



# Study of alternative ILC final focus optical configurations

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### Idea

#### —Reduced bunch length enables:

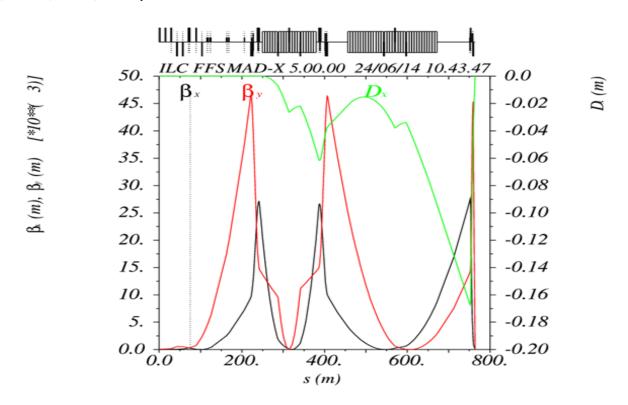
- 1) less beamstrahlung with the same luminosity,
- 2) or higher luminosity with equal amount beamstrahlung.

#### The approach is to use flatter beams

— using exactly the same magnets as ILC nominal design, only refitting them, but requiring a short bunch length (150 or 200 microns), which is the price to pay...

### ILC FFS nominal design

- L\*=3.5m
- Total length: 760m
- $\beta x^*/\beta y^*=15$ mm/0.4mm
- local chromaticity correction scheme was adopted
- The chromaticity of IR was corrected to third order by five sextupoles (SD0,SF1,SD4,SF5,SF6)



### Luminosity for linear collider

#### Yokoya and Chen theory:

$$L_0 = \frac{f_{rep} N_b N_e^2}{4\pi \sigma_x^* \sigma_y^*} H_D$$

 $H_D$  -- luminosity enhance factor

$$D_{x,y} = \frac{2N_e r_e}{\gamma} \frac{\sigma_z}{\sigma_{x,y}(\sigma_x + \sigma_y)}$$

 $D_{x,y} = \frac{2N_e r_e}{\gamma} \frac{\sigma_z}{\sigma_{x,y}(\sigma_x + \sigma_y)}$   $D_{x,y} -- disruption factor due to beam-beam pinch effect$ 

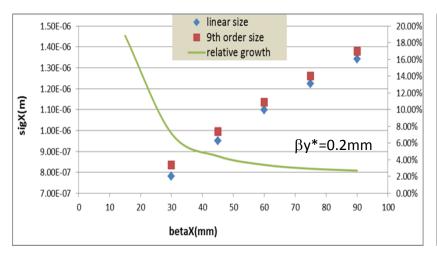
$$H_{D_{x,y}} = 1 + D_{x,y}^{1/4} \frac{D_{x,y}^3}{D_{x,y}^3 + 1} \left[ \ln(\sqrt{D_{x,y}} + 1) + 2\ln(0.8 \frac{\beta_{x,y}}{\sigma_z}) \right]$$

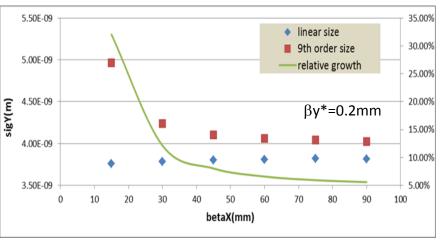
$$H_{D} = \sqrt{H_{D_{x}}} H_{D_{y}}^{(1+2(\frac{\sigma_{x}}{\sigma_{y}})^{3})/6(\frac{\sigma_{x}}{\sigma_{y}})^{3}}$$
 (  $H_{D} \approx H_{D_{y}}^{1/3}$  for flat beam)

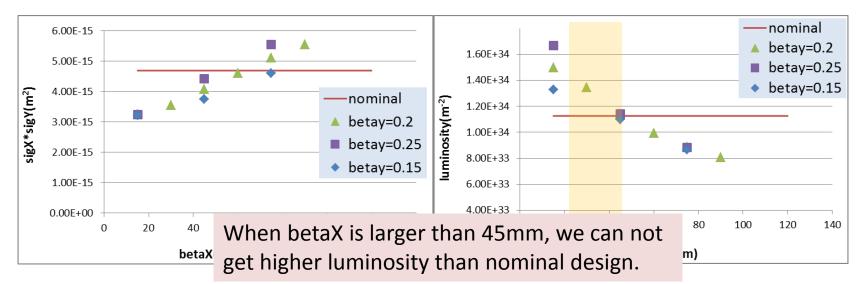
- $\blacksquare$  These formulae are valid when the hour glass effect is small (  $A_y = \frac{\partial_z}{\beta^*} < 1$  ).
- Beam-beam interaction simulation by Guineapig++ is a better way to give more realistic estimates of the luminosity.

### Chromaticity correction using 5 sextupoles

- minimize the product of  $\sigma x^* \times \sigma y^*$  with fixed  $\beta y^*$  and  $\sigma z$  ( $\sigma z = 150 \mu m$ )
- Quick beam-beam simulations with RMS beam size.
- The energy spread for both beam is 0.0006.







## Alternative optical parameters for ILC FFS with five sextupoles

|  | ILC nominal | ILC-low BS | ILC-high Lum |
|--|-------------|------------|--------------|
| E/beam (GeV)   | 250         | 250        | 250          |
| Ne (×10 <sup>10</sup> )  | 2           | 2          | 2            |
| $\sigma_{z}$ (um)  | 300         | 150        | 150          |
| $\beta^*_{x/y}$ (mm)   | 15/0.4      | 45/0.2     | 20/0.2       |
| Ay   | 0.75        | 0.75       | 0.75         |
| σ* <sub>x/v</sub> by MAPCLASS (nm)                               | 594/7.89    | 994/4.10   | 750/4.6      |
| σ* <sub>x</sub> ×σ* <sub>v</sub> (nm²)                           | 4687        | 4075       | 3450         |
| Luminosity from guineapig++ (×10 <sup>34</sup> m <sup>-2</sup> ) | 1.126       | 1.143      | 1.40         |
| Beamstrahlung energy spread from guineapig++ (%)                 | 2.8         | 1.8        | 2.8          |

We can get higher luminosity while keeping similar beamstrahlung level as nominal design when  $\beta x^*$  is smaller than 45 mm, or we can get same luminosity as nominal design with much weaker beamstrahlung effect if we just choose 45 mm  $\beta x^*$ .

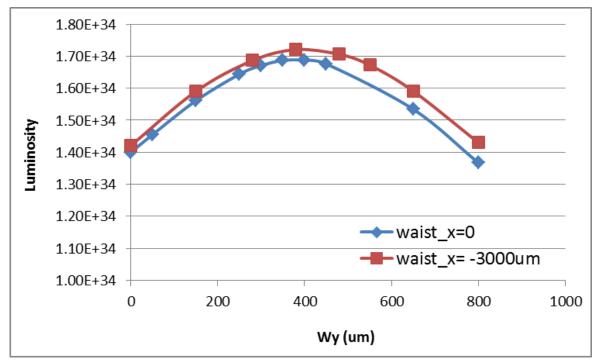
### Summary of sextupoles strength

• alternative design with full 5 sextupoles ( $\sigma z=150 \mu m$ )

|             | nominal | alternative |         |           |        |            |         |
|-------------|---------|-------------|---------|-----------|--------|------------|---------|
|             |         | βy*=0.15mm  |         | βy*=0.2mm |        | βy*=0.25mm |         |
| βx/βy [mm]  | 15/0.4  | 15/0.15     | 45/0.15 | 15/0.2    | 45/0.2 | 15/0.25    | 45/0.25 |
| SF6 [T/m^2] | 1.668   | -1.326      | -0.748  | -1.273    | -0.806 | -1.365     | -0.845  |
| SF5 [T/m^2] | -0.341  | -2.480      | -1.937  | -2.361    | -1.933 | -2.556     | -2.117  |
| SD4 [T/m^2] | 3.101   | 3.088       | 3.013   | 3.044     | 2.988  | 3.115      | 3.076   |
| SF1 [T/m^2] | -4.959  | -2.092      | -2.376  | -1.924    | -2.212 | -2.182     | -2.545  |
| SD0 [T/m^2] | 7.324   | 7.419       | 7.282   | 7.334     | 7.242  | 7.471      | 7.393   |

#### Vertical waist scan

- We can increase the luminosity by seperating the focusing points of two beam because the beam-beam effects give a strong focusing force just like an additional quadrupole.
  - —beam-beam simulations with real beam distribution at IP
  - —ILC nominal design was used



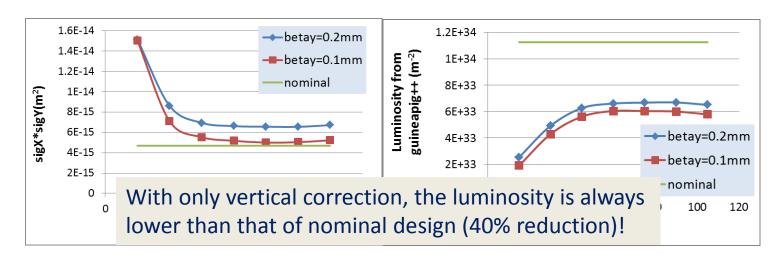
- Real beam distribution give higher luminosity than just use RMS beam size. (The beam distribution at IP may far deviate from Gaussian shape so that RMS size overestimate the size of beam core.)
- Highest luminosity is at Wy=380um (~20% growth).
- Horizontal waist shift has little effect to luminosity.

## New FFS optics with real beam distribution and coherent waist shift

|  | ILC nominal (theoretical) | ILC nominal<br>(real) | ILC-low BS<br>(real) | ILC-high Lum<br>(real) |
|--|---------------------------|-----------------------|----------------------|------------------------|
| E/beam (GeV)   | 250                       | 250                   | 250                  | 250                    |
| Repetition rate (Hz)   | 5                         | 5                     | 5                    | 5                      |
| Bunch number/pulse   | 2625                      | 2625                  | 2625                 | 2625                   |
| Ne (×10 <sup>10</sup> )  | 2                         | 2                     | 2                    | 2                      |
| $\sigma_{z}$ (um)  | 300                       | 300                   | 150                  | 150                    |
| β* <sub>x/y</sub> (mm)   | 15/0.4                    | 15/0.4                | 45/0.2               | 20/0.2                 |
| Luminosity by single collision (×10 <sup>34</sup> m <sup>-2</sup> )                                | 1.8                       | 1.40                  | 1.42                 | 1.82                   |
| Luminosity by single collision (inc. vertical waist shift) (×10 <sup>34</sup> m <sup>-2</sup> )    |                           | 1.69                  | 1.72                 | 2.21                   |
| Total luminosity (inc. vertical waist shift) (×10 <sup>34</sup> cm <sup>-2</sup> s <sup>-1</sup> ) | 2.4                       | 2.22                  | 2.25                 | 2.9                    |

## ILC luminosity with pure vertical chromaticity correction scheme

- enlarge  $\beta x^*$  and reduce  $\beta y^*$  in order to reduce the horizontal chromaticity and meanwhile keep similar value for  $\sigma x^* \times \sigma y^*$ .
- this scheme only works for beams with very small energy spread (e.g. 0.06% for e+ at 500 GeV c.m.)
- Reduce  $\sigma_7$  from nominal 300um to 150um to cure hourglass effect
- Choose two cases for βy\*:
  - $\beta y^*=0.1$ mm: minimum vertical beam size
  - $\beta y^* = 0.2$ mm: keep same hourglass effect as ILC nominal design (Ay= $\sigma_z/\beta y^* = 0.75$ )
- Luminosity simulations from guineapig++ (Single collision ).
- Quick beam-beam simulations with RMS beam size from Mapclass.



The reason of luminosity reduction in spite of both the product of  $\sigma x^* \times \sigma y^*$  and the ratio of  $\sigma_z/\beta y^*$  being close to the nominal design is that the shorter bunch length by a half gives much smaller disruption parameter  $D_{x,y}$  and hence results in less luminosity enhancement  $H_D$  from the pinch effect.

## partial correction for the horizontal chromaticity

- add a horizontal sextupole to recover the luminosity drop from the pure vertical correction scheme
- SF5 is most effective to realize horizontal chromaticity correction and hence to recover the luminosity
- 0.06% energy spread was used

|   | ILC nominal             | New-1      | New-2       |
|---|-------------------------|------------|-------------|
| Sextupoles used   | SD0,SF1,SD4,SF<br>5,SF6 | SD0,SD4    | SD0,SD4,SF5 |
| E/beam (GeV)  | 250                     | 250        | 250         |
| Ne (×10 <sup>10</sup> )   | 2                       | 2          | 2           |
| $\sigma_{z}$ (um)   | 300                     | 150        | 150         |
| $\beta^*_{x/y}$ (mm)  | 15/0.4                  | 60/0.2     | 60/0.2      |
| Ау  | 0.75                    | 0.75       | 0.75        |
| $\sigma^*_{x/y}$ by MAPCLASS (nm)   | 594/7.89                | 1689 /3.88 | 1524/3.92   |
| $\sigma^*_{x} \times \sigma^*_{y}$  | 4687                    | 6553       | 5974        |
| *Luminosity of single collision from guineapig++ (×10 <sup>34</sup> m <sup>-2</sup> ) | 1.126                   | 0.668      | 0.741       |

<sup>\*</sup>For the total luminosity, we need to multiply the bunch number and the repetition frequency.

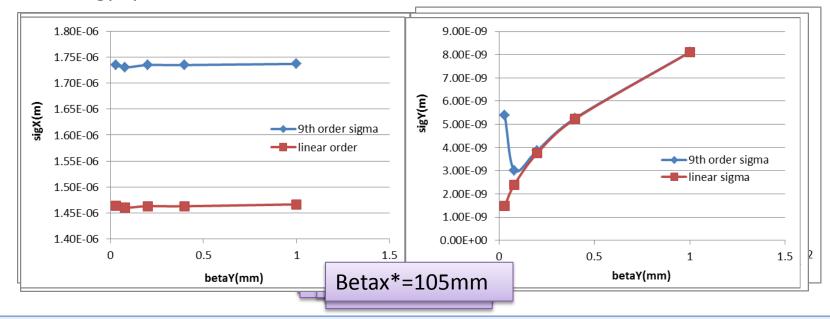
#### Summary

- We have tried both the simplified chromaticity scheme which is mainly in vertical direction with fewer sextupoles (2 or 3) and the thorough chromaticity scheme with 5 sextupoles.
- With an enlarged  $\sigma x^*/\beta x^*$  and a smaller  $\sigma y^*/\beta y^*$ , we expect less beamstrahlung effect at IP.
- Luminosity for alternative ILC FFS optics were studied through beam-beam simulations by Guineapig++.
- With 5 sextupoles, we can either recover the luminosity with much lower beamstrahlung effect or get a higher luminosity while keeping same beamstrahlung as nominal design. No changes in the present FFS design are needed, only refitting of existing magnets.
- 150um bunch length is needed to reduce the hour glass effect => it seems worthwhile to invest in some additional bunch compression
- Thorough luminosity simulations with real beam distribution and coherent waist shift were done based on the newly proposed ILC FFS design.
- For 2 sextupoles's (SD0, SD4) correction, we get a simple FFS and much less beamstrahlung, at the expense of much lower luminosity (40% drop). The luminosity reduction will be 34% with 3 sextupoles (SD0, SD4, SF5).
- Study will be continued based on ILC TDR parameters and newest FFS optics.

### Reserved

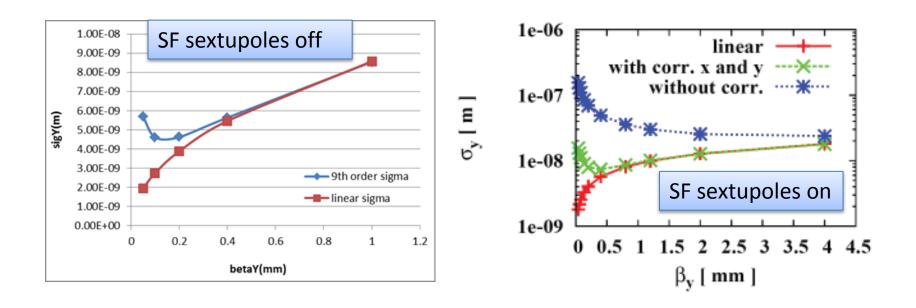
## Pure vertical chromaticity correction with SD0 and SD4

- Rematch the IP beta function to a different value using six matching quadrupoles (QM16 to QM11)
- Use SD0 and SD4 to correct the second order vertical chromatic item  $T_{342}$  and  $T_{346}$  by the code of Madx
- Beam size at IP was simulated by Mapclass
- The energy spread for both beam which was used is 0.0006.



- -- There is always a minimum for  $\sigma y^*$  around  $\beta y^*=0.1$ mm.
- -- The minimum value for  $\sigma y^*$  is 3nm when  $\beta x^*$  is at the range [60mm, 90 mm].

## Comparison of nominal design and pure vertical correction scheme ( $\beta x^*=15 \text{ mm}$ )



The vertical beam size is limited in the nominal design. The reason is the higher order coupling terms such as  $T_{313}$ ,  $T_{314}$ ,  $U_{3136}$ ,  $U_{3246}$  and so on due to three SF sextupoles.