

# Model Dependent Higgs Couplings

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# Model Independent Coupling Determination

Fit for 9 couplings and the Higgs total width

(  $g_Z, g_W, g_b, g_c, g_s, g_\tau, g_\mu, g_t, g_\gamma, \Gamma_0$  )

by minimizing  $\chi^2$  :

$$\chi^2 = \sum_{i=1}^{33} \left( \frac{Y_i - Y_i'}{\Delta Y_i} \right)^2 \quad Y_i = \begin{cases} \sigma \times BR, & i=1, \dots, 32 \\ \sigma_{ZH}, & i = 33 \end{cases}$$

$$Y_i' = F_i \cdot \frac{g_Z^2 g_X^2}{\Gamma_0}, \quad F_i \cdot \frac{g_W^2 g_X^2}{\Gamma_0} \quad \text{or} \quad F_i \cdot \frac{g_t^2 g_X^2}{\Gamma_0}$$

We neglect theory errors on  $F_i$

# Model Independent Coupling Summary

$$\Delta g_{Hxx} / g_{Hxx}$$

| Mode           | ILC(250) | ILC500   | ILC(1000) | ILC(LumUp) |
|----------------|----------|----------|-----------|------------|
| $WW$           | 4.8 %    | 1.4 %    | 1.4 %     | 0.65 %     |
| $ZZ$           | 1.3 %    | 1.3 %    | 1.3 %     | 0.61 %     |
| $t\bar{t}$     | –        | 18 %     | 4.0 %     | 2.5 %      |
| $b\bar{b}$     | 5.3 %    | 1.8 %    | 1.5 %     | 0.75 %     |
| $\tau^+\tau^-$ | 5.7 %    | 2.5 %    | 2.0 %     | 1.0 %      |
| $\gamma\gamma$ | 18 %     | 8.4 %    | 4.1 %     | 2.4 %      |
| $gg$           | 6.4 %    | 2.5 %    | 1.8 %     | 0.94 %     |
| $c\bar{c}$     | 6.8 %    | 3.0 %    | 2.0 %     | 1.1 %      |
| $\mu^+\mu^-$   | –        | –        | 16 %      | 10 %       |
| $\Gamma_T(h)$  | 11 %     | 6.0 %    | 5.6 %     | 2.7 %      |
| self           | –        | 88%      | 25 %      | 16 %       |
| * BR(invis.)   | < 0.69 % | < 0.69 % | < 0.69 %  | < 0.32 %   |

\* 95% C.L. limit

# Model Dependent Coupling Fits

Alternatively, ILC can fit for the  $\kappa_i$  coupling scaling factors of arXiv : 1029.0040.

SFitter  
ILC (250)

## Model Independent Coupling Fits

SFitter  
ILC (LumUp)

| coupling        | 250 GeV | Mode           | ILC(250) | ILC500 | ILC(1000) | ILC(LumUp) | coupling        | high-lumi |
|-----------------|---------|----------------|----------|--------|-----------|------------|-----------------|-----------|
| $\kappa_W$      | 5.6 %   | $WW$           | 4.8 %    | 1.4 %  | 1.4 %     | 0.65 %     | $\kappa_W$      | 0.57 %    |
| $\kappa_Z$      | 1.1 %   | $ZZ$           | 1.3 %    | 1.3 %  | 1.3 %     | 0.61 %     | $\kappa_Z$      | 0.47 %    |
| $\kappa_t$      | 9.8 %   | $t\bar{t}$     | –        | 18 %   | 4.0 %     | 2.5 %      | $\kappa_t$      | 1.7 %     |
| $\kappa_b$      | 6.0 %   | $b\bar{b}$     | 5.3 %    | 1.8 %  | 1.5 %     | 0.75 %     | $\kappa_b$      | 1.2 %     |
| $\kappa_\tau$   | 7.2 %   | $\tau^+\tau^-$ | 5.7 %    | 2.5 %  | 2.0 %     | 1.0 %      | $\kappa_\tau$   | 1.7 %     |
| $\kappa_\gamma$ | 18.0 %  | $\gamma\gamma$ | 18 %     | 8.4 %  | 4.1 %     | 2.4 %      | $\kappa_\gamma$ | 3.4 %     |
| $\kappa_g$      | 8.6 %   | $gg$           | 6.4 %    | 2.5 %  | 1.8 %     | 0.94 %     | $\kappa_g$      | 1.7 %     |

This isn't right. The model dependent values should ALWAYS be better than the model independent values because we are adding constraints to the model independent fits when we do model dependent fits.

## Model Dependent Coupling Determination Proposal

This example uses the constraints from the 7 parameter fit

$(\kappa_Z, \kappa_W, \kappa_b, \kappa_g, \kappa_\tau, \kappa_t, \kappa_\gamma)$  by ATLAS and CMS

The constraints are  $\kappa_c = \kappa_t$  &  $\kappa_H^2 \cdot \Gamma_0 = \sum_i \kappa_i^2 \cdot \Gamma_i$

For ILC we still fit for 9 couplings and the Higgs total width

$(g_Z, g_W, g_b, g_c, g_g, g_\tau, g_\mu, g_t, g_\gamma, \Gamma_0)$

but now by minimizing this  $\chi^2$ :

$$\chi^2 = \sum_{i=1}^{33} \left( \frac{Y_i - Y_i'}{\Delta Y_i} \right)^2 + \left( \frac{\xi_{ct}}{\Delta \xi_{ct}} \right)^2 + \left( \frac{\xi_\Gamma}{\Delta \xi_\Gamma} \right)^2$$

where

$$\xi_{ct} = \frac{g_c}{g_c^{SM}(M_c, \dots)} - \frac{g_t}{g_t^{SM}(M_t, \dots)} \quad \xi_\Gamma = \Gamma_0 - \sum_{i=1}^9 \Gamma_i \quad , \quad \Gamma_i = G_i(M_H, \dots) \cdot g_i^2$$

$\Delta \xi_{ct}$  = theory error on  $\xi_{ct}$  obtained by propagating theory errors on  $g_c^{SM}(M_c, \dots)$  and  $g_t^{SM}(M_t, \dots)$

$\Delta \xi_\Gamma$  = theory error on  $\xi_\Gamma$  obtained by propagating (correlated) theory errors on  $G_i(M_H, \dots)$