

Higgs Recoil Mass Study

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www.researchgate.net

recoil mass study using $e^+e^- \rightarrow Zh \rightarrow \mu^+\mu^-h$

Ec.m.s. = 250 GeV, $L = 250 \text{ fb}^{-1}$

Ec.m.s. = 350 GeV, $L = 333 \text{ fb}^{-1}$

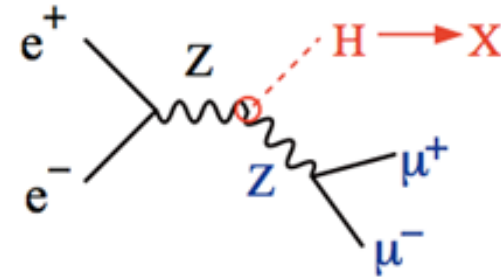
Goal:

precise measurement of

- Higgs mass
- cross section σ_H : $N = \sigma * L * \epsilon$

polarization:

$$(e^-, e^+) = (-0.8, +0.3)$$



$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

What's new this week

study using MC particle "truth"

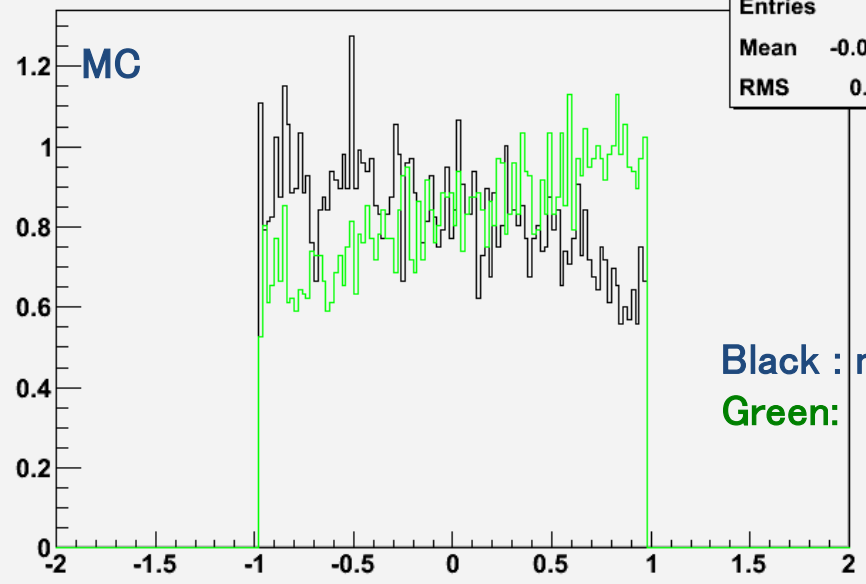
- observe cut efficiency
- observe muon track angle

fitting with weighted bins → use fitted results

- What is best recoil mass range for fitting ?

Study using MC particles

hist_cosmu1_mc_jackieZH_higgs_ffh_Pe2e2h_eR_pL

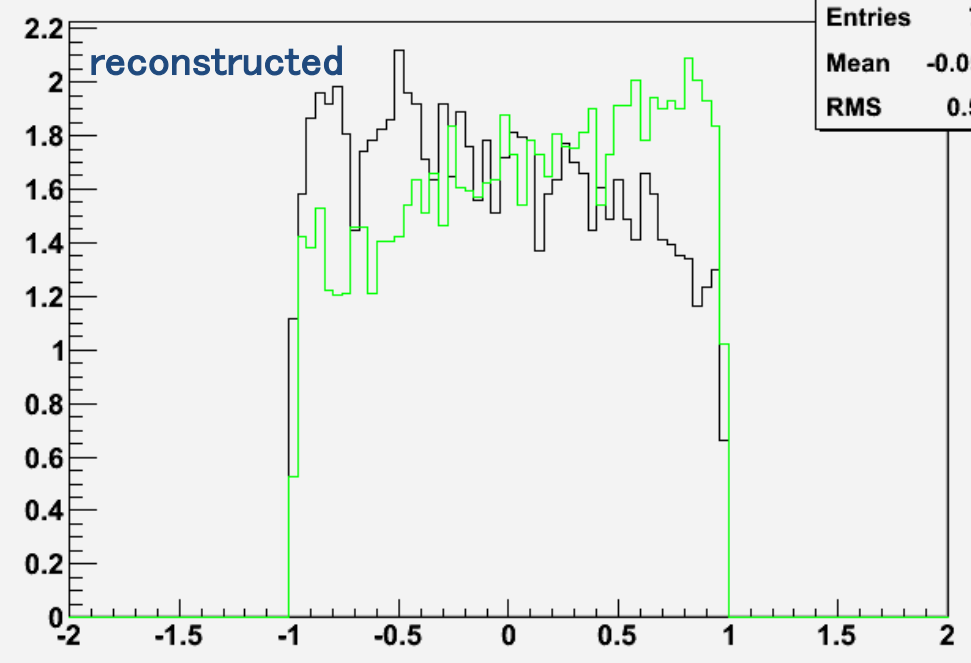


Entries	7711
Mean	-0.05792
RMS	0.5552

Black : muon-
Green: muon +

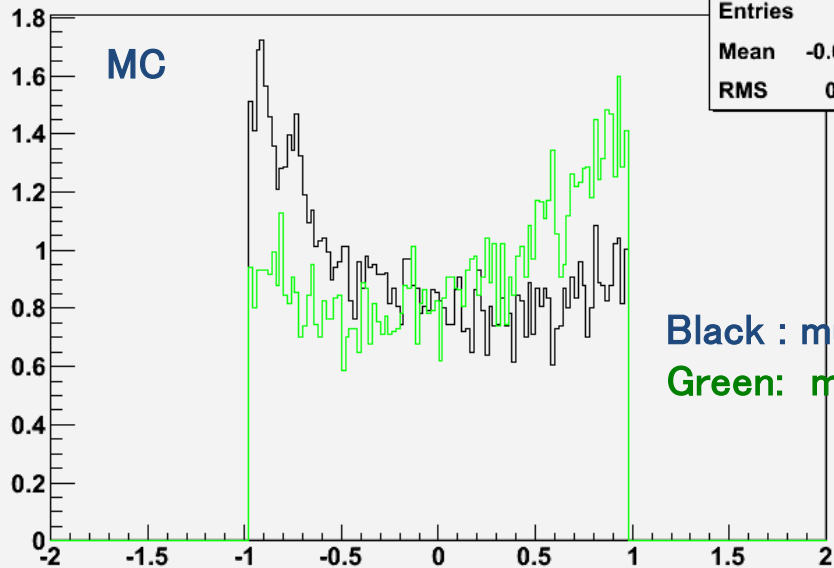
Muon track angle
sqrt(s) = 350 GeV

hist_trackAng1_jackieZH_higgs_ffh_Pe2e2h_eR_pL



Entries	7706
Mean	-0.05787
RMS	0.5554

hist_cosmu1_mc_jackieZH_higgs_ffh_Pe2e2h_eR_pL



Entries 10411
Mean -0.09175
RMS 0.5964

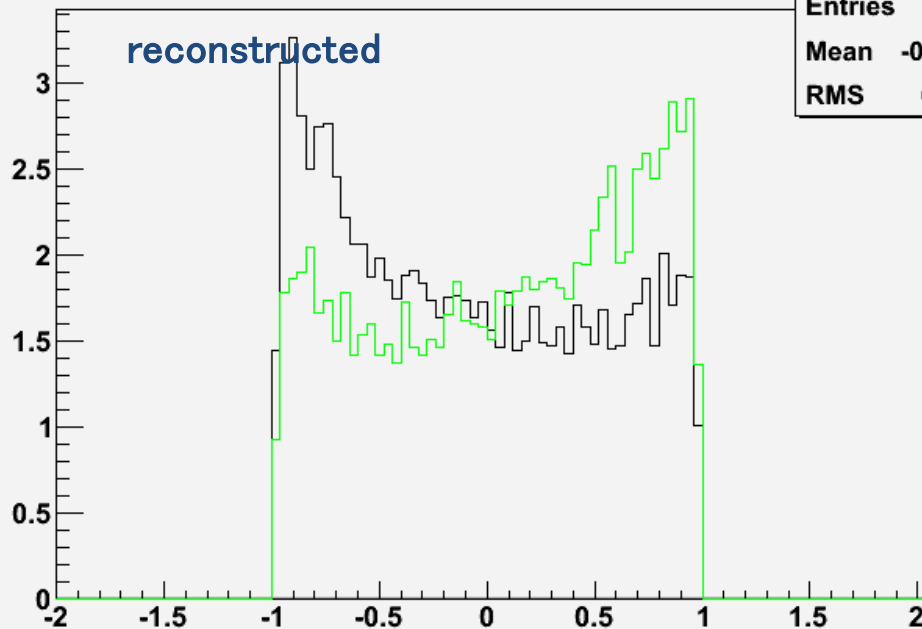
Black : muon
Green: muon +

more forward/ asymmetrical
than 350 GeV

Muon track angle

sqrt(s) = 250 GeV

hist_trackAng1_jackieZH_higgs_ffh_Pe2e2h_eR_pL

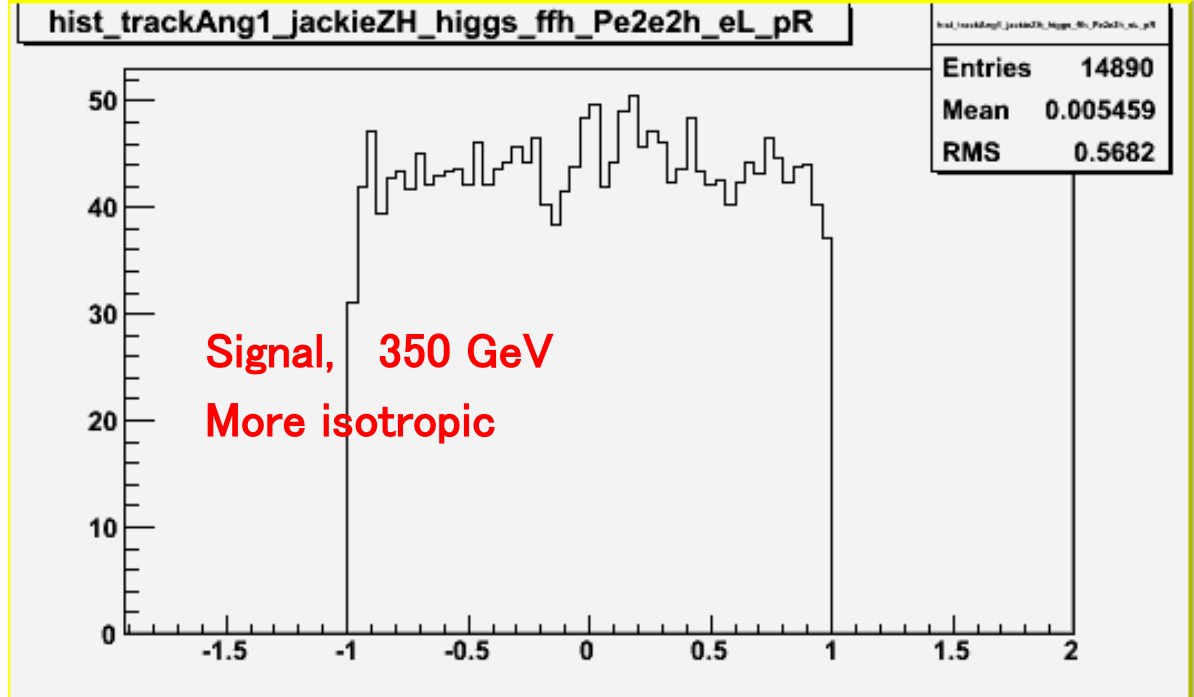


Entries 10406
Mean -0.09141
RMS 0.5966

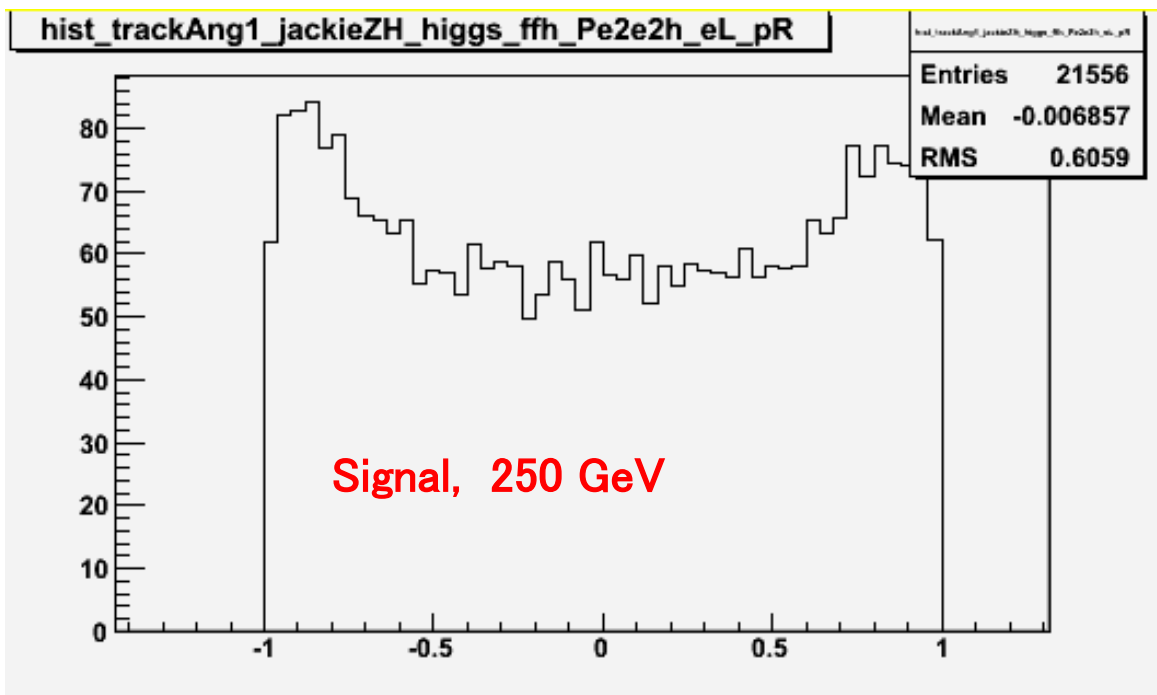
reconstructed

Cos(track angle),
350 GeV

do cut
 $\cos(\text{trackAngle}) < 0.98$



do cut :
 $\cos(\text{trackAngle}) < 0.98$



- **preliminary comparison of cut efficiency between MC truth and reconstructed for 350 GeV**
for now, just observe signal and dominant BGs

Rec

cut	signal	eff	4f_ZZ_sl	eff	2f_Z_l	eff
raw	2288	100%	188087	100.00%	2226361	100.00%
only best mu pair	2214	97%	25217	13.41%	329581	14.80%
cos(trackAng)<0.98	2202	96%	19906	10.58%	305146	13.71%
84 <M_inv <98	1824	80%	5314	2.83%	94671	4.25%
10 <P_Td<140	1817	79%	5198	2.76%	26063	1.17%
copl < 3	1790	78%	4853	2.58%	22766	1.02%
cos(θ Z)<0.91	1707	75%	3672	1.95%	10765	0.48%
120 GeV <M_rec <140 GeV	1089	48%	1133	0.60%	1050	0.05%

signal efficiency and BG cut is slightly better for MC (?), but mostly similar

MC

cut	signal	eff	4f_ZZ_sl	eff	2f_Z_l	eff
raw	2288	100%	188087	100.00%	2226361	100.00%
only best mu pair	2288	100%	26219	13.94%	417982	18.77%
cos(trackAng)<0.98	2208	97%	17385	9.24%	306297	13.76%
84 <M_inv <98	1981	87%	5115	2.72%	102691	4.61%
10 <P_Td<140	1945	85%	5006	2.66%	24539	1.10%
copl < 3	1945	85%	4691	2.49%	24539	1.10%
cos(θ Z)<0.91	1852	81%	3599	1.91%	11813	0.53%
120 GeV <M_rec <140 GeV	1256	55%	1056	0.56%	986	0.04%

Results for 350 GeV

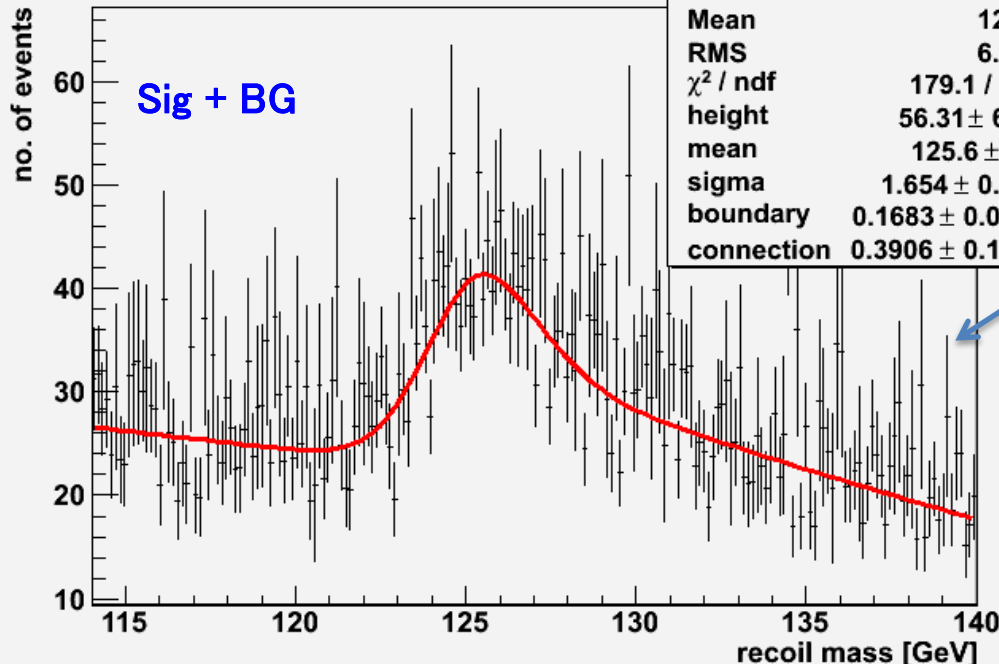
Tried to fit in wider range

[114– 140 GeV] → Changed to [115 – 150 GeV]

Tried widening recoil mass window

[123– 135 GeV] → Changed to [120 – 140 GeV]

hist_recoil_all



new fitting: using weighted bins

Integrated fitted func in (120 – 140 GeV)

Nsig = 1115

(error is 133 ? = relative error of fitted height ?)

Integrated BG fitted func in (120 – 140 GeV)

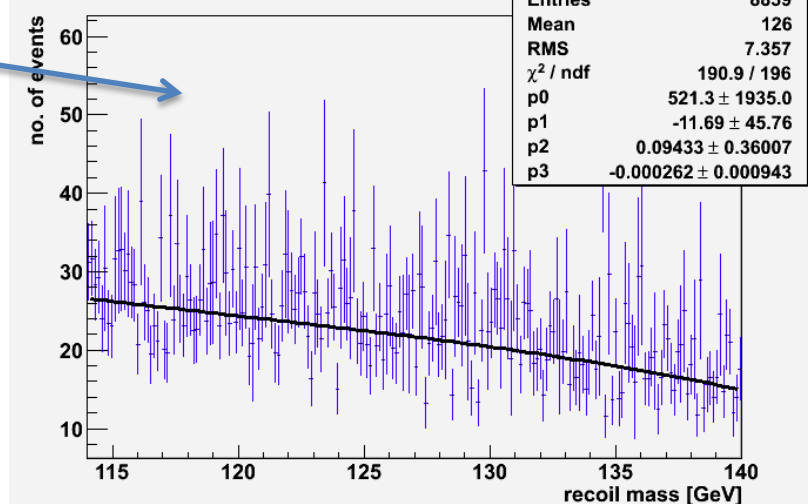
- $N_{bg} = 3100$
- $S/BG = 1115 / 3100 = 0.36$
- **significance = 17.2**

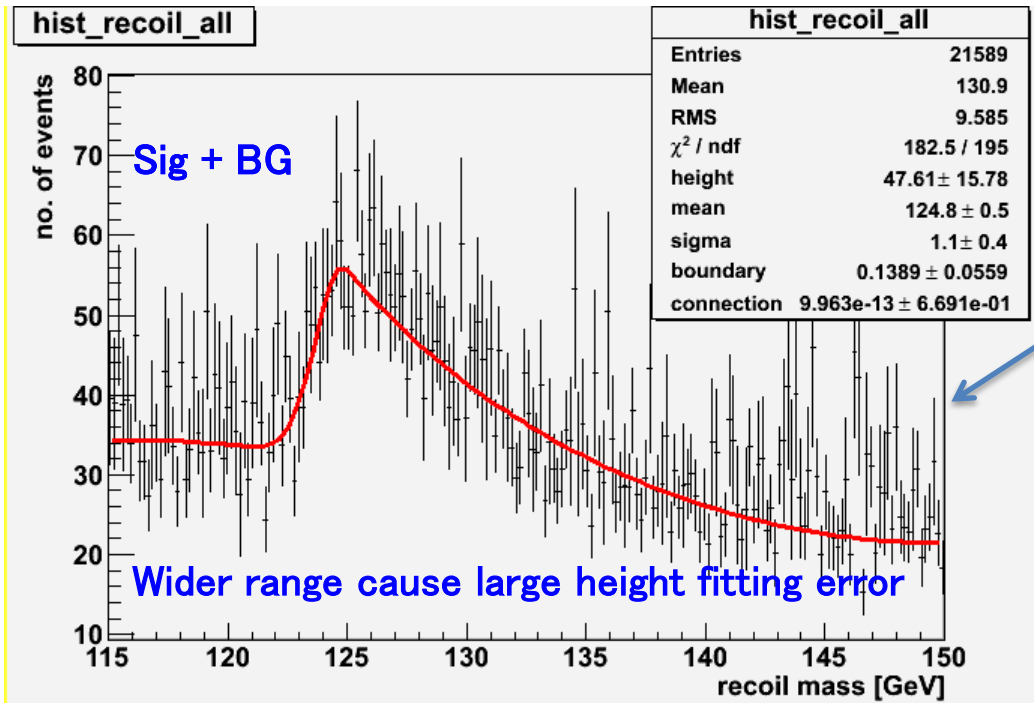
Result from counting under histogram

- $\langle n \rangle = 1125 \pm 24$
- $\langle \epsilon \rangle = 47.4 \pm 0.5 \%$
- $\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.0$
- $\langle n \rangle / \langle B \rangle = 0.31$

$\Delta \sigma_{meas} / \langle \sigma_{meas} \rangle = 6.3 \%$
 9.3 % if consider BG uncertainty

hist_recoil_BG





new fitting: using weighted bins

Fitting in range **115-150 GeV**

Wider range !!

Integrated fitted func in (120 – 140 GeV)

Nsig = 1145

Integrated BG fitted func in (120 – 140 GeV)

Nbg= 3255

S/BG = 1145 / 3255 = 0.35

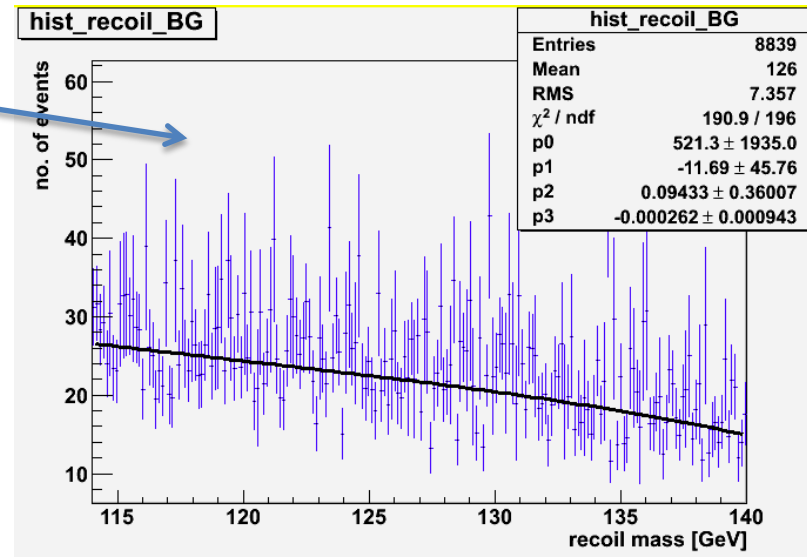
significance = 17.3

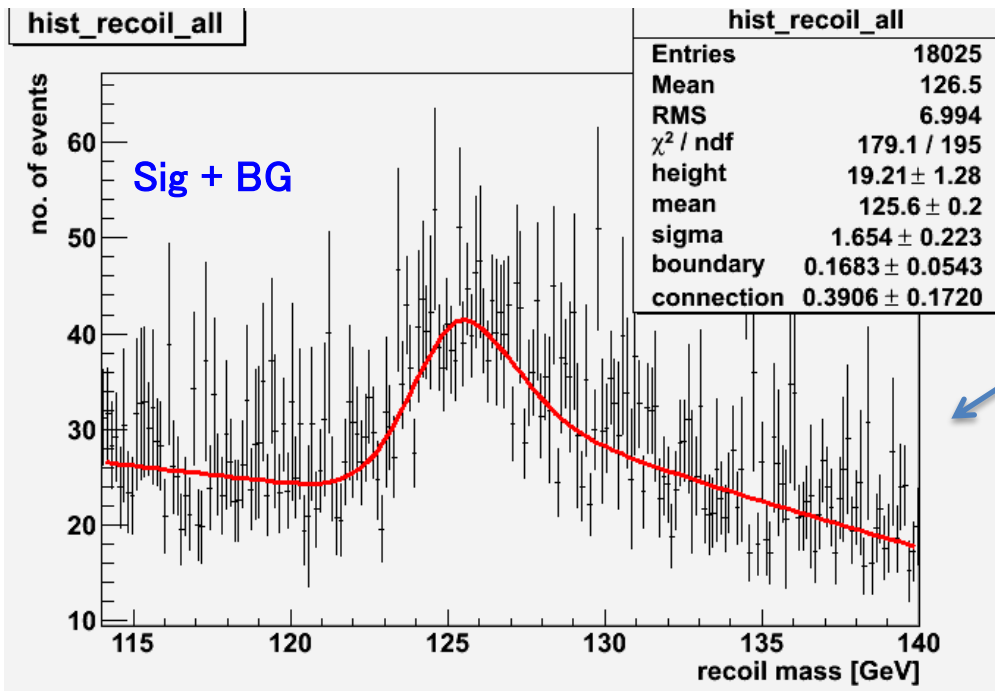
Result from counting under histogram

- $\langle n \rangle = 1125 \pm 24$
- $\langle \epsilon \rangle = 47.4 \pm 0.5 \%$
- $\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.0$
- $\langle n \rangle / \langle B \rangle = 0.31$

$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.3 \%$

9.3 % if consider BG uncertainty





new fitting: using weighted bins

Before fixing overall factor of 1/sigma

Integrated fitted func in (120 – 140 GeV)

Nsig = 1115

(error is 74 ? 6.7%)

= relative error of fitted height ?)

Integrated BG fitted func in (120 – 140 GeV)

Nbg = 3100

• **S/BG = 1115 / 3100 = 0.36**

• **significance = 17.2**

Result from counting under histogram

• $\langle n \rangle = 1125 \pm 24$

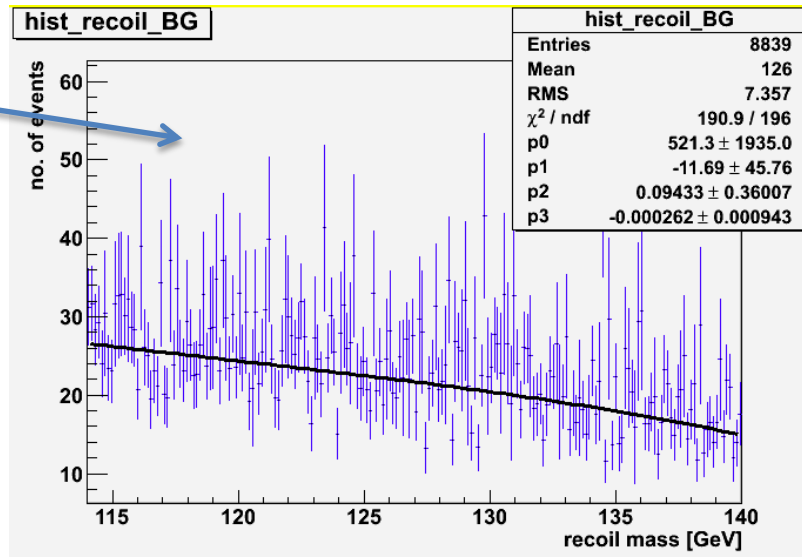
• $\langle \epsilon \rangle = 47.4 \pm 0.5 \%$

• $\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.0$

• $\langle n \rangle / \langle B \rangle = 0.31$

$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.3 \%$

9.3 % if consider BG uncertainty



Tried to widen recoil mass cut window

$\sqrt{s} = 350 \text{ GeV}$ $L = 333 \text{ fb}^{-1}$

M_recoil: 123 – 135 GeV

$$\langle n \rangle = 923 \pm 23$$

$$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$$

$$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.6$$

$$\langle n \rangle / \langle B \rangle = 0.42$$

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.0 \%$$

8.8 % if consider BG uncertainty

M_recoil: 120 – 140 GeV

$$\langle n \rangle = 1125 \pm 24$$

$$\langle \epsilon \rangle = 47.4 \pm 0.5 \%$$

$$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.0$$

$$\langle n \rangle / \langle B \rangle = 0.31$$

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.3 \%$$

9.3 % if consider BG uncertainty

If I just count inside histogram :

- signal efficiency is increased by widening recoil mass cut window
- But S/N is worse

S/N and significance is better when I use fitted results

Next : I need to do double loop fitting (leave only mean and height as free parameters)

Data selection : 123 – 135 GeV

$\sqrt{s} = 350 \text{ GeV}$

with all 6f BG included, whizard events (no NRQCD correction?)

cut	signal	eff	BG_all	eff	S/B	S/sqrt(S+B)
raw	2288	100%	6242481	100.00%	0.0004	0.92
only best mu pair	2202	96%	689050	11.04%	0.0032	2.65
$\Delta D0/D0 < 5$	2190	96%	610653	9.78%	0.0036	2.80
$\cos(\text{trackAng}) < 0.98$	2161	94%	543876	8.71%	0.0040	2.92
$84 < M_{\text{inv}} < 98$	1791	78%	115244	1.85%	0.0155	5.24
$10 < P_{\text{Tdl}} < 140$	1786	78%	46855	0.75%	0.0381	8.10
$\text{copl} < 3$	1759	77%	41849	0.67%	0.042	8.42
$\cos(\theta_Z) < 0.91$	1677	73%	25623	0.41%	0.065	10.15
123 GeV $< M_{\text{rec}} < 135 \text{ GeV}$	924	40%	2188	0.04%	0.422	16.57

Signal efficiency 40%

$S/N \rightarrow 0.42$

Significance ~ 16.6

cut	4f_ZZ		2f_Z	4f_WW		4fSingleZe	4fSingleZ	4f_ZZWWMix_l	6f
	l	sl	l	l	sl	e_l	nn_l		
raw	19632	188087	2226358	226193	2715937	243879	43056	541352	37989
only best mu pair	4231	20482	349026	25340	145897	37121	8924	94303	3726
$\Delta D0/D0 < 5$	3969	17431	330450	10706	112044	36560	8760	88832	1901
$\cos(\text{trackAng}) < 0.98$	3574	15647	296010	9227	101276	24582	7880	83874	1806
$84 < M_{\text{inv}} < 98$	1512	4950	93061	912	4469	1367	3042	5769	162
$10 < P_{\text{Tdl}} < 140$	1293	4836	25448	901	4456	1280	2967	5518	156
$\text{copl} < 3$	1200	4520	22234	808	3842	1174	2736	5191	144
$\cos(\theta_Z) < 0.91$	855	3450	10501	644	2613	809	2299	4319	133
123 GeV $< M_{\text{rec}} < 135 \text{ GeV}$	149	704	634	18	300	58	108	216	0

BACKUP

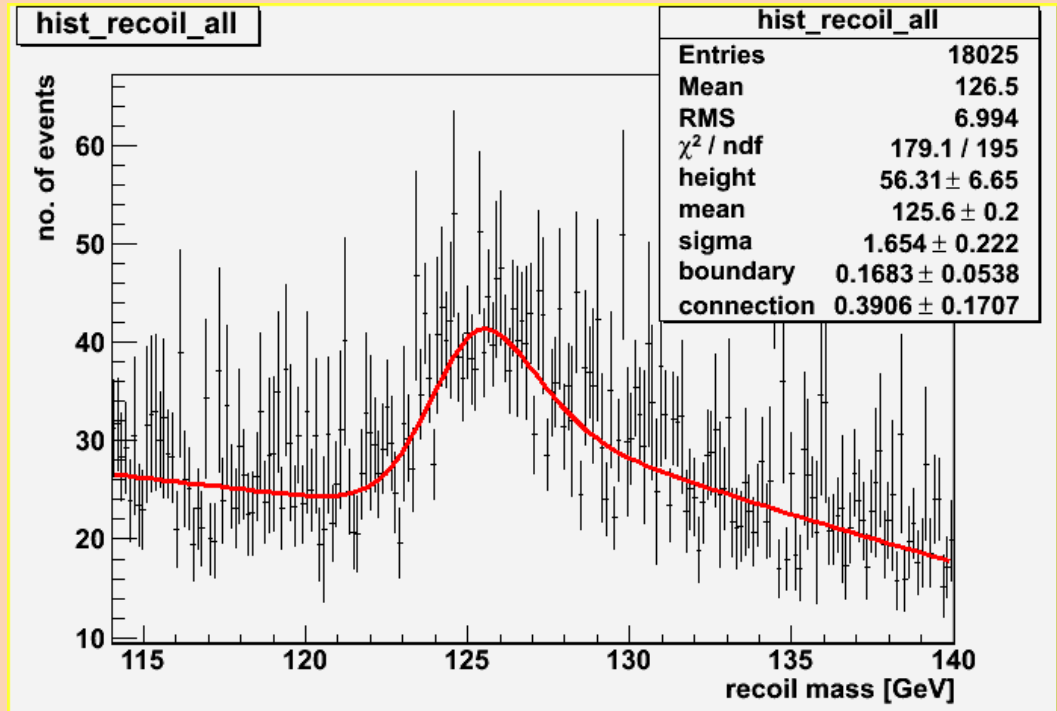
recoil mass

fitted recoil mass :

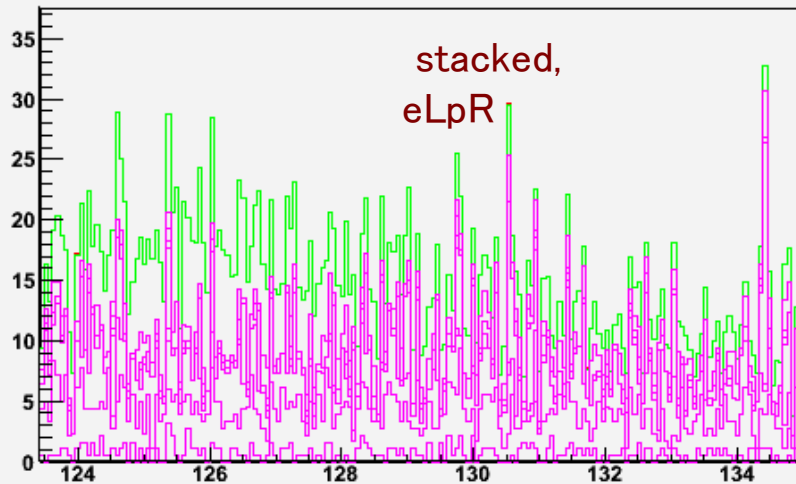
$$M_h = 125.6 \pm 0.3 \text{ GeV}$$

calculate recoil mass with
correction for 14 mrad beam
crossing angle

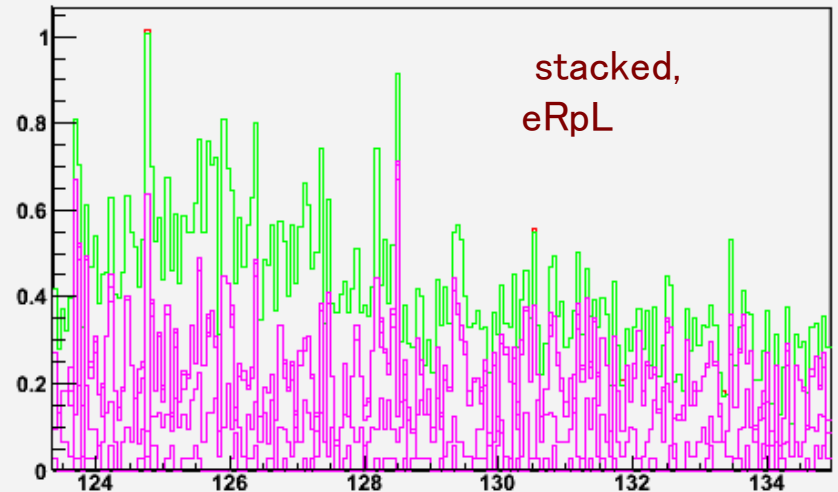
after implementing all cuts



hist_recoil_stackeLpR



hist_recoil_stackerpL



Results for 250 GeV

efficiency problem resolved

Muon Selection

- reject neutrals
- $P_{tot} > 5 \text{ GeV}$
- $\text{small } E_{\text{cluster}} / P_{\text{total}} < 0.5$
- opposite charge
- **Best track selection**
 - $\cos(\text{track angle}) < 0.98$
 - $|\text{D0}/\delta\text{D0}| < 5$

Wider cut window

Final Selection for 250 GeV

analysis after filling root files

- $84 \text{ GeV} < M_{\text{mumu}} < 98 \text{ GeV}$
- $10 \text{ GeV} < pT_{\text{mumu}} < 70 \text{ GeV}$
- $|\cos(\theta_{\text{Zpro}})| < 0.91$
(Z production angle)
- $123 \text{ GeV} < M_{\text{recoil}} < 135 \text{ GeV}$

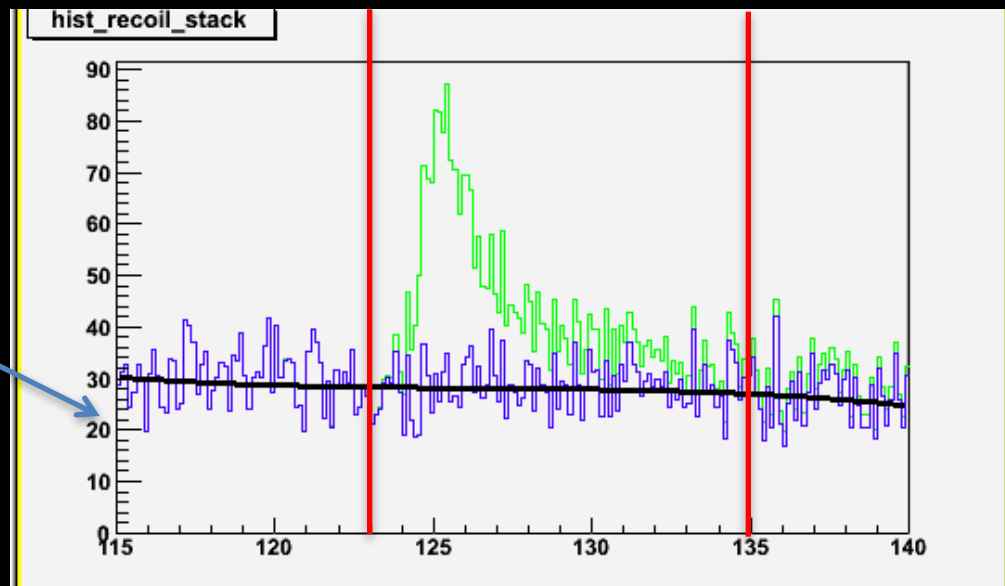
Moved to last

Best Z Candidate Selection

2 mu candidates with **opposite charge**
if several possibilities :
choose pair **with invariant mass closest to Z mass**

Evaluate data selection
efficiency in within range
of 123 – 135 GeV

calculate recoil mass with
correction for 14 mrad beam
crossing angle



This Week 's updated results : 250 GeV

Calculation of Error of σ_{meas}

- Case#1: ignore uncertainty of $\langle B \rangle$ i.e. MC statistics
- Case#2: taking into account uncertainty of ε and $\langle B \rangle$ *is this necessary ?*

Usual signal samples (1000 fb⁻¹)

$$\langle n \rangle = 1598 \pm 25$$

$$\langle \varepsilon \rangle = 61.4 \pm 0.4 \%$$

$$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 21.2$$

$$\langle n \rangle / \langle B \rangle = 0.39$$

If Case#1

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 4.7 \%$$

If Case#2

$$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.4 \%$$

NEW: Sqrt(s)= 250 GeV

After fixing efficiency problem

I had been counting eberything only in 123 – 135 GeV region

sorry !!!

cut	signal	eff	BG_all	eff	S/B	S/sqrt(S+B)
raw	2605	100%	6923287	100.00%	0.0004	0.99
only best mu pair	2519	97%	1767237	25.53%	0.0014	1.89
$\Delta D0/D0 < 5$	2504	96%	1683552	24.32%	0.0015	1.93
$\cos(\text{trackAng}) < 0.98$	2446	94%	1571532	22.70%	0.0016	1.95
$84 < M_{\text{inv}} < 98$	2110	81%	506279	7.31%	0.0042	2.96
$10 < P_{\text{Tdl}} < 70$	2073	80%	113512	1.64%	0.0183	6.10
$\cos(\theta_Z) < 0.91$	1945	75%	50111	0.72%	0.004	0.99
$123 \text{ GeV} < M_{\text{rec}} < 135 \text{ GeV}$	1598	61%	4108	0.06%	0.389	21.15

Signal efficiency 61 %

S/N → 0.39

Significance ~21.2

cut	4f_ZZ_l	4f_ZZ_sl	2f_Z_l	4f_WW_l	4f_WW_sl	4fSingleZee	4fSingleZn	4f_ZZWWMix_l
raw	23972	214232	3248465	228894	2771978	167469	28534	239742
only best mu pair	12235	48144	1394970	33608	125335	29953	7262	115732
$\Delta D0/D0 < 5$	11997	45974	1365080	14489	96125	29554	7150	113183
$\cos(\text{trackAng}) < 0.98$	11104	42140	1279342	13403	90499	20132	6488	108423
$84 < M_{\text{inv}} < 98$	5673	19101	465555	1605	1299	1942	2539	8566
$10 < P_{\text{Tdl}} < 70$	3363	13273	84497	1438	1143	1438	1934	6426
$\cos(\theta_Z) < 0.91$	2067	9652	28439	1231	951	862	1521	5388
$123 \text{ GeV} < M_{\text{rec}} < 135 \text{ GeV}$	178	749	1584	264	157	92	209	875

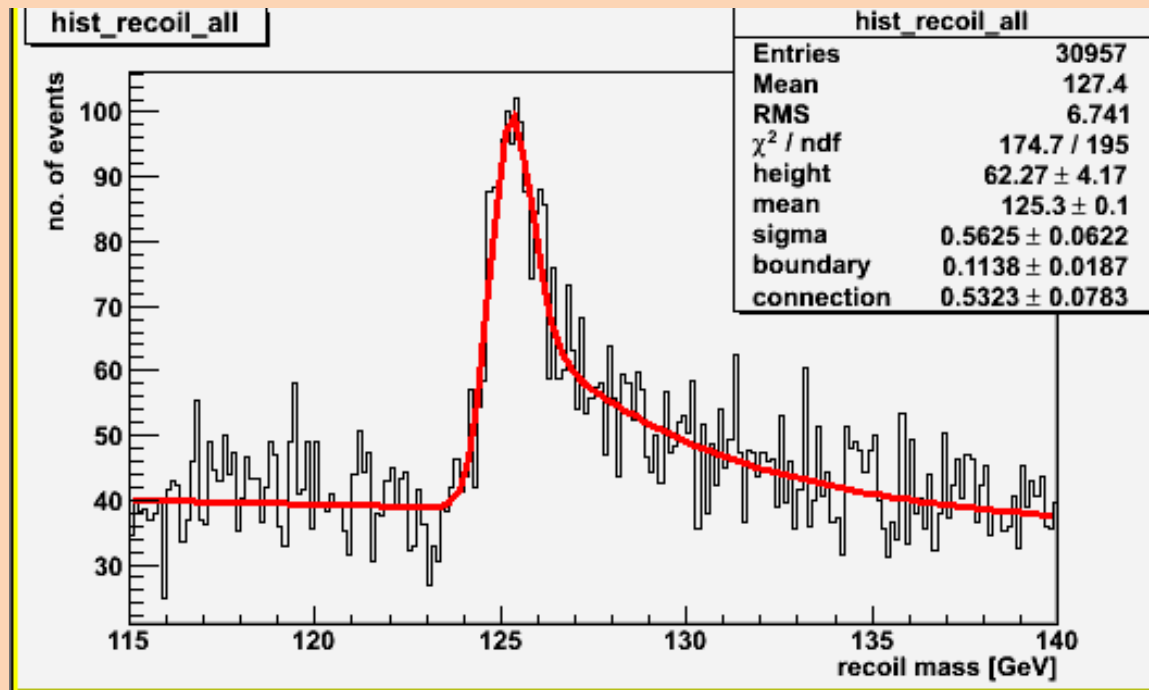
recoil mass

after implementing all cuts

fitted recoil mass :

$$M_h = 125.3 \text{ GeV} \pm 70 \text{ MeV}$$

calculate recoil mass with
correction for 14 mrad beam
crossing angle



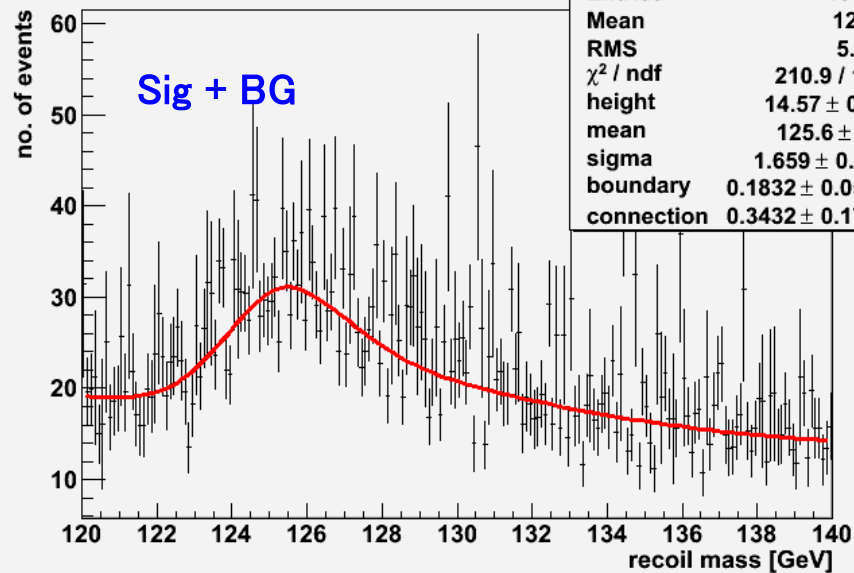
◆ BG: 3rd order polynomial

◆ signal : GPET: 5 parameters : Gaus (left-side) , Gaus + expo (right side)

$$N \exp\left[-\frac{1}{2} \frac{(x - x_{\text{mean}})^2}{\sigma^2}\right] + (1 - b) \exp\left[-k \frac{(x - x_{\text{mean}})^2}{\sigma^2}\right] \exp\left(-\frac{x - x_{\text{mean}}}{\lambda}\right)$$

$$N \left[b \exp\left[-\frac{1}{2} \frac{(x - x_{\text{mean}})^2}{\sigma^2}\right] + (1 - b) \exp\left[-k \frac{(x - x_{\text{mean}})^2}{\sigma^2}\right] \exp\left(-\frac{x - x_{\text{mean}}}{\lambda}\right) \right]$$

hist_recoil_all



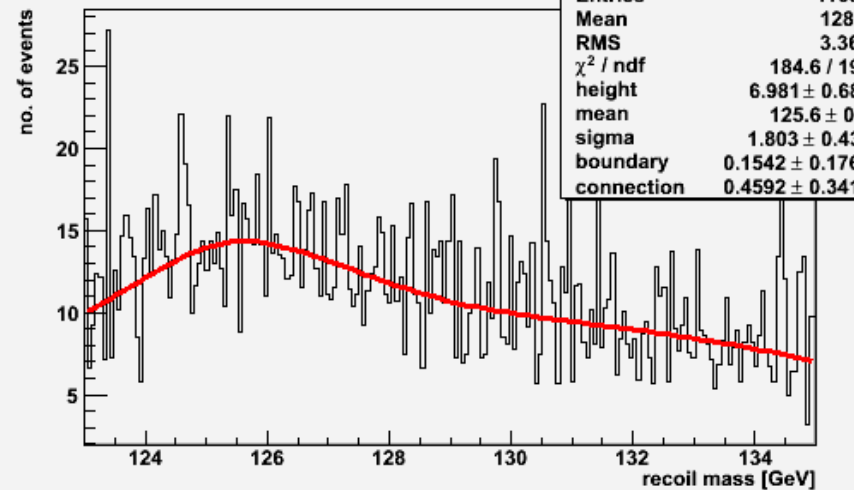
hist_recoil_all

Entries	15520
Mean	129.2
RMS	5.411
χ^2 / ndf	210.9 / 195
height	14.57 ± 0.92
mean	125.6 ± 0.2
sigma	1.659 ± 0.231
boundary	0.1832 ± 0.0538
connection	0.3432 ± 0.1798

new fitting: using weighted bins

Only fit in region (120 – 140 GeV)

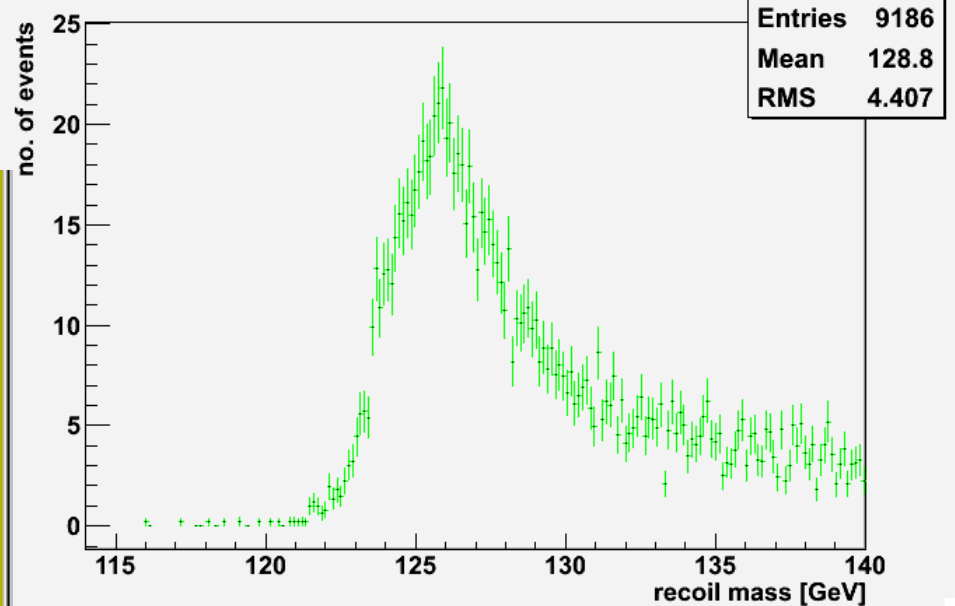
hist_recoil_all



hist_recoil_all

Entries	11684
Mean	128.5
RMS	3.369
χ^2 / ndf	184.6 / 195
height	6.981 ± 0.682
mean	125.6 ± 0.3
sigma	1.803 ± 0.432
boundary	0.1542 ± 0.1760
connection	0.4592 ± 0.3410

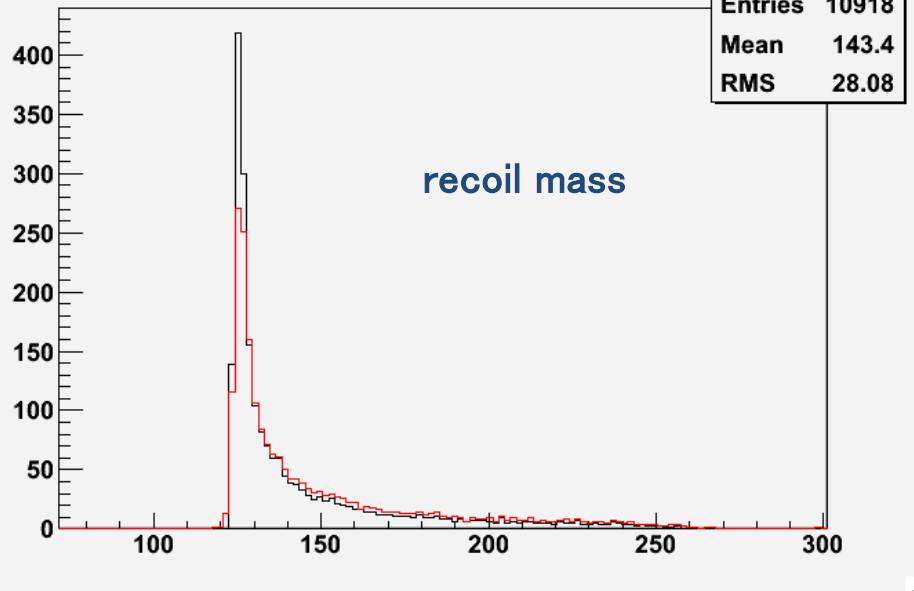
hist_recoil_sig



hist_recoil_sig

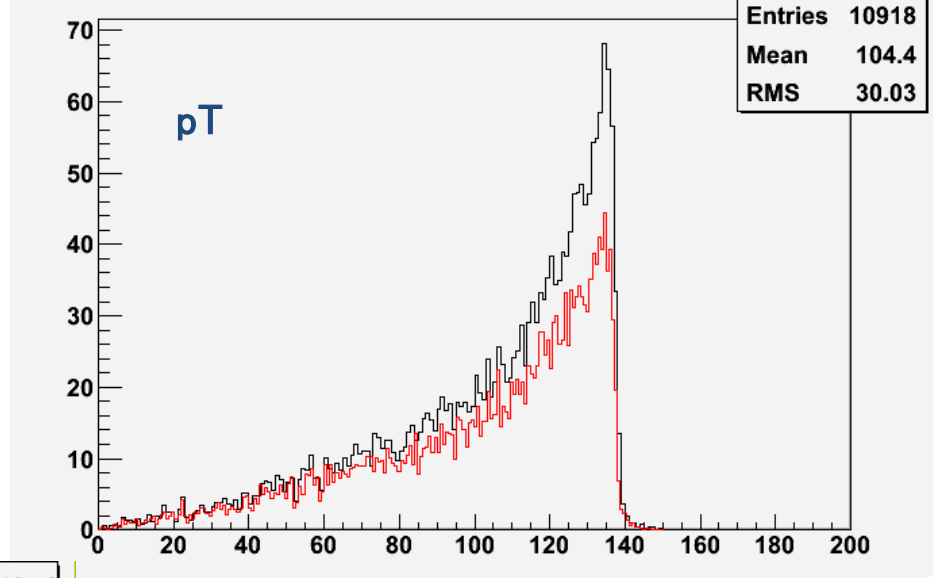
Entries	9186
Mean	128.8
RMS	4.407

hist_mass_mc_jackieZH_higgs_ffh_Pe2e2h_eL_pR

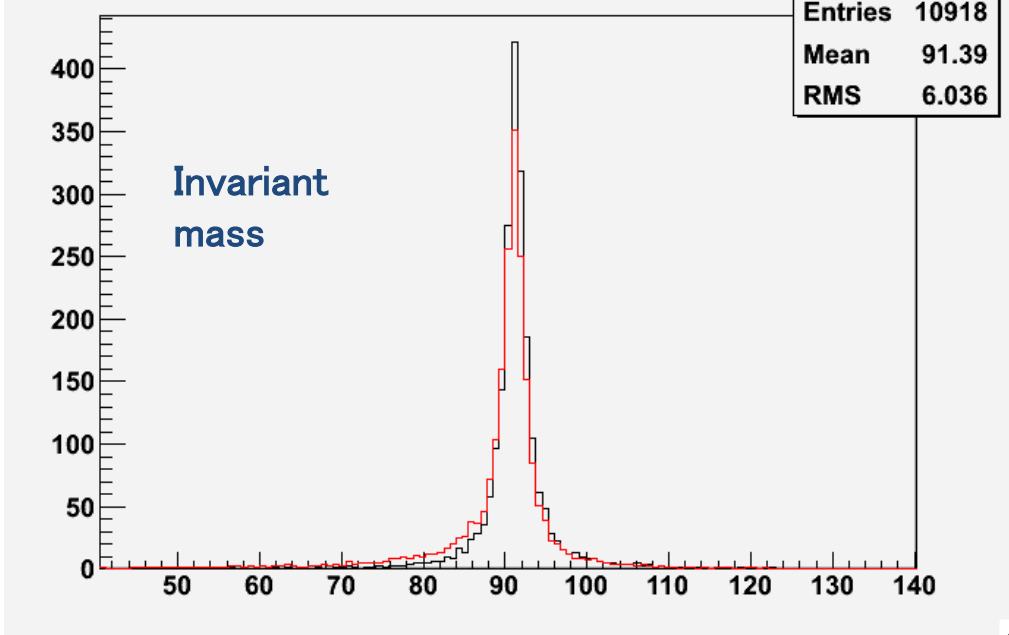


after implementing all cuts

hist_pT_mc_jackieZH_higgs_ffh_Pe2e2h_eL_pR



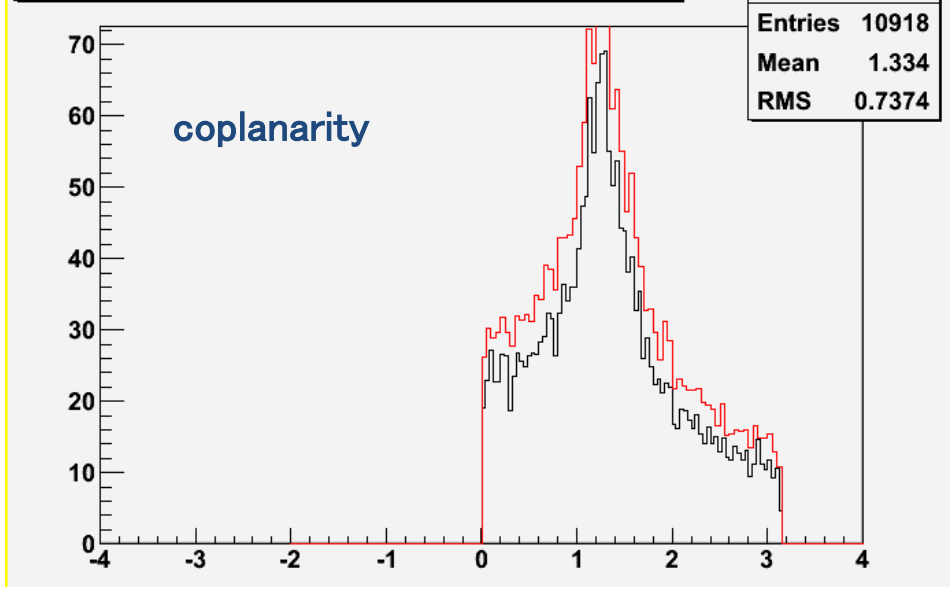
hist_inv_mc_jackieZH_higgs_ffh_Pe2e2h_eL_pR



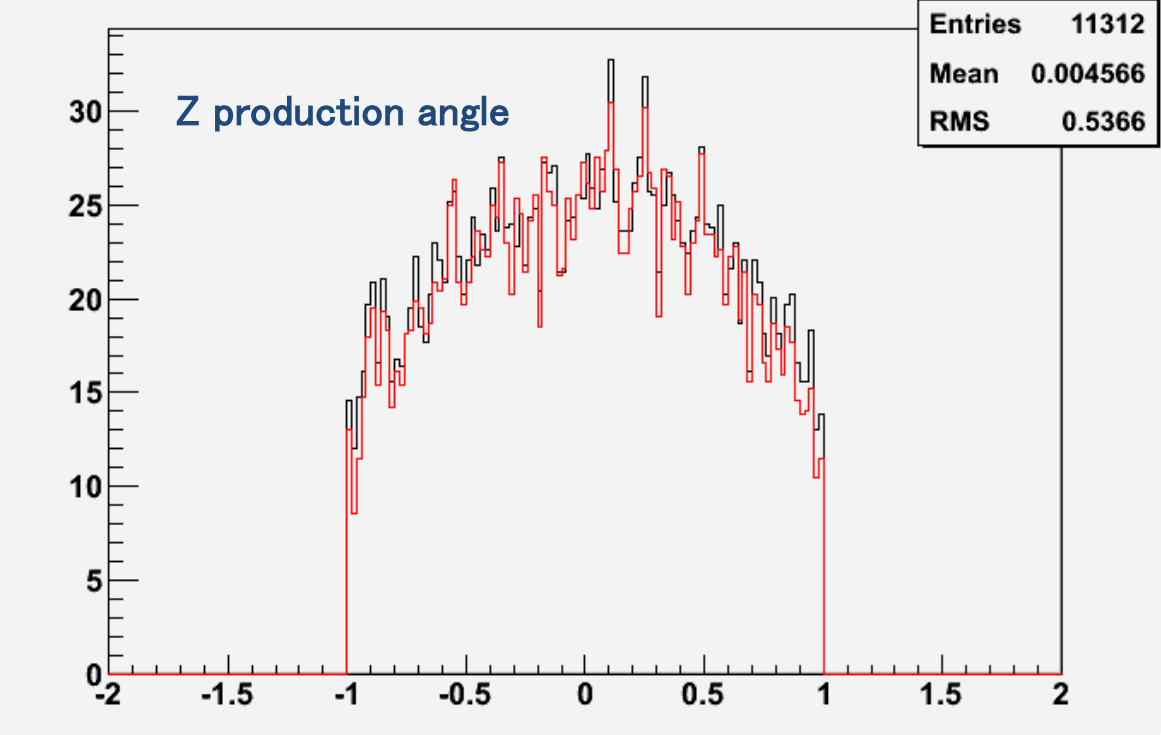
Black : MC

Red: reconstructed

hist_acos_mc_jackieZH_higgs_ffh_Pe2e2h_eL_pR



hist_cosZ_mc_jackieZH_higgs_ffh_Pe2e2h_eL_pR



Black : MC

Red: reconstructed

(-0.8, + 0.3)

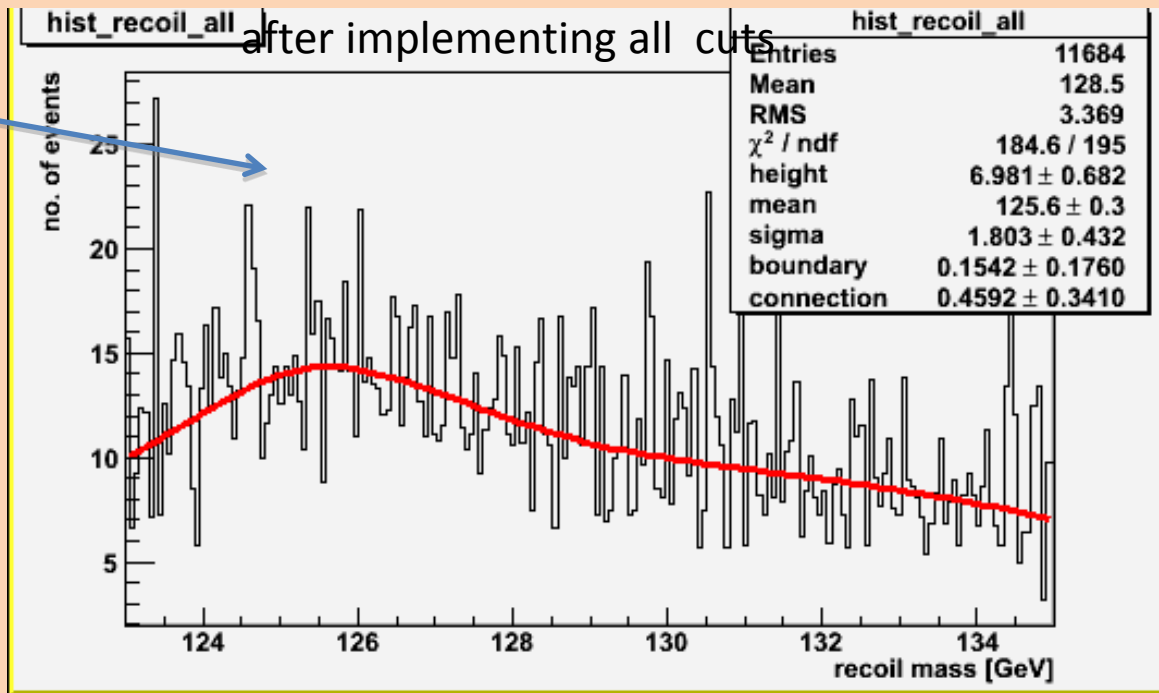
$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.6$

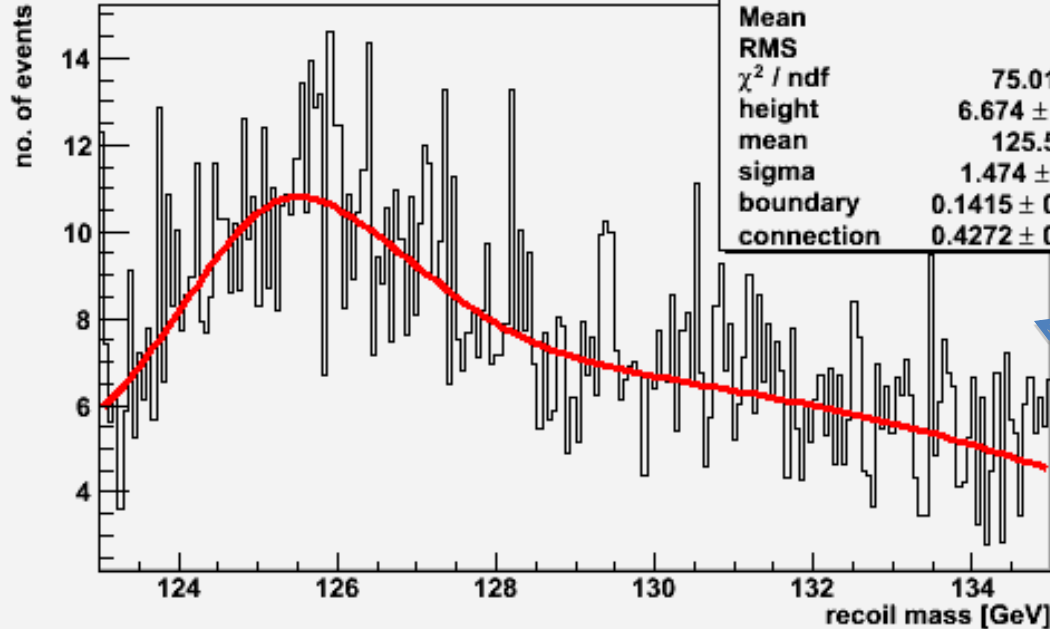
$\langle n \rangle / \langle B \rangle = 0.42$

fitted recoil mass :

$M_h = 125.6 \pm 0.3 \text{ GeV}$



hist_recoil_all



(+0.8, - 0.3)

$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 15.8$

$\langle n \rangle / \langle B \rangle = 0.68$

fitted recoil mass :

$M_h = 125.6 \pm 0.2 \text{ GeV}$

Compare different polarization scenarios

$\sqrt{s} = 350 \text{ GeV}$ $L = 333 \text{ fb}^{-1}$

For now, keep same cut parameters as (-0.8, +0.3)
(they could be optimized)

(-0.8, + 0.3)

Pol weight(eLpR) = $0.9 \cdot 0.65$

Pol weight(eRpL) = $0.1 \cdot 0.35$

$\langle n \rangle = 923 \pm 23$

$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 16.6$

$\langle n \rangle / \langle B \rangle = 0.42$

$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.0 \%$

8.8 % if consider BG uncertainty

(+0.8, -0.3)

Pol weight(eLpR) = $0.1 \cdot 0.35$

Pol weight(eRpL) = $0.9 \cdot 0.65$

$\langle n \rangle = 625 \pm 19$

$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 15.9$

$\langle n \rangle / \langle B \rangle = 0.68$

$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.4 \%$

7.6 % if consider BG uncertainty

(-0.8, 0)

Pol weight(eLpR) = $0.9 \cdot 0.5$

Pol weight(eRpL) = $0.1 \cdot 0.5$

$\langle n \rangle = 733 \pm 21$

$\langle \epsilon \rangle = 40.4 \pm 0.5 \%$

$\langle n \rangle / \sqrt{\langle n \rangle + \langle B \rangle} = 14.8$

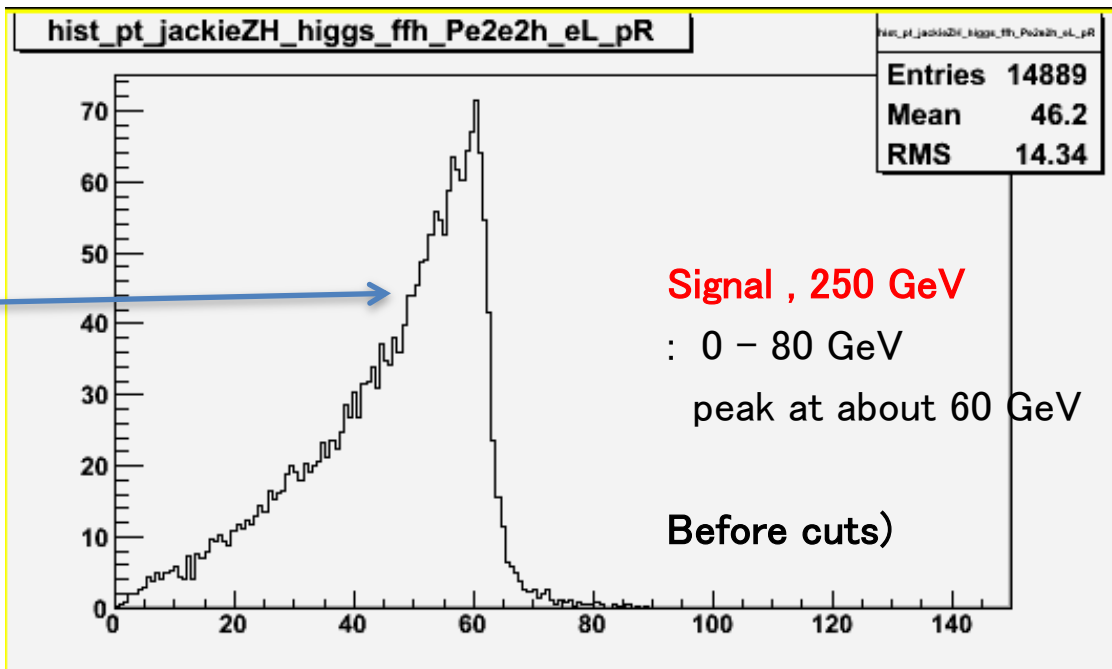
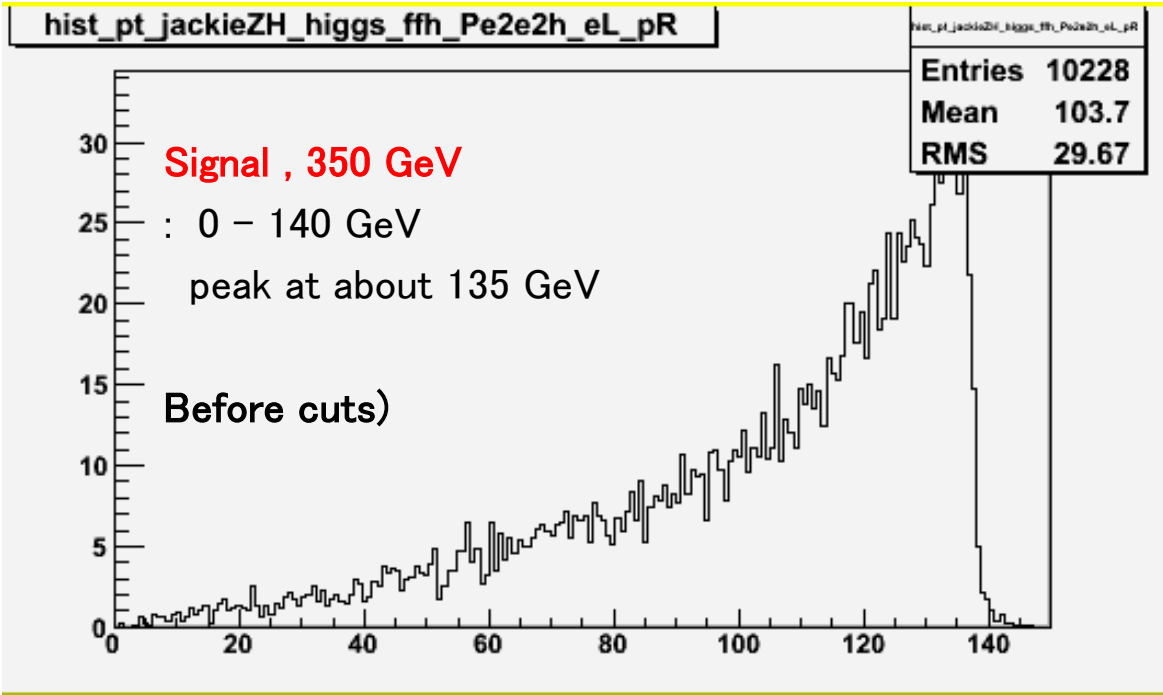
$\langle n \rangle / \langle B \rangle = 0.43$

$\Delta \sigma_{\text{meas}} / \langle \sigma_{\text{meas}} \rangle = 6.8 \%$

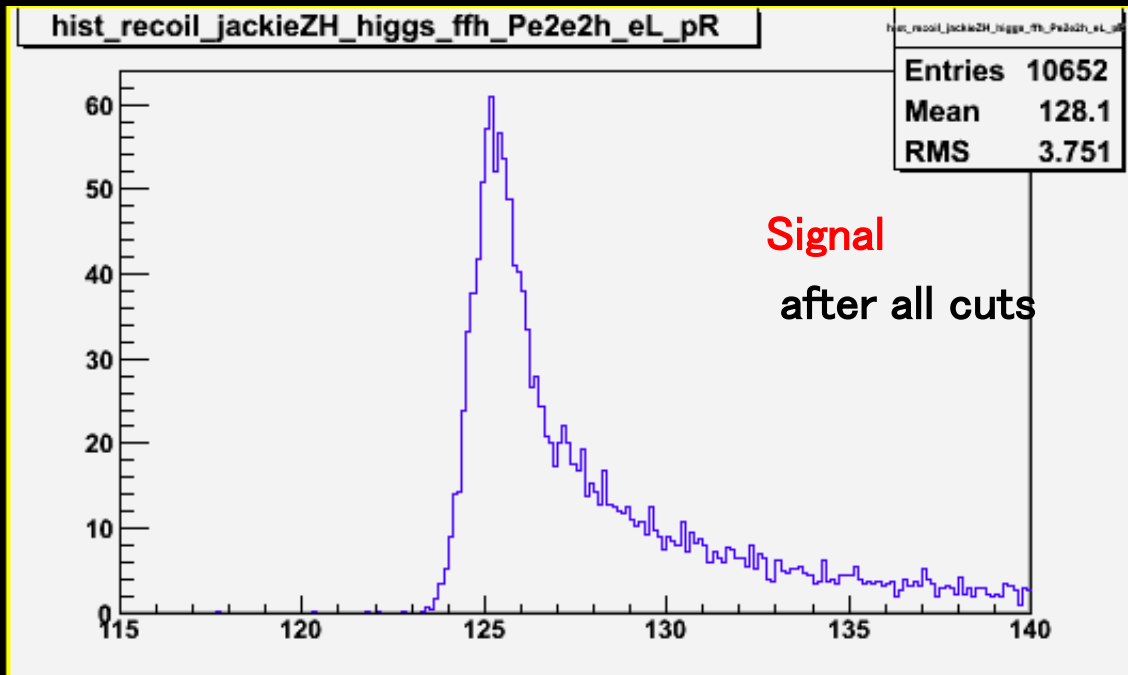
9.2% if consider BG uncertainty

dilepton PT, 350 GeV

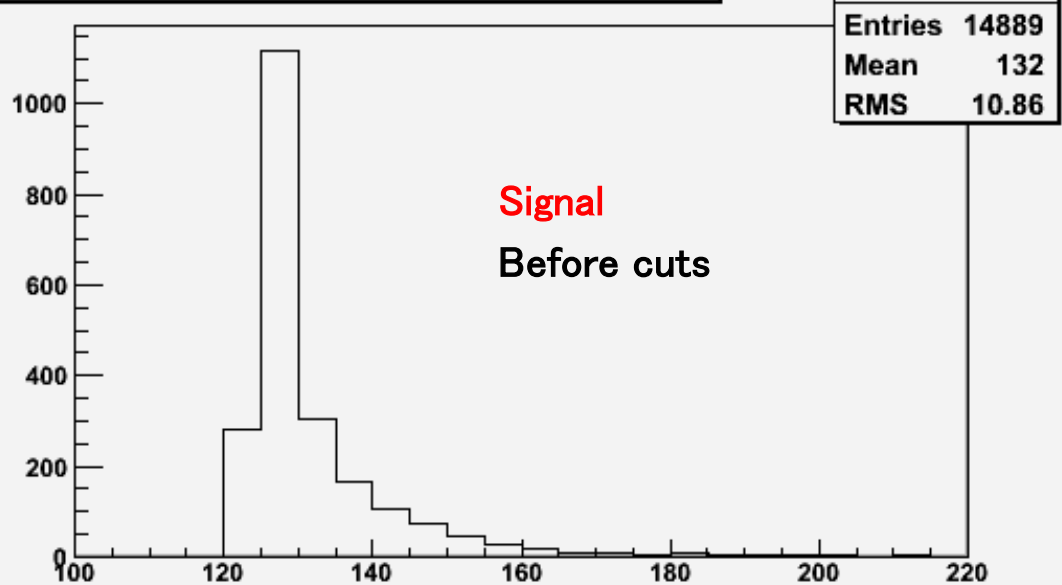
do cut :
 $10 \text{ GeV} < p_{T_dl} < 140 \text{ GeV}$



recoil mass of
signal, 250 GeV



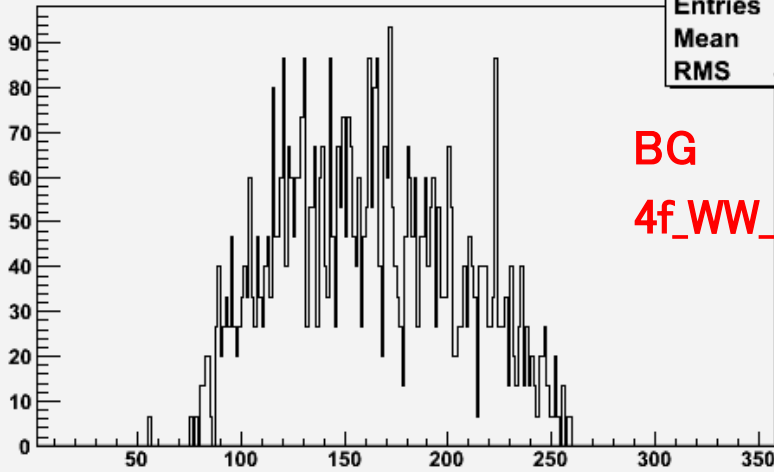
hist_recoil2_jackieZH_higgs_ffh_Pe2e2h_eL_pR



recoil mass 350 GeV

After inv mass cut

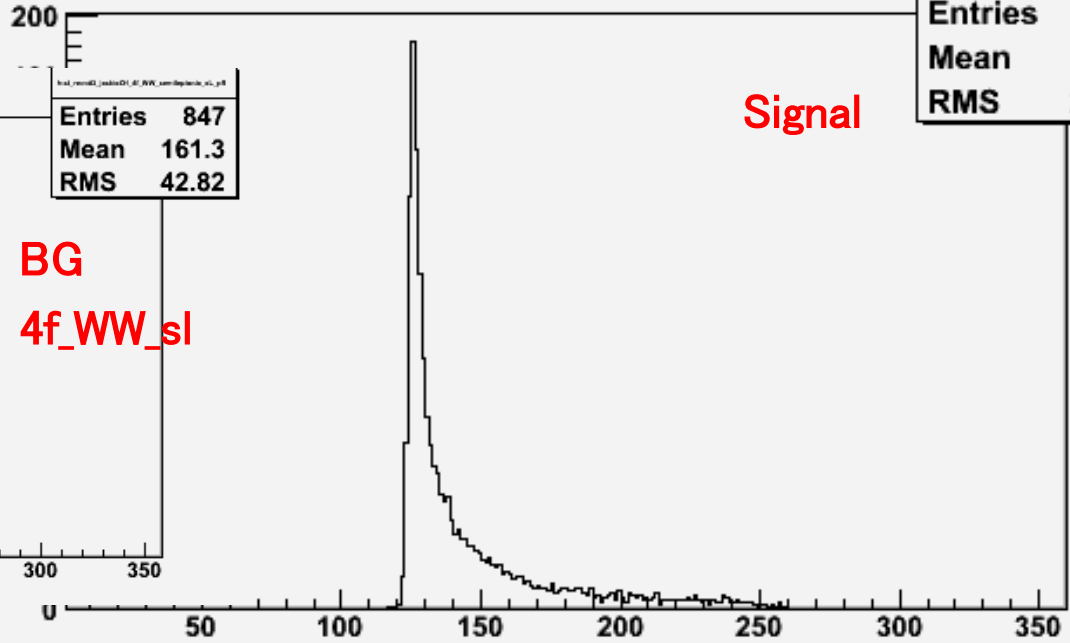
hist_recoil3_jackieZH_4f_WW_semileptonic_eL_pR



BG
4f_WW_sl

Entries	847
Mean	161.3
RMS	42.82

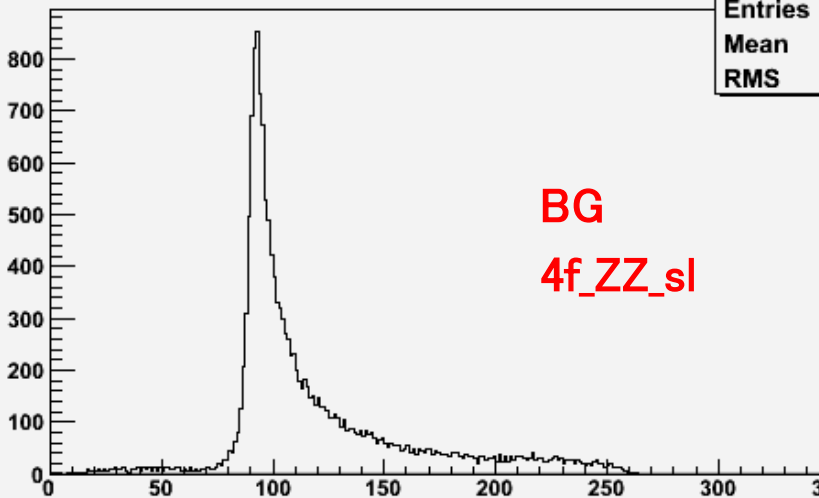
hist_recoil3_jackieZH_higgs_ffh_Pe2e2h_eL_pR



Signal

Entries	8989
Mean	145.1
RMS	28.47

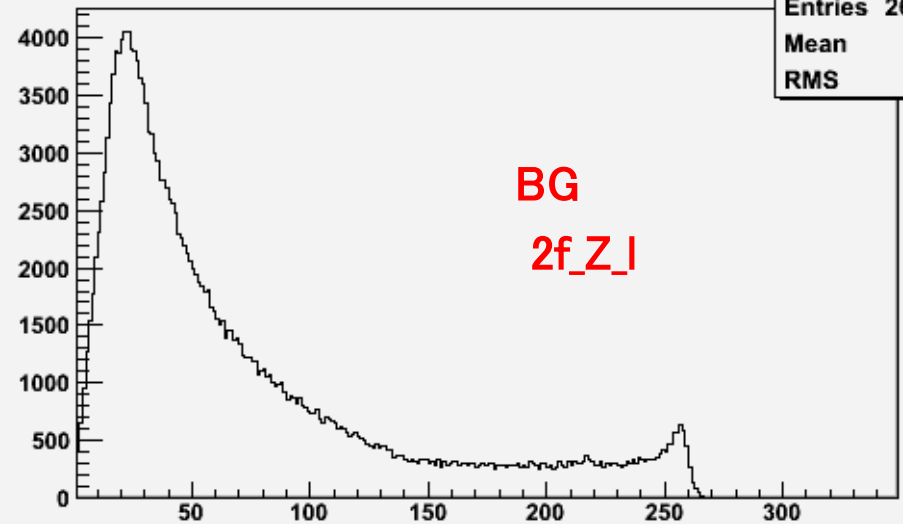
hist_recoil3_jackieZH_4f_ZZ_semileptonic_eL_pR



BG
4f_ZZ_sl

Entries	
Mean	
RMS	

hist_recoil3_jackieZH_2f_Z_leptonic_eL_pR



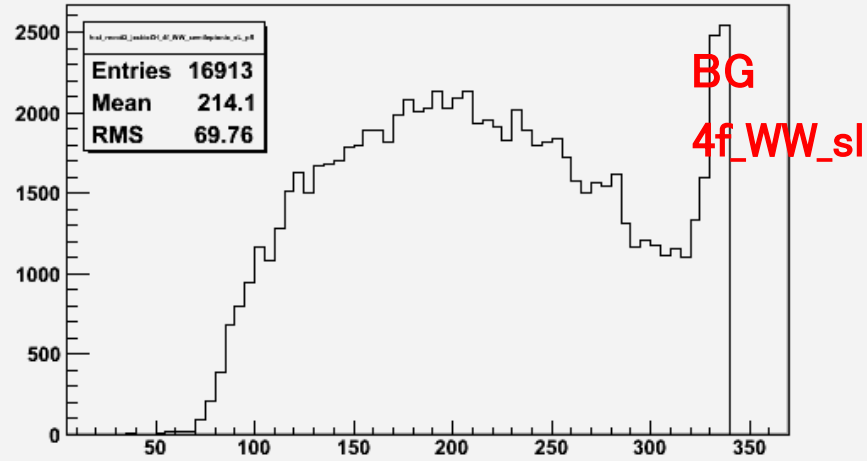
BG
2f_Z_l

Entries	265426
Mean	71.94
RMS	65.01

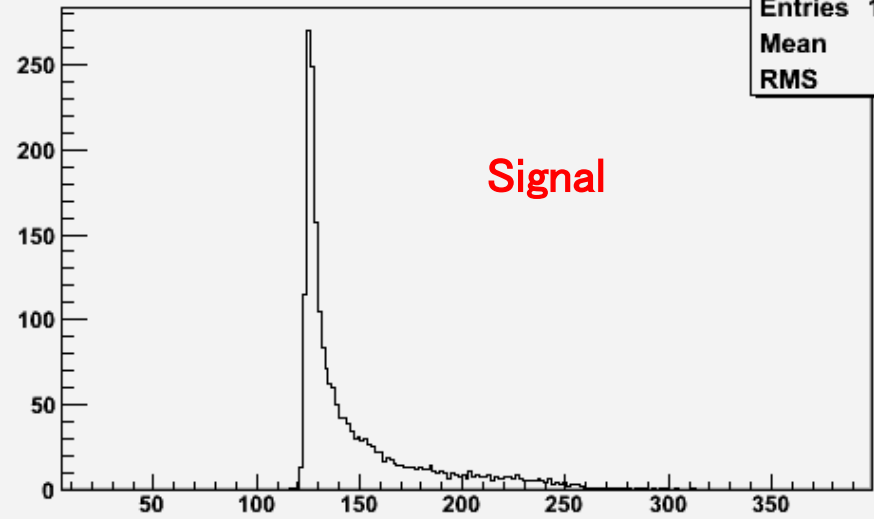
recoil mass 350 GeV

Before cut

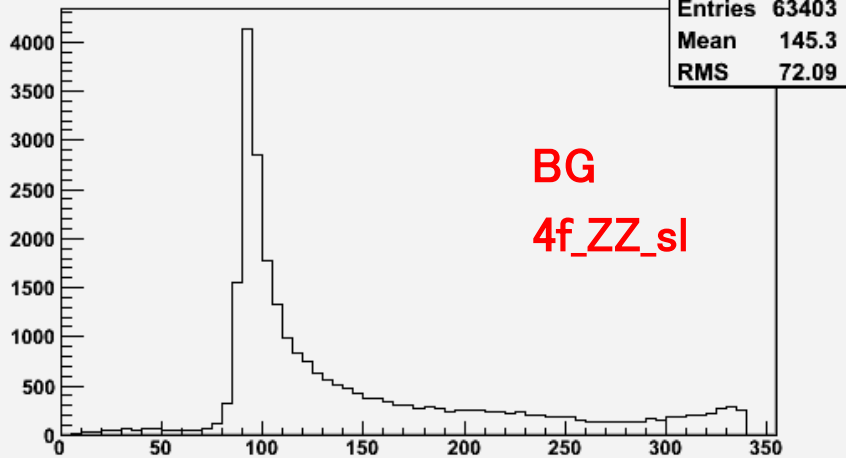
hist_recoil2_jackieZH_4f_WW_semileptonic_eL_pR



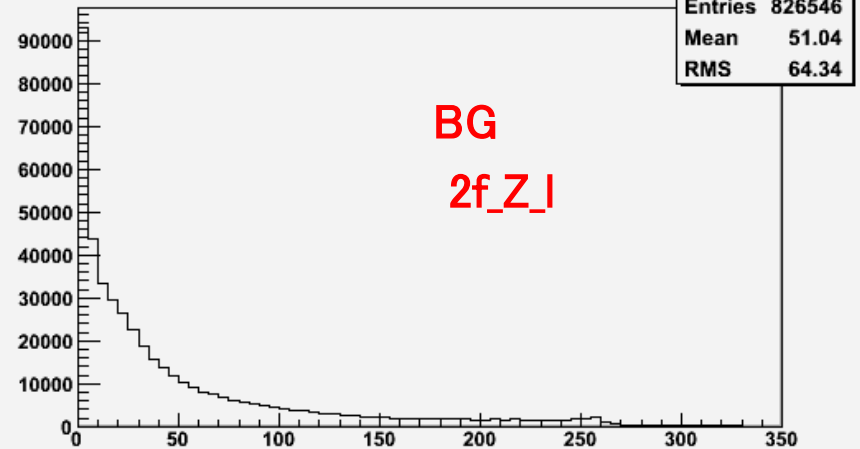
hist_recoil2_jackieZH_higgs_ffh_Pe2e2h_eL_pR



hist_recoil2_jackieZH_4f_ZZ_semileptonic_eL_pR



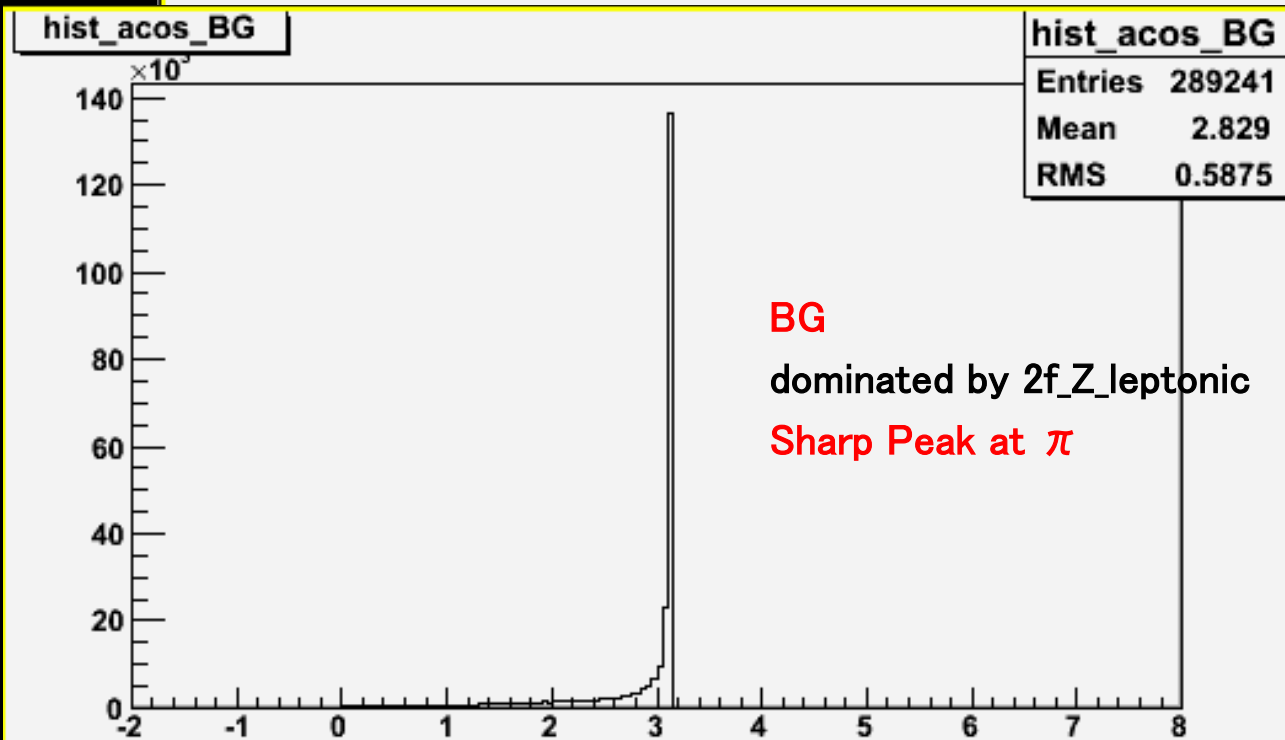
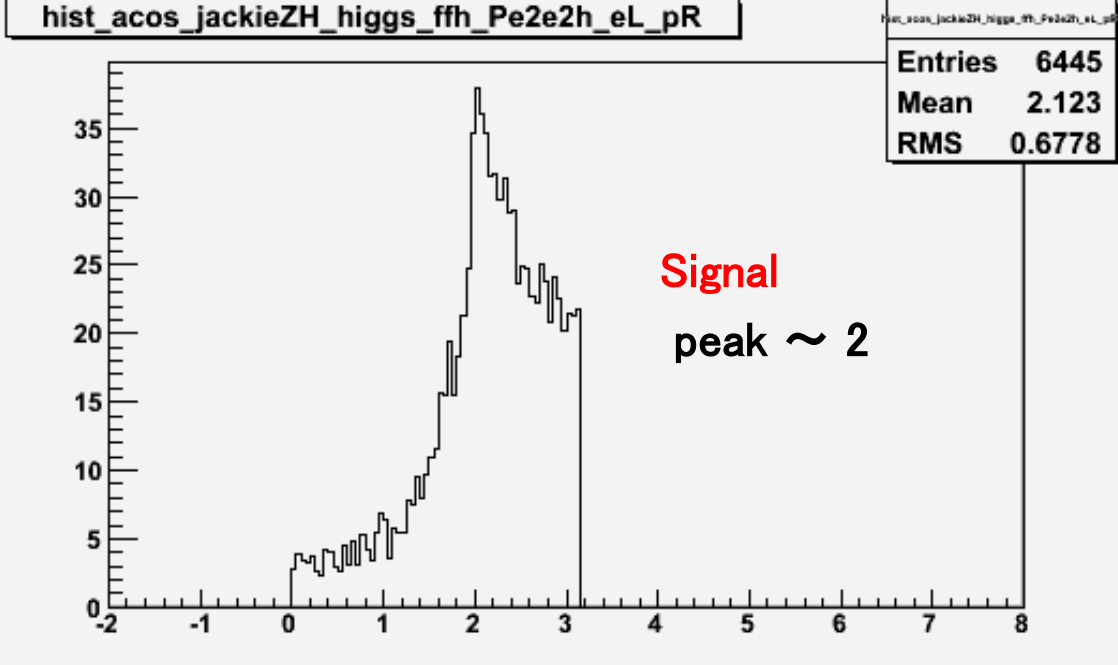
hist_recoil2_jackieZH_2f_Z_leptonic_eL_pR



coplanarity, before cut ,
250 GeV

No coplanarity cut applied

wanted to maintain high signal eff.



coplanarity, before cut

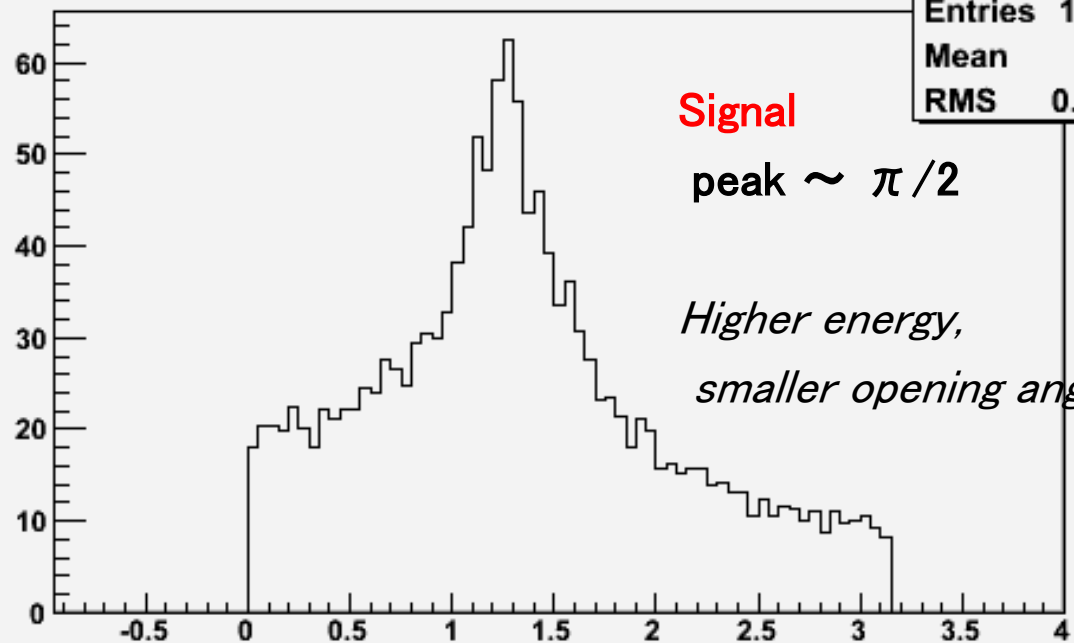
350 GeV

Cut:

coplanarity < 0.29

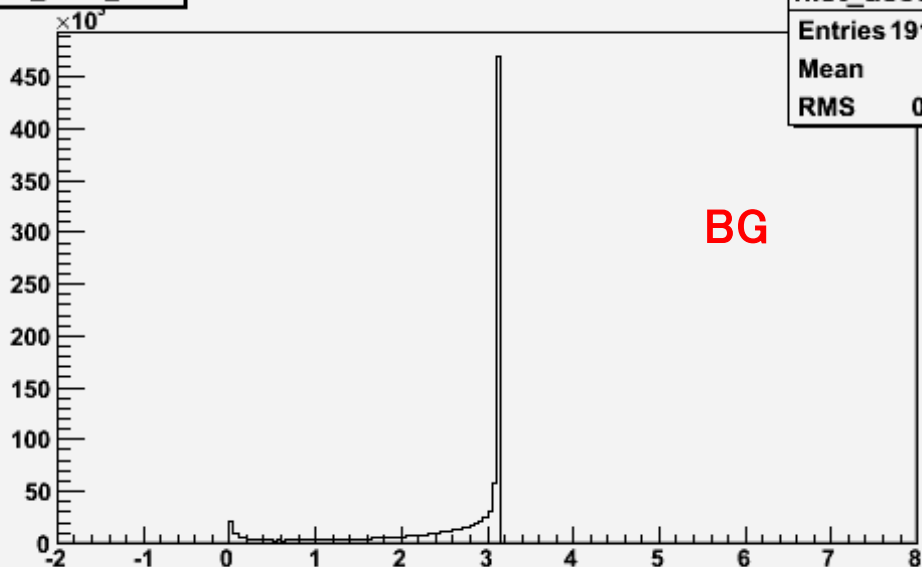
in order to remove more BG

hist_acos_jackieZH_higgs_ffh_Pe2e2h_eL_pR



hist_acos_jackieZH_higgs_ffh_Pe2e2h_eL_pR	
Entries	10228
Mean	1.341
RMS	0.7352

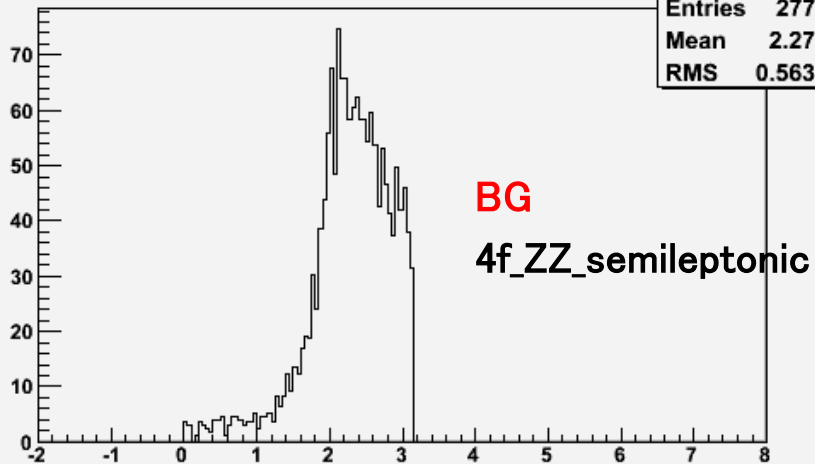
hist_acos_BG



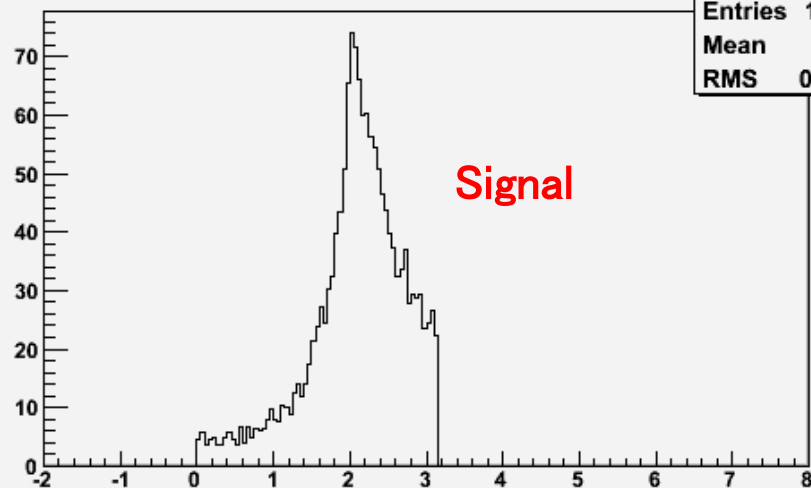
hist_acos_BG	
Entries	1916353
Mean	2.608
RMS	0.8562

coplanarity, after all other cuts

hist_acos2_jackieZH_4f_ZZ_semileptonic_eL_pR

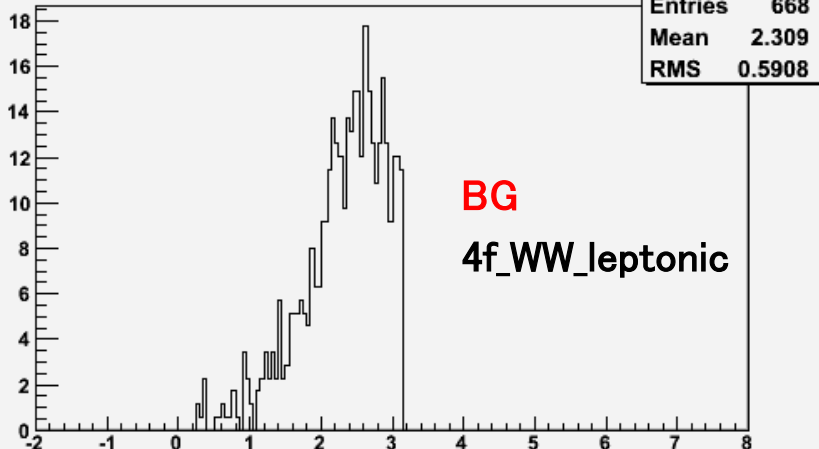


hist_acos2_jackieZH_higgs_ffh_Pe2e2h_eL_pR

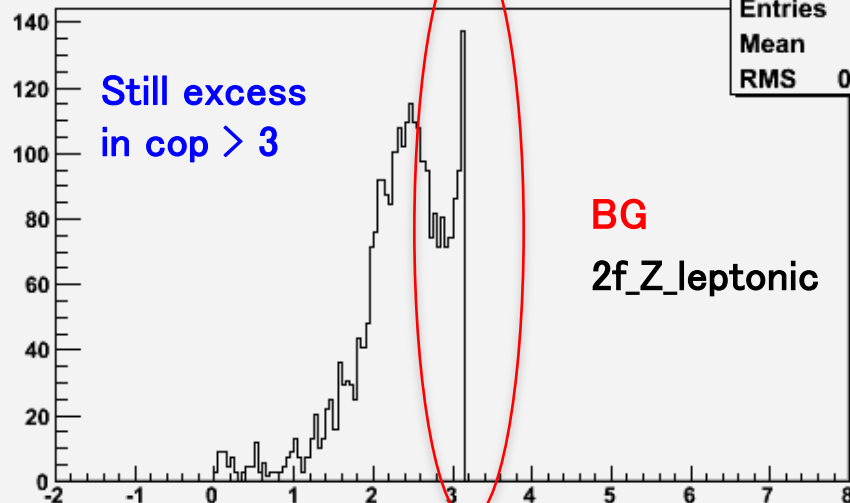


Trying to decide whether to use coplanarity cut

hist_acos2_jackieZH_4f_WW_leptonic_eL_pR

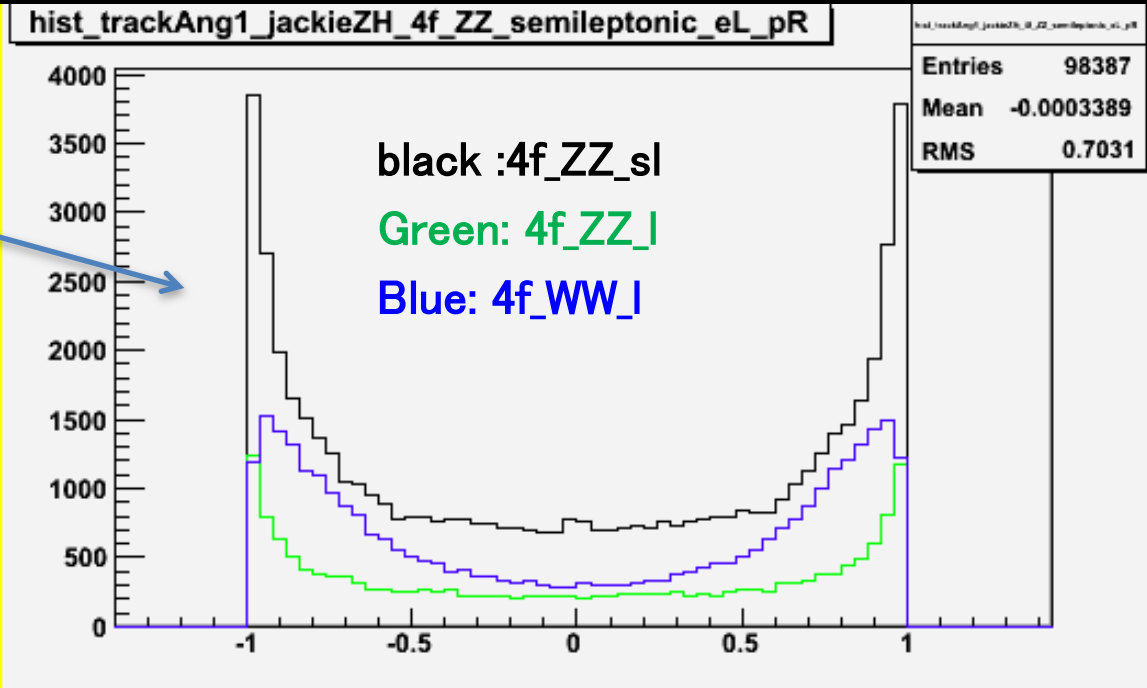
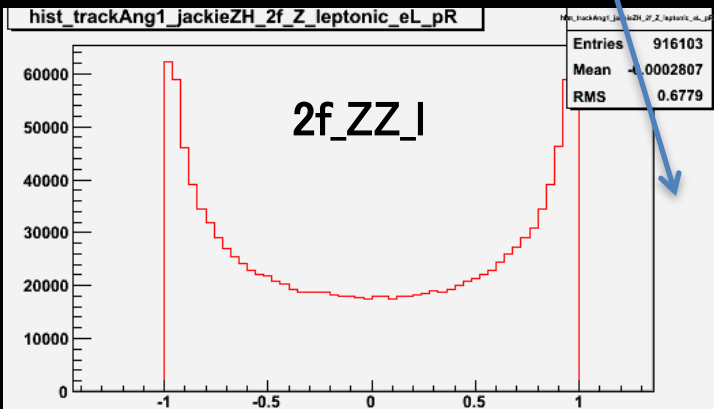


hist_acos2_jackieZH_2f_Z_leptonic_eL_pR

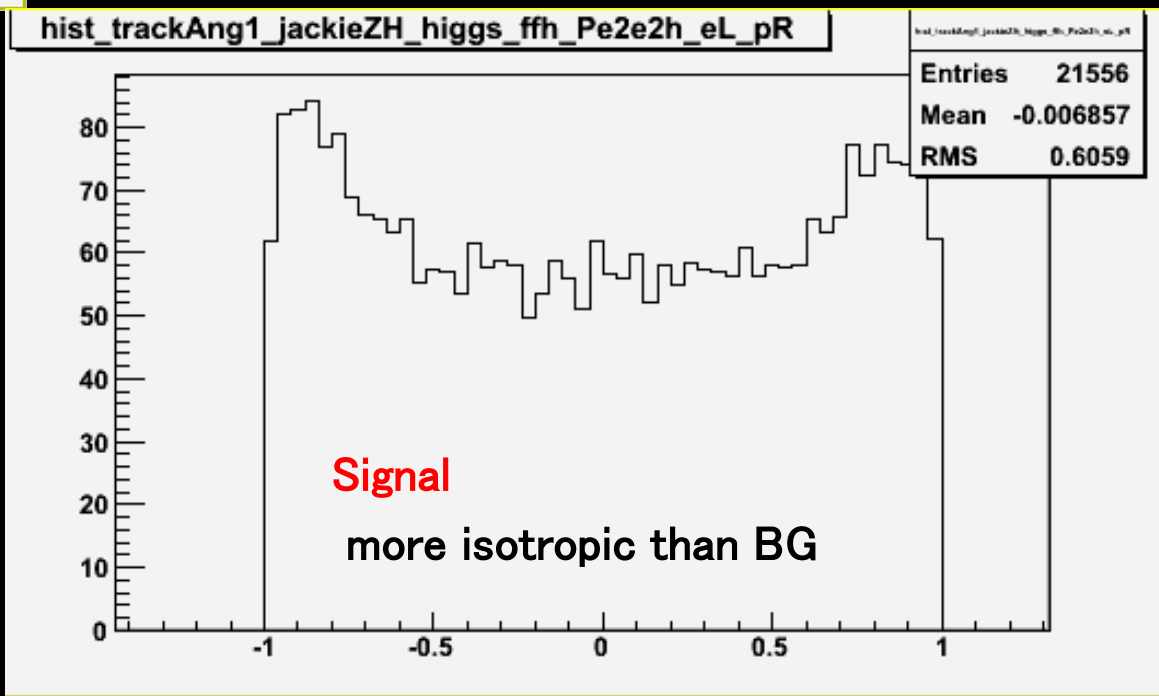


Cos(track angle),
250 GeV

BG is More forward

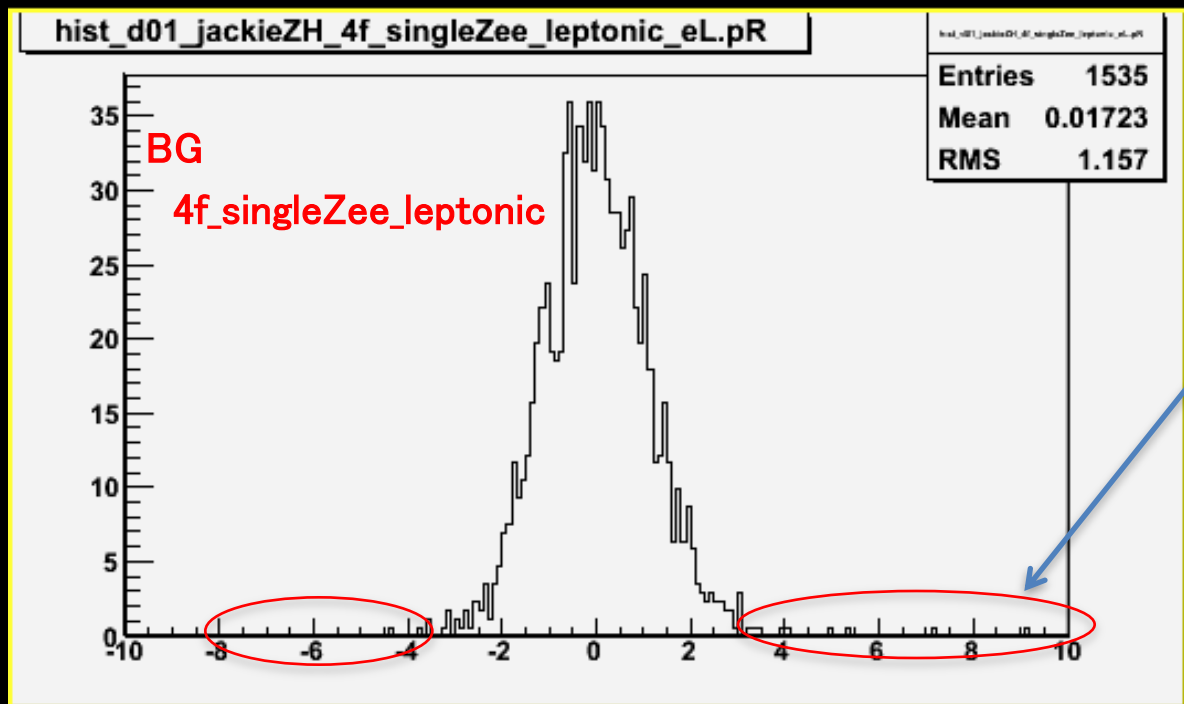
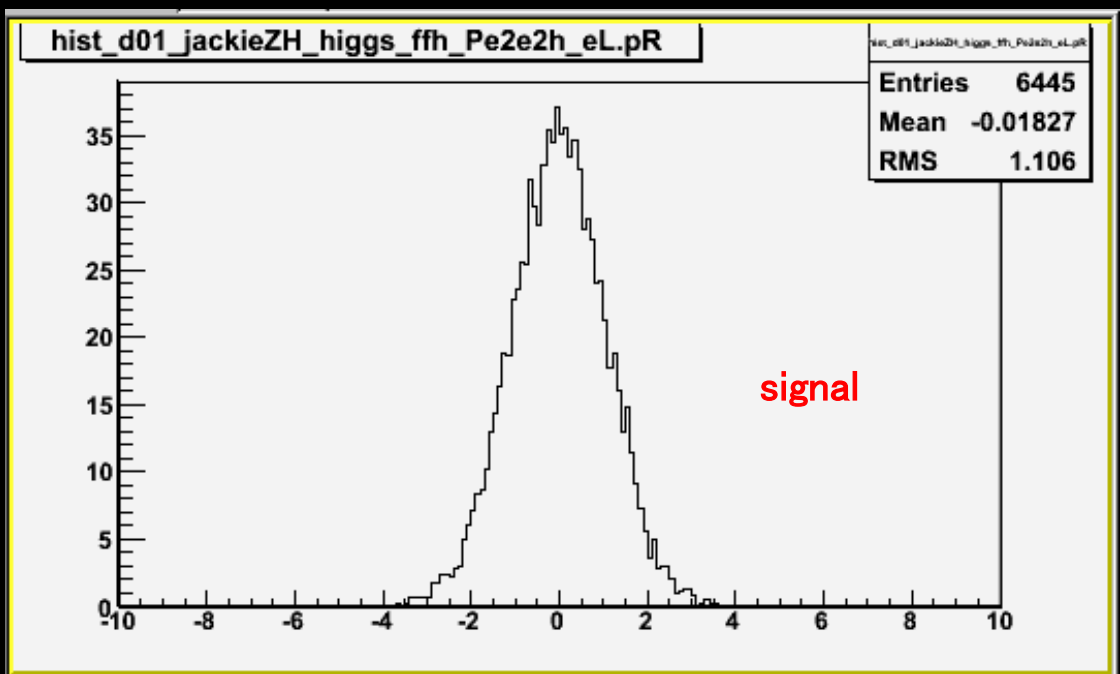


do cut :
 $\cos(\text{trackAngle}) < 0.95$



Impact parameter

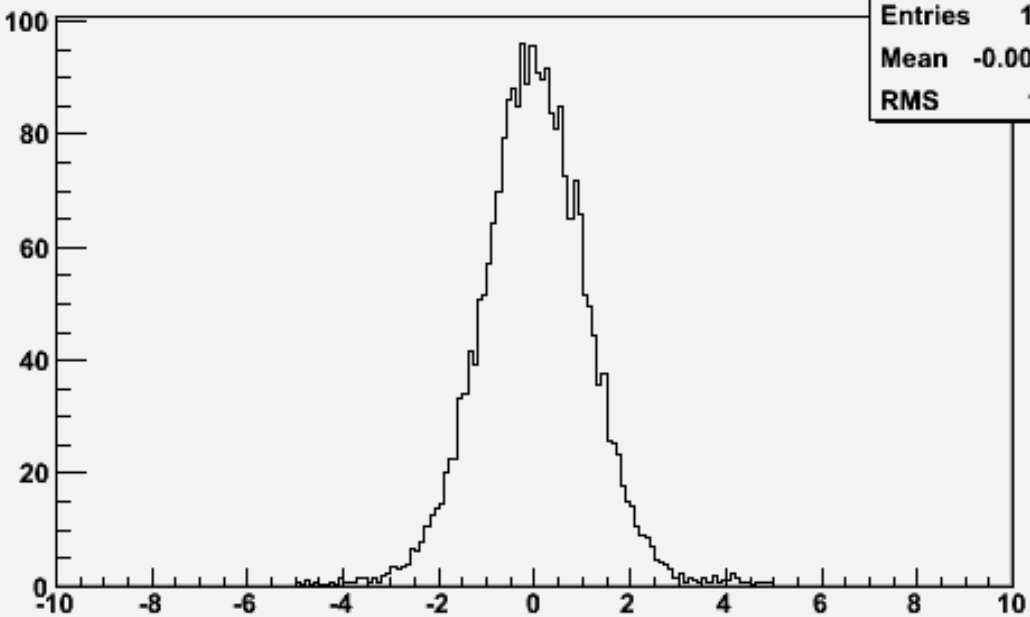
$D0 / \delta D0$



For some BG processes
exceed ± 4 slightly

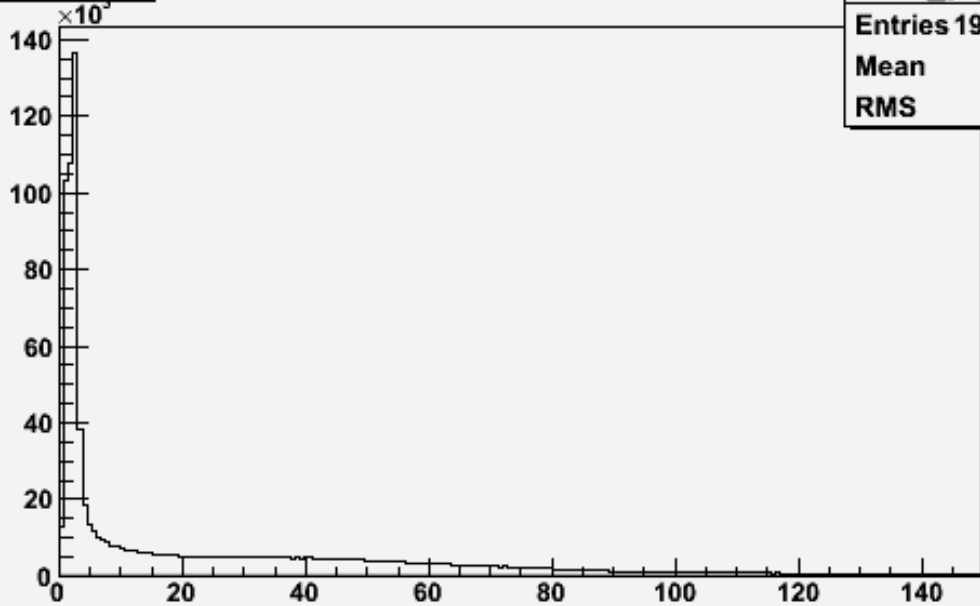
do cut : $|D0 / \delta D0| < 4$

hist_d01_jackieZH_higgs_ffh_Pe2e2h_eL_pR



Entries	16702
Mean	-0.002884
RMS	1.137

hist_pt_BG



Entries	1916353
Mean	26.52
RMS	33.32