



HIGGS SELF COUPLING ANALYSIS USING THE EVENTS CONTAINING $H \rightarrow WW^*$ DECAY

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ECFA LC 2013, 05/27/2013-05/31/2013

INTRODUCTION

- Measuring the Higgs self coupling is the key point to prove the electroweak symmetry breaking mechanism
 - Higgs potential in SM:

$$V = \lambda v^2 H^2 + \lambda v H^3 + \frac{1}{4} \lambda H^4$$

Mass term

Trilinear coupling

Quartic coupling

→ difficult to measure

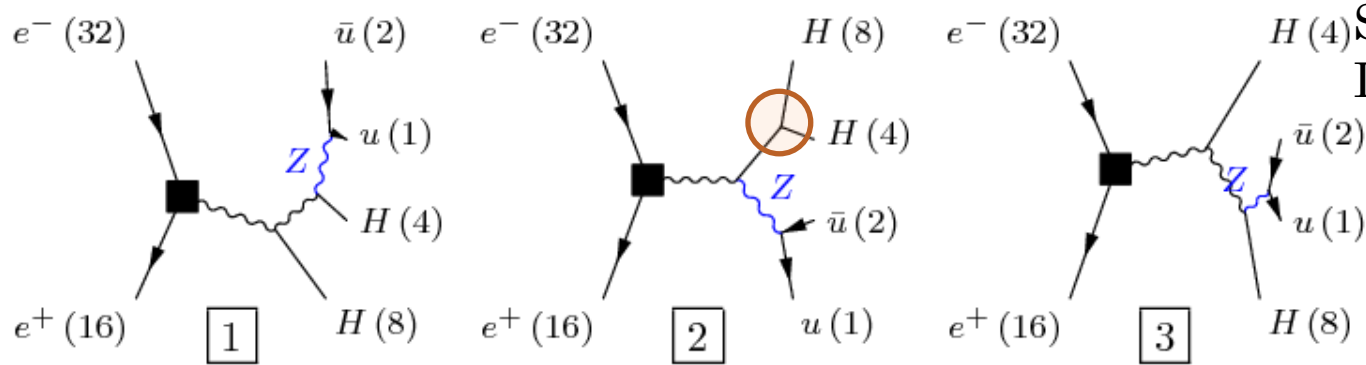
$$SM: \lambda = \frac{m_H^2}{2v^2} \quad v \sim 246 GeV$$

- Observing two Higgs bosons in the event is the only way to measure the self coupling
- Accurate test of the coupling may lead to the extended nature of Higgs sector → may go to new physics
- Our goal is to observe and measure the Higgs self coupling first

SIGNAL EVENTS

Signal: $e^+e^- \rightarrow Z^* \rightarrow ZH \rightarrow ZHH$ is used for the analysis

- Cross section is largest @ 500 GeV for the self coupling analysis



Signal: 2

Irreducible B.G.: 1 and 3

Golden channel is $Z(bb)(bb)$

- Large cross section
- b-tagging reduces the backgrounds drastically

Requirement of $H \rightarrow WW^*$ decay will contribute the total sensitivity

- Need to reduce the backgrounds using kinematics of the events

		H1		
H2	Br	bb		WW
	bb			
	WW			

BACKGROUNDS AND SIMULATION

○ Backgrounds:

- **ttbar**: extremely huge number of events
→ flavor tagging can reduce it extremely
- **ttbar + X**: bjet rich and the final state is similar to signal
→ reject those backgrounds using kinematics
- **ZZ + H**
- Triple Z boson events
→ small cross section but b jet rich
- S/B ~ 1/3000

○ Simulation

- Polarization: (e, p)=(-0.8, +0.3)
- Higgs mass is set @125GeV/c²
- Using the full simulation with latest detector configuration

process	$\sigma(\text{fb})$
Signal(inclusive)	0.2
ttbar - lep+jets	179.8
ttbar - allhad	301.7
ttbar - dilepton	100.3
ttbar + QQ	0.83
ttbar + Z	0.98
ttbar + H	0.14
ZZ + H	0.77
ZZZ	1.83

ANALYSIS STRATEGY FOR $HH \rightarrow (BB)(WW)$

- Classify the events with Z and W decays:

	$WW \rightarrow (qq)(qq)$	$WW \rightarrow (qq)(l\nu)$
$Z \rightarrow bb$	8jets	Lepton+6jets
$Z \rightarrow cc$	8jets	Lepton+6jets
$Z \rightarrow ll$	Dilepton+6jets	Trilepton+4jets

- **Z decays into heavy flavor pair or lepton pair mainly**
 - Need flavor tagger or clean Z mass distribution to reject huge backgrounds
- 1) **Both W bosons from Higgs decay into quarks.**
 - Largest cross section
 - Final state: **8 jets**
- 2) **One of the W bosons from Higgs decays into lepton and neutrino**
→ requiring one isolated lepton and large missing energy
 - The process seems easier than all hadronic events to handle though it has smaller cross section
 - Final state: **lepton + 6jets + missing energy**
- 3) **Z decays into lepton pair:**
 - a) **all the W bosons into quarks**
 - b) **one of the W bosons decays into lepton & neutrino**
 - Cross section is small...
 - Final state:
 - a) **dilepton + 6jets** : b) **trilepton + 4jets + missing energy**

EVENT SELECTION & MAKING SAMPLES

○ preselection

- lepton selection – looking for isolated leptons
 - Electron and muon from primary vertex
 - Lepton energy cut – $E > 15 \text{ GeV}$ to reject soft leptons
 - **Divide into orthogonal samples based on the lepton number in the events**
 - From 0 to 3
 - For 2 and 3 lepton samples, looking for a lepton pair from Z boson

• Jet selection – jet clustering

- Require proper number of jets for each sample – 4, 6, or 8 jets
- Minimum jet energy cut is required to reject trivial backgrounds

	4jets	6jets	8jets
Min. Energy(GeV)	1.0	3.0	2.0

- b likeliness > 0.4 is required for b jet candidates
- Missing momentum
 - Lep+jets sample – $P(\text{miss}) > 15 \text{ GeV}/c$ to reject $HH \rightarrow bbbb$ or hadronic events
 - 0 or 2-lepton sample – $P(\text{miss}) < 80 \text{ GeV}$
 - 3-lepton sample – $P(\text{miss}) < 150 \text{ GeV}$ to avoid reducing signal acceptance

SOLVING THE COMBINATION OF JETS

- Jets should be assigned to their parent particles correctly to obtain good kinematic variables

- **Jet pairing is based on the χ^2 technique**

- b jet assignment to Higgs and Z boson:

$$\chi^2 = \frac{(m_1 - m_Z)^2}{\sigma_Z^2} + \frac{(m_2 - m_H)^2}{\sigma_H^2}$$

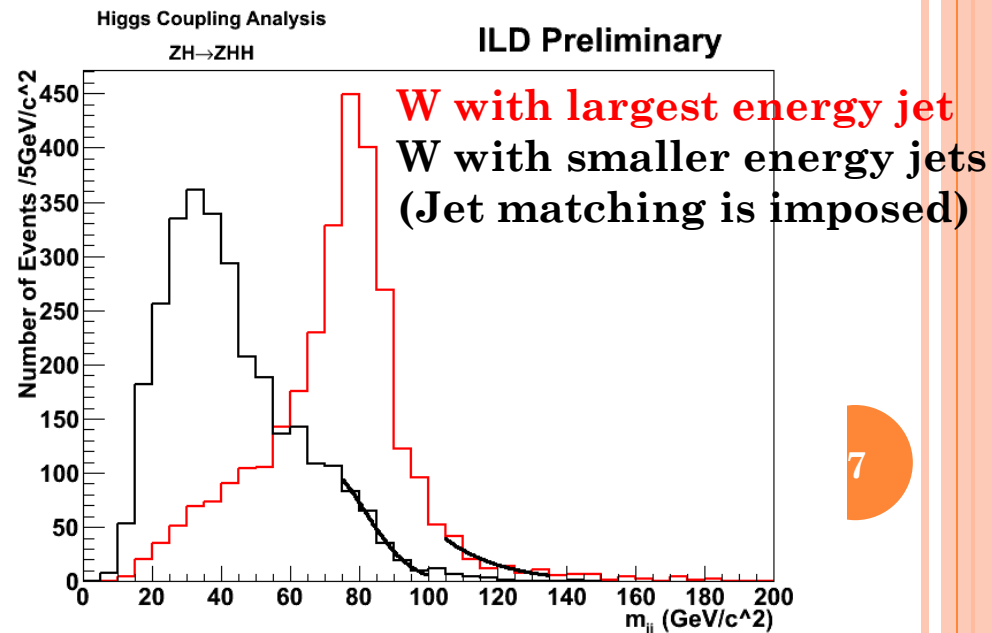
- Light flavor jet assignment to 2 W bosons:

- Mass constraint is imposed only to the W boson with largest energy jets

- Breit-Wigner is assumed

for W mass shape

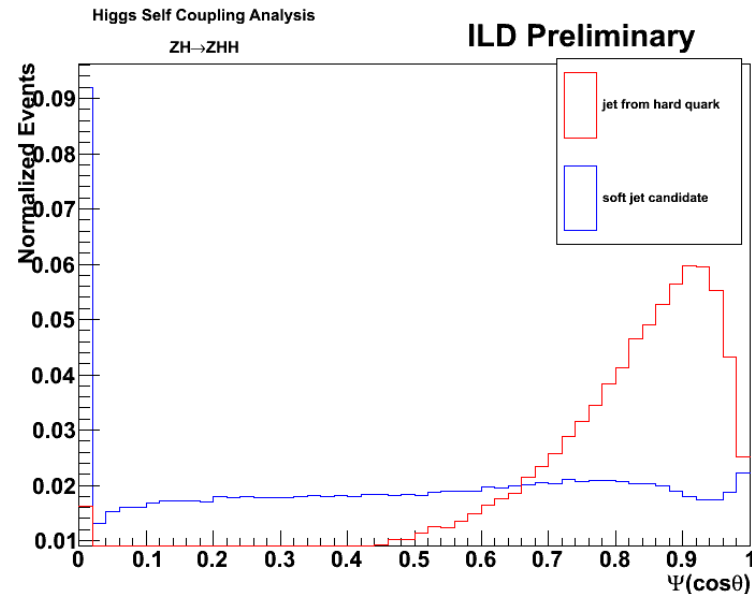
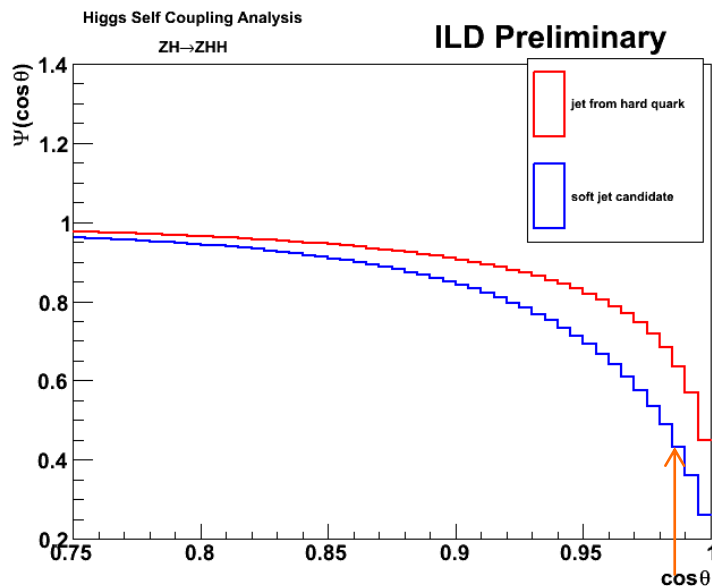
- $\chi^2 = -2\text{Log}(\text{BW}(m_{W1}|m_W, \Gamma_W))$



SOFT JET FINDING

- Tracks in the gluon jets spread wider than those in quark jets(e.g. analyses on hadron collider)
- Soft jet finding may be available for the events with extra jets not coming from hard process quarks
 - e.g. 8 jets requirement to $t\bar{t}$ hadronic events(6 jets from hard quarks)
- Traditional jet shape indicates the same tendency as hadron collider analysis

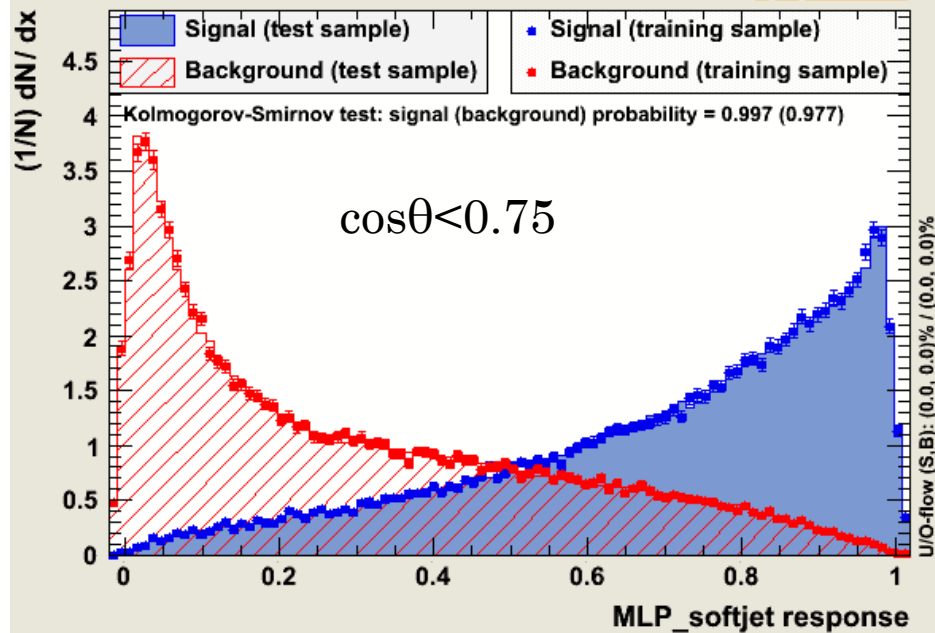
$$\psi(\cos\theta) = \int_1^{\cos\theta} \frac{p(r)}{p_{jet}} dr$$



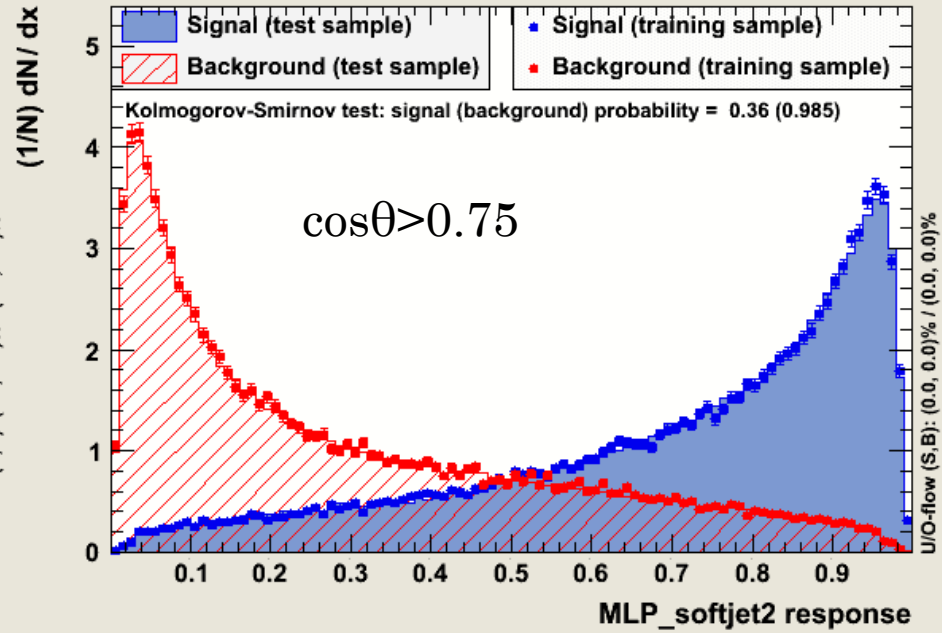
SOFT JET FINDING

- Hard jet likeliness is introduced
 - Using MVA to form it
 - Analysis samples are divided into 2 based on the angle with the nearest jet
 - large shared area for both jets deteriorate the traditional jet shape
- Use the likeliness for the input of background rejection MVA or simple cut of backgrounds

TMVA overtraining check for classifier: MLP_softjet

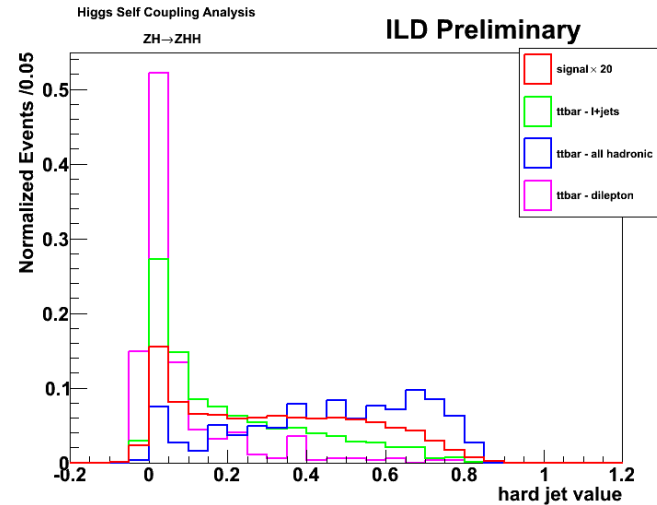
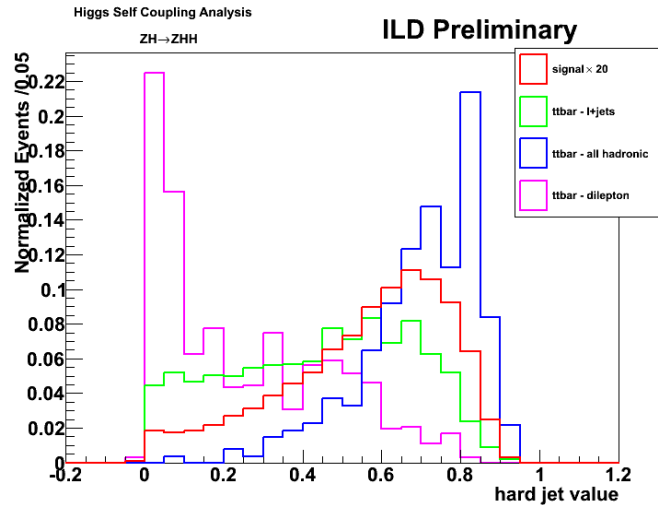


TMVA overtraining check for classifier: MLP_softjet2

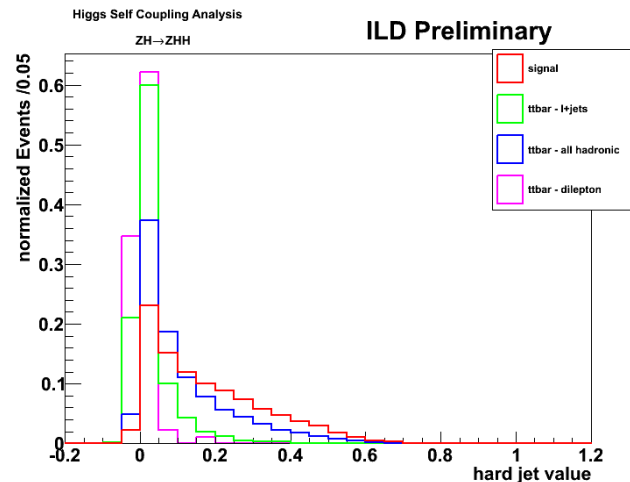
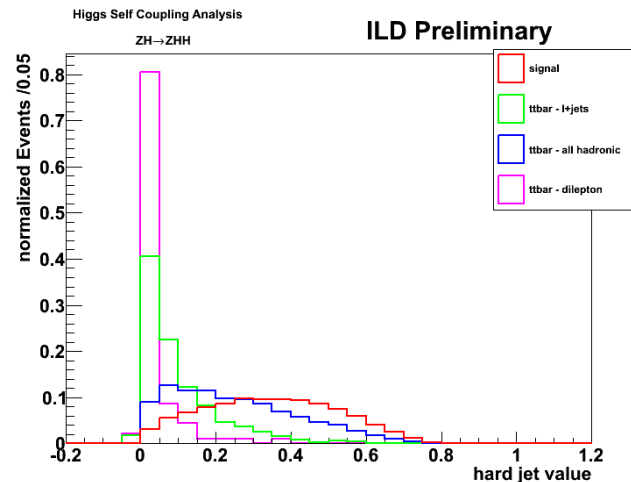


CHECK THE PERFORMANCE

- Check the jets with small hard jet likelihood – signal vs. $t\bar{t}$
- For 6jets



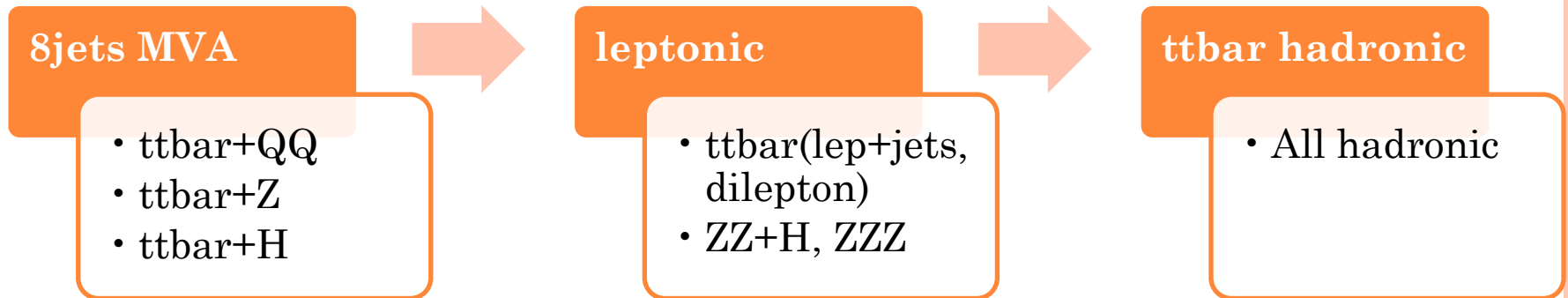
- For 8jets



BACKGROUND REJECTION

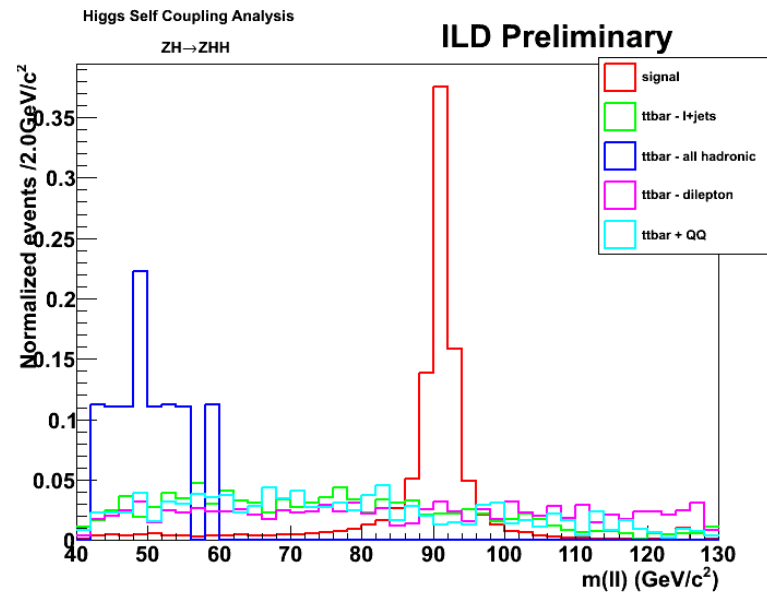
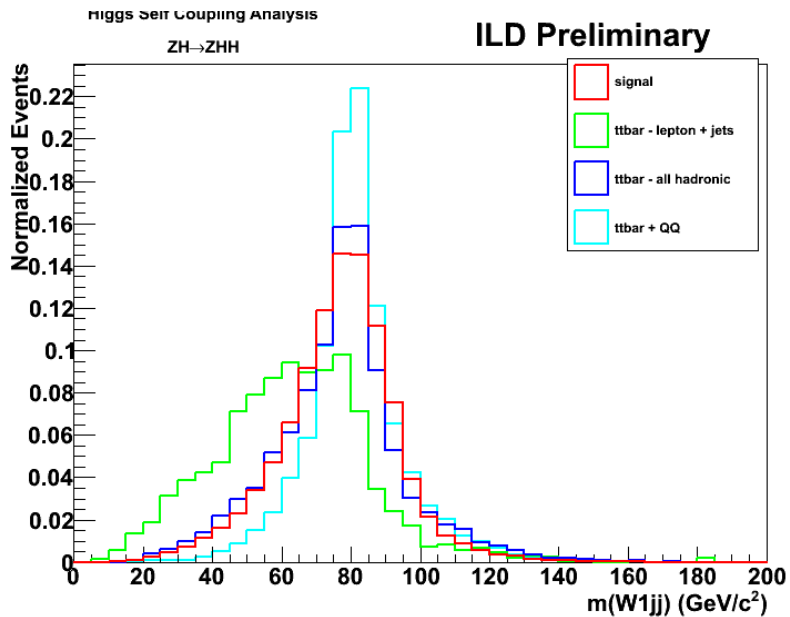
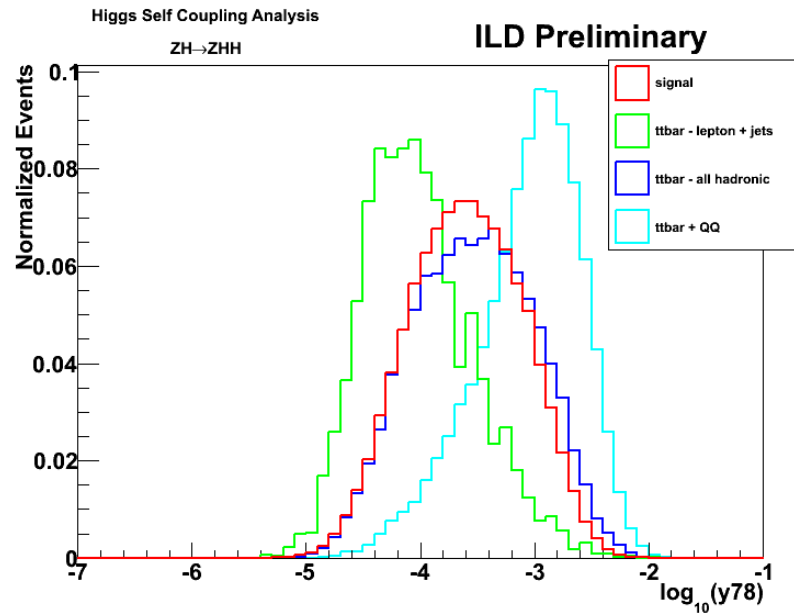
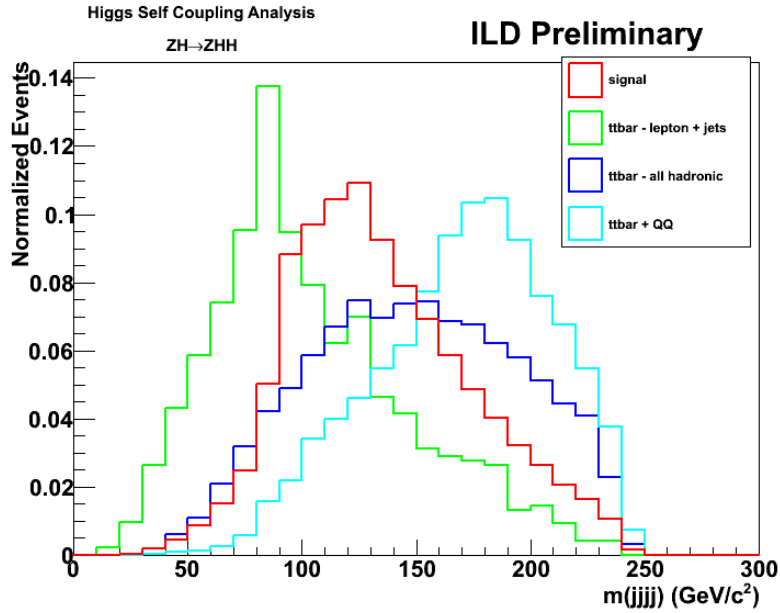
Using Multi Variate Analysis

- Some cuts are implemented before MVA to tighten the input variable space – jet energy, χ^2 , visible energy, (Z mass)
- Background rejection strategy : rejecting small backgrounds first and then rejecting main background
 - Tighten the variable space when rejecting main backgrounds
- e.g. all hadronic case:



SOME KINEMATIC VARIABLES USED FOR MVA

Very powerful variable: $m(jjjj)$, $m(lvjj)$



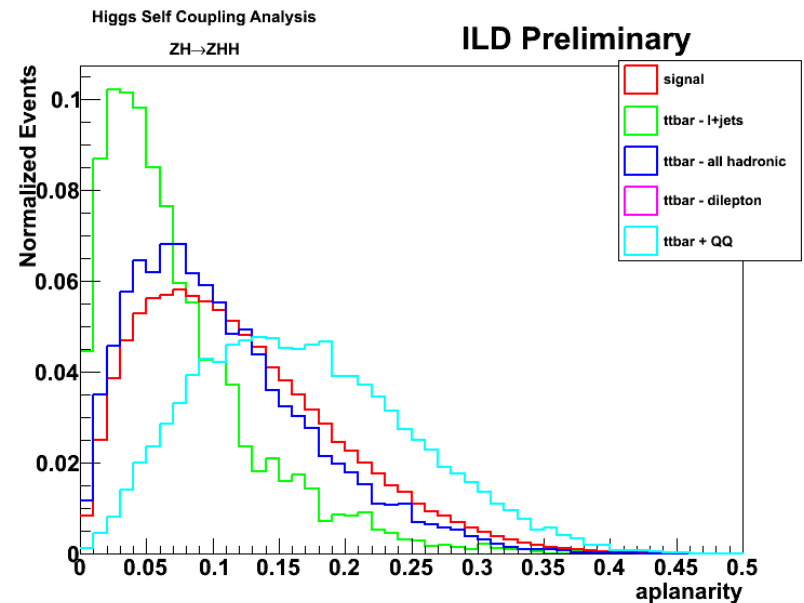
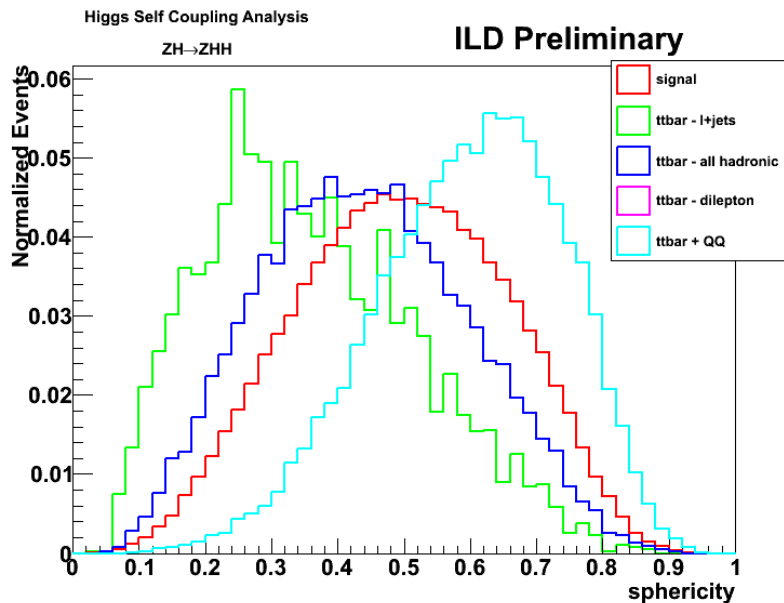
NON-SIMPLE VARIABLES USED FOR MVA

○ Sphericity and aplanarity

- Eigenvalue combinations of sphericity tensor:

$$S^{\alpha\beta} = \frac{\sum_i p_i^\alpha p_i^\beta}{\sum_i |\mathbf{p}_i|^2}, \quad \text{eigenvalues: } \lambda_1 > \lambda_2 > \lambda_3$$

- Sphericity: $S = \frac{3}{2}(\lambda_2 + \lambda_3)$
- Aplanarity: $A = \frac{3}{2}\lambda_3$
- Indicates whether the event is 2-jets like or isotropic

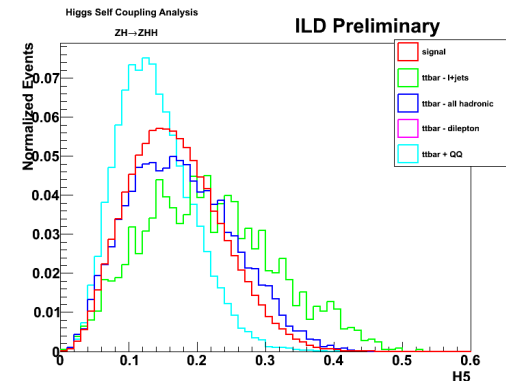
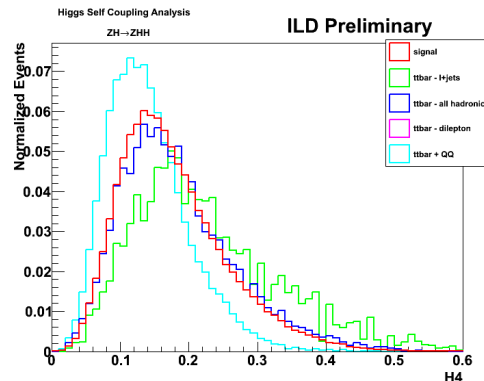
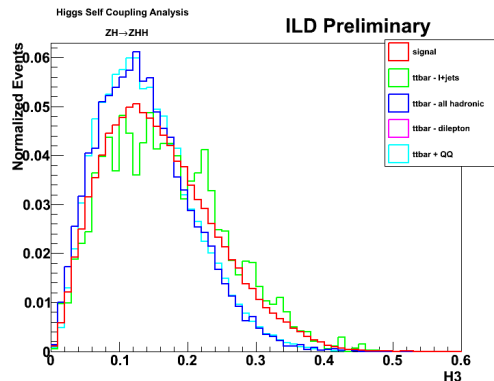
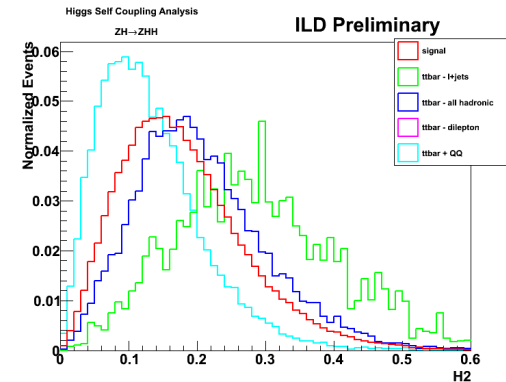
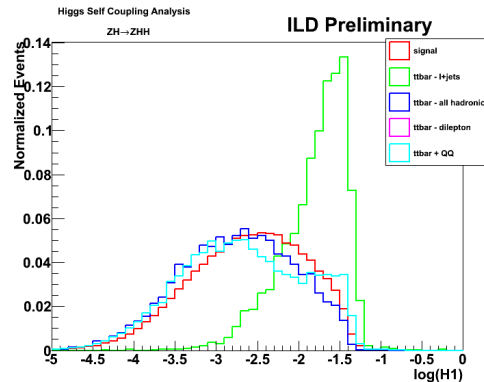
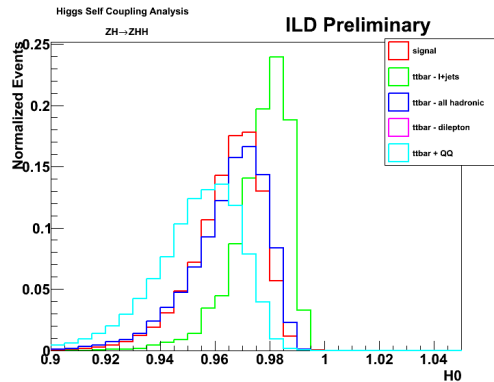


NON-SIMPLE VARIABLES USED FOR MVA

○ Fox-wolfram moments

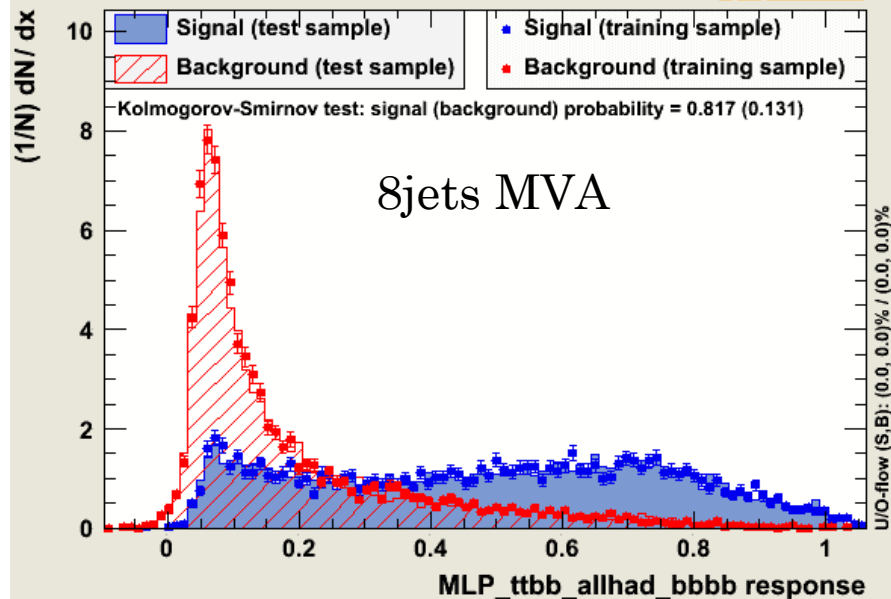
$$H_l = \sum_{i,j} \frac{|\mathbf{p}_i| |\mathbf{p}_j|}{E_{\text{vis}}^2} P_l(\cos \theta_{ij}) ,$$

- P_l is Legendre polynomials
- Those moments characterize the structures of 2jets, 3jets, or isotropic events

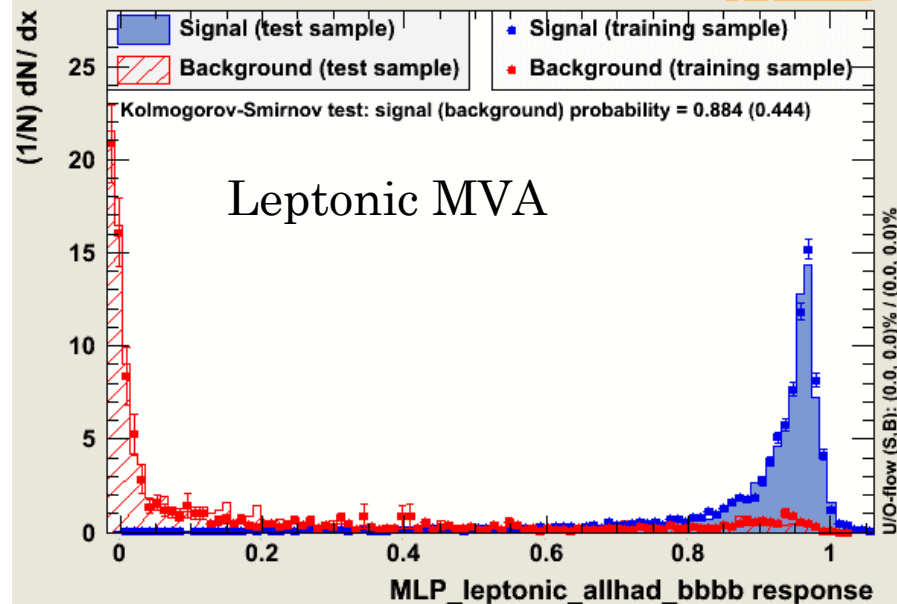


MVA OUTPUTS EXAMPLES(ALLHADRONIC)

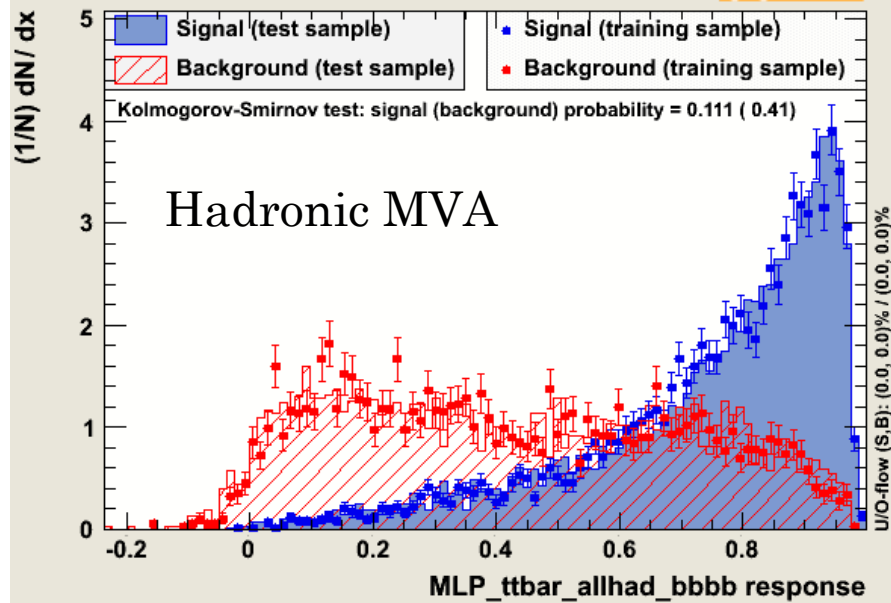
TMVA overtraining check for classifier: MLP_ttbb_allhad_bbbb



TMVA overtraining check for classifier: MLP_leptonic_allhad_bbbb



TMVA overtraining check for classifier: MLP_ttbar_allhad_bbbb



cut of MVA:
MVA_{8jets} > 0.10
MVA_{lep} > 0.02
MVA_{had} > 0.42

SENSITIVITY

○ Progress for b jet related analysis:

- Checking event samples with lepton numbers from 0 to 3
- Multi Variate Analysis
- $E_{\text{CM}}=500\text{GeV}$, $L=2\text{ab}^{-1}$
- **Significance $\sim 1.37\sigma$**

2ab-1	allhad	Lep+jets	Dilepton	trilepton
signal	14.92	1.55	1.08	1.15
ttbar(lep+jets)	8.34	6.74	1.95	0.0
ttbar(allhad)	79.29	4.57	0.0	0.10
ttbar(dilepton)	0.0	0.19	0.0	3.42
tt + QQ	17.54	2.67	0.03	0.15
tt + Z	16.41	1.13	0.18	1.82
tt + H	9.13	1.39	0.01	0.16
ZZ + H	16.10	0.18	1.09	1.28
ZZZ	6.03	0.07	0.11	0.58
significance	1.15σ	0.36σ	0.51σ	0.39σ

SENSITIVITY

○ Progress for c jet related analysis:

- Checking event samples with lepton numbers from 0 and 1
- Multi Variate Analysis
- $E_{\text{CM}}=500\text{GeV}$, $L=2\text{ab}^{-1}$
- **Significance $\sim 0.18\sigma$**
 - c jet analysis don't give large contribution on the total sensitivity

- **Total significance $\sim 1.38\sigma$**

2ab-1	allhad	Lep+jets
signal	2.70	0.88
ttbar(lep+jets)	6.17	75.68
ttbar(allhad)	189.51	62.25
ttbar(dilepton)	0.0	5.57
tt + QQ	12.42	1.67
tt + Z	8.30	0.46
tt + H	1.42	0.36
ZZ + H	3.86	0.07
ZZZ	2.20	0.03
significance	0.18σ	0.04σ

REDUCTION TABLE

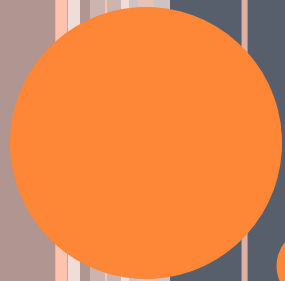
All hadronic

- Final b-tagging: $\text{btag}(3) > 0.92$ && $\text{btag}(4) > 0.44$
- $\text{HH} \rightarrow \text{bbbb}$ contamination is 5.41 events

process	signal	ttbar	tt + QQ	tt+Z	tt + H	ZZ + H	ZZZ
expected	354.00	1.16×10^6	1660.00	3307.00	280.00	1540.00	3660.00
preselection	49.47	2462.09	79.11	76.25	38.32	87.22	70.72
Jet energy	47.92	1970.58	77.62	74.98	37.96	72.88	57.28
χ^2	44.32	1353.38	64.57	62.41	34.02	61.60	48.16
Visible energy	44.23	1326.19	64.31	62.00	33.92	61.18	47.90
NN for 8 jets	36.51	1011.92	36.37	34.37	16.38	51.59	47.90
NN for ttbar	20.53 (9.85)	302.59	26.44	25.17	13.07	21.71	9.00
b-tagging	14.92 (5.41)	87.54	17.54	16.42	9.13	16.10	6.03

SUMMARY AND PLAN

- Higgs self coupling analysis using the events with $H \rightarrow WW^*$ is ongoing.
 - Multi variate analysis to reject the backgrounds
 - Unfortunately, c jet analysis doesn't give significant contribution
 - Total sensitivity is $\sim 1.4\sigma$
- **Plan:**
 - Add the looser tag category
 - Fewer number of b-tagging samples
 - Acceptance is relatively large, but very small S/N. need some idea to reject huge backgrounds
 - Improvement of b-tagging
 - More accurate jet pairing technique
 - Analysis@1TeV



BACKUPS

EVENT SELECTION

○ Lepton selection

- Lepton ID: The isolated lepton coming from the primary vertex

lepton	electron	muon
cut	$0.65 < E/p < 1.25$ $E(\text{EM}) / (E(\text{EM}) + E(\text{HAD})) > 0.90$ $ d_0 < 0.02$ $ z_0 < 0.02$ Cone Energy $< 61.10 - 0.28P$	$E/p < \min(0.5, 10.0/E)$ $E(\text{EM}) / (E(\text{EM}) + E(\text{HAD})) < 0.45$ $ d_0 < 0.02$ $ z_0 < 0.02$ Cone Energy $< 52.45 - 0.28P$

- Detection efficiency of Lepton ID $\sim 98.4\%$ for lep+jets signal events

	Signal	ttbar – lep+jets	ttbar - allhad
Efficiency(%)	98.4	71.4	7.9

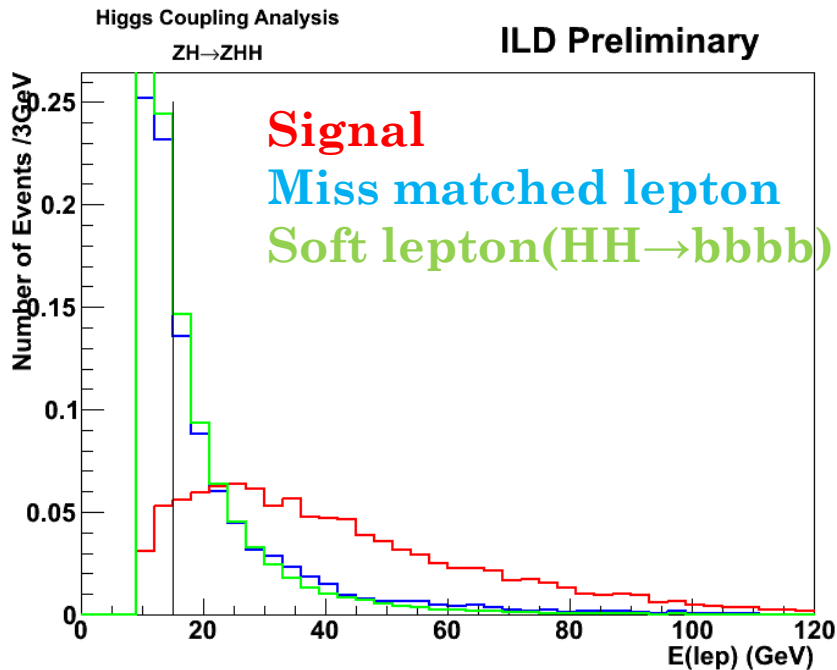
- For dilepton events $\sim 83.8\%$ of signal events

	Signal	ttbar – dilepton
Efficiency(%)	83.8	84.5

EVENT SELECTION

○ Lepton selection

- $E(\text{lep}) > 15\text{GeV}$ is required to suppress soft leptons
- Dividing into 3 samples:
 - one lepton for **lepton + jets**
 - two leptons for **dilepton** → opposite charge & same flavor
 - three leptons for **trilepton** → looking for the lepton pair from Z
 - tight lepton veto for **all hadronic**



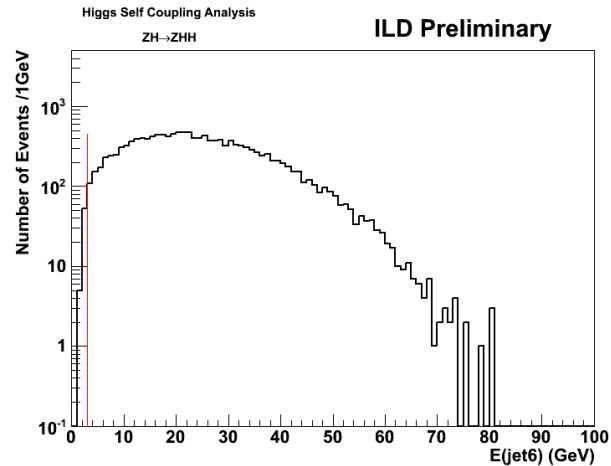
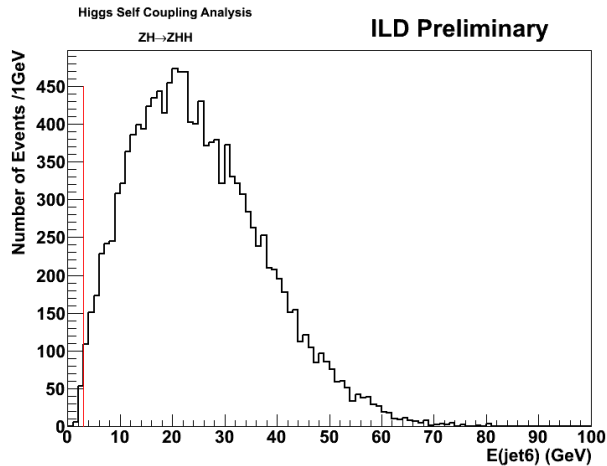
Lepton matching is required:
 $\cos\theta > 0.9$

EVENT SELECTION

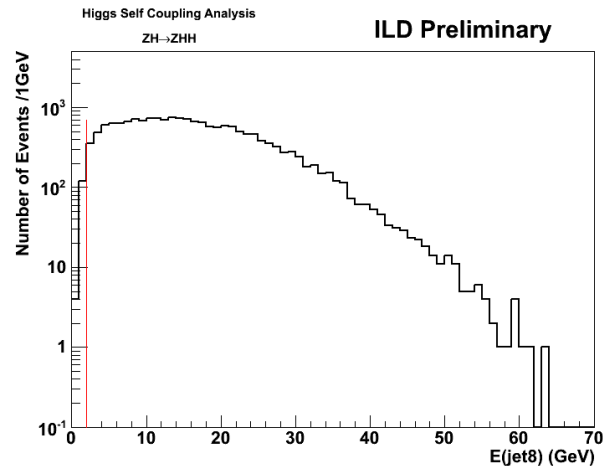
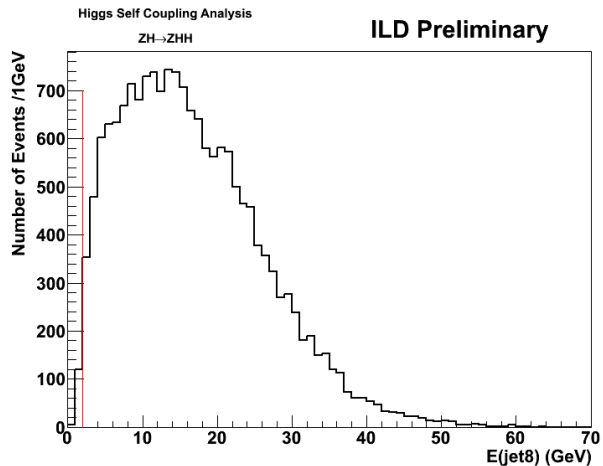
○ jet selection

- requiring 4jets, 6 jets or 8 jets using LCFIPlus & Durham
- $E(\text{jet}) > 3\text{GeV}$ is required to care the lowest energy jet for **6 jets** case

•



- $E(\text{jet}) > 2\text{GeV}$ is required to care the lowest energy jet for **8 jets** case



EVENT SELECTION

- Detection efficiency after the jet energy cut:

signal	4jets requirement	6jets requirement	8jets requirement
Efficiency(%)	99.0	99.4	99.6

- Missing momentum

- **lepton + jets**: $P(\text{Miss}) > 15 \text{ GeV}/c$ to suppress $\text{HH} \rightarrow \text{bbbb}$ events
- **All hadronic & dilepton**: $P(\text{Miss}) < 80 \text{ GeV}/c$ required
- **Trilepton**: $P(\text{Miss}) < 150 \text{ GeV}/c$ to gain the acceptance

