

# Measurement of the top quark mass and couplings at Linear Colliders

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On behalf of the ILC Physics and Detector Study and CLICdp



37<sup>th</sup> INTERNATIONAL CONFERENCE  
ON HIGH ENERGY PHYSICS

2 - 9 - JULY - 2014 - VALENCIA



# OUTLINE

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Compact Linear Collider (CLIC)

Motivation

## 2. Top quark mass measurement at threshold

Precision in the measurement of the top quark mass

The  $t\bar{t}$  threshold

Event generation, detector simulation and reconstruction

Measurement of the  $m_t$  and  $\alpha_s$  at CLIC and ILC

## 3. Top quark electroweak couplings

Top quark electroweak couplings at ILC

Event generation, detector simulation and reconstruction

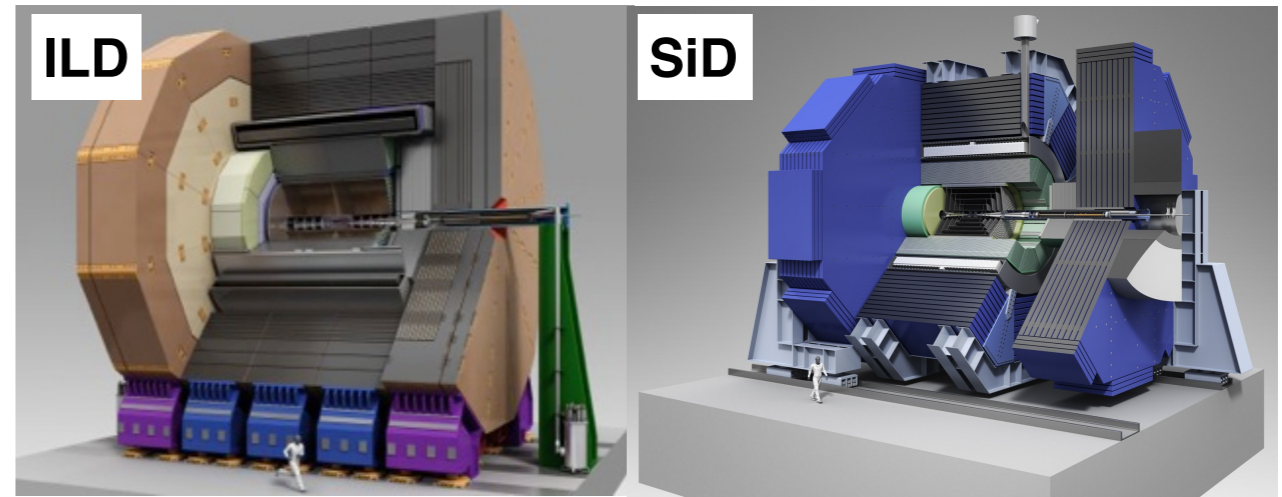
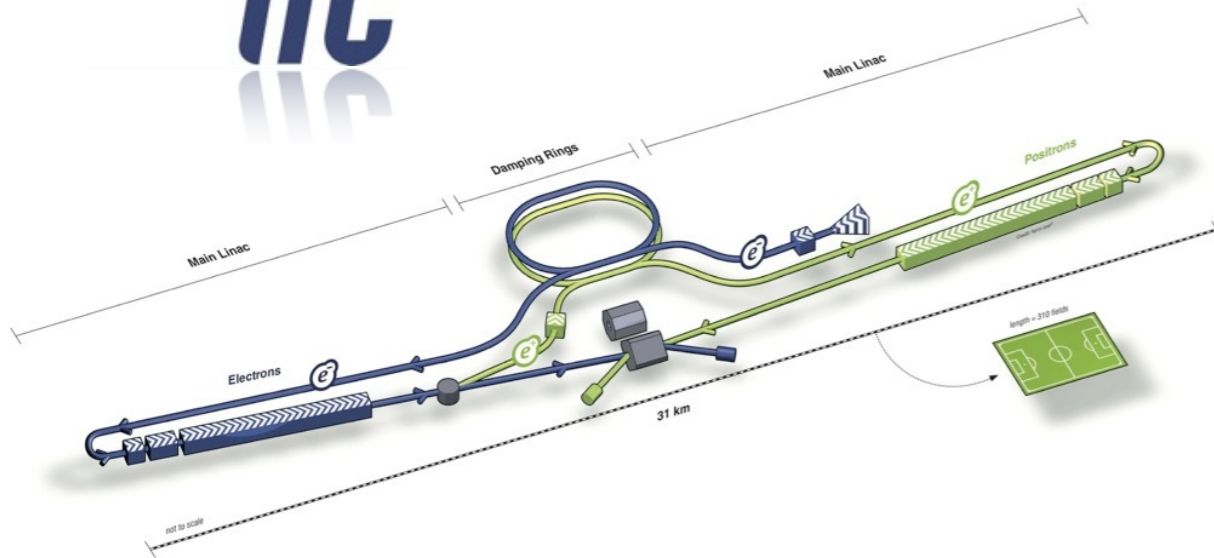
Observables

Sensitivities for the top electroweak couplings at ILC

## 4. Summary and conclusions



# International Linear Collider (ILC)



**ILD** and **SiD** detectors are optimised for:  
**Particle Flow Algorithm (PFLOW)**

## Electron positron collisions

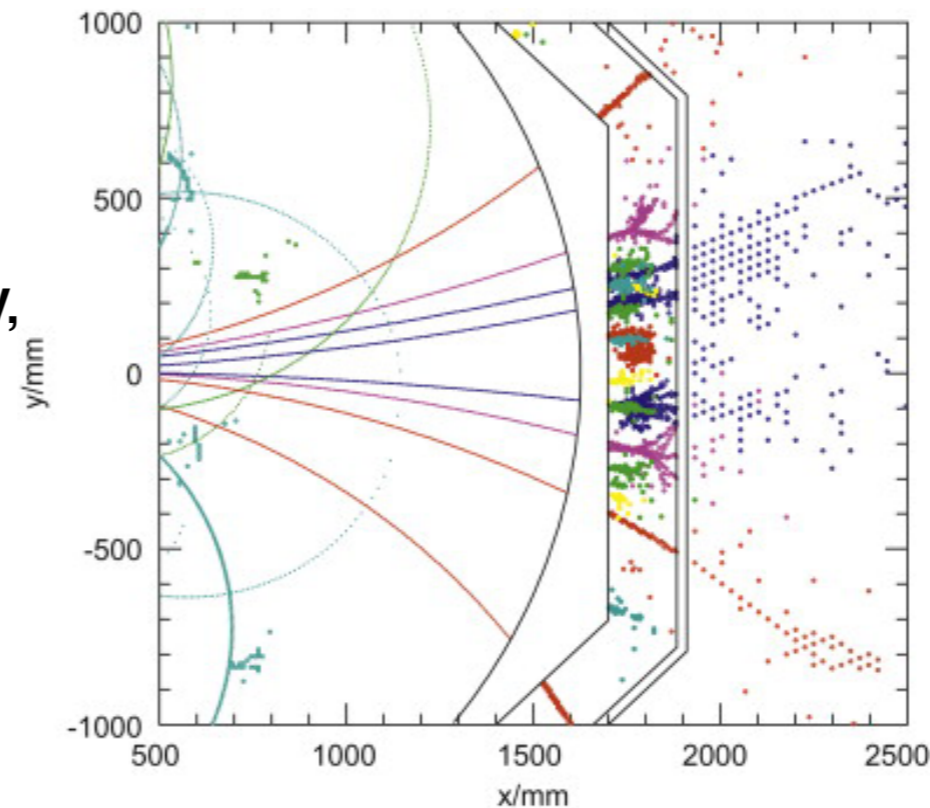
Superconducting acceleration technology

$E_{\text{cms}}$  tuneable between **200 GeV** and **500 GeV**,  
possible upgrade to **1 TeV**

Integrated  $\mathcal{L} = 500 \text{ fb}^{-1}$  (2 years of running)

Beams are polarised:  
 $P(e^-) \approx \pm 80\%$  ,  $P(e^+) \approx \pm 30\%$

About **31 km** site length



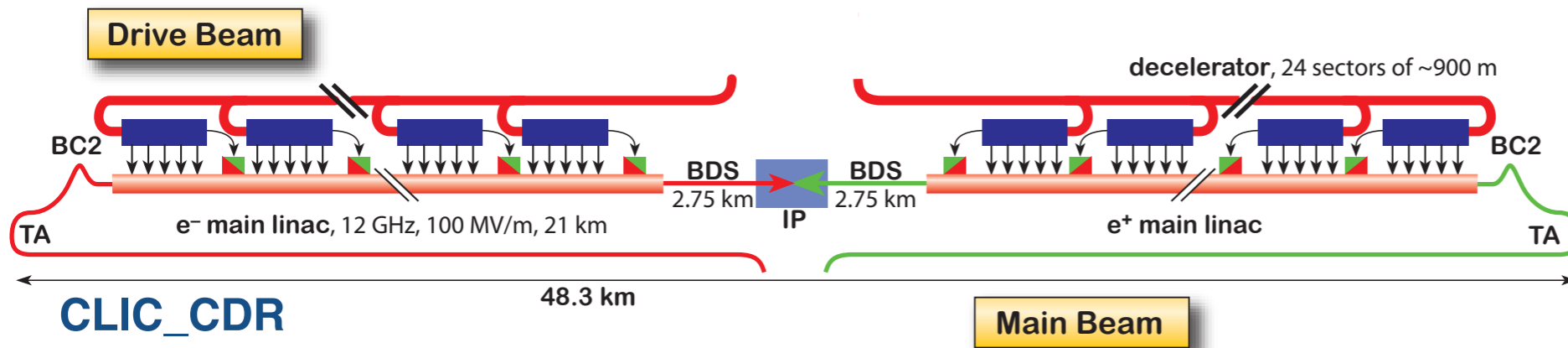
The **energy of charged hadrons** will be measured by the **tracking detectors**

The **energy of photons** will be measured by the **electromagnetic calorimeter**

The **hadronic calorimeter** is then used only to measure the **energy of neutral hadrons**



# Compact Linear Collider (CLIC)

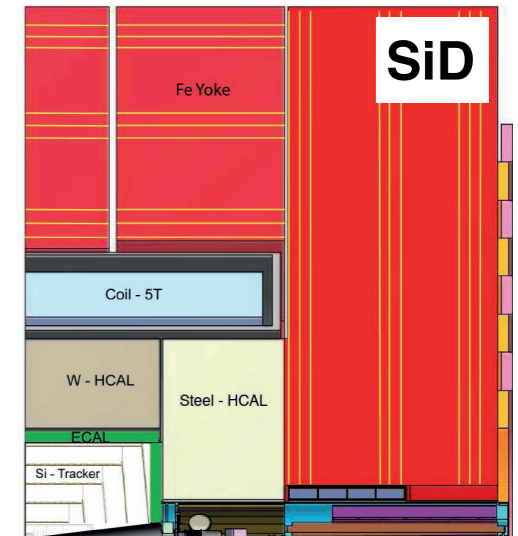
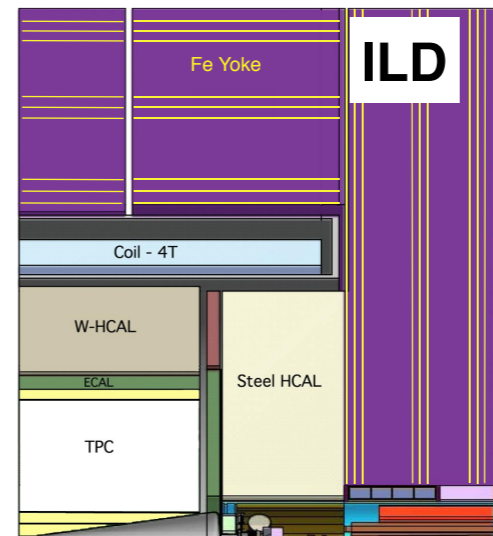


Electron-positron collider in the **multi-TeV** energy range

About **48 km** site length

The c.o.m. energy:  $\sqrt{s} = 3 \text{ TeV}$  (default design)  
500 GeV - 1.5 TeV

Luminosity:  $\mathcal{L} = 2 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$



A **CLIC\_ILD** and **CLIC\_SiD** detector concepts have been developed from the ILD and SiD detector concepts for ILC

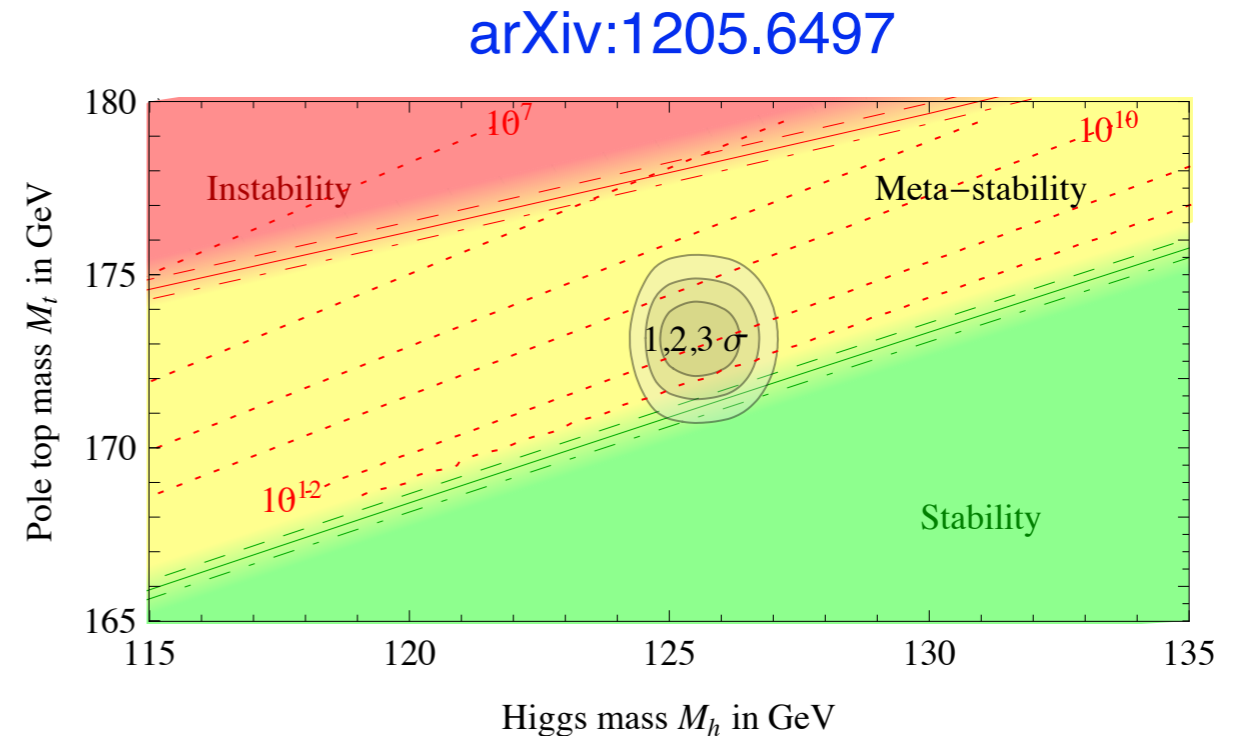
Modifications motivated by the **more challenging experimental conditions** at CLIC and by the **higher collision energy**

Intense R&D in the CLIC collaboration to fully develop two-beam acceleration at high gradients

# Motivation

## Top quark mass

- A small change in  $M_h$  and  $M_t$  can **drastically modify** the conclusions regarding **vacuum stability**
- $M_t$  must be characterised well



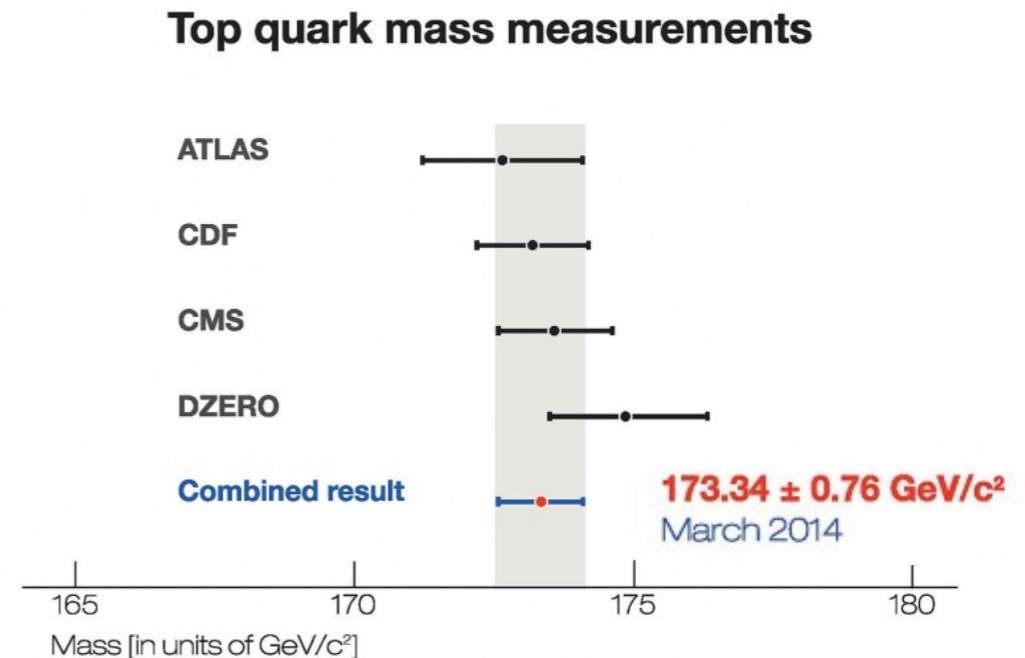
## Top quark electroweak couplings

- **Learn about BSM** physics from the deviations observed on Higgs and top EW couplings.
- LHC cannot achieve enough accuracy in the measurement of the coupling deviations -> **ILC accuracies** are needed to access to **fully significant deviations**  
[arXiv:1403.2893](#)

# Precision in the measurement of the top quark mass

- **Hadron colliders** achieve precisions in the measurement of the top mass of  $\sim 0.76 \text{ GeV}$

Historical result, first ever LHC/Tevatron Combination [arXiv:1403.4427]



- At **linear colliders** there are **two techniques** to determine the mass of the top quark

## 1. Direct reconstruction of top from its decay products (above threshold)

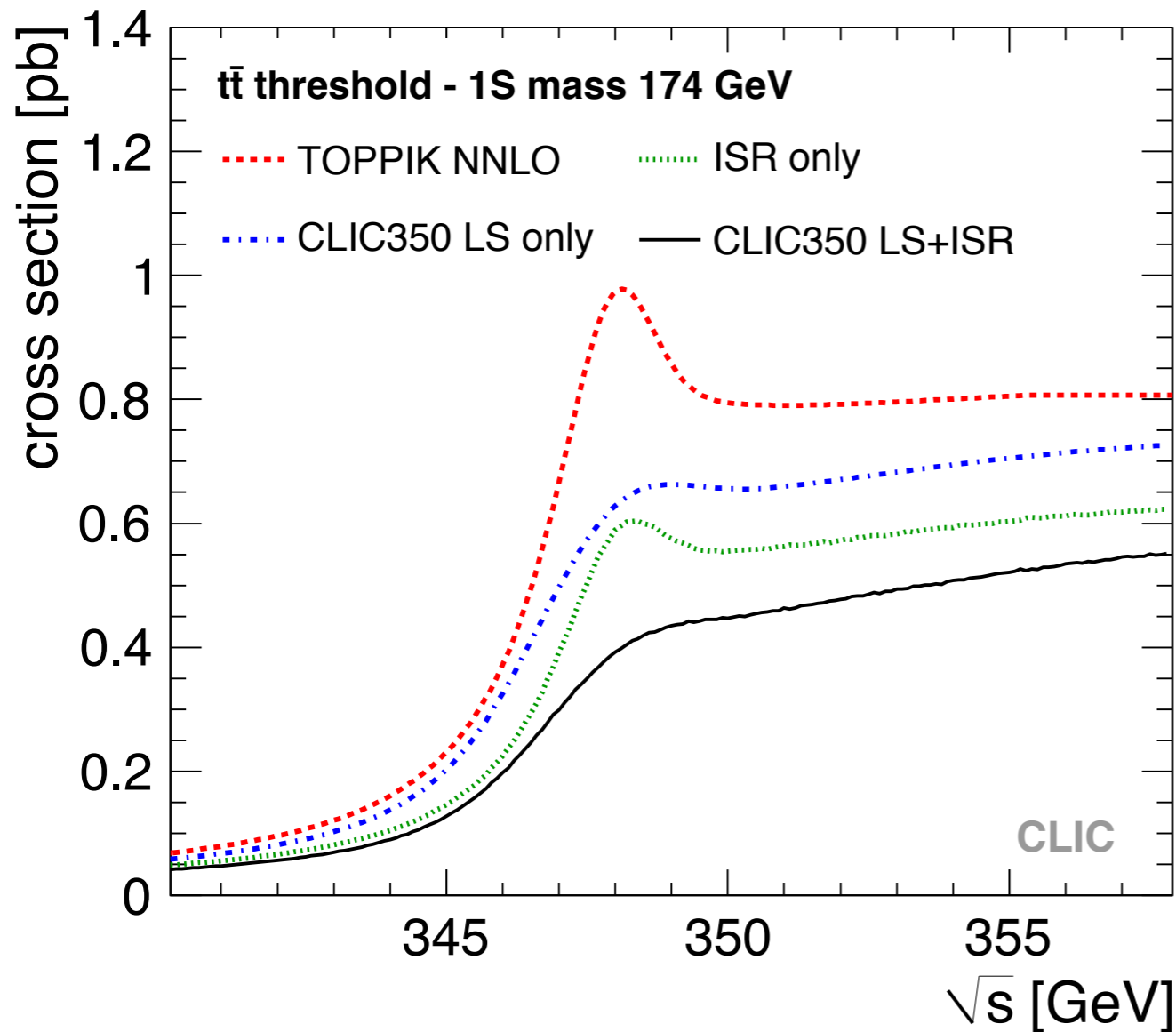
**Experimentally well-defined** but the generated mass is **not well-defined theoretically** and non-perturbative corrections could be substantial

## 2. A scan of the top pair production threshold

**High degree of precision** using a **theoretically** well-defined top mass (**1S mass**, can be transformed into other mass schemes). Precise top mass measurement with **well-controlled theory uncertainties**

See details about the **1S mass scheme**: [arXiv:hep-ph/9904468v2](https://arxiv.org/abs/hep-ph/9904468v2)

# The $t\bar{t}$ threshold



- Top mass input **174 GeV** in the **1S mass scheme** and  $\alpha_s = 0.118$
- **NNLO calculations** provided by the code *TOPPIK*
- Corrections for **ISR** and **luminosity spectrum**
- These corrections result in a **smearing of the cross section** peak at threshold

- The **smearing** is due to the **statistical efficiency**, reduced by the luminosity spectra. Not affected by systematics.

# Event generation, detector simulation and reconstruction

$e^+e^- \rightarrow t\bar{t}$  production at threshold CLIC@352 GeV

$m_t = 174.0$  GeV

$\Gamma_t = 1.37$  GeV

## 1. Generated events (signal + background)

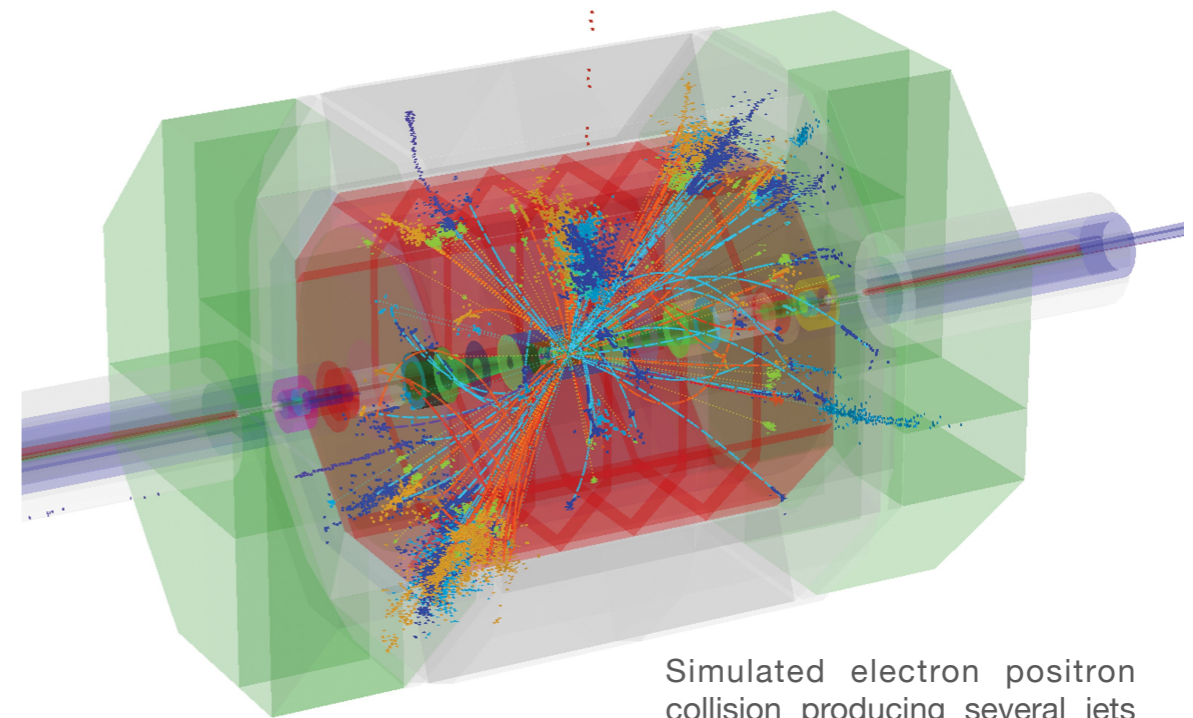
Pythia:  $e^+e^- \rightarrow t\bar{t}, WW, ZZ$

+ beam backgrounds are included

WHIZARD:  $e^+e^- \rightarrow q\bar{q}, q\bar{q}e^+e^-, q\bar{q}\nu$

## 2. Simulation of the detector

Full simulation with high level of realism



Simulated electron positron collision producing several jets in the ILD-like detector at CLIC

## 3. Reconstruction

Standard algorithms

**Kinematic fitting:** Grouping W-bosons and b-jets into top quarks

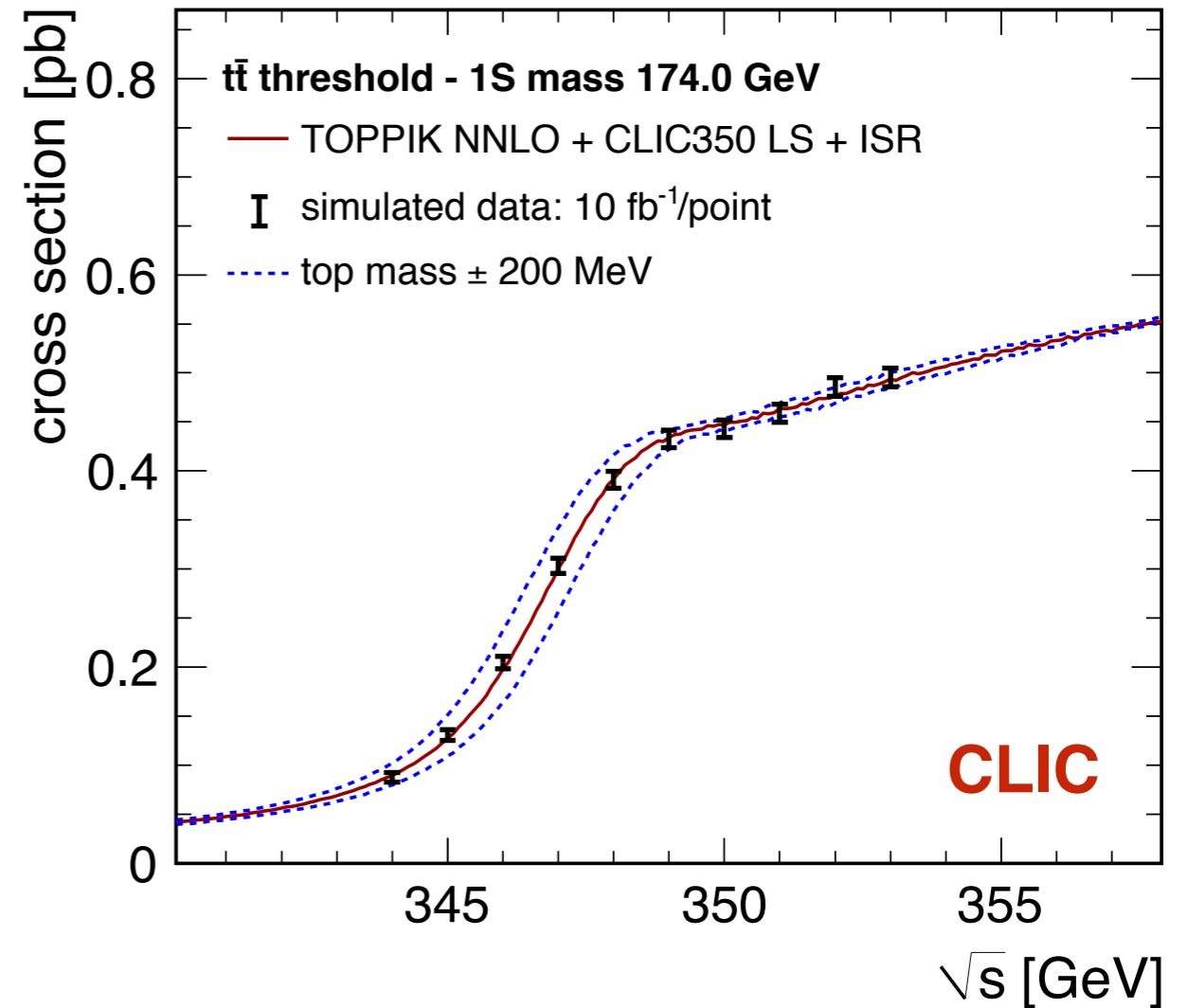
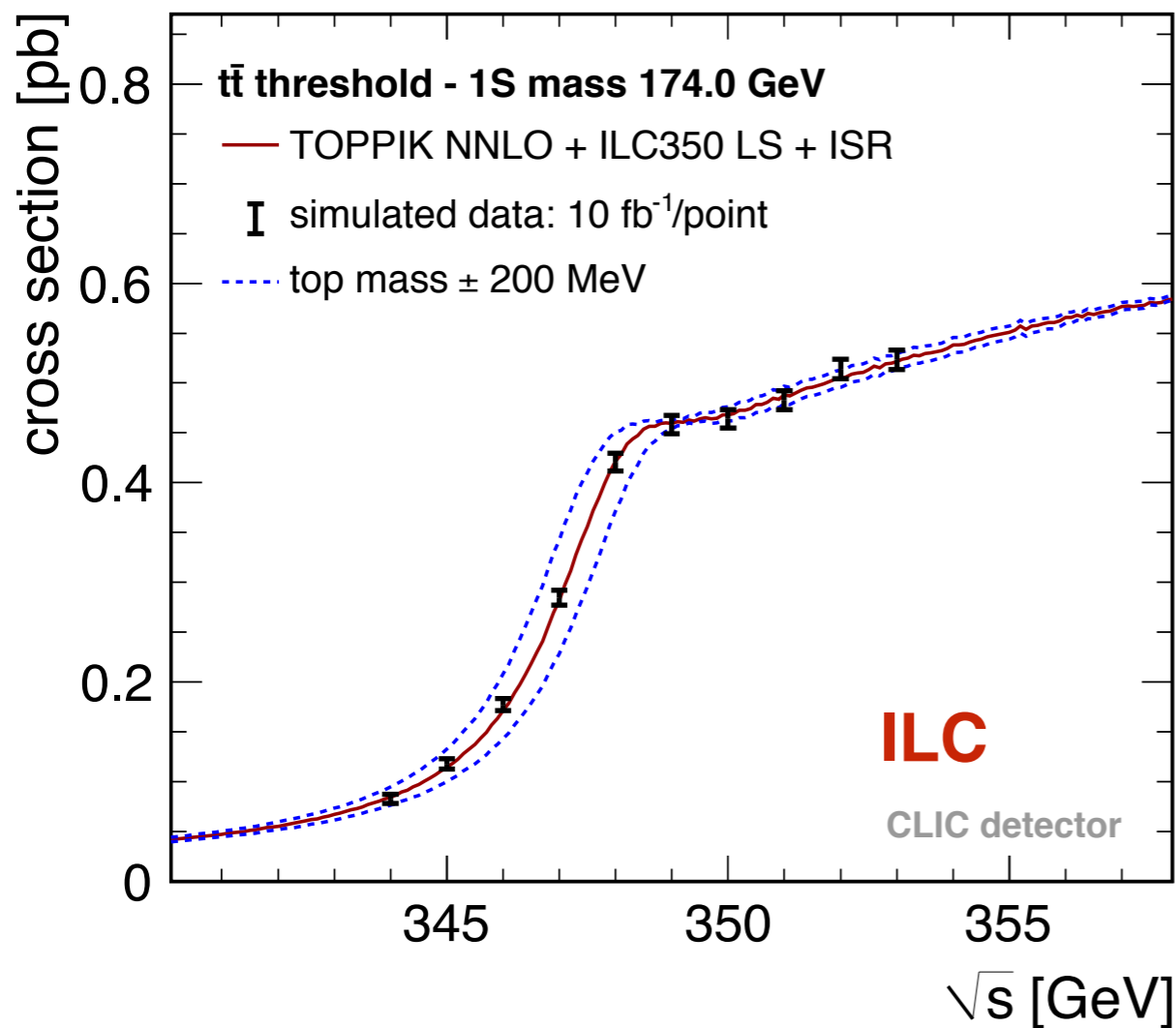
Katja Seidel, Frank Simon, Michal Tesar, Stephane Poss  
Eur. Phys. J. C73 (2013) 2530



# Top mass measurement in a threshold scan

- The **cross-section depends on** the **top mass**, so measuring the cross-section the top mass can be extracted (Also the  $\alpha_s$ , Yukawa coupling, top width...)
- Inclusion of **higher-order QCD contributions** are needed for a correct description of the cross section
- Determination of **event selection efficiency** and **background contamination**
- Threshold scan with **10 energy points** spaced by 1 GeV **from 344 GeV to 353 GeV** with an integrated **luminosity of 10 fb<sup>-1</sup>**

# Threshold scans at ILC and CLIC



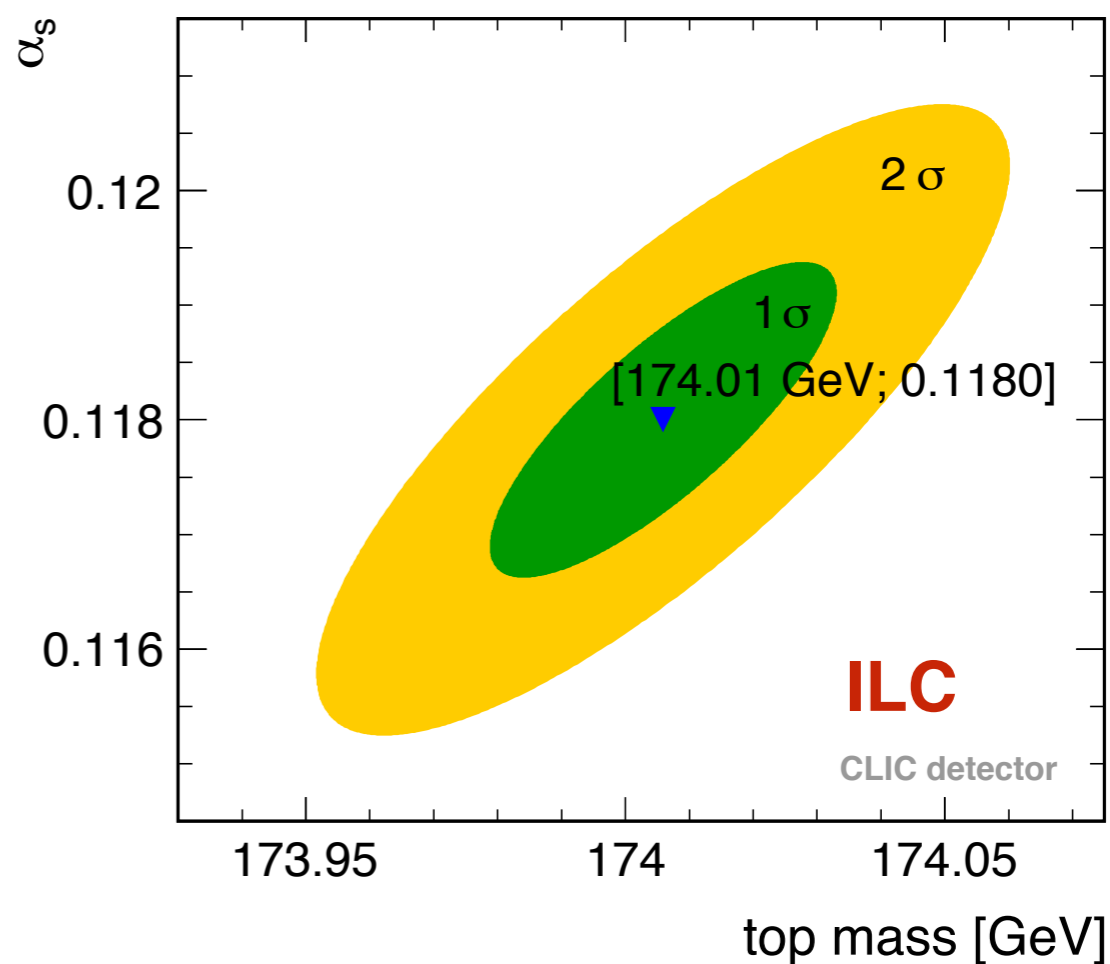
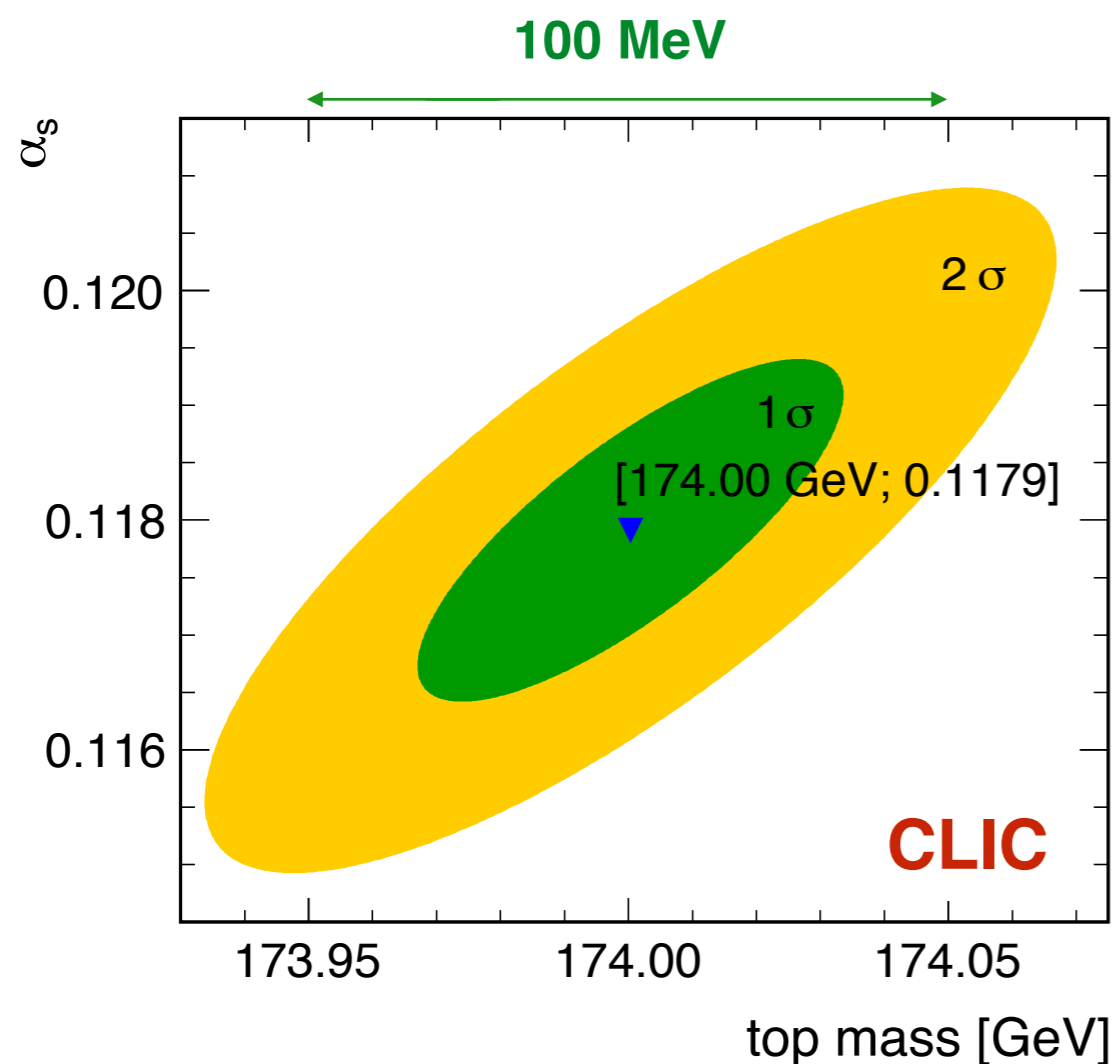
**The cross section for ILC rises faster due to the luminosity peak is narrower**

But it does not result in a significant difference of the precision of the top quark mass measurement



# Measurement of the top mass and $\alpha_s$ at CLIC and ILC

- **Statistical uncertainty of top mass around 30 MeV** (CLIC  $\sim$  20% larger than ILC due to different luminosity spectrum)
- In addition: **Experimental** and **theoretical systematics**, and uncertainties from the **conversion to the  $\overline{\text{MS}}$**  mass scheme. **Total uncertainty below 100 MeV** within reach.



# Top quark electroweak couplings at the ILC

- **The process  $e^+e^- \rightarrow t\bar{t}$  involves only  $t\bar{t}Z_0$  and  $t\bar{t}\gamma$  primary vertices**
- A way to describe the current at the  $t\bar{t}X$  vertex:
- See details in: [arxiv.org/abs/hep-ph/0601112](http://arxiv.org/abs/hep-ph/0601112)

$$\Gamma_{\mu}^{ttX}(k^2, q, \bar{q}) = ie \left\{ \gamma_{\mu} \left( \tilde{F}_{1V}^X(k^2) + \gamma_5 \tilde{F}_{1A}^X(k^2) \right) + \frac{(q - \bar{q})_{\mu}}{2m_t} \left( \tilde{F}_{2V}^X(k^2) + \gamma_5 \tilde{F}_{2A}^X(k^2) \right) \right\}$$

where:

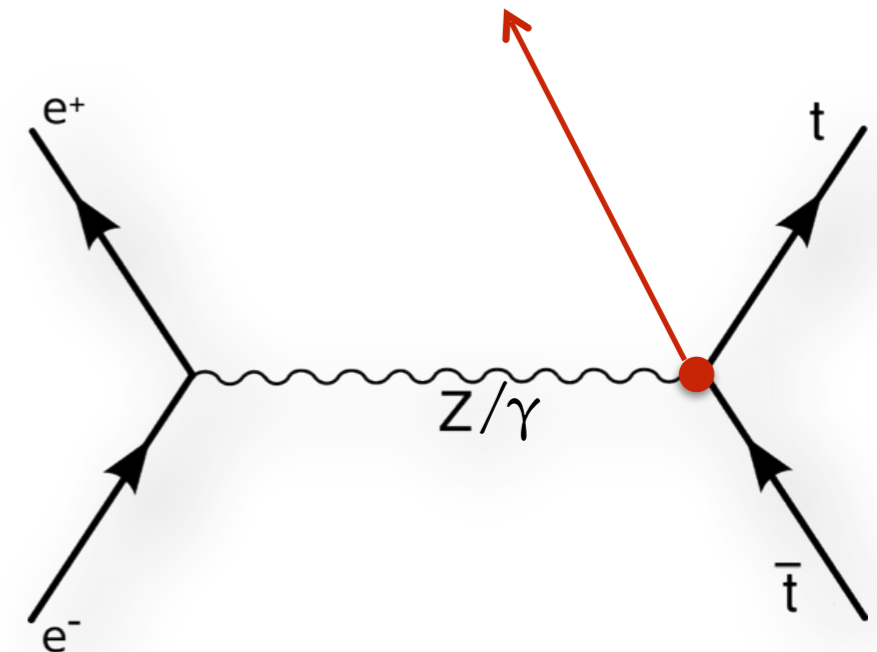
**V** = Vector coupling

**A** = Axial coupling

**X** = Z,  $\gamma$

$$\begin{array}{ccc} F_{1V}^{\gamma} & F_{1A}^{\gamma} & F_{2V}^{\gamma} \\ F_{1V}^Z & F_{1A}^Z & F_{2V}^Z \end{array}$$

**Non CP violating top quark couplings**





$e^+e^- \rightarrow t\bar{t}$  semi-leptonic channel at ILC@500 GeV

M.S. Amjad, M. Boronat, et al  
<http://www-flc.desy.de/lcnotes/LC-REP-2013-007>

## 1. Generated events (signal)

**WHIZARD:** Generate 6 fermions final state  $e^+e^- \rightarrow q\bar{q}b\bar{b}l\nu$

**Pythia:** Parton shower and hadronisation

+ *WbWb and beam backgrounds added*

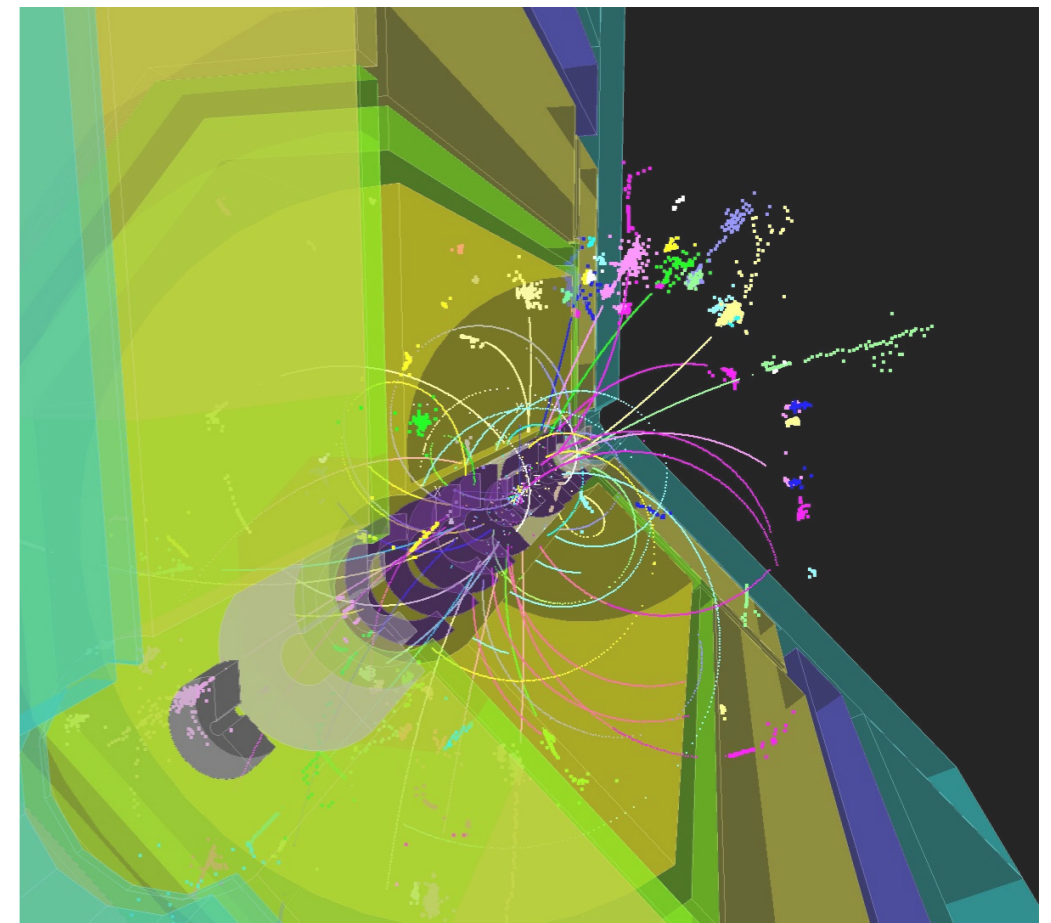
**Beams are polarised**

**(2 samples)**

1.  $e_L^- e_R^+$   $P(e^-) \approx -80\%$  ,  $P(e^+) \approx +30\%$
2.  $e_R^- e_L^+$   $P(e^-) \approx +80\%$  ,  $P(e^+) \approx -30\%$

## 2. Simulation of the detector

**Full realistic simulation of the ILD detector concept**



Three-dimensional image of a 500-GeV  $t\bar{t}$  event simulated in the ILD detector

# Event generation, detector simulation and reconstruction

## 3. Reconstruction

### Standard algorithms for event selection

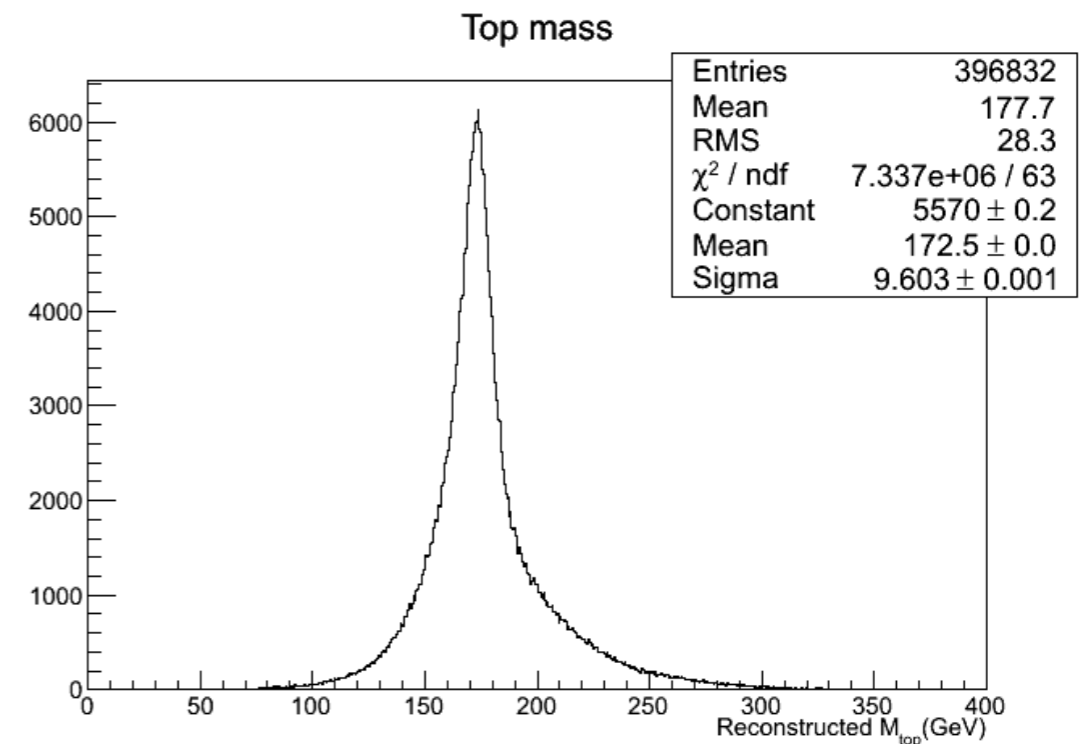
**Signal reconstruction: combination of  $b$  quark jet and  $W$  boson that minimises the following equation**

$$d^2 = \left( \frac{m_{cand.} - m_t}{\sigma_{m_t}} \right)^2 + \left( \frac{E_{cand.} - E_{beam}}{\sigma_{E_{cand.}}} \right)^2 + \left( \frac{p_b^* - 68}{\sigma_{p_b^*}} \right)^2 + \left( \frac{\cos\theta_{bW} - 0.23}{\sigma_{\cos\theta_{bW}}} \right)^2$$

### Efficiency of selection

**51.9%** for  $P, P' = -1, +1$  (Left-handed electrons)

**55.0%** for  $P, P' = +1, -1$  (Right-handed electrons)



# Observables

**Total cross section ( $\sigma$ )**

**The Forward-Backward Asymmetry ( $A_{FB}^{\text{top}}$ )**

**The slope of the distribution of the helicity angle ( $\lambda_t$ )**

Standard model values

Observables	$e^-_L e^+_R$	$e^-_R e^+_L$
$\sigma(\text{fb})$	1564	724
$A_{FB}$	0.38	0.47
$F_R = (1 + \lambda_t)/2$	0.25	0.76

But actually there are **6 independent observables** = 3 observables x 2 polarisations

So we can obtain the following **CP conserving 6 couplings of the top to Z and  $\gamma$**

$$\left. \begin{array}{l} \sigma(+), A_{FB}(+), \lambda_{hel}(+) \quad (+ = e^-_R) \\ \sigma(-), A_{FB}(-), \lambda_{hel}(-) \quad (- = e^-_L) \end{array} \right\} \Rightarrow \left\{ \begin{array}{l} F_{1V}^\gamma, F_{1A}^\gamma, F_{2V}^\gamma \\ F_{1V}^Z, F_{1A}^Z, F_{2V}^Z \end{array} \right\}$$

\*  $F_{1A}^\gamma = 0$  because of the gauge invariance

# Measurement of observables

## The cross section

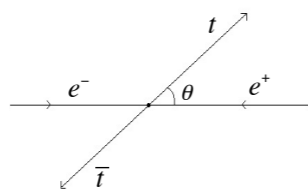
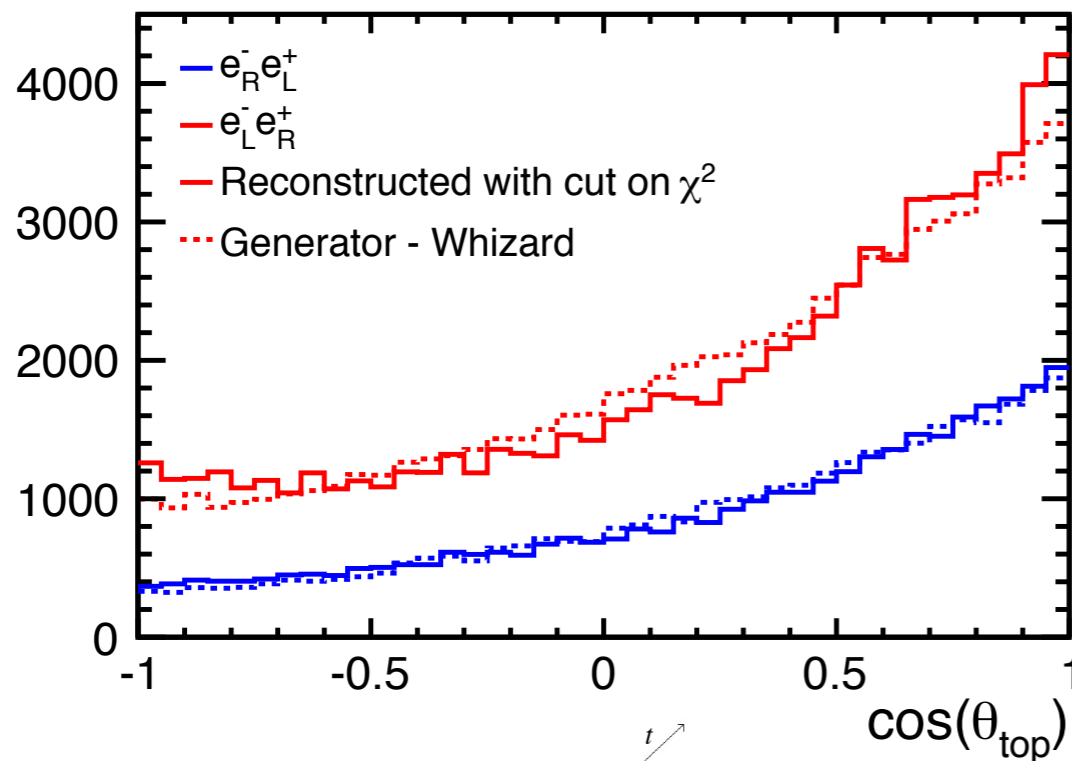
The cross section can be measured to

**0.5% (stat. + lumi)**

## The Forward-Backward Asymmetry

$$A_{FB}^t = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)}$$

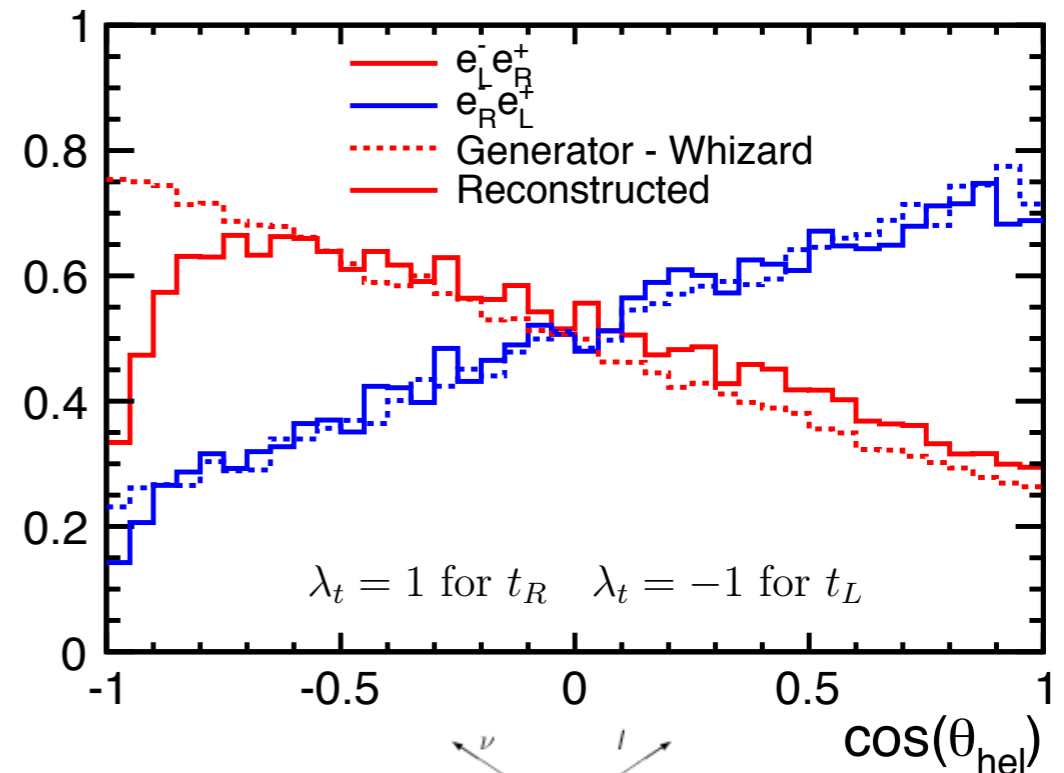
**2% (stat. + syst.)**



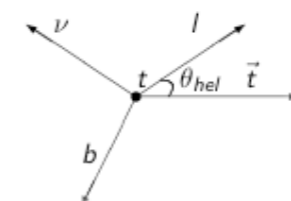
## The helicity angle

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_{hel}} = \frac{1 + \lambda_t \cos\theta_{hel}}{2} = \frac{1}{2} + (2F_R - 1) \frac{\cos\theta_{hel}}{2}$$

**~4% (stat. + syst.)**



$\lambda_t = 1$  for  $t_R$   $\lambda_t = -1$  for  $t_L$





# Sensitivities for the electroweak couplings

[1] [arXiv:hep-ph/0601112](https://arxiv.org/abs/hep-ph/0601112)

**500/fb at 500 GeV** yields 1-2 orders of magnitude better sensitivity than the **LHC (300/fb at 14 TeV)**

Coupling	SM value	LHC [1] $\mathcal{L} = 300 \text{ fb}^{-1}$	$e^+e^-$ [ILC DBD] $\mathcal{L} = 500 \text{ fb}^{-1}$ $\mathcal{P}, \mathcal{P}' = \pm 0.8, \mp 0.3$
$\Delta \tilde{F}_{1V}^\gamma$	0.66	+0.043 -0.041	+0.002 -0.002
$\Delta \tilde{F}_{1V}^Z$	0.23	+0.240 -0.620	+0.003 -0.003
$\Delta \tilde{F}_{1A}^Z$	-0.59	+0.052 -0.060	+0.005 -0.005
$\Delta \tilde{F}_{2V}^\gamma$	0.015	+0.038 -0.035	+0.003 -0.003
$\Delta \tilde{F}_{2V}^Z$	0.018	+0.270 -0.190	+0.006 -0.006

**LHC studies  
(Snowmass 2005)**

**Present study denoted  
as ILC DBD**

# Summary

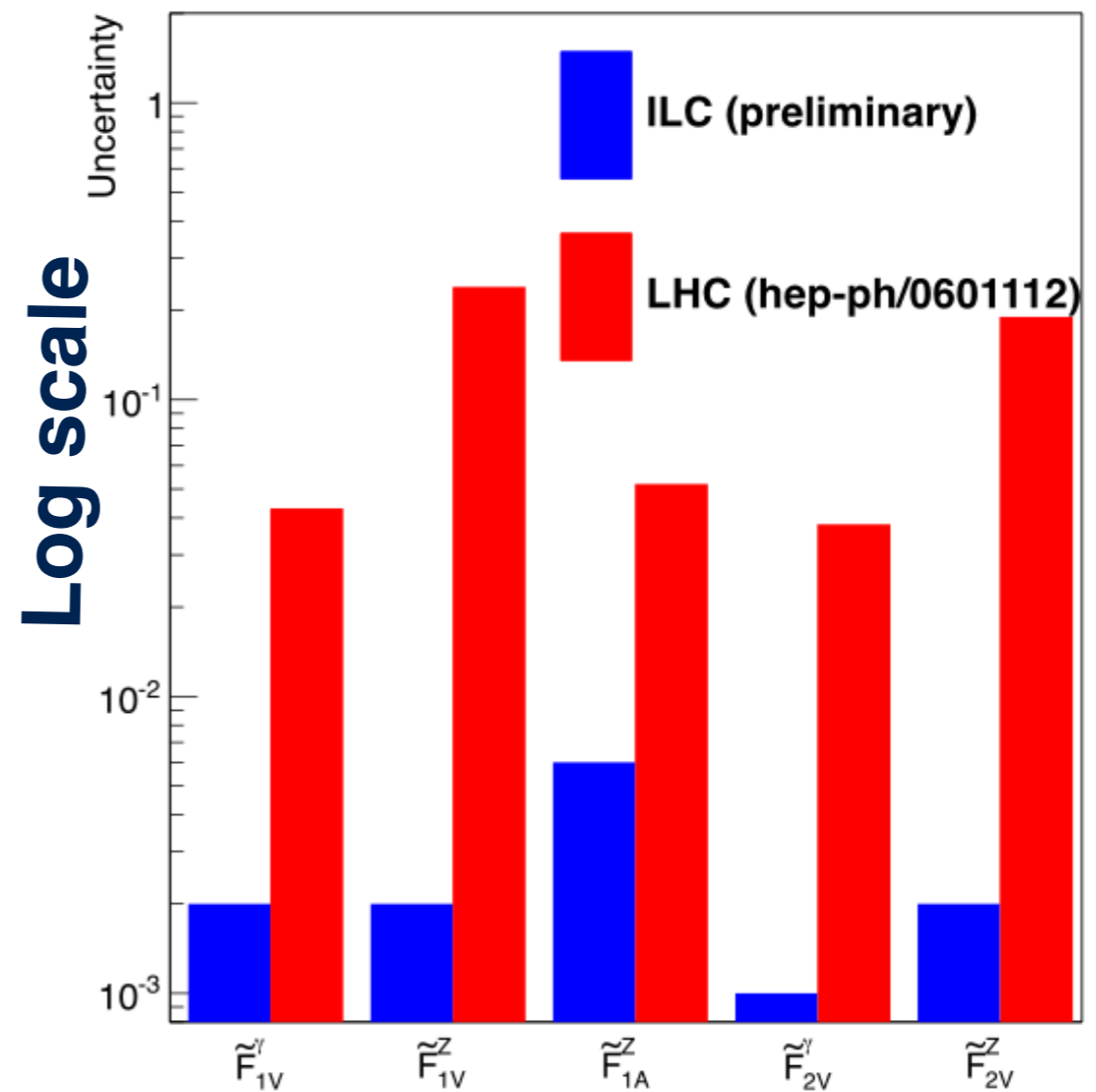
## Top mass at threshold

**Statistical uncertainty of top mass around 30 MeV**

(CLIC ~ 20% larger than ILC due to different luminosity spectrum).

**Total uncertainty below 100 MeV** in reach, expected to be dominated by theory systematics.

## Top electroweak couplings



# Conclusions

- In a **threshold scan**, the **top mass** can be determined in a **theoretically well defined** way, using 1S mass scheme
- These studies confirm the expectation that a **linear  $e^+e^-$  collider** will be capable of measuring the mass of the top quark with **30 MeV error**
- **Polarisation** allows to **double the number of observables**
- **It is a powerful tool for analysis** because it also allows **full separation** between **axial and vectorial couplings** and between  **$t\bar{t}Z$  and  $t\bar{t}\gamma$  vertices**
- In LC with polarised beams we can measure with **accuracies** one or two orders of magnitude **better than LHC**

THANK YOU FOR YOUR ATTENTION



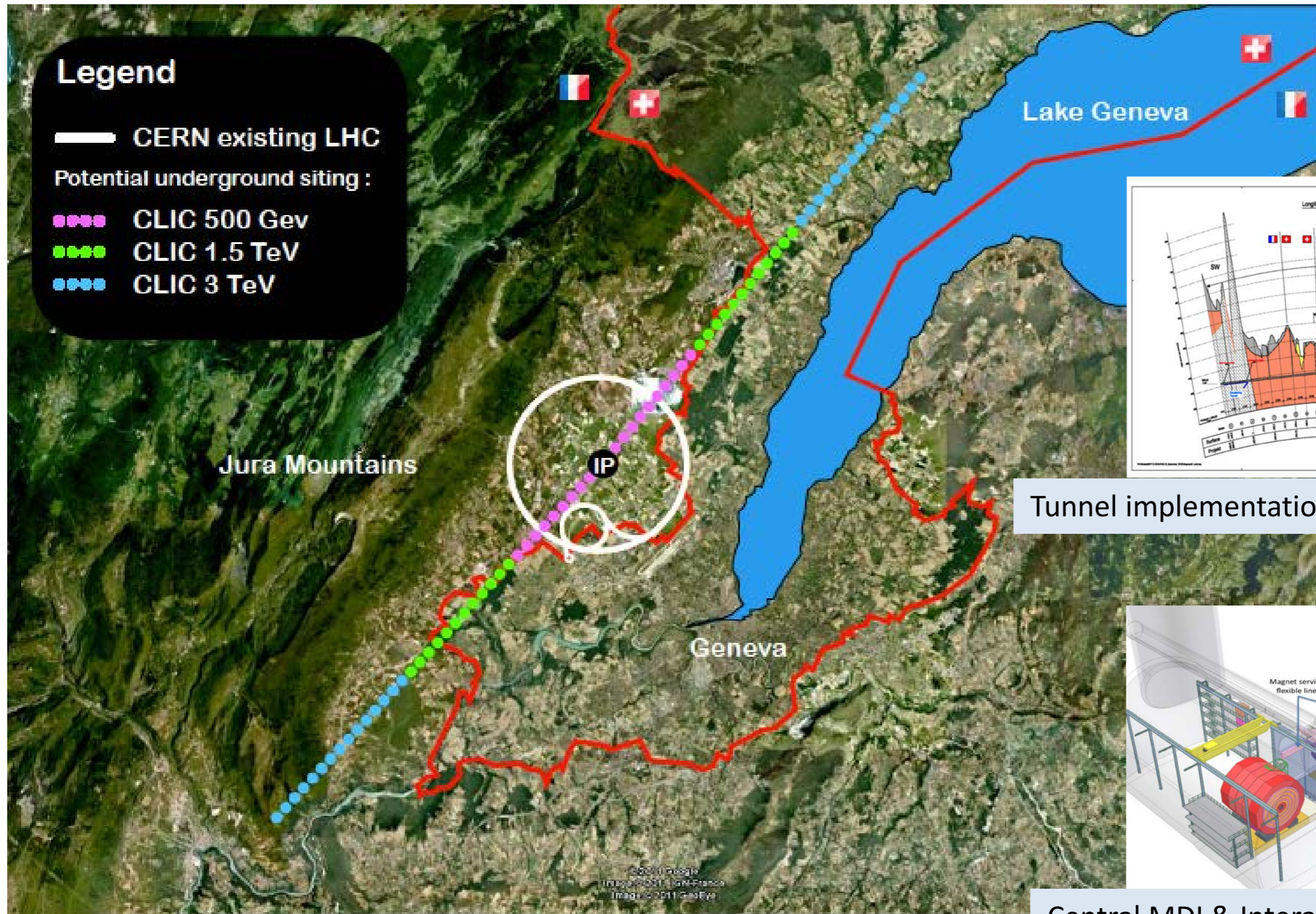


# BACKUP SLIDES



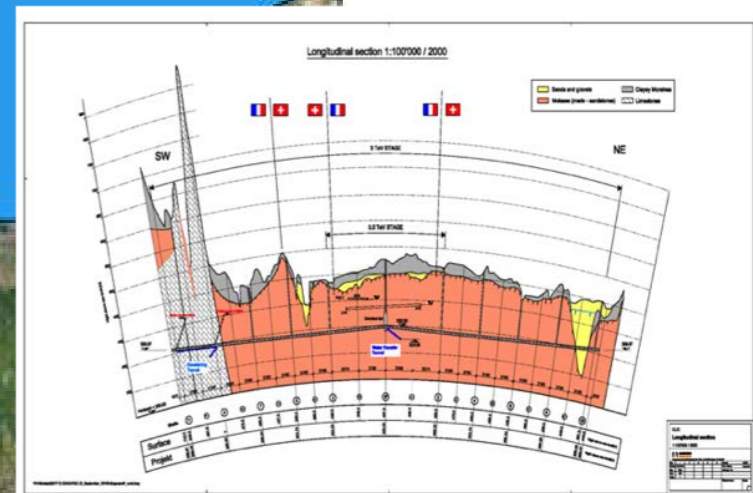
# CLIC@CERN

Slide by Steinar Stapnes, CERN

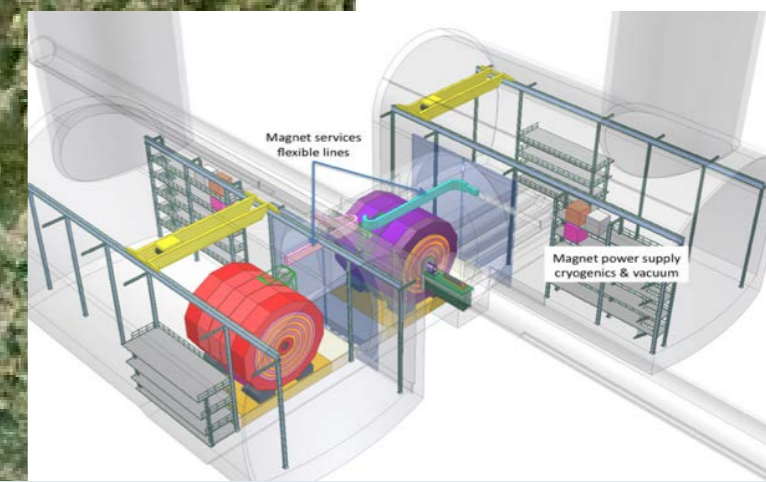


Ties Bennke, 27.5.2014

ILC - ILD



Tunnel implementations (laser straight)



Central MDI & Interaction Region





# ILC@Japan

Planned construction candidate site for the International linear collider and main surrounding facilities



Oshu General Gymnasium



Lime-kun Farmer's Market



Ichinoseki National College of Technology



Ichinoseki Cultural Center

## World Heritage HIRAIZUMI

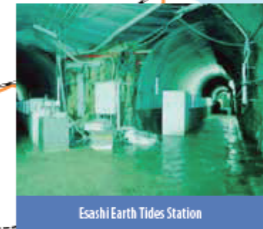


Many temples, gardens, and ruins that were built based on the philosophies of Pureland Buddhism remain in excellent condition in Hiraizumi. The temples and gardens were an attempt to make an ideal world in our own reality. While receiving influence from abroad, it accomplished its own original development so that Hiraizumi expresses an ideal world the like of which can be found nowhere else.

<http://www.city.oshu.iwate.jp/htm/ilc/archives/rayoffhopee.pdf>



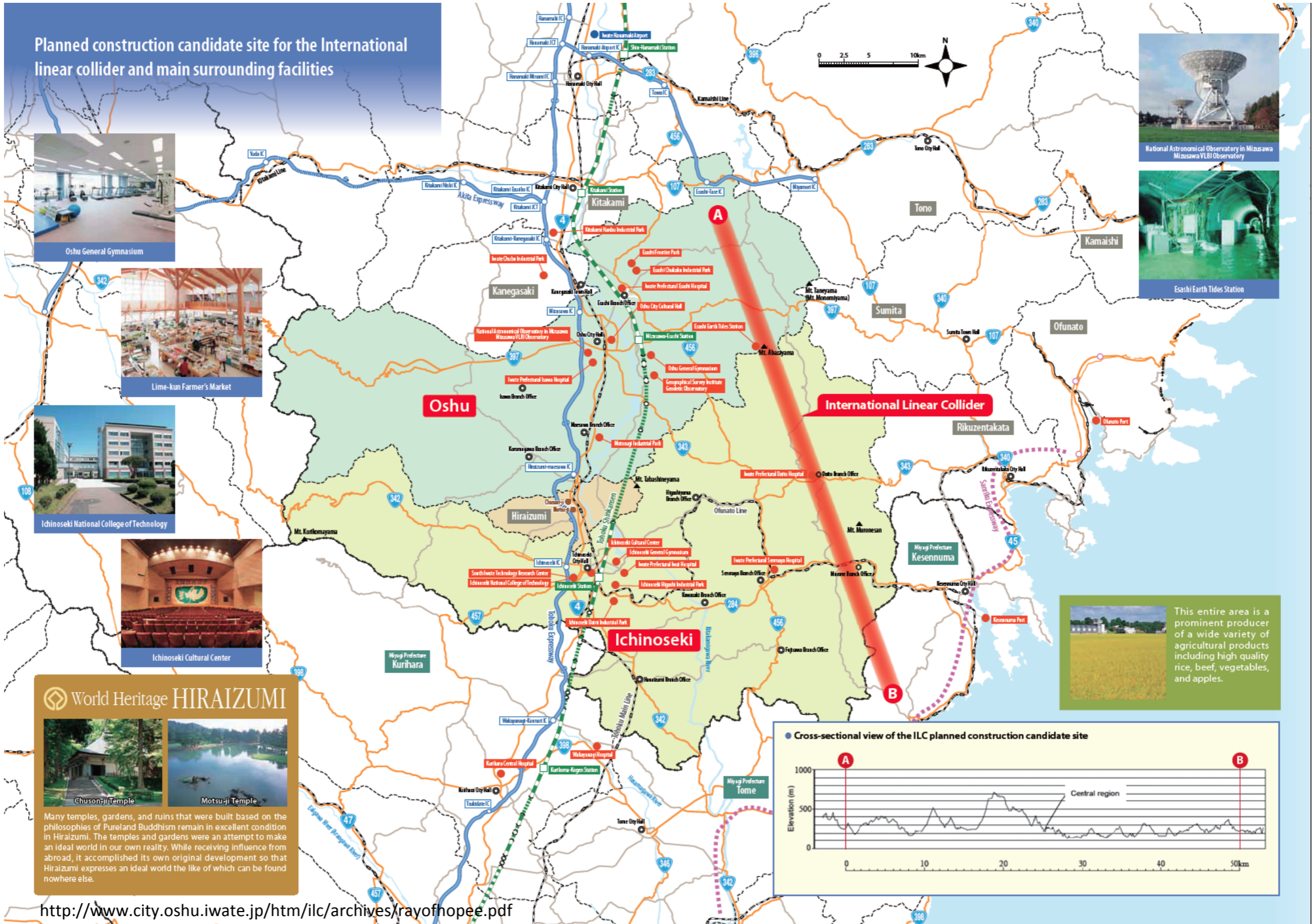
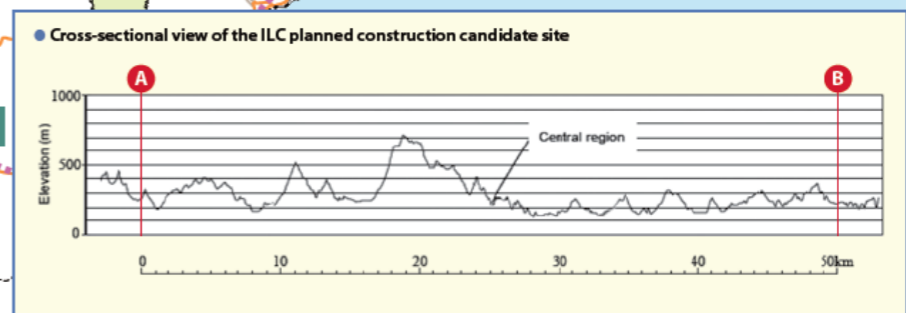
National Astronomical Observatory in Mizusawa  
Mizusawa VLBI Observatory



Esashi Earth Tides Station



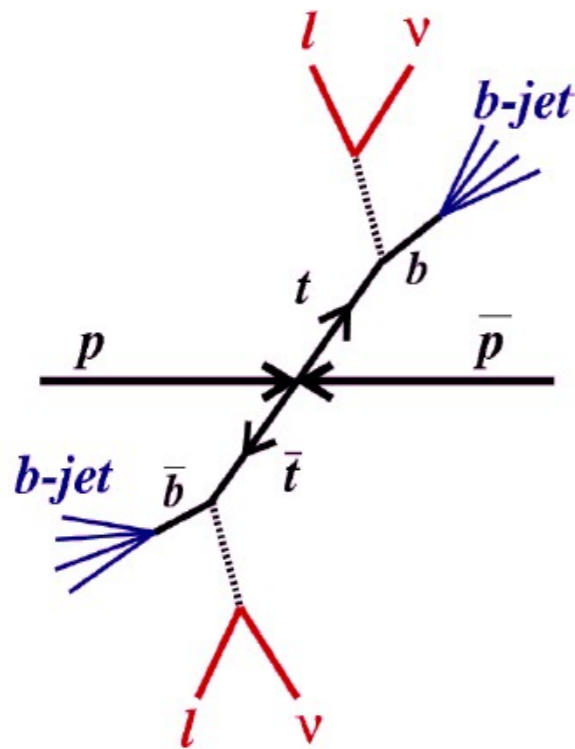
This entire area is a prominent producer of a wide variety of agricultural products including high quality rice, beef, vegetables, and apples.



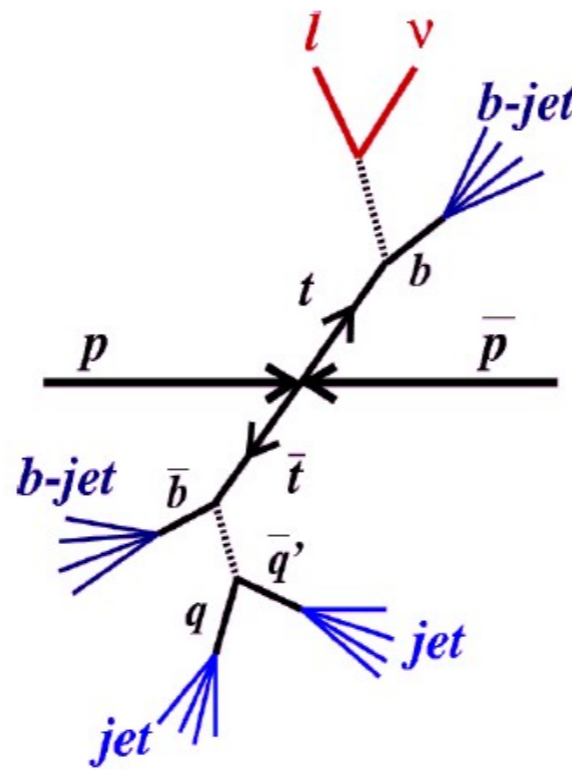
# tt decay modes

$e^+e^- \rightarrow t\bar{t}$  gives three different final states:

**Fully leptonic** (10.3%)  
2 jets + 2 leptons + 2 neutrinos



**Semi-leptonic** (43.5%)  
4 jets + lepton + neutrino



**Fully hadronic** (46.2%)  
6 jets at final state

