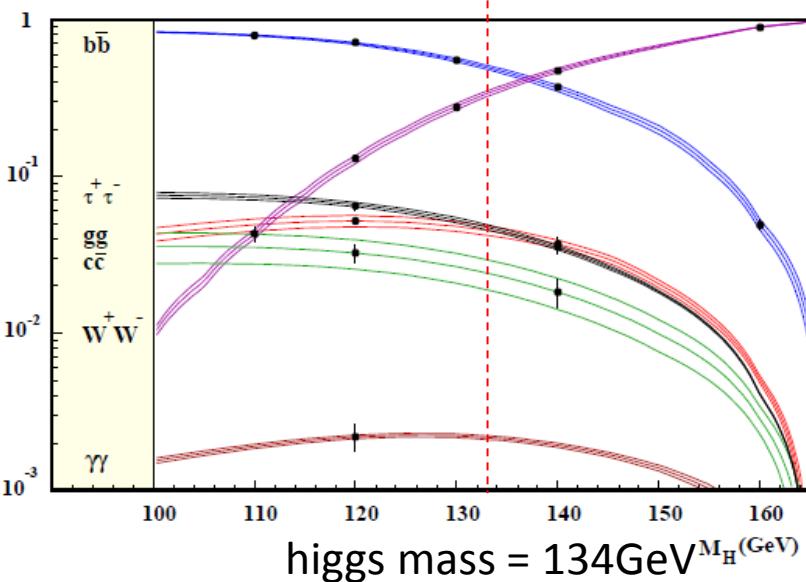


Signal Electron selection

- $e_H e_H \rightarrow e Z_H e Z_H$ analysis: 2e + 4jet
 - Higgs decay: ○ save full hadronic events
× lose isolated electron emitting events
- ⇒ optimize isolated electron selection



Higgs branching ratio



$\text{Br}(h \rightarrow b\bar{b}) = 42.35\%$ ○
 $\text{Br}(h \rightarrow WW) = 39.57\%$ {
 $\text{Br}(h \rightarrow ZZ) = 5.50\%$
 $\text{Br}(h \rightarrow \tau\tau) = 5.21\%$
 $\text{Br}(h \rightarrow gg) = 4.49\%$
 $\text{Br}(h \rightarrow cc) = 2.31\%$ ○
 \times Isolated electron emitting decay
 On non electron emitting Full hadronic decay

e_H Branching ratio study

$$\begin{aligned}\mathcal{L}_L^{(\text{Gauge})} = \dots + \frac{g}{\sqrt{2}} & [\bar{e}_H W_H P_L \nu \\ & - \frac{g}{2} \left[\bar{e}_H Z_H \left(c_H - \frac{s_W}{5c_W} s_H \right) P_L e \right. \\ & \left. - \frac{g}{2} \left[\bar{e}_H A_H \left(s_H + \frac{s_W}{5c_W} c_H \right) P_L e \right] \right].\end{aligned}$$

Charge suppress
されている。

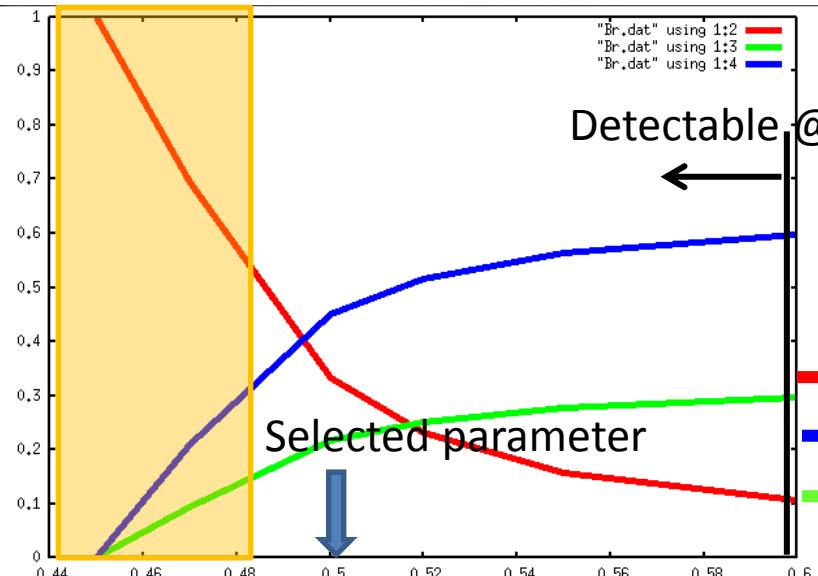
Mixing angle非常に小さい
 $s_H \sim 0.1$

e_H Branching ratio study

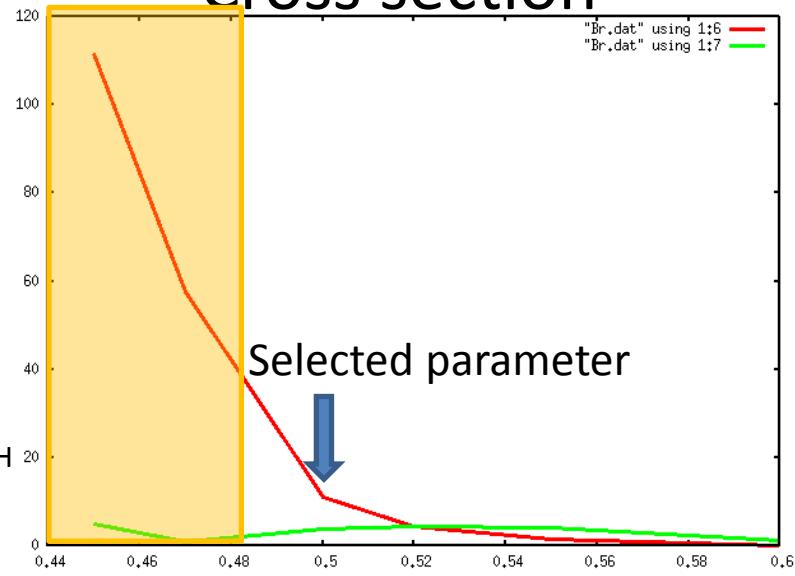
Branching ratio

@ $f = 580[\text{GeV}]$

Cross section



K



K

detectable@ 3fb^{-1} LHC. 2011-12ATLAS+CMS

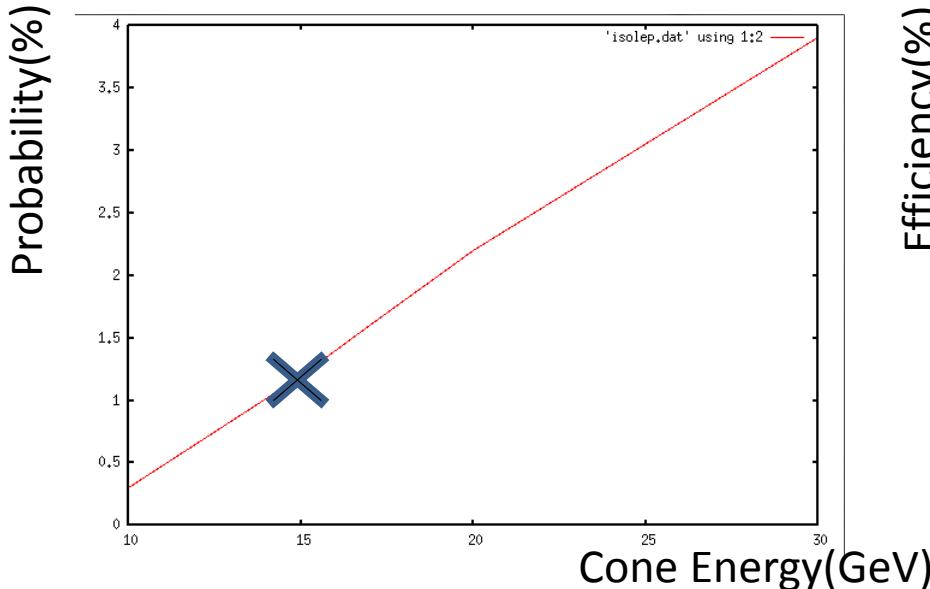
$$m_{e_H} \doteq m_{Z_H}, m_{W_H}$$

- Large $K \rightarrow$ heavy l_H small cross section
 eA_H small branching ratio
- $K > 0.5$ 300fb^{-1} LHC $4.2\sigma(vW_H)$
- eA_H : large SM & NP background
- eZ_H : 2higgs(134GeV) characteristic final state small background

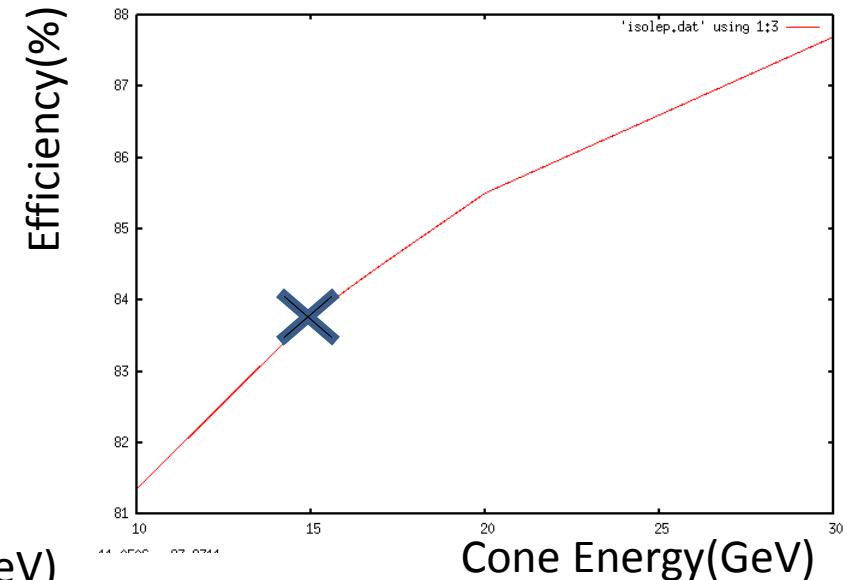
Signal Electron selection

- Probability of missIDing e from b jet is small.(signal: $H \rightarrow bb$)
⇒Optimize with selection efficiency of e from e_H .
 - Select point right before slope becomes shallow.
- Cone Energy <15GeV : $P(\text{missID})=1.2\%$,signal efficiency=84%

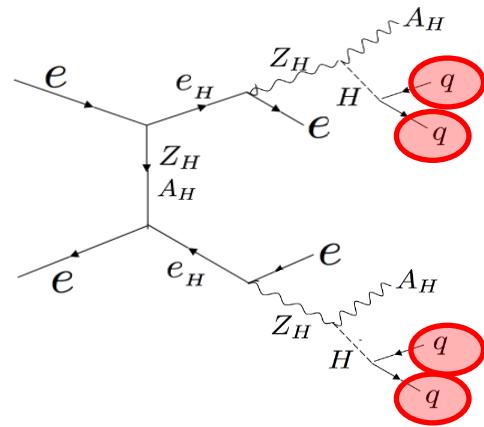
Probability of miss IDing e from b jet



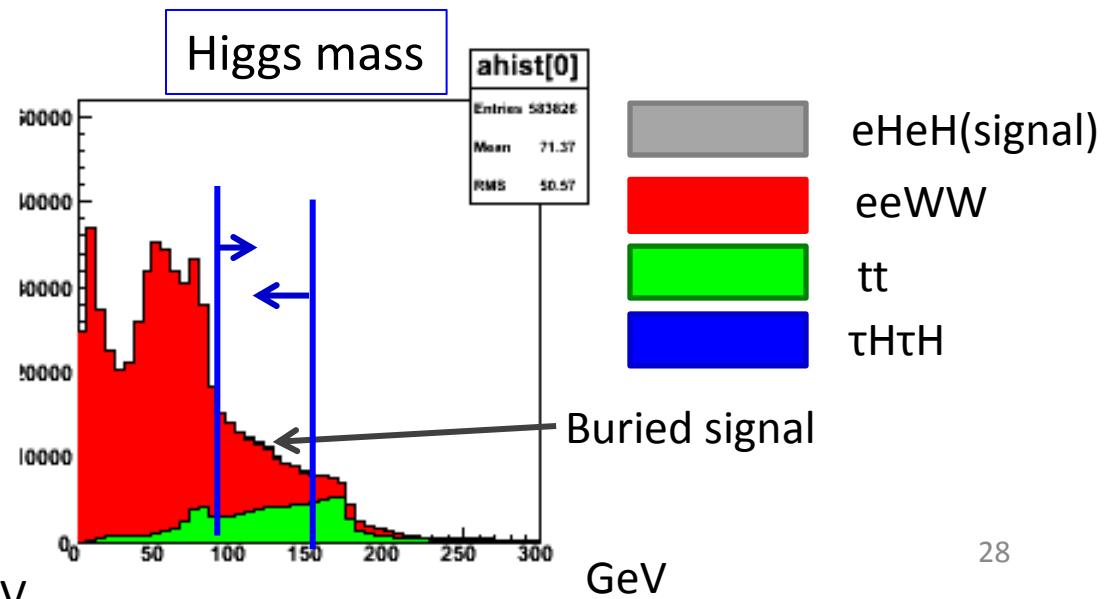
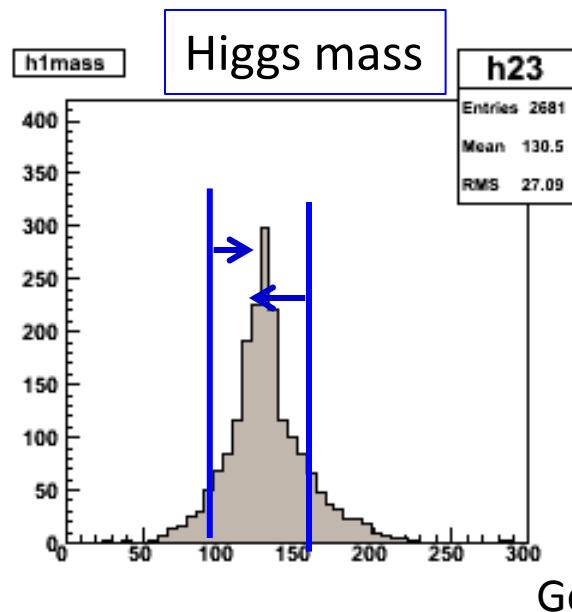
Selection efficiency of e from e_H



Reconstructed Higgs mass

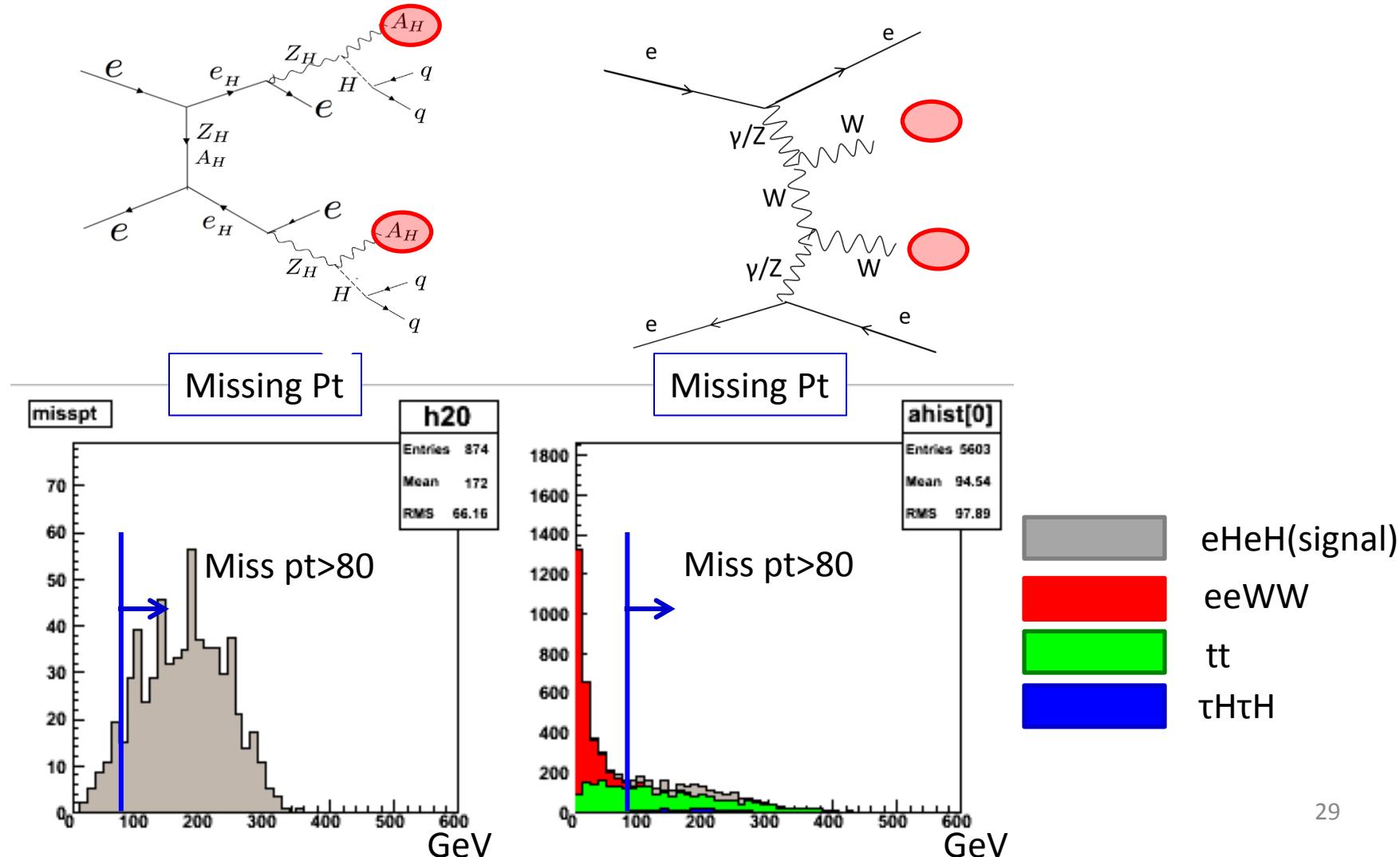


Decay mode	Reconstructed particle
$e_H e_H$	Higgs
$eeWW$	W boson
tt	B meson
$\tau_H \tau_H$	Higgs



Missing transverse momentum

■ Signal has large missing transverse momentum



Parameter extraction

- Through Toy MC, Confirmed that fitting is valid.
 - extracted value: $f=579.6 \pm 3.0(\text{GeV})$, $\kappa=0.5 \pm 4\text{e-}4$
 - True value: $f=580(\text{GeV})$, $\kappa=0.5$
- Extracted parameters include true value

