

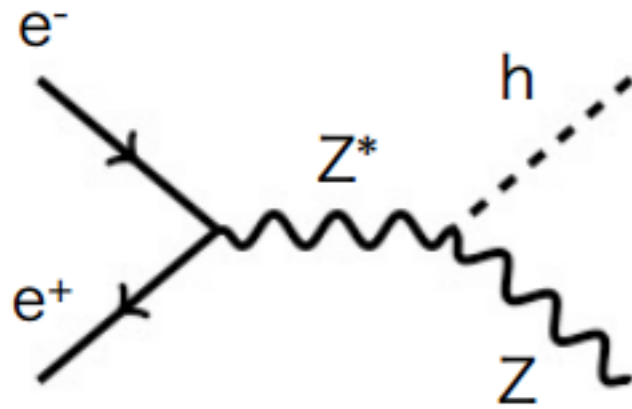
# Hadronic Higgs Recoil Mass Study with ILD at 250GeV

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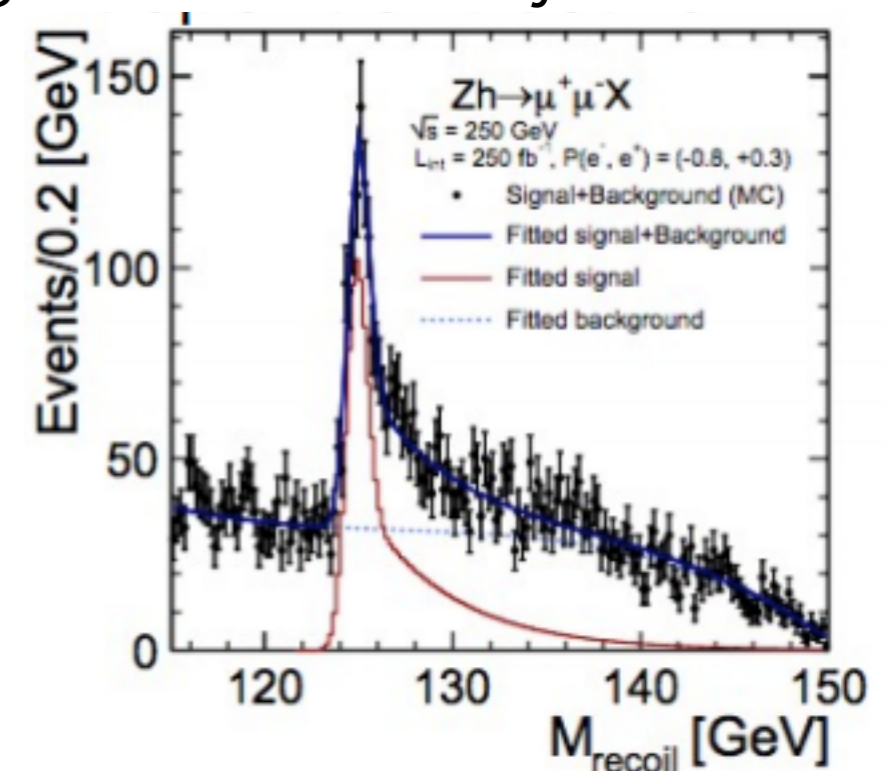


# Overview - qqH channel



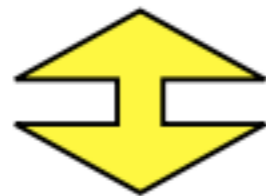
Using 4 momentum conservation, we can calculate the mass of Higgs boson without observing Higgs boson directly.

Especially in  $Z \rightarrow$  leptonic channel, its mass distribution has quite high precision. But, its BR is only  $\sim 3.4\%$  for each generation.



In contrast, the branching ratio of  $Z \rightarrow$  hadronic is  $\sim 70\%$ .

- **More statistics**

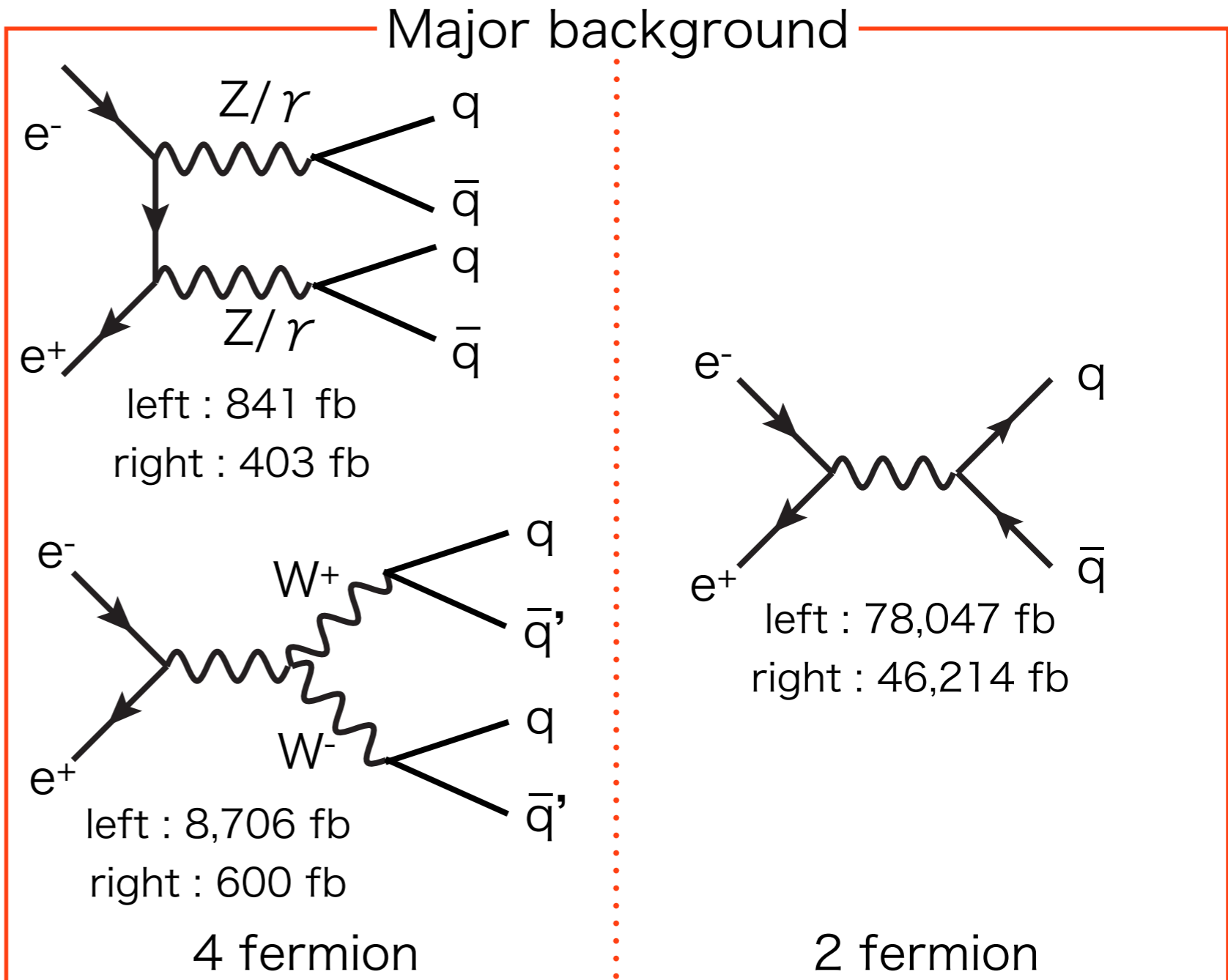
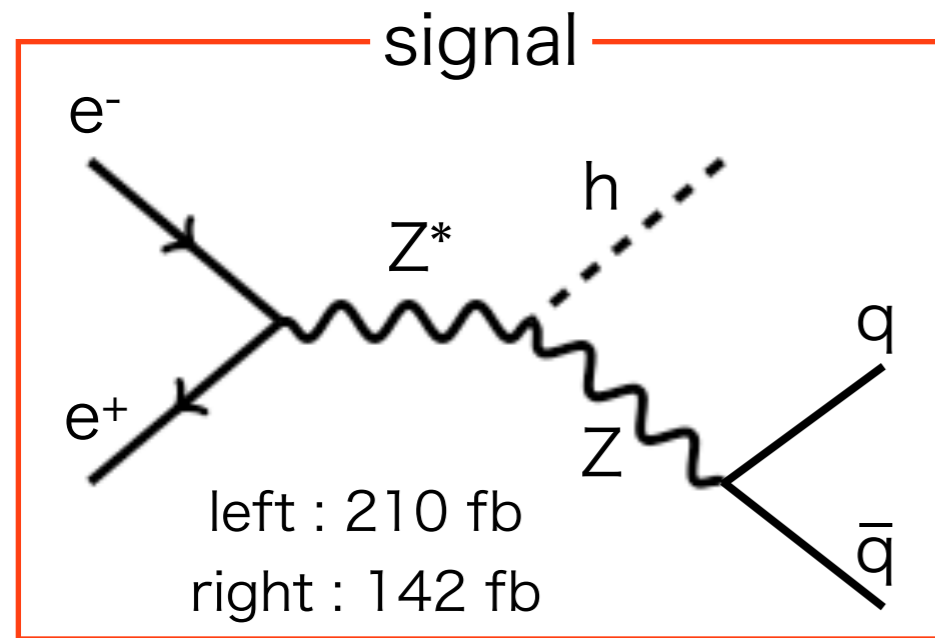


Model independent?

- **More background**

# Data samples

| Higgs mass | $E_{CM}$ | Luminosity           | Polarization                              | Detector        |
|------------|----------|----------------------|---|-----------------|
| 125 GeV    | 250 GeV  | 250 fb <sup>-1</sup> | left: (-0.8, +0.3)<br>right: (+0.8, -0.3) | ILD_DBD<br>ver. |



semi-leptonic events  
are also considerable BG.

# Analysis flow

- To improve jet clustering,
  - Initial state radiation
  - Isolated lepton
  - Hadronic tau jet were removed from events.
- Durham jet clustering was applied to the remaining events.

$$y = \frac{2\min(E_i^2, E_j^2)(1 - \cos \theta_{ij})}{Q^2}$$

- Forced 4 jet clustering,  $y$  threshold clustering were used.

# Background reduction

- 4 fermion background - using forced 4 jet clustering,
- 2 fermion background - Thrust and Sphericity were used.
- S/N separation
  - reconstructed the mass of Z candidate 2-jet with y value clustering ( $y = 0.0025$ ).
  - reconstructed the transverse momentum of Z candidate.
  - The distribution of Hadronic recoil mass.
- After applying these cuts,

|                        | signal | 4 fermion | 2 fermion | others |
|------------------------|--------|-----------|-----------|--------|
| % of events after cuts | 46.2%  | 8.3%      | 1.4%      | 0.3%   |

# Cut efficiency issue

- After applying cuts, tested cut efficiencies for each Higgs decay.

| mode                         | After cuts (%) | diff./mean |
|------------------------------|----------------|------------|
| H->all                       | 46.2%          | -----      |
| H->bb (57.7%)                | 43.3%          | -6.3%      |
| H->WW(leptonic) (2.3%)       | 45.3%          | -2.0%      |
| H->WW(semi-leptonic) (9.5%)  | 46.9%          | +1.4%      |
| H->WW(hadronic) (9.8%)       | 54.4%          | +17.7%     |
| H->gg (8.6%)                 | 55.2%          | +19.5%     |
| H-> $\tau\tau$ (6.3%)        | 45.3%          | -2.1%      |
| H->ZZ (2.6%)                 | 48.6%          | +5.1%      |
| H->cc (2.9%)                 | 47.1%          | +1.8%      |
| H->invisible (ZZ->4n) (0.1%) | 35.4%          | -23.4%     |

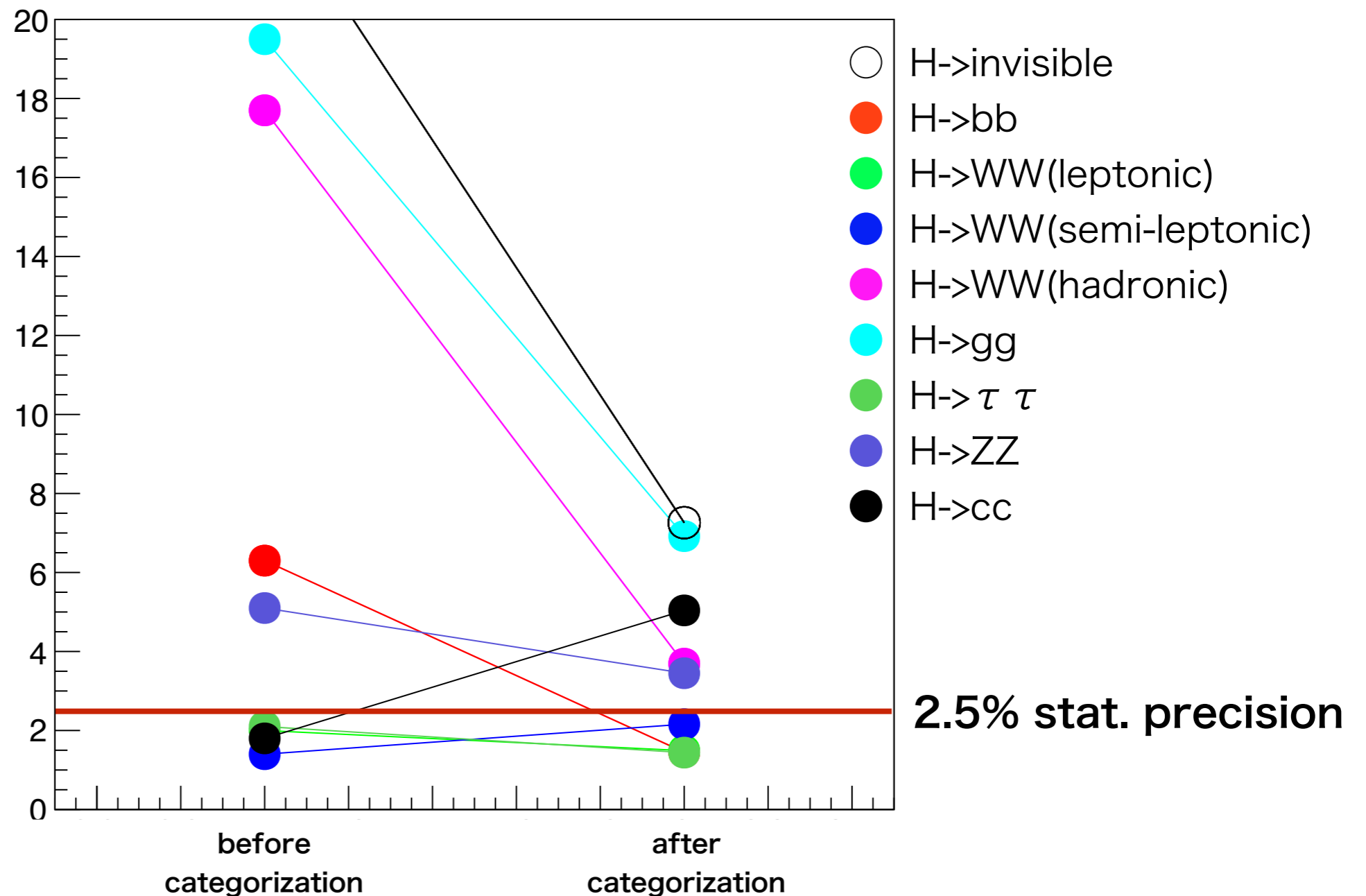
- The large inconsistency was found in H->gg, H->WW->4q and invisible.

# Categorization (Reduction of inconsistency)

- The inconsistency of cut efficiency will affect the measurements of  $\sigma_{ZH}$ .
- This systematic uncertainty should be smaller than the statistical one.
- For reducing this inconsistency, the categorization is one of the powerful solution.
- Classify the whole event into the nine categories using number of isolated leptons, tau jets, b-tag ( $>0.6$ ), c-tag ( $>0.6$ ).
- Then, optimize the cut in each category.

# Cut efficiency and Categorization

- After categorizing events and applying much optimized cuts,
- The efficiency inconsistency is at most  $\sim 7\%$ .





# Two Luminosity case

| polarization<br>and Luminosity                           | significance<br>$\sigma_{ZH}$   | stat. precision<br>$\sigma_{ZH}$ | stat. precision<br>$g_{ZZH}$ | stat. precision<br>$g_{ZZH}$<br>(combined) |
|--|---------------------------------|----------------------------------|------------------------------|--|
| left (-0.8, +0.3)<br>250 fb <sup>-1</sup>                | <b>38.0 <math>\sigma</math></b> | <b>2.6%</b>                      | <b>1.3%</b>                  | <b>1.0%</b>                                |
| right (+0.8, -0.3)<br>250 fb <sup>-1</sup>               | <b>41.8 <math>\sigma</math></b> | <b>2.4%</b>                      | <b>1.2%</b>                  | <b>1.0%</b>                                |
| left (-0.8, +0.3)<br>1150 fb <sup>-1</sup><br>(Lumi UP)  | <b>81.5 <math>\sigma</math></b> | <b>1.2%</b>                      | <b>0.6%</b>                  | <b>0.5%</b>                                |
| right (+0.8, -0.3)<br>1150 fb <sup>-1</sup><br>(Lumi UP) | <b>89.7 <math>\sigma</math></b> | <b>1.1%</b>                      | <b>0.6%</b>                  | <b>0.5%</b>                                |

# The effect of the different BR from SM

|                           |        |        |       |       |
|---------------------------|--------|--------|-------|-------|
| base                      | 210.06 | 141.70 | —     | —     |
| bb + 5% (57.7->62.7)      | 210.15 | 141.64 | ~0.0% | ~0.0% |
| bb - 5% (57.7->52.7)      | 209.95 | 141.77 | ~0.0% | ~0.0% |
| cc + 5% (2.9->7.9)        | 208.92 | 140.99 | -0.5% | -0.5% |
| cc - 5% (2.9->0.0)        | 210.68 | 142.09 | +0.3% | +0.3% |
| gg + 5% (8.6->13.6)       | 209.84 | 141.74 | -0.1% | ~0.0% |
| gg - 5% (8.6->3.6)        | 210.27 | 141.66 | +0.1% | ~0.0% |
| WW + 5% (21.6->26.6)      | 209.92 | 141.70 | -0.1% | ~0.0% |
| WW - 5% (21.6->16.6)      | 210.02 | 141.58 | ~0.0% | -0.1% |
| tau + 5% (6.3->11.3)      | 210.29 | 141.85 | +0.1% | +0.1% |
| tau - 5% (6.3->1.3)       | 209.82 | 141.55 | -0.1% | -0.1% |
| ZZ + 5% (2.6->7.6)        | 210.40 | 141.96 | +0.2% | +0.2% |
| ZZ - 5% (2.6->0.0)        | 209.97 | 141.63 | ~0.0% | -0.1% |
| invisible + 5% (0.1->5.1) | 210.29 | 142.34 | +0.1% | +0.5% |
| invisible - 5% (0.1->0.0) | 210.10 | 141.73 | ~0.0% | ~0.0% |

The different BR has only ~0.5 % effect on total cross section of ZH production. This is much smaller than current stat. precision.

# Stat. precision in the “worst case”

- If  $\sigma_{\text{tot}} \times \text{BR}$  is not changed from SM, but  $g_{\text{ZZH}}$  is changed.  
The stat. precision of some major decay mode will be suppressed.
- bb and tau tau mode were examined because these two decay modes mainly contribute to the significance of  $\sigma_{\text{tot}}$ .

- Tau decay is not so serious a problem for stat. precision.

- Still keep less than 4 % stat. precision in right polarization

|   | stat. precision<br>of $\sigma_{\text{ZH}}$ | stat. precision<br>of $g_{\text{ZZH}}$ |
|---|--|--|
| $\sigma_{\text{tot}} \times \text{BR}_{\text{bb}} = \text{SM}$  | left : 3.8%<br>right : 3.0%                | left : 1.9%<br>right : 1.5%            |
| $\sigma_{\text{tot}} \times \text{BR}_{\tau\tau} = \text{SM}$   | left : 2.8%<br>right : 2.6%                | left : 1.4%<br>right : 1.3%            |
| $\sigma_{\text{tot}} \times \text{BR}_{\tau\tau} = \text{SM}$<br>$\sigma_{\text{tot}} \times \text{BR}_{\text{bb}} = \text{SM}$ | left : 4.7%<br>right : 3.5%                | left : 2.3%<br>right : 1.8%            |

# 350 GeV case

| polarization<br>and Luminosity                        | significance<br>$\sigma_{ZH}$   | stat. precision<br>$\sigma_{ZH}$ | stat. precision<br>$g_{ZZH}$ | stat. precision<br>$g_{ZZH}$<br>(combined) |
|---|---------------------------------|----------------------------------|------------------------------|--|
| 350 GeV<br>left (-0.8, +0.3)<br>333 fb <sup>-1</sup>  | <b>30.1 <math>\sigma</math></b> | <b>3.3%</b>                      | <b>1.7%</b>                  | <b>1.4%</b>                                |
| 350 GeV<br>right (+0.8, -0.3)<br>333 fb <sup>-1</sup> | <b>31.1 <math>\sigma</math></b> | <b>3.2%</b>                      | <b>1.6%</b>                  | <b>1.3%</b>                                |

The inconsistency of cut efficiency is about 10 %.

※ cut variables was slightly optimized from 250 GeV, but need more effort.

# Summary and Prospects

## summary

- Using categorization, the difference of cut efficiency is suppressed at most  $\sim 7\%$ .
- Stat. precision is about  $\sim 2.5\%$  which is almost the same as leptonic channel (ILC Higgs White paper's results)
- In worst case, the stat. precision is less than  $4.0\%$  ( $\sigma_{ZH}$ )

|   | significance                    | stat. precision |
|---|---------------------------------|-----------------|
| 250 GeV (-0.8,+0.3) 250fb <sup>-1</sup> | <b>38.0 <math>\sigma</math></b> | <b>2.6%</b>     |
| 250 GeV (+0.8,-0.3) 250fb <sup>-1</sup> | <b>41.8 <math>\sigma</math></b> | <b>2.4%</b>     |
| 350 GeV (-0.8,+0.3) 333fb <sup>-1</sup> | <b>30.1 <math>\sigma</math></b> | <b>3.3%</b>     |
| 350 GeV (+0.8,-0.3) 333fb <sup>-1</sup> | <b>31.1 <math>\sigma</math></b> | <b>3.2%</b>     |

## prospects

- cut optimization for 350 GeV (flavor tagging, cut variables...)
- Investigate the systematic uncertainty in both  $E_{CM}$ .

# backup slides

# Strategy to reduce inconsistency (Categorization)

- Categorization is a powerful tool to reduce difference of efficiency among Higgs decay modes.
- Categorize events using number of jets, leptons, taus, etc.
- Minimize the difference of efficiency in each category (decay modes with too small fraction in the category is negligible.)
- Calculate partial cross section from each category
- Combine all cross section from categories to get the total cross section of ZH production.

# Categorization -1

To resolve efficiency inconsistent issue, we will categorize events using

- the number of tau jets (0, 1, and  $\geq 2$ )
- the number of isolated lepton (0, 1, and  $\geq 2$ )

$$N^i = \sum_n \sigma_{\text{tot}} \cdot \text{BR}_n \cdot \theta_n^i \cdot \epsilon_n^i$$

$n = (b, W, g, \tau, \dots)$

$N^i$  is a number of events in category  $i$ ,  $\sigma_{\text{tot}}$  is total cross section,  $\text{BR}_n$  is Higgs decay branching ratio,  $\theta_n^i$  is fraction in category  $i$ ,  $\epsilon_n^i$  is cut efficiency for category  $i$ .

If the cut efficiency of each decay mode can be assumed to be the same as  $\epsilon^i (= \epsilon_n^i)$ .

$$\frac{N^i}{\epsilon^i} = \sigma_{\text{tot}} \sum_n \text{BR}_n \cdot \theta_n^i$$

Then we can get

$$\sum_i \frac{N^i}{\epsilon^i} = \sigma_{\text{tot}} \sum_n \sum_i \text{BR}_n \cdot \theta_n^i = \sigma_{\text{tot}}$$



# Categorization

If the cut efficiency is not exactly the same,  
we should consider the systematic effect caused by the difference.

$$\delta\epsilon_n^i = \epsilon_n^i - \epsilon^i$$

And the cross section is

$$\sigma_{\text{tot}} = \frac{\sum_i \frac{N^i}{\epsilon^i}}{1 + \sum_n \sum_i \text{BR}_n \cdot \theta_n^i \cdot \frac{\delta\epsilon_n^i}{\epsilon^i}}$$

We want to keep systematic uncertainty is less than 1 % to do model independent analysis.

If we don't assume any models, we should keep  $\theta_n^i \cdot \frac{\delta\epsilon_n^i}{\epsilon^i} \ll 1 \%$ .

If we can assume SM like Higgs, we should keep  $\text{BR}_n \cdot \theta_n^i \cdot \frac{\delta\epsilon_n^i}{\epsilon^i} \ll 1 \%$ .

# 背景事象の低減 ①

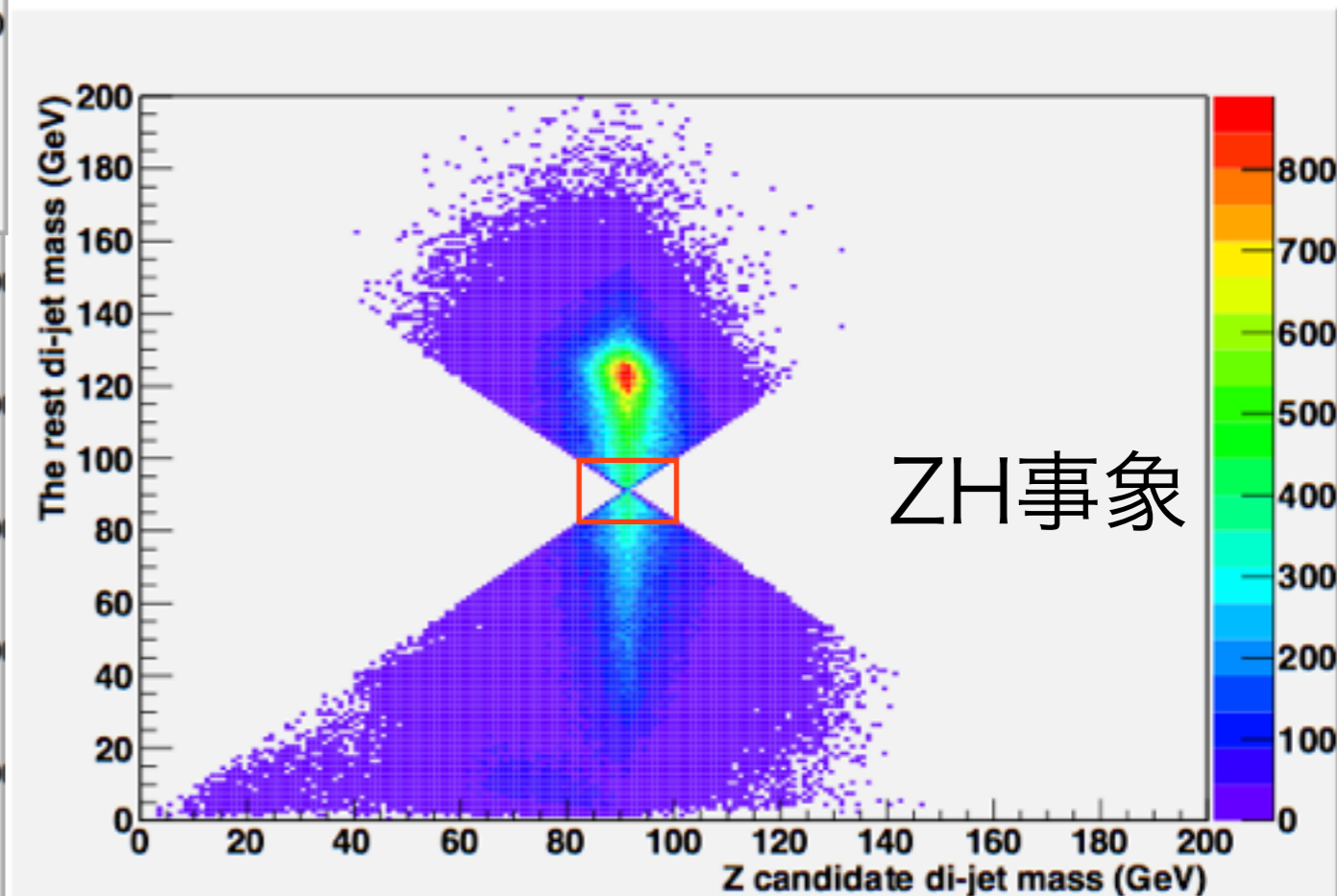
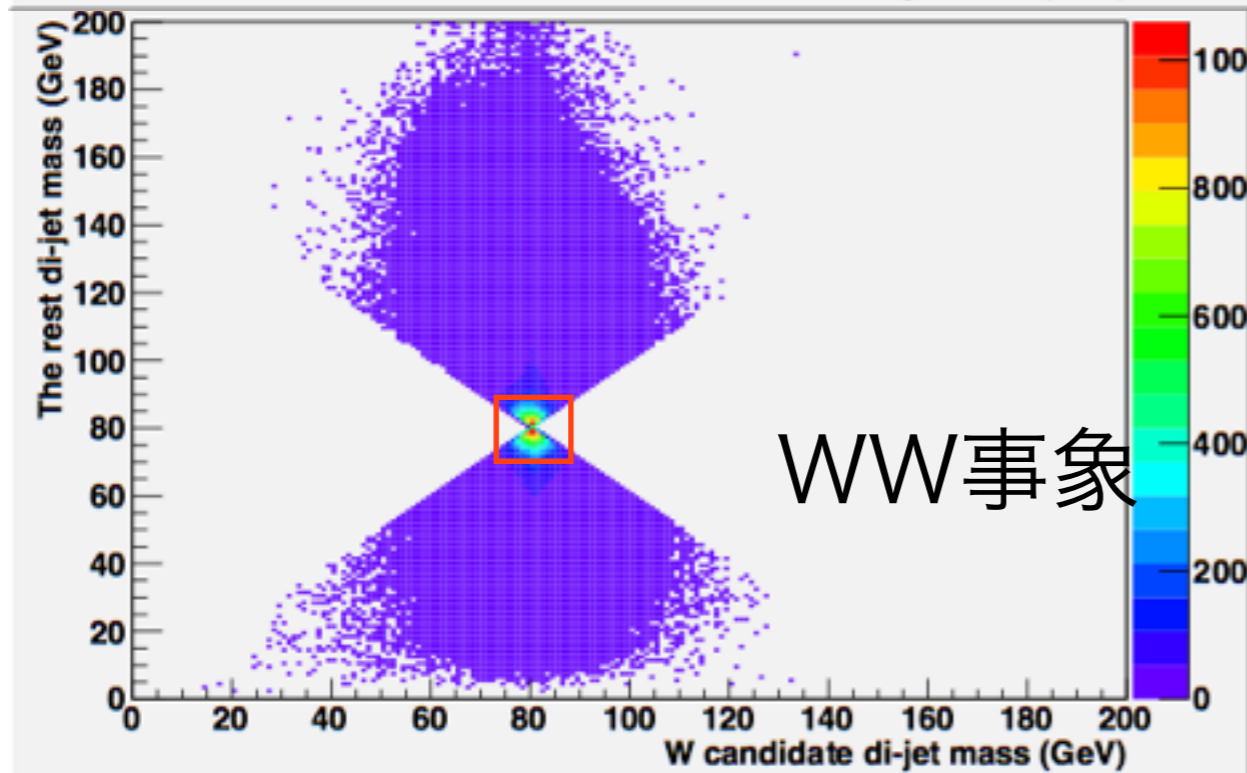
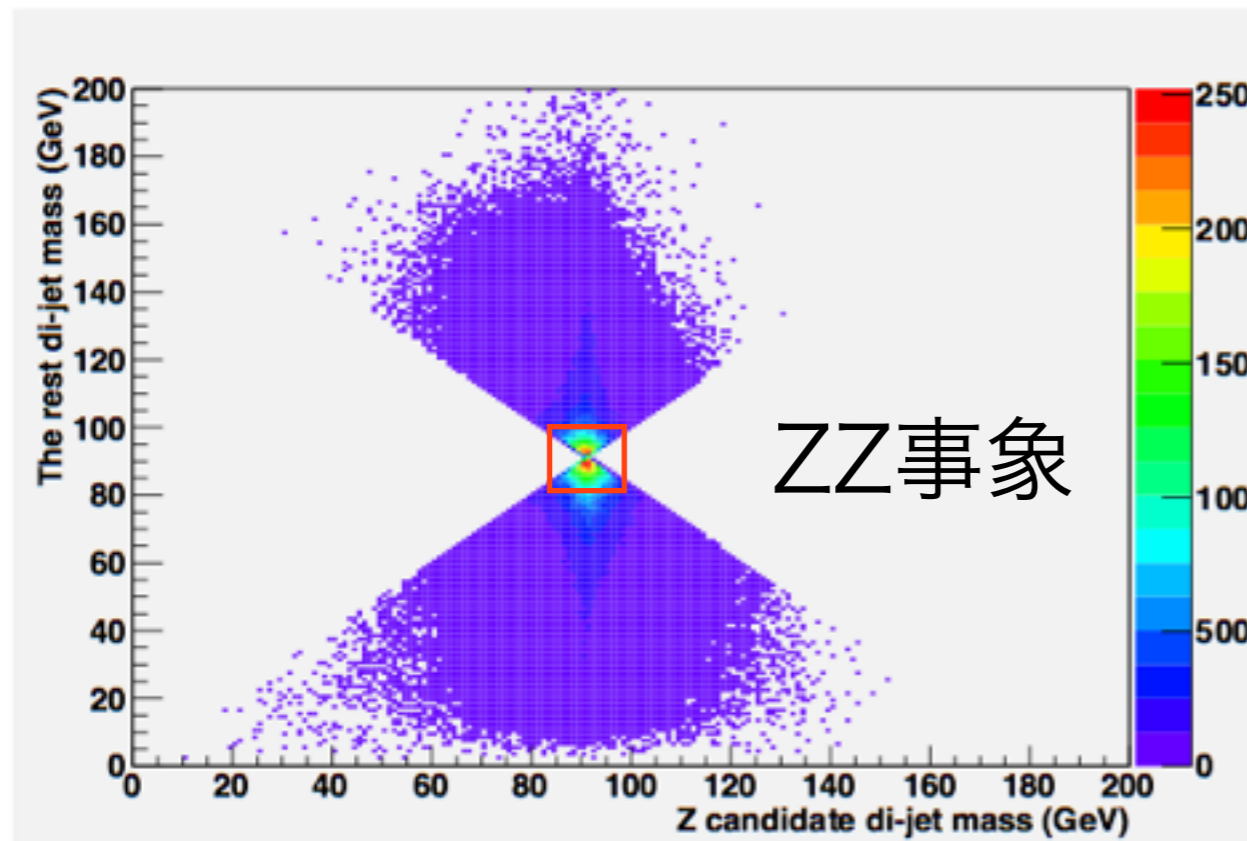
- 4 fermion事象の低減 -> 各粒子の質量差を利用  
4つのジェットにクラスタリング -> 2つずつのジェットの組みで

質量を再構成する

Z粒子 91GeV

W粒子 80GeV

ヒッグス粒子 125GeV



# 背景事象の低減 ②

- 2 fermion 事象の低減のために、SphericityとThrustによるカットを適用した

- Sphericity
  - 観測された事象の球度を表す指標
  - ~0で直線状 ~1で球形

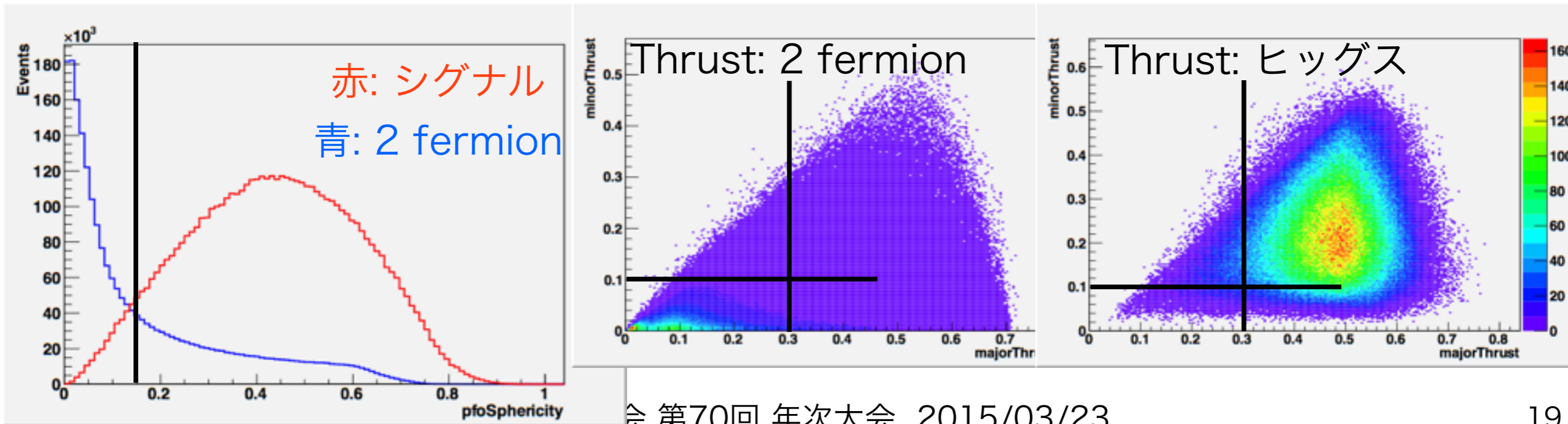
$$S^{ab} = \frac{\sum_i p_i^a p_i^b}{\sum_i p_i^2} \quad a, b = x, y, z$$

- Major Thrust, Minor Thrust
  - 事象のジェットの細さを表す指標

$$T_{major} = \max_{|\vec{n}'|=1, \vec{n}' \cdot \vec{n}=0} \frac{\sum_i |\vec{p}_i \cdot \vec{n}'|}{\sum_i |\vec{p}_i|}$$

$$T_{minor} = \frac{\sum_i |\vec{p}_i \cdot \vec{n}''|}{\sum_i |\vec{p}_i|} \quad \text{with } \vec{n}'' \cdot \vec{n} = \vec{n}'' \cdot \vec{n}' = 0$$

Major Thrust ~ 0 で 3-jet未満、Minor Thrust ~ 0 で 4-jet未満

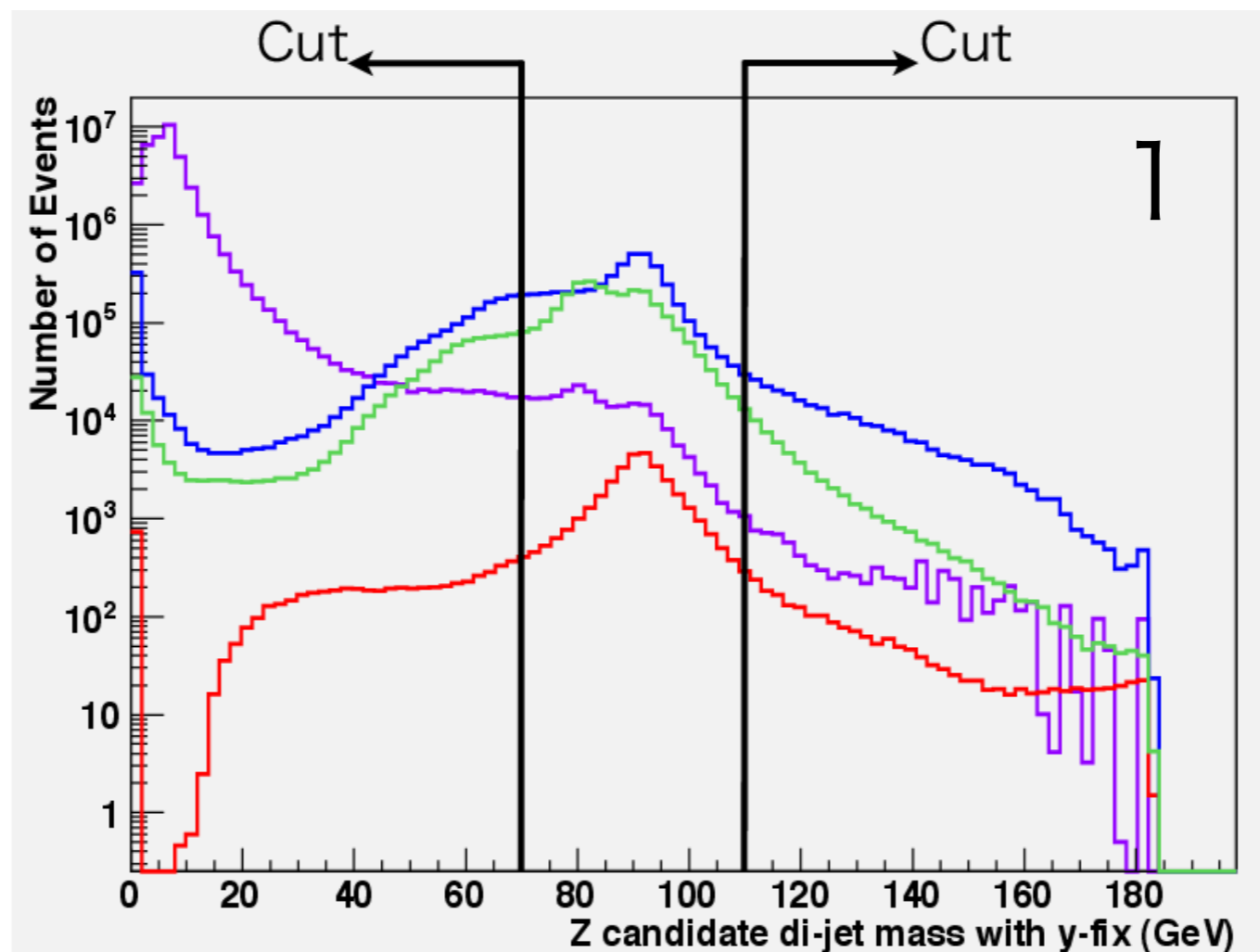


# 背景事象の低減 ③

- 背景事象と信号事象の更なる切り分けのために、  
閾値を設定したジェットクラスタリングにおいて
  - 再構成されたZ粒子の質量 1
  - 再構成されたZ粒子の横方向運動量 2
  - 反跳質量 3

の分布を用いて事象選別をおこなった

シグナル  
2 fermion  
4 fermion  
その他

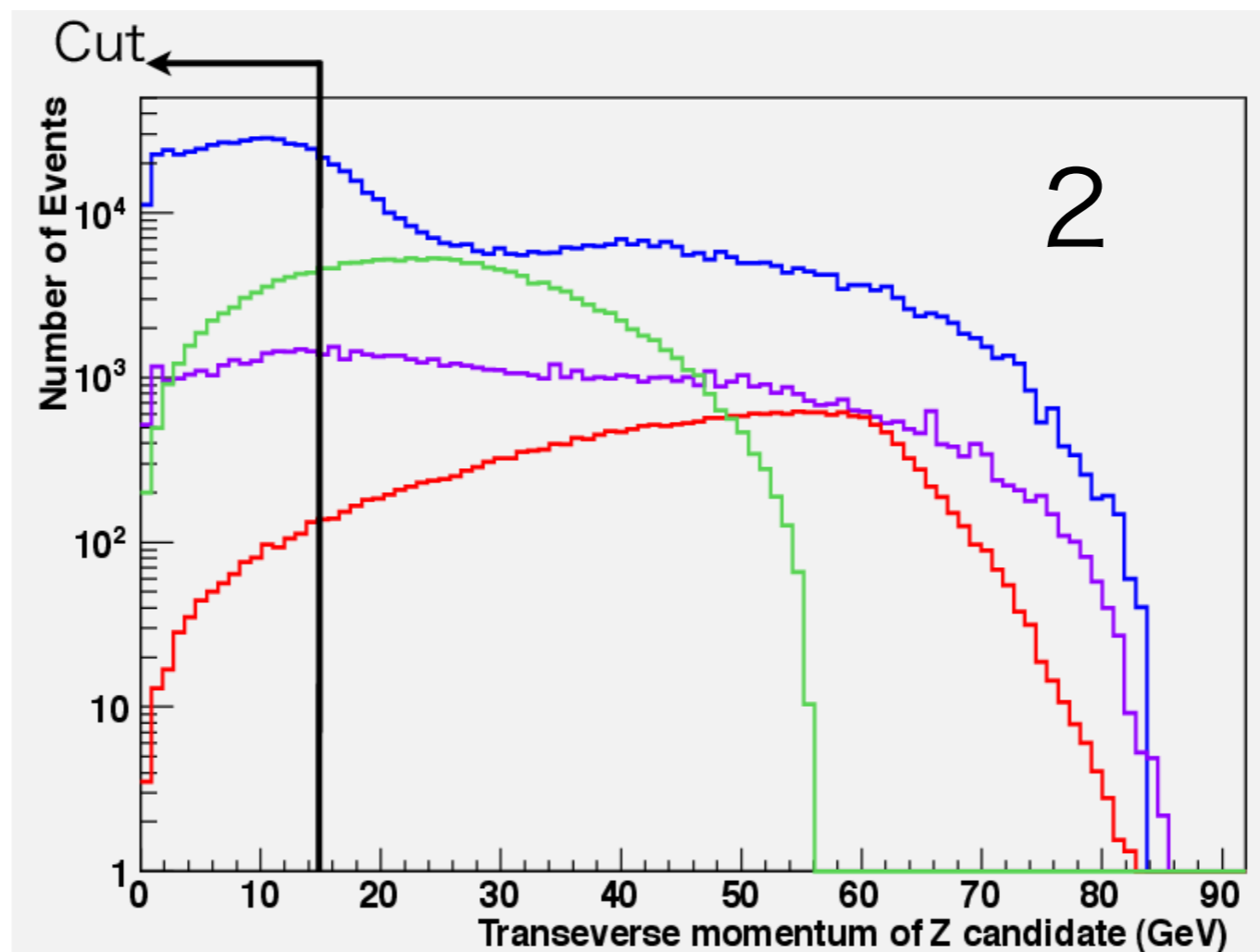


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