
RF operation with fixed Pks

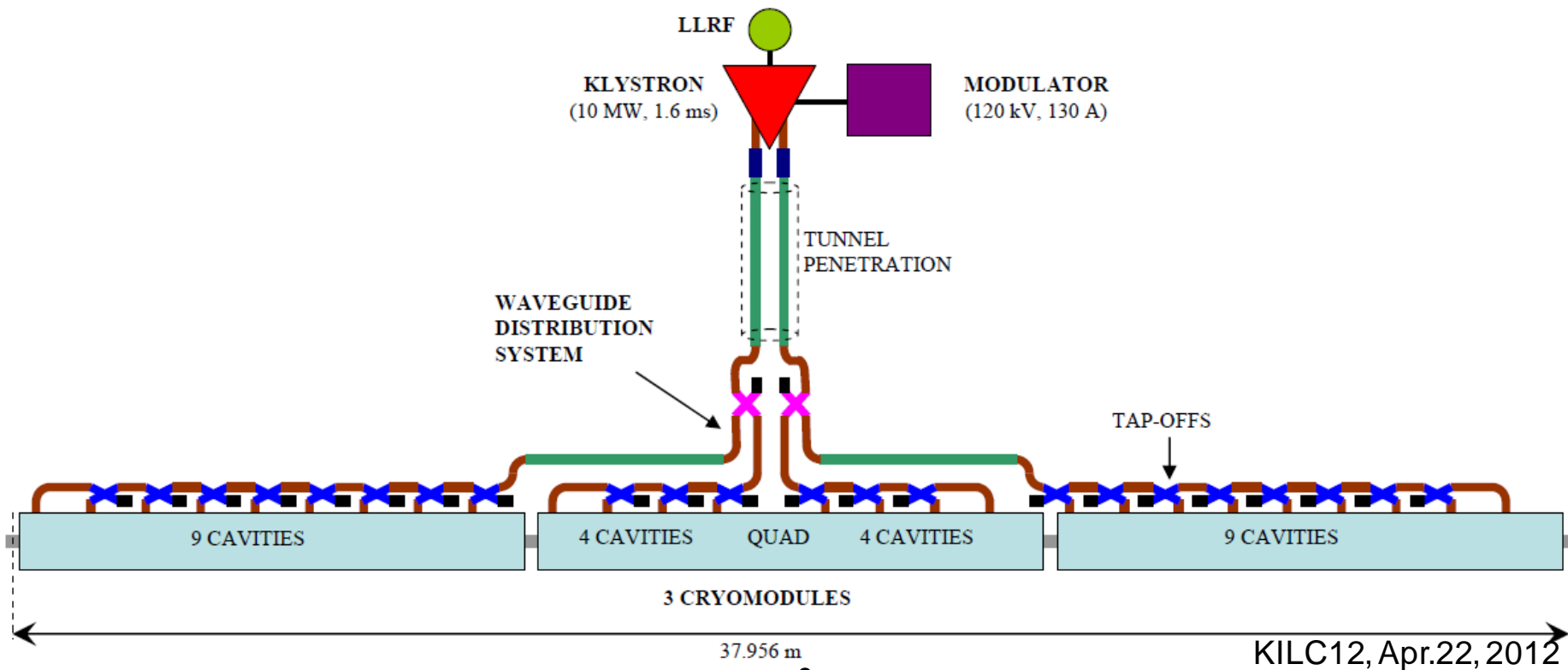
Shin MICHIZONO (KEK)

- Solution (1); QI proportional to I_b
- Simulation configuration –rectangular distribution
- Solution (2); QI optimization with 20% gradient distribution
- Solution (3); QI optimization with 10% gradient distribution

RF distribution system (RDS)

- RDR: 1 klystron drives 26 same gradient cavities (31.5MV/m).
- TDR: 1 klystron drives 39 cavities with gradient variation (25 MV/m ~ 38 MV/m).
 - 1) PkQI control is proposed.
 - 2) new: semi-fixed Pks were proposed to reduce the RDS cost.

-> Pks are optimized at some beam current and are not changed during various beam operation. -> Is it reasonable to fix Pks for near-quench-limit operation?



Solution (1) – QI proportional to Ib

PkQI control

$$V_{\text{cav}} = 2 \frac{r}{Q} Q_L I_{\text{gen}} \cdot \left(1 - \exp\left(-\frac{T_{\text{inj}}}{\tau}\right)\right)$$

If we select QI to be proportional to beam current (so I_{gen}) and select filling time also proportional to QI (or I_{beam}), we can keep V_{cav} with various beam current.

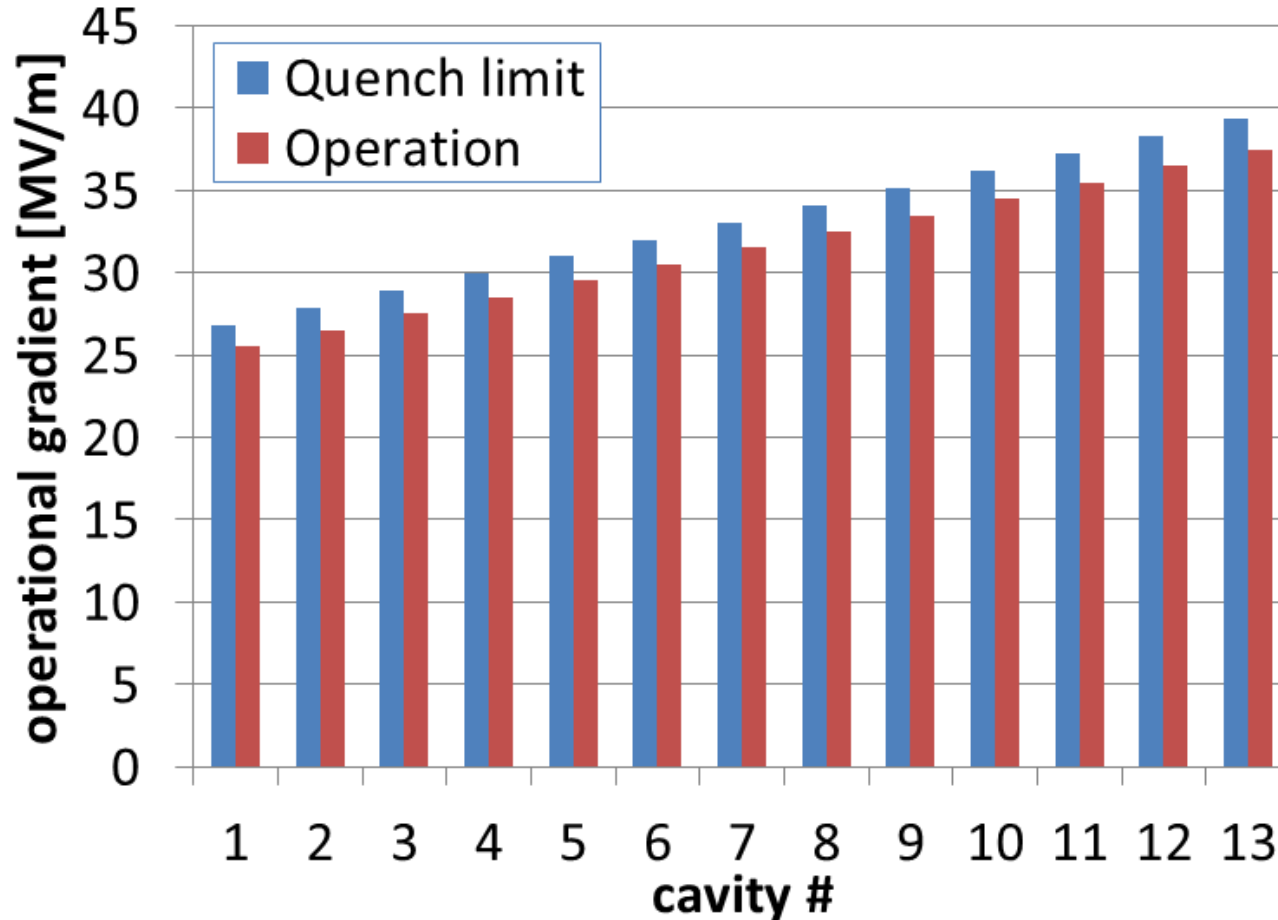
$$Q_L = \frac{I_{\text{gen}0}}{I_{\text{gen}}} Q_{L0} = \frac{I_{\text{beam}0}}{I_{\text{beam}}} Q_{L0}$$

$$T_{\text{inj}} = \frac{\tau}{\tau_0} T_{\text{inj}0} = \frac{I_{\text{beam}}}{I_{\text{beam}0}} T_{\text{inj}0}$$

$$P_k = \frac{1}{4} \frac{r}{Q} Q_L (I_{\text{gen}})^2 = \frac{1}{4} \frac{r}{Q} Q_{L0} I_{\text{gen}0} I_{\text{gen}} = \frac{I_{\text{beam}}}{I_{\text{beam}0}} P_{k0}$$

Configuration: QIs with 20% V_{cav} variation

- 13 cavities having the operational gradient from 25.5 MV/m to 37.5 MV/m.
- Gradient spread is ~ rectangular distribution.

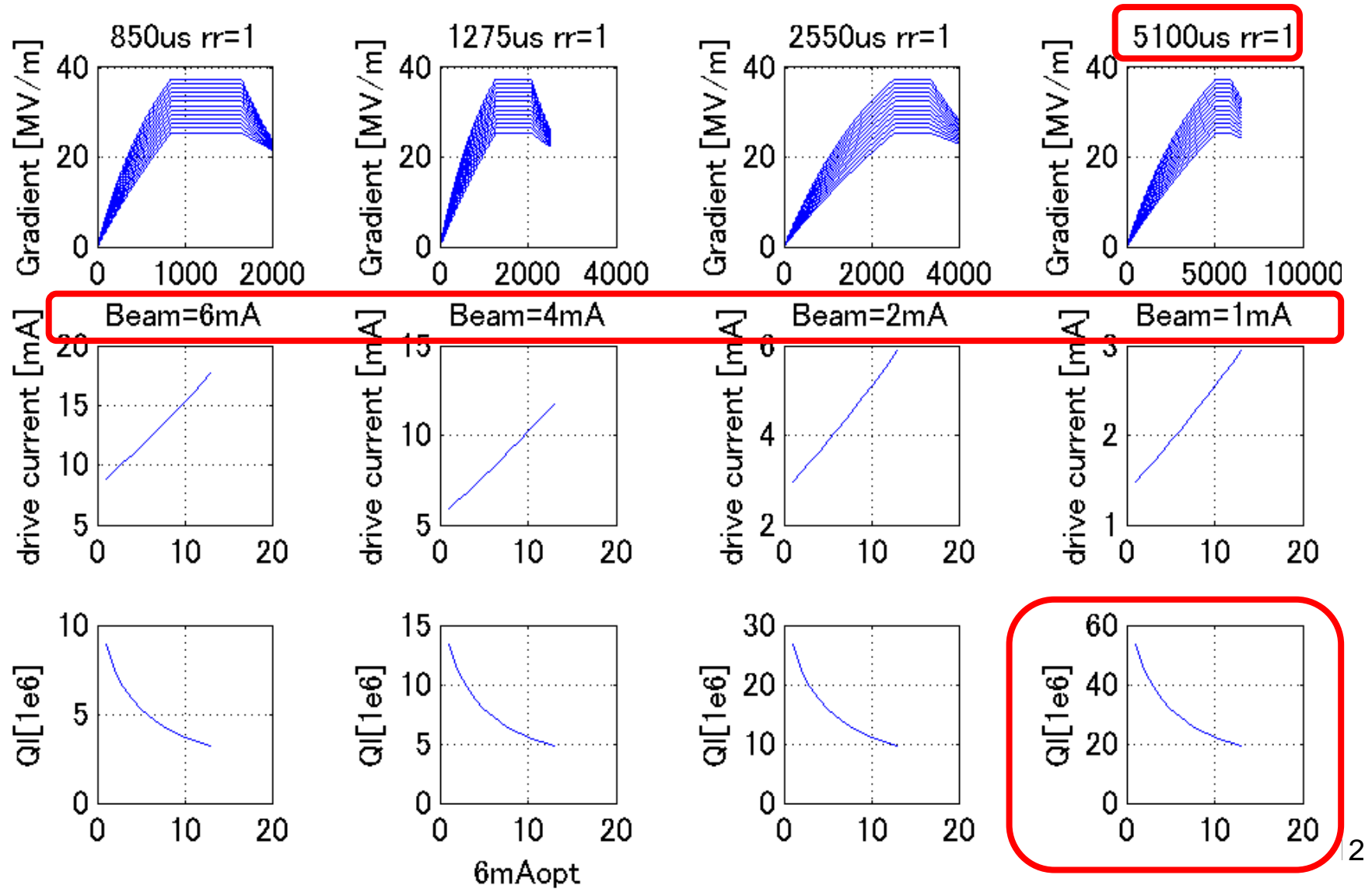


Suppose operational gradients (25.5 MV/m~37.5MV/m) are 5% lower than quench limit.

Solution (1) – QI proportional to Ib

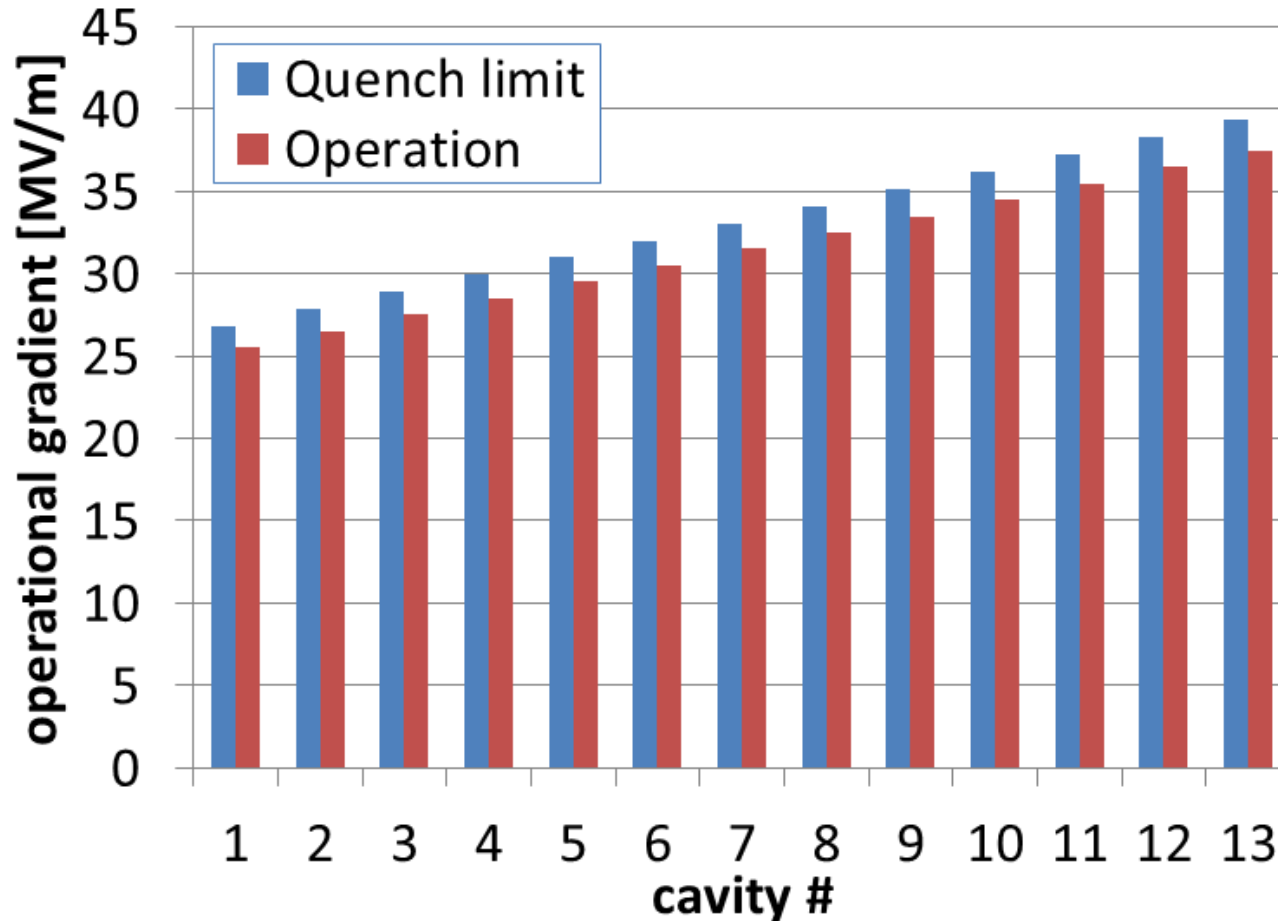
Cavity gradient can keep the same value with various beam current.

However, filling time (and QIs) becomes too large (~5ms filling time at 1mA beam).



Solution (2) -QIs with 20% V_{cav} variation

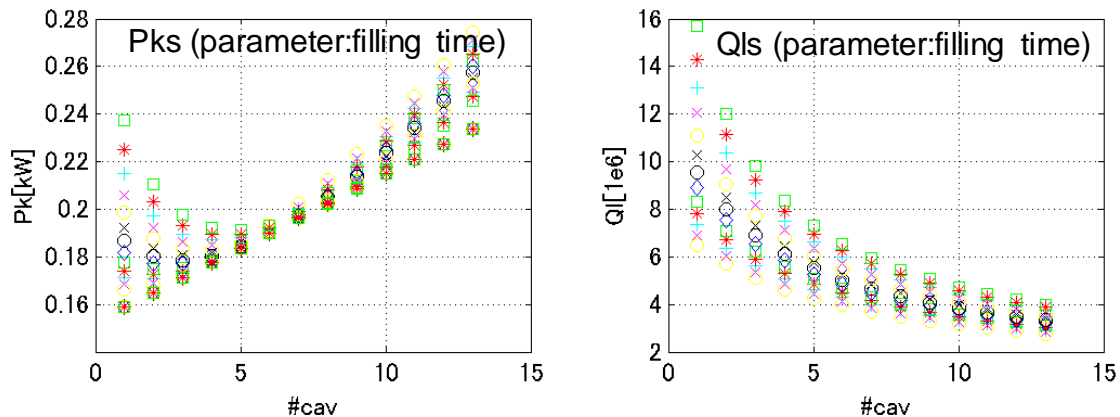
- 13 cavities having the operational gradient from 25.5 MV/m to 37.5 MV/m.
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Suppose operational gradients (25.5 MV/m~37.5MV/m) are 5% lower than quench limit.

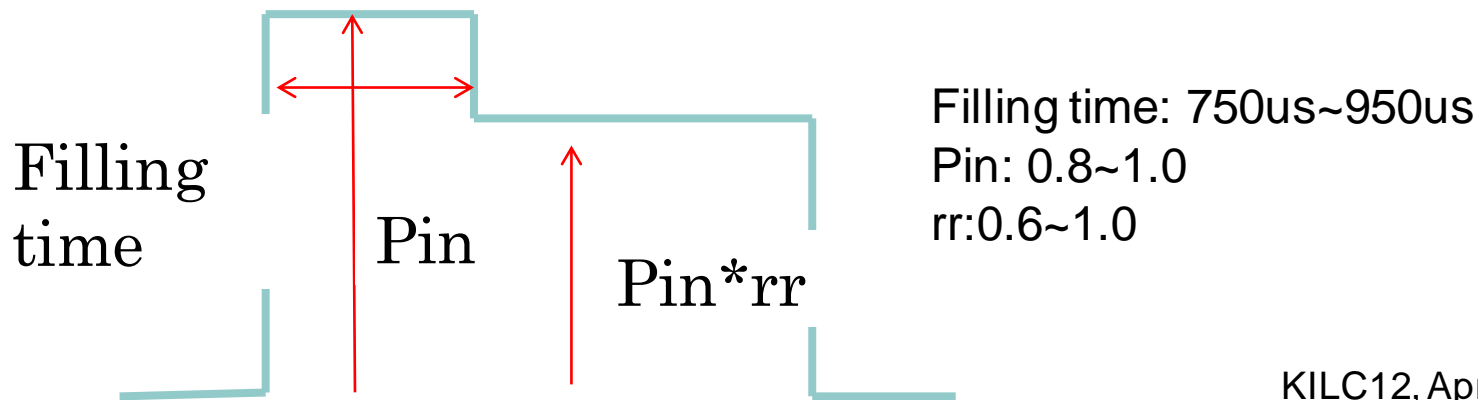
Simulation procedure

1. Optimize the Pks for 6mA beam operation

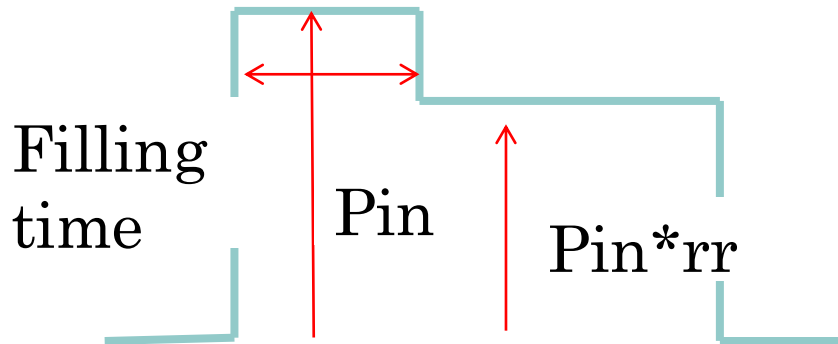


I select 850us filling time. (lowest rf power =2.677MW($\sim 4.9\%$ higher than beam loading(= optimized same Ql, Vacc control))
Qls are $8.9e6(24.5MV/m)$ $\sim 3.2e6(37.5MV/m)$

2. Under these Pks, optimize filling time, Pin, step ratio (rr) and Qls.



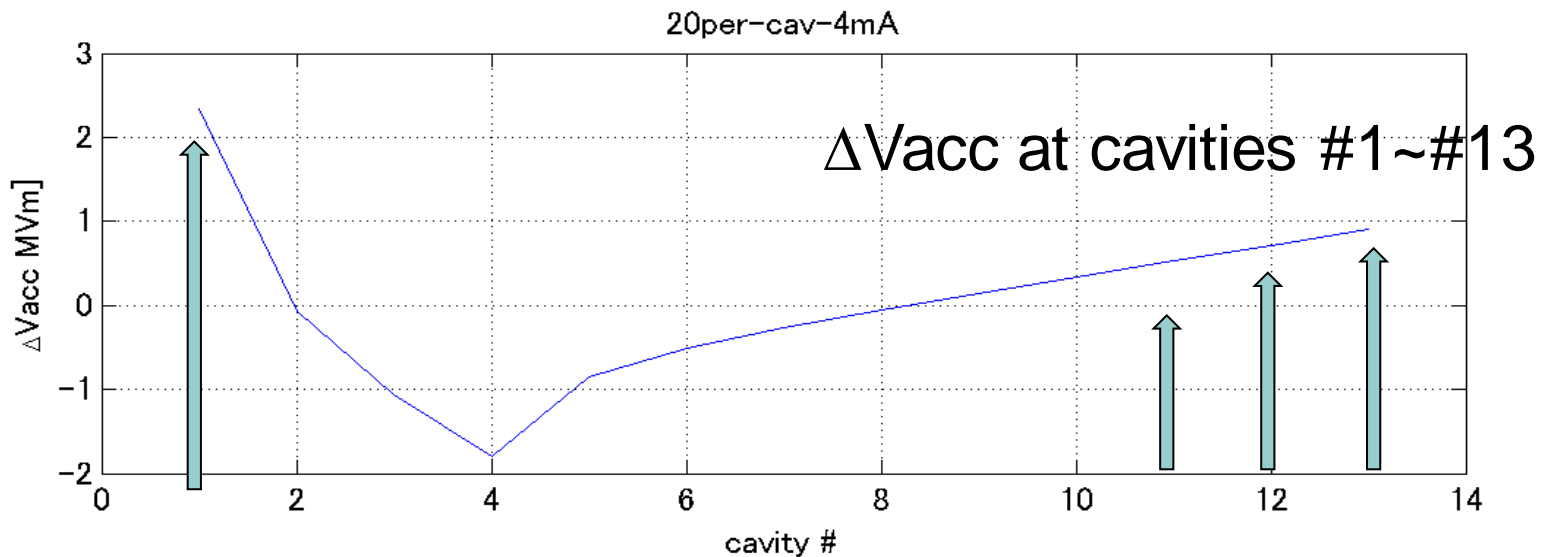
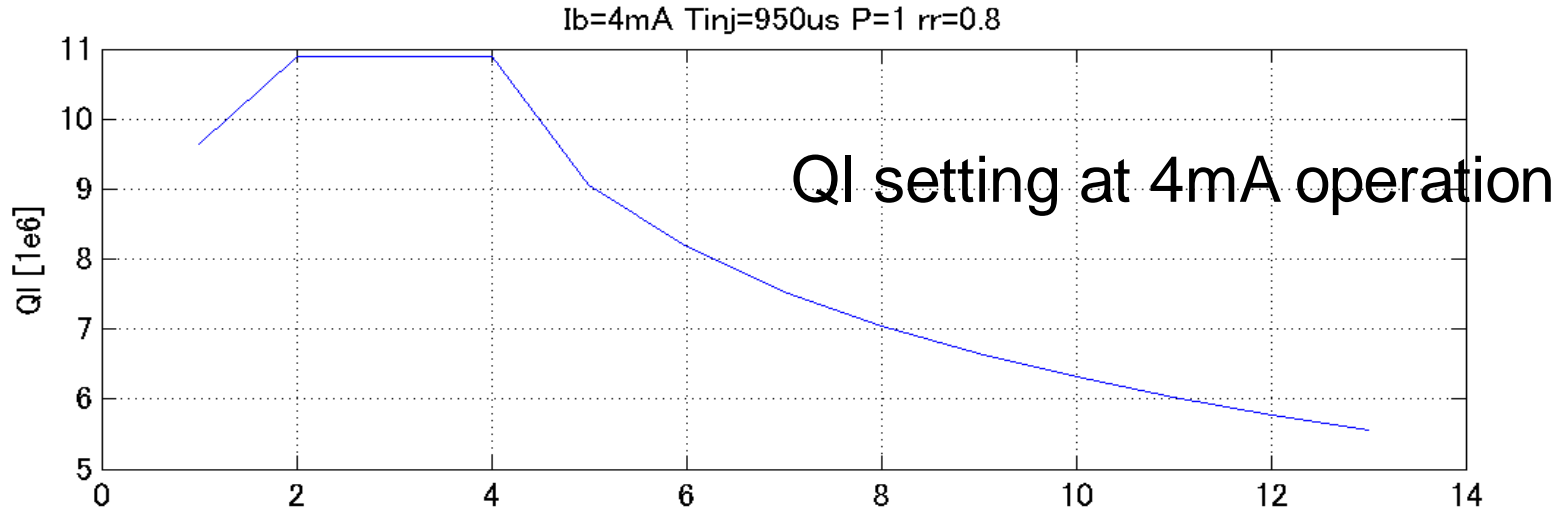
Performance at various Ibeam



Ibeam [mA]	Filling [us]	Pin	rr	Additional Vacc [MV/m]	Additional Vacc [%]
6	850	1	1	0	0
4	950	1	0.8	2.35	9.2
2	870	1	0.6	3.63	14.2
0	800	1	0.9	4.03	15.8

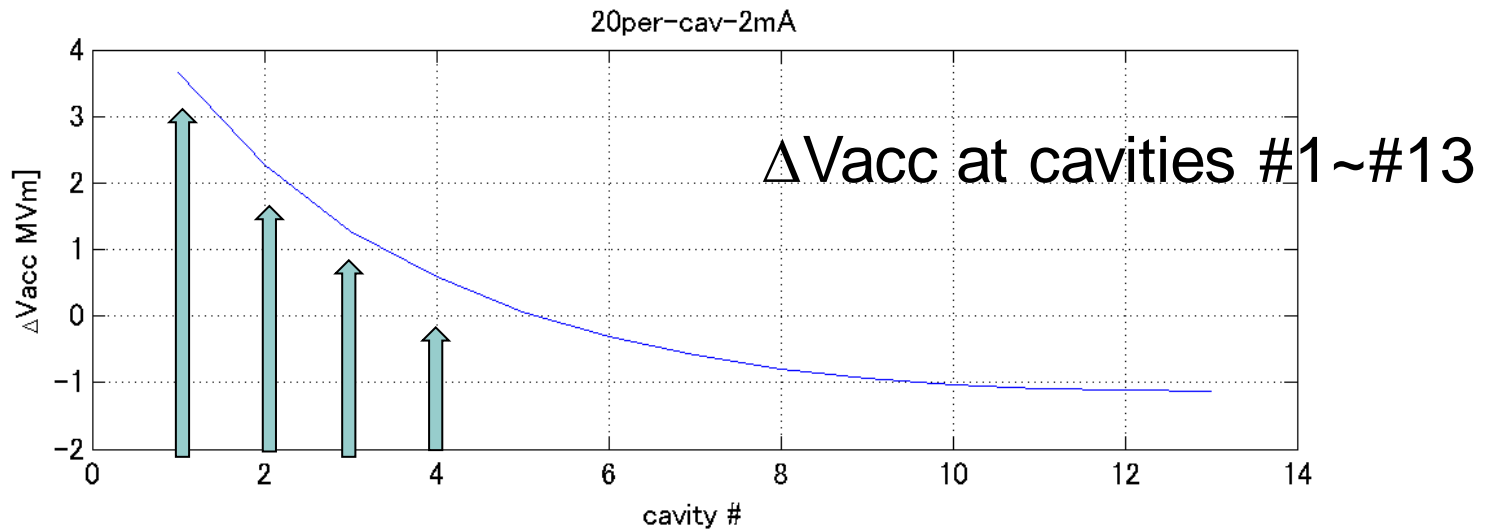
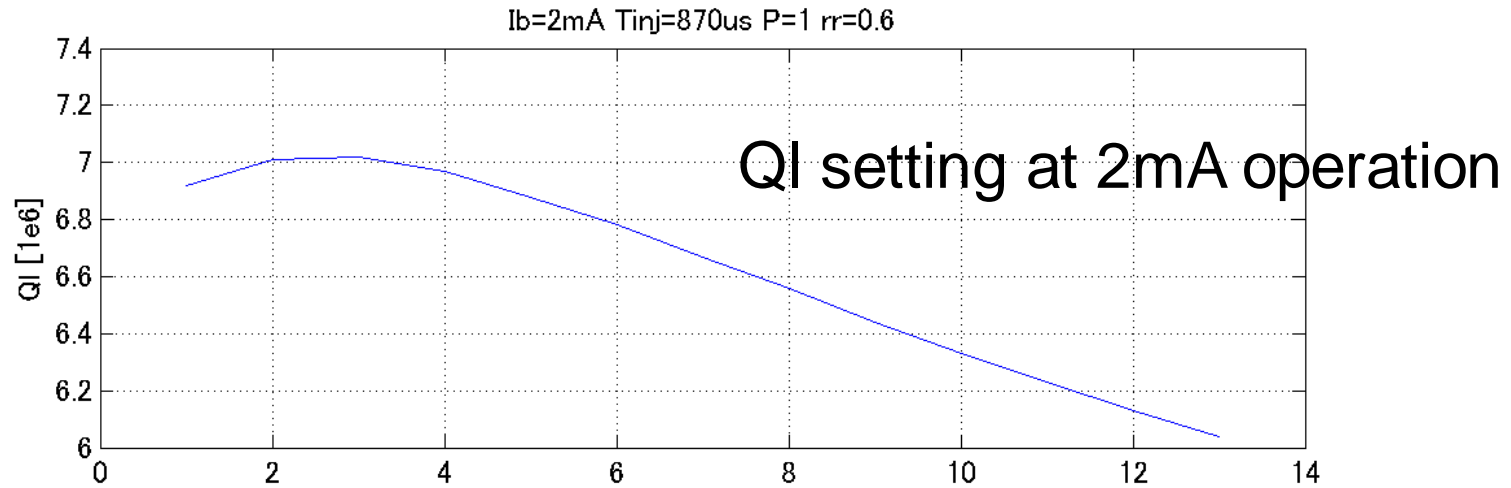
Low gradient cavity shows the gradient ~10% higher.

Performance at 4mA



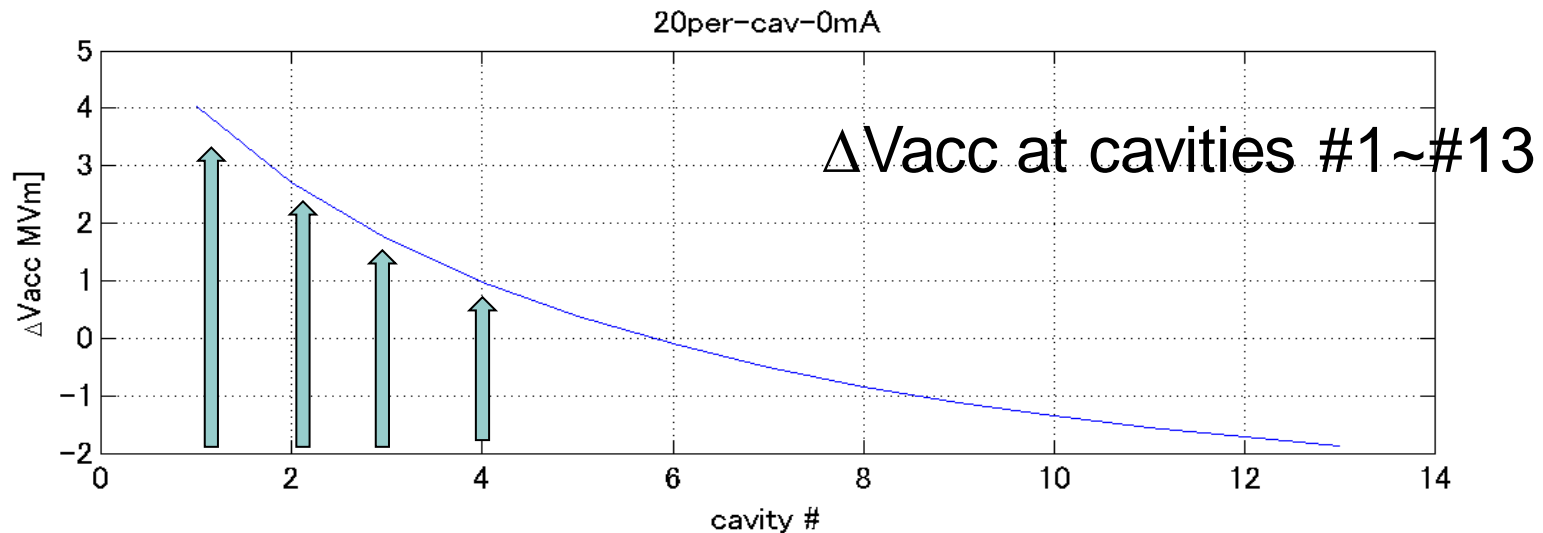
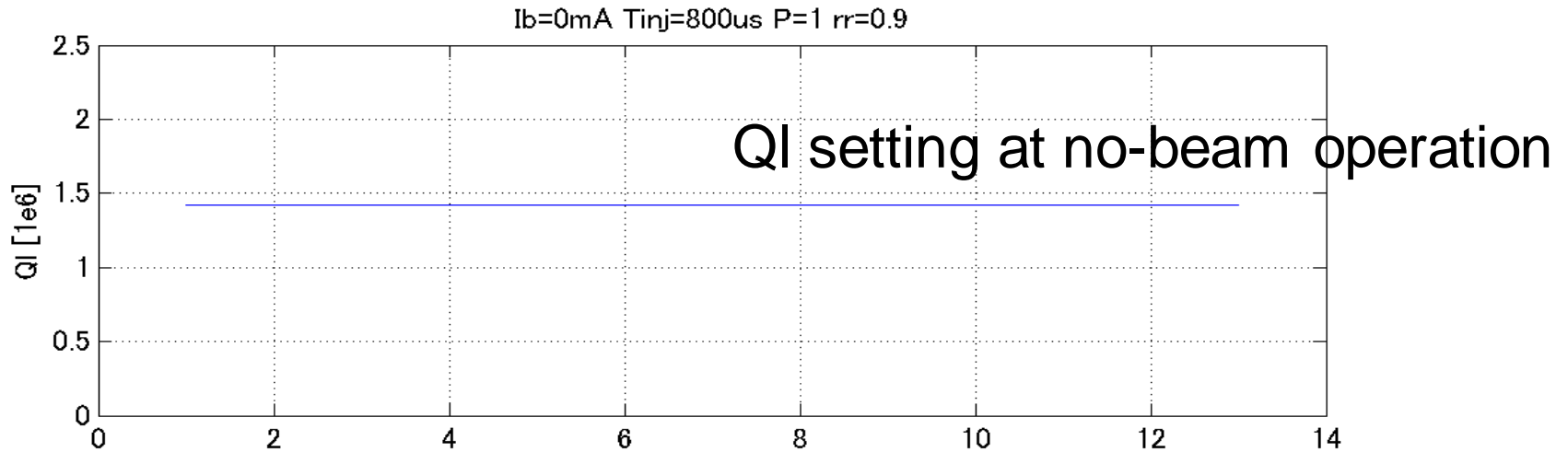
Lowest gradient cavity exceeds the 6mA operated gradient.

Performance at 2mA



Lower 4 cavities exceed their V_{acc} value at 6mA.

Performance at 0mA



Lower 4 cavities exceed their V_{acc} value at 6mA.

Performance at various Ibeam

Ibeam [mA]	Filling [us]	Pin	rr	Additional Vacc [MV/m]	Additional Vacc [%]
6	850	1	1	0	0
4	950	1	0.8	2.35	9.2
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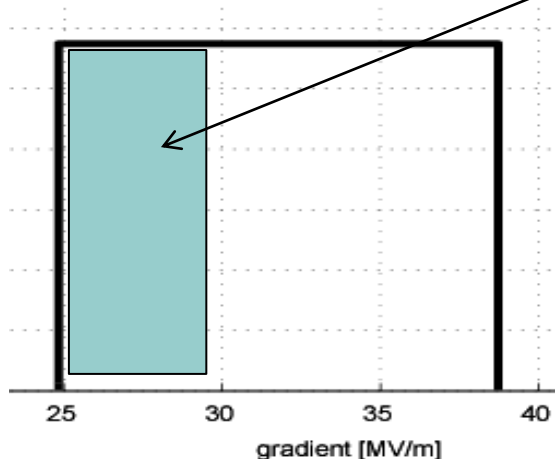
25MV/m~30MV/m cavities should be operated <20% than quench limit.

-> In case of the **rectangular gradient variation**, 25~30MV/m cavities are 5/13(=38%)

Average gradient of 25-30MV/m=27.5MV/m

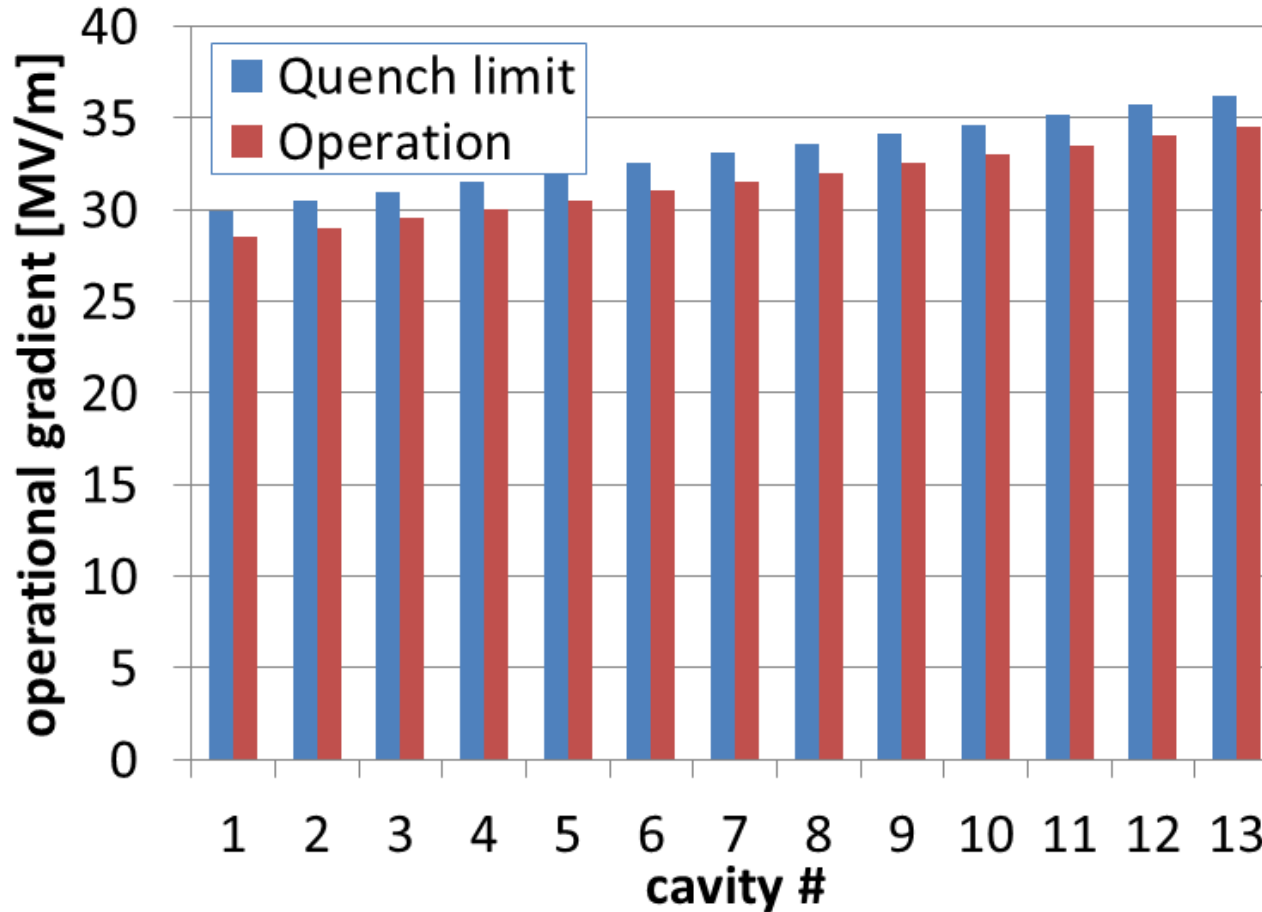
15% more margin than nominal cavities; $27.5 * 0.15 * 0.38 / 31.5 = 0.0503$ (=5%)

Total accelerating energy decrease ~5% in case of the semi-fixed Pks configuration.



Solution (3) -QIs with 10% Vcav variation

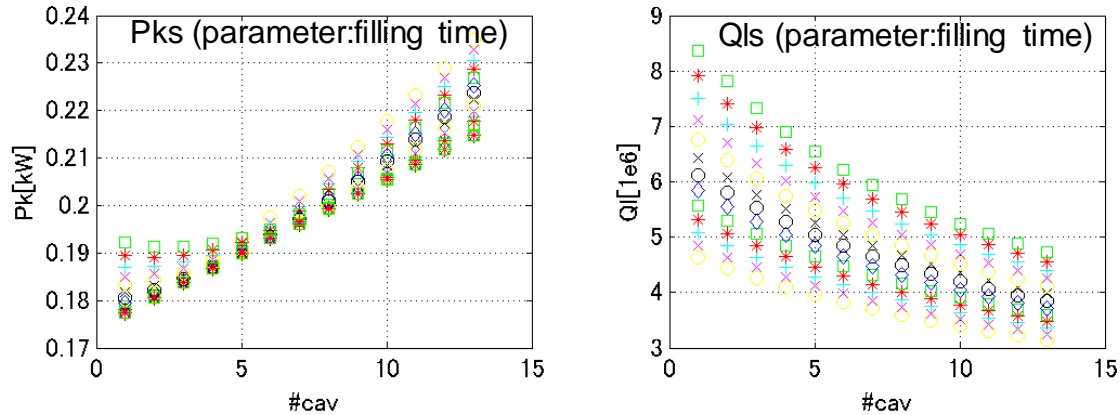
- 13 cavities having the operational gradient from 28.5 MV/m to 34.5 MV/m.
- Gradient spread is ~ rectangular distribution.



Suppose operational gradients (28.5 MV/m~34.5MV/m) are 5% lower than quench limit.

Simulation procedure

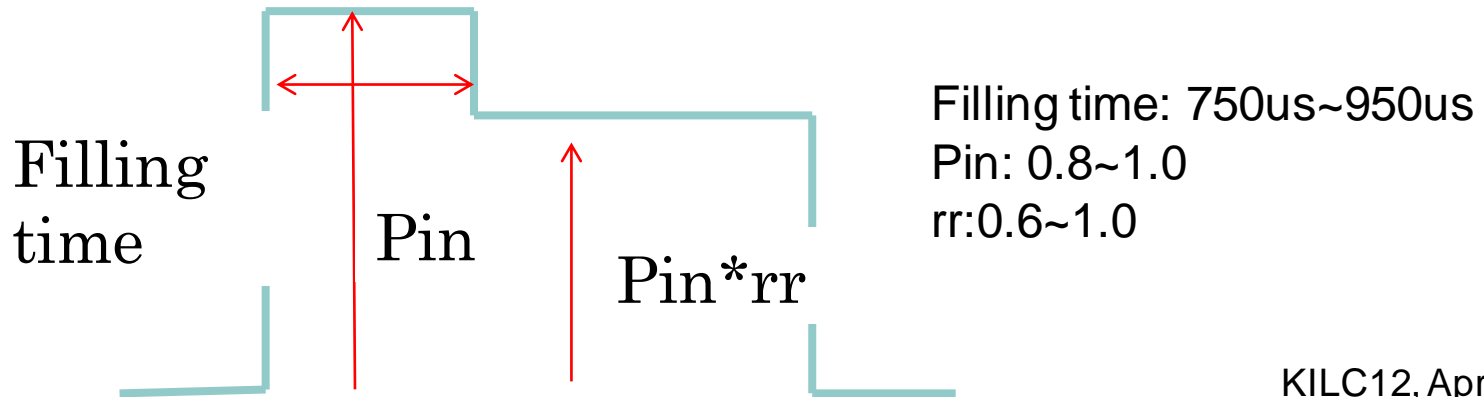
1. Optimize the Pks for 6mA beam operation



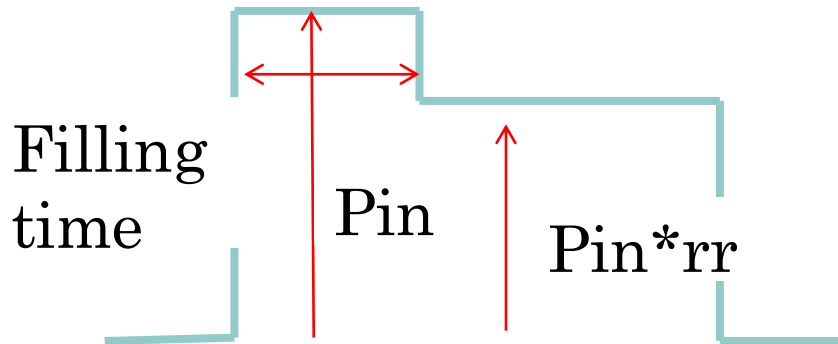
I select 850us filling time. (lowest rf power = 2.58MW (~1.2% higher than beam loading (= optimized same Ql, Vacc control)))

Qls are $6.77e6$ (28.5MV/m) ~ $4.11e6$ (34.5MV/m).

2. Under these Pks, optimize filling time, Pin, step ratio (rr) and Qls.



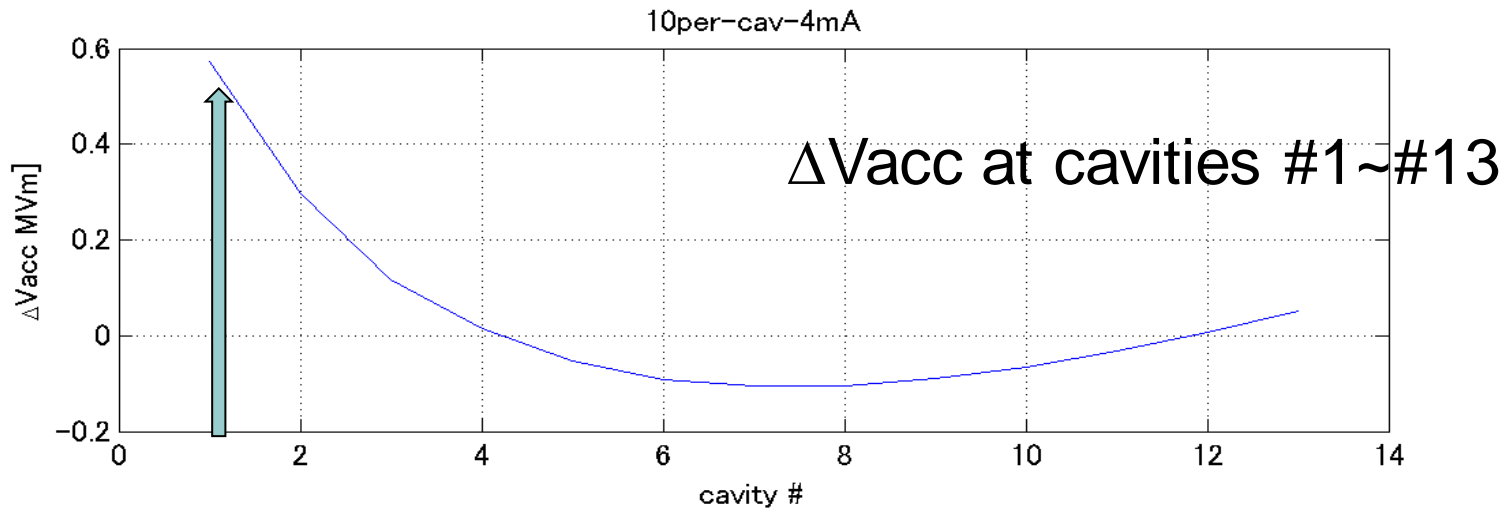
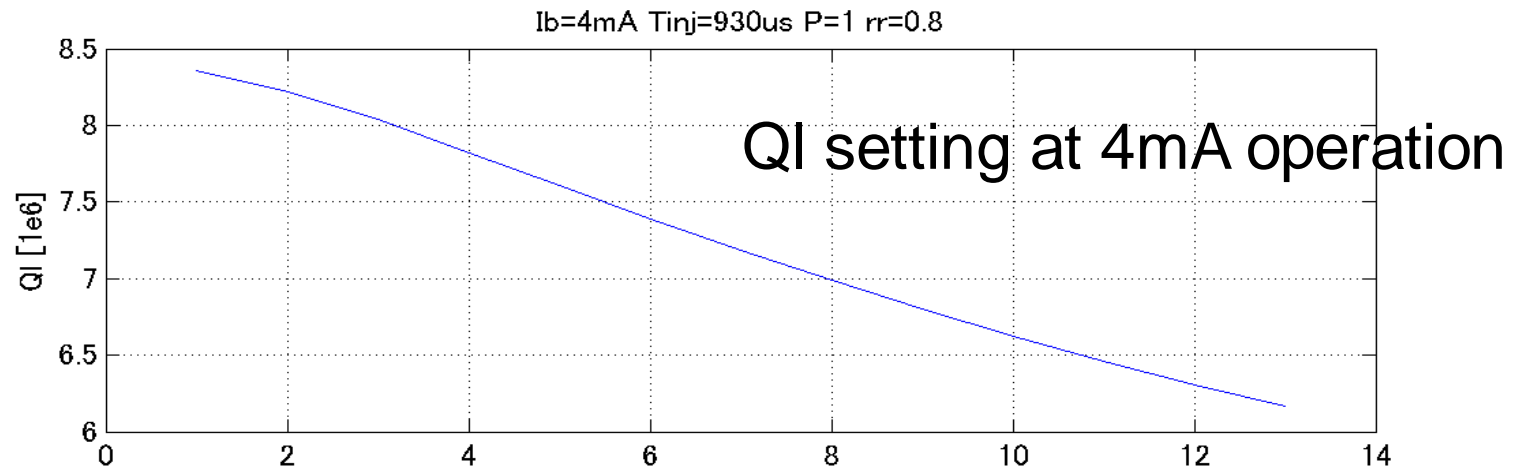
Performance at various Ibeam



Ibeam [mA]	Filling [us]	Pin	rr	Additional Vacc [MV/m]	Additional Vacc [%]
6	850	1	1	0	0
4	930	1	0.8	0.57	2.00
2	980	1	0.6	1.42	5.00
0	780	1	0.6	1.75	6.15

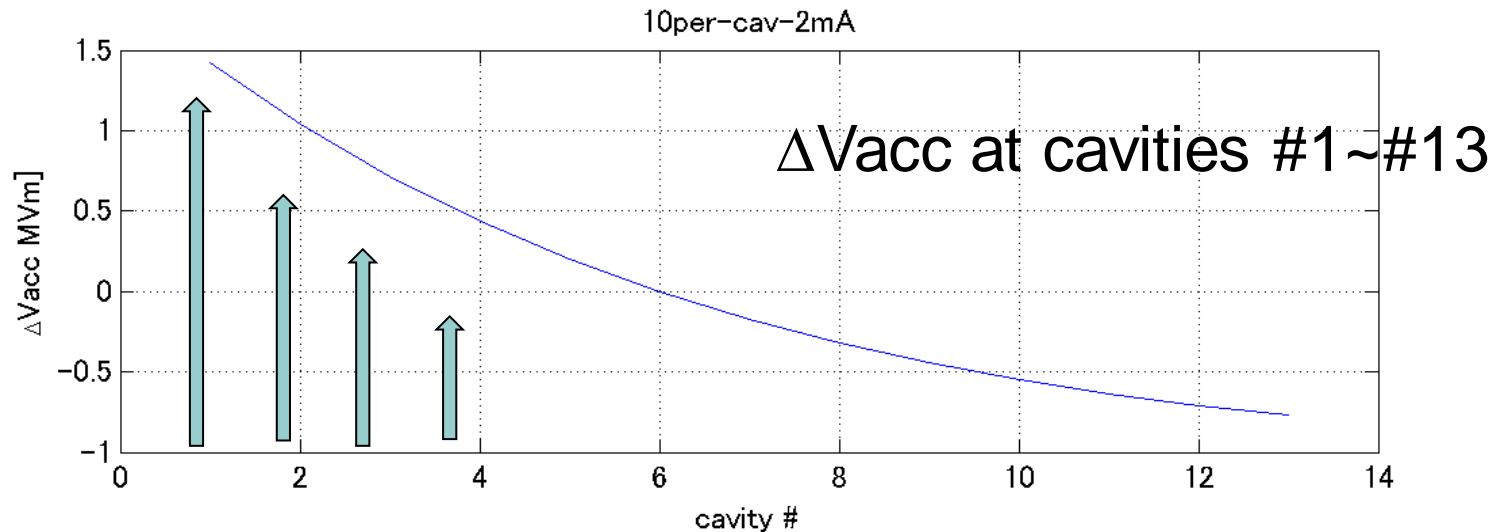
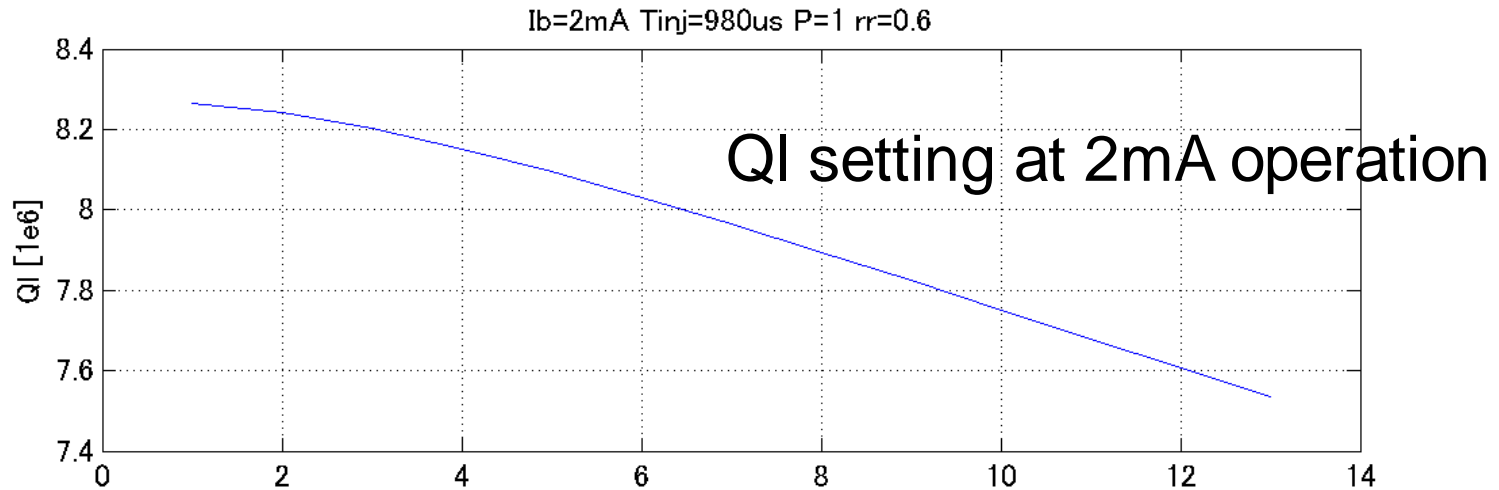
Low gradient cavity shows the gradient ~5% higher.

Performance at 4mA



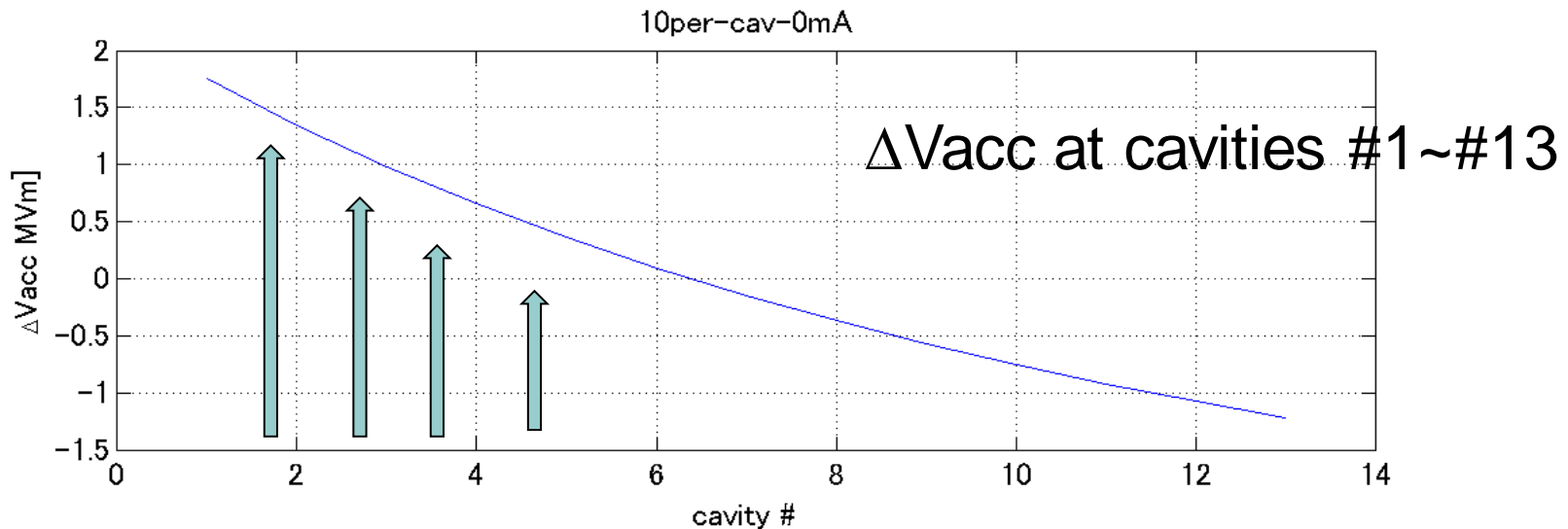
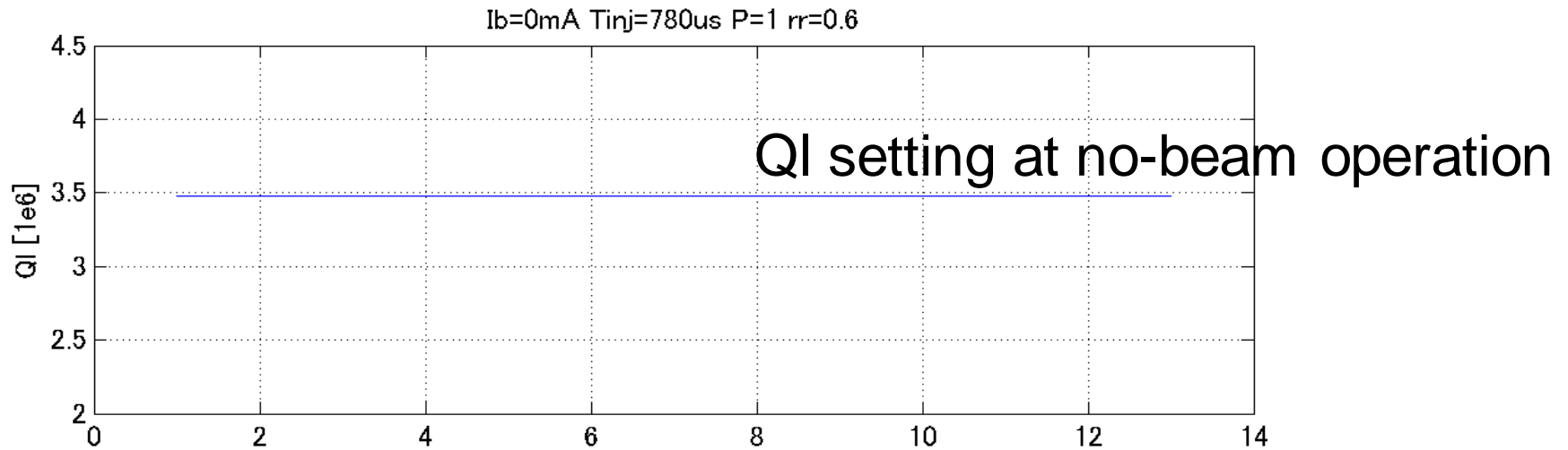
Lowest gradient cavity slightly exceeds the 6mA operated gradient.

Performance at 2mA



Lower 4 cavities slightly exceed their V_{acc} value at 6mA.

Performance at 0mA



Lower 4 cavities slightly exceed their V_{acc} value at 6mA.

Performance at various Ibeam

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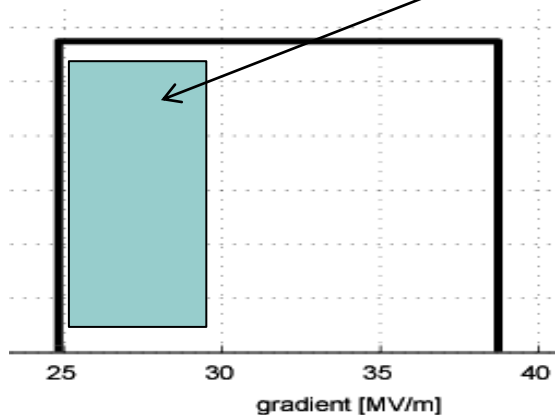
28.5MV/m~30MV/m cavities should be operated <10% than quench limit.

-> In case of the **rectangular gradient variation**, 28.5~30MV/m cavities are 4/13(=31%)

Average gradient of 28.5-30MV/m=29.25MV/m

5% more margin than nominal cavities; $29.25 * 0.05 * 0.31 / 31.5 = 0.014$ (=1.4%)

Total accelerating energy decrease ~1.4% in case of the semi-fixed Pks configuration with 10% gradient variation..



Summary

- Semi-fixed Pks are simulated.
- Solution (1); QI proportional to beam current
 - Perfect cavity gradient with any beam current
 - **Huge filling time** (and huge QI ($\sim 7e7$)) is required at low current (such as 1mA).
- Solution (2); Filling time, QI adjustment to minimize the difference in operational gradient **under 20% cavity gradient variation**.
 - 15% gradient increase at lower gradient cavity.
 - Such cavities should be operated at lower gradient at 6mA.
 - Rough estimate indicates **we lose 5% acc. energy** (or 5% longer ML is required.)
- Solution (3); Filling time, QI adjustment to minimize the difference in operational gradient **under 10% cavity gradient variation**.
 - 5% gradient increase at lower gradient cavity.
 - Such cavities should be operated at slightly lower gradient at 6mA.
 - Rough estimate indicates **we lose 1.5% acc. energy** (or 1.5% longer ML is required.)
- In addition to these difference in cavity gradient with various beam current, we should include the tolerance of the Pks.

Thank you for your attention