

# **A model for the Higgs inflation and its testability at the ILC**

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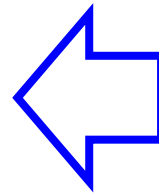
**LCWS12: 23 Oct. 2012**

# 1.Introduction

## Why we need an inflation?

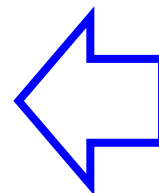
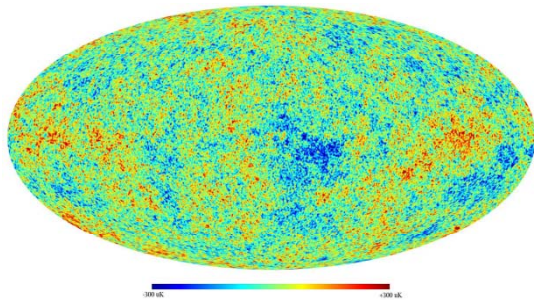
- The flatness problem

$$\Omega_0 = 1.002 \pm 0.011$$
$$|\Omega_p - 1| \lesssim O(10^{-60})$$



The Universe is flat  
but the standard cosmology  
cannot explain this flatness.

- The horizon problem



The temperature of the CMB  
is almost the same value but  
light cone cover less than  $2^\circ$

These problems can be solved by exponential expansion.

# 1.Introduction

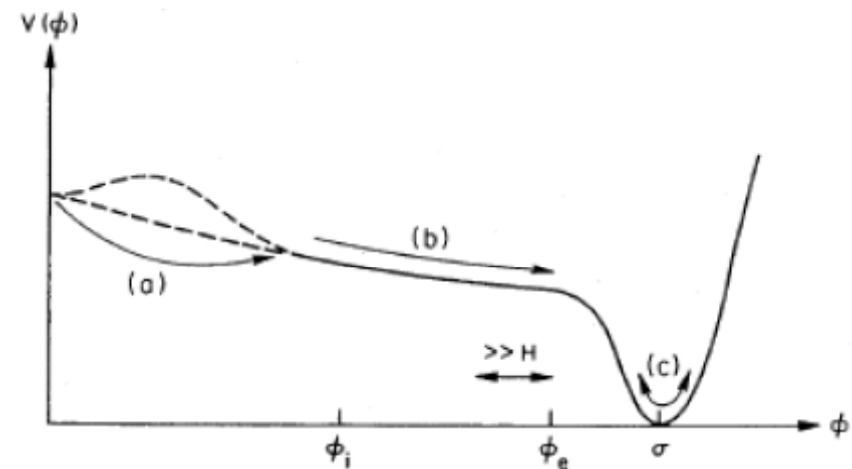
## Inflation

We introduce a real scalar  $\phi$

$$\mathcal{L} = \frac{1}{2}\dot{\phi}^2 - V(\phi)$$



$$H^2 = \frac{V}{3M_P^2} \quad \left( H = \frac{\dot{a}}{a} \right)$$



If  $H$  is a constant, **The Universe expands by exponential.**



$$\varepsilon \equiv \frac{1}{2} M_P^2 (V'/V)^2 \ll 1 \quad \eta \equiv M_P^2 V''/V \ll 1$$

**If potential satisfies the slow-roll condition,  
 $\phi$  can act as an inflaton.**

# 2.Higgs inflation

Inflaton = Higgs

- Higgs boson mass ( $m_h=126\text{GeV}$ )
- Slow-roll condition ( $\epsilon, \eta$ )
- CMB temperature fluctuations ( $P_R$ )

$$\epsilon \equiv \frac{1}{2} M_P^2 (V'/V)^2 \ll 1$$

$$\eta \equiv M_P^2 V''/V \ll 1$$

$$L_{\text{tot}} = L_{\text{SM}} - \frac{M^2}{2} R - \xi H^\dagger H R$$

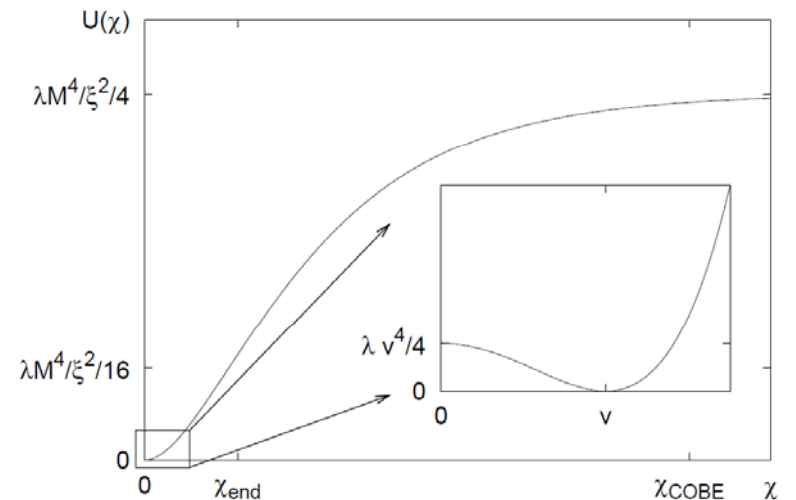
$$V(\chi) = \left( 1 + \exp\left(-\frac{2\chi}{\sqrt{6}M_P}\right) \right)^{-2}$$

$$\left( \frac{d\chi}{dh} = \sqrt{\frac{\Omega^2 + 6\xi^2 h^2/M_P^2}{\Omega^4}} \right)$$

WMAP:

$$P_R = 2.430 \pm 0.091 \times 10^{-9}$$

$$\Rightarrow \xi = 5 \times 10^4 \sqrt{\lambda}$$



Bezrukov and Shaposhnikov (2008)

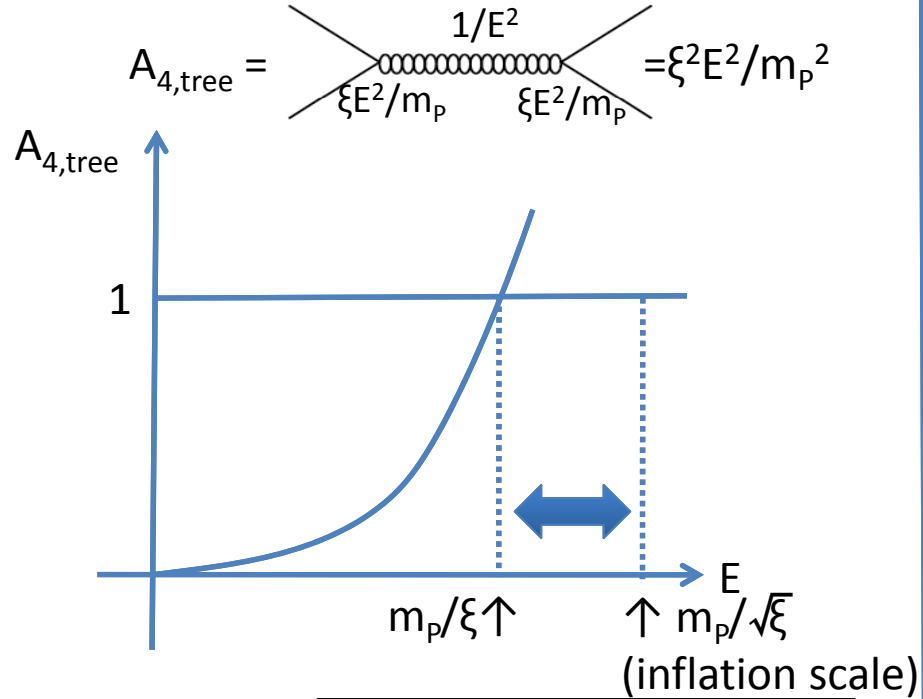
SM-Higgs satisfies  $\epsilon, \eta$  and  $P_R$  !

**But!**

# Problems in the simplest case

## ( I ) Unitarity

T. Han and S. Willenbrock, Phys. Lett. B 616, 215 (2005)

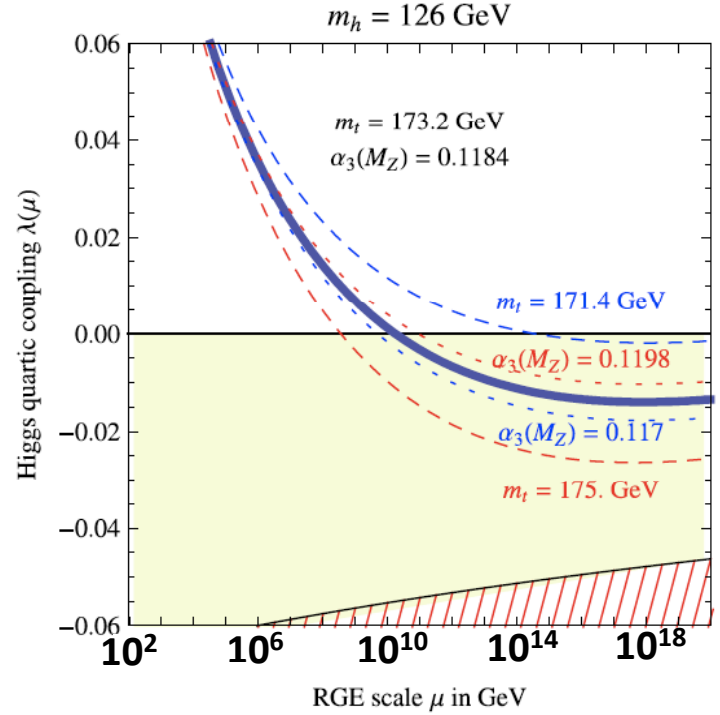


$$\xi = O(10^4) \Rightarrow \Lambda \sim m_p / \xi$$

Unitarity is broken at  $O(10^{15})$  GeV

## ( II ) Vacuum stability

J. Elias-Miro et al, Phys. Lett. B 709, 222 (2012)



$$m_h = 126 \text{ GeV} \Rightarrow \Lambda \sim 10^{10} \text{ GeV}$$

Vacuum cannot be stabilized at  $O(10^{10})$  GeV

**⇒ Simplest Higgs inflation cannot reach to the inflation scale**

# Solutions for the problems

## ( I ) Unitarity

G.F.Giudice, H.M.Lee, PLB694, 294(2011)

We add a heavy scalar particle saving unitarity.

## ( II ) Vacuum stability $\Rightarrow$ **Extended Higgs sector.**

• Renormalization group equations

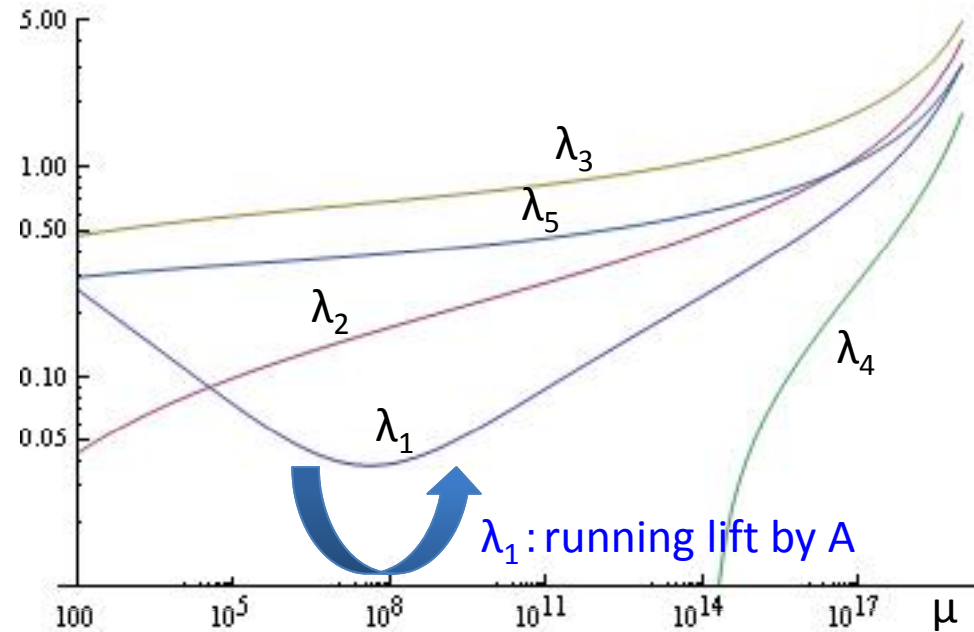
$$16\pi^2\mu \frac{d\lambda_1}{d\mu} \sim 12\lambda_1^2 - 12y_t^4 + \underline{A}$$

**The new bosonic loop  
cancel the  $y_t$  effect!**

2HDM

$$A = 2\lambda_3^2 + 2(\lambda_3 + \lambda_4)^2 + 2\lambda_5^2 > 0$$

S.Kanemura, T.Kasai, Y.Okada, Phys.Lett. B471 (1999)



$m_h=126\text{GeV}, m_t=173.5\text{GeV}$

# The inert doublet model

$$\begin{aligned}
 V = & \frac{M_P R}{2} + (\xi_1 |\Phi_1|^2 + \xi_2 |\Phi_2|^2) R \\
 & + \mu_1^2 |\Phi_1|^2 + \mu_2^2 |\Phi_2|^2 + \frac{1}{2} \lambda_1 |\Phi_1|^4 + \frac{1}{2} \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 \\
 & + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \left[ \frac{1}{2} \lambda_5 ((\Phi_1^\dagger \Phi_2)^2) \right]
 \end{aligned}$$

Gong, Lee and Kang (2012)

$$\begin{aligned}
 \Phi_1 &= (\phi^+, \phi^0) \\
 \Phi_2 &= [H^+, (H^0 + iA^0)/\sqrt{2}]
 \end{aligned}$$

$$m_h^2 = \lambda_1 v^2$$

$$m_{H^\pm}^2 = \mu_2^2 + \frac{1}{2} \lambda_3 v^2$$

$$m_H^2 = \mu_2^2 + \frac{1}{2} (\lambda_3 + \lambda_4 + \lambda_5) v^2$$

$$m_A^2 = \mu_2^2 + \frac{1}{2} (\lambda_3 + \lambda_4 - \lambda_5) v^2$$

## Vacuum stability:

$$\lambda_1 > 0, \quad \lambda_2 > 0, \quad \lambda_3 + \lambda_4 + \lambda_5 + \sqrt{\lambda_1 \lambda_2} > 0$$

## Inflaton condition:

$$\lambda_2 \xi_1 - (\lambda_3 + \lambda_4) \xi_2 > 0$$

$$\lambda_1 \xi_2 - (\lambda_3 + \lambda_4) \xi_1 > 0$$

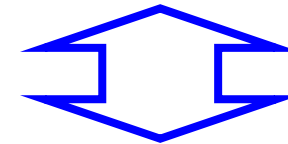
$$\lambda_1 \lambda_2 - (\lambda_3 + \lambda_4)^2 > 0$$

## CMB temperature fluctuations: $a \equiv \xi_1 / \xi_2$

$$\xi_2 \sqrt{\frac{2(\lambda_1 + a^2 \lambda_2 - 2a(\lambda_3 + \lambda_4))}{\lambda_1 \lambda_2 - (\lambda_3 + \lambda_4)^2}} \simeq 5 \times 10^4$$

$$\frac{\lambda_5}{\xi_2} \frac{a \lambda_2 - (\lambda_3 + \lambda_4)}{\lambda_1 + a^2 \lambda_2 - a(\lambda_3 + \lambda_4)} \leq 4 \times 10^{-12}$$

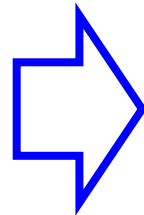
Inflation can be explained



Dark matter and neutrino masses cannot be explained.

# 3. Our Model

Inert +  $v_R$

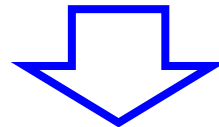


Our model can explain:

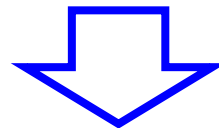
Inflation (inert doublet model)

Neutrino masses (radiative seesaw)

Dark matter (CP-odd higgs A)



The mass spectrum is almost determined from the current data.



Our model can be tested by measuring model parameters at collider experiments



# 3. Our Model

## Inflation

$$V = \frac{M_{Pl}^2}{2} + (\xi_1 |\Phi_1|^2 + \xi_2 |\Phi_2|^2) R + \mu_1^2 |\Phi_1|^2 + \mu_2^2 |\Phi_2|^2 + \frac{1}{2} \lambda_1 |\Phi_1|^4 + \frac{1}{2} \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \left[ \frac{1}{2} \lambda_5 ((\Phi_1^\dagger \Phi_2)^2) \right]$$

**Vacuum stability:**

$$\lambda_1 > 0, \quad \lambda_2 > 0, \quad \lambda_3 + \lambda_4 + \lambda_5 + \sqrt{\lambda_1 \lambda_2} > 0$$

**Inflaton condition:**

$$\lambda_2 \xi_1 - (\lambda_3 + \lambda_4) \xi_2 > 0$$

$$\lambda_1 \xi_2 - (\lambda_3 + \lambda_4) \xi_1 > 0$$

$$\lambda_1 \lambda_2 - (\lambda_3 + \lambda_4)^2 > 0$$

**CMB temperature fluctuations:**

$$\xi_2 \sqrt{\frac{2(\lambda_1 + a^2 \lambda_2 - 2a(\lambda_3 + \lambda_4))}{\lambda_1 \lambda_2 - (\lambda_3 + \lambda_4)^2}} \quad a \equiv \xi_1 / \xi_2 \quad \simeq 5 \times 10^4$$

$$\frac{\lambda_5}{\xi_2} \frac{a \lambda_2 - (\lambda_3 + \lambda_4)}{\lambda_1 + a^2 \lambda_2 - a(\lambda_3 + \lambda_4)} \leq 4 \times 10^{-12}$$

# 3. Our Model

## Inflation

$$V = \frac{M_{Pl}^2 R^2}{2} + (\xi_1 |\Phi_1|^2 + \xi_2 |\Phi_2|^2) R^2 + \mu_1^2 |\Phi_1|^2 + \mu_2^2 |\Phi_2|^2 + \frac{1}{2} \lambda_1 |\Phi_1|^4 + \frac{1}{2} \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 (\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) + \left[ \frac{1}{2} \lambda_5 ((\Phi_1^\dagger \Phi_2)^2) \right]$$

**Vacuum stability:**

$$\lambda_1 > 0, \quad \lambda_2 > 0, \quad \lambda_3 + \lambda_4 + \lambda_5 + \sqrt{\lambda_1 \lambda_2} > 0$$

**Inflaton condition:**

$$\lambda_2 \xi_1 - (\lambda_3 + \lambda_4) \xi_2 > 0$$

$$\lambda_1 \xi_2 - (\lambda_3 + \lambda_4) \xi_1 > 0$$

$$\lambda_1 \lambda_2 - (\lambda_3 + \lambda_4)^2 > 0$$

**CMB temperature fluctuations:**

$$\xi_2 \sqrt{\frac{2(\lambda_1 + a^2 \lambda_2 - 2a(\lambda_3 + \lambda_4))}{\lambda_1 \lambda_2 - (\lambda_3 + \lambda_4)^2}} \simeq 5 \times 10^4 \quad a \equiv \xi_1 / \xi_2$$

$$\frac{\lambda_5}{\xi_2} \frac{a \lambda_2 - (\lambda_3 + \lambda_4)}{\lambda_1 + a^2 \lambda_2 - a(\lambda_3 + \lambda_4)} \leq 4 \times 10^{-12}$$

$$a \lambda_2 - (\lambda_3 + \lambda_4) \approx 0$$

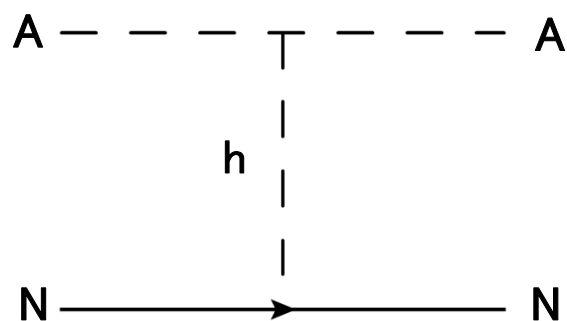
**at the inflation scale**



**$\lambda_5$  becomes a large value**

# 3. Our Model

Dark matter



$$\sigma(AN \rightarrow AN) = \frac{\lambda_{hAA}^2}{4m_h^4} \frac{m_N^2}{\pi(m_A + m_N)^2} f_N^2$$

$$\lambda_{hAA} \equiv \lambda_3 + \lambda_4 - \lambda_5$$

$$f_N \equiv \sum_{q=u,d,s} m_N f_{Tq} + \frac{2}{9} m_N f_{Tg}$$

For vacuum stability bound  $\lambda_1 > 0 \rightarrow \lambda_{3,4,5} \gtrsim \mathcal{O}(0.1)$

$$\lambda_{hAA} = 0.1 \rightarrow \sigma(AN \rightarrow AN) \sim 1.5 \times 10^{-44} \text{ cm}^2$$

(XENON100:  $\sigma(AN \rightarrow AN) < 2 \times 10^{-45} \text{ cm}^2$ )

XENON collaboration (2012)

$$\lambda_3 + \lambda_4 - \lambda_5 \approx \mathcal{O}(0.01) \text{ at } \mathcal{O}(10^2) \text{ GeV}$$

# 3. Our Model

## Mass spectrum

	$10^2 \text{GeV}$	$10^{17} \text{GeV}$
$\lambda_1$	0.262	1.75
$\lambda_2$	0.367	9.00
$\lambda_3$	0.495	7.11
$\lambda_4$	-0.447	-3.16
$\lambda_5$	0.0700	0.116

←  $m_H = 126 \text{GeV}$  (LHC)

← Inflation

← Dark matter (WMAP+XENON100)

$m_h = 126 \text{GeV}$

$m_H = 92.0 \text{GeV}$

$m_{H^\pm} = 141 \text{GeV}$

$m_A = 65.0 \text{GeV}$

$a = 0.4,$

$\xi_2 = 5 \times 10^5,$

$\mu_2^2 \sim 4230 \text{GeV}^2$

$$m_A < m_H (\approx 90 \text{GeV}) < m_h < m_{H^\pm} (\approx 140 \text{GeV})$$

**Our model predicts**

**the mass spectrum of inert scalar bosons !**

# 4. Phenomenology

LHC

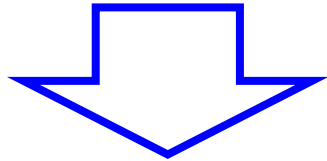
Q.H.Cao, E.Ma, G.Rajasekaran(2007)

$$pp \rightarrow Z^* \rightarrow AH \rightarrow HHZ^* \rightarrow HH\ell^+\ell^-$$

$$15 \text{ GeV} \leq P_T^\ell \leq 40 \text{ GeV} \quad |\eta^\ell| \leq 3.0$$

$$\cos \theta_{\ell\ell} \geq 0.9 \quad \cos \phi_{\ell\ell} \geq 0.9$$

$$E_{Tmiss} \leq 60 \text{ GeV} \quad m_{\ell\ell} \leq 10 \text{ GeV}$$



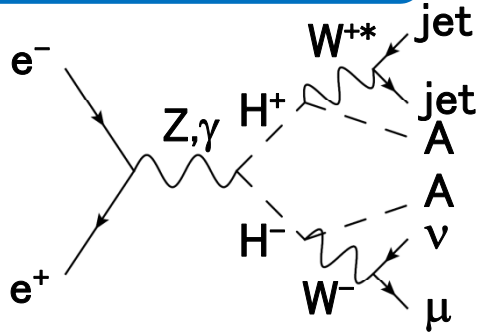
If  $m_A = 65 \text{ GeV}$  and  $m_H$  is large,  
it would be difficult to test  
at the LHC

BKGD	basic	optimal	$m_{\ell\ell} < 10 \text{ GeV}$
WW	$1.1 \times 10^5$	110	62
ZZ	$2.1 \times 10^4$	3	0
total	$1.3 \times 10^5$	113	62

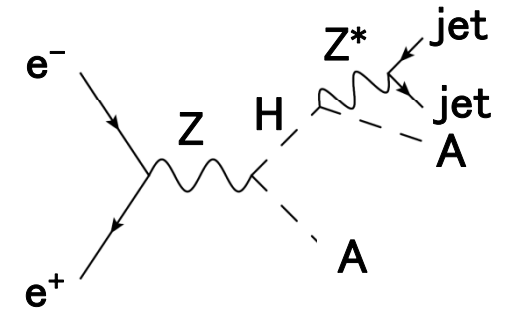
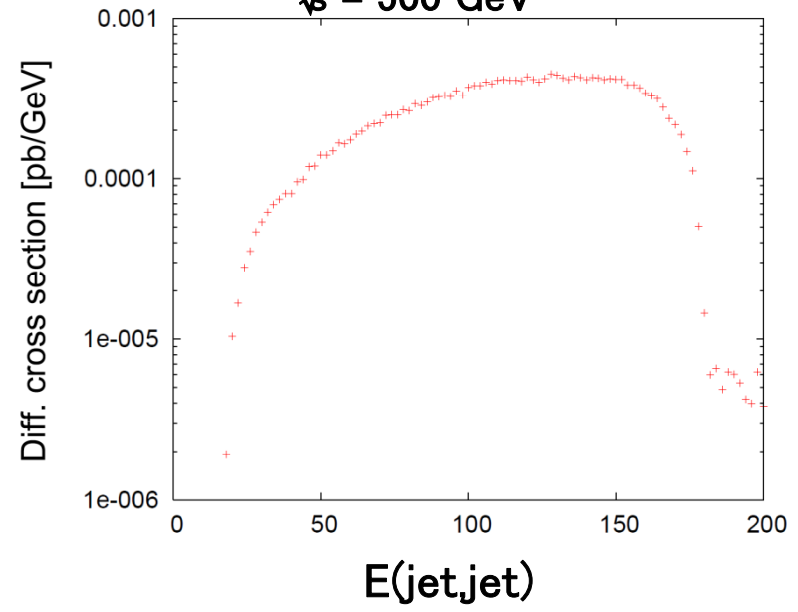
Signal ( $m_{H^0}, m_{A^0}$ )	basic	optimal	$m_{\ell\ell} < 10 \text{ GeV}$
(50, 60)	117	37	37
$S/B$	$9 \times 10^{-4}$	0.33	0.60
$S/\sqrt{B}$	0.32	3.48	4.70
(50, 70)	433	56	50
$S/B$	$3.3 \times 10^{-3}$	0.50	0.81
$S/\sqrt{B}$	1.20	5.27	6.35
(50, 80)	680	38	26
$S/B$	$5.2 \times 10^{-3}$	0.34	0.42
$S/\sqrt{B}$	1.89	3.57	3.3

# 4. Phenomenology

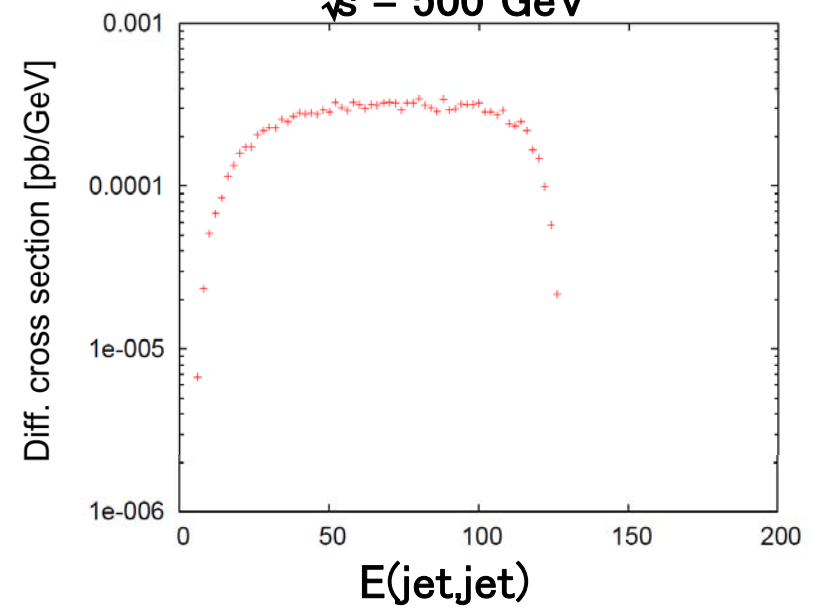
ILC



$\sqrt{s} = 500 \text{ GeV}$

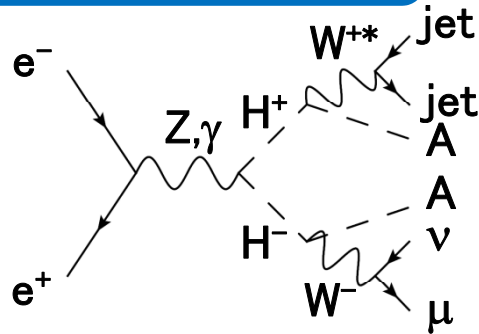


$\sqrt{s} = 500 \text{ GeV}$

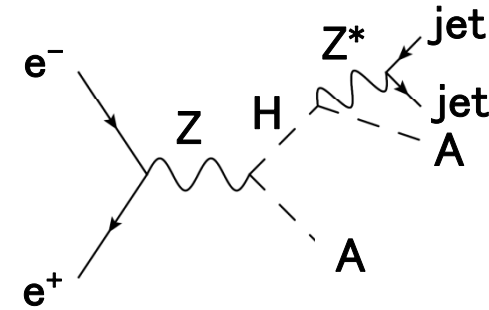
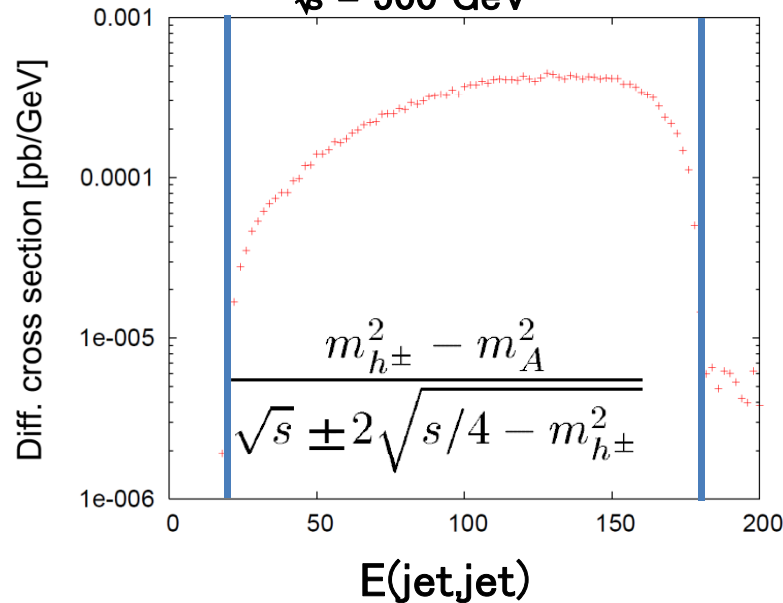


# 4. Phenomenology

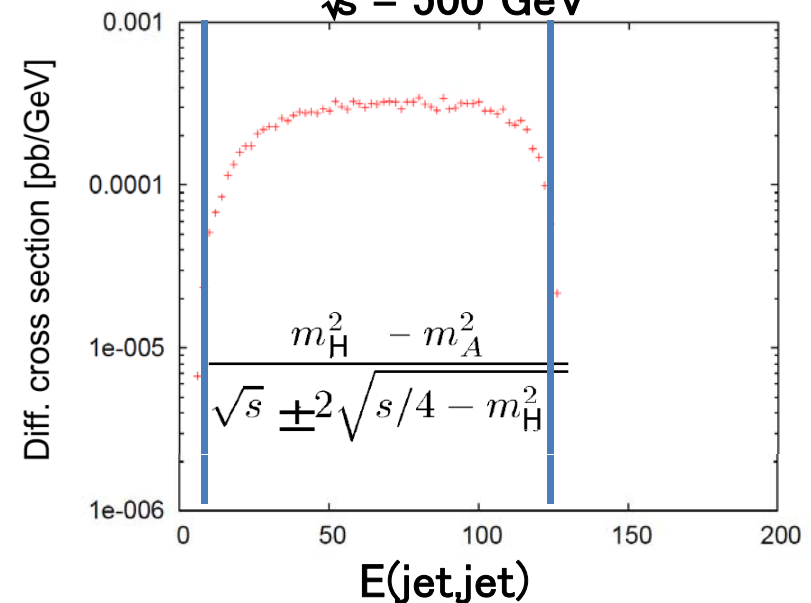
ILC



$\sqrt{s} = 500 \text{ GeV}$



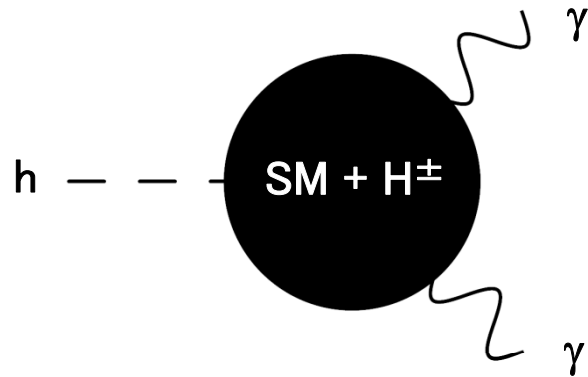
$\sqrt{s} = 500 \text{ GeV}$



The mass spectrum of inert scalar bosons could be measured at the ILC

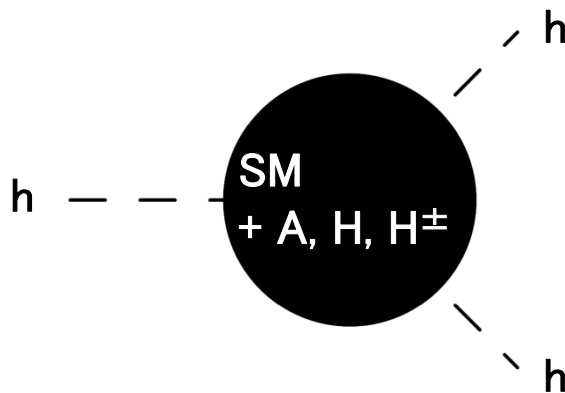
# 4. Phenomenology

h to  $\gamma\gamma$



$$\frac{BR[h_1 \rightarrow \gamma\gamma]}{BR[h_{SM} \rightarrow \gamma\gamma]} \approx 0.982$$

$\lambda_{hhh}$



$$\frac{\lambda_{hhh} - \lambda_{hhh}^{SM}}{\lambda_{hhh}^{SM}} \approx 0.0118$$



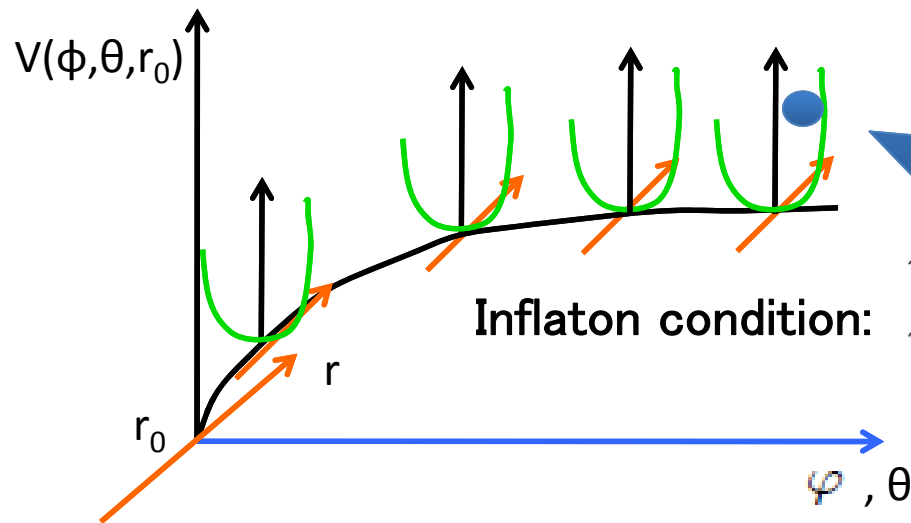
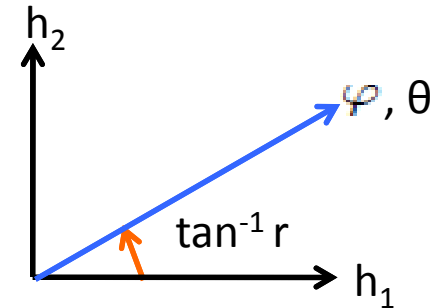
# 5. Conclusion

- ① We consider the case of the Higgs inflation.
- ② It is difficult that SM act as the inflation
- ③ We show that inflation, dark matter and neutrino masses can be explained simultaneously by the inert doublet with right handed neutrinos.
- ④ **Our model predicts mass spectrum of inert scalar boson.**
- ⑤ **Mass spectrum of inert scalar boson could be tested at the ILC.**
- ⑥ **If Higgs and inert doublet components act as an inflaton, this case could be tested at the ILC.**

Back up

# Inflation of inert doublet model

$$\begin{cases} \Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ h_1 \end{pmatrix} \\ \Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ h_2 e^{i\theta} \end{pmatrix} \end{cases} \rightarrow \begin{cases} r = \frac{h_2}{h_1} \\ \varphi = \sqrt{\frac{3}{2}} \log(1 + \xi_1 h_1^2 + \xi_2 h_2^2) \end{cases}$$



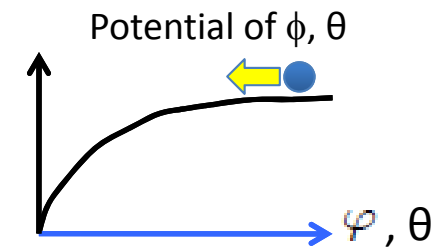
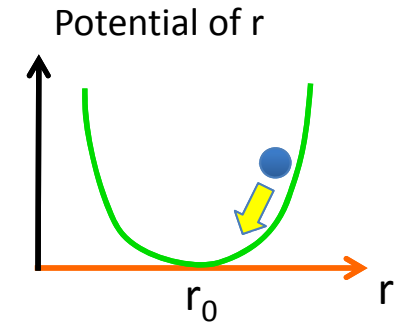
Start point of inflaton

$$\lambda_2 \xi_1 - (\lambda_3 + \lambda_4) \xi_2 > 0$$

$$\lambda_1 \xi_2 - (\lambda_3 + \lambda_4) \xi_1 > 0$$

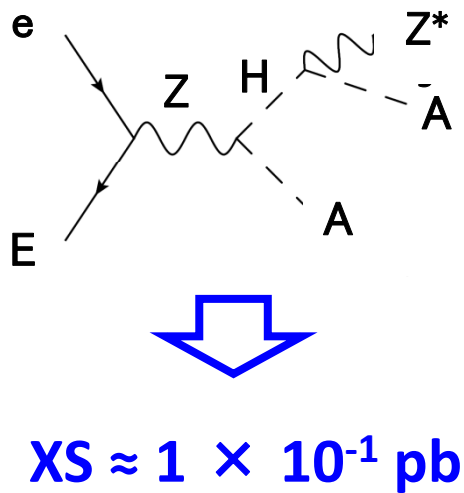
$$\lambda_1 \lambda_2 - (\lambda_3 + \lambda_4)^2 > 0$$

Inflaton condition:

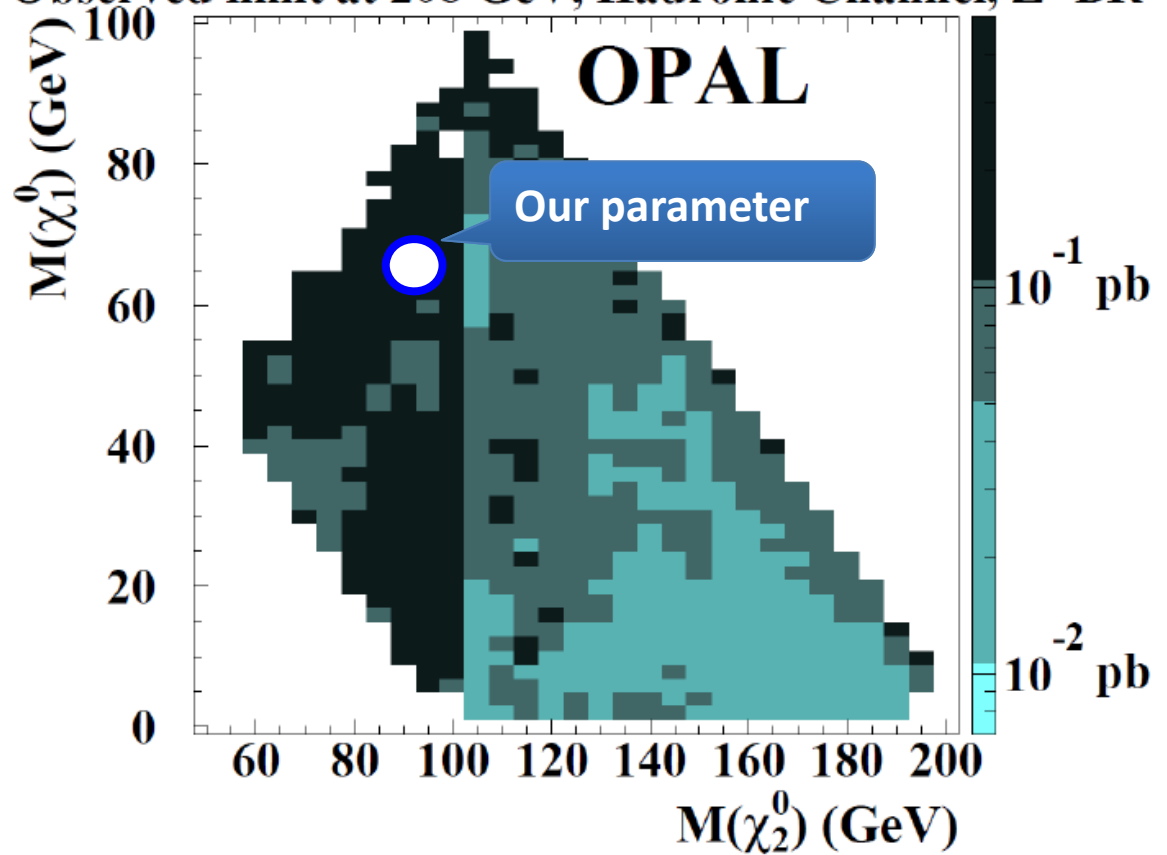


Inflation is happened on minimum value of  $r$

# LEP bound

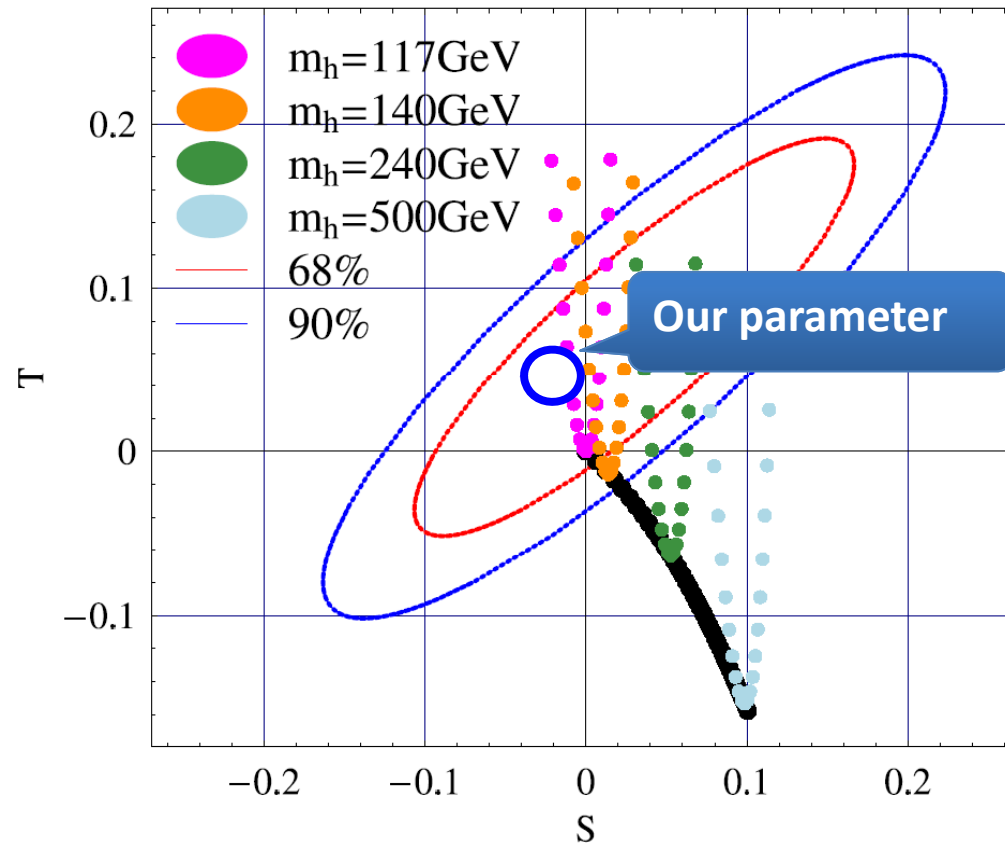


Observed limit at 208 GeV, Hadronic Channel,  $Z^0$  BR



**Our parameter consistent with LEP bound**

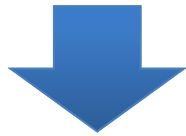
# LEP bound



**Our parameter consistent with LEP bound**

# 3.Our model

Inert +  $\nu_R$



- Inflation
- Dark matter
- neutrino masses

Ma model

$$m_\nu = \frac{\lambda_5 v^2 y_n^2}{8\pi^2 M} \left( \ln \frac{M^2}{m_0^2} - 1 \right)$$

M:majorana mass of  $N_k$   
 $m_0$ :mass of inert higgs ( $\eta^0$ )

E. Ma, Phys. Rev. D **73**, 077301 (2006)

**Our model can explain these problem  
 and would be tested at collider experiments**