

# $\tau$ reconstruction using impact parameters

arXiv:1507.01700

motivation

traditional methods

using impact parameters

application to  $Z H \rightarrow \mu\mu \tau\tau$  in ILD

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# Motivation

tau leptons' decay distributions depend on its spin  
→ we can use them to probe spin-dependent effects

e.g. in  $H \rightarrow \tau \tau$ ,  
different CP states of Higgs induce  
different correlations between tau spins

Fully reconstructing tau decay maximises available information

Difficulty:  
 $\tau$  decays to (at least) one neutrino  
→ missing information

<b>Tau Decay Mode</b>	<b>Branching Fraction</b>
leptonic	~35%
hadronic single prong	~50%
$\pi^+ \nu$	~11%
$\rho^+ \nu \rightarrow \pi^+ \pi^0 \nu$	~26%
hadronic multiprong	~15%
$a_1^+ \nu \rightarrow \pi^+ \pi^+ \pi^- \nu$	~9%

Leptonic tau decays  
involve two neutrinos:  
- less available information  
- ignore for now

Usually have system of two tau leptons

Each hadronic tau decay has 3 unknown parameters (neutrino 3-mom)  
→ 6 unknowns in di-tau system

We can use constraints to induce the value of these unknowns

invariant mass of each tau: 2 constraints

overall  $p_x$ ,  $p_y$  conservation: 2 constraints (if no extra neutrinos in event)

overall  $p_z$ , E conservation ← invalidated by forward ISR/beamstrahlung

need 2 more:

invariant mass of tau-tau system ? (assume from H) ← backgrounds

rest frame of tau-tau system ? (e.g. recoil against Z) ← ISR/bs

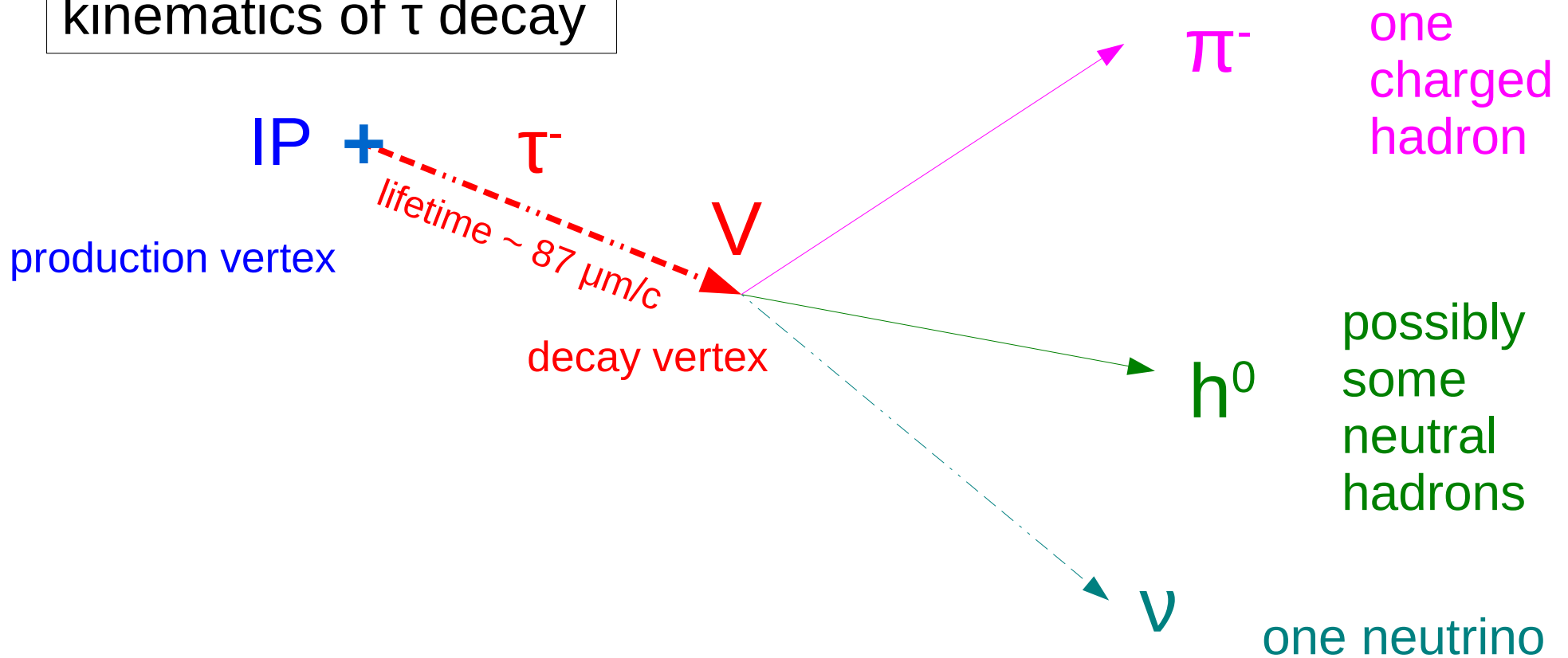
impact parameter information ← if vertex detector is good enough

can consider under-constrained system (e.g. done @ LHC):

scan over solutions allowed by constraints,

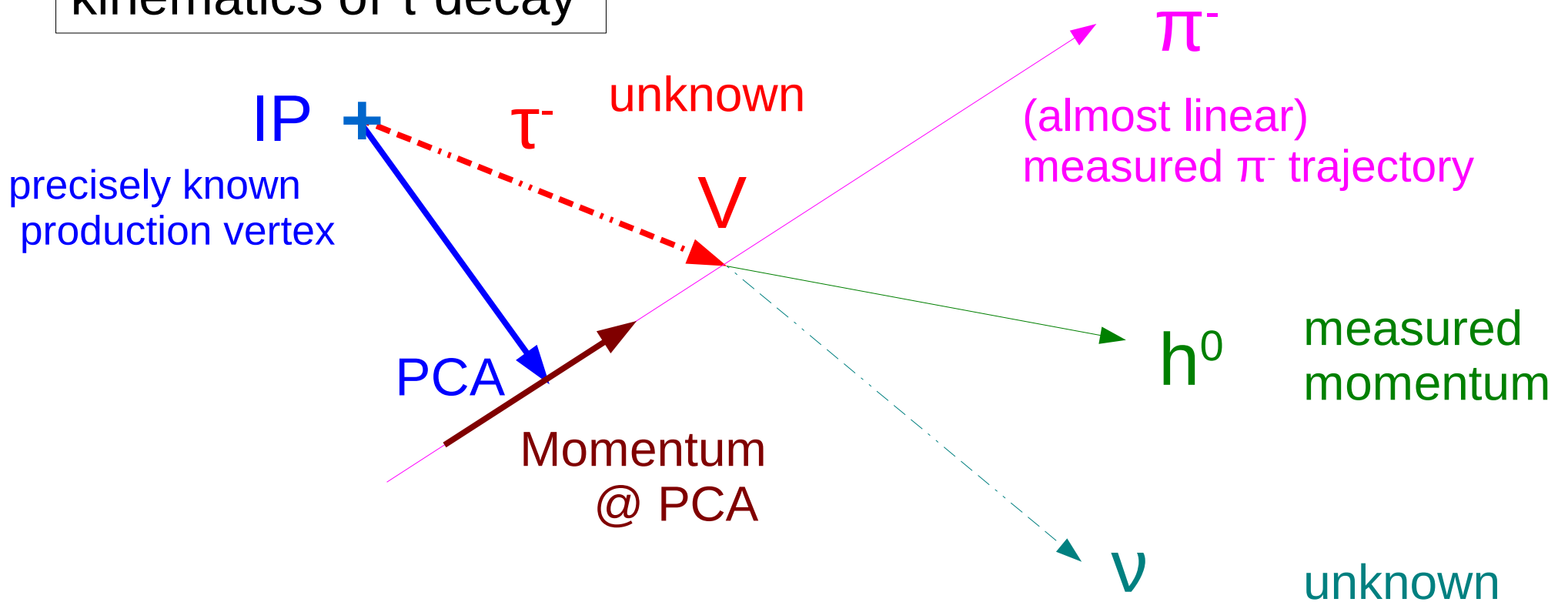
choose most likely one according to known tau decay distributions

# kinematics of $\tau$ decay



For typical tau energies at ILC,  
and for typical experimental B fields,  
trajectories of tau and charged hadron  $\sim$  linear at this scale

# kinematics of $\tau$ decay

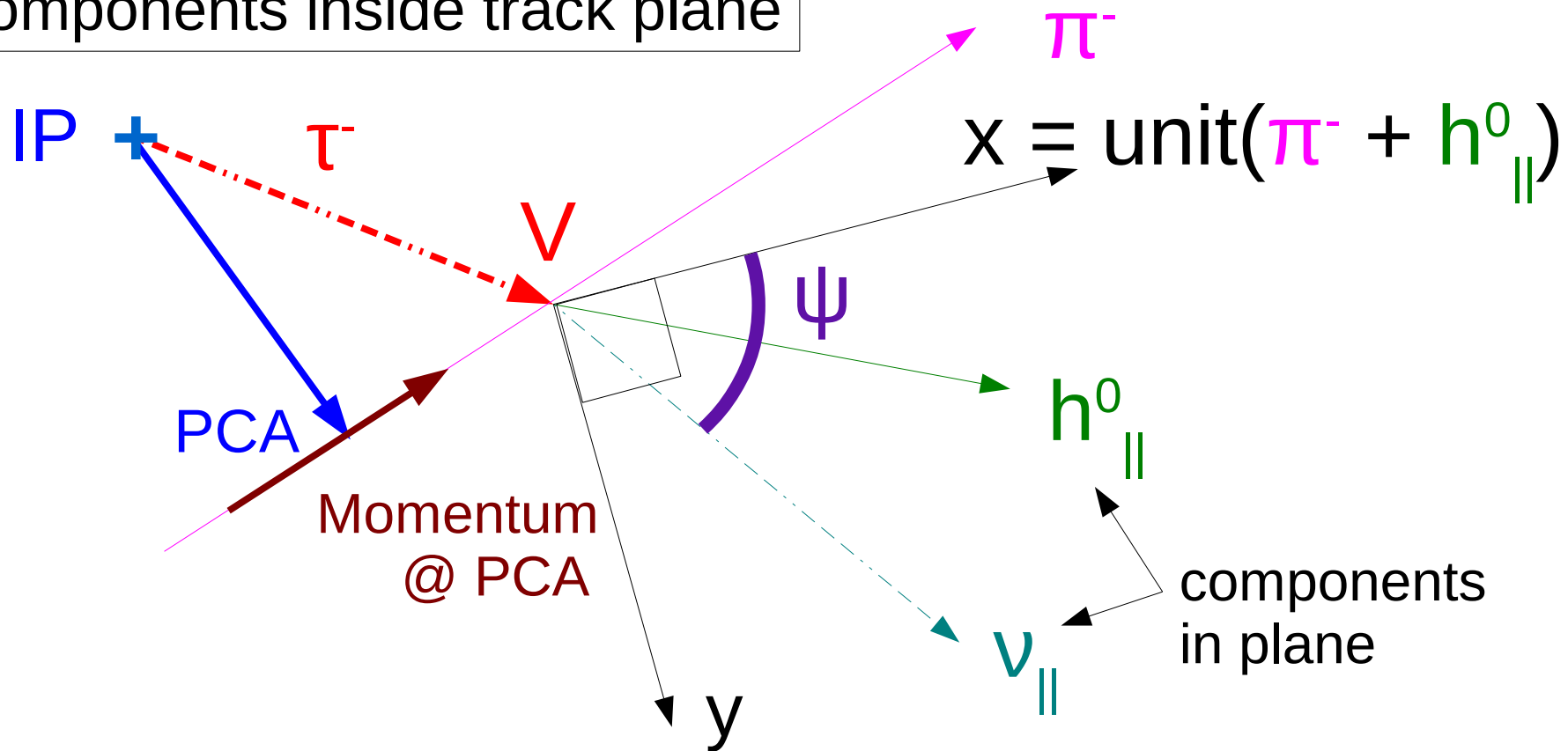


“track plane” defined by **IP-PCA** and **Momentum@PCA**  
(these two vectors are perpendicular for 3d PCA)  
→ requires well measured **IP** and  **$\pi^-$  trajectory**

**$\tau$**  momentum lies inside track plane (linear approx.)  
→ **( $h^0 + \nu$ )** momentum lies in track plane  
→  **$\nu$**  momentum out of plane = -  **$h^0$**  momentum out of plane

→ **we have used the track plane information to infer one component of the neutrino's momentum**

only components inside track plane



parameterise  $v$  momentum inside plane:

$x$  is unit vector parallel to hadronic momentum inside plane

$y$  is unit vector in plane, perpendicular to  $x$

$Q$  is magnitude of momentum in plane

$$v_{||} = Q ( x \cos \psi + y \sin \psi )$$

We can then write the neutrino momentum as

$$\mathbf{v} = Q ( x \cos \psi + y \sin \psi ) - h^0_{\text{perp}}$$

two unknown parameters,  $Q$  and  $\psi$

4-momentum of  $\tau = \pi + h^0 + \nu$

Use  $\tau$  invariant mass to remove one unknown

→ for each choice of  $\psi$  can calculate  $Q$  (in general 2 solutions)

can calculate full kinematics of  $\tau$  for any assumed  $\psi$  : decay length, lifetime  
define likelihood of reconstructed lifetime

(in  $\pi\nu$  decays, one  $Q$  solution gives a negative decay length, can be rejected)

we have reduced unknown  $\nu$  momentum from

three parameters to one (  $\psi$  ) + 2-fold ambiguity

using impact parameter and tau mass constraints

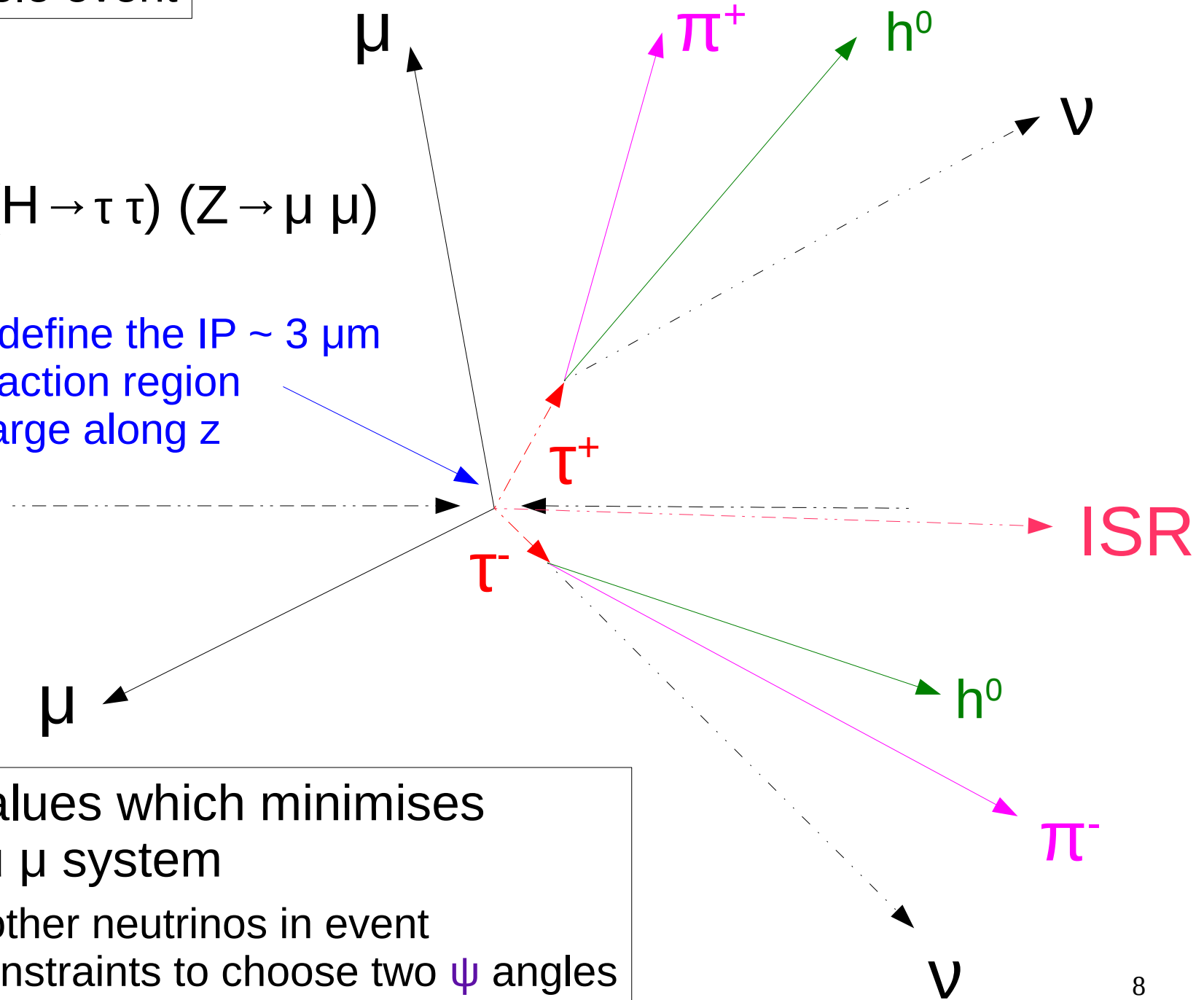
how to determine  $\psi$  ?

consider whole event

*e.g.*

$e^+ e^- \rightarrow (H \rightarrow \tau \tau) (Z \rightarrow \mu \mu)$

$\mu$  tracks define the IP  $\sim 3 \mu\text{m}$   
ILC interaction region  
too large along z



choose  $\psi$  values which minimises  
 $p_T$  of  $\tau \tau \mu \mu$  system

- works if no other neutrinos in event
- use  $p_x, p_y$  constraints to choose two  $\psi$  angles  
→ fully constrained system



...that's the theory

Recap: method needs

precise measurement of charged prong trajectory

precise knowledge of IP in all 3 dimensions

[ “precise” means  $\ll$  typical impact parameters ]

good estimation of neutral hadronic momentum

[ if present ]

balanced  $p_T$  (e.g. no extra neutrinos)

...can it work @ ILC / ILD?

## Test the method

$e^+ e^- \rightarrow H \mu^+ \mu^-$  events generated @ 250 GeV: Whizard2 with CIRCE1 ISR/BS

$H \rightarrow \tau \tau$ ;  $\tau$  decayed by TAUOLA: either both  $\pi^+ \nu$  or both  $\pi^+ \pi^0 \nu$  ( $\rho \nu$ )

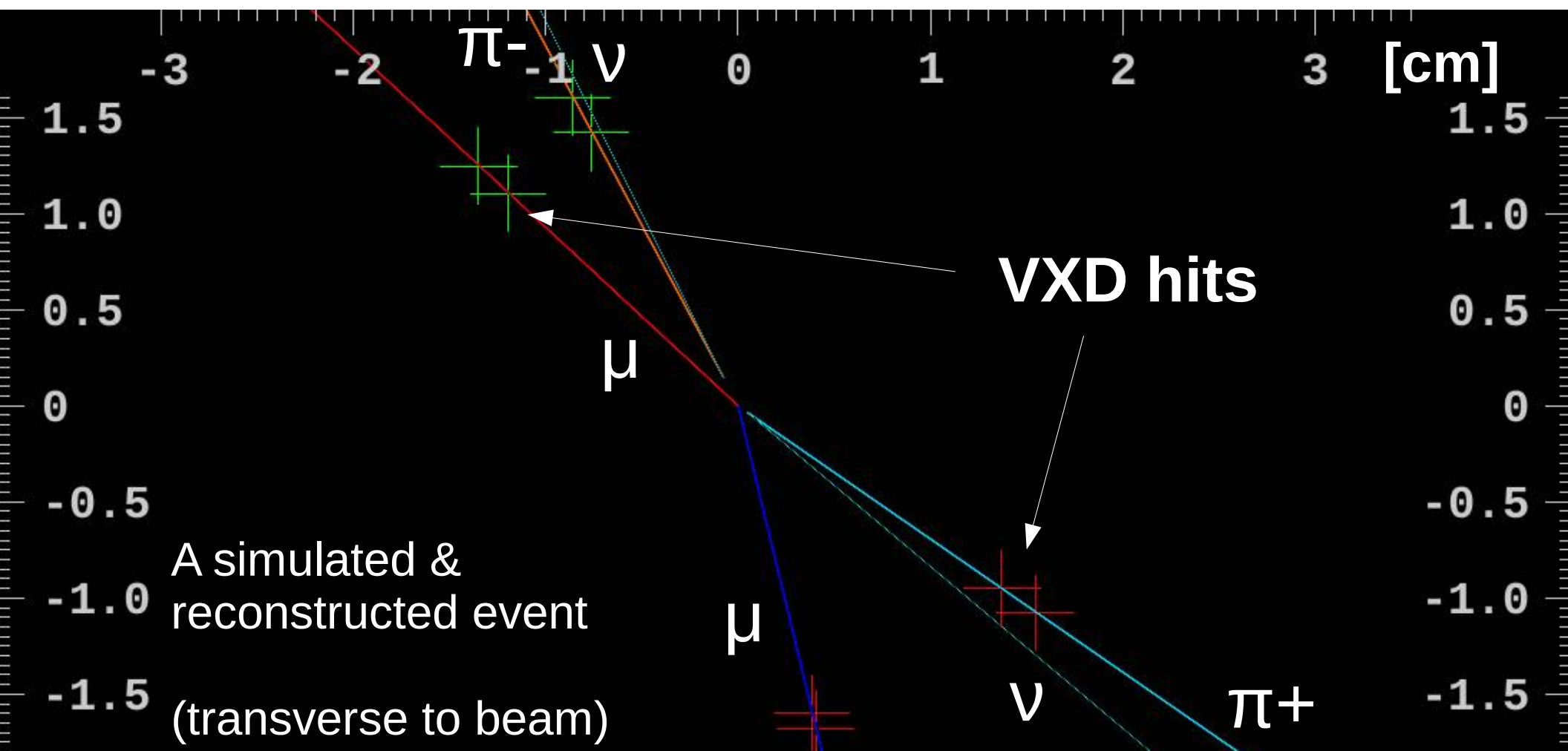
Full ILD simulation, DBD version ILD\_v05\_o1 [no underlying event]

Usual ILD reconstruction + GARLIC photon reconstruction

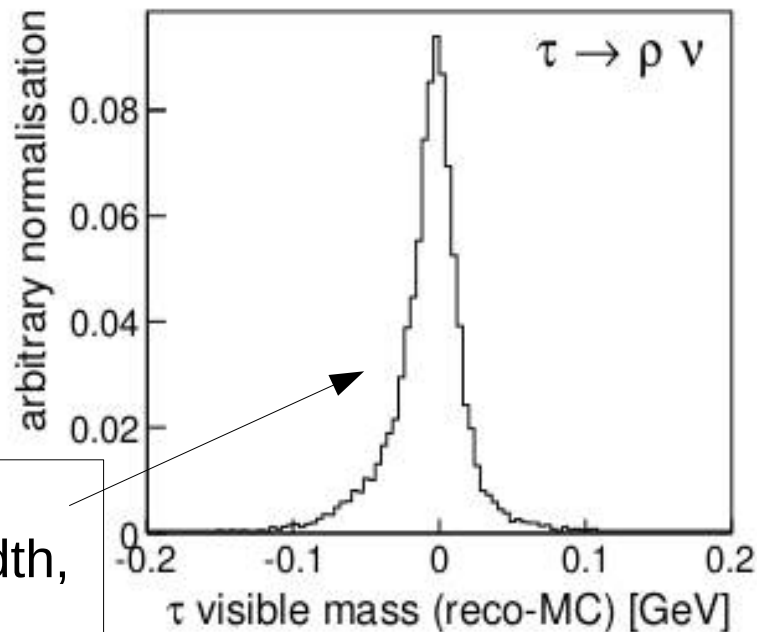
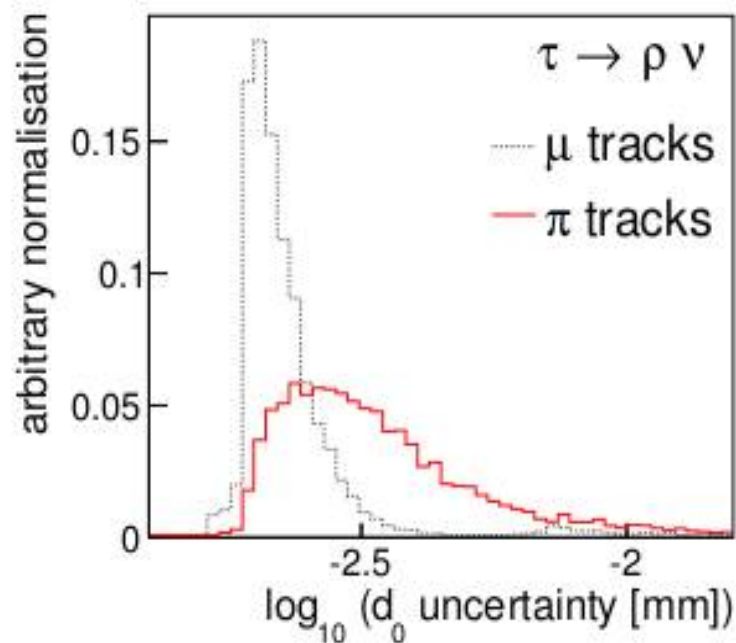
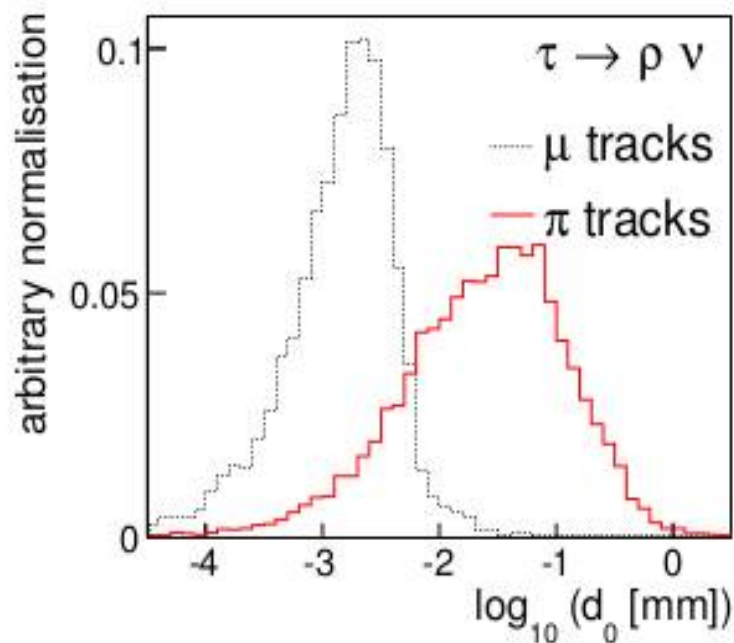
Cheating matching of GARLIC/Pandora clusters to  $\pi^0$ , and of  $\pi$ s to  $\tau$

apply  $\pi^0$  mass constraint to two photon system

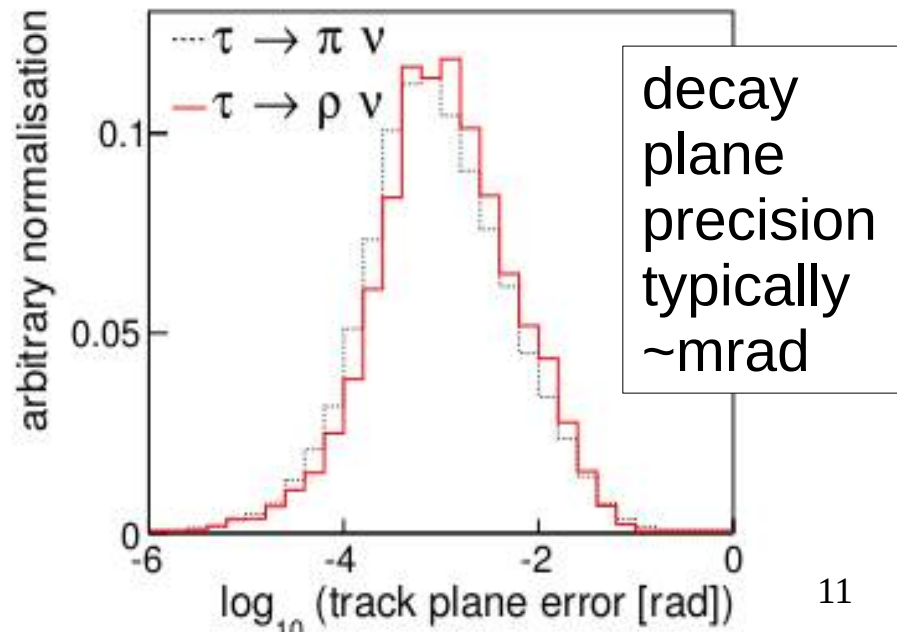
Use  $\mu^+ \mu^-$  tracks to reconstruct IP:  $\sim 3\mu\text{m}$  precision



# reconstruction of tracks, $\rho$ ( $\pi^0$ )



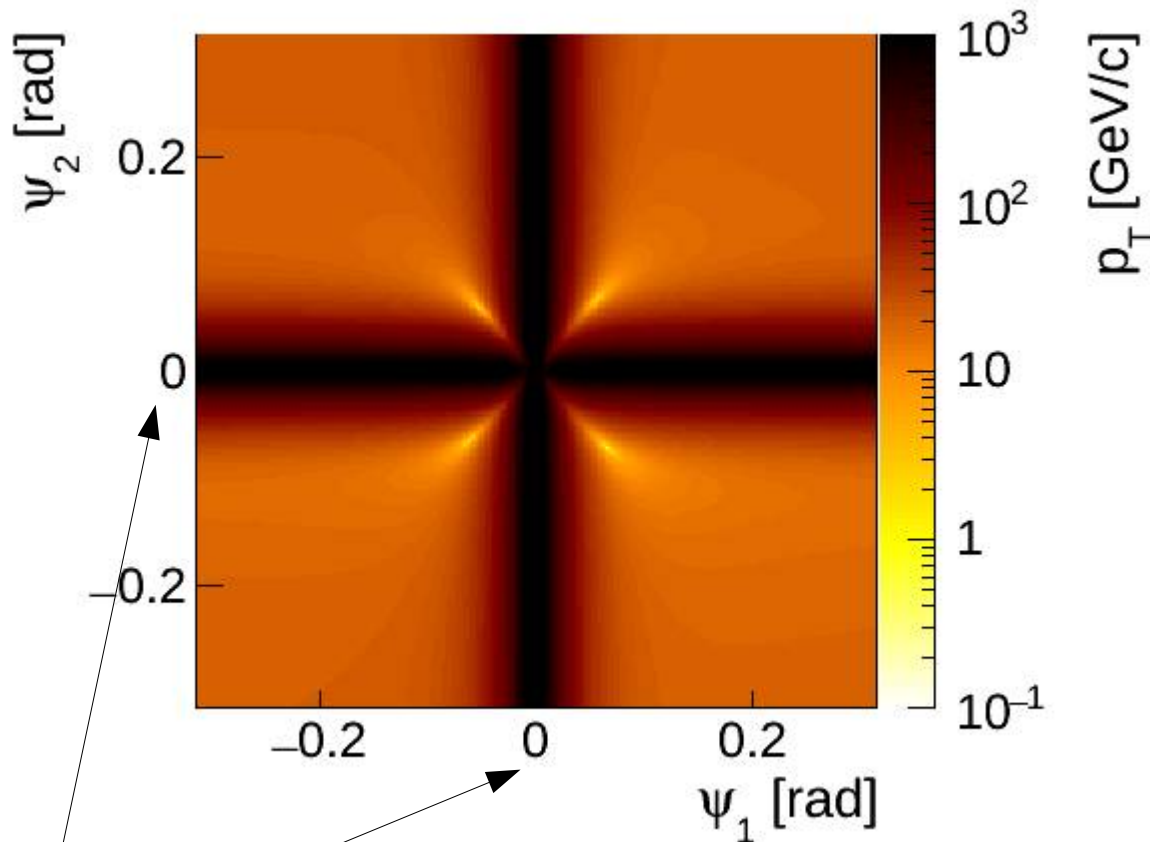
smaller than natural  $\rho$  width, small bias



decay plane precision typically  $\sim$  mrad

angle  $p_\tau$  makes to reconstructed plane

How does event  $p_T$  depend on neutrino angles  $\psi$  chosen for two taus?



one event @ 250 GeV  
 $e^+e^- \rightarrow (H \rightarrow \tau\tau) (Z \rightarrow \mu\mu)$

both  $\tau \rightarrow \pi \nu$

simulated and  
reconstructed in ILD

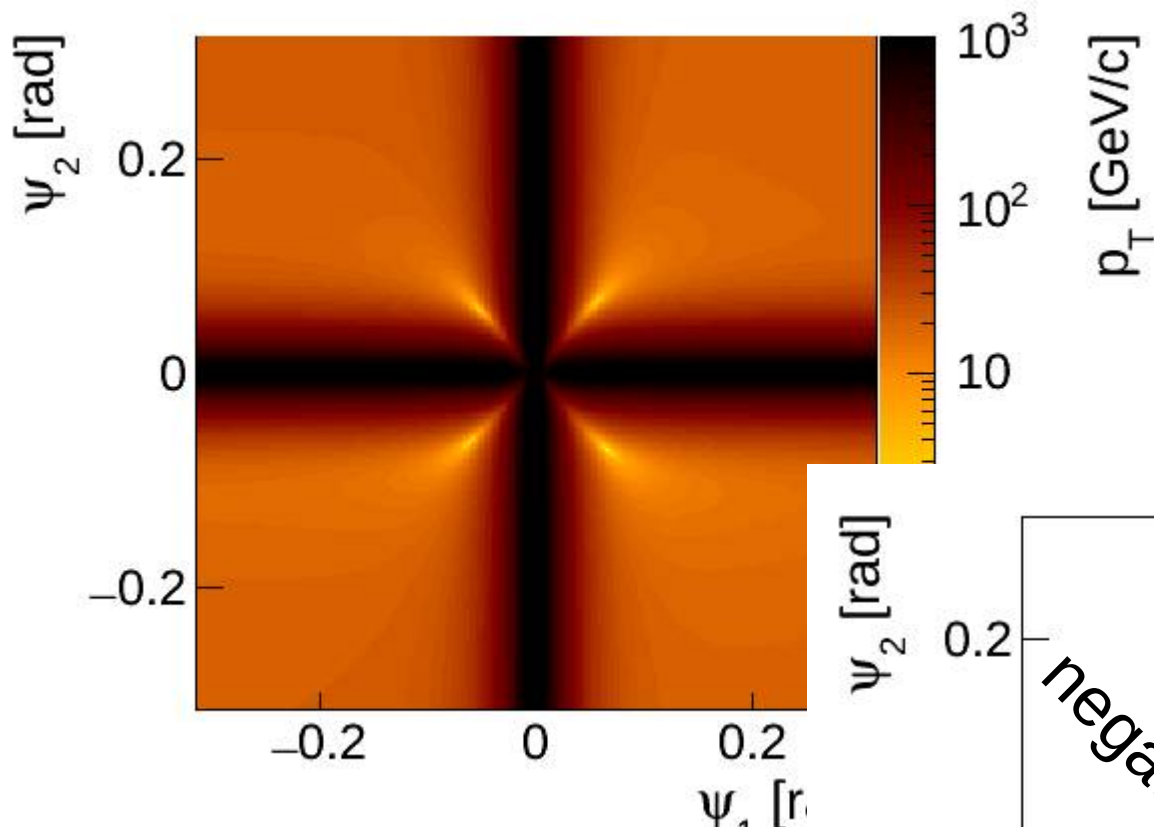
neutrinos collinear  
with hadron momentum  
in track plane

Naturally splits into 4 quadrants @  $\psi=0$

Each quadrant has solution with small  $p_T$   
easy to find using e.g. MINUIT  
rather complicated to do analytically...

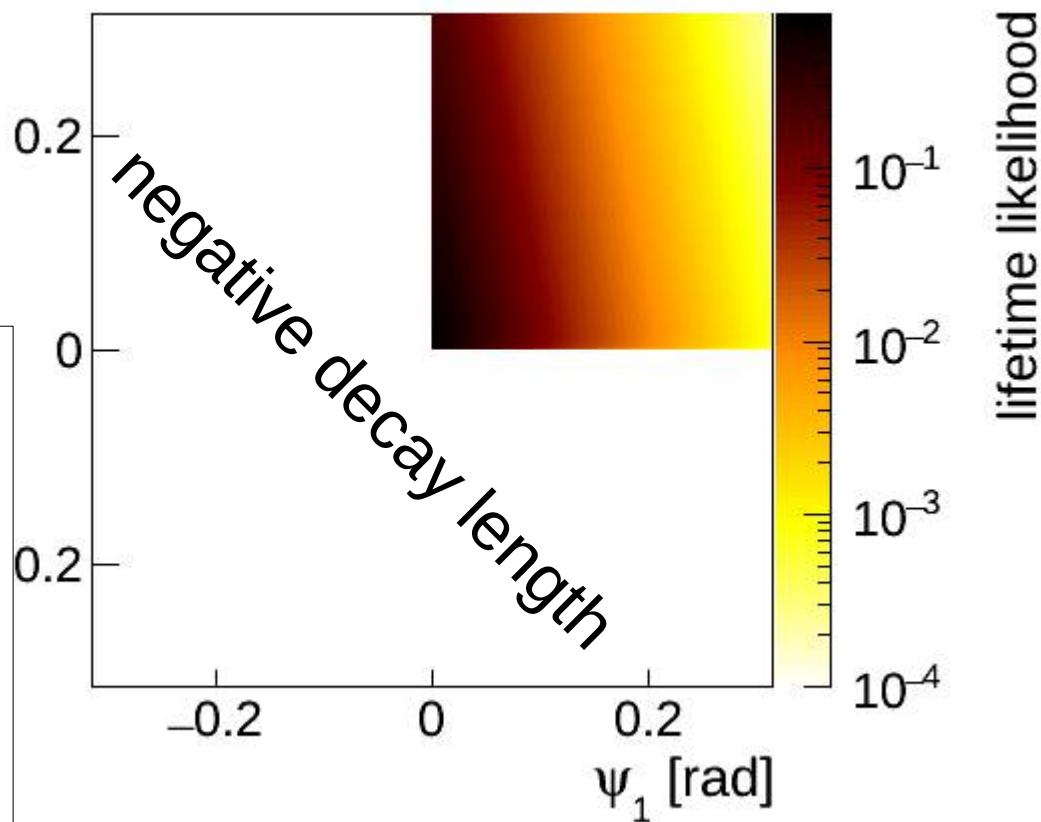
**how to choose which one?**

How does event  $p_T$  depend on neutrino angle  $\psi$  chosen for two taus?



**lifetime likelihood =**

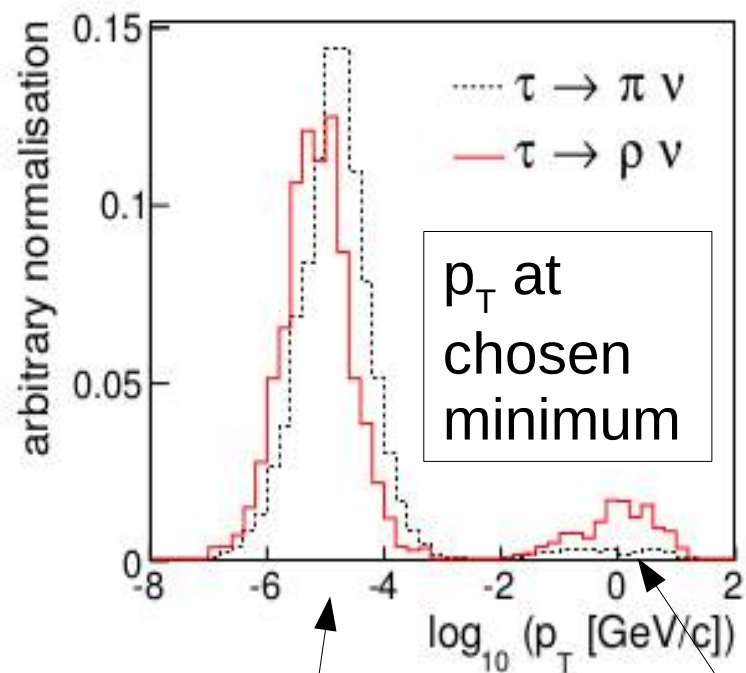
$\exp\{-\text{reconstructed lifetime} / \text{mean tau lifetime}\}$   
 for +ve candidate decay length,  
 0 for -ve decay length



For each event,  
 for each combination of  
 (2-fold) energy solutions

- find  $p_T$  minimum in each quadrant
- reconstruct tau decay length @ minima,  
 reject negative decay lengths
- choose minimum with smallest  $p_T$

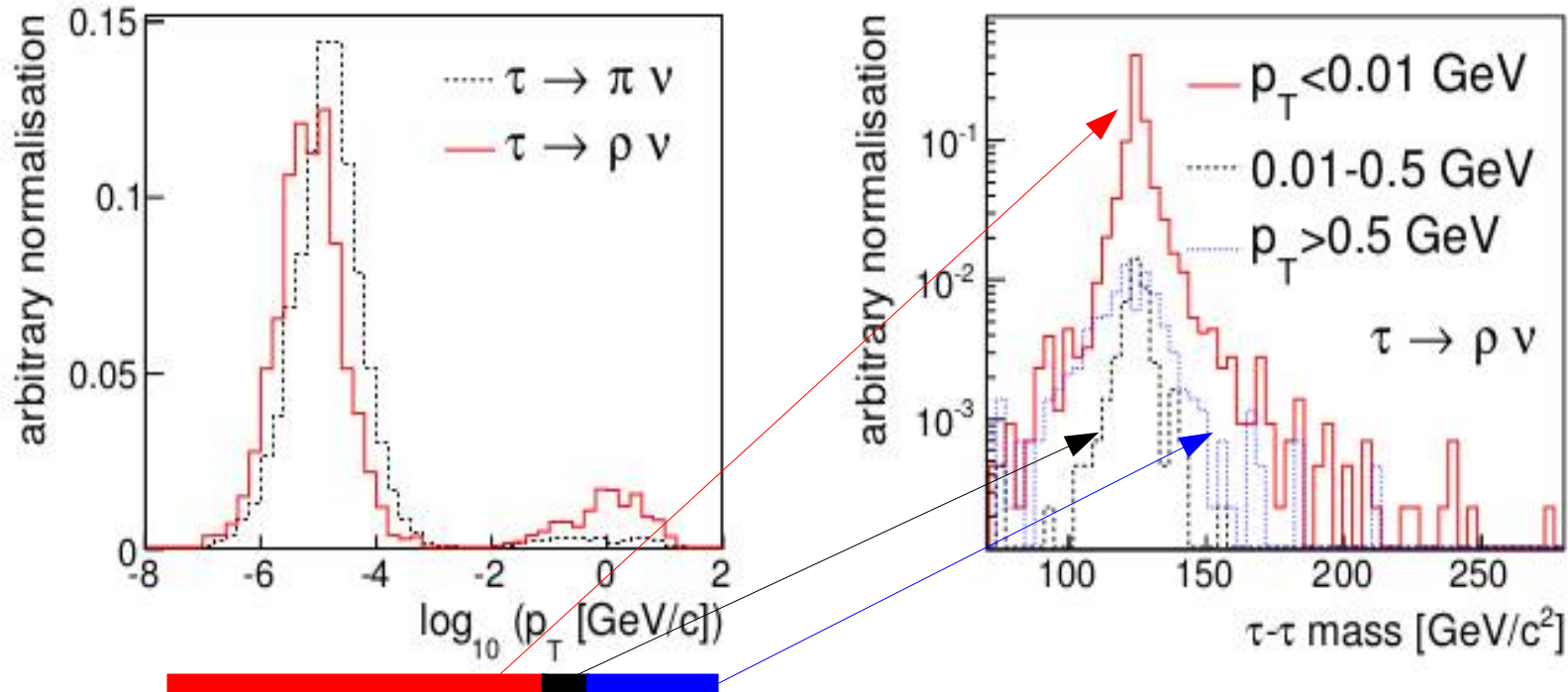
# How well does it work?



a nice minimum is found for most events:  $p_T \sim 10$  keV

some fraction of mis-reconstructed events  
 $p_T \sim 0.1 \rightarrow 10$  GeV  
larger fraction for  $\rho$  decay mode  
(ECAL resolution?)

Check the invariant mass of  $\tau\tau$  system: should be 125 GeV

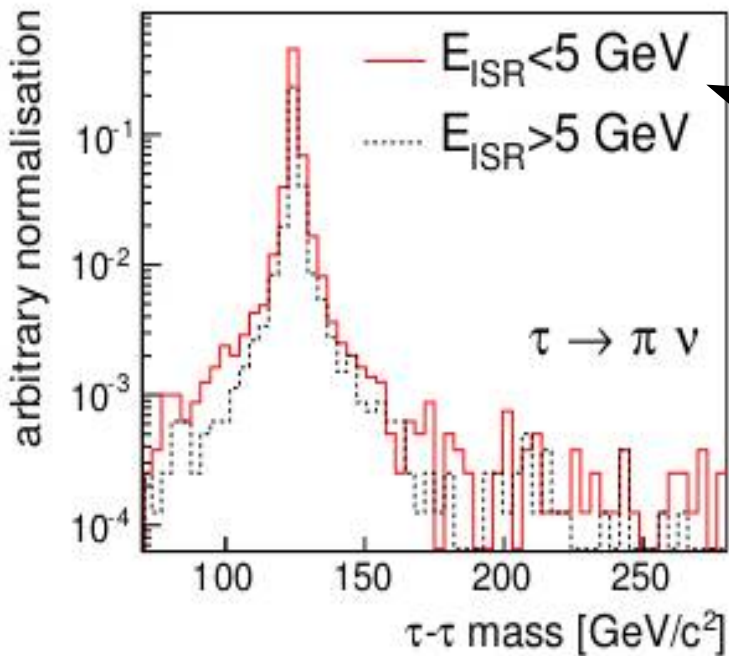
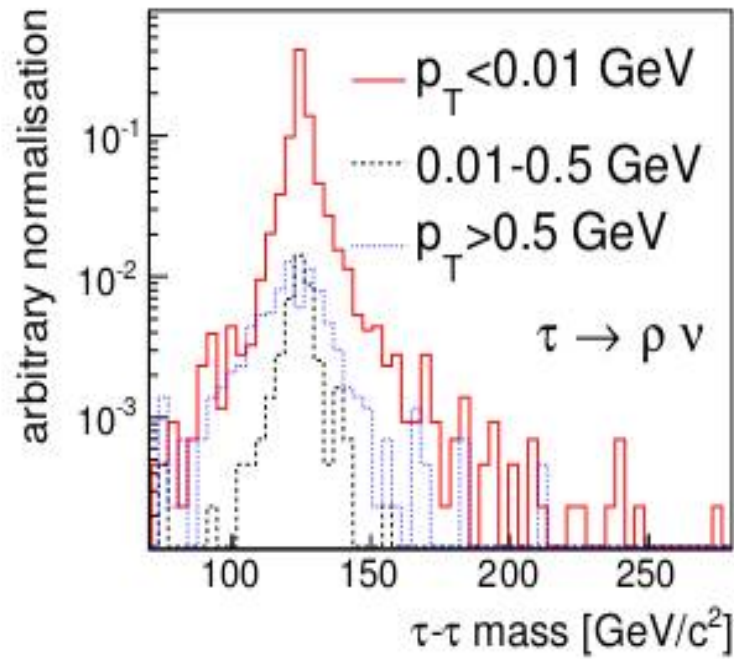
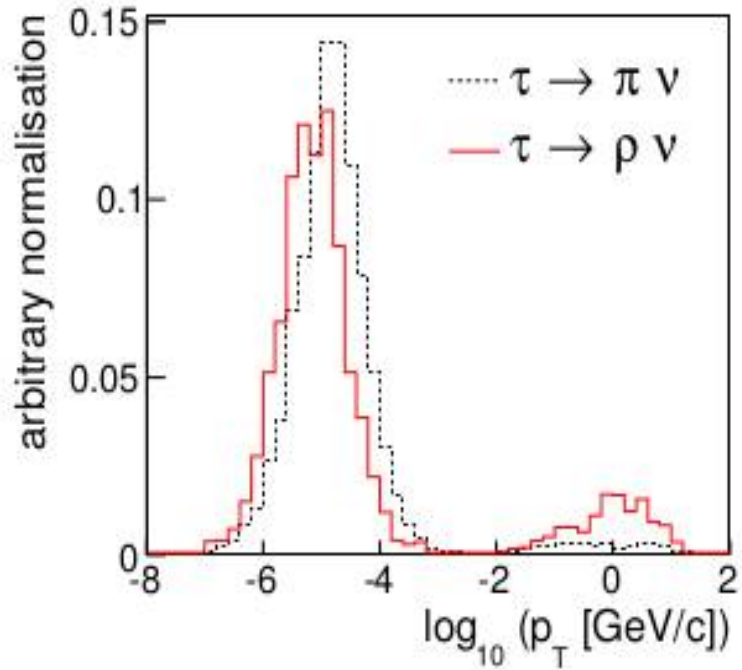


rather sharp mass distribution

even “**misreconstructed events**”  
peaked at 125 GeV



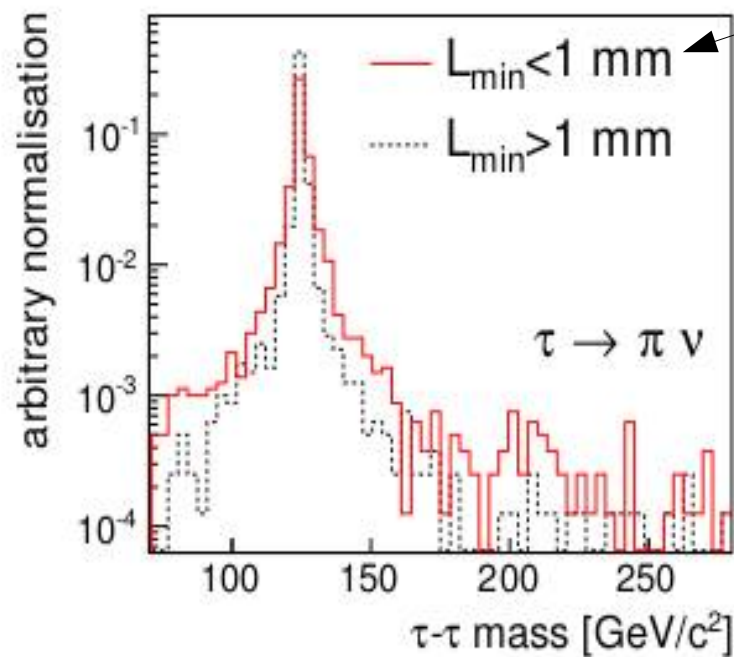
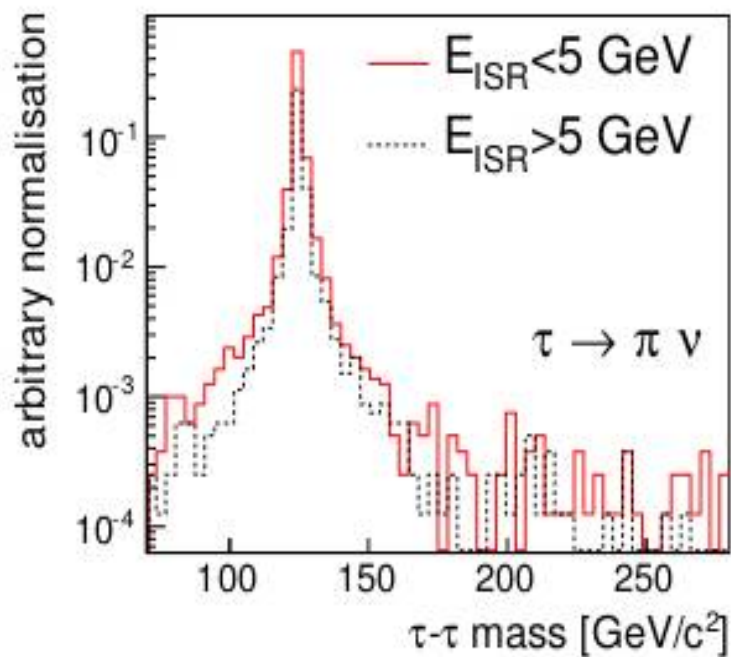
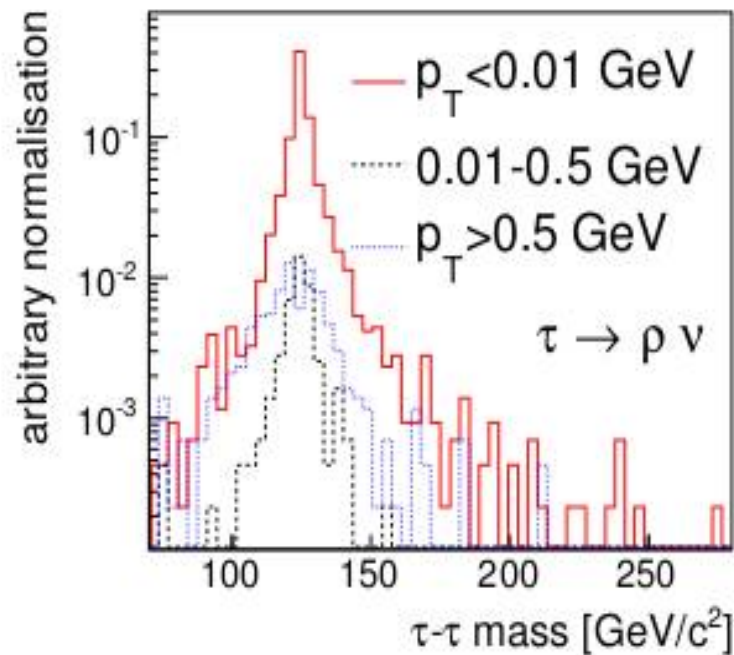
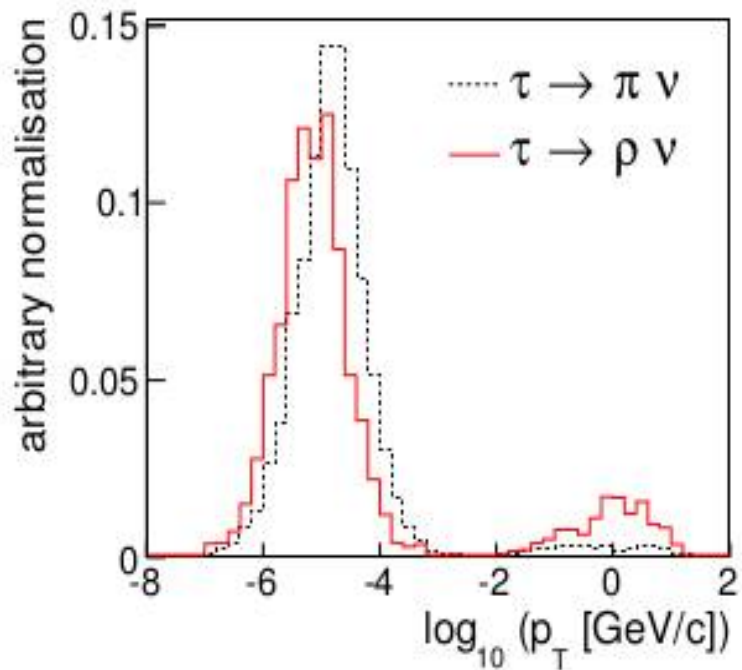
Check the invariant mass of  $\tau\tau$  system: should be 125 GeV



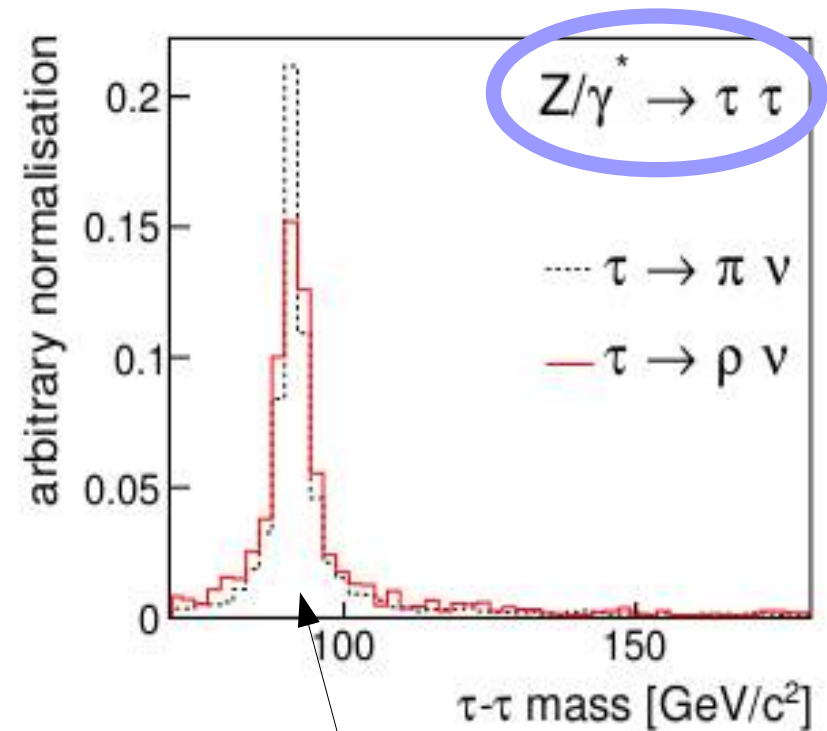
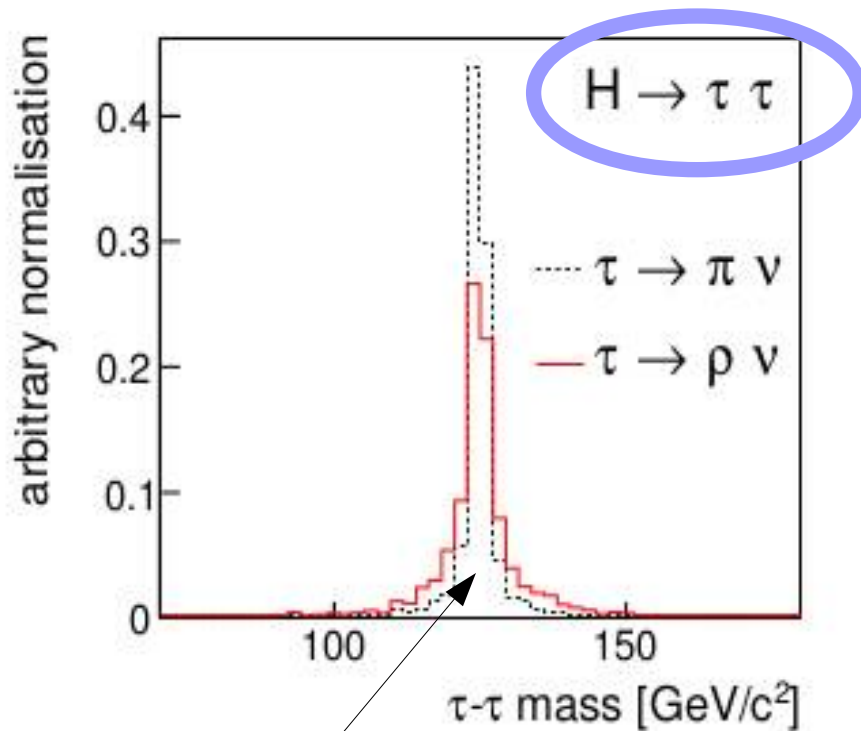
Events with large ISR/bs  
~equally well reconstructed



Check the invariant mass of  $\tau\tau$  system: should be 125 GeV



“unlucky” short-lived taus are somewhat less-well measured



Sharp central peak with longer tails

Gaussian width of central peak

~ 0.6 GeV for  $\pi^+\nu$

~ 1.1 GeV for  $\pi^+\pi^0\nu$

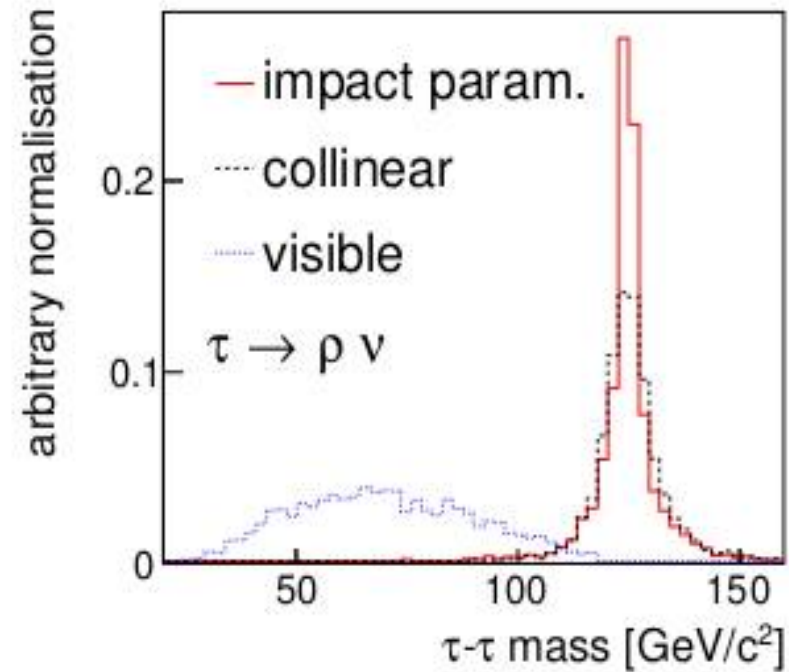
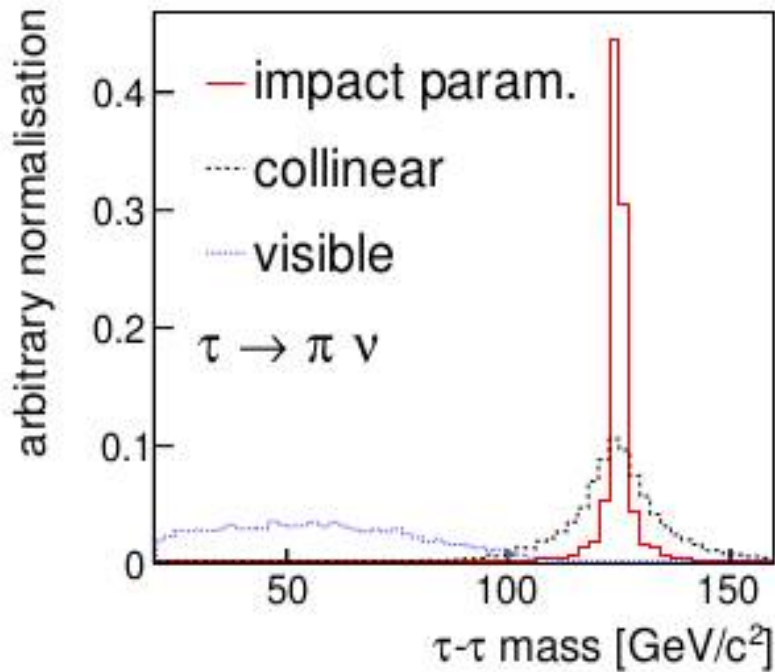
within  $(125 \pm 10)$  GeV:

~ 95% of  $\pi^+\nu$

~ 89% of  $\pi^+\pi^0\nu$

H easily distinguished  
from Z pole

# Comparison to other methods



**impact param.**

method presented in this talk

collinear

assume neutrino collinear with visible tau decay products,

balance event  $p_T$

visible

consider only visible decay products

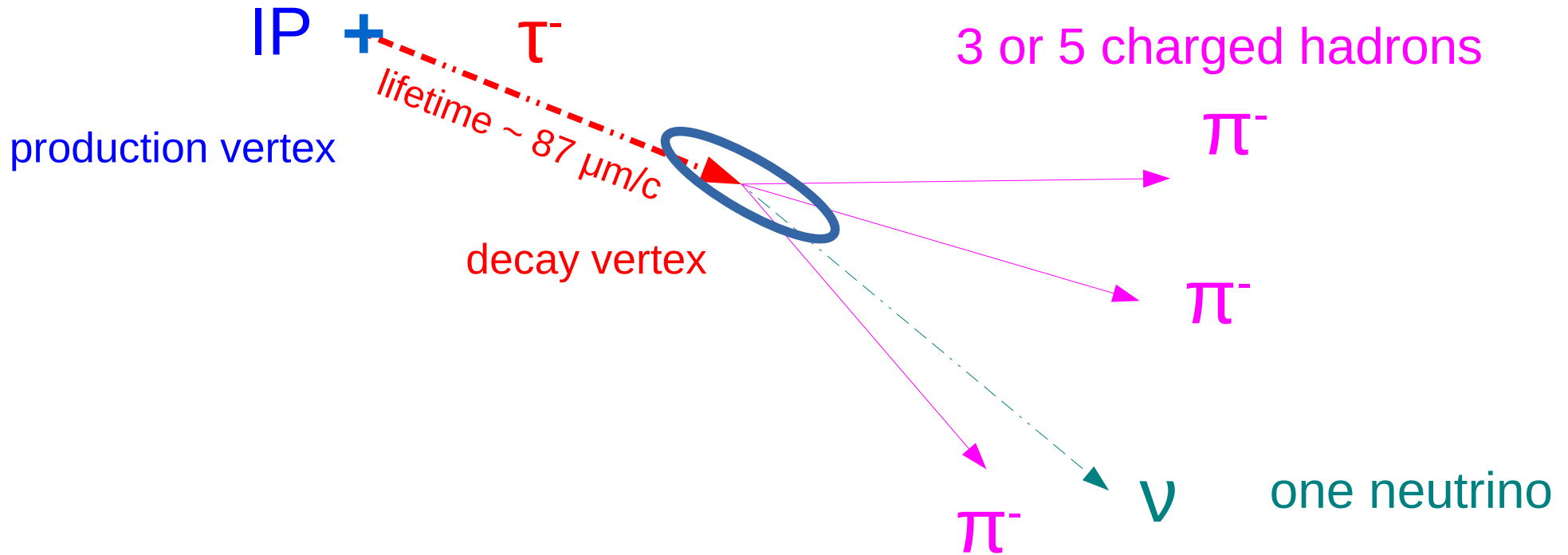
Especially in  $\pi\nu$  channel,

using impact parameters results in much better resolution

Also some improvement in  $\rho\nu$ ,

but limited (probably) by  $\pi^0$  energy resolution

# Multiprong decays



Multiprong vertex to directly measure tau momentum direction:  
applying tau mass constraint gives 2 solutions for neutrino momentum

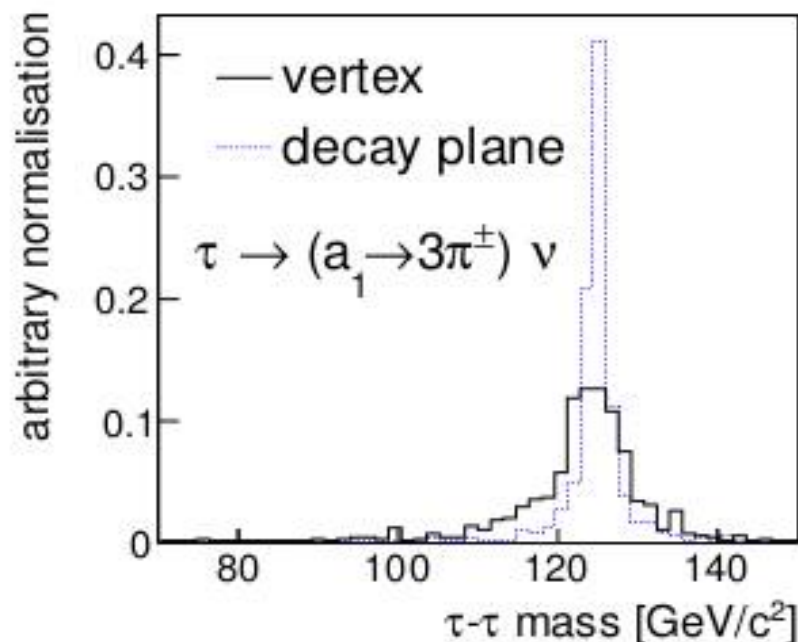
For taus from Higgs decay, error ellipsoid of  
reconstructed tau decay vertex has dimensions  $\sim 2 \times 2 \times 100 \mu\text{m}$

## 1) directly use vertex position

neutrino can be calculated using only tau mass constraint (with 2-fold ambiguity)  
event  $p_T$  used only to distinguish between possible solutions

## 2) use major axis of multiprong vertex ellipsoid to

define tau decay plane, then proceed as for single prong  
event  $p_T$  used to find best solution, check compatibility with measured vertex



Precision of tau decay vertex reconstruction  
less good than of event  $p_T$ ,  
at least when recoiling against muons

# leptonic tau decays

one more constraint required per leptonic tau decay  
(energy of 2-neutrino system)

possible strategies:

assume no ISR ?	+ 2 constraints
assume 1 ISR photon ?	+ 1 constraint
assume $\tau$ $\tau$ mass ?	+ 1 constraint

not hopeless, to be studied...

# Summary

Impact parameters of tau decay prongs can help reconstruct tau decays if IP is well-known:

either very small interaction region (smaller than ILC in  $z$ )  
or tau recoils against prompt charged particles  
and vertex detector sufficiently precise

Tau pair events can then be completely reconstructed by assuming only event's  $p_T$  balance (if both decay hadronically:  $\sim 40\%$  of events)

Works well in ILD:  $\tau\tau$  mass resolution  $\sim 1 - \text{few GeV}$   
when recoiling against muons (hadronic system to be checked)

Since only  $p_T$  balance is used,  
can work at hadron collider experiments

Powerful tool to measure CP structure of Higgs

