



Higgs recoil mass study

**ILC Physics Meeting
3/13/2015**

Jacqueline Yan (Univ. of Tokyo)

This week

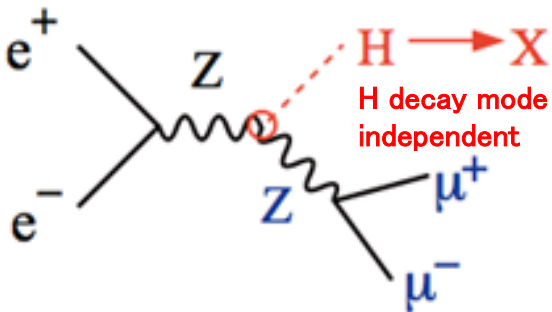
- Further improvement of xsec precision and BG rejection
- new techniques in removing 2f_Z_leptonic BG while preventing signal loss
- implemented isolation cut for muon and gamma
- optimization of likelihood cut
- began applying to 250 GeV

ILC sample used in analysis

channel	mh	ECM	L	Spin polarization	Detector simulation
$e^+e^- \rightarrow Zh \rightarrow \mu\mu h$	125 GeV	350 GeV	333 fb ⁻¹	$P(e^-, e^+) = (-0.8, +0.3)$ $(+0.8, -0.3)$	Full ILD (ILD_01_v05 DBD ver.)

signal

Pe2e2h_eL.pR / Pe2e2h_eR.pL



$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

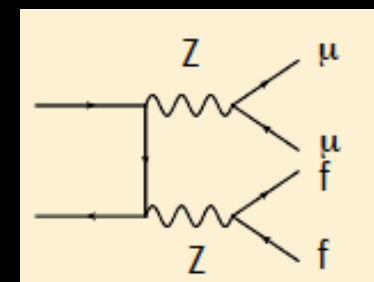
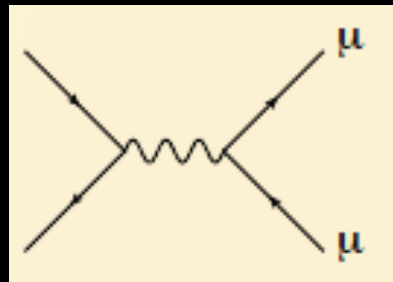
Higgs recoil against di-lepton ($\mu\mu$) system

BG :

all 2f, 4f, 6f processes

major BG after event selection:

2f_Z_l ($\mu\mu$), 4f_WWsl, 4f_ZZ_sl ($\mu\mu ff$, $\mu\mu\nu\nu$)



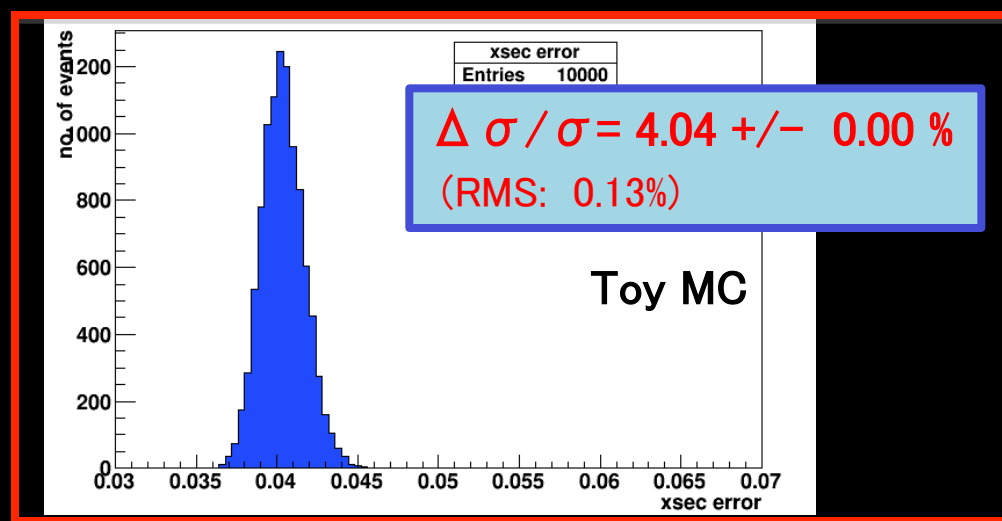
History of past weeks

cuts	(both eLpR and eRpL)		S/B ratio	sig eff	$\Delta \sigma / \sigma_{MC}$	(only eLpR)			
	Nsig	Nbg				2f_Z_l	4f_WW_sl	4f_ZZ_sl	
2 weeks ago	1056	2189	0.48	46.1 (74%)	4.39+/-0.00% (RMS: 0.16%)	225 (0.011%)	241 (0.009%)	950 (0.52%)	
1 week ago (best result)	1062	2010	0.53	46.4 (74%)	4.27+/-0.00% (RMS: 0.15%)	95 (0.004%)	306 (0.010%)	967 (0.53%)	
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- Significant reduction in each major BG (25% reduction !!)
- improvement in xsec precision
- Signal efficiency before M_{recoil} cut is about 10% higher

What contributed ??

- More sophisticated methods to remove 2f_Z BG without losing much signal
- isolation cuts for muon and gamma
- usage of likelihood cut



Muon Selection

event selection

- reject neutrals
- $P_{\text{total}} > 5 \text{ GeV}$
- $E_{\text{cluster}} / P_{\text{total}} < 0.5$
- $\cos(\text{track angle}) < 0.98$ & $|D0/\delta D0| < 5$

Best muon pair candidate Selection

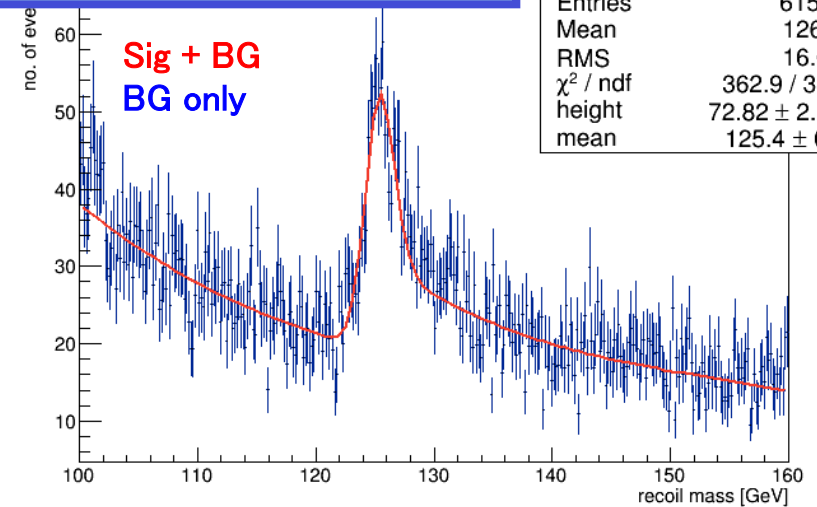
- opposite charge
- invariant mass closest to Z mass

Final Selection

- $84 \text{ GeV} < M_{\text{inv}} < 98 \text{ GeV}$
- $10 \text{ GeV} < pT_{\text{mumu}} < 140 \text{ GeV}$
- $dpt_{\text{bal}} = |pT_{\text{mumu}} - pT_{\gamma_{\text{max}}}| > 10 \text{ GeV}$
- $|\cos(\theta_{Z\text{pro}})| < 0.91$
- $120 \text{ GeV} < M_{\text{recoil}} < 140 \text{ GeV}$

Cut values optimized in terms of signal efficiency and $\Delta \sigma / \sigma$

recoil mass fitting



- Signal: GPET
- BG: 3rd order polynomial

definition

- M_{inv} : invariant mass of 2 muons
- pT_{mumu} : pT of reconstructed muons
- $pT_{\gamma_{\text{max}}}$: pT of most energetic photon
- $\theta_{Z\text{pro}}$ = Z production angle

This part is changed !!

Final Selection

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definition

- M_{inv} : invariant mass of 2 muons
- pT_{mumu} : pT of reconstructed muons
- $pT_{\gamma_{\text{max}}}$: pT of most energetic photon
- θ_{Zpro} = Z production angle
- $E_{\text{cone_mu}}$: cone energy ($\cos\theta > 0.9$) around muon
- $E_{\text{cone_}\gamma}$: cone energy ($\cos\theta > 0.9$) around most energetic γ
- $Pt_{\text{sum}} = |Pt_{\text{dl}} - Pt_{\gamma}|$ (in vectors)

Final Selection NEW

- $E_{\text{cone_mu}} < 110 \text{ GeV}$
- $73 \text{ GeV} < M_{\text{inv}} < 120 \text{ GeV}$ widened
- $10 \text{ GeV} < pT_{\text{mumu}} < 140 \text{ GeV}$
- $E_{\text{cone_}\gamma} > 10 \text{ GeV}$ (*)
- $Pt_{\text{sum}} > 40 \text{ GeV}$
- $dptbal = pT_{\text{mumu}} - pT_{\gamma_{\text{max}}} > 60 \text{ GeV}$ (*)
- $|\cos(\theta_{\text{Zpro}})| < 0.91$
- $120 \text{ GeV} < M_{\text{recoil}} < 140 \text{ GeV}$

Added isolation

Combine two types of
pt_balance cuts

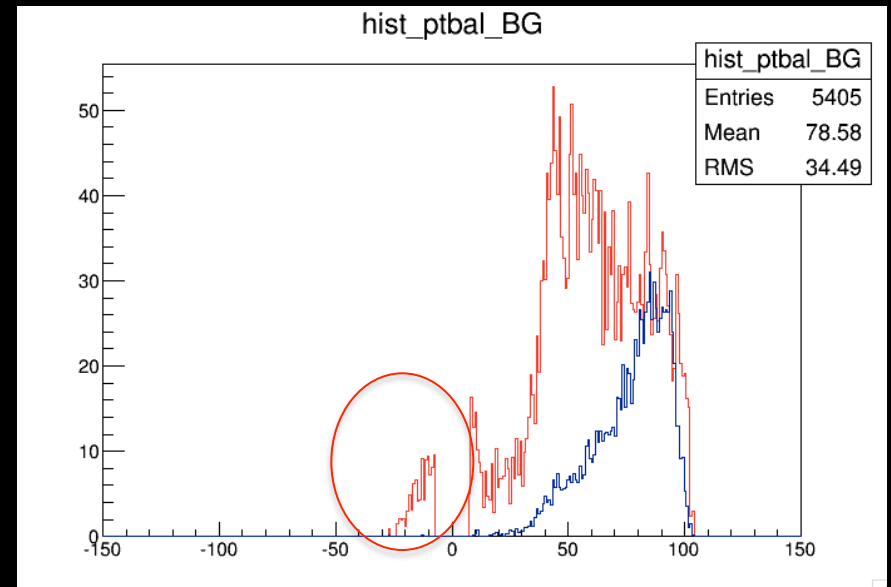
(*) used in coincidence with
extra requirements to prevent
signal loss

First of all...

Thanks to Junping-san's suggestions

Now I do $d_{\text{ptbal}} > 10 \text{ GeV}$ (instead of $|d_{\text{ptbal}}| > 10 \text{ GeV}$)
→ some improvement

	Nsig	NBG	S/B	$\Delta\sigma/\sigma(\text{MC})$
Old: $ d_{\text{ptbal}} > 10 \text{ GeV}$	1056	2189	0.48	4.39+/- 0.00 % (rms: 0.16%)
New : $d_{\text{ptbal}} > 10 \text{ GeV}$	1055	2119	0.50	4.33+/- 0.00 % (rms: 0.15%)



NEW Concern

possible slight bias on signal due to dptbal cut

(I just didn't realize it before since I was observing events AFTER Mrecoil cut)

to escape bias on signal

I tried to cut events that can be identified as 2f_Z_leptonic BG

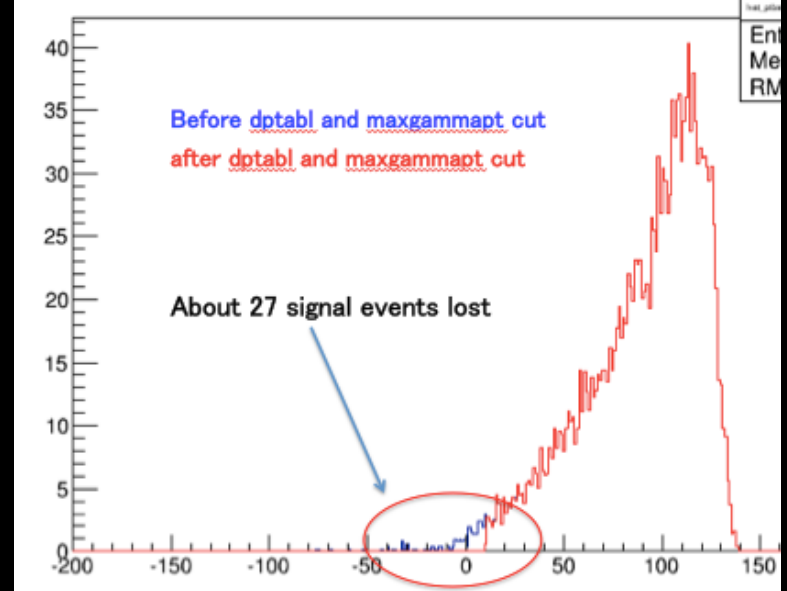
do if (A) && (B) continue

where (A, B) = conditions on

- (maxgammaPt) and (dPtbal)
- (cos θ bal) and (Ebal)

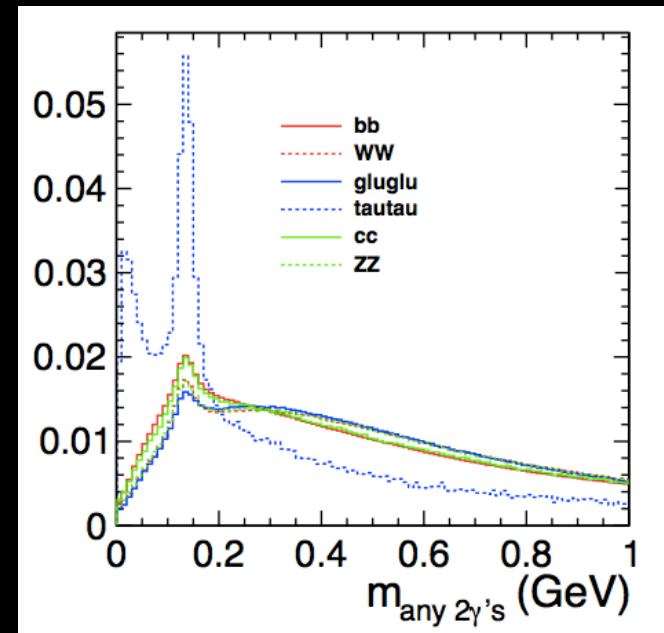
Added new variables to tree for γ momentum vectors

- cos θ bal = angle between γ and di-muon
- Ebal = (γ energy) - (di-muon energy)



From Watanuki-san

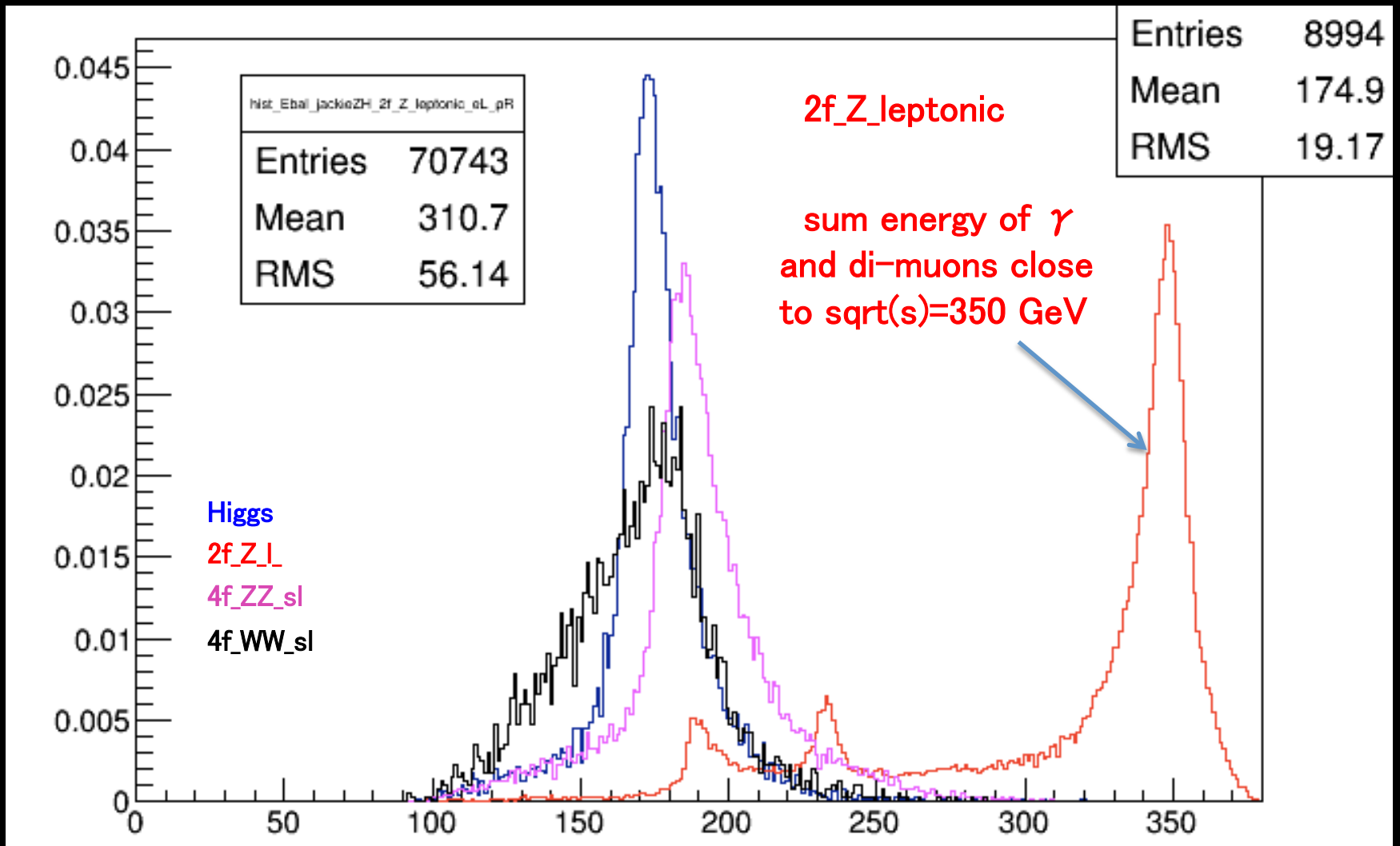
$H \rightarrow \tau \tau$ mode is major cause of bias



I applied a condition to prevent signal bias

I required energy sum of γ and di-muon to be $> 0.8 * \sqrt{s}$

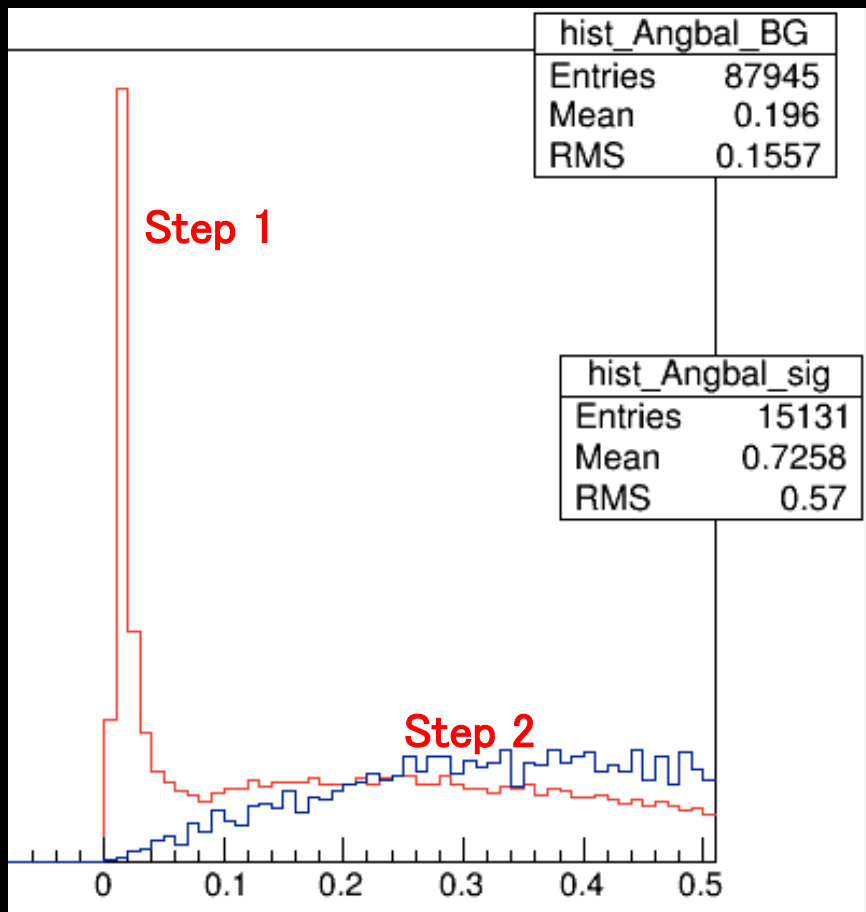
signature of $2f_Z$ leptonic BG



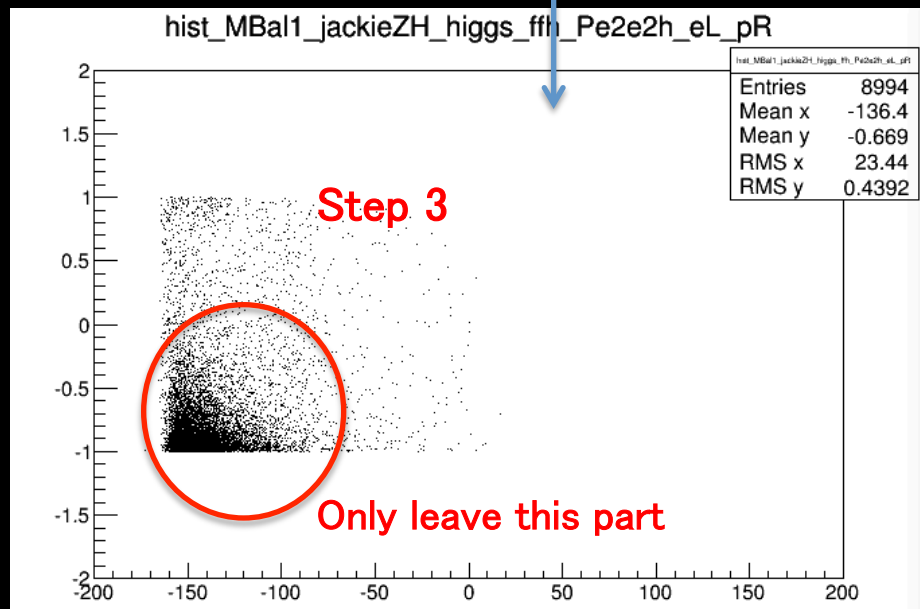
Last week's strategy in order to cut more BG

Divide into three cut regions

1. cut all events in sharp peak ($\theta_{\text{bal}} < 0.045$ rad)
2. then cut events satisfy both θ_{bal} and E_{bal} conditions
3. Then leave events only in bottom left corner



- X: $\cos \theta_{\text{bal}}$ = angle between γ and di-muon
- Y: $E_{\text{bal}} = (\gamma \text{ energy}) - (\text{di-muon energy})$



I played around for a long time with the event selection criteria and likelihood cut values

in aim of

- Highest signal to BG ratio
 - Smallest xsec error

It seems that

Low BG improves xsec precision,
but NOT if signal efficiency is too low

The best result from last week

	Nsig	Nbg	S/B ratio	sig eff	$\Delta \sigma / \sigma \text{MC}$
2 weeks ago	1056	2189	0.48	46.1+/-0.5%	4.39+/-0.00%
This week					
Likelihood L1	Minv, CosZ, Pt, max γ Pt				
$\ln(L1) > -19.8$	1057	2025	0.52	46.2+/-0.5%	4.29+/-0.00%
$\ln(L1) > -19$	1026	1746	0.59	44.8+/-0.5%	4.16+/-0.00%
Likelihood L2	Minv, CosZ, Pt				
$\ln(L2) > -16$	1062	2010	0.53	46.4+/-0.5%	4.27+/-0.00%

Maybe the last one is best ???

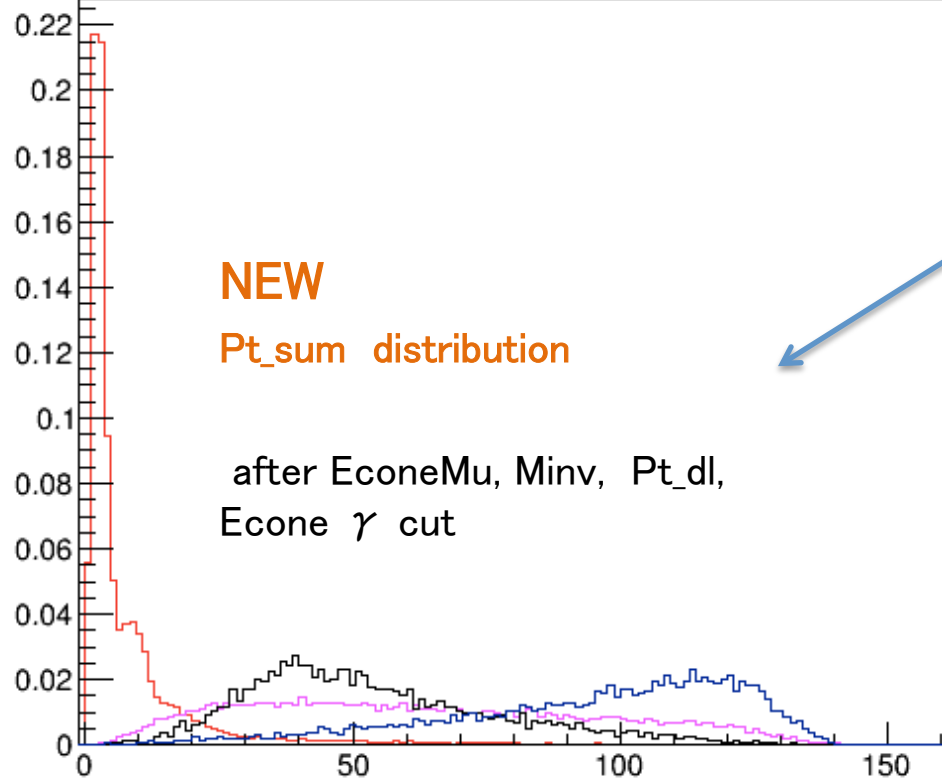
I tried a different type of pt_bal cut

$$Pt_sum = |Pt_dl - Pt_\gamma| \text{ (in vectors)}$$

NEW

Pt_sum distribution

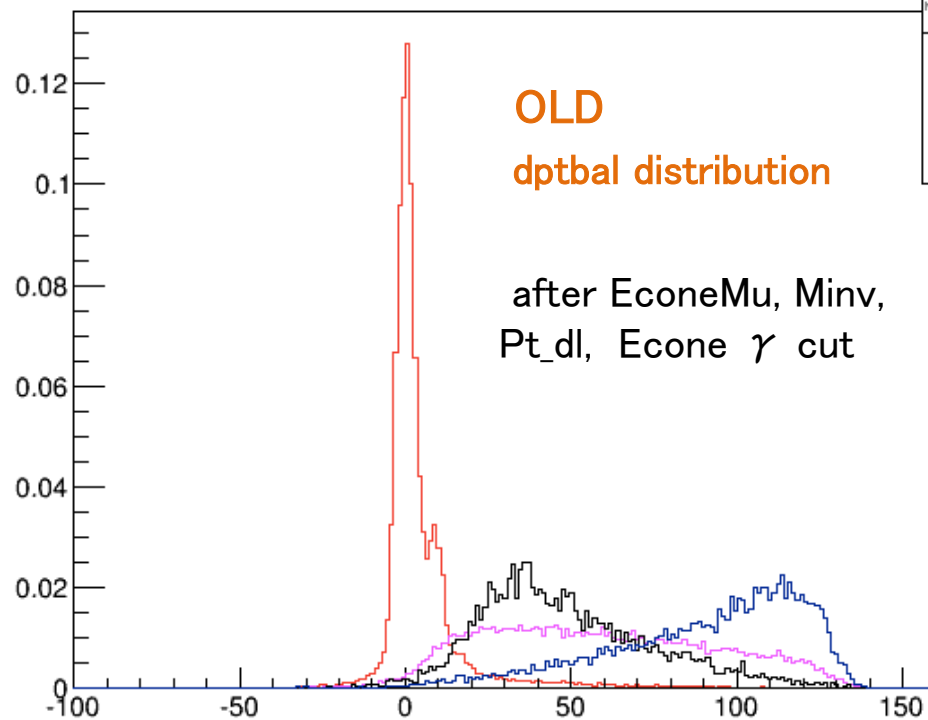
after EconeMu, Minv, Pt_dl,
Econe γ cut



OLD

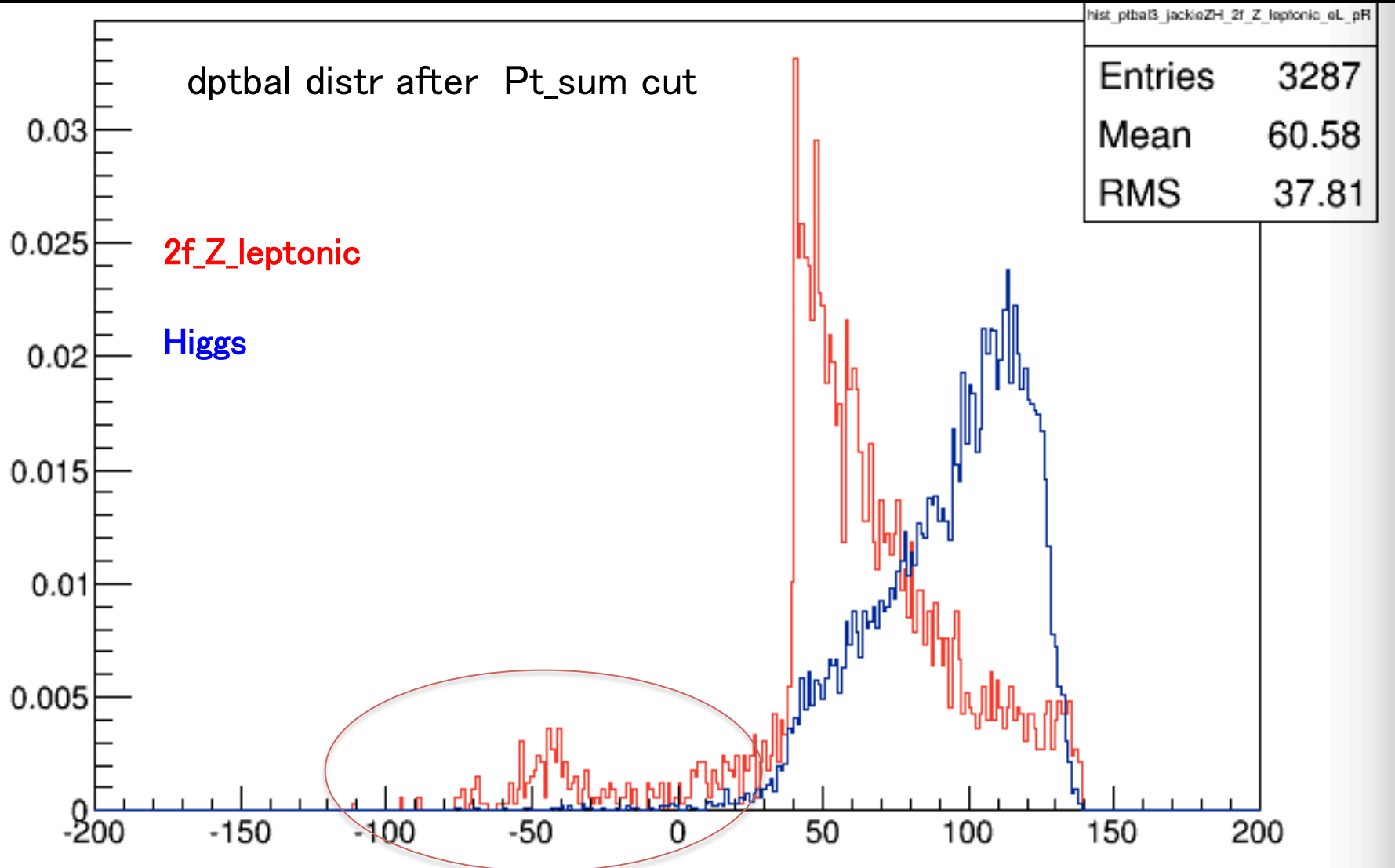
dptbal distribution

after EconeMu, Minv,
Pt_dl, Econe γ cut



After various tests, I found it is most effective to combine the two types

Still some BG events need to be cut after using Pt_sum cut



The strategies from last week helped me understand
2f_Z_leptonic BG better

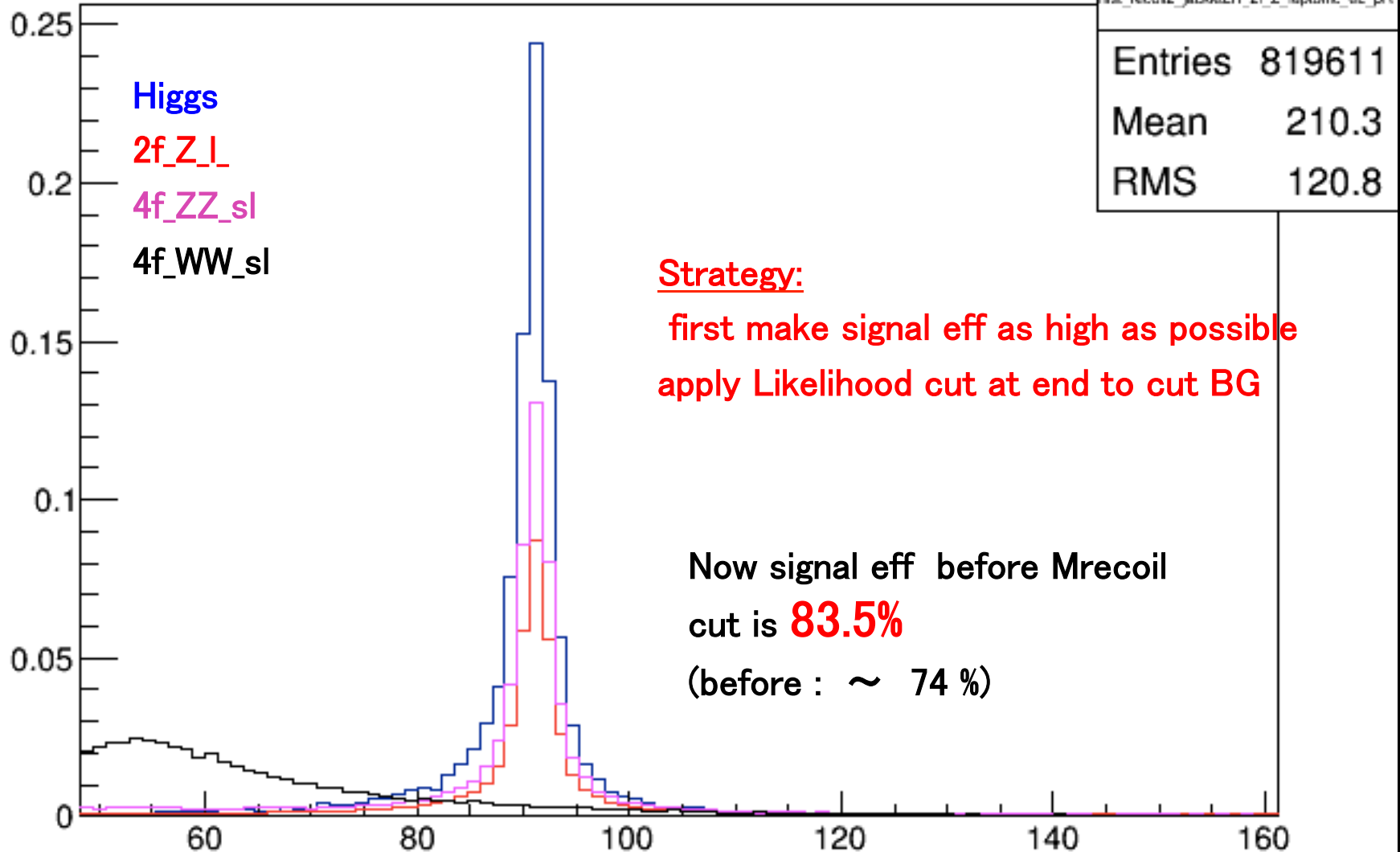
but the combinations were too complex

Besides, we still have the problem of
4f_WW_semileptonic BG

This is where I began implementing isolation cuts for
muon (against 4f_WW_sl)
and
gamma (against 2f_Z_leptonic)

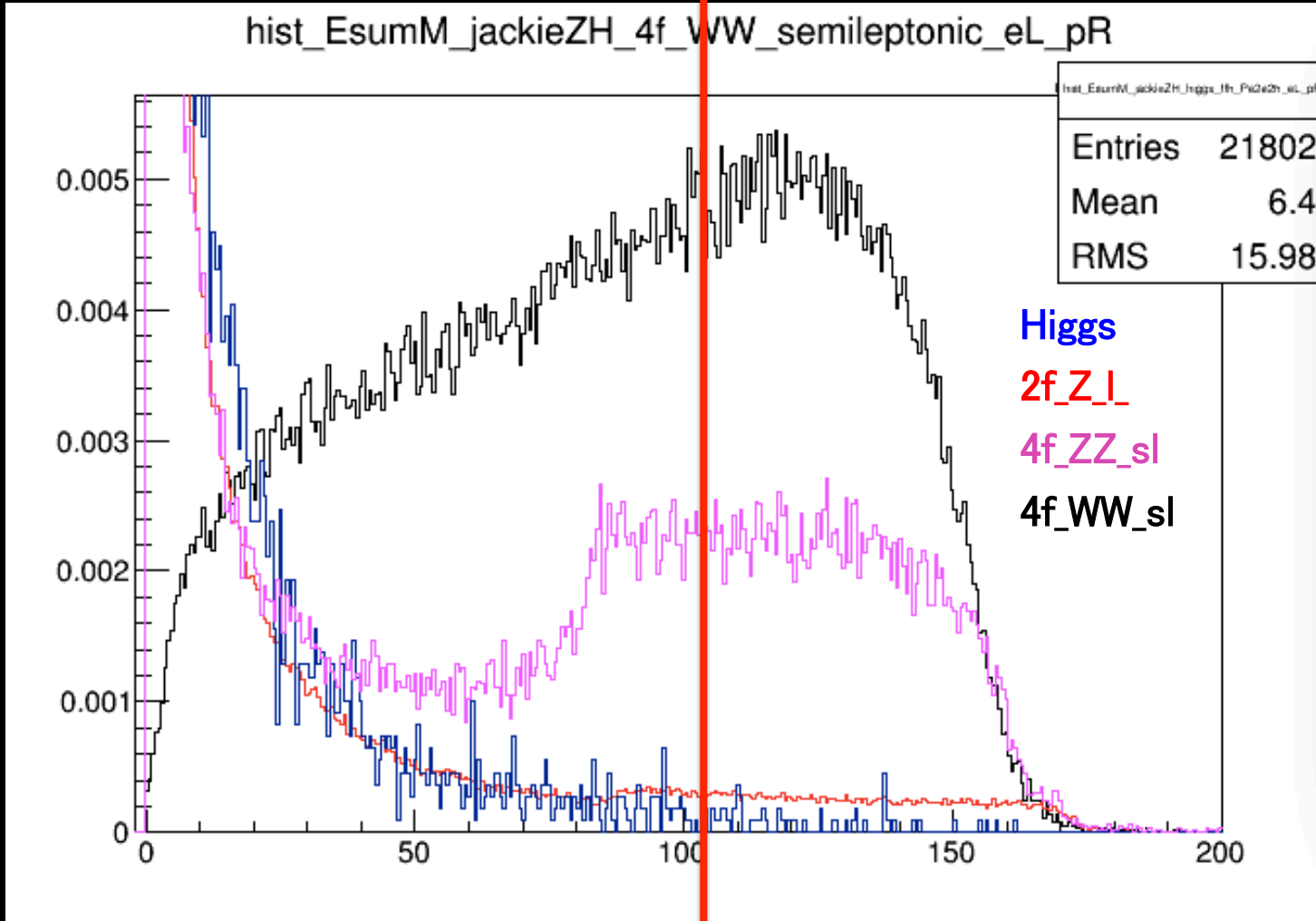
Reoptimization of invariant mass cut : widened the Minv window

- Before : 84 <Minv< 98 GeV : lose 10% signal
- Now: 73 <Minv < 120 GeV : lose 5% signal



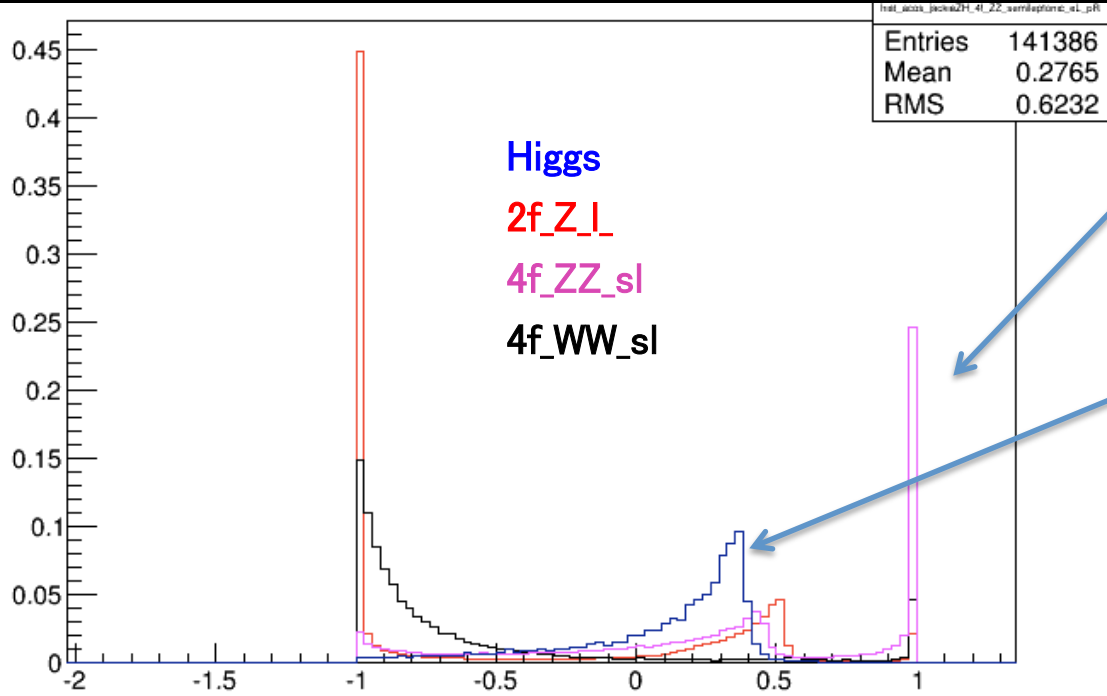
Cone energy around muon (~ 26 deg)

Effective for removing 4f_WW_sl BG



cut above 110 GeV

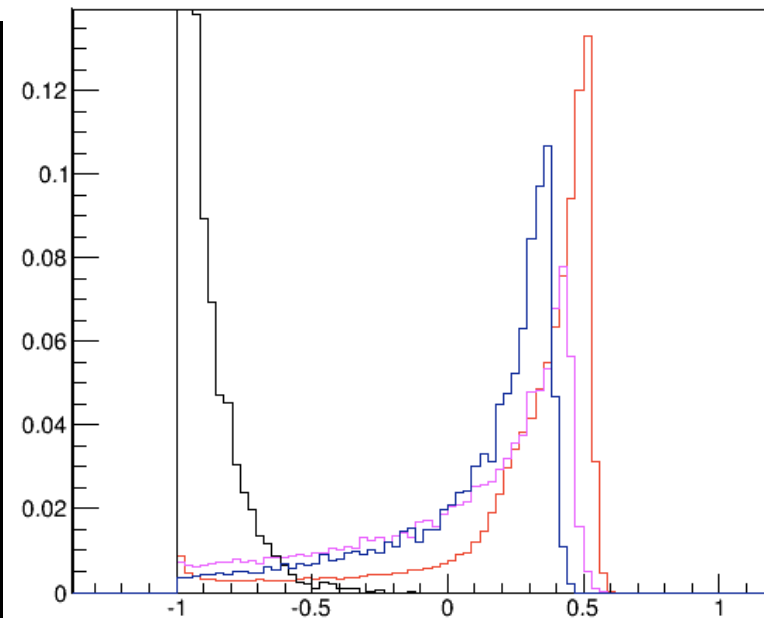
cosine of angle between two muons (before invariant mass cut)



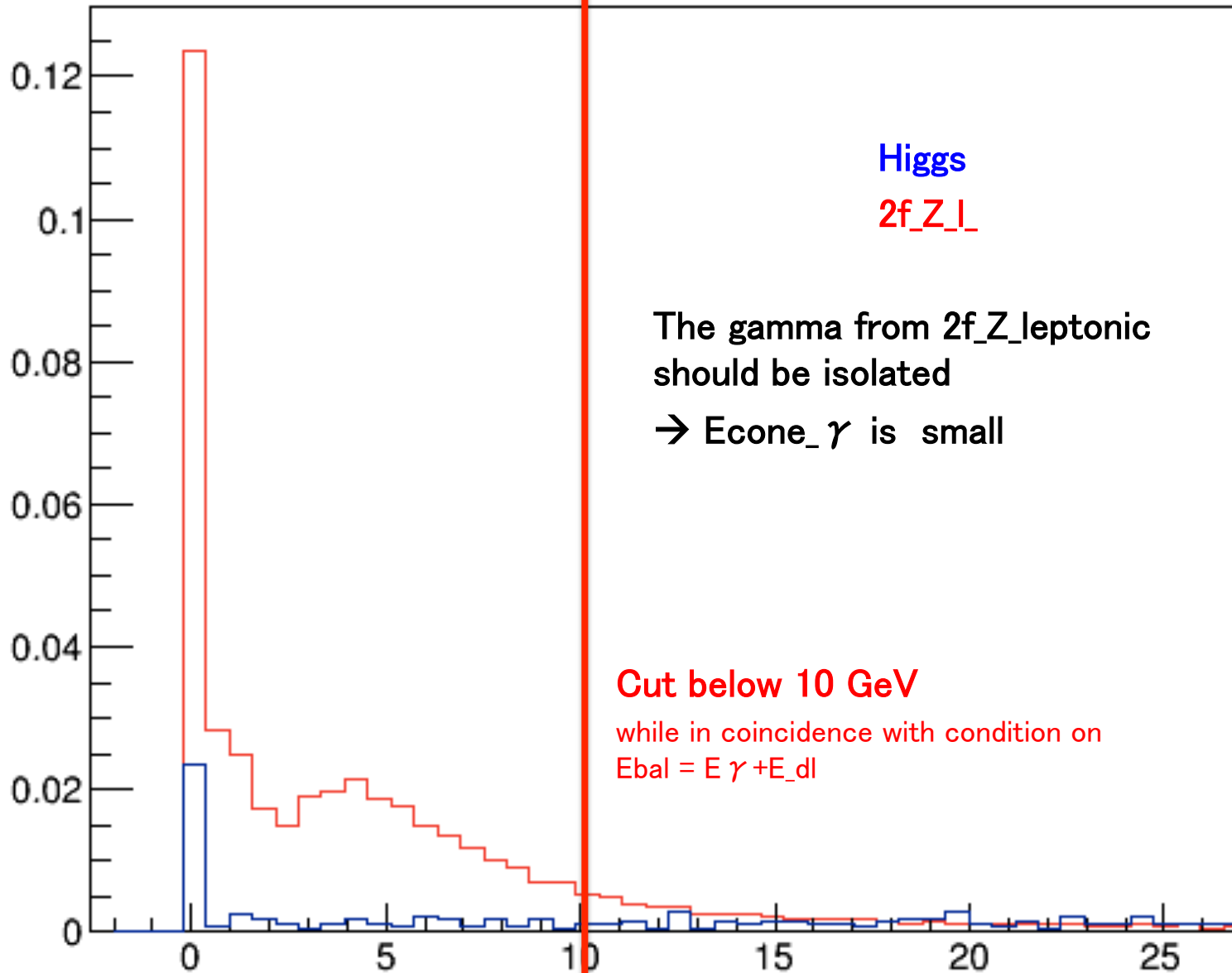
4f_ZZ_sl muons are quite collinear (> 25%)

Muons from Higgs events are not collinear GOOD
→ should not cause signal bias

after invariant mass cut
collinear muon events are removed anyways



Cone energy around most energetic gamma
(~ 26 deg)



Higgs

2f_Z_l

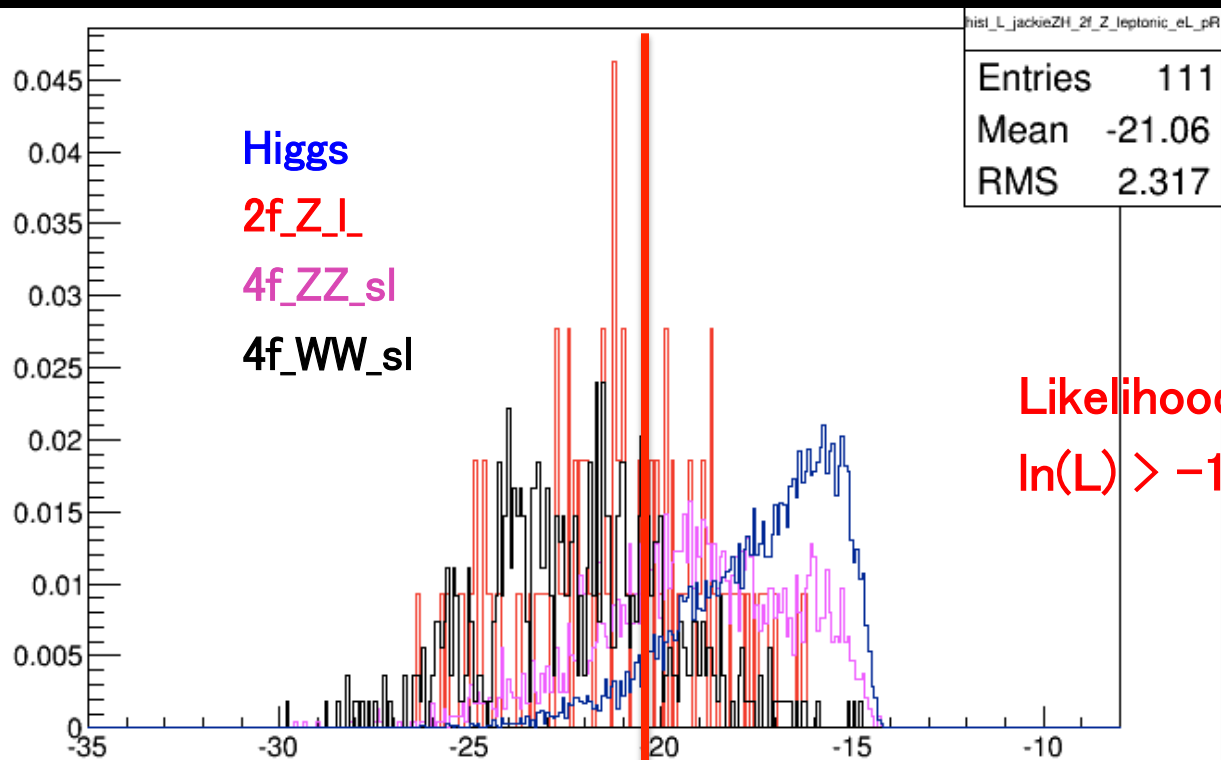
The gamma from 2f_Z_leptonic
should be isolated

→ E_{cone_γ} is small

Cut below 10 GeV

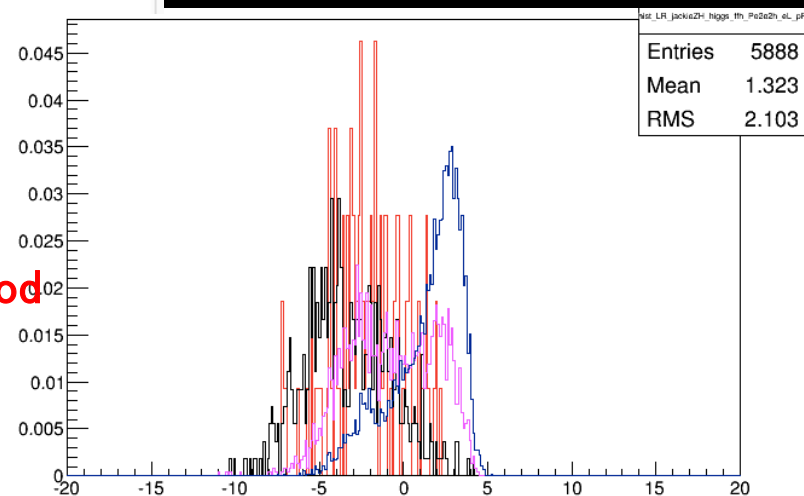
while in coincidence with condition on
 $E_{\text{bal}} = E_\gamma + E_{\text{dl}}$

Likelihood function: $L = P(M_{inv}) * P(Pt) * P(CosZ) * P(Pt_{sum})$



Likelihood cut
 $\ln(L) > -19.8$ seems best

tried to use ratio of signal likelihood to BG likelihood
but not effective



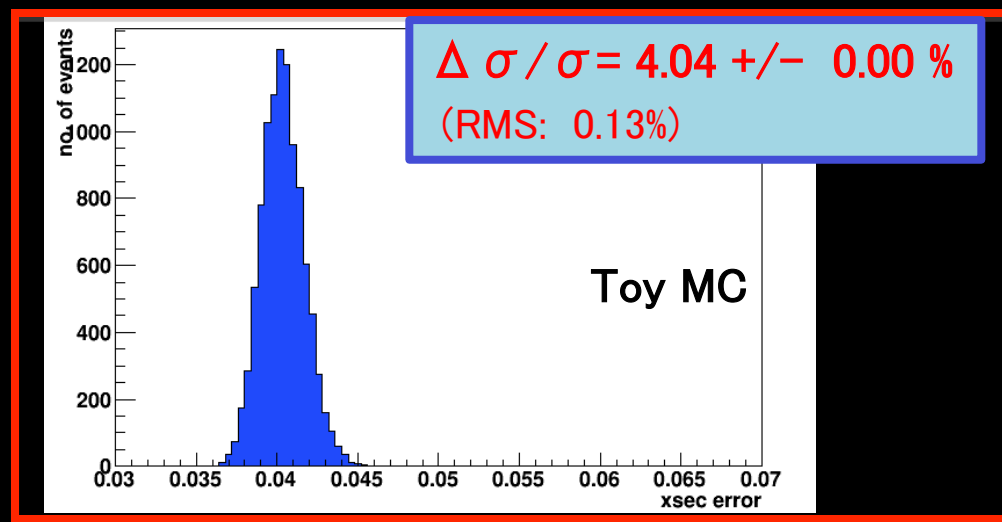
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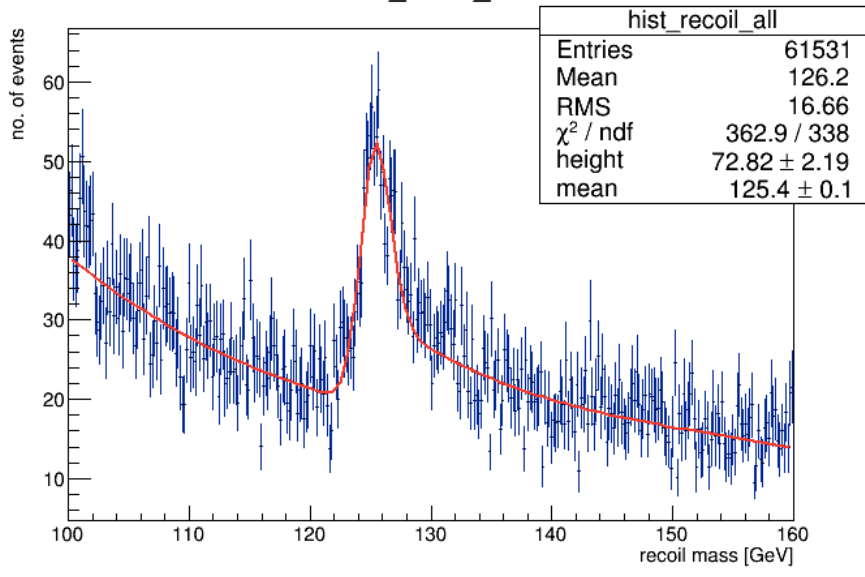
What contributed ??

- More sophisticated methods to remove 2f_Z BG without losing much signal
- isolation cuts for muon and gamma
- usage of likelihood cut



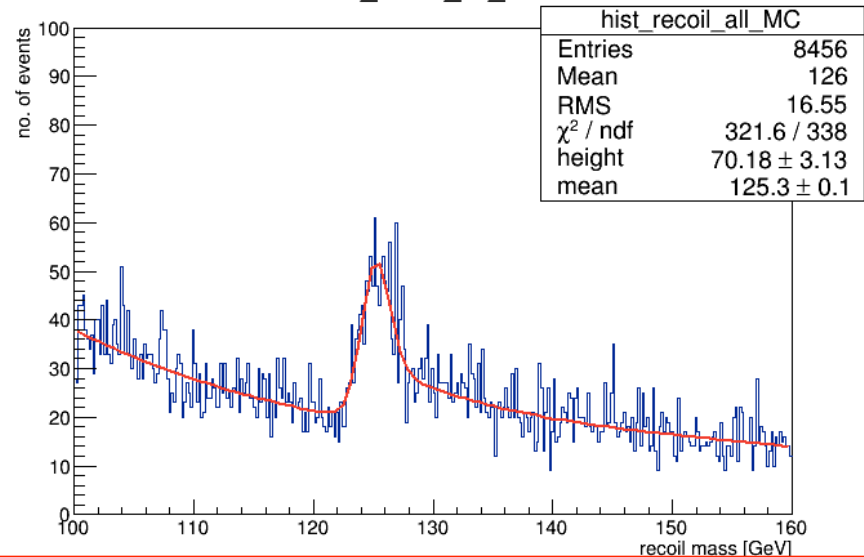
2 weeks ago:

hist_recoil_all



Fit range: 100–160 GeV

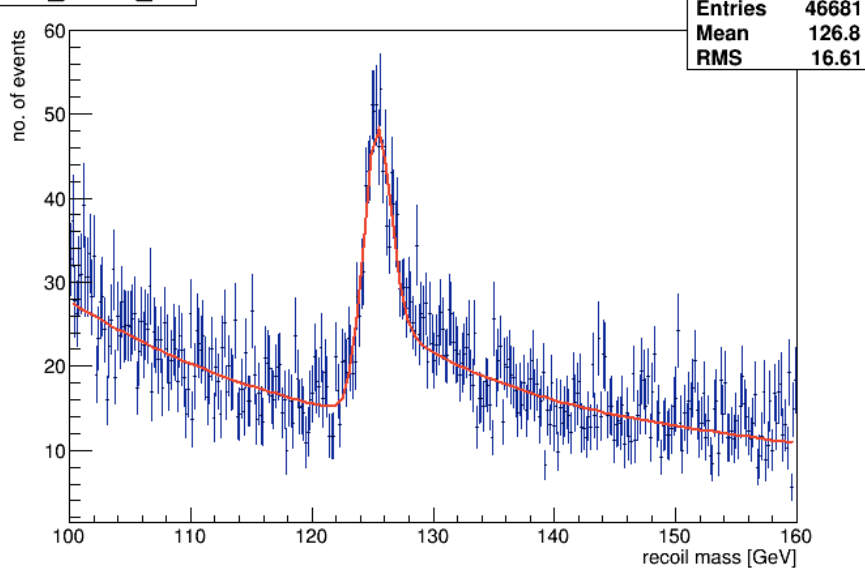
hist_recoil_all_MC



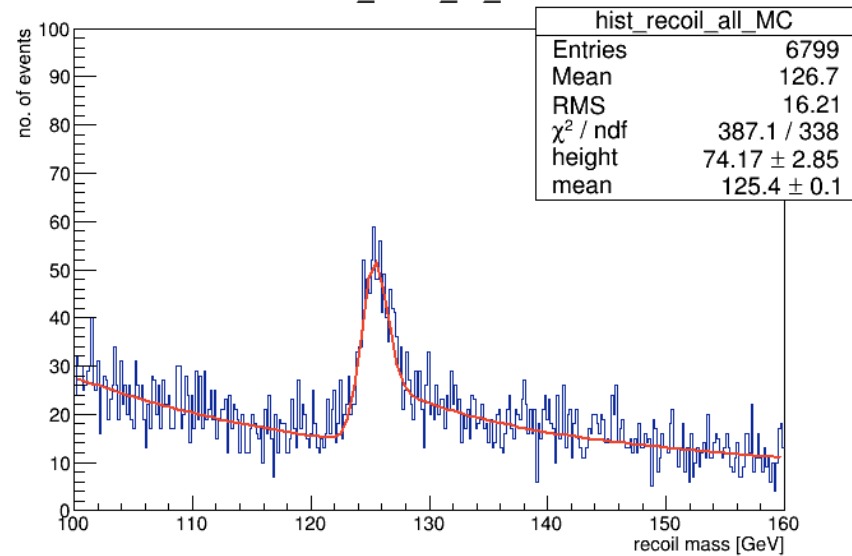
NEWEST

BG is reduced

hist_recoil_all



hist_recoil_all_MC



Conclusion

(1) Significant reduction in BG

(2) improved xsec precision : now 4.0 %

These are mainly due to

- new strategies in pt_bal cut
- isolation cuts for muon and gamma
- gain in signal

Next steps :

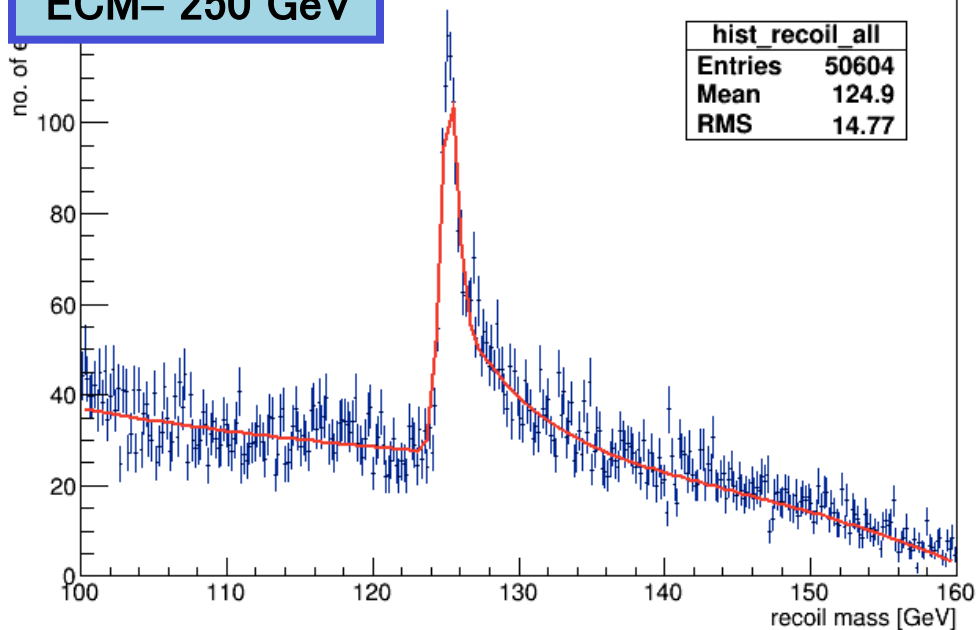
How can I make xsec error go below 4% ????

However, for now ... I will apply similar method to
other polarization scenarios and **ECM= 250 GeV**
and **compare**

In time for **ALCW15** (physics session)

Preview on re-visit of $E_{CM} = 250$ GeV

ECM= 250 GeV



250 GeV:

$\Delta \sigma / \sigma = 3.46 \pm 0.00 \%$ (Toy MC)

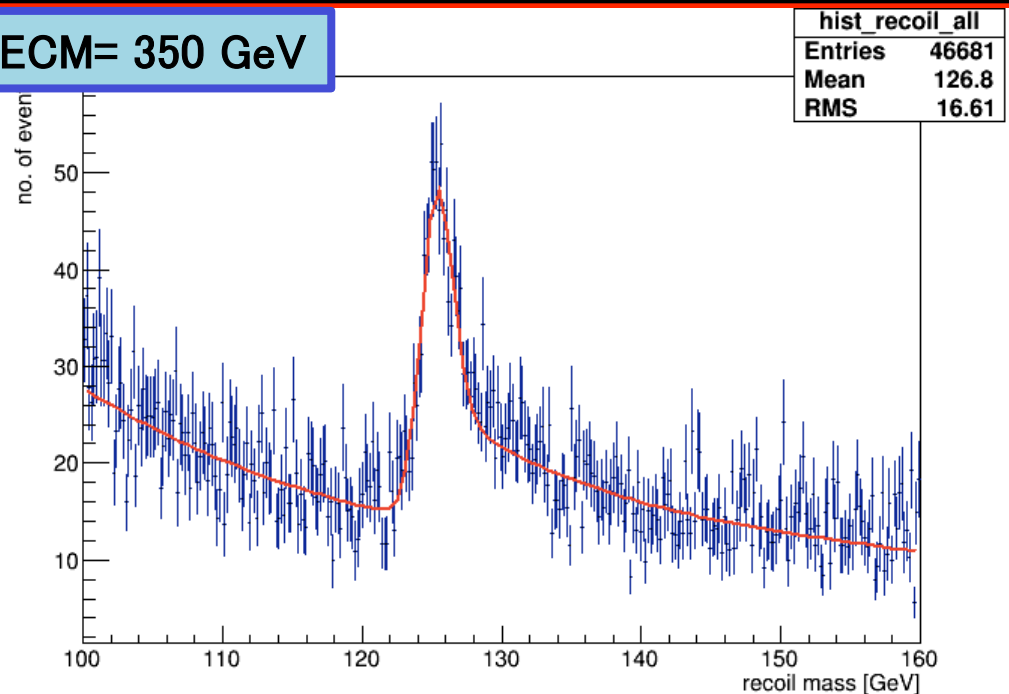
- Major residual BG for 250 GeV
- 4f_ZZWWMix_l
- 4f_ZZ_l
- 4f_WW_l

350 GeV

$\Delta \sigma / \sigma = 4.04 \pm 0.00 \%$ (Toy MC)

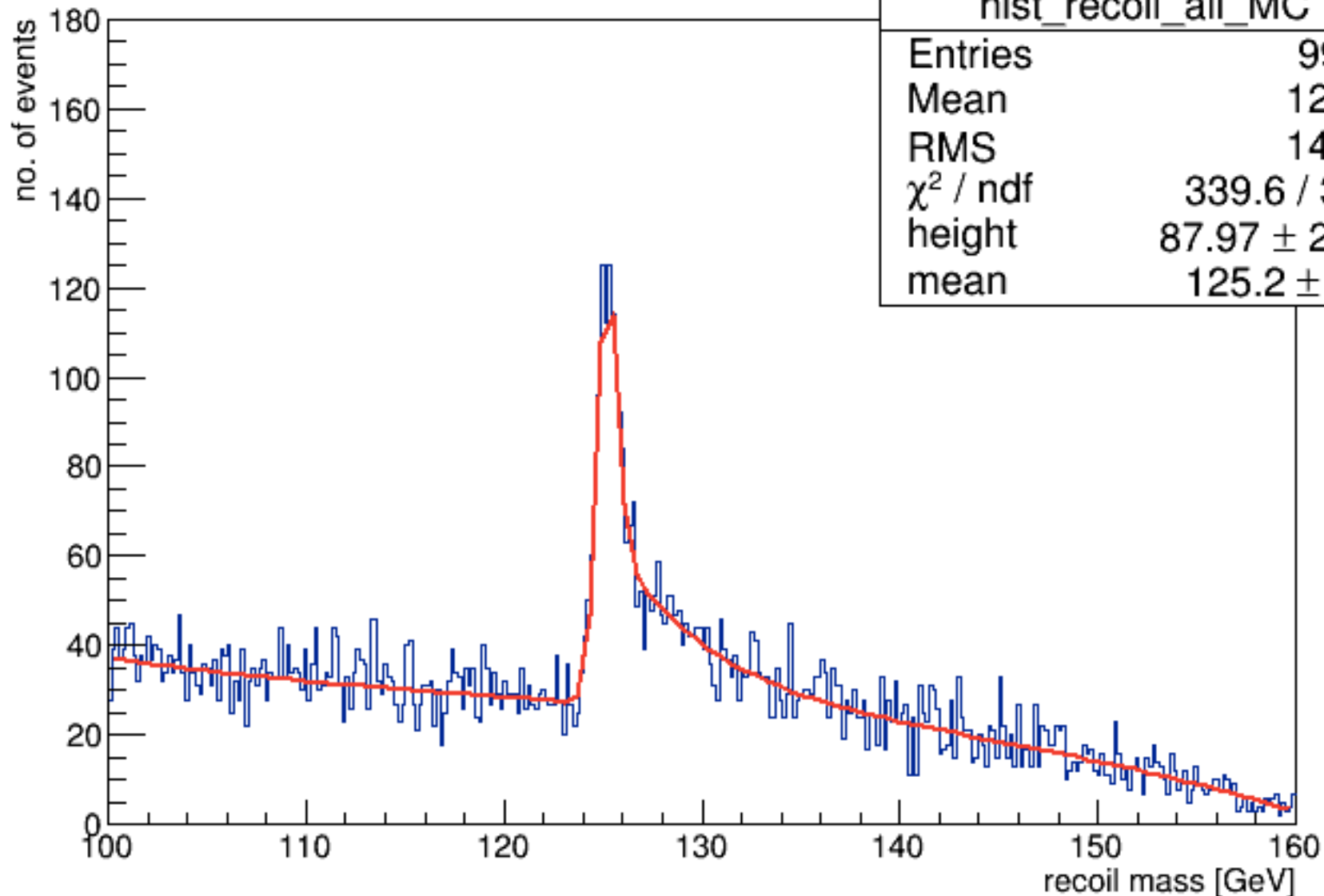
- Major residual BG for 350 GeV
- 4f_WW_sl
- 4f_ZZ_l
- 2f_Z_l

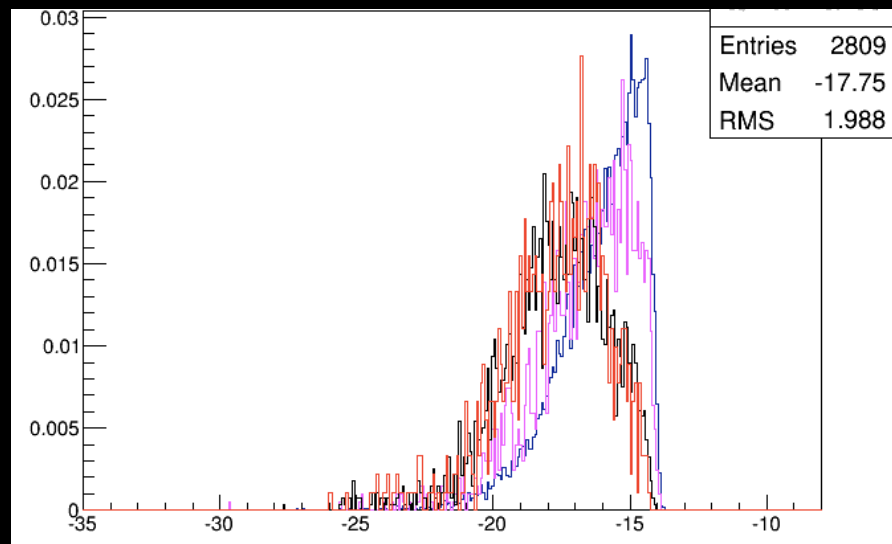
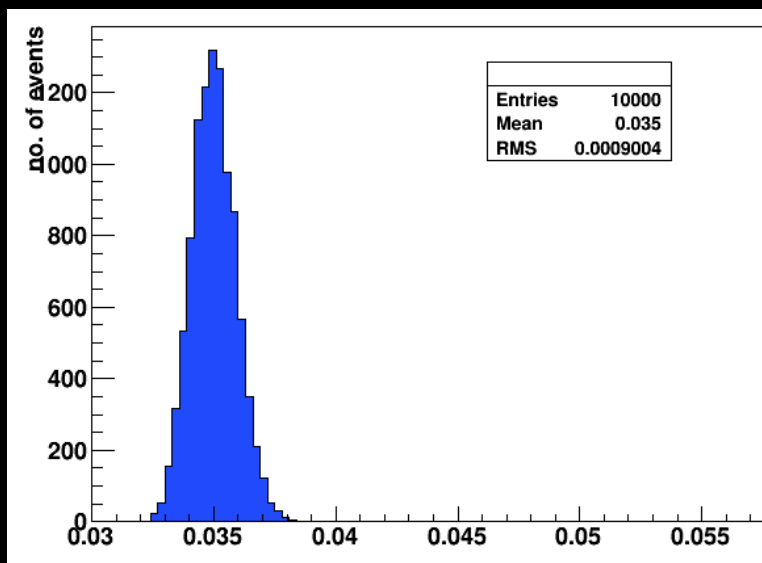
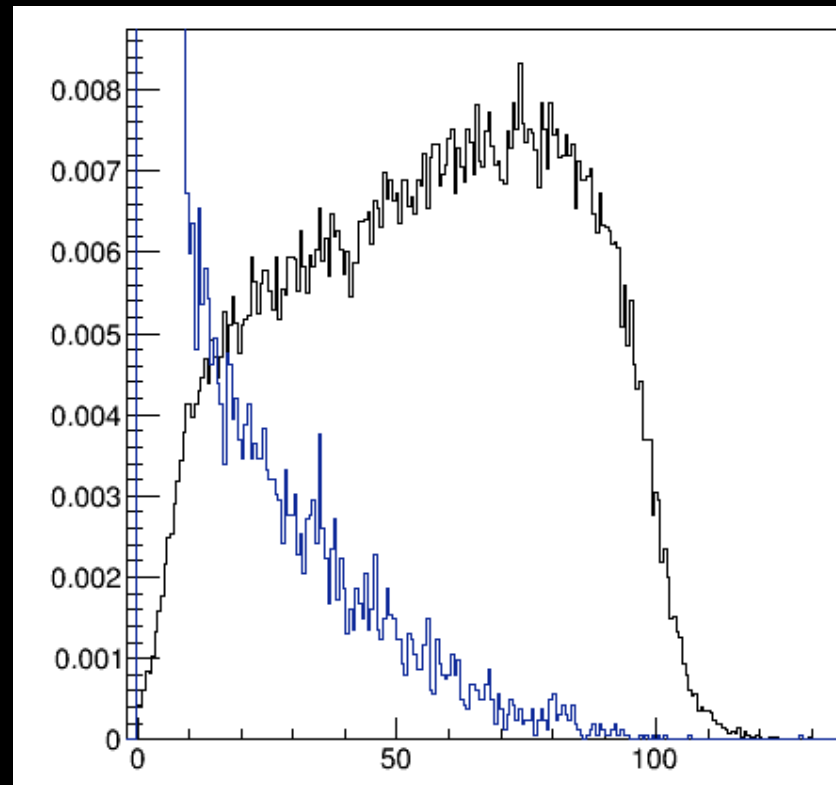
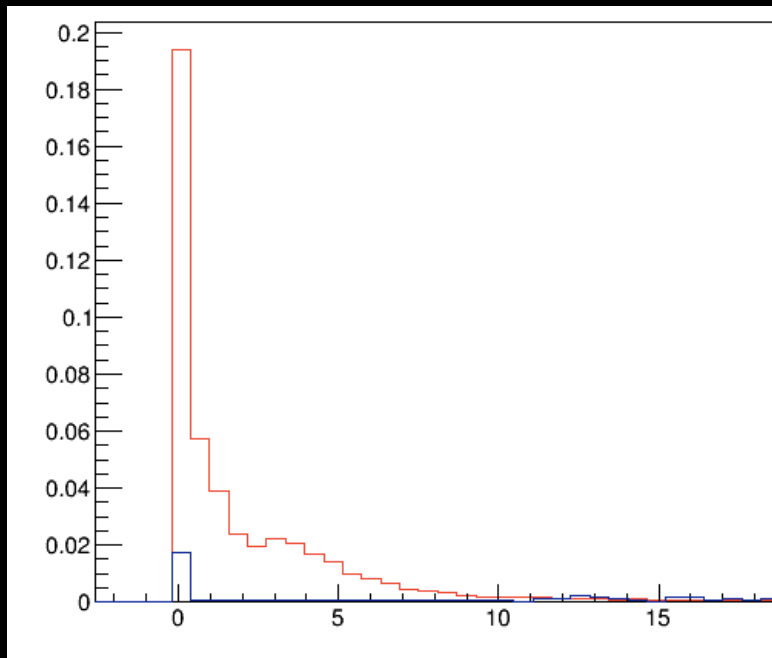
ECM= 350 GeV



BACKUP

hist_recoil_all_MC





recoil mass fitting method

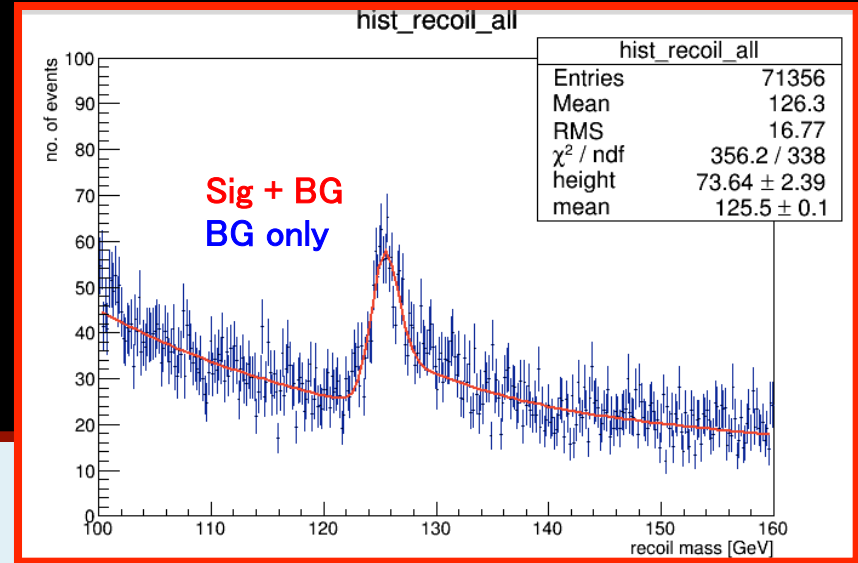
Fit range: 100–160 GeV

1st step:

- Fit only signal with GPET float all 5 pars
- Fit only BG: 3rd order polynomial

2nd step:

fit Sig + BG : only float height and mean
fix others from step 1



◆ SIGNAL: GPET: 5 parameters :

$$\frac{N}{\sqrt{\pi}\sigma} \exp\left\{-\frac{1}{2}\left(\frac{x-x_{mean}}{\sigma}\right)^2\right\} \quad \left(\frac{x-x_{mean}}{\sigma} \leq k\right) \quad \text{Gaus (left-side) ,}$$

$$\frac{N}{\sqrt{\pi}\sigma} \left[b \cdot \exp\left\{-\frac{1}{2}\left(\frac{x-x_{mean}}{\sigma}\right)^2\right\} + (1-b) \exp\left\{-k\left(\frac{x-x_{mean}}{\sigma}\right)\right\} \exp(k^2/2) \right] \quad \left(\frac{x-x_{mean}}{\sigma} \geq k\right) \quad \text{Gaus + expo (right side)}$$

Toy MC study

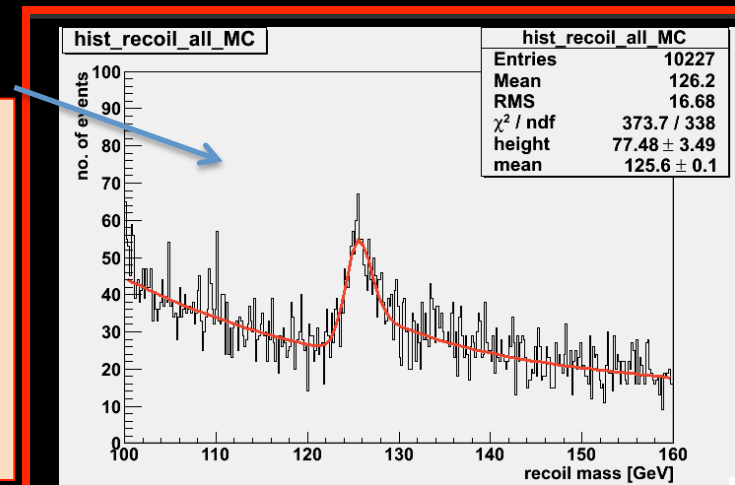
Toy MC 10000 seeds

goal: test quality of fitting method
in terms of M_h , x_{sec} etc.....

method:

generate MC events according to fitted “real” data
(Poisson)

fit MC hist with same GPET function → get N_{sig} , x_{sec}

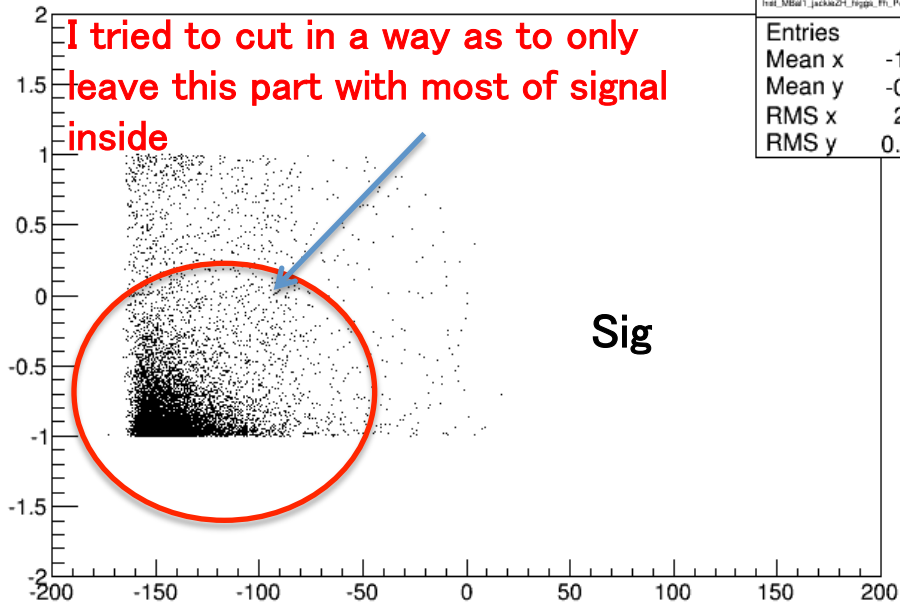


X: Ebal

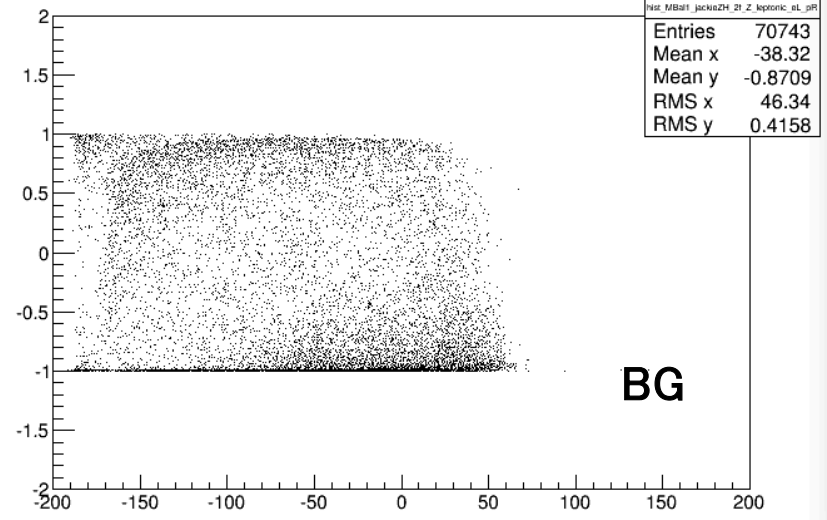
Y: $\cos(\theta_{bal})$

2D distribution before maxgammapt cut

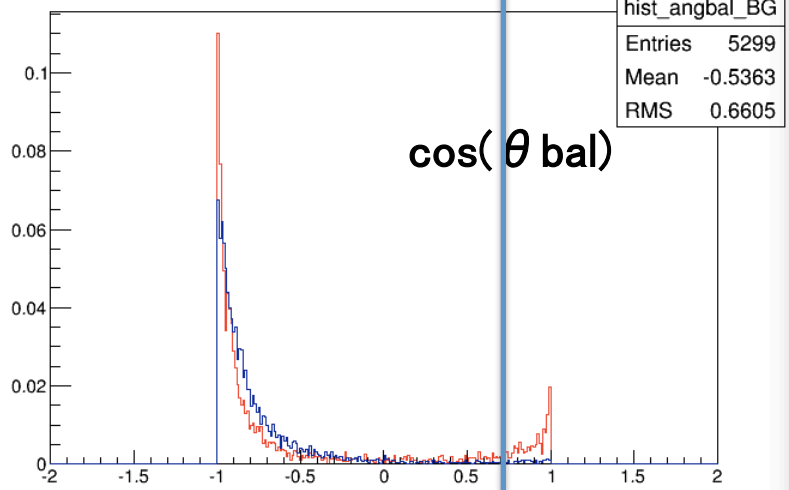
hist_MBal1_jackieZH_higgs_ffh_Pe2e2h_eL_pR



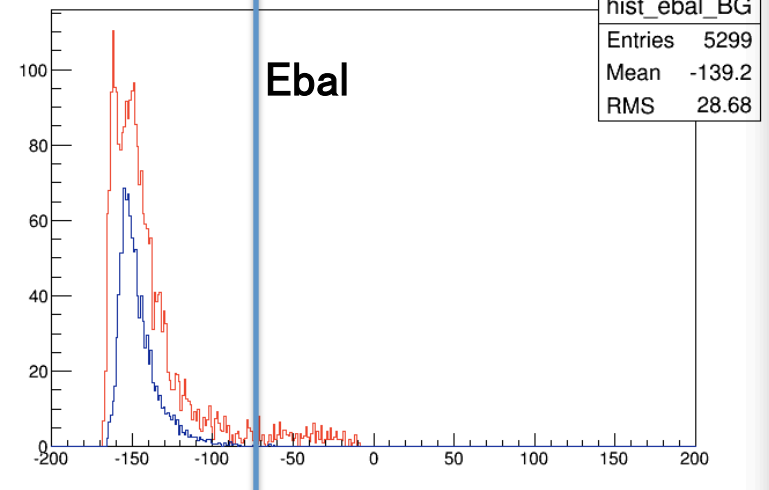
hist_MBal1_jackieZH_2f_Z_leptonic_eL_pR

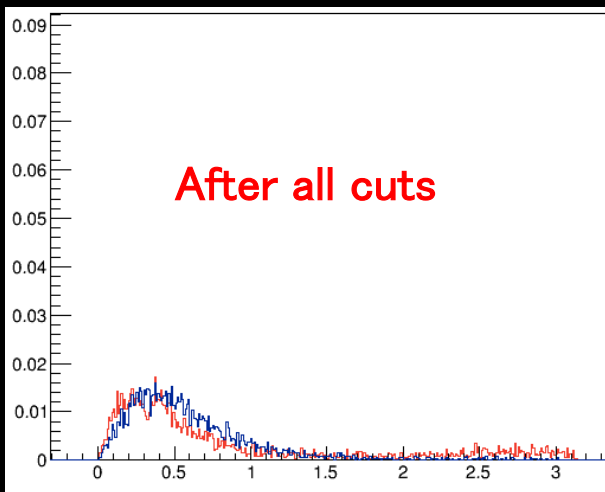
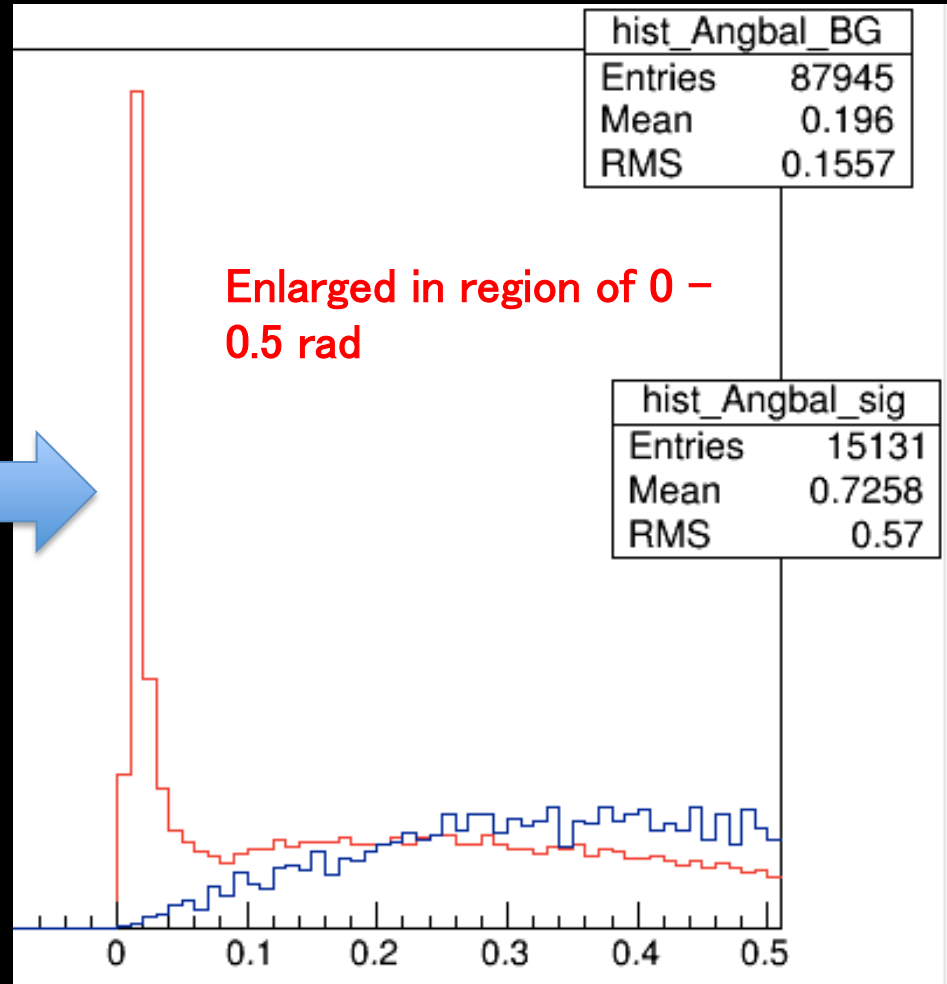
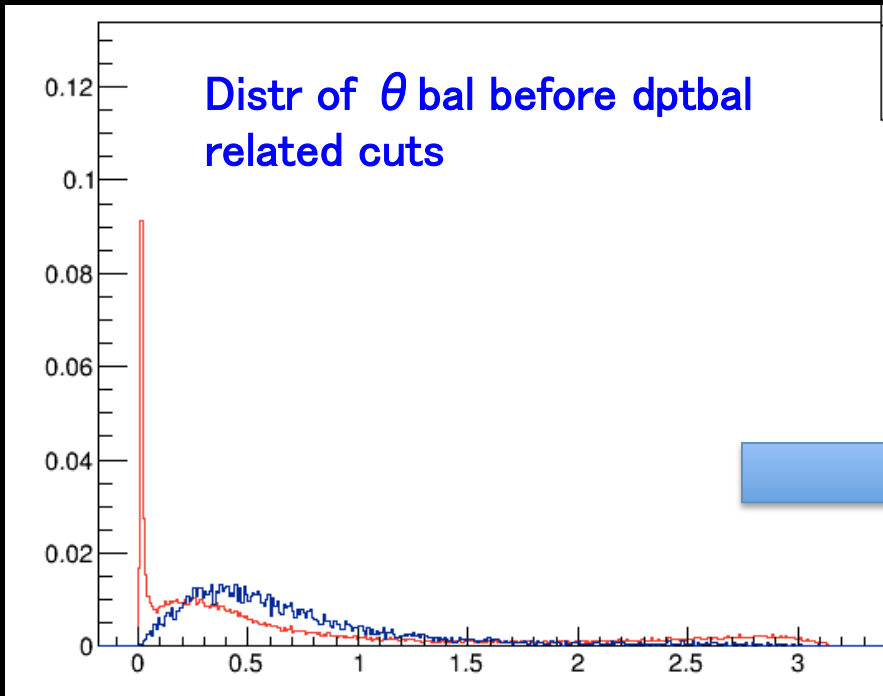


hist_angbal_BG



hist_ebal_BG

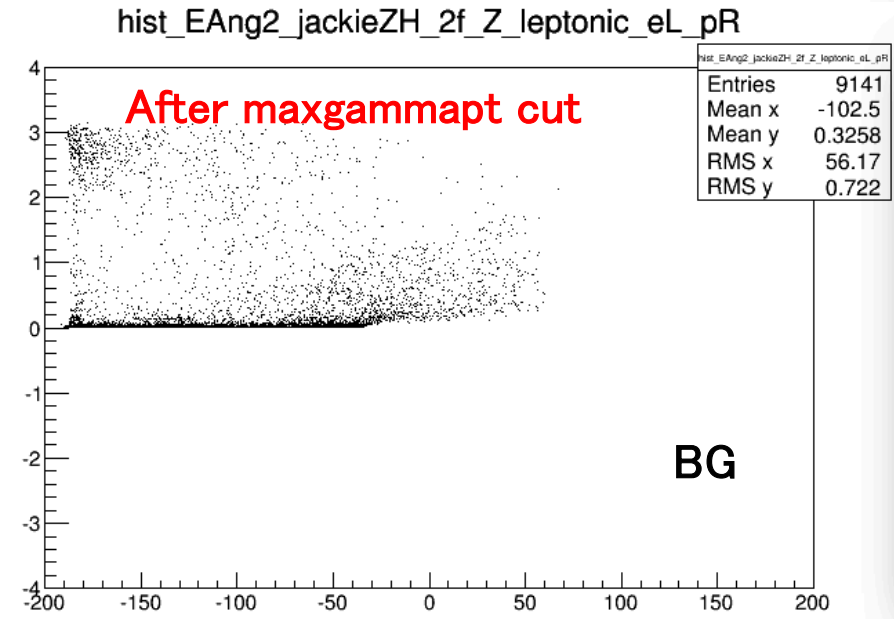
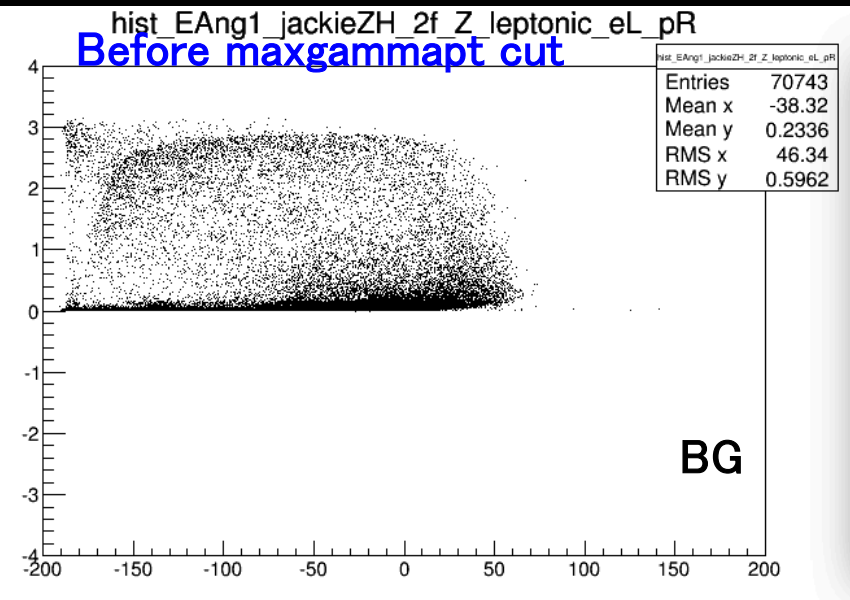
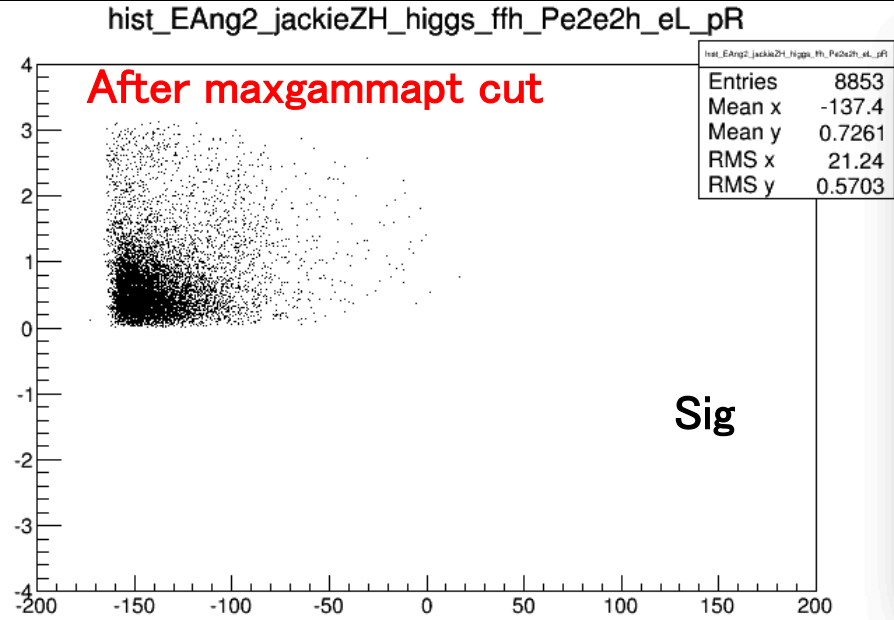
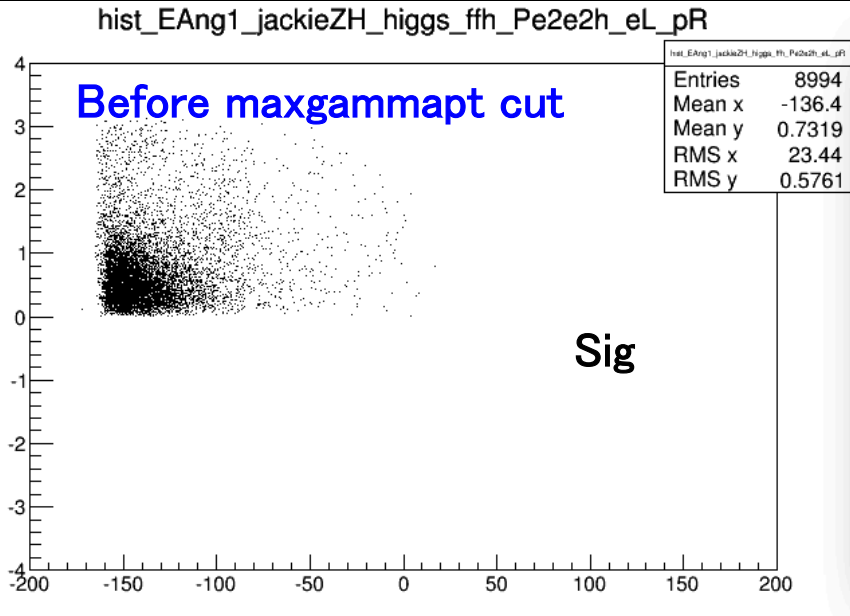




- $\cos \theta_{bal}$ = angle between γ and di-muon
- $E_{bal} = (\gamma \text{ energy}) - (\text{di-muon energy})$

X: Ebal

Y: $PI - \theta_{bal}$



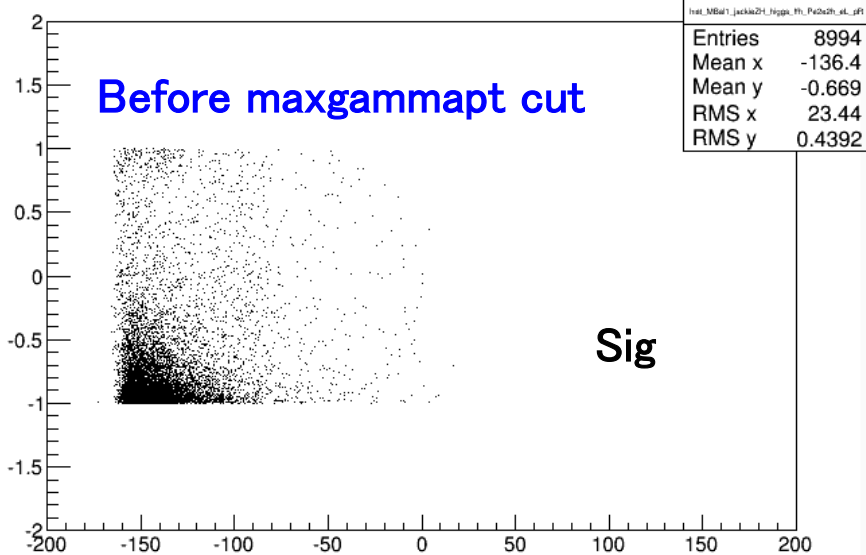
X: Ebal

Y: $\cos(\theta_{\text{bal}})$

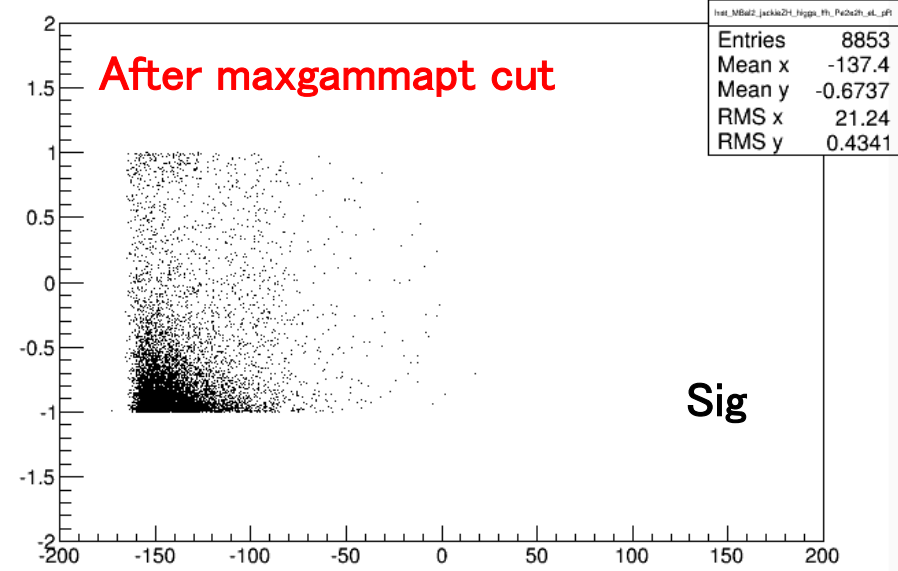
• $\cos \theta_{\text{bal}}$ = angle between γ and di-muon

• Ebal = (γ energy) - (di-muon energy)

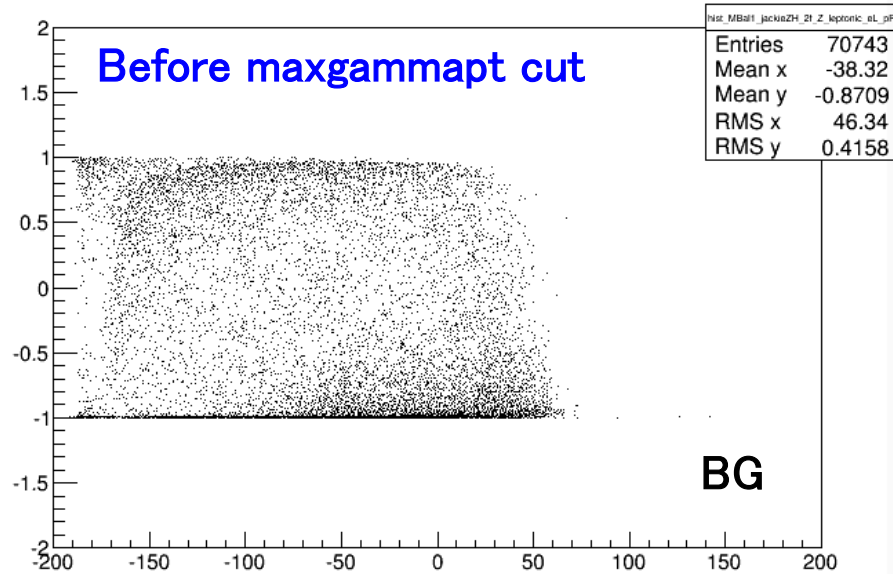
hist_MBal1_jackieZH_higgs_ffh_Pe2e2h_eL_pR



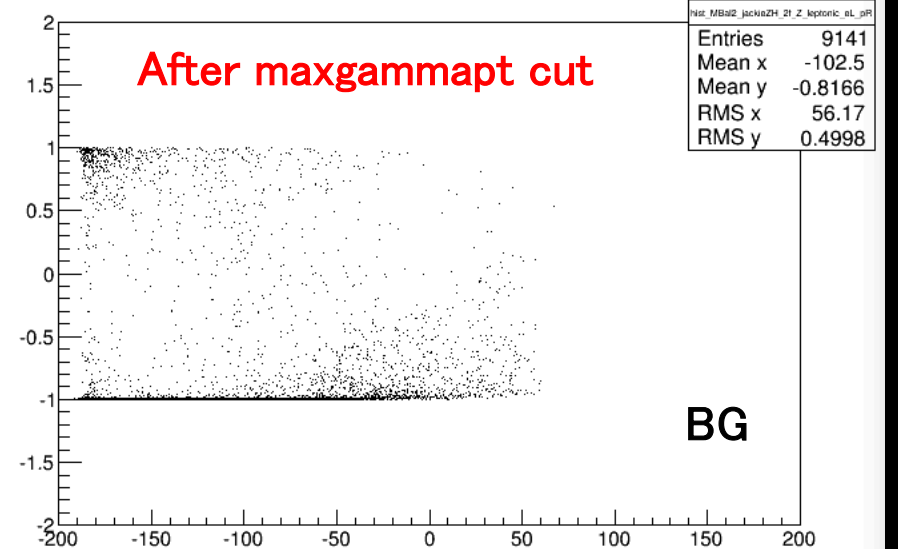
hist_MBal2_jackieZH_higgs_ffh_Pe2e2h_eL_pR



hist_MBal1_jackieZH_2f_Z_leptonic_eL_pR



hist_MBal2_jackieZH_2f_Z_leptonic_eL_pR

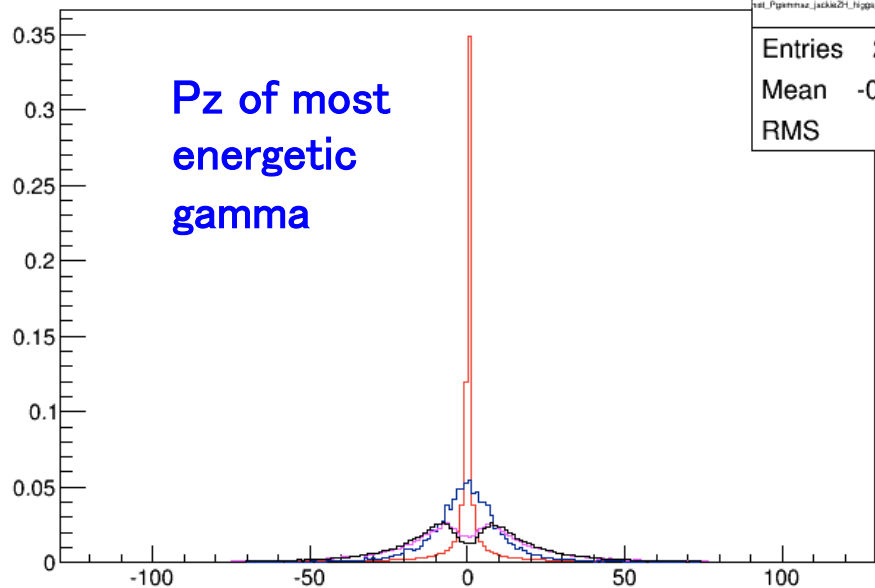


slight improvement w.r.t. just using ptbal info.

	Nsig	NBG	S/B	Eff_sig
dptbal > 10 GeV	1100	2771	0.40	48.0+/-0.5%
dptbal > 15 GeV	1099	2711	0.41	48.0+/-0.5%
(cos(θ_{bal})<0.6) &&(Ebal<-70)	1076	2336	0.46	47.0+/-0.5%
(cos(θ_{bal})<0.8) &&(Ebal<-70)	1083	2431	0.45	47.3+/-0.5%

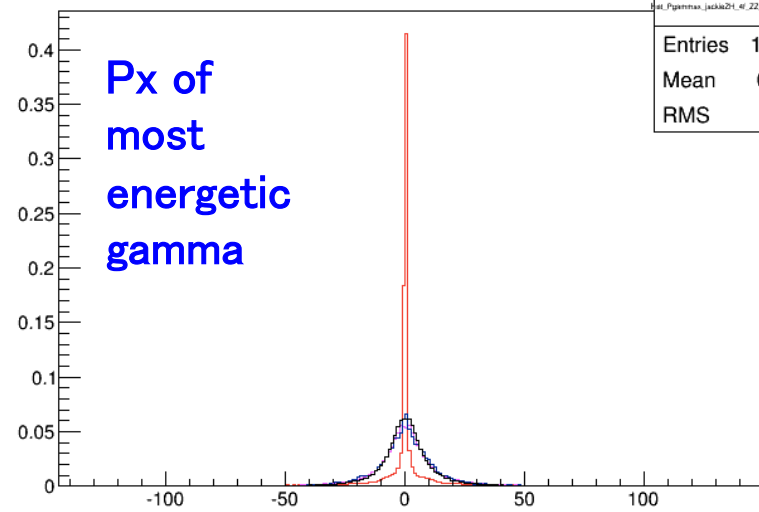
- $\cos \theta_{bal}$ = angle between γ and di-muon
- $E_{bal} = (\gamma \text{ energy}) - (\text{di-muon energy})$

hist_Pgammaz_jackieZH_2f_Z_leptonic_eL_pR



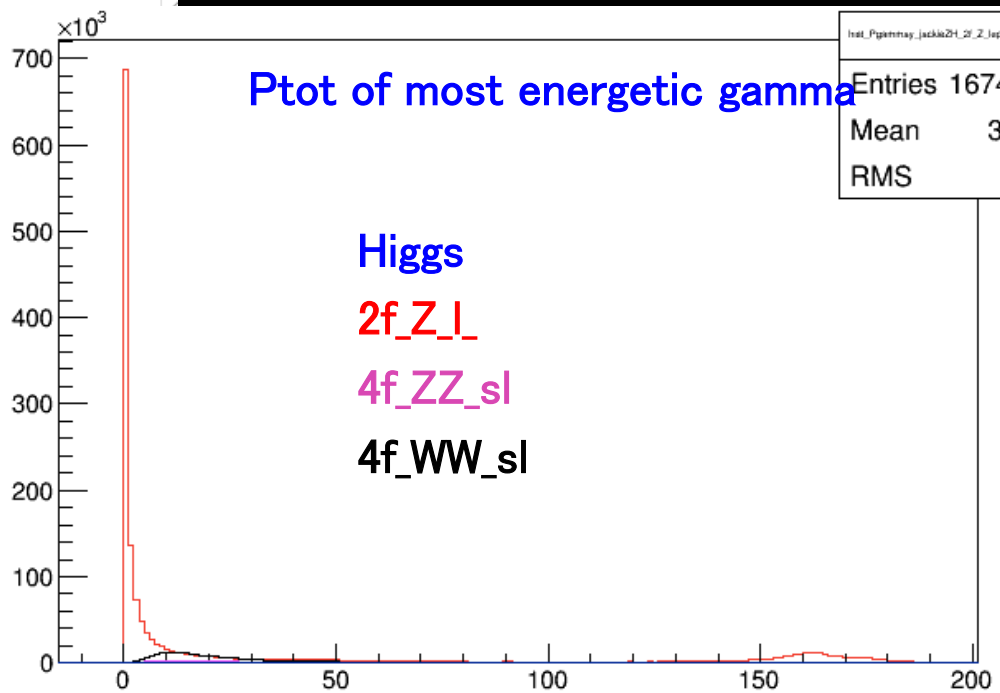
Entries	21802
Mean	-0.1825
RMS	16.95

hist_Pgammaz_jackieZH_2f_Z_leptonic_eL_pR



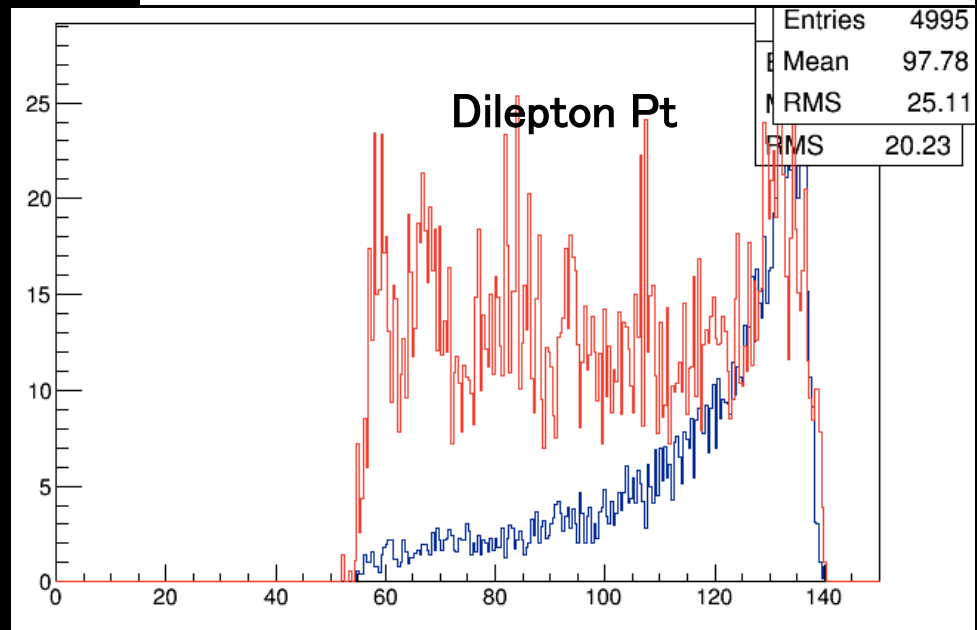
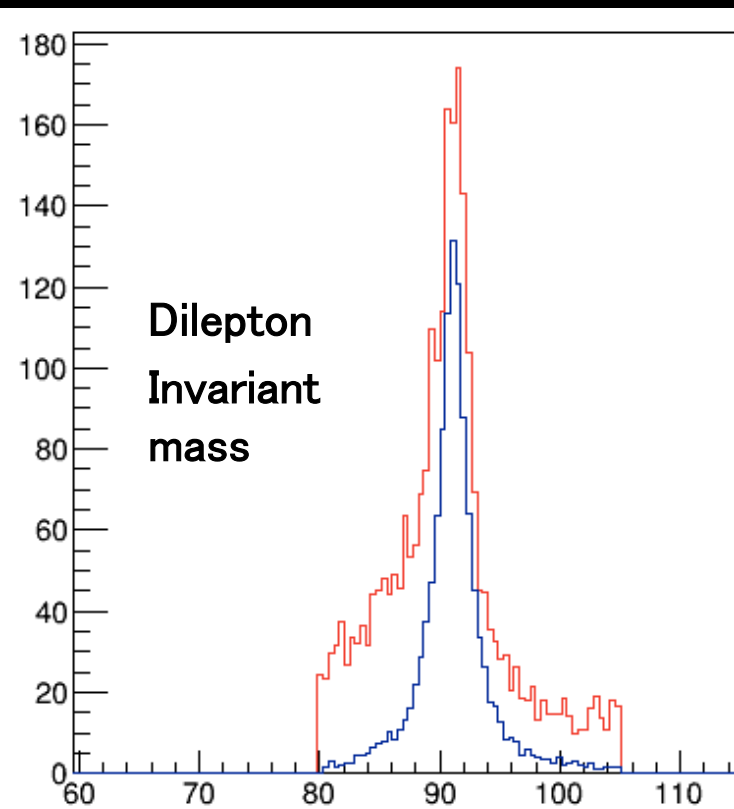
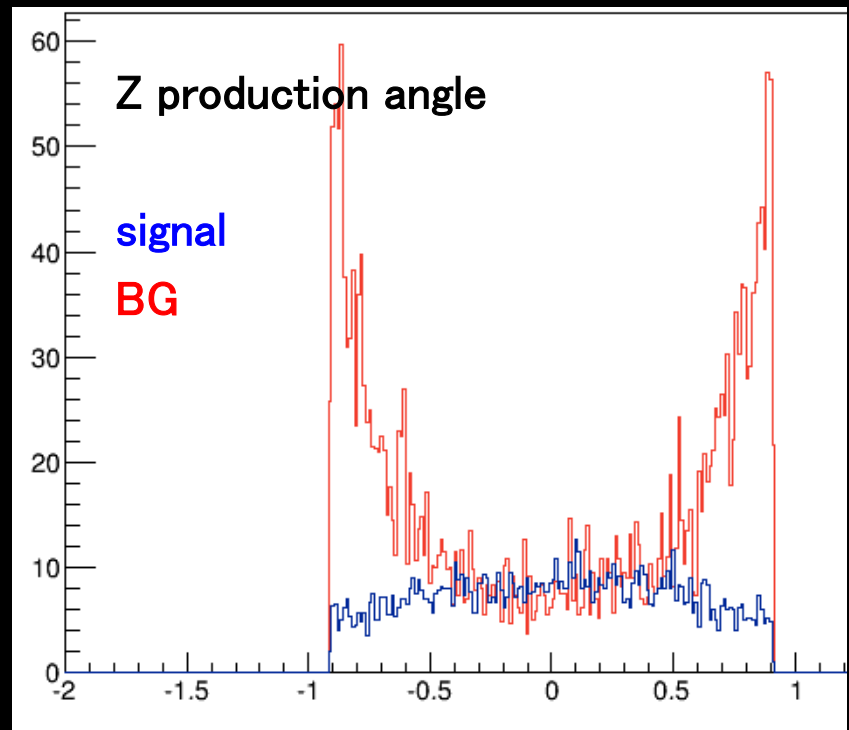
Entries	141386
Mean	0.2313
RMS	17.81

Ptot of most energetic gamma



Entries	1674168
Mean	35.68
RMS	59.2

formed using templates
for signal events



Chose the conditions that give relatively high signal efficiency and low BG

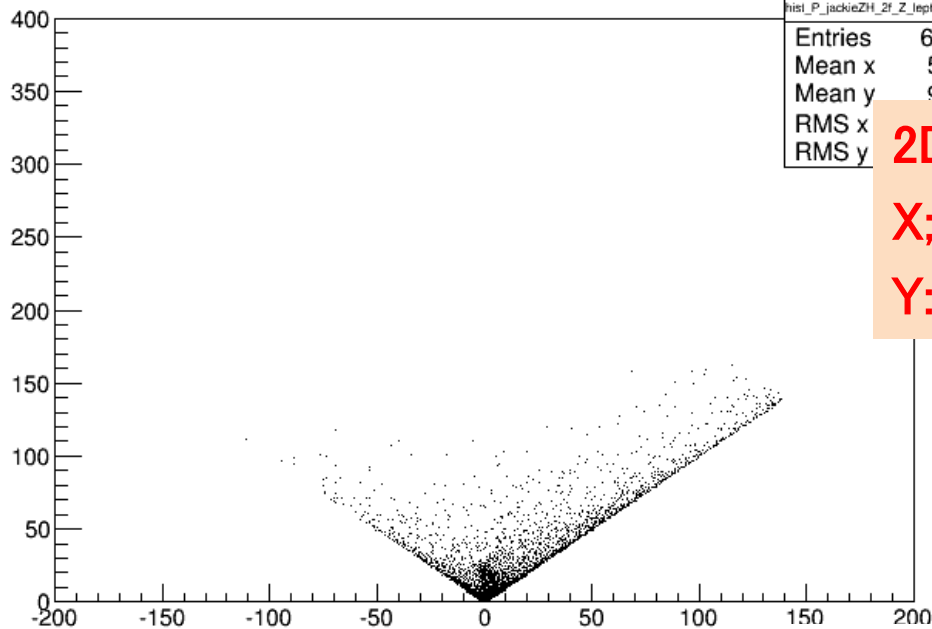
- then played with likelihood cut
- and observed cross section measurement precision

cuts	(both eLpR and eRpL)		S/B ratio	sig eff	$\Delta \sigma / \sigma_{MC}$	(only eLpR)			
	Nsig	Nbg				2f_Z_l	4f_WW_sl	4f_ZZ_sl	
last week	1056	2189	0.48	46.1+/-0.5%	4.39+/-0.00% (RMS: 0.16%)	225 (0.011%)	241 (0.009%)	950 (0.52%)	
this week									
Likelihood L1 using Minv, CosZ, Pt, max γ Pt	ln(L1)>-19.8	1057	2025	0.52	46.2+/-0.5%	4.29+/-0.00% (RMS: 0.15%)	28 (0.002%)	377 (0.014%)	967 (0.53%)
	ln(L1)>-19	1026	1746	0.59	44.8+/-0.5%	4.16+/-0.00% (RMS: 0.15%)	25 (0.001%)	270 (0.010%)	868 (0.48%)
Likelihood L2 using Minv, CosZ, Pt	ln(L2)>-15.8	1054	1949	0.54	46.1+/-0.5%	4.28+/-0.00% (RMS: 0.15%)	90 (0.004%)	285 (0.010%)	947 (0.52%)
	ln(L2)>-16	1062	2010	0.53	46.4+/-0.5%	4.27+/-0.00% (RMS: 0.15%)	95 (0.004%)	306 (0.010%)	967 (0.53%)

Observations

- Likelihood cut using max γ Pt (L1) is effective for 2f_Z_leptonic
- It is hard to cut 4f_ZZ_semileptonic BG without removing too much signal
- Residual 4f_WW_semileptonic BG depends on likelihood cut value
- → can resolve by adding muon isolation cut (?)

hist_P_jackieZH_2f_Z_leptonic_eL_pR



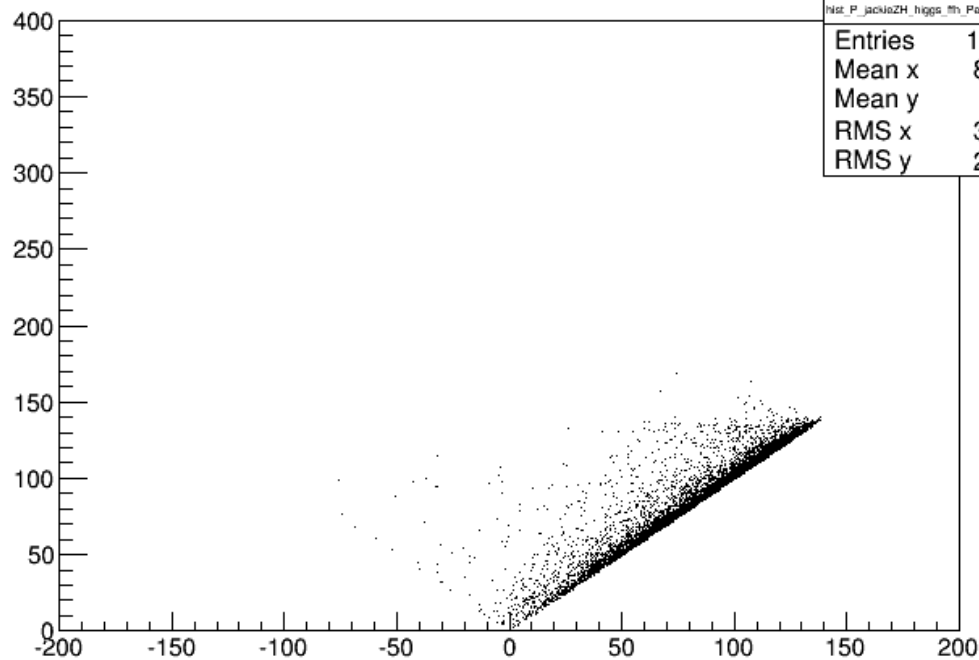
hist_P_jackieZH_2f_Z_leptonic_eL_pR	
Entries	68655
Mean x	5.474
Mean y	9.504
RMS x	
RMS y	

2D distr of

X; $dpt_{bal} = pt_{dl} - pt_{\gamma}$

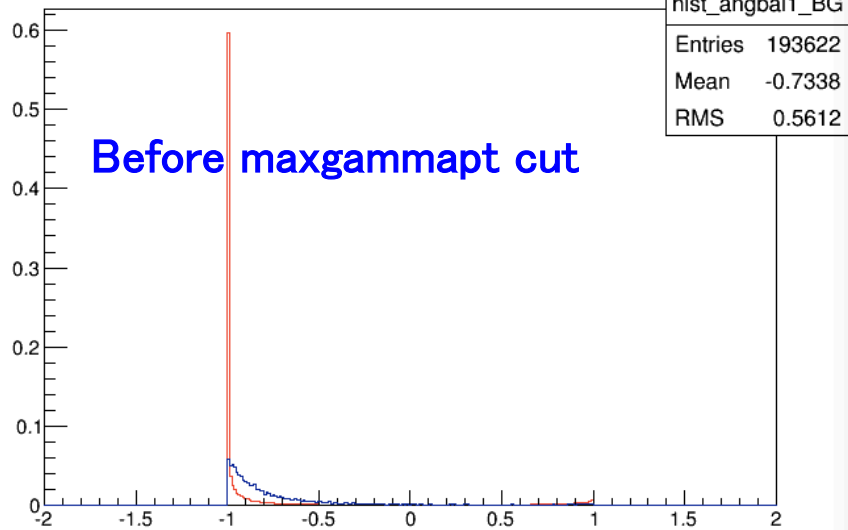
Y: $Pt_{sum} = |Pt_{dl} - Pt_{\gamma}|$ (in vectors)

hist_P_jackieZH_higgs_ffh_Pe2e2h_eL_pR

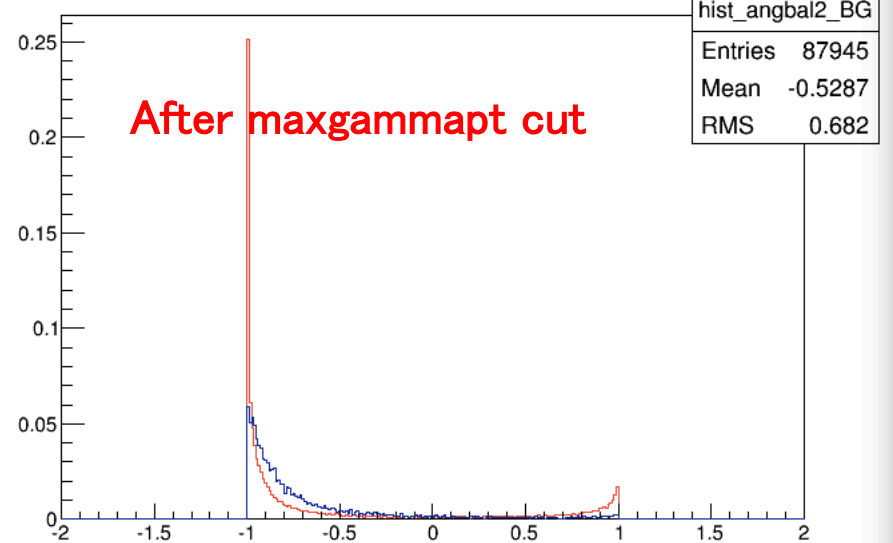


hist_P_jackieZH_higgs_ffh_Pe2e2h_eL_pR	
Entries	10184
Mean x	89.56
Mean y	94.1
RMS x	30.48
RMS y	28.15

hist_angbal1_BG

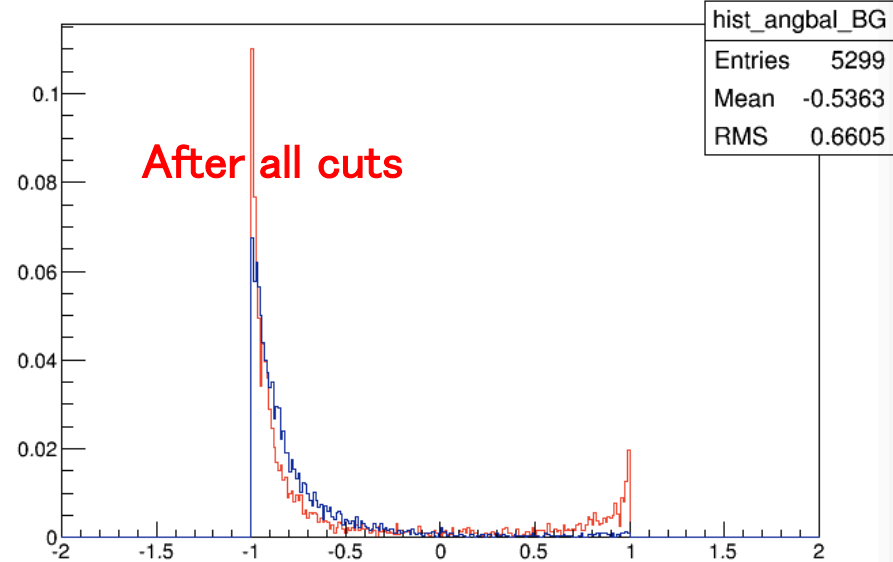


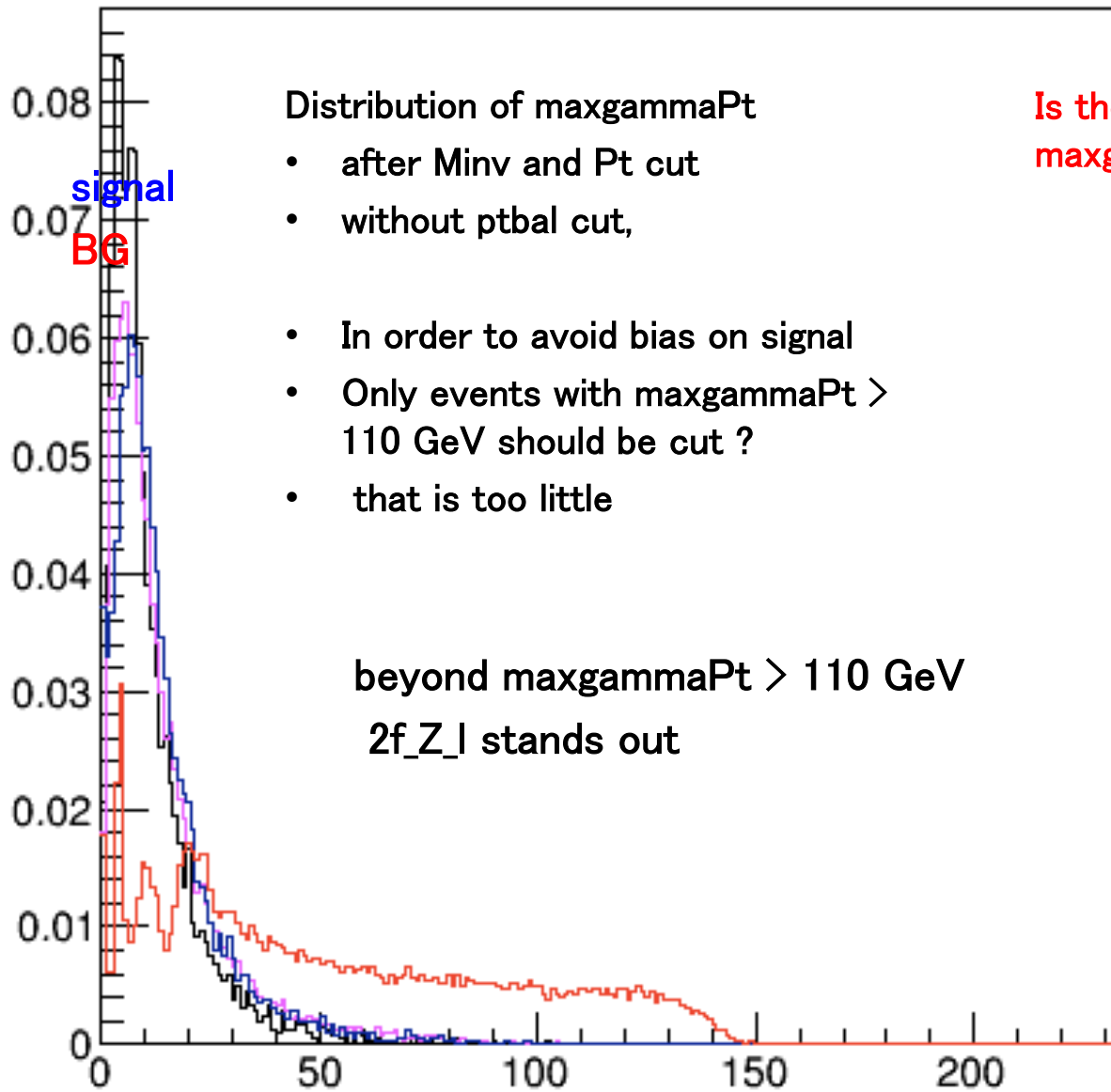
hist_angbal2_BG



Distr of $\cos(\theta_{bal})$

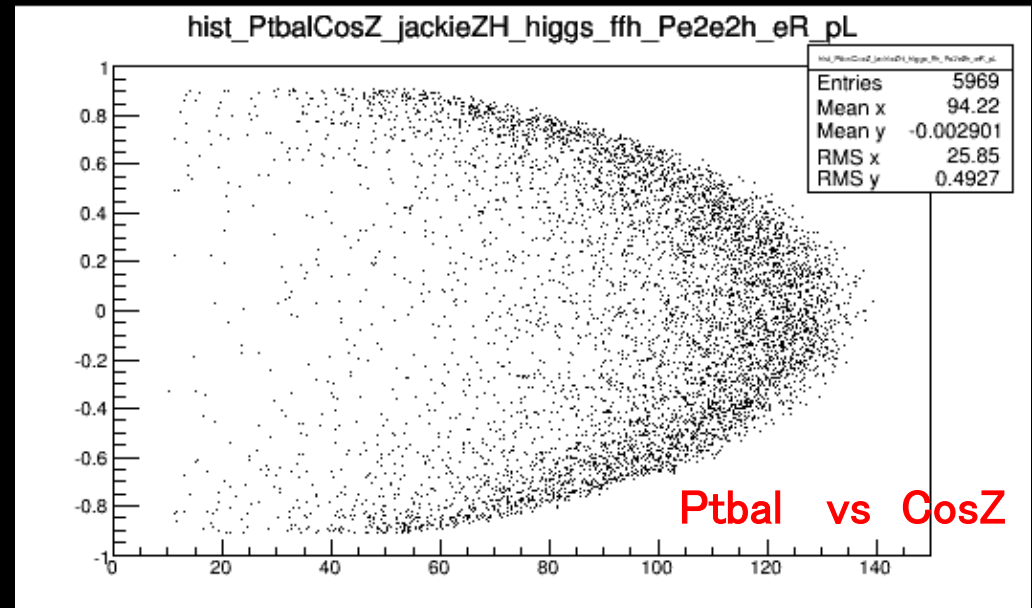
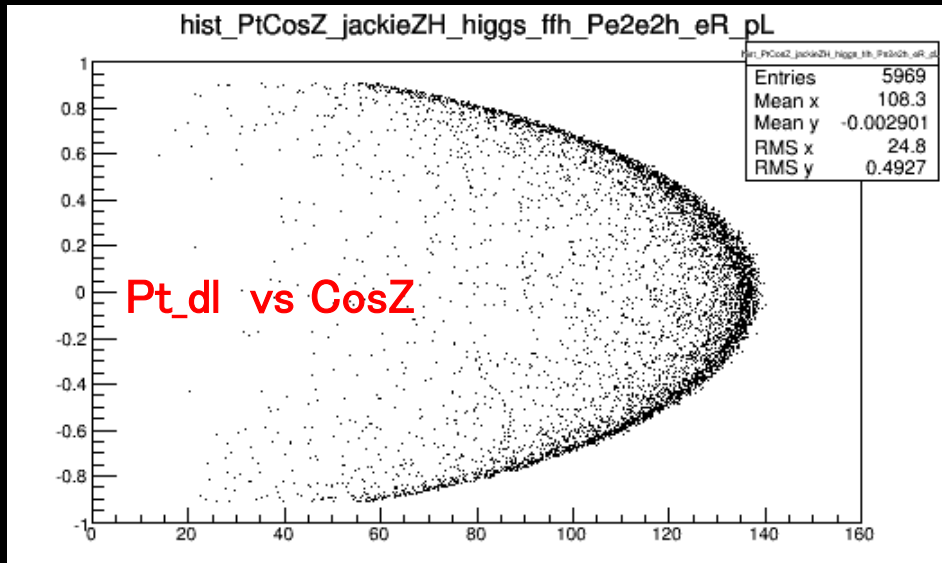
hist_angbal_BG



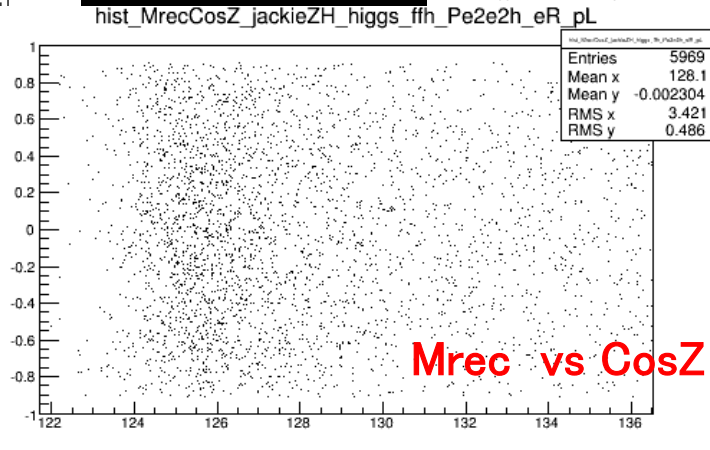
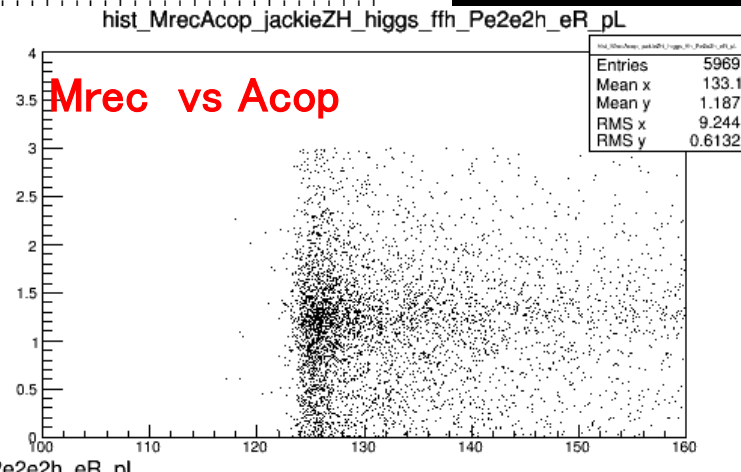
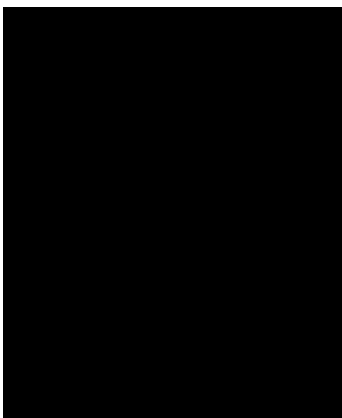
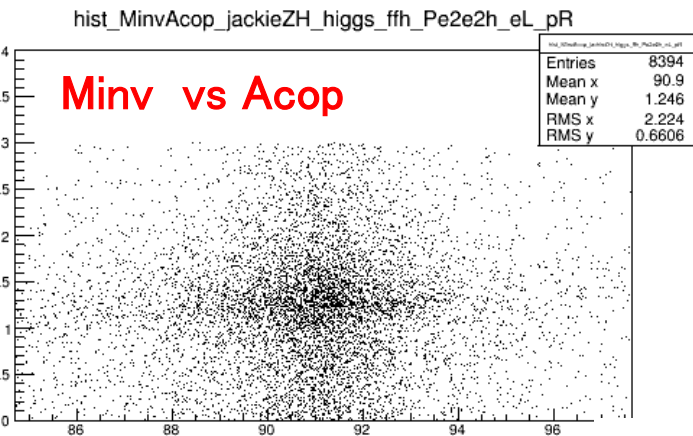
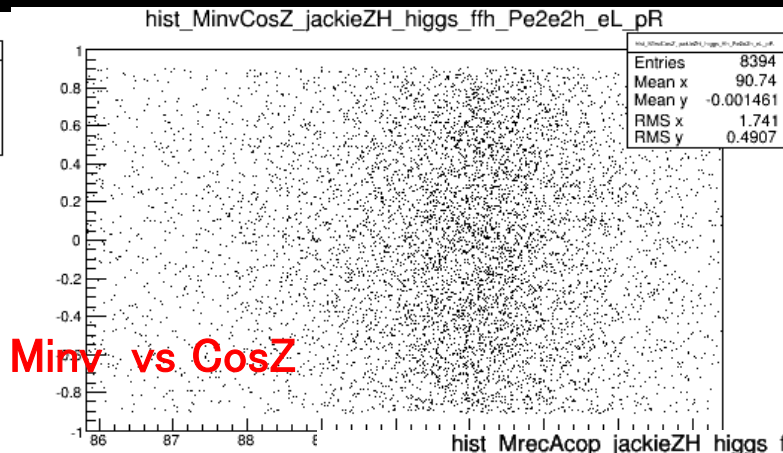
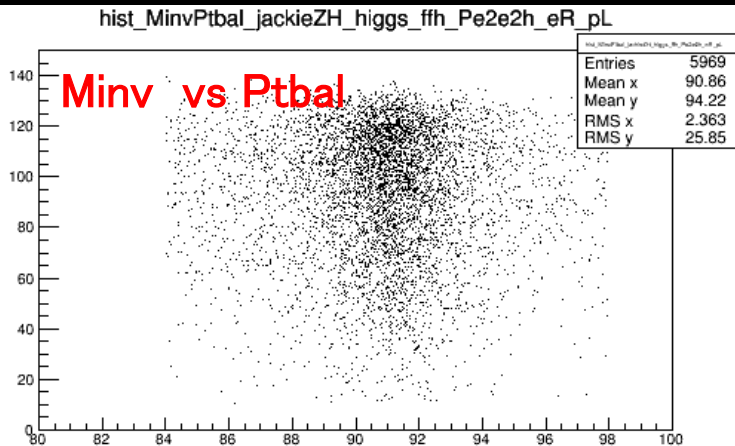


Is there some way to combine info of maxgammaPt and dptbal ?

Parameters showing correlation: not good for likelihood cut (?)



Parameters with no apparent correlation: good for likelihood cut (?)



断面積測定の精度の評価 : 異なるECMとビーム偏極の比較 NEW

ECM	Pol	ϵ	$\Delta \sigma / \sigma$	xsec [fb]	Nsig	significance
350 GeV	(-0.8,+0.3)	47.7+/-0.5%	4.9+/-0.2%	6.71+/-0.34	1092+/-55	17.7
	(+0.8,-0.3)	47.8+/-0.5%	5.0+/-0.2%	4.53+/-0.26	720+/-41	17.8
250 GeV	(-0.8,+0.3)	66.4+/-0.5%	3.6+/-0.1%	10.52+/-0.38	1747+/-64	21.7
	(+0.8,-0.3)	64.4+/-0.5%	3.3+/-0.1%	8.68+/-0.30	1398+/-48	22.7

注) この表の fitting範囲は115-150 GeV (AWLC14 @ Fermilabより)
 現在350 GeV のみ範囲を広げて、 $\Delta \sigma / \sigma$ が 4.7 +/- 0.2 % へ改善した

比較#1: ECM = 350 GeV \leftrightarrow ECM = 250 GeV :

ECM= 250 GeVの方が $\Delta \sigma / \sigma$ と Mh 精度 が良い μ の運動量測定の分解能は低いPTほど良い

比較#2: Pol: (-0.8,+0.3) \leftrightarrow (+0.8, -0.3):

- 異なる偏極の間で $\Delta \sigma / \sigma$ に大きな差がなさそう
- (+0.8, -0.3): 統計が少ないが、S/B がずっと高い: WW BGが顕著に抑制

注意) 先行studyとの色んな違い:

- assumed L (350, 250 GeV) = (333, 250 fb-1) vs RDR: (300 fb-1, 188 fb-1)
- このstudy : ALL 2f, 4f, 6f BGs (whizard generator) vs only WW, ZZ (pythia generator ?)

results for $\sqrt{s} = 250$ GeV , $L = 250$ fb $^{-1}$

evaluated using Toy MC generated from fitted function shapes

	ϵ	$\Delta \sigma / \sigma$	xsec	Nsig	S/N	significance
250 GeV						
(-0.8,+0.3)	66.4 \pm 0.5%	3.6 \pm 0.1%	10.52 \pm 0.38	1747 \pm 64	0.37	21.7
(+0.8,-0.3)	64.4 \pm 0.5%	3.3 \pm 0.1%	8.68 \pm 0.30	1398 \pm 48	0.81	22.7

