

Seesaw model with a loop-induced
Dirac mass term and dark matter
From $U(1)_{B-L}$ gauge symmetry breaking

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S. Kanemura, T.N., H. Sugiyama, *Phys. Lett.* B703:66–70
S. Kanemura, T.N., H. Sugiyama, *Phys. Rev.* D85, 033004

KILC12 25 Apr. 2012

1.Introduction

The standard model (SM) is a very successful model to describe physics below $O(100)\text{GeV}$.

However,

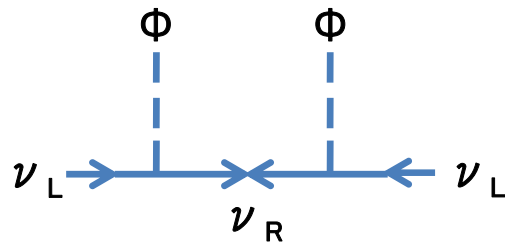
we know the phenomena of the beyond-SM.

1. Neutrino oscillation
2. Dark matter
3. Baryon asymmetry of the Universe

Especially, neutrino oscillation and dark matter would be explained by radiative seesaw models at TeV scale.

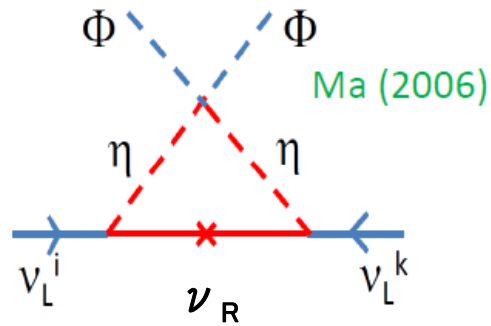
1. Introduction

Neutrino masses



$$M \sim O(1) \text{ TeV}$$

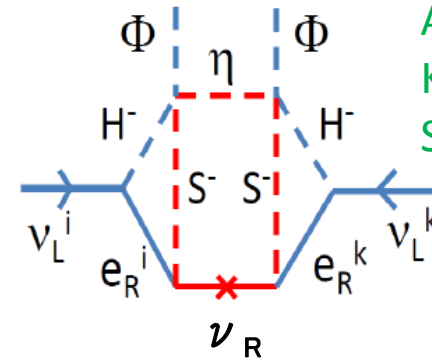
$$\rightarrow c \sim O(10^{-6})$$



Ma (2006)

$$M \sim O(1) \text{ TeV}$$

$$\rightarrow c \sim O(10^{-4})$$



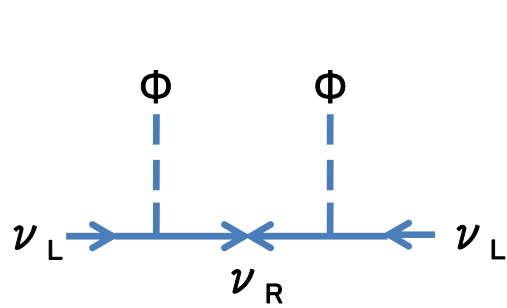
Aoki,
Kanemura,
Seto (2008)

$$M \sim O(1) \text{ TeV}$$

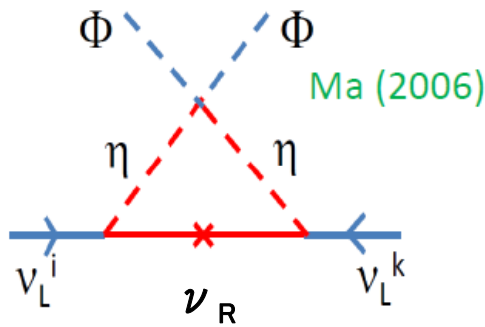
$$\rightarrow c \sim O(1)$$

1.Introduction

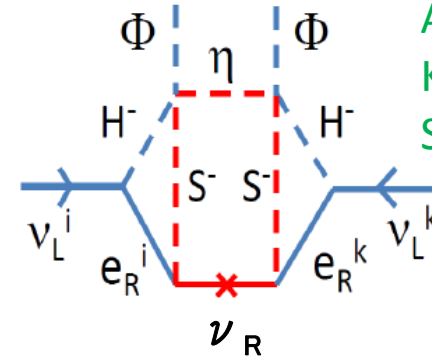
Neutrino masses



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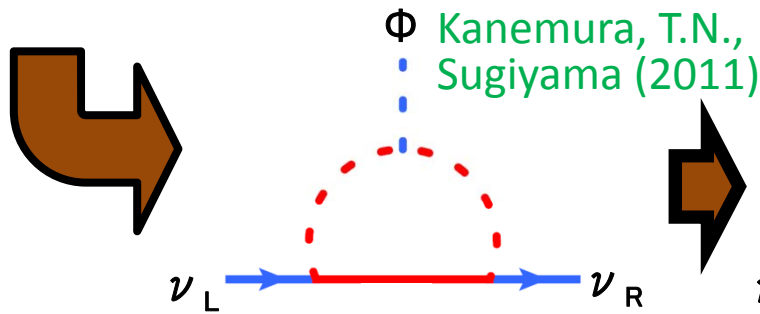


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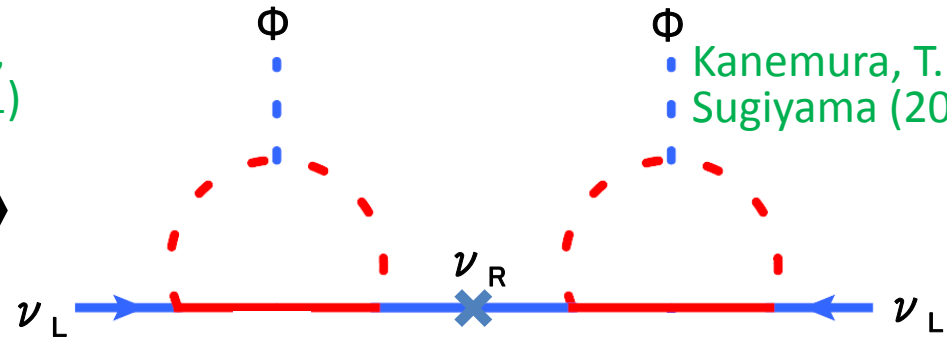


$M \sim O(1) \text{ TeV}$
 $\rightarrow c \sim O(1)$

Aoki,
 Kanemura,
 Seto (2008)



Kanemura, T.N.,
 Sugiyama (2011)

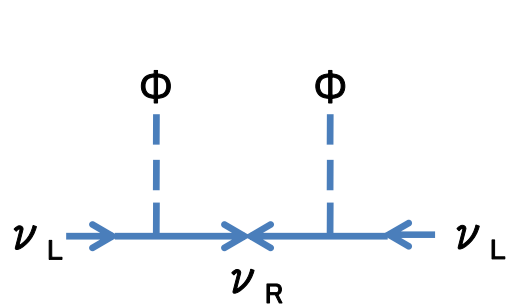


Kanemura, T.N.,
 Sugiyama (2012)

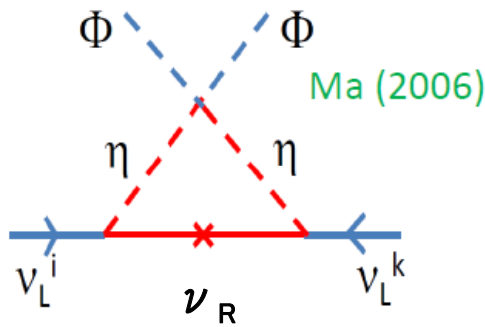
$M \sim O(1) \text{ TeV}$
 $\rightarrow c \sim O(10^{-2}-10^{-1})$ - ν_R are not stable.

1.Introduction

Neutrino masses

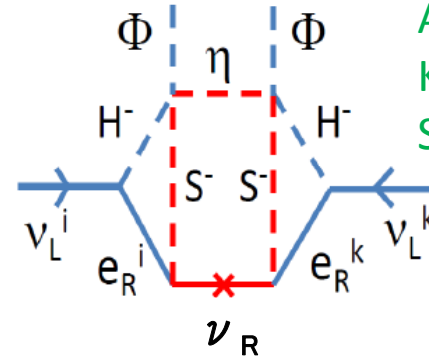


$M \sim O(1) \text{ TeV}$
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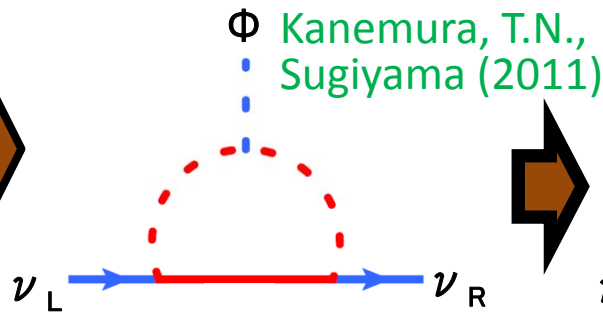
Ma (2006)

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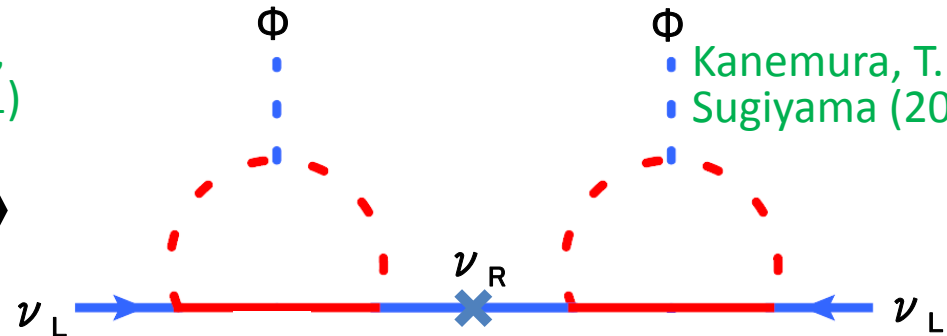


Aoki,
 Kanemura,
 Seto (2008)

$M \sim O(1) \text{ TeV}$
 $\rightarrow c \sim O(1)$



Kanemura, T.N.,
 Sugiyama (2011)



Kanemura, T.N.,
 Sugiyama (2012)

$M \sim O(1) \text{ TeV}$
 $\rightarrow c \sim O(10^{-2}-10^{-1})$ - ν_R are not stable.

We consider this case.

1.Introduction

WIMP dark matter

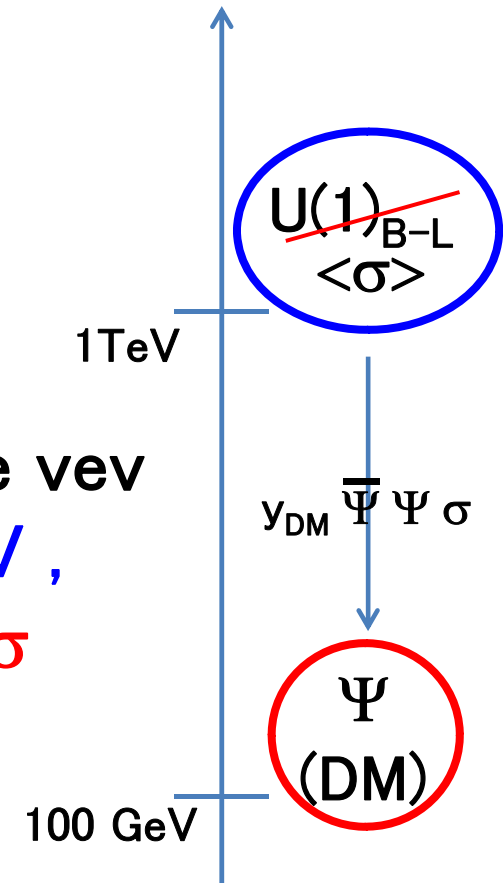
- WIMP dark matter mass:

$$M_{\text{DM}} \sim O(100-1000)\text{GeV}$$



What is the origin of M_{DM} ?

If $U(1)_{\text{B-L}}$ gauge symmetry is broken by the vev of additional scalar boson σ at $O(1-10)\text{TeV}$, M_{DM} is given by this vev through $y_{\text{DM}} \bar{\Psi} \Psi \sigma$ coupling.



1.Introduction

WIMP dark matter

- WIMP dark matter mass:

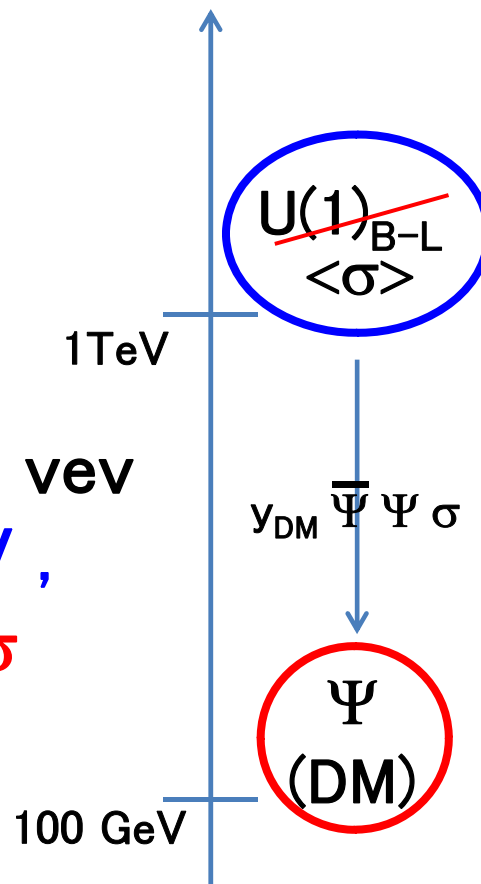
$$M_{\text{DM}} \sim O(100-1000)\text{GeV}$$



What is the origin of M_{DM} ?

If $U(1)_{\text{B-L}}$ gauge symmetry is broken by the vev of additional scalar boson σ at $O(1-10)\text{TeV}$,

M_{DM} is given by this vev through $y_{\text{DM}} \bar{\Psi} \Psi \sigma$ coupling.



Dark matter and neutrino masses could be naturally explain by TeV scale physics with $U(1)_{\text{B-L}}$ gauge symmetry.

2. Model

• $SU(3)_C \times SU(2)_I \times U(1)_Y \times U(1)_{B-L}$

	s	η	$(\Psi_R)_i$	$(\Psi_L)_i$	$(\nu_R)_i$	σ
$SU(2)_I$	<u>1</u>	<u>2</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>
$U(1)_Y$	0	1/2	0	0	0	0
$U(1)_{B-L}$	1/2	1/2	-1/2	3/2	1	2

• New matter particle:

- B-L Higgs scalar σ

- Right handed neutrinos $\nu_R^{1,2}$

- $SU(2)_I$ singlet scalar s

- $SU(2)_I$ doublet scalar η

- Chiral fermion $\Psi_{R,L}^{1,2}$



Half unit of
 $U(1)_{B-L}$ charge
 $\rightarrow U(1)_{DM}$

$U(1)_{B-L}$ protect: Tree-level $L\phi_{SM}\nu_R$
 Majorana mass of ν_R
 Dirac mass of Ψ

2. Model

$U(1)_{B-L}$ symmetry breaking

▪ ν_R , Ψ_R and Ψ_L

$$\mathcal{L}_{\text{Yukawa}} = - (y_R)_i (\nu_R)_i^c (\nu_R)_i (\sigma^0)^* - (y_\Psi)_i \overline{(\Psi_R)_i} (\Psi_L)_i (\sigma^0)^*$$

$$\rightarrow \frac{(M_R)_{ii}}{2} = (y_R)_{ii} \frac{v_\sigma}{\sqrt{2}}, \quad (M_\Psi)_{ii} = (y_\Psi)_{ii} \frac{v_\sigma}{\sqrt{2}} \quad \leftarrow \text{tree level}$$

Electroweak symmetry breaking

▪ ϕ , σ , s and η → Physical state: h, H, S_1, S_2, η^\pm

$$\begin{pmatrix} h^0 \\ H^0 \end{pmatrix} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \phi_r^0 \\ \sigma_r^0 \end{pmatrix}, \quad \begin{pmatrix} s_1^0 \\ s_2^0 \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \eta^0 \\ s^0 \end{pmatrix}$$

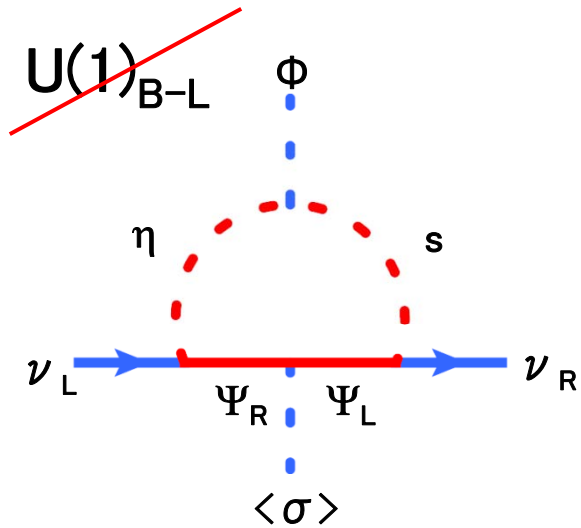
Global $U(1)_{DM}$ remains after $U(1)_{B-L}$ gauge symmetry breaking.

We assume that the Ψ_1 is the lightest $U(1)_{DM}$ particle.

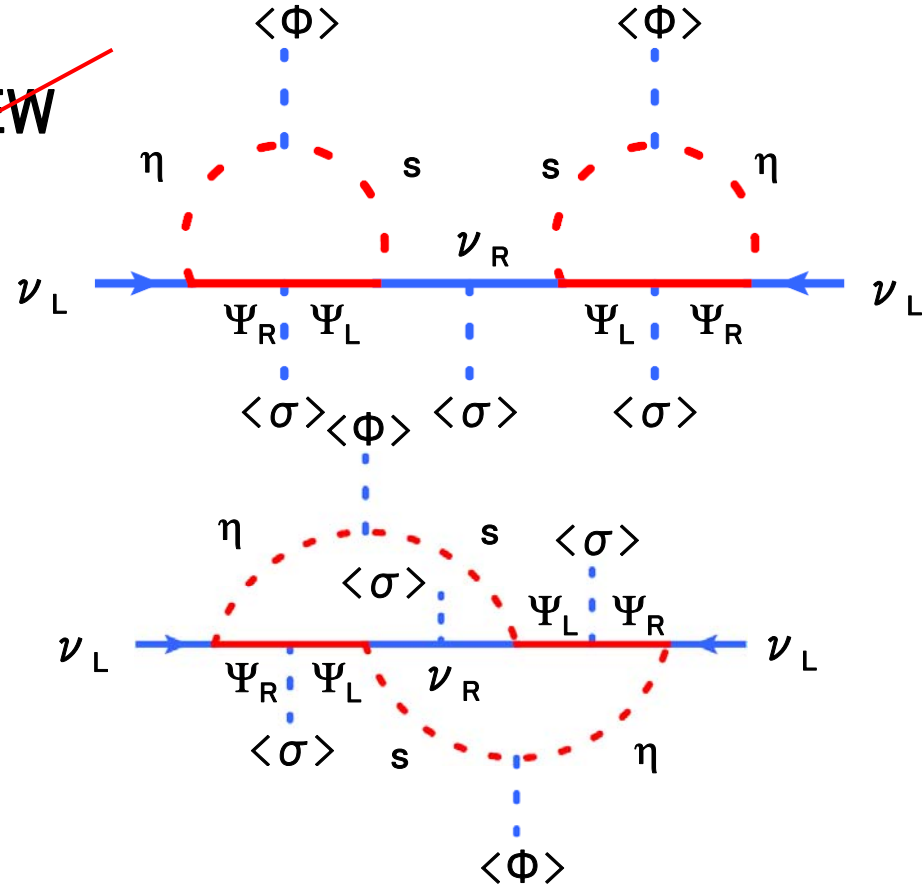
$U(1)_{B-L}$: Neutrino masses
The dark matter mass
Stability of the dark matter

2. Model

Neutrino masses



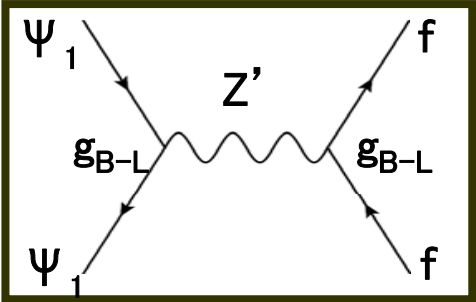
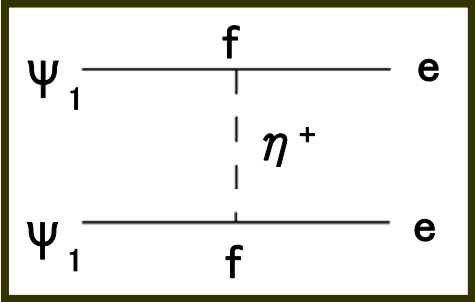
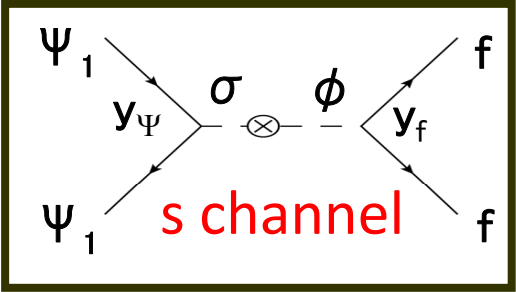
EW



The $O(0.1)$ eV neutrino masses can be naturally deduced from TeV scale physics with $O(0.01-0.1)$ coupling constant

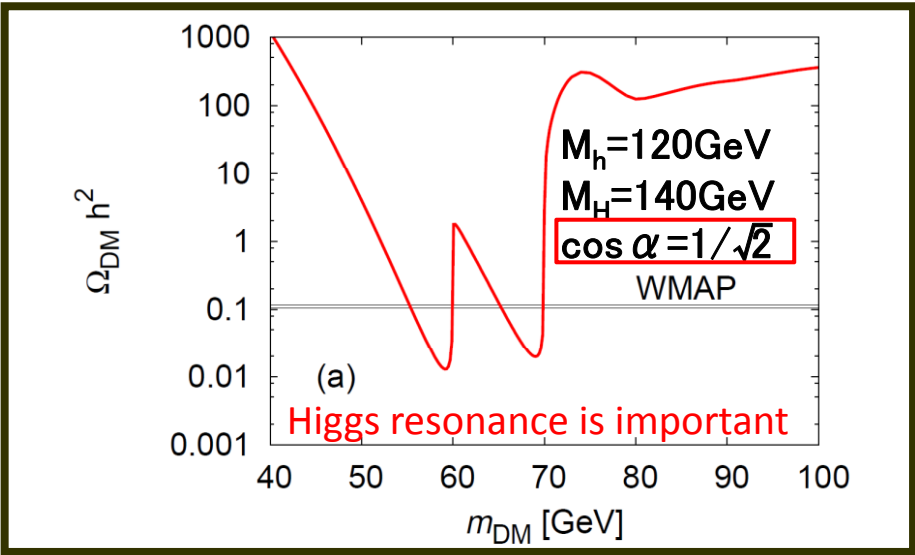
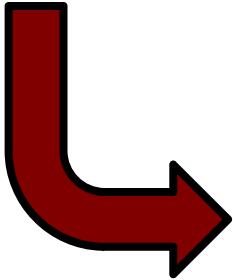
2.Model

Abundance of Ψ_1



constraint by $\mu \rightarrow e \gamma$

Z' is heavy

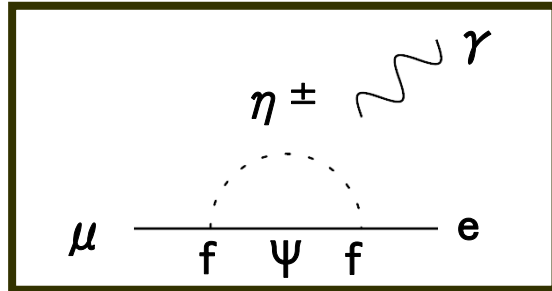


Okada and Seto (2010)
 Kanemura, Seto and Shimomura (2011)

Maximal mixing between σ and ϕ is required!

2. Model

LFV constraint



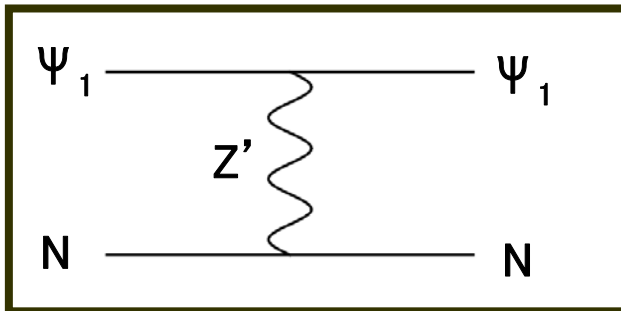
$$BR(\mu \rightarrow e\gamma) = \frac{3\alpha_{\text{em}}}{64\pi G_F^2} \left| \frac{1}{M_{\eta^\pm}^2} f_{\mu i} F_2 \left(\frac{(M_\Psi)_i^2}{M_{\eta^\pm}^2} \right) (f^\dagger)_{ie} \right|^2,$$

$$F_2(a) \equiv \frac{1 - 6a + 3a^2 + 2a^3 - 6a^2 \ln(a)}{6(1-a)^4}.$$

Experimental bound(MEG): $BR(\mu \rightarrow e, \gamma) < 2.4 \times 10^{-12}$

J. Adam et al.(2011)

Direct detection of Ψ^1



$$\sigma(\Psi_1 N \rightarrow \Psi_1 N) \simeq \left(\frac{g_{B-L}}{m_{Z'}} \right)^4 \frac{m_{\Psi_1}^2 m_N^2}{4\pi(m_{\Psi_1} + m_N)^2}.$$

Experimental bound(XENON100): $\sigma(\Psi_1 N \rightarrow \Psi_1 N) < 8 \times 10^{-45} \text{cm}^2$

E. Aprile et al. (2011)

Consistent with current experimental bound.

2.Model

Parameter set

- neutrino oscillation
- LFV
- LEP
- DM abundance
- DM direct detection

Normal Hierarchy, Tri-bi maximal

(Our results are **not sensitive to value of θ_{13}**)

$$f_{ij} = \begin{pmatrix} 0.0757 & 0.0445 \\ 0.01 & -0.0123 \\ -0.141 & -0.0723 \end{pmatrix} \quad h_{ij} = \begin{pmatrix} -0.131 & 0.1 \\ 0.1 & 0.1 \end{pmatrix}$$

$$M_R = 250 \text{ GeV}, \quad M_{\psi_1} = 57.0 \text{ GeV}, \quad M_{\psi_2} = 800 \text{ GeV}$$

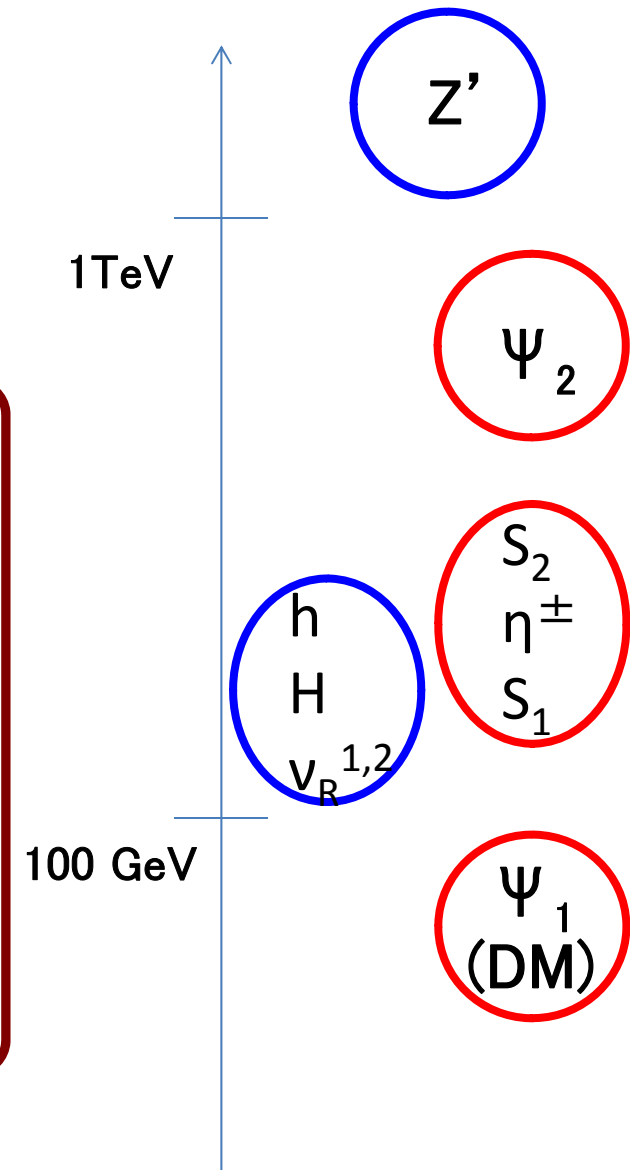
$$M_{S_1} = 200 \text{ GeV}, \quad M_{S_2} = 300 \text{ GeV},$$

$$M_h = 120 \text{ GeV}, \quad M_H = 140 \text{ GeV},$$

$$M_{\eta^\pm} = 280 \text{ GeV}, \quad \cos \theta = 0.05, \quad \cos \alpha = 1/\sqrt{2},$$

$$g_{B-L} = 0.2, \quad M_{Z'} = 2000 \text{ GeV}, \quad v_\phi = 246 \text{ GeV}, \quad v_\sigma = 5 \text{ TeV}$$

All coupling constant are **$O(0.01-0.1)$** and
all masses are **$O(100-1000)$ GeV**.



3. Physics at the LHC

Physics of Z'

Z' mass: $O(1-10)\text{TeV}$

$\Gamma(Z' \rightarrow XX) \propto (\text{B-L charge})^2$

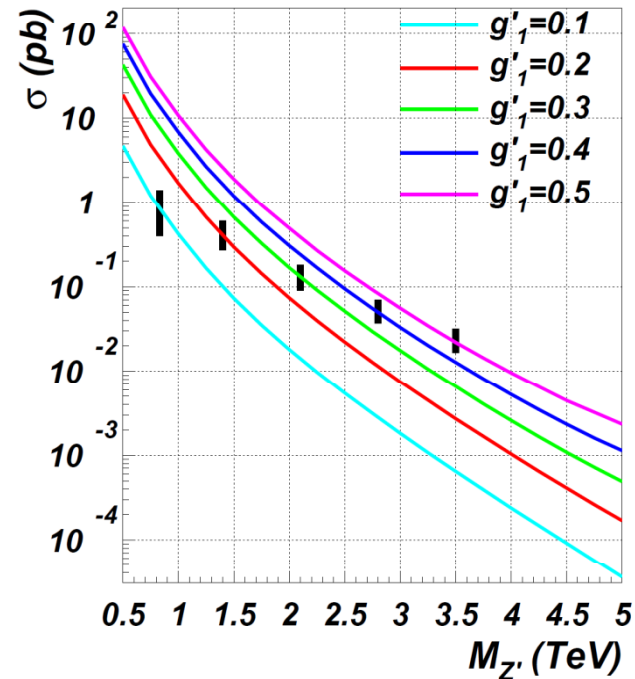
Z' decay into

invisible about 30%

Z' production cross section is **70 pb**
at the LHC for $\sqrt{s} = 14 \text{ TeV}$,
 $M_{Z'} = 2000 \text{ GeV}$ and $g_{B-L} = 0.2$

Our model could be tested
by **measuring decay of the Z'**
at the LHC.

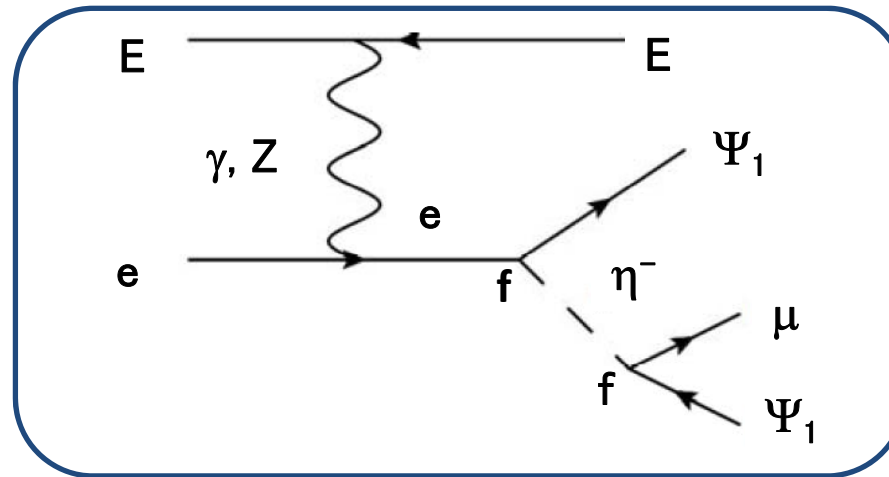
However, if Z' mass is heavy,
our model would be difficult to be tested at the LHC.



L. Basso, A. Belyaev, S. Moretti and
C. H. Shepherd-Themistocleous (2009);
L. Basso (2011)

4. Physics at the ILC

Physics of Ψ_1



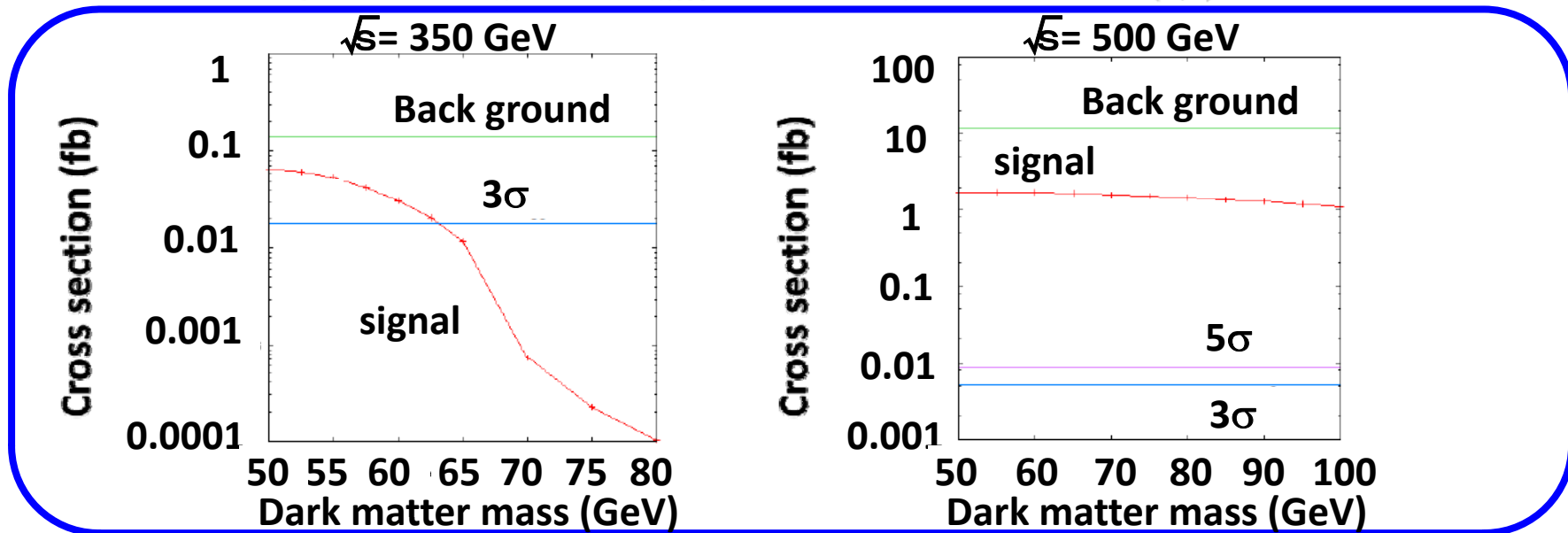
1. In our model, **dark matter and electron are coupled via the $L\psi\eta$ coupling (f)**.
2. The energy momentum conservation is used to detect the dark matter.
3. Background are **$e, E \rightarrow e, \mu, \cancel{p}$** processes.

4. Physics at the ILC

The cross section of the signal is very low in this case.
The kinematical cuts to reduce B.G.

$$-0.8 < \cos(\mu) < 0.8, \quad E_\mu > 80\text{GeV},$$

$$E_e < 120\text{GeV}, \quad M_{\text{miss}} > 120\text{GeV}, \quad -0.8 < \cos(e\mu) < 0.8.$$

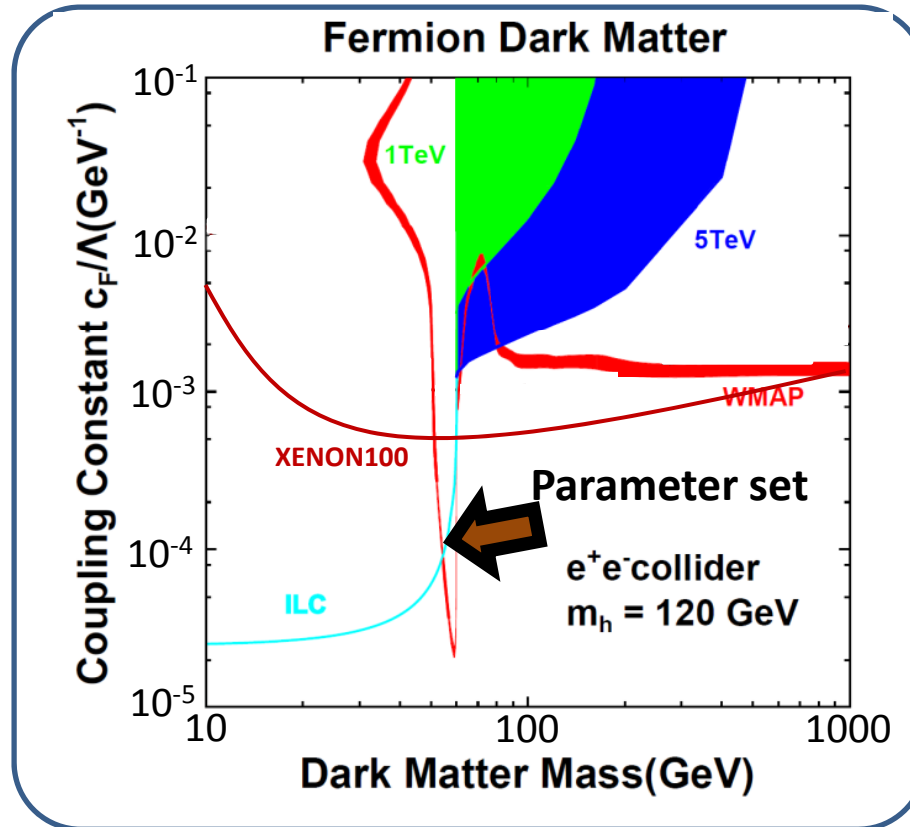


Dark matter can be tested **with 1ab^{-1} data:**

at the $\sqrt{s} = 350\text{GeV}$ collider for $M_{\text{DM}} \lesssim 63$ GeV at 3σ C.L.

at the $\sqrt{s} = 500\text{GeV}$ collider at 5σ C.L.

4. Physics at the ILC

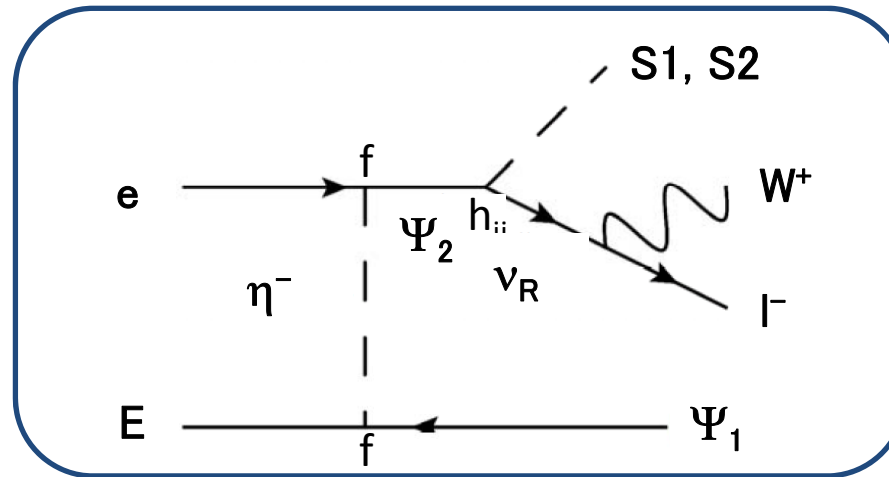


S.Kanemura, S.Matsumoto,
TN, H.Taniguchi (2011).

Ψ_1 would be tested by invisible decay of h
at $\sqrt{s}=350 \text{ GeV}$ with 500fb^{-1} at 3σ C.L.

4. Physics at the ILC

Physics of ν_R



1. In our parameter set, $\nu_R \rightarrow W^\pm, l^\mp$ is main decay mode.
2. We consider $W \rightarrow \text{jet}, \text{jet}$ process.
3. Background are $e, E \rightarrow e$ (or μ), $W, \cancel{\nu}$ processes.

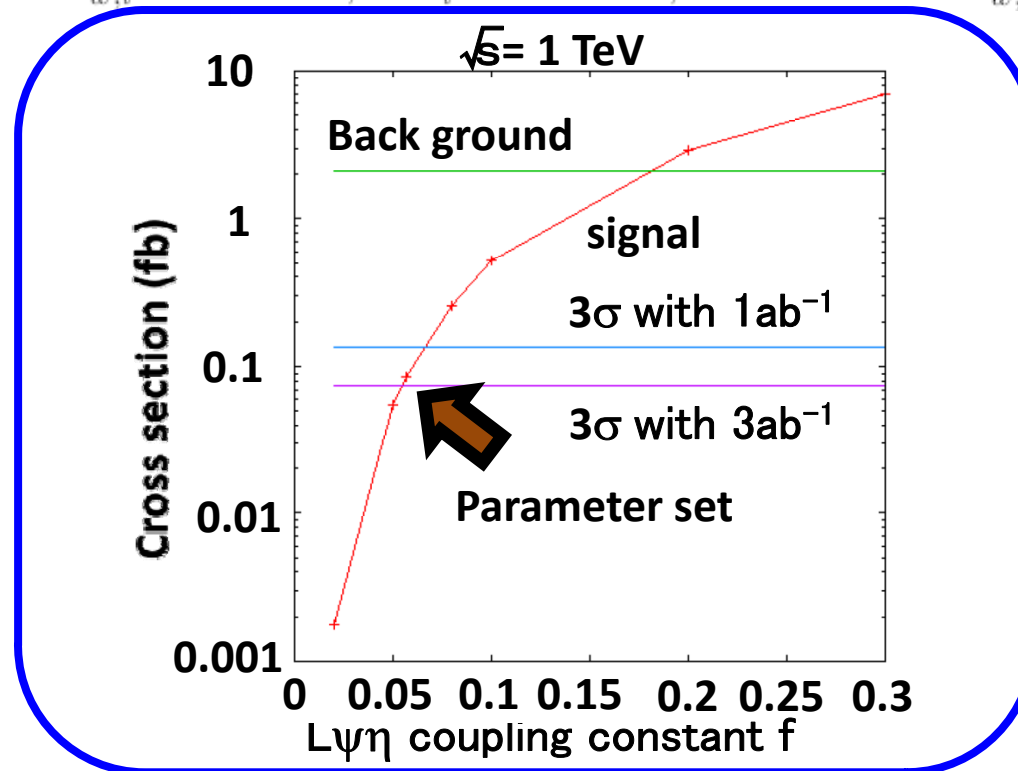
4. Physics at the ILC

The cross section of the signal is very low in this case.

The kinematical cuts to reduce B.G.

$$-0.95 < \cos(\theta) < 0.95, \quad 200\text{GeV} < M_{\text{miss}} < 600\text{GeV},$$

$$240\text{GeV} < M_{w,l} < 260\text{GeV}, \quad E_l < 300\text{GeV}, \quad 300\text{GeV} < E_{w,l} < 600\text{GeV}.$$



Right handed neutrino can be tested at 3σ C.L.
at the $\sqrt{s} = 1 \text{ TeV}$ collider with 3 ab^{-1} data.

Most optimistic case

LHC

Z'_{B-L} is detected at the LHC



ILC

- 350 GeV – 500 GeV (also 1 TeV)
e, μ with missing momentum
→ Dark matter which is directly coupled to charged lepton is detected.
- 1 TeV
e, W with Missing momentum
→ O(100) GeV right handed neutrino is detected.



Radiative seesaw model with B-L gauge symmetry which include unstable right handed neutrino exist at TeV scale.

5. Conclusion

- ① We consider possibility of testing the TeV-scale seesaw model in which $U(1)_{B-L}$ gauge symmetry is the common origin of neutrino masses, the dark matter mass, and stability of the dark matter.
- ② Z' boson could be tested at the LHC.
- ③ Dark matter Ψ_1 can be tested with 1 ab^{-1} data:
at $\sqrt{s} = 350 \text{ GeV}$ ILC with $M_{DM} \lesssim 63 \text{ GeV}$ at 3σ C.L.
at $\sqrt{s} = 500 \text{ GeV}$ ILC at 5σ C.L.
- ⑤ Right handed neutrino could be tested at 3σ C.L.
at $\sqrt{s} = 1 \text{ TeV}$ ILC with 3 ab^{-1} data.
- ⑥ ILC have potential to distinguish $U(1)_{B-L}$ models.

Back up

2.Model

$U(1)_{B-L}$ anomaly

Our model focus to explain TeV scale physics.



$U(1)_{B-L}$ anomaly would be resolved by some heavy singlet fermions with appropriate B-L charge.

For example;

Right hand: $1 \times 9, -1/2 \times 14, 1/3 \times 9$

left hand: $3/2 \times 14, -5/3 \times 9$



$U(1)_{B-L}$ anomaly is not serious

Lagrangian

$U(1)_{B-L}$ breaking

$$\begin{aligned}
 \mathcal{L}_{\text{int}} = & \mathcal{L}_{\text{SMYukawa}} - \{(y_R)_{ij}(\bar{\nu}_R^c)_i(\nu_R)_j\sigma + h.c.\} - \{(y_\Psi)_i(\bar{\Psi}_R)_i(\Psi_L)_i\sigma + h.c.\} \\
 & - (h_{ij}(\bar{\Psi}_L)_i(\nu_R)_j s + h.c.) - (f_{ij}(\bar{L}_L)_i(\Psi_R)_j\eta^c + h.c.) - \{(y_3)_{ij}(\bar{\nu}_R^c)_i(\Psi_R)_j s^* + h.c.\} \\
 & - \mu_\phi^2 \Phi^\dagger \Phi + \mu_s^2 s^\dagger s + \mu_\eta^2 \eta^\dagger \eta - \mu_\sigma^2 \sigma^\dagger \sigma + \lambda (\Phi^\dagger \Phi)^2 + \lambda_1 (s^\dagger s)^2 + \lambda_2 (\eta^\dagger \eta)^2 + \lambda_3 (\sigma^\dagger \sigma)^2 \\
 & + \lambda_4 s^\dagger s \eta^\dagger \eta + \lambda_5 s^\dagger s \Phi^\dagger \Phi + \lambda_6 \eta^\dagger \eta \Phi^\dagger \Phi + \lambda_7 \eta^\dagger \eta \sigma^\dagger \sigma \\
 & + \lambda_8 s^\dagger s \sigma^\dagger \sigma + \lambda_9 \eta^\dagger \eta \sigma^\dagger \sigma + \lambda_{10} \Phi^\dagger \Phi \sigma^\dagger \sigma + (\mu s \eta^\dagger \Phi + h.c.).
 \end{aligned}$$

~~$U(1)_{B-L}$~~

$$\frac{(M_R)_{ii}}{2} = (y_R)_{ii} \frac{v_\sigma}{\sqrt{2}}, \quad (M_\Psi)_{ii} = (y_\Psi)_{ii} \frac{v_\sigma}{\sqrt{2}}, \quad M_{Z'}^2 = 4g_{B-L}^2 v_\sigma^2$$

Remnant global $U(1)_{DM}$ remains on **half unit of $U(1)_{B-L}$ charged particles** after SSB of $U(1)_{B-L}$.

$U(1)_{DM}$ guarantee stability of dark matter.

We consider that the Ψ^1 is lightest $U(1)_{DM}$ particle case.

