

# Jets at a future $e^+e^-$ collider

*Marcel Vos  
IFIC (UVEG/CSIC) Valencia*

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Vinca Institute, Belgrade, Serbia***

***With thanks to Nacho García, Gavin Salam, André Sailer, Jesse Thaler***



# Scope of this talk

Jet reconstruction at the ILC is not simply an extension of the LEP/SLC experience

- higher energy, higher jet multiplicity, more background, better detectors

After introduction of  $\gamma\gamma \rightarrow$  hadrons in full simulation, most LC physics studies now use hadron collider algorithms,

- is this the best we can do?

Time for a critical evaluation...

- understand impact of jet reconstruction on physics performance
- Rethink jet reconstruction algorithms

Can we benefit from recent progress in jet algorithms?

- Pile-up correction/mitigation?
- Jet substructure as a driver for detector design?
- Boosted objects?

Take advantage of “future projects” session of the BOOST workshop series



# An Australian analogy

The pig-footed bandicoot had lived in Australia for millions of years, and was (according to Mr. Darwin) very well adapted to its environment. Still it went extinct (almost without putting up a fight) soon after the arrival of Europeans.



The rabbit had adapted, over millions of generations, to its European habitat. It conquered Australia in a few years after its (unfortunate) introduction in the country.

Moral, so far:

yes, a hadron collider algorithm may work better...

But, is the rabbit the optimal animal for Australia?





# An Australian analogy

But, is the rabbit the optimal animal for Australia?

Probably not... one ought to be able to design a better rabbit especially for Australia.

Moral: understand what makes longitudinally invariant jet finding work so well. And adapt the jet finding to make it even better for the purpose of high energy  $e^+e^-$  collisions.





# Jets in $e^+e^-$ colliders

## Jet physics AND jet reconstruction performance are important at $e^+e^-$ colliders

After a top (W, Z, Higgs) factory like the LHC,  $e^+e^-$  collider samples are relatively small:

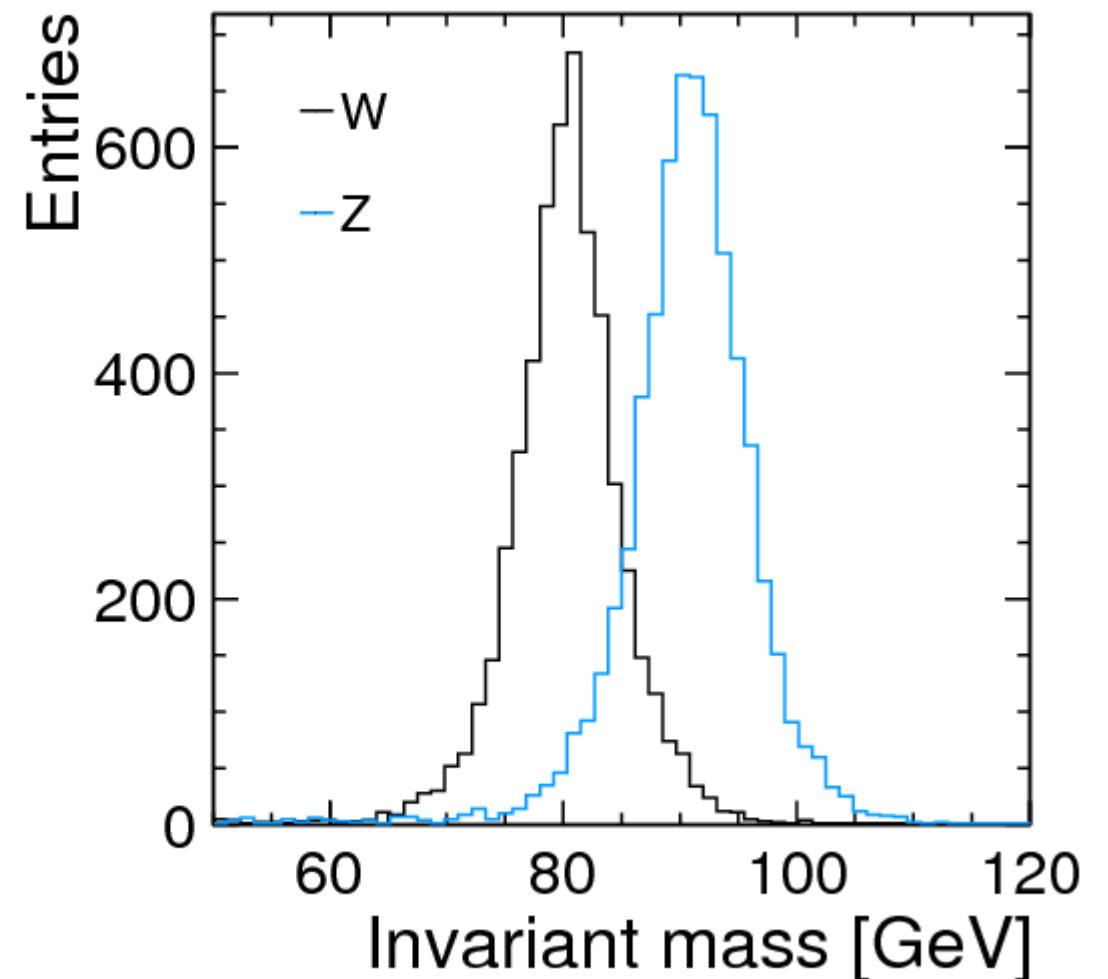
→ 300.000  $t\bar{t}$  pairs at 500 GeV

*Use hadronic final states (also in Higgsstrahlung analysis)*

### Distinguish hadronic W and Z decays

*(the main calorimeter specification on energy resolution at low energy, a requirement on the jet mass resolution at high energy)*

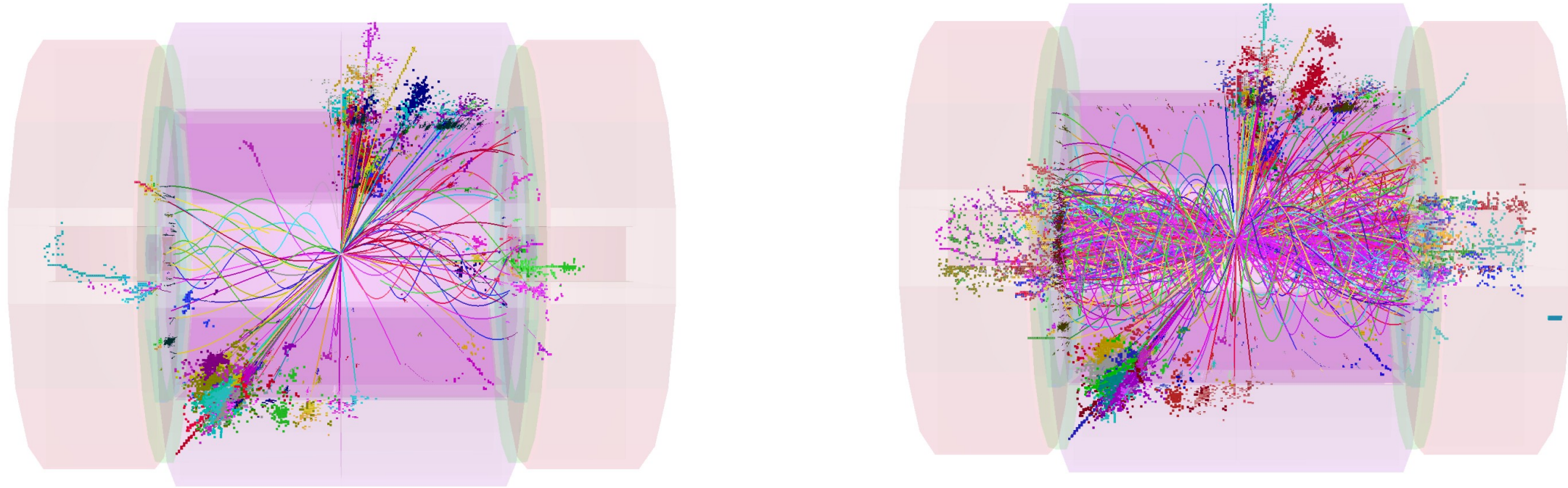
Jet multiplicity increases with center-of-mass energy  
di-boson → 4 jets, Zh → 4 jets,  $t\bar{t}$  → 6 jets,  $t\bar{t}h$  → 8 jets  
*(jet reconstruction can spoil the energy measurement even if all particles are precisely measured)*



# LC backgrounds

**Lepton colliders offer a relatively clean environment (compared to the LHC), but not quite to the level that we can ignore backgrounds completely:**

- Incoherent pair production
- $\gamma\gamma \rightarrow$  hadrons production



Example: a CLIC bunch train worth of  $\gamma\gamma \rightarrow$  hadrons superposed on a physics event. If all CLIC3TeV detector systems integrate over 10 ns (=20BX), background deposits 1.2 TeV of energy in the calorimeter systems.

## $\gamma\gamma \rightarrow$ hadrons

- Strongly peaked in the forward direction
- For a given machine, background level scales with instantaneous luminosity
  - Much larger at 3 TeV than at 500 GeV (even with the same technology)
- Its impact depends on the bunch structure and detector read-out speed
  - ILC, 1300 bunches spaced by 500 ns (typically single-BX read-out possible)
  - CLIC, 312 bunches spaced by 0.5 ns

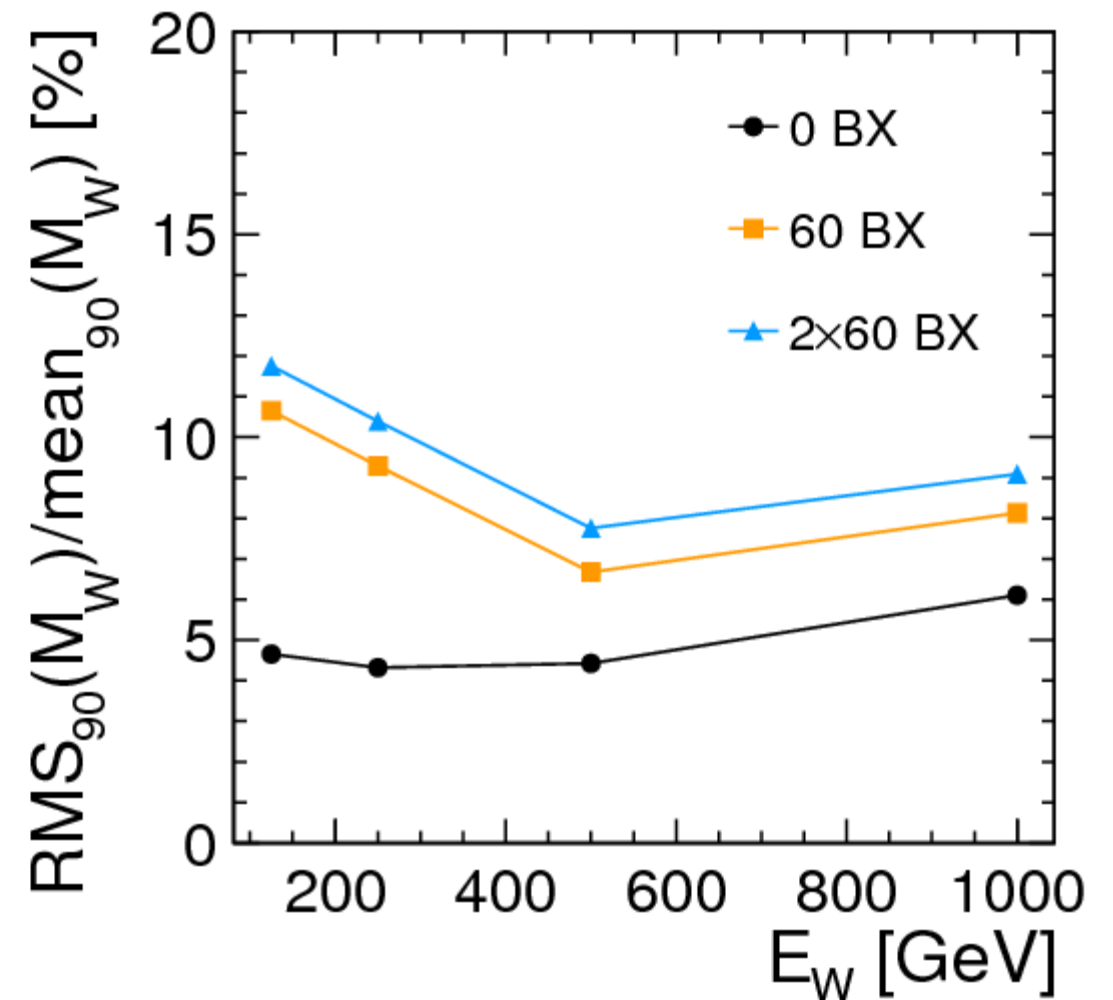
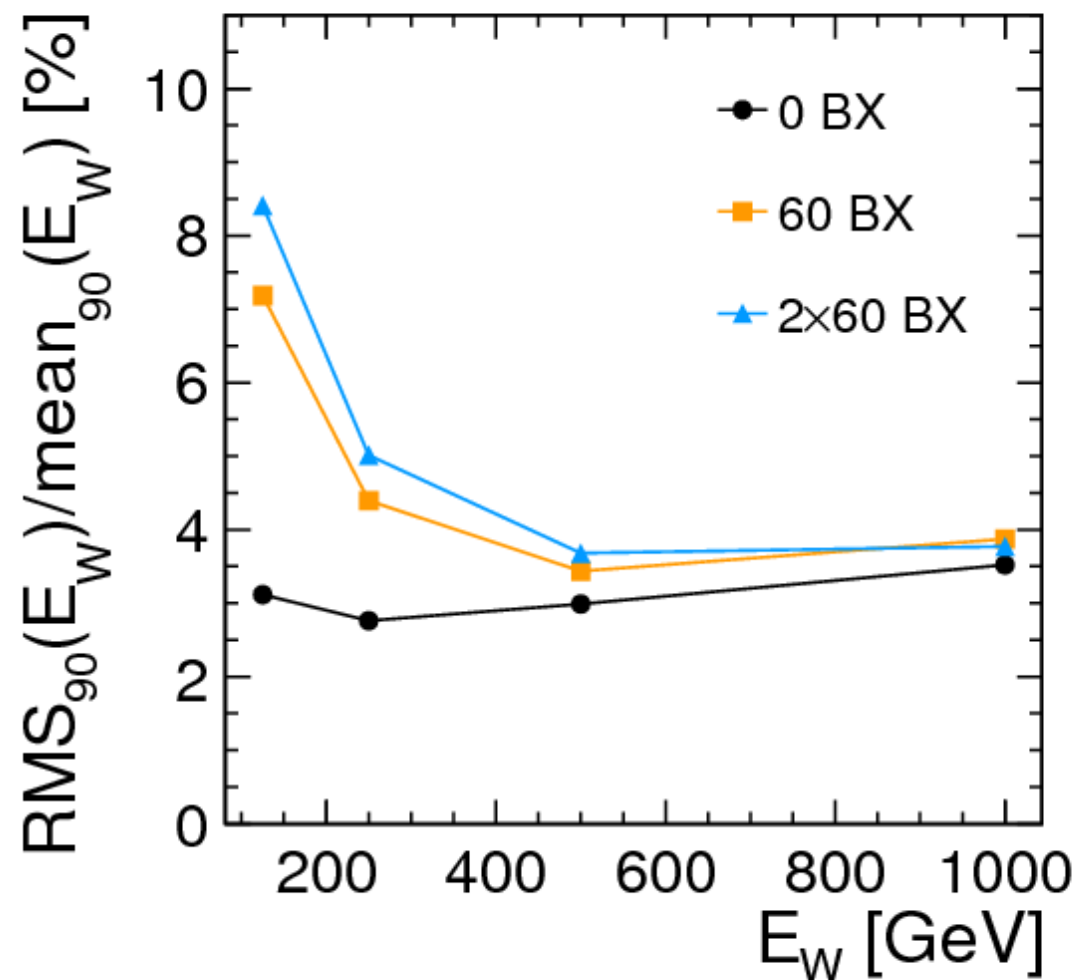
Use CLIC case as a stress test for jet reconstruction; if it works there, it's good for ILC too.

# Impact of background

$e^+e^- \rightarrow W^+W^- \rightarrow l\nu qq$  events at CLIC with W energies of 100, 250, 500 and 1000 GeV

Overlay 60 (120) BX worth of  $\gamma\gamma \rightarrow$  hadrons, select in-time reconstructed particles, remove lepton

Reconstruct long. inv.  $k_t$  jets exclusively (N=2, R=0.7)



Energy resolution at high energy is not too badly affected,  
mass resolution suffers everywhere

[CLIC CDR, Marshall, Münnich & Thomson, arXiv:1209.4039], non-negligible even for ILC physics [many studies, arXiv:1307.8102]



# Jet energy resolution

Most of our jet studies analyze the power of Particle Flow and optimize detector designs

*look at simple systems (i.e. di-jets)*

*minimize the dependence on the jet reconstruction algorithm (measure visible energy...)*

For physics analyses we care about the W, Z and Higgs mass resolution in complex final states

*may be considerably worse than expected from detector performance alone*

Define intermediate level: truth-particle jets constructed with the same algorithm

(for LCIO software, contact [ignacio.garcia@ific.uv.es](mailto:ignacio.garcia@ific.uv.es))

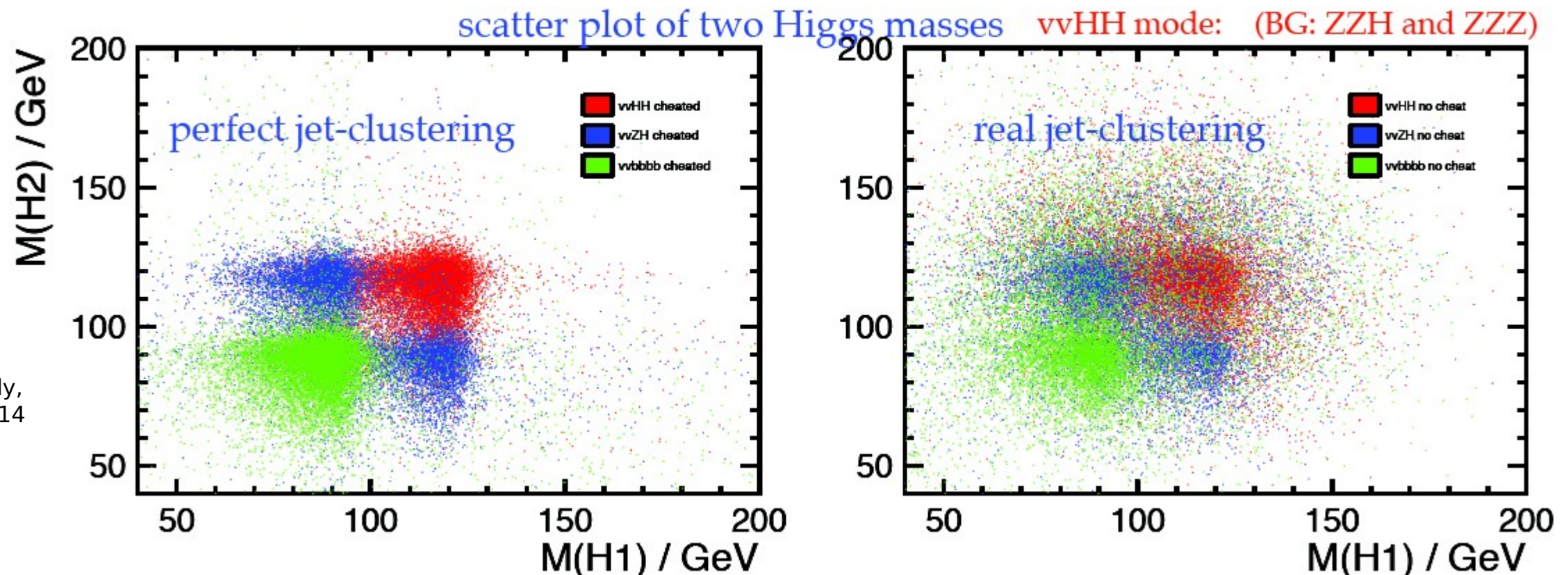
Detector level (Particle Flow objects)

Particle level (stable MC particles)

Parton level (W, Z, Higgs or top mass)

Detector limitations...

Inherent limitations  
of jet algorithms...



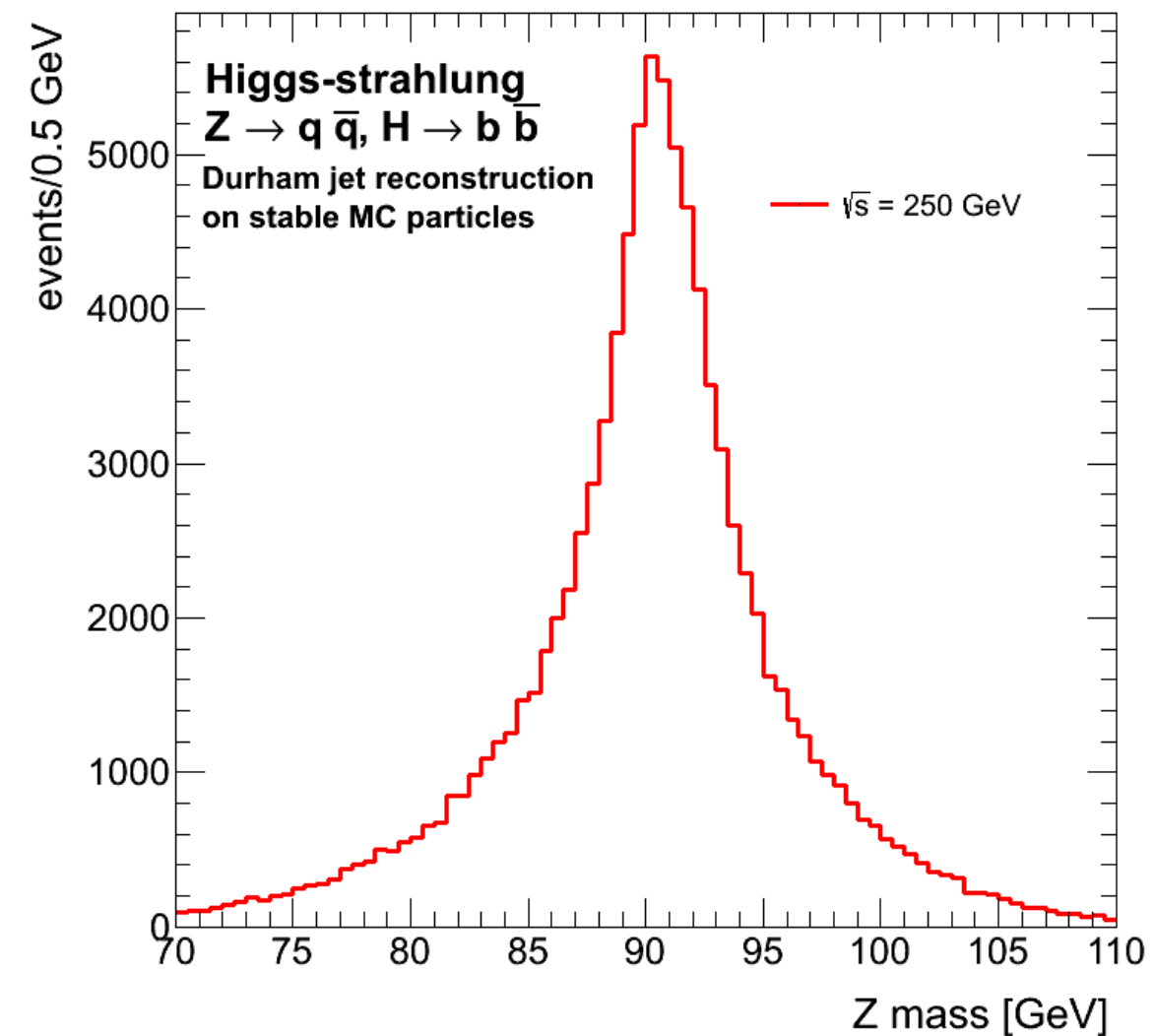


# Toy setup

MadGraph 5 Matrix Element

Pythia8 parton shower

FastJet + fjcontrib



Very useful to try out new ideas:

- can access FastJet plugins  $\rightarrow$  sophisticated tool set
- isolate the effect of the algorithm  $\rightarrow$  no noise from detector, ISR, bkg.
- not limited to benchmarks  $\rightarrow$  study behaviour in a 18 TeV  $e^+e^-$  collider
- fast (no GRID)  $\rightarrow$  turn-around time 5-10 minutes

*Z mass resolution for ZH  
production at 250 GeV  
RMS = 6 GeV due to “confusion”  
in jet algorithm alone*

# Jet algorithms

## Lepton colliders:

Distance based on E, angle

$$d_{ij} = \min(E_i^{2n}, E_j^{2n}) (1 - \cos \theta_{ij})$$

Good old Durham ( $n=1$ ,  $e^+e^- k_t$ ) and  
Cambridge/Aachen ( $n=0$ )

Generalized lepton collider algorithms:

$$d_{ij} = \min(E_i^2, E_j^2) (1 - \cos \theta_{ij}) / (1 - \cos R)$$

$$d_{iB} = E_i^2$$

Introduce beam jets  $\rightarrow$  jet size R

A new kid on the block: the Valencia algorithm

$$d_{ij} = \min(E_i^{2\beta}, E_j^{2\beta}) (1 - \cos \theta_{ij}) / R^2$$

$$d_{iB} = p_T^{2\beta}$$

## Hadron colliders:

Hadron colliders:  
longitudinally invariant  
algorithms based on  $p_T$ ,  $\Delta R$

$$d_{ij} = \min(p_{Ti}^{2n}, p_{Tj}^{2n}) \Delta R_{ij}^2 / R^2$$

$$d_{iB} = p_{Ti}^{2n}$$

$N=1$ , longitudinally invariant kt  
 $N=0$ , Cambridge/Aachen  
 $N=-1$ , anti-kt

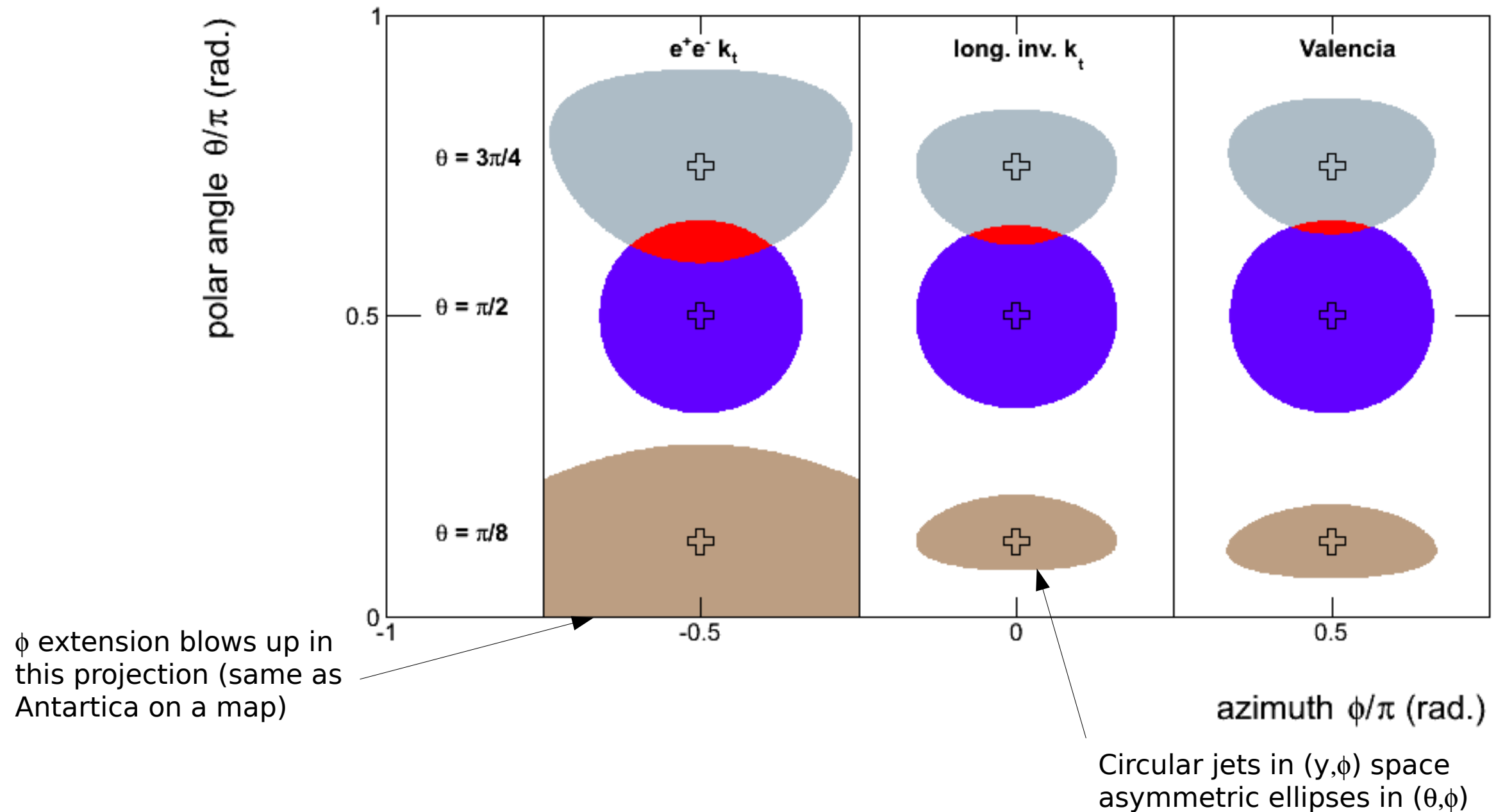
Maintain energy and angle  
Choose beam distance to increase robustness

Georgi's simple alternative (arXiv:1408.1161)





# Jet sizes



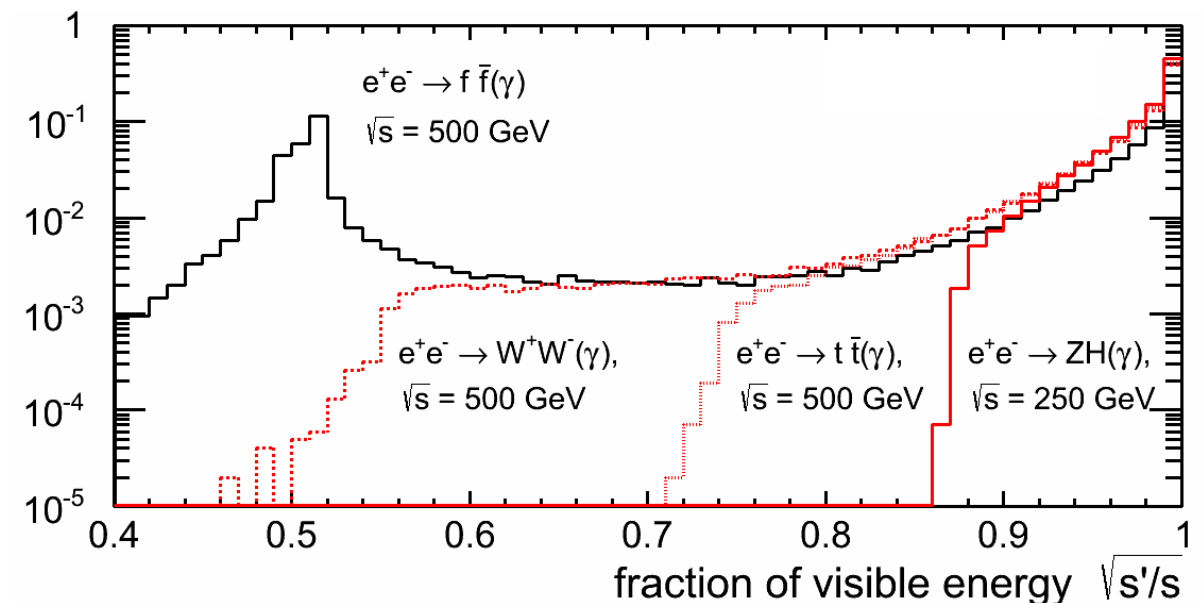
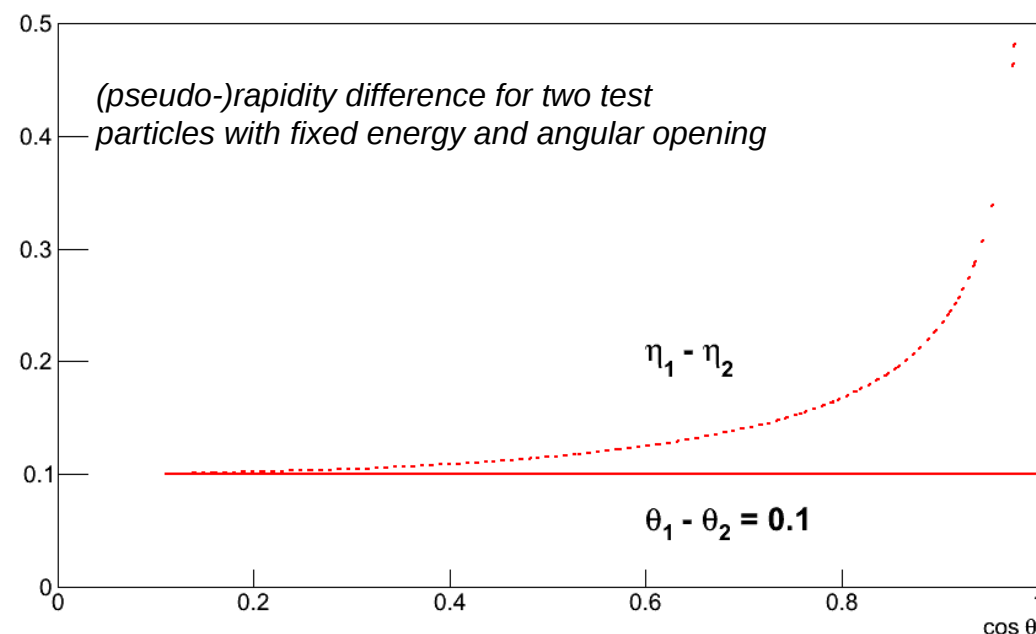
The footprint or area of jets depends on the jet algorithm  
Three algorithms that yield a similar, circular area in the central detector produce very different jets in the forward region

# Jet reconstruction

Why does a hadron collider algorithm work better at a lepton collider than the equivalent lepton collider algorithm?

Do we need/want longitudinal invariance?

No. ISR and beamstrahlung lead to some boost, but in most interesting processes, it's very small.



No. It's potentially harmful. The rapidity difference is a poor measure of angular separation in collisions that are at rest in the laboratory.



# Jet reconstruction

Why does a hadron collider algorithm work better at a lepton collider than the equivalent lepton collider algorithm?

$$d_{ij} = \min(p_{Ti}^{2n}, p_{Tj}^{2n}) \Delta R_{ij}^2 / R^2$$

$$d_{iB} = p_{Ti}^{2n}$$

VS.

$$d_{ij} = \min(E_i^{2n}, E_j^{2n}) (1 - \cos \theta_{ij})$$

**Beam jets + shrinking footprint with polar angle yields increased robustness against forward-peaked  $\gamma\gamma \rightarrow$  hadrons!**

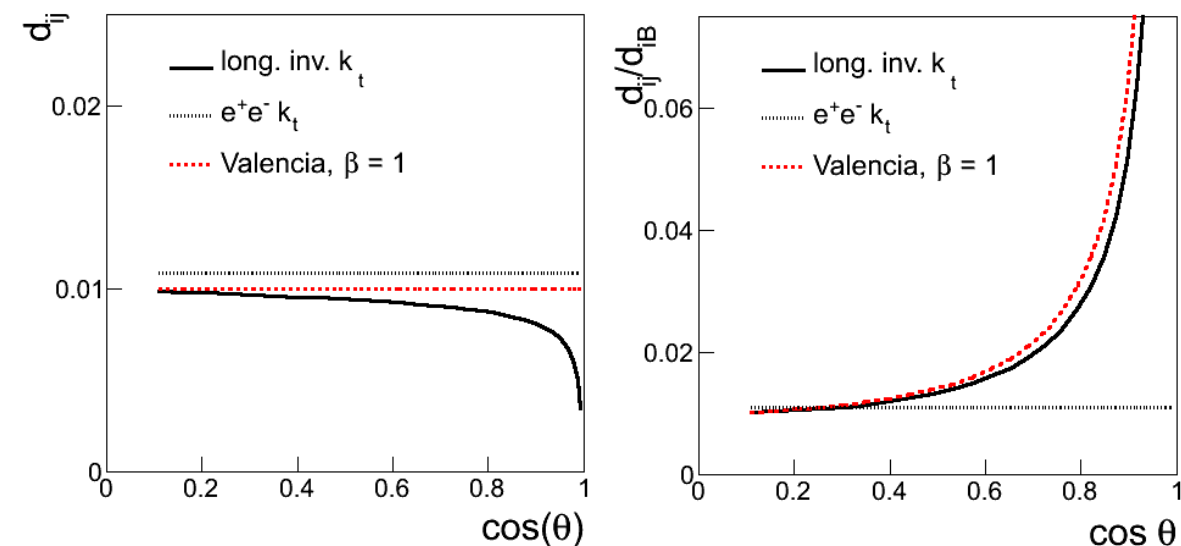
The Valencia algorithm is an attempt to get the best of both worlds (with a twist):

$$d_{ij} = \min(E_j^{2\beta}, E_i^{2\beta}) (1 - \cos \theta_{ij}) / R^2$$

*$e^+e^-$  distance between particles*

$$d_{iB} = p_T^{2\beta}$$

*beam distance to mimic  $d_{ij}/d_{iB}$  behaviour  
 $\beta$  to tweak background rejection*



Two test particles with constant energy ( $E = 1$  GeV)  
and fixed polar angle separation (100 mrad)

# Perturbative corrections

following Dasgupta, Magnea, Salam, Non-perturbative QCD effects in jets at hadron colliders, JHEP0802 (2008) 055

$e^+e^- \rightarrow q\bar{q}$  events at  $\sqrt{s} = 250$  GeV (toy setup)

Total energy correction: difference between jet energy and  $\sqrt{s}/2$

Dominated by perturbative corrections

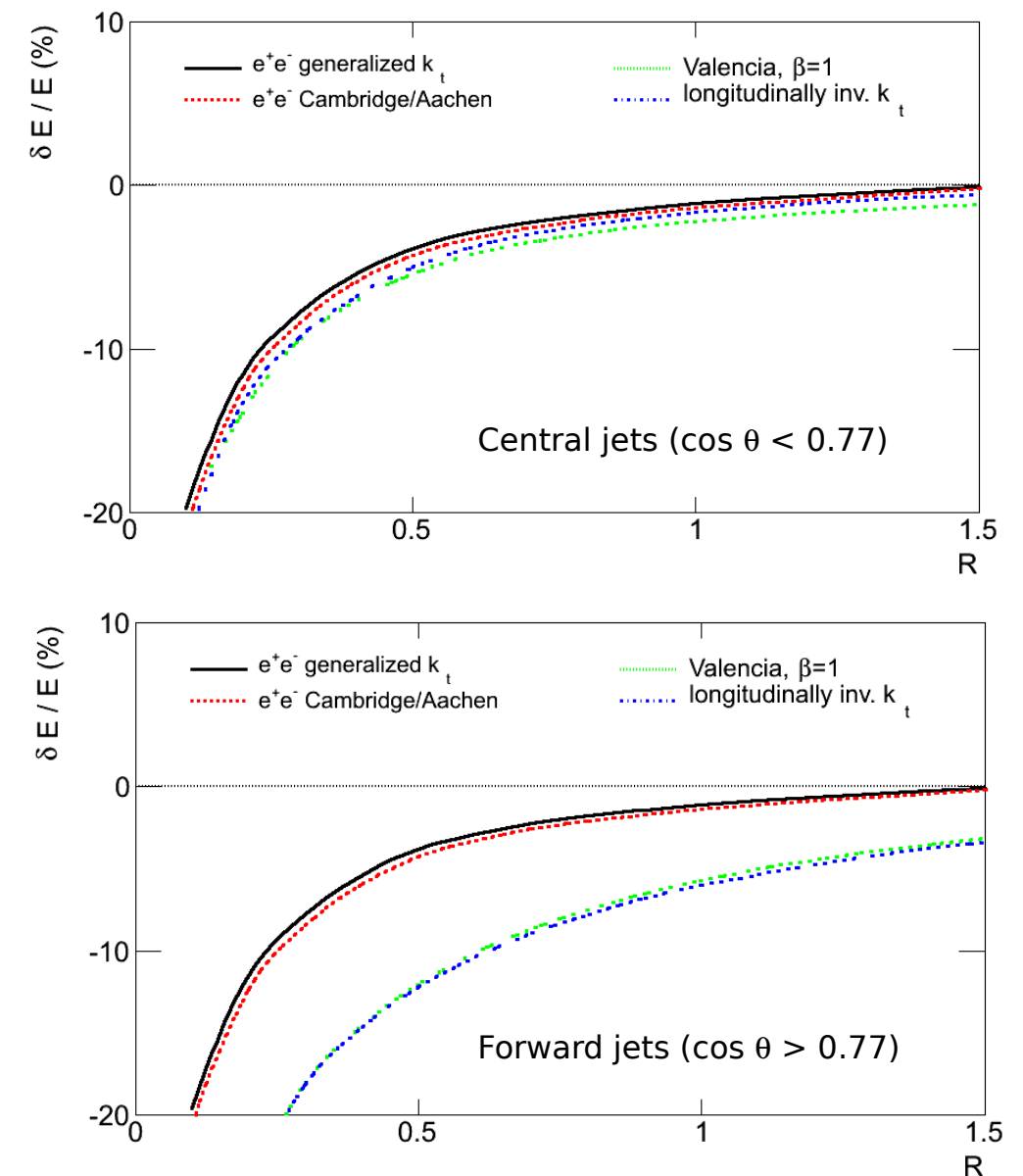
Corrections become large for  $R < 0.5$

Corrections tend to 0 for  $R > 1$

All algorithms are similar for central jets

Relative corrections are smaller for higher energy

Corrections are much larger in forward detector for robust algorithms with shrinking footprint (*longitudinally invariant algorithms, Valencia*)

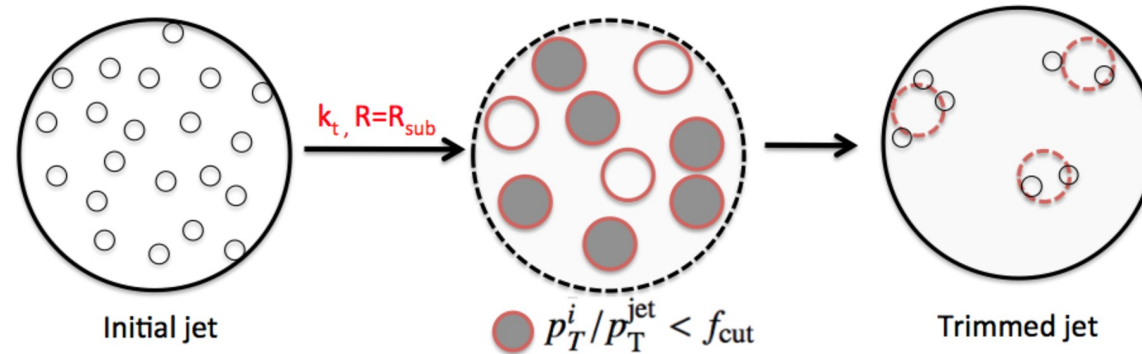




# Jet grooming

## Jet grooming

One of the main recipes at the LHC to deal with pile-up contamination of large-area jets

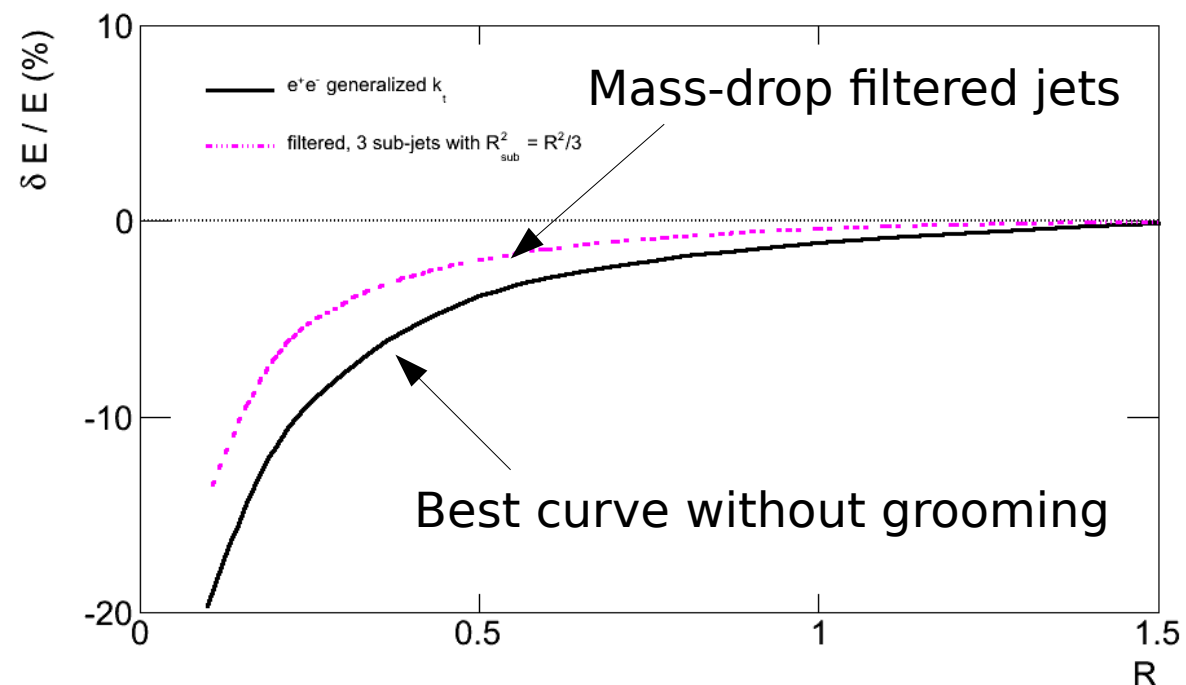


## $e^+e^-$ grooming

Reconstruct exclusive Durham jets in  $e^+e^- \rightarrow q\bar{q}$  ( $N=2$ ), break up into sub-jets with mass-drop filtering with  $R = R_{\text{sub}}$ ,

Select 3 hardest sub-jets

For fair comparison, choose  $R_{\text{sub}}^2 = R^2/3$  so that area of 3 sub-jets adds up to same area



**Grooming reduces perturbative corrections for a given jet area**

- better energy response
- less exposure to background

Large improvement! Deserves further study!

# Non-perturbative corrections

following Dasgupta, Magnea, Salam, Non-perturbative QCD effects in jets at hadron colliders, JHEP0802 (2008) 055

$e^+e^- \rightarrow q\bar{q}$  events at  $\sqrt{s} = 250$  GeV (toy setup)

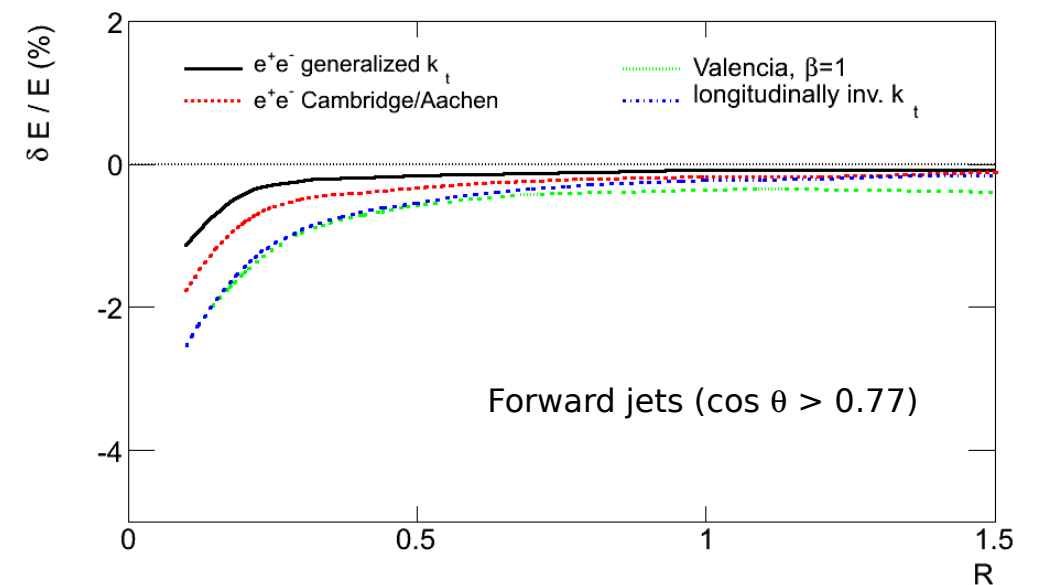
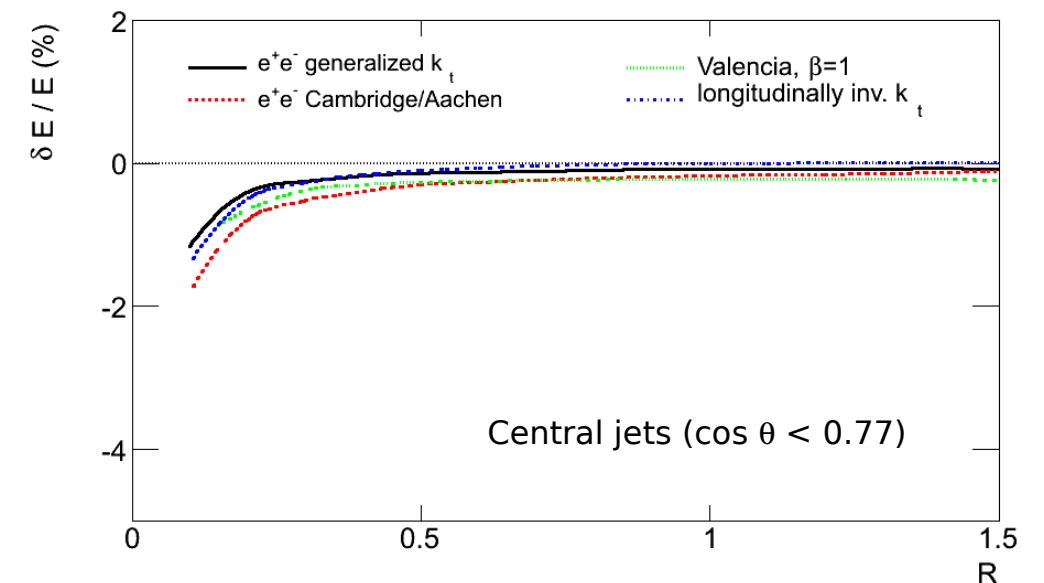
*Non-perturbative correction: difference between particle-level and parton-level jet energy (a.k.a. hadronization corrections)*

Non-perturbative corrections (hadronization)  
→ source of uncertainty in the Jet Energy Scale

Numerically much smaller  
> 1% only for very small  $R$

Shape similar to perturbative corrections

Interesting: fluctuations in correction are typically 10-20% smaller for round jets (anti- $k_t$ ) than for jets with more irregular shapes ( $k_t$ , C/A)



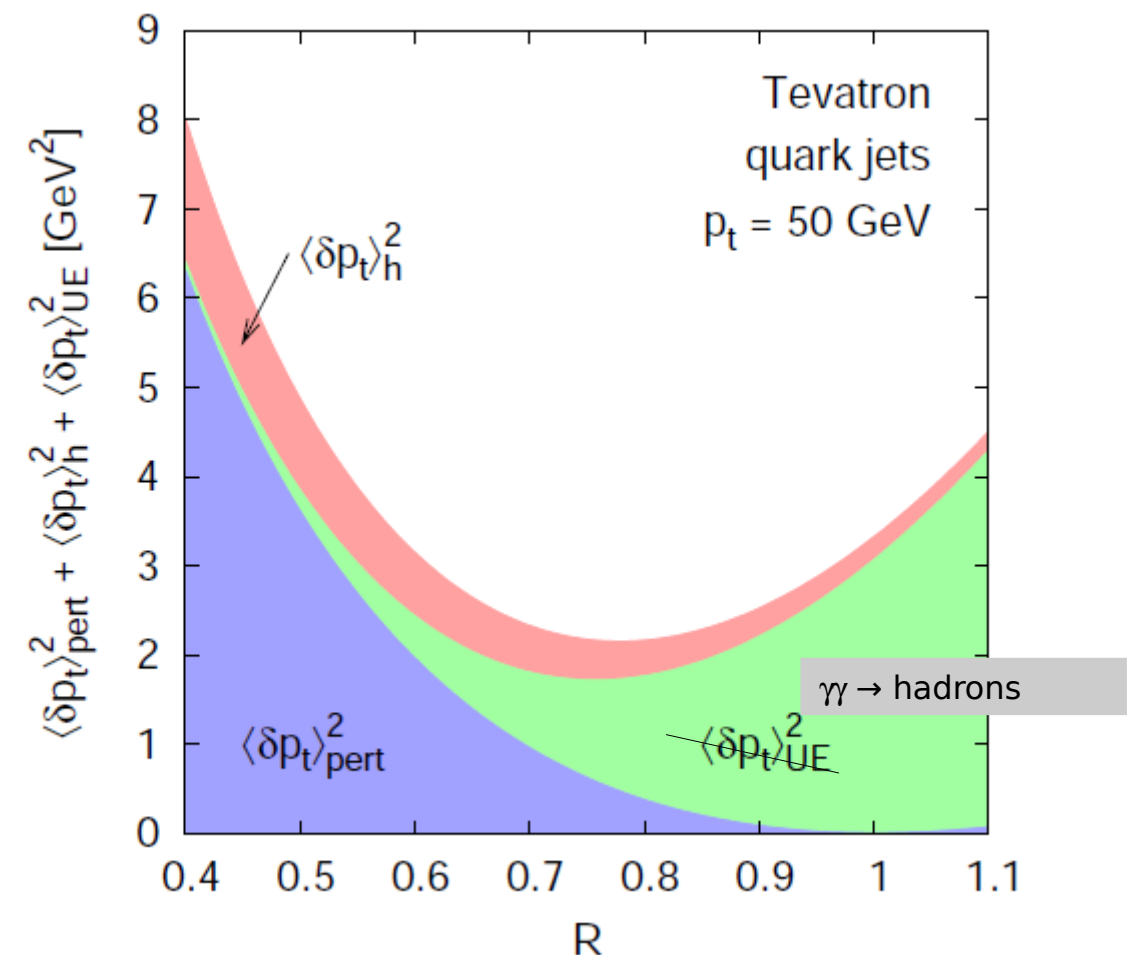
# $\gamma\gamma \rightarrow \text{hadrons}$

Background contribution scales with  $R^2$

Strongly dependent on center-of-mass energy

Much more important for forward jets than for central jets

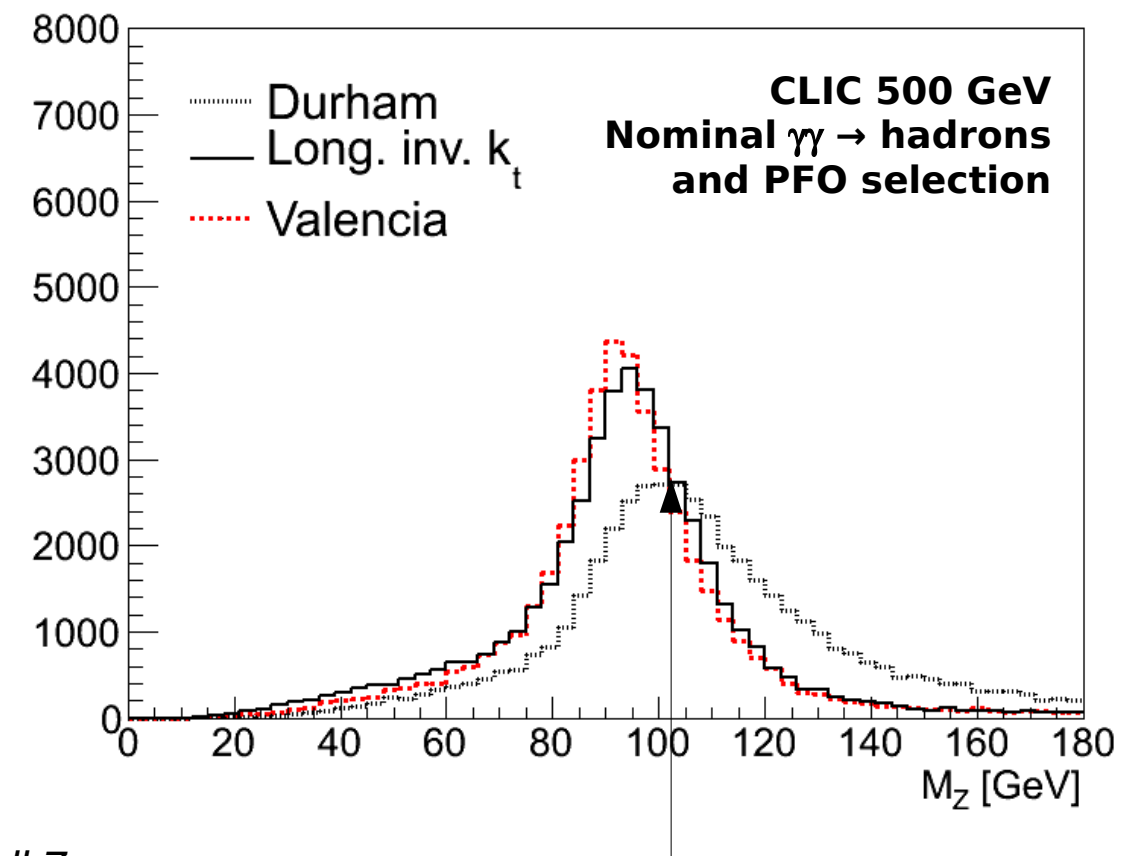
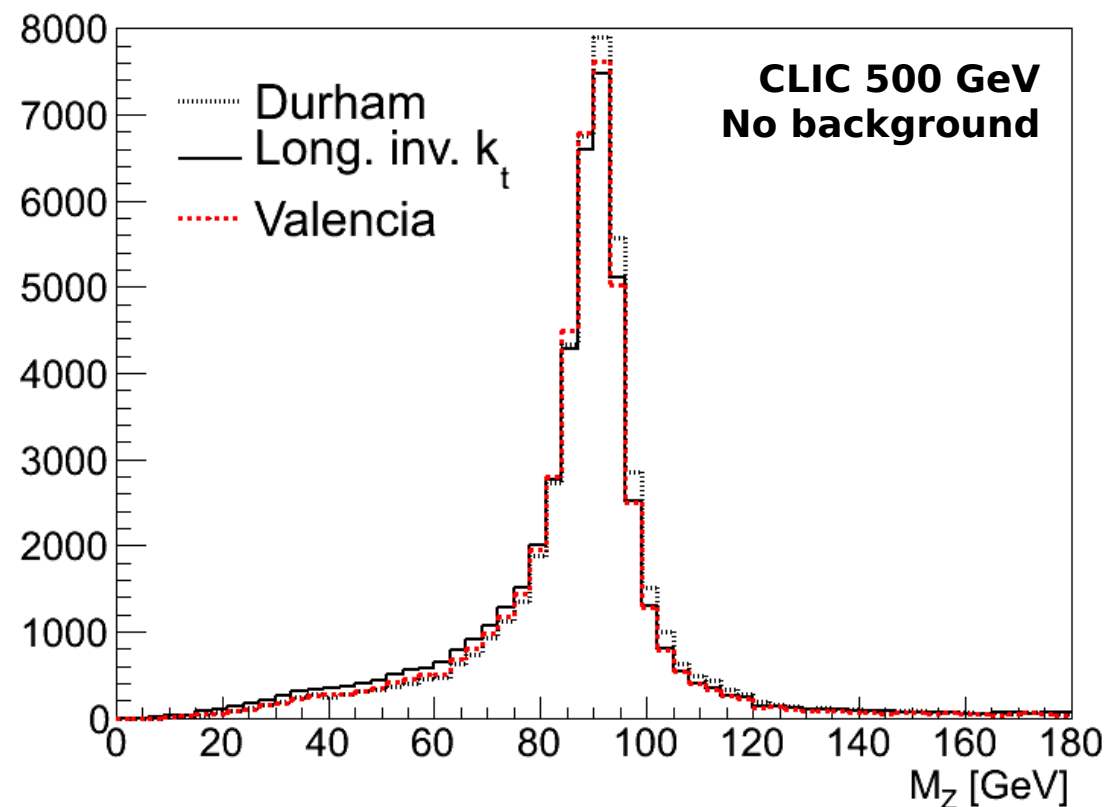
Reproduce a figure like this one from Dasgupta, Magnea, Salam, JHEP0802 (2008) 055 for several operation conditions: 250 GeV, 350 GeV, 500 GeV, 1 TeV, 1.4 TeV, 3 TeV





# Realistic benchmark including background

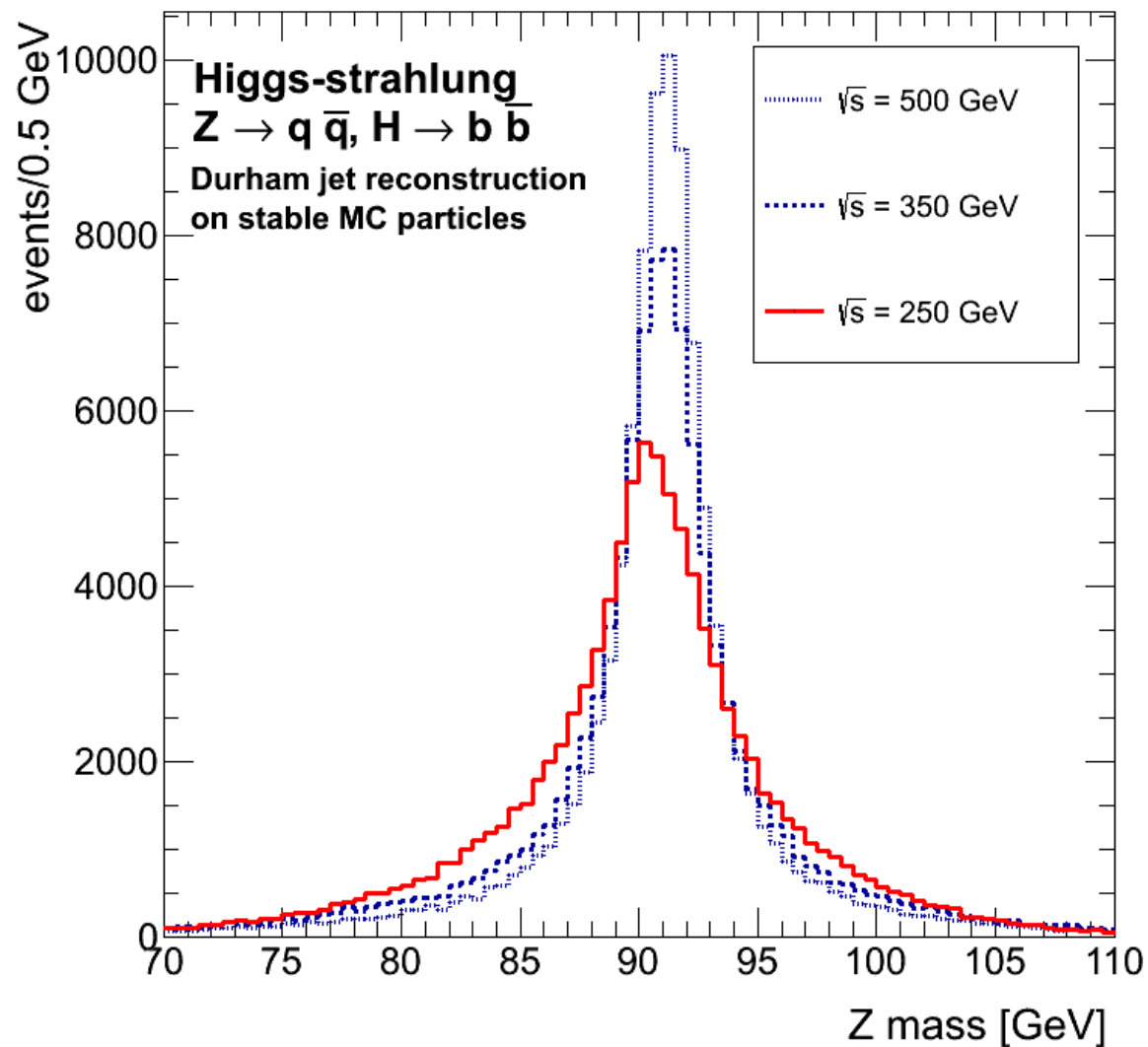
Jet energy reconstruction with nominal background much less degraded with algorithms with shrinking footprint (long. Invariant algorithms, Valencia) than  $e^+e^-$  algorithms (CLIC, high energy)



$ZZ \rightarrow q\bar{q}q\bar{q}$  events at CLIC with  $\sqrt{s} = 500$  GeV. Remove forward, or off-shell Z  
Reconstruct exactly 4 jets, with optimized  $R$  ( $=1.2$  for longitudinally invariant  $k_t$ ,  $1.0$  for Valencia)  
Find best pairs and report di-jet mass for background-free and nominal background

Here, Durham is clearly broken...

# Confusion in multi-jet final states



$e^+e^- \rightarrow ZH$  production cross section  
peaks at  $\sim 250$  GeV

The improved jet energy resolution  
and greater luminosity at 350 GeV  
may compensate

250 GeV	$\rightarrow$	$\text{RMS}_{90} = 4.2$ GeV
350 GeV	$\rightarrow$	$\text{RMS}_{90} = 2.7$ GeV
500 GeV	$\rightarrow$	$\text{RMS}_{90} = 1.3$ GeV

# Inclusive vs. exclusive

An easy example: top quark pair production

Exclusive clustering assumes that  $N$  hardest splits correspond to  $N$  final state partons

$N=6$  exclusive clustering works well at low energy

$K_t$  distance between top quark decay products governed by  $t$  and  $W$  mass

→  $\sqrt{d_{qq}}$  roughly constant

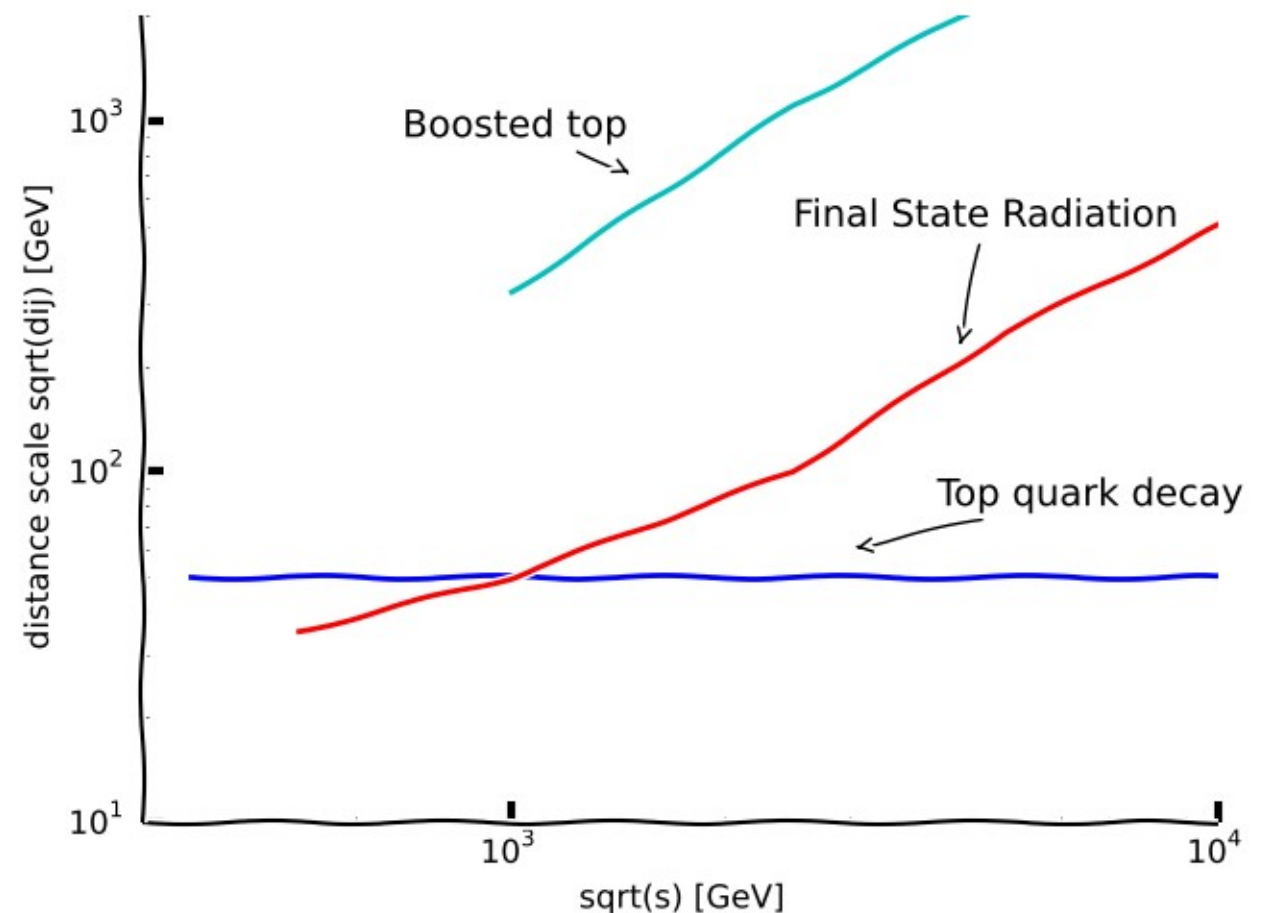
Distance of QCD final state radiation  $d_{qg}$  increases with available phase space

→  $\sqrt{d_{qg}}$  proportional to  $\alpha_s \sqrt{s}$

$N=2$  exclusive clustering at  $\sqrt{s} \sim 1$

→  $\sqrt{d_{tg}}$  is approx.  $\sqrt{s}/2$

Radiation from top quarks threatens  $N=6$  exclusive clustering at high energy, but  $N=2$  clustering takes over right in time



"Evolution of average distance scales"



# Inclusive vs. exclusive

Not-so-easy: ZHH production

Hierarchy in energies increases with  $\sqrt{s}$

When  $q\bar{q}$  split is harder than  $Z \rightarrow q\bar{q}$  or  $H \rightarrow b\bar{b}$ :

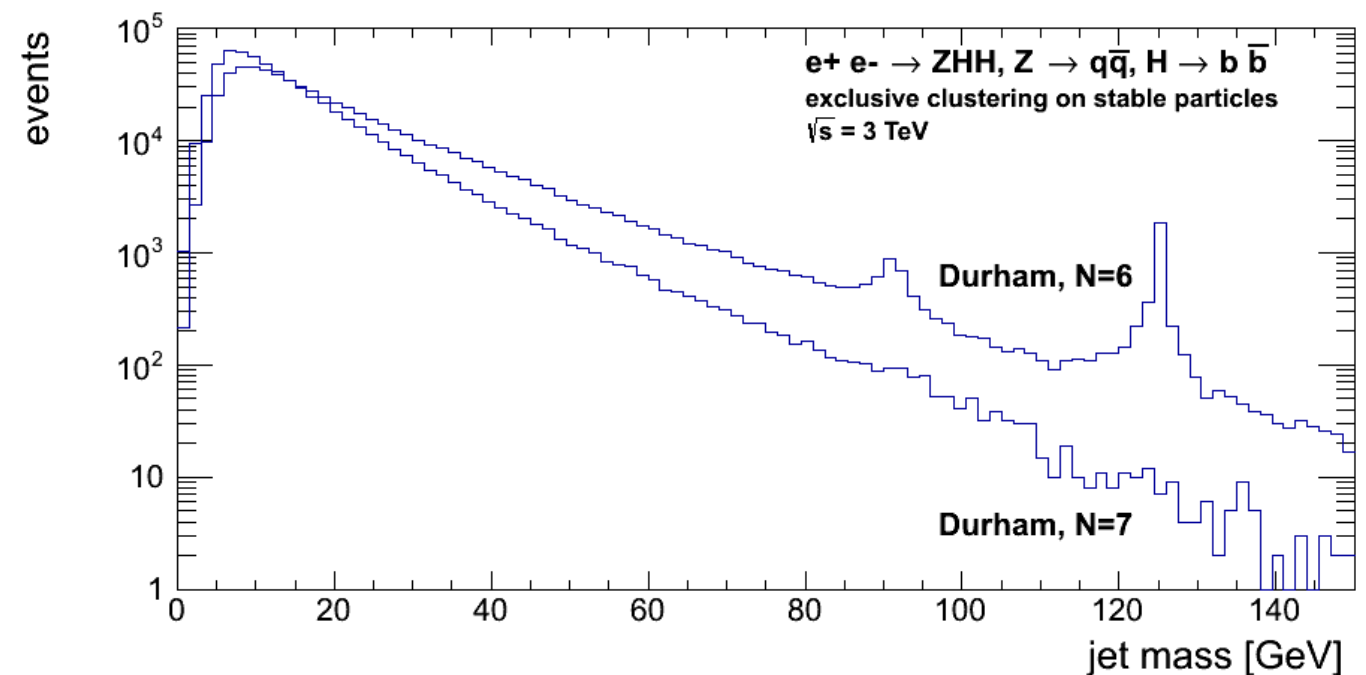
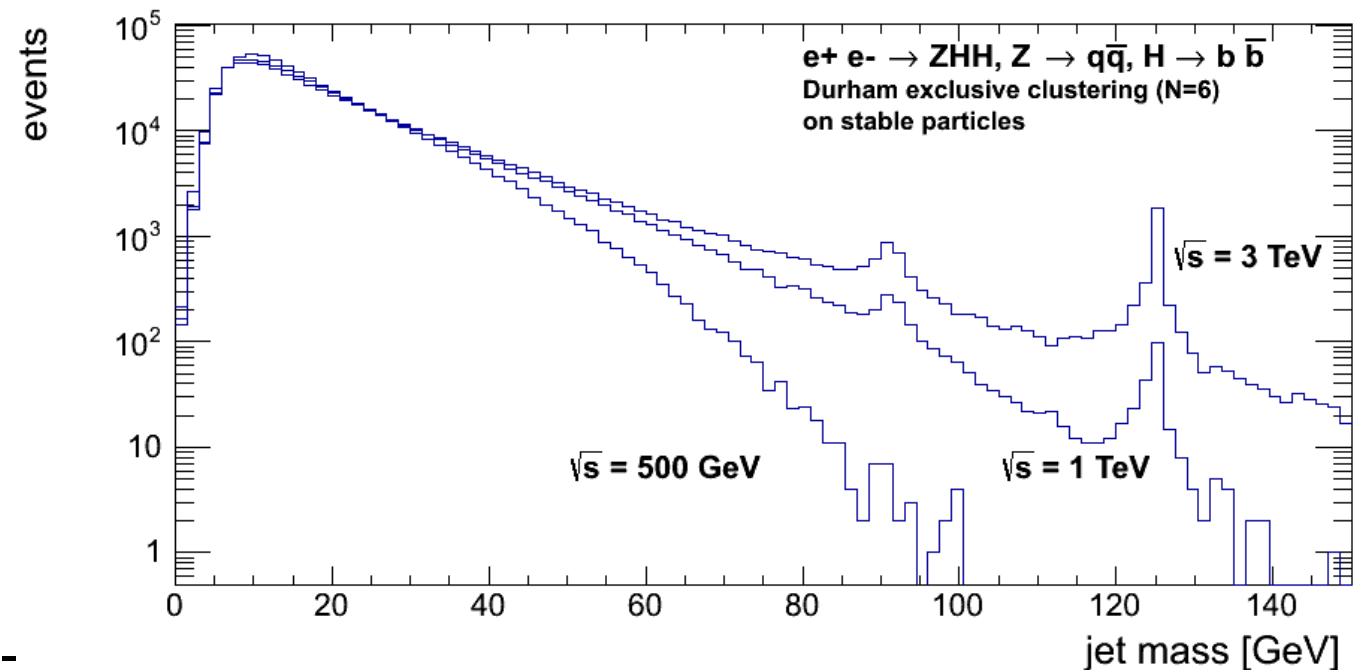
$Z \rightarrow q\bar{q}$  or  $H \rightarrow b\bar{b}$  erroneously merged

Failure mode is indeed observed in a small fraction (few %) of events at high energy (1-3 TeV)

Ironed out by allowing a seventh split (N=7).

Merge using extra information

N=3 not very satisfactory at relevant energy



# Inclusive vs. exclusive

Exclusive: user specifies # jets or max. distance where clustering stops.

- Vast majority of lepton collider analyses

Inclusive: cluster until  $d_{iB} > d_{ij}$  for all pseudo-jets

- Probably 100% of hadron collider analyses

Exclusive jet clustering is very powerful and versatile.

FastJet WARNING: `dcut` and exclusive jets for jet-finders other than `kt` should be interpreted with care.

Exclusive clustering cannot be used (in a meaningful way) with jet algorithms with null or negative energy exponent (Cambridge-Aachen, anti- $k_t$ )

# Jet Energy Scale and Resolution

LHC: dominant detector-related uncertainty in nearly all analyses

(even if an analysis doesn't “use” jets, it suffers from jet-related uncertainties)

- Fragmentation, parton shower, hadronic shower model and dead material lead to large uncertainty in response
- JES constrained to approx 1% in  $\gamma$  + jet or Z + jet events; additional systematic for difference wrt calibration sample (response differences between quark and gluon jets, dense/less dense environment, extrapolation to different energy range, pile-up)

LC: very good Particle Flow

Even the best PF cannot do much about neutrinos in jets (b/c-quark JES)

We need numbers for the difference in response for gluon and quark jets,  
for 2-jet versus 4-jet versus 6-jet versus 8-jet events

LC: excellent in situ handles (Z-pole run (without background)  $Z \rightarrow q\bar{q}$ )

(response differences between quark and gluon jets, dense/less dense environment, extrapolation to different energy range, background)

Realistic energy uncertainty for ILC analyses:

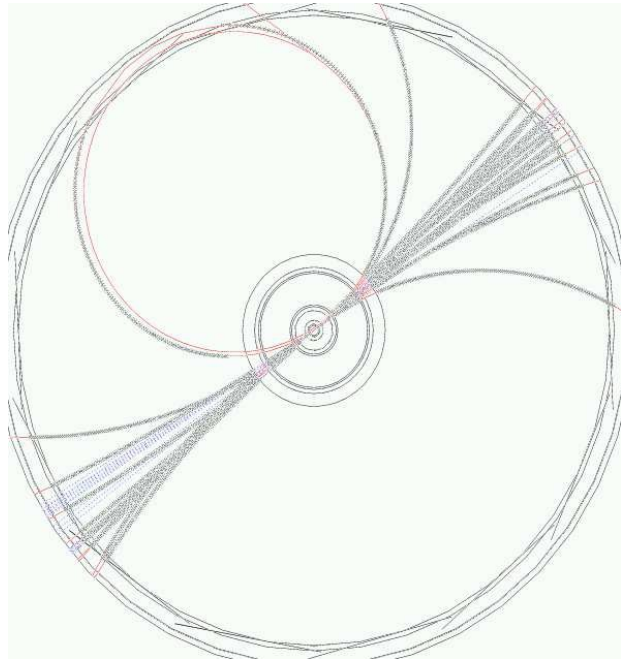
- can we define a one-uncertainty-fits-all-analyses number?
- is it 0.1%, 1%...? (any guess is better than assuming 0%; a newly formed team will provide realistic numbers )

For now, I'd recommend to simply run a simple check:

document how a 0.1%, 0.3%, 1% error in JES affect your result

(you should probably be cautious if you find a 0.001% JES uncertainty ruins the result)

# Boosted objects

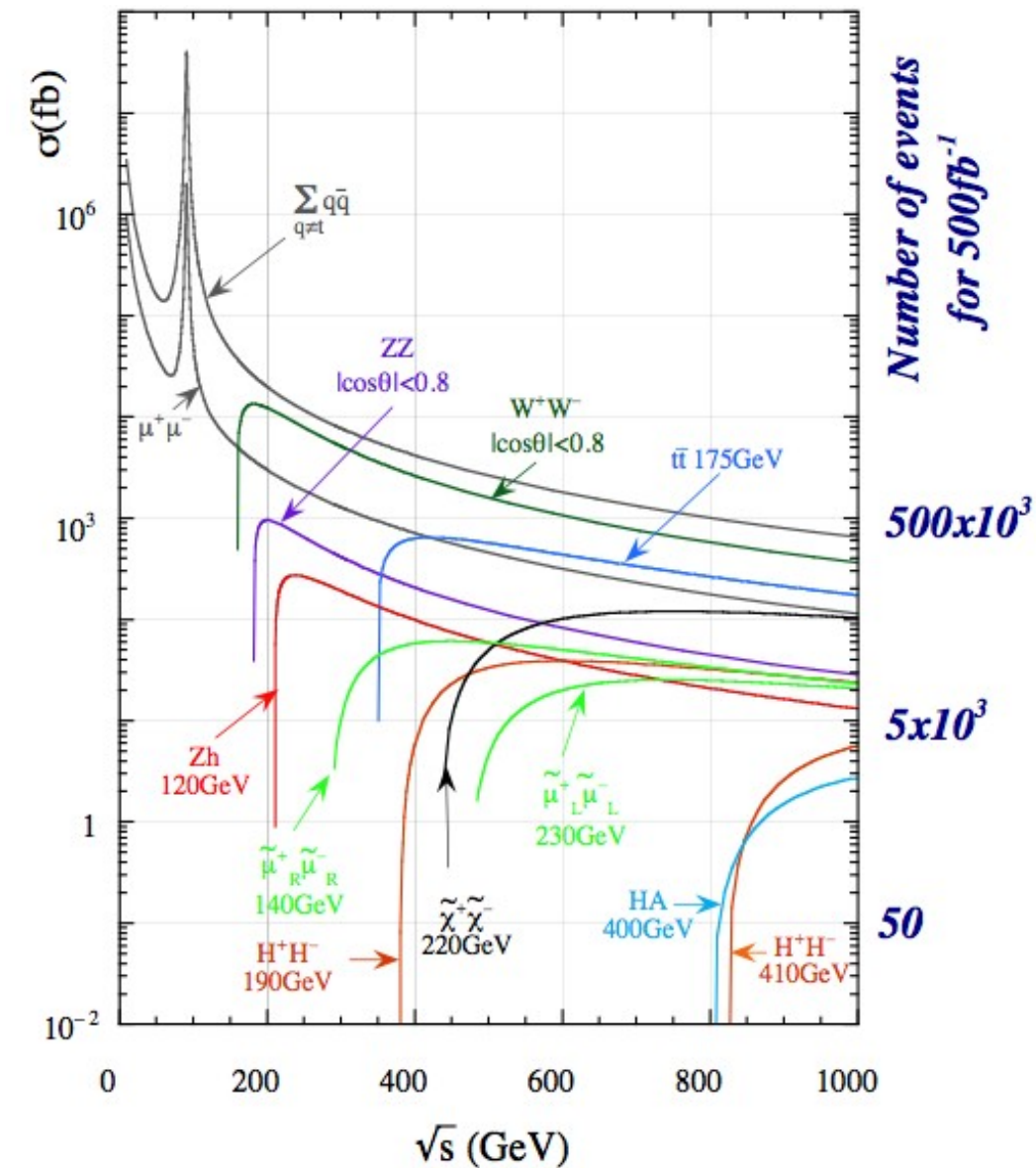
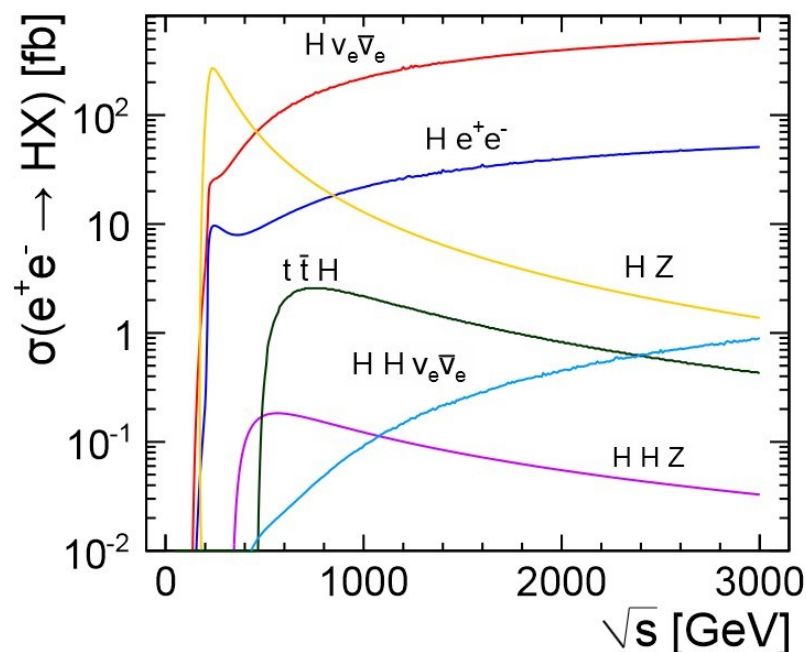


All objects (known so far) will be boosted in ILC upgrade (1 TeV)  
And even more so during the CLIC high-energy stage (1.4, 3 TeV)

## The role of boosted object tagging

In the continuum above  $\sqrt{s} \gg m_Z$  the  $e^+e^- \rightarrow q\bar{q}$  rate is of the same order as WW production, only one order of magnitude larger than  $t\bar{t}$  production, and two orders above ZZ and Zh

Relative to the LHC the role of boosted object tagging shifts from the “battle against QCD multi-jet production” to the more subtle art of separating W, Z, Higgs and top

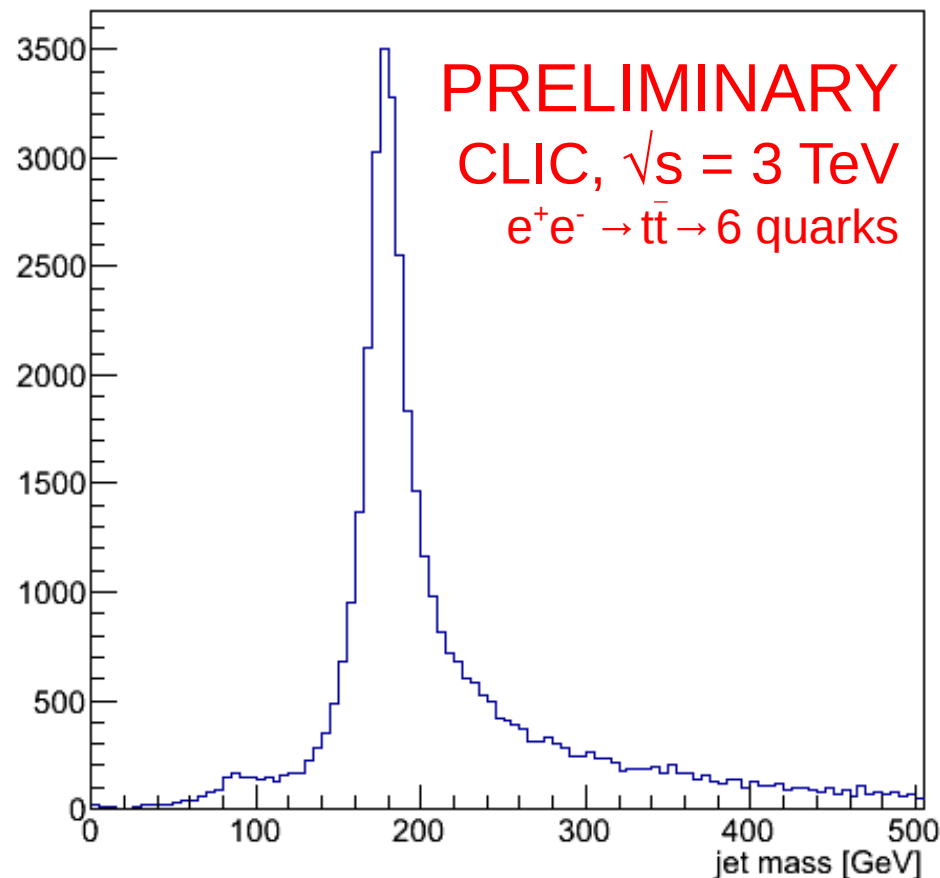


Tag ZZ against WW  
HHZ against WWZ



# Boosted top quarks

Without  $\gamma\gamma \rightarrow$  hadrons background



## Detector performance for boosted hadronic top jets ( $E \sim 1200$ GeV)

- Energy resolution (RMS90) = 2.4%
- Jet mass resolution (RMS90) = 3.2% (WOW!)

Good selling point for ultra-granular calorimetry!

CLIC 3 TeV  $e^+e^- \rightarrow t\bar{t}$

No background

CLIC-ILD detector simulation

PANDORA PFA

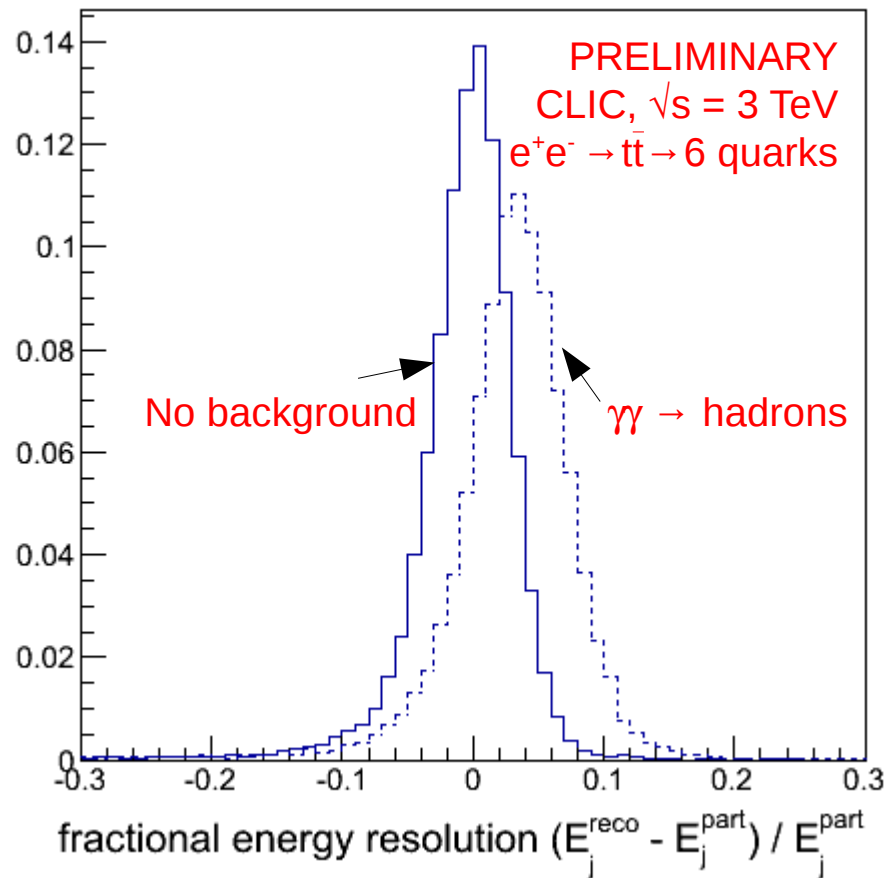
Valencia  $e^+e^-$  jet algorithm ( $N_j = 2$ ,  $R = 1$ ,  $\beta = 1$ )

Could have picked long. inv.  $k_t$  with  $R = 0.8-1.2$

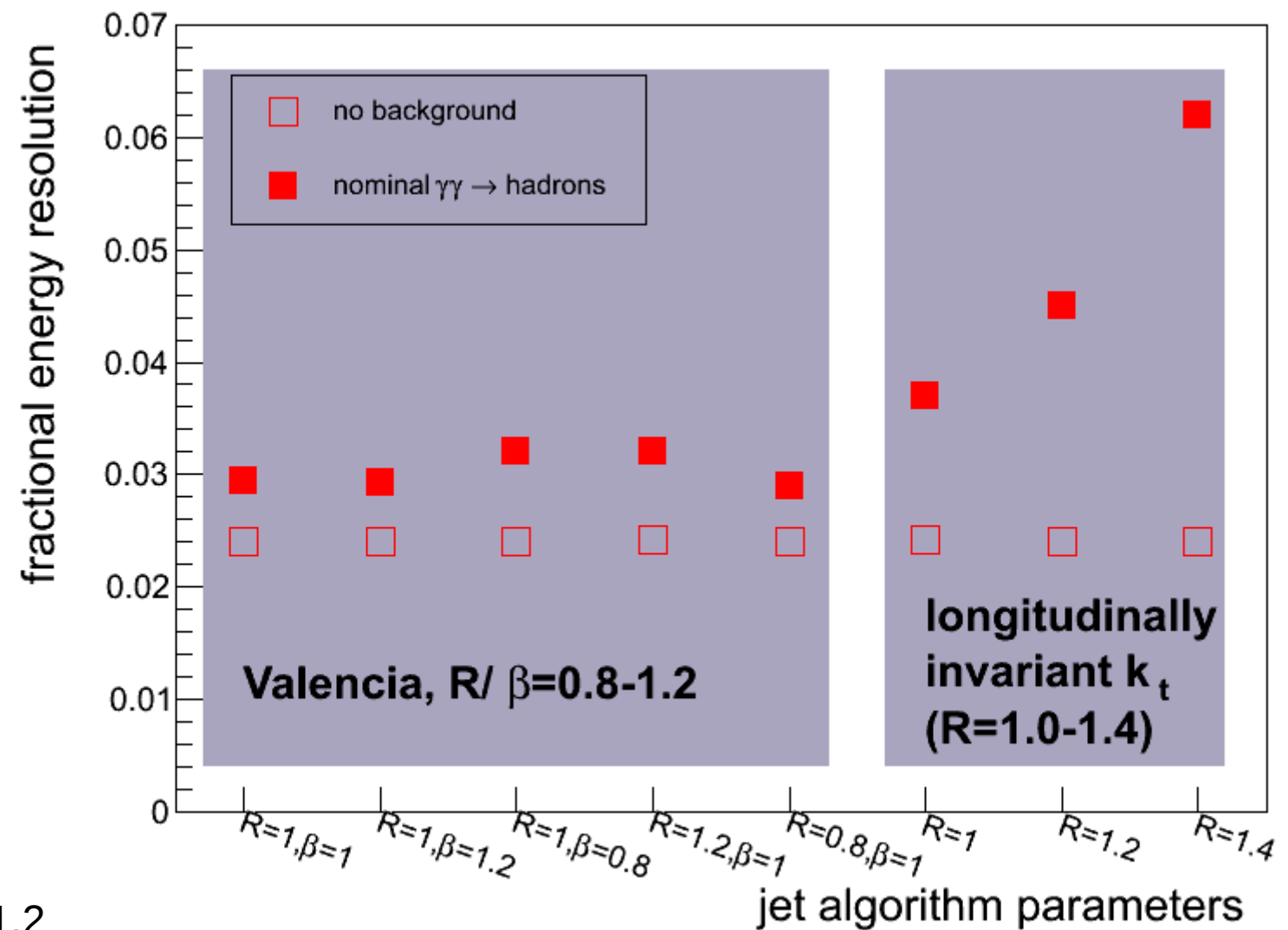
Note: resolution considers reconstructed energy versus stable particle jets; relative to the actual top parton the energy resolution is 5% and the width of the mass peak  $\sim 7\%$

# Boosted top quarks

With  $\gamma\gamma \rightarrow \text{hadrons}$  background



**Background has impact on fat jets:**  
Energy resolution degraded 2.4%  $\rightarrow$  2.9%



CLIC 3 TeV  $e^+e^- \rightarrow t\bar{t}$

Adding  $\gamma\gamma \rightarrow \text{hadrons}$  background

CLIC-ILD detector simulation

PANDORA PFA

Valencia  $e^+e^-$  jet algorithm ( $N_j=2$ ,  $R=1$ ,  $\beta=1.2$ )

Significantly better now than long. inv.  $k_t$  with  $R=0.8-1.2$



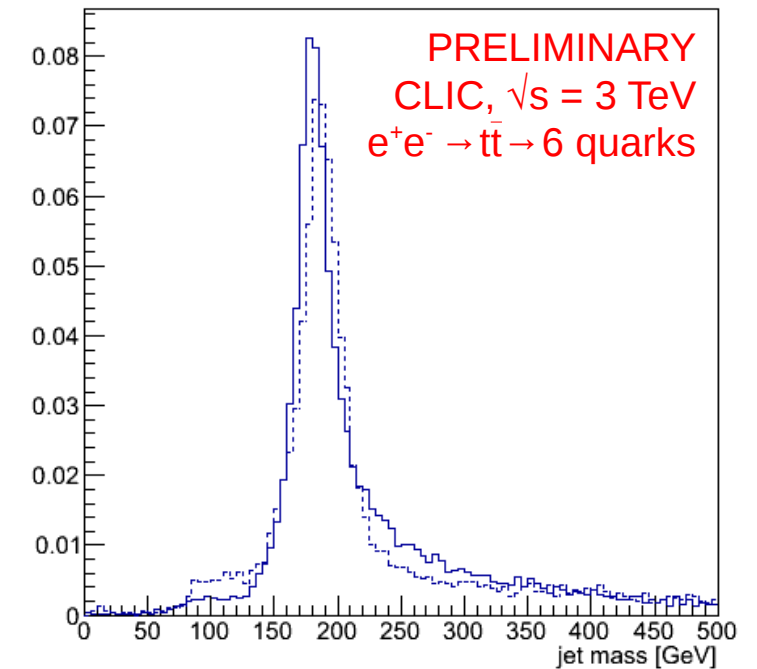
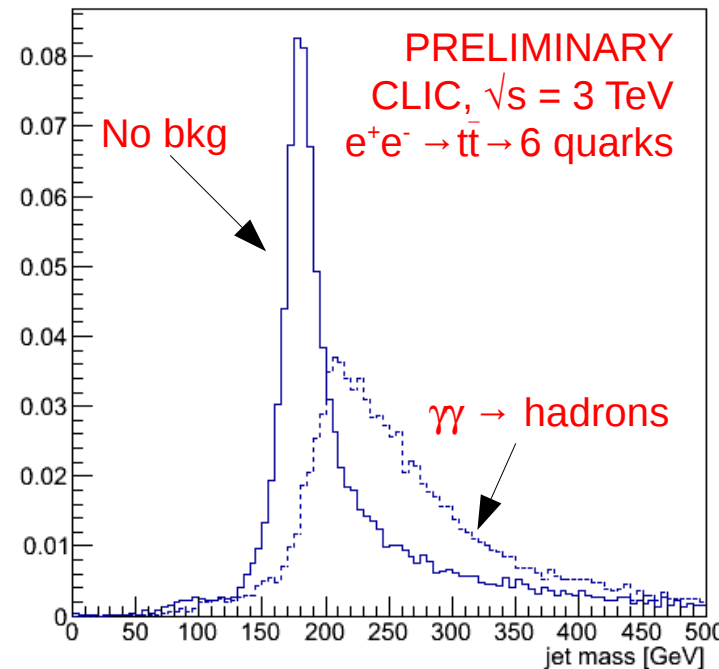
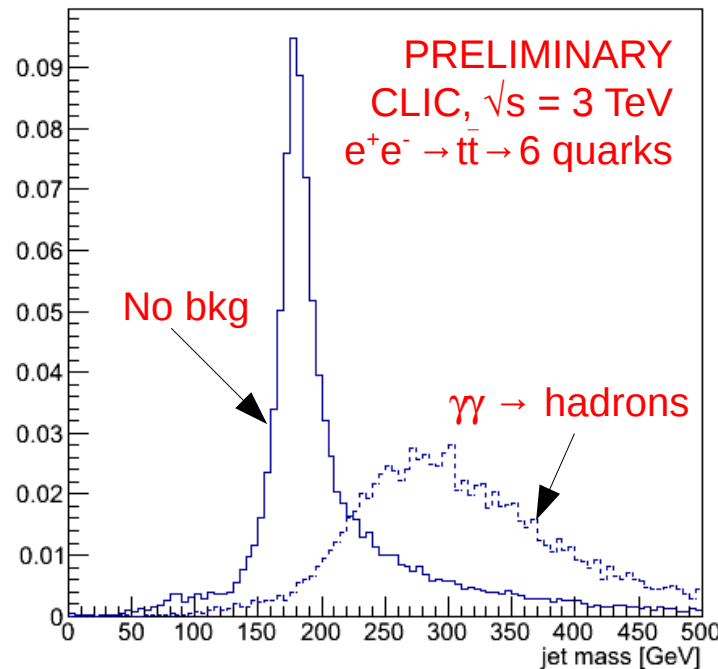
# Boosted top quarks

With  $\gamma\gamma \rightarrow$  hadrons background

Longitudinally invariant  $k_t$  ( $R=1$ )

Valencia ( $R=1, \beta=1$ )

Valencia trimming



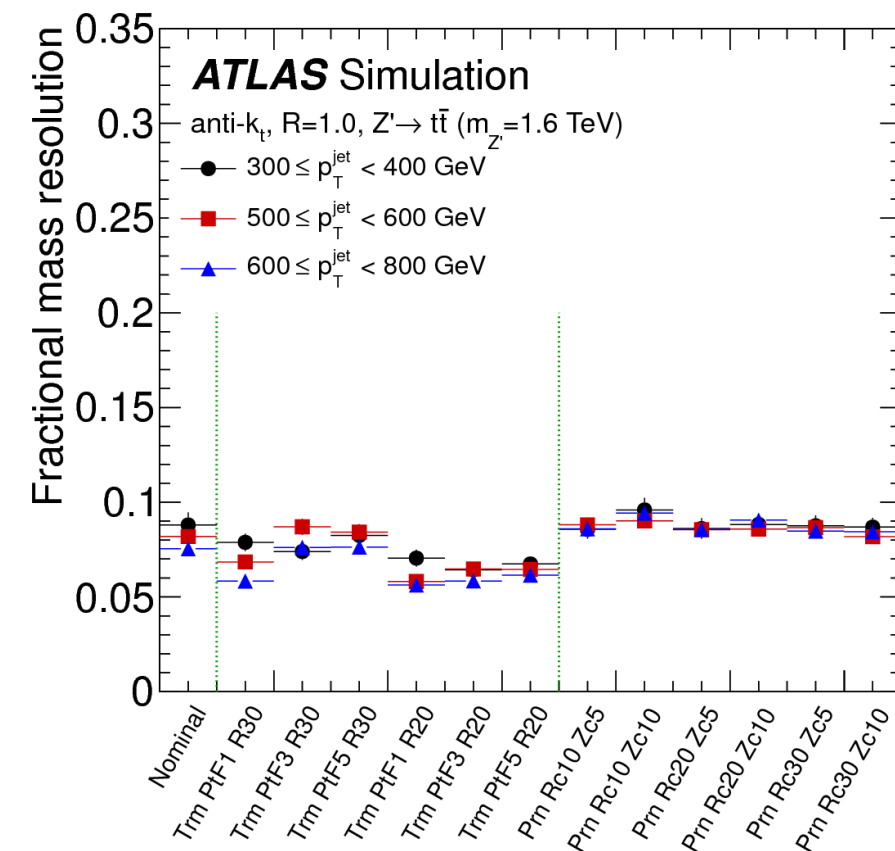
**Background has a profound impact on fat jet substructure:**

Raw jet mass resolution badly degraded

(from dream 3.2% to nightmare 16%)

Preliminary: grooming jets restores jet mass resolution to ~4%

Results correspond to a primitive  $e^+e^-$  variant of trimming based on 3+3 Valencia  $R=0.2$  jets → optimisation needed



# Summary

Particle flow detector concepts exist that measure stable particles very precisely:

$\Delta E/E \sim 3\%$  (weighted for relative abundance of particle species in jets)

Jet clustering is far from trivial in many-jet final states and with background overlay

- perturbative corrections
- non-perturbative (hadronization) corrections
- confusion due to multi-jet final states
- $\gamma\gamma \rightarrow$  hadrons background

LC is qualitatively different from LEP/SLC: a fresh look at  $e^+e^-$  jet reconstruction is needed

- Back to basic: understand what you optimize
- Isolate and quantify the impact on performance of above effects
  - a mild boost helps to sharpen the algorithm-related jet energy resolution
- Adapt new tools from the LHC: groomed jets may yield better performance

Jet-related systematics are important

- evaluate sensitivity of key analyses while we come up with estimates

Every EW-scale particle is a boosted object in a high energy (1-3 TeV) linear  $e^+e^-$  collider

Distinguish di-boson from  $q\bar{q}$  production AND separate W, Z and Higgs

Highly granular particle flow calorimetry is great for substructure response

Background is a powerful enemy of fat jet substructure

Preliminary results indicate adapting existing tools (grooming) for pile-up mitigation is effective

