

**Higgs Recoil Mass Study using  $Z \rightarrow \ell\ell$   
at ECM=250, 350 GeV and 500 GeV ILC**

**The 42<sup>nd</sup> General Meeting  
of the ILC Physics Working Group**

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and the ILC Physics Working Group**

## recoil mass study using leptonic channels

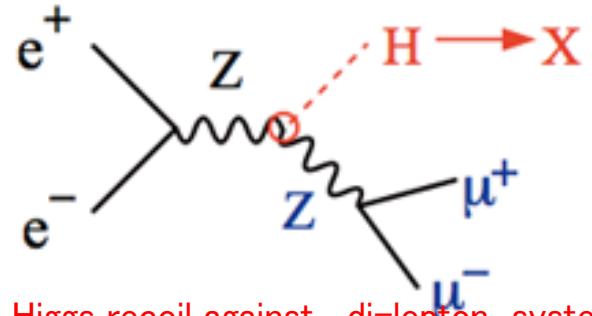
ECM = 250 GeV, 350 GeV, and 500 GeV

### precise model-independent measurement of absolute Higgs cross section and recoil mass

- $\sigma_{ZH}$  is a “must-have”  
for measurement of total Higgs width & couplings
- study impact of ECM and polarization
- contribute to the decision for ILC run scenario  
originally study was focused on the new field of 350 GeV since many physics become important

signal

H decay mode independent



Higgs recoil against di-lepton system

$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

this time, extended to all ECM and both leptonic channels

### ILC sample used in analysis

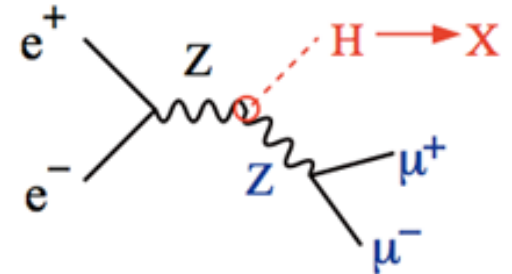
channel	mH	ECM	L	Spin polarization	Detector simulation
$e^+e^- \rightarrow Zh \rightarrow \mu\mu h$	125 GeV	250 GeV	250 fb <sup>-1</sup>	P(e <sup>-</sup> ,e <sup>+</sup> ) = (-0.8,+0.3) (+0.8,-0.3)	Full ILD (ILD_01_v05 DBD ver.)
$e^+e^- \rightarrow Zh \rightarrow eeh$		350 GeV	333 fb <sup>-1</sup>		
		500 GeV	500 fb <sup>-1</sup>		

### Layout of this Talk

- ◆ Evaluation of data analysis performance
- ◆ Comparison between different ECM and polarization
- ◆ Summary & Plans

## Signal signature

a pair of isolated energetic leptons ( $\mu / e$ ) with invariant mass ( $M_{inv}$ ) close to Z mass



$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

*Recoil mass*

## Dominant backgrounds

- $e^+ e^- \rightarrow Z Z \rightarrow l^+ l^- X$  : forward Z production angle
- $e^+ e^- \rightarrow \gamma Z \rightarrow \gamma l^+ l^-$  : energetic ISR  $\gamma$  which balance dilepton pt
- $e^+ e^- \rightarrow W W \rightarrow l^+ l^- \nu \nu$  : broad  $M_{inv}$  distr.

## Signatures

- data selection is based on signal / BG characteristics
- a final recoil mass window (100 – 160 GeV) is effective for cutting BG

## Progress since the last (41th) General Meeting (April 11)

### Last Time

- only  $Z \rightarrow \mu\mu$  channel
- only ECM = 250 GeV and 350 GeV
- only study of xsec precision
- slight Higgs decay mode bias caused by BG rejection method

### Features of This Time

- both  $Z \rightarrow \mu\mu$  and  $Z \rightarrow ee$  channels
  - all three ECM (250 , 350 , 500 GeV)
  - study of both xsec and mass precision
  - signal bias is minimized due to improved techniques (details later)
- + *deeper study of the signal and BG statistics of each channel*

- Currently converging towards a **full set of statistical error study results**
- **optimized data selection method for each of the 12 scenarios** (3 ECM x 2 leptonic channels x 2 polarizations) in aim of best xsec and mass precision
- Removed systematic bias due to method of fitting or data selection

## Lepton Pair Candidate Selection

opposite  $\pm$  1 charge

•  $E_{\text{cluster}} / P_{\text{total}} : < 0.5 (\mu) / > 0.9 (e)$

• **isolation (small cone energy)**

→ removes nearly all  $4f_{WW,sl}$  BG

•  $M_{\text{inv}}$  closest to Z mass

•  $|D0/\delta D0| < 5$

## Final Selection

•  $73 < \text{GeV} < M_{\text{inv}} < 120 \text{ GeV}$

•  $10 \text{ GeV} < p_{t,dl} < 140 \text{ GeV}$

•  $\left| \vec{P}_{t,sum} \right| \circ \left| \vec{P}_{t,g} + \vec{P}_{t,dl} \right| > 10 \text{ GeV}$

•  $|\cos(\theta_{\text{missing}})| < 0.98$

•  $|\cos(\theta_Z)| < 0.9$

•  $100 \text{ GeV} < M_{\text{recoil}} < 160 \text{ GeV}$

• **Likelihood cut**

Example of  
ECM=350 GeV,

Data selections designed to guarantee  
Higgs decay mode independence

Optimized in terms of signal significance and  
xsec measurement precision

definition

- $M_{\text{inv}}$  : invariant mass of 2 muons
- $p_{t,dl}$  : pt of reconstructed lepton pair
- $p_{t,\gamma}$  : pt of most energetic photon
- $\theta_{\text{missing}}$  = polar angle of undetected particles
- $\theta_Z$  = Z production angle

- Effective for cutting  $\mu\mu / ee$  BG
- Use info of most energetic photon ( $p_{t,\gamma}$ , cone energy) meanwhile minimize bias on signal

red box:

key improvements w.r.t. previous studies

similar methods applied to all ECM and polarizations

# Performance of data selection

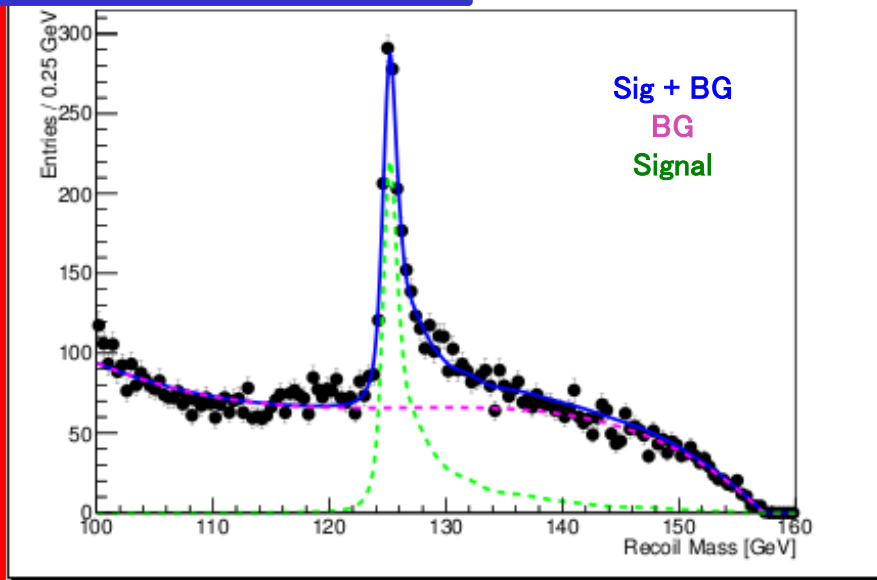
in fitting range 100–160 GeV

(-0.8,+0.3)		significance	Nsig	Nbg
250GeV	Zmm	18.3	1879	8692
	Zee	14.4	1502	9394
350GeV	Zmm	17.7	1462	5332
	Zee	14.1	1156	5597
500GeV	Zmm	11.1	626	2572
	Zee	8.7	439	2087
(+0.8,-0.3)		significance	Nsig	Nbg
250GeV	Zmm	19.7	1264	2834
	Zee	12.8	1096	6231
350GeV	Zmm	17	1002	2486
	Zee	12.7	602	1627
500GeV	Zmm	9.9	414	1339
	Zee	8.9	325	1003

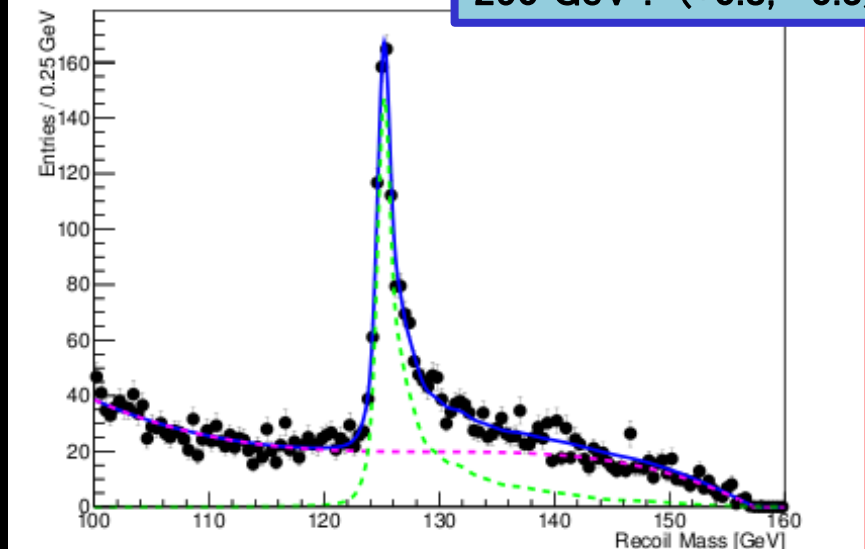
- In general, significance is  $250 > 350 > 500$  GeV,  $Zmm > Zee$
- right hand polarization: case by case:  
(lower BG, but also smaller signal statistics)

# $Z \rightarrow \mu\mu$ channel

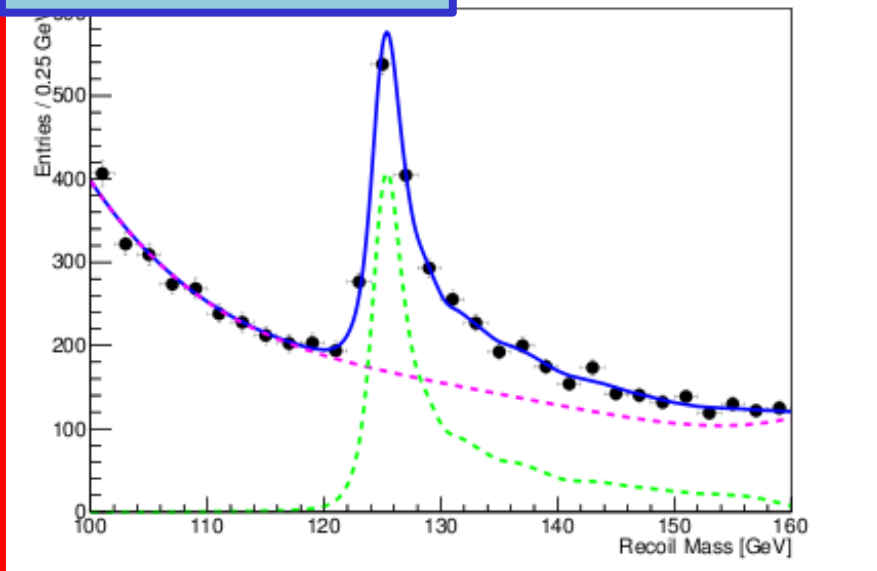
250 GeV : (-0.8, +0.3)



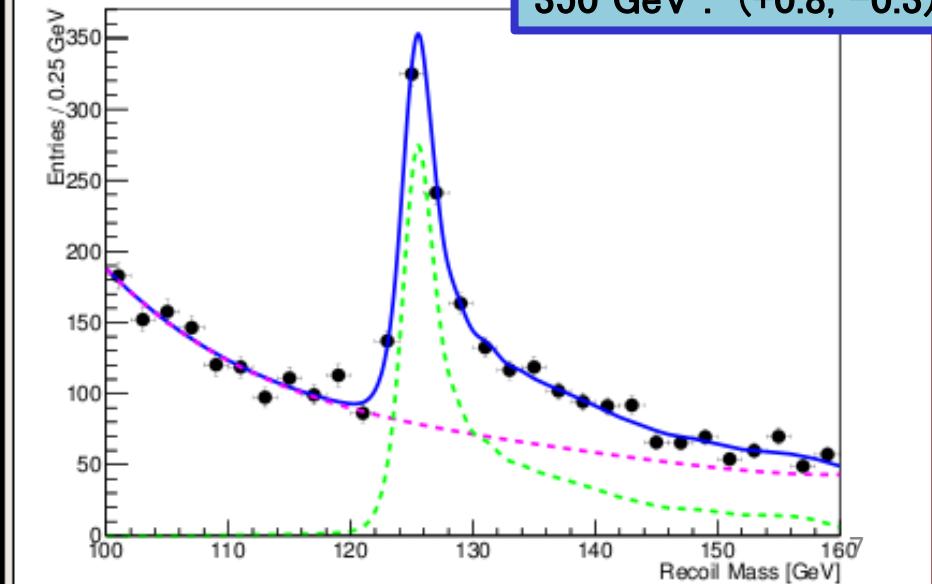
250 GeV : (+0.8, -0.3)



350 GeV : (-0.8, +0.3)

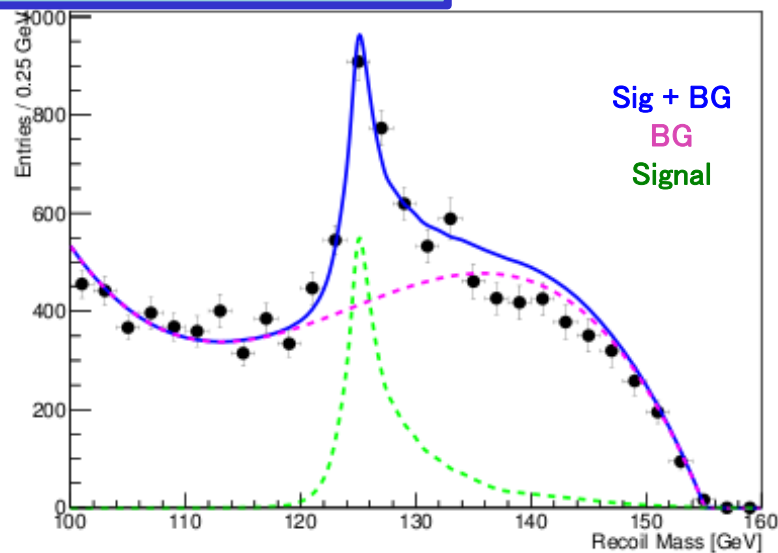


350 GeV : (+0.8, -0.3)

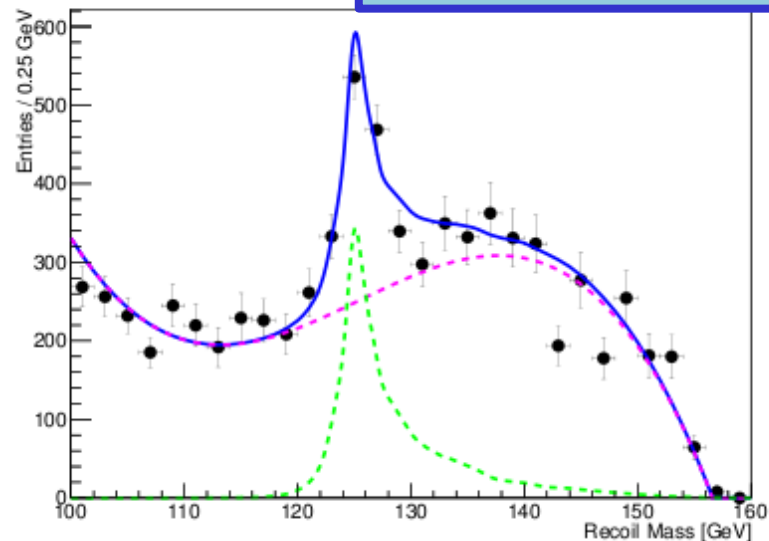


$Z \rightarrow ee$  channel

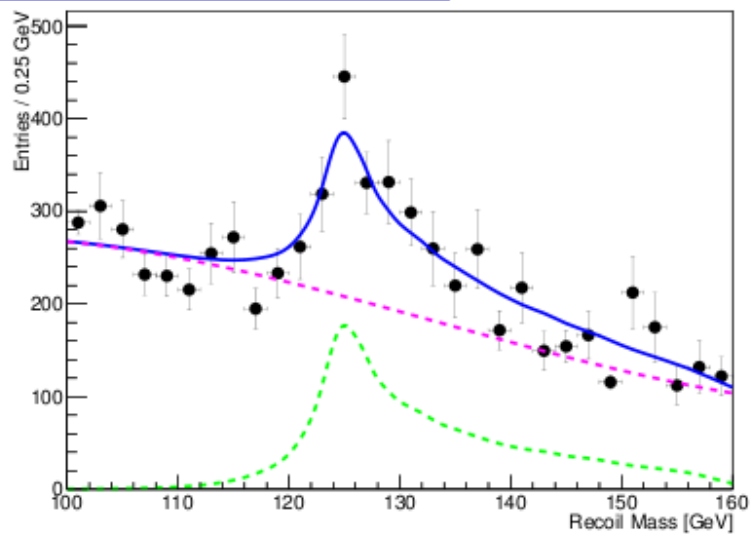
250 GeV : (-0.8, +0.3)



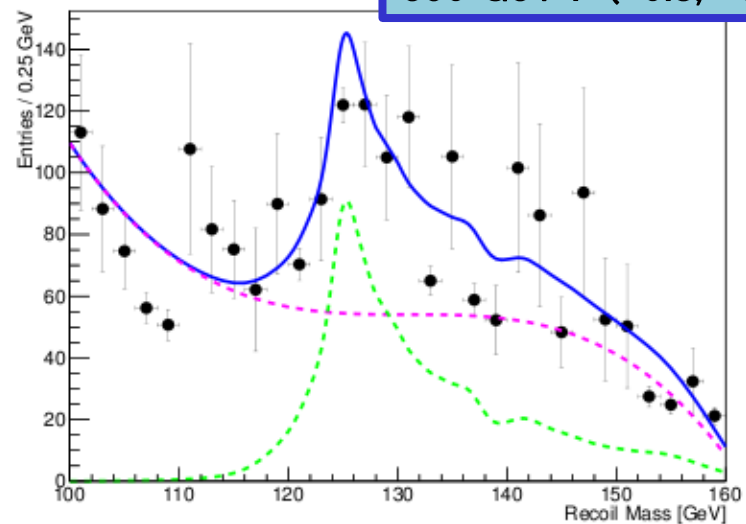
250 GeV : (+0.8, -0.3)



350 GeV : (-0.8, +0.3)



350 GeV : (+0.8, -0.3)

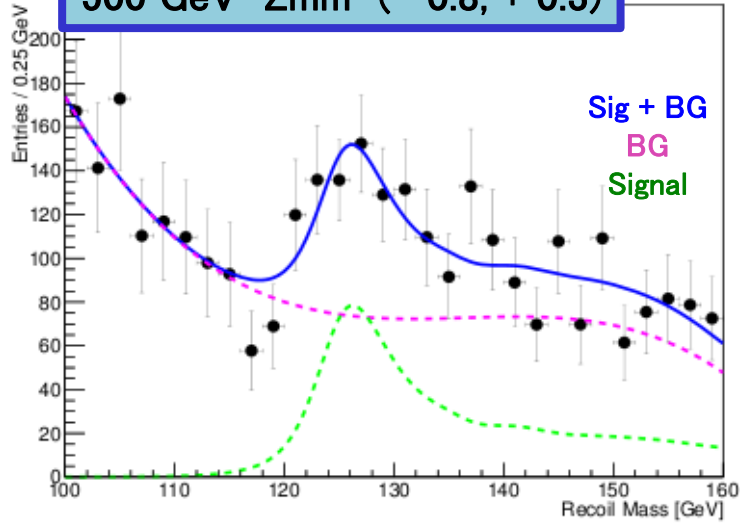




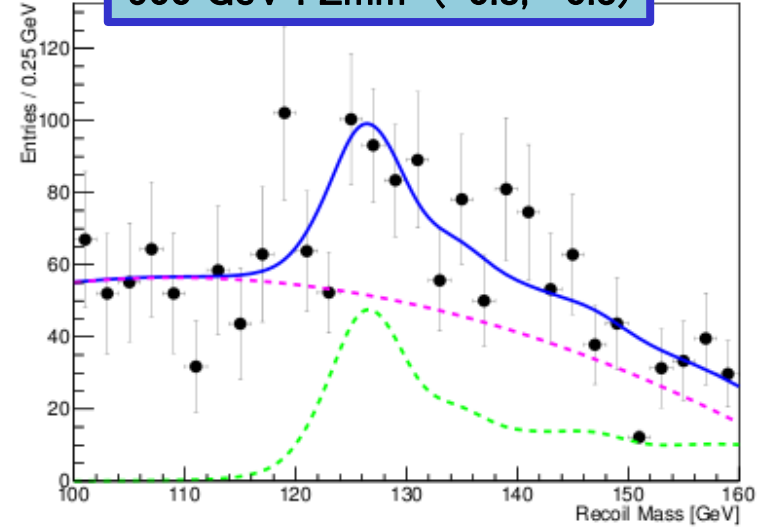
500 GeV

many challenges remaining : low statistics, low S/B ratio , ect...

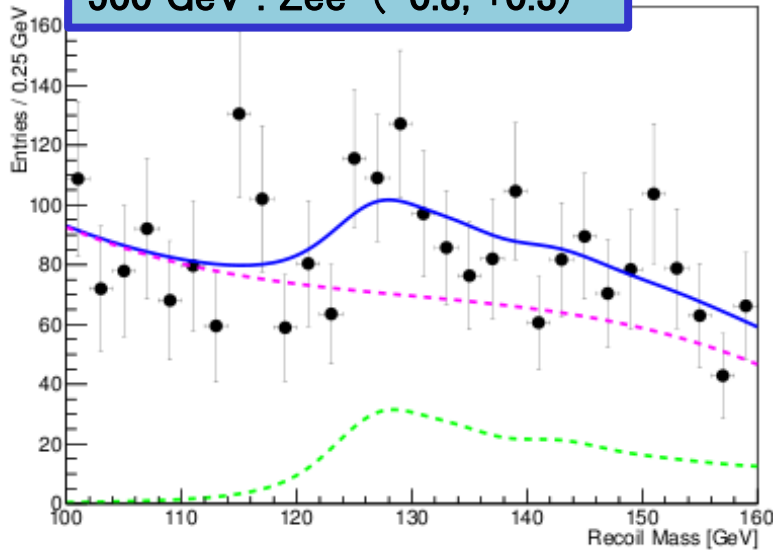
500 GeV Zmm (-0.8, +0.3)



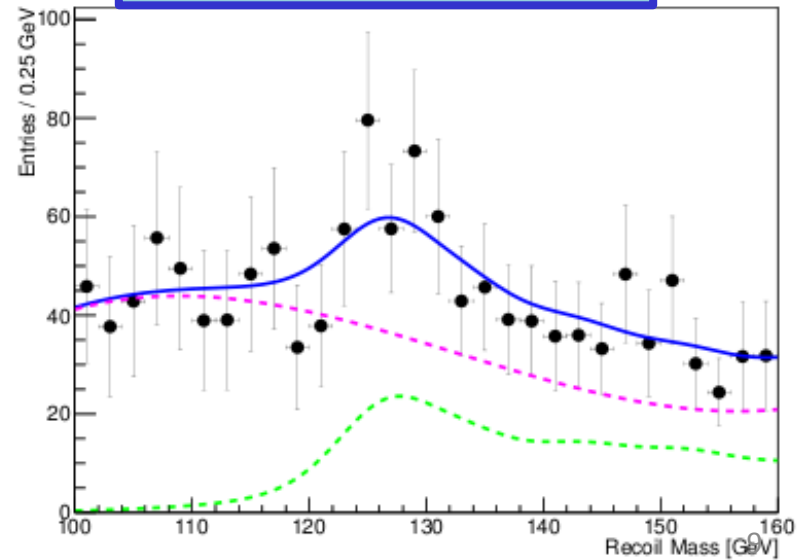
500 GeV : Zmm (+0.8, -0.3)



500 GeV : Zee (-0.8, +0.3)



500 GeV : Zee (+0.8, -0.3)

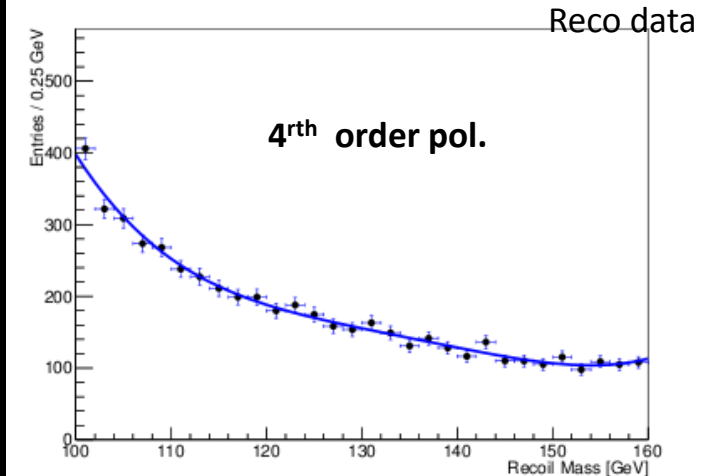
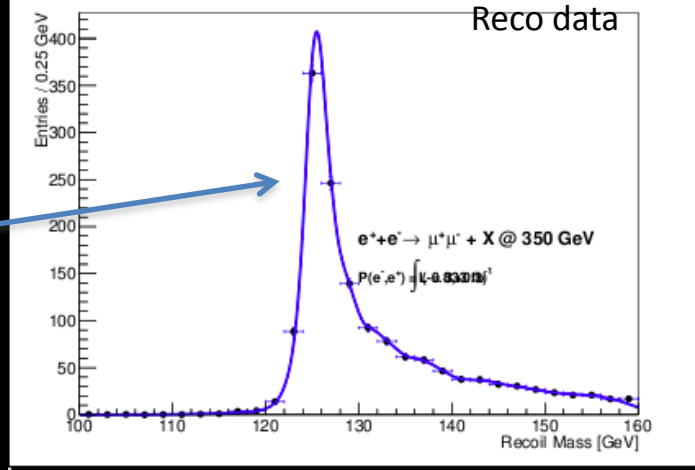


## Fitting of recoil mass spectrum

Signal : Kernel function

BG : 3<sup>rd</sup> or 4<sup>th</sup> order polynomial

Kernel function fitting does not cause significant systematic bias in recoil mass (c.f. GPET)



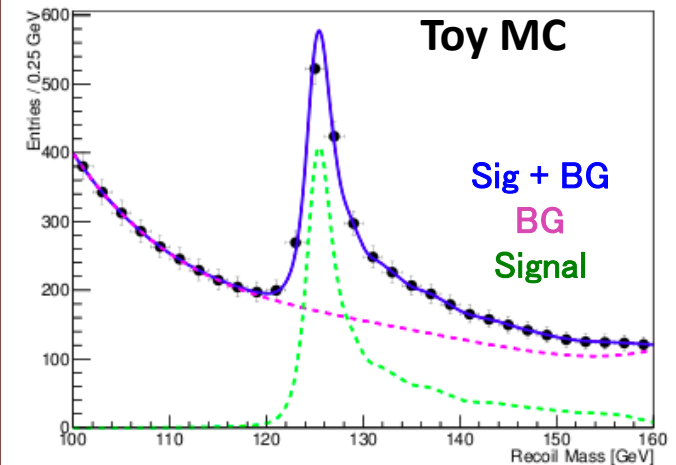
Observe distribution to determine best function for each channel

## Toy MC study

goal: test quality of fitting method  
evaluate precision of xsec and recoil mass

method:

- generate MC events with 1000 x statistics according to fitted result of “real” data
- fit Toy events with same function : Kernel + polynomial  
→ get **signal yield, mass shift, and errors**



## Statistical error study results

$Z \rightarrow \mu\mu$  and  $Z \rightarrow ee$  combined

(-0.8,+0.3)

		xsec err	mass err [MeV]
250GeV	Zmm	3.35%	40.4
	Zee	4.76%	109
	<b>Total</b>	<b>2.74%</b>	<b>37.9</b>
350GeV	Zmm	3.90%	101
	Zee	5.63%	327
	<b>Total</b>	<b>3.21%</b>	<b>96.5</b>
500GeV	Zmm	6.95%	474
	Zee	9.89%	1540
	<b>Total</b>	<b>5.69%</b>	<b>453</b>

### xsec error

- 350 GeV is 17 % worse w.r.t. 250 GeV
- 500 GeV is much worse
- Zee is worse by > 40% w.r.t. Zmm
- right hand pol is worse by 5 – 10 % w.r.t. left hand

### Mass error

- 350 GeV is worse by factor of slightly less than 3 w.r.t. 250 GeV
- Zee is worse by a factor of 2 – 3 w.r.t. Zmm
- Systematic error of fitted recoil mass is negligible (< few MeV for 250 , 350 GeV)

xsec error almost same as past results using GPET

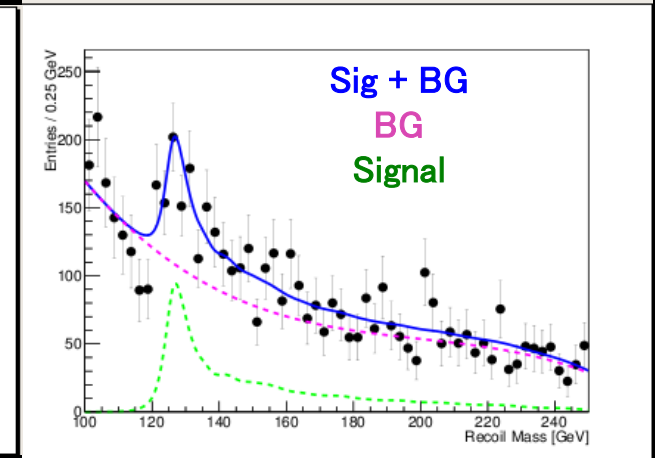
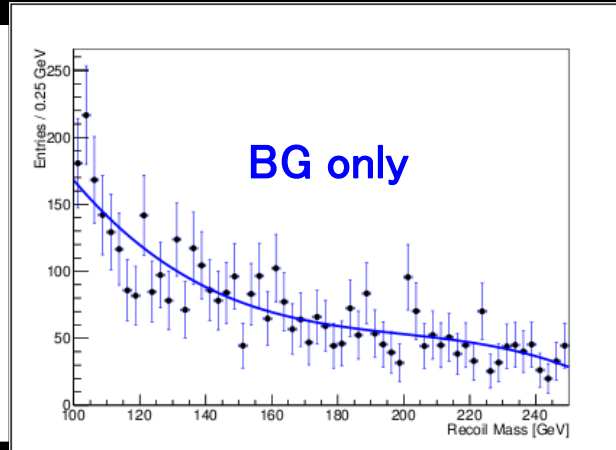
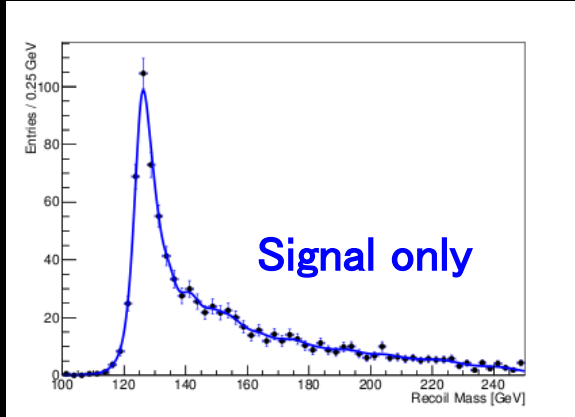
(+0.8,-0.3)

		xsec err	mass err [MeV]
250GeV	Zmm	3.57%	40.5
	Zee	5.14%	121
	<b>Total</b>	<b>2.93%</b>	<b>38.4</b>
350GeV	Zmm	4.31%	112
	Zee	6.26%	296
	<b>Total</b>	<b>3.55%</b>	<b>105</b>
500GeV	Zmm	8.36%	613
	Zee	9.85%	1510
	<b>Total</b>	<b>6.37%</b>	<b>568<sup>11</sup></b>

Can precision can be slightly improved if we fit over a wider range ?  
 assuming we can neglect the  $H^* \rightarrow WW$  bump beyond 160 GeV

500 GeV, Zee (-0.8,+0.3)

fit in 100 – 250 GeV (c.f. 100-160 GeV)



xsec error (%)

mass error (MeV)

(-0.8,+0.3)

narrow

wide

narrow

wide

500GeV

Zmm

6.95%

6.50%

474

468

Zee

9.89%

7.86%

1540

1540

**Total**

**5.69%**

**5.01%**

**453**

**448**

(+0.8,-0.3)

500GeV

Zmm

8.36%

7.27%

613

572

Zee

9.85%

7.86%

1510

1530

**Total**

**6.37%**

**5.33%**

**568**

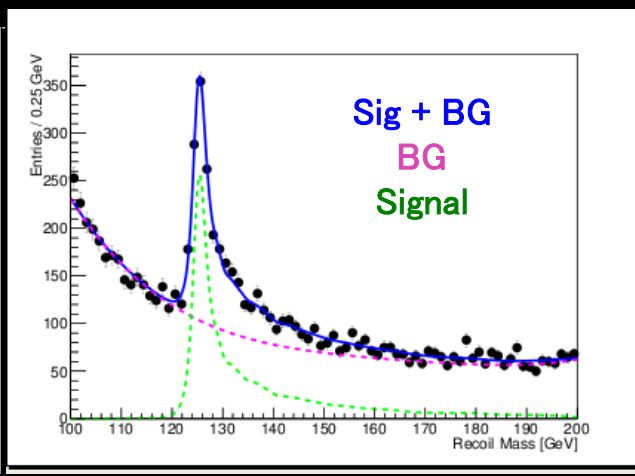
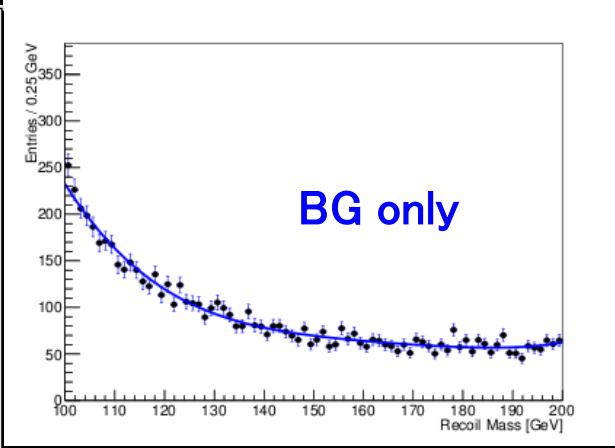
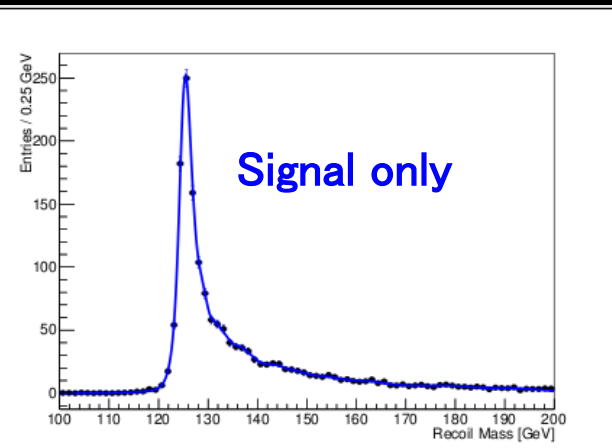
**536**

**10-20 %  
 improvement on  
 xsec and a few %  
 on mass precision**

Can precision can be slightly improved if we fit over a wider range ??  
 assuming we can neglect the  $H^* \rightarrow WW$  bump beyond 160 GeV

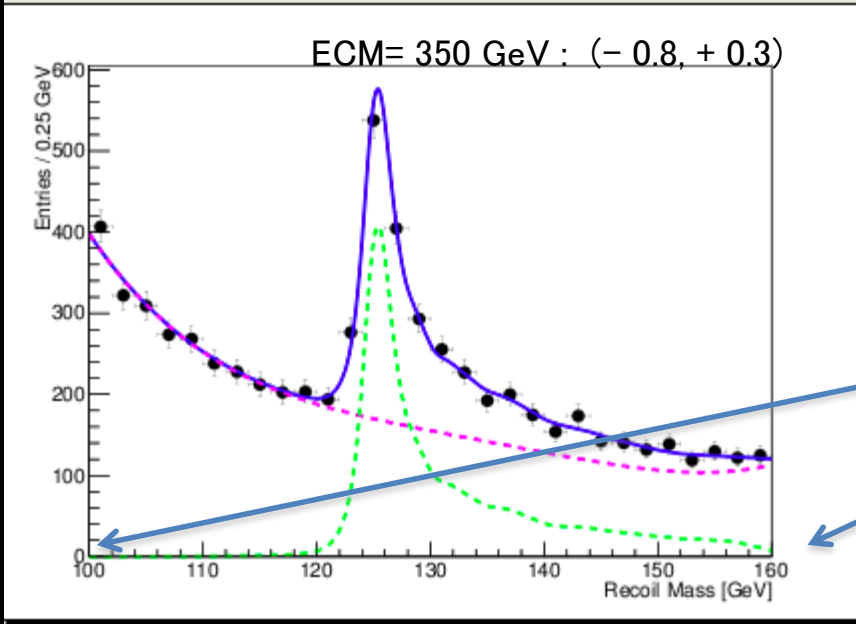
350 GeV, Zee (-0.8,+0.3)

fit in 100 – 200 GeV (c.f. 100-160 GeV)



		xsec error (%)		mass error (MeV)	
(-0.8,+0.3)		narrow	wide	narrow	wide
350GeV	Zmm	3.90%	3.83%	101	103
	Zee	5.63%	5.48%	327	340
	<b>Total</b>	<b>3.21%</b>	<b>3.14%</b>	<b>96.5</b>	<b>98.6</b>
(+0.8,-0.3)		narrow	wide	narrow	wide
350GeV	Zmm	4.31%	4.24%	112	113
	Zee	6.26%	6.15%	296	328
	<b>Total</b>	<b>3.55%</b>	<b>3.49%</b>	<b>105</b>	<b>107</b>

Not much room for improvement



**BG level fluctuation is controlled by fitting recoil mass over a wide range (100 – 160 GeV)**

*an improvement from previous studies*

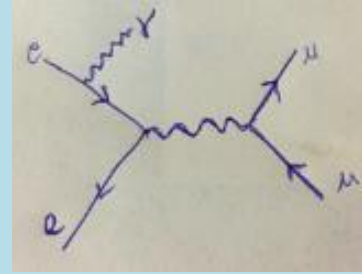
- BG level is usually fixed for Toy MC (optimistic scenario)
- **xsec error is about 10 % worse if we float BG** (pessimistic scenario)  
not a big degradation since I fit recoil mass spectrum over a wide range

**GOOD**

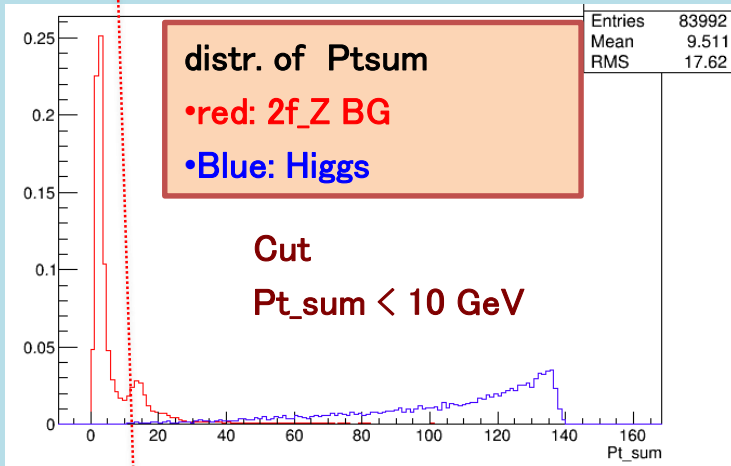
*Example:*

Zmm	xsec	Recoil mass	BG fluc
250GeV	3.35% → 3.62%	40 MeV, no change	1.23%
350GeV	3.90% → 4.39%	101 → 95 MeV	1.67%

# Prevention of signal bias i.e. Higgs decay mode dependence



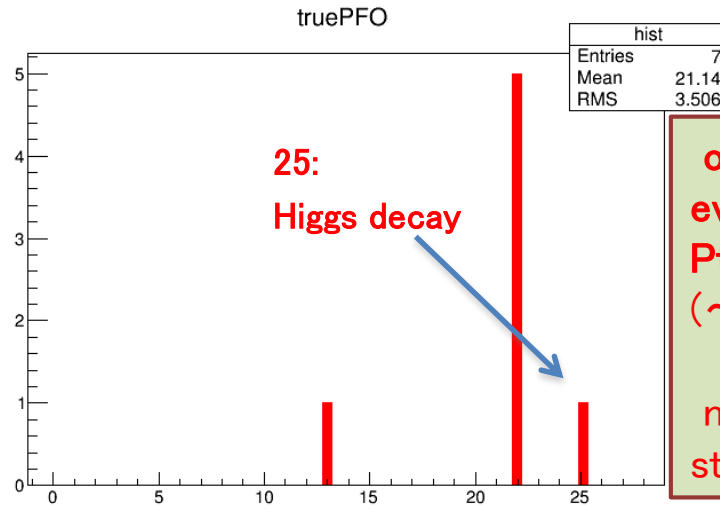
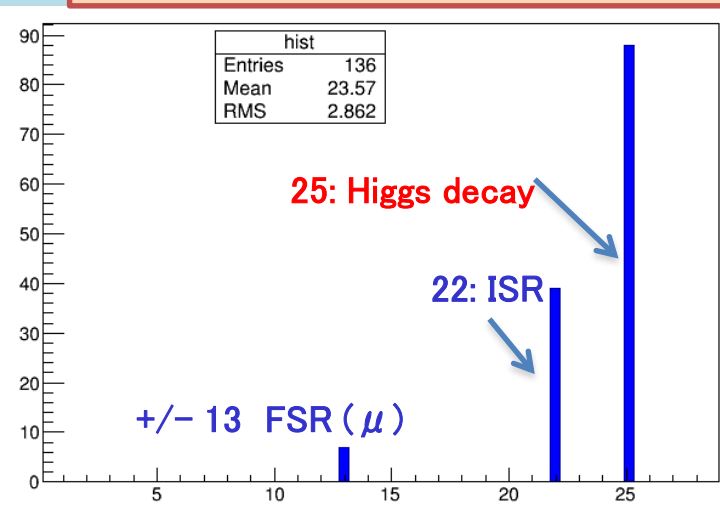
- the “traditional”  $d_{ptbal} (= |P_{t,dl}| - |P_{t,\gamma}|)$  cut for removing 2f BG ( $\gamma$  back-to-back w.r.t. di-lepton) caused signal bias (esp.  $H \rightarrow \tau\tau, \gamma\gamma$ )



**NEW #1** isolated photon finder:  $\gamma$  we look at have small cone energy) not from Higgs decay

**NEW #2** Now use  $\left| \vec{P}_{t,sum} \right| \circ \left| \vec{P}_{t,g} + \vec{P}_{t,dl} \right|$  (instead of  $d_{ptbal}$ )  
vector direction info singles out back to back events

## PDG of $\gamma$ for events removed by $P_{tsum} / d_{ptbal}$ cut (250 GeV $Z_{mm}$ )



only < few unweighed events removed by  $P_{tsum}$  cut ( $\sim 0$  weighed events)

negligible compared to statistical uncertainties

$\sim 100$  Higgs decay related  $\gamma$  events removed by  $d_{ptbal}$  cut !!

need more careful study of Higgs decay mode bias using high stat sample

Higgs recoil study using  $e^+e^- \rightarrow ZH \rightarrow l+l-H$  ( $l = \mu / e$ )

@ ECM = 250 , 350 , 500 GeV

## Summary

studied impact of ECM and polarization on model – independent measurement of ZH xsec

- contributes to deciding ILC run scenario and detector design optimization

**Study has made progress since previous general meeting  
converging towards a full set of study results**

< Preliminary results >

(both leptonic channels combined)

250 GeV: (-0.8, +0.3)  $\Delta\sigma / \sigma = 2.7\%$   $\Delta M = 38$  MeV      (+0.8, -0.3)  $\Delta\sigma / \sigma = 2.9\%$   $\Delta M = 38$  MeV

350 GeV: (-0.8, +0.3)  $\Delta\sigma / \sigma = 3.2\%$   $\Delta M = 97$  MeV      (+0.8, -0.3)  $\Delta\sigma / \sigma = 3.5\%$   $\Delta M = 105$  MeV

500 GeV: (-0.8, +0.3)  $\Delta\sigma / \sigma = 5.7\%$   $\Delta M = 453$  MeV      (+0.8, -0.3)  $\Delta\sigma / \sigma = 6.4\%$   $\Delta M = 568$  MeV

- signal bias is minimized i.e. prevent Higgs decay mode dependence
- negligible systematic error due to fitting method

### xsec precision :

- ECM= 350 GeV worse by 17% w.r.t. 250 GeV
- Zee worse by > 40% w.r.t. Zmm
- right pol worse by 5-10% w.r.t. left pol.

### Higgs mass precision:

- ECM=350 GeV worse by factor of < 3 w.r.t. ECM = 250 GeV
- Zee worse by factor of 2 -3 w.r.t. Zmm

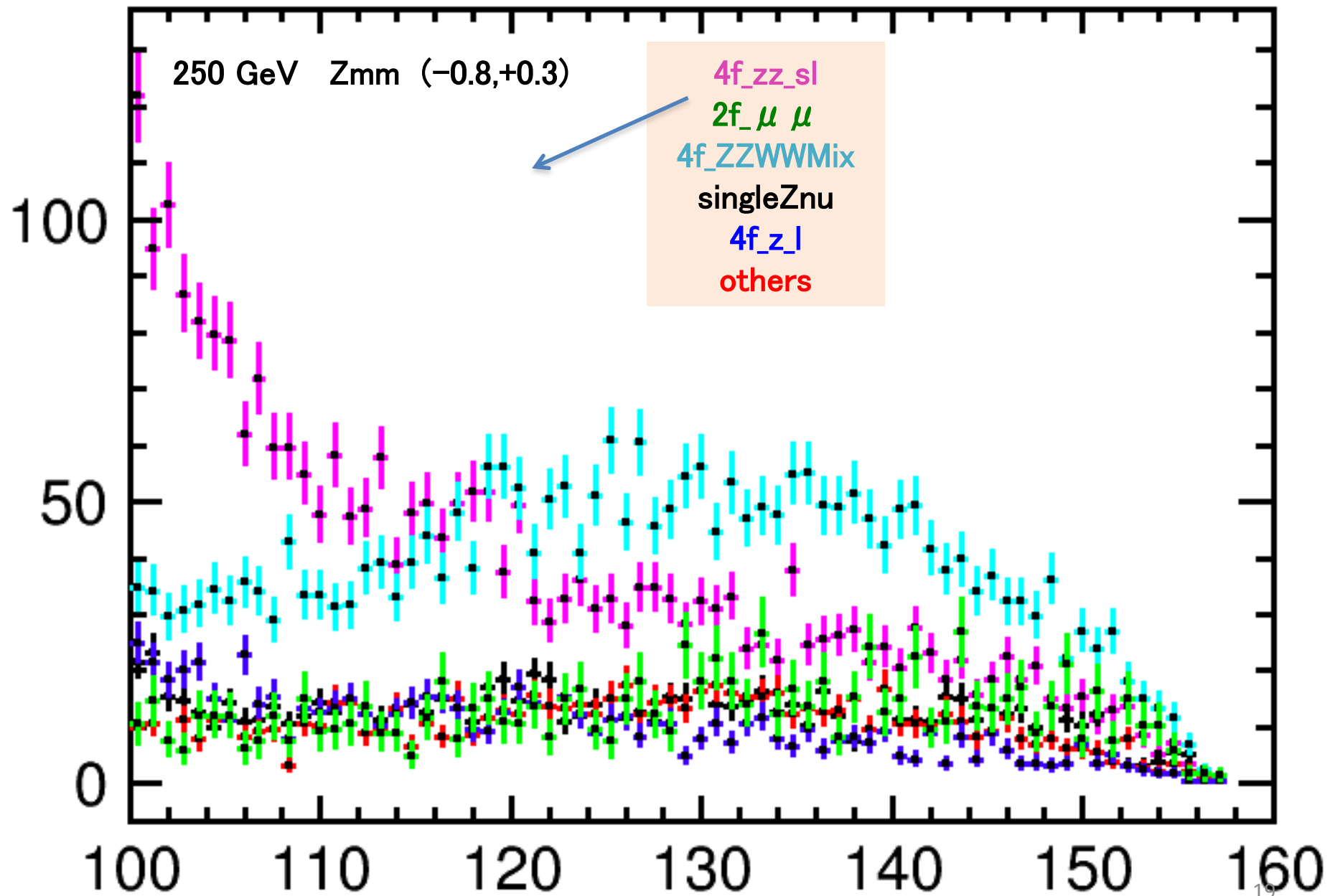
Note : extrapolated results (TDR) for 250 GeV : xsec error 2.6%,  $\Delta M = 32$  MeV  
methods are slightly different, hard to directly compare

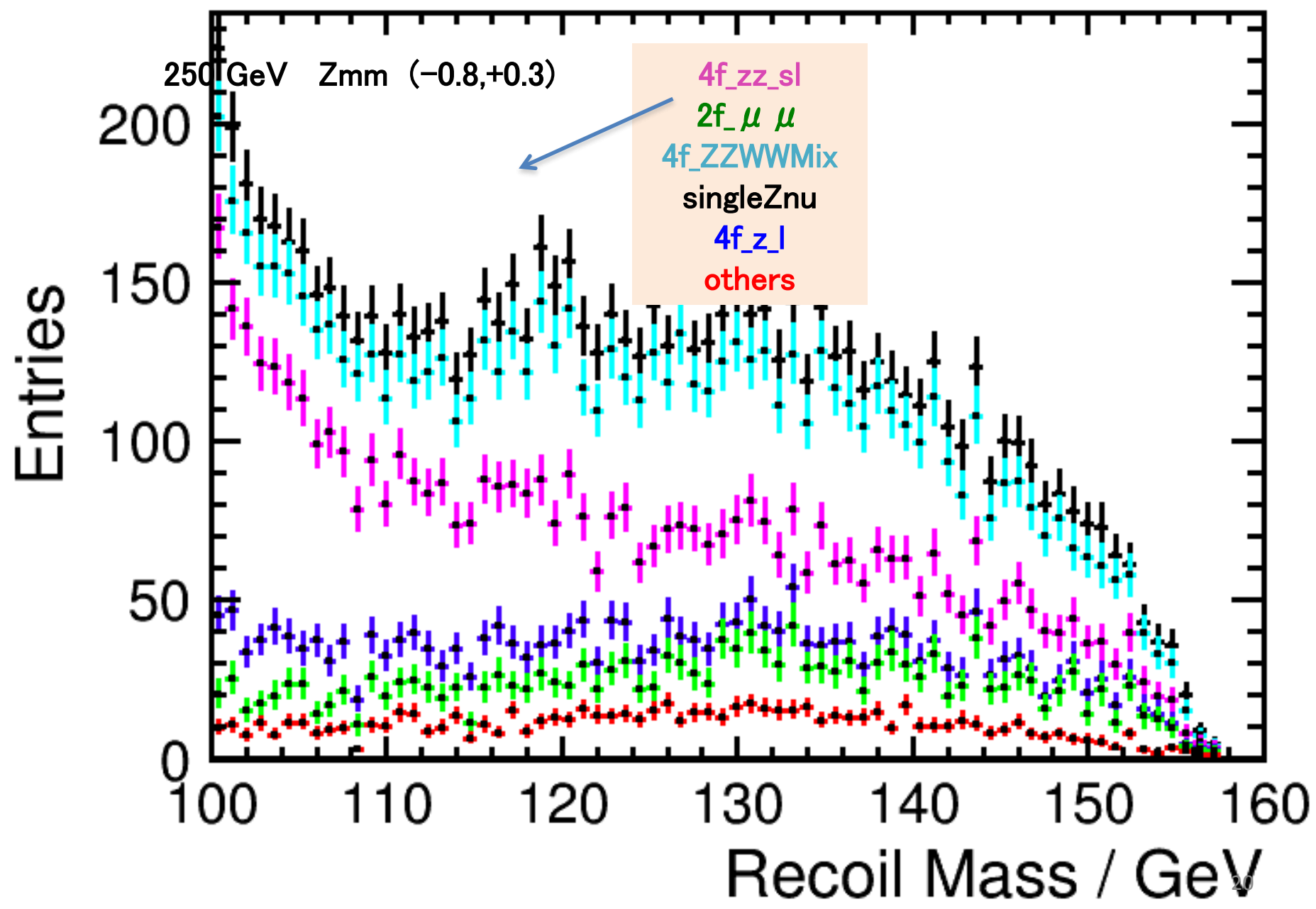


## Plans and Goals

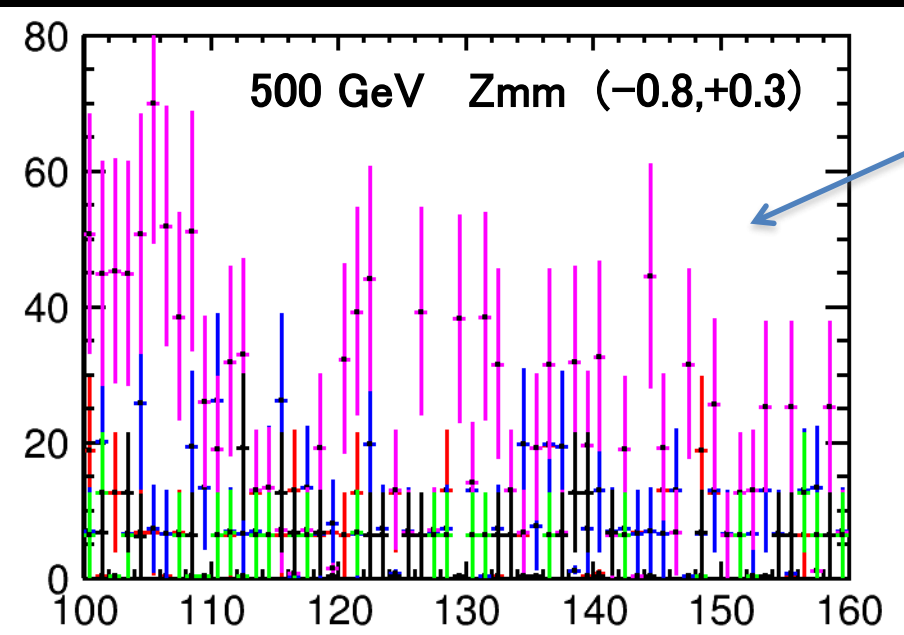
- ❖ **analysis using higher MC statistics sample**  
→ deeper investigations of systematic errors
- ❖ **ZZ fusion analysis (Zee mode)**
- ❖ **semi-model independent analysis:**  
separate Higgs visible and invisible decay modes.  
→ this will suppress the major BG  $ll \nu \nu$   
expect improvement in xsec precision

# BACKUP



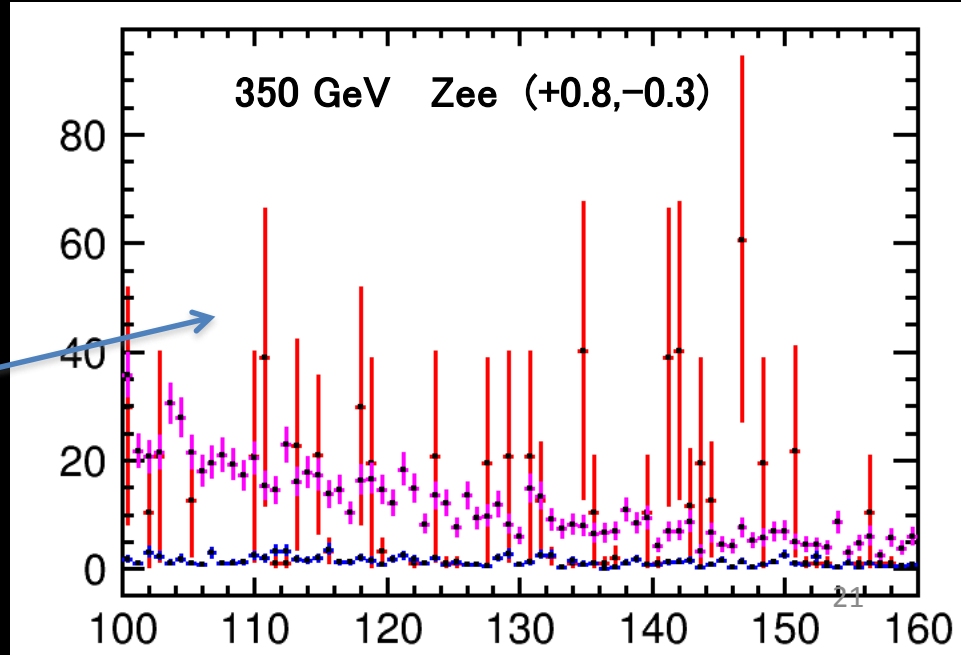


**Dominant BG with low MC statistics cause large errorbars**  
**(a technical problem planned to be solved by generating higher statistics samples)**

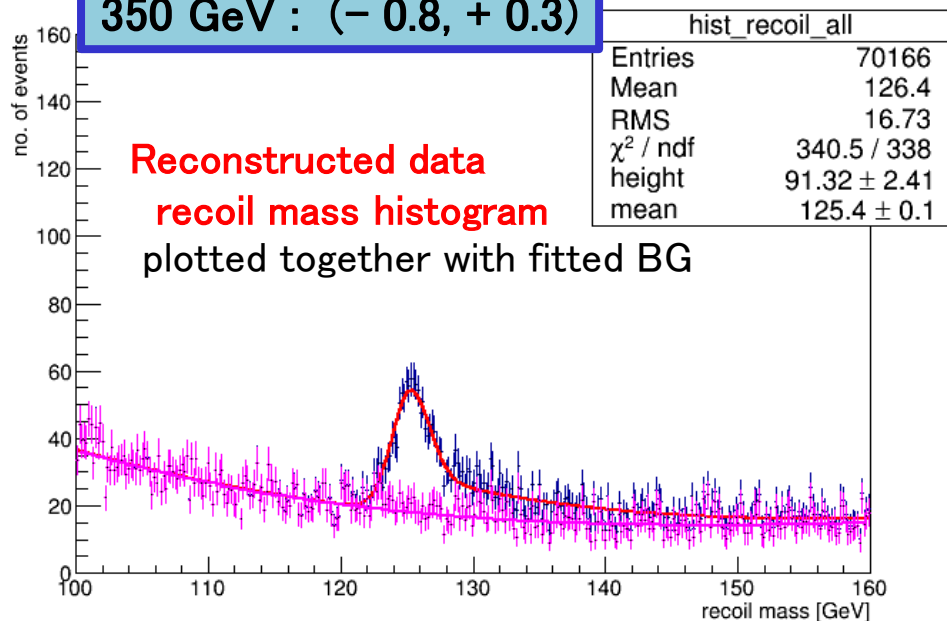


4f\_zz\_sl  
2f\_μ μ  
singleZnu  
others

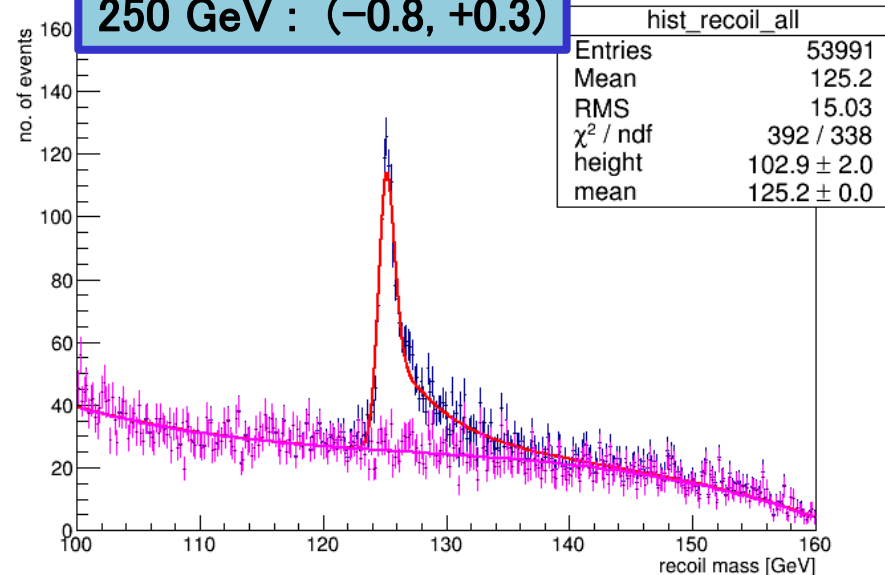
2f\_bhabhag  
4f\_singleZe  
others



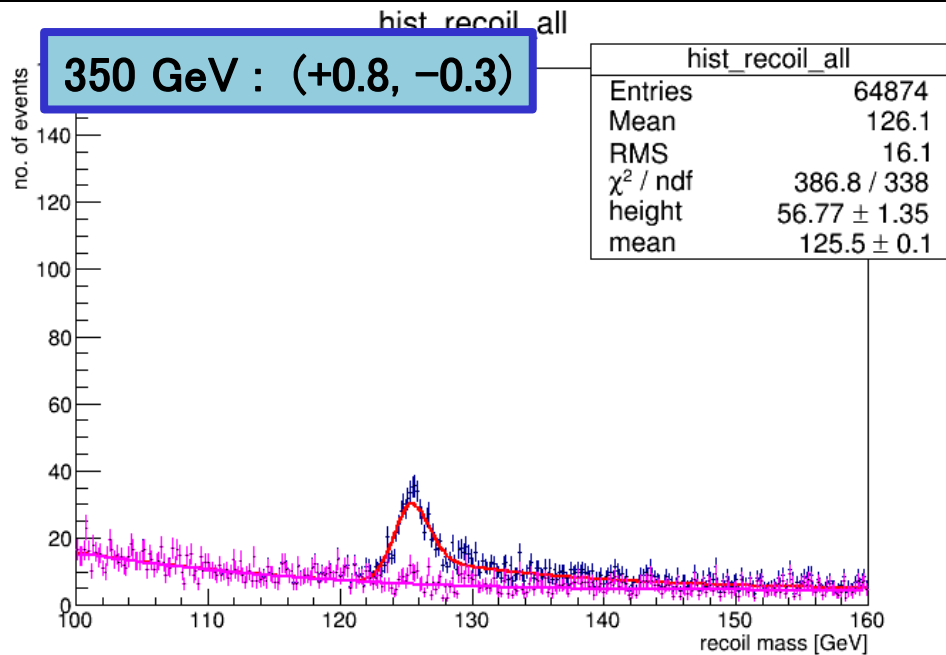
350 GeV : (-0.8, +0.3)



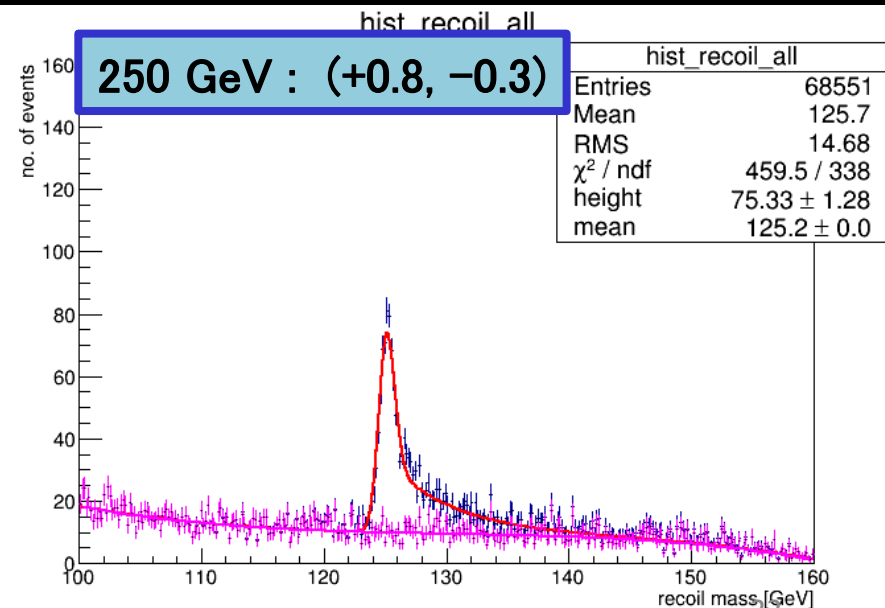
250 GeV : (-0.8, +0.3)



350 GeV : (+0.8, -0.3)



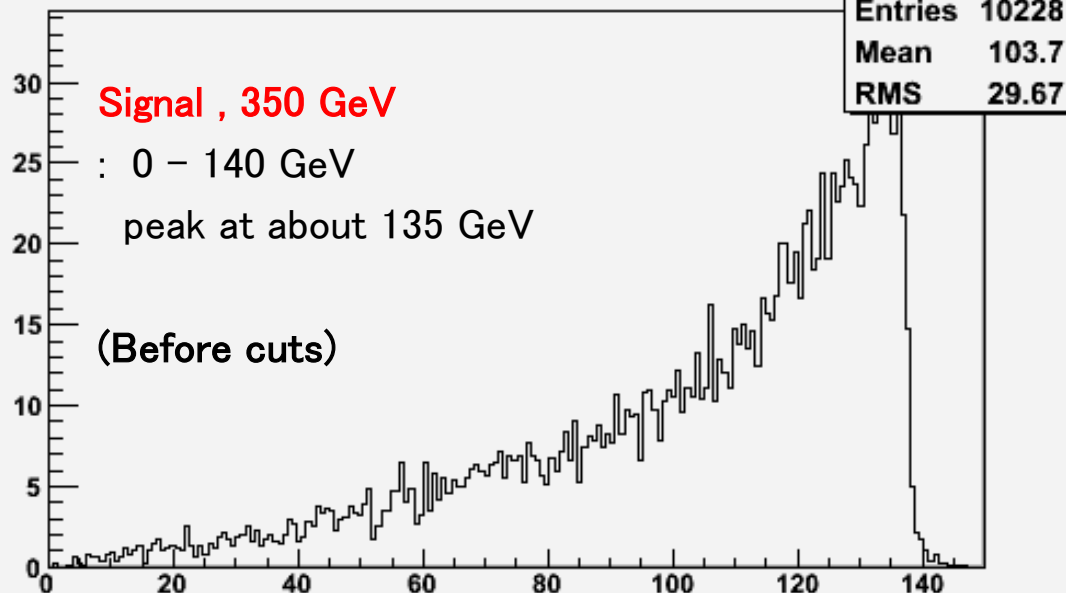
250 GeV : (+0.8, -0.3)



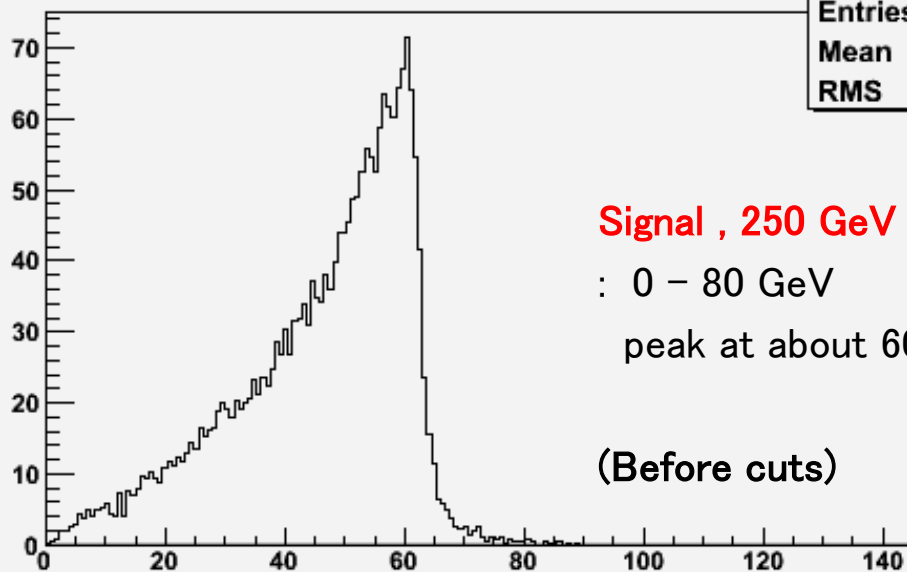
## dilepton PT, 350 GeV

do cut :  
 $10 \text{ GeV} < p_{T\_dl} < 140 \text{ GeV}$

hist\_pt\_jackieZH\_higgs\_ffh\_Pe2e2h\_eL\_pR



hist\_pt\_jackieZH\_higgs\_ffh\_Pe2e2h\_eL\_pR



## Pe2e2h\_eL.pR & Pe2e2h\_eR.pL

- 4f\_ZZ\_leptonic
- 4f\_ZZ\_semileptonic
- 2f\_Z\_leptonic
- 4f\_WW\_leptonic
- 4f\_WW\_semileptonic
- 4fSingleZee\_leptonic
- 4fSingleZnunu\_leptonic
- 4f\_ZZWWMix\_leptonic
- 6f backgrounds ( $\sqrt{s}=350$  GeV)

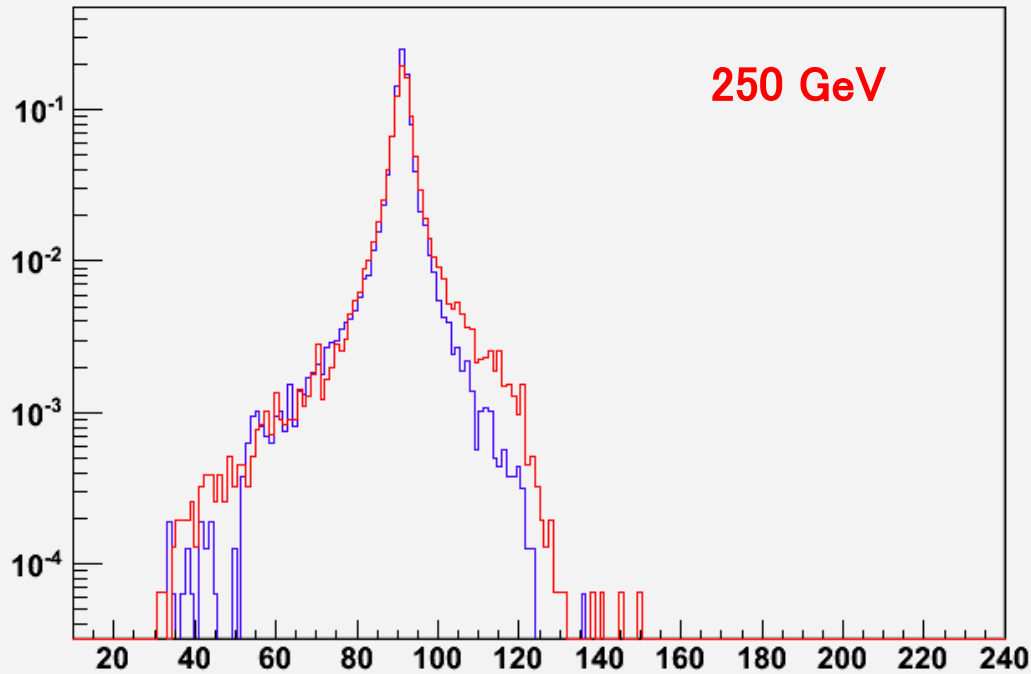
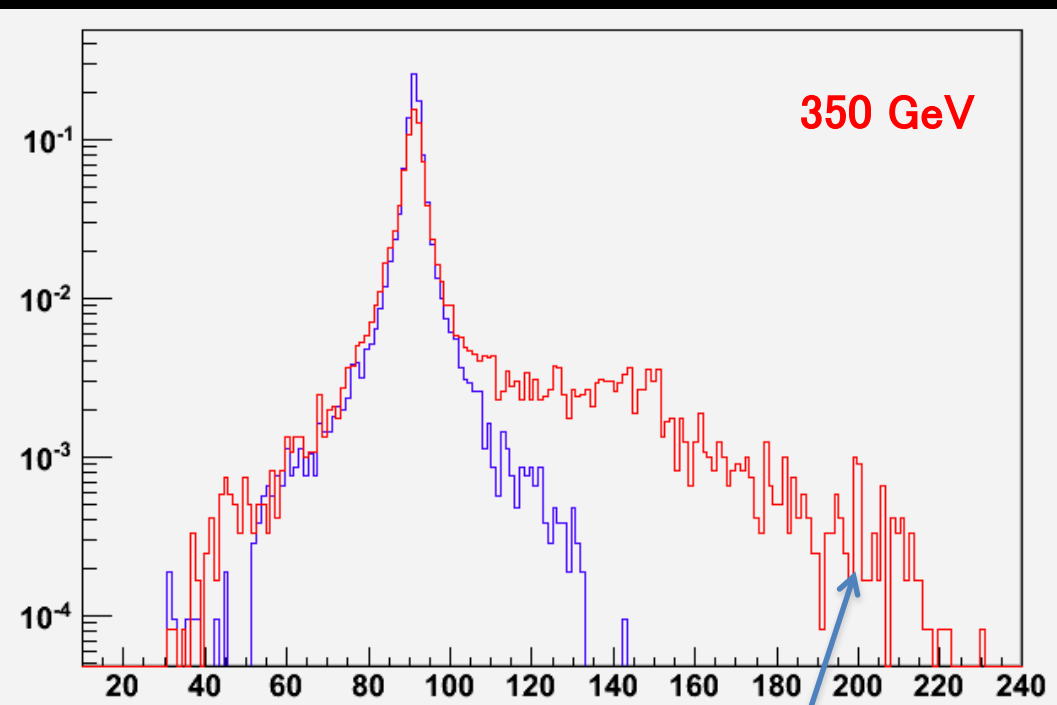
note that difference from past studies maybe sue to:

- assumed L (350, 250 GeV) = (333 , 250 fb<sup>-1</sup>) vs RDR: (300 fb<sup>-1</sup>, 188 fb<sup>-1</sup>)
- this analysis include all 2f, 4f, 6f BGs (whizard generator) vs only WW, ZZ (pythia generator ?)

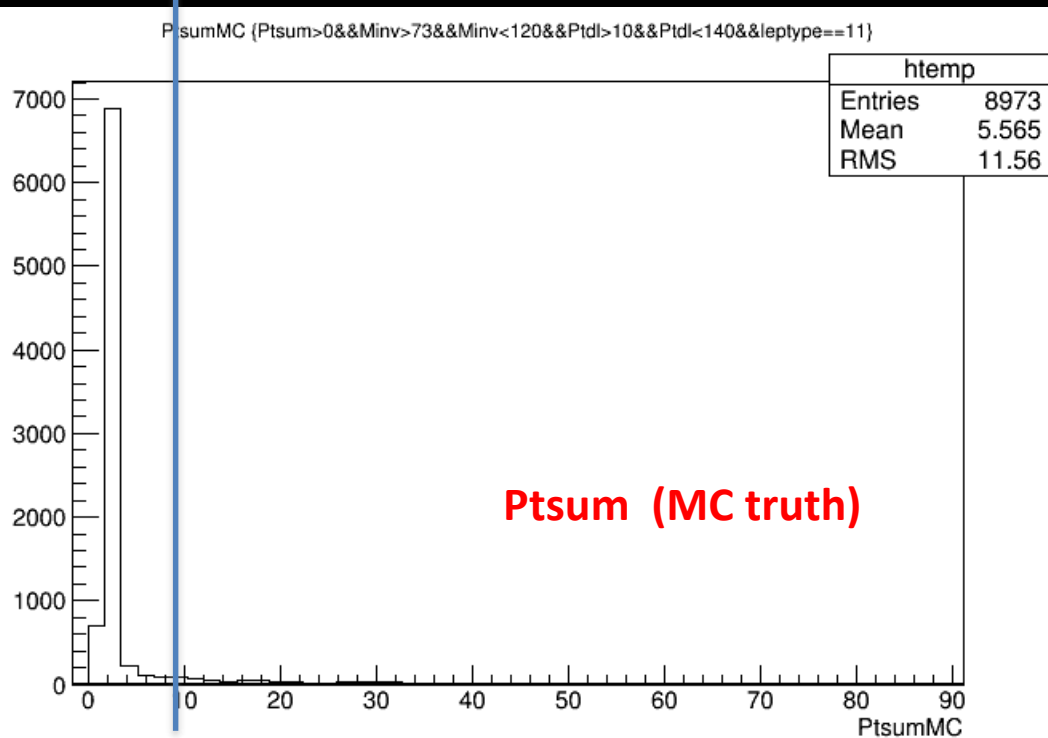
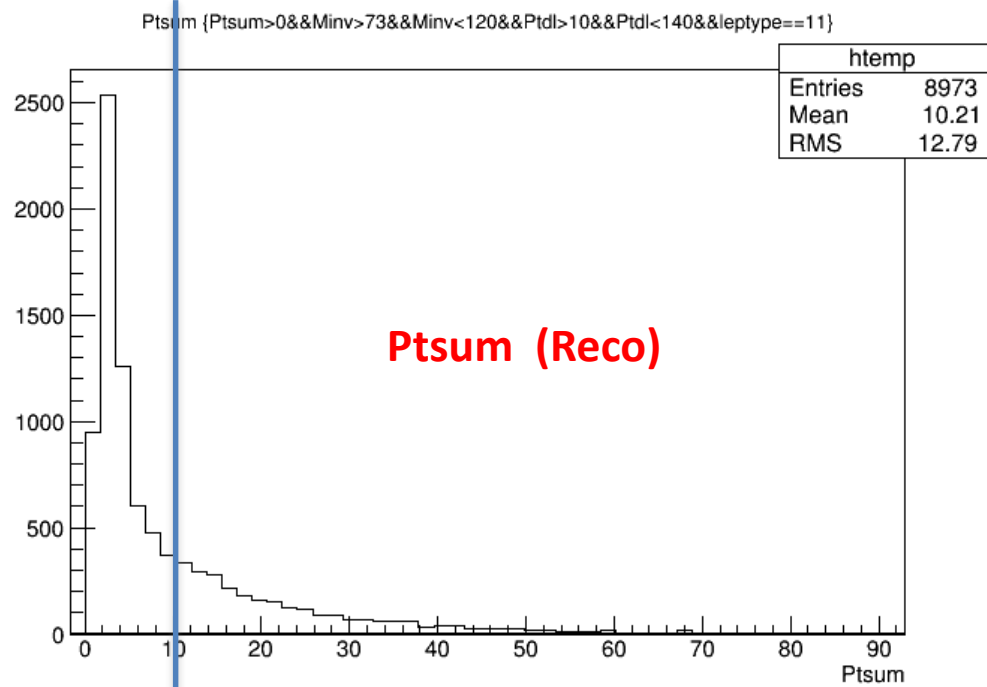


# compare dilepton invariant mass distribution

**Zee (red)**  
vs **Zmumu (blue)**



- Zmumu much sharper
- Zee has a long tail towards large inv. Mass (ZZ fusion)
- Broader width due to bremsstrahlung (partially recovered)



events before Ptsum cut

2f\_bb

Realized a large difference in Ptsum between Reconstructed particles and MC Truth

Ptsum is formed from sum of vectors !!

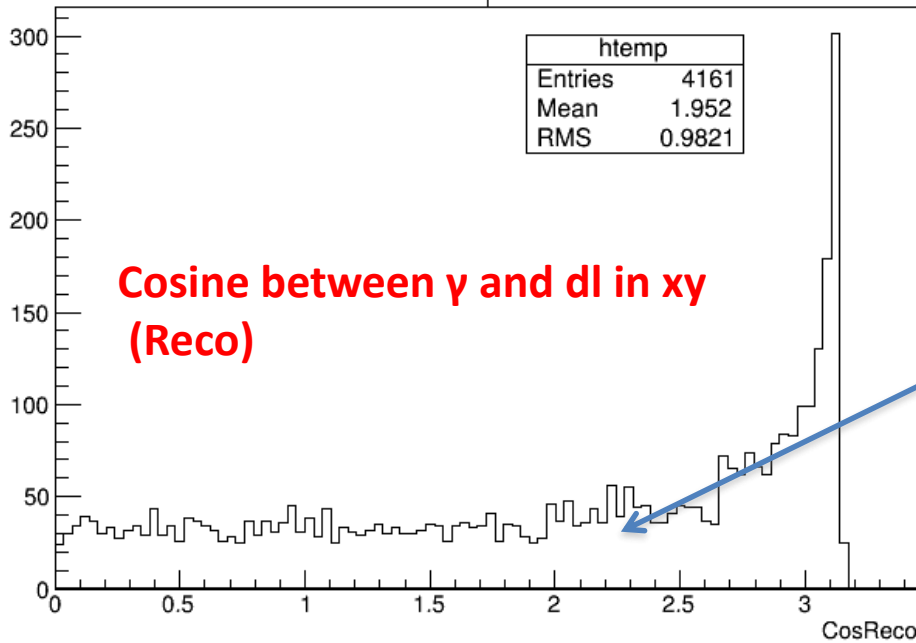
Ptdl should be near zero if no brem  
If one lepton emits brem and loses energy,

Pt\_dl will increase

→ long Ptsum tail

→ Ptsum cut loses power

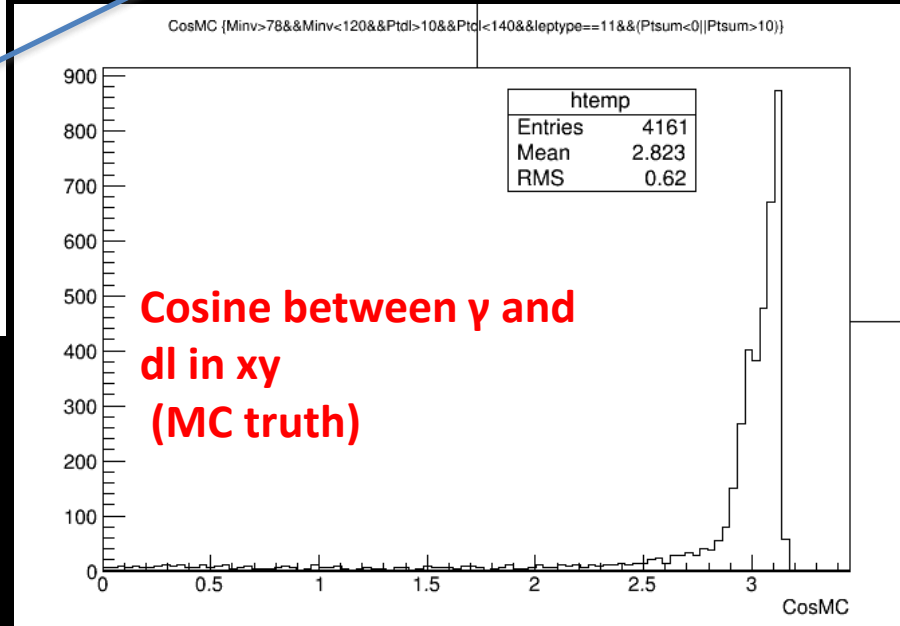
CosReco {Minv>78&&Minv<120&&Ptdl>10&&Ptdl<140&&leptype==11&&(Ptsum<0)|(Ptsum>10)}



**MC truth is much more back-to-back (as expected)**

**How to explain the long isotropic tail for Reco ?**

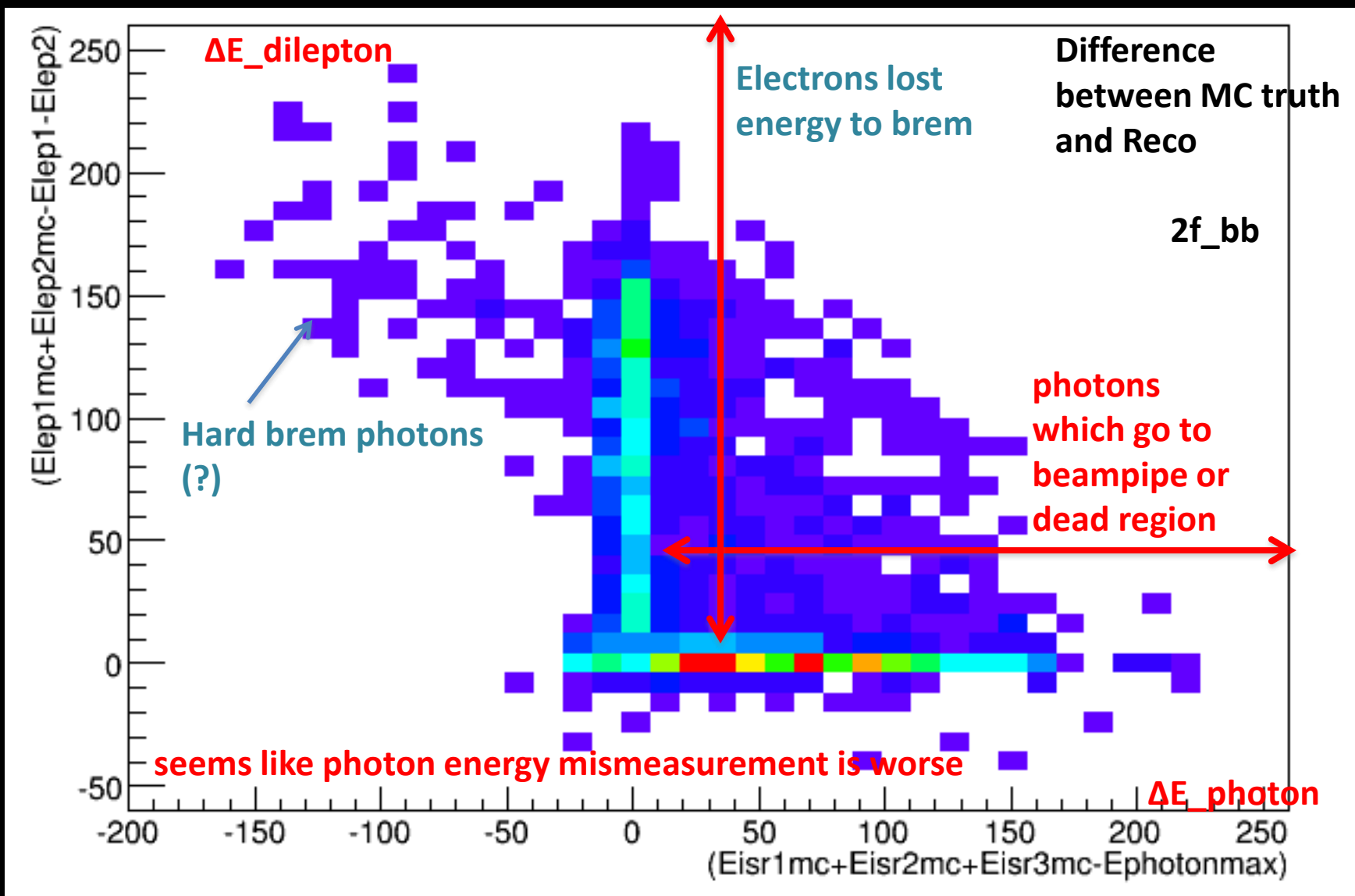
**Cosine between  $\gamma$  and dl in xy (MC truth)**



**There are a few potential explanations**

**From here on we will investigate the reason for the non-back-to-back ness**

**especially the long isotropic tail**

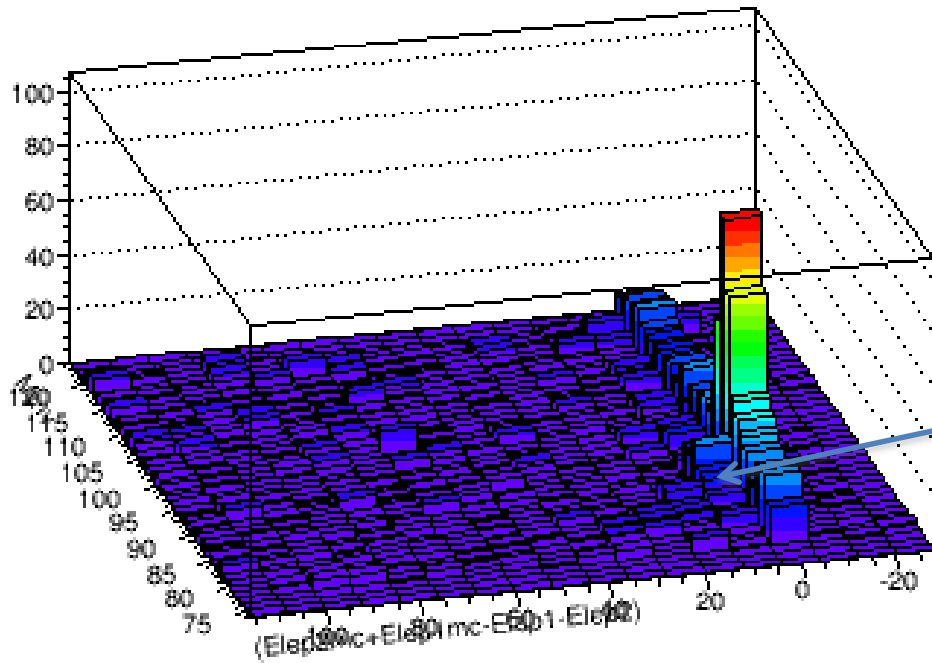


energy mis-measurements explain ONLY A PART of discrepancy in non - BTB ness

- leptons lose energy due to brem
- Photons go very forward to beampipe or dead regions of detector

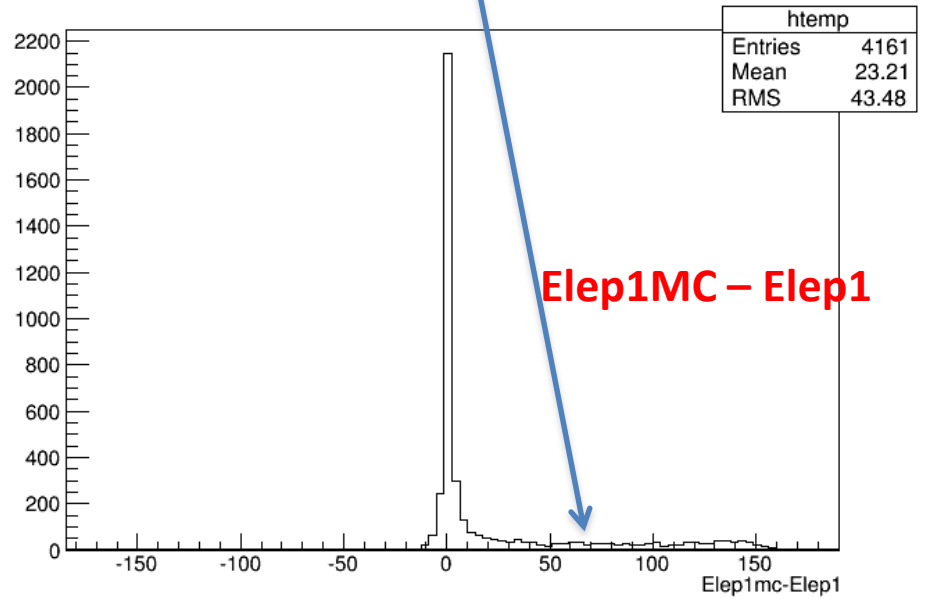
Other parts : angle resolution (?), More than 1 hard ISR photon (still needs confirmation)

(Elep2mc-Elep1-Elep2)Minv>78&&Minv<120&&Ptdl>10&&Ptdl<140&&leptype==11&&(Ptsum<0)|Ptsum>10)



Events which emit brem  
contribute to lower Minv  
tail

Elep1mc-Elep1 (Minv>78&&Minv<120&&Ptdl>10&&Ptdl<140&&leptype==11&&(Ptsum<0)|Ptsum>10)

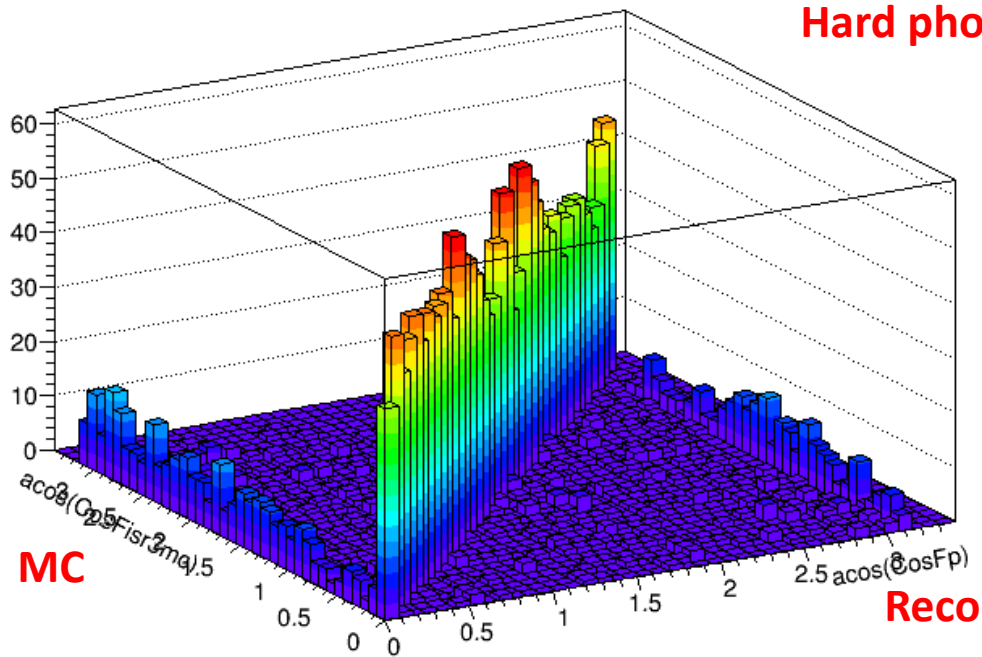


Elep1MC - Elep1

$\text{acos}(\text{CosFis3mc}) : \text{acos}(\text{CosFp})$  (Minv>78&&Minv<120&&Ptdl>10&&Ptdl<140&&leptype==11&&(Psum<0)|(Psum>10)&&Psum>0)

Hard photon

Angle  $\phi$  in x-y plane

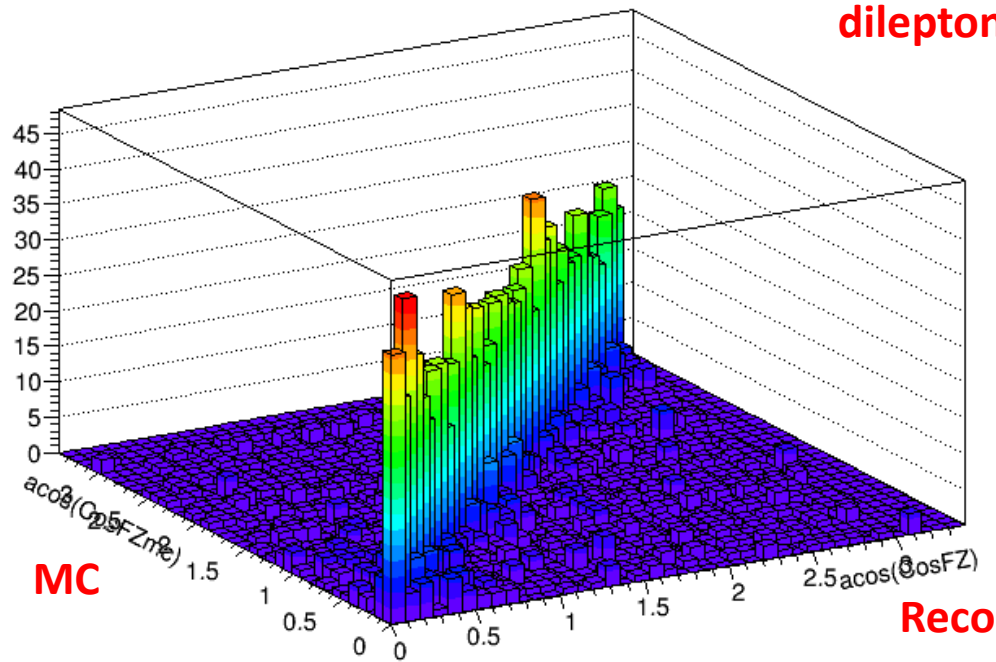


MC

Reco

$\text{acos}(\text{CosFZ})$  (Minv>78&&Minv<120&&Ptdl>10&&Ptdl<140&&leptype==11&&(Psum<0)|(Psum>10)&&Psum>0)

dilepton



MC

Reco

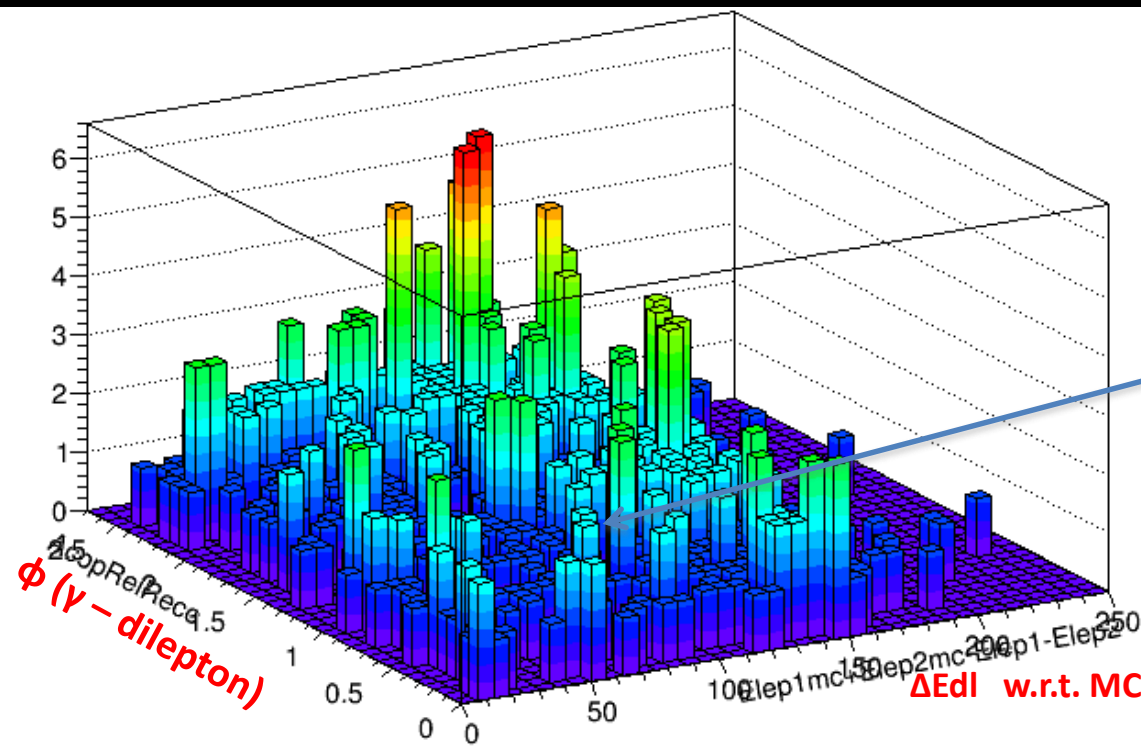
Angle precision seems not too bad for lepton and photon

(photon slightly worse)

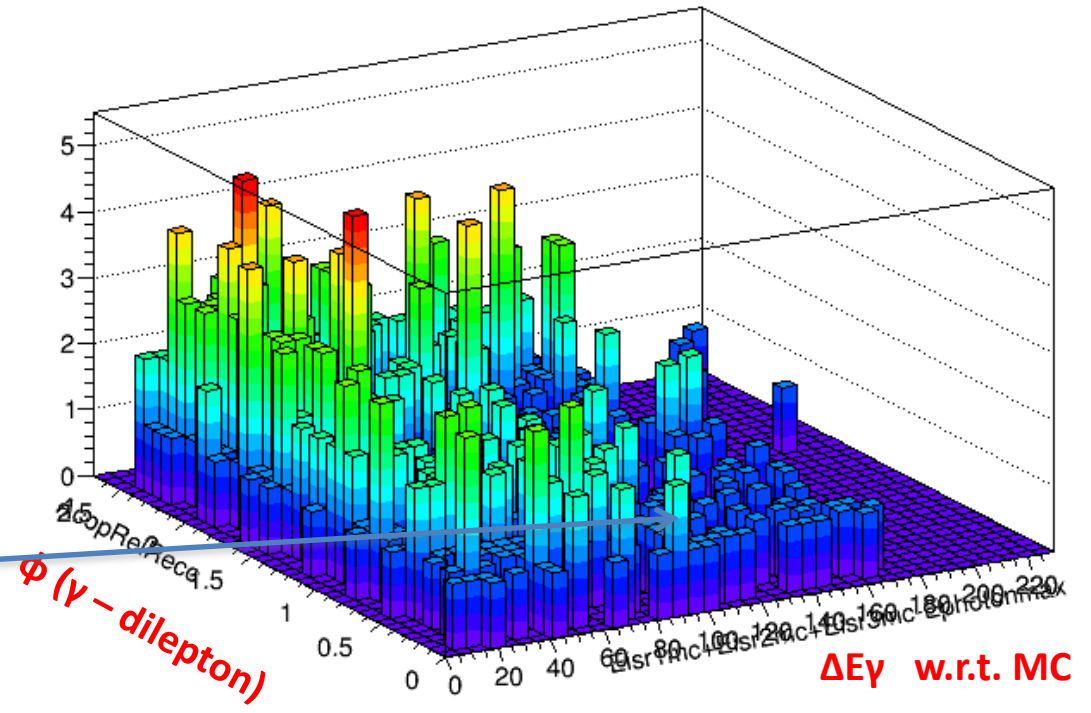
Only events with non-"back-to-back" ness (angle < 2.5 rad)

Not well measured dilepton energy: 60%

brems explains part of non-"BTB"

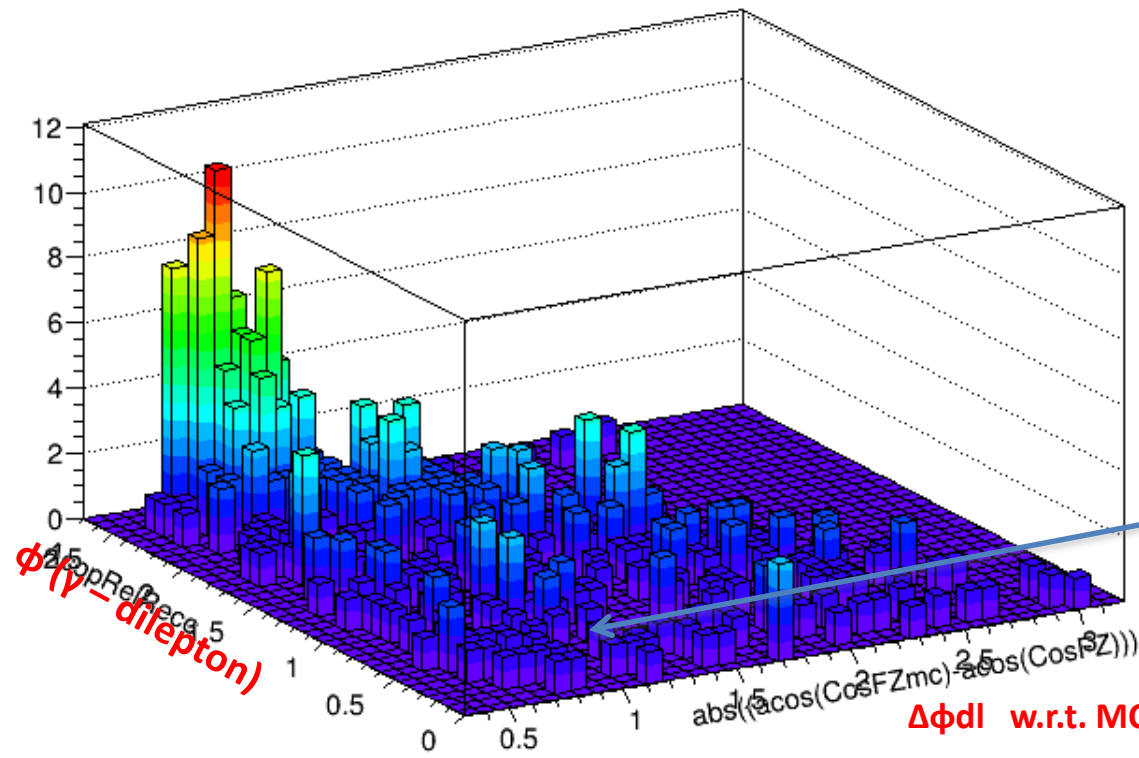


Not well measured  $\gamma$  energy: 55%

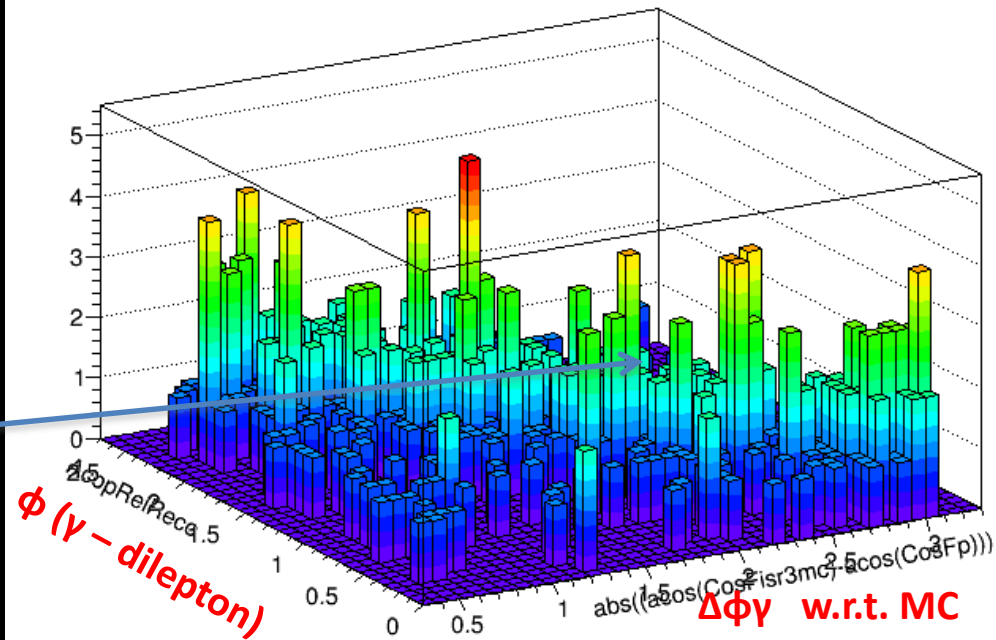


Only events with non-"back-to-back" ness (angle < 2.5 rad)

Not well measured dilepton angle : 40%



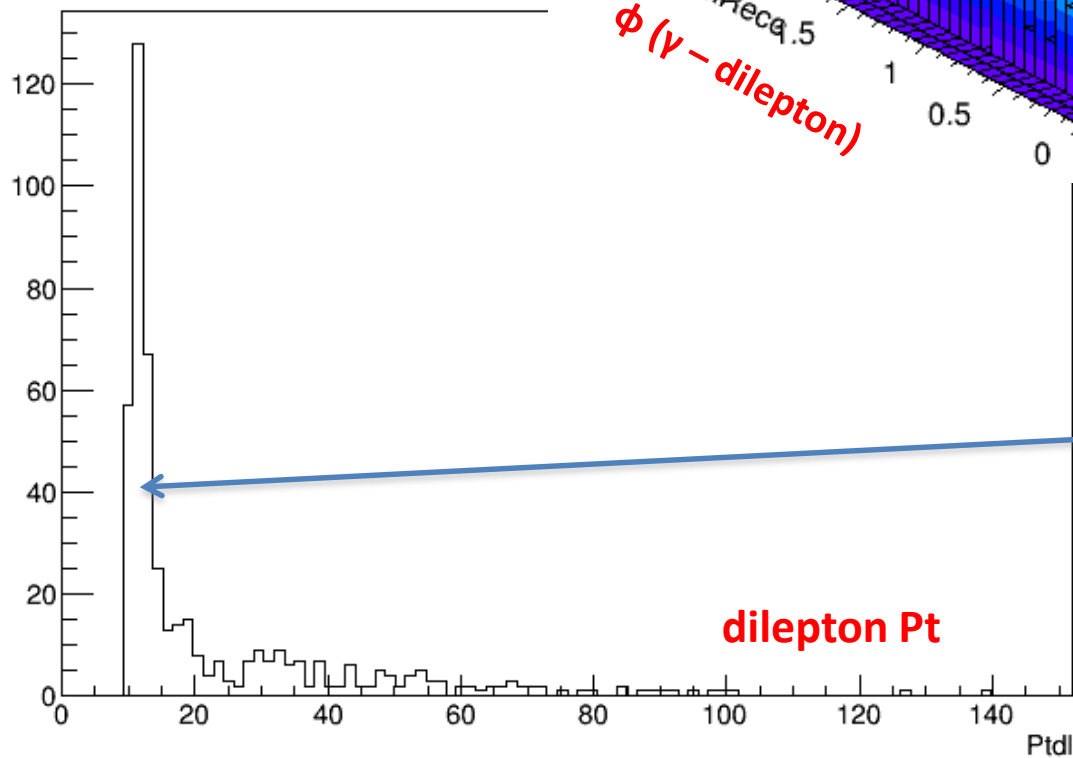
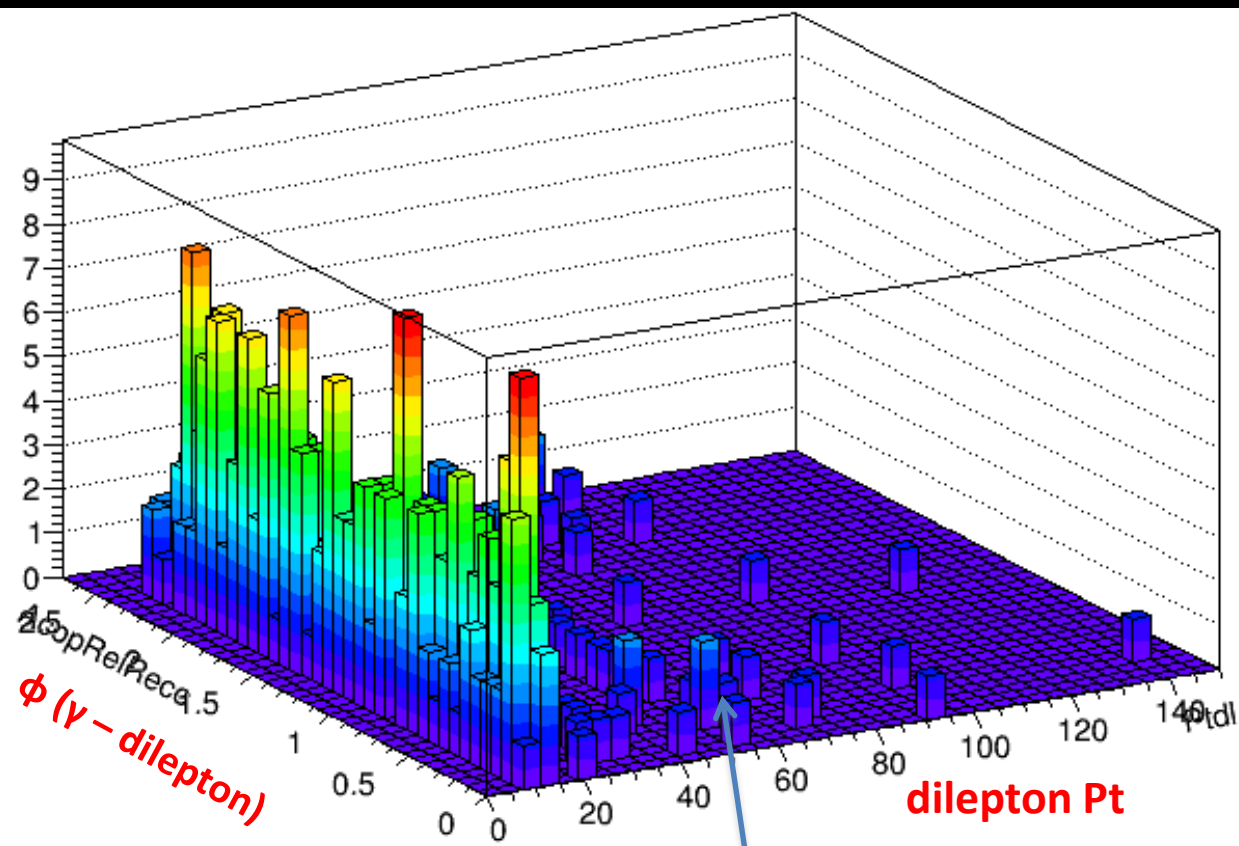
Not well measured  $\gamma$  angle : 45%





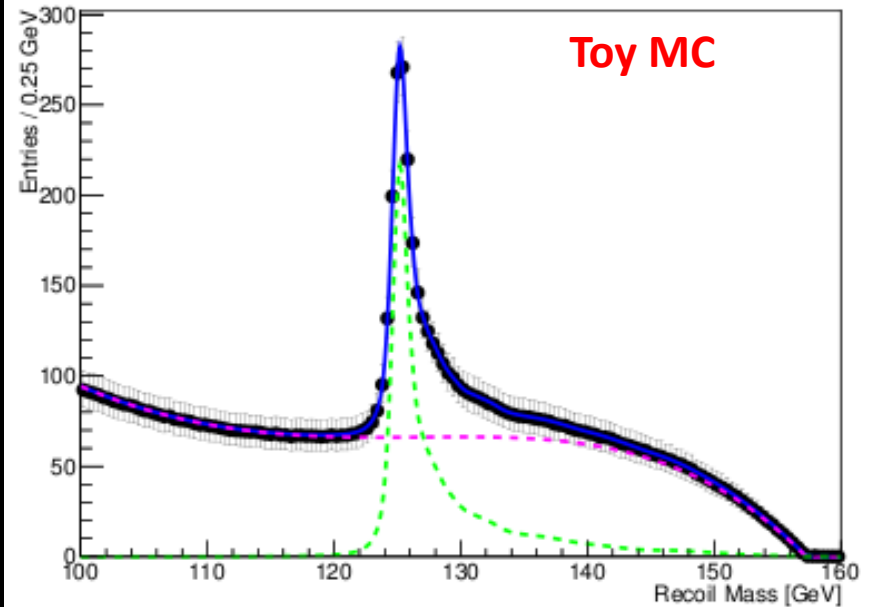
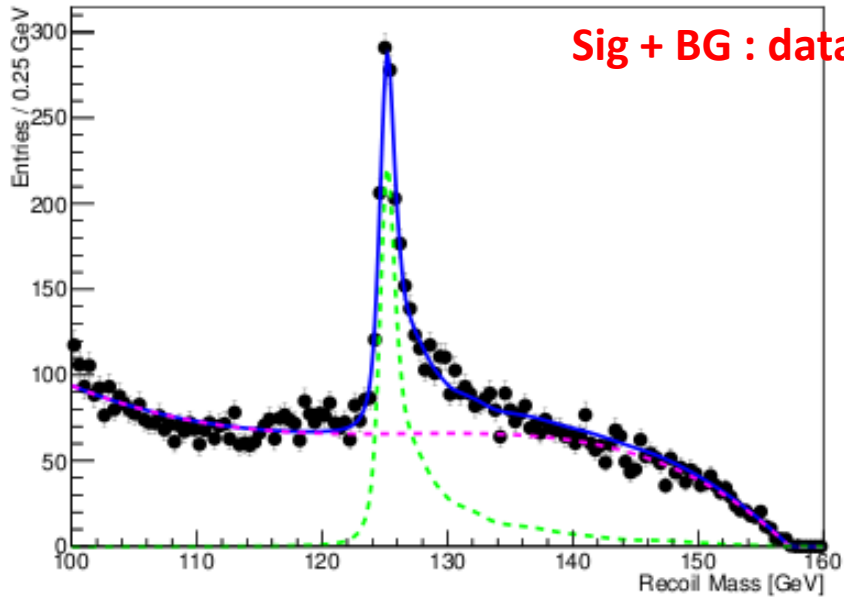
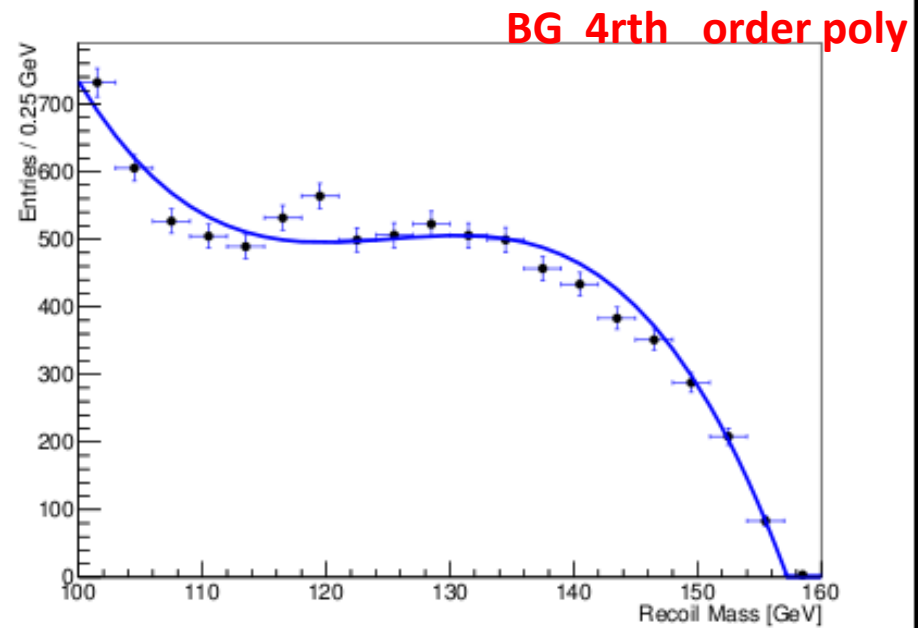
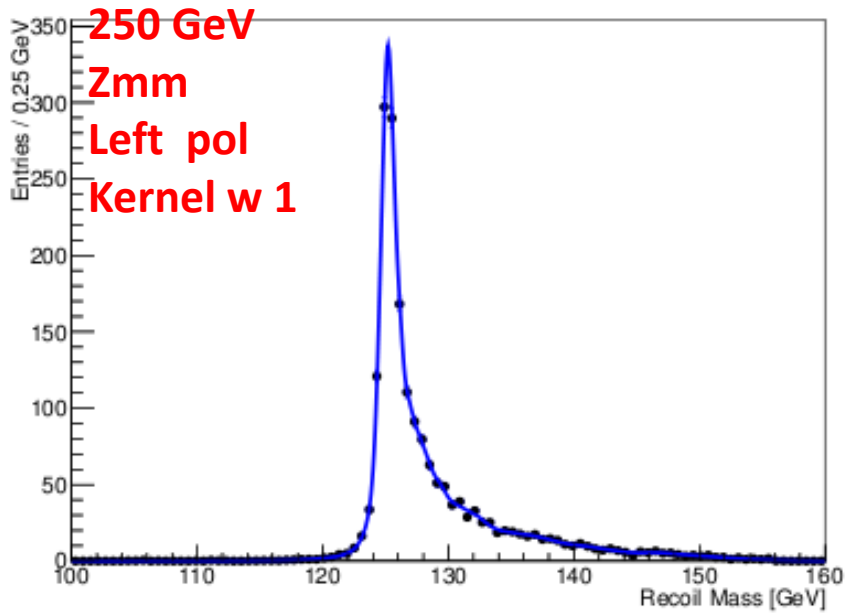
events with non-"back-to-back"ness (angle  $< 2.5\text{rad}$ )

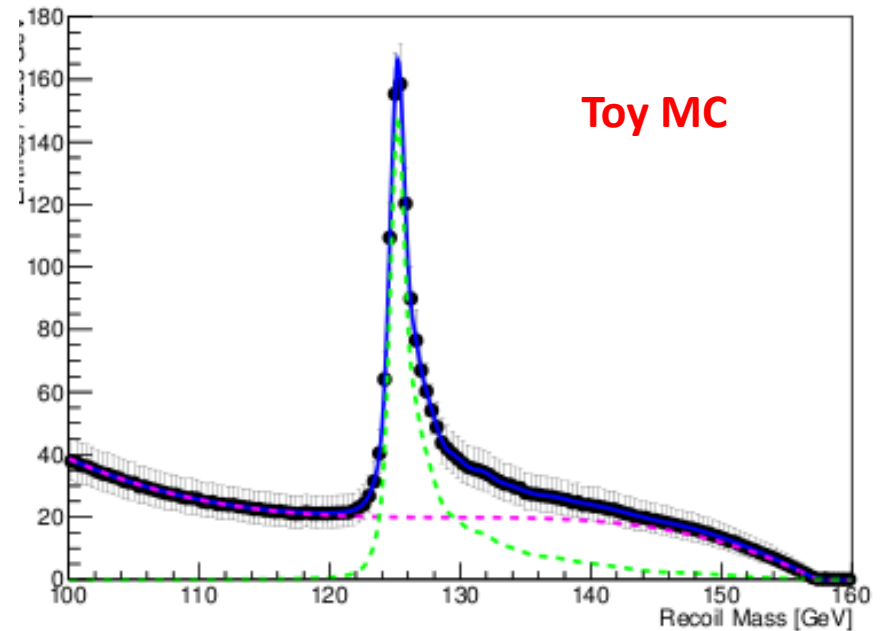
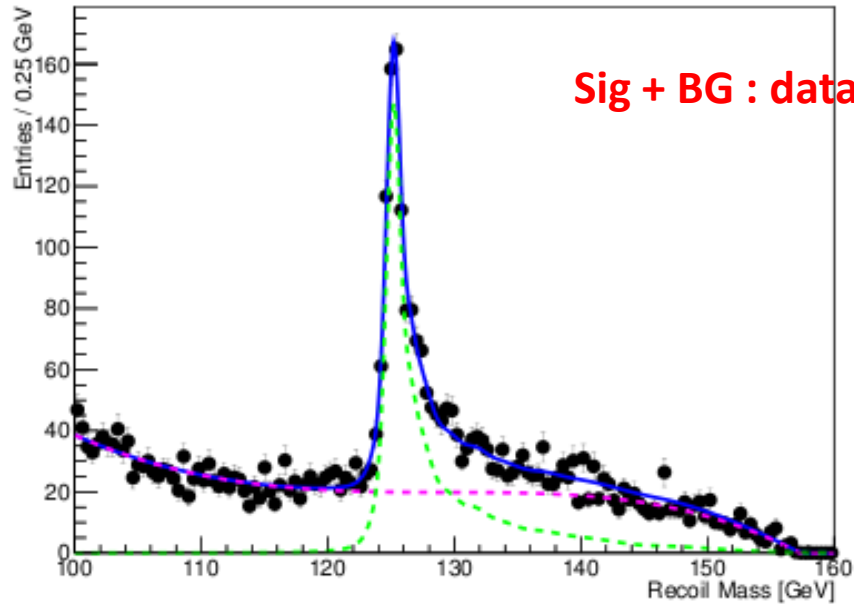
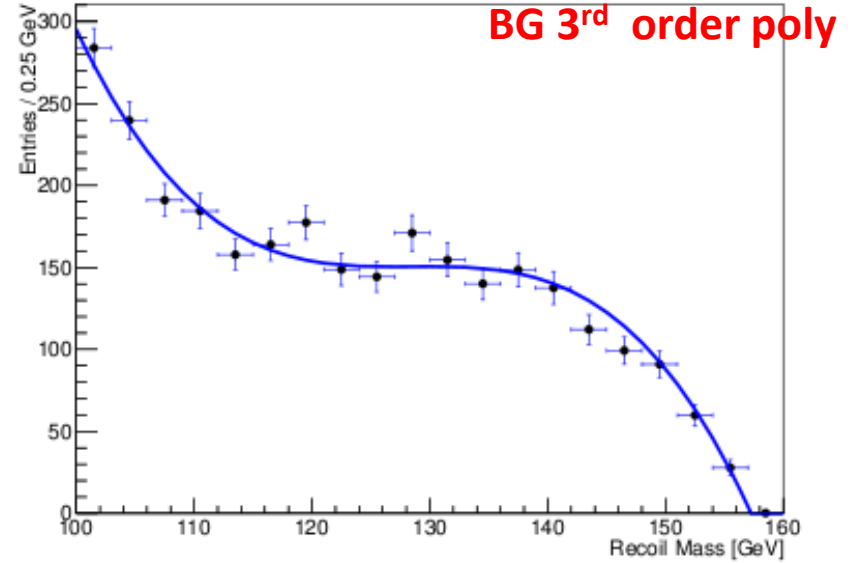
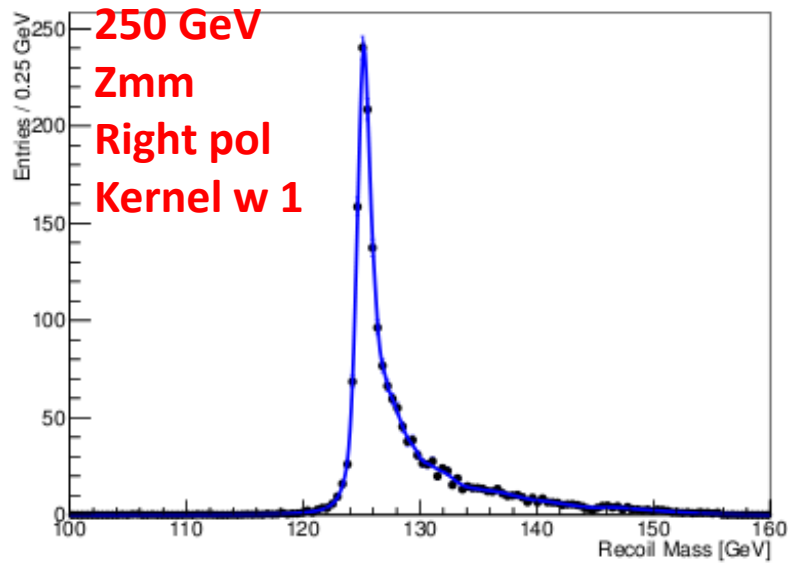
and well measured dilepton energy and angles

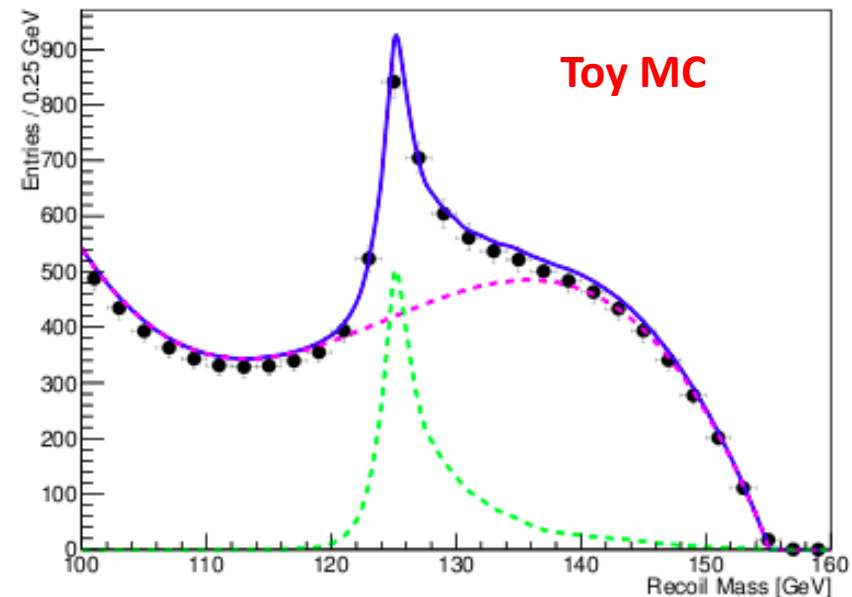
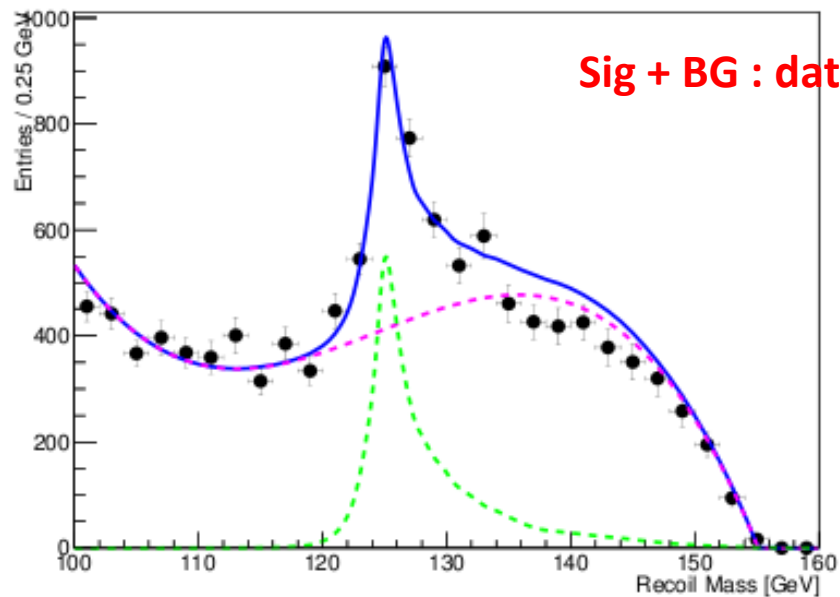
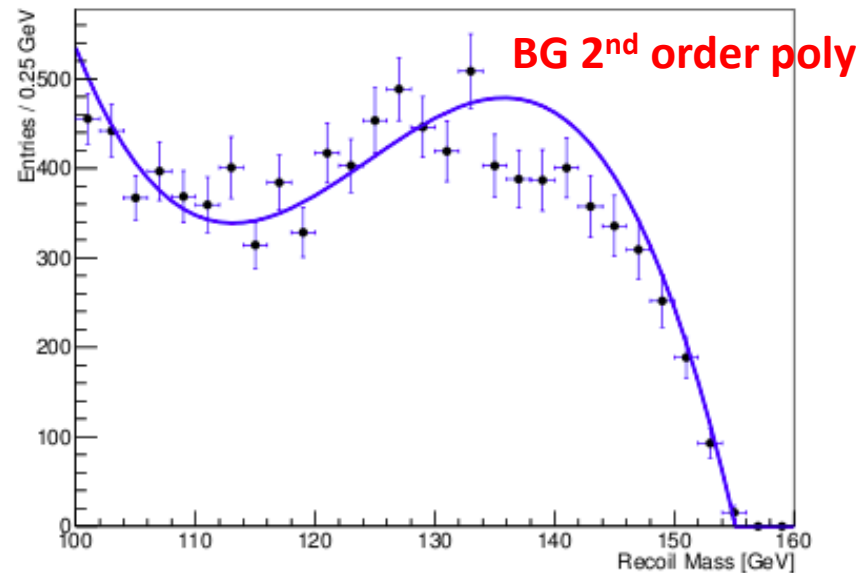
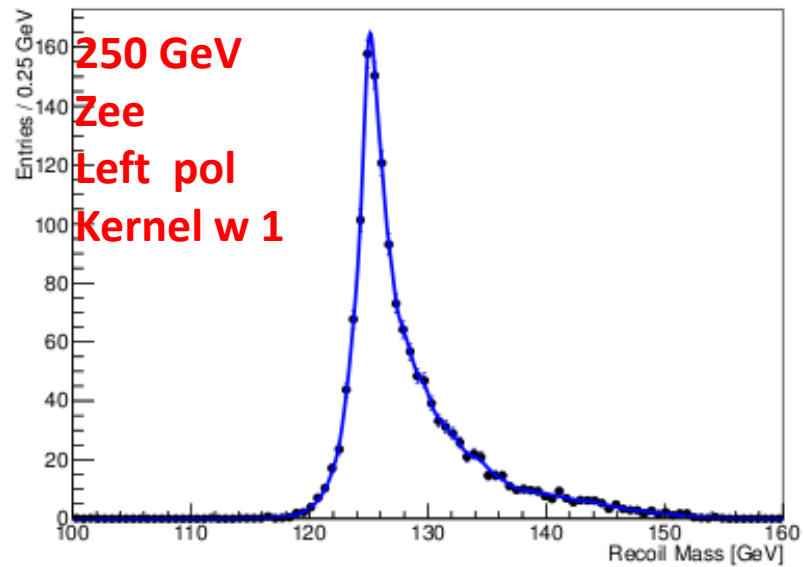


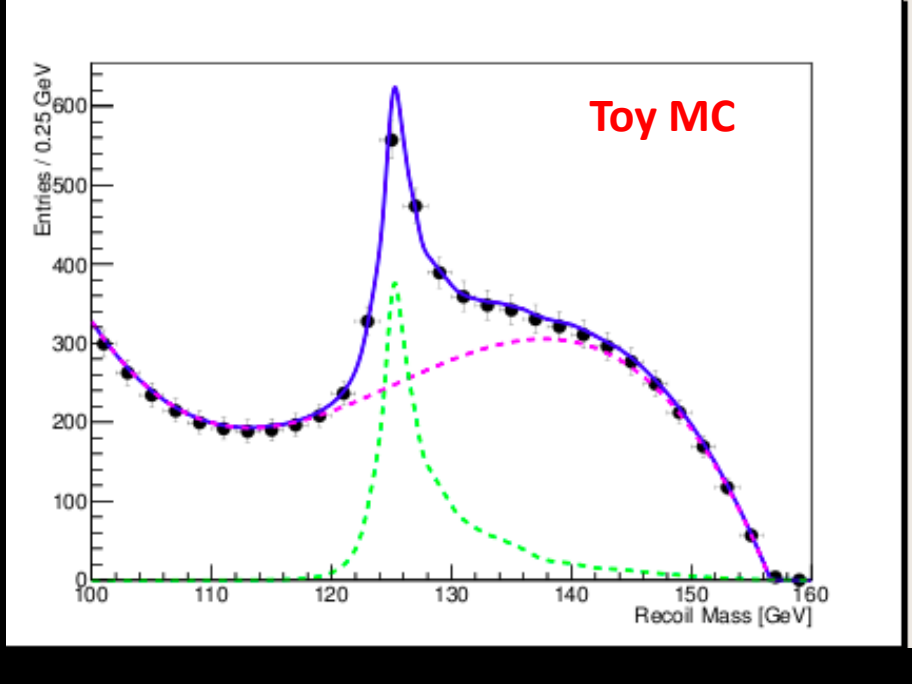
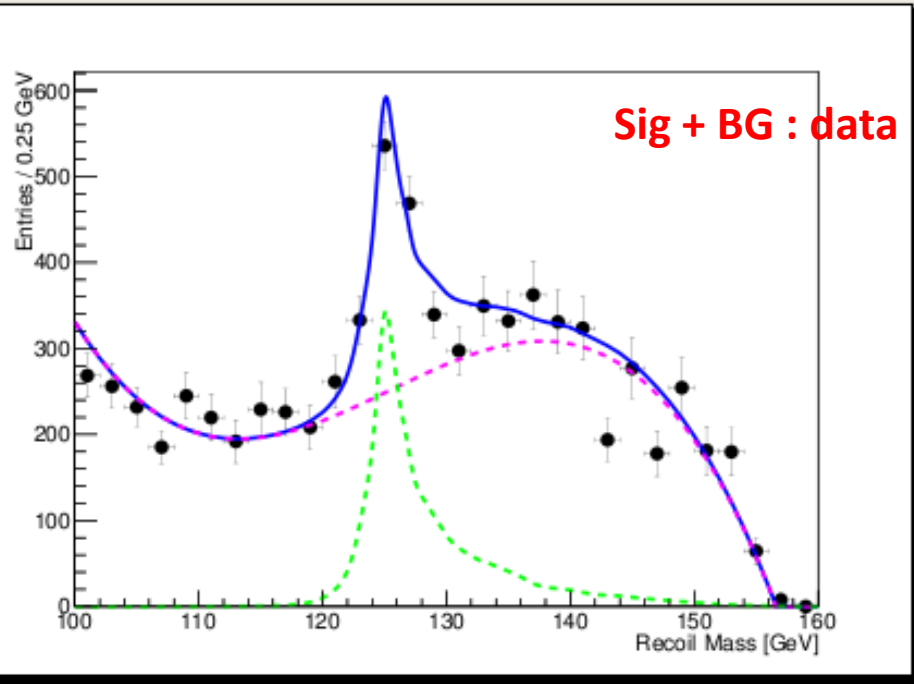
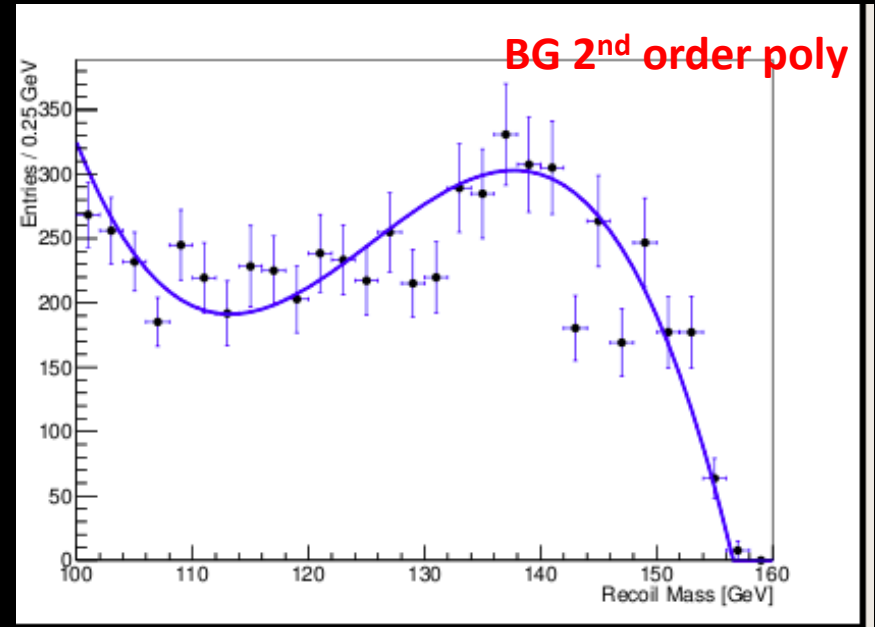
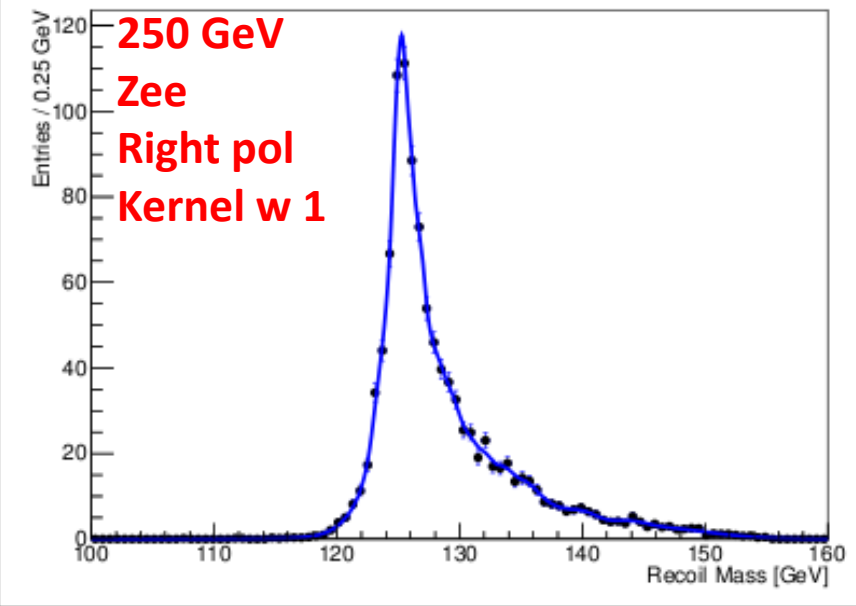
For these events, dilepton  $P_t$  is very small (limit of  $P_t$  resolution?)

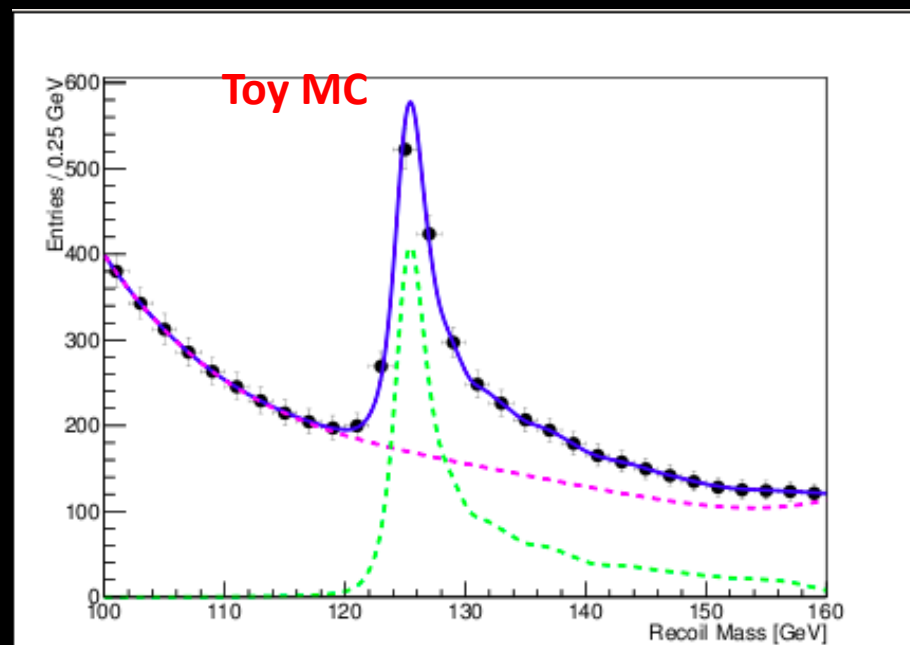
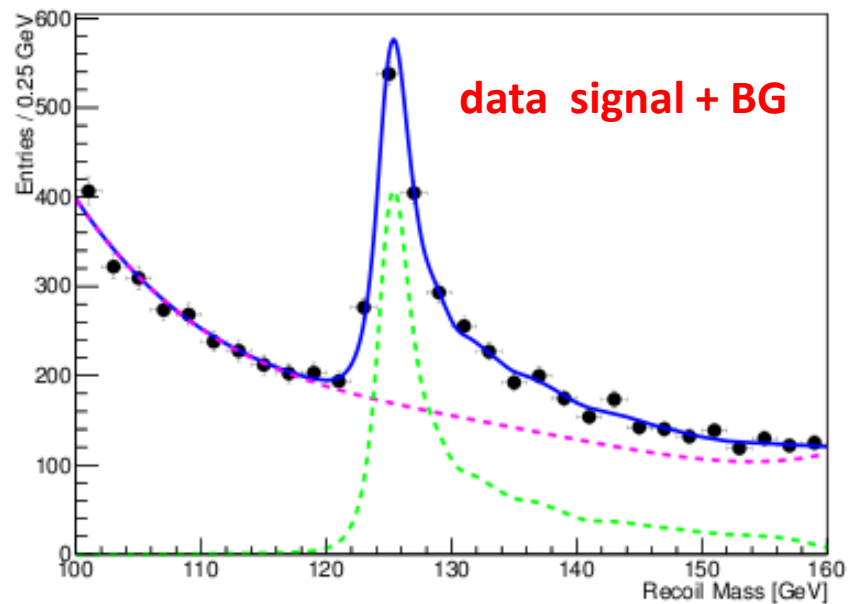
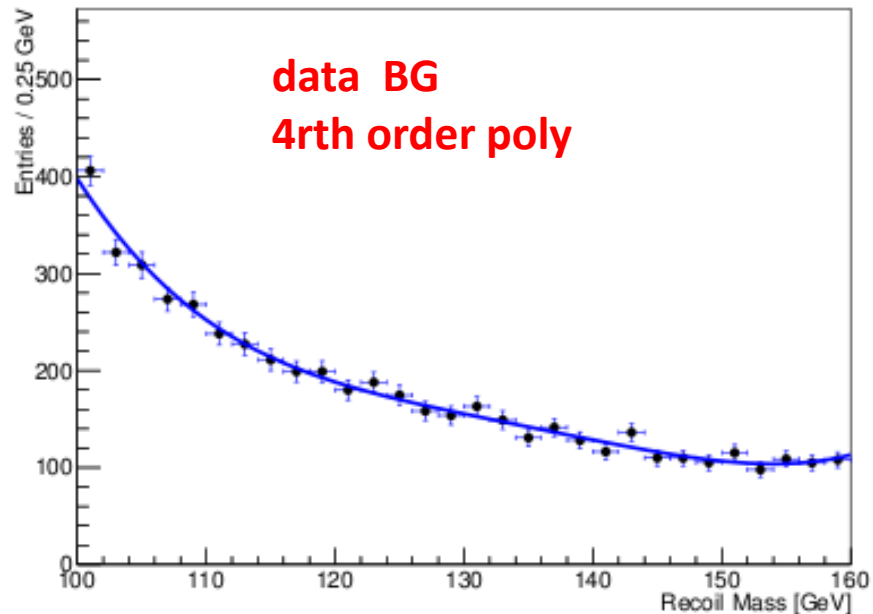
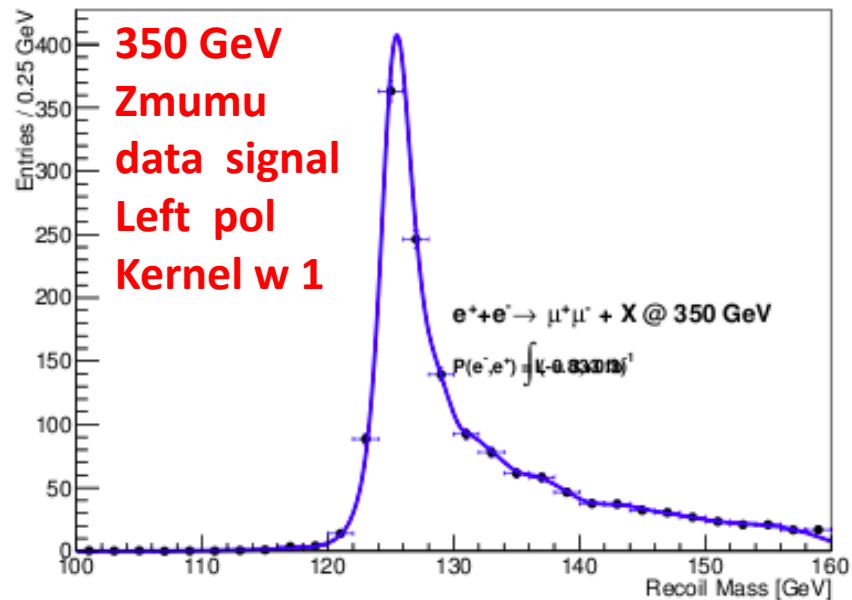


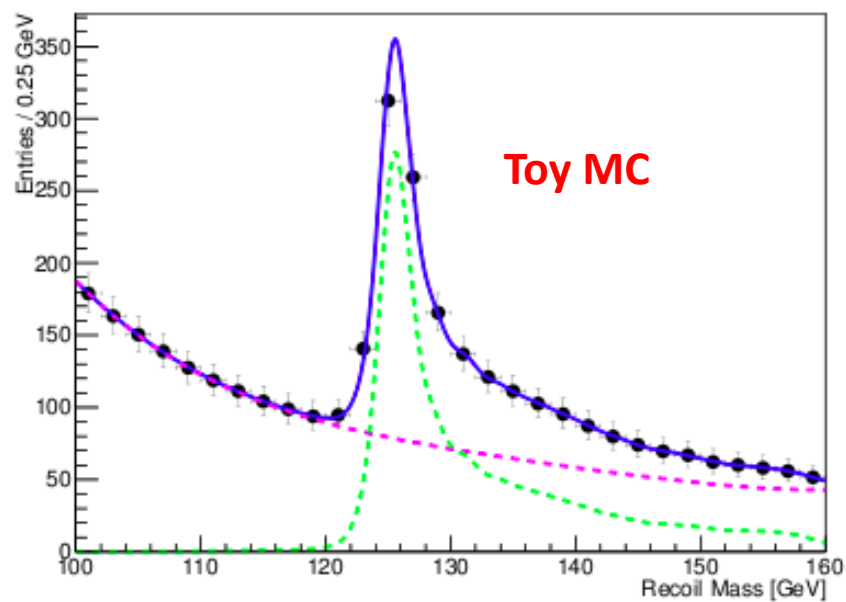
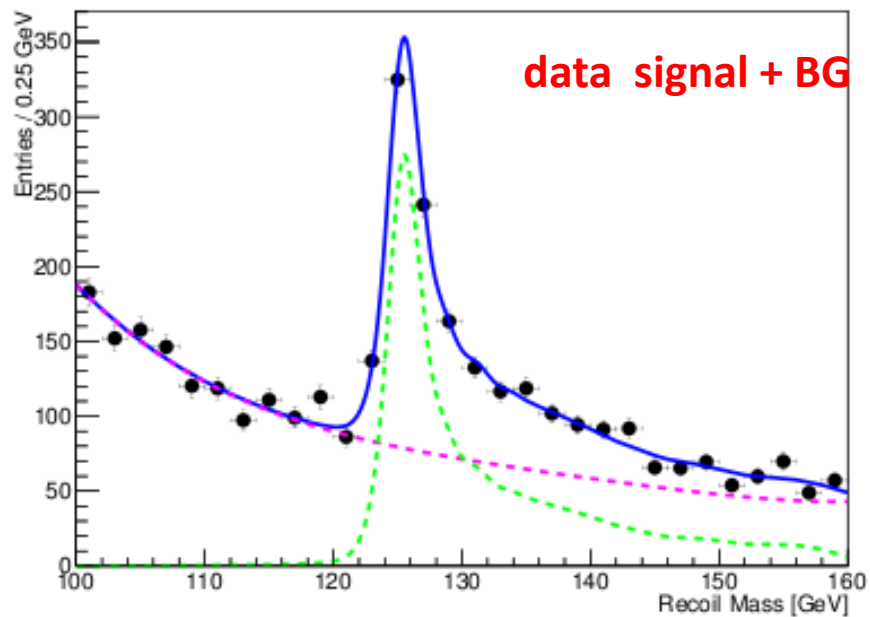
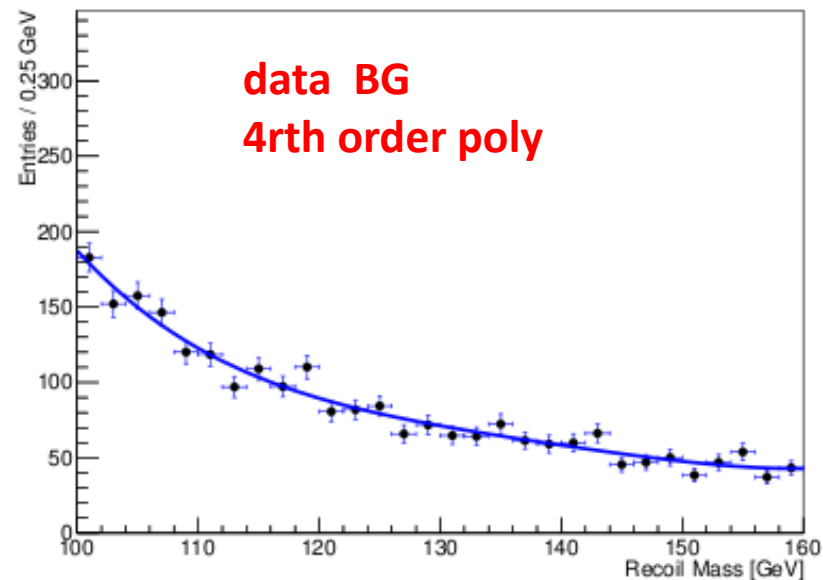
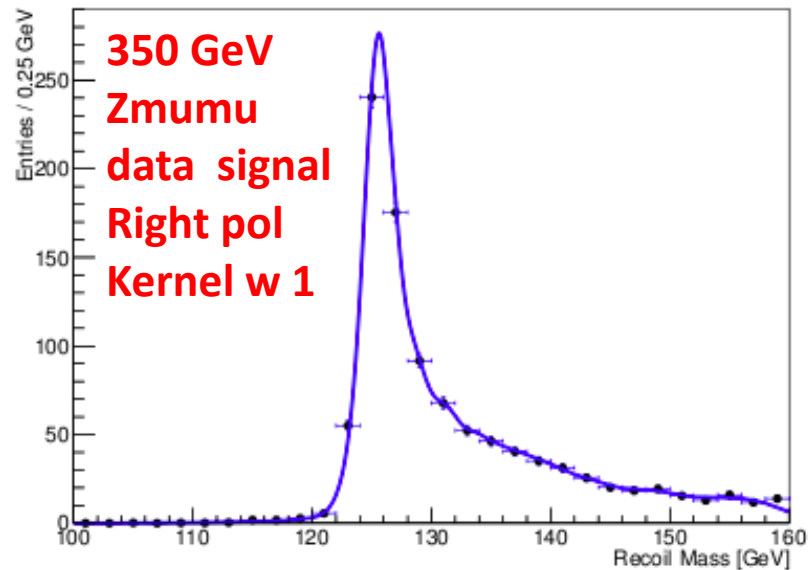






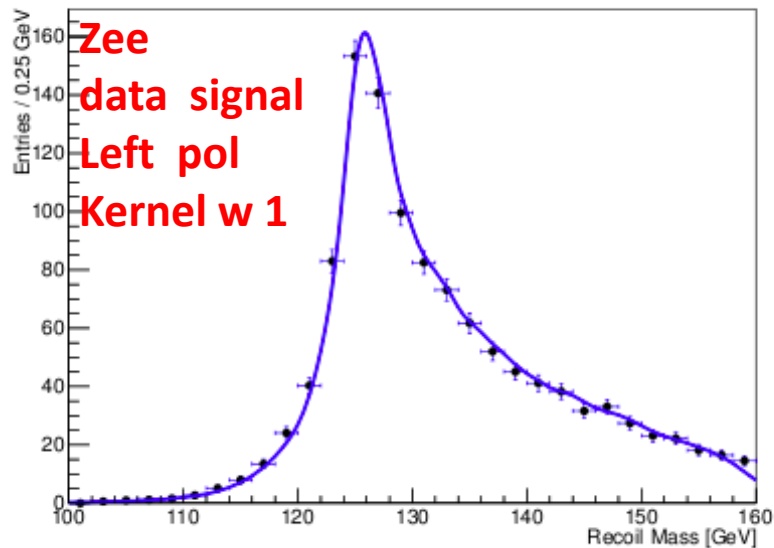




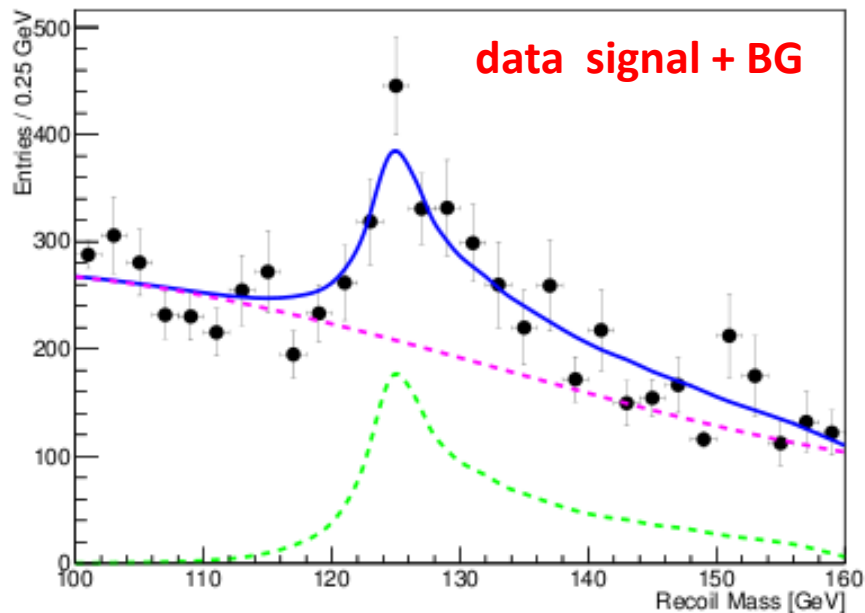
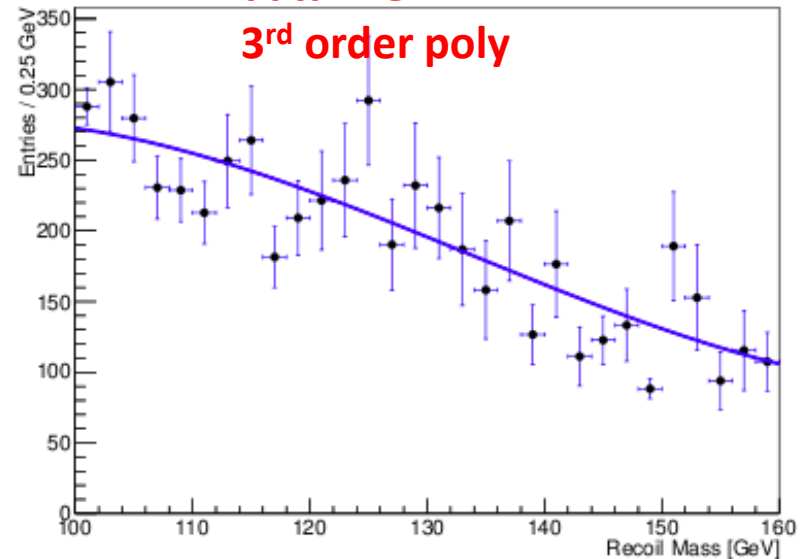




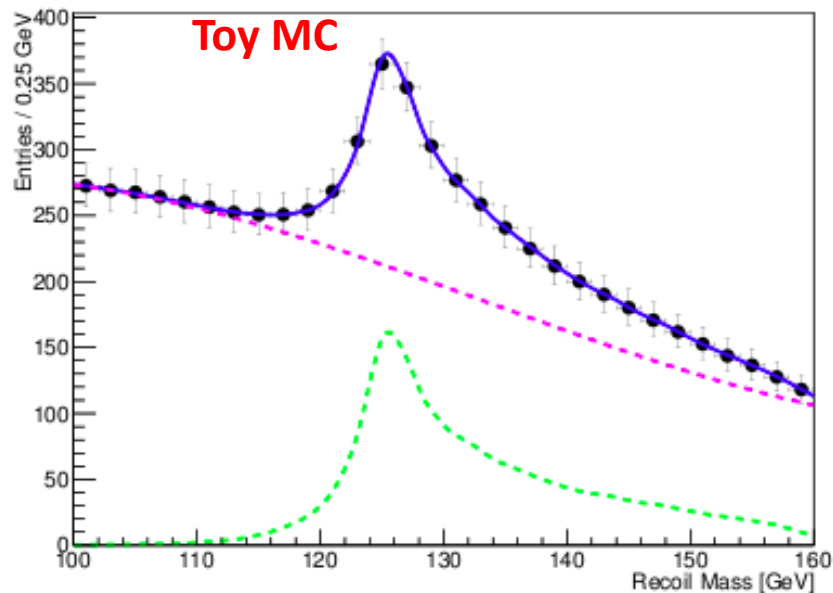
**350 GeV**



**data BG**

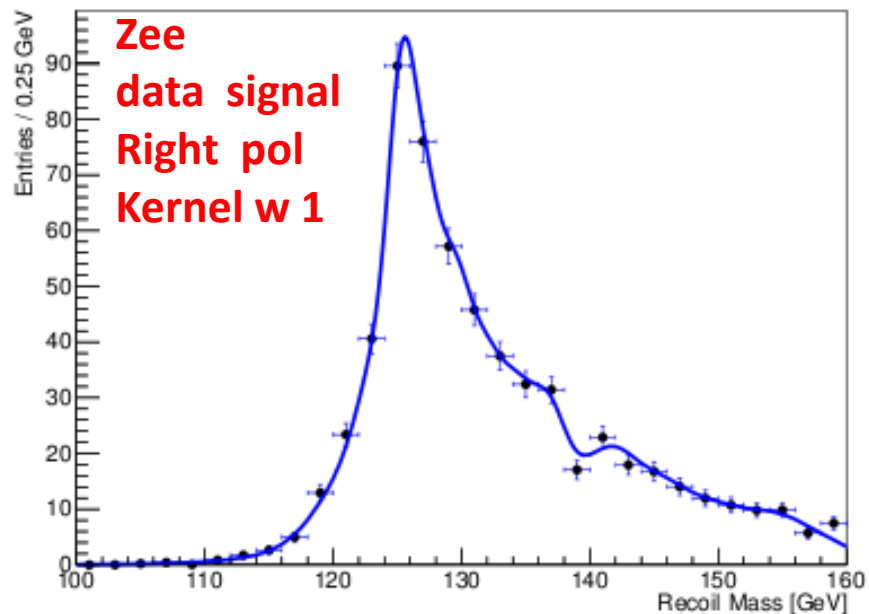


**Toy MC**

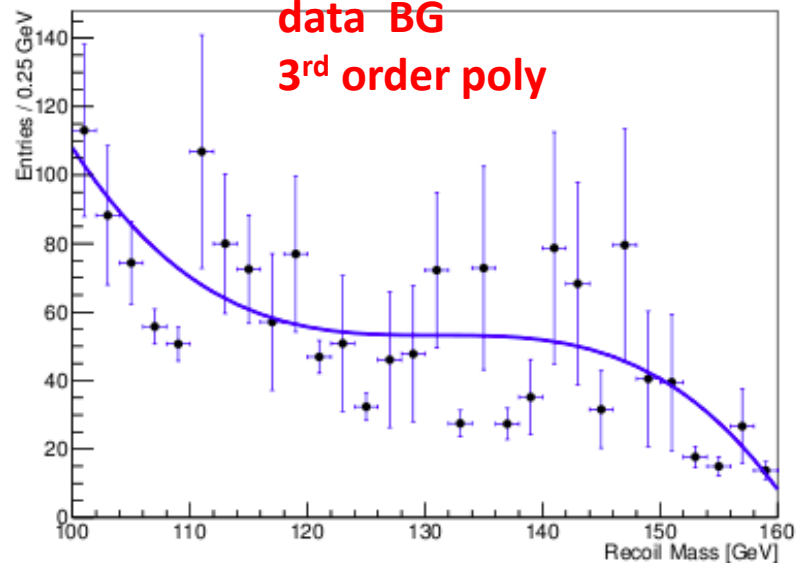


**350 GeV**

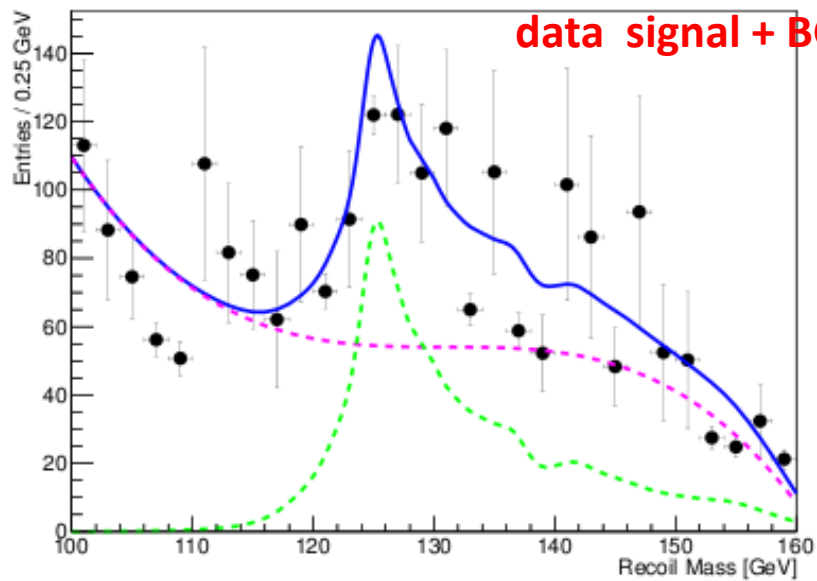
**Zee  
data signal  
Right pol  
Kernel w 1**



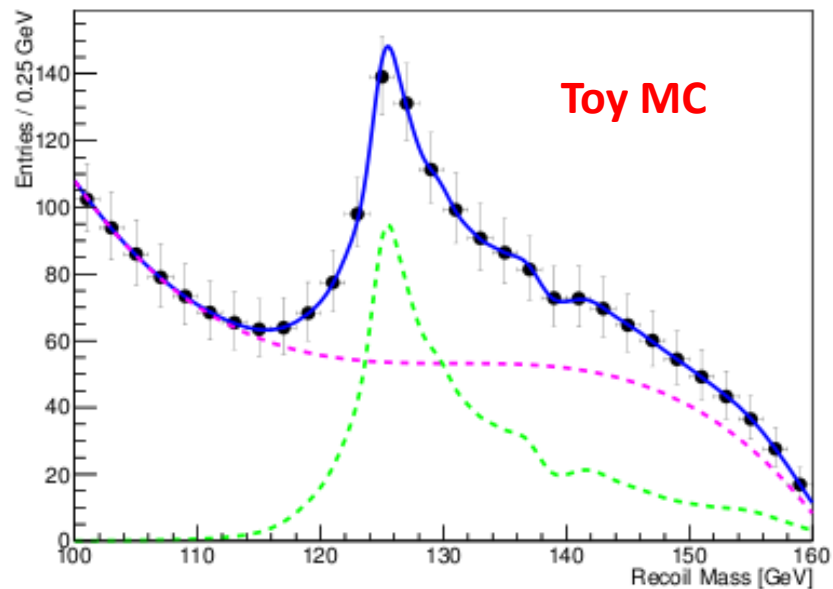
**data BG  
3<sup>rd</sup> order poly**

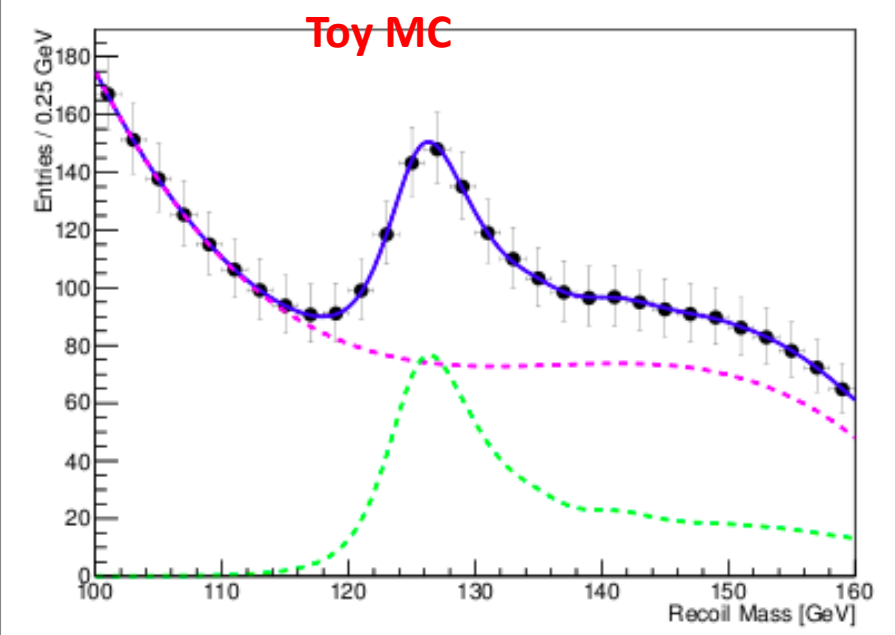
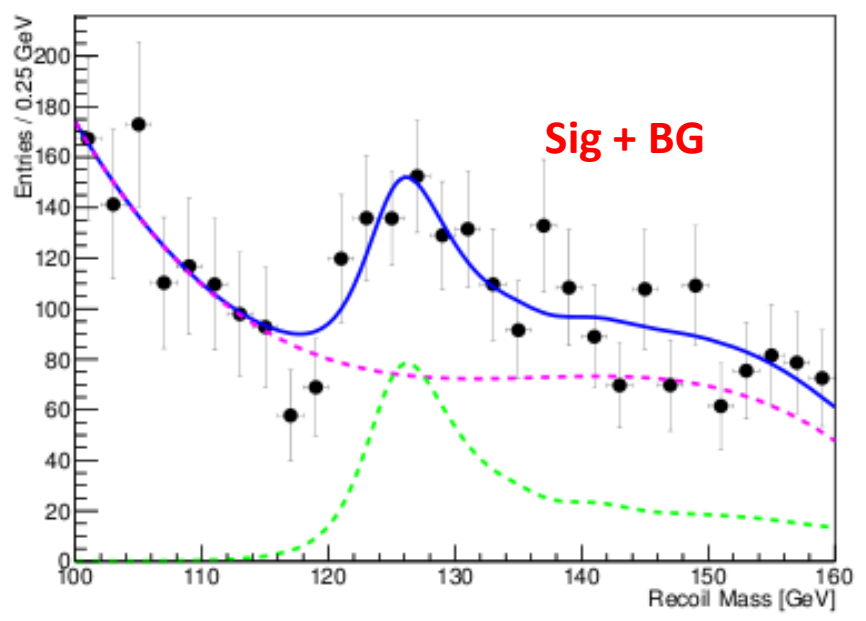
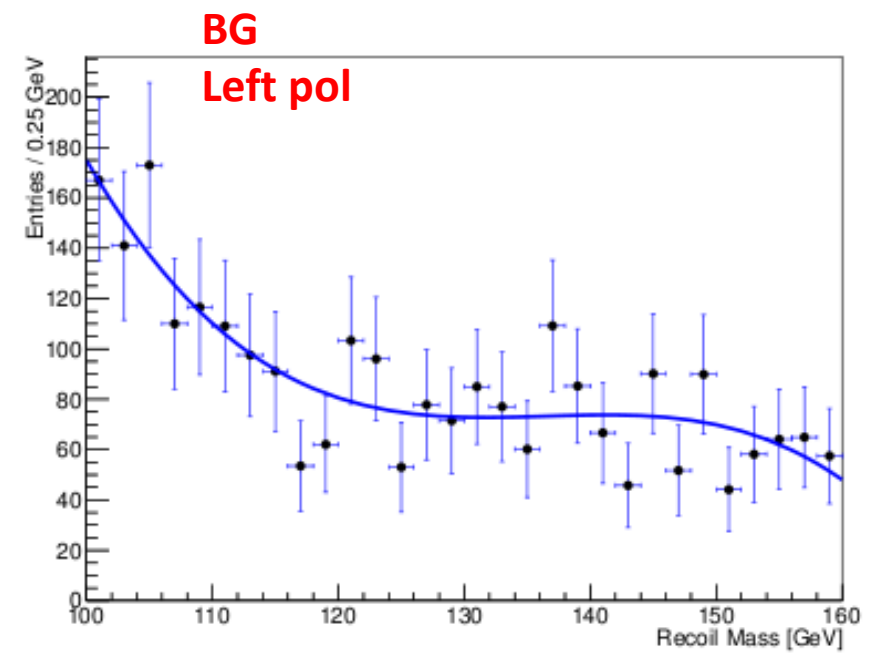
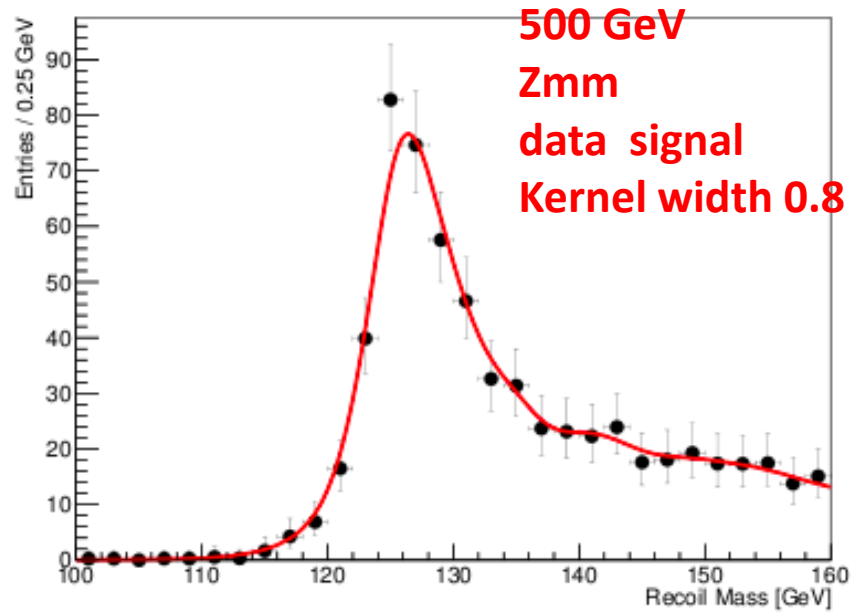


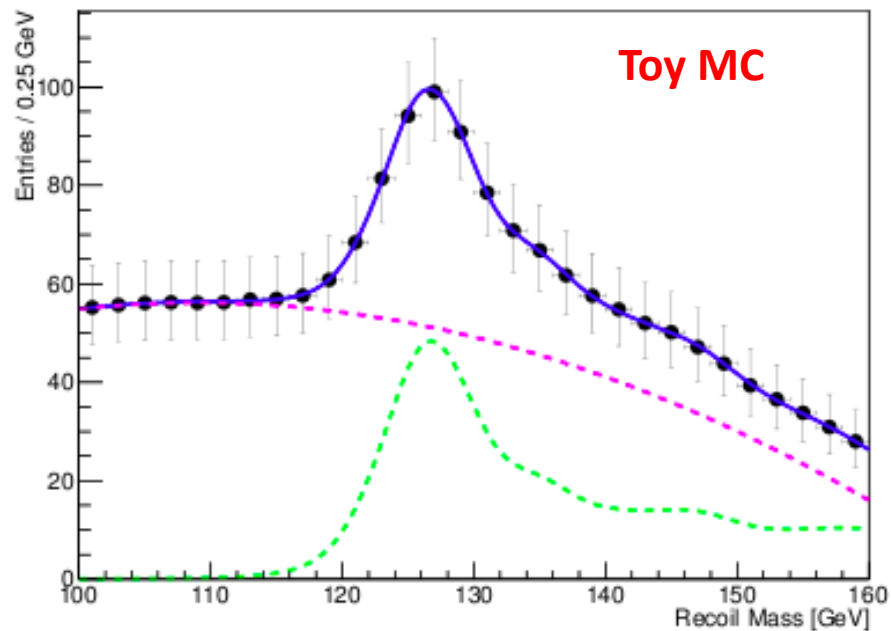
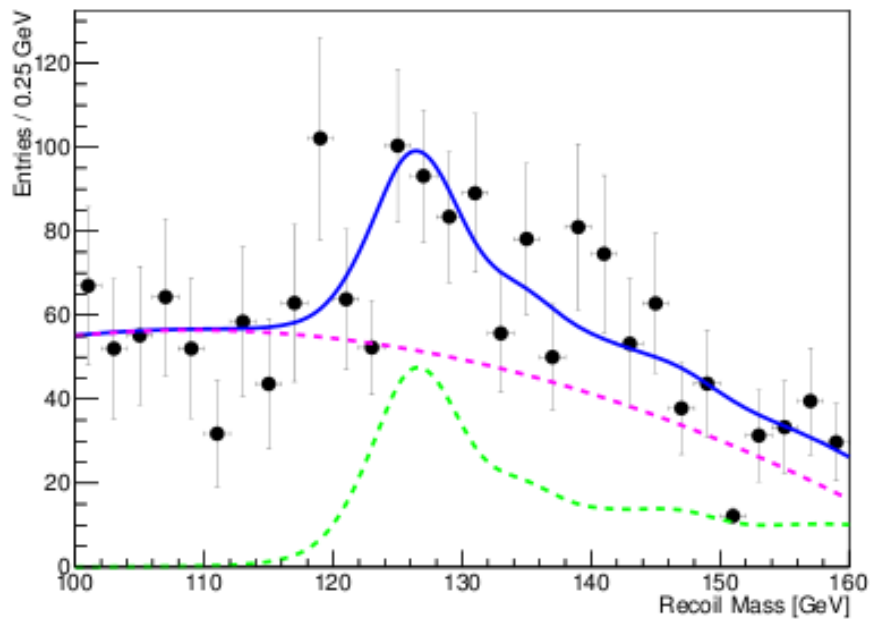
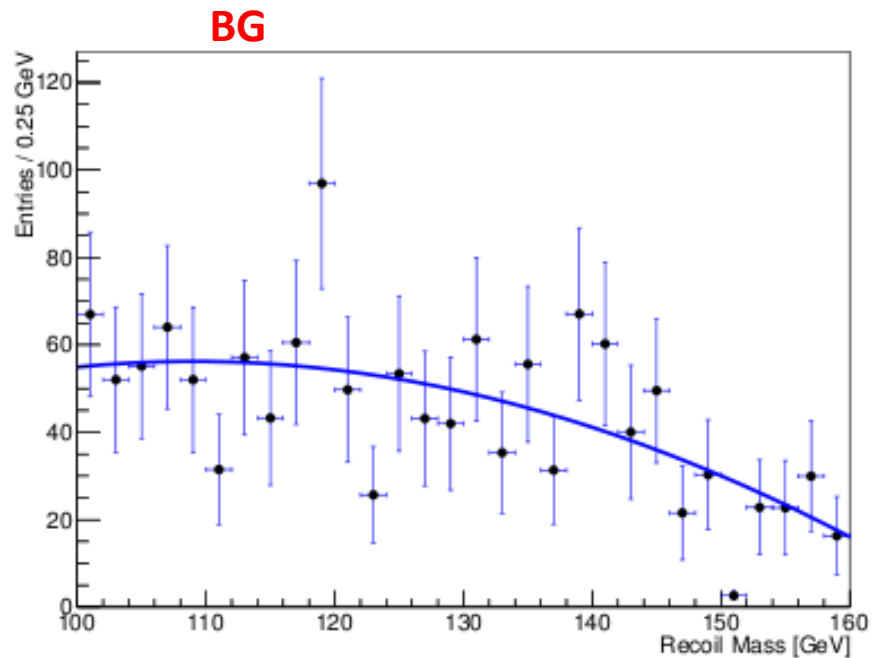
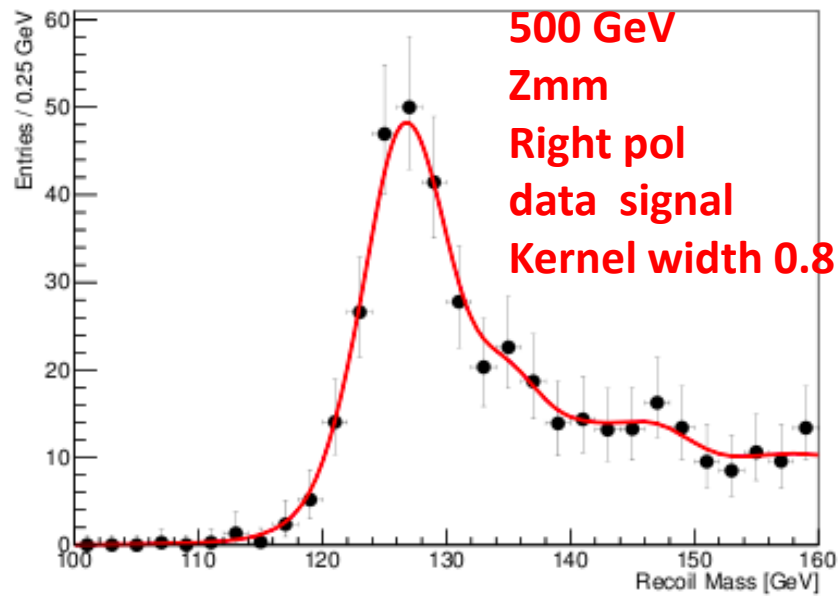
**data signal + BG**

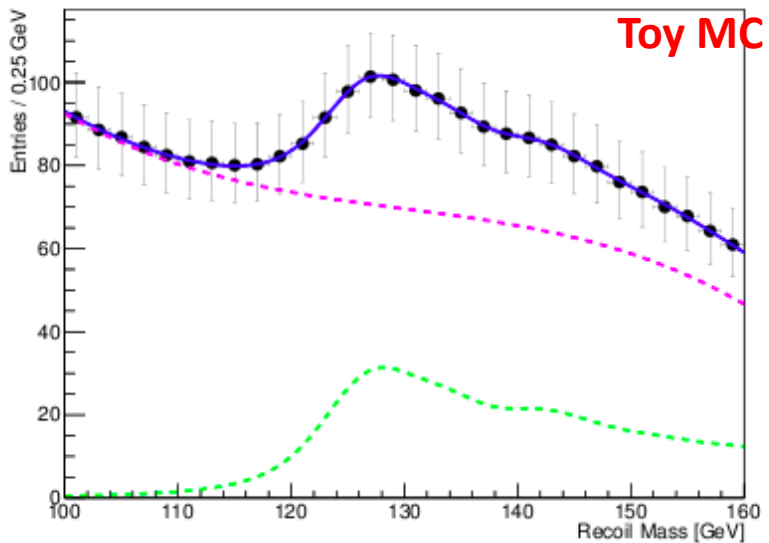
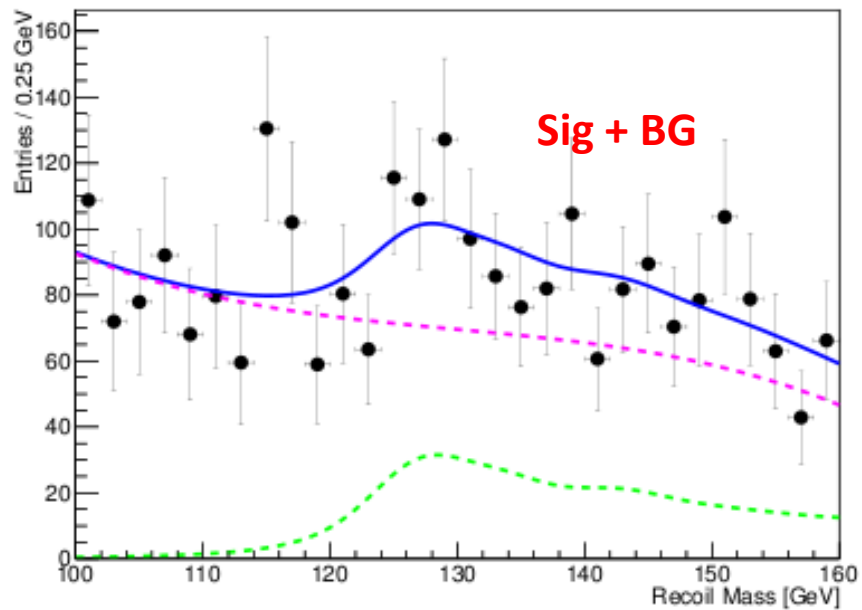
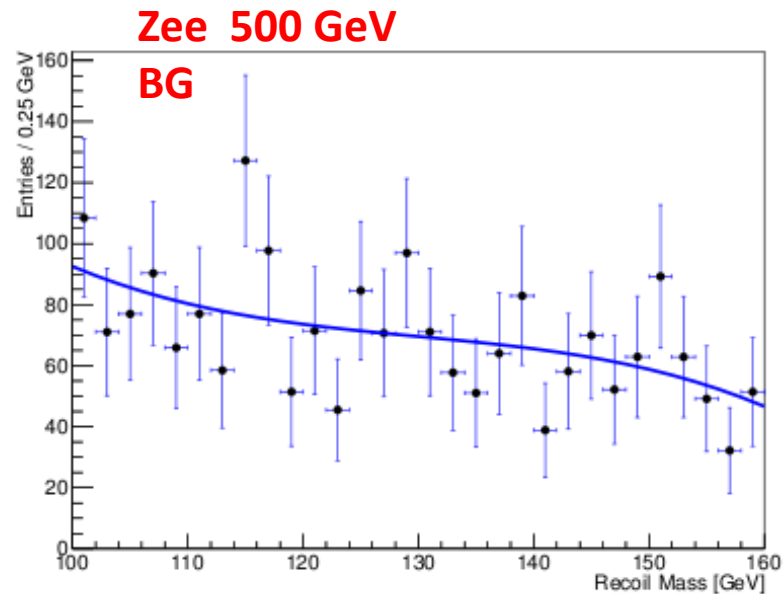
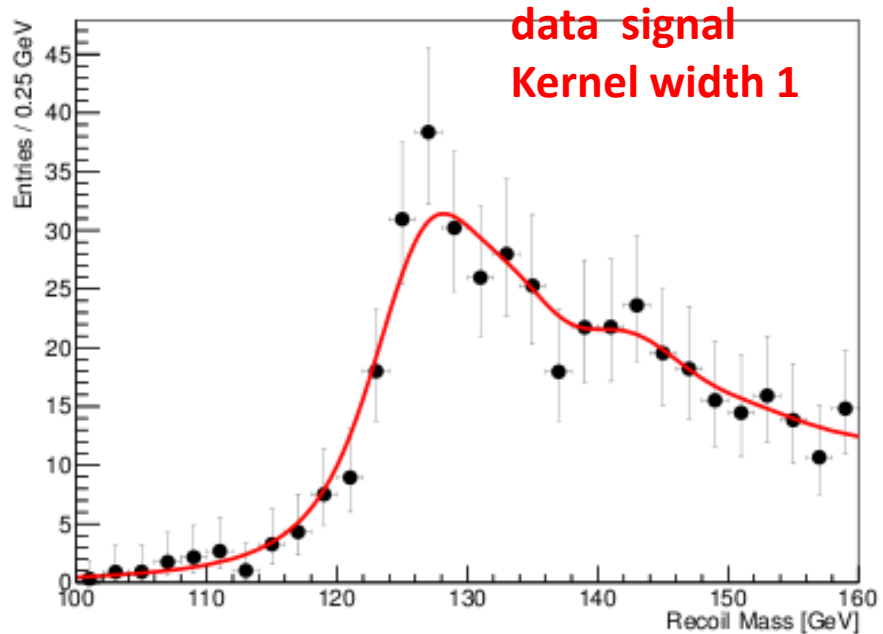


**Toy MC**

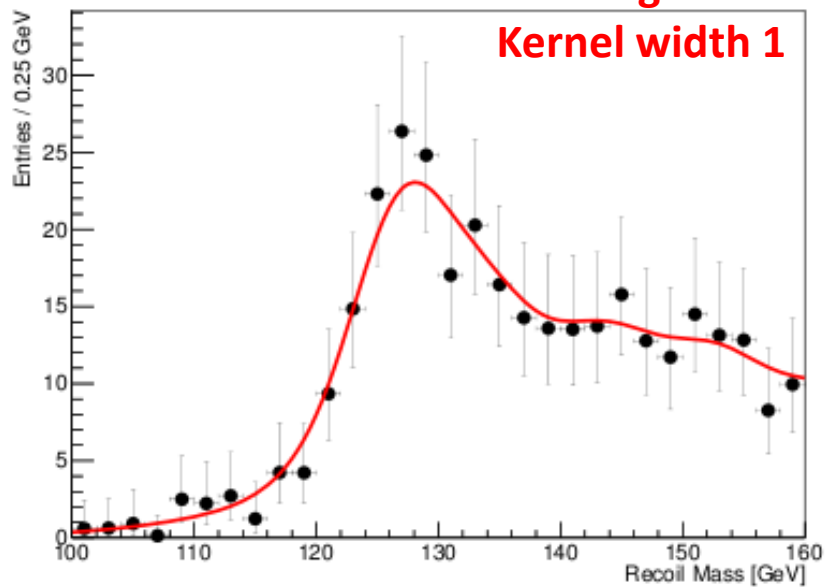




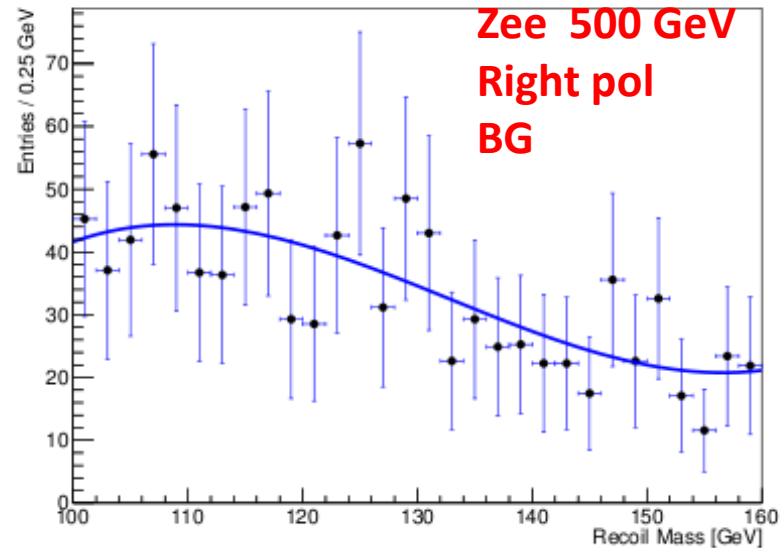




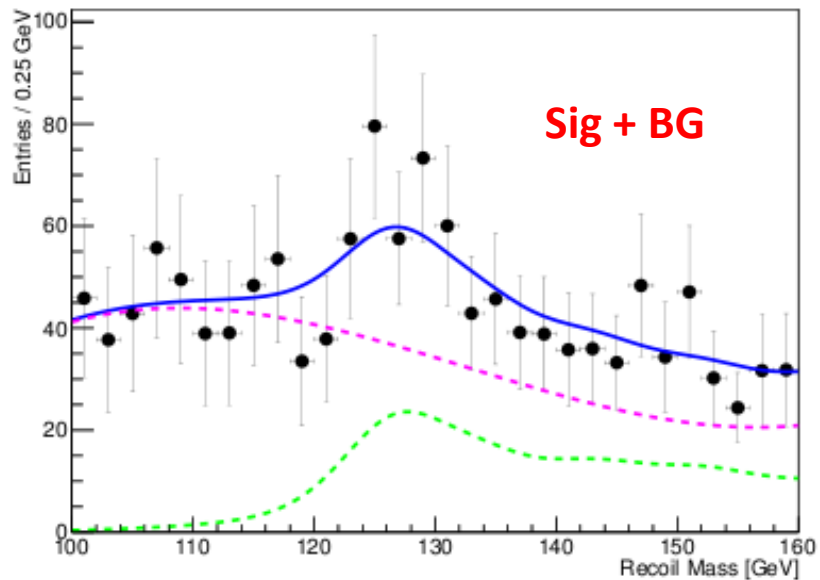
**data signal**  
**Kernel width 1**



**Zee 500 GeV**  
**Right pol**  
**BG**



**Sig + BG**



**Toy MC**

