

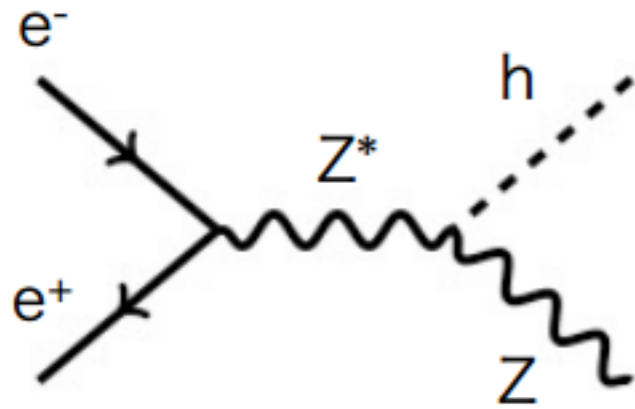
# Hadronic Recoil Mass Study with ILD at 250GeV/350GeV

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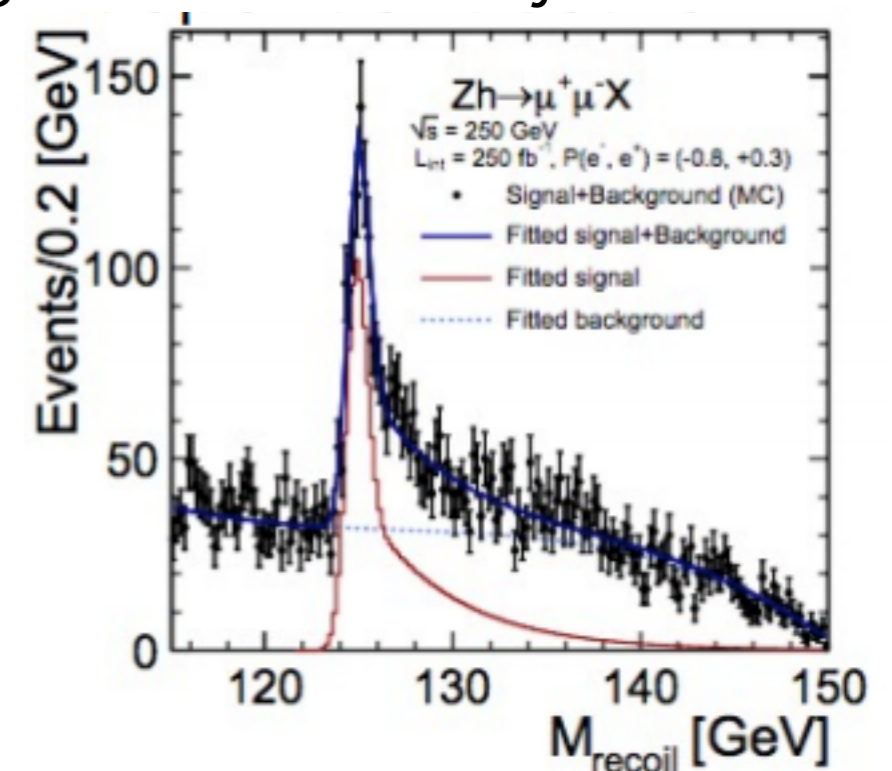


# Overview - qqH channel



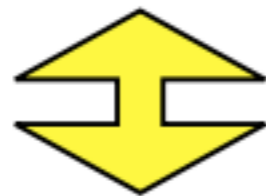
Using 4 momentum conservation, we can calculate the mass of Higgs boson without observing Higgs boson directly.

Especially in  $Z \rightarrow$  leptonic channel, its mass distribution has quite high precision. But, its BR is only  $\sim 3.4\%$  for each generation.



In contrast, the branching ratio of  $Z \rightarrow$  hadronic is  $\sim 70\%$ .

- **More statistics**

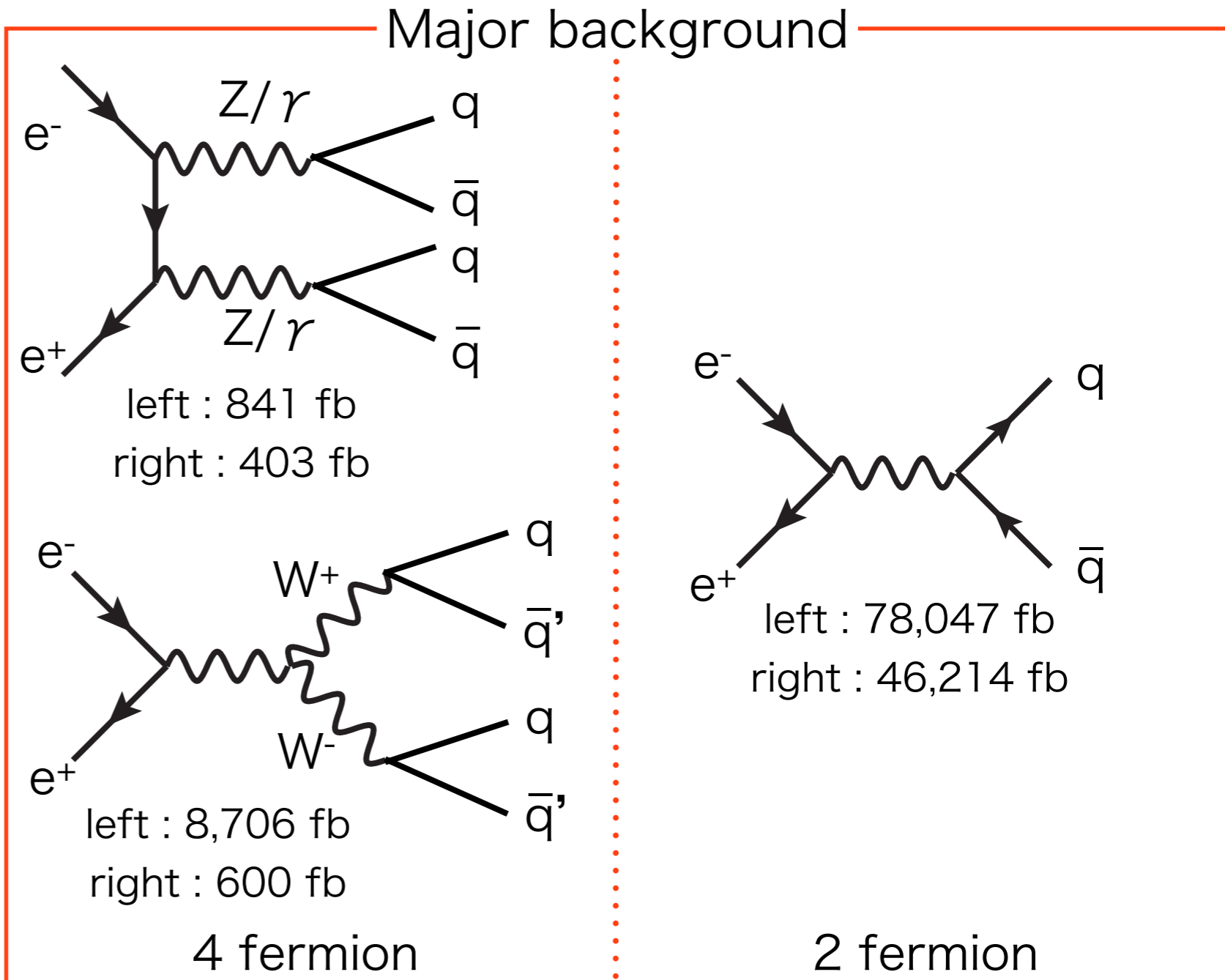
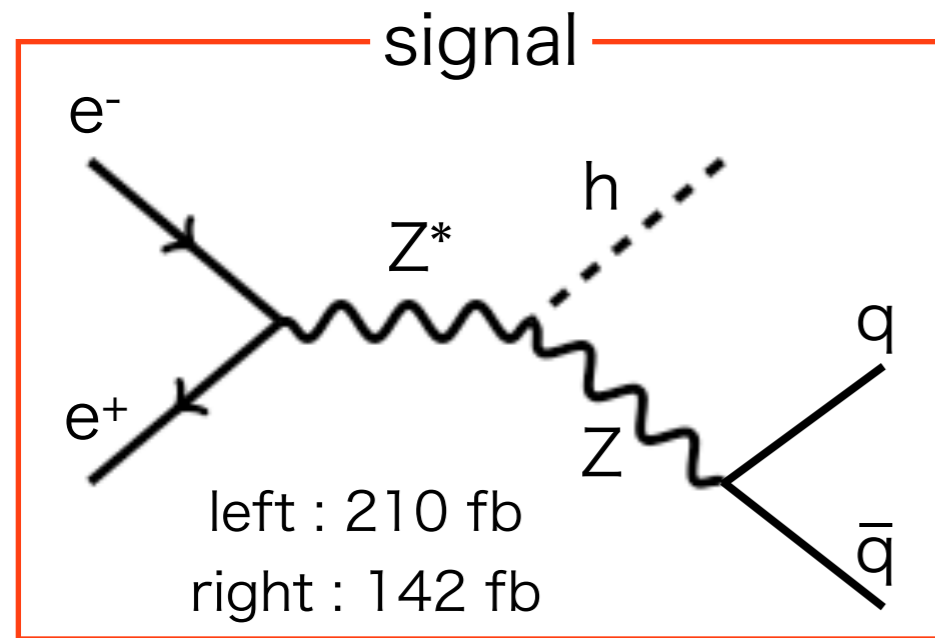


Model independent?

- **More background**

# Data samples

Higgs mass	$E_{\text{CM}}$	Luminosity	Polarization	Detector
125 GeV	250 GeV 350 GeV	250 fb <sup>-1</sup> 333 fb <sup>-1</sup>	left: (-0.8, +0.3) right: (+0.8, -0.3)	ILD_DBD ver.



semi-leptonic events  
are also considerable BG.

# Analysis flow

- To improve jet clustering,
  - Initial state radiation
  - Isolated lepton
  - Hadronic tau jet were removed from events.
- Durham jet clustering was applied to the remaining particles.

$$y = \frac{2\min(E_i^2, E_j^2)(1 - \cos \theta_{ij})}{Q^2}$$

- Forced 4 jet clustering (for BG estimation),  
y threshold clustering were used (for recoil mass analysis).

250 GeV

# Background reduction

- 4 fermion background - using forced 4 jet clustering, mass box ZZ(81,101), WW(70,90)
- 2 fermion background - Thrust and Sphericity were used.
- S/N separation
  - reconstructed the mass of Z candidate 2-jet with y value clustering ( $y = 0.0025$ ).
  - reconstructed the transverse momentum of Z candidate.
  - The distribution of Hadronic recoil mass.
- After applying these cuts,

	signal	4 fermion	2 fermion	others
% of events after cuts	46.2%	8.3%	1.4%	0.3%

# Cut efficiency issue

- After applying cuts, tested cut efficiencies for each Higgs decay.

mode	After cuts (%)	difference/mean
H->all	46.2%	-----
H->bb (57.7%)	43.3%	-6.3%
H->WW(leptonic) (2.3%)	45.3%	-1.9%
H->WW(semi-leptonic) (9.5%)	46.9%	+1.5%
H->WW(hadronic) (9.8%)	54.4%	+17.7%
H->gg (8.6%)	55.2%	+19.5%
H-> $\tau\tau$ (6.3%)	45.3%	-1.9%
H->ZZ (2.6%)	48.6%	+5.2%
H->cc (2.9%)	47.1%	+6.3%
H->invisible (ZZ->4n) (0.1%)	35.4%	-23.4%

- The large inconsistency was found in H->gg, H->WW->4q and invisible.

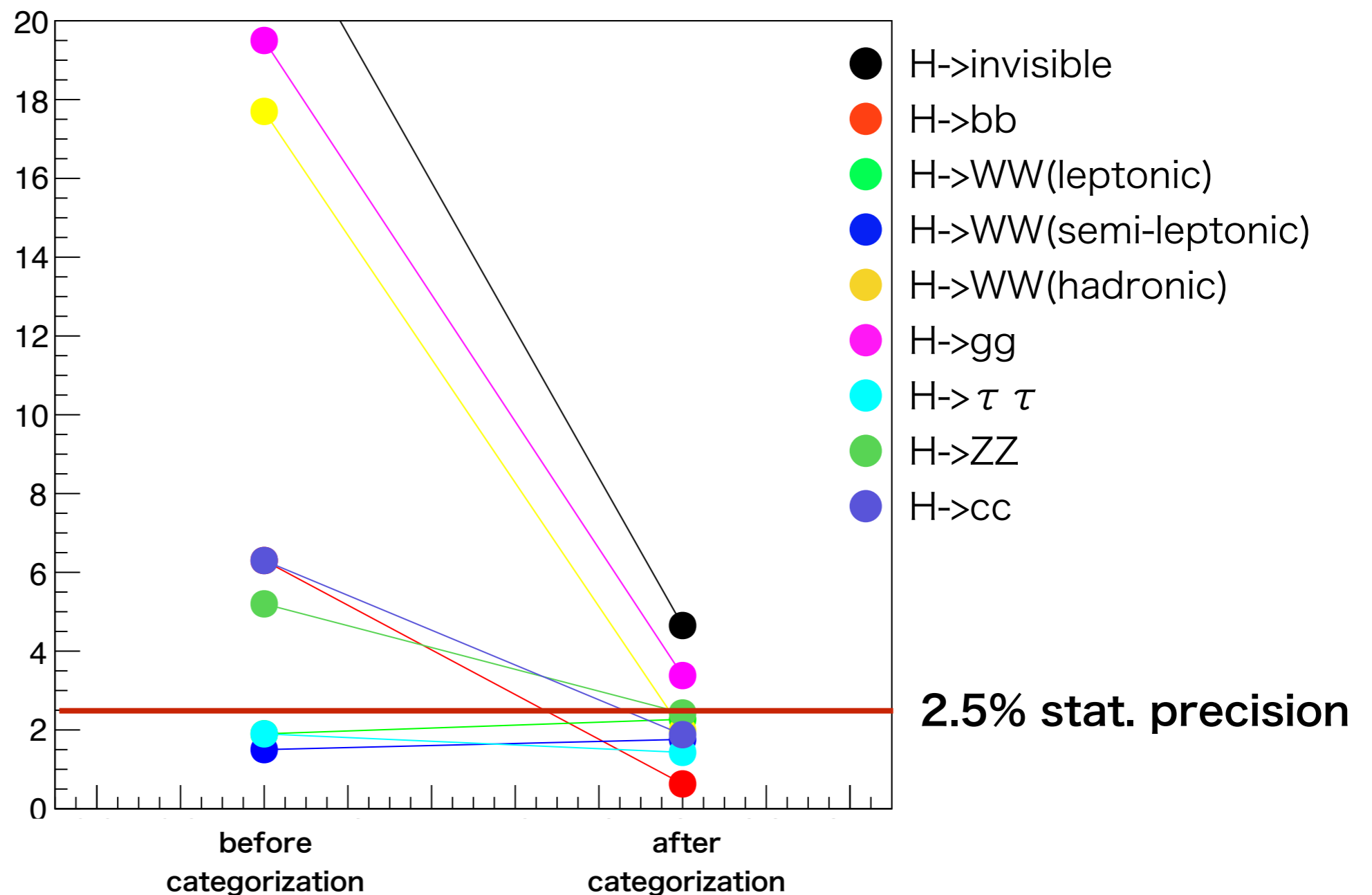
# Categorization (inconsistency reduction)

- The inconsistency of cut efficiency will affect the measurements of  $\sigma_{ZH}$ .
- This systematic uncertainty should be kept as small as possible.
- The categorization is one of the powerful solution.
- Classify the whole event into the nine categories using number of isolated leptons, tau jets, b-tag ( $>0.8$ ), c-tag ( $>0.7$ ).
- Then, optimize the cut in each category.



# Cut efficiency and Categorization

- After categorizing events and applying much optimized cuts,
- The efficiency inconsistency is at most  $\sim 3.5\%$ . (exc. inv.)



# Two Luminosity cases

polarization and Luminosity	significance $\sigma_{ZH}$	stat. precision $\sigma_{ZH}$	stat. precision $g_{ZZH}$	stat. precision $g_{ZZH}$ (combined)
left (-0.8, +0.3) 250 fb <sup>-1</sup>	<b>37.6 <math>\sigma</math></b>	<b>2.7%</b>	<b>1.4%</b>	<b>1.1%</b>
right (+0.8, -0.3) 250 fb <sup>-1</sup>	<b>41.1 <math>\sigma</math></b>	<b>2.4%</b>	<b>1.2%</b>	<b>1.0%</b>
left (-0.8, +0.3) 2000 fb <sup>-1</sup> (Lumi UP)	<b>106.3 <math>\sigma</math></b>	<b>0.9%</b>	<b>0.5%</b>	<b>0.4%</b>
right (+0.8, -0.3) 2000 fb <sup>-1</sup> (Lumi UP)	<b>116.2 <math>\sigma</math></b>	<b>0.9%</b>	<b>0.4%</b>	<b>0.3%</b>

# The effect of the Branching Ratio

base	209.80	141.95	—	—
bb + 5% (57.7->62.7)	209.90	141.88	~0.0%	~0.0%
bb - 5% (57.7->52.7)	209.69	142.03	-0.1%	~0.0%
cc + 5% (2.9->7.9)	208.70	141.21	-0.5%	-0.5%
cc - 5% (2.9->0.0)	210.40	142.37	+0.3%	+0.3%
gg + 5% (8.6->13.6)	209.59	141.99	-0.1%	~0.0%
gg - 5% (8.6->3.6)	210.00	141.92	+0.1%	~0.0%
WW + 5% (21.6->26.6)	209.64	141.98	-0.1%	~0.0%
WW - 5% (21.6->16.6)	209.79	141.82	~0.0%	-0.1%
tau + 5% (6.3->11.3)	210.05	141.08	+0.1%	+0.1%
tau - 5% (6.3->1.3)	209.55	141.83	-0.1%	-0.1%
ZZ + 5% (2.6->7.6)	210.13	142.23	+0.2%	+0.2%
ZZ - 5% (2.6->0.0)	209.72	141.88	~0.0%	-0.1%
invisible + 5% (0.1->5.1)	213.95	147.44	+2.0%	+3.9%
invisible - 5% (0.1->0.0)	210.10	141.73	~0.0%	~0.0%

The changing of branching ratio has only ~0.5 % effect on total cross section of ZH production. This is much smaller than current stat. precision. (exc. inv.)

•  
350 GeV

# Background reduction

- 4 fermion background - using forced 4 jet clustering, mass box ZZ(81,101), WW(70,90,75,85)
- 2 fermion background - Thrust and Sphericity were used.
- S/N separation
  - reconstructed the mass of Z candidate 2-jet with y value clustering ( $y = 0.0025$ ).
  - reconstructed the transverse momentum of Z candidate.
  - The distribution of Hadronic recoil mass.
- After applying these cuts,

	signal	2 fermion	4 fermion	6 fermion	tt	others
% of events after cuts	30.8%	0.4%	3.6%	7.0%	6.1%	0.3%

# Cut efficiency in 350 GeV

- After applying cuts, tested cut efficiencies for each Higgs decay.

mode	After cuts (%)	difference/mean
H->all	30.8%	-----
H->bb (57.7%)	29.6%	-3.9%
H->WW(leptonic) (2.3%)	33.7%	+9.4%
H->WW(semi-leptonic) (9.5%)	26.4%	-14.4%
H->WW(hadronic) (9.8%)	32.1%	+4.1%
H->gg (8.6%)	39.1%	+27.0%
H-> $\tau\tau$ (6.3%)	34.0%	+10.3%
H->ZZ (2.6%)	28.6%	-7.2%
H->cc (2.9%)	33.0%	+7.1%

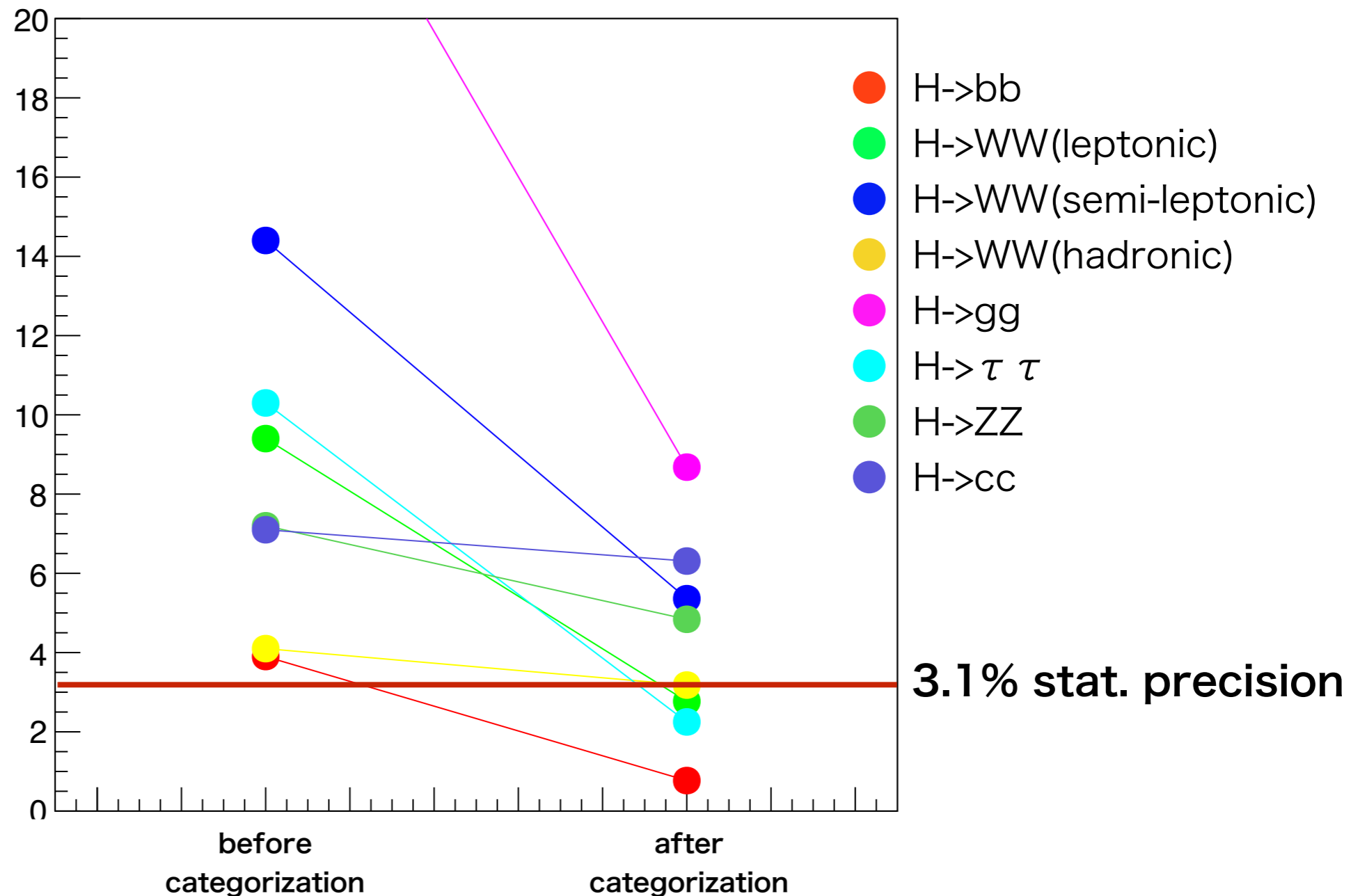
- H->gg, WW(leptonic/semi-leptonic),  $\tau\tau$  has large inconsistency.

# The same strategy (categorization)

- Used number of lepton, number of tau, b-tag(0.8) and c-tag(0.7).
- Currently, the same number of categories (13) are used.
- Possibly we can simplify in 350 GeV case...  
( jet separation is much better than 250 GeV )
- Cut efficiency inconsistency is still problem in 350 GeV.
- Need more effort to solve this problem.

# Cut efficiency and Categorization

- In 350 GeV, categories have not been optimized yet.  
H->gg has large inconsistency from mean cut efficiency.





# 350 GeV case

polarization and Luminosity	significance $\sigma_{ZH}$	stat. precision $\sigma_{ZH}$	stat. precision $g_{ZZH}$	stat. precision $g_{ZZH}$ (combined)
350 GeV left (-0.8, +0.3) 333 fb <sup>-1</sup>	<b>32.5 <math>\sigma</math></b>	<b>3.1%</b>	<b>1.5%</b>	<b>1.3%</b>
350 GeV right (+0.8, -0.3) 333 fb <sup>-1</sup>	<b>32.9 <math>\sigma</math></b>	<b>3.1%</b>	<b>1.5%</b>	<b>1.3%</b>

# Summary and Prospects

## summary

- Using categorization, the difference of cut efficiency is suppressed at most  $\sim 3.5\%$ .
- Stat. precision is about  $\sim 2.5\%$  which is almost the same as leptonic channel (ILC Higgs White paper's results)
- 350 GeV needs more effort.

	significance	stat. precision
250 GeV (-0.8,+0.3) 250fb <sup>-1</sup>	<b>37.6 <math>\sigma</math></b>	<b>2.7%</b>
250 GeV (+0.8,-0.3) 250fb <sup>-1</sup>	<b>41.1 <math>\sigma</math></b>	<b>2.4%</b>
350 GeV (-0.8,+0.3) 333fb <sup>-1</sup>	<b>32.5 <math>\sigma</math></b>	<b>3.1%</b>
350 GeV (+0.8,-0.3) 333fb <sup>-1</sup>	<b>32.9 <math>\sigma</math></b>	<b>3.1%</b>

## prospects

- 500 GeV will be performed by my successor.
- 350 GeV also...

# backup slides

# Strategy to reduce inconsistency (Categorization)

- Categorization is a powerful tool to reduce difference of efficiency among Higgs decay modes.
- Categorize events using number of jets, leptons, taus, etc.
- Minimize the difference of efficiency in each category (decay modes with too small fraction in the category is negligible.)
- Calculate partial cross section from each category
- Combine all cross section from categories to get the total cross section of ZH production.

# Categorization -1

To resolve efficiency inconsistent issue, we will categorize events using

- the number of tau jets (0, 1, and  $\geq 2$ )
- the number of isolated lepton (0, 1, and  $\geq 2$ )

$$N^i = \sum_n \sigma_{\text{tot}} \cdot \text{BR}_n \cdot \theta_n^i \cdot \epsilon_n^i$$

$n = (b, W, g, \tau, \dots)$

$N^i$  is a number of events in category  $i$ ,  $\sigma_{\text{tot}}$  is total cross section,  $\text{BR}_n$  is Higgs decay branching ratio,  $\theta_n^i$  is fraction in category  $i$ ,  $\epsilon_n^i$  is cut efficiency for category  $i$ .

If the cut efficiency of each decay mode can be assumed to be the same as  $\epsilon^i (= \epsilon_n^i)$ .

$$\frac{N^i}{\epsilon^i} = \sigma_{\text{tot}} \sum_n \text{BR}_n \cdot \theta_n^i$$

Then we can get

$$\sum_i \frac{N^i}{\epsilon^i} = \sigma_{\text{tot}} \sum_n \sum_i \text{BR}_n \cdot \theta_n^i = \sigma_{\text{tot}}$$

# Categorization

If the cut efficiency is not exactly the same,  
we should consider the systematic effect caused by the difference.

$$\delta\epsilon_n^i = \epsilon_n^i - \epsilon^i$$

And the cross section is

$$\sigma_{\text{tot}} = \frac{\sum_i \frac{N^i}{\epsilon^i}}{1 + \sum_n \sum_i \text{BR}_n \cdot \theta_n^i \cdot \frac{\delta\epsilon_n^i}{\epsilon^i}}$$

We want to keep systematic uncertainty is less than 1 % to do model independent analysis.

If we don't assume any models, we should keep  $\theta_n^i \cdot \frac{\delta\epsilon_n^i}{\epsilon^i} \ll 1 \%$ .

If we can assume SM like Higgs, we should keep  $\text{BR}_n \cdot \theta_n^i \cdot \frac{\delta\epsilon_n^i}{\epsilon^i} \ll 1 \%$ .

# 背景事象の低減 ①

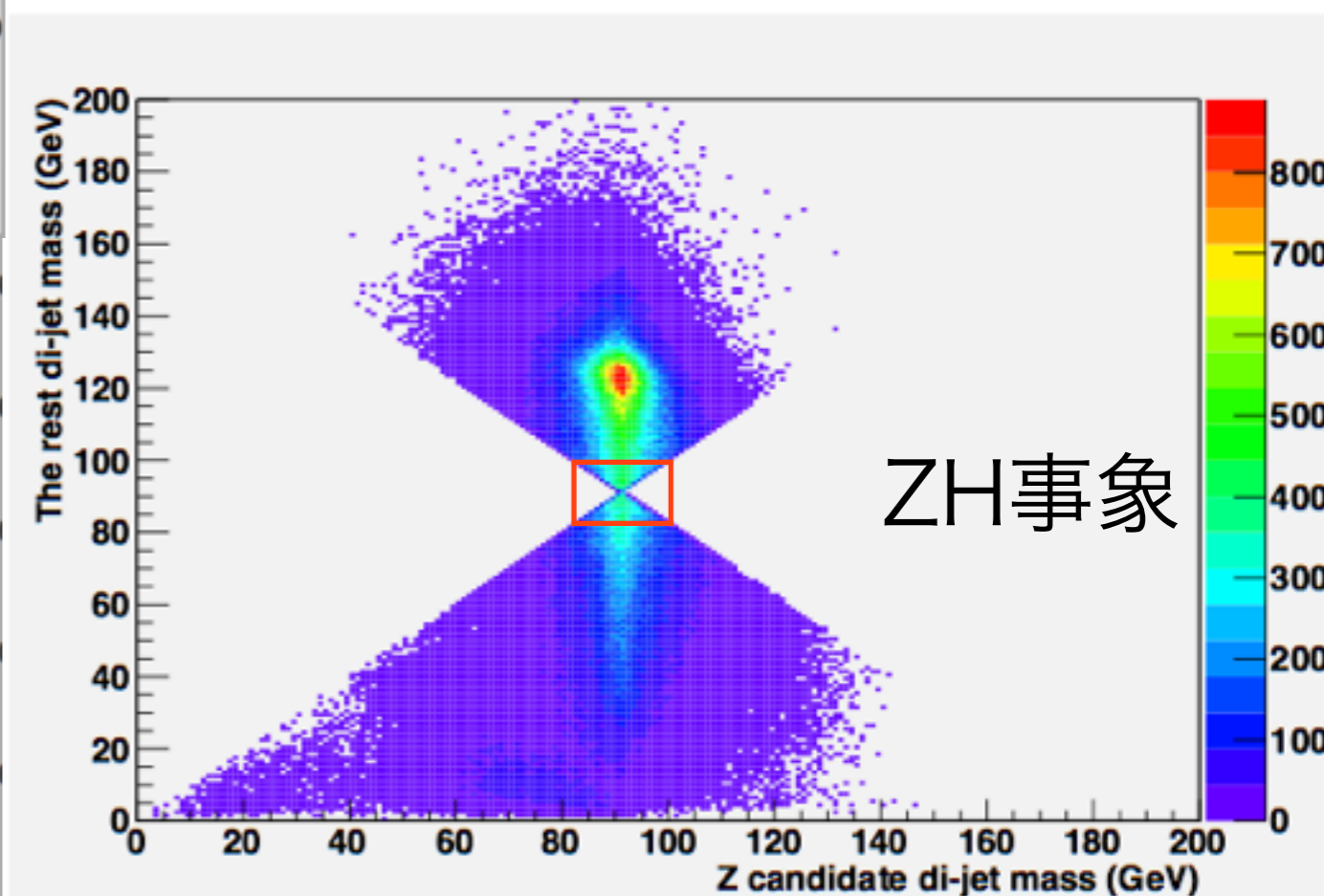
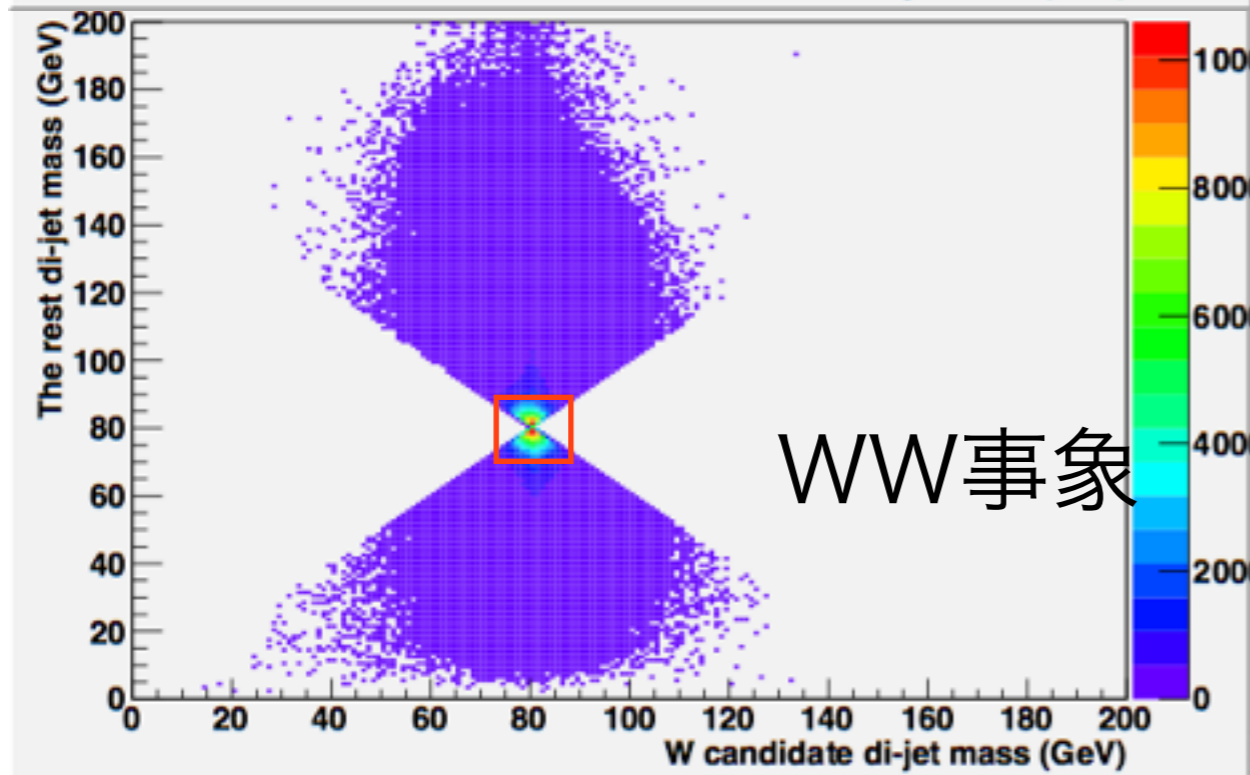
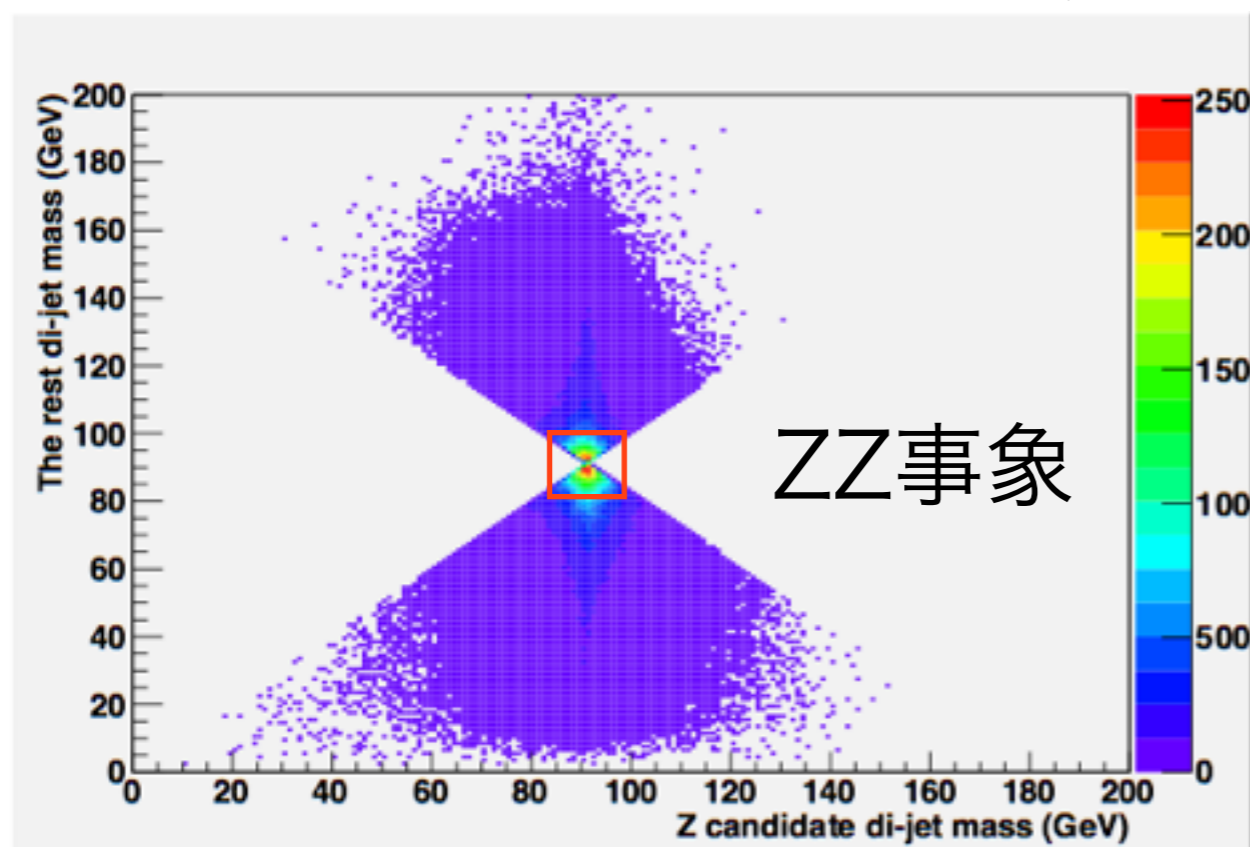
- 4 fermion事象の低減 -> 各粒子の質量差を利用  
4つのジェットにクラスタリング -> 2つずつのジェットの組みで

質量を再構成する

Z粒子 91GeV

W粒子 80GeV

ヒッグス粒子 125GeV



# 背景事象の低減 ②

- 2 fermion 事象の低減のために、SphericityとThrustによるカットを適用した

- Sphericity
  - 観測された事象の球度を表す指標
  - ~0で直線状 ~1で球形

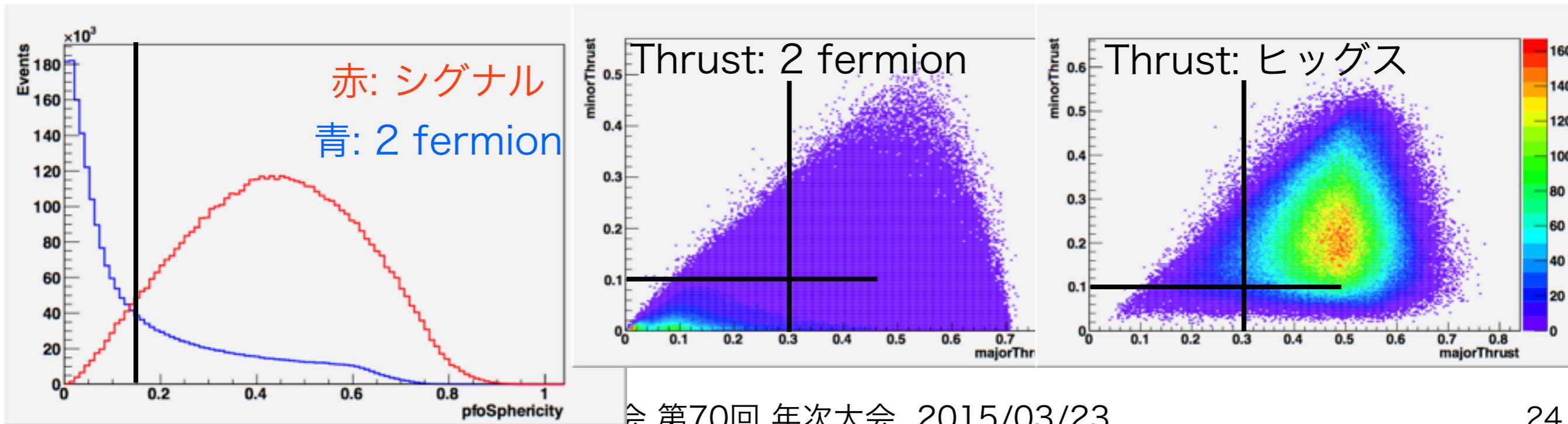
$$S^{ab} = \frac{\sum_i p_i^a p_i^b}{\sum_i p_i^2} \quad a, b = x, y, z$$

- Major Thrust, Minor Thrust
  - 事象のジェットの細さを表す指標

$$T_{major} = \max_{|\vec{n}'|=1, \vec{n}' \cdot \vec{n}=0} \frac{\sum_i |\vec{p}_i \cdot \vec{n}'|}{\sum_i |\vec{p}_i|}$$

$$T_{minor} = \frac{\sum_i |\vec{p}_i \cdot \vec{n}''|}{\sum_i |\vec{p}_i|} \quad \text{with } \vec{n}'' \cdot \vec{n} = \vec{n}'' \cdot \vec{n}' = 0$$

Major Thrust ~ 0 で 3-jet未満、Minor Thrust ~ 0 で 4-jet未満



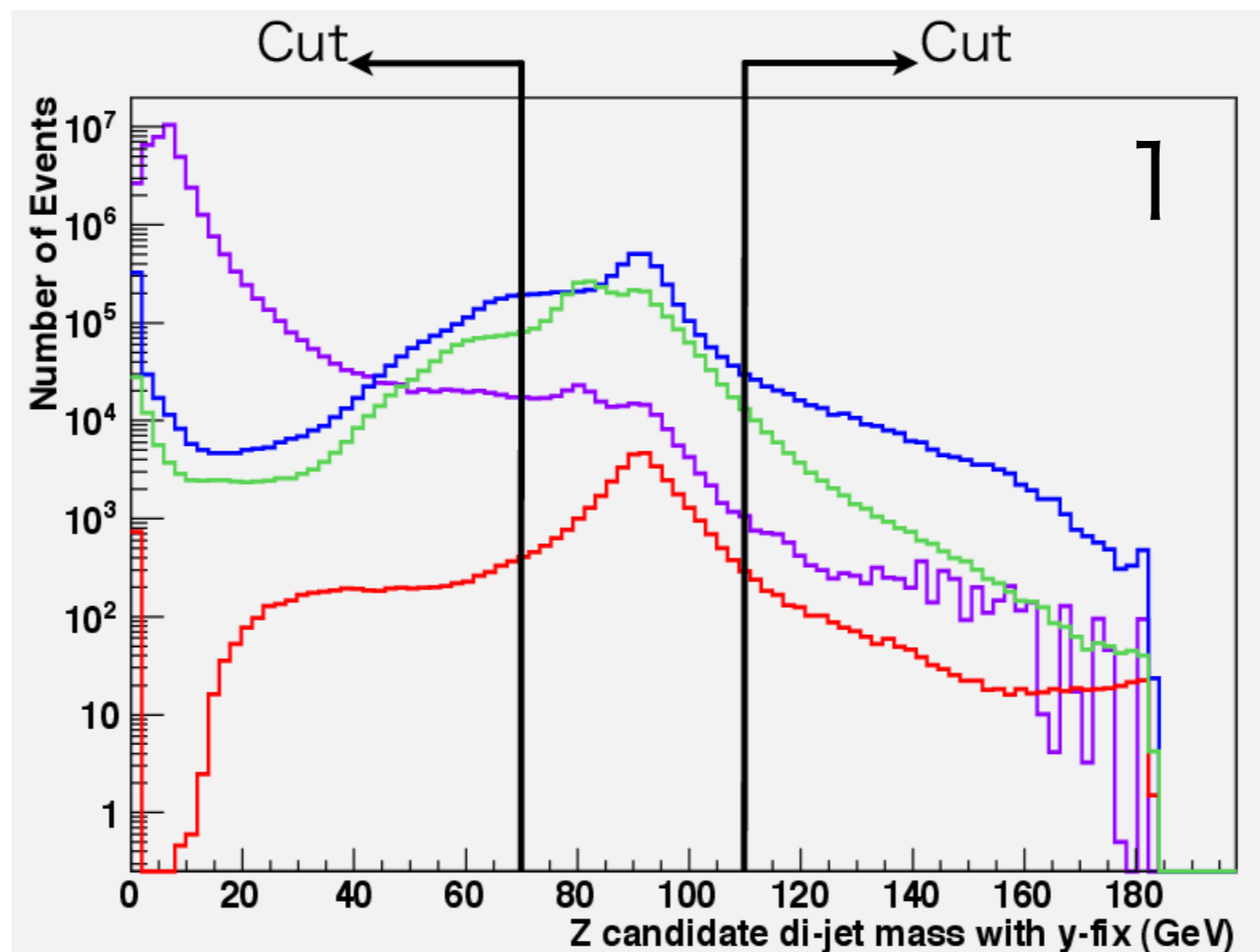


# 背景事象の低減 ③

- 背景事象と信号事象の更なる切り分けのために、  
閾値を設定したジェットクラスタリングにおいて
  - 再構成されたZ粒子の質量 1
  - 再構成されたZ粒子の横方向運動量 2
  - 反跳質量 3

の分布を用いて事象選別をおこなった

シグナル  
2 fermion  
4 fermion  
その他

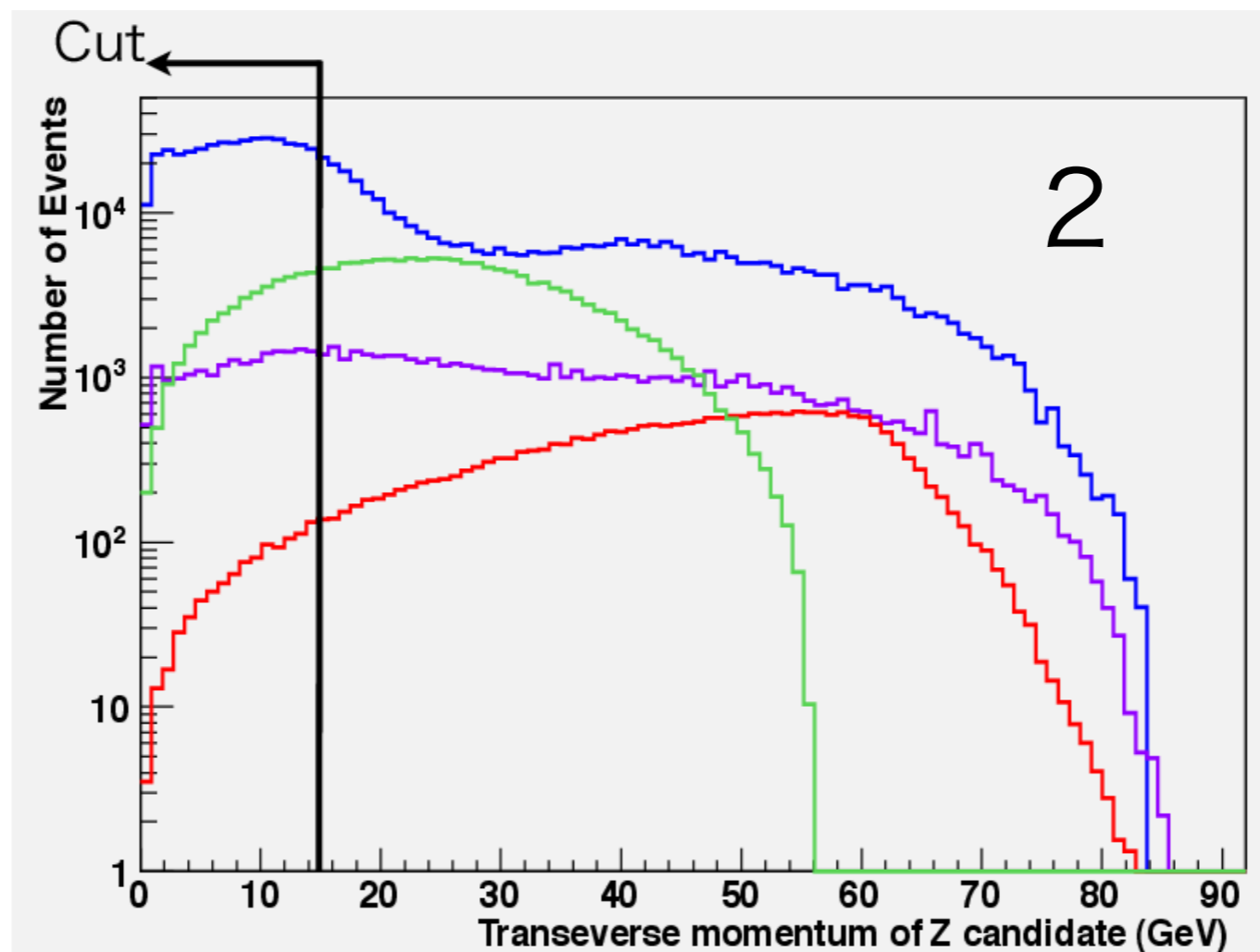


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