

# The ILC Higgs White Paper

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# ILC HIGGS WHITE PAPER

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## A U T H O R S

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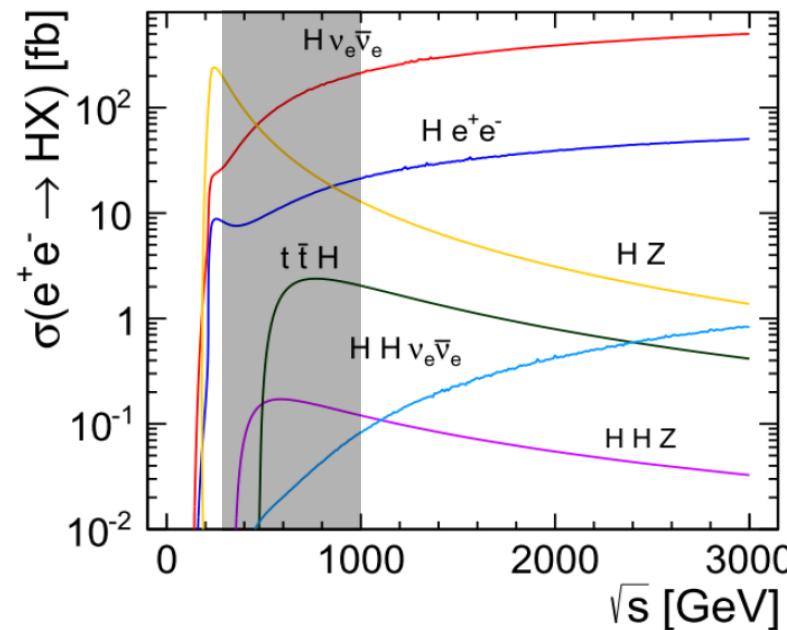
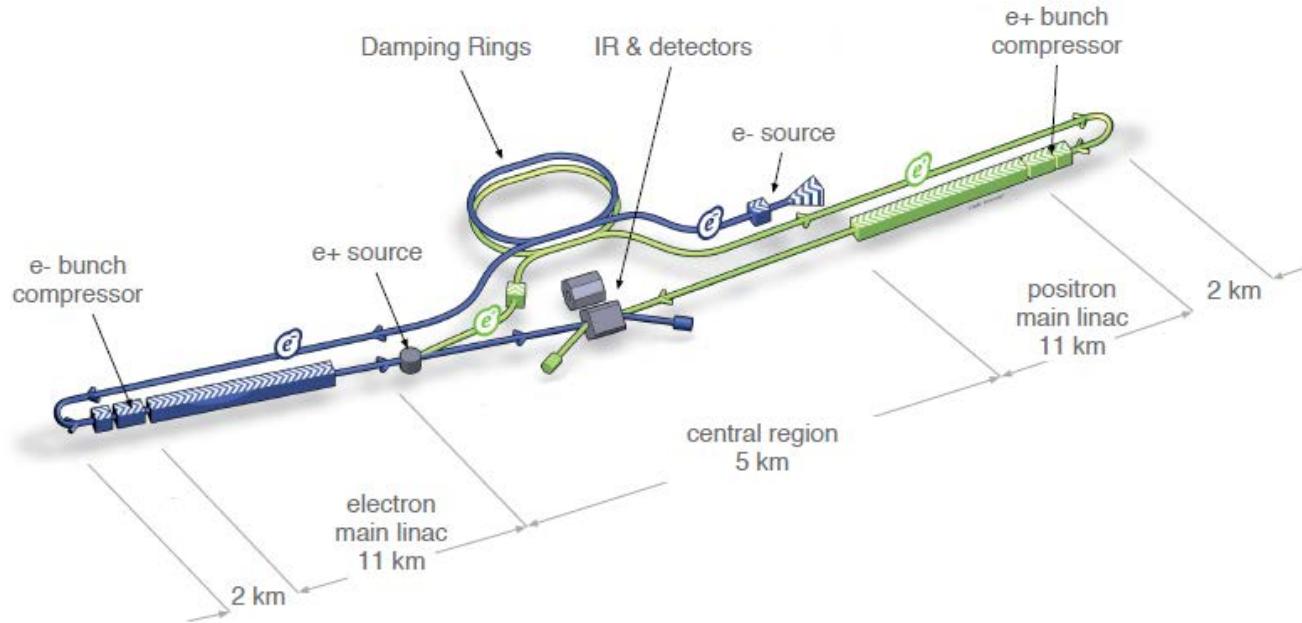
## Luminosity based on ILC TDR

## Many New Post-DBD Studies

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## Model Independent Fits as Usual; Also Model Dependent Fits for LHC Comparison

# ILC: $e^+e^-$ Linear Collider at $250 \text{ GeV} < \sqrt{s} < 1000 \text{ GeV}$



# Energy/Lumi Scenarios for White Paper

- ▶ Each scenario corresponds to accumulated luminosity at a certain point in time.
- ▶ Assumption: run for  $3 \times 10^7$  s at baseline lumi at each of  $E_{cm}=250, 500, 1000$  GeV, in that order. Then go back and run for  $3 \times 10^7$  s at upgrade lumi at each of  $E_{cm}=250, 500, 1000$  GeV.

Nickname	$E_{cm}(1)$ (GeV)	$Lumi(1)$ ( $fb^{-1}$ )	+	$E_{cm}(2)$ (GeV)	$Lumi(2)$ ( $fb^{-1}$ )	+	$E_{cm}(3)$ (GeV)	$Lumi(3)$ ( $fb^{-1}$ )	Runtime (yr)	Wallplug E (MW-yr)
ILC(250)	250	250							1.1	130
ILC(500)	250	250		500	500				2.0	270
ILC(1000)	250	250		500	500		1000	1000	2.9	540
ILC(LumUp)	250	1150		500	1600		1000	2500	5.8	1220

# Systematic Errors at ILC

*b*-tag efficiency study  
for White Paper,  
[T. Suehara ,Tohoku Univ. &](#)  
[T. Tanabe, Univ Tokyo](#)

**Table 2.6.** Expected *b*-tagging uncertainties at various selection efficiencies.

Efficiency	Uncertainty
80%	0.46%
70%	0.53%
60%	0.57%
50%	0.58%

**Table 2.7.** Summary of selection for the fake rate measurement. Here the *b* tag selection is such that one of the two jets will pass the *b* tag requirement at the specified efficiency.

Process	Before selection	After selection	<i>b</i> tag ( $\epsilon_b = 80\%$ )	<i>b</i> tag ( $\epsilon_b = 50\%$ )
$WW \rightarrow \ell\nu cs$	$1.3 \times 10^6$	$1.3 \times 10^5$ (10%)	11310 (8.7%)	234 (0.18%)
$WW \rightarrow \ell\nu ud$	$1.3 \times 10^6$	$1.3 \times 10^5$ (10%)	2080 (1.6%)	130 (0.1%)
$ZZ \rightarrow \tau\tau b\bar{b}$	8500	85 (1%)	82 (96%)	64 (75%)

**Table 2.8.** Systematic errors assumed throughout the paper.

	Baseline	LumUp
luminosity	0.1%	0.05%
polarization	0.1%	0.05%
<i>b</i> -tag efficiency	0.3%	0.15%

ILC model independent global coupling fit using 32  $\sigma \cdot BR$   
measurements  $Y_i$  and  $\sigma_{ZH}$  measurement  $Y_{33}$

$$\chi^2 = \sum_{i=1}^{i=33} \left( \frac{Y_i - Y'_i}{\Delta Y_i} \right)^2,$$

$$Y'_i = F_i \cdot \frac{g_{HZZ}^2 g_{Hb\bar{b}}^2}{\Gamma_0}, \text{ or } Y'_i = F_i \cdot \frac{g_{HWW}^2 g_{Hb\bar{b}}^2}{\Gamma_0}, \text{ or } Y'_i = F_i \cdot \frac{g_{Htt}^2 g_{Hb\bar{b}}^2}{\Gamma_0}$$

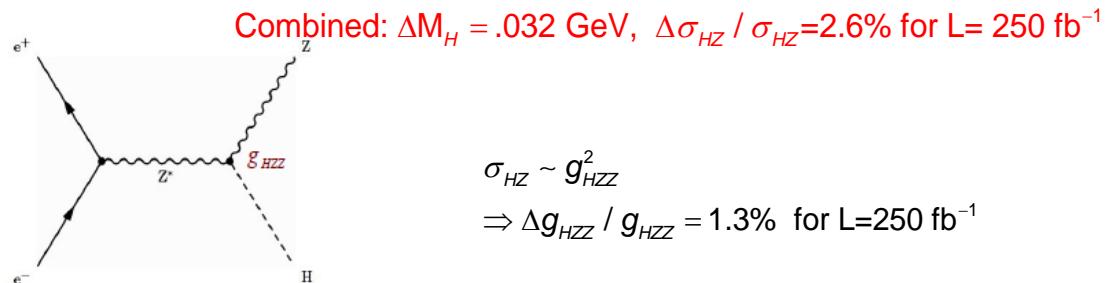
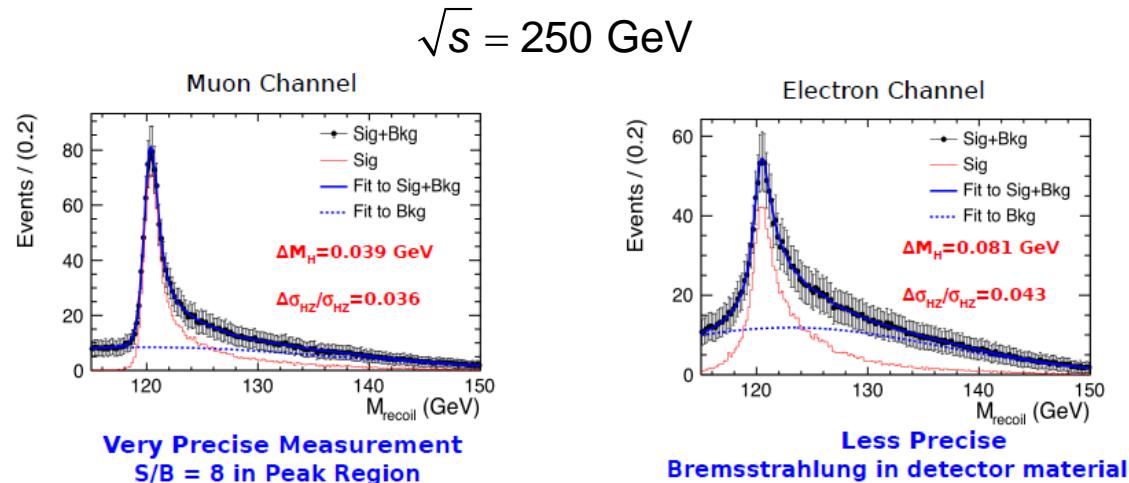
$$F_i = S_i G_i \quad \text{where } S_i = \left( \frac{\sigma_{ZH}}{g_Z^2} \right), \left( \frac{\sigma_{\nu\bar{\nu}H}}{g_W^2} \right), \text{ or } \left( \frac{\sigma_{t\bar{t}H}}{g_t^2} \right), \text{ and } G_i = \left( \frac{\Gamma_i}{g_i^2} \right).$$

The cross section calculations  $S_i$  do not involve QCD ISR.

The partial width calculations  $G_i$  do not require quark masses as input.

We are confident that the total theory errors for  $S_i$  and  $G_i$  will be at the 0.1% level at the time of ILC running.

- Almost all ILC Higgs measurements are measurements of  $\sigma \cdot BR$ .
- One crucial measurement is different: the Higgs recoil measurement of  $\sigma(e^+e^- \rightarrow ZH)$ .
- $\sigma_{ZH}$  is the key that unlocks the door to model independent measurements of the Higgs BR's and  $\Gamma_{tot}$  at the ILC.



ILD & SiD LOI  
& new  $M_H=125$  GeV study by  
S. Watanuki, Tohoku Univ.

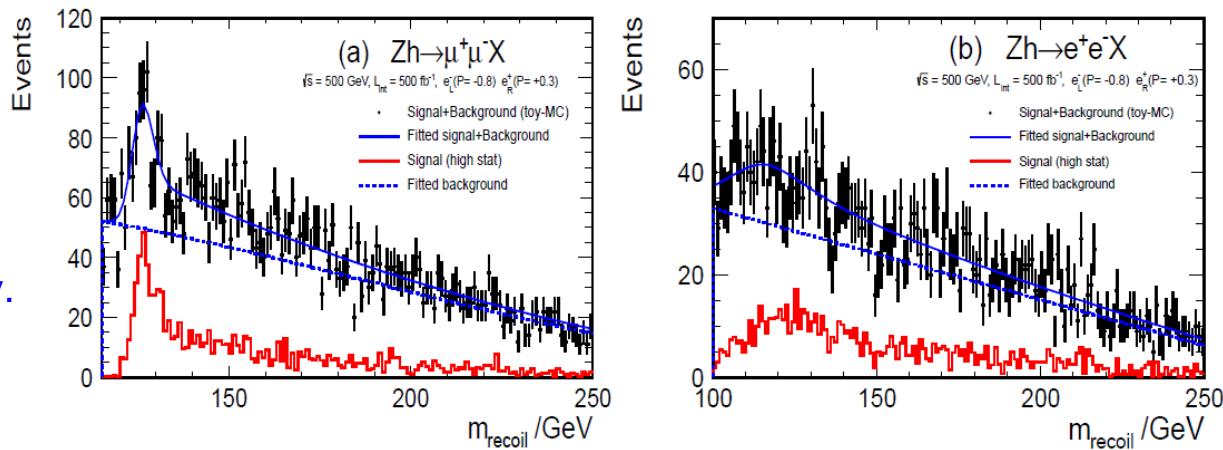
# $\sigma(e^+e^- \rightarrow ZH)$ : New Analyses at $\sqrt{s} = 500$ GeV

$ZH \rightarrow l^+l^-X$

$\Delta\sigma / \sigma = 4.8\%$

for  $500 \text{ fb}^{-1}$

T. Suehara, Tohoku Univ.

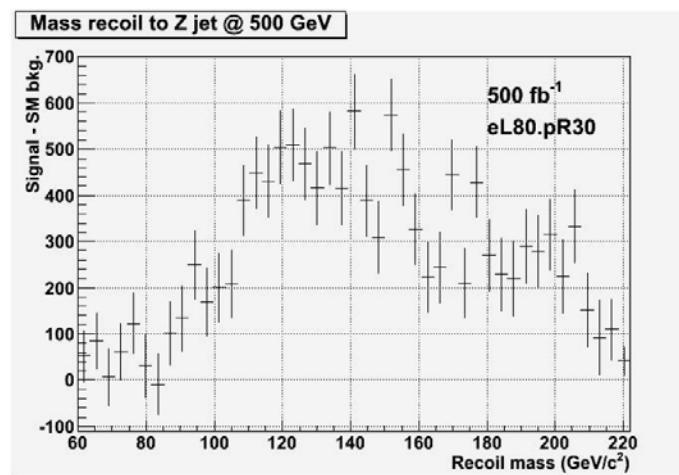


$ZH \rightarrow q\bar{q}X$

$\Delta\sigma / \sigma = 3.9\%$

for  $500 \text{ fb}^{-1}$

A. Miyamoto, KEK



Combining all channels for  $500 \text{ fb}^{-1}$  at  $\sqrt{s} = 500$  GeV:  $\Delta\sigma(e^+e^- \rightarrow ZH) / \sigma(e^+e^- \rightarrow ZH) = 3.0\%$

Combining 250  $\text{fb}^{-1}$  at  $\sqrt{s} = 250$  GeV & 500  $\text{fb}^{-1}$  at  $\sqrt{s} = 500$  GeV:  $\Delta\sigma(e^+e^- \rightarrow ZH) / \sigma(e^+e^- \rightarrow ZH) = 2.0\%$

$\sigma \bullet BR(H \rightarrow \tau^+ \tau^-)$ : New Analysis at  $\sqrt{s} = 250$  GeV

$ZH \rightarrow q\bar{q}\tau^+\tau^-$

$H \rightarrow \tau^+ \tau^-$

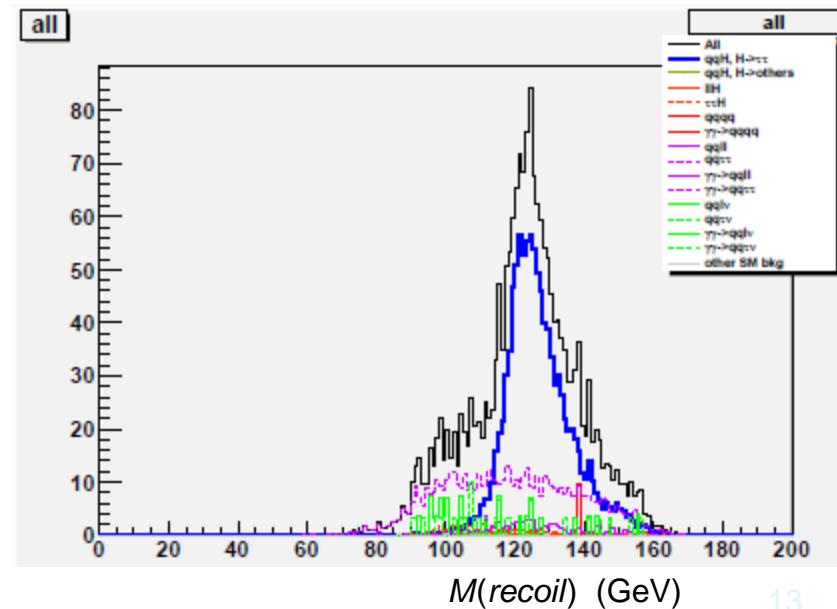
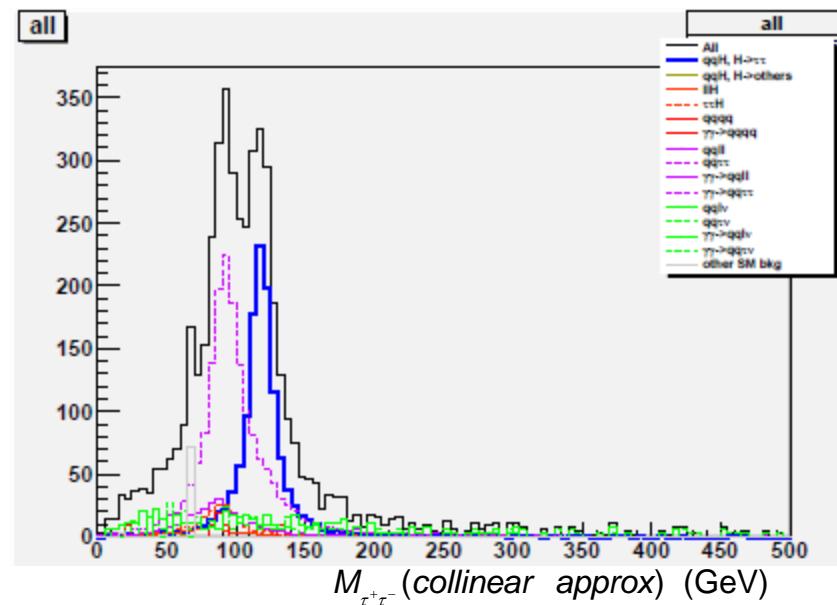
$\Delta\sigma \bullet B / \sigma \bullet B = 4.2\%$

for  $250 \text{ fb}^{-1}$  @  $\sqrt{s} = 250$  GeV

S. Kawada & T. Takahashi (Hiroshima Univ)

K. Fujii (KEK)

T. Suehara & T. Tanabe (Univ Tokyo)



$H \rightarrow b\bar{b}$

$\Delta\sigma \bullet B / \sigma \bullet B = 0.7\%$

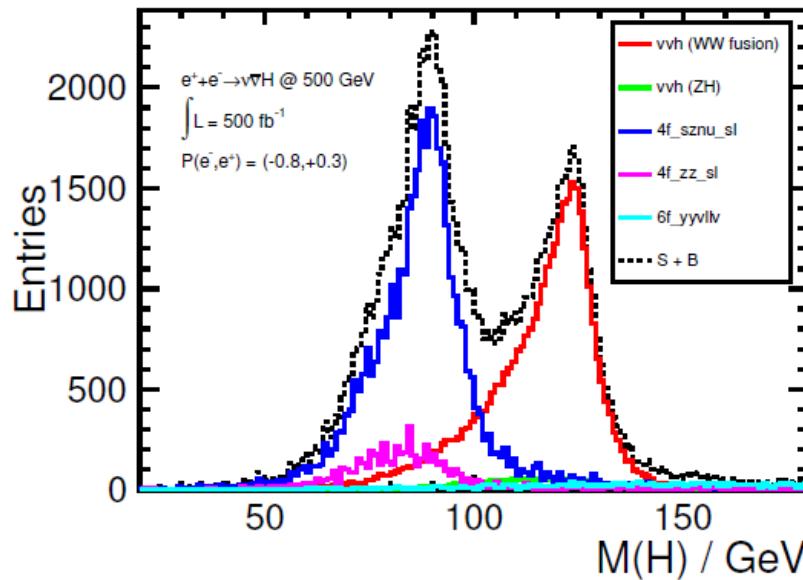
for  $500 \text{ fb}^{-1}$  @  $\sqrt{s} = 500$  GeV

J.Tian & K. Fujii (KEK)

C. Dürig & J. List (DESY)

TABLE II: The reduction table for signal and backgrounds in the analysis of  $\nu\bar{\nu}H \rightarrow \nu\bar{\nu}b\bar{b}$  at 500 GeV. The cut names are explained in text.  $\nu\bar{\nu}H$  has two types, one of signal WW-fusion process, the other from ZH process. The number of signal events after Cut5 in the parenthesis is for  $H \rightarrow b\bar{b}$ .

Process	expected	pre-selection	Cut1	Cut2	Cut3	Cut4	Cut5
$\nu\bar{\nu}H$ (fusion)	$7.47 \times 10^4$	59698	54529	54048	35598	34278	299199 (28598)
$\nu\bar{\nu}H$ (ZH)	$1.02 \times 10^4$	7839	7301	7224	4863	1951	1512
4f_sznu_sl	$2.79 \times 10^5$	234259	203489	202977	44943	39125	3957
4f_sw_sl	$2.43 \times 10^6$	228436	135164	121791	1495	911	132
4f_zz_sl	$1.83 \times 10^5$	102172	60684	59865	13036	5736	461
4f_ww_sl	$2.78 \times 10^6$	653997	287428	250944	3851	1145	176
4f_sze_sl	$9.41 \times 10^5$	65011	1311	1259	91.1	40.7	5.51
6f_yyveev	$6.05 \times 10^3$	931	306	104	96.6	87.4	20.4
6f_yyvelv	$2.37 \times 10^4$	5450	2425	1116	997	907	237
6f_yyvllv	$2.36 \times 10^4$	8009	4272	2813	2556	2383	674
BG	$6.68 \times 10^6$	$1.31 \times 10^6$	702379	648094	71929	52285	7176
significance	16.6	35.0	43.3	44.6	106	114	150



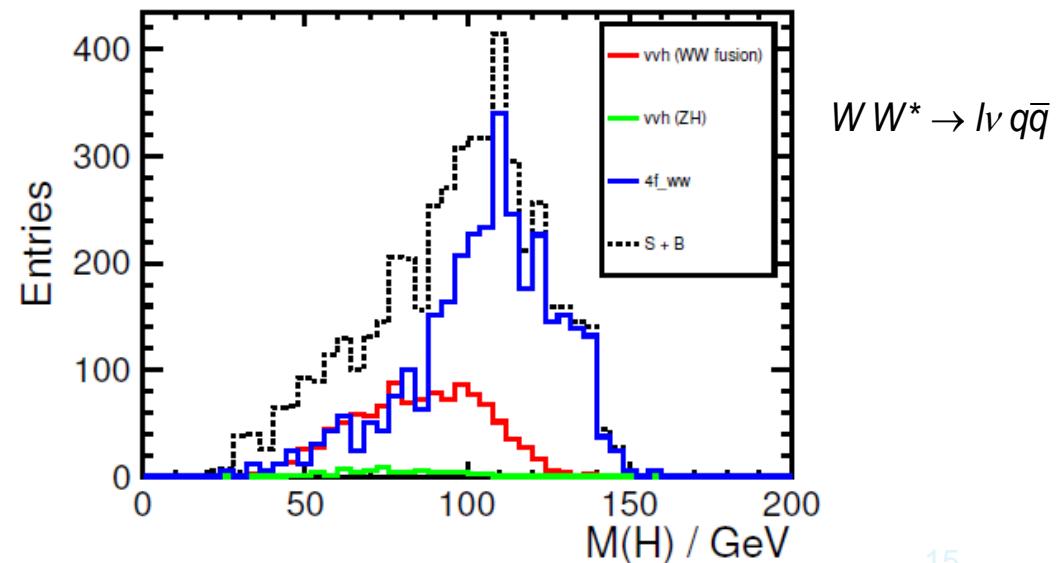
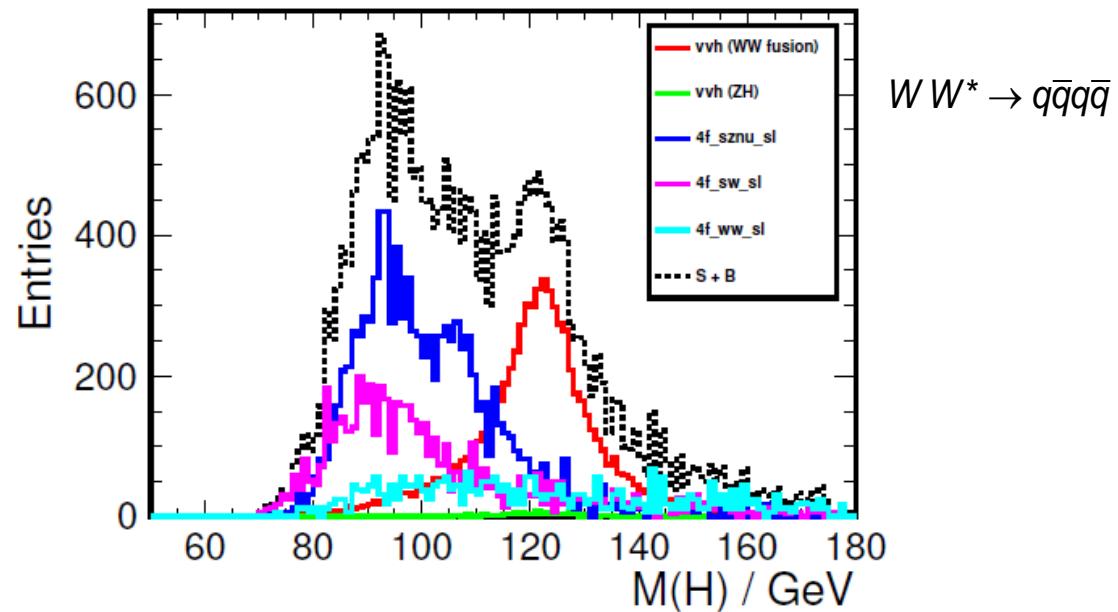
$H \rightarrow WW^*$

$\Delta\sigma \bullet B / \sigma \bullet B = 2.4\%$

for  $500 \text{ fb}^{-1}$  @  $\sqrt{s} = 500 \text{ GeV}$

J.Tian & K. Fujii (KEK)

C. Dürig & J. List (DESY)



$\sigma \bullet BR(H \rightarrow \gamma\gamma)$ : New Analysis at  $\sqrt{s} = 250$  & 500 GeV

$H \rightarrow \gamma\gamma$

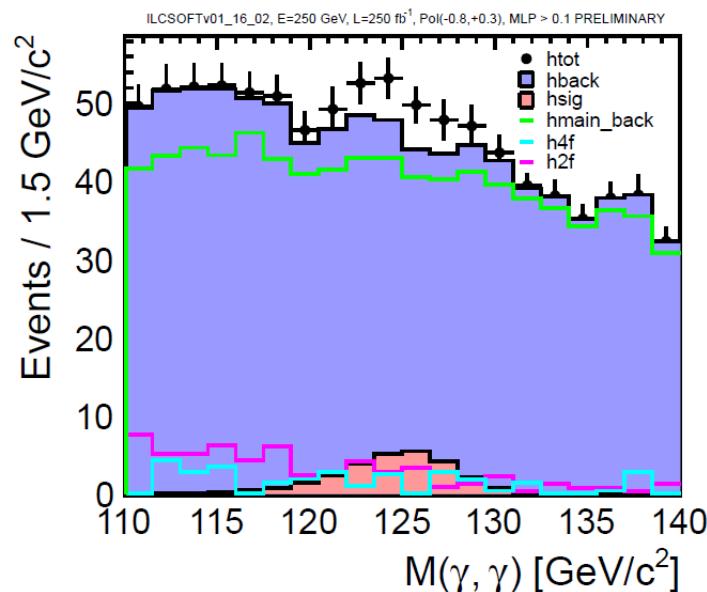
$\Delta\sigma \bullet B / \sigma \bullet B = 34\%$

for  $250 \text{ fb}^{-1}$  @  $\sqrt{s} = 250 \text{ GeV}$

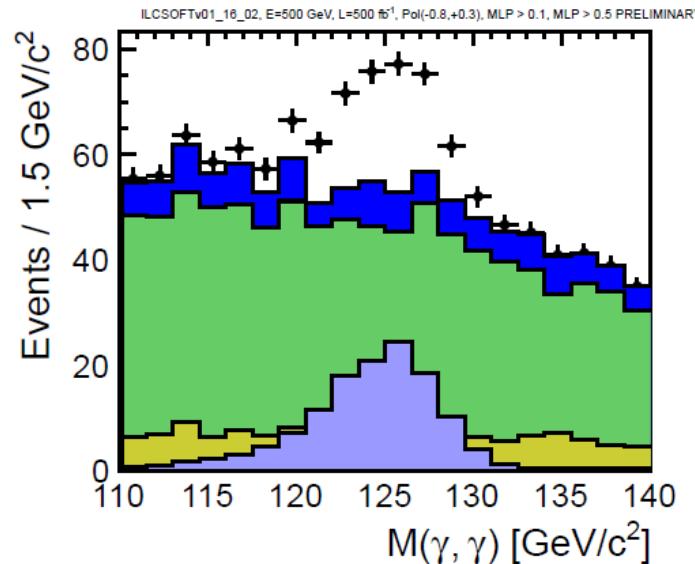
$\Delta\sigma \bullet B / \sigma \bullet B = 23\%$

for  $500 \text{ fb}^{-1}$  @  $\sqrt{s} = 500 \text{ GeV}$

C. Calancha (KEK)



$\sqrt{s} = 250 \text{ GeV}$



$\sqrt{s} = 500 \text{ GeV}$

# $\sigma \bullet BR(H \rightarrow ZZ^*)$ : New Analysis at $\sqrt{s} = 250$ GeV

**Table 5.3.** Composition of the events passing all analysis selections for the polarizations  $P(e^-) = +80\%$ ,  $P(e^+) = -30\%$  and an integrated luminosity of  $250 \text{ fb}^{-1}$  collected by SiD at a center of mass energy of 250 GeV.

	$h \rightarrow ZZ^*$ (%)
$e^+e^- \rightarrow 2 \text{ fermions}$	50
$e^+e^- \rightarrow 4 \text{ fermions}$	462
$e^+e^- \rightarrow 6 \text{ fermions}$	0
$\gamma\gamma \rightarrow X$	0
$\gamma e^+ \rightarrow X$	0
$e^- \gamma \rightarrow X$	0
$qqh \rightarrow ZZ^*$	68
$eeh, \mu\mu h \rightarrow ZZ^*$	24
$\tau\tau h \rightarrow ZZ^*$	3
$\nu\nu h \rightarrow ZZ^*$	49

$H \rightarrow ZZ^*$

$\Delta\sigma \bullet B / \sigma \bullet B = 18\%$

for  $250 \text{ fb}^{-1}$  @  $\sqrt{s} = 250$  GeV

H. Neal, SLAC

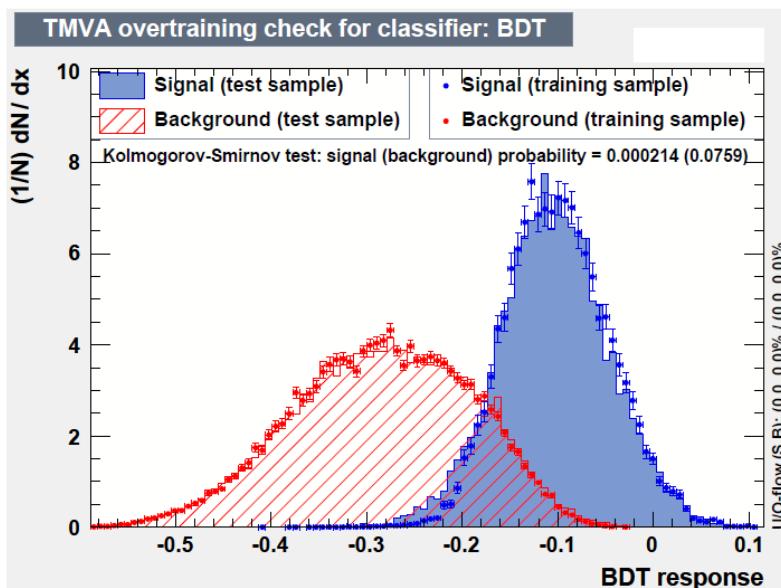


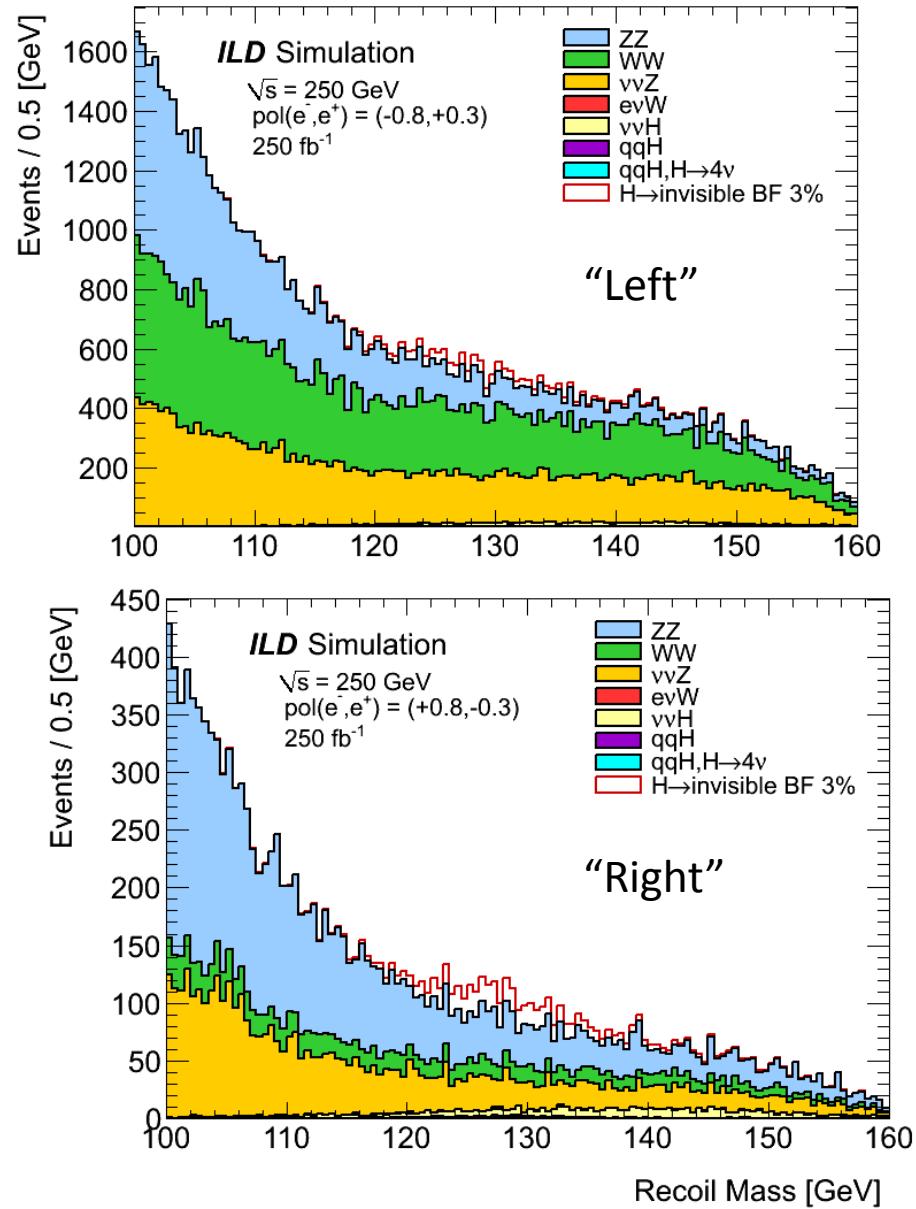
Figure 5.2. The multi-variate BDT output for the signal ( $h \rightarrow ZZ^*$ ) and background for the training samples and test samples (points).

$\sigma \bullet BR(H \rightarrow invisible)$  : New Analysis at  $\sqrt{s} = 250$  GeV

$H \rightarrow invisible$

$BR(invisible) < 0.9\%$  at 95% CL  
for  $250 \text{ fb}^{-1}$  @  $\sqrt{s} = 250$  GeV

A. Ishikawa (Tohoku Univ)



$e^+e^- \rightarrow ZHH$

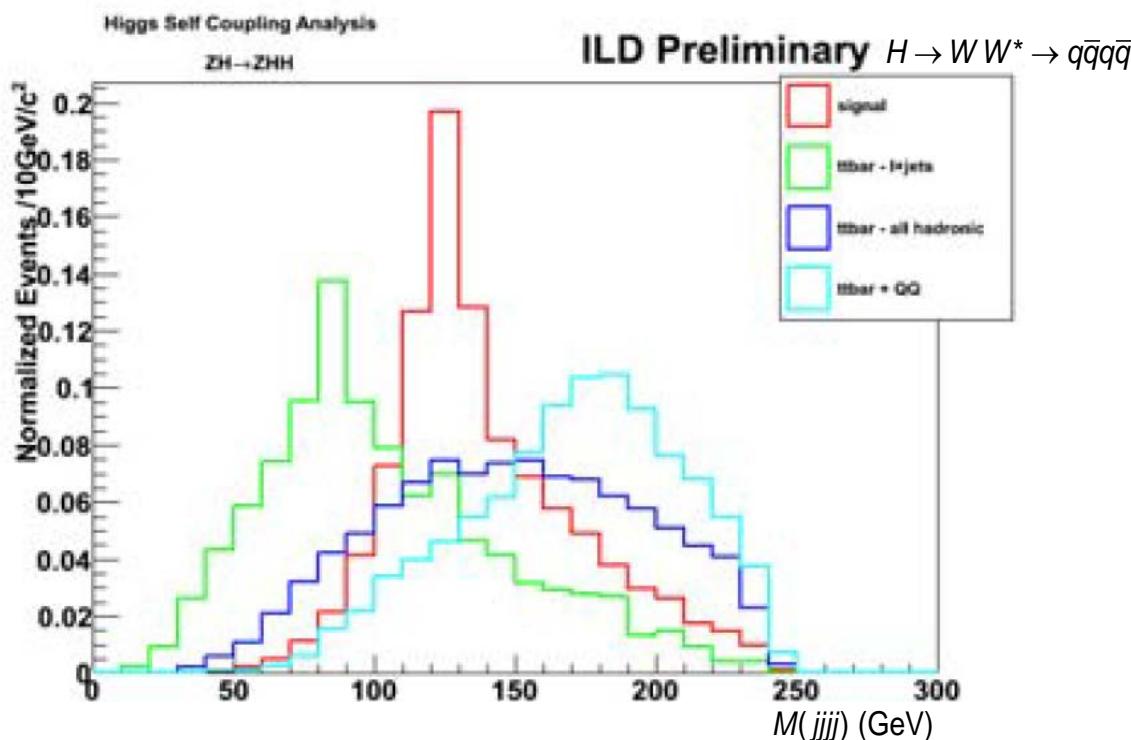
Combining  $HH \rightarrow b\bar{b}b\bar{b}$  &  $b\bar{b}WW^*$

$\Delta\sigma/\sigma = 42.7\%$  for  $500 \text{ fb}^{-1}$  at  $\sqrt{s} = 500 \text{ GeV}$

M. Kurata, T. Tanbe (Univ Tokyo)

J. Tlan, K. Fujii (KEK)

T. Suehara (Tohoku Univ)



Energy(GeV)	Modes	Z decay	Signal	Background	Significance
500	All hadronic	$Z \rightarrow b\bar{b}$ 4-btag	15.20	87.52	$1.50\sigma$
		$Z \rightarrow b\bar{b}$ 3-btag	19.43	3099.49	$0.35\sigma$
		$Z \rightarrow c\bar{c}$	11.29	366.13	$0.58\sigma$
500	Lepton + jets	$Z \rightarrow b\bar{b}$	1.65	17.62	$0.38\sigma$
		$Z \rightarrow c\bar{c}$	0.88	146.09	$0.04\sigma$
500	Dilepton	$Z \rightarrow l\bar{l}$	2.24	8.44	$0.69\sigma$
500	Trilepton	$Z \rightarrow l\bar{l}$	1.05	2.60	$0.55\sigma$
combined					$1.91\sigma$

# ILC Measurement Summary

**Table 5.1.** Expected accuracies for cross section and cross section times branching ratio measurements for the 125 GeV  $h$  boson assuming you run  $3 \times 10^7$  s at the baseline differential luminosity for each center of mass energy. For invisible decays of the Higgs, the number quoted is the 95% confidence upper limit on the branching ratio.

$\sqrt{s}$ and $\mathcal{L}$ ( $P_{e-}, P_{e+}$ )	250 $\text{fb}^{-1}$ at 250 GeV (-0.8,+0.3)		500 $\text{fb}^{-1}$ at 500 GeV (-0.8,+0.3)			1 $\text{ab}^{-1}$ at 1 TeV (-0.8,+0.2)			
	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$tth$	$Zhh$	$\nu\bar{\nu}h$	$tth$	$\nu\bar{\nu}hh$
$\Delta\sigma/\sigma$	2.6%	-	3.0	-		42.7%			26.3%
BR(invis.)	< 0.9 %	-	-	-	-				
mode	$\Delta(\sigma \cdot BR)/(\sigma \cdot BR)$								
$h \rightarrow bb$	1.2%	10.5%	1.8%	0.7%	28%		0.5%	6.0%	
$h \rightarrow c\bar{c}$	8.3%	-	13%	6.2%			3.1%		
$h \rightarrow gg$	7.0%	-	11%	4.1%			2.3%		
$h \rightarrow WW^*$	6.4%	-	9.2%	2.4%			1.6%		
$h \rightarrow \tau^+\tau^-$	4.2%	-	5.4%	9.0%			3.1%		
$h \rightarrow ZZ^*$	19%	-	25%	8.2%			4.1%		
$h \rightarrow \gamma\gamma$	34%	-	34%	23%			8.5%		
$h \rightarrow \mu^+\mu^-$	100%	-	-	-			31%		

**Table 5.2.** Expected accuracies for cross section and cross section times branching ratio measurements for the 125 GeV  $h$  boson assuming you run  $3 \times 10^7$  s at the sum of the baseline and upgrade differential luminosities for each center of mass energy. For invisible decays of the Higgs, the number quoted is the 95% confidence upper limit on the branching ratio.

$\sqrt{s}$ and $\mathcal{L}$ ( $P_{e-}, P_{e+}$ )	1150 $\text{fb}^{-1}$ at 250 GeV (-0.8,+0.3)		1600 $\text{fb}^{-1}$ at 500 GeV (-0.8,+0.3)			2.5 $\text{ab}^{-1}$ at 1 TeV (-0.8,+0.2)			
	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$tth$	$Zhh$	$\nu\bar{\nu}h$	$tth$	$\nu\bar{\nu}hh$
$\Delta\sigma/\sigma$	1.2%	-	1.7	-		23.7%			16.7%
BR(invis.)	< 0.4 %	-	-	-	-		-		
mode	$\Delta(\sigma \cdot BR)/(\sigma \cdot BR)$								
$h \rightarrow bb$	0.6%	4.9%	1.0%	0.4%	16%		0.3%	3.8%	
$h \rightarrow c\bar{c}$	3.9%	-	7.2%	3.5%			2.0%		
$h \rightarrow gg$	3.3%	-	6.0%	2.3%			1.4%		
$h \rightarrow WW^*$	3.0%	-	5.1%	1.3%			1.0%		
$h \rightarrow \tau^+\tau^-$	2.0%	-	3.0%	5.0%			2.0%		
$h \rightarrow ZZ^*$	8.8%	-	14%	4.6%			2.6%		
$h \rightarrow \gamma\gamma$	16%	-	19%	13%			5.4%		
$h \rightarrow \mu^+\mu^-$	46.6%	-	-	-			20%		

## Model Independent Fit of Cross Sections and BR's

**Table 6.3.** Summary of expected accuracies for the three cross sections and eight branching ratios obtained from an eleven parameter global fit of all available data.

	ILC(250)	ILC500	ILC(1000)	ILC(LumUp)
process	$\Delta\sigma/\sigma$			
$e^+e^- \rightarrow ZH$	2.6 %	2.0 %	2.0 %	1.0 %
$e^+e^- \rightarrow \nu\bar{\nu}H$	11 %	2.3 %	2.2 %	1.1 %
$e^+e^- \rightarrow t\bar{t}H$	-	28 %	6.3 %	3.8 %
mode	$\Delta\text{Br}/\text{Br}$			
$H \rightarrow ZZ$	19 %	7.5 %	4.2 %	2.4 %
$H \rightarrow WW$	6.9 %	3.1 %	2.5 %	1.3 %
$H \rightarrow b\bar{b}$	2.9 %	2.2 %	2.2 %	1.1 %
$H \rightarrow c\bar{c}$	8.7 %	5.1 %	3.4 %	1.9 %
$H \rightarrow gg$	7.5 %	4.0 %	2.9 %	1.6 %
$H \rightarrow \tau^+\tau^-$	4.9 %	3.7 %	3.0 %	1.6 %
$H \rightarrow \gamma\gamma$	34 %	17 %	7.9 %	4.7 %
$H \rightarrow \mu^+\mu^-$	100 %	100 %	31 %	20 %

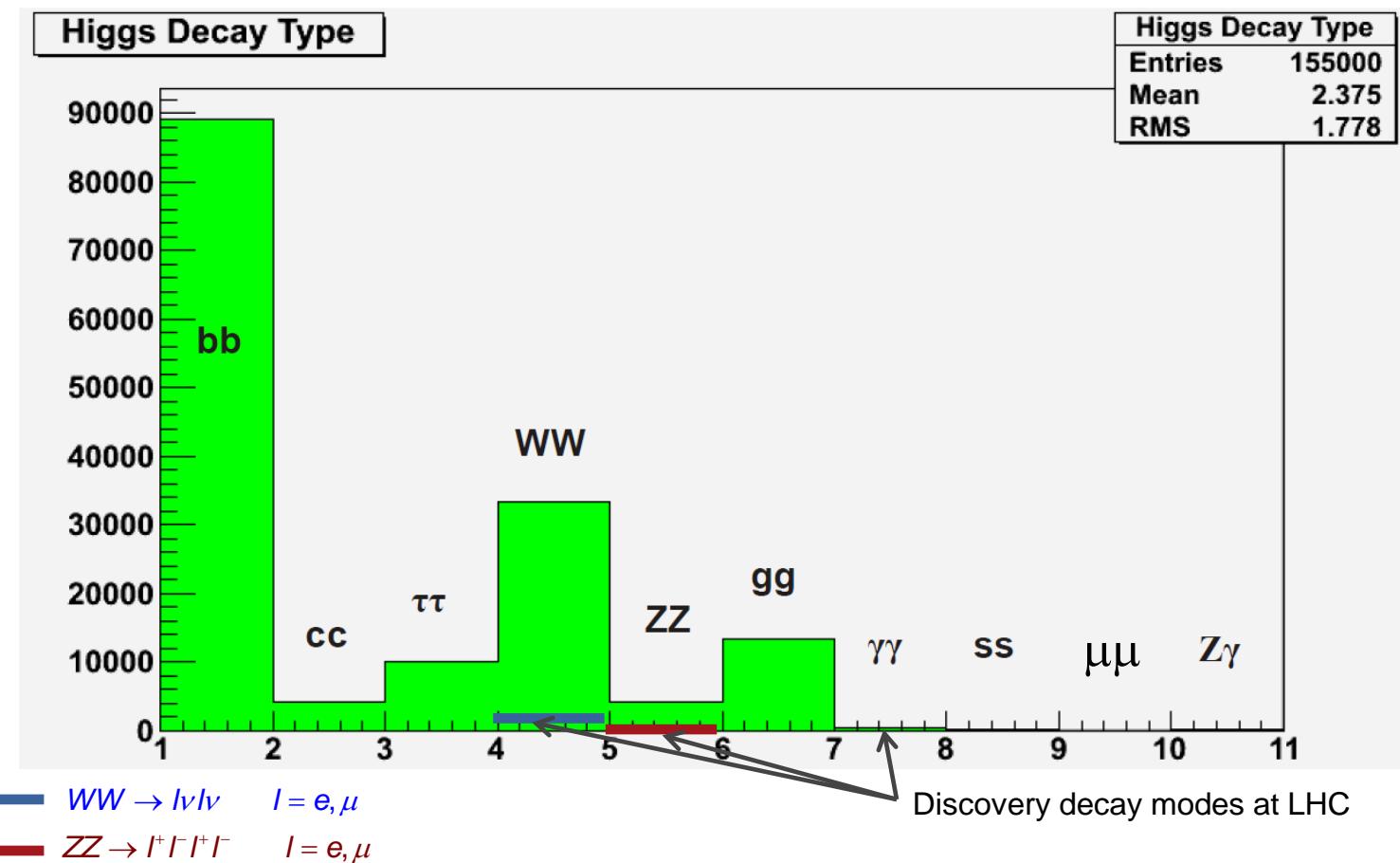
# Model Independent Fit of Higgs Couplings

**Table 9.1.** Summary of expected accuracies  $\Delta g_i/g_i$  for model independent determinations of the Higgs boson couplings. The theory errors are  $\Delta F_i/F_i = 0.1\%$ . For the invisible branching ratio, the numbers quoted are 95% confidence upper limits.

	ILC(250)	ILC(500)	ILC(1000)	ILC(LumUp)
$\sqrt{s}$ (GeV)	250	250+500	250+500+1000	250+500+1000
L ( $\text{fb}^{-1}$ )	250	250+500	250+500+1000	1150+1600+2500
$\gamma\gamma$	18 %	8.4 %	4.0 %	2.4 %
$gg$	6.4 %	2.3 %	1.6 %	0.9 %
$WW$	4.8 %	1.1 %	1.1 %	0.6 %
$ZZ$	1.3 %	1.0 %	1.0 %	0.5 %
$t\bar{t}$	–	14 %	3.1 %	1.9 %
$b\bar{b}$	5.3 %	1.6 %	1.3 %	0.7 %
$\tau^+\tau^-$	5.7 %	2.3 %	1.6 %	0.9 %
$c\bar{c}$	6.8 %	2.8 %	1.8 %	1.0 %
$\mu^+\mu^-$	91%	91%	16 %	10 %
$\Gamma_T(h)$	12 %	4.9 %	4.5 %	2.3 %
$hh$	–	83 %	21 %	13 %
BR(invis.)	< 0.9 %	< 0.9 %	< 0.9 %	< 0.4 %

## ILC vs LHC: General Considerations

- All beam crossings are triggered at the ILC
- All background is electroweak.
- Roughly, the detection efficiency is independent of decay mode  $\Rightarrow \Delta(\sigma \cdot BR) / (\sigma \cdot BR) \propto 1/\sqrt{BR}$
- LHC Higgs detection efficiency is uneven across decay modes.
- Higgs was discovered in decays modes with  $\gamma, e, \mu$ , which have relatively small BR's
- Qualitatively, there is complementarity between the ILC and LHC with respect to decay modes.



## 7 Parameter HXSWG Benchmark \*

Mode	LHC		ILC(1000)	ILC(LumUp)	$\sqrt{s}$ (GeV) L ( $\text{fb}^{-1}$ )
	300 $\text{fb}^{-1}$	3000 $\text{fb}^{-1}$	250+500+1000	250+500+1000	
	250+500+1000	1150+1600+2500			
$\gamma\gamma$	(5 – 7)%	(2 – 5)%	3.8 %	2.3 %	
$gg$	(6 – 8)%	(3 – 5)%	1.1 %	0.7 %	
$WW$	(4 – 5)%	(2 – 3)%	0.3 %	0.2 %	
$ZZ$	(4 – 5)%	(2 – 3)%	0.5 %	0.3 %	
$t\bar{t}$	(14 – 15)%	(7 – 10)%	1.3 %	0.9 %	
$b\bar{b}$	(10 – 13)%	(4 – 7)%	0.6 %	0.4 %	
$\tau^+\tau^-$	(6 – 8)%	(2 – 5)%	1.3 %	0.7 %	

\* Assume  $\kappa_c = \kappa_t$  &  $\Gamma_{tot} = \sum_{\text{SM decays i}} \Gamma_i^{SM} \kappa_i^2$

## Other Higgs Couplings

Mode	LHC		ILC(1000) 250+500+1000	ILC(LumUp) 250+500+1000 1150+1600+2500	$\sqrt{s}$ (GeV)
	300 $\text{fb}^{-1}$	3000 $\text{fb}^{-1}$	250+500+1000	1150+1600+2500	$L (\text{fb}^{-1})$
$c\bar{c}$	-	-	1.8 %	1.0 %	
$\mu^+\mu^-$	30%	10%	16 %	10 %	
$\Gamma_T(h)$	-	-	4.5 %	2.3 %*	
$hh$	-	50%	21 %	13 %*	
BR(invis.)	<(17–28)%	<(6-17)%	< 0.9 %	< 0.4 %	

\* Does not include results from searches for non-SM decays, including invisible decays. The error on the total width will improve significantly once these results are incorporated into the fit.

\* Current full simulation result using  $H \rightarrow b\bar{b}$ ,  $WW^*$  only. Results will improve as more Higgs decay modes are added, and as jet combinatoric problems are solved.

## Alternate Luminosity Scenario

Nickname	Ecm(1) (GeV)	Lumi(1) (fb $^{-1}$ )	+	Ecm(2) (GeV)	Lumi(2) (fb $^{-1}$ )	Runtime (yr)	Wallplug E (MW-yr)
ILC(250)	250	250				1.1	130
ILC(500)	250	250		500	500	2.0	270
ILC500(LumUp)	250	1150		500	1600	3.9	660

### 7 Parameter HXSWG Benchmark \*

	ILC500(LumUp)	ILC(LumUp)
$\sqrt{s}$ (GeV)	250+500	250+500+1000
$L$ (fb $^{-1}$ )	1150+1600	1150+1600+2500
$\gamma\gamma$	4.4 %	2.3 %
$gg$	1.1 %	0.7 %
$WW$	0.3 %	0.2 %
$ZZ$	0.3 %	0.3 %
$t\bar{t}$	1.4 %	0.9 %
$b\bar{b}$	0.6 %	0.4 %
$\tau^+\tau^-$	1.0 %	0.7 %

\* Assume  $\kappa_c = \kappa_t$  &  $\Gamma_{tot} = \sum_{SM \text{ decays i}} \Gamma_i^{SM} \kappa_i^2$

## Alternate Luminosity Scenario

Nickname	Ecm(1) (GeV)	Lumi(1) (fb $^{-1}$ )	+	Ecm(2) (GeV)	Lumi(2) (fb $^{-1}$ )	Runtime (yr)	Wallplug E (MW-yr)
ILC(250)	250	250				1.1	130
ILC(500)	250	250		500	500	2.0	270
ILC500(LumUp)	250	1150		500	1600	3.9	660

## Other Higgs Couplings

	ILC500(LumUp)	ILC(LumUp)
$\sqrt{s}$ (GeV)	250+500	250+500+1000
$L$ (fb $^{-1}$ )	1150+1600	1150+1600+2500
$c\bar{c}$	1.5 %	1.0 %
$\mu^+\mu^-$	42 %	10 %
$\Gamma_T(h)$	2.5 %	2.3 %
$hhh$	46 %	13 %
BR(invis.)	< 0.4 %	< 0.4 %

Combining LHC Results with Results from Various Future  $e^+e^-$  Colliders  
 (from D. Zerwas and the SFITTER Group)

Range corresponds to 2 different sys error assumptions for HL-LHC

coupling	LHC +ILC	LHC +ILC Lumi-up	HL-LHC +ILC Lumi-up	HL-LHC +CLIC	HL-LHC +ILC Lumi-up +CLIC	HL-LHC +TLEP +CLIC
$\Gamma_H$	2.0 – 2.0%	1.1 – 1.1%	1.1 – 1.1%	4.4 – 7.3%	0.9 – 1.0%	1.1 – 1.2%
$BR_{inv}$	0.8 – 0.8%	0.4 – 0.4%	0.4 – 0.4%	2.2 – 3.9%	0.4 – 0.4%	0.5 – 0.5%
$\kappa_\gamma$	2.4 – 2.7%	2.0 – 2.2%	1.3 – 2.0%	1.8 – 3.4%	1.2 – 2.0%	1.2 – 1.6%
$\kappa_g$	1.3 – 1.3%	0.8 – 0.8%	0.8 – 0.8%	1.3 – 2.0%	0.6 – 0.6%	0.6 – 0.6%
$\kappa_W$	0.5 – 0.5%	0.3 – 0.3%	0.3 – 0.3%	1.1 – 1.9%	0.3 – 0.3%	0.3 – 0.3%
$\kappa_Z$	0.6 – 0.6%	0.3 – 0.3%	0.3 – 0.3%	1.1 – 1.9%	0.3 – 0.3%	0.3 – 0.3%
$\kappa_\mu$	13.8 – 14.2%	9.9 – 9.9%	7.0 – 7.8%	5.2 – 6.0%	4.6 – 4.7%	4.0 – 4.1%
$\kappa_\tau$	1.5 – 1.6%	0.9 – 0.9%	0.7 – 0.9%	1.3 – 2.3%	0.7 – 0.8%	0.5 – 0.6%
$\kappa_c$	1.6 – 1.6%	0.9 – 0.9%	0.9 – 0.9%	1.4 – 2.1%	0.7 – 0.7%	0.7 – 0.7%
$\kappa_b$	0.8 – 0.8%	0.5 – 0.5%	0.5 – 0.5%	1.1 – 1.9%	0.3 – 0.3%	0.4 – 0.4%
$\kappa_t$	2.8 – 2.9%	1.9 – 1.9%	1.7 – 1.8%	3.5 – 4.5%	1.7 – 1.8%	3.2 – 3.8%
$\Delta_\gamma$	2.5 – 2.8%	2.0 – 2.2%	1.5 – 2.1%	2.8 – 4.6%	1.4 – 2.0%	1.7 – 2.0%
$\Delta_g$	3.8 – 3.8%	2.5 – 2.5%	2.3 – 2.4%	4.1 – 4.8%	2.1 – 2.3%	4.0 – 4.7%

Typical coupling variations for several BSM Higgs models:

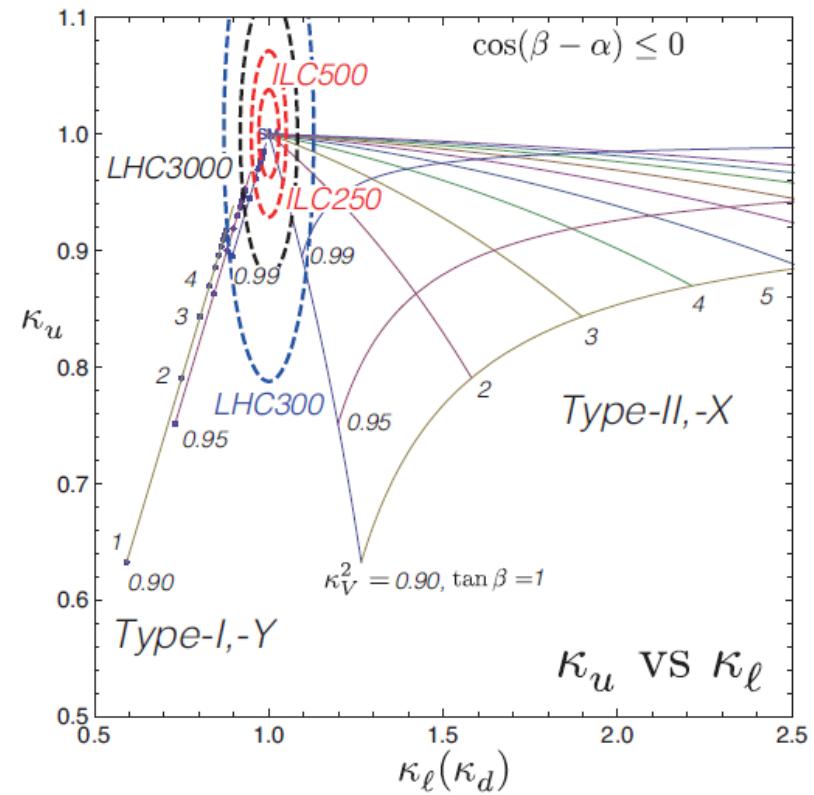
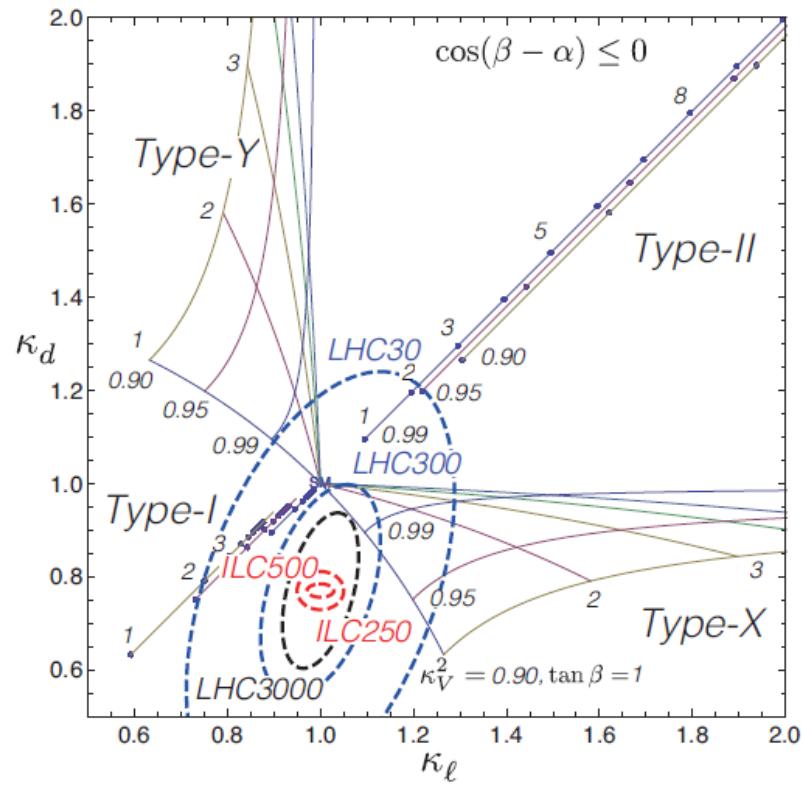
What do these precision values mean?

For Higgs couplings, better precision means greater discovery potential.

	$\kappa_V$	$\kappa_b$	$\kappa_\gamma$
Singlet Mixing	$\sim 6\%$	$\sim 6\%$	$\sim 6\%$
2HDM	$\sim 1\%$	$\sim 10\%$	$\sim 1\%$
Decoupling MSSM	$\sim -0.0013\%$	$\sim 1.6\%$	$< 1.5\%$
Composite	$\sim -3\%$	$\sim -(3 - 9)\%$	$\sim -9\%$
Top Partner	$\sim -2\%$	$\sim -2\%$	$\sim -3\%$

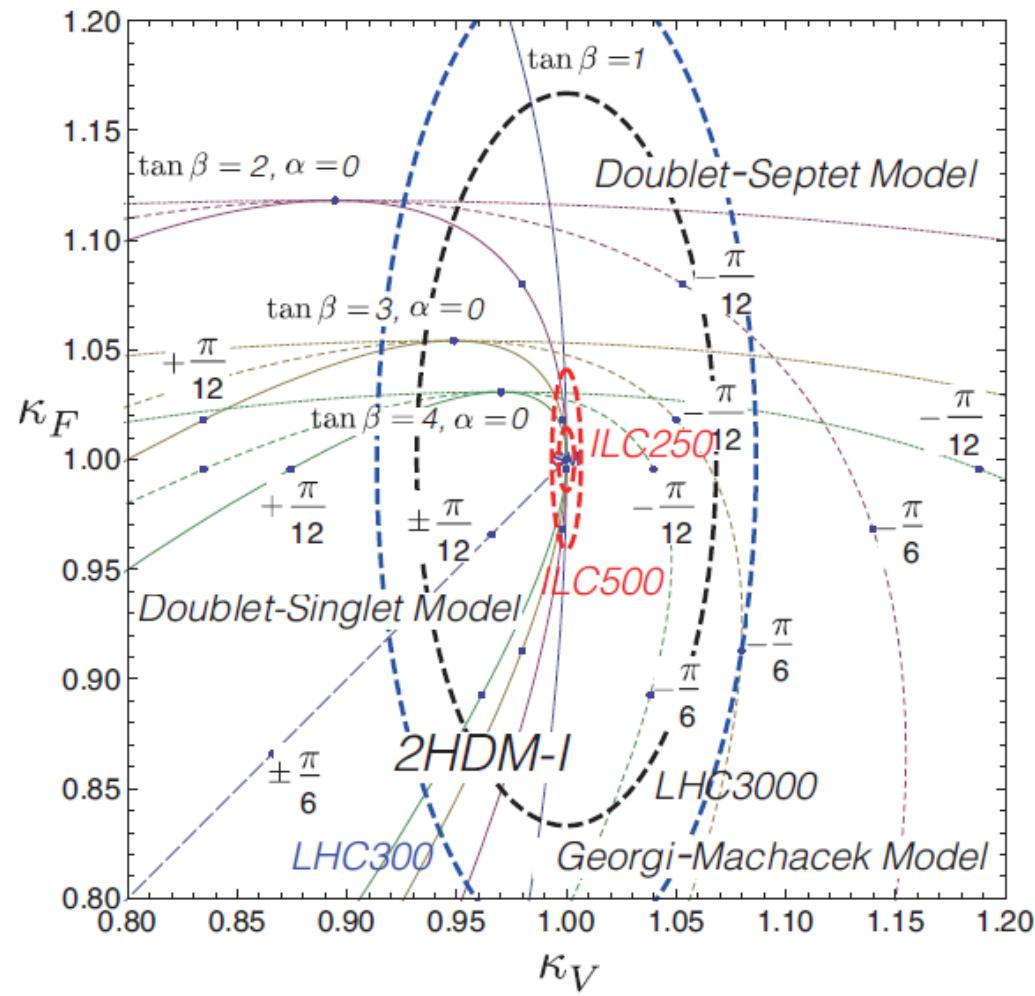
# Plots from Theory Section of ILC Higgs White Paper

2HDM:



# Plots from Theory Section of ILC Higgs White Paper

Models with Universal  
Yukawa and Gauge  
Couplings



## Other Studies Included in ILC Higgs White Paper

- Higgs CP using  $e^+e^- \rightarrow t\bar{t}h$
- Lorentz Structure of  $hWW$  coupling
- Higgs physics with an ILC  $\gamma\gamma$  collider