

Introduction to the phenomenology of extra dimensions recent results from CMS some prospects at ILC

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ILC physics case SPP may 23rd

Extra dimensions phenomenology

outline

- motivations, models
- ADD approach (and black holes)
- TeV⁻¹ extra dimension(s)
- Universal Extra Dimensions (UED)
- Randall Sundrum approach (RS) and bulk RS
- string states, intersecting branes (at angles)
- extra-dimensions, GUT, supersymmetry

Motivations for extra dimensions

- top-down
 - unification

superstring theories (branes, duality, M-theory)

- **bottom-up**
 - address hierarchy problem of SM
 - can address :
 - symmetry breaking (EW, SUSY) ____ boundary conditions
 - SM fermions masses and mixing

EW observables precision measurements K and B physics (CP violation), rare decays, ... model building
is challenging !

Models for extra dimensions

many possible approaches

with different impact on phenomenology depending on

how many extra dimensions ? 1 or more ?

which geometry ? which type of compactification ?

how large and which consequences?

which fields where ?

How many and which "geometry"?

- factorizable or 'flat' (3 space + 1 time + D - 4 extra space dimensions)

$$ds^{2} = g_{\mu\nu} dx^{\mu} dx^{\nu}$$
 $\mu, \nu = 0, 1, 2, 3, ... D$

- non factorizable or warped (3 space + 1 time + 1 extra space dimension y)

$$ds^{2} = a(y)(\eta_{\mu\nu} dx^{\mu} dx^{\nu}) + dy^{2} \qquad \mu, \nu = 0, 1, 2, 3$$
warp factor

6D multiple warping ? arXiv:1001.2666 $ds^{2} = b(z)[a(y)\eta_{\mu\nu}dx^{\mu}dx^{\nu}+r_{y}^{2}dy^{2}]+r_{z}^{2}dz^{2}$ see also Davoudiasl, Rizzo JHEP11(2008)013

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which type of compactifications ?

extra dimensions not (yet) seen → must be small and 'compact'





- **ON Orbifolds** (coset space M/H where H is a group of discrete symmetries of a manifold M,

 \rightarrow space singular at some fixed points) e.g. one of the simplest case S^{1}/Z_{2} :



'fixed points ' with respect to the Z_2 discrete symmetry $\Gamma: y \rightarrow -y$

How Large and which consequence?



compactified dimensions leads to periodicity conditions

Fourier mode expansion of fields



infinite number of Kaluza-Klein (KK) modes/states/excitations

kth **mode mass**

$$m_k^2 = m_0^2 + \frac{k^2}{R^2}$$

tower of KK states



space time of D = 4 + n dimensions

only gravity propagates in D dimensional (bulk) full space

factorizable geometry
compactified n extra-dimensions
(on circle / torus) as small as ~ mm ?

ADD model

Arkani-Hamed Dimopoulos Dvali, PLB 429 (1998) 263, PRD59 (1999) 086004 Antoniadis Arkani-Hamed Dimopoulos Dvali, PLB 436 (1998) 257





Universal Extra-Dimensions (UED)

D = 4 + n bulk (n=1 mostly)

where SM gauge AND fermion fields propagate

factorizable geometry compactified extra-dimensions (on simplest orbifold)

Appelquist, Cheng, Dobrescu, PRD64, 035002





PRD 60, 107505, PBL 474 (2000) 275



not only gravity propagates in a 5D warped bulk

but also fermion and gauge fields

Higgs localized close to TeV brane

Bulk RS





space time of D = 4 + n dimensions

only gravity propagates in D dimensional (bulk) full space

factorizable geometry
compactified n extra-dimensions
(on circle / torus) as small as ~ mm ?

ADD model

Arkani-Hamed Dimopoulos Dvali, PLB 429 (1998) 263, PRD59 (1999) 086004 Antoniadis Arkani-Hamed Dimopoulos Dvali, PLB 436 (1998) 257

ADD approach

Arkani-Hamed Dimopoulos Dvali, PLB 429 (1998) 263, PRD59 (1999) 086004 Antoniadis Arkani-Hamed Dimopoulos Dvali, PLB 436 (1998) 257

gravity at TeV scale in a bulk of 4 + n compactified dimensions SM fields confined in 4D brane

one of 1st approach of the KK idea renewal after the string duality and brane revolution

address the hierarchy problem

$$M_{Pl(4)}^2 \sim M_{Pl(4+n)}^{n+2} R^n$$

$$for M_D \equiv M_{Pl(4+n)} = 1 TeV \qquad \frac{N}{R} \qquad \frac{1}{10^{10} \text{ km}} \qquad 1 \text{ mm} \qquad 1 \text{ nm}}{R} \qquad \frac{10^{10} \text{ km}}{10^{10} \text{ km}} \qquad 1 \text{ mm} \qquad 1 \text{ nm}}{r}$$

phenomenology and constraints from various areas:

- short distance gravity measurement (backup)
- astrophysics and cosmology (backup)
- collider physics

Han, Lykken, Zhang, PRD5 9, 105006 Hewett, PRL 82 (1999) 4760 Giudice, Rattazzi, Wells, NPB 544 (1999) 3 Mirabelli, Perelstein, Peskin, PRL 82 (1999) 2236

ADD approach

the graviton Kaluza-Klein modes have masses equal to |k|/R and therefore the different excitations have mass splittings

$$\Delta m \sim \frac{1}{R} = M_D \left(\frac{M_D}{\bar{M}_{Pl}}\right)^2 = \left(\frac{M_D}{\mathrm{TeV}}\right)^{\frac{n+2}{2}} 10^{\frac{12n-31}{n}}$$

using
$$\bar{M}_{Pl} \equiv \sqrt{V_n} \bar{M}_D^{\frac{n}{2}+1} = (2\pi R)^{\frac{n}{2}} \bar{M}_D^{\frac{n}{2}+1} \equiv R^{\frac{n}{2}} M^{\frac{n}{2}+1}$$

for
$$M_D \equiv \sqrt{V_n} \bar{M}_D^{\frac{n}{2}+1} = (2\pi R)^{\frac{n}{2}} \bar{M}_D^{\frac{n}{2}+1} \equiv R^{\frac{n}{2}} M^{\frac{n}{2}+1}$$

n	4	6	8
Δm	20 keV	7 MeV	0.1 GeV

ADD signatures at colliders in a nutshell

- direct searches _____ KK graviton in final states states close to each other in mass O(fraction of eV) quasi-continuum compensating ~O(1/Mpl) coupling of each KK state to SM fields

look for jet + missing energy photon + missing energy Z + missing energy



sizeable Xsection directly related to n and scale $M_D = \sigma \approx E^n / M_D^{n+2}$

- indirect searches



no KK states in final states

look for deviation in fermion or boson pairs production (diff.) Xsections measurements

Xsection divergent for n > 1 \longrightarrow need a cutoff cut-off M not related to scale M \longrightarrow assume $M_S \approx M_D$

(possible regularization in string theories context)

PreLHC collider constraints on scales $\sim O(1.6 - 2.1 \text{ TeV})$ for n = 2

ADD Formalism issues

 $F = \log \frac{M_{HLZ}^2}{s}$ $F = \frac{2}{n-2}$

- Hewett

interference (sign and n dependence undetermined)

$$\pm \lambda / M_s^4$$
 with λ conventionally $\lambda = \pm 1$

- Giudice Rattazzi Wells

interference (sign fixed and n dependence undetermined) $\sim 1/\Lambda_T^4$

 F/M_{HIZ}^4

- Han Lykken Zhang

interference (sign fixed)

- conversion rules

$$M_{s}[Hewett \ \lambda=+1] = \left[\frac{2}{\pi}\right]^{\frac{1}{4}} \Lambda_{T}(GRW)$$
$$\frac{\lambda}{M_{S}^{4}(Hewett)} = \frac{\pi}{2} \frac{F}{M_{HLZ}^{4}}$$
$$\frac{1}{\Lambda^{4}(GRW)} = \frac{F}{M_{HLZ}^{4}}$$
Han, Lyki Giudice, Ratta

TB

Han, Lykken, Zhang, PRD5 9, 105006 Hewett, PRL 82 (1999) 4760 Giudice, Rattazzi, Wells, NPB 544 (1999) 3

n=2

n > 2

From torsion balance test of gravitational Inverse square law



Kapner, Cook, Adelberger, Gundlach, Heckel, Hoyle, Swanson, PRL 98 (2007) 021101

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Branon

- in ('flat') extra-dimensions models with low brane tension f (lower than M_D) fluctuations of the brane position along the extra-dimensions are the only relevant low energy modes
- the particles associated to the fluctuations of the brane in the extra dimensions are scalar particles called branons π^{α}
- branons can be massive (with mass M)

m

- branons interact by pairs with the SM energy momentum tensor via a mass term and derivative term with f^4 suppressed couplings

$$L_{\text{branon}} = \frac{1}{2} g^{\mu\nu} \partial_{\mu} \pi^{\alpha} \partial_{\nu} \pi^{\alpha} - \frac{1}{2} M^2 \pi^{\alpha} \pi^{\alpha} + \frac{1}{8f^4} \left(4 \partial_{\mu} \pi^{\alpha} \partial_{\nu} \pi^{\alpha} - M^2 \pi^{\alpha} \pi^{\alpha} g_{\mu\nu} \right) T^{\mu\nu}$$

- branons are stable, weakly interacting and invisible \rightarrow DM candidate
- despite their coupling suppression, branons can be abundantly pair produced in association SM particles at the LHC (and to some extent also at ILC and CLIC, ...)
- for example branons can be pair produced in association with one γ

Branons



e.g. J.A.R. Cembranos, A. Dobado, A.L. Maroto PRD 88 (2013) 075021

Black Holes

Myers, Perry, Annals, Phys. 172 (1986) 304 Argyres, Dimopoulos, March-Russel, PLB 441 (1998) 96 Banks, Fischler, hep-th/9906038 Emparan, Horowitz, PRL 85 (2000) 499 Giddings, Thomas, PRD65, 056010 Dimopoulos, Landsberg, PRL 87 (2001) 161602 Anchordoqui, Goldberg, Shapere, PRD 66, 024033 Dimopoulos, Emparan, PLB 526 (2002) 393 Kanti, Int.J.Mod.Phys. A19 (2004) 4899 Lect.Notes.Phys.769(2009)387

Schwarzschild radius ('flat' ED ~ ADD)

4D
$$R_s \approx \frac{2}{M_{Pl}^2} \frac{M_{BH}}{c^2}$$
 $R_s \ll 10^{-35} m$
(4+n)D $R_s \approx \frac{1}{M_d} \left(\frac{M_{BH}}{M_D}\right)^{\frac{1}{n+1}}$ $R_s \approx 10^{-19} m$

if **colliding parton impact parameter** < **R** and **E** ~ **M** > **M** <u>CM BH D</u>

a black hole can form

Cross sections are large

 $\sigma(parton_i parton_j \rightarrow BH) \approx \pi R_s^2$ semi-classical approach

$$\sigma(pp \rightarrow BH) \approx 1nb - 1fk$$



Dimopoulos, Landsberg, PRL 87 (2001) 161602

Black Holes decay

a highly asymetric rotating created Black Hole goes through

Balding phase

shedding of quantum numbers except a few i.e. M, Q \dots invisible energy (15% of total energy ?)

Spin-down phase

loss of angular momentum by Hawking radiation visible energy (25% of total energy ?)

Schwarzschild phase $M_{BH} > > M_{D}$

Hawking radiation at $T_H \approx M_D (\frac{M_D}{M_{BH}})^{\frac{1}{n+1}} (n+1)$

thermal evaporation black body spectrum + grey-body factors from strong. Grav. field)

visible energy (60% of total energy ?) \rightarrow mostly in SM particles on our brane Planck phase $M_{BH} \approx M_D$ (regime of quantum gravity)

quanta emission ? string ball formation and evaporation at Hagedorn temperature ?

Black Holes

BH evaporate/decay democratically into SM particles (or SM+SUSY) mainly on the brane through Hawking radiation decay is fast $\sim 10^{-26}$ s \longrightarrow Black Holes do not escape the detector

spectacular signatures with large jet/lepton multiplicities and small MET

possible to carry dedicated studies \rightarrow dimensionality of space-time

measure Hawking temperature of black hole T_{BH} (e.g. from energy spectrum of some decay product)

as a function of its mass M_{BH} (e.g. from total energy of all of its decay product)



and check that $\log(T_{BH}) = -\frac{1}{n+1} \log(M_{BH}) + \text{ const}$ (extra-dimension equivalent of the Wien law)

Astrophysical Constraints

	M _D	M _D		
Y ray from galactic bulge (from EGRET)	450 TeV (n=2) $3.8 \ 10^{-10}$ m	1.9 TeV (n=3) $4.2 \ 10^{-12}$ m		
neutron star halo (KK decay) (from EGRET)	454 TeV (n=2)	27 TeV (n=3)		
neutron star excess heat (from HST)	1680 TeV (n=2)	60 TeV (n=3)		



Antoniadis PLB246 (1990) 377 Antoniadis, Benakli, Quiros, PLB 331 (1994) 313 Dienes, Dudas, Gherghetta, PLB 436 (1998) 55, NPB 537 (1999) 47 Antoniadis, Benakli, Quiros, PLB 460 (1999) 176 Rizzo, Wells, PRD61, 016007 Cheung, Landsberg, PRD65, 076003

- gauge bosons in 'flat' 5D bulk with $R = O(TEV^{-1})$ extra dimension
- KK 0th mode identified with SM gauge bosons (can mix with non-zero modes)
- combined constraints from LEP, HERA, TEVATRON: $M_{KK} = R^{-1} > 6.8 \text{ TeV}$ Cheung, Landsberg, PRD65, 076003

direct searches (before LHC): M_{KK} > O (1 TeV)

- resonant production if $M_{KK} < E_{CM}$ search for dilepton or dijet invariant mass peak (or transverse mass jacobian peak from single lepton) to look for the 1st mode at least 2^{nd} , 3^{rd} modes for KK pattern would be desirable

- virtual effects (?) if $M_{KK} > E_{CM}$

Xsection deviations, asymmetries



Coupling: finite at 5D, divergent for > 5D but can regularized in specific approaches

naively, from normalization of gauge fields kinetic energy term \rightarrow KK gauge bosons couple to SM fermions with a strength larger than the 0-mode by a universal factor of $\sqrt{2}$ example of 4, 5 and 6 TeV $\gamma_{KK}^{(1)}$ and $Z_{KK}^{(1)}$ (which are nearly degenerate in mass as well as with $W_{KK}^{(1)}$) production at the 14 TeV LHC (fermions in one 4D brane)



angular distributions to demonstrate that states are spin-1 (if enough statistics) dips in the distributions \rightarrow signal for KK scenarios ?

dips in the distributions \rightarrow signal for KK scenarios ?

may depend on fermion location \rightarrow dips can disappear with different fermions assignments



if access to second KK level kinematically difficult at LHC \rightarrow

difficult to distinguish an ordinary Z' and degenerate $\gamma_{KK}^{()1}/Z_{KK}^{(1)}$ difficult to demonstrate the KK nature of the resonance at the LHC ? way out with lepton collider even below the resonance (see later on) ?

what if more than one TeV^{-1} extra dimension ?

- ⇒ details of compactifying manifold may become important
 - KK excitation spacings more intricate
 - many levels degenerate in mass
 - strength of couplings to fermions may become level dependent
- ⇒ constraints from precision measurement more tricky to derive
 - assume that the couplings of at least the first few levels to fermions are not vastly different than the naive one (see few slides above)
 - in the limit where the effects KK states exchanges viewed as a set as a set of contact interaction (effective approach)
 - → new dimension-6 operators with coefficient proportional to a dimensionless quantity V q_n is the coupling of the *n* th level q_n is the couple q_n is the coupling of the *n* th level q_n is the couple q_n is the c

$$V = \left(M_W R\right) \sum_{n=1}^{\infty} \frac{g_n^2}{g_0^2} \frac{1}{n \cdot n}$$

 g_n is the coupling of the *n*th level and assuming a simple compactification where 1st KK excitation(s) have mass $\propto \frac{1}{R}$

the sum in V does not converge with more than one extra dimension

- 1st way out : truncation (T)
- ⇒ sum over a finite number of terms n_{max} i.e only those states whose mass is below M_s which now acts simply as cutoff
- 2nd way out : exponential (E)
- ⇒ exponential damping of contribution from higher terms in the sum (from considerations of the flexibility of the brane or in string context)

$$V = (M_W R) \sum_{n=1}^{\infty} \frac{g_n^2}{g_0^2} \frac{1}{n \cdot n} e^{-\frac{n \cdot n}{n_{\max}}}$$

		$Z_2 \times Z_2$		Z _{3,6}		$Z_2 \times Z_2 \times Z_2$	
lower bound on the mass	n _{max}	Т	Е	Т	Е	Т	Е
of the 1st VV state (TeV)	2	5.69*	4.23*	6.63*	4.77*	8.65	8.01
of the 1st KK state (1ev)	3	6.64	4.87*	7.41	5.43*	11.7	10.8
for different compactifications	4	7.20	5.28*	7.95	5.85*	13.7	13.0
ie 7×7 7 and $7 \times 7 \times 7$	5	7.69	5.58*	8.36	6.17*	15.7	14.9
i.e. $\mathbb{Z}_2/\mathbb{Z}_2$, $\mathbb{Z}_{3,6}$ and $\mathbb{Z}_2/\mathbb{Z}_2/\mathbb{Z}_2$	10	8.89	6.42	9.61	7.05	23.2	22.0
	20	9.95	7.16	10.2	7.83	33.5	31.8
	50	11.2	8.04	12.1	8.75	53.5	50.9



Universal Extra-Dimensions (UED)

D = 4 + n bulk (n=1 mostly)

where SM gauge AND fermion fields propagate

factorizable geometry compactified extra-dimensions (on simplest orbifold)

Appelquist, Cheng, Dobrescu, PRD64, 035002

Minimal Universal Extra Dimensions (mUED)



- KK states produced in pairs

- 1 KK + 1 SM in a KK state decay possible cascade decays
- stable LKP (DM candidate) source of MET

Minimal UED

- pair production of lightest
 coloured KK states
 → largest Xsection
- possible signatures:
 - 4 leptons + MET
 - 3 (or 2 leptons ...) + jets + MET
 - 2 (or more) jets + MET



Minimal UED

example of decay flow

 $\begin{aligned} &Br(g_1 \to Q_1 Q_1) \approx 0.5 \\ &Br(g_1 \to q_1 q_1) \approx 0.5 \\ &Br(q_1 \to q \gamma_1) \approx 1 \\ &Br(Q_1 \to QZ_1: W1: \gamma_1) \approx 0.33: 0.65: 0.02 \end{aligned}$

 $Br(W_1 \rightarrow \nu L_1:\nu_1 L) \approx 1/6:1/6$ $Br(Z_1 \rightarrow \nu \nu_1:LL_1) \approx 1/6:1/6$ $Br(L_1 \rightarrow \gamma_1 L) \approx 1$ $Br(\nu_1 \rightarrow \gamma_1 \nu) \approx 1$



Cheng Matchev Schmaltz PRD66, 056006

discriminating mUED Datta w.r.t SUSY?



- both L and R handed SU(2) doublet KK fermions in UED (in susy only L handed SU(2) doublet squarks)

- integrating different angular distributions for fermions $(1 + \cos^2 \theta)$ vs scalars $(1 - \cos^2 \theta)$

- for production close to threshold (heavy particles)

different X section threshold suppression for fermions (β) vs $\,$ scalars (β^3)

Level 2 KK-quarks (pairs or associated with KK gluons) can be produced directly

BUT Br (Nleptons + MET) • Xsection still challengingly small & challenging small statistics to distinguish from level 1 modes
which fields/particles and where ?



which fields/particles and where?



PRD 60, 107505, PBL 474 (2000) 275

Minimal RS

- gravity only in a 5D warped bulk (with 1 compact ED) and 2 4D branes $ds^{2} = e^{\left[-2kr_{c}\phi\right]} \left(\eta_{\mu\nu} dx^{\mu} dx^{\nu}\right) + r_{c} d\phi^{2} \qquad \phi \in \left[0,\pi\right] \qquad k \sim M_{Pl(4)}$
- warp factor allows to generate TeV scale on one brane (TeV Brane)
 from Planck scale on the other brane (Planck Brane)

$$\Lambda_{\pi} = M_{Pl(4)} e^{-\pi k r_c} \rightarrow \Lambda_{\pi} \sim 1 \text{ TeV} \quad \text{for} \quad k r_c \sim 12 \quad r_c = 10^{-32} \text{ cm}$$

- **KK graviton** with O(TeV) spacing $m_n = k x_n e^{-kr_c \pi} x_n$ roots of Bessel function J_1
- SM fields on TeV brane coupling to massive KK graviton $~~\sim 1/\Lambda_{\pi}$
- phenomenology described by 2 parameters

$$m_1$$
 mass of 1st mode, and $c = \frac{m_1}{x_1 \Lambda_{\pi}}$

0.01 < c < 0.1 theoretically reasonable range

search for narrow resonances $pp \rightarrow G_{KK} \rightarrow e^+ e^-$, $\mu^+ \mu^-$, $\gamma \gamma$, ZZ

minimal RS



Davoudiasl, Hewett, Rizzo, PRD 63, 075004

Minimal RS: $G_{_{KK}}$ decays



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Stabilized RS

gravitational fluctuations around RS metric $ds^2 = e^{-2kr_c\phi}(\eta_{\mu\nu} dx^{\mu} dx^{\nu}) + r_c d\phi^2$

contain massless scalar mode (modulus) $r_c \rightarrow T(x)$: the radion

(Goldberger Wise mechanism) • v.e.v stabilizing the interbrane distance $< T(x) > = r_c$ bulk scalar generating potential can stabilize the modulus at minimum of potential

radion must be massive to recover ordinary 4D Einstein gravity

in order to have $k r_c \approx 12$ radion should be lighter than O(TeV) KK graviton

radion likely the lightest state from RS models radion couples directly to gluon and photon

possible Higgs-radion mixing (also in type I string) parameterized by ξ with $|\xi| \approx O(1)$

Goldberger, Wise, PRL 83 (1999) 4922 Goldberger, Wise, PRD 60, 107505 Goldberger, Wise, PBL 474 (2000) 275 Csaki, Graesser, Randall, Terning, PRD 62 (2000) 045015 Charmousis, Gregory, Rubakov, PRD 62 (2000) 067505

stabilized RS

Mahanta, Rakshit, PLB 480 (2000) 176 Mahanta, Datta, PLB 483 (2000) 196 Bae, Ko, Lee, Lee, PLB 487 (2000) 299 Mahanta, PRD 63, 076006 Cheung, PRD 63, 056007 Giudice, Rattazzi, Wells, NPB 595 (2001) 250 Rizzo, JHEP 06 (2002) 056 Bae, Lee, PLB 506 (2001) 147 Chaichian, Datta, Huitu, Yu, PLB 524 (2002) 161 Das, Mahanta, PLB 529 (2002) 253 Azuelos, Cavalli, Przysiezniak, Vacavant, Eur. Phys. J. Direct C4 (2002) 16

Csaki, Graesser, Kribs, PRD63, 065002 Han, Kribs, McElrath, PRD 64, 076003 Antoniadis, Sturani, NPB 631 (2002) 66 Gupta, Mahajan, PRD 65, 056003 Hewett, Rizzo, JHEP, 08 (2003) 028 Battaglia, De Curtis, De Roeck, Dominici, Gunion, PLB 568 (2003), 92 Das, Mahanta, Mod. Phys. Lett. A19 (2004) 1855 Gunion, Toharia, Wells, PLB 585 (2004) 295 Cheung, Kim, Song, PRD69, 075011 Das, PRD 72,055009 Csaki, Hubisz, Lee, PRD 76,125005

radion production



stabilized RS

- pure radion effects on precision EW data are small

Gunion, Toharia, Wells, PLB 585 (2004) 295



Bulk RS models

- to solve hierarchy problem

- fermion and gauge fields allowed to propagate in the Xtra dim
- SM particles correspond to KK zero modes of 5D fields

bulk profile of SM fermion depends on its 5D mass parameter

- choose to localize $1^{\rm st}$ and $2^{\rm nd}$ generation fermions near Planck brane
- FCNC from higher dim operator suppressed by scales >> TeV
- ► SM Yukawa coupling hierarchies
- $1^{\rm st}$ and $2^{\rm nd}$ generation small Yuk. coup. with Higgs localized near TeV brane







constraints on Bulk RS models

from:

- **EW precision data** via Oblique parameters S T U
- FCNC (K physics, CPV, B physics, rare decays)
- $Z \rightarrow b_L b_L$ i.e. (t_L, b_L) not too close to TeV brane

and with various symmetries in the bulk

- larger bulk gauge symmetry i.e. $SU(2)_{R} \times U(2)_{R} \times U(1)_{Y}$, $SO(5) \times U(1)$,
- flavor symmetries

→ KK gauge mass > 3 TeV

KK graviton mass > 2 - 4 TeV dependent on specific models

w/o fermions in bulk and bulk symmetry > 23 TeV

→ Fermionic excitations > 1 – 2 TeV

Additional SU(2) doublet states with exotic charge (5/3) 0.5 – 0.8 TeV

constraints on Bulk RS models

from:



Additional SU(2) doublet states with exotic charge (5/3) 0.5 – 0.8 TeV

Bulk RS models signatures

- KK graviton

$$g g \to G \to t \overline{t}$$

$$g g \to G \to W_L W_L \to l \nu j j$$

$$g g \to G \to W_L W_L \to e^{\pm} \mu^{\mp} 2 \nu$$

$$g g \to G \to Z_L Z_L \to 4 l$$

- KK Gluon

 $pp \rightarrow g^{(1)} \rightarrow t \ \overline{t}$

- KK EW neutral gauge boson

$$p p \rightarrow Z' \rightarrow W W \rightarrow 2l 2v$$

$$\rightarrow l v j j$$

KK EW charged gauge bos

$$pp \rightarrow W' \rightarrow t \overline{b} \rightarrow W \overline{b} b \rightarrow l v \overline{b} b$$

$$pp \rightarrow W'^{+} \rightarrow W^{+} h$$

- KK fermions (e.g.)

Davoudiasl, Hewett, Rizzo, PLB 473 (2000) 43 Grossman, Neubert, PLB474 (2000) 361 Pomarol, PLB 486 (2000) 153 Chang, Hisano, Okada, Yamaguchi, PRD62, 084025 Randall, Schwartz, JHEP 11 (2001) 003 Huber, Shafi PRD 63, 045010, PLB 498 (2001) 256 Randall, Schwartz, PRL 88 (2002) 081801 Csaki, Erlich, Terning, PRD66 (2002) 064021 Hewett, Petriello, Rizzo, JHEP 09 (2002) 030 Agashe, Delgado, May, Sundrum, JHEP08 (2003) 050 Carena, Delgado, Ponton, Tait, Wagner, PRD68, 035010, PRD71, 015010 Carena, Ponton, Santiago, Wagner, NPB 759 (2006) 202, PRD76, 035006 Skiba, Tucker-Smith, PRD75, 115010 Aguilar-Saavedra, PLB 625 (2005) 234, PLB 633 (2006) 792 Agashe, Contino, Darold, Pomarol, PLB 641 (2006) 62 Fitzpatrick, Kaplan, Randall, Wang, JHEP 09 (2007) 013 Agashe, Davoudiasl, Perez, Soni, PRD76, 036006 Holdom, JHEP 03 (2007) 063 Antipin, Atwood, Soni, PLB 666 (2008) 155 Antipin, Soni, JHEP10 (2008) 018 Lillie, Randall, Wang, JHEP 09 (2007) 074 Agashe, Belyaev, Krupovnickas, Perez, Virzi, PRD 77, 015003 Allanach, Mahmoudi, Skittrall, Sridhar, arXiv:0910.1350 Baur, Orr. PRD 77, 114001 Guchait, Mahmoudi, Sridhar, JHEP05 (2007) 103, PLB 666 (2008) 347 on Lillie, Shu, Tait, PRD 76, 115016 Carena, Medina, Panes, Shah, Wagner, PRD 77, 076003 Agashe, Davoudiasl, Gopalakrishna, Han, Huang, Perez, PRD76, 115015 Djouadi, Moreau, Singh, NPB 797 (2008) 1 Contino Servant, JHEP 06 (2008) 026 Antipin, Tuominen, PRD 79, 075011 Aguilar, Aguilar-Saavedra, Moretti, Piccinini, Pittau, Treccani,

arXiv:0912.3799

 $pp \rightarrow g + g^{(1)} \rightarrow t^{(1)} \overline{t}^{(1)} \rightarrow W^+ b W^- \overline{b} \rightarrow l^- \nu b \overline{b} jj (l = e, \mu)$

Bulk RS models KK Graviton search

- KK Graviton close to TeV Brane
- 1st (and 2nd) generation fermion near Planck brane
 i.e. small coupling with 1st and 2nd quark generation
- gluon profile is flat
- t and b quark close to TeV brane



Fitzpatrick, Kaplan, Randall, Wang, JHEP 09 (2007) 013 Agashe, Davoudiasl, Perez, Soni, PRD76, 036006 Antipin, Atwood, Soni, PLB 666 (2008) 155 Antipin, Soni, JHEP10 (2008) 018





States with exotic charge (bulk RS)

MCHM₅ example : $SO(5) \times U(1)_X \times SU(3)_C$ as gauge symmetry in the RS bulk

 $SO(5) \times U(1)_X \times SU(3)_C$ broken down to $SO(4) \times U(1)_X \times SU(3)_C$ near IR brane with 4 pseudo Goldstone bosons identified with the Higgs doublet

 $SO(4) \approx SU(2)_L \times SU(2)_R$ enlarged to O(4) seen as the custodial symmetry

 $G_{SM} = SU(2)_L \times U(1)_Y \times SU(3)_C$ near UV brane and with $Y = X + T_3^R$

heaviness of top quark \Rightarrow lowest t_{KK} and lightest O(4) custodial partners (i.e. custodians) are significantly lighter than the other KK resonances

light custodians have e.m charges 5/3, 2/3, -1/3 they have mass roughly in the 500-1500 GeV range

Agashe, Delgado, May, Sundrum, JHEP08 (2003) 050 Agashe, Contino, Pomarol,, NPB 719 2005 165 Carena, Ponton, Santiago, Wagner, NPB 759 (2006) 202, PRD76, 035006 Contino, Darold, Pomarol,, PRD 75 2007 055014 Contino, Servant, JHEP 06 2008 026

States with exotic charge (bulk RS)





Contino, Servant, JHEP 06 2008 026

String states

assume fundamental scale is low (TeV) and fundamental theory is string theories

 \rightarrow strings scale Ms is low (TeV)

spectrum of string states made of 'zero' mass states and massive states

'zero' mass states \rightarrow graviton, anti-sym tensor field, dilaton (scalar)

+ others identified with SM fields

massive states \rightarrow (infinite number of) massive Regge excitations of various spinwith masses of order of string scale \rightarrow then here low (TeV) !

'correction' from Regge excitations : $\frac{s^2}{M_s^4}$, $\frac{t^2}{M_s^4}$, $\frac{u^2}{M_s^4}$ (back to pointlike particle limit when $s^2/M_s^4 \rightarrow 0$) 4-point amplitudes with Regge excitation : $O(g_s) \sim \frac{1}{25}$ i.e. bigger than the one from QFT with KK graviton exchange which is $O(g_s^2)$

also present in spectrum : KK AND winding excitations of the SM fields with masses near string scale, AND moduli

String states

Cullen, Perelstein, Peskin, PRD 62 (2000) 055012 Dudas, Mourad, NPB 575 (2000) 3 Anchordogui, Goldberg, Nawata, Taylor, PRL 100 (2008) 171603 Anchordoqui, Goldberg, Nawata, Taylor, arXiv:0804.2013 Anchordogui, Goldberg, Lust, Nawata, Stieberger, Taylor, PRL 101 (2008) 241803 Lust, Stieberger, Taylor, NPB 808 (2009) 1 Anchordogui, Goldberg, Lust, Nawata, Stieberger, Taylor, NPB 821 (2009) 181 Lust, Schlotterer Stieberger, Taylor, NPB 828 (2010) 139

dijets production via Regge excitations

Lust Int. J. Mod. Phys A26 (2011) 4686



excitations also possible

String states





Recent Results at CMS

- mono- photon, mono jet
- non resonant and resonant dilepton
- resonant dijet
- lepton + MET
- resonant diboson (W&Z)
- resonant bt and tt
- resonant HH
- exotic fermions
- black holes



mono-photon ("direct" ADD)

CMS-EXO-12-047













non resonant dilepton

CMS-EXO-12-027 CMS-EXO-12-031

("indirect" ADD)







non resonant dilepton

CMS-EXO-12-027

CMS-EXO-12-031

("indirect" ADD)

ADD k-factor	Λ_T [TeV] (GRW)	M_s [TeV] (HLZ)					
8		<i>n</i> = 2	n = 3	n = 4	n = 5	<i>n</i> = 6	n = 7
$\mu\mu$, $\sigma_{s,\mu\mu}$ < 0.25 fb (0.25 fb expected) at 95% CL							
1.0 (observed)	3.64	3.48	4.33	3.64	3.29	3.06	2.89
1.0 (expected)	3.65	3.50	4.34	3.65	3.30	3.07	2.90
1.3 (observed)	3.77	3.69	4.49	3.77	3.41	3.17	3.00
1.3 (expected)	3.78	3.70	4.50	3.78	3.42	3.18	3.01
ee, $\sigma_{\rm s,ee} < 0.19$ fb (0.19 fb expected) at 95% CL							
1.0 (observed)	3.90	3.72	4.64	3.90	3.52	3.28	3.10
1.0 (expected)	3.89	3.70	4.62	3.89	3.51	3.27	3.09
1.3 (observed)	4.01	3.99	4.77	4.01	3.63	3.37	3.19
1.3 (expected)	4.00	3.95	4.76	4.00	3.61	3.36	3.18
$\mu\mu$ and ee, per channel $\sigma_{ m s} < 0.12$ fb (0.12 fb expected) at 95% CL							
1.0 (observed)	4.01	4.14	4.77	4.01	3.63	3.37	3.19
1.0 (expected)	4.00	4.13	4.76	4.00	3.62	3.37	3.18
1.3 (observed)	4.15	4.35	4.94	4.15	3.75	3.49	3.30
1.3 (expected)	4.14	4.37	4.93	4.14	3.74	3.48	3.30



10-4

70

100

200

300 400

1000 200 m(ee) [GeV]

2000



resonant dilepton

PLB 714 (2012) 158

(RS, final state also suited to search for, TeV-1, Bulk RS) $ee(5.0fb^{-1})+\mu^+\mu^-(5.3fb^{-1})$ 10^{-4} 95% C.L. limit median expected 68% expected



 $m_{G_{KK}^{(1)}}$ > 1.81 TeV ($\tilde{k} = 0.05$)



resonant dijets

CMS-EXO-12-059

(RS, string states, final state also suited for search for TeV-1, Bulk RS)







resonant dijets

CMS-EXO-12-059

(RS, string states, final state also suited for search for TeV-1, Bulk RS)





resonant dijets (with b-jet)

CMS-EXO-12-023

(RS, bb final state also suited for search for TeV-1, Bulk RS)

- anti k_t 0.5 jets, $\eta < 2.5$, $|\Delta \eta| < 1.3$
- 3 channels : 0, 1, 2 b-tags





resonant dijets (with b-jet)

CMS-EXO-12-023

(RS, bb final state also suited for search for TeV-1, Bulk RS)



 $m_{G_{KK}^{(1)}}$ in the 1.42 - 1.57 TeV range is excluded







CMS-EXO-12-060



(TeV-1, UED, Bulk RS)



 $m_{W_{KK}^{(1)}}$ > 3.7 TeV (µ=10 TeV)





semi leptonic resonant diboson (ZZ)

CMS-EXO-13-009, arXiv:1405.3447

aiming at $G_{KK}^{RS} \rightarrow ZZ$



categorize into *ee* and $\mu\mu$ and low (LP) and high (HP) purity





for $m_{G_{KK}^{(1)}}$ in the 0.6–2.5 TeV range



semi-leptonic resonant diboson (WW)

CMS-EXO-13-009, arXiv:1405.3447

aiming at $G_{KK}^{RS} \rightarrow WW$



categorize into e v and μv and low (LP) and high (HP) purity







resonant diboson (jets channel)

CMS-EXO-12-024, arXiv:1405.1994

- 1 or 2 leading jet, **W/Z tagged**








resonant diboson (jets channel)

CMS-EXO-12-024, arXiv:1405.1994





resonant bt

CMS-B2G-12-010

(final state suited for search for TeV-1, Bulk RS)



 $m_{W'} > 2.03 \text{ TeV (obs)}$



 $m_{W'} > 2.09 \text{ TeV} (\exp)$



semileptonic tť

CMS-B2G-12-006



(bulk RS, also suited for search for TeV-1, RS)

- 2 analyses low/high mass coverage i.e. threshold/boosted
- transition at ~ 1 TeV
- for boosted analysis less isolation smaller b-tagged jet multiplicity higher 'wide' jet multiplicity jet substructure
- limits from the combination of the 2 analyses



 $m_{g_{KK}^{(1)}} > 2.54 \text{ TeV}$ $\sigma.Br(pp \rightarrow g_{KK}^{(1)} \rightarrow t\bar{t}) < 0.101 \text{ pb} (0.150_{-0.055}^{+0.072} \text{ pb expected})$ for $m_{g_{KK}^{(1)}} = 2 \text{ TeV}$



hadronic tť

CMS-B2G-12-005

(Bulk RS, final state also suited for search for TeV-1, RS)

- look at hadronically decaying boosted top quarks
- use a (boosted) top tagging algorithm





hadronic tť

CMS-B2G-12-005

(Bulk RS, final state also suited for search for TeV-1, RS)



obtain constraint on KK gluon mass *m*

 $m_{g_{KK}^{(1)}} > 1.8 \text{ TeV}$



resonant HH

HIG-PAS-12-032

(stabilized RS, Bulk RS, RS)

$X \to HH \to \gamma \gamma b \bar{b}$



 M_{radion} < 0.97 TeV excluded at 95% C.L. for Λ_R =1 TeV RS KK graviton excluded [340, 400] GeV at 95% C.L.





Exotic fermions (5 e/3)

CMS-B2G-12-012

(bulk RS)



 $M_{T_{5/3}}$ > 770 GeV



black holes

CMS-EXO-12-009, arXiv:1303.5338, jhep 07 (2013) 158





black holes

CMS-EXO-12-009, arXiv:1303.5338, jhep 07 (2013) 158



95 % CL lower limits on BH mass as a function of M_D

area below the curves are excluded



black holes

CMS-EXO-12-009, arXiv:1303.5338, jhep 07 (2013) 158







https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResults





Some propects at ILC



ADD direct



mono photon production

most sensitive

background from $e^+e^- \rightarrow \nu \bar{\nu} \gamma$

(with dominant W^+W^- intermediate state)

measured directly by modifying beam polarization

δ	2	3	4	5	6
$M_D(P_{-,+}=0)$	5.9	4.4	3.5	2.9	2.5
$M_D(P=0.8)$	8.3	5.8	4.4	3.5	2.9
$M_D(P = 0.8, P_+ = 0.6)$	10.4	6.9	5.1	4.0	3.3

sensitivity on M_D (TeV) at \sqrt{s} = 800 GeV





ADD indirect



 $e^+e^- \rightarrow f\bar{f}$ 2500 SM (a) e⁺e⁻→b⁻b 2000 angular distribution Events/bin 1500 $\lambda = \pm 1$ $\cos \theta$ dependent left-right asymmetry 1000 (if polarized beams are available) 500 assuming : 60 % b-tagging efficiency $\cos \theta$ -0.5 0.5 90 % electron beam polarization 75 fb^{-1} of integrated luminosity 0.5 $\lambda = \pm 1$ 0.0 KK graviton exchanges do not have the $1 + \cos^2 \theta$ shape 4 that is typical of the SM or any spin-1 exchange

-0.5

φ

-1

-0.5

Hewett, PRL 82 (1999) 4765

0.5

0

(b) e⁺e⁻→bb

 $\cos \theta$



ADD indirect



summing over e, μ, τ, c, b, t final states including τ polarization asymmetry

	\sqrt{s} (TeV)	\mathcal{L} (fb ⁻¹)	$\lambda = \pm$
LEP II	0.195	2.5	1.1
Linear collider	0.5	75	3.4
	0.5	500	4.1
	1.0	200	6.6
Tevatron	1.8	0.11	0.99
	2.0	2	1.3
	2.0	30	1.7
LHC	14	10	5.2
	14	100	6.0

reaches in TeV on M_s



TeV-1 extra dimensions



most likely below resonance → indirect effect

combining angular distributions and A_{LR}^{f} measurements using $f = e, \mu, \tau, b, c, t$ and assuming 90% beam polarization





TeV-1 extra dimensions



- if resonance mass is known from elsewhere (e.g. LHC)
- ⇒ couplings to fermions can be 'precisely' measured for example using $A_{LR}^{f=e,\mu\tau}$



Rizzo, PRD61 (2000) 055005



string states influences



influence on KK states production $e^+e^- \rightarrow \gamma G_{KK}$

stringy correction → enhancement of rate for graviton emission processes (by a common factor)

influence on Bhabha scattering $e^+e^- \rightarrow e^+e^-$



string states



E

string states influence on Bhabha scattering $e^+e^- \rightarrow e^+e^-$



Cullen, Perelstein, Peskin, PRD 62 (2000) 055012







$e^+e^- \rightarrow e^{(1)+}_{KK}e^{(1)-}_{KK} \rightarrow \gamma^{(1)}_{KK}e^+ \gamma^{(1)}_{KK}e^-$ i.e. $e^+e^- + \text{MET}$ final state



Bhattacharyya, Dey, Kundu, Raychaudhuri, PLB 628 (2005) 141







KK level 2 gauge boson exchange in $e^+e^- \rightarrow f \bar{f}$ with KK-number violating coupling



Riemann, eConf C 050318 (2005)0303, hep-ph/0508136









indirect effect if below resonance

Aguilar Saavedra et al. ,hep-ph/0106315



RS approaches





Davoudiasl, Hewett, Rizzo PRL 83 (2000) 2080



Higgs-graviscalars mixing



Higgs-graviscalars (only 1 in RS i.e. the radion) mixing and invisible Higgs decay



Giudice, Rattazzi, Wells, NPB 595 (2001) 250 see also Kubota, Nojiri, arXiv:1404.3013



summary



- present constraints from LHC8 and future contraints (discovery ?)
 from LHC13 have (will have) profound impact on the searches for
 for extra dimension at ILC
- few room left for direct searches at ILC
 polarization is very important in the few applicable cases
- ILC with polarization is good at measurements of indirect effects (ADD, TEV-1, RS)
- precision measurements of Higgs invisible width very important per se to explore some extra dimensions scenarii

BACKUP

Extra dimensions phenomenology

- K .R. Dienes, TASI lectures 2002
- C. Csaki, TASI lectures 2002, hep-ph/0404096
- A. Muck, diplomarbeit, 2001

Pioneering articles of (see specific references later on) :
I. Antoniadis, N. Arkani-Hamed, S. Dimopoulos, G. Dvali
R.K. Dienes, E. Dudas, T. Ghergetta
I. Antoniadis, K. Benakli, M. Quiros
L. Randall, R. Sundrum
W.D. Goldberger, M.B. Wise
T. Appelquist H.S. Cheng, B.A. Dobrescu

G.F. Giudice, R. Rattazzi, J.D. Wells NPB 544 (1999)

M.B. arXiv1005.2755, Acta Phys. Polon. B36 (2005) 3487 and CR phys. 4 (2003) 319

and references therein !

Some historical milestones

- 1914 G. Nordström : Maxwell equations in 5D recovering 4D EM + gravity
- 1915 A. Einstein, D. Hilbert : general relativity (GR) in 4D
- 1918 H. Weyl : attempt to use its geometrical formulation to unify EM and gravity leading to the gauge invariance concept
- 1919-1921 T. Kaluza : Einstein-Hilbert theory in 5D leading to Maxwell-Einstein theory
- 1926 O. Klein : Schrödinger equation in a 5D framework
- 1938 P. Bergmann, A. Einstein : emphasize the link between compactification and (abelian) gauge symmetry
- 1938 O. Klein : Einstein-Hilbert theory in more than 5D leading to the notion of non abelian gauge symmetry (Yang Mills 1954)

extra dimensions linked to the concept of unification of forces (gravity and EM) from the beginning

even more so in the context of supersymmetry, supergravity and superstrings

Some historical milestones

- 1971-1974 P. Ramond (2D), A. Neveu, J. Gervais, B. Sakita,
L. Susskind and Y. Golfand, E. Likhtman,
D. Volkov, A. Akulov and then J. Wess, B Zumino,
P. Fayet, beginning of supersymmetry (see also W. Heisenberg, L. Okun, R.M. Weiner in the 60's)

- 1974 J. Scherk, J. Schwarz, **beginning of string theories** for the description of the gravitational interaction (see also G. Veneziano 1968)

- 1976 V. A. Soroka, S. Deser, D.Z. Freedman, S. Ferrara, P. Van Nieuwenhuizen, B Zumino, **beginning of supergravity**

- 1978 E. Cremmer, B. Julia, J. Scherk, 11D supergravity

- 1974-1984 26D strings and 10D superstrings developments (type I and type Iia and IIb)

-1984 10D heterotic superstrings (SO(32) and E8xE8)

5 known 10D superstrings theories in total

Some historical milestones

- 1990 I. Antoniadis : possible extra dimensions at TeV scales

from considerations on superstrings in the non perturbative regime and supersymmetry breaking)

- 1995 C.M. Hull, P.K. Townsend M. J. Duff, E. Witten, J. Dai, R.G. Leigh, J. Polchinski C. Bachas, dualities (T-Duality het SO(32)/het E8xE8, S-Duality type I/het SO(32)) and branes (D-brane for type I and type II)
- 1996 E. Witten from duality arguments string scale not fixed at the Planck mass anymore but arbitrary (1 order of magnitude lower)
- 1996 P. Horava and E. Witten, Horava-Witten theory
 (11D bulk and 2 10D branes addressing susy breaking issues i.e. susy broken in one brane and transmitted to the other brane via bulk)
- 1996 J. Lykken : if string (fundamental) scale is arbitrary why not push it down to TeV values10D
- 1998 renewal of the idea of extra dimensions at TeV scale for low energy phenomenological purposes then for more

ADD direct searches





Fig. 3. The total jet + nothing cross section at the LHC integrated for all $E_{T,jet} > E_{T,jet}^{min}$ with the requirement that $|\eta_{jet}| < 3.0$. The Standard Model background is the dash-dotted line, and the signal is plotted as solid and dashed lines for fixed $M_D = 5$ TeV with $\delta = 2$ and 4 extra dimensions. The **a** (**b**) lines are constructed by integrating the cross section over $\hat{s} < M_D^2$ (all \hat{s}).

ADD direct searches



G.F. Giudice et al. /Nuclear Physics B 544 (1999) 3-38

Fig. 5. The total γ + nothing cross section at the LHC integrated for all $E_{T,\gamma} > E_{T,\gamma}^{\min}$ with the requirement that $|\eta_{\gamma}| < 2.5$. The Standard Model background is the dash-dotted line, and the signal is plotted as solid and dashed lines for fixed $M_D = 2$ TeV with $\delta = 2$ and 4 extra dimensions. The **a** (**b**) lines are constructed by integrating the cross section over $\hat{s} < M_D^2$ (all \hat{s}).

ADD direct searches



Fig. 6. The total γ + nothing cross section versus M_D at the LHC integrated for all $E_{T,\gamma} > 400 \text{ GeV}$ with the requirement that $|\eta_{\gamma}| < 2.5$. The Standard Model background is the dash-dotted line, and the signal is plotted as solid lines for $\delta = 2$ and 4 extra dimensions. The **a** (**b**) lines are constructed by integrating the cross section over $\hat{s} < M_D^2$ (all \hat{s}).

ADD indirect searches



G.F. Giudice et al. / Nuclear Physics B 544 (1999) 3-38

Fig. 10. The total cross section for $pp \rightarrow \gamma\gamma$ integrated for $\sqrt{\hat{s}} > M_{\gamma\gamma}^{\min}$ with the requirement that $E_{T,\gamma} > 50 \text{ GeV}$ and $|\eta_{\gamma}| < 2.5$ for each photon. The dashed line is the Standard Model background and the solid lines are the total cross sections for various values of Λ_T .

discriminating mUED w.r.t SUSY?

KK gauge bosons offer good prospects

prospects to discover level 2 structure

KK number conservating interactions (and KK-parity conserved) allows for

$$V_2 \rightarrow f_1 \overline{f}_1$$
 or $V_2 \rightarrow f_2 \overline{f}_0 = f_2 \overline{f}_{SM}$

kinematically not suppressed w.r.t pair production

Datta, Kong, Matchev, PRD75 (2005) 096006


mUED w.r.t SUSY?

- look for level 2 KK gauge bosons production including single production (KK number violation)

$$pp \rightarrow V_2 \rightarrow f_0 \overline{f}_0 = f_{SM} \overline{f}_{SM}$$

- double peak structure in dilepton mass
- near mass-degeneracy further corroborating UED interpretation w.r.t susy or Z'







open string sweeping out a 2d worldsheet (as τ increases) parameterized by σ and τ



closed string → the 2 endpoints of the open string tied together i.e. periodic conditions imposed

 $X^{\mu}(\tau,0) = X^{\mu}(\tau,\pi)$ $\frac{\partial X^{\mu}(\tau,0)}{\partial \sigma} = \frac{\partial X^{\mu}(\tau,\pi)}{\partial \sigma}$

closed string sweeping out a 2d worldsheet (as τ increases) parameterized by σ and τ



also embedded in a D dimensional spacetime X^{μ} ($\mu = 0, 1, 2 \dots D-1$)

	# of Q 's	# of ψ_{μ} 's	bosonic spectrum]		
IIA	32	2	NS-NS	$g_{\mu u},b_{\mu u},D$	1	closed strings	
	2		R-R	$A_{\mu}, C_{\mu u ho}$]∫	closed strings	
IIB	32	2	NS-NS	$g_{\mu u},b_{\mu u},D$	1	closed strings	
			R-R	$c^*_{\mu u ho\sigma},b'_{\mu u},D'$]]	closed sulligs	
heterotic	16	1		$g_{\mu u},b_{\mu u},D$	โ	alagad strings	
$E_8 \times E_8$			A^a_μ in adjoint of $E_8 \times E_8$]]	f closed strings	
heterotic	16	1		$g_{\mu u},b_{\mu u},D$	1	alagad strings	
SO(32)	1		A^a_μ in	adjoint of $SO(32)$]]	closed strings	
type I	16	1	NS-NS	$g_{\mu\nu}, D$	1	alaged and anon	
SO(32)			open string	A^a_μ in adjoint of $SO(32)$	1 }	ciosed and open	
			R-R	$b_{\mu u}$	ן ן	strings	

5 consistent fundamental string theories in 10 D

 D_p brane (or Dirichlet brane or D-brane) as a p-dimensional extended object on which open strings end (one or both) can be attached

string endpoints coordinates $X^{\mu}(\tau, \sigma)$ satisfy boundary conditions :

Dirichlet boundary conditions
$$\frac{\partial X^{\mu}}{\partial \tau}\Big|_{\sigma=0,\pi} = 0$$

integrating over τ specifies a spacetime location on which the string ends

Dirichlet boudary conditions are equivalent to fixing the endpoints of the string hence the name Dirichlet Brane

- Neumann boundary conditions

$$\frac{X^{\mu}}{\sigma}\bigg|_{\sigma=0,\,\pi}=0$$



in this case the ends of the string can sit anywhere in space

example of string duality

take type II closed string theories (D=10, N=2) and compactify one dimension on a circle of radius R \rightarrow this results into the appearance of :

- *m* massive winding modes with mass
- *k* massive Kaluza-Klein (KK) modes with mass :

$$: M^{2} = \frac{m^{2}R^{4}}{4}$$
$$: M^{2} = \frac{k^{2}}{R^{2}}$$

spectrum of modes invariant under $R \rightarrow \frac{2}{R}$

this T-duality of type IIA and type IIB closed string theories

for $R \rightarrow \infty$ winding modes are 'out' \Rightarrow quasi continuum of KK modesfor $R \rightarrow 0$ infinitely massive KK modes decouple 'out' \Rightarrow quasi continuum
of winding modes

T-duality exchanges the Neumann and Dirichlet boundary conditions



D-brane with one attached open string and one closed string moving in the bulk

- physics away from the D-brane can be described by a type II string theory
- everything happen as if the closed string 'feels' the hypersurface via closed-open string interactions

it is possible to assume that open string carries 'charges' at its enpoints

⇒ assume non-dynamical degrees of freedom at the endpoints in a way which preserves Poincare invariance and invariance of the worldsheet

in addition to the usual fock space labels of string state

- demand that each end of the string be in a state *i* or *j*
- demand that Hamiltonian of the states i = 1, ..., n is 0 so that they stay in the state that we originally put them in for all time



decompose open string wavefunction |k;ij> in a basis of λ_{ij}^a of $n \times n$ matrices as

$$|k;a\rangle = \sum_{i,j=1}^{n} |k;ij\rangle \lambda_{ij}^{a}$$

these matrices are called **Chan-Paton factors**

open string scattering amplitudes contain traces of products of Chan Paton factors

amplitudes are invariant under a global U(n) worldsheet symmetry under which the endpoint *i* transforms in the fundamental representation of U(n)

> global U(n) symmetry on the worldsheet can be promoted to a local U(n) gauge symmetry in spacetime

⇒ endpoints of open string carry gauge charges and describe gauge symmetries

- consider an open string with endpoints moving on p-dimensional hypersurface i.e. a D_p brane or D-brane
- under which the endpoint *i* transforms in the fundamental representation of U(n)
- 'zero' mass state of the open string are :
 - 1 vector (see the table few slides above the bosonic content of the open string zero mass states of the type I string theory)
 - 1 spinor
- forming a supermultipet of a supersymmetric gauge theory with gauge group U(1)
- the zero mass boson moves as a U(1) gauge boson in the p-dimensional D-brane
- the 10-p remaining components appear as scalars in the 'bulk'

stack of N coincident D-branes corresponds to an unbroken U(N) gauge symmetry whose effective action is a 10D U(N) SYM theory reduced to p dimensions D-branes brake half of the supersymmetries

some examples with two D-branes

- → open string with both endpoints on the D-brane gives a $U(1) \times U(1)$ theory
- → open string stretching between two D-branes with one endpoint on one D-brane and the other one on another D-brane **parallel** to the first one with a distance given by the string length also gives a $U(1) \times U(1)$ theory
- → if the two branes coincide (string length going to zero giving rise to new massless states) the gauge group becomes U(2)
- a 2 coincident branes separation viewed as a symmetry breaking $U(2) \rightarrow U(1) \times U(1)$
- U(2) symmetry restauration when the 2 parallel branes become coincident
- → interesting configurations:
 - 5 coincident D-branes or **stack** of 5 D-branes giving U(5)
 - stack of 3 D-branes + stack of 2 D-branes + 1 D-brane give $U(3) \times U(2) \times (U1)$



D-branes brake half of the supersymmetries

'far' from the D-brane (bulk)

- physics can be described by a type II closed string theory
- D-brane 'sees' only the type II (B) string spectrum
- in particular it 'sees' its 2 gravitinos (recall we have N=2 in 10 D for type II)

'closer' to the brane 'sees' only a linear combination of the 2 gravitinos

- which is the gravitino of the type I theory (recall we have N=1 in 10 D for type I
- this defines one the duality 'symmetry' between string theories (called Ω projection) here between type IIB and type I

D-brane responsible for: $N = 2 \rightarrow N = 1$

i.e. half of the supersymmetry breaking



vacuum without D-brane is invariant under 10D N=2 susy state with D-brane invariant under 10D N=1 susy only this is a called a BPS state (Polchinski hep-th/9510017, hep-th/9611050)

stack of D-branes can break supersymmetry further



exchange of a closed string between two D-branes

equivalently a vacuum loop of an open string with one end on each D-brane



D-branes or stack of D-branes can intersect at right angles or at (any) angles

- → can preserve a supersymmetry
- → scalars and **chiral** fermions **localized at branes intersections**
- → SM-like susy or non-susy model building often with extra U(1) i.e. Z', extra exotic chiral matter (large literature on this)



Bachas, hep-th/9503030,,Berkooz, Douglas, Leigh, hep-th/9606139

D-branes or stack of D-branes can intersect at right angles or at (any) angles

- → can preserve a supersymmetry
- → scalars and **chiral** fermions **localized at branes intersections**
- → SM-like susy or non-susy model building often with extra U(1) i.e. Z', extra exotic chiral matter (large literature on this)



Bachas, hep-th/9503030,,Berkooz, Douglas, Leigh, hep-th/9606139





all SM invariances and Poincare invariance on the TeV brane are still fulfilled if one add the following term to the SM lagrangian :

$$S_{\xi} = \xi \int dx^4 \sqrt{g_{\text{induced}}} R(g_{\text{induced}}) \Phi^{\dagger} \Phi$$

mixing the Ricci scalar from the 4D induced metric on the TeV brane and the Higgs field Φ

- → gives additional effective contribution to the SM $T^{\mu\nu}$ (which is a total divergence)
- → $T^{\mu\nu}$ still conserved (invariances are unchanged)
- → contribution ressembling to the one generically coming from dilatation invariance (4d conformal invariance)

⇒ mixing term between Higgs and curvature

- Higgs-graviscalar mixing (ADD)
- Higgs-radion mixing (stabilized RS)

example of the dilatation invariance from the current $j_{\nu}^{(D)} = x^{\mu}T_{\mu\nu}$

which is conserved **classically** i.e. $\partial^{\mu} j_{\mu}^{(D)} = T_{\mu}^{\mu} = 0$ (trace of $T_{\mu\nu}$ is zero)

$$\phi^4$$
 theory $\rightarrow \xi = \frac{1}{6}$

(see P. Ramond : Field theory a modern primer p30-33 Gursey : Ann. of Phys. 24 (1963) 211 Coleman Jackiw: Ann. of Phys. 67 (1971) 552

QCD (with m=0) is **classically** invariant but with quantum corrections $T^{\mu\nu}_{QCD}$ is not traceless anymore T^{μ}_{μ} given by the trace anomaly

(see for example M. Shifman Phys. Rep. 209 (1991) 341)

more convenient to express radion field in terms of a field ϕ with : $\phi \equiv \Lambda_{\phi} e^{-k\pi(T-r_c)}$

with
$$\Lambda_{\phi} = \langle \phi \rangle = \sqrt{\frac{24 M_5^3}{k}} e^{-k\pi r_c}$$

integrating over the 5th dimension one gets a canonically normalized effective action

$$S_{\phi} = \int d^4 x \sqrt{-g} \left[\frac{2M_5^3}{k} \left(1 - \frac{\phi^2}{\Lambda_{\phi}^2} e^{-2k\pi r_c} \right) R + \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi - V(\phi) + \left(1 - \frac{\phi}{\Lambda_{\phi}} \right) T_{\mu}^{\mu} \right]$$

 $T^{(1)\mu}_{\mu} = 6\,\xi\,\nu \ \Box h$

$$T_{\mu}^{(2)\mu} = (6\xi - 1)\partial_{\mu}h\partial^{\mu}h + 6\xi h \Box h + 2m_{h}^{2}h^{2} + m_{ij}\overline{\Psi}_{i}\Psi_{j} - M_{V}^{2}V_{A\mu}V_{A\mu}^{\mu}$$

 $T^{(1)\mu}_{\mu}$ induces a kinetic mixing between ϕ and h

fields re-defined by :

 $\phi = (\sin \theta - \sin \rho \cos \theta) h' + (\cos \theta + \sin \rho \sin \theta) \phi'$ $h = \cos \rho \cos \theta h' - \cos \rho \sin \theta \phi'$

with
$$\tan \rho \equiv \frac{6 \xi v}{\Lambda_{\phi}}$$
 and $\tan 2 \theta \equiv \frac{2 \sin \rho m_{\phi}^2}{\cos^2 \rho \left(m_{\phi}^2 - m_h^2\right)}$

new fields ϕ' and h' are mass eigenstates with eigenvalues :

$$m_{\phi',h'}^2 = \frac{1}{2} \left[(1 + \sin^2 \rho) m_{\phi}^2 + \cos^2 \phi m_h^2 \pm \sqrt{\cos^4 \rho (m_{\phi}^2 - m_h^2)^2} + 4 \sin^2 \rho m_{\phi}^4 \right]$$



 $m_h = 125 \text{ GeV}, \Lambda_{\phi} = 10 \text{ TeV}, \xi = 0$

 $m_h = 125 \text{ GeV}, \ \Lambda_{\phi} = 10 \text{ TeV}, \ \xi = 1/6$



 $m_h = 125 \text{ GeV}, \Lambda_{\phi} = 10 \text{ TeV}, \xi = 0$

 $m_h = 125 \text{ GeV}, \ \Lambda_{\phi} = 10 \text{ TeV}, \ \xi = 1/6$



 $m_h = 125 \text{ GeV}, \ \Lambda_{\phi} = 10 \text{ TeV}$

$$R_{S}^{\gamma\gamma}(\phi') = \frac{\Gamma(\phi' \rightarrow gg)}{\Gamma(h_{SM} \rightarrow gg)} \frac{B(\phi' \rightarrow \gamma\gamma)}{B(h_{SM} \rightarrow \gamma\gamma)} \sqrt{\frac{\max(\Gamma_{tot}(h_{SM}), \Delta M_{\gamma\gamma})}{\max(\Gamma_{tot}(\phi'), \Delta M_{\gamma\gamma})}}$$



 $m_h = 125 \text{ GeV}, \ \Lambda_{\phi} = 10 \text{ TeV}$

$$R_{S}^{4l}(\mathbf{\phi}') = \frac{\Gamma(\mathbf{\phi}' \mathbf{a} g g)}{\Gamma(h_{SM} \mathbf{a} g g)} \frac{B(\mathbf{\phi}' \mathbf{a} Z Z)}{B(h_{SM} \mathbf{a} Z Z)} \sqrt{\frac{\max(\Gamma_{tot}(h_{SM}), \Delta M_{4l})}{\max(\Gamma_{tot}(\mathbf{\phi}'), \Delta M_{4l})}}$$



 $m_h = 125 \text{ GeV}, \ \Lambda_{\phi} = 10 \text{ TeV}$

Higgs radion mixing term also in the context of type I strings theory and D-branes mixing between brane fluctuations (branons) and closed string excitations modes of the type I theory (containing gravitons, graviphoton, dilaton, graviscalar) described in terms of mixing of open and closed strings excitations modes

several possible configurations

- Higgs identified to excitations of open string with both ends attached to same stack of D-branes

- → Higgs-graviscalar mixing (but also Higgs-graviphoton)
- \rightarrow effective conformal coupling
- \rightarrow 4D effective theory as a N=4 SYM conformal theory
- Higgs identified to excitations of open string with one end attached to one brane and the other end to another brane
 - → Higgs-graviscalar mixing disappears but Higgs-graviphoton mixing stays
- Higgs localized at the (orthogonal) intersection of 2 branes
 - \rightarrow Higgs-graviphoton mixing disappears

effective conformal coupling

$$\boldsymbol{\xi} = \sqrt{\frac{\boldsymbol{\delta} + 5}{6 \, \boldsymbol{\delta} (\boldsymbol{\delta} - 1)}}$$

 $\begin{aligned} \delta &= 2 & \xi \sim 0.76 \\ \delta &= 3 & \xi \sim 0.47 \\ \delta &= 6 & \xi \sim 1/4 \end{aligned}$

Antoniadis, Sturani, NPB 631 (2002) 66



Bulk RS models: KK gluon in all hadronic mode



Bulk RS models : KK gluon in all hadronic mode



The nesonance Mass (GeV/C)		True	Resonance	Mass	(GeV/c^2)
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Mass and Width	Background	$\epsilon \cdot \mathbf{A} \cdot \mathbf{BR}$	95% C.L. limit	3σ Evidence	5σ Discovery
(GeV/c^2)	(events)	(%)	(pb)	(pb)	(pb)
M = 1000, w = 10	2.18 ± 0.90	0.34 ± 0.05	17.2	23.0	43.6
M = 2000, w = 20	5.81 ± 2.18	6.06 ± 0.85	1.45	2.18 t	3.99 tu
M = 3000, w = 30	0.95 ± 0.41	6.21 ± 0.88	0.74	0.97	1.62
M = 4000, w = 40	0.11 ± 0.12	4.62 ± 0.66	0.75	0.62 🗘	1.27 ^{LO}
M = 1000, w = 100	2.18 ± 0.90	0.30 ± 0.05	19.3	25.7 g	48.6 ⁸⁸
M = 2000, w = 200	9.04 ± 3.31	4.90 ± 0.69	2.30	3.46 ¹	6.32 t
M = 3000, w = 300	2.04 ± 0.79	4.25 ± 0.61	1.34	1.87	3.28
M = 4000, w = 400	0.98 ± 0.41	2.21 ± 0.34	2.13	2.73	5.00

Bulk RS models

Lillie, Randall, Wang, JHEP 09 (2007) 074 Agashe, Belvaev, Krupovnickas, Perez, Virzi, PRD 77, 015003 Guchait, Mahmoudi, Sridhar, JHEP05 (2007) 103, PLB 666 (2008) 347

> Lillie, Shu, Tait, PRD 76, 115016 Carena, Medina, Panes, Shah, Wagner, PRD 77, 076003 Baur, Orr, PRD 77, 114001 Allanach, Mahmoudi, Skittrall, Sridhar, arXiv:0910.1350

> > m,,/GeV

KK gluon $p p \rightarrow g^{(1)} \rightarrow t \overline{t} \rightarrow b \overline{b} j j l \nu$ background: SM $t \overline{t}$, single top, W+jets $\frac{d\sigma}{dm_{tr}}(pp \rightarrow t\bar{t} \rightarrow b\bar{b}Ivjj)$ # of events / 200 GeV 00 **for 100 pb⁻¹** $M_{e^{(1)}} = 3 TeV S / \sqrt{B} \approx 11$ $\int Ldt = 100 \text{ fb}^{-1}$ $M_{g^{(1)}} = 4 TeV S / \sqrt{B} \approx 4.2$ $\downarrow M_{o^{(1)}} = 3 TeV$ Signal + Background reach < 4 TeV Background 2500 m_{tt} / GeV 1000 1500 2000 3000 3500 **asymmetry** $2 \times \frac{N_+ - N_-}{N_+ + N_-}$ $M_{g^{(1)}} = 3 TeV$ N_ number of positron 0.5 along direction of top-quark boost (in top pair c.m) N-¹N⁺N expect strong bias towards RH top -0.5 PLR from KK gluon decay $Ldt = 100 \text{ fb}^{-1}$ total reconstructed total partonic SM prediction 1800 2000 2400 2600 2800 3000 3400 2200 3200 3600

Bulk RS models

Lillie, Randall, Wang, JHEP 09 (2007) 074 Agashe, Belyaev, Krupovnickas, Perez, Virzi, PRD 77, 015003 Allanach, Mahmoudi, Skittrall, Sridhar, arXiv:0910.1350

KK gluon

 $p p \rightarrow g^{(1)} \rightarrow t \overline{t} \rightarrow b \overline{b} j j l \nu$

Selection	Variables	Cuts	
Kinematic and acceptance	Lepton	$p_T > 10 \text{ GeV}, \eta < 2.5$	
	≥ 2 jets	$p_T > 30 \text{ GeV}, \eta < 2.5$	
	Tagged <i>b</i> -jets	≥ 1	
	Missing energy (ν)	$p_T^{\text{miss}} > 20 \text{ GeV}$	
	Lepton isolation	$\Delta R \ge 0.4 \text{ (non-}b \text{ jets)}$	
	b-jet lepton isolation	$\Delta R \ge 0.4 \text{ or } m_{bl} \ge 40 \text{ GeV}$	
Reconstruction quality	$ M_W^{\rm had} - M_W $	<50 GeV	
for $\#$ jets > 2,	$ M_t^{\rm had} - M_t $	<50 GeV	
2 <i>b</i> -jets required	$ M_t^{\text{lep}} - M_t $	<50 GeV	
Reconstruction quality	$ M_t^{\text{lep}} - M_t $	<50 GeV	
a b -jet + t -jet	"Top jet"	$p_{T'} > 800 \text{ GeV}$	

one could use in addition the fowardness of the SM $t \overline{t}$

i.e. dominant production via gluon fusion more forward

KK gluons produced by quark annihilation



 $\rightarrow WW \rightarrow 2l_{2V}$ sensitivity up to 2 fev (5 fev) with 100 fb (1 ab or $\rightarrow l_{V}jj$ luminosity upgrade crucial

luminosity upgrade also crucial for associate production with heavy quarks
Bulk RS models

Warped EW charged gauge bosons





Bulk RS modelsWarped EW charged gauge boson decay

i) t_R close-to-flat profile in bulk and $(t,b)_L$ profile close to TeV brane

ii) vice versa





Bulk RS models

1 example of KK fermions search

 $pp \rightarrow g + g^{(1)} \rightarrow t^{(1)} \overline{t}^{(1)} \rightarrow W^+ b W^- \overline{b} \rightarrow l^- \nu b \overline{b} jj (l = e, \mu)$

Backgrounds :

SM model top pair prod. and W/Z + jets top pair prod. from KK gluon decay (!)

high pT lepton, high pT jets, MET, Ht, 2b-tags, single jet from boosted W and Wb system requirement i.e. bottom having biggest ΔR w.r.t W



Aguilar-Saavedra, PLB 625 (2005) 234, PLB 633 (2006) 792 Carena, Ponton, Santiago, Wagner, NPB 759 (2006) 202 Holdom, JHEP 03 (2007) 063 Skiba, Tucker-Smith, PRD75, 115010 Carena, Medina, Panes, Shah, Wagner, PRD 77, 076003 Contino Servant, JHEP 06 (2008) 026





resonant dijets (with b-jet)

CMS-EXO-12-023

tagging rates





Bulk RS models: KK gluon in all hadronic mode



semi leptonic resonant diboson (ZZ)



categorize into *ee* and $\mu\mu$ and low (LP) and high (HP) purity



 $m_{G_{KK}^{(1)}} > 710$ GeV

semi-leptonic resonant diboson (WW)

CMS-EXO-12-021

aiming at $G_{KK}^{RS} \rightarrow WW$







 $\sigma \cdot BR < 70 \text{ fb} - 3 \text{ fb}$ for $m_{G_{KK}^{(1)}}$ in the 0.8-2.5 TeV range



categorize into e v and μv and low (LP) and high (HP) purity



ADD indirect







