

Higgs Recoil Mass Study

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www.researchgate.net

recoil mass study using $e^+e^- \rightarrow Zh \rightarrow \mu^+\mu^-h$

Ec.m.s. = 250 GeV, $L = 250 \text{ fb}^{-1}$

Ec.m.s. = 350 GeV, $L = 333 \text{ fb}^{-1}$

Goal:

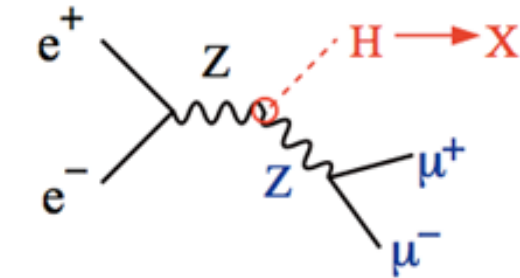
precise measurement of

- Higgs mass
- cross section σ_H : $N = \sigma * L * \epsilon$

What's new this week

- ◆ updated results for 250 GeV
 - included all BG and signal processes
 - calculate cross section error taking into account uncertainty of BG and efficiency
- ◆ Tried 20 x higher statistic signal samples (20000 fb)
- ◆ first attempt at 350 GeV

polarization:
 $(e^-, e^+) = (-0.8, +0.3)$



$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

DBD Samples

Sample statistics 1000 fb-1

$$\text{event weight} = \text{pol_weight} * (\text{process_cross_section} * \text{assumed_integrated_luminosity}) / (\text{number_of_reconstructed_events})$$

250 GeV

/grid/ilc/prod/ilc/mc-dbd/ild/dst-merged/250-TDR_ws/

20 x Higher statistics data : /hsm/ilc/grid/storm/user/a/amiyamot/myprod/ild/dst-merged /250-TDR_ws/
reference: meta files and diagrams in <http://ilcsoft.desy.de/dbd/generated/other.html>

350 GeV

/grid/ilc/prod/ilc/mc-dbd/ild/dst-merged/350-TDR_ws/

List of samples: http://www-jlc.kek.jp/~miyamoto/CDS/prod_status/REC_ILD_o1_v05_350GeV.html

Lumosity

TDR baseline

$\sqrt{s}=250$ GeV, Lumi= $0.75 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ → assume L = 250 fb⁻¹

$\sqrt{s}=350$ GeV, Lumi= $1.0 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ → assume L = 333 fb⁻¹

Polarization: (-0.8, + 0.3) → compare with (+0.8, -0.3)

Signal sample:

Pe2e2h.eL.pR & Pe2e2h.eR.pL

relevant BG process for Zmumu

- 4f_ZZ_leptonic
- 4f_ZZ_semileptonic
- 2f_Z_leptonic
- 4f_WW_leptonic
- 4f_WW_semileptonic
- 4fSingleZee_leptonic
- 4fSingleZnnu_leptonic
- 4f_ZZWWMix_leptonic

250 GeV

eLpR	cross sec	weight
higgs	17.14	0.146
BG in order of large cross section		
2f_Z_l	21226.4	1.46
4f_ZZWWMix_l	1636.04	0.583
4f_WW_l	1564.21	0.573
4f_ZZ_sl	1422.14	0.583
4f_singleZee_l	1084.1	0.581
4f_singleZnn_l	192.75	0.47
4f_ZZ_l	157.96	0.578

after all cuts, dominant BG are:

sqrt(s) = 250 GeV : #1) 2f_Z_l #2) 4f_ZZ_sl #3) 4f_ZZWWMix_l

sqrt(s) = 350 GeV : #1) 4f_ZZ_sl #2) 2f_Z_l #3) 4f_WW_sl

no ttbar BG left after data selection

Results for 250 GeV

Muon Selection

- reject neutrals
- $P_{tot} > 5 \text{ GeV}$
- $\text{small } E_{\text{cluster}} / P_{\text{total}} < 0.5$
- opposite charge
- **Best track selection**
 - $\cos(\text{track angle}) < 0.95$
 - $|D0/\delta D0| < 4$

Best Z Candidate Selection

- 2 mu candidates with **opposite charge**
if several possibilities :
choose pair **with invariant mass closest to Z mass**

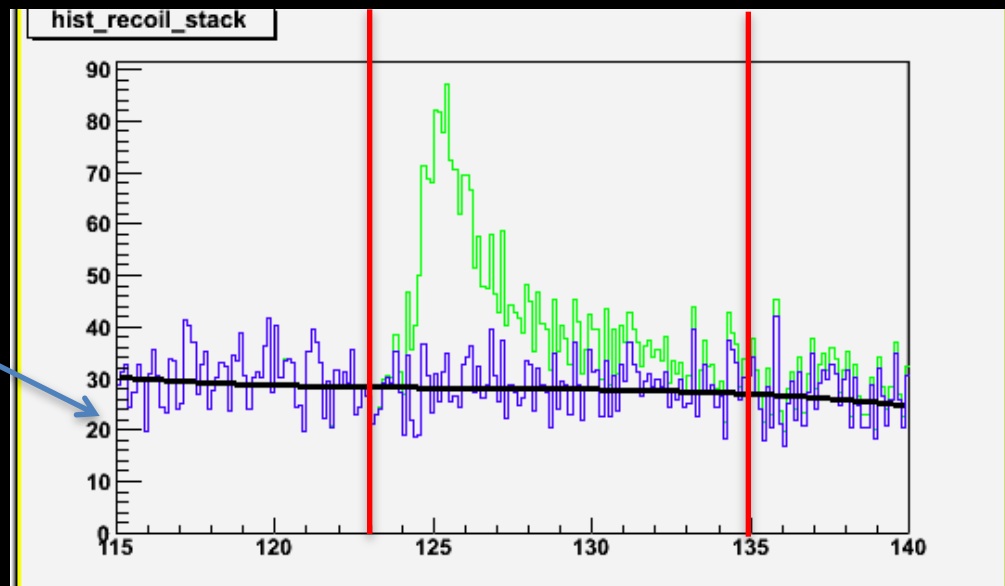
Final Selection for 250 GeV

analysis after filling root files

- **84 GeV < M_mumu < 98 GeV**
- $123 \text{ GeV} < M_{\text{recoil}} < 135 \text{ GeV}$
- $10 \text{ GeV} < pT_{\text{mumu}} < 70 \text{ GeV}$
- $|\cos(\theta_{Z\text{pro}})| < 0.91$
(Z production angle)

Evaluate data selection
efficiency in within range
of 123 – 135 GeV

calculate recoil mass with
correction for 14 mrad beam
crossing angle



This Week 's updated results : 250 GeV

Calculation of Error of σ_{meas}

- Case#1: ignore uncertainty of $\langle B \rangle$ i.e. MC statistics
- Case#2: taking into account uncertainty of ε and $\langle B \rangle$ *is this necessary ?*

Usual signal samples (1000 fb⁻¹)

$$\begin{aligned}\langle n \rangle &= 1487 \pm 25 \\ \langle \varepsilon \rangle &= 57.1 \pm 0.4 \% \\ \langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} &= 20.6 \\ \langle n \rangle / \langle B \rangle &= 0.40\end{aligned}$$

If Case#1

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 4.9 \%$$

If Case#2

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.5\%$$

20 x high statistic signal samples (20000 fb⁻¹)

$$\begin{aligned}\langle n \rangle &= 1469 \pm 25 \\ \langle \varepsilon \rangle &= 56.4 \pm 0.1 \% \\ \langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} &= 20.7 \\ \langle n \rangle / \langle B \rangle &= 0.40\end{aligned}$$

Case#1

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 4.8 \%$$

If Case#2

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.6\%$$

No significant difference for higher statistic signal samples

Data selection : 123 – 135 GeV

$\sqrt{s} = 250 \text{ GeV}$

cut	signal	eff	BG_all	eff	S/B	S/sqrt(S+B)
raw, no inv mass cut	2605	100.0%	6923287	100%	0.000	0.990
track	1764	67.7%	27560	0.40%	0.064	10.301
84 <M_inv <98	1601	61.5%	9364	0.14%	0.171	15.290
10 <P_Td<70	1579	60.6%	4873	0.07%	0.324	19.658
final cos(θ_Z)<0.91	1487	57.1%	3724	0.05%	0.399	20.599

Signal efficiency 57 %

S/N → 0.40

Significance ~20.6

cut	4f_ZZ_l	4f_ZZ_sl	2f_Z_l	4f_WW_l	4f_WW_sl	4fSingleZee_l	4fSingleZnn_l	4f_ZZWWMix_l
raw, no inv mass cut	23972	214232	3248465	228894	2771978	167469	28534	239742
track	456	1971	11540	960	6984	530	408	4711
84 <M_inv <98	226	844	6636	210	138	106	240	964
10 <P_Td<70	202	820	2237	206	138	104	233	933
cos(θ_Z)<0.91	166	710	1428	191	131	86	199	813

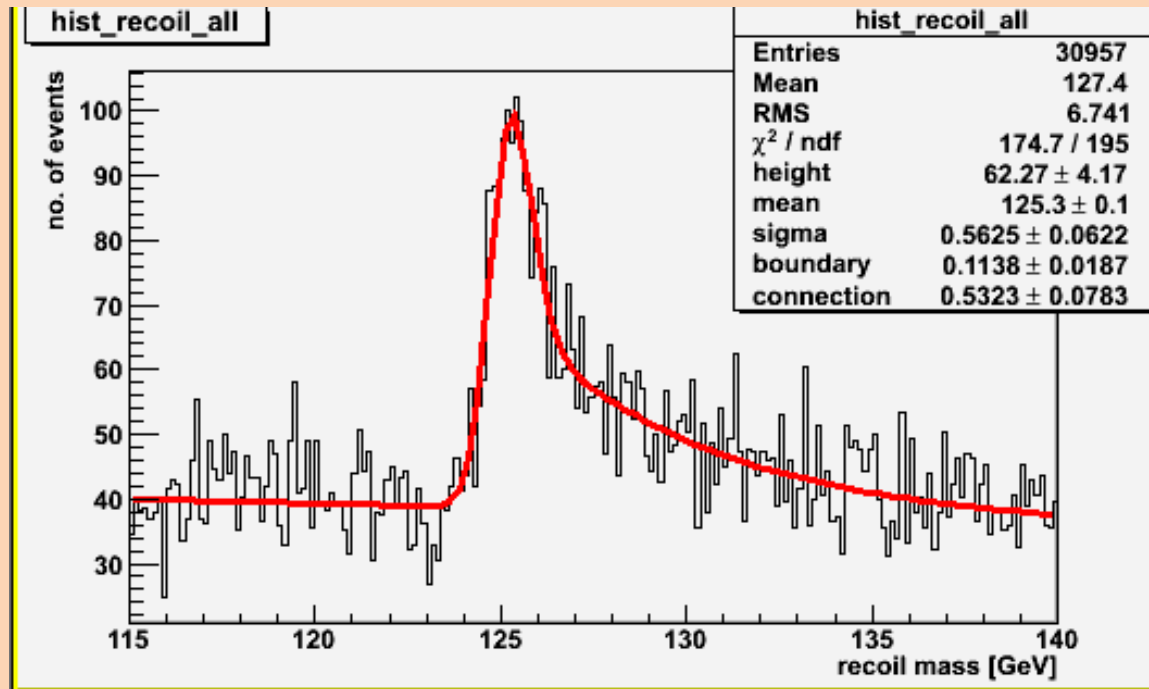
recoil mass

after implementing all cuts

fitted recoil mass :

$$M_h = 125.3 \text{ GeV} \pm 70 \text{ MeV}$$

calculate recoil mass with correction for 14 mrad beam crossing angle



◆ BG: 3rd order polynomial

◆ signal : GPET: 5 parameters : Gaus (left-side) , Gaus + expo (right side)

$$N \exp\left[-\frac{1}{2} \frac{(x - x_{\text{mean}})^2}{\sigma^2}\right] \exp\left[-\frac{(x - x_{\text{mean}})}{k}\right]$$

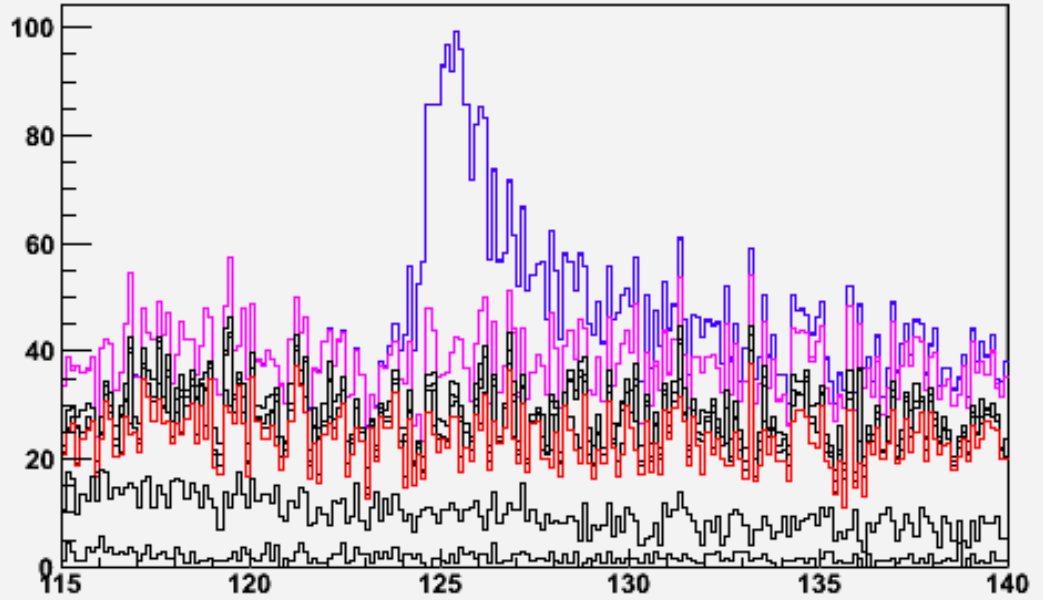
$$N \left[b \exp\left[-\frac{1}{2} \frac{(x - x_{\text{mean}})^2}{\sigma^2}\right] + (1 - b) \exp\left[-\frac{(x - x_{\text{mean}})^2}{2\sigma^2}\right] \exp\left[-\frac{(x - x_{\text{mean}})}{k}\right] \right]$$

recoil mass (stacked)

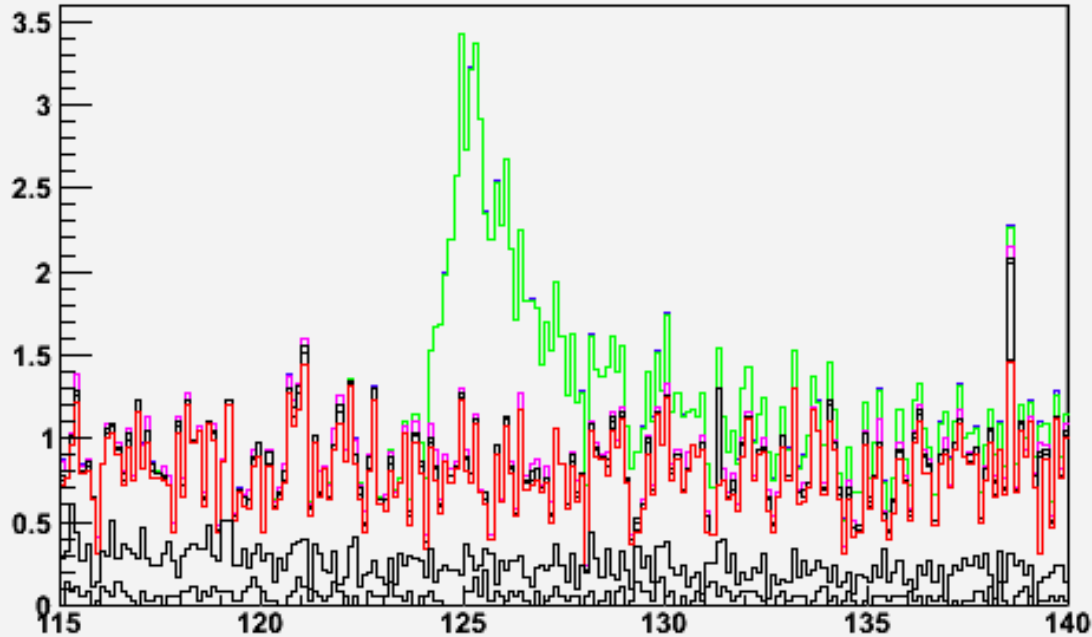
Red: 2f_Z_I

Pink: 4f_ZZWWMix_I :
small for eRpL

hist_recoil_stackeLpR



hist_recoil_stackeRpL



Results for 350 GeV

Muon Selection

- reject neutrals
- $P_{tot} > 5 \text{ GeV}$
- $\text{small } E_{\text{cluster}} / P_{\text{total}} < 0.5$
- opposite charge

■ Best track selection

$$\cos(\text{track angle}) < 0.98$$

$$|D0/\delta D0| < 5$$

Best Z Candidate Selection

2 mu candidates with **opposite charge**
choose pair **with invariant mass closest to Z mass**

Final Selection for 350 GeV

- $84 \text{ GeV} < M_{\text{mumu}} < 98 \text{ GeV}$
- $123 \text{ GeV} < M_{\text{recoil}} < 135 \text{ GeV}$
- $10 \text{ GeV} < pT_{\text{mumu}} < 140 \text{ GeV}$
- coplanarity < 3
- $|\cos(\theta_{Z\text{pro}})| < 0.91$
(Z production angle)

calculate recoil mass with correction
for 14 mrad beam crossing angle

Evaluated within range of 123 – 135 GeV

L = 333 fb⁻¹

$$\langle n \rangle = 923 \pm 23$$

$$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$$

$$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.6$$

$$\langle n \rangle / \langle B \rangle = 0.42$$

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.0 \%$$

8.8 % if consider BG uncertainty

L = 250 fb⁻¹

$$\langle n \rangle = 694 \pm 20$$

$$\langle \epsilon \rangle = 40.4 \pm 0.4 \%$$

$$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 14.4$$

$$\langle n \rangle / \langle B \rangle = 0.42$$

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.9 \%$$

9.5% if consider BG uncertainty

Compare different polarization scenarios

$\sqrt{s} = 350 \text{ GeV}$ $L = 333 \text{ fb}^{-1}$

For now, keep same cut parameters as (-0.8, +0.3)
(they could be optimized)

(-0.8, + 0.3)

Pol weight(eLpR) = $0.9 \cdot 0.65$

Pol weight(eRpL) = $0.1 \cdot 0.35$

$\langle n \rangle = 923 \pm 23$

$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.6$

$\langle n \rangle / \langle B \rangle = 0.42$

$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.0 \%$

8.8 % if consider BG uncertainty

(+0.8, -0.3)

Pol weight(eLpR) = $0.1 \cdot 0.35$

Pol weight(eRpL) = $0.9 \cdot 0.65$

$\langle n \rangle = 625 \pm 19$

$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 15.9$

$\langle n \rangle / \langle B \rangle = 0.68$

$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.4 \%$

7.6 % if consider BG uncertainty

(-0.8, 0)

Pol weight(eLpR) = $0.9 \cdot 0.5$

Pol weight(eRpL) = $0.1 \cdot 0.5$

$\langle n \rangle = 733 \pm 21$

$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 14.8$

$\langle n \rangle / \langle B \rangle = 0.43$

$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.8 \%$

9.2% if consider BG uncertainty

Data selection : 123 – 135 GeV

$\sqrt{s} = 350 \text{ GeV}$

with all 6f BG included, whizard events (no NRQCD correction?)

cut	signal	eff	BG_all	eff	S/B	S/sqrt(S+B)
raw	2288	100%	6242481	100.00%	0.0004	0.92
only best mu pair	1098	48%	37801	0.61%	0.0290	5.57
$\Delta D0/D0 < 5$	1101	48%	35087	0.56%	0.0314	5.79
$\cos(\text{trackAng}) < 0.98$	1089	48%	31242	0.50%	0.0349	6.06
$84 < M_{\text{inv}} < 98$	978	43%	6970	0.11%	0.1403	10.97
$10 < P_{\text{Tdl}} < 140$	977	43%	4024	0.06%	0.2428	13.82
$\text{copl} < 3$	966	42%	3638	0.06%	0.266	14.24
$\cos(\theta_Z) < 0.91$	924	40%	2188	0.04%	0.422	16.57

Signal efficiency 40% *S/N → 0.42* *Significance e ~16.6*

cut	4f_ZZ_l	4f_ZZ_sl	2f_Z_l	4f_WW_l	4f_WW_sl	4fSingleZee_l	4fSingleZnn_l	4f_ZZWWMix_l	6f
raw	19632	188087	2226358	226193	2715937	243879	43056	541352	37989
only best mu pair	484	2204	11406	2386	6655	781	367	13516	2
$\Delta D0/D0 < 5$	484	2218	11001	1044	5757	773	367	13441	2
$\cos(\text{trackAng}) < 0.98$	445	2023	9504	871	5069	479	326	12523	2
$84 < M_{\text{inv}} < 98$	252	1042	4439	33	582	129	168	325	0
$10 < P_{\text{Tdl}} < 140$	236	1027	1542	33	582	120	162	322	0
$\text{copl} < 3$	225	979	1323	27	502	111	158	313	0
$\cos(\theta_Z) < 0.91$	149	704	634	18	300	58	108	216	0

Data selection : 123 – 135 GeV

$\sqrt{s}= 350 \text{ GeV}$

with ttbar physsim events (with NRQCD correction?)
no other 6f BGs

cut	signal	eff	BG_all	eff	S/B	S/sqrt(S+B)
raw, no inv mass cut	2288	100%	6204492	100%	0.0004	0.92
track	1089	47.6%	31240	0.50%	0.0349	6.06
84 <M_inv <98	978	42.7%	6970	0.11%	0.1403	10.97
10 <P_Td<140	977	42.7%	4024	0.06%	0.2428	13.82
copl < 3	966	42.2%	3638	0.06%	0.2655	14.24
cos(θ_Z)<0.91	924	40.4%	2188	0.04%	0.4224	16.57

Signal efficiency 40 %

S/N \rightarrow 0.42

Significance \sim 16.6

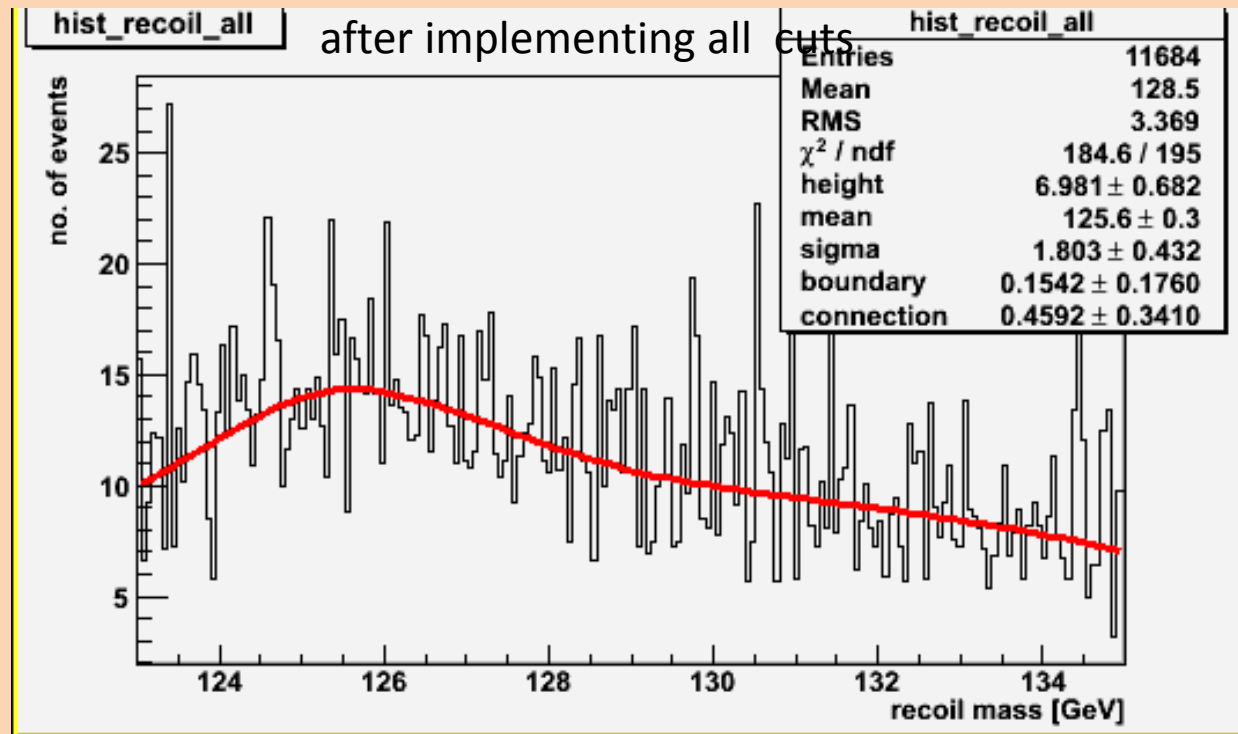
cut	4f_ZZ_l	4f_ZZ_sl	2f_Z_l	4f_WW_l	4f_WW_sl	4fSingleZee_l	4fSingleZnn_l	4f_ZZWWMix_l
raw, no inv mass cut	19632	188087	2226358	226193	2715937	243879	43056	541352
track	445	2023	9504	871	5069	479	326	12523
84 <M_inv <98	252	1042	4439	33	582	129	168	325
10 <P_Td<140	236	1027	1542	33	582	120	162	322
copl < 3	225	979	1323	27	502	111	158	313
cos(θ_Z)<0.91	149	704	634	18	300	58	108	216

recoil mass

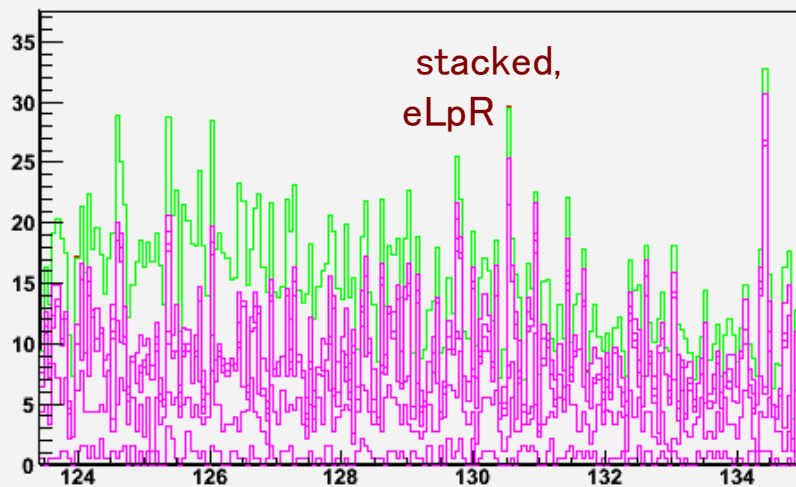
fitted recoil mass :

$$M_h = 125.6 \pm 0.3 \text{ GeV}$$

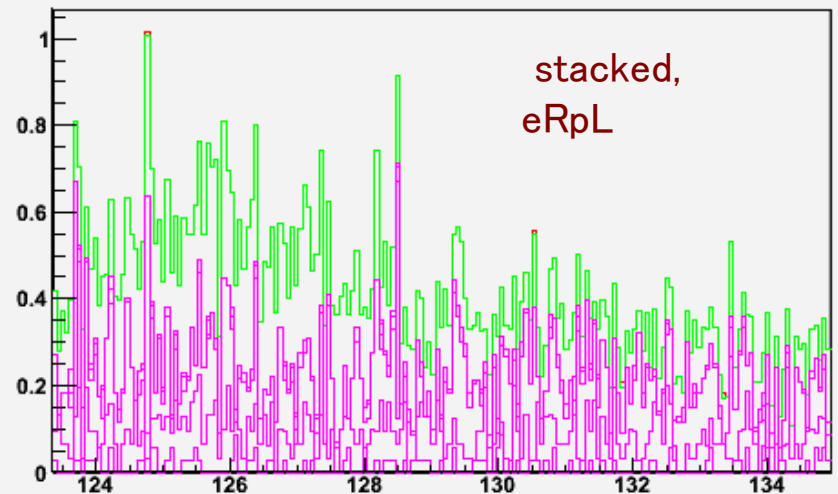
calculate recoil mass with
correction for 14 mrad beam
crossing angle



hist_recoil_stackeLpR



hist_recoil_stackeRpL



(-0.8, + 0.3)

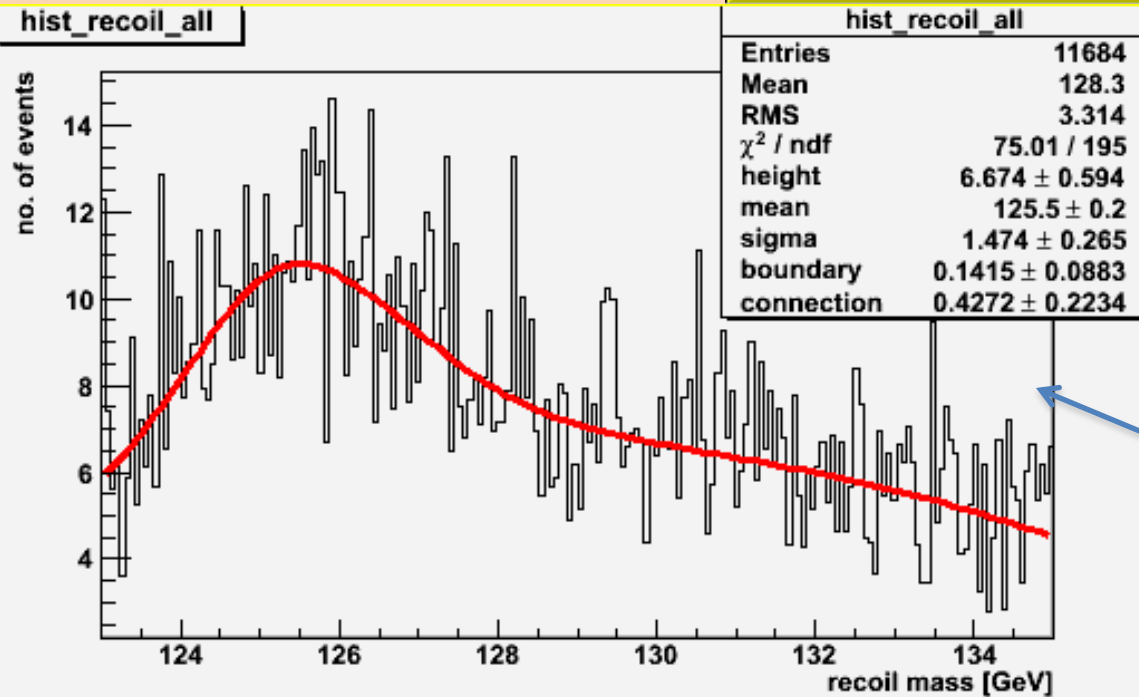
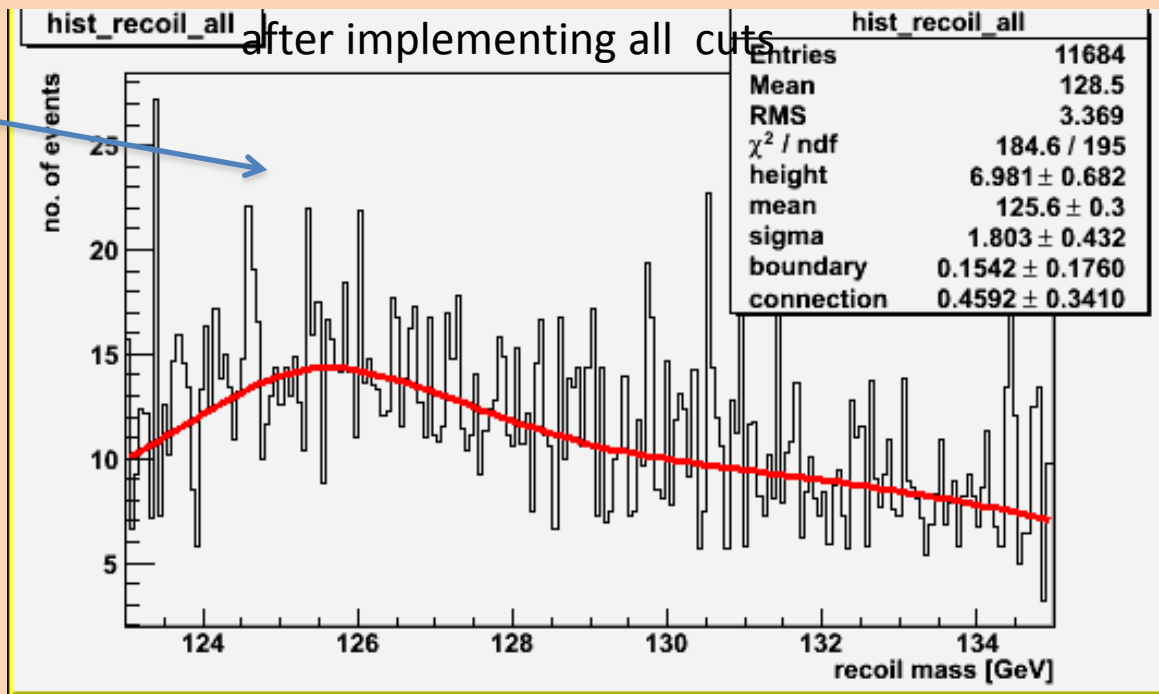
$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.6$

$\langle n \rangle / \langle B \rangle = 0.42$

fitted recoil mass :

$M_h = 125.6 \pm 0.3 \text{ GeV}$



(+0.8, - 0.3)

$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 15.8$

$\langle n \rangle / \langle B \rangle = 0.68$

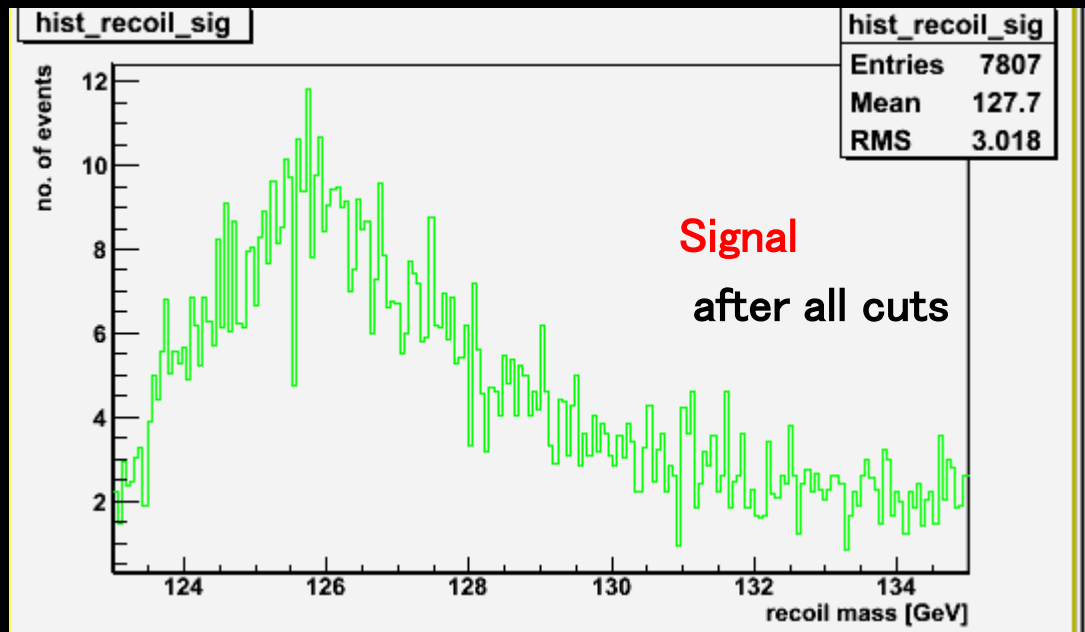
fitted recoil mass :

$M_h = 125.6 \pm 0.2 \text{ GeV}$

recoil mass 350 GeV

After cuts

There is still too much BG left
covers up signal peak !!



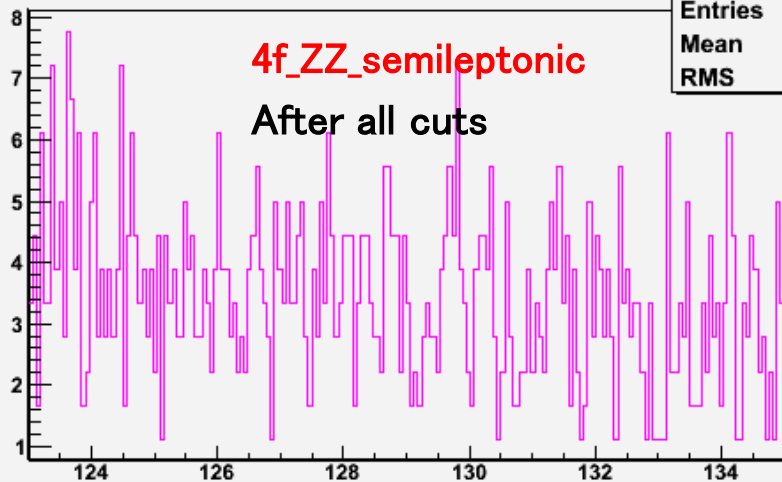
hist_recoil_jackieZH_4f_ZZ_semileptonic_eL_pR

hist_recoil_jackieZH_4f_ZZ_semileptonic_eL_pR

Entries	1241
Mean	128.6
RMS	3.446

4f_ZZ_semileptonic

After all cuts



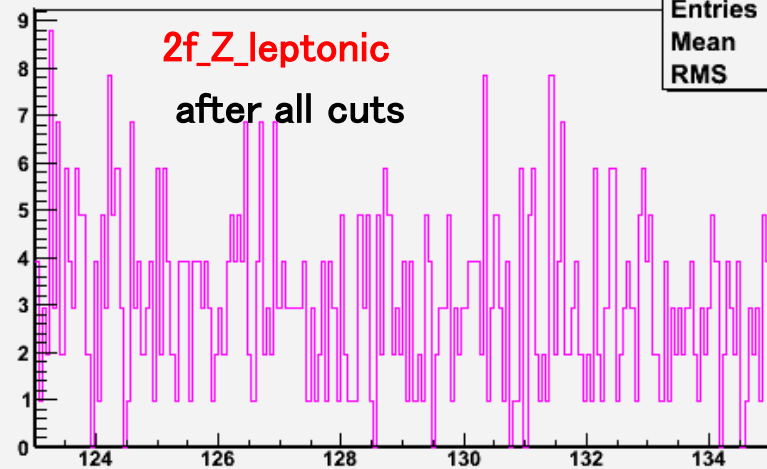
hist_recoil_jackieZH_2f_Z_leptonic_eL_pR

hist_recoil_jackieZH_2f_Z_leptonic_eL_pR

Entries	622
Mean	128.7
RMS	3.512

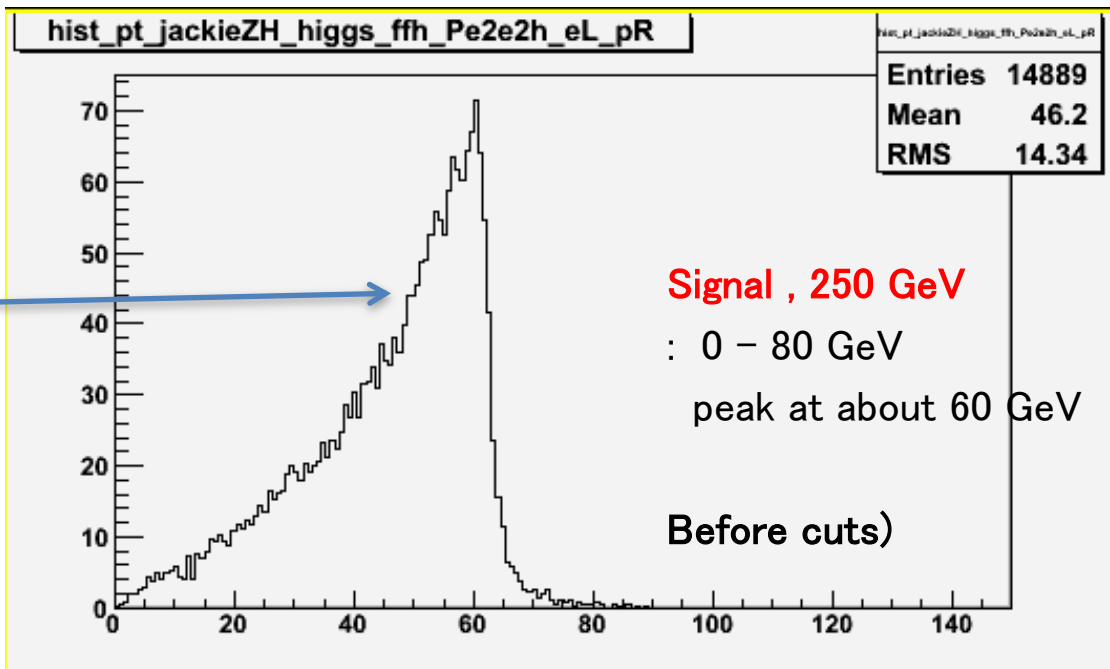
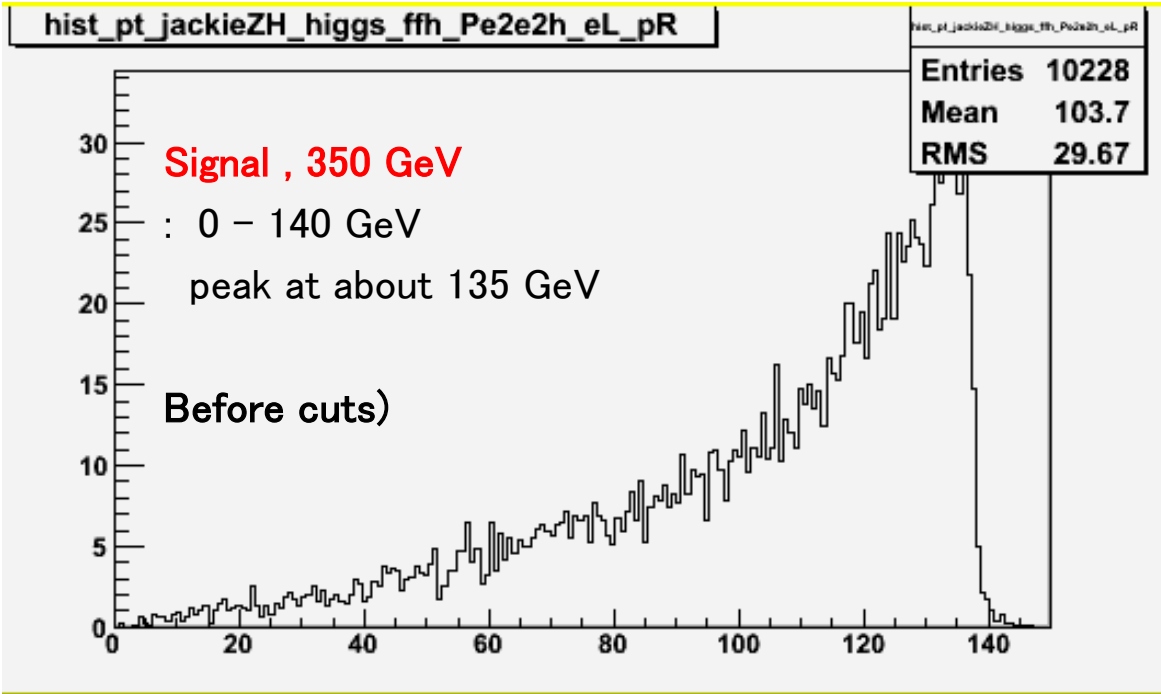
2f_Z_leptonic

after all cuts

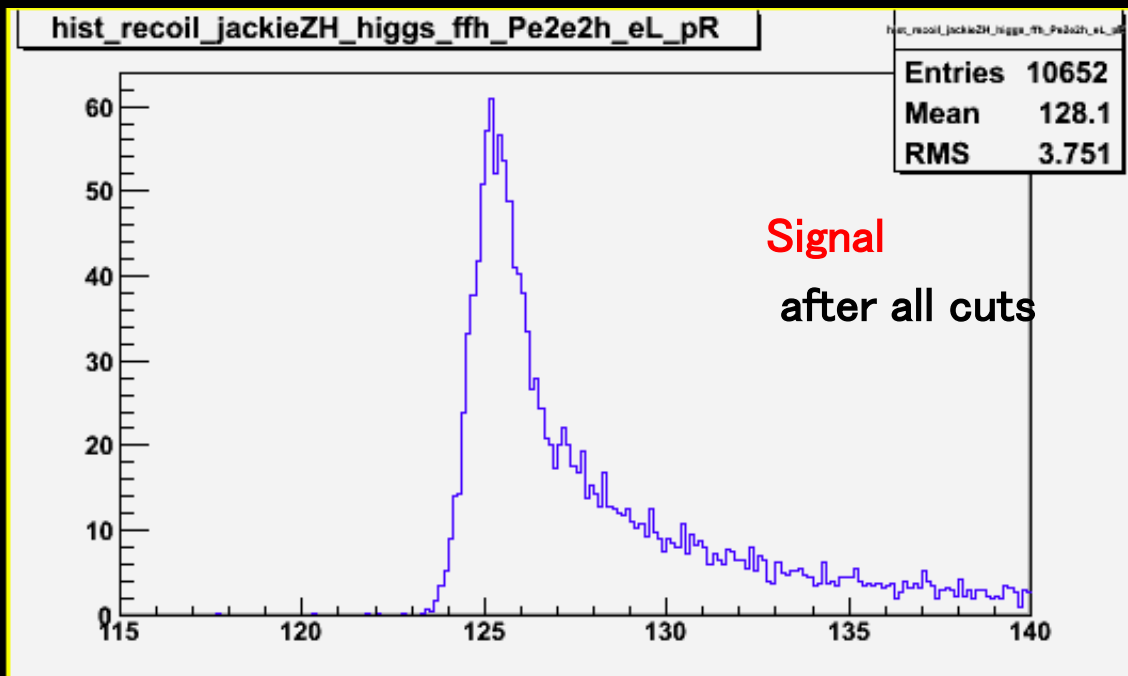


dilepton PT, 350 GeV

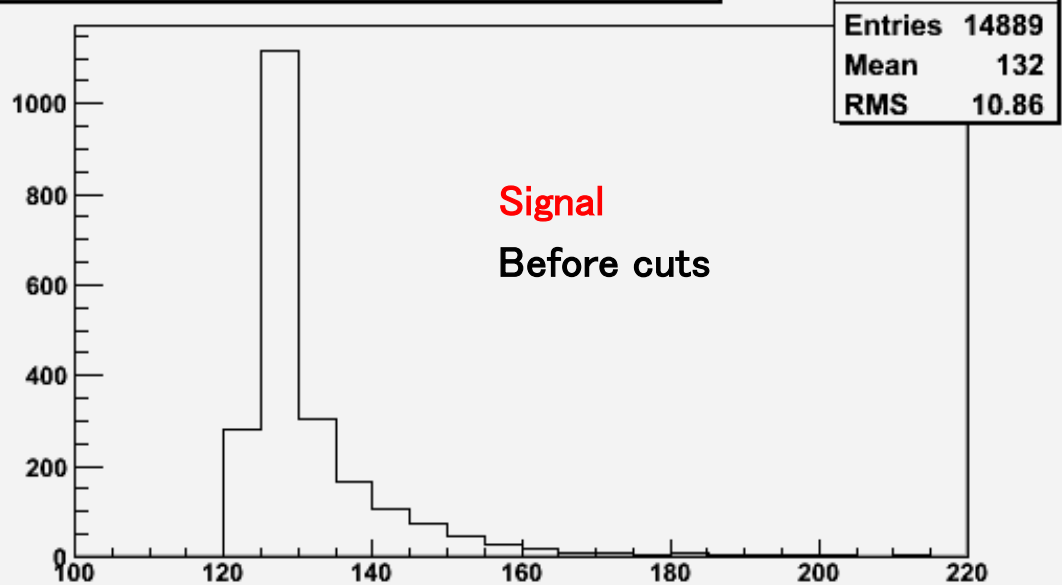
do cut :
 $10 \text{ GeV} < p_{T_dl} < 140 \text{ GeV}$



recoil mass of
signal, 250 GeV

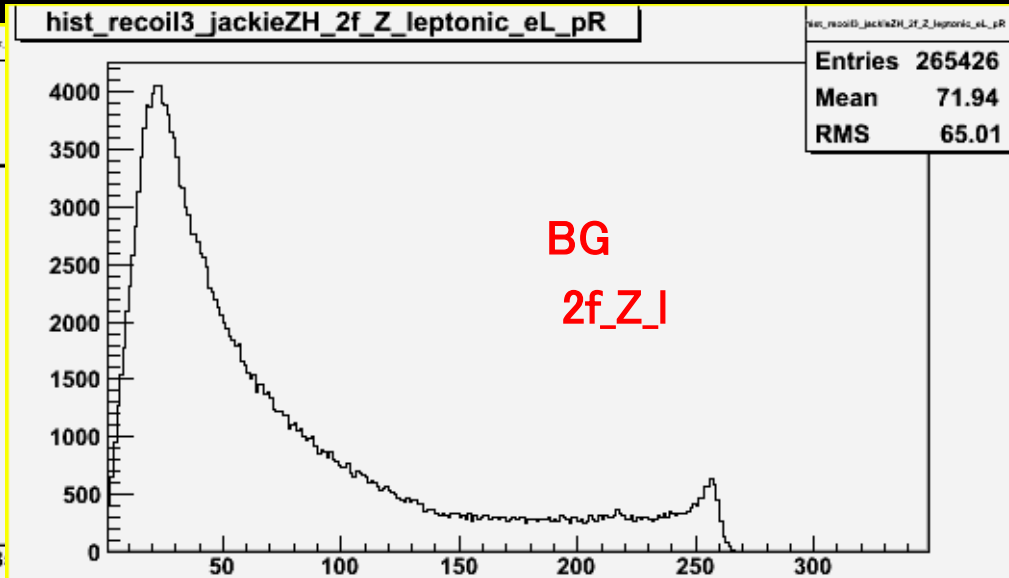
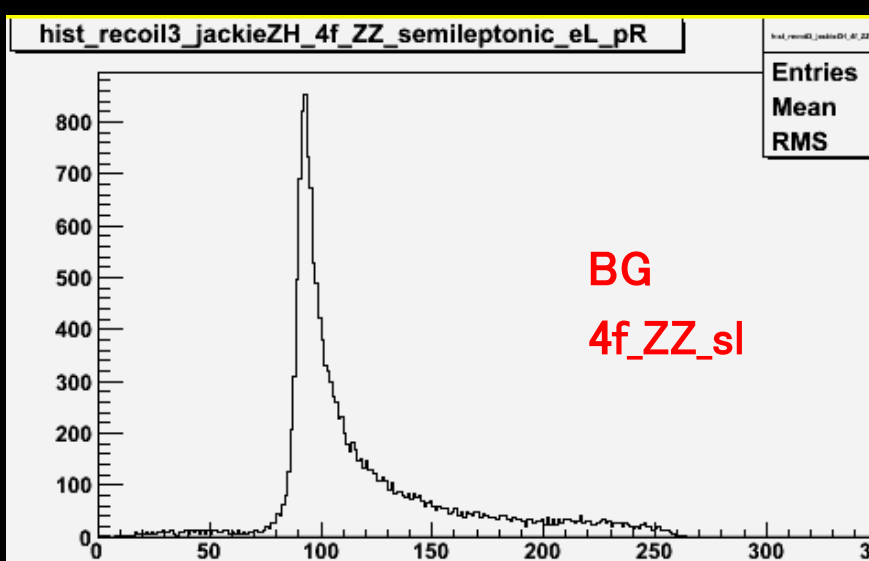
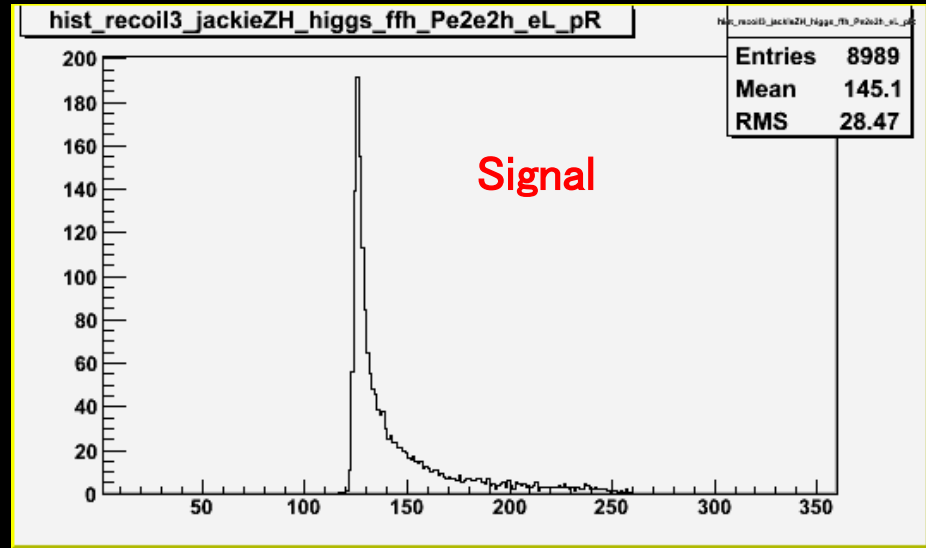
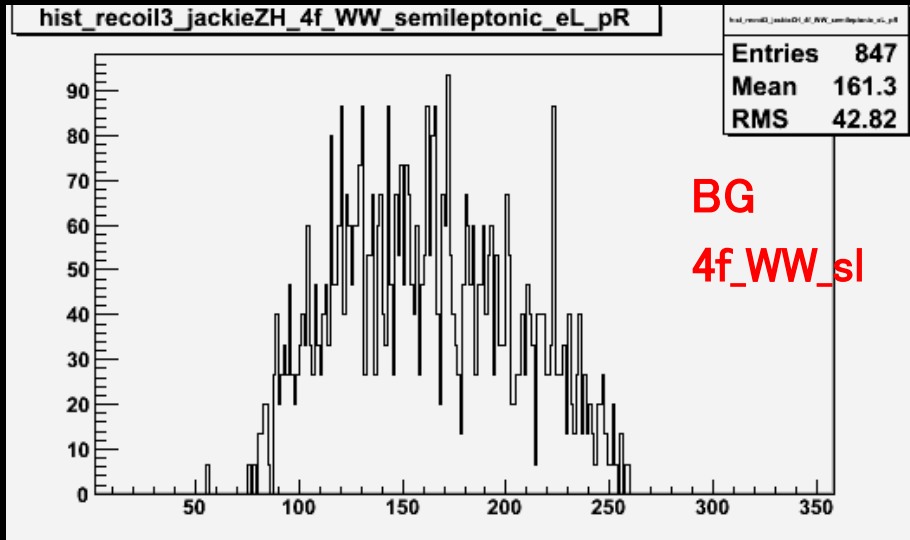


hist_recoil2_jackieZH_higgs_ffh_Pe2e2h_eL_pR



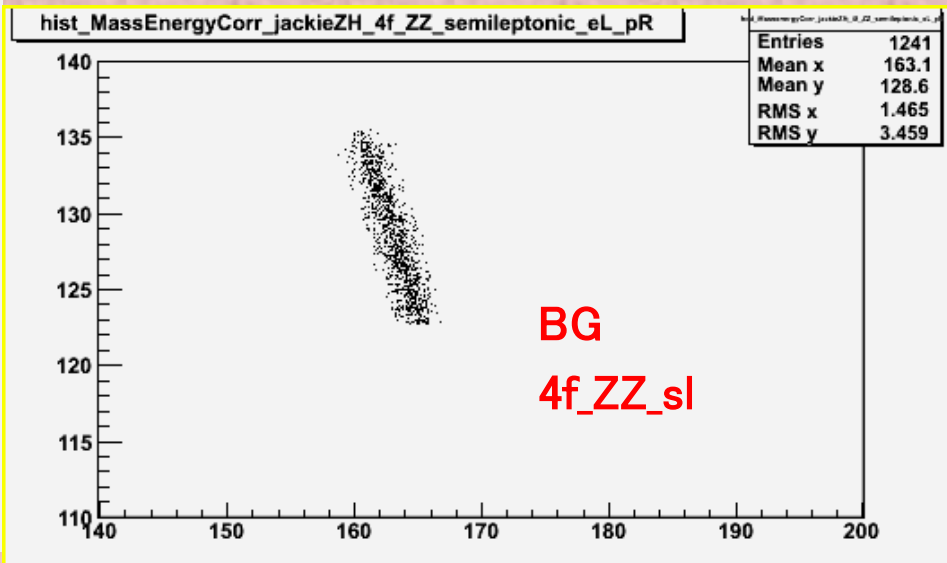
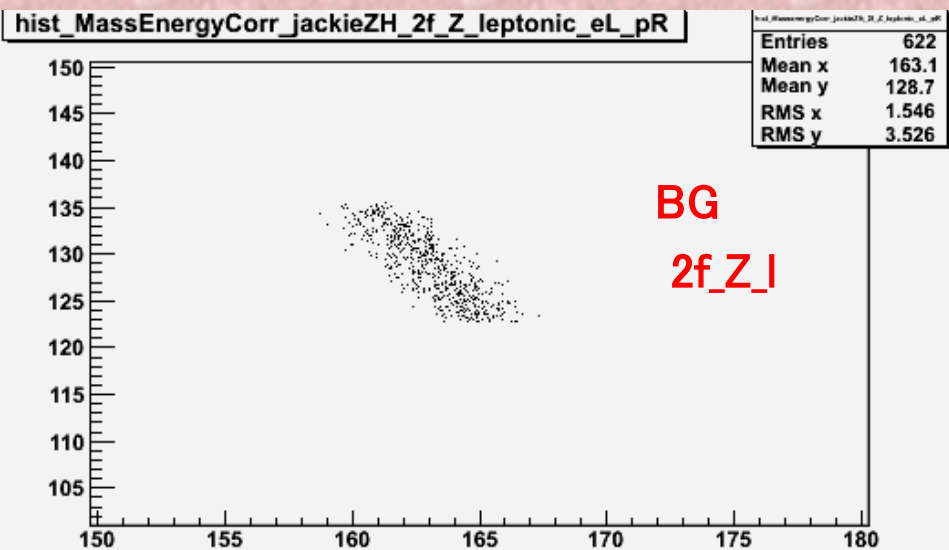
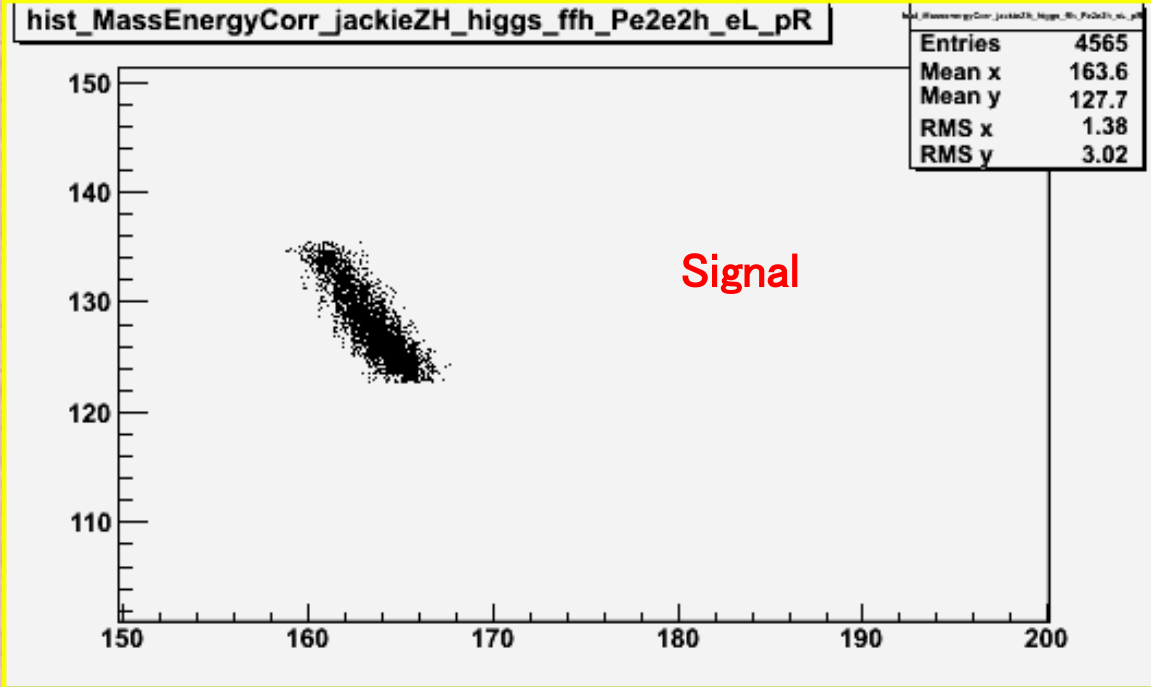
recoil mass 350 GeV

After inv mass cut



X axis : Z energy
Y axis : recoil mass

After cut



Summary

- **Higgs recoil mass study using $e^+e^- \rightarrow Zh \rightarrow \mu^+\mu^-h$**
@ $\text{Ec.m.s.} = 250 \text{ GeV}$, $L = 250 \text{ fb}^{-1}$ and @ $\text{Ec.m.s.} = 350 \text{ GeV}$, $L = 333 \text{ fb}^{-1}$
- **optimized data selection method**
- Compared cross section error with (without) considering BG MC statistics
- tried higher statistic samples (250 GeV only)
- updated results:
250 GeV:
 - $\epsilon_{\text{sig}} = 57.1 \pm 0.4 \%$, $S/B \sim 0.04$, **significance ~ 20.6**
 $\Delta\sigma_{\text{meas}} / \langle\sigma_{\text{meas}}\rangle = 4.9 \%$ (6.5%)
fitted recoil mass : $125.2 \text{ GeV} \pm 70 \text{ MeV}$
- **350 GeV:**
 - $\epsilon_{\text{sig}} = 40.4 \pm 0.4 \%$, $S/B \sim 0.42$, **significance ~ 16.6**
 $\Delta\sigma_{\text{meas}} / \langle\sigma_{\text{meas}}\rangle = 6.0 \%$ (8.8%)
fitted recoil mass : $125.6 \pm 0.3 \text{ GeV}$
- Compared different **polarization** scenarios : **$(-0.8, 0.3)$ vs $(+0.8, -0.3)$ vs $(0,0)$**

Further Plans

- **focus on analysis at Ec.m.s. = 350 GeV**
- **how to cut much more BG without losing too much signal ?**
 - find out why lots of signal lost after track quality selection
 - further optimization of data cut values, add dPT, bal cut
- **improve fitting method**
 - Multiple step fitting, fix values from previous fit
 - evaluate efficiency by integrating fitted curve (c.f. integrate histogram)

BACKUP

DBD Samples

350 GeV

/grid/ilc/prod/ilc/mc-dbd/ild/dst-merged/350-TDR_ws/

Most important 6f BG

2048 May 29 18:05 WW + two other charged leptons (2 other ch leptons could be mu mu)

and the 2 samples with "Z":

2048 May 29 18:05 Z + four up type quarks

2048 May 29 18:05 Z + four down type quarks

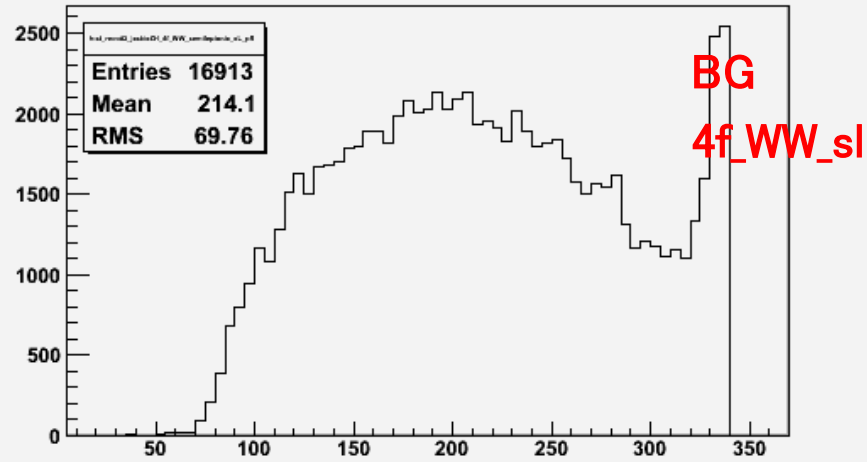
List of files

http://www-jlc.kek.jp/~miyamoto/CDS/prod_status/REC_ILD_o1_v05_350GeV.html

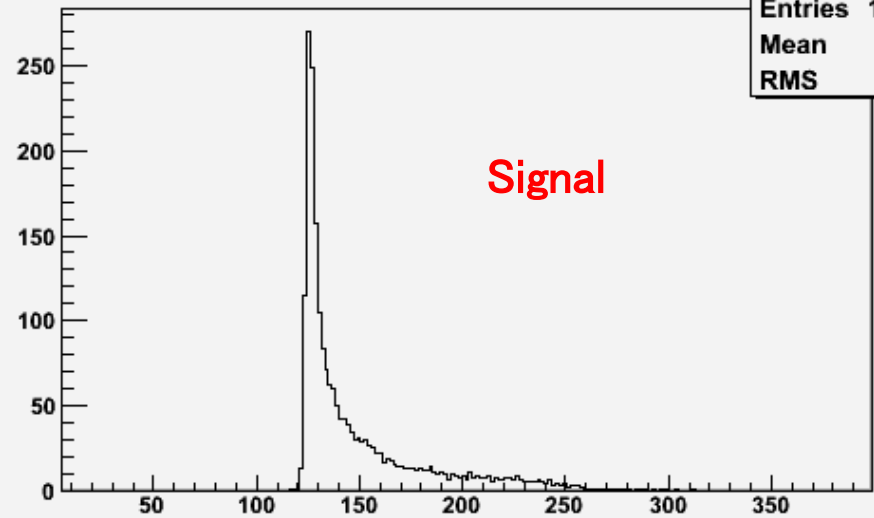
recoil mass 350 GeV

Before cut

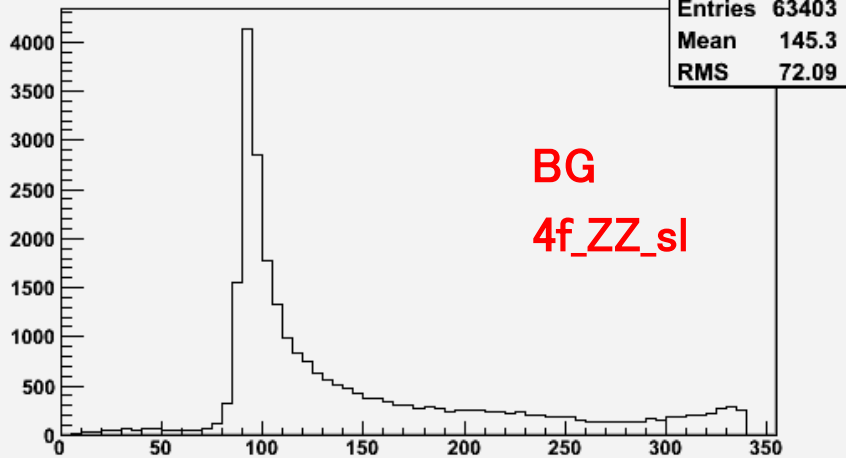
hist_recoil2_jackieZH_4f_WW_semileptonic_eL_pR



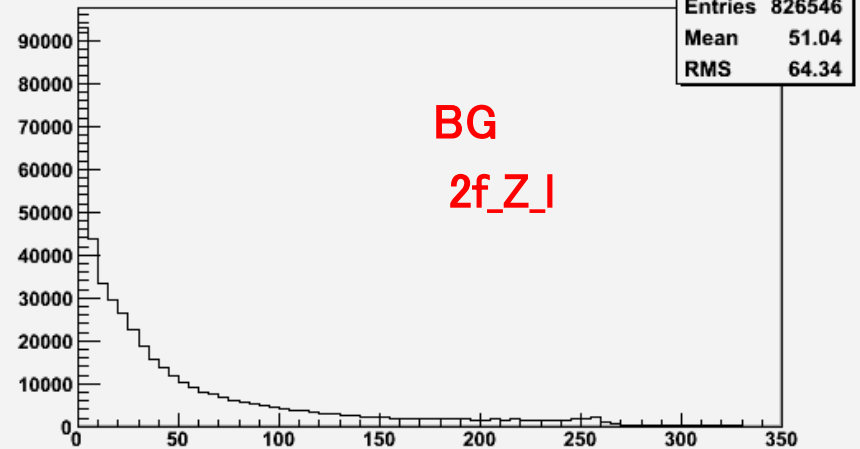
hist_recoil2_jackieZH_higgs_ffh_Pe2e2h_eL_pR



hist_recoil2_jackieZH_4f_ZZ_semileptonic_eL_pR

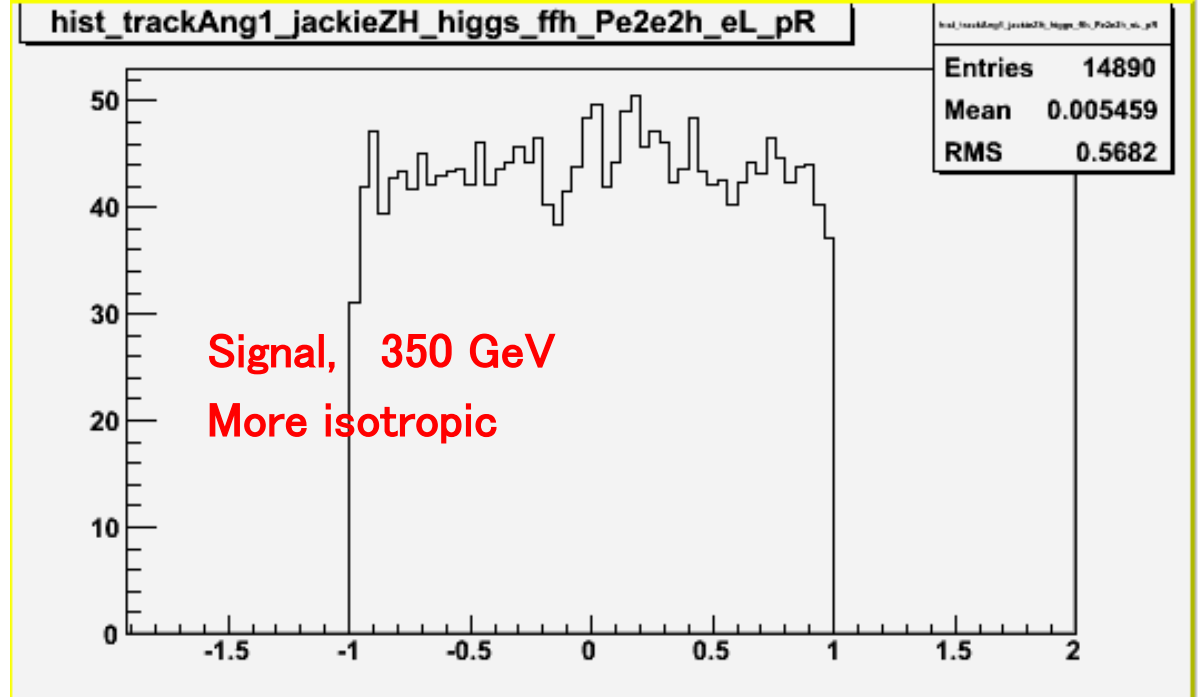


hist_recoil2_jackieZH_2f_Z_leptonic_eL_pR

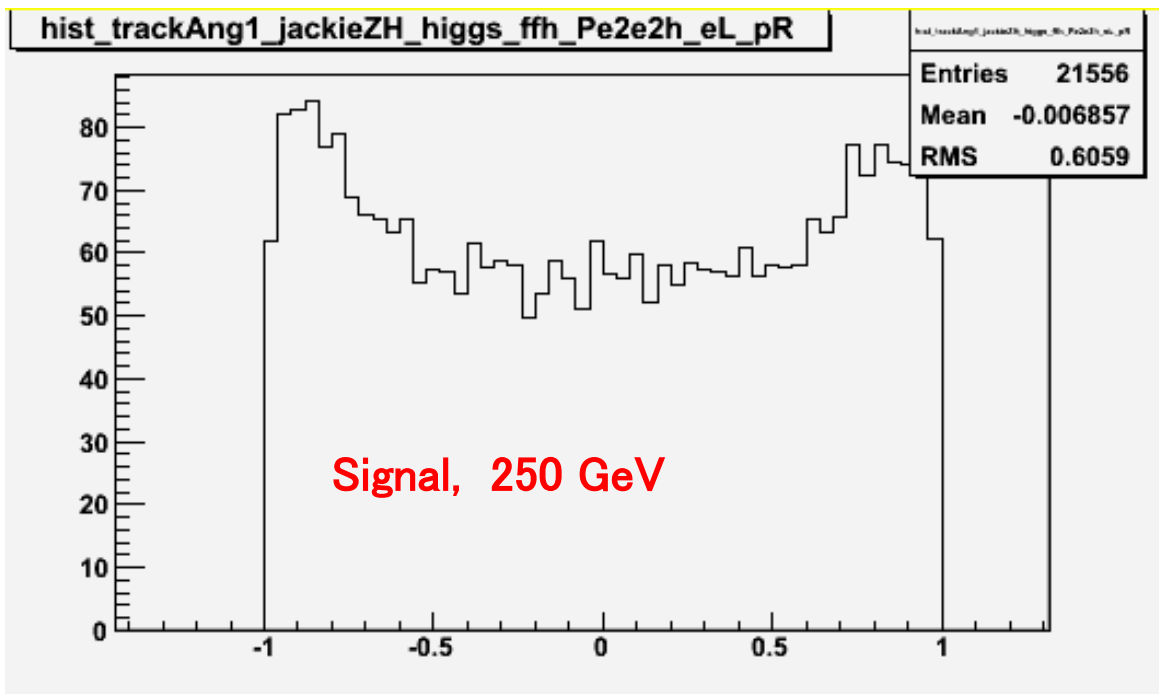


Cos(track angle),
350 GeV

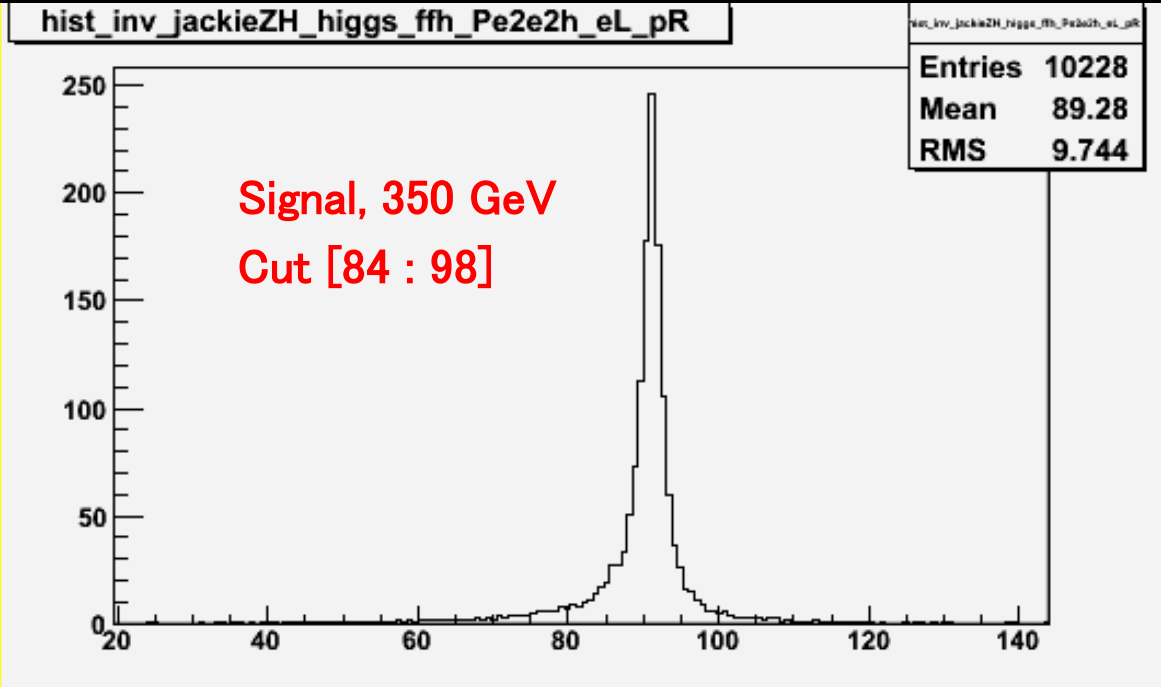
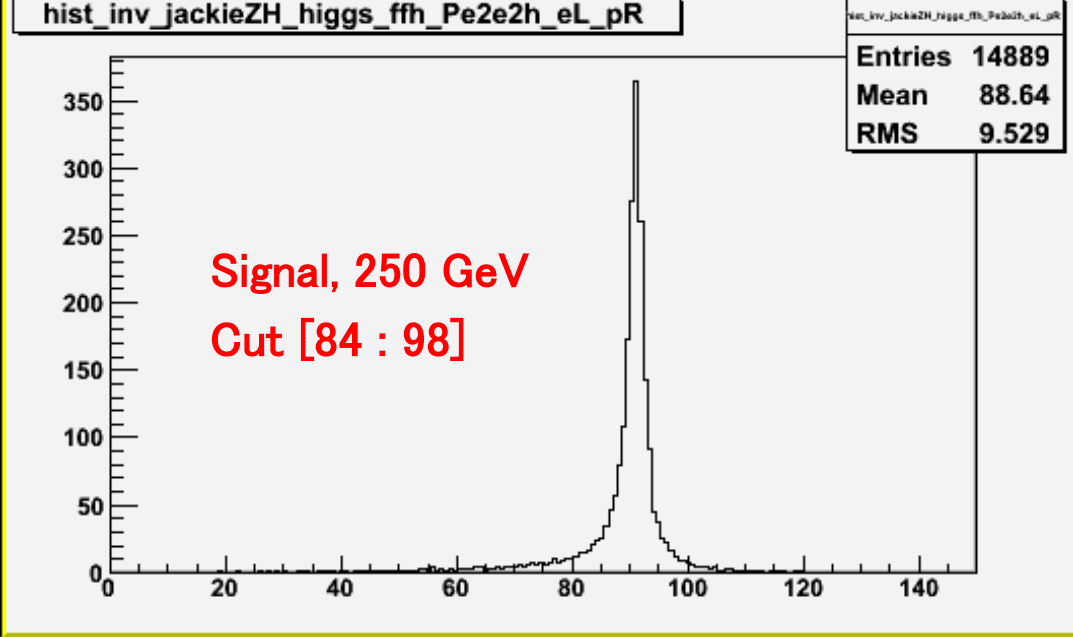
do cut
 $\cos(\text{trackAngle}) < 0.98$



do cut :
 $\cos(\text{trackAngle}) < 0.95$



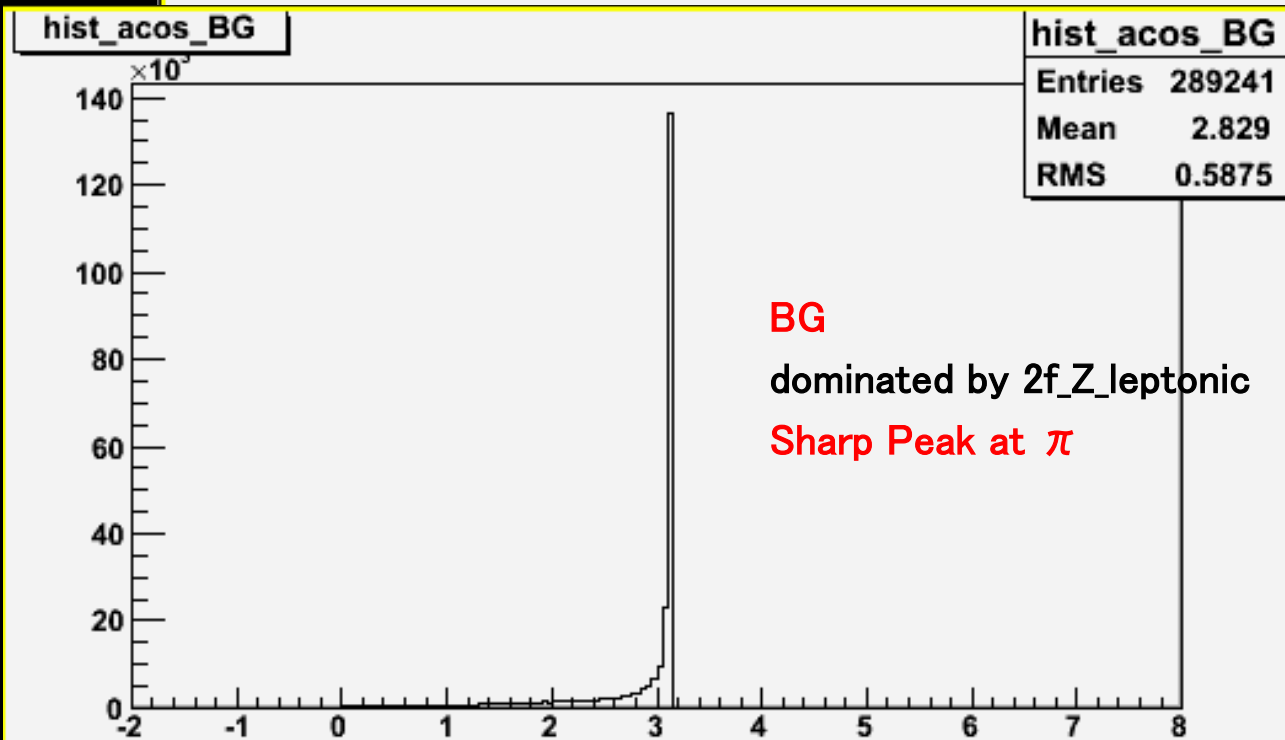
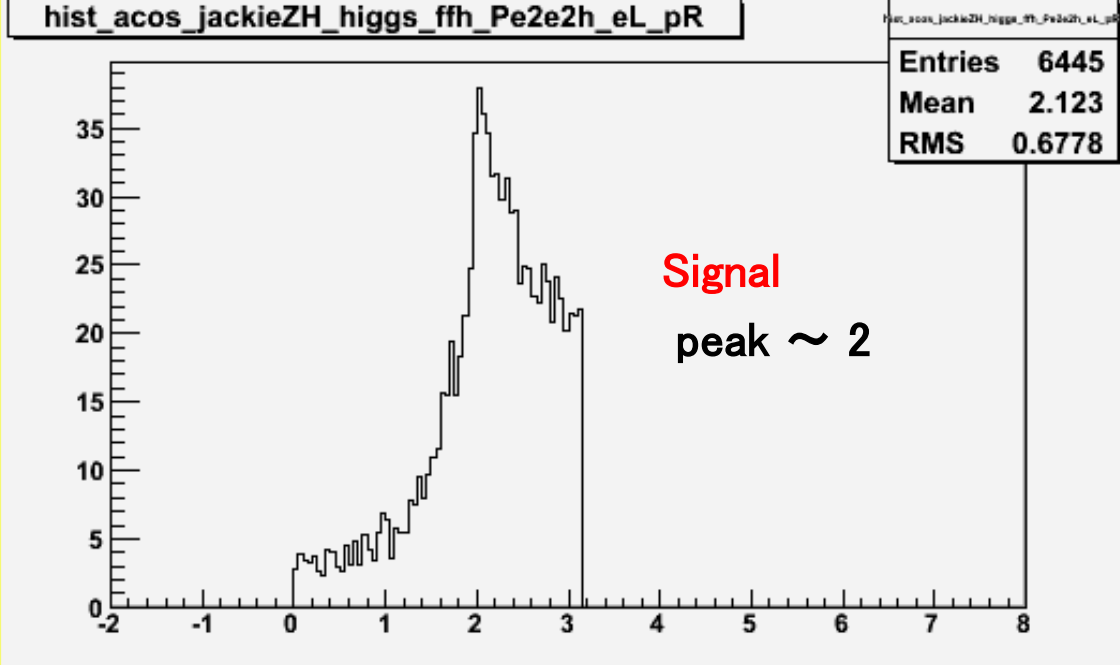
invariant mass
before cut



coplanarity, before cut ,
250 GeV

No coplanarity cut applied

wanted to maintain high signal eff.



coplanarity, before cut

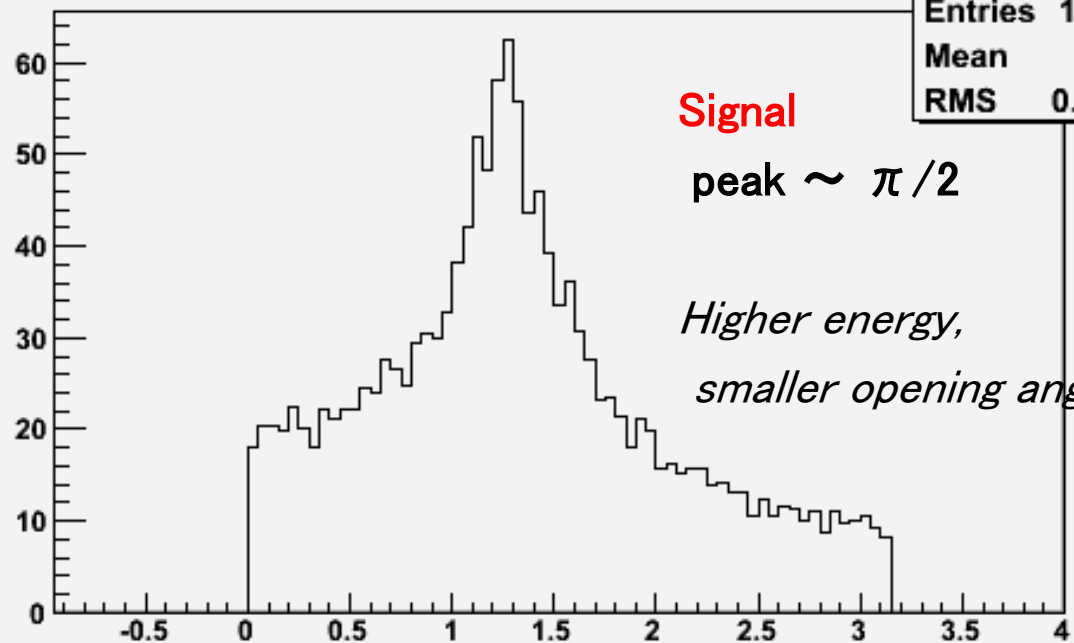
350 GeV

Cut:

coplanarity < 0.29

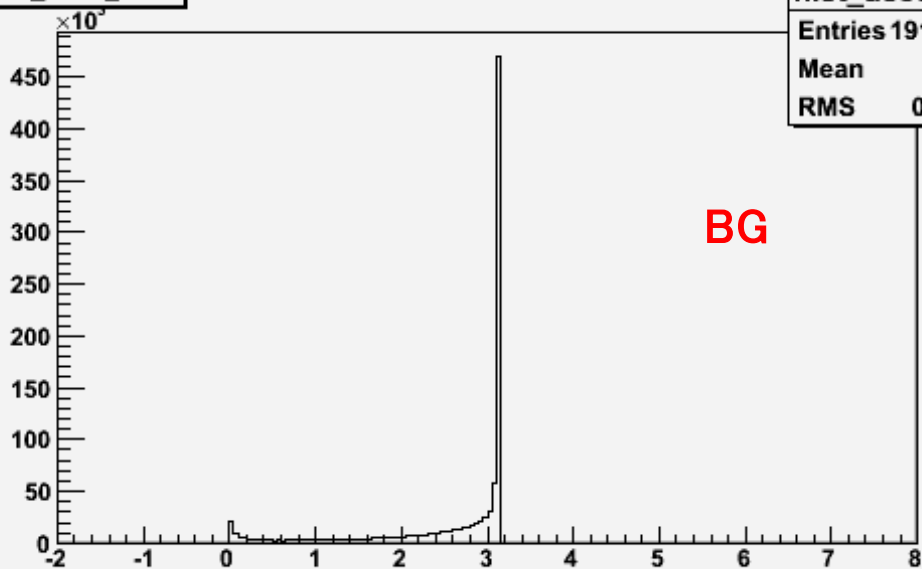
in order to remove more BG

hist_acos_jackieZH_higgs_ffh_Pe2e2h_eL_pR



hist_acos_jackieZH_higgs_ffh_Pe2e2h_eL_pR	
Entries	10228
Mean	1.341
RMS	0.7352

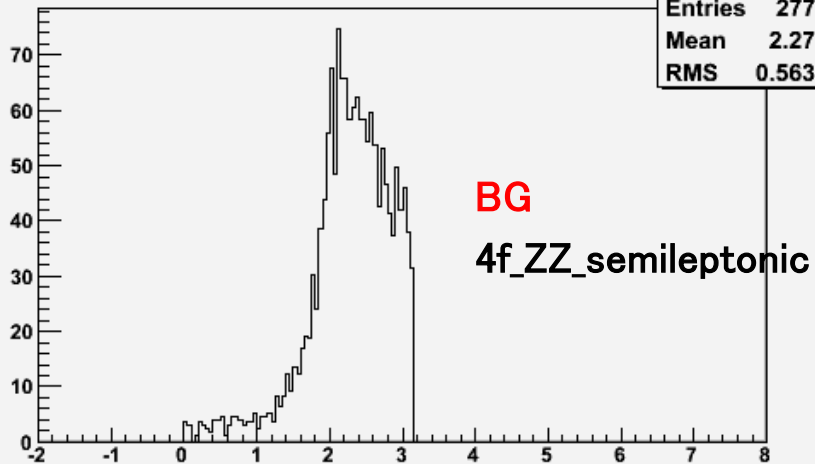
hist_acos_BG



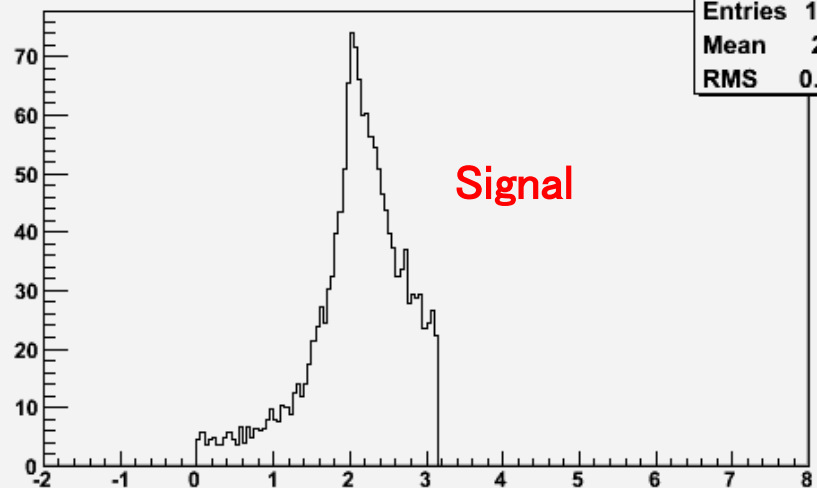
hist_acos_BG	
Entries	1916353
Mean	2.608
RMS	0.8562

coplanarity, after all other cuts

hist_acos2_jackieZH_4f_ZZ_semileptonic_eL_pR

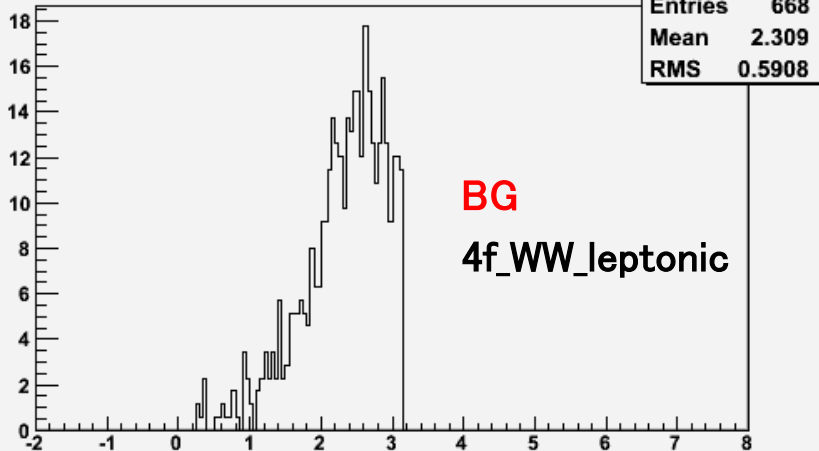


hist_acos2_jackieZH_higgs_ffh_Pe2e2h_eL_pR

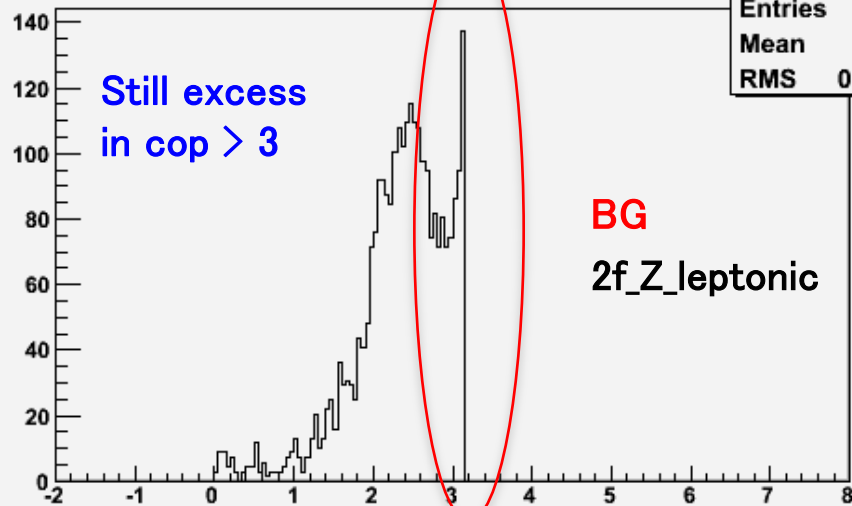


Trying to decide whether to use coplanarity cut

hist_acos2_jackieZH_4f_WW_leptonic_eL_pR



hist_acos2_jackieZH_2f_Z_leptonic_eL_pR

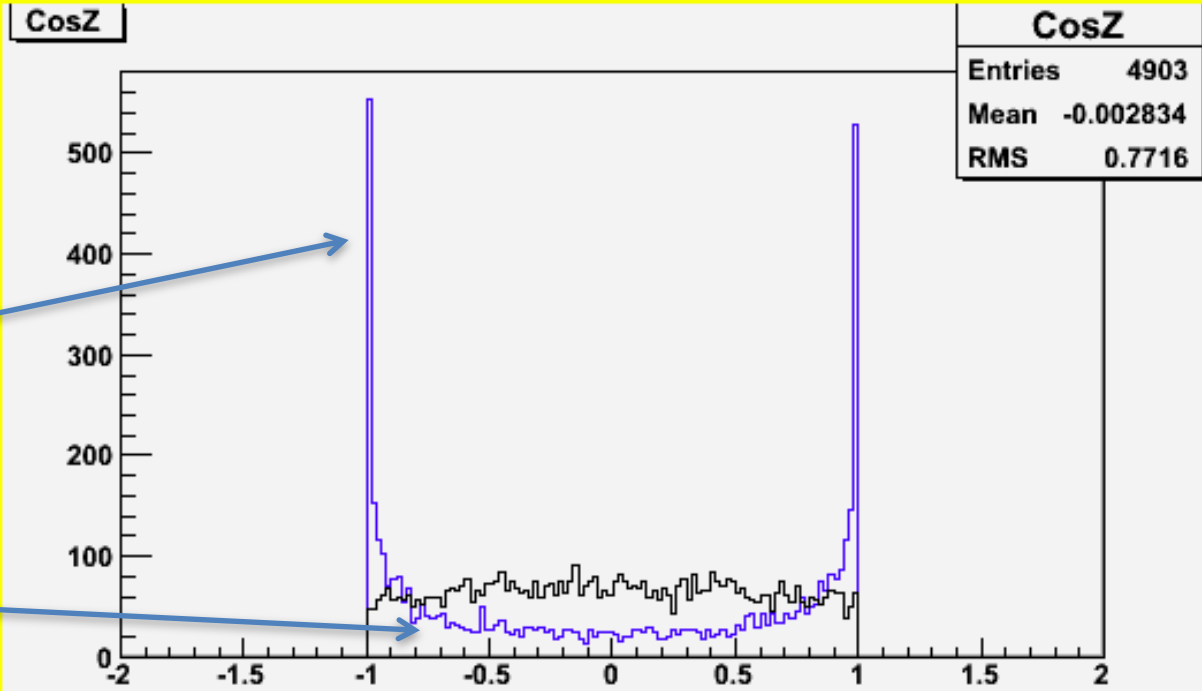


Z production angle

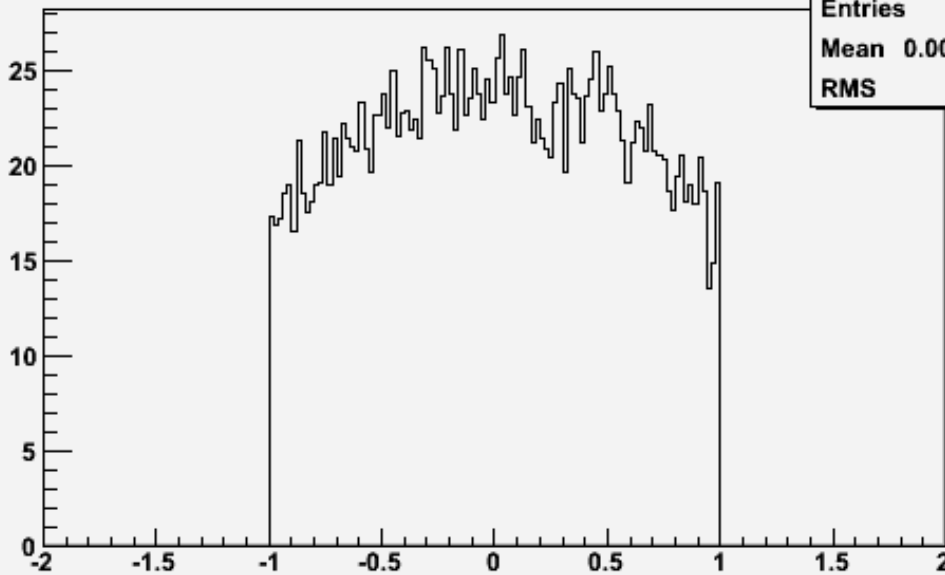
blue: BG (4f_ZZ_1
very forward

→ use for cut

Black: Signal
isotropic



hist_cos_jackieZH_higgs_ffh_Pe2e2h_eL_pR

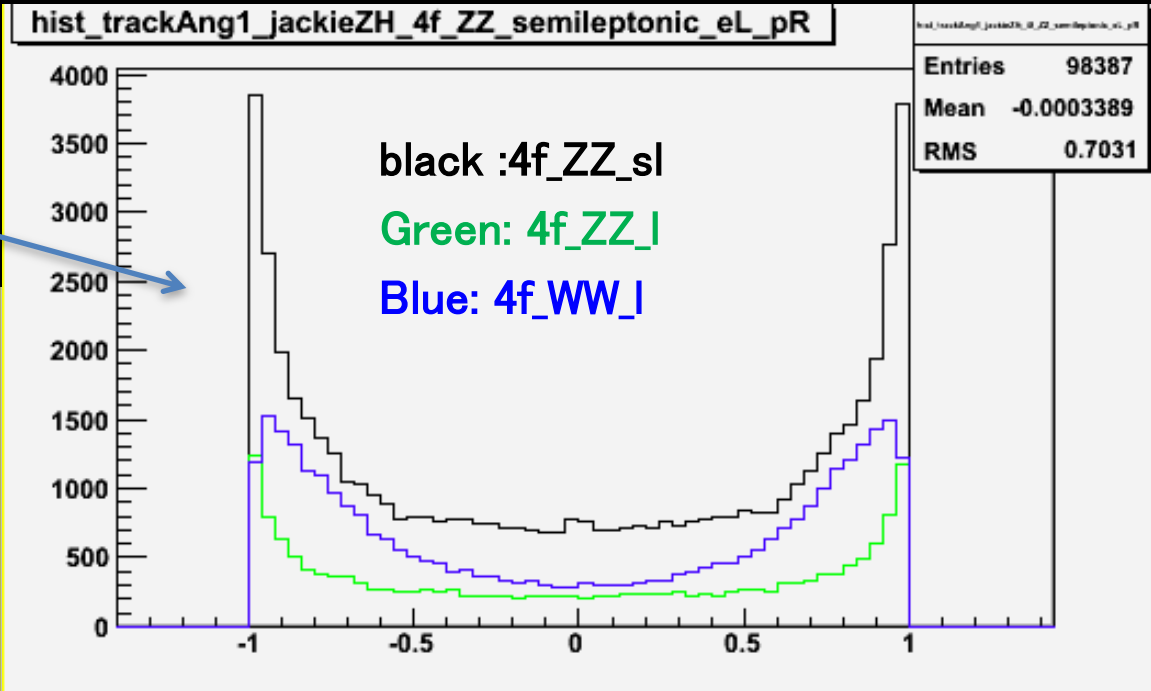
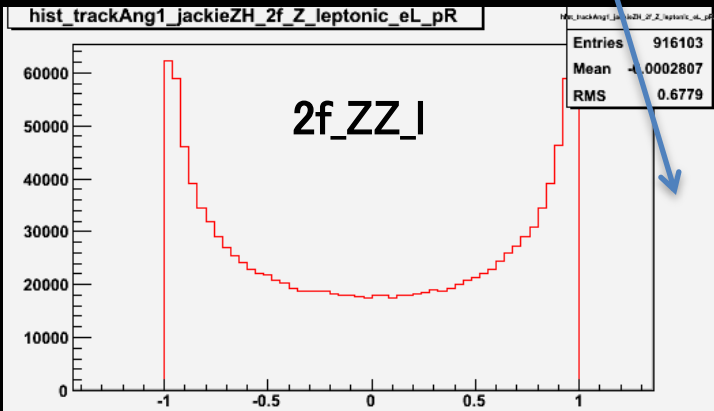


do cut :

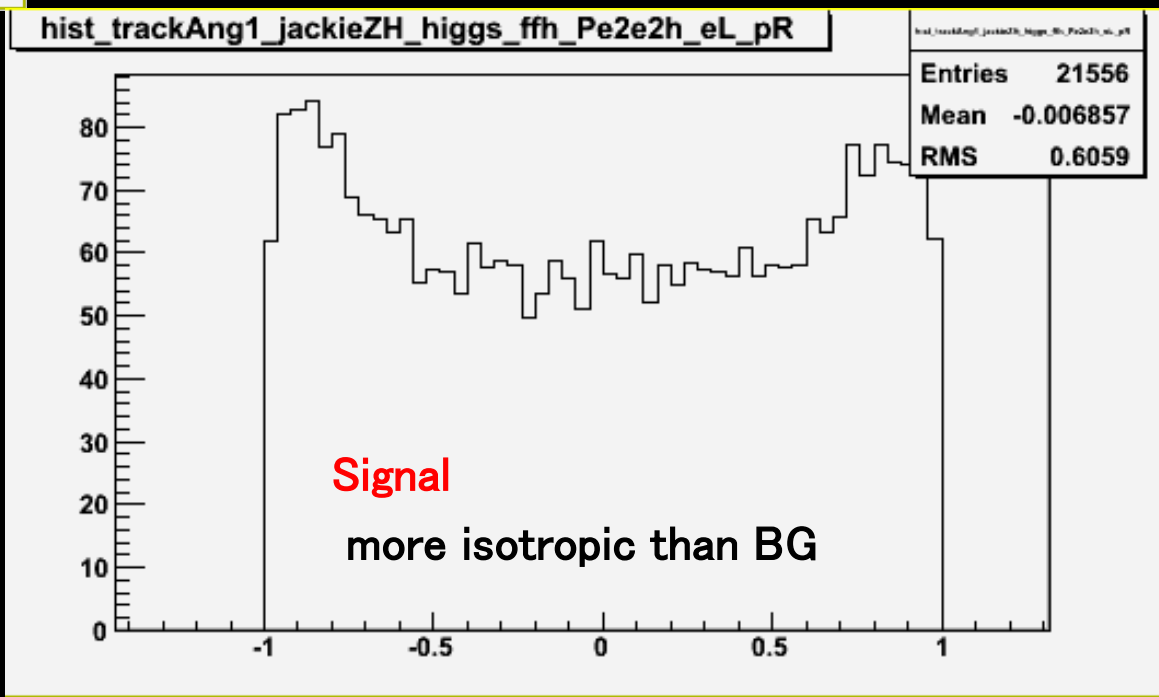
$$|\cos(\theta_{Zpro})| < 0.91$$

Cos(track angle),
250 GeV

BG is More forward

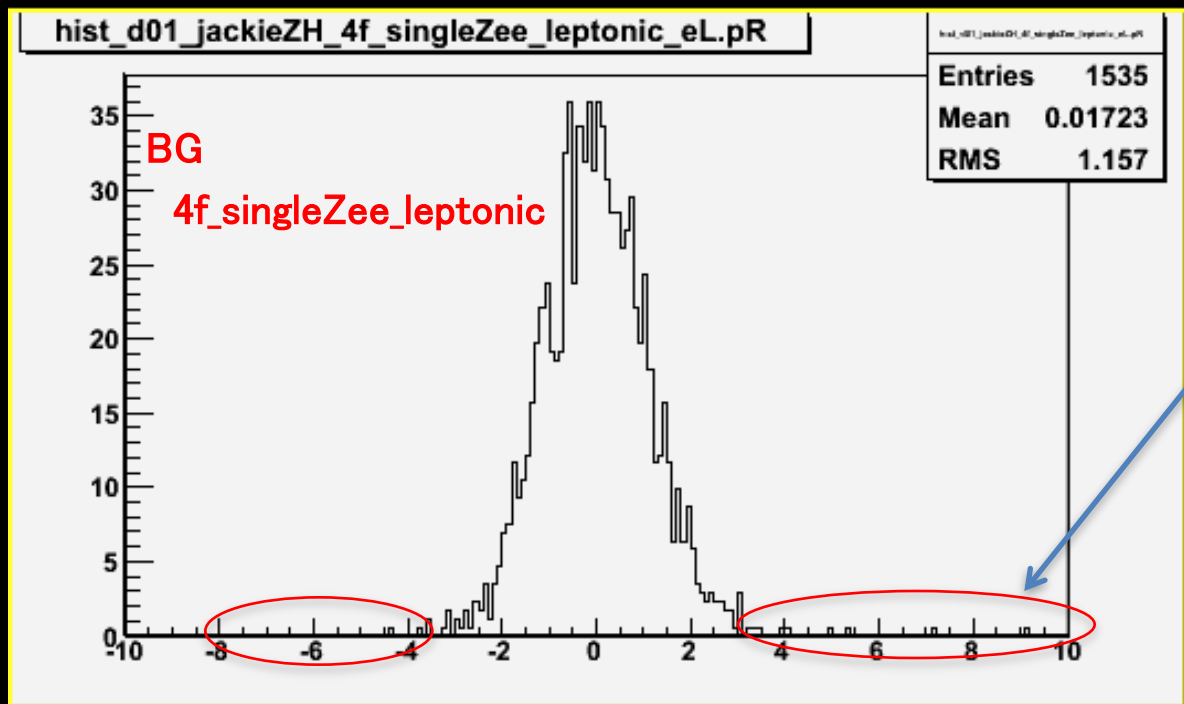
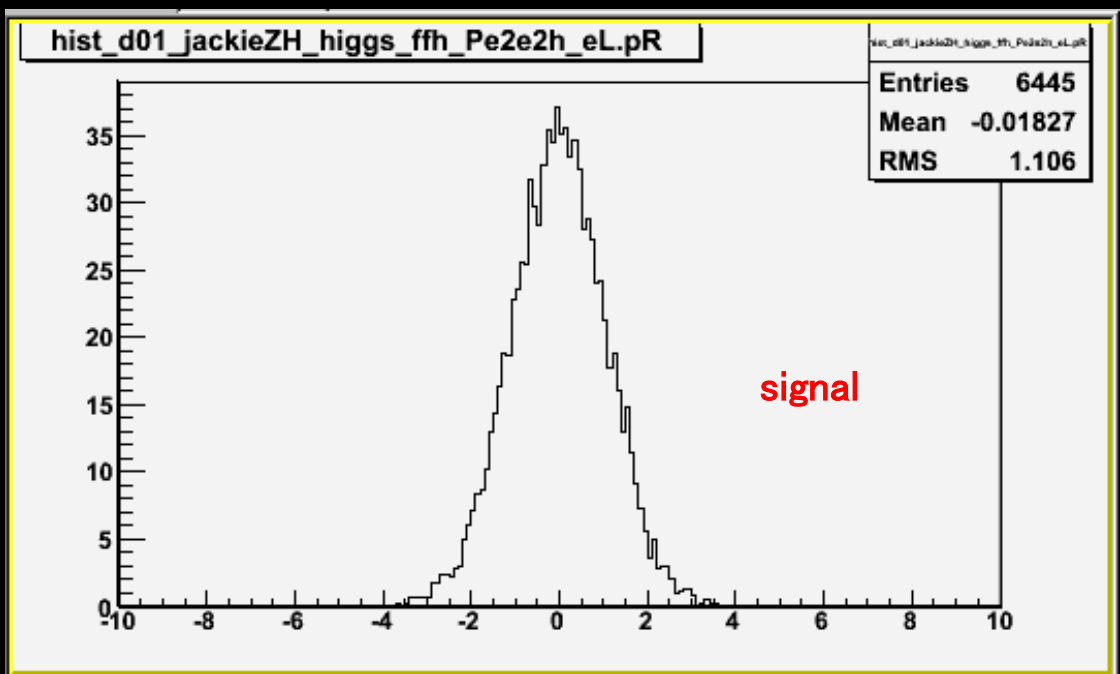


do cut :
 $\cos(\text{trackAngle}) < 0.95$



Impact parameter

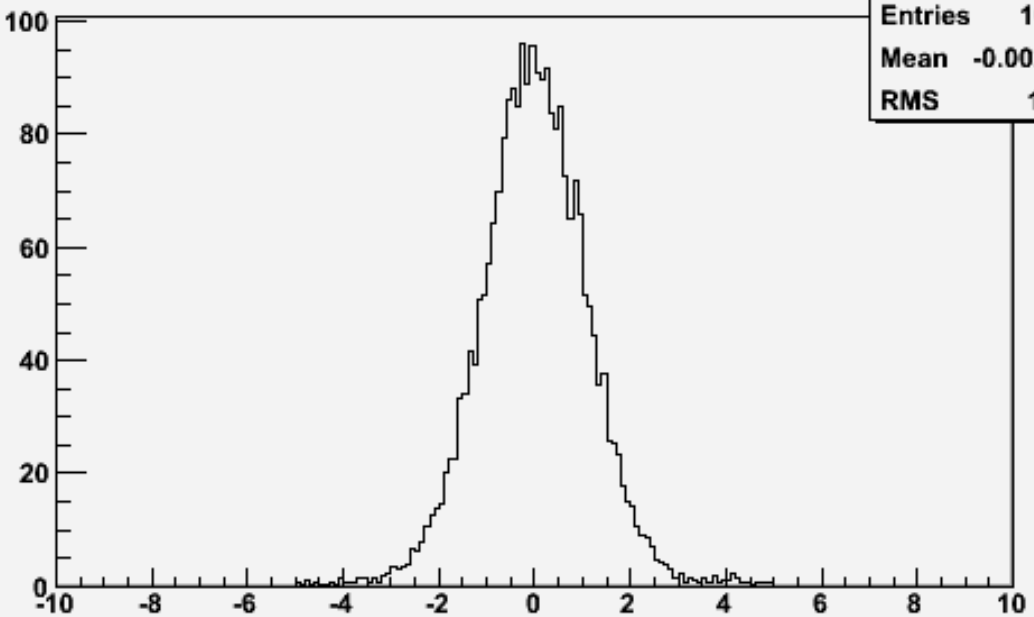
$D0 / \delta D0$



For some BG processes
exceed ± 4 slightly

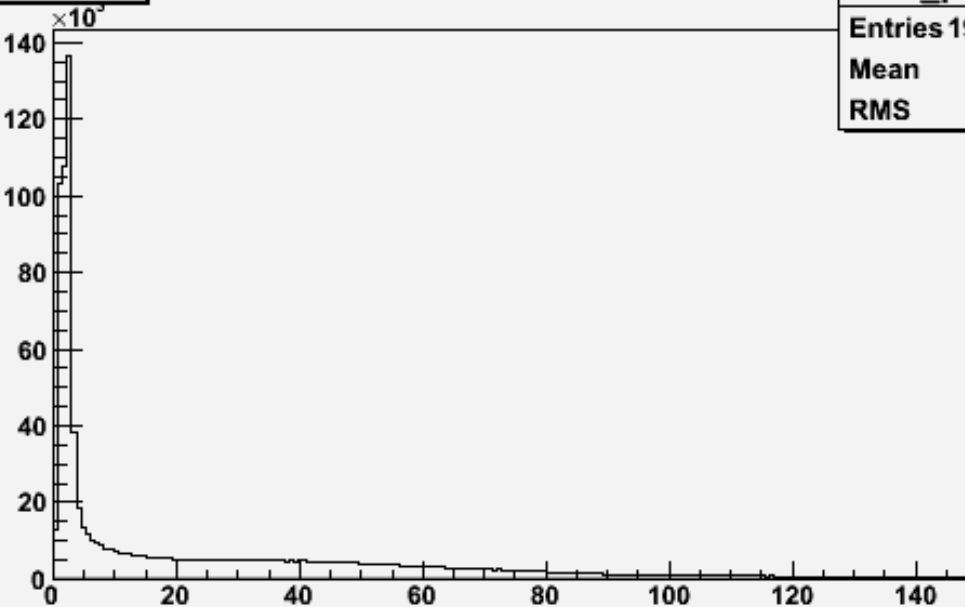
do cut : $|D0 / \delta D0| < 4$

hist_d01_jackieZH_higgs_ffh_Pe2e2h_eL_pR



Entries	16702
Mean	-0.002884
RMS	1.137

hist_pt_BG



Entries	1916353
Mean	26.52
RMS	33.32

statistic error of cross section σ

we want to maximize **significance** = $\langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle}$

i.e. optimize (efficiency ϵ) x (purity $\pi = \langle S \rangle / \langle N \rangle$)

expected # of signal events $\langle S \rangle = \epsilon * L * \sigma$ (L: integrated Luminosity)

assume $\langle B \rangle$ in signal region is "known" with small uncertainty

if observe N events and ignore uncertainty of Bg and eff :

$\langle \Delta \sigma_{\text{meas}} \rangle / \langle \sigma_{\text{meas}} \rangle = \text{inversely of } \{ \text{significance} = \langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle} \}$

Error on efficiency = n/N

binomial distr.

if detect n signal events out of N events : **efficiency = n/N** (assume N is constant)

stat error on n : $\Delta n = \sqrt{N * \epsilon * (1 - \epsilon)}$ $\rightarrow \Delta n / n = \sqrt{((1 - \epsilon) / n)}$)

higher ϵ , larger n is better

How to estimate error of cross section σ_s ?

when measuring σ_s , we want to maximize $\langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle}$

i.e. optimize (efficiency ϵ) x (purity π)

Why ??

A:

- expected # of signal events $\langle S \rangle = \epsilon * L * \sigma_s$ (L: integrated Luminosity)
- Expected # of BG events $\langle B \rangle$ in signal region
assume $\langle B \rangle$ is "known" with small uncertainty compared to stat. error on $\langle S \rangle$
- total # of events $\langle N \rangle = \langle S \rangle + \langle B \rangle = \epsilon * L * \sigma_s + \langle B \rangle$

if observe N events : $\sigma_{meas} = (N - \langle B \rangle) / (\epsilon * L)$

Stat error $\langle \Delta \sigma_{meas} \rangle = \Delta N / (\epsilon * L) = \sqrt{\langle N \rangle} / (\epsilon * L)$

Purity $\pi = \langle S \rangle / (\langle S \rangle + \langle B \rangle) = \langle S \rangle / \langle N \rangle$

$\sqrt{\langle S \rangle * \pi} = \langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle}$

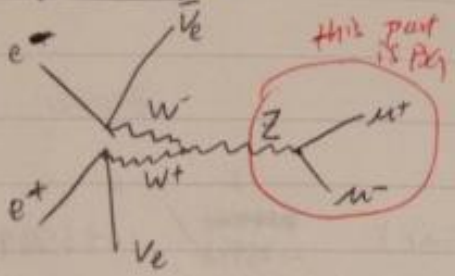
$\langle N \rangle = \langle S \rangle / \pi = \epsilon * L * \sigma_s / \pi$

$\langle \Delta \sigma_{meas} \rangle = \sqrt{\epsilon * L * \sigma_s / \pi} / (\epsilon * L) = \sqrt{\sigma_s / \epsilon * L * \pi}$

$\langle \Delta \sigma_{meas} \rangle / \langle \sigma_{meas} \rangle = 1 / \sqrt{\epsilon * L * \sigma_s * \pi} = 1 / \sqrt{\langle S \rangle * \pi}$

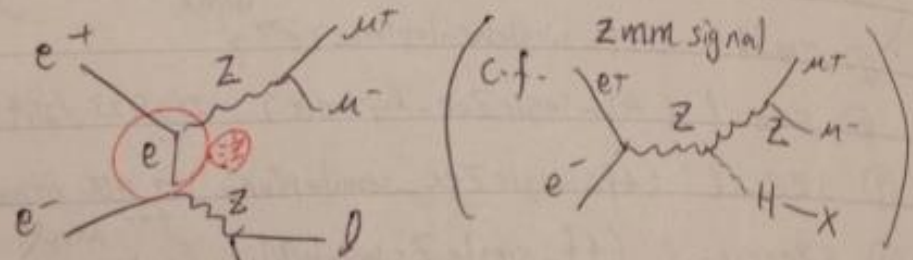
→ σ_s measurement error is inversely proportional to $\langle S \rangle / \sqrt{\langle S \rangle + \langle B \rangle}$!!

single Zmumu



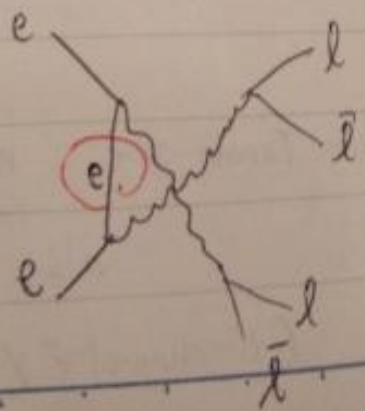
example diagrams for BG process for Zmumu

4f-ZZ-0

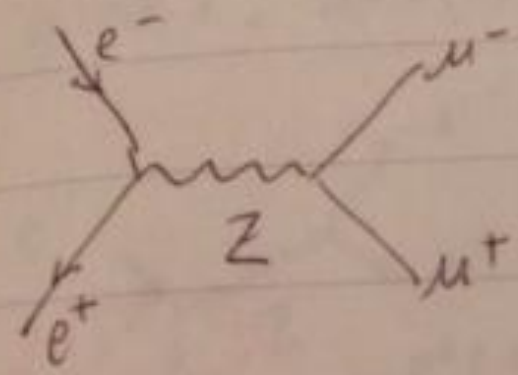


$e^+e^- \rightarrow$
 $\nu_e \bar{\nu}_e \mu^+ \mu^-$
 $e^+ e^- \mu^+ \mu^-$
 $\mu^+ \mu^- \mu^+ \mu^-$
 (or Z)?

crossed



Zl (2f)



4f ZZ-sl

