



HIGGS SELF COUPLING ANALYSIS USING THE EVENTS CONTAINING $H \rightarrow WW^*$ DECAY

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INTRODUCTION

- Measuring the Higgs self coupling is the key point to prove the electroweak symmetry breaking mechanism

- Higgs potential in SM:

$$V = \lambda v^2 H^2 + \lambda v H^3 + \frac{1}{4} \lambda H^4$$

Mass term

Trilinear coupling

Quartic coupling

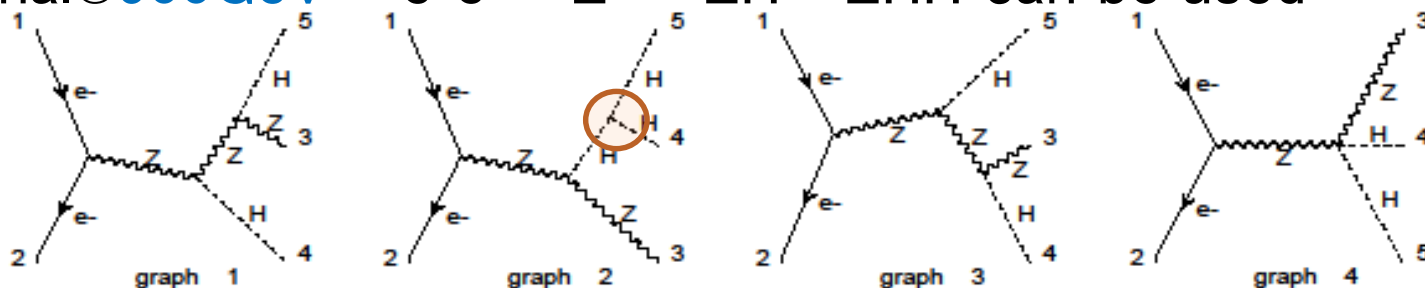
→ difficult to measure

SM: $\lambda = \frac{m_H^2}{2v^2} \quad v \sim 246 \text{ GeV}$

- Observing two Higgs bosons in the event is the only way to measure the self coupling
- Accurate test of the coupling may lead to the extended nature of Higgs sector → may go to new physics
- Our goal is to observe and measure the Higgs self coupling first

SIGNAL EVENTS

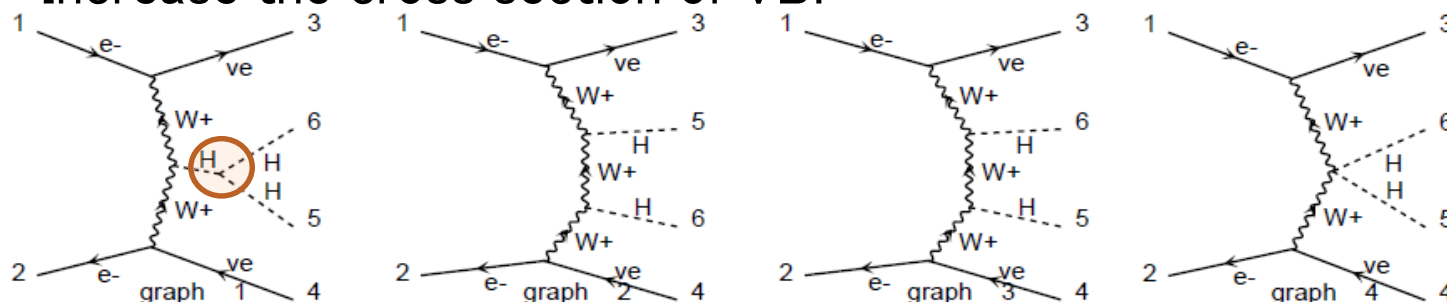
Signal@500GeV – $e^+e^- \rightarrow Z^* \rightarrow ZH \rightarrow ZHH$ can be used



Signal: 2 Irreducible B.G.: 1, 3, 4

Signal@1TeV – VBF $e^+e^- \rightarrow \nu \nu HH$ channel is opened

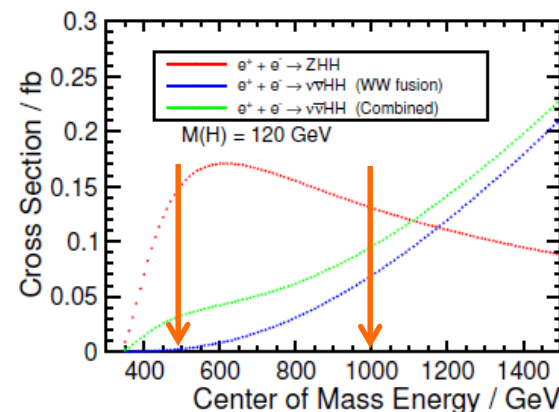
- Increase the cross section of VBF



Signal:1 Irreducible B.G.: 2, 3, 4

Higgs decay modes:

- $HH \rightarrow (bb)(bb)$: golden channel thanks to b-tag
- $HH \rightarrow (bb)(WW)$: improve the final result



COMPONENTS FOR BETTER RESULTS

- Basic components for better sensitivity
 - **Lepton ID**: Isolated leptons can be identified well, and **very good fake suppression**
 - many idea have been introduced
 - **B-tagging**: better b-tagging algorithm provides better background suppression
 - **Jet pairing**: good jet pairing can obtain good kinematic variables, which leads to good background suppression
 - **Good energy & momentum resolution**: of course, but limited by the detector performance
 - particle ID will be the key to energy correction
 - **Jet clustering**: jet reconstruction is the key to the analysis, but it is difficult
- All the components are related each other

TRACK ENERGY CORRECTION

Track energies are corrected using momentum & mass

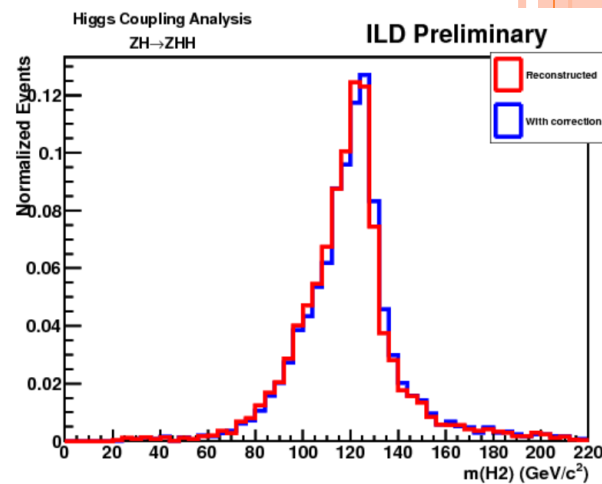
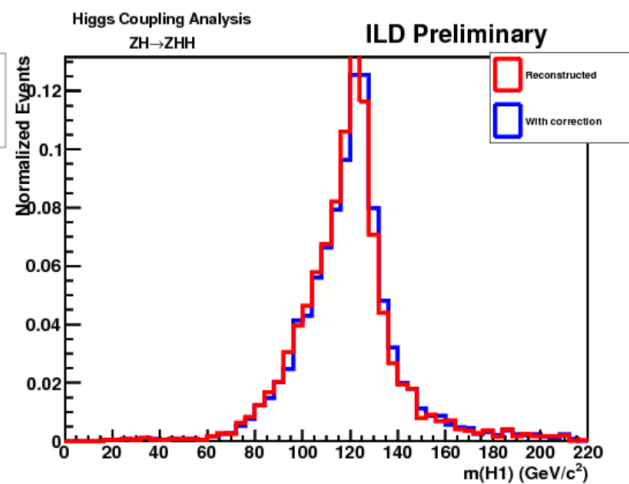
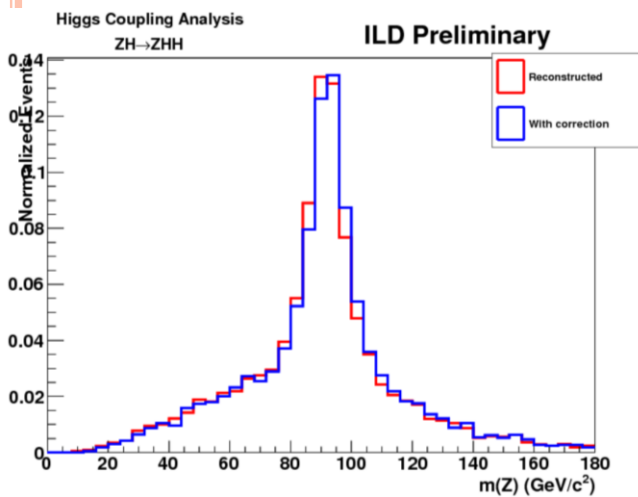
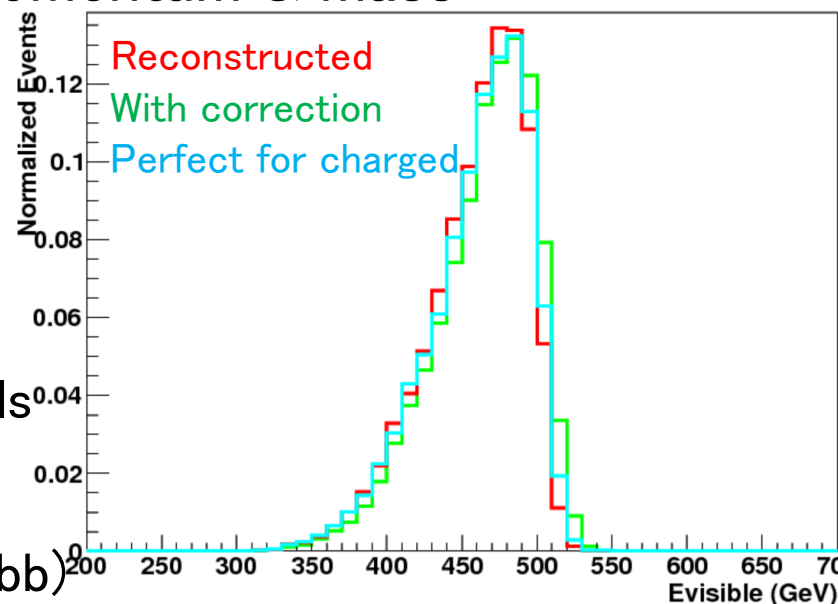
- Using **particle ID** to identify tracks

Visible energy

- Using $qqHH \rightarrow qq(bb)(bb)$
- So far, overestimated due to misID
- Correction effect is small due to neutrals

Mass distribution

- Checking $Z(Z \rightarrow qq, q \text{ is light})$ and $H(H \rightarrow bb)$
- Jet matching with MC truth is applied
- Effect is small too due to neutrals



JET PAIRING USING BAYESIAN APPROACH

- Bayesian probability – posterior probability when x is given

$$P(A|x) = \frac{P(x|A) \cdot P(A)}{P(x)}$$

$P(x|A)$: likelihood(probability when x is given from class A)

$P(A)$: prior probability of class A

$P(x)$: probability of variable x (sum of all the classes' p.d.f.)

- Bayesian classifier – regard x as the element of class A ,

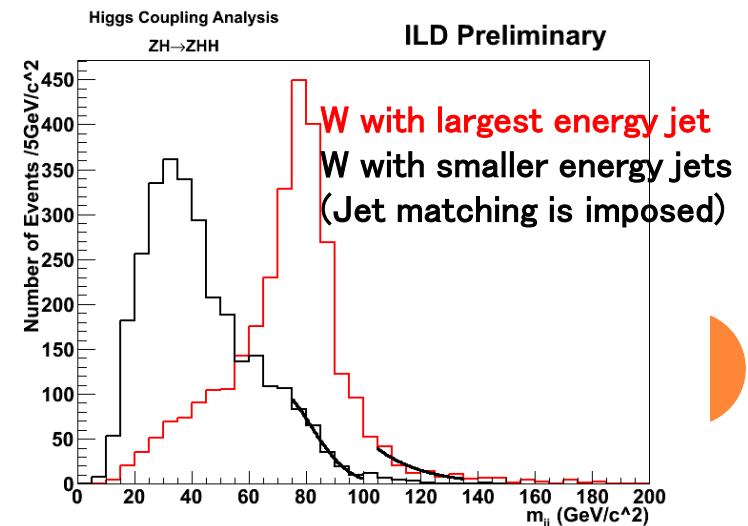
- When $P(A|x)$ is largest of all the classes
 - e.g. x belongs to A when $P(A|x) > P(B|x)$, $P(A|x) > P(C|x)$, etc.

- Likelihood – introduce angle information

- In $WW^* \rightarrow jjjj$ case, combination

is **3**

- Jet with large energy tends to come from **on-shell** W



PRELIMINARY RESULTS & PROBLEM

- WW→jjjj pairing case
 - Also check maximum likelihood using LDA
 - $\chi^2 = -2\log BW(m(j1j2)|m_W, \Gamma_W)$

Pairing type	χ^2	Just likelihood	Naïve Bayes
True positive(%)	60.2	70.1	74.7

- Good improvement can be obtained!

Looks hopeful, but...

- ZH→(bb)(bb) case

- $$\chi^2 = \frac{(m_1 - m_Z)^2}{\sigma_Z^2} + \frac{(m_2 - m_H)^2}{\sigma_H^2}$$

Pairing type	χ^2	Just likelihood	Naïve Bayes
True positive(%)	56.6	59.8	59.8

- Improve slightly thanks to the angle information
- But, need more improvement...
 - No improvement even if using naïve Bayes...

- Can we get better result?

TRYING KINEMATIC FITTER

- Determining the kinematics globally in the events
 - Distort the event kinematics to meet the constraint in specific process
 - Estimate how much is a event likely to the specific process?
 - Mass resolution will be improved by using χ^2 minimization

- First trial: $ZHH \rightarrow (bb)(bb)(WW^*) \rightarrow (bb)(bb)(l\nu jj)$ kinematic fitter

- Constraints:

$$m(bb) = m_Z$$

$$\text{Max}(m(l\nu), m(jj)) = m_W$$

$$m(bb) = m(l\nu jj)$$

$$E(H) + E(Z) + E(jj) + E(l\nu) = \sqrt{s}$$

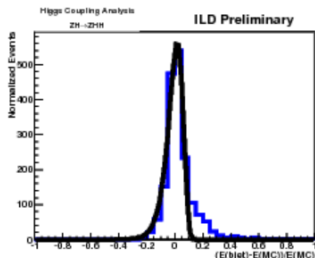
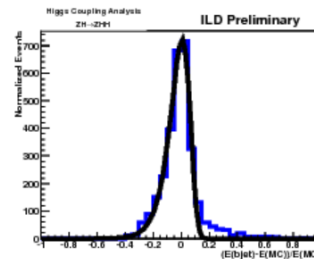
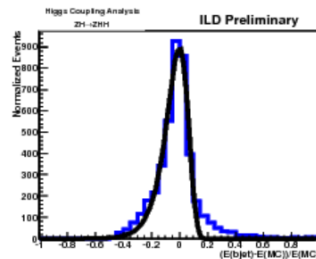
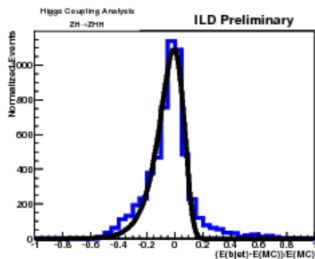
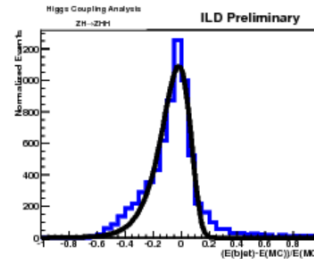
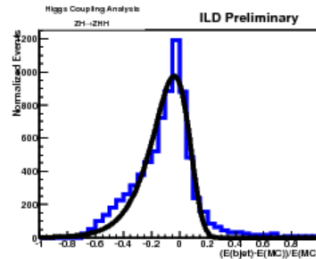
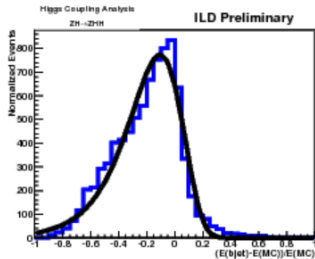
$$\vec{p}_H + \vec{p}_Z + \vec{p}_{jj} + \vec{p}_{l\nu} = \vec{0}$$

JET ENERGY RESOLUTION

- Most critical factor which degrades mass resolution is jet energy resolution

- So it is necessary to include this effect into Kinematic fitter
- Jet energy resolution has energy dependence of jets

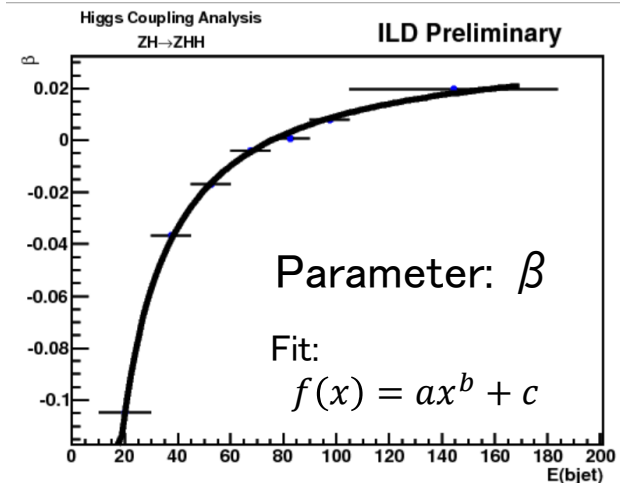
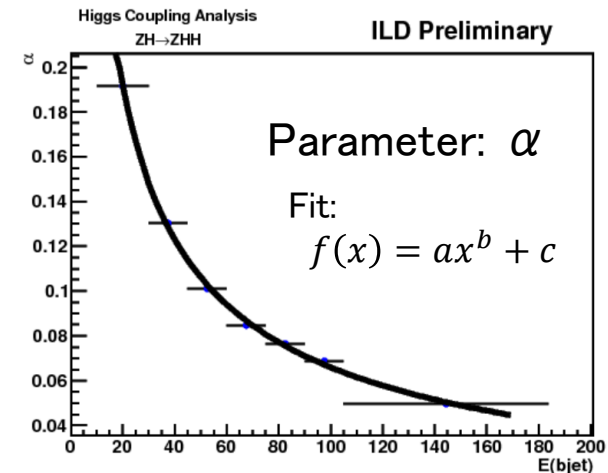
- Parameterize fit parameters with jet energy



Fit: Gumbel dist.

$$f(x) = \frac{1}{\beta} \exp\left(\frac{x - \alpha}{\beta}\right) \exp(-\exp(\frac{x - \alpha}{\beta}))$$

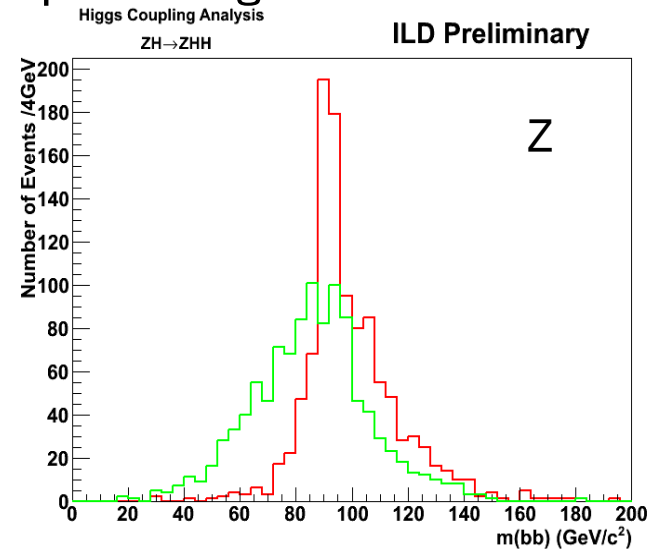
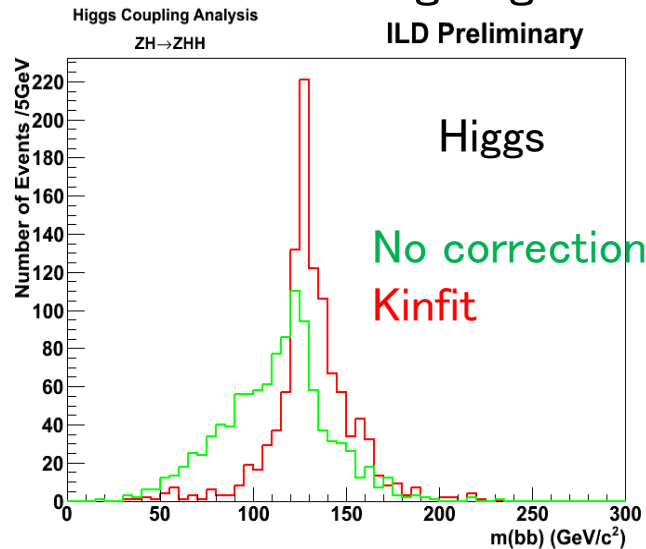
To include asymmetric energy resolution



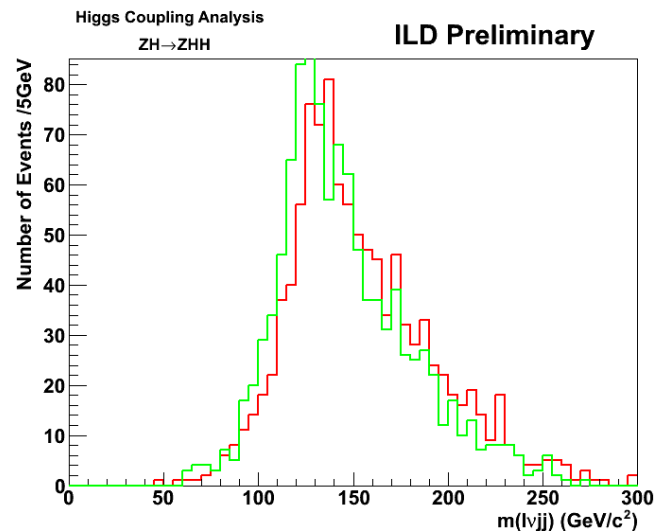
PERFORMANCE CHECK

- Higgs mass($H \rightarrow b\bar{b}$) & Z mass distribution

- Mass resolution is going better! → promising



- Higgs($H \rightarrow WW^* \rightarrow l \nu jj$)
 - No resolution improvement...
→ under investigation

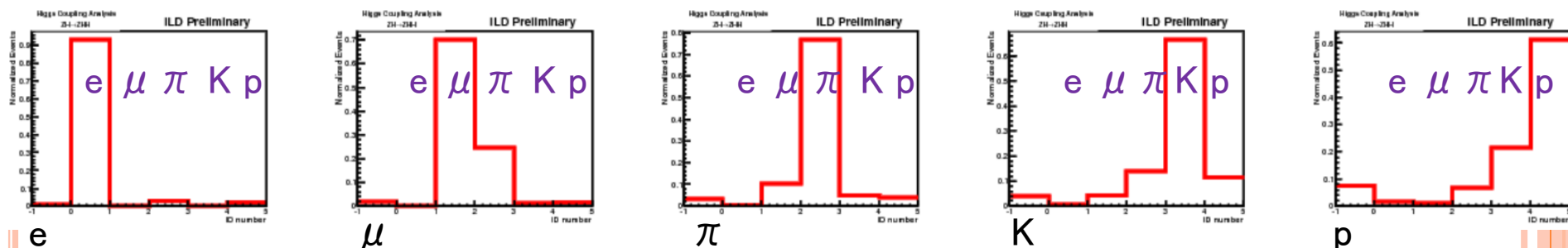


POSSIBILITY OF FLAVOR TAGGING IMPROVEMENT

- For flavor tagging improvement
 - Vertex mass is the key to separate heavy/light flavor vertex
 - Many π^0 s will escape from B/D vertex \rightarrow checked that using MC truth
 - Mass resolution will be degrade due to escaping neutrals
 - Is there possibility to recover π^0 s which escape from vertices?
- Building π^0 finder – many components are necessary
 - Gamma finder – using shower profile in calorimeters
 - π^0 finder – solving gamma pairing
 - Vertex finder – which vertex is the π^0 coming?
- Find vertex of π^0 s:
 - Very difficult to identify vertex – depends on detector configuration
 - Making the best of decay kinematics
 - Using TMVA to find π^0 candidates from the vertex
 - Details: my talks@software/simulation session(Thursday)

A CLUE FOR FLAVOR TAGGING IMPROVEMENT

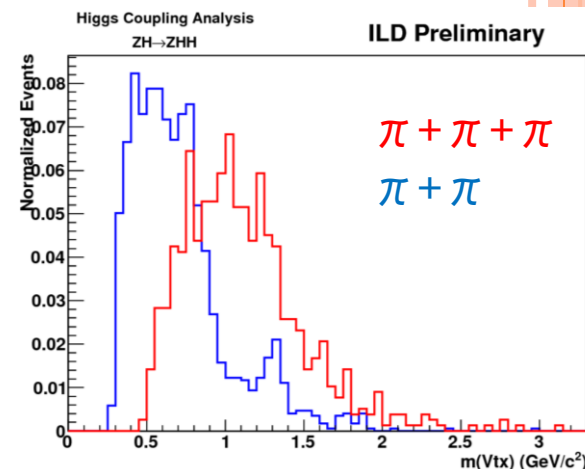
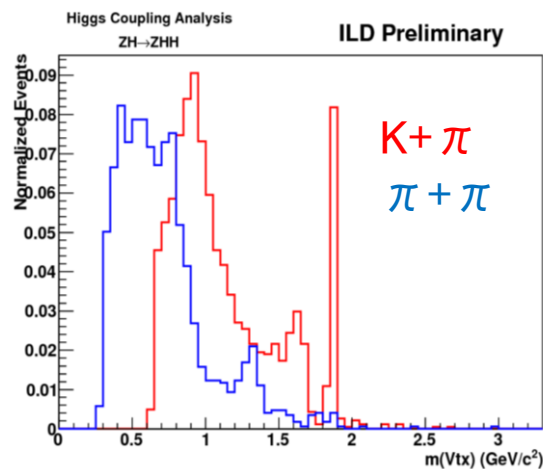
- We have **Particle ID!** – it is the key
 - Using TPC dE/dx and shower profile in calorimeters
 - ID efficiency using Particle ID



- From PID – Different vertex patterns have different **vertex mass patterns**

- examples

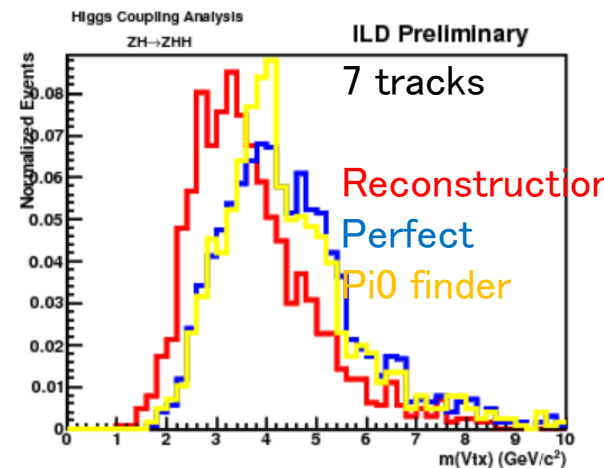
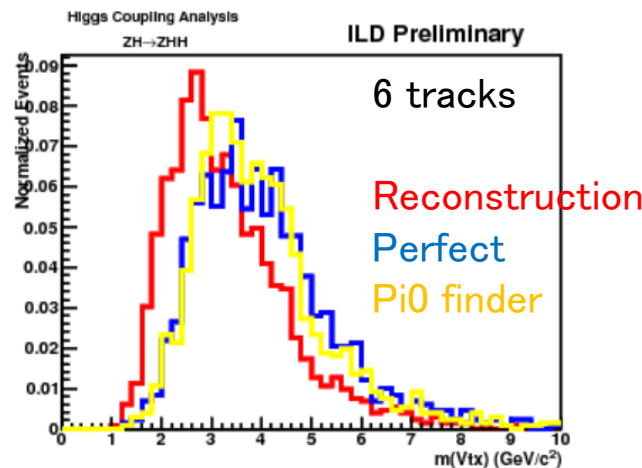
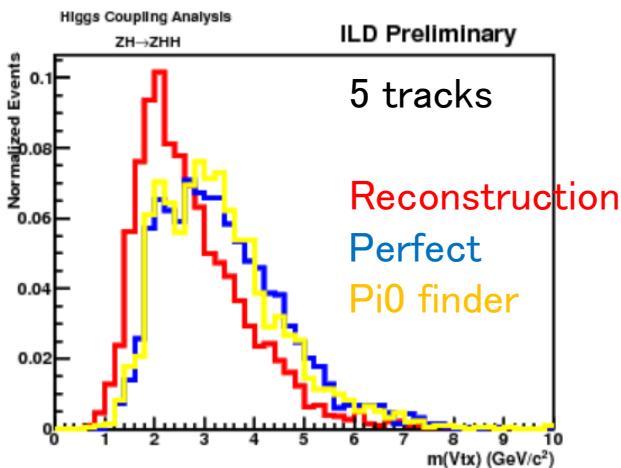
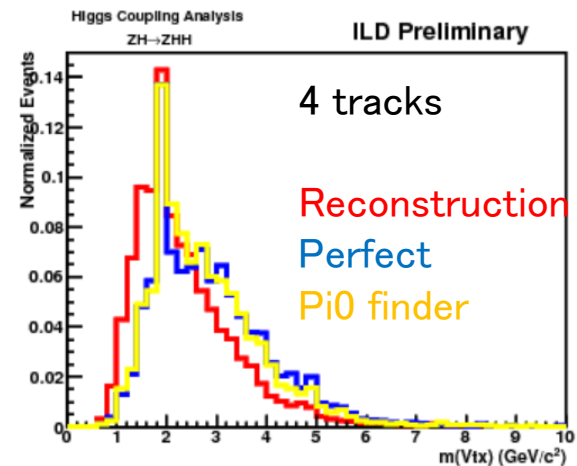
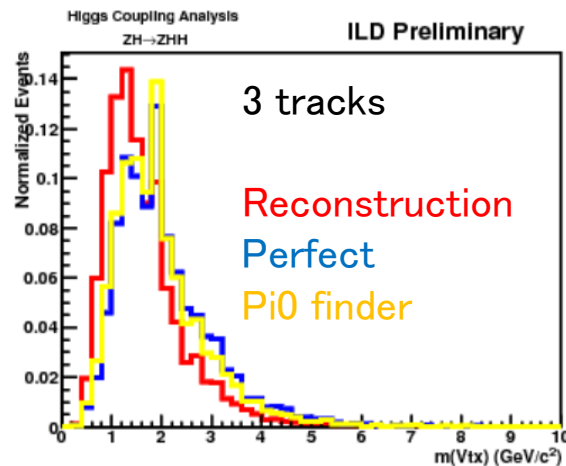
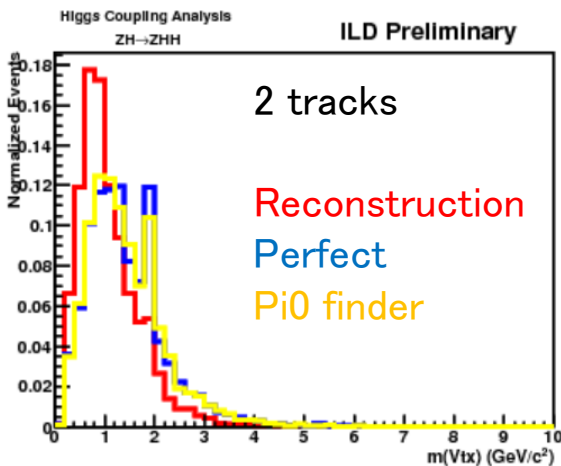
- 1) $K + \pi$ vs. $\pi + \pi$
- 2) $\pi + \pi$ vs. $\pi + \pi + \pi$



- Can good and general classifier(MVA) to separate **pi0s from vertices** and **pi0s from IP** be constructed?

Vtx MASS RECOVERY USING π^0 VERTEX FINDER

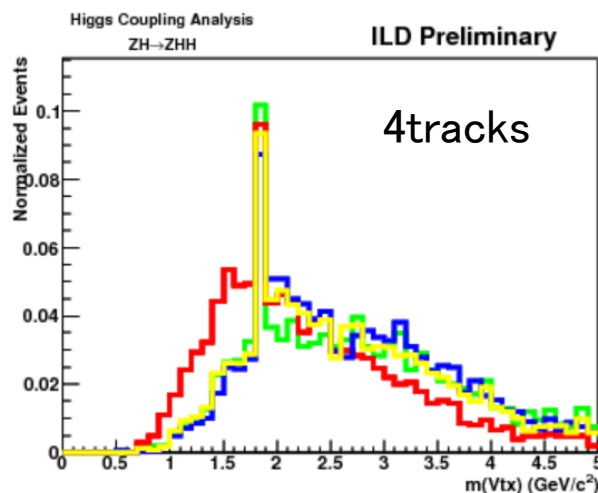
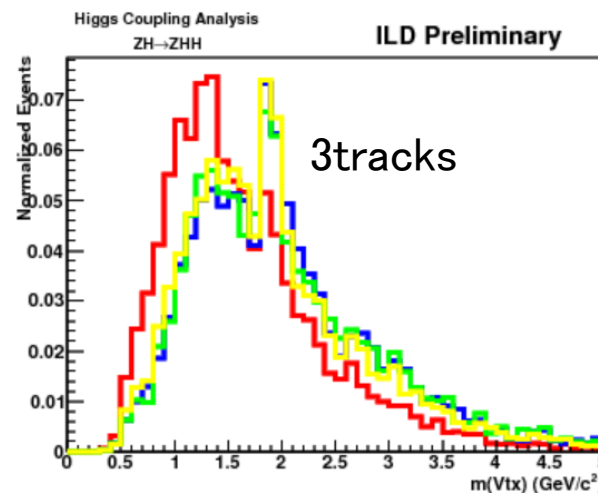
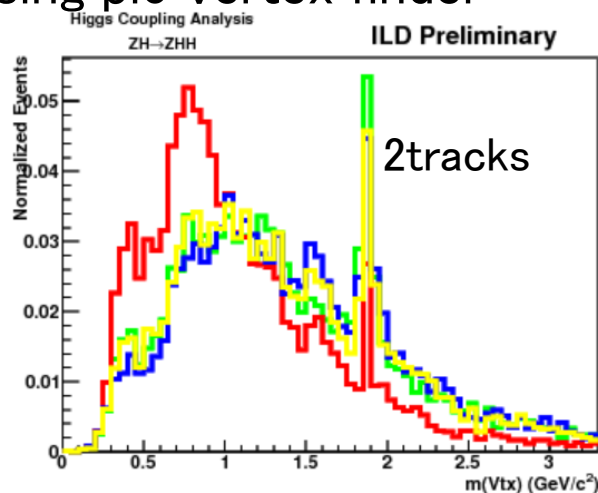
- Vtx mass distributions for each vertex pattern(ntrk)
 - When a jet has 1 vertex(secondary) inside itself
 - Gamma pairing is perfect within π^0 reconstruction capacity



MOST REALISTIC SITUATION

- Pi0 is reconstructed from PFO gamma candidates

- Using gamma finder
- Using pi0 reconstruction
- Using pi0 vertex finder



Reconstruction

Pairing & pi0 attachment perfect

Pairing perfect

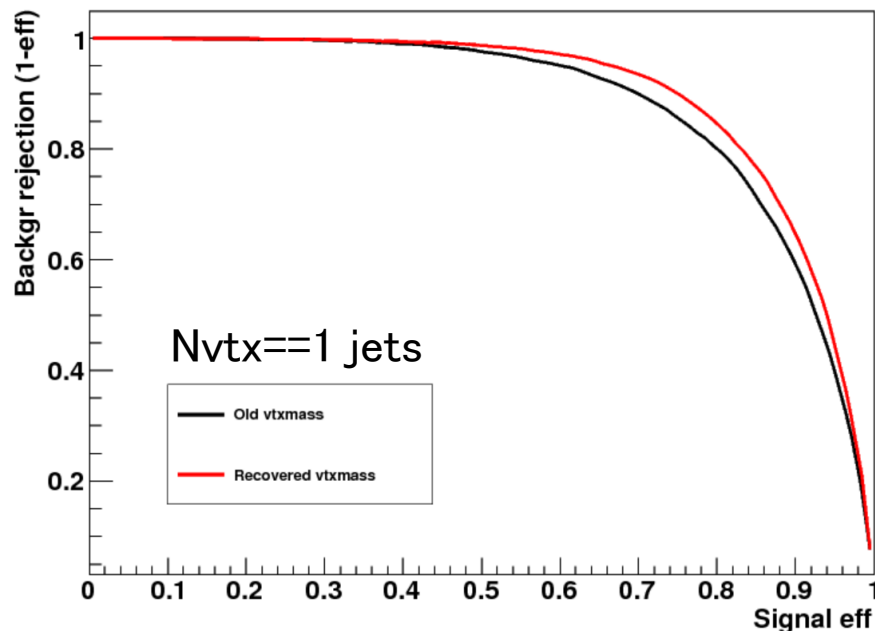
Realistic situation

VERTEX MASS RECOVERY EFFECT ON FLAVOR TAGGING

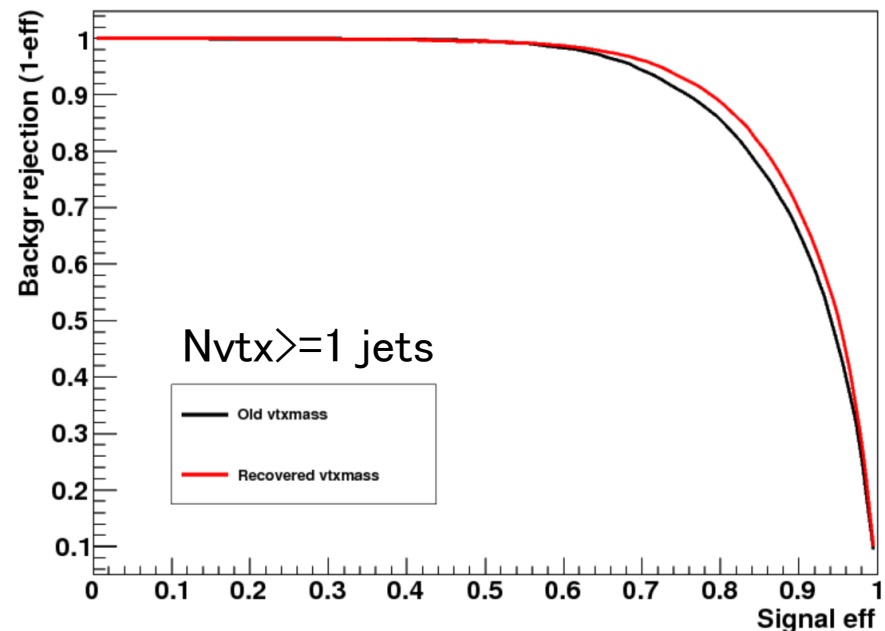
○ Construct a “toy” flavor tagger

- Variables are obtained from LCFIPlus
- Input variable selection is too primitive!
- Only vertex mass is replaced to recovered vertex mass
- Compare with ROC curve

MVA_BDTG_flavortagger_bcseparation



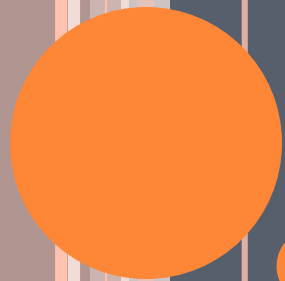
MVA_BDTG_flavortagger_bcseparation



○ For more precise study, need to step into LCFIPlus

SUMMARY AND PLAN

- Higgs self coupling analysis using the events with $H \rightarrow WW^*$ is ongoing.
 - Improvement of basic analysis components is necessary
 - Effect of track energy correction using particle ID is small, but going to good direction
 - Kinematic fitting will be a good tool for mass resolution improvement
 - There is hope for flavor tagging improvement!
- **Plan:**
 - Optimization of kinematic fitter & performance check of signal & backgrounds
 - Flavor tagging study inside LCFIPlus
 - Study of flavor tagging improvement in 0 vertex jet case
 - Finally, incorporate all the improvements and update the self-coupling result!



BACKUPS



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ANALYSIS STRATEGY FOR $HH \rightarrow (BB)(WW)$

○ Classify the events with Z and W decays:

@500GeV	$WW \rightarrow (qq)(qq)$	$WW \rightarrow (qq)(l \nu)$	@1TeV	$WW \rightarrow (qq)(qq)$	$WW \rightarrow (qq)(l \nu)$
$Z \rightarrow bb$	8jets	Lepton+6jets	$Z \rightarrow bb$	8jets	Lepton+6jets
$Z \rightarrow cc$	8jets	Lepton+6jets	$Z \rightarrow ll$	Dilepton+6jets	N/A
$Z \rightarrow ll$	Dilepton+6jets	Trilepton+4jets	$\nu \nu HH$	6jets (+missing)	N/A

○ Z decays into heavy flavor pair or lepton pair mainly

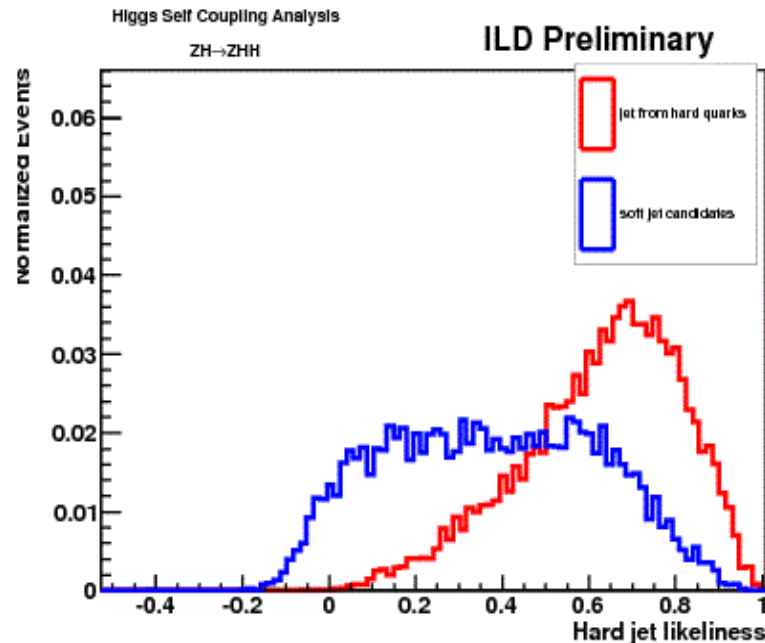
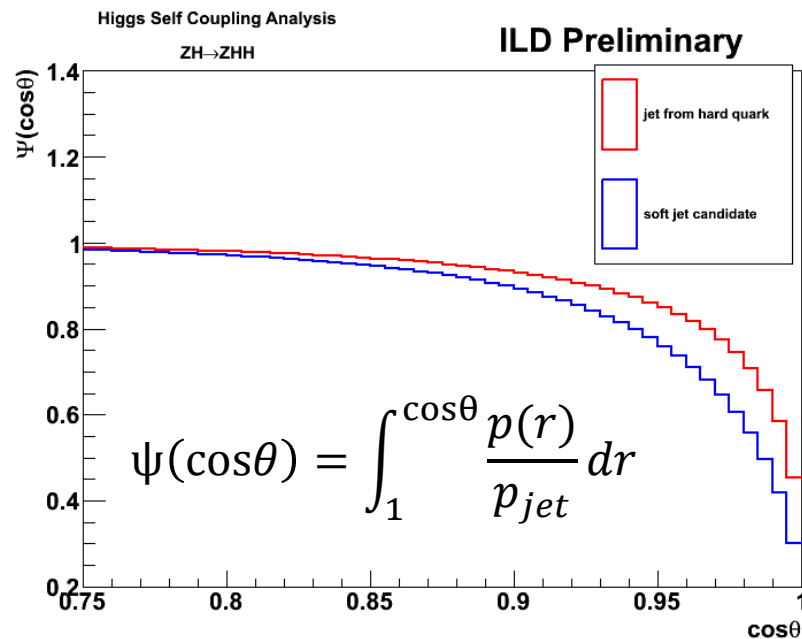
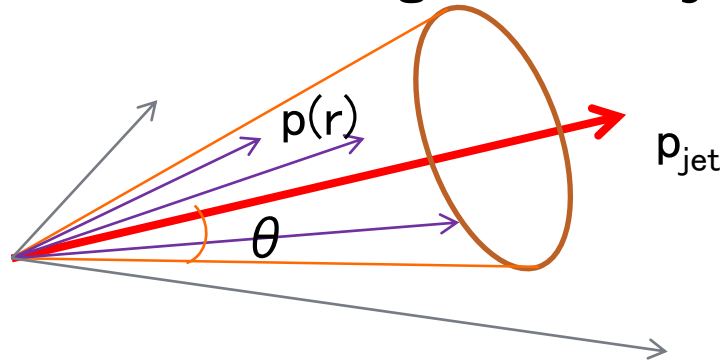
- Need flavor tagger or clean Z mass distribution to reject huge backgrounds

○ Number of b jet candidates in the event and number of leptons can form exclusive samples

- Number of b-tagging available: up to 4
 - Basically, 2 or 4 b-tagged jets events can be used
 - c-tagging is also available
- Number of leptons: from 0 to 3

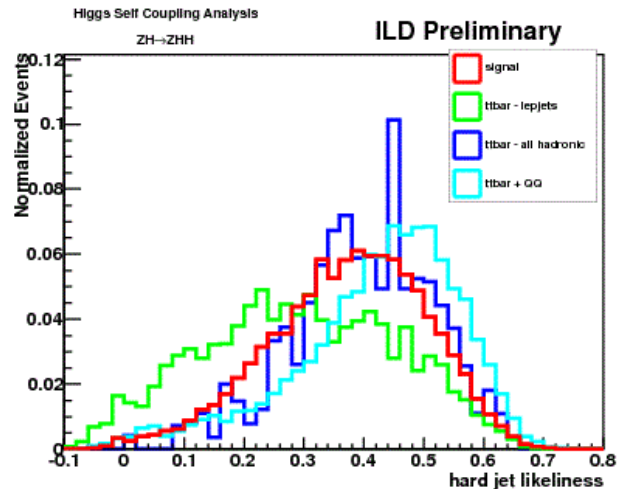
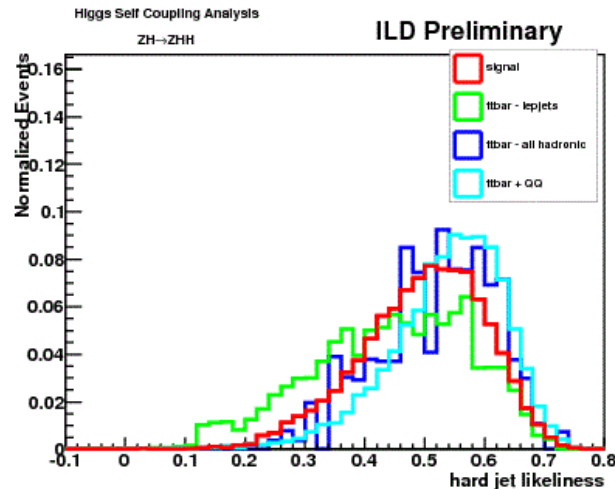
SOFT JET FINDING

- Tracks in the gluon jets spread wider than those in quark jets(e.g. analyses on hadron collider)
 - Traditional jet shape can be a good estimator
- Using Multivariate Analysis and estimating the hard jet likeliness for each jet

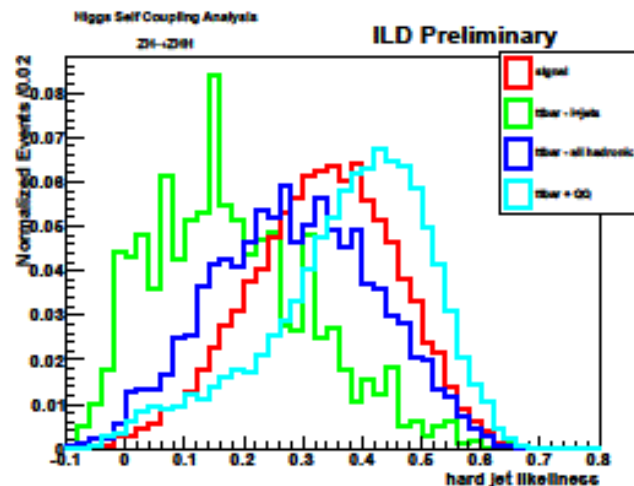
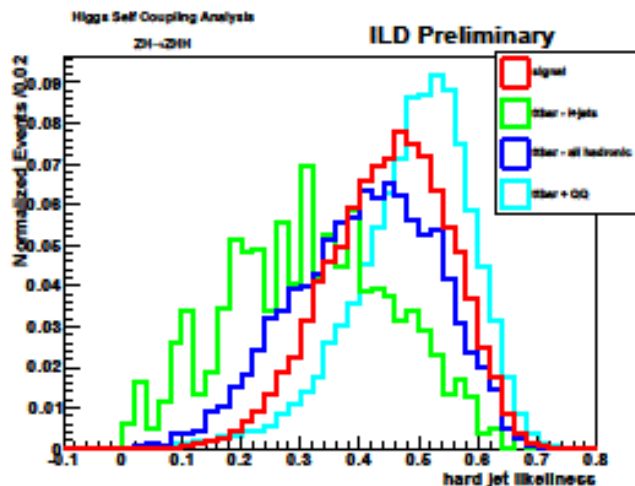


CHECK THE PERFORMANCE

- Check the jets with small hard jet likelihood – signal vs. $t\bar{t}$
- For 6jets



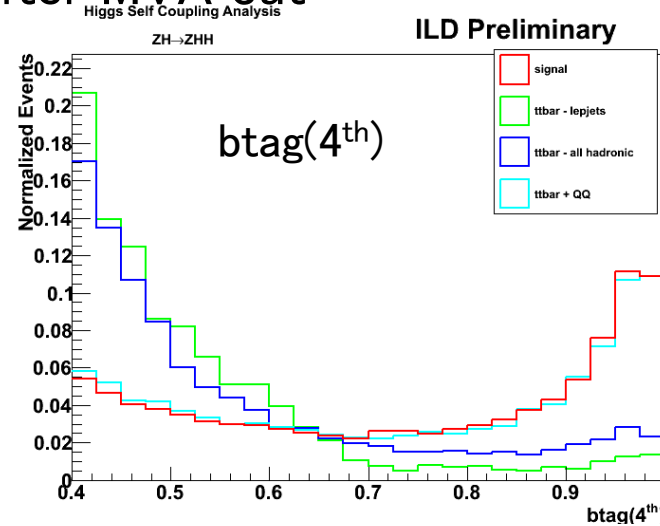
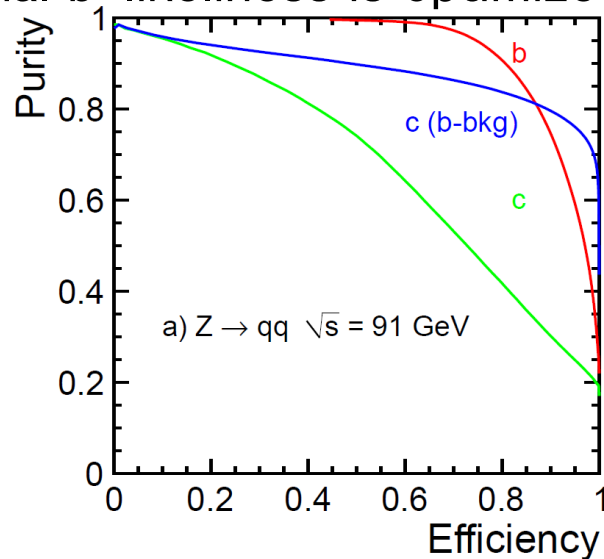
- For 8jets



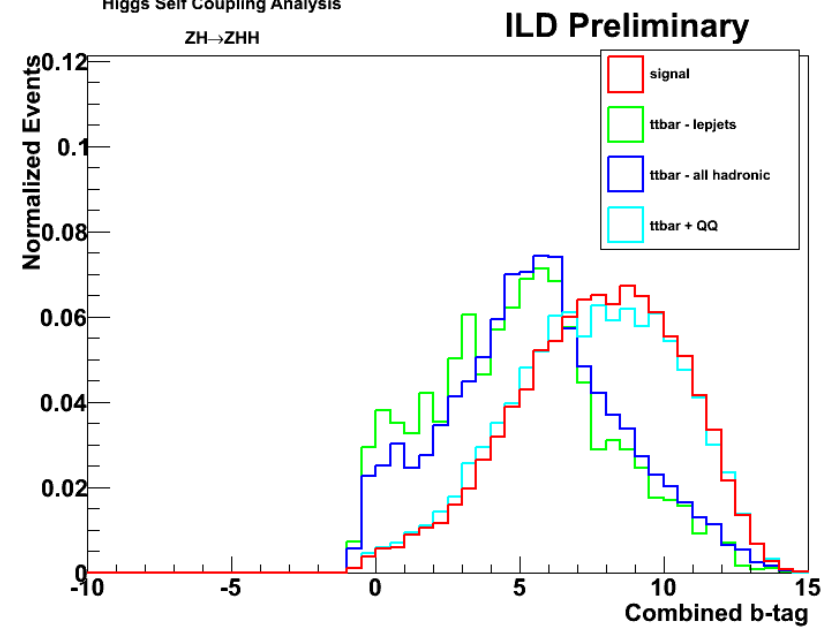
FLAVOR TAGGING

Using LCFIPlus

- b candidate is set >0.4
- Final b-likelihood is optimized after MVA cut



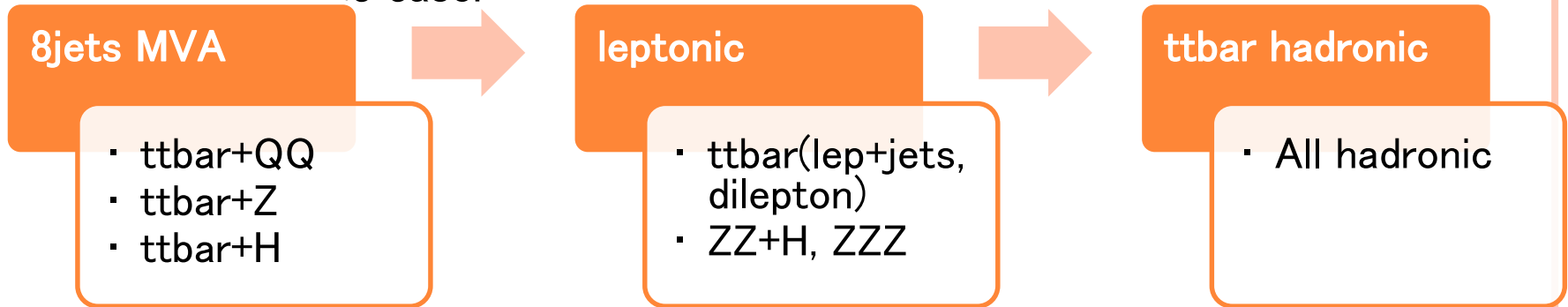
- Introduce combined b-tagging
 - After solving the jet pairing
 - $b(\text{Combined}) = \log\left(\frac{b_1 b_2}{(1-b_1)(1-b_2)}\right)$
 - Use as an input variable for MVA



BACKGROUND REJECTION

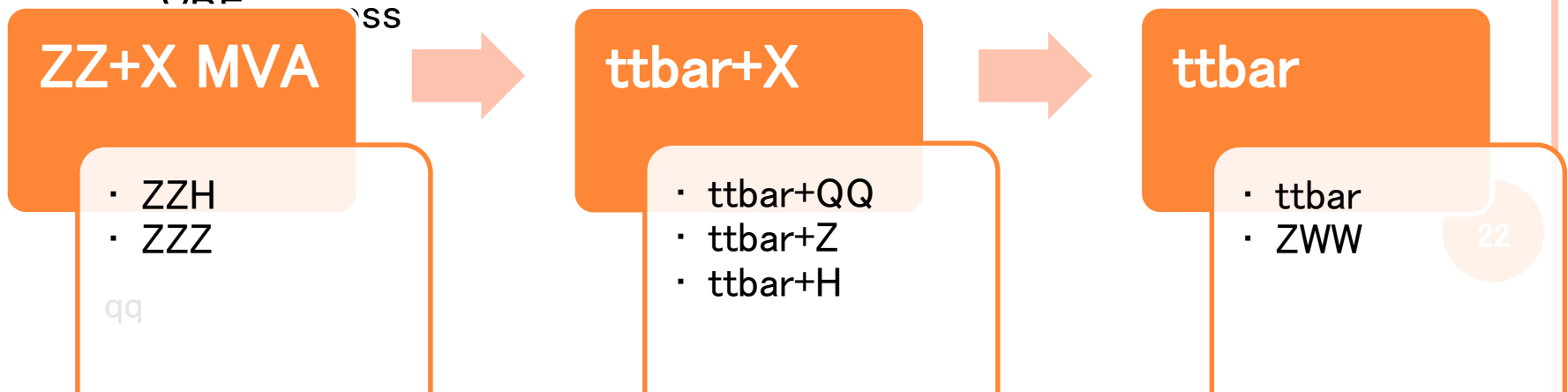
Multi Variate Analysis @500GeV

- Some cuts are implemented before MVA to tighten the input variable space – jet energy, χ^2 , visible energy, (Z mass)
- Background rejection strategy : rejecting small backgrounds first and then rejecting main background
 - Tighten the variable space when rejecting main backgrounds
- e.g. all hadronic case:



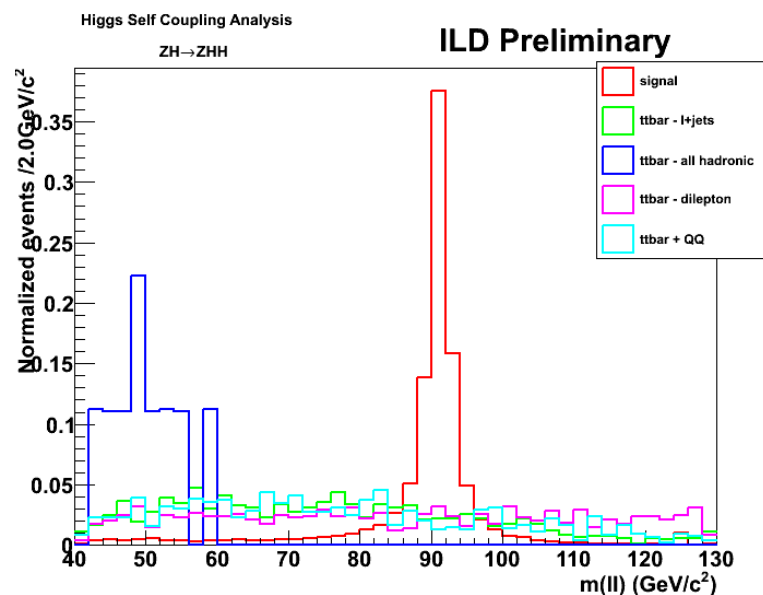
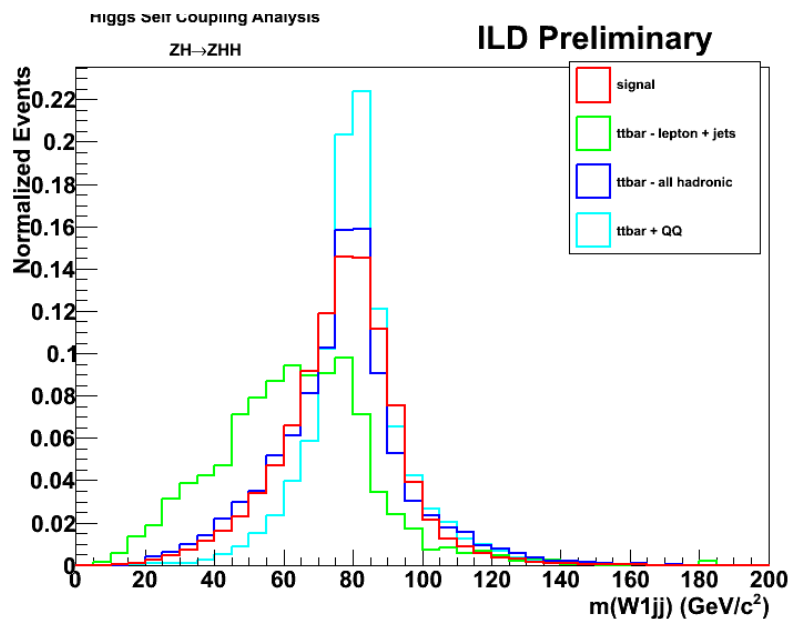
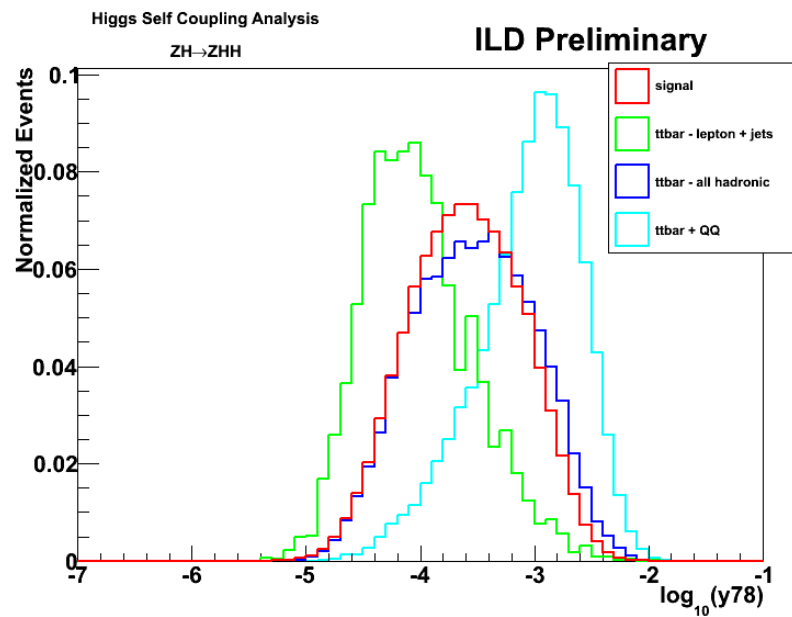
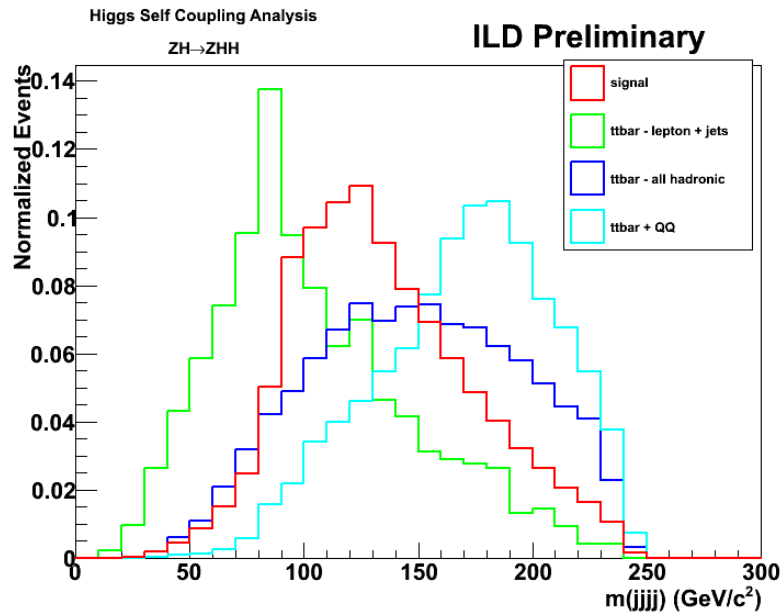
Multi Variate Analysis @1TeV

- Same strategy as the case of 500GeV



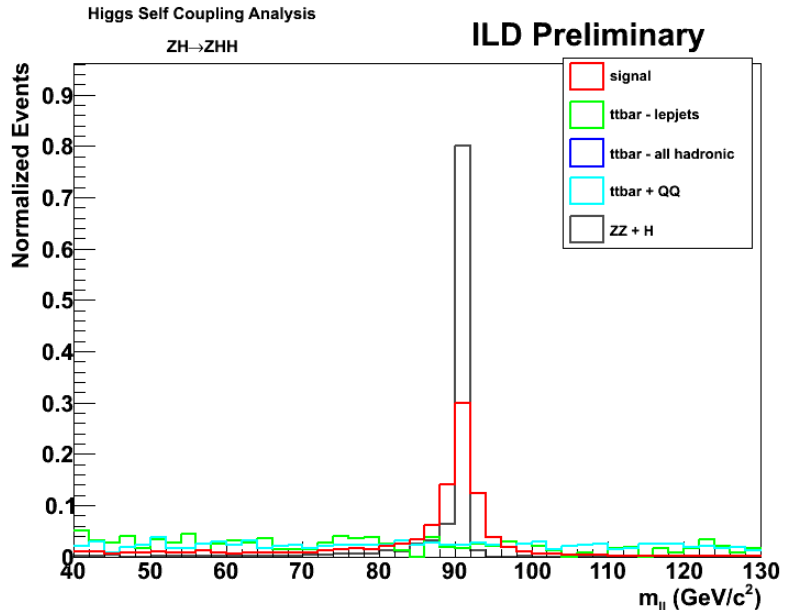
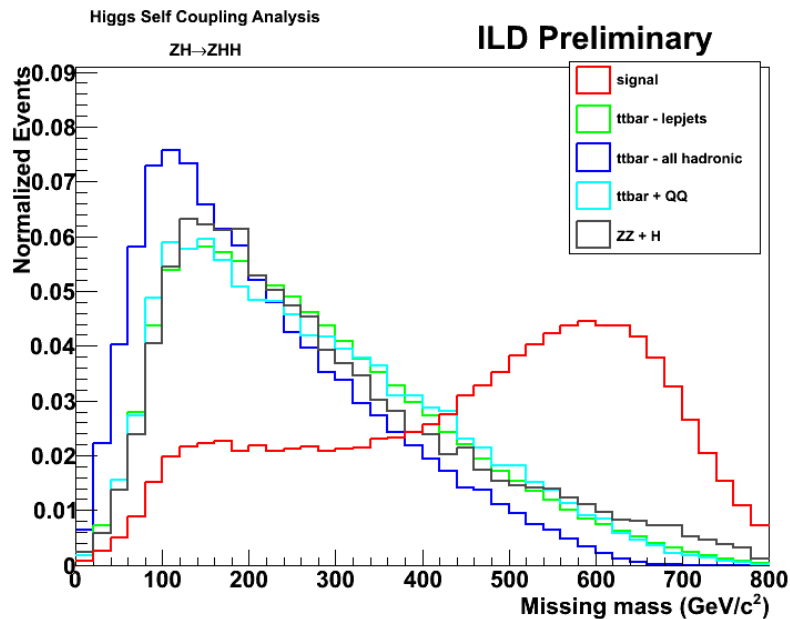
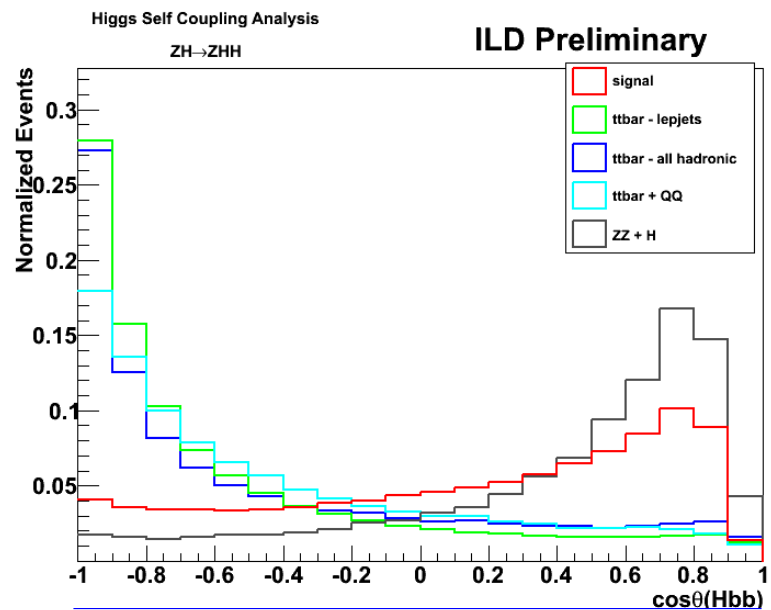
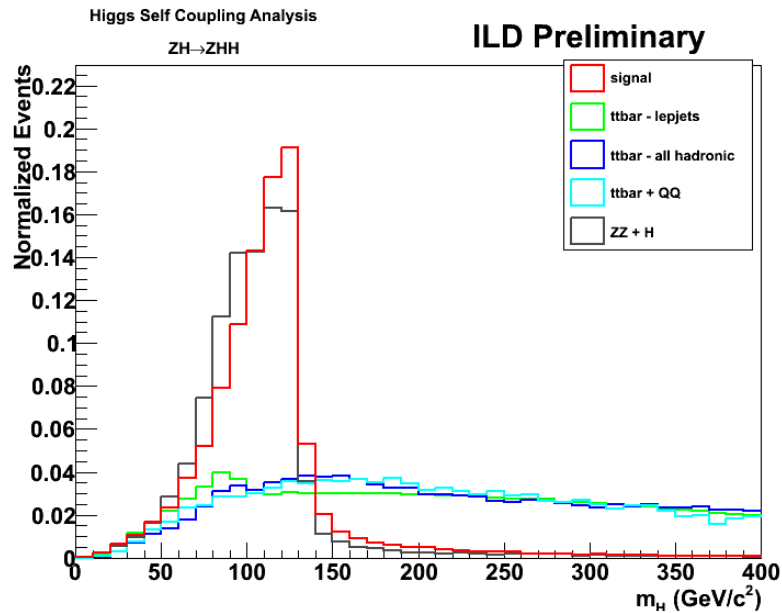
SOME KINEMATIC VARIABLES USED FOR MVA

Very powerful variable @500GeV: $m(jjjj)$, $m(l \nu jj)$



SOME KINEMATIC VARIABLES USED FOR MVA

Very powerful variable @1TeV: m_H , $\cos \theta(Hbb)$



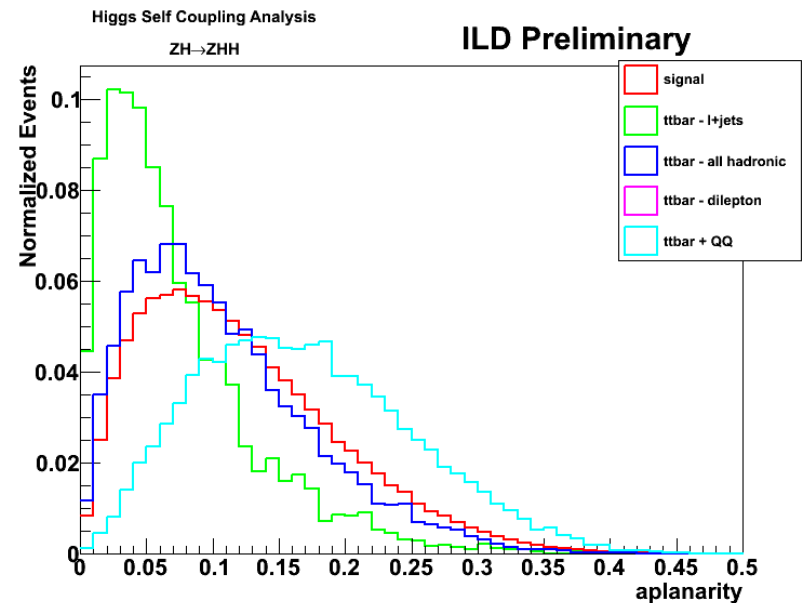
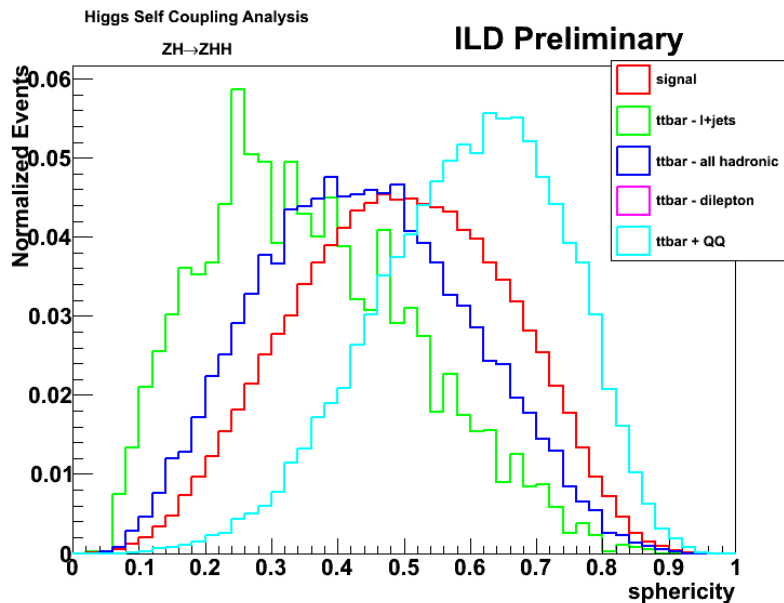
NON-SIMPLE VARIABLES USED FOR MVA

○ Sphericity and aplanarity

- Eigenvalue combinations of sphericity tensor:

$$S^{\alpha\beta} = \frac{\sum_i p_i^\alpha p_i^\beta}{\sum_i |\mathbf{p}_i|^2}, \quad \text{eigenvalues: } \lambda_1 > \lambda_2 > \lambda_3$$

- Sphericity: $S = \frac{3}{2}(\lambda_2 + \lambda_3)$
- Aplanarity: $A = \frac{3}{2}\lambda_3$
- Indicates whether the event is 2-jets like or isotropic

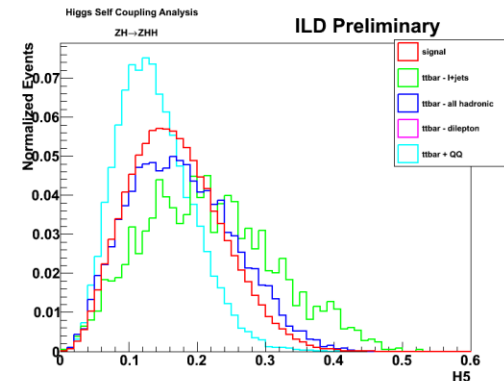
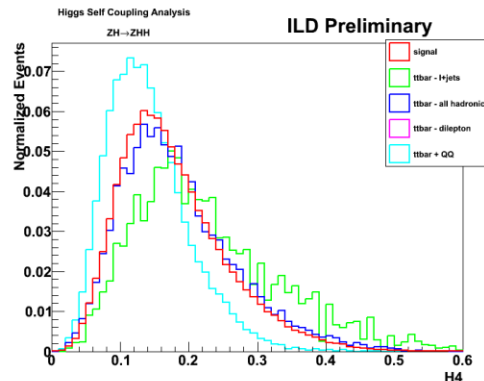
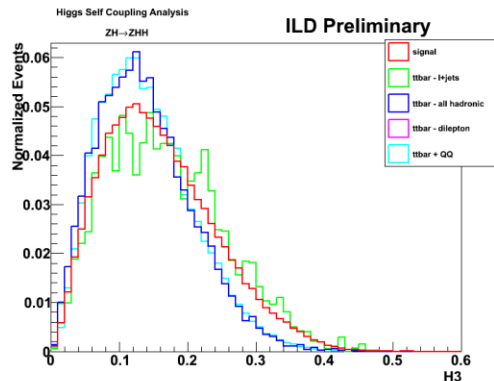
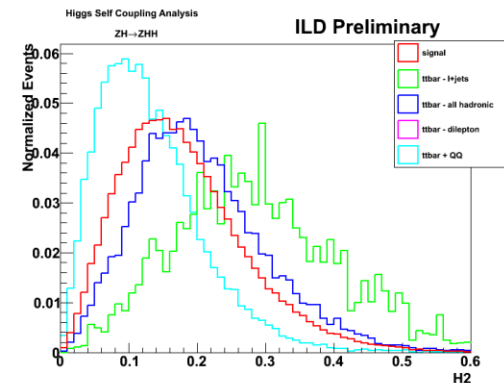
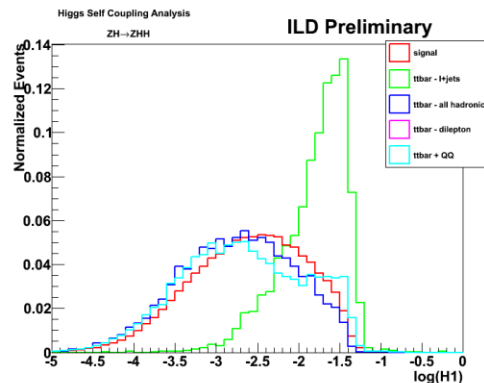
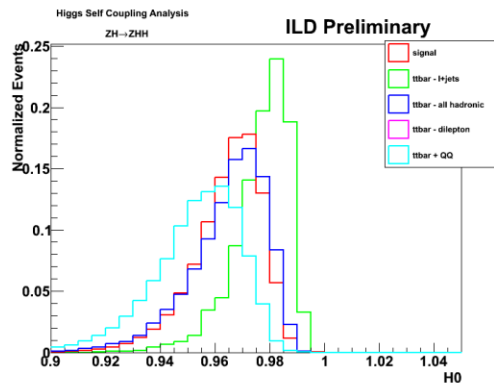


NON-SIMPLE VARIABLES USED FOR MVA

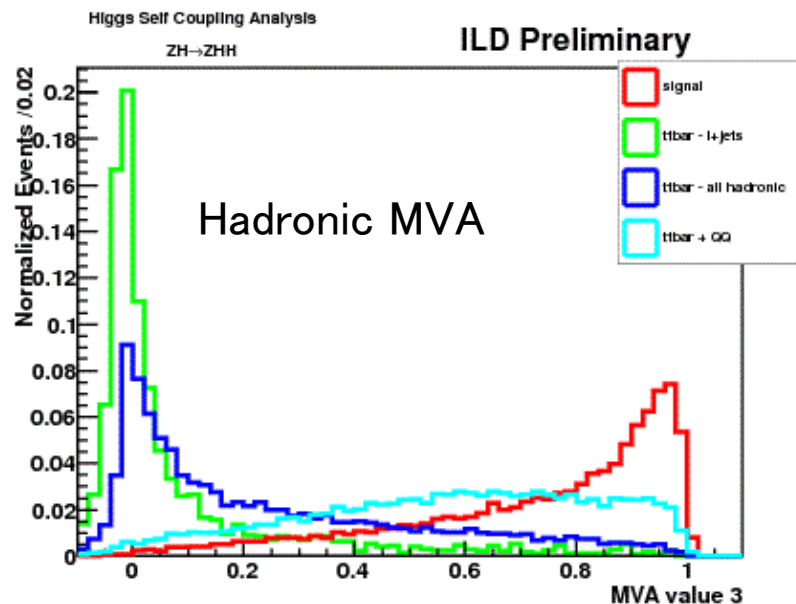
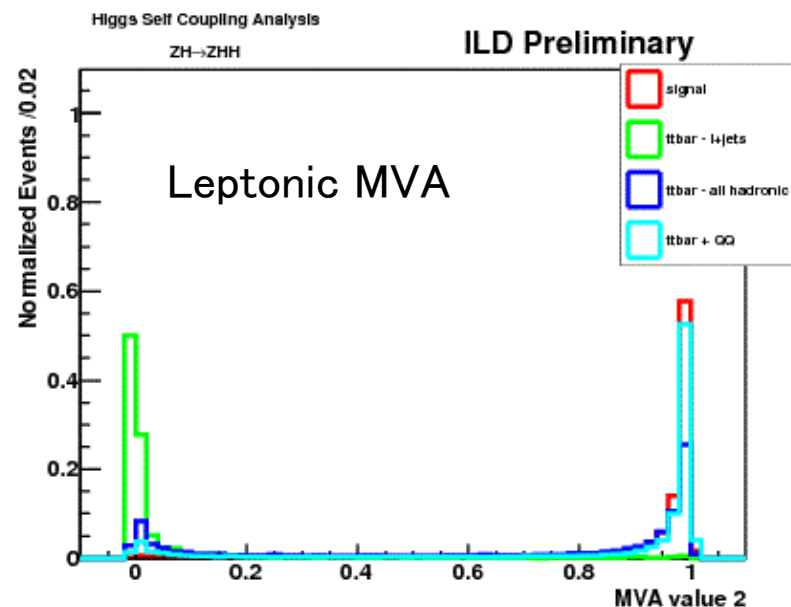
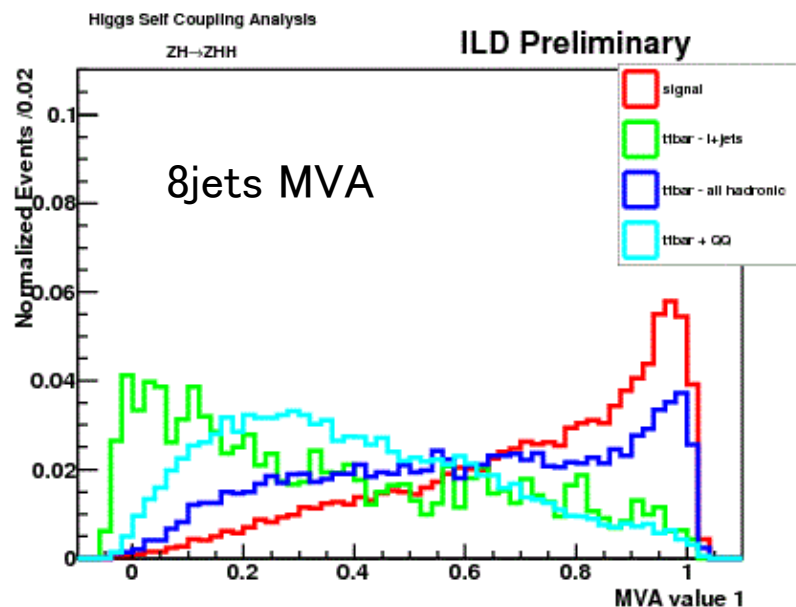
○ Fox-wolfram moments

$$H_l = \sum_{i,j} \frac{|\mathbf{p}_i| |\mathbf{p}_j|}{E_{\text{vis}}^2} P_l(\cos \theta_{ij}) ,$$

- P_l is Legendre polynomials
- Those moments characterize the structures of 2jets, 3jets, or isotropic events



MVA OUTPUTS EXAMPLES(ALLHADRONIC@500GeV)



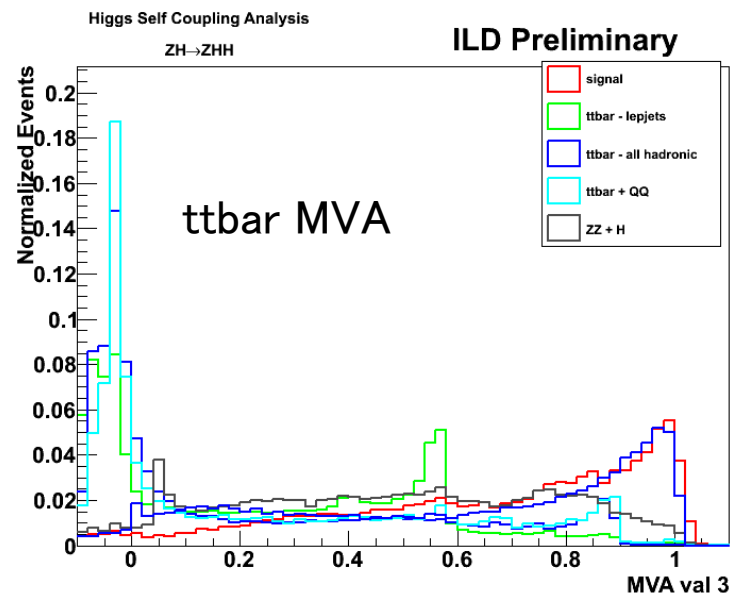
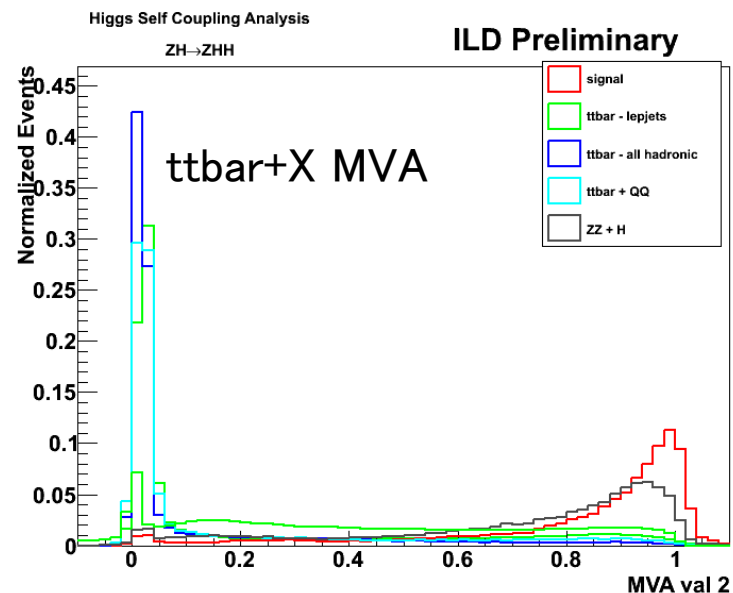
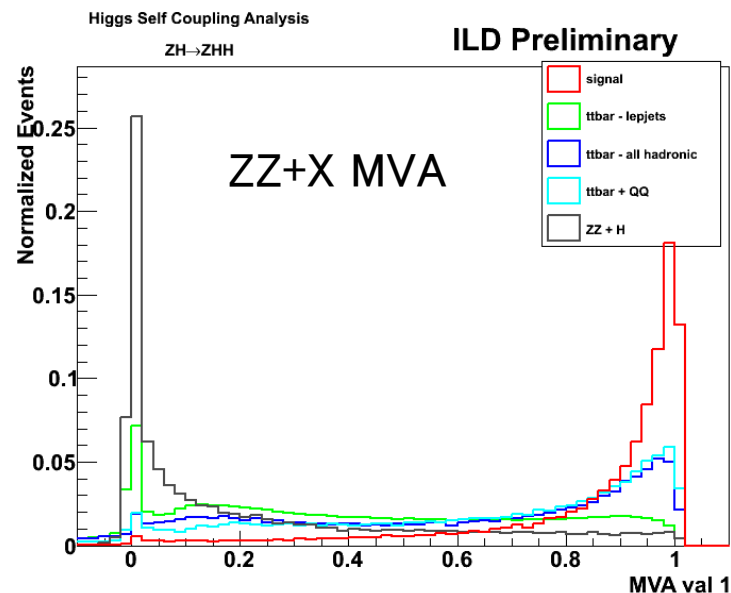
cut of MVA:

MVA8jets>0.08

MVAlep>0.02

MVAhad>0.74

MVA OUTPUTS EXAMPLES(N NHH@1TeV)



cut of MVA:

$$MVA_{ZZX} > 0.34$$

$$MVA_{ttbarX} > 0.86$$

$$MVA_{ttbar} > 0.91$$

SENSITIVITY@500GeV

○ $HH \rightarrow (bb)(WW)$

- As mentioned, categorized with decay types of Z and W boson
 - $Z \rightarrow bb, cc$ or ll
- b-tagging strategy – introduce looser b-tag category
 - 4-btag & 3-btag
- $E_{CM}=500\text{GeV}$, $L=2\text{ab}^{-1}$
- **Significance $\sim 1.91 \sigma$**

Modes	Z decay	b tag	Signal	Background	Significance
All hadronic	$Z \rightarrow bb$	4btag	15.20	87.52	1.50σ
		3btag	19.43	3099.49	0.35σ
	$Z \rightarrow cc$		11.29	366.13	0.58σ
Lepton + jets	$Z \rightarrow bb$		1.65	17.62	0.38σ
	$Z \rightarrow cc$		1.50	819.61	0.05σ
Dilepton	$Z \rightarrow ll$		2.24	8.44	0.69σ
Trilepton	$Z \rightarrow ll$		1.05	2.60	0.55σ
Combined					1.91σ

SENSITIVITY@1TeV

○ $HH \rightarrow (bb)(WW)$

- As mentioned, categorized with decay types of Z and W boson
 - $Z \rightarrow bb$ and ll , VBF channel
- b-tagging strategy – fully used the b-tagging for each category
- $E_{CM}=1\text{TeV}$, $L=2\text{ab}^{-1}$
- **Significance $\sim 2.80 \sigma$**

Modes	Z decay	Signal	Background	Significance
All hadronic	$Z \rightarrow bb$	17.15	48.17	2.12σ
Lepton + jets	$Z \rightarrow bb$	1.16	9.24	0.36σ
Dilepton	$Z \rightarrow ll$	1.03	14.30	0.26σ
6jets+ Missing	No Z, $\nu \nu HH$	6.90	8.24	1.77σ
Combined				2.80σ

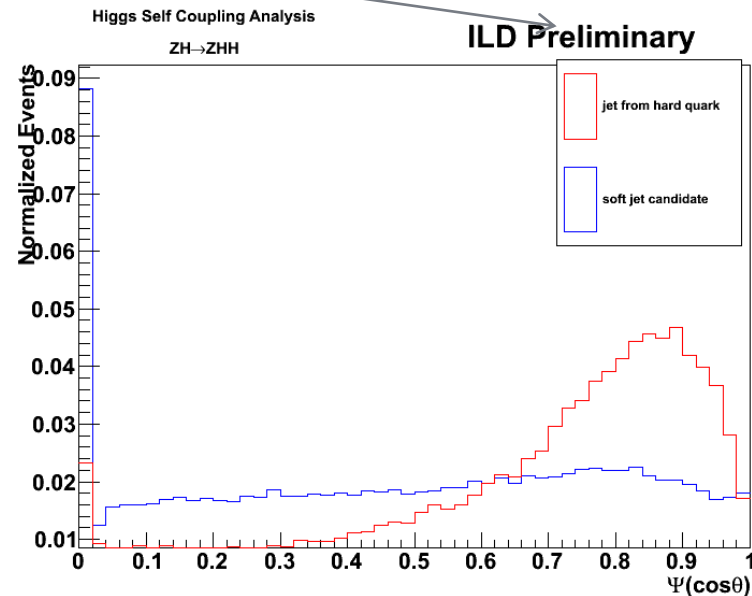
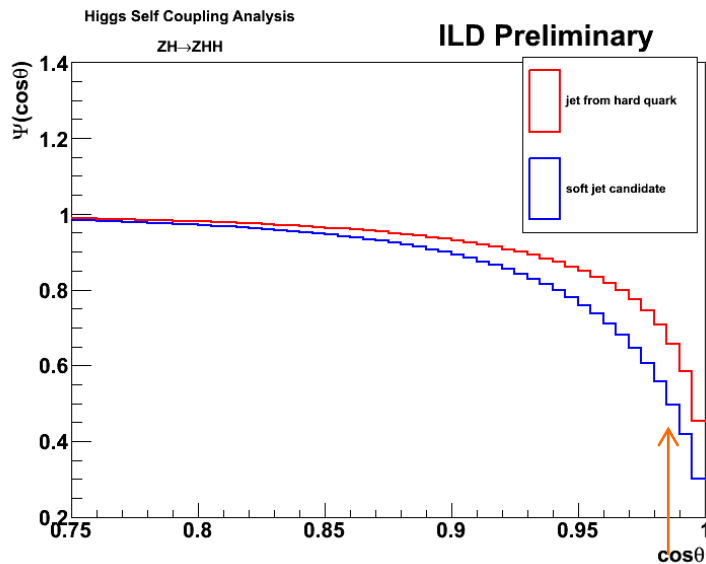
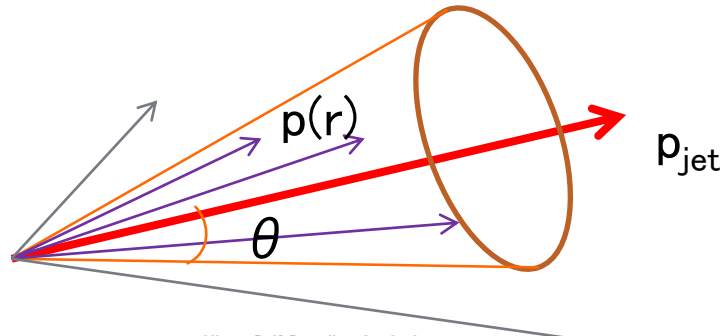
SUMMARY AND PLAN

- Higgs self coupling analysis using the events with $H \rightarrow WW^*$ is ongoing.
 - Multi variate analysis to reject the backgrounds
 - Total sensitivity @500GeV is $\sim 1.91 \sigma$
 - Total sensitivity @1TeV is $\sim 2.80 \sigma$
- Plan:
 - Start to combine with golden channel and estimate the Higgs self coupling
 - Full simulation @1TeV
 - Optimize b-tagging strategy
 - Forming looser b-tag category
 - Improvement of basic components for the analysis
 - Lepton ID
 - b-tagging
 - Jet energy correction
 - Jet clustering

SOFT JET FINDING

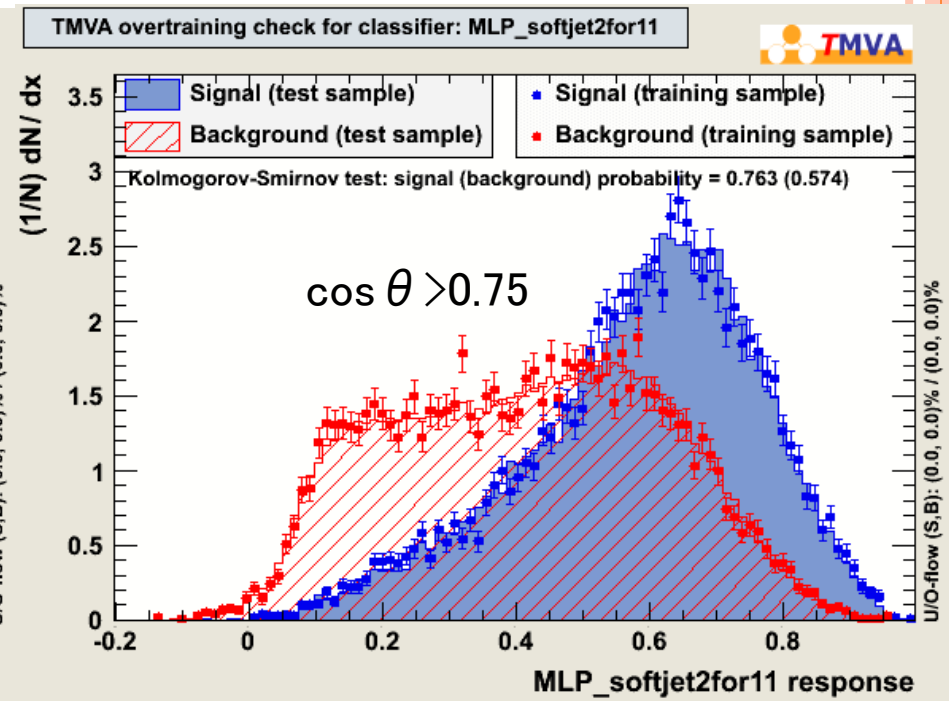
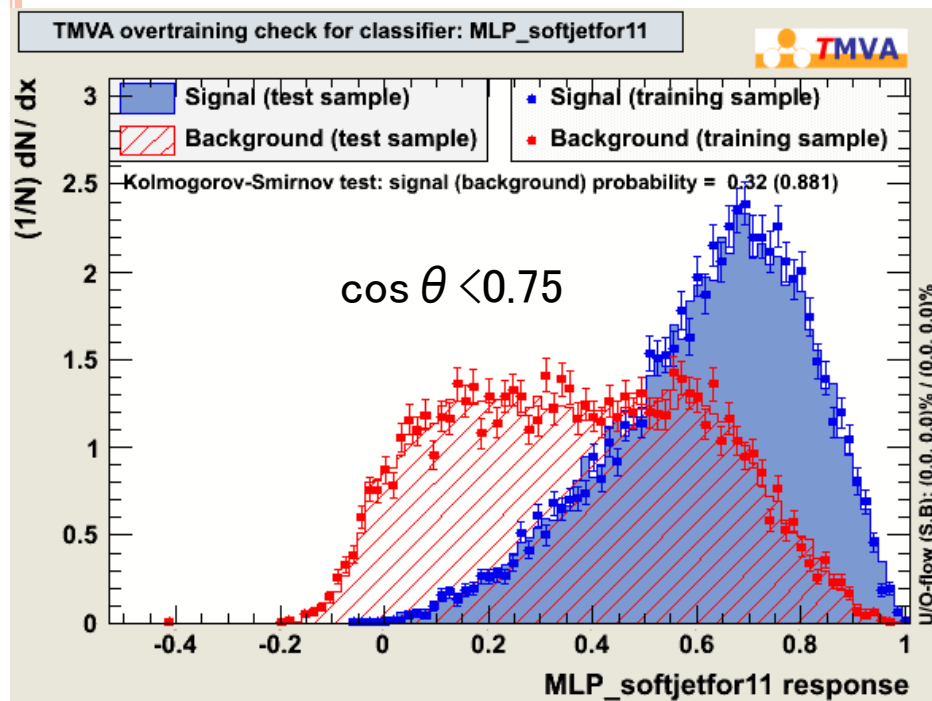
- Soft jet finding may be available for the events with extra jets not coming from hard process quarks
 - e.g. 8 jets requirement to $t\bar{t}$ hadronic events (6 jets from hard quarks)
- Traditional jet shape indicates the same tendency as hadron collider analysis

$$\psi(\cos\theta) = \int_1^{\cos\theta} \frac{p(r)}{p_{\text{jet}}} dr$$



SOFT JET FINDING

- Hard jet likeliness is introduced
 - Using MVA to form it
 - Analysis samples are divided into 2 based on the angle with the nearest jet
→ large shared area for both jets deteriorate the traditional jet shape
- Use the likeliness for the input of background rejection MVA or simple cut of backgrounds



REDUCTION TABLE

All hadronic

- Final b-tagging: $\text{btag}(3) > 0.92 \ \&\& \ \text{btag}(4) > 0.44$
- $\text{HH} \rightarrow \text{bbbb}$ contamination is 5.41 events

process	signal	ttbar	tt + QQ	tt+Z	tt + H	ZZ + H	ZZZ
expected	354.00	1.16×10^6	1660.00	3307.00	280.00	1540.00	3660.00
preselection	49.47	2462.09	79.11	76.25	38.32	87.22	70.72
Jet energy	47.92	1970.58	77.62	74.98	37.96	72.88	57.28
χ^2	44.32	1353.38	64.57	62.41	34.02	61.60	48.16
Visible energy	44.23	1326.19	64.31	62.00	33.92	61.18	47.90
NN for 8 jets	36.51	1011.92	36.37	34.37	16.38	51.59	47.90
NN for ttbar	20.53 (9.85)	302.59	26.44	25.17	13.07	21.71	9.00
b-tagging	14.92 (5.41)	87.54	17.54	16.42	9.13	16.10	6.03