

Higgs Recoil Mass Study

Feb 7, 2014

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www.illustrationart.com

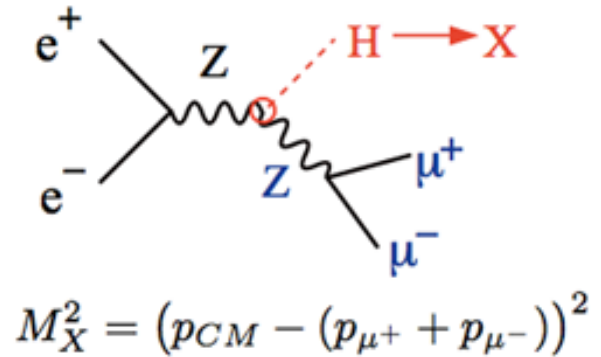
**recoil mass study using $e^+e^- \rightarrow Zh \rightarrow \mu^+\mu^-h$
@ $E_{c.m.s.} = 250 \text{ GeV}$, $L = 250 \text{ fb}^{-1}$**

Goal:

precise measurement of

- Higgs mass
- cross section σ_H : $N = \sigma * L * \epsilon$

polarization:
 $(e^-, e^+) = (0.8, 0.3)$



Changes from previous week

- ❑ data selection optimization (adjust cut window for invariant mass and coplanarity)
→ **improved signal efficiency and significance**
- ❑ estimate error on efficiency and cross section
- ❑ compare with results between different polarization
 $(-0.8, +0.3)$ vs $(-0.8, 0)$ vs $(0, 0)$
- ❑ added all signal and BG processes, just to make sure



DBD Samples

event weight = $\text{pol_weight} * (\text{process_cross_section} * \text{assumed_integrated_luminosity})$
/ (number_of_reconstructed_events)

Signal sample:

Pe2e2h.eL.pR & Pe2e2h.eR.pL

relevant BG process for Zmumu

- 4f_ZZ_leptonic
- 4f_ZZ_semileptonic
- 2f_Z_leptonic
- 4f_WW_leptonic
- 4fSingleZee_leptonic
- 4fSingleZnnu_leptonic
- 4f_ZZWWMix_leptonic

dominant ones

eLpR	cross sec	weight
higgs	17.14	0.146
BG in order of large cross section		
2f_Z_l	21226.4	1.46
4f_ZZWWMix_l	1636.04	0.583
4f_WW_l	1564.21	0.573
4f_ZZ_sl	1422.14	0.583
4f_singleZee_l	1084.1	0.581
4f_singleZnn_l	192.75	0.47
4f_ZZ_l	157.96	0.578

Muon Selection

- reject neutrals
- $P_{tot} > 5 \text{ GeV}$
- $\text{small } E_{\text{cluster}} / P_{\text{total}} < 0.5$
- opposite charge

■ Best track selection

$$\cos(\text{track angle}) < 0.95$$
$$|D0/\delta D0| < 4$$

Next optimized
these parameters

Best Z Candidate Selection

2 mu candidates with **opposite charge**
if several possibilities :
choose pair **with invariant mass closest to Z mass**

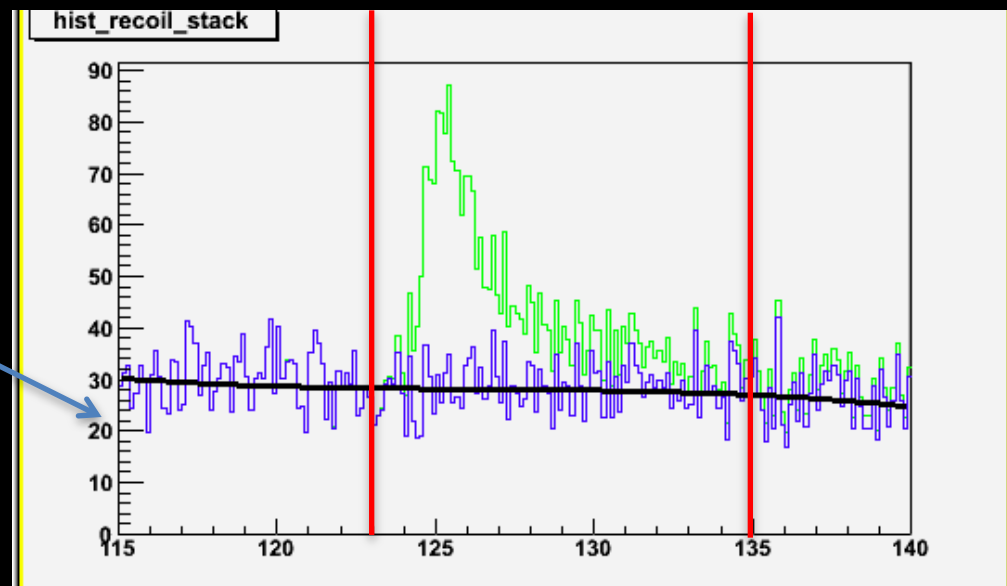
Final Selection from LAST WEEK

analysis after filling root files

- $86 \text{ GeV} < M_{\text{mumu}} < 95 \text{ GeV}$
- $123 \text{ GeV} < M_{\text{recoil}} < 135 \text{ GeV}$
- $10 \text{ GeV} < pT_{\text{mumu}} < 70 \text{ GeV}$
- $0.2 < \text{mumu_coplanarity} < 3$
- $|\cos(\theta_{\text{Zpro}})| < 0.91$
(Z production angle)

Evaluate data selection
efficiency in within range
of 123 – 135 GeV

calculate recoil mass with
correction for 14 mrad beam
crossing angle



Final Selection Optimization #1

Wider Minv cut

- $84 \text{ GeV} < M_{\text{mumu}} < 98 \text{ GeV}$
- $123 \text{ GeV} < M_{\text{recoil}} < 135 \text{ GeV}$
- $10 \text{ GeV} < pT_{\text{mumu}} < 70 \text{ GeV}$
- $\text{mumu_coplanarity} < 3$ removed lower limit on coplanarity
- $|\cos(\theta_{\text{Zpro}})| < 0.91$
(Z production angle)



Final Selection Optimization #2

- $84 \text{ GeV} < M_{\text{mumu}} < 98 \text{ GeV}$
- $123 \text{ GeV} < M_{\text{recoil}} < 135 \text{ GeV}$
- $10 \text{ GeV} < pT_{\text{mumu}} < 70 \text{ GeV}$
- $\text{mumu_coplanarity} < 3$ removed coplanarity cut
- $|\cos(\theta_{\text{Zpro}})| < 0.91$
(Z production angle)

Comparison of Some Parameters between Signal and BG Processes

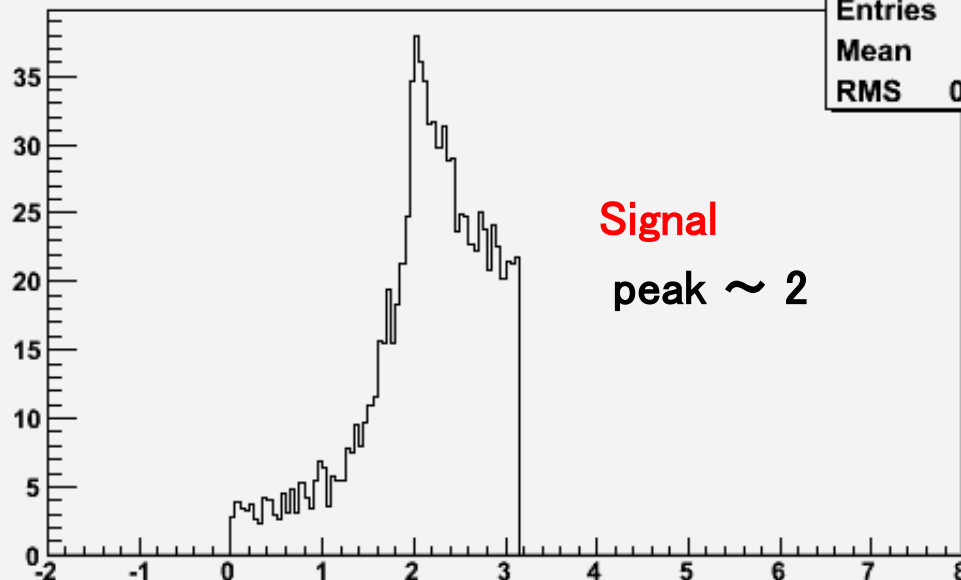
coplanarity
before cut

Tried to cut:

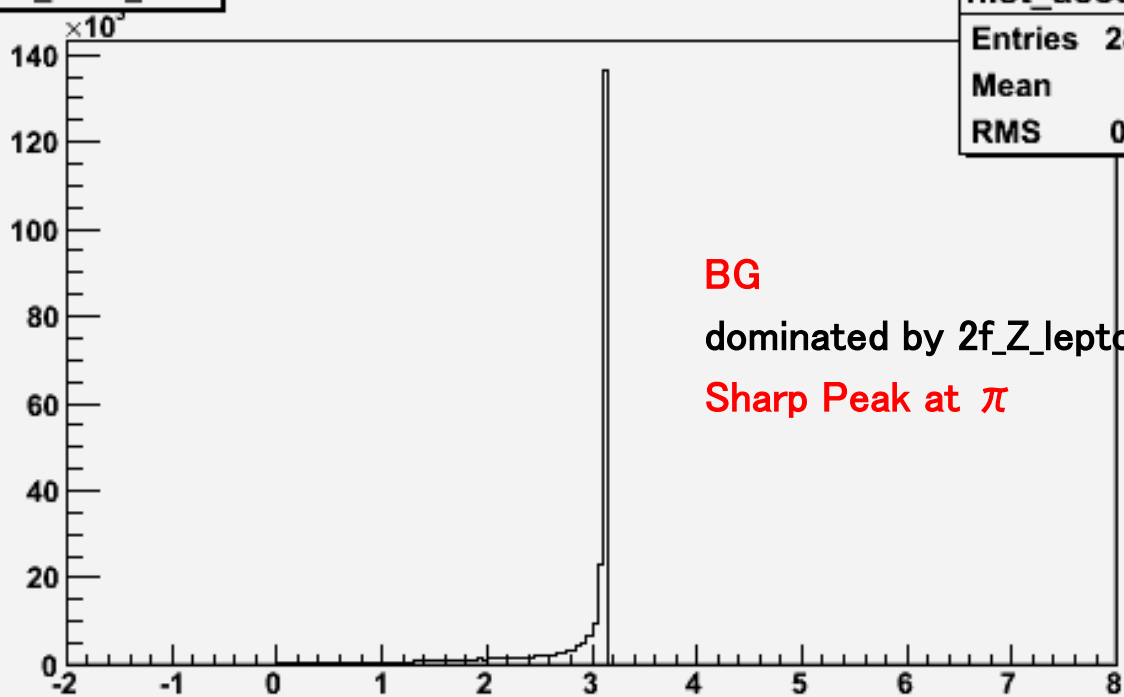
$0.2 < \text{cop} < 3$

or just $\text{cop} < 3$

hist_acos_jackieZH_higgs_ffh_Pe2e2h_eL_pR

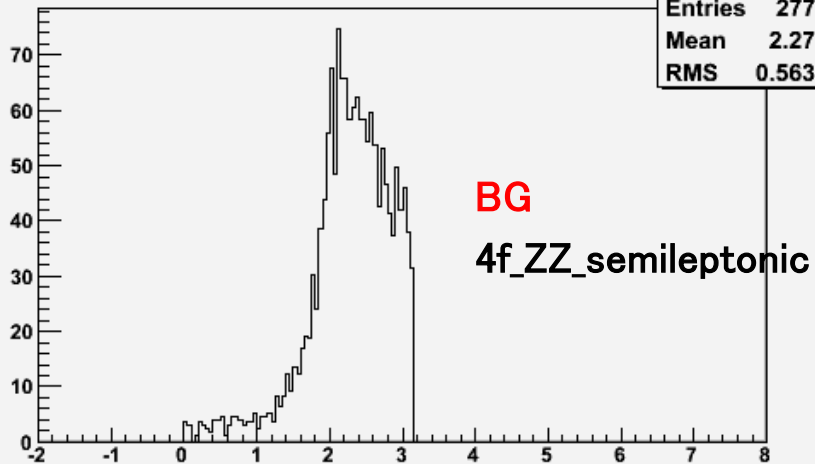


hist_acos_BG

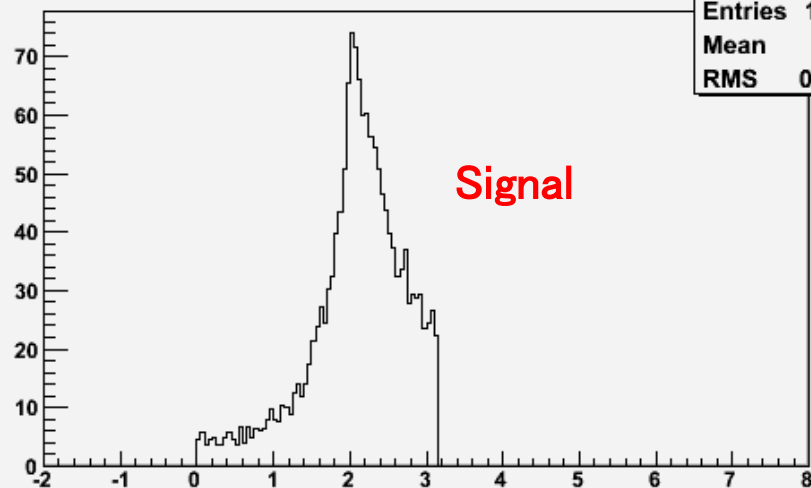


coplanarity, after all other cuts

hist_acos2_jackieZH_4f_ZZ_semileptonic_eL_pR



hist_acos2_jackieZH_higgs_ffh_Pe2e2h_eL_pR

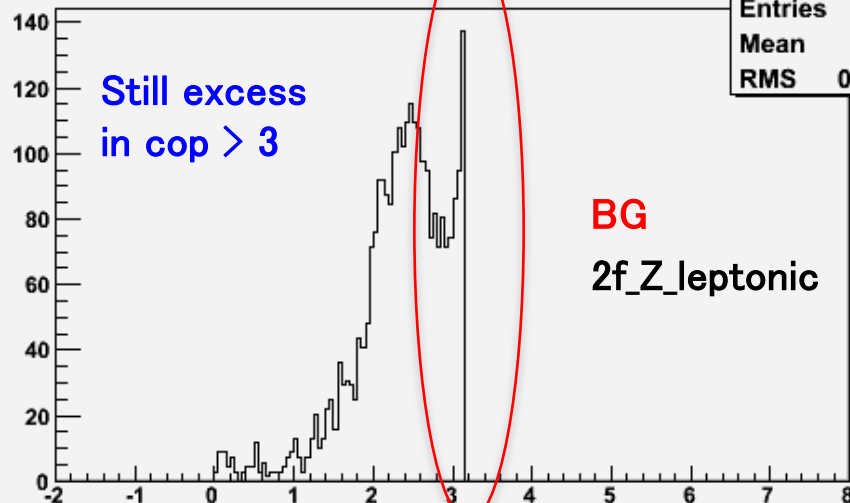


Trying to decide whether to use coplanarity cut

hist_acos2_jackieZH_4f_WW_leptonic_eL_pR



hist_acos2_jackieZH_2f_Z_leptonic_eL_pR



Z production angle

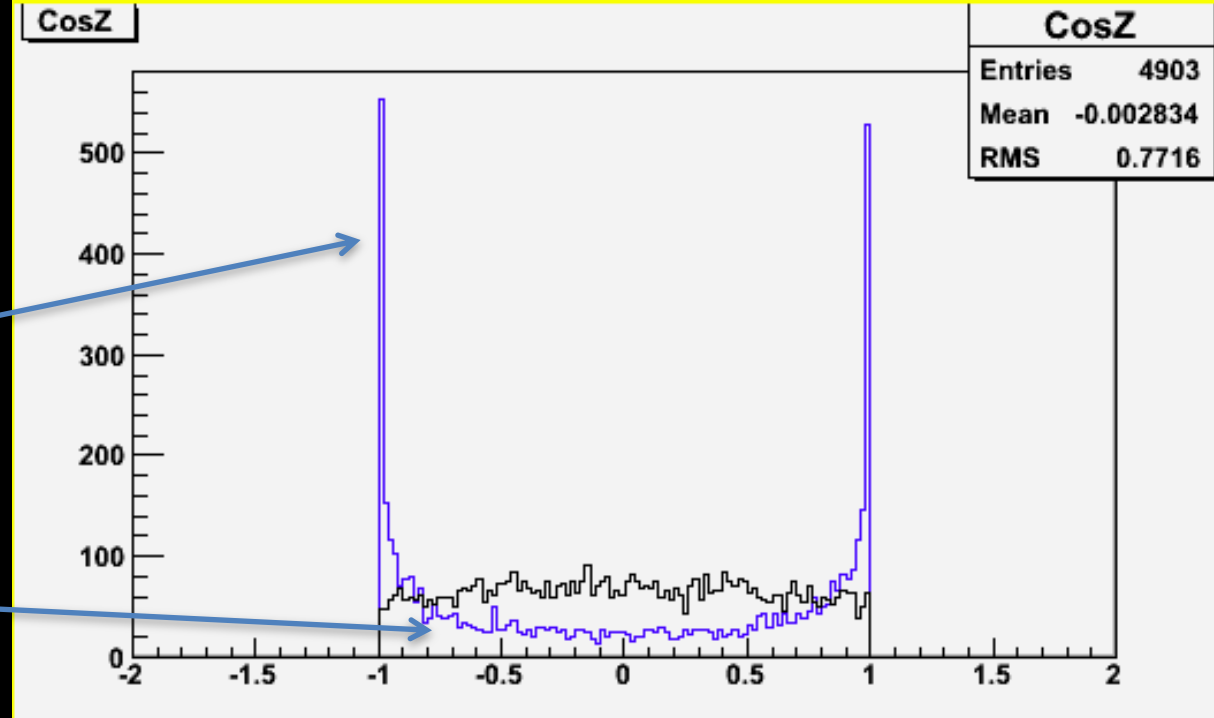
blue: BG (4f_ZZ_I)

very forward

→ use for cut

Black: Signal

isotropic



do cut : $|\cos(\theta_{Zpro})| < 0.91$

BG Rejection Efficiency : 123 – 135 GeV: last week

cut	signal	eff	BG_all	eff	S/N	S/sqrt(S+N)
no cut	2160	100%	50461	100%	0.043	9.416
best mu	1938	90%	34109	67.59%	0.057	10.207
M_inv	1600	74%	13283	26.32%	0.120	13.115
M_rec	1482	69%	8097	16.05%	0.183	15.142
P_Tdl	1463	68%	4032	7.99%	0.363	19.736
acop	1366	63%	3546	7.03%	0.385	19.490
θ_Z	1296	60%	2788	5.53%	0.465	20.280

Signal efficiency 60 %

S/N \rightarrow 0.47

Significance \sim 20.3

Improvement after change to coplanarity < 3 (remove lower limit)
 $\langle S \rangle = 1421$, Sig eff 66 %, S/B = 0.47, S/sqrt(S+B) = 20.6

after M_rec cut $\cos\theta_Z$ cut seem quite effective for improving S/N

cut	4f_ZZ_]	4f_ZZ_sl	2f_Z_]	4f_WW_]	4fSingleZee_]	4fSingleZnn_]	4f_ZZWWMix_]
no cut	989	4163	27574	5735	2295	810	8896
best mu	753	3251	19228	1543	880	668	7787
M_inv	337	1264	9865	219	151	356	1091
M_rec	204	765	6011	136	95	224	663
P_Tdl	181	742	2021	134	92	218	643
$0.2 < \text{cop} < 3$	156	680	1695	124	80	199	610
θ_Z	132	596	1164	115	69	175	537

NEWEST

BG Rejection Efficiency : 123 – 135 GeV

removed coplanarity altogether

cut	signal	eff	BG_all	eff	S/N	S/sqrt(S+N)
no cut	2160	100%	50461	100%	0.043	9.416
best mu	1938	90%	34109	67.59%	0.057	10.207
84 <M_inv <98	1742	81%	15359	30.44%	0.120	13.321
123 <M_rec <135	1606	74%	9330	18.49%	0.183	15.357
10 <P_TdI<70	1584	73%	4785	9.48%	0.363	19.848
cos(θ_Z)<0.91	1491	69%	3637	7.21%	0.385	20.821

Signal efficiency 69%

S/N \rightarrow 0.39

Significance \sim 20.8

cut	4f_ZZ_l	4f_ZZ_sl	2f_Z_l	4f_WW_l	4fSingleZe	4fSingleZr	4f_ZZWWMix_l
no cut	989	4163	27574	5735	2295	810	8896
best mu	753	3251	19228	1543	880	668	7787
84 <M_inv <98	379	1407	11047	350	174	392	1612
123 <M_rec <135	229	854	6710	212	108	242	976
10 <P_TdI<70	205	831	2259	208	105	235	944
cos(θ_Z)<0.91	168	719	1447	193	86	200	824

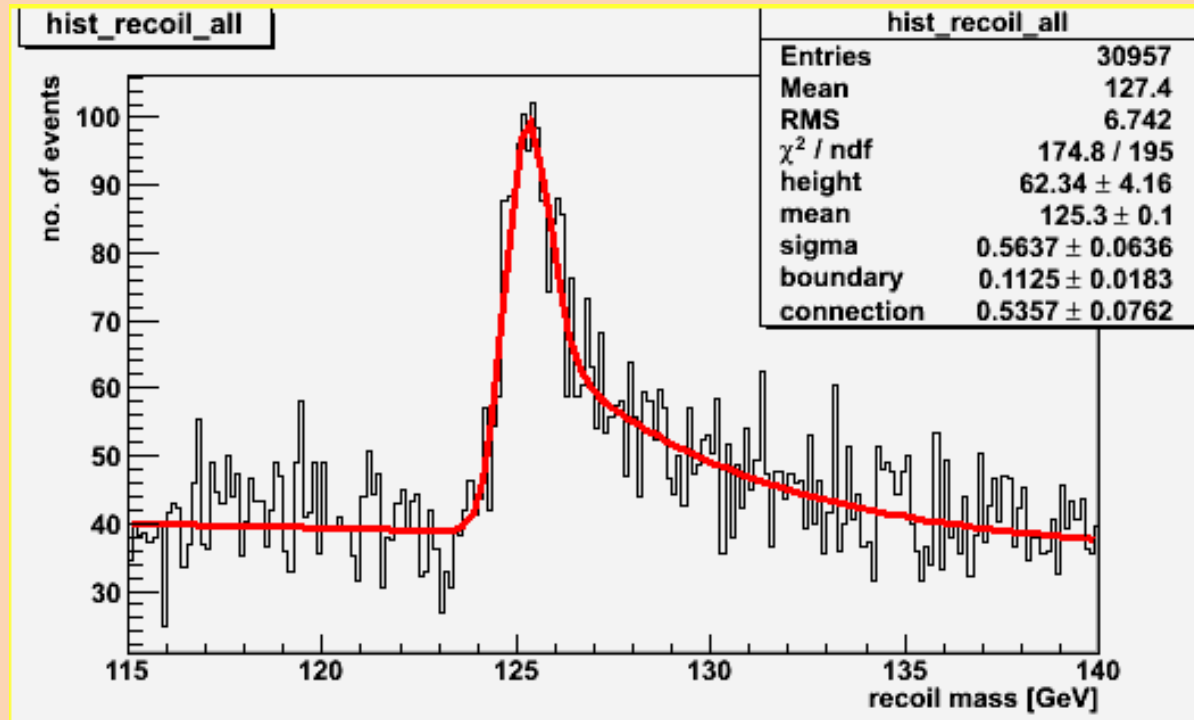
recoil mass

after implementing all cuts

fitted recoil mass :

$$M_h = 125.3 \text{ GeV} \pm 70 \text{ MeV}$$

calculate recoil mass with correction for 14 mrad beam crossing angle



◆ BG: 3rd order polynomial

◆ signal : GPET: 5 parameters : Gaus (left-side) , Gaus + expo (right side)

$$N \exp\left[-\frac{1}{2} \frac{(x - x_{\text{mean}})^2}{\sigma^2}\right] \exp\left[-k \frac{(x - x_{\text{mean}})}{\sigma}\right]$$

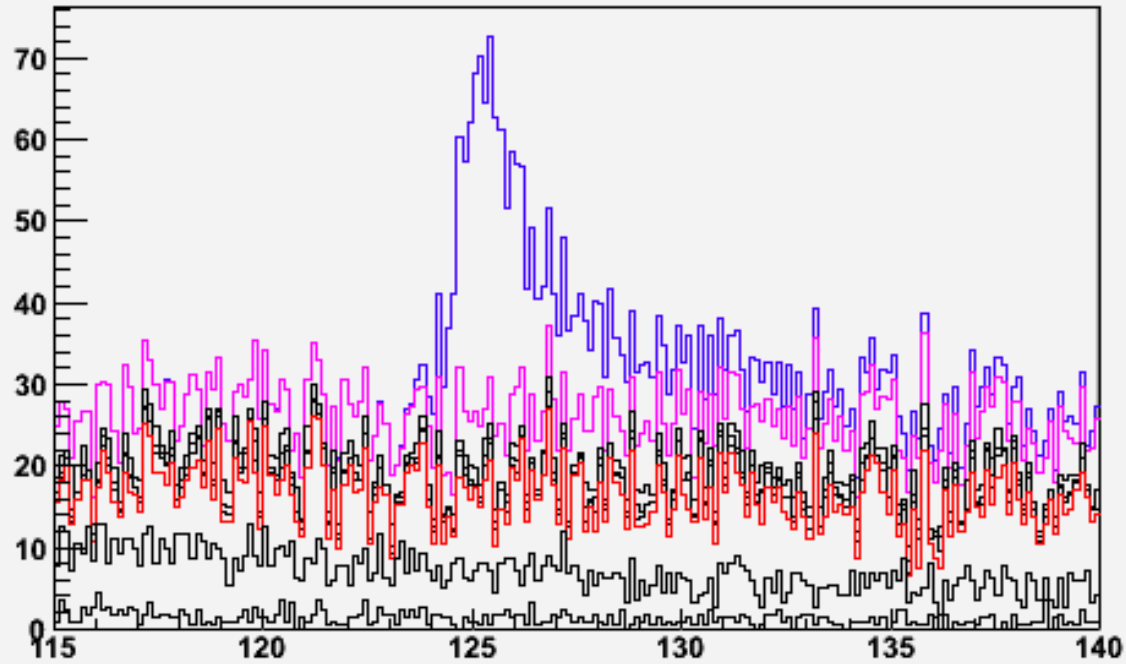
$$N \left[b \exp\left[-\frac{1}{2} \frac{(x - x_{\text{mean}})^2}{\sigma^2}\right] + (1 - b) \exp\left[-\frac{1}{2} \frac{(x - x_{\text{mean}})^2}{\sigma^2}\right] \exp\left(-k \frac{(x - x_{\text{mean}})}{\sigma}\right) \right]$$

recoil mass (stacked)

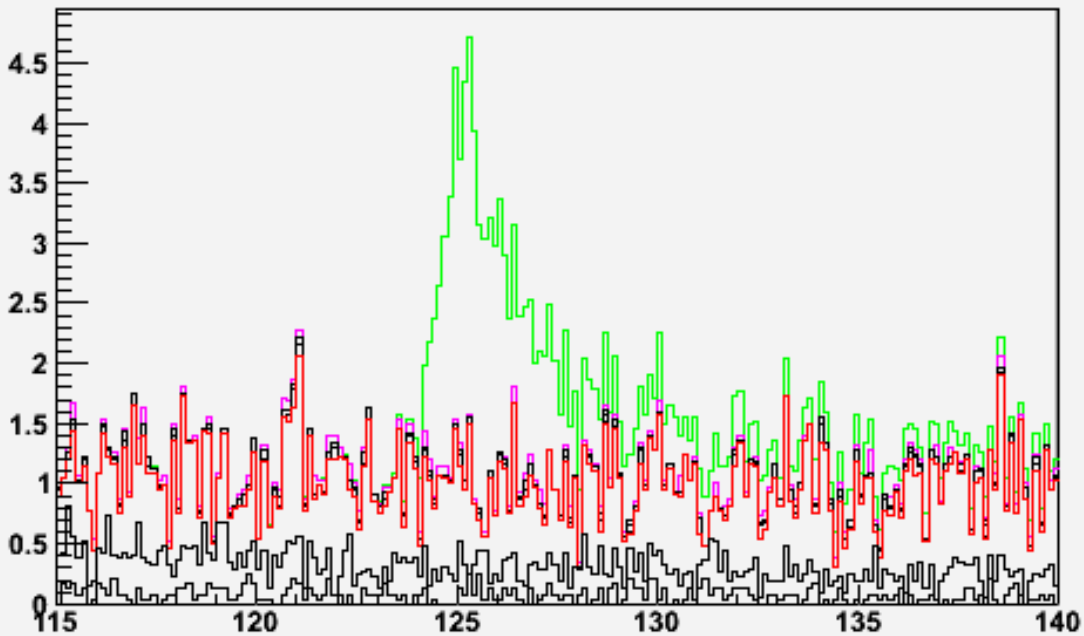
Red: 2f_Z_I

Pink: 4f_ZZWWMix_I :
small for eRpL

hist_recoil_stackLpR



hist_recoil_stackRpL



statistic error of cross section σ

we want to maximize **significance** = $\langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle}$

i.e. optimize (efficiency ϵ) x (purity $\pi = \langle S \rangle / \langle N \rangle$)

expected # of signal events $\langle S \rangle = \epsilon * L * \sigma$ (L: integrated Luminosity)

assume $\langle B \rangle$ in signal region is "known" with small uncertainty

if observe N events : $\langle \Delta \sigma_{\text{meas}} \rangle / \langle \sigma_{\text{meas}} \rangle = \text{inversely of } \{ \text{significance} = \langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle} \}$

Error on efficiency = n/N

binomial distr.

if detect n signal events out of N events : **efficiency = n/N** (assume N is constant)

stat error on n : $\Delta n = \sqrt{N * \epsilon * (1-\epsilon)}$ $\rightarrow \Delta n/n = \sqrt{(1-\epsilon)/n}$)

higher ϵ , larger n is better

My updated results:

- $\epsilon = 0.69$
- $\langle n \rangle = 1491$
- $\langle \Delta n \rangle / \langle n \rangle = \sqrt{(1-\epsilon)/\langle n \rangle} = 1.4 \%$
- purity := $\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 20.8$

$$\langle n \rangle = 1491 \pm 21$$

$$\langle \Delta \sigma_{\text{meas}} \rangle / \langle \sigma_{\text{meas}} \rangle = 1 / \sqrt{\langle n \rangle * \pi} = 4.8 \%$$

After including all BG and signal processes

added all other (possibly not relevant) signal and BG processes

signal : added Pqqh, Pnnh, Pe1e1h (Zee), Pe3e3h (Z $\tau\tau$)

what did I miss ?

Events left after all cuts:

- **WW_sl \sim 130** *oh no.....*
- Pqqh $< \sim 7$
- Pnnh $< \sim 4$
- All others ~ 0

Now results are (after all cuts) :

$\langle S \rangle = 1508$, sig eff = 0.68, $\langle S \rangle / B = 0.40$, $\langle S \rangle / \sqrt{\langle S \rangle + B} = 20.7$

not that much difference

Compare different polarization scenarios

	(-0.8,0.3)	(-0.8,0)	(0,0)
$\langle \Delta S \rangle$	1491	1183	1005
efficiency	0.69	0.69	0.686
$\langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle}$	20.82	18.63	18.04
$\langle S \rangle / \langle B \rangle$	0.41	0.42	0.48
$\langle \Delta S \rangle / \langle S \rangle$	1.52%	1.62%	1.77%
$\langle \sigma \rangle / \sigma$	4.80%	5.37%	5.54%

Summary

- Higgs recoil mass study using $e^+e^- \rightarrow Zh \rightarrow \mu^+\mu^-h$ @ Ec.m.s. = 250 GeV, $L = 250 \text{ fb}^{-1}$
- improved data selection method
- included all other BG processes (tau related , hadronic , ect..... just to be sure)
- updated results: **signal $\epsilon = 69\%$, $S/B \sim 0.4$, $S/\sqrt{S+B} \sim 20.7$**
- fitted recoil mass : **125.2 GeV +/- 70 MeV** ← *will aim for better precision*
- Compared different **polarization** scenarios : **(-0.8, 0.3)** vs **(-0.8, 0)** vs **(0,0)**

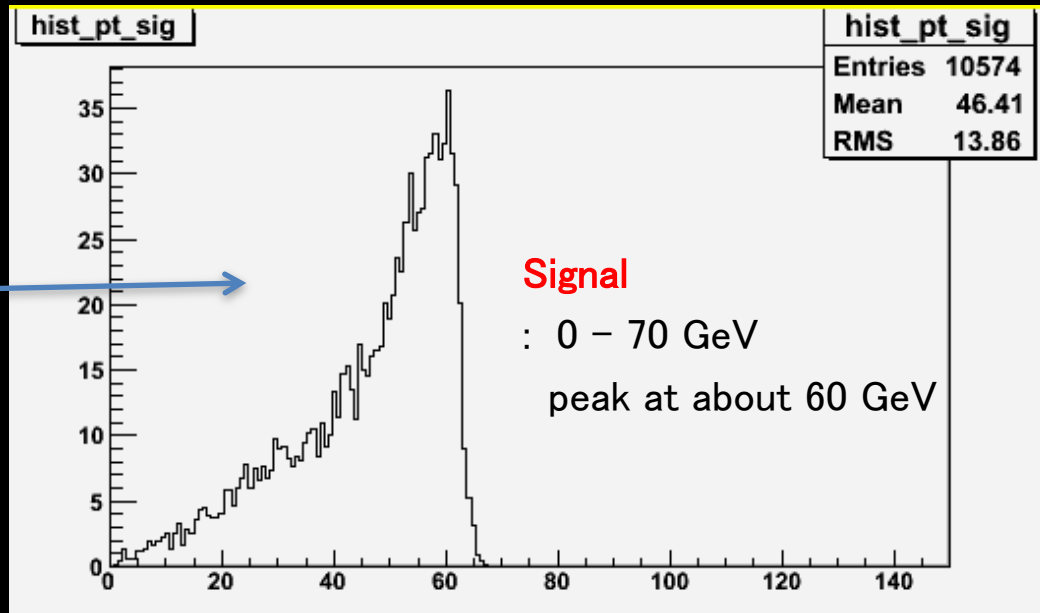
Further Plans

- further optimize data selection method
- try higher statistics ($L=20000 \text{ fb}^{-1}$) sample only available for 250 GeV (?)
- move on soon to **analysis at Ec.m.s. = 350 GeV**

BACKUP

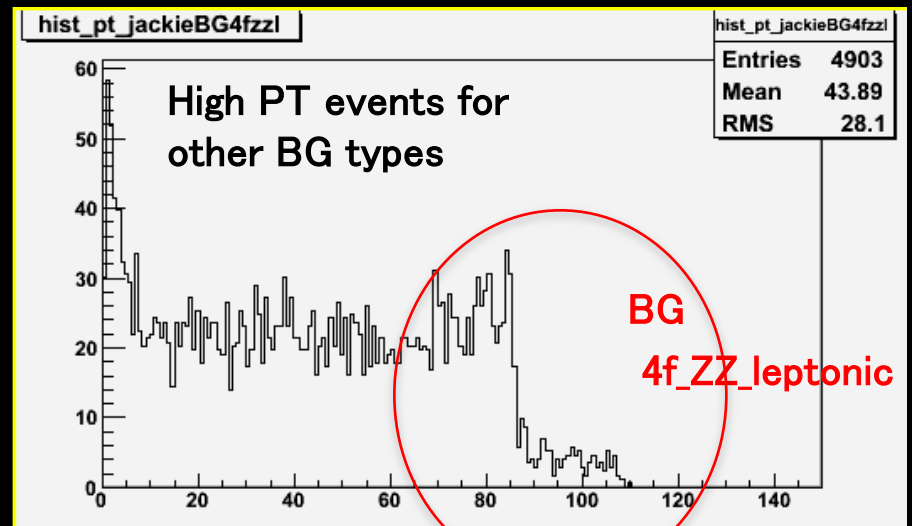
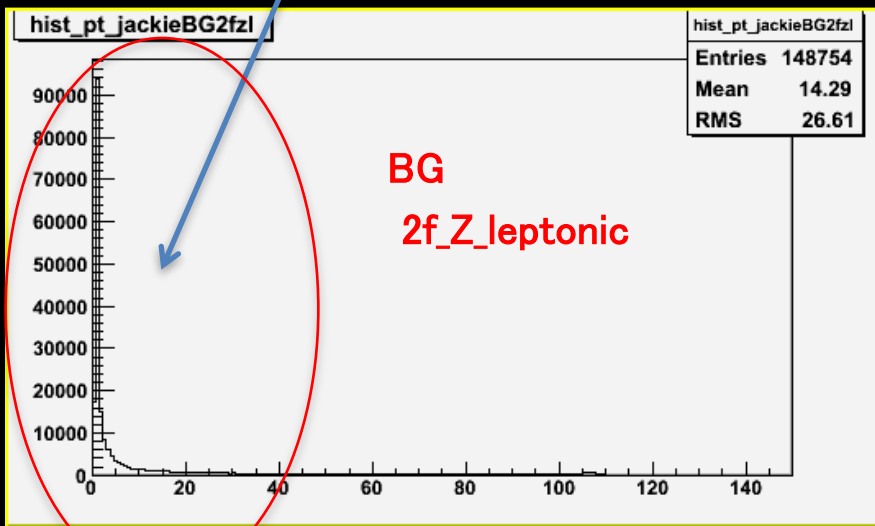
PT of dilepton system

do cut : $10 \text{ GeV} < p_{T_dl} < 70 \text{ GeV}$



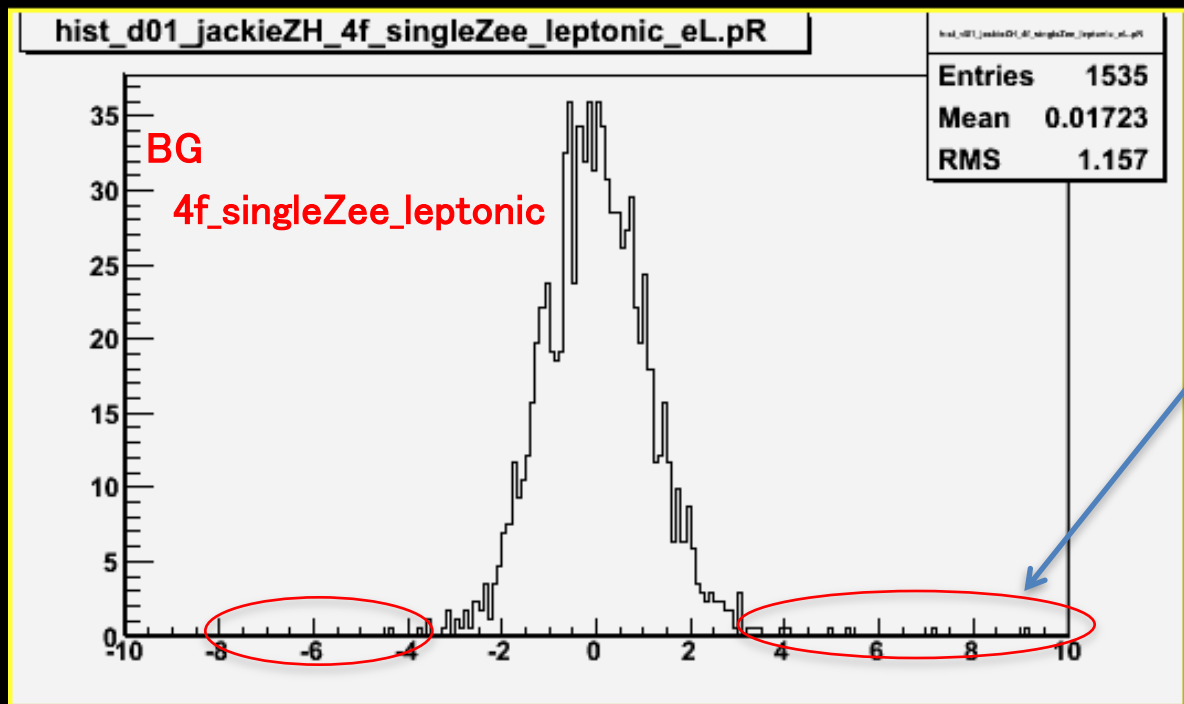
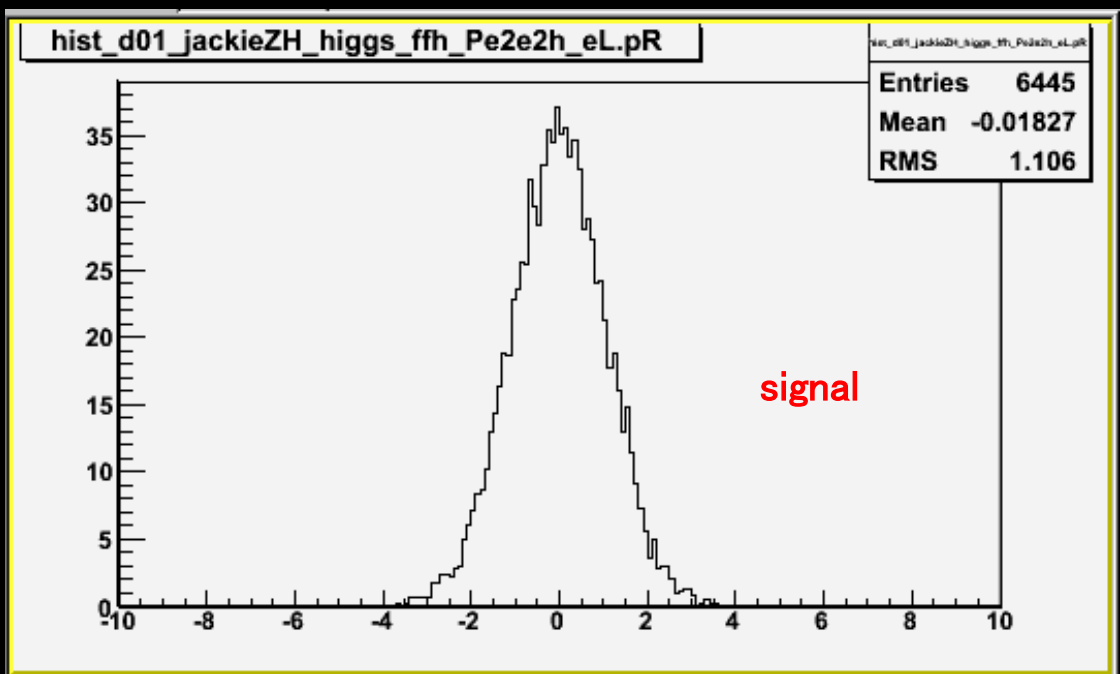
BG

dominated by 2f_Z_leptonic,
many low PT events



Impact parameter

$D0 / \delta D0$

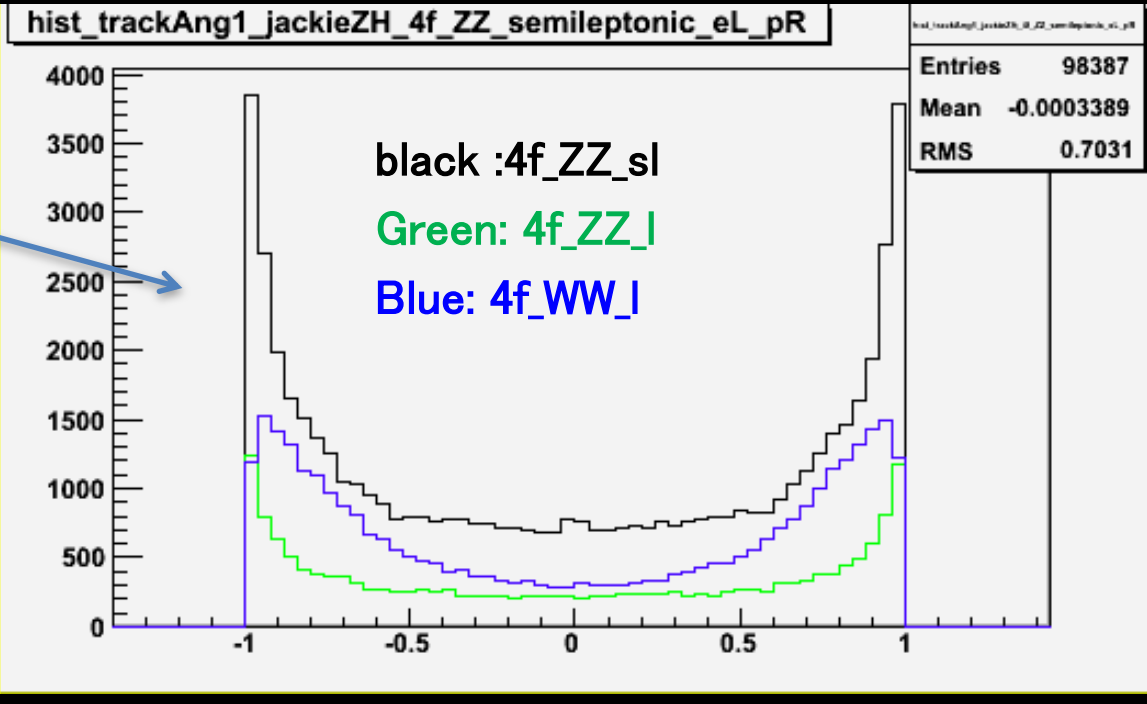
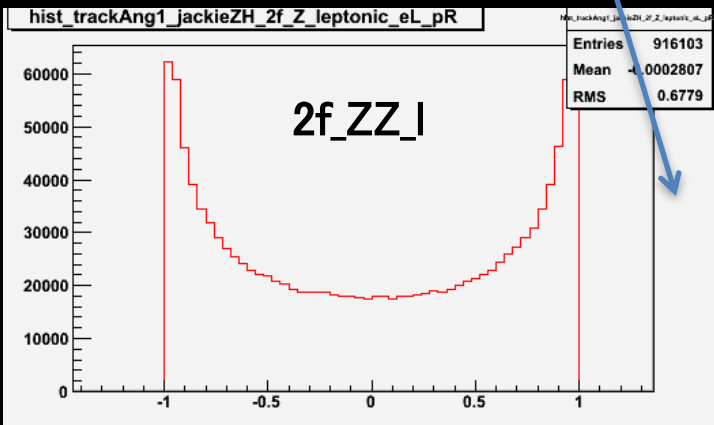


For some BG processes
exceed ± 4 slightly

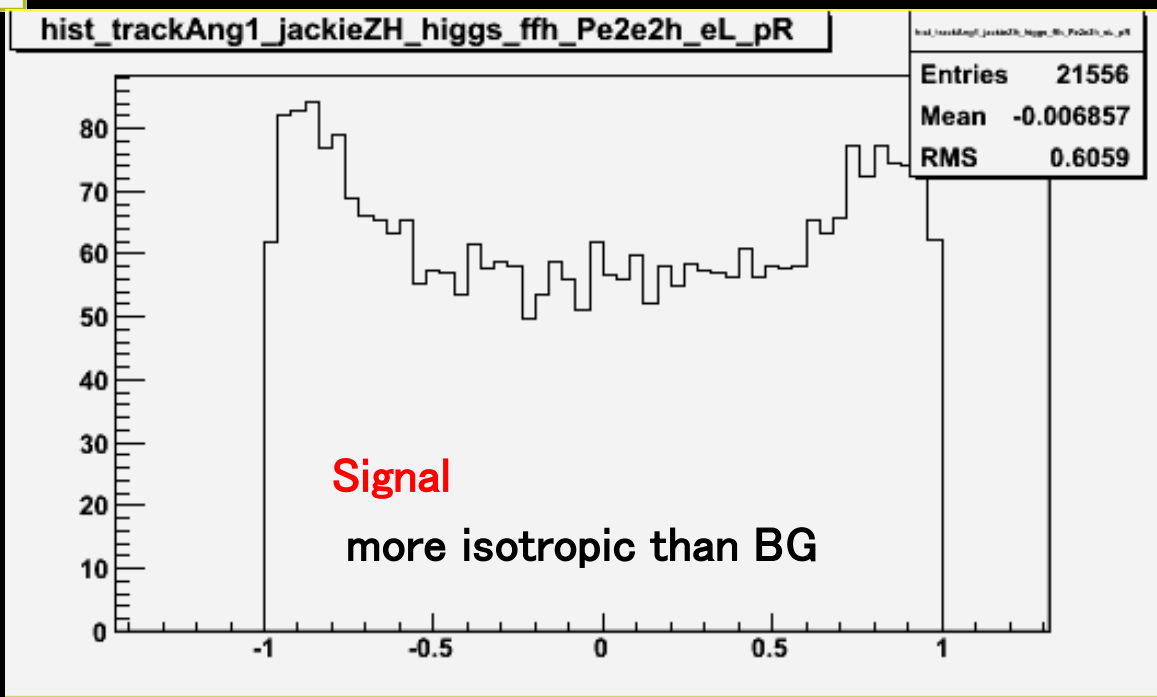
do cut : $|D0 / \delta D0| < 4$

Cos(track angle)

BG is More forward



do cut :
 $\cos(\text{trackAngle}) < 0.95$



How to estimate error of cross section σ_s ?

when measuring σ_s , we want to maximize $\langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle}$

i.e. optimize (efficiency ϵ) \times (purity π)

Why ??

A:

- expected # of signal events $\langle S \rangle = \epsilon * L * \sigma_s$ (L: integrated Luminosity)
- Expected # of BG events $\langle B \rangle$ in signal region
assume $\langle B \rangle$ is "known" with small uncertainty compared to stat. error on $\langle S \rangle$
- total # of events $\langle N \rangle = \langle S \rangle + \langle B \rangle = \epsilon * L * \sigma_s + \langle B \rangle$

if observe N events : $\sigma_{\text{meas}} = (N - \langle B \rangle) / (\epsilon * L)$

Stat error $\langle \Delta \sigma_{\text{meas}} \rangle = \Delta N / (\epsilon * L) = \sqrt{\langle N \rangle} / (\epsilon * L)$

Purity $\pi = \langle S \rangle / (\langle S \rangle + \langle B \rangle) = \langle S \rangle / \langle N \rangle$

$\sqrt{\langle S \rangle * \pi} = \langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle}$

$\langle N \rangle = \langle S \rangle / \pi = \epsilon * L * \sigma_s / \pi$

$\langle \Delta \sigma_{\text{meas}} \rangle = \sqrt{\epsilon * L * \sigma_s / \pi} / (\epsilon * L) = \sqrt{\sigma_s / \epsilon * L * \pi}$

$\langle \Delta \sigma_{\text{meas}} \rangle / \langle \sigma_{\text{meas}} \rangle = 1 / \sqrt{\epsilon * L * \sigma_s * \pi} = 1 / \sqrt{\langle S \rangle * \pi}$

→ σ_s measurement error is inversely proportional to $\langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle}$!!

Estimate Stat errors

Error on $\langle n \rangle$ ($\langle S \rangle$) depend on **binomial distr.**

if detect n out of N events : **efficiency = n/N**

$$\text{stat error on } n : \Delta n = \sqrt{N * \epsilon * (1-\epsilon)} = \sqrt{n * (1-\epsilon)} \quad \Delta n/n = \sqrt{(1-\epsilon)/n}$$

(c.f. If n is big \rightarrow Poisson distr.: $1/\sqrt{n}$)

higher ϵ , larger n is better

My updated results:

- $\epsilon = 0.66$
- $\langle n \rangle = 1422$ ($= \langle S \rangle$)
- $\langle \Delta n \rangle / \langle n \rangle = \sqrt{(1-\epsilon)/\langle n \rangle} = 1.6 \% \rightarrow \langle n \rangle = 1422 \pm 23$

$$\text{purity : } \sqrt{\langle n \rangle * \pi} = \langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 20.6$$

$$\text{Error of cross section } \langle \Delta \sigma_{\text{meas}} \rangle / \langle \sigma_{\text{meas}} \rangle = 1 / \sqrt{\langle n \rangle * \pi} = 4.9 \%$$

dependent on sample size \rightarrow try higher statistics

Now integrated $L = 2000 \text{ fb}^{-1}$

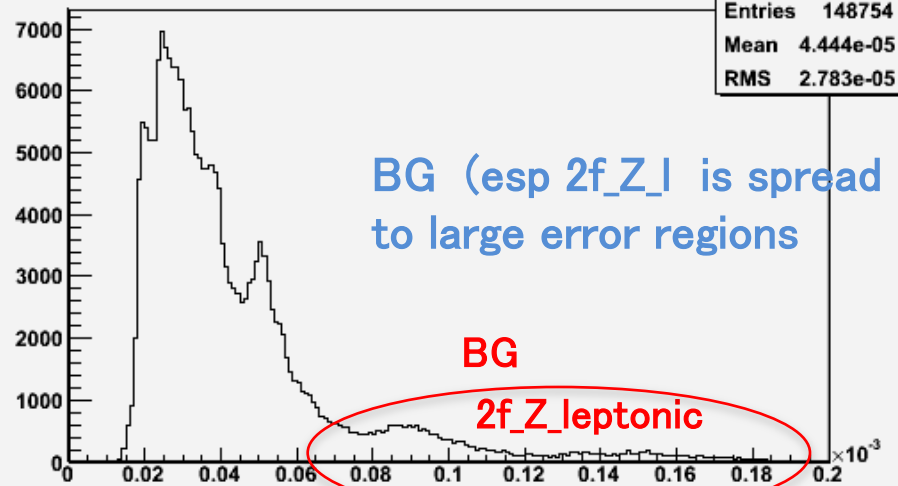
$$\sigma_s = \langle n \rangle / (L * \epsilon) = 1422 / 2000 / 0.66 = 1.077 \text{ fb}$$

good track selection

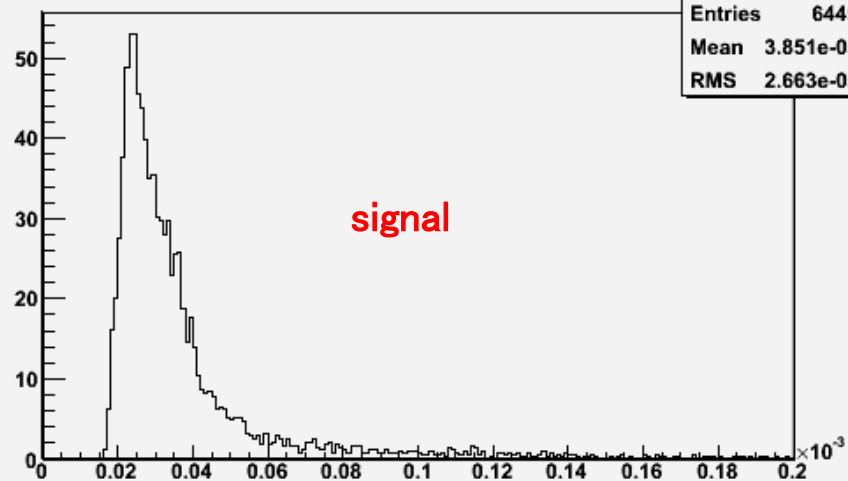
dP/P^2

Used to do cut : $dp/p^2 < 5E-5$

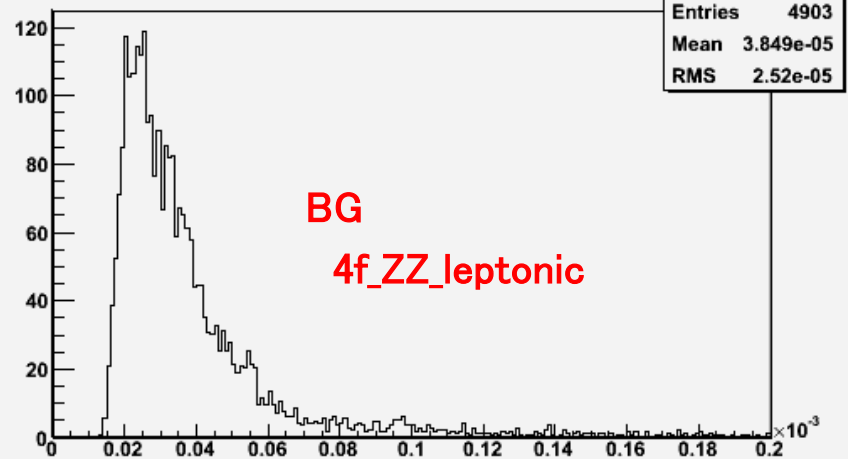
hist_track1_jackieZH_2f_Z_leptonic_eL.pR



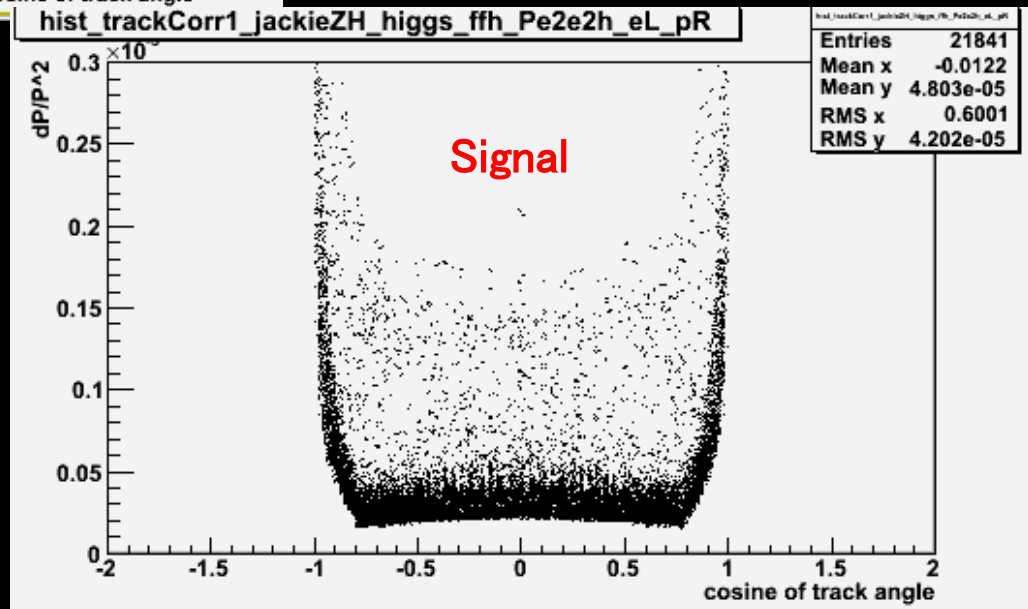
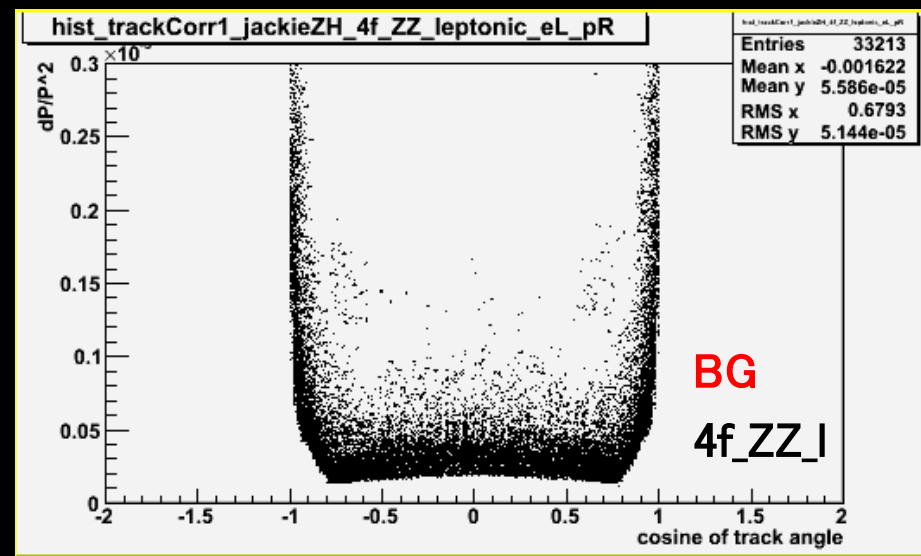
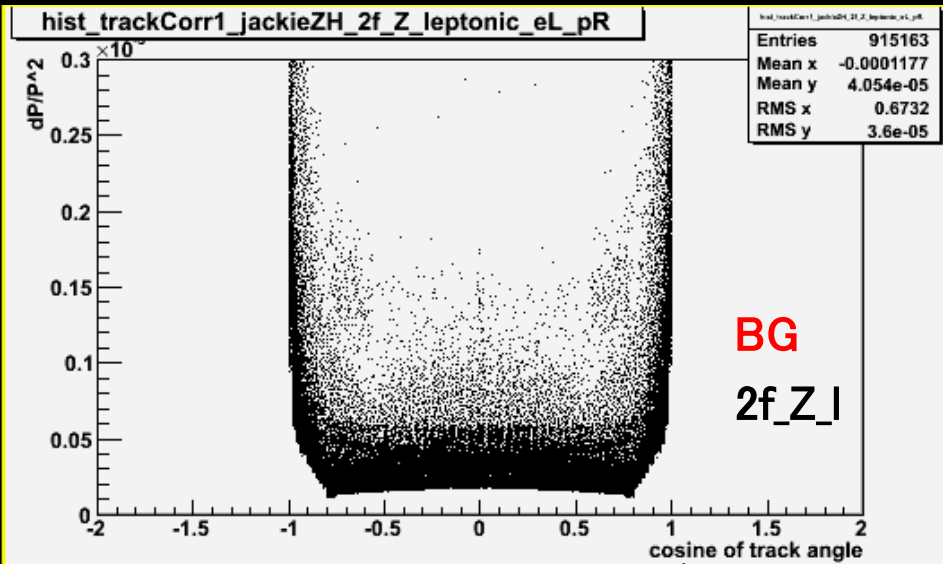
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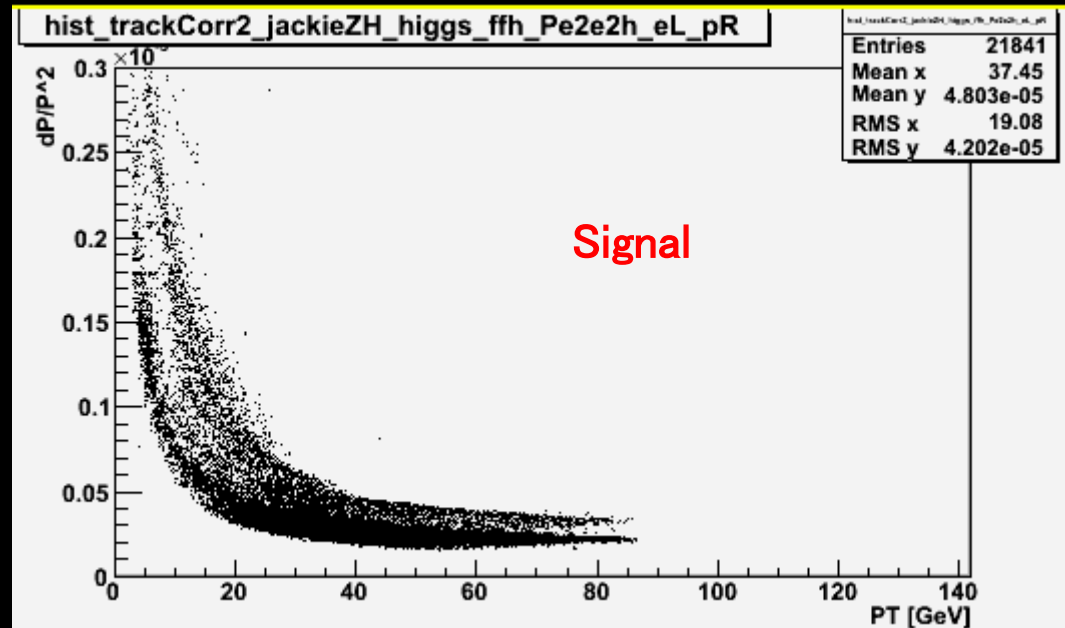
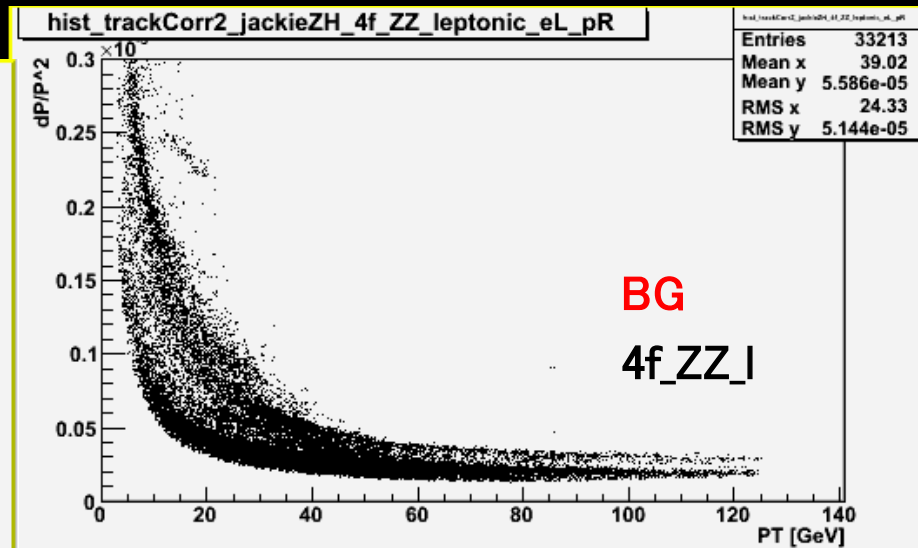
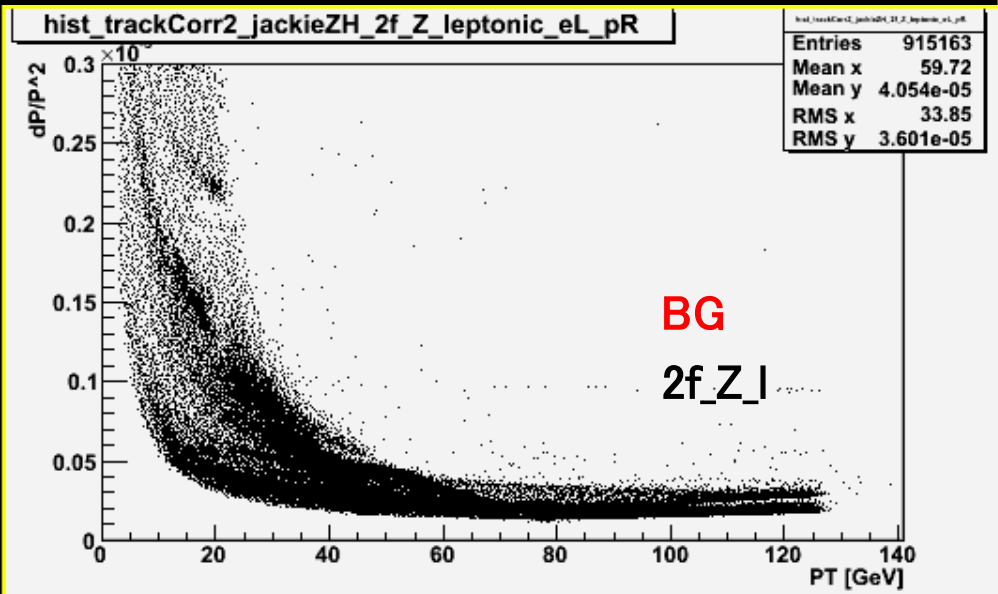
hist_track1_jackieZH_4f_ZZ_leptonic_eL.pR



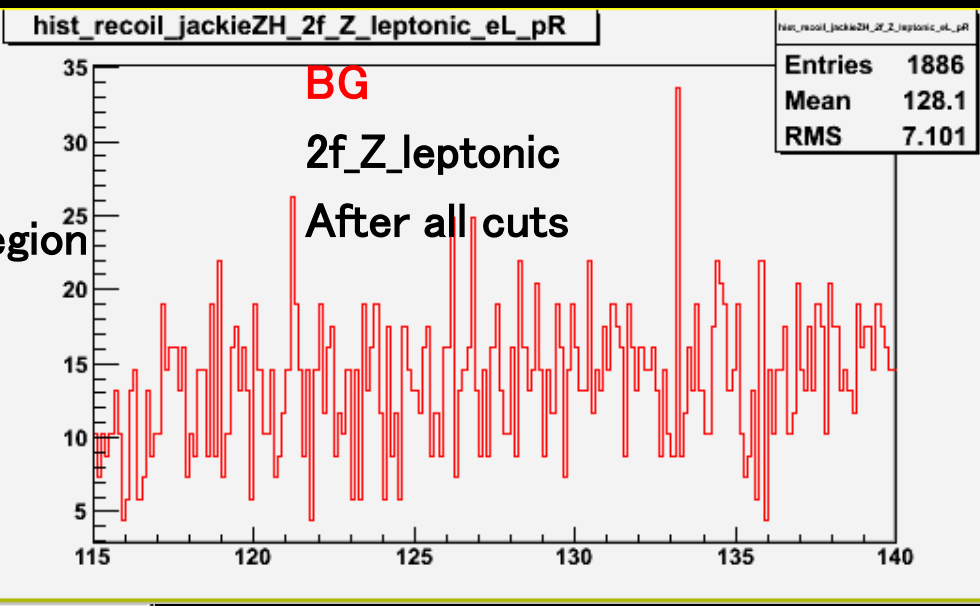
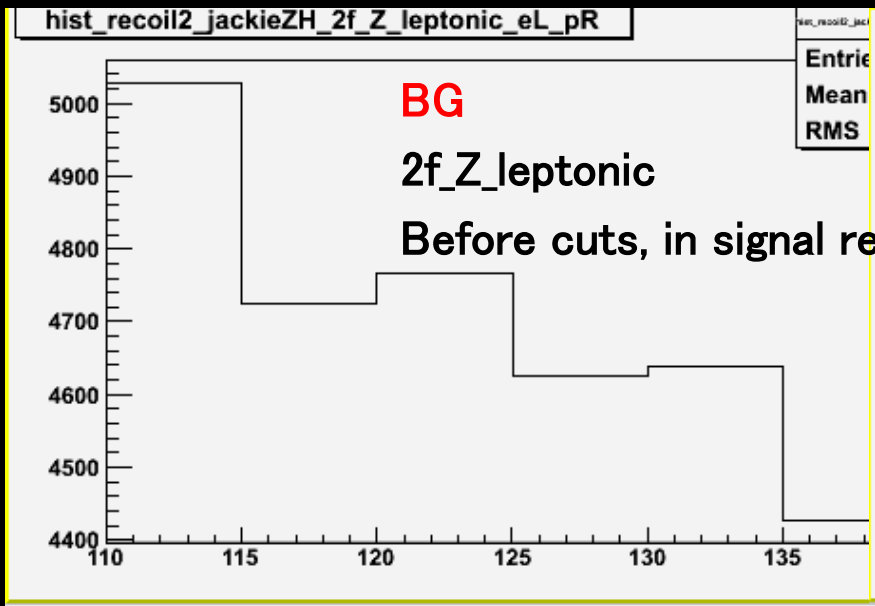
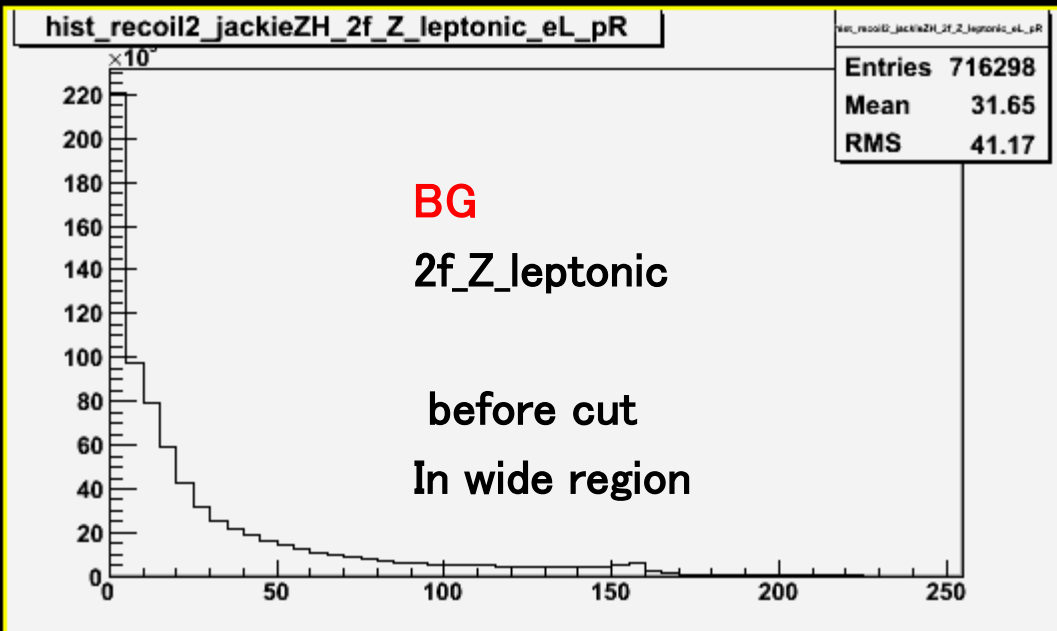
correlation between $\text{Cos}(\text{track angle})$ and dP/P^2



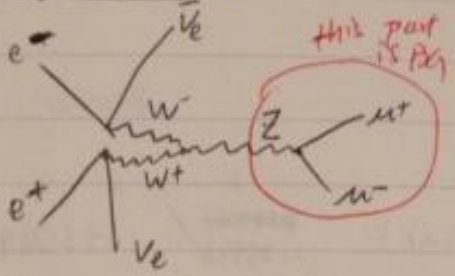
correlation between PT and dP/P^2



Recoil mass of 2f_Z_leptonic
before and after all [cuts](#)

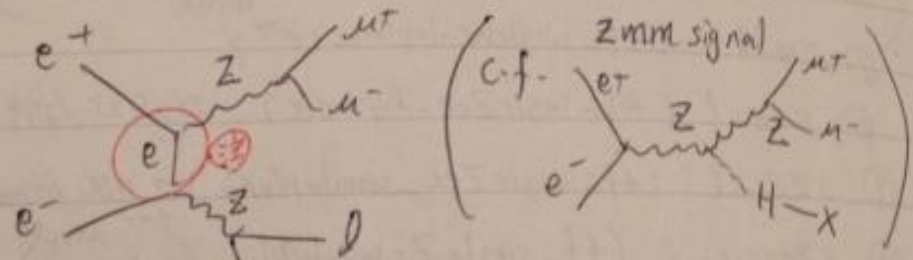


single Zmumu

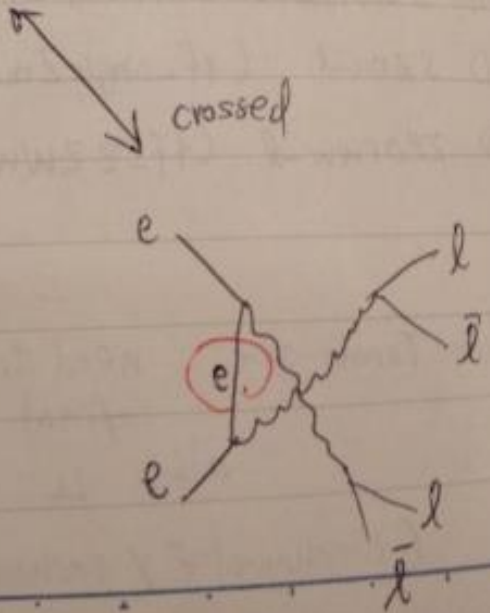


example diagrams for BG process for Zmumu

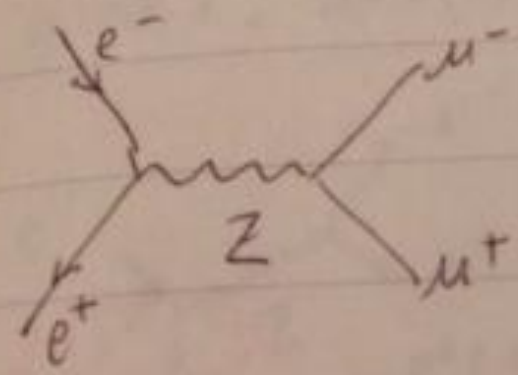
4f-ZZ-0



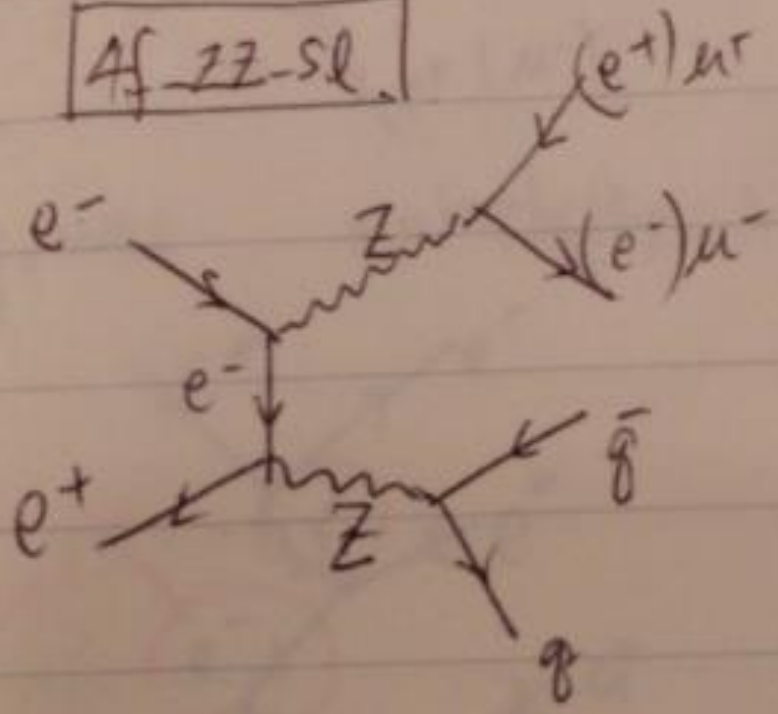
$e^+e^- \rightarrow$
 $\nu_e \bar{\nu}_e \mu^+ \mu^-$
 $e^+ e^- \mu^+ \mu^-$
 $\mu^+ \mu^- \mu^+ \mu^-$
 (or Z)?

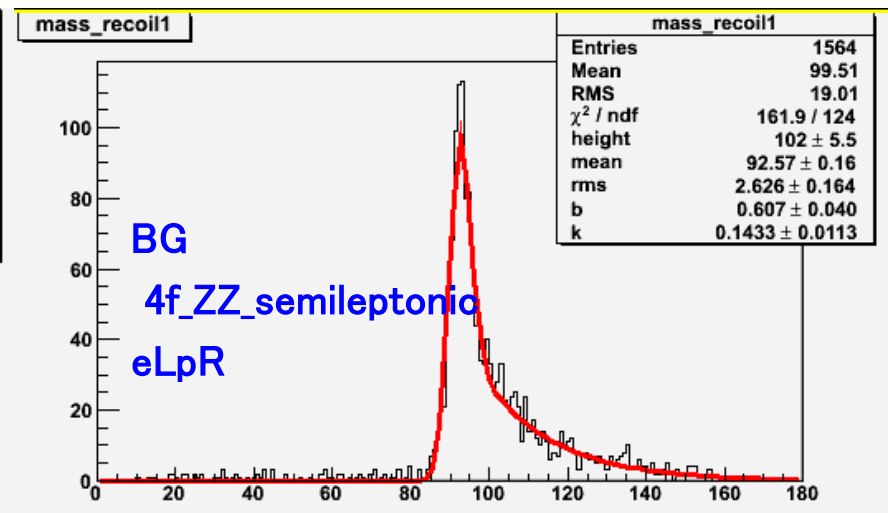
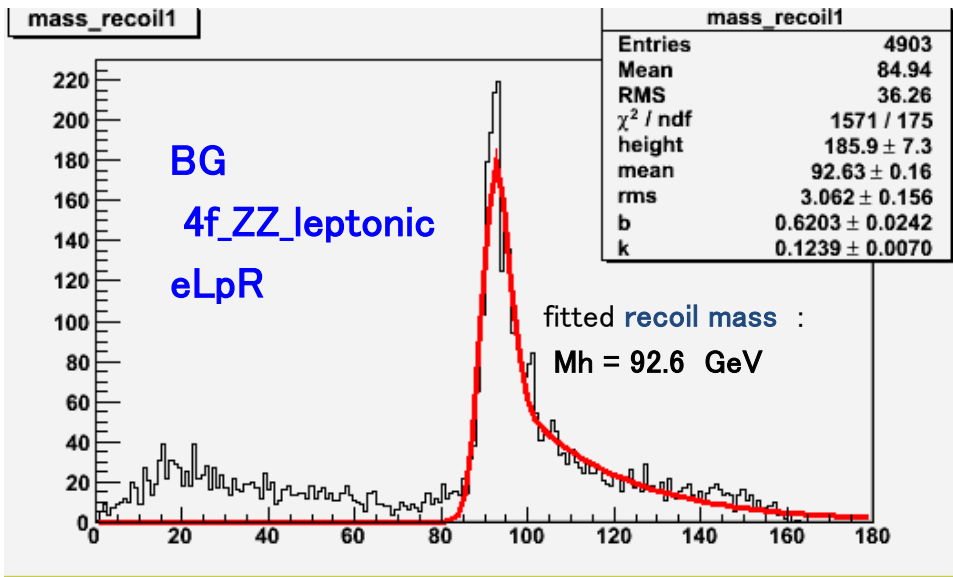


Zl (2f)



4f ZZ-sl





recoil mass distribution for some BG processes

2f_Z_leptonic

This may be causing high energy BG in combined histogram

